

Axion stars and their possible astrophysical manifestations

I. Tkachev

INR RAS, Moscow

11 November 2020, LTPDM ICTS, India

- Formation of Bose Stars

D.Levkov, A.Panin, & IT, PRL 121 (2018) 151301

- QCD axion miniclusters

- Axion Bose Star collapse

D.Levkov, A.Panin, & IT, PRL 118 (2017) 011301

- Cosmological and astrophysical implications

- Bose star is a self-gravitating clump of Bosons in the lowest energy state.

Ruffini & Bonazzola, Phys. Rev. 187 (1969) 1767

- May appear in Dark Matter models with light Bose particles.
Mainstream candidates - QCD axion or ALP in general:

Axion stars

IT, Sov. Astron. Lett. 12 (1986) 305

- Vast literature, but little attention to the problem of their formation.

- Interactions are needed to form Bose condensate
- But ALP couplings are extremely small

QCD axions

- Solve strong CP problem
- CDM: $m \approx 26 \mu\text{eV}$
- $\lambda \sim 10^{-50}$

String axions

- Appear in string models
- Fuzzy DM: $m \sim 10^{-22} \text{ eV}$
- $\lambda \sim 10^{-100}$

- Relaxation time is enhanced due to large phase space density f
IT, Phys. Lett. B 261 (1991) 289

$$\tau_R^{-1} \sim \sigma v n (1 + f) \quad \text{where } f \sim \frac{n}{(mv)^3} \gg 1$$

which is still not enough to beat small λ (except in rare axion miniclusters)

Bose condensation by gravitational interactions

Are we crazy?

- No
- $f \gg 1$ — classical fields
- $v \ll 1$ — nonrelativistic approximation
- Gravity but no other interactions

$$\begin{array}{c} \psi(t, x) \\ U(t, x) \end{array}$$

Field equations for light DM (Schrödinger-Poisson system)

$$\begin{aligned} i\partial_t\psi &= -\Delta\psi/2m + mU\psi \\ \Delta U &= 4\pi G(\underbrace{m|\psi|^2}_{\rho} - \langle\rho\rangle) \end{aligned}$$

Bose star is a stationary solution:
 $\psi = \psi_s(r)e^{-i\omega t}$

Solving these equations in time, we find Bose condensation!

Bose condensation by gravitational interactions

Are we crazy?

- No
- $f \gg 1$ — classical fields
- $v \ll 1$ — nonrelativistic approximation
- Gravity but no other interactions

$$\begin{array}{c} \psi(t, x) \\ U(t, x) \end{array}$$

Field equations for light DM (Schrödinger-Poisson system)

$$\begin{aligned} i\partial_t\psi &= -\Delta\psi/2m + mU\psi \\ \Delta U &= 4\pi G(\underbrace{m|\psi|^2}_{\rho} - \langle\rho\rangle) \end{aligned}$$

Bose star is a stationary solution:
 $\psi = \psi_s(r)e^{-i\omega t}$

Solving these equations in time, we find Bose condensation!

Bose condensation by gravitational interactions

Are we crazy?

- No
- $f \gg 1$ — classical fields
- $v \ll 1$ — nonrelativistic approximation
- Gravity but no other interactions

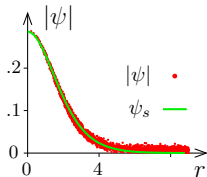
$$\left. \begin{array}{l} \psi(t, x) \\ U(t, x) \end{array} \right\}$$

Field equations for light DM (Schrödinger-Poisson system)

$$\begin{aligned} i\partial_t\psi &= -\Delta\psi/2m + mU\psi \\ \Delta U &= 4\pi G(\underbrace{m|\psi|^2}_{\rho} - \langle\rho\rangle) \end{aligned}$$

Bose star is a stationary solution:

$$\psi = \psi_s(r)e^{-i\omega t}$$



Solving these equations in time, we find Bose condensation!

