

Kinetic and Chemical Equilibration Of Quark Gluon Plasma at Zero and Finite Density

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Extreme Nonequilibrium QCD

International Center for Theoretical Sciences, India (Online)

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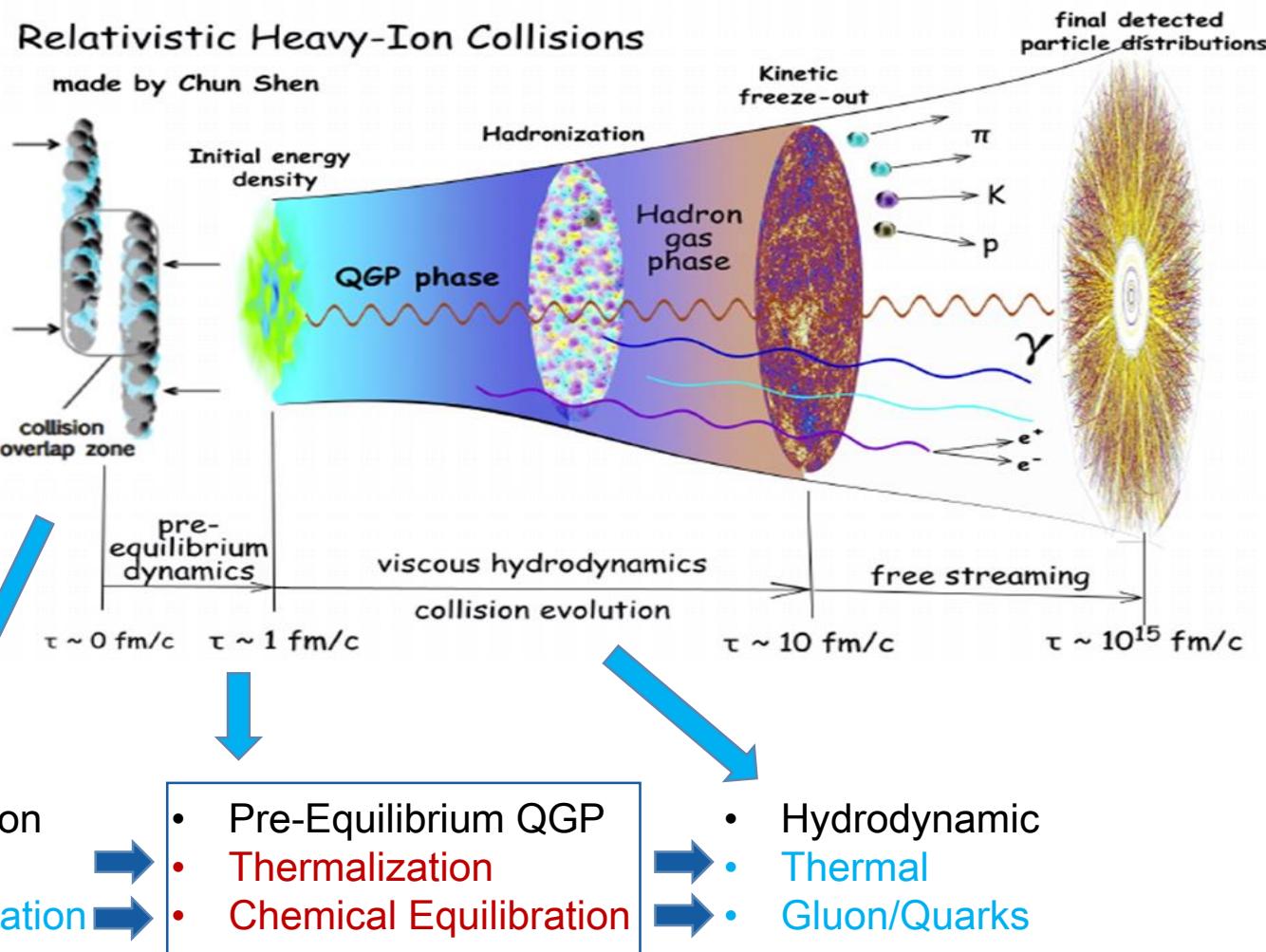
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CRC-TR 211
Strong-interaction matter
under extreme conditions

Pre-Equilibration Quark-Gluon Plasma



Effective Kinetic QCD

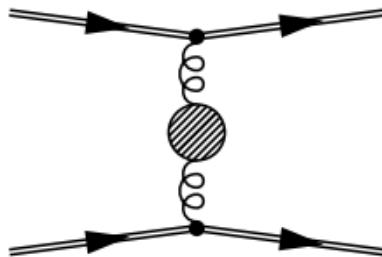
Effective Kinetic Theory (Arnold, Moore, Yaffe) at LO

$$\frac{\partial}{\partial t} f_a(\vec{p}, t) = -C_a^{2 \leftrightarrow 2}[f](\vec{p}, t) - C_a^{1 \leftrightarrow 2}[f](\vec{p}, t)$$

