



Kobayashi-Maskawa Institute
for the Origin of
Particles and the Universe



名古屋大学
NAGOYA UNIVERSITY

Axions, Dark Matter, and the Primordial Density Perturbation

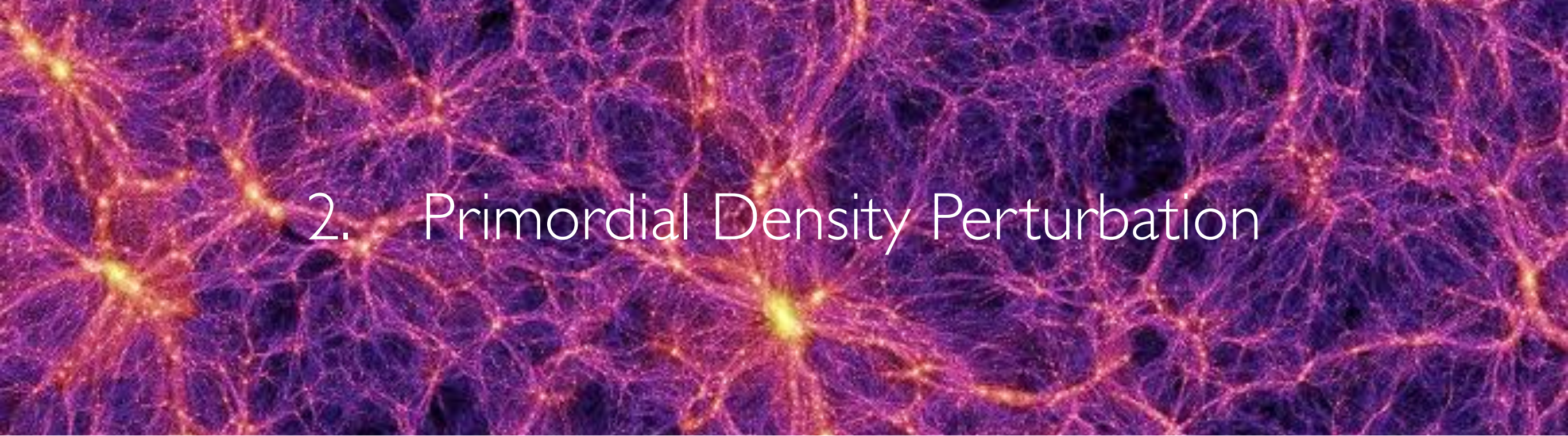
Takeshi Kobayashi

TK, Ubaldi 1907.00984, 2006.09389
TK 2005.01741

AXIONS FOR:



1. Dark Matter



2. Primordial Density Perturbation

* In this talk, an “axion” refers to a generic PNGB of a spontaneously broken global $U(1)$ (e.g. QCD axion, string axions)