Initial conditions

- Maximally mixed (virialized) initial state
- Subsequent evolution in kinetic regime

$$l_{coh} \sim (mv)^{-1} \ll R$$

$$(mv^2)^{-1} \ll \tau_{gr}$$

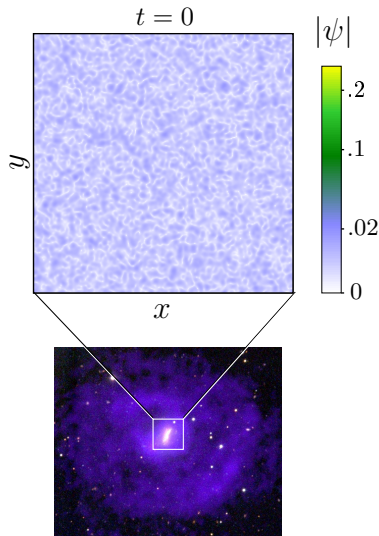
⇒ Random initial field:

$$\psi_p \propto \underbrace{e^{-p^2/2(mv_0)^2}}_{\text{momentum distribution}} \times \underbrace{e^{iA_p}}_{\text{random phases}}$$

$$\langle \psi(x)\psi(y) \rangle \propto e^{-\frac{(x-y)^2}{l_{coh}^2}}$$

$$l_{coh} = \frac{2}{mv_0}$$

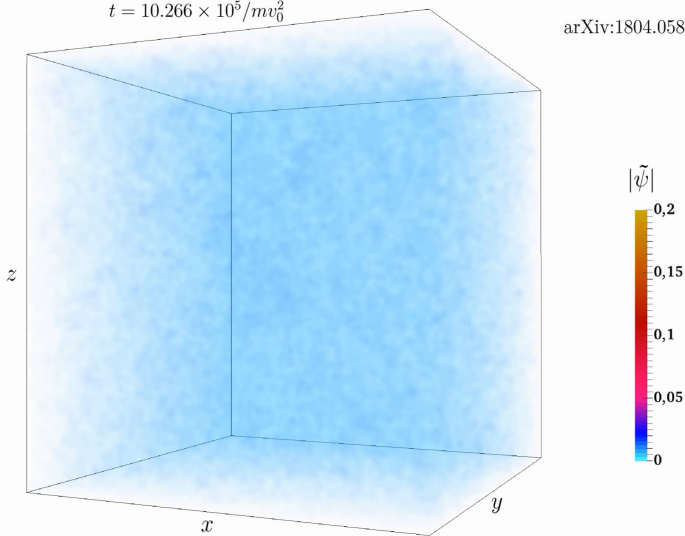
and $R \gg (mv_0)^{-1}$ is assumed



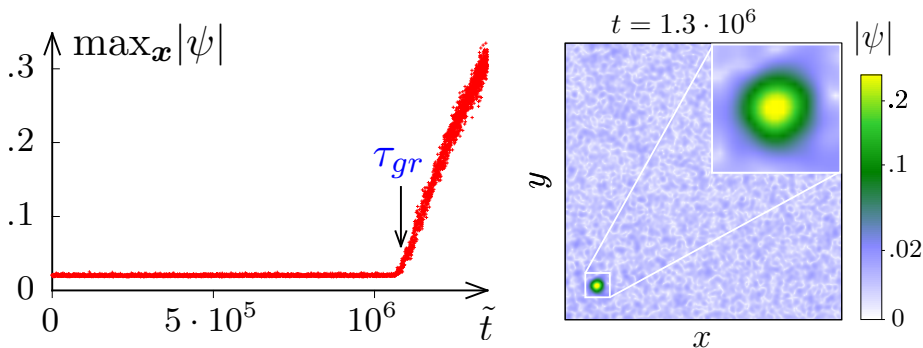
Virialized DM halo

$$t = 10.266 \times 10^5 / m v_0^2$$

arXiv:1804.05857



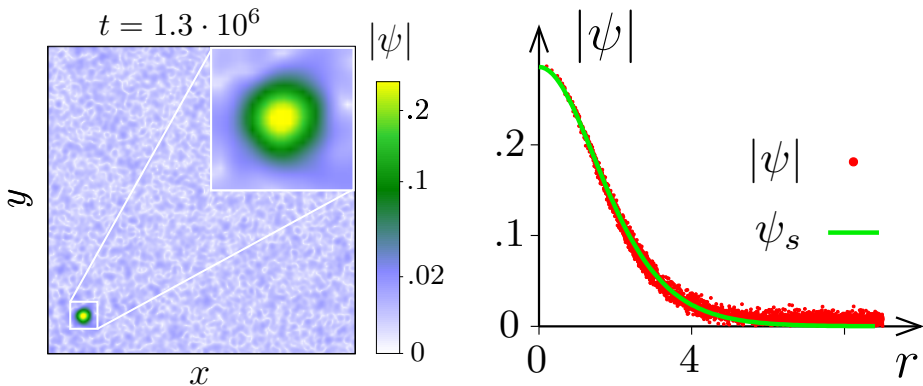
Maximum field value over the simulation box



This is **not** a Jeans instability

Simulation variables: $x = \frac{\tilde{x}}{mv_0}$, $t = \frac{\tilde{t}}{mv_0^2}$, $U = v_0^2 \tilde{U}$, $\psi = v_0^2 \tilde{\psi} \sqrt{\frac{m}{G}}$

It's a Bose star

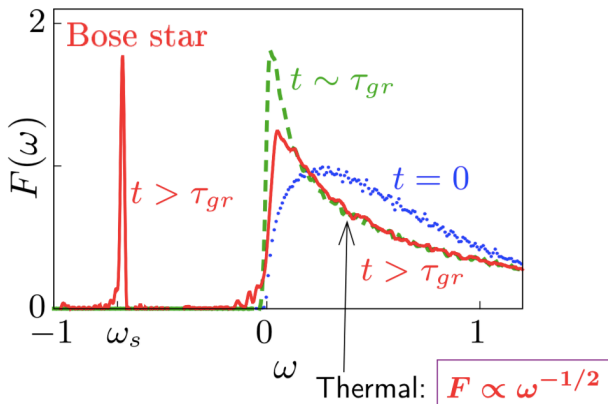


We observe formation of a Bose star at $t = \tau_{gr}$

Bose star appearance: another signature

Energy distribution at different moments of time