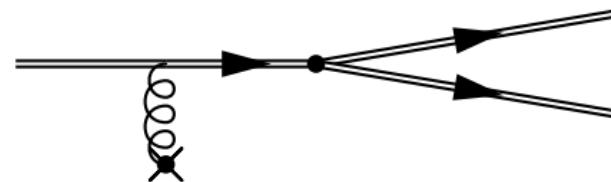
AMY,JHEP01 (2003) 030
AMY,JHEP0206(2002)030
Kurkela, Mazeliauskas, PRD99 (2019) 054018

$$s = g, u, \bar{u}, d, \bar{d}, s, \bar{s}$$

Explicitly solve Boltzmann equation for massless gluon and 3 light quarks/anti-quarks as an integro-differential equation including 2-2 elastic processes and 1-2 inelastic processes



2-2: Color screening by Debye mass fit to HTL calculation

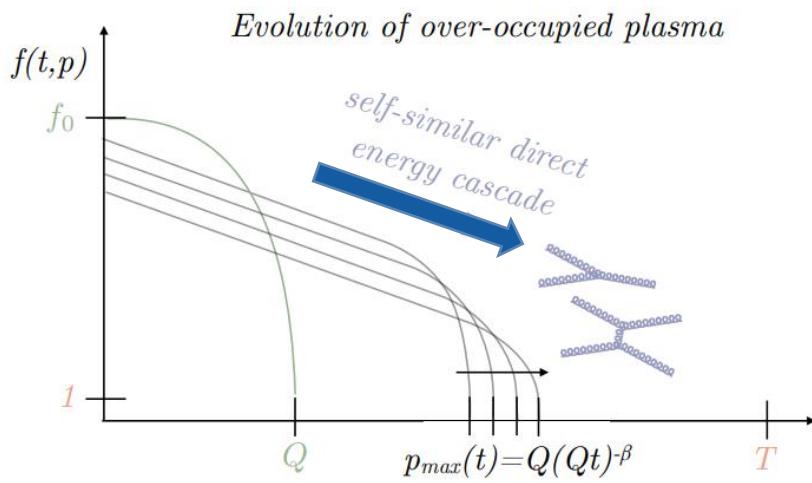


1-2: Collinear radiation including LPM effect via effective vertex resummation

Kinetic and Chemical Equilibration without Long. Expansion

Turbulence in Quark-Gluon Plasma

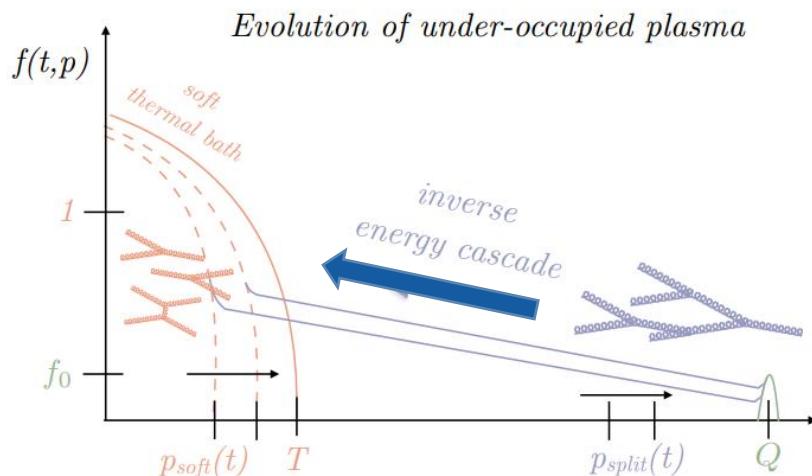
Weak-Coupling Thermalization



Over-occupied systems
 $\langle p \rangle \ll T$

Direct energy cascade

Far from equilibrium
Large separation of scales

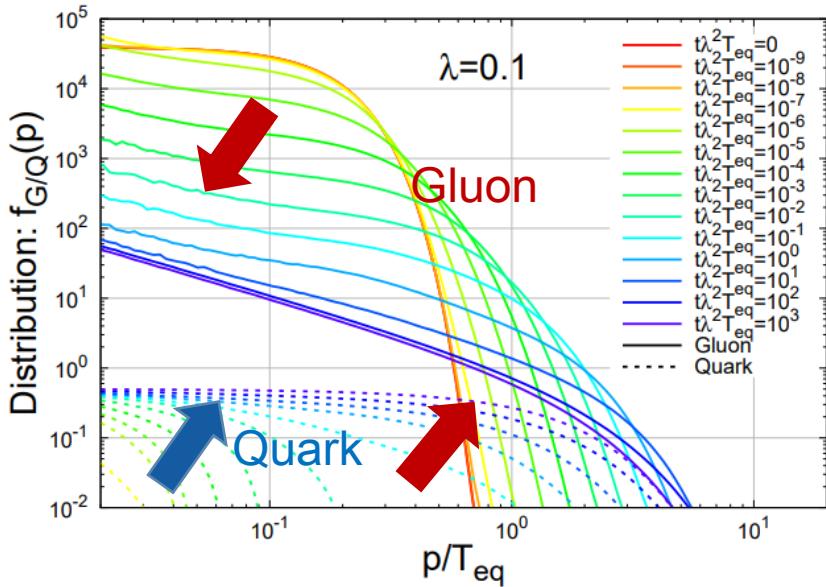


Under-occupied systems
 $\langle p \rangle \gg T$

Inverse energy cascade

Schlichting, Teaney, Ann. Rev. of Nuc & Part. Sci. 69:447 (2019)