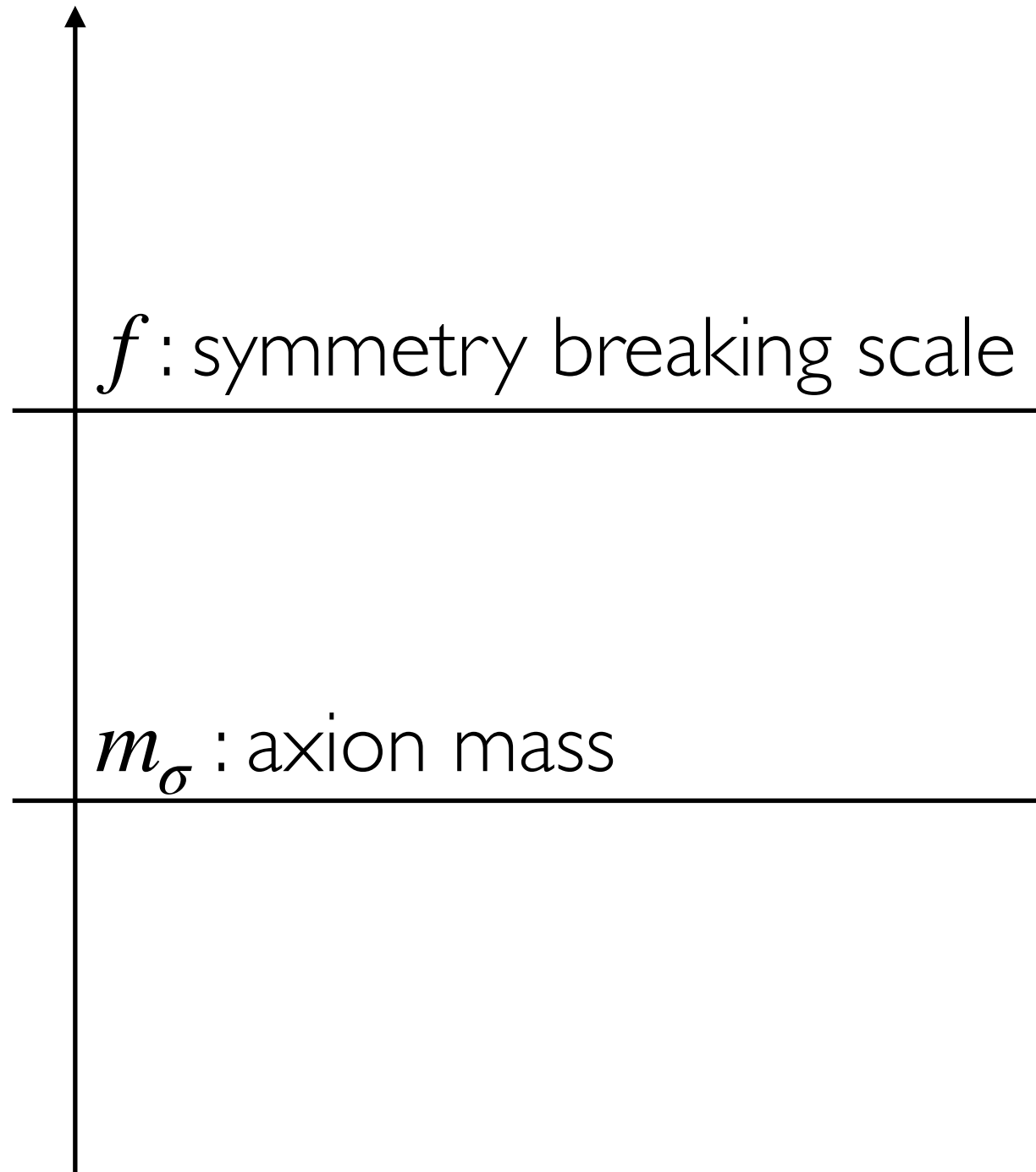
I. Dark Matter

“Inflaxion” mechanism for producing axion DM

TK, Ubaldi 1907.00984, 2006.09389

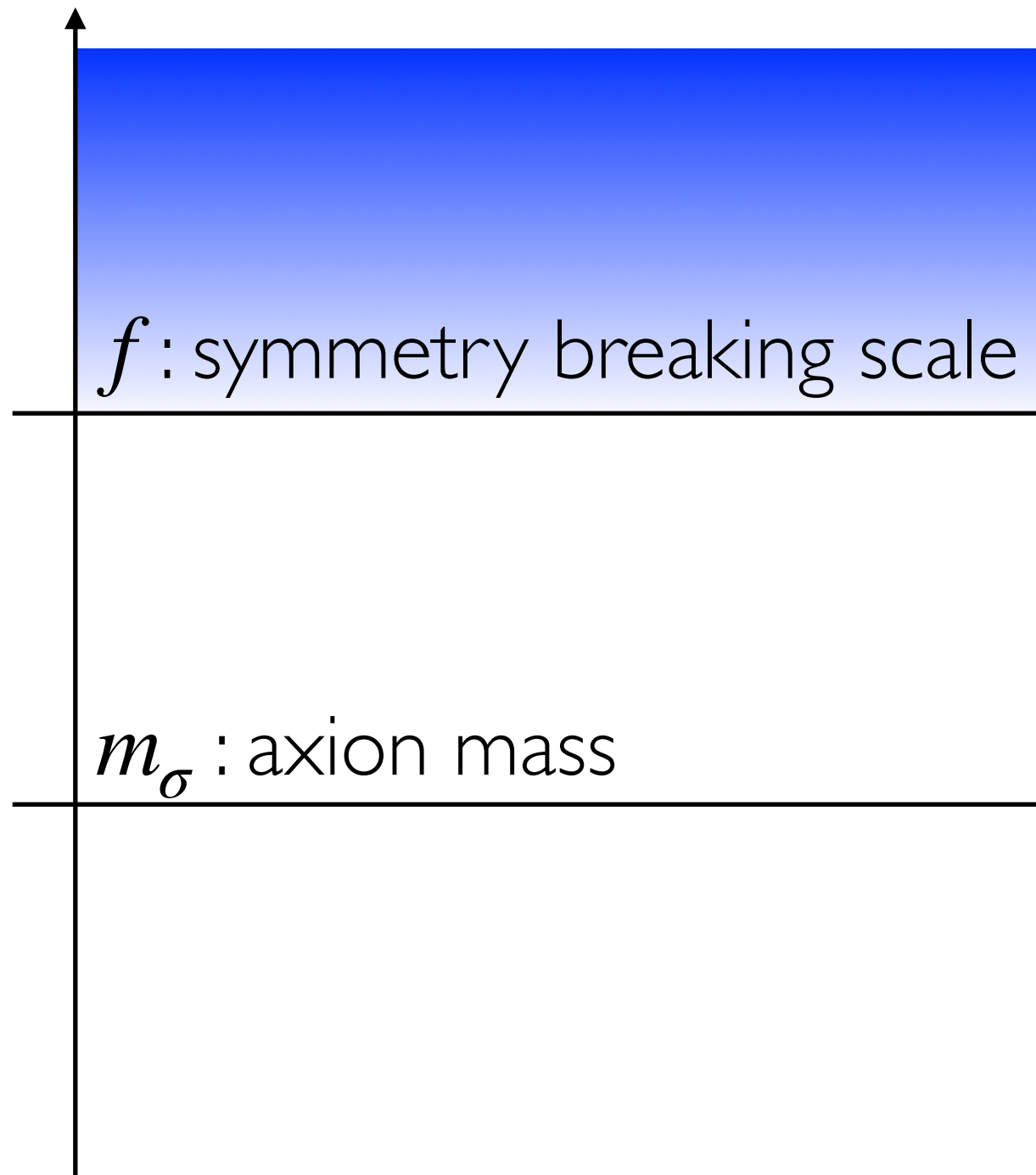
PRODUCTION OF AXION DARK MATTER

H_{inf} (and/or T_{reh})



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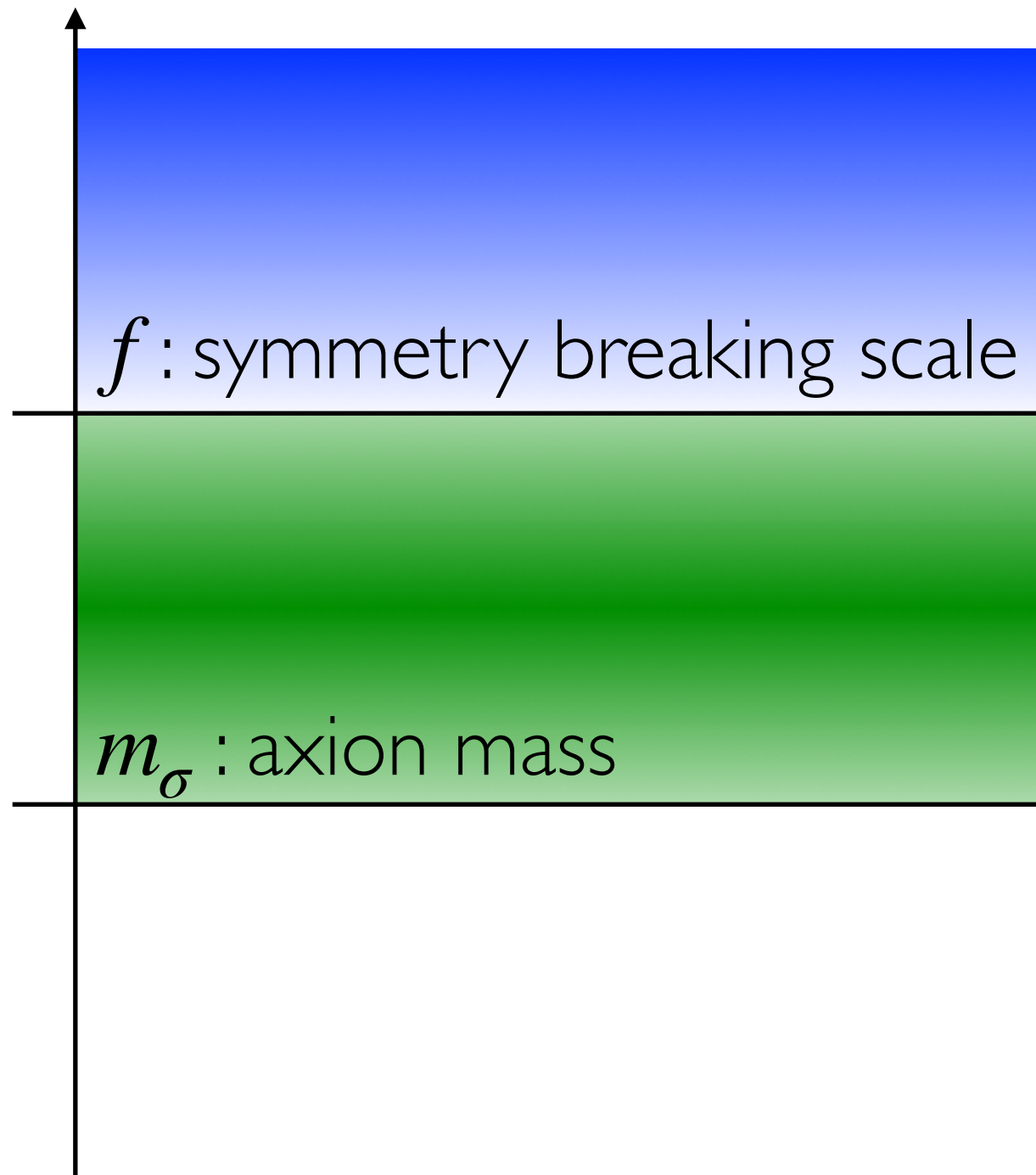
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emission from
topological defects