$$F(\omega, t) \equiv \frac{dn}{d\omega} = \int d^3x \int \frac{dt_1}{2\pi} \psi^*(t, x) \psi(t + t_1, x) e^{i\omega t_1 - t_1^2/\tau_1^2}$$



Landau equation — derivation

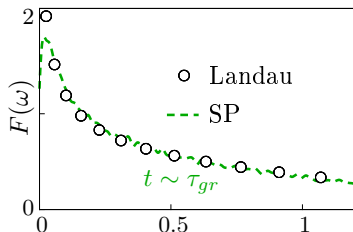
- **Perturbative** solution of Schrödinger-Poisson equation
- **Kinetic approximations** $(mv)^{-1} \ll x$, $(mv^2)^{-1} \ll t$
- Compute **Wigner distribution**

$$f_p(t, x) = \int d^3y e^{-ipy} \langle \psi(x + y/2) \psi^*(x - y/2) \rangle$$

random phase average

$$\partial_t f_p + \frac{p}{m} \nabla_x f_p - m \nabla_x \bar{U} \nabla_p f_p = \text{St } f_p$$

D.Levkov, A.Panin, & IT, PRL 121 (2018) 151301



Good agreement of lattice F and kinetic f ,

$$F(\omega) = \frac{mpf_p}{2\pi^2}, \quad \omega = \frac{p^2}{2m}$$

Landau equation — derivation

- **Perturbative** solution of Schrödinger-Poisson equation
- **Kinetic approximations** $(mv)^{-1} \ll x$, $(mv^2)^{-1} \ll t$
- Compute **Wigner distribution**

$$f_p(t, x) = \int d^3y e^{-ipy} \langle \psi(x + y/2) \psi^*(x - y/2) \rangle$$

random phase average

$$\partial_t f_p + \frac{p}{m} \nabla_x f_p - m \nabla_x \bar{U} \nabla_p f_p = \text{St } f_p \equiv \boxed{\frac{f}{\tau_R}} \leftarrow \text{relaxation time}$$

