

Kinetic and Chemical Equilibration Of Quark Gluon Plasma at Zero and Finite Density

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In collaboration with Sören Schlichting

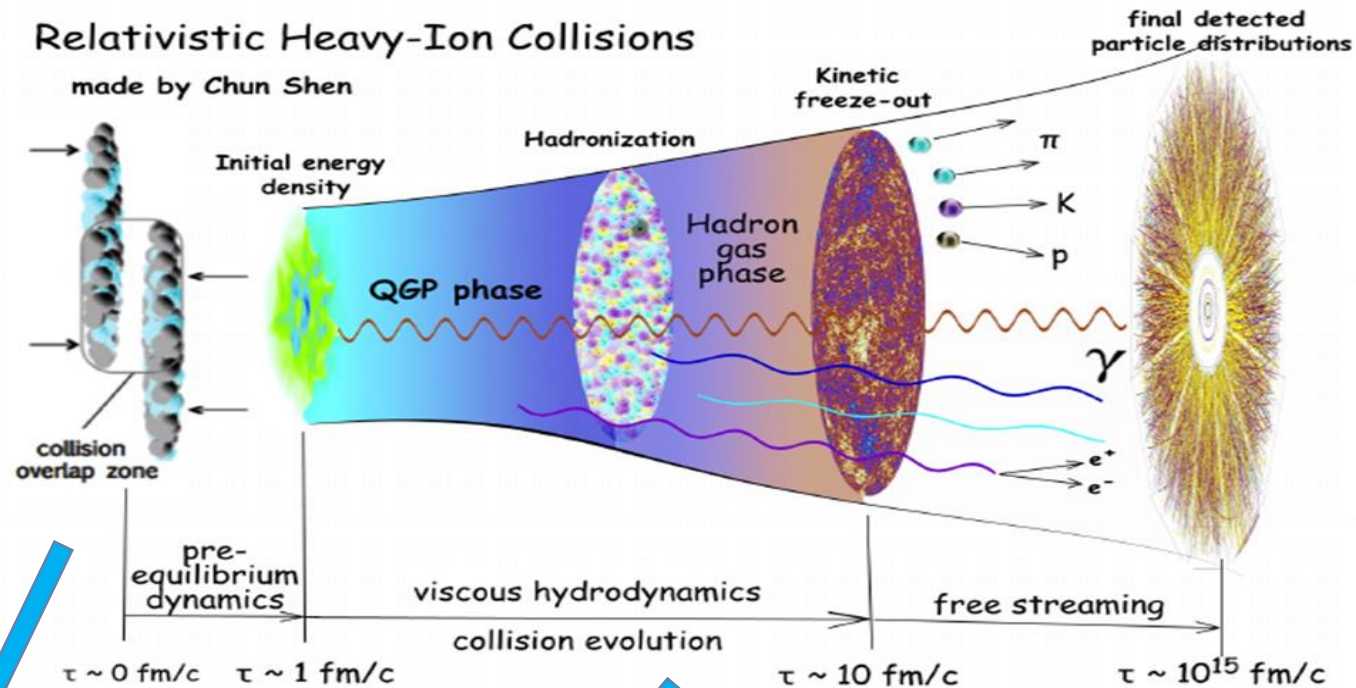
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Extreme Nonequilibrium QCD

International Center for Theoretical Sciences, India (Online)

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Pre-Equilibration Quark-Gluon Plasma



- Initial Collision
 - Off-Thermal
 - Gluon Saturation
-
- Pre-Equilibrium QGP
 - Thermalization
 - Chemical Equilibration
-
- Hydrodynamic
 - Thermal
 - Gluon/Quarks

Effective Kinetic QCD

Effective Kinetic Theory (Arnold, Moore, Yaffe) at LO

$$\frac{\partial}{\partial t} f_a(\vec{p}, t) = -C_a^{2 \leftrightarrow 2}[f](\vec{p}, t) - C_a^{1 \leftrightarrow 2}[f](\vec{p}, t)$$

AMY, JHEP01 (2003) 030

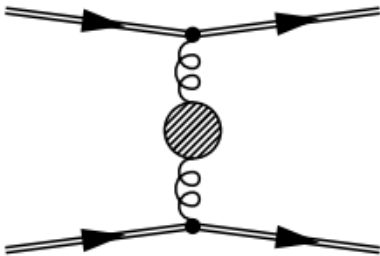
AMY, JHEP0206(2002)030

Kurkela, Mazeliauskas, PRD99 (2019) 054018

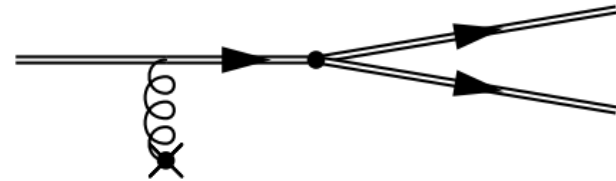
$$s = g, u, \bar{u}, d, \bar{d}, s, \bar{s}$$