Over-Occupied Plasma



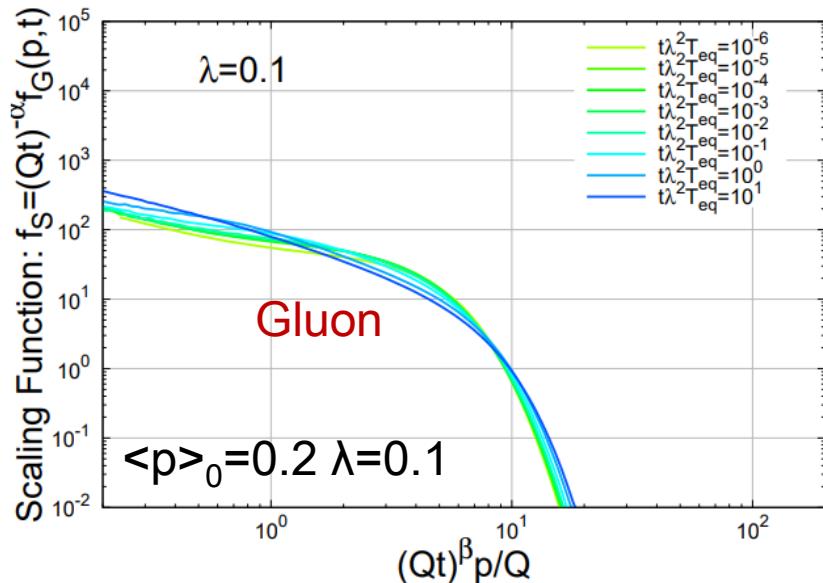
Self-similar Turbulence

$$f_G(p, t) = (Qt)^\alpha f_S \left((Qt)^\beta \frac{p}{Q} \right)$$

Scaling Exponents from pure Yang-Mills plasma

Also work for QCD plasma: **Gluon domination**

Quark spectra are following gluon spectrum



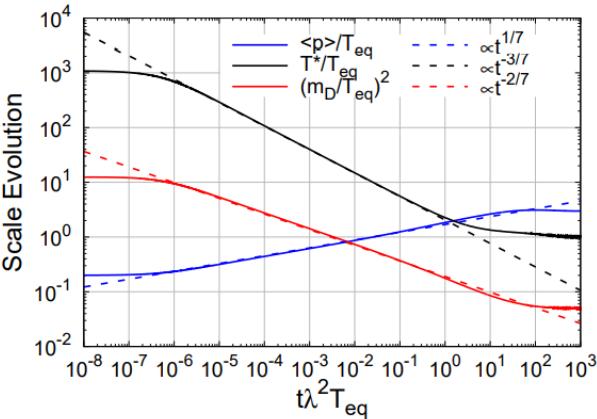
Universal Scaling Function

$$f_S \left((Qt)^\beta \frac{p}{Q} \right)$$

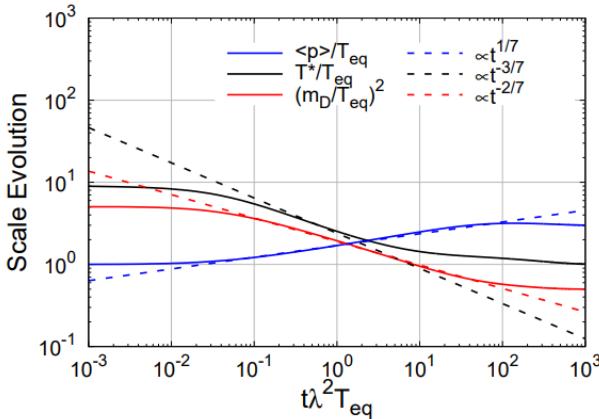
$$\alpha = -4/7, \beta = -1/7$$

Berges, Boguslavski, Schlichting,
Venugopalan, PRD89(2014)114007
Abraao York, Kurkela, Lu, Moore,
PED89(2014)074036

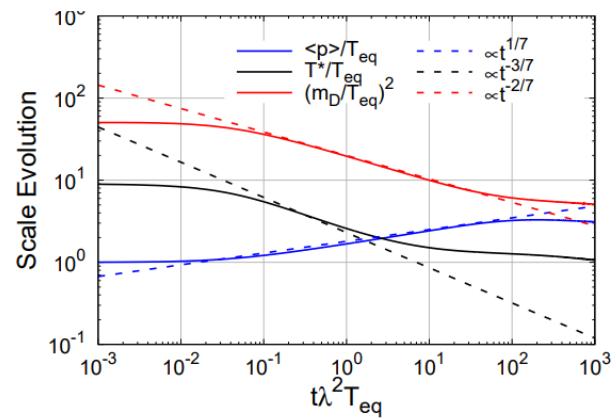
Over-Occupied Plasma



$$\langle p \rangle_0 = 0.2 \quad \lambda = 0.1$$



$$\langle p \rangle_0 = 1.0 \quad \lambda = 1.0$$



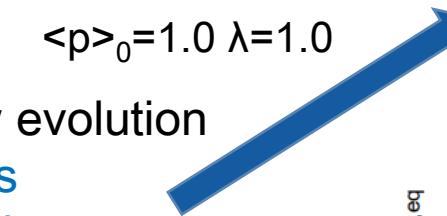
$$\langle p \rangle_0 = 1.0 \quad \lambda = 10.0$$