$\Downarrow$

$$f_p^3 \leftarrow \text{Bose amplification}$$

Time to Bose star formation: $\tau_{gr} = \underset{\substack{\uparrow \\ O(1) \text{ correction}}}{b} \tau_R = \frac{4\sqrt{2}b}{\sigma_{gr} v n f}$

Time to Bose star formation

$$\tau_{gr} = \frac{4\sqrt{2}b}{\sigma_{gr} v n f}$$

Rutherford cross section: $\sigma_{gr} \approx 8\pi(mG)^2 \Lambda / v^4$

$$\Lambda = \log(mvR)$$

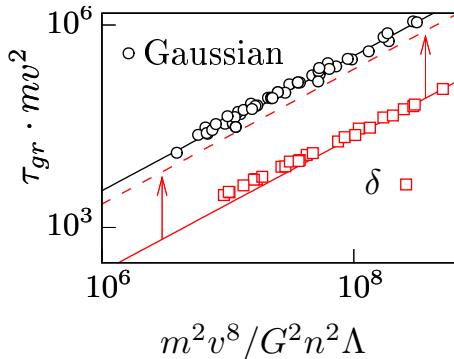
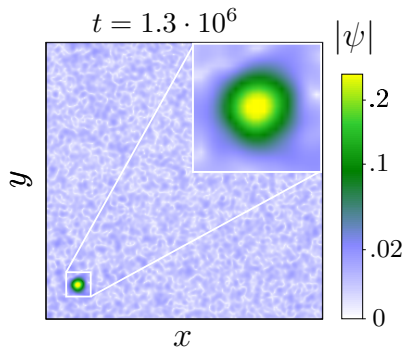
Coulomb logarithm

Average phase-space density: $f = 6\pi^2 n / (mv)^3$

$$\tau_{gr} = \frac{b\sqrt{2}}{12\pi^3} \frac{mv^6}{G^2 \Lambda n^2} = \frac{b\sqrt{2}\pi}{3G^2 m^5 \Lambda} f^{-2}$$

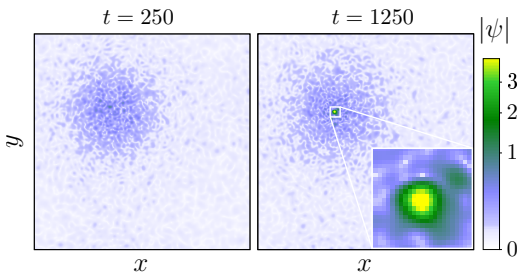
- Strongly depends on **local** quantities: n , v , f
- Involves **global** logarithm $\Lambda = \log(mvR)$

Kinetic scaling of τ_{gr} with parameters

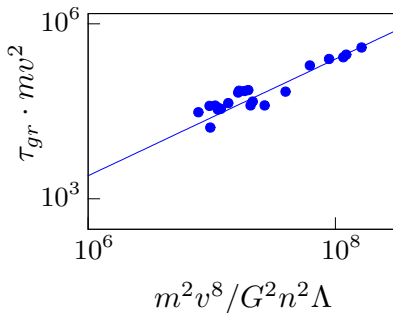


- Gaussian: $f_p \propto |\psi_p|^2 \propto e^{-p^2/(mv_0^2)}$, $b \approx 0.9$
- δ : $f_p \propto \delta(|p - p_0|)$, $b \approx 0.6$