Explicitly solve Boltzmann equation for massless **gluon** and **3 light quarks/anti-quarks** as an **integro-differential equation**

including **2-2 elastic processes** and **1-2 inelastic processes**



2-2: Color screening by Debye mass fit to HTL calculation

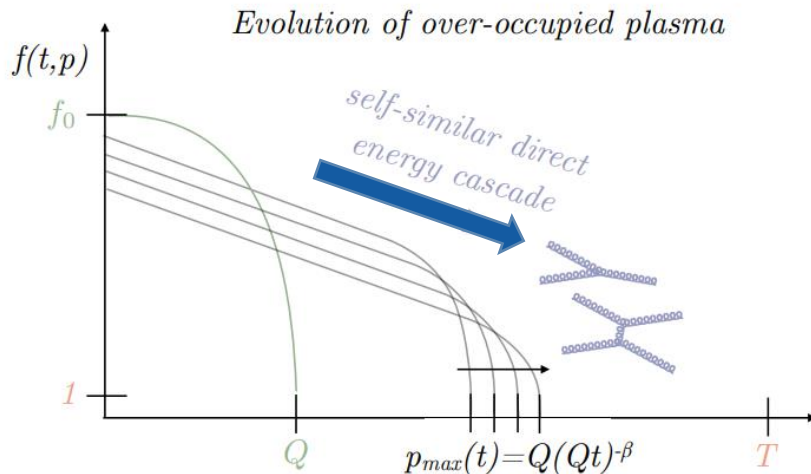


1-2: Collinear radiation including LPM effect via effective vertex resummation

Kinetic and Chemical Equilibration without Long. Expansion

Turbulence in Quark-Gluon Plasma

Weak-Coupling Thermalization



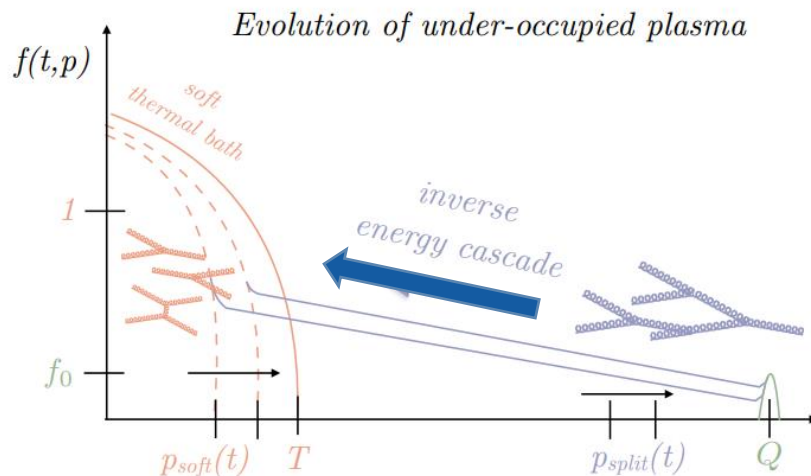
Over-occupied systems

$$\langle p \rangle \ll T$$

Direct energy cascade

Far from equilibrium

Large separation of scales



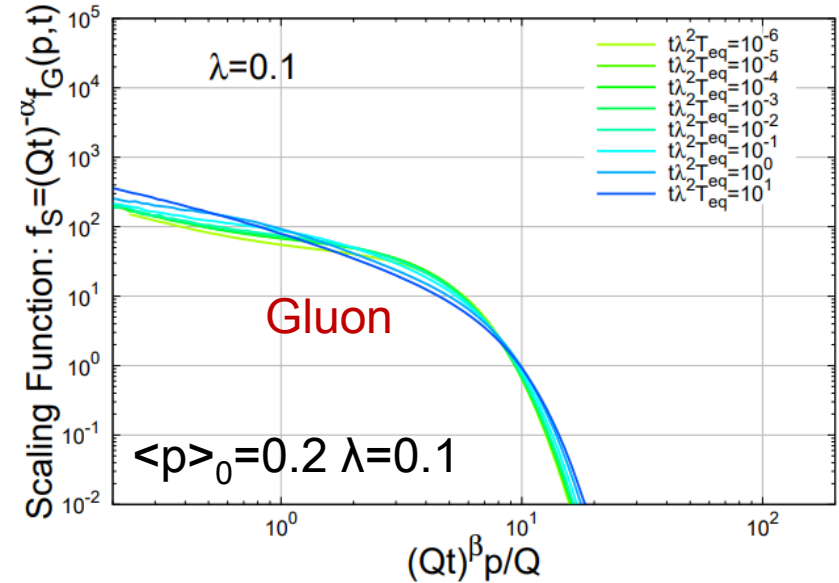
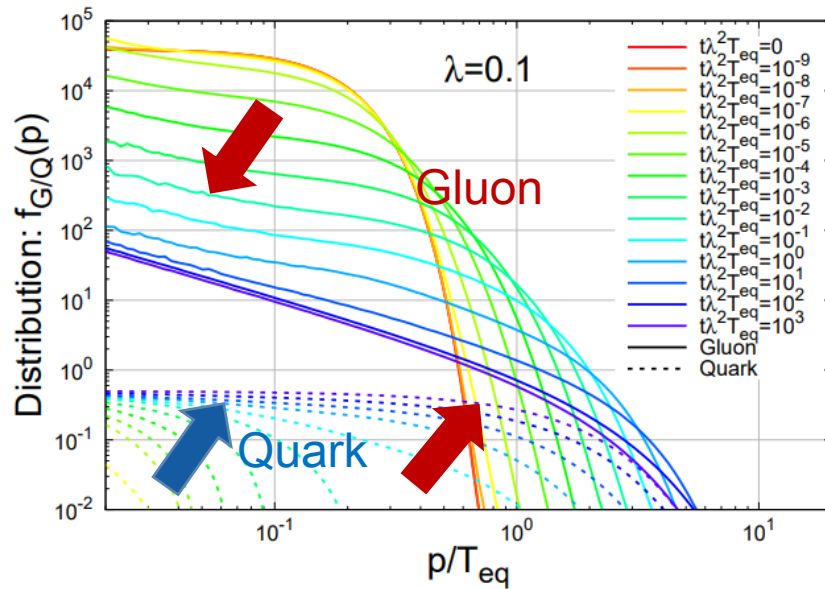
Under-occupied systems