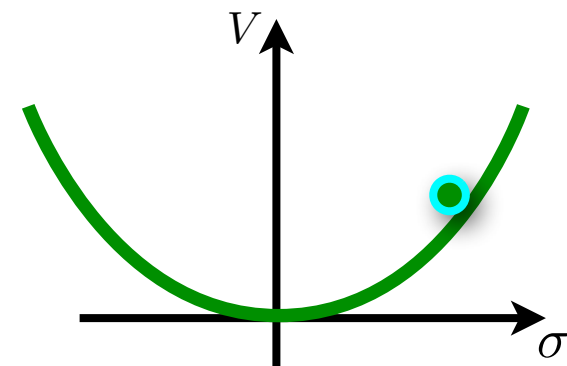
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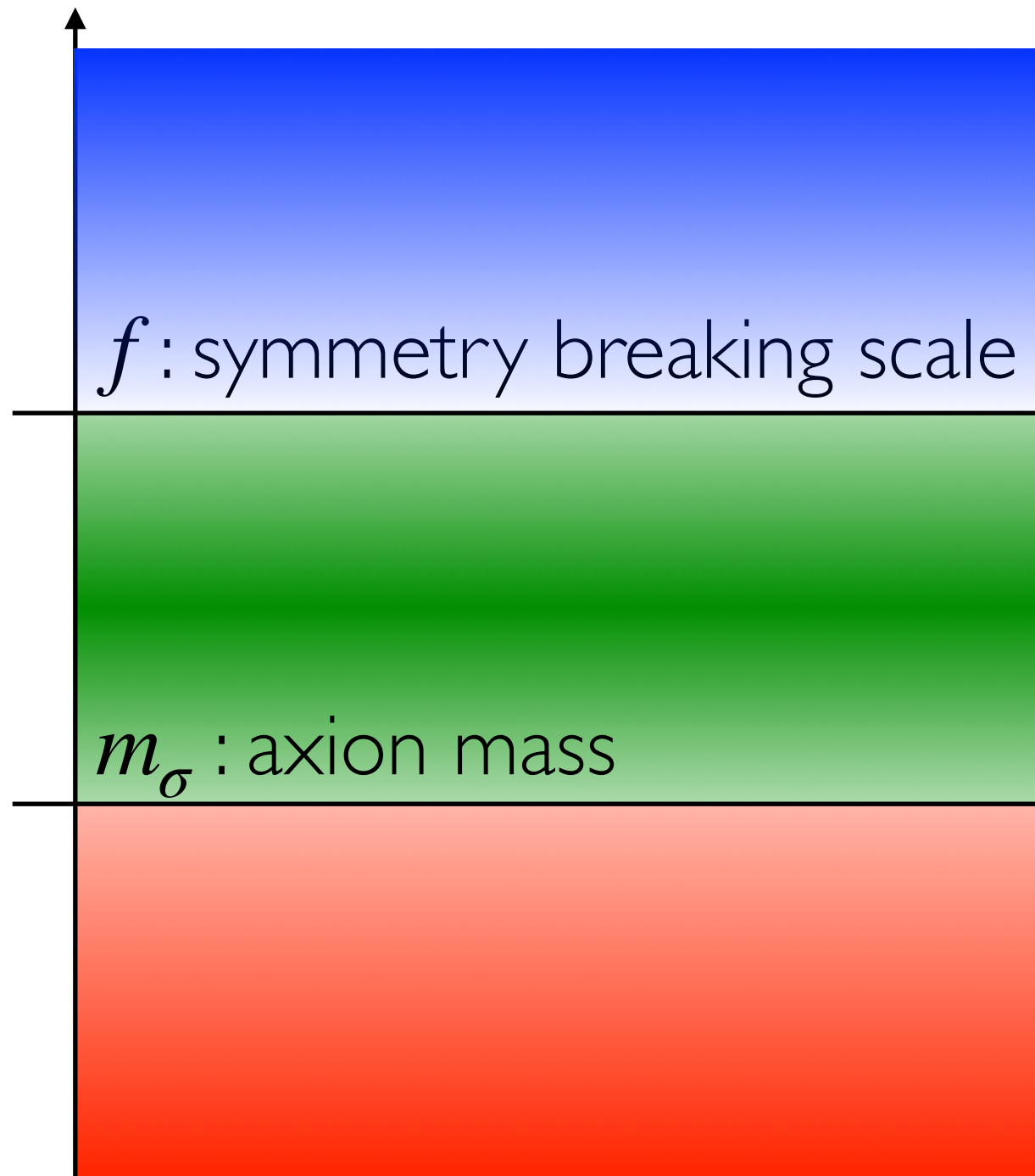
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PRODUCTION OF AXION DARK MATTER

H_{inf} (and/or T_{reh})



emission from
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influxion

INFLAXION MECHANISM

$$\frac{\mathcal{L}}{\sqrt{-g}} = -\frac{1}{2}(\partial\sigma)^2 - \frac{1}{2}m_\sigma^2\sigma^2 - \frac{1}{2}(\partial\phi)^2 - V(\phi)$$

σ : axion

ϕ : inflaton

INFLAXION MECHANISM

$$\frac{\mathcal{L}}{\sqrt{-g}} = -\frac{1}{2}(\partial\sigma)^2 - \frac{1}{2}m_\sigma^2\sigma^2 - \frac{1}{2}(\partial\phi)^2 - V(\phi) - \alpha \partial\sigma \cdot \partial\phi$$

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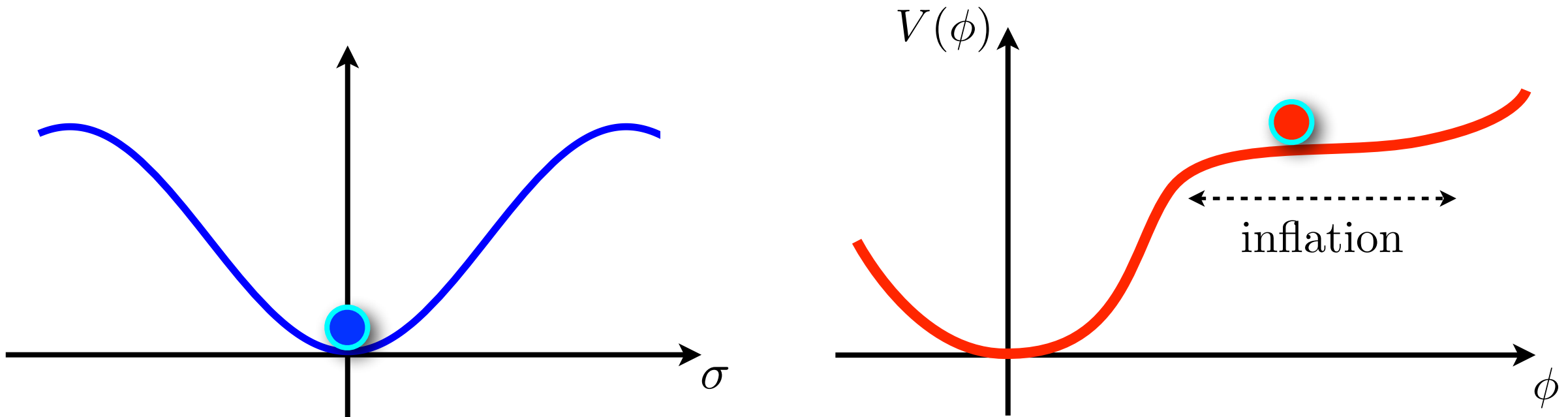
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low-scale inflation with $H_{\text{inf}} < m_\sigma$