Bose star formation in halo/minicluster



$$\tau_{gr} = \frac{b\sqrt{2}}{12\pi^3} \frac{mv^6}{G^2\Lambda n^2}$$



Virial velocity: $v^2 \sim 4\pi GmnR^2/3$

$$\tau_{gr} \sim \frac{0.05}{\Lambda} \frac{R}{v} (Rmv)^3$$

$\tau_{gr} \gg R/v \leftarrow$ free-fall time

$Rmv \sim 1$ — condense immediately

String axions

$$\tau_{bs} \sim 10^6 \text{ yr} \left(\frac{m}{10^{-22} \text{ eV}} \right)^3 \left(\frac{v}{30 \text{ km/s}} \right)^6 \left(\frac{0.1 M_{\odot}/\text{pc}^3}{\rho} \right)^2$$

Fornax dwarf galaxy



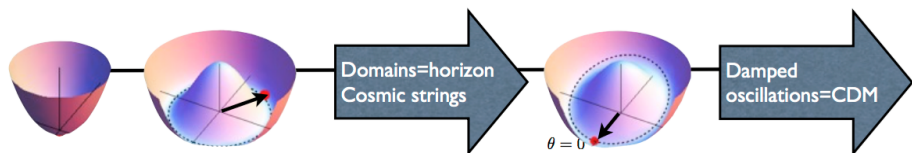
$$v \sim 11 \text{ km/s}$$

$$\rho \sim 0.1 M_{\odot}/\text{pc}^3$$

$$\tau_{bs} \sim 1000 \text{ yr}$$

Universe filled with Bose stars!

Models: QCD axion



Peccei-Quinn phase transition at $T \sim f_a$

Axion potential switches on at QCD epoch

$$V(a) = f_a m_a(T) [1 - \cos(\theta)]$$

$$\theta \equiv a/f_a$$

PQ phase transition before inflation is disfavored

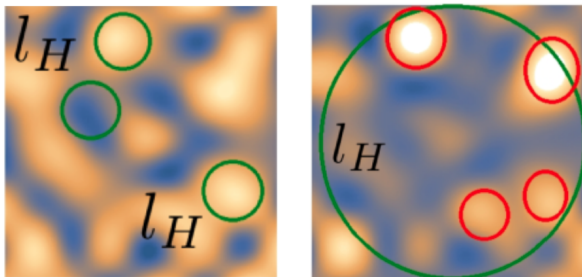
PQ phase transition after inflation:

Three contributions to axion DM

- Coherent oscillations of axion field (misalignment angle)
- Decay of PQ strings
- Decay of QCD axion domain walls

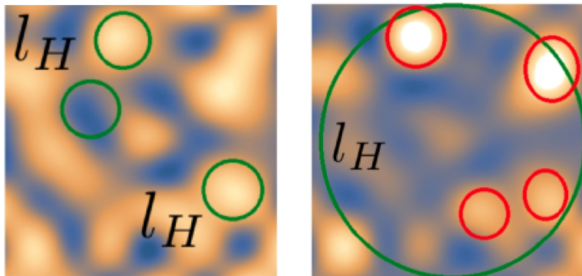
see lectures by David Marsh, this workshop

PQ phase transition after inflation $\rightarrow$ Miniclusters



- After phase transition $0 < \theta < 2\pi$ from horizon to horizon, but $\theta \approx \text{const}$ on a horizon scale l_H
- Dark Matter should be very clumpy
- Mass scale of the clumps is set by $M \sim 10^{-11} M_\odot$, which is DM mass within horizon at $T_{\text{osc}} \approx 1 \text{ GeV}$

PQ phase transition after inflation $\rightarrow$ Miniclusters

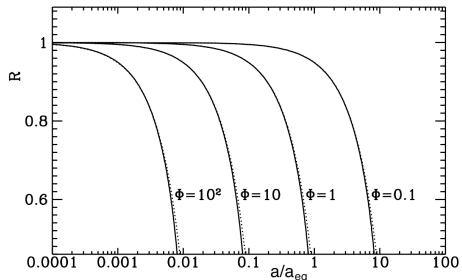


- Naively, initial DM density contrast is $\delta\rho_a/\rho_a \equiv \Phi \sim 1$
- In fact, very dense objects can form, $\Phi \gg 1$, since for $\theta \sim 1$ the axion **attractive** self-coupling is non-negligible,

$$V(a) = m^2 f_a^2 \left(\frac{\theta^2}{2} - \frac{\theta^4}{4!} + \dots \right)$$