$$\langle p \rangle \gg T$$

Inverse energy cascade

Schlichting, Teaney, Ann. Rev. of Nuc & Part. Sci. 69:447 (2019)

Over-Occupied Plasma



Self-similar Turbulence

$$f_G(p, t) = (Qt)^\alpha f_S \left((Qt)^\beta \frac{p}{Q} \right)$$

Scaling Exponents from pure Yang-Mills plasma

Also work for QCD plasma: **Gluon domination**

Quark spectra are following gluon spectrum

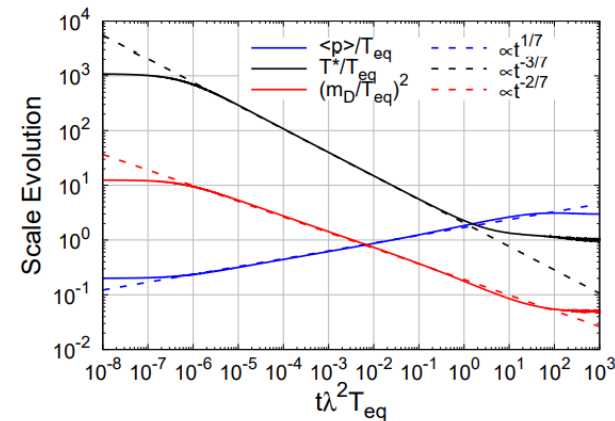
Universal Scaling Function

$$f_S \left((Qt)^\beta \frac{p}{Q} \right)$$

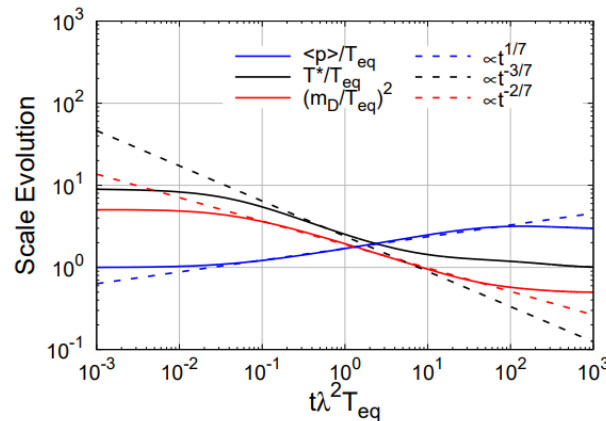
$$\alpha = -4/7, \beta = -1/7$$

Berges, Boguslavski, Schlichting,
Venugopalan, PRD89(2014)114007
Abraao York, Kurkela, Lu, Moore,
PED89(2014)074036