Self-similar Scaling: pow-law evolution
 Not limited to pure Yang-Mills
 Even work for stronger coupling

Chemical Equilibration
 Later than kinetic equilibration

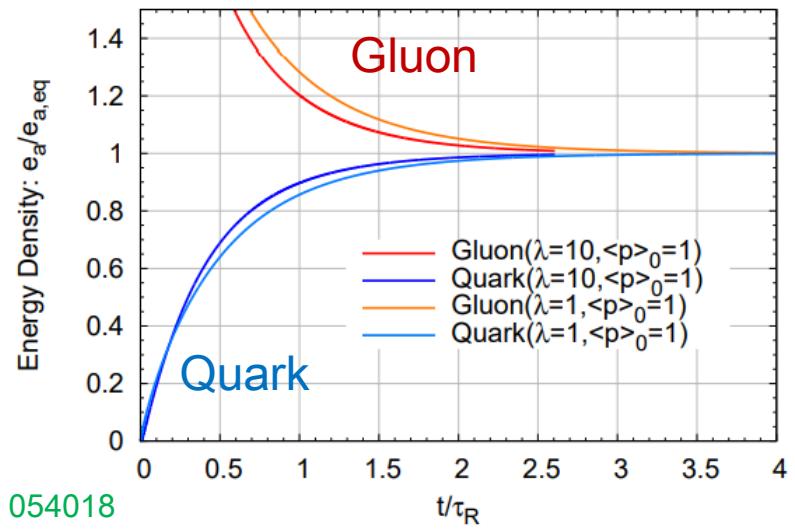
Equilibration relaxation time

$$\tau_R = \frac{4\pi\eta/s}{T_{eq}}$$

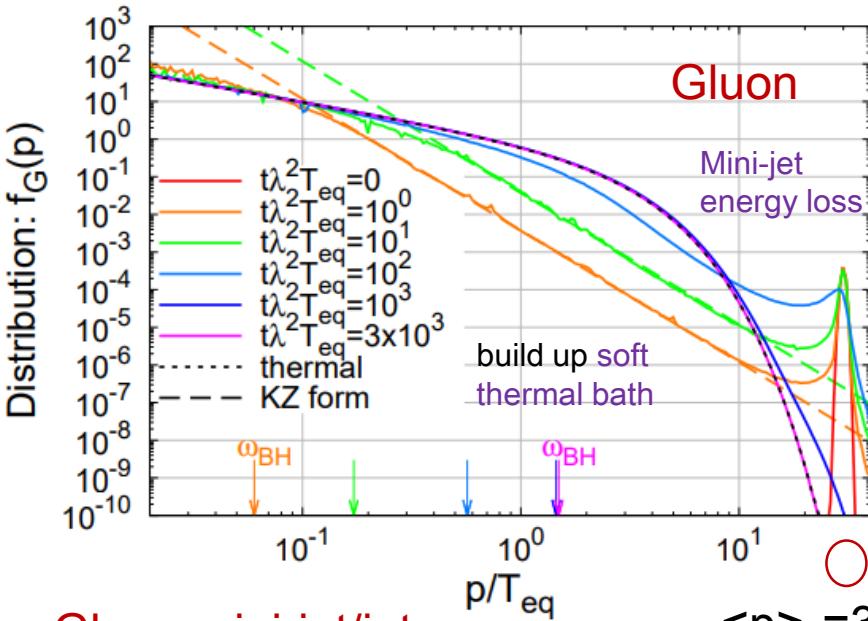


t'Hooft coupling
 $\lambda = 4\pi\alpha_s N_c$

Kurkela, Mazeliauskas, PRD99 (2019) 054018
 KOMPOST, PRC99 (2019) 034910



Under-Occupied Plasma



Gluon mini-jet/jet:

$$\langle p \rangle_0 = 30, \lambda = 1$$

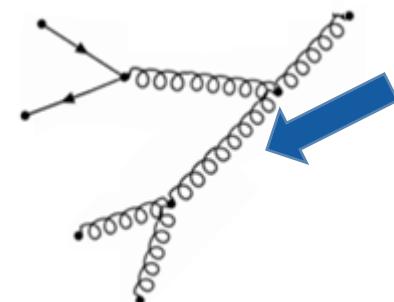
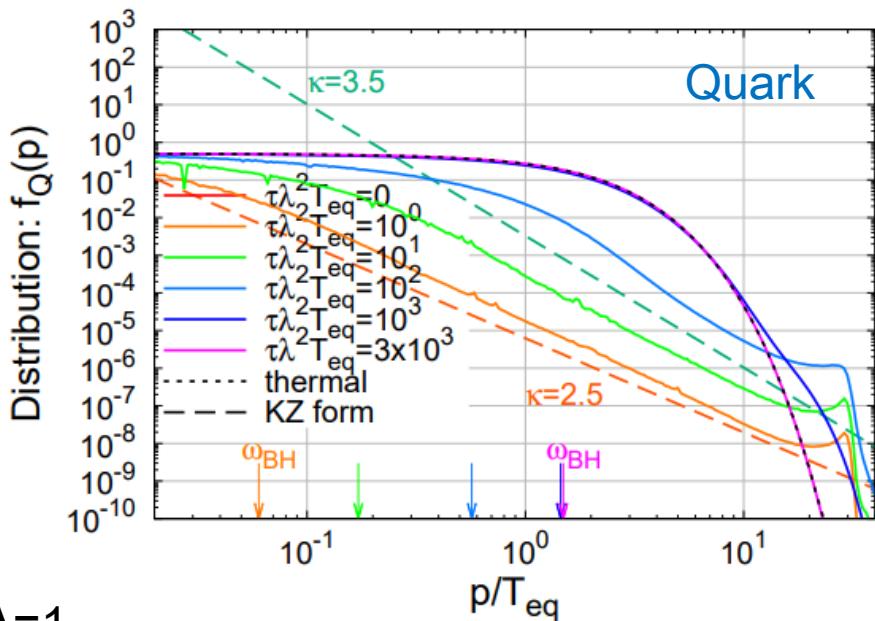
- Kolmogorov-Zakharov spectrum (exponent $\kappa = 7/2$ for gluon)

$$f_{KZ}(\vec{p}, t) = \eta(t) \left(\frac{\langle p \rangle_0}{p} \right)^\kappa$$

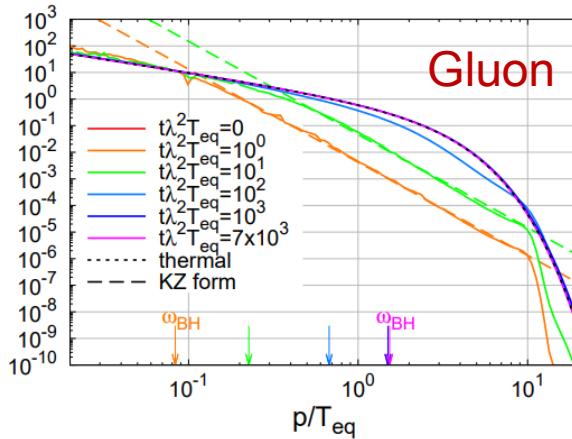
- Bottom-up thermalization

R. Baier, et al. PLB502(2001)51

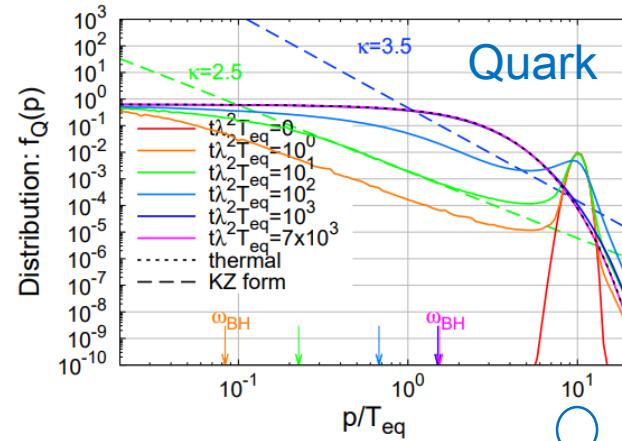
1. Emission of (soft) **quarks** and **gluons**
2. Radiative breakup by multiple branchings -> build up **soft thermal bath**
3. **Mini-jet energy loss** -> heating up thermal bath



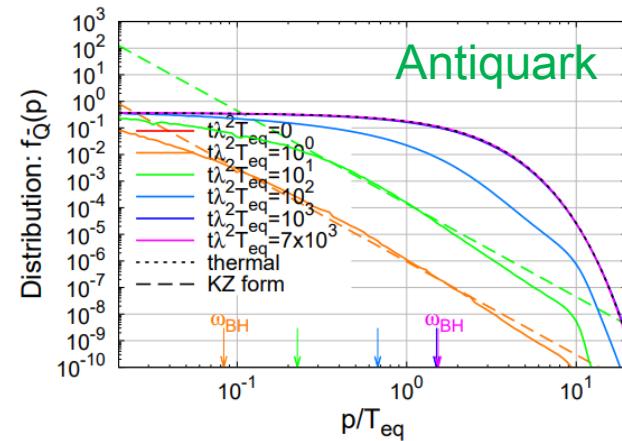
Under-Occupied Plasma



Gluon



Quark



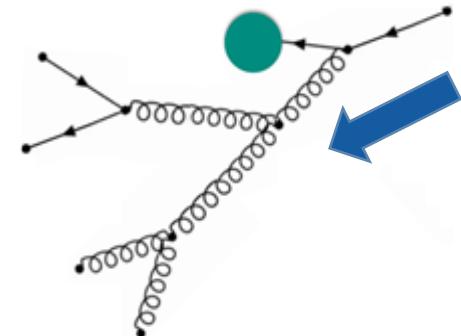
Antiquark

Quark mini-jet/jet:

- Bottom up thermalization
- Kolmogorov-Zakharov spectrum
 1. Quark follows $\kappa=5/2$ to $\kappa=7/2$
 2. Gluon follows $\kappa=7/2$
 3. Antiquark follows gluon (secondary production)
- Same pattern as for in-medium mini-jet/jet evolution with unified description of soft and hard sectors
- Equilibration of Jets

$\langle p \rangle_0 = 10, \lambda = 1$

Soudi, Schlichting, 2008.04928

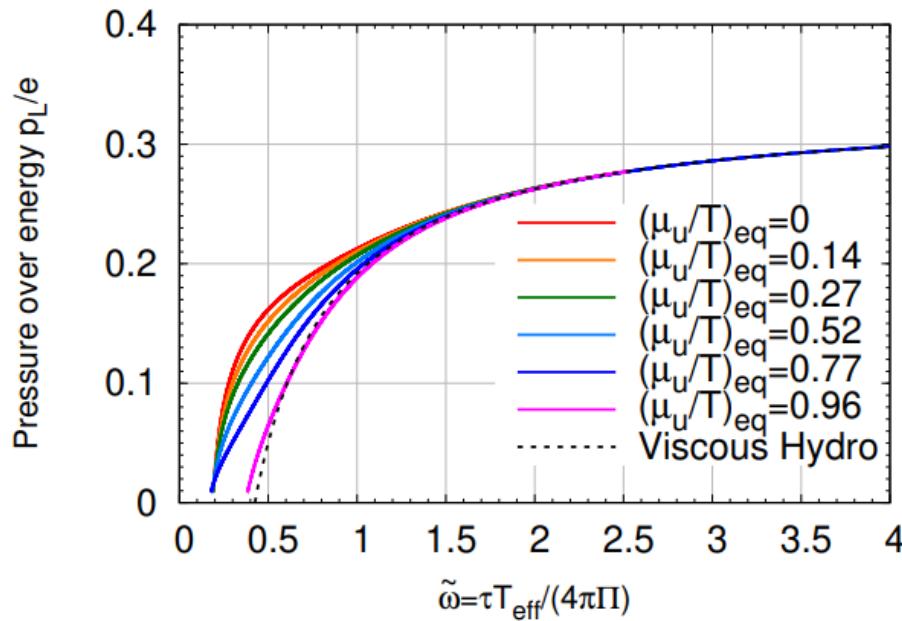


Kinetic and Chemical Equilibration with Long. Expansion

Hydrodynamic Attractor

Isotropization

System initially highly anisotropic with CGC inspired gluon dist. & finite charge density



1st-order hydrodynamics near equilibrium

$$\frac{p_L}{e} = \frac{1}{3} - \frac{16}{9} \frac{\eta}{(e+p)\tau} = \frac{1}{3} - \frac{4}{9\pi} \left(\frac{\eta T_{\text{eff}}}{e+p} \right) \frac{4\pi}{\tau T_{\text{eff}}} \text{ const. } \Pi$$

Isotropization:
Larger chemical potential

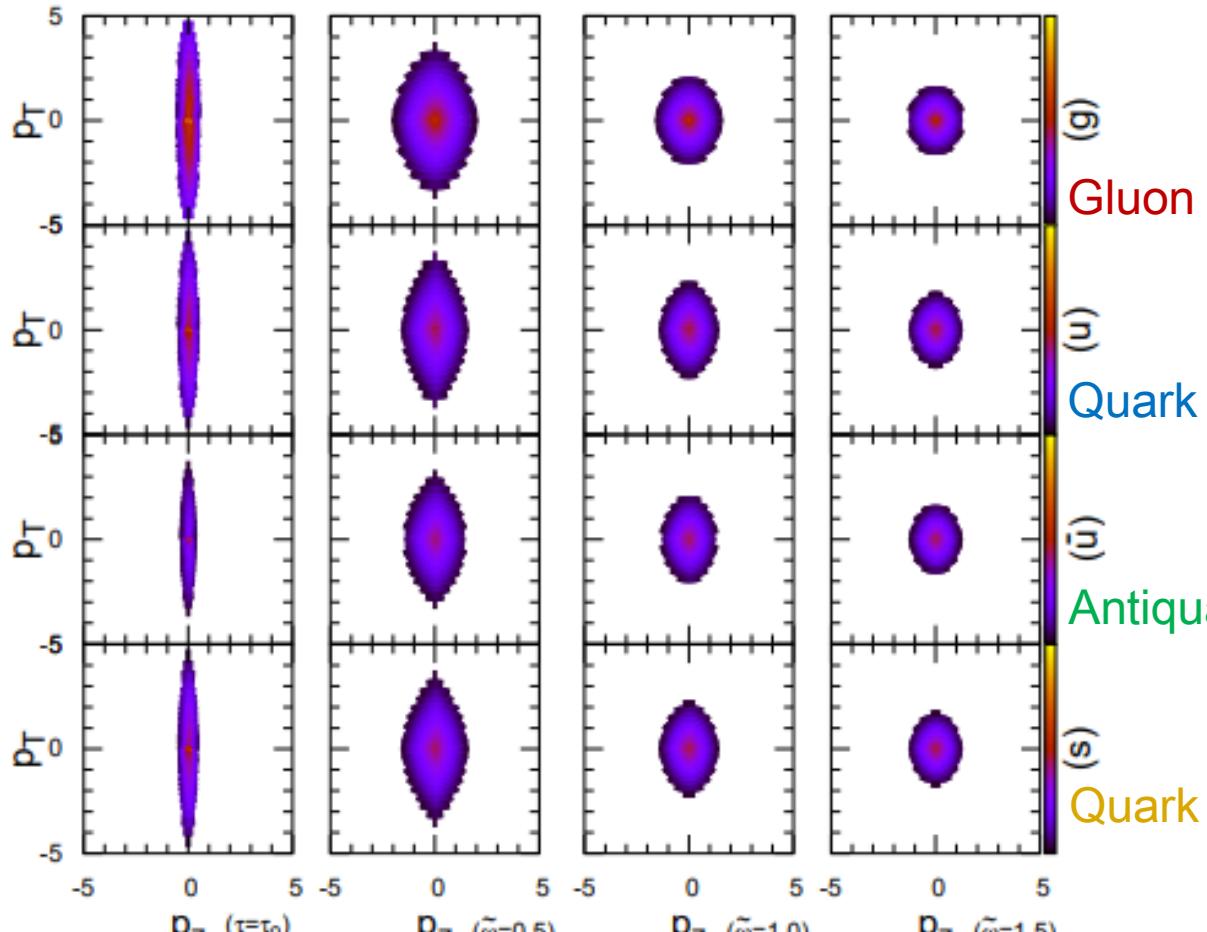
Larger fraction of quarks
↓
Slower isotropization

Ineffectiveness of quark interaction:
Color factor
Spin degeneracy
Quantum statistics

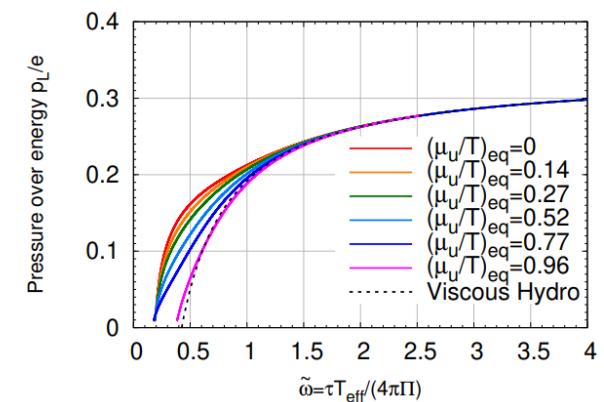
Non-equilibrium attractors
from kinetic theory

↓
effective constitutive
relations far-from equilibrium

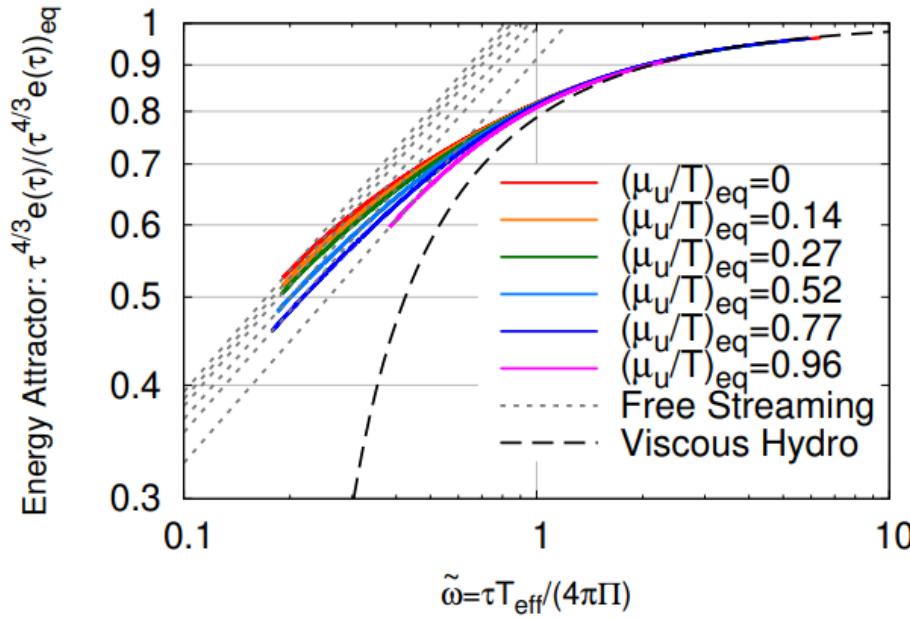
Isotropization



Gluon isotropy faster
 Quarks isotropy slower
 Systems eventually isotropy
 hydrodynamization
 ~ 2 kinetic equilibration time



Energy Attractor



Energy attractor

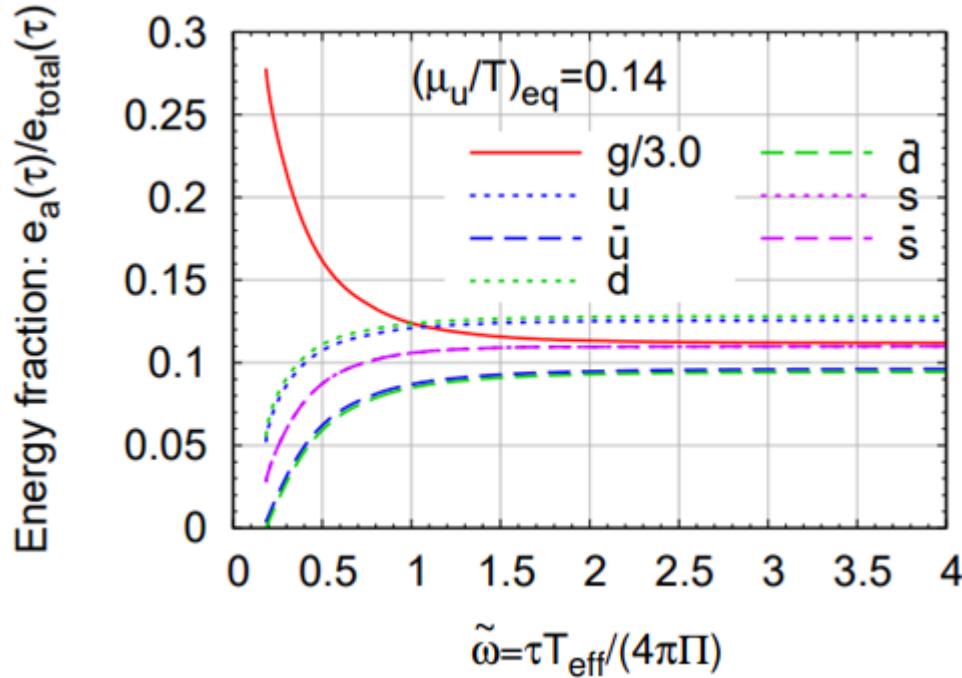
$$\mathcal{E} \left(\tilde{\omega} = \frac{T_{\text{eff}} \tau}{4\pi\Pi} \right) = \frac{\tau^{\frac{4}{3}} e}{(\tau^{\frac{4}{3}} e)_{eq}}$$

Overall Universal attractor

From conservation laws, connecting [initial state](#) to [hydrodynamics](#)

$$\begin{aligned} (\tau^{\frac{4}{3}} e)_{\tilde{\omega}} &= \frac{\mathcal{E}(\tilde{\omega})}{\mathcal{E}(\tilde{\omega}_0)} (\tau^{\frac{4}{3}} e)_0 \simeq \mathcal{E}(\tilde{\omega}) C_{\infty} \left(\frac{4\pi\Pi}{T_{0,\text{eff}} \tau_0} \right)^{\frac{4}{9}} (\tau^{\frac{4}{3}} e)_0 \\ (\tau \Delta n_f)_{\tilde{\omega}} &= (\tau \Delta n_f)_0 \end{aligned}$$

Realistic Matching



Match
net baryon density/chemical potential
charged particle multiplicity

$$\left(\frac{\mu_f}{T}\right)_{\tilde{\omega}} \approx \frac{6(\tau \Delta n_f)_0 \left(\frac{\pi^2}{30} \nu_{\text{eff}}\right)^{\frac{2}{3}}}{\nu_Q C_{\infty}^{\frac{3}{4}} \mathcal{E}(\tilde{\omega})^{\frac{3}{4}} (4\pi\Pi)^{\frac{1}{3}} (\tau e)_0^{\frac{2}{3}}}$$

$$\mu_u = \frac{1}{3}\mu_B + \frac{2}{3}\mu_Q$$

$$\mu_d = \frac{1}{3}\mu_B - \frac{1}{3}\mu_Q$$

$$\mu_s = \frac{1}{3}\mu_B - \frac{1}{3}\mu_Q - \mu_S$$

$$(s\tau)_{\text{eq}} = \frac{(e + p - \sum_f \mu_f \Delta n_f) \tau}{T}$$

Realistic matching to hydrodynamics at finite density
(lower energy heavy-ion collisions, forward rapidity, etc...)

Chemical equilibration ~ 2 kinetic equilibration

Summary

- Turbulent Nature of Quark-Gluon Plasma
 - Over-occupied system follows a self-similar universal scaling, not limited to pure Yang-Mills theory, even for moderately strongly coupled system
 - Under-occupied system follows a bottom-up thermalization
 - Radiations dominate the energy cascade
- Hydrodynamic Attractor at zero and finite charge density.
 - Ineffectiveness of quarks in isotropization / equilibration
 - Universal attractor towards hydrodynamics
 - Validation of hydrodynamics \sim kinetic equilibration time \ll isotropization time
 - Realistic matching to hydrodynamics at finite density by fixing certain scales (entropy, baryon density, etc..)

Thank you!