E. Kolb & IT, Phys.Rev. D49 (1994) 5040

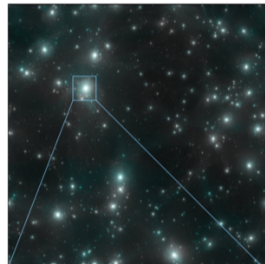
Minicluster formation around equality



A clump becomes gravitationally bound at $T \approx \Phi T_{\text{eq}}$, i.e. its density today

$$\rho_{\text{mc}} \approx 140 \Phi^3 (1 + \Phi) \bar{\rho}_a(T_{\text{eq}})$$

E.Kolb & IT, Phys.Rev. D50 (1994) 769

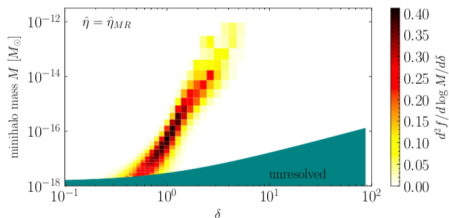


B.Eggemeier, et al arXiv:1911.09417

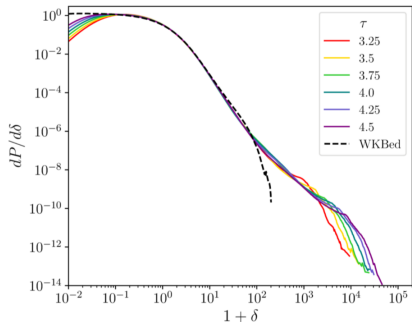
Bose-star formation: QCD axions

$$\tau_{bs} \sim \frac{10^9 \text{ yr}}{\Phi^4} \left(\frac{M_c}{10^{-13} M_\odot} \right)^2 \left(\frac{m}{26 \mu\text{eV}} \right)^3$$

Mass fraction in miniclusters



M. Buschmann, J. Foster, B. Safdi,
arXiv:arXiv:1906.00967



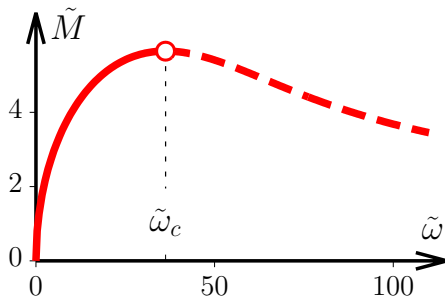
A. Vaquero et al (2019)

- $\Phi \sim 1, M \sim 10^{-16} M_\odot \Rightarrow \tau_{bs} \sim 10^3 \text{ yr}$
- $\Phi \sim 5, M \sim 10^{-13} M_\odot \Rightarrow \tau_{bs} \sim 10^6 \text{ yr}$

Universe filled with axion Bose stars!

$$V(a) = m^2 f_a^2 \left(\frac{\theta^2}{2} - \frac{\theta^4}{4!} + \dots \right)$$

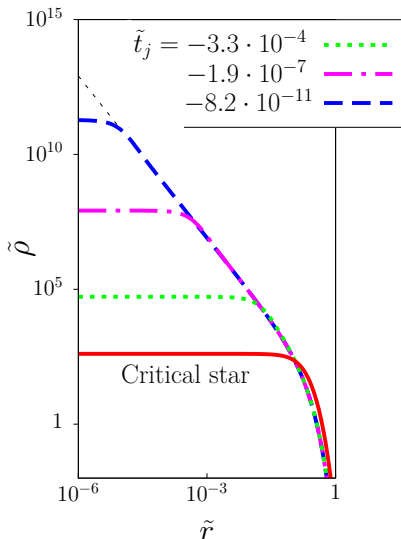
Self-coupling of axions is negative and axion Bose stars are unstable against collapse.