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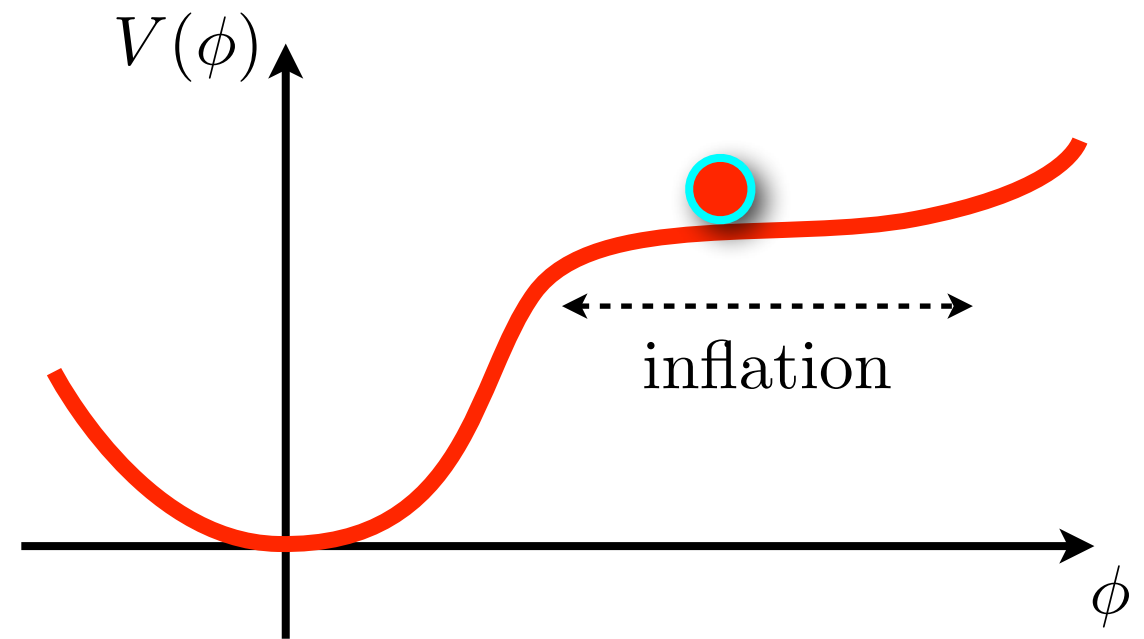
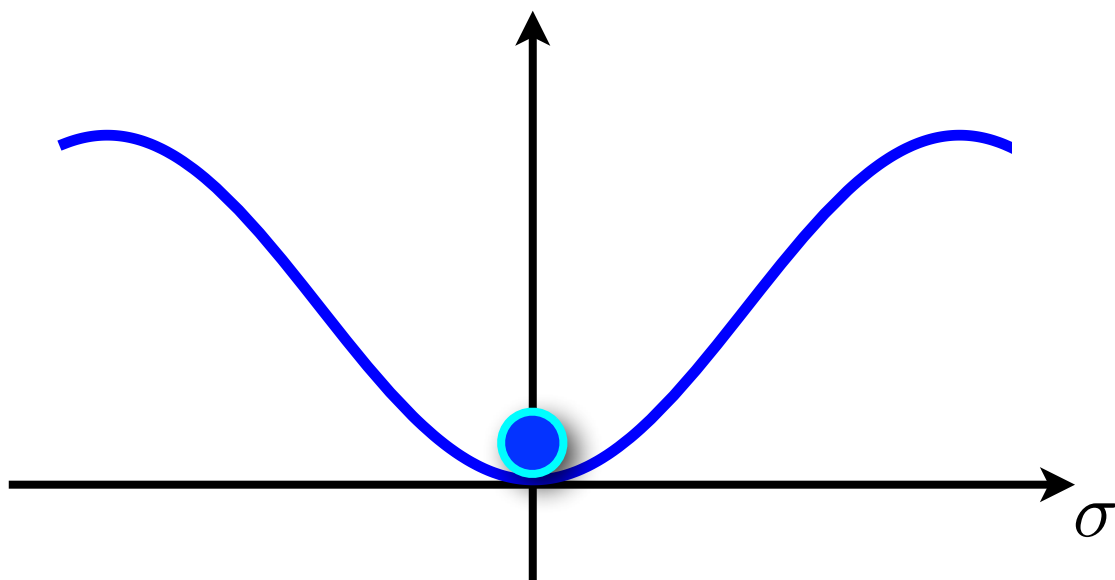
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$$\simeq \alpha\sigma\Box\phi$$

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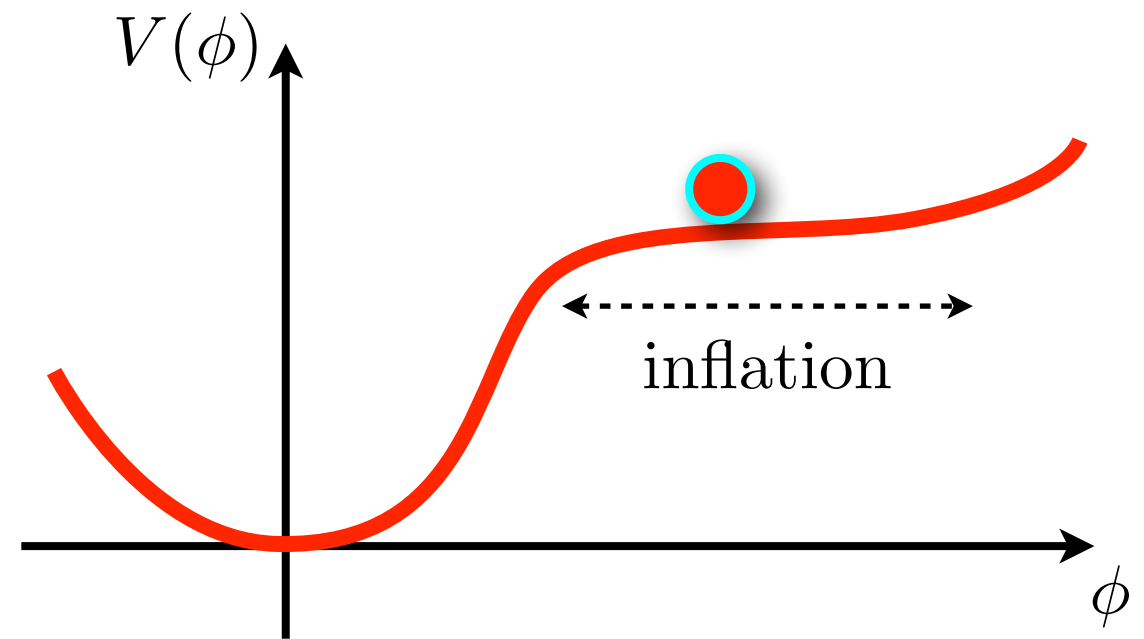
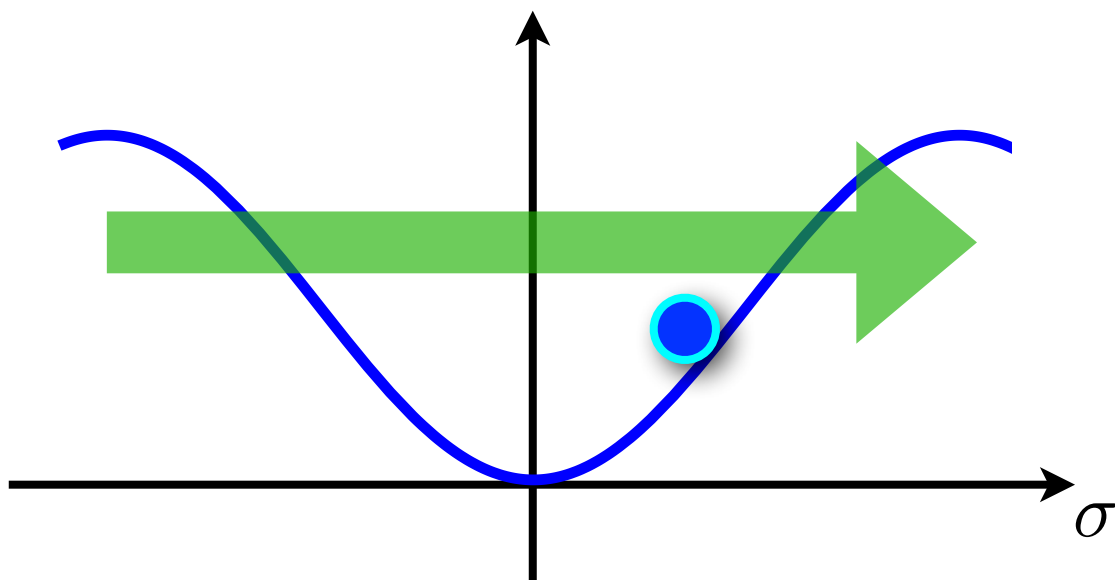
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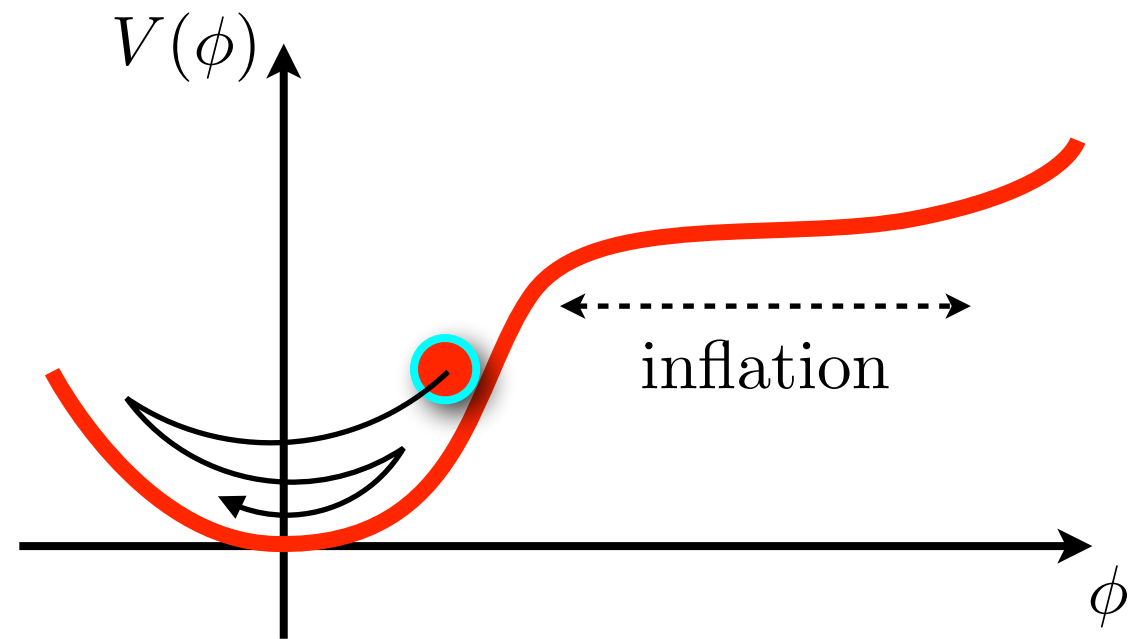
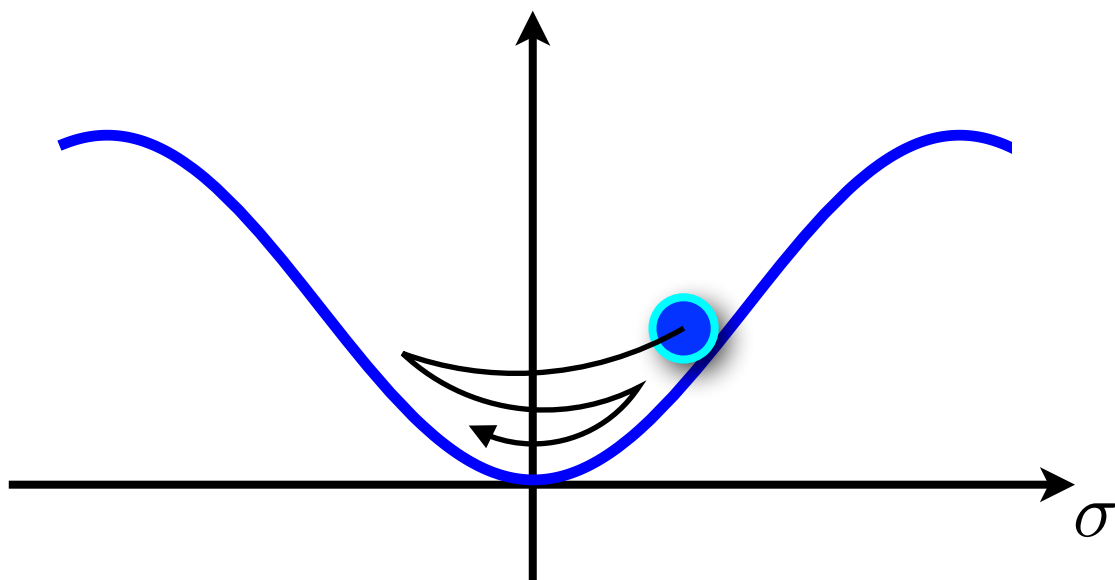
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after inflation



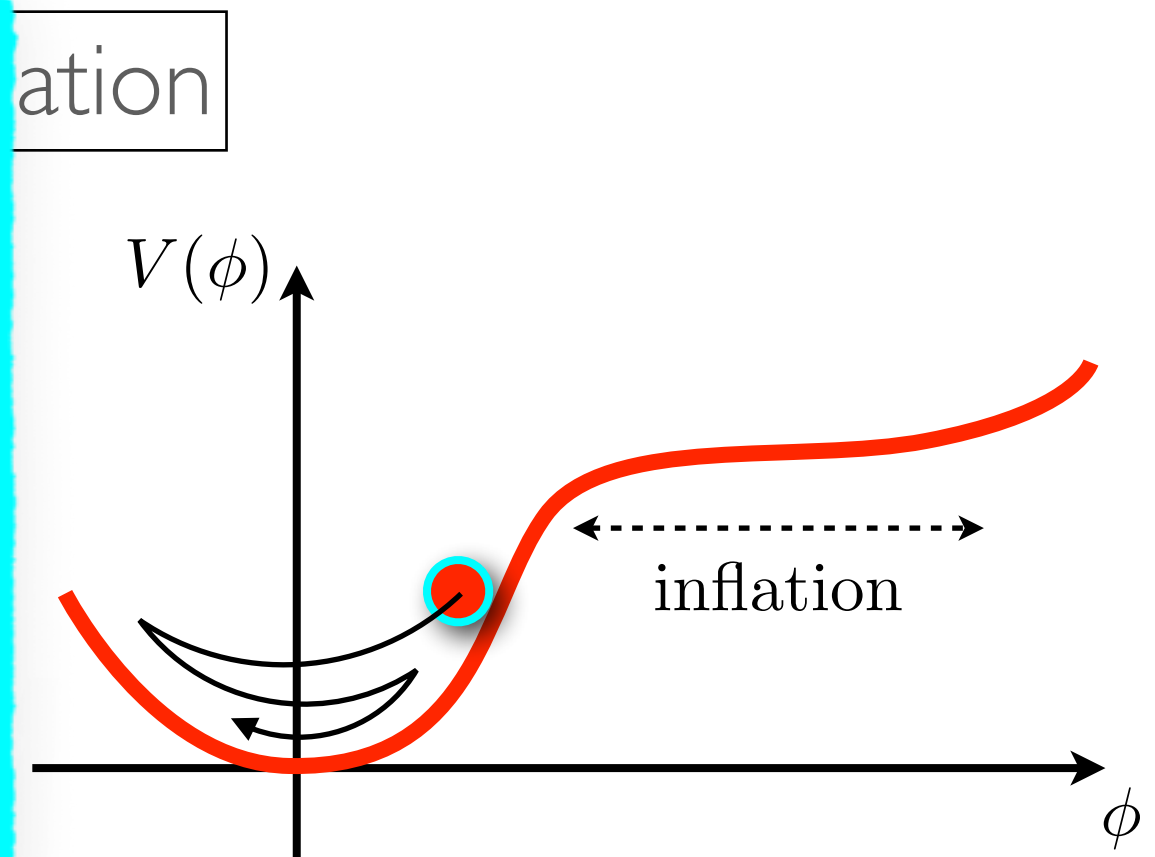
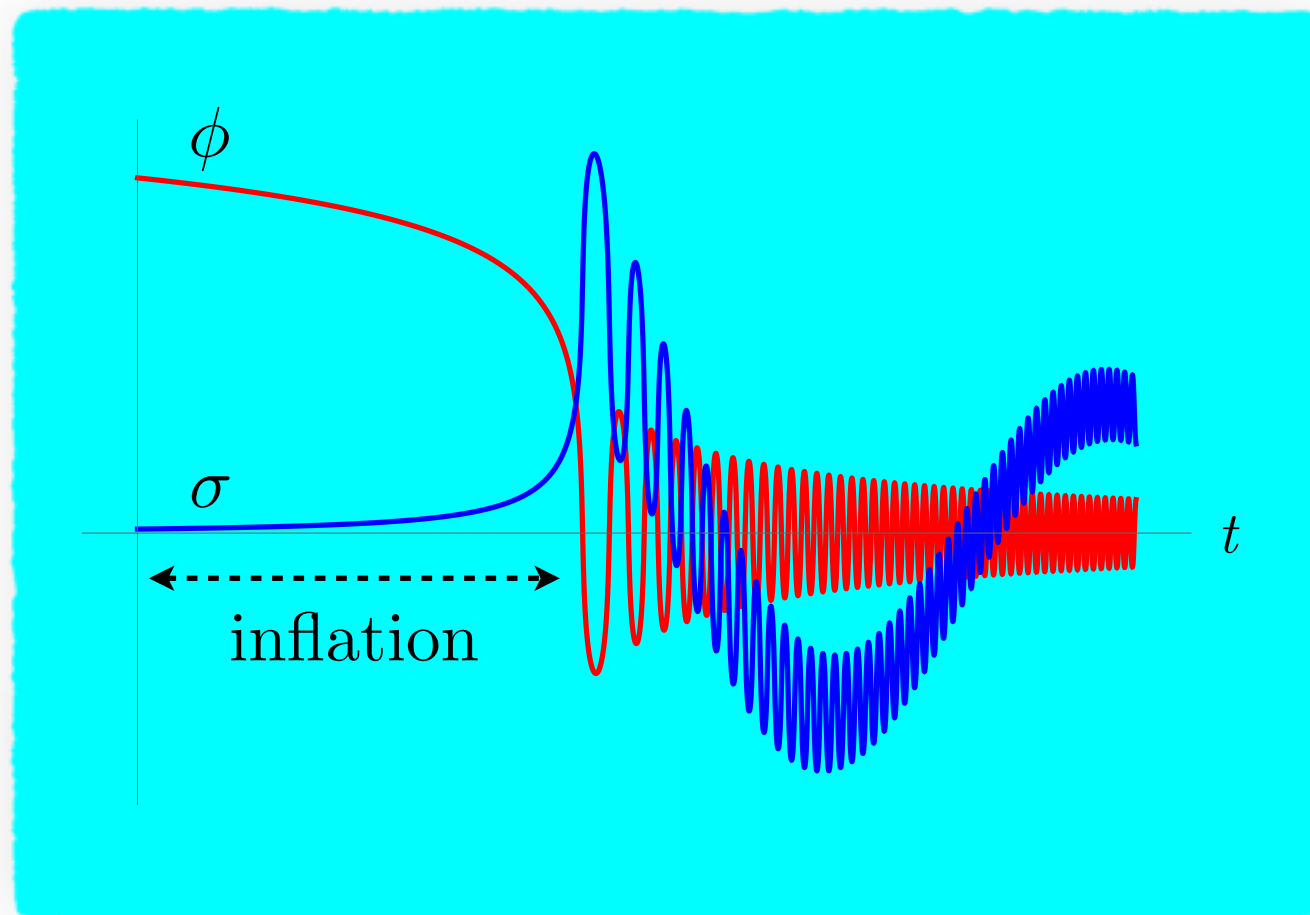
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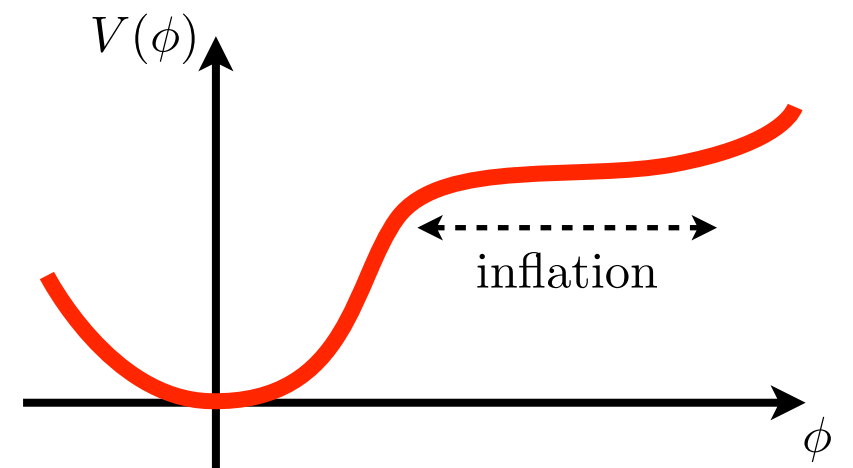
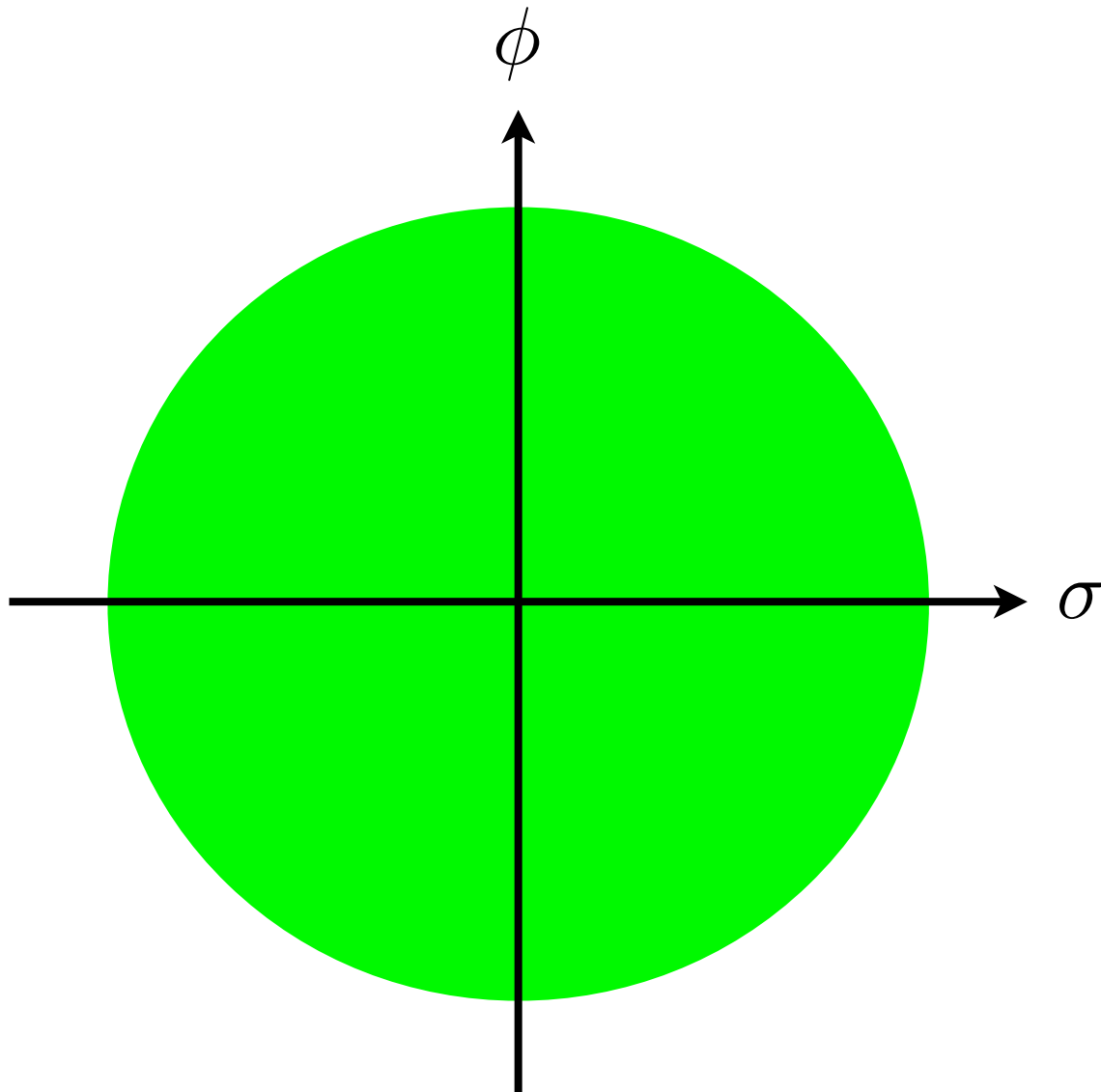
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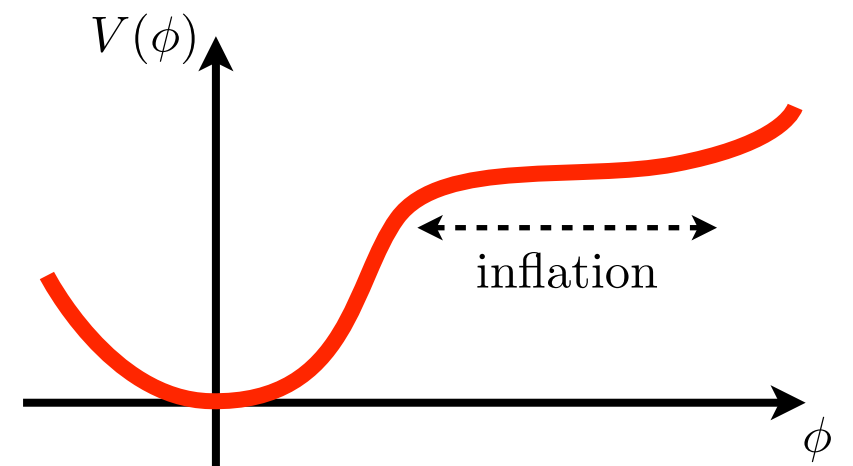
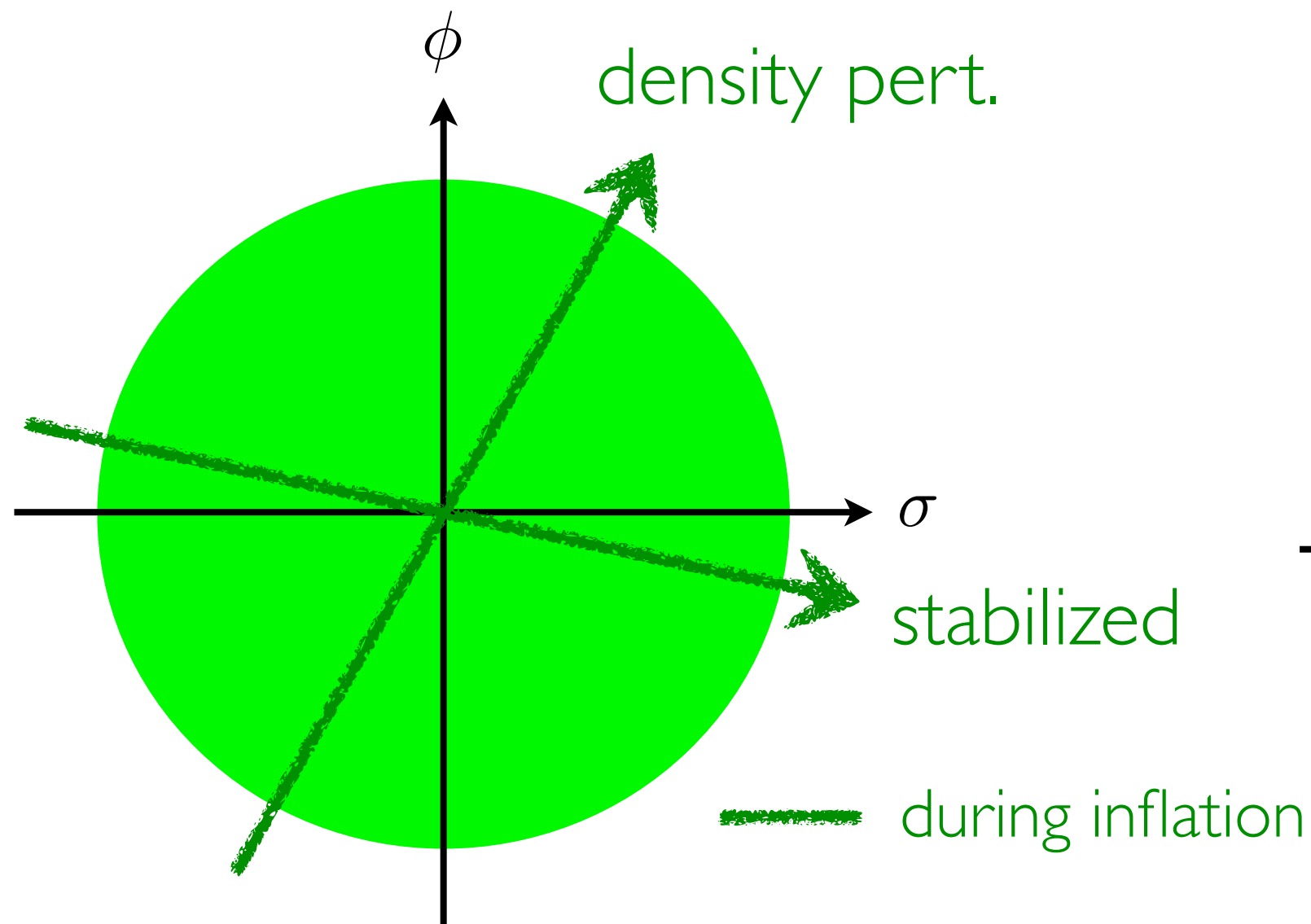
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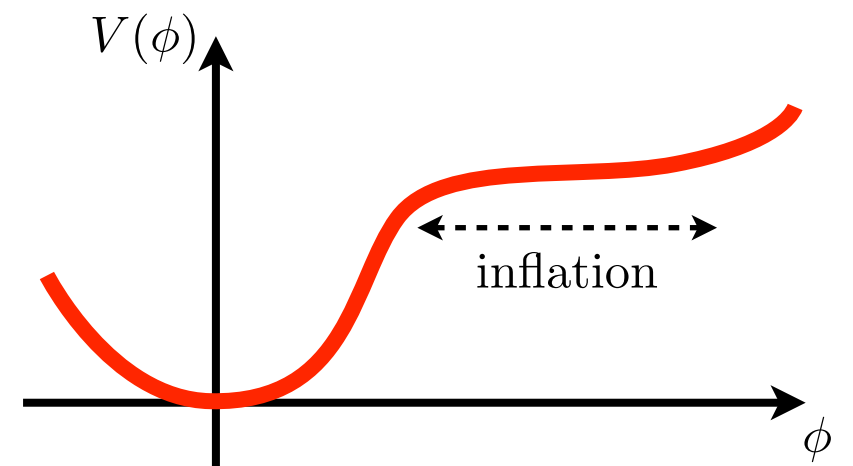
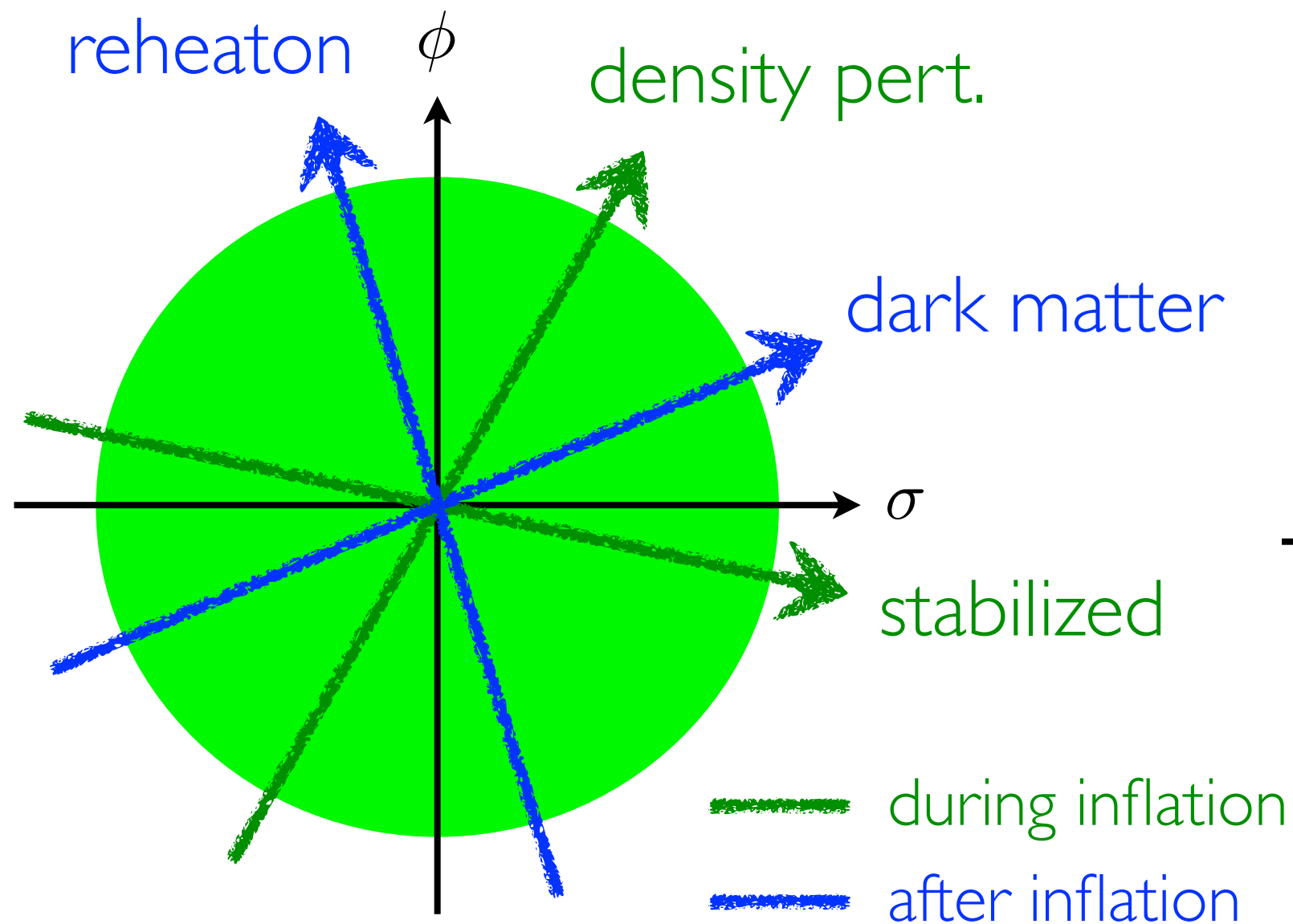
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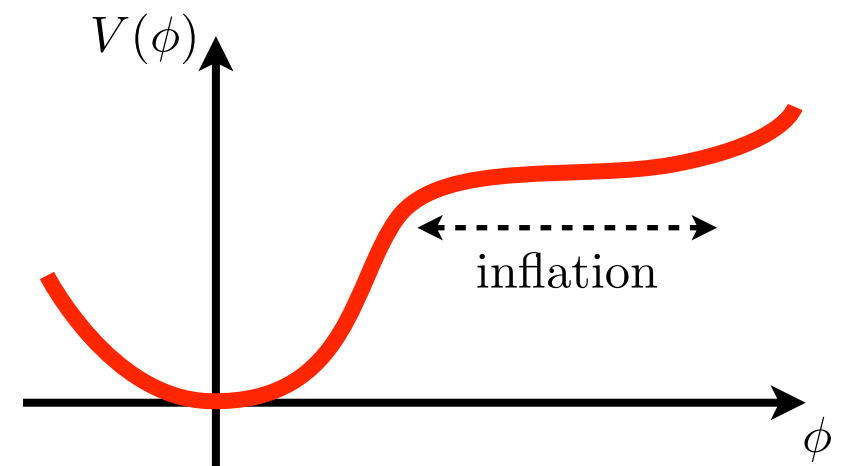