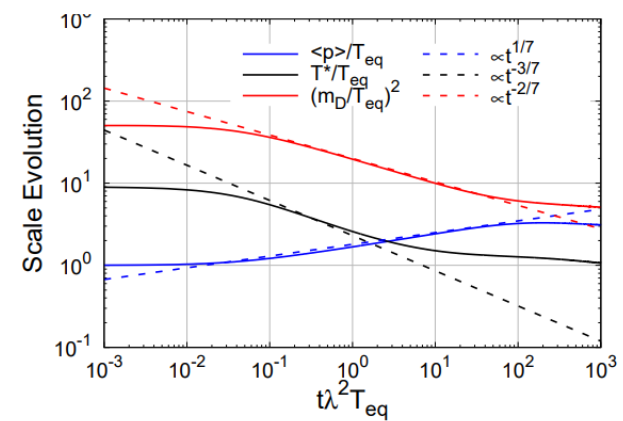
Over-Occupied Plasma



$\langle p \rangle_0 = 0.2 \quad \lambda = 0.1$



$\langle p \rangle_0 = 1.0 \quad \lambda = 1.0$



$\langle p \rangle_0 = 1.0 \quad \lambda = 10.0$

Self-similar Scaling: pow-law evolution

Not limited to pure Yang-Mills

Even work for stronger coupling

Chemical Equilibration

Later than kinetic equilibration

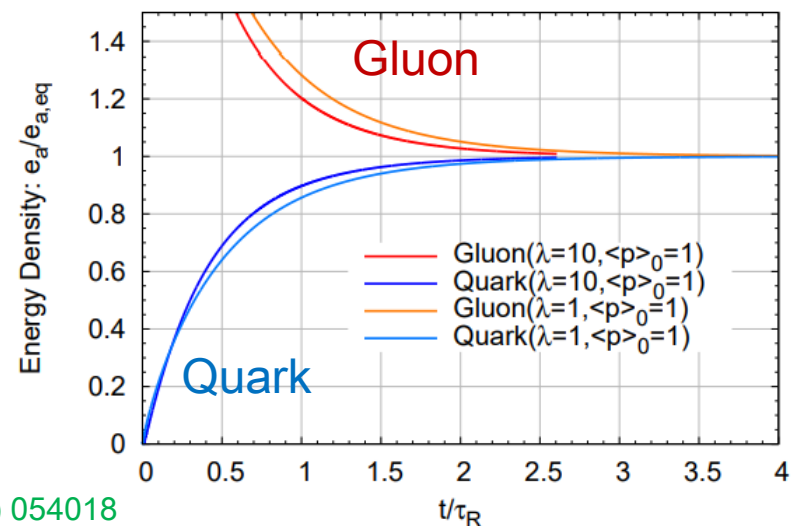
Equilibration relaxation time

$$\tau_R = \frac{4\pi\eta/s}{T_{eq}}$$

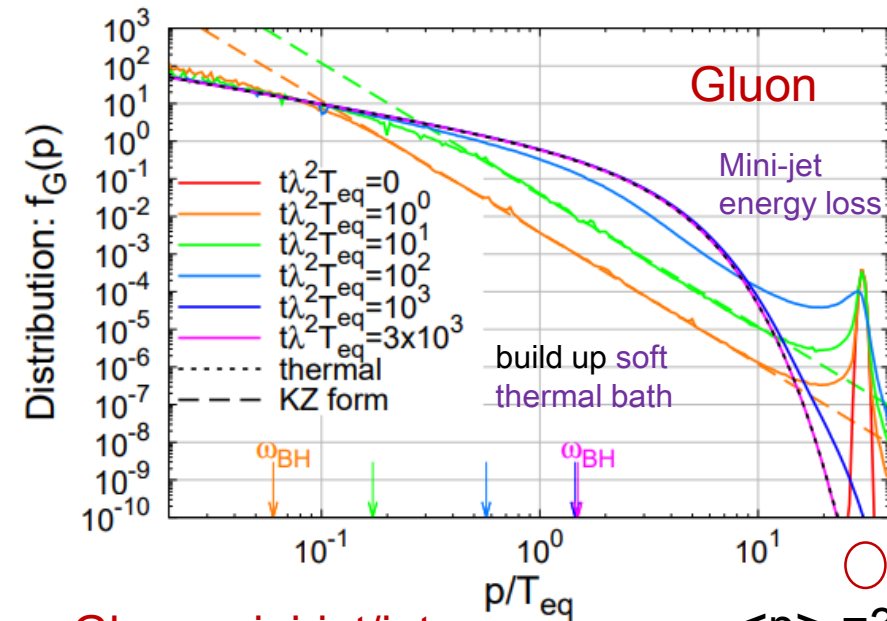
t'Hooft coupling

$$\lambda = 4\pi\alpha_s N_c$$

Kurkela, Mazeliauskas, PRD99 (2019) 054018
KOMPOST, PRC99 (2019) 034910



Under-Occupied Plasma



$$\langle p \rangle_0 = 30, \lambda = 1$$

Glueon mini-jet/jet:

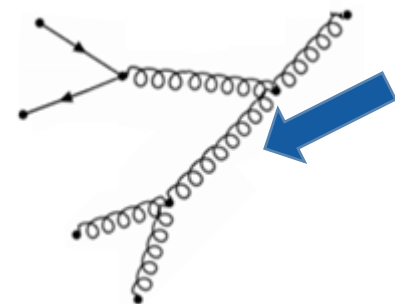
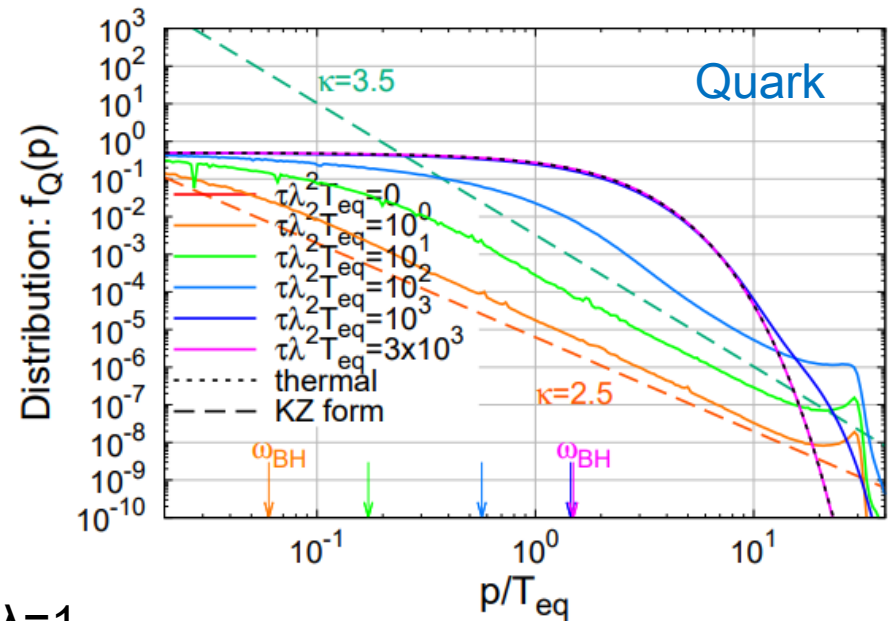
- Kolmogorov-Zakharov spectrum (exponent $\kappa = 7/2$ for glueon)

$$f_{KZ}(\vec{p}, t) = \eta(t) \left(\frac{\langle p \rangle_0}{p} \right)^\kappa$$

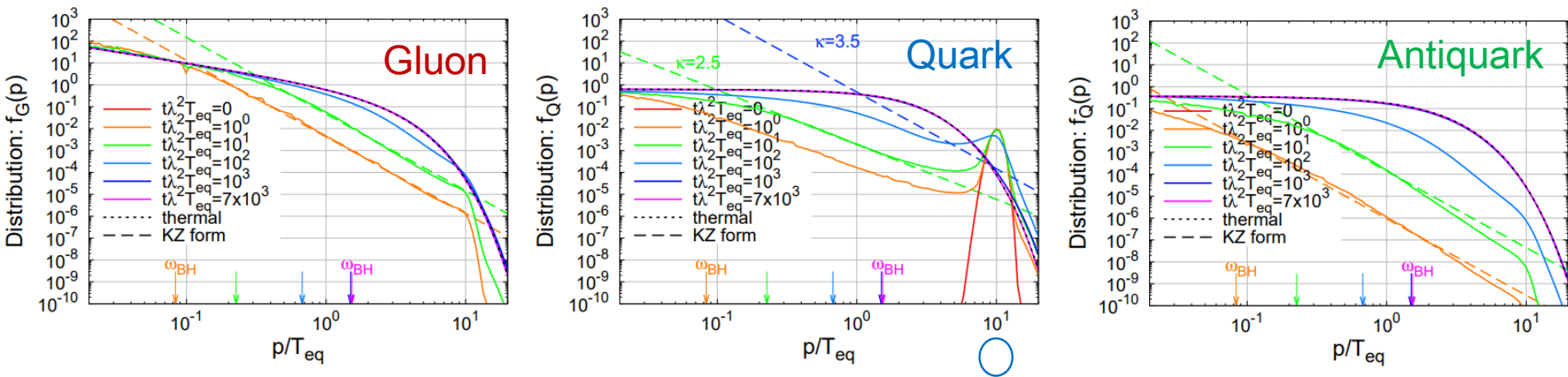
- Bottom-up thermalization

R. Baier, et al. PLB502(2001)51

- Emission of (soft) quarks and glueons
- Radiative breakup by multiple branchings -> build up soft thermal bath
- Mini-jet energy loss -> heating up thermal bath



Under-Occupied Plasma

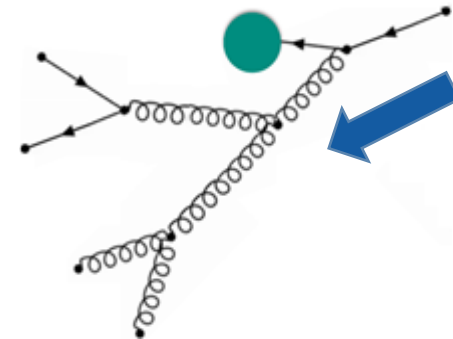


Quark mini-jet/jet:

- Bottom up thermalization
- Kolmogorov-Zakharov spectrum
 1. Quark follows $\kappa=5/2$ to $\kappa=7/2$
 2. Gluon follows $\kappa=7/2$
 3. Antiquark follows gluon (secondary production)
- Same pattern as for in-medium mini-jet/jet evolution with unified description of soft and hard sectors
- Equilibration of Jets

$$\langle p \rangle_0 = 10, \lambda = 1$$

Soudi, Schlichting, 2008.04928

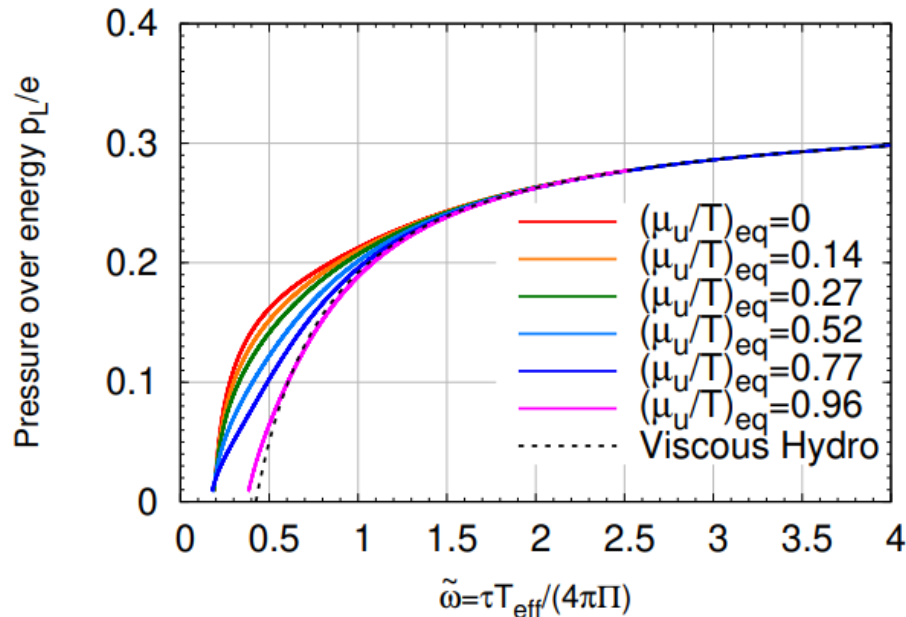


Kinetic and Chemical Equilibration with Long. Expansion

Hydrodynamic Attractor

Isotropization

System initially highly anisotropic with CGC inspired gluon dist. & finite charge density



1st-order hydrodynamics near equilibrium

$$\frac{p_L}{e} = \frac{1}{3} - \frac{16}{9} \frac{\eta}{(e+p)\tau} = \frac{1}{3} - \frac{4}{9\pi} \underbrace{\left(\frac{\eta T_{eff}}{e+p} \right)}_{\text{const. } \Pi} \frac{4\pi}{\tau T_{eff}}$$

Isotropization:

Larger chemical potential



Larger fraction of quarks



Slower isotropization

Ineffectiveness of quark interaction:

Color factor

Spin degeneracy

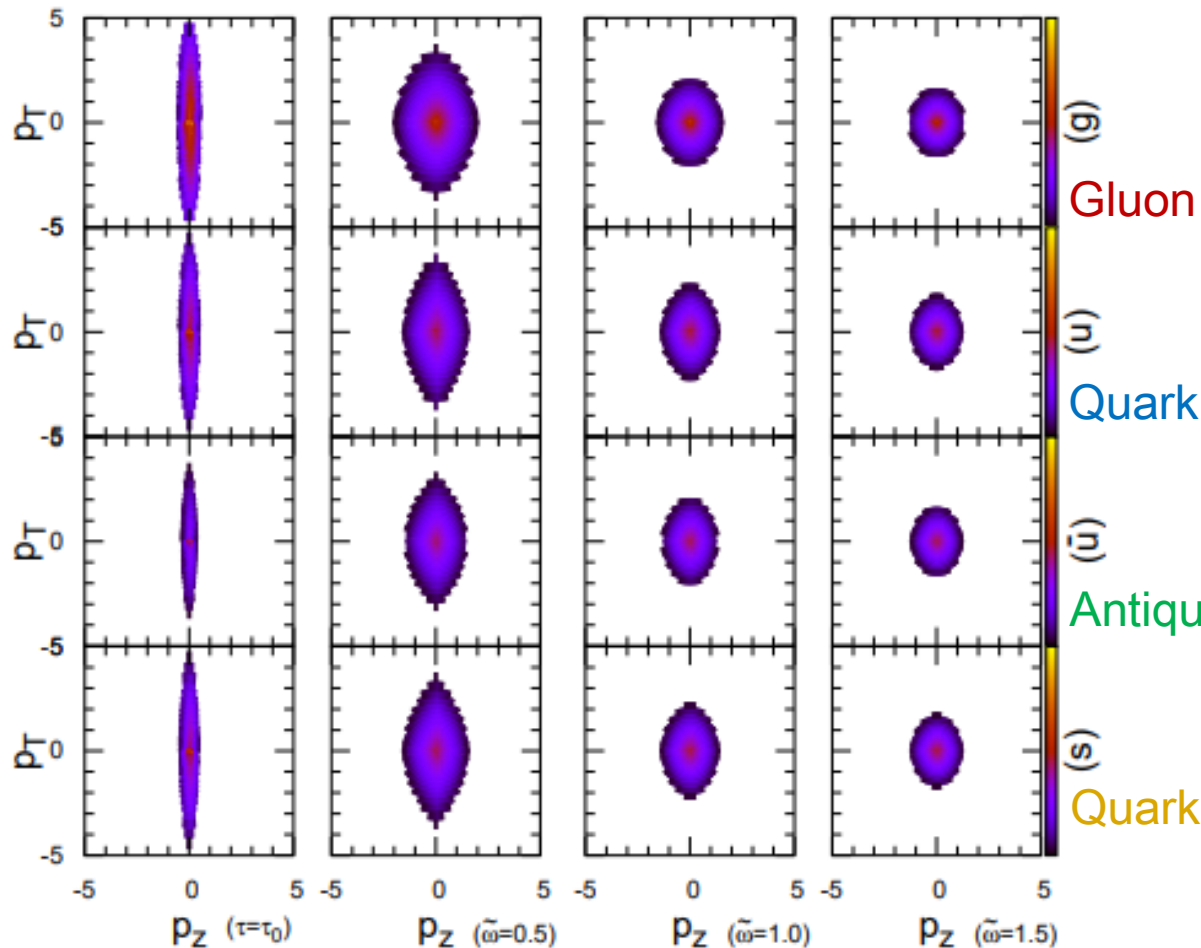
Quantum statistics

Non-equilibrium attractors
from kinetic theory

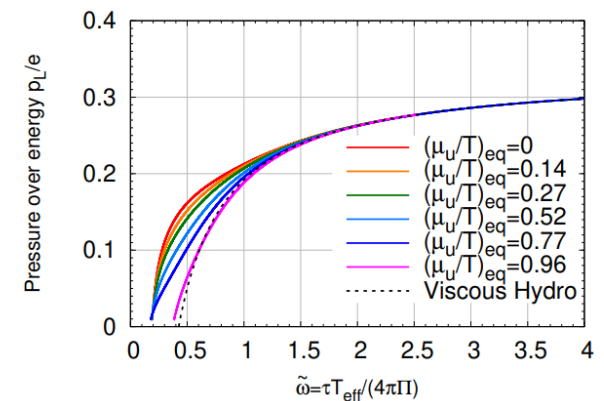


effective constitutive
relations far-from equilibrium

Isotropization

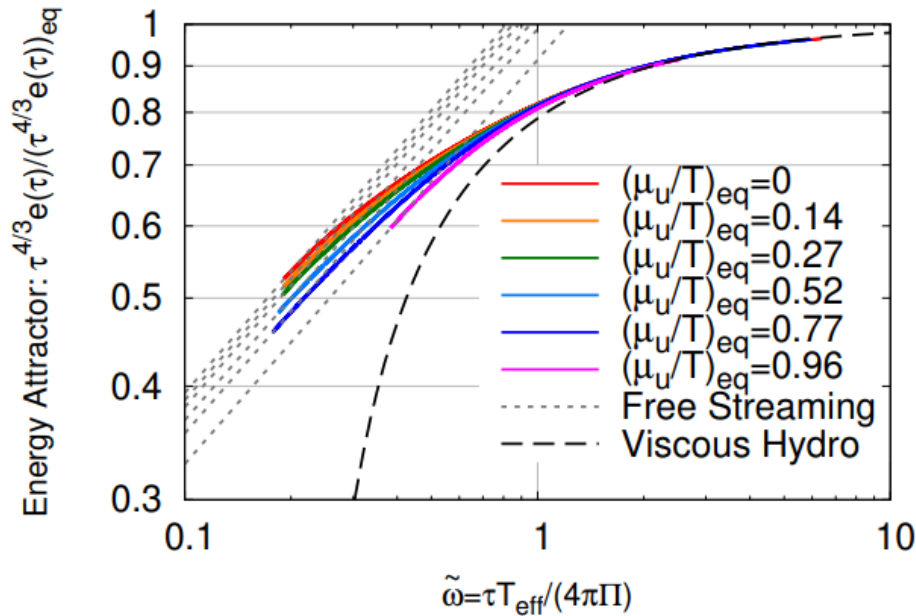


Gluon isotropy faster
 Quarks isotropy slower
 Systems eventually isotropy
 hydrodynamization
 ~2 kinetic equilibration time



$\mu/T=0.14$

Energy Attractor



Energy attractor

$$\mathcal{E}\left(\tilde{\omega} = \frac{T_{\text{eff}}\tau}{4\pi\Pi}\right) = \frac{\tau^{\frac{4}{3}}e}{\left(\tau^{\frac{4}{3}}e\right)_{eq}}$$

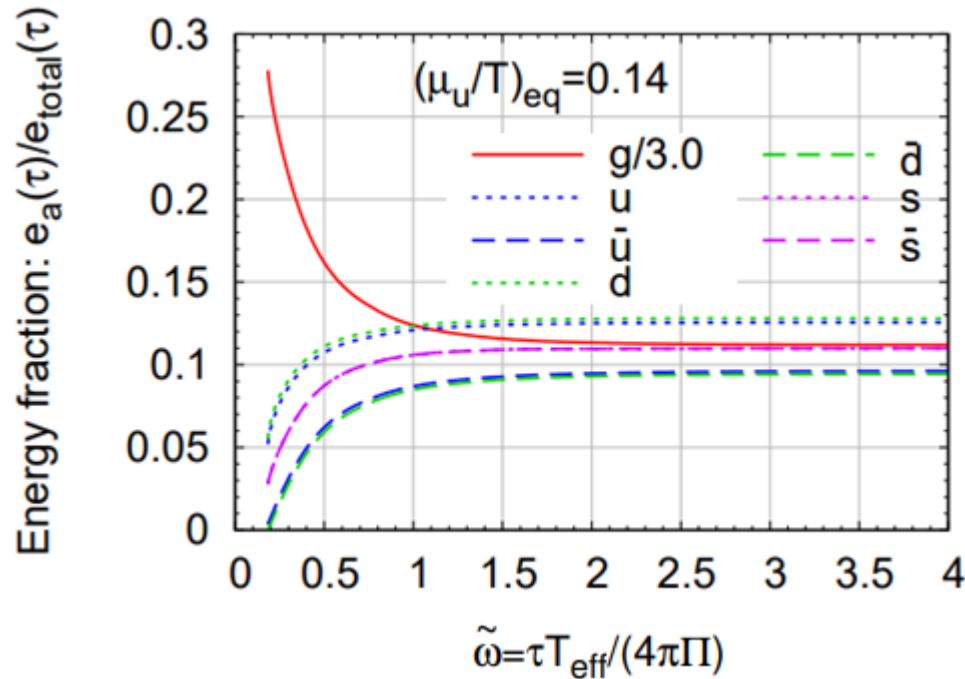
Overall Universal attractor

From conservation laws, connecting **initial state** to **hydrodynamics**

$$\left(\tau^{\frac{4}{3}}e\right)_{\tilde{\omega}} = \frac{\mathcal{E}(\tilde{\omega})}{\mathcal{E}(\tilde{\omega}_0)} \left(\tau^{\frac{4}{3}}e\right)_0 \simeq \mathcal{E}(\tilde{\omega}) C_{\infty} \left(\frac{4\pi\Pi}{T_{0,\text{eff}}\tau_0}\right)^{\frac{4}{9}} \left(\tau^{\frac{4}{3}}e\right)_0$$

$$(\tau\Delta n_f)_{\tilde{\omega}} = (\tau\Delta n_f)_0$$

Realistic Matching



Match

net baryon density/chemical potential
charged particle multiplicity

$$\left(\frac{\mu_f}{T}\right)_{\tilde{\omega}} \simeq \frac{6(\tau\Delta n_f)_0 \left(\frac{\pi^2}{30}\nu_{\text{eff}}\right)^{\frac{2}{3}}}{\nu_Q C_\infty^{\frac{3}{4}} \mathcal{E}(\tilde{\omega})^{\frac{3}{4}} (4\pi\Pi)^{\frac{1}{3}} (\tau e)_0^{\frac{2}{3}}}$$

$$\mu_u = \frac{1}{3}\mu_B + \frac{2}{3}\mu_Q$$

$$\mu_d = \frac{1}{3}\mu_B - \frac{1}{3}\mu_Q$$

$$\mu_s = \frac{1}{3}\mu_B - \frac{1}{3}\mu_Q - \mu_S$$

$$(s\tau)_{\text{eq}} = \frac{(e + p - \sum_f \mu_f \Delta n_f) \tau}{T}$$

Realistic matching to hydrodynamics at finite density
(lower energy heavy-ion collisions, forward rapidity, etc...)

Chemical equilibration \sim 2 kinetic equilibration

Summary

- Turbulent Nature of Quark-Gluon Plasma
 - Over-occupied system follows a self-similar universal scaling, not limited to pure Yang-Mills theory, even for moderately strongly coupled system
 - Under-occupied system follows a bottom-up thermalization
 - Radiations dominate the energy cascade
- Hydrodynamic Attractor at zero and finite charge density.
 - Ineffectiveness of quarks in isotropization / equilibration
 - Universal attractor towards hydrodynamics
 - Validation of hydrodynamics \sim kinetic equilibration time \ll isotropization time
 - Realistic matching to hydrodynamics at finite density by fixing certain scales (entropy, baryon density, etc..)

Thank you!