Here ω is gravitational binding energy,

$$\psi = \psi_s(r) e^{-i\omega t}$$

Self-similar wave collapse



$$\rho \propto \frac{1}{r^2} \Rightarrow$$

$$\Phi(r) \propto \log(r) \Rightarrow$$

Black holes can form if

$$f_a \sim M_{\text{Pl}}$$

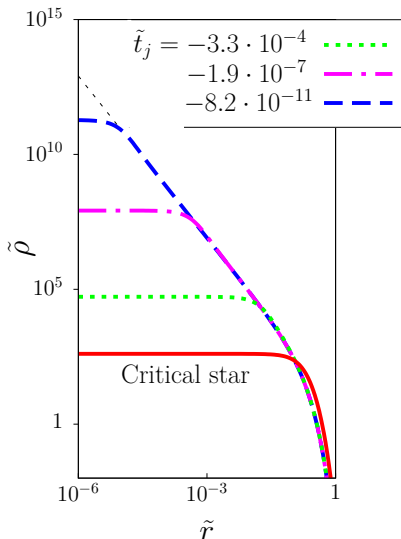
T. Helfer et al. JCAP 03 (2017) 055

Black holes does not form if

$$f_a < M_{\text{Pl}}$$

What is outcome then?

Self-similar wave collapse



$$\rho \propto \frac{1}{r^2} \Rightarrow$$

$$\Phi(r) \propto \log(r) \Rightarrow$$

Black holes can form if

$$f_a \sim M_{\text{Pl}}$$

T. Helfer et al. JCAP 03 (2017) 055

Black holes does not form if

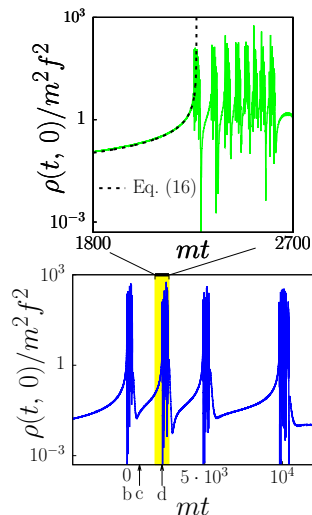
$$f_a < M_{\text{Pl}}$$

What is outcome then?

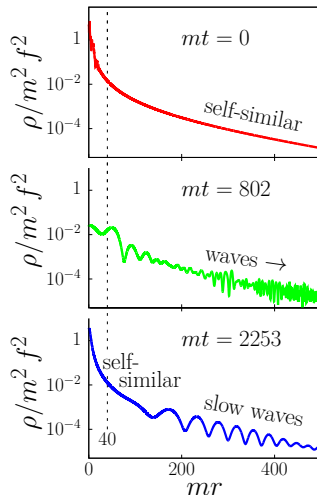
Collapse, stage II: Relativistic Bosenova

Repeated explosions

Field evolution in the center



Radial profiles at different times



- Less diffuse DM $\Rightarrow$ smaller signals in DM detectorts
- Gravitational lensing, microlensing and femtolensing
- Decay of Bose stars
 - Can produce black holes if $f_a \sim M_{\text{Pl}}$
 - Decay to relativistic self *D.Levkov, A.Panin, & IT, PRL 118 (2017) 011301*
 - Resolution of tension between low and high z observations?
 - Decay to radiophotons *D.Levkov, A.Panin, & IT, Phys.Rev.D 102 (2020) 023501*
 - Produces clear signature, emission line at $\nu = m_a/2$
 - Can produce excess radio-background (ARCADE?)
 - Relation to FRB?
- Coalescence $\Rightarrow$ specific signal in gravitational waves?

- Bose condensation by gravitational interactions is very efficient
- Large fraction of axion dark matter may consist of Bose stars
- Phenomenological implications of axion star existence are reach and deserve further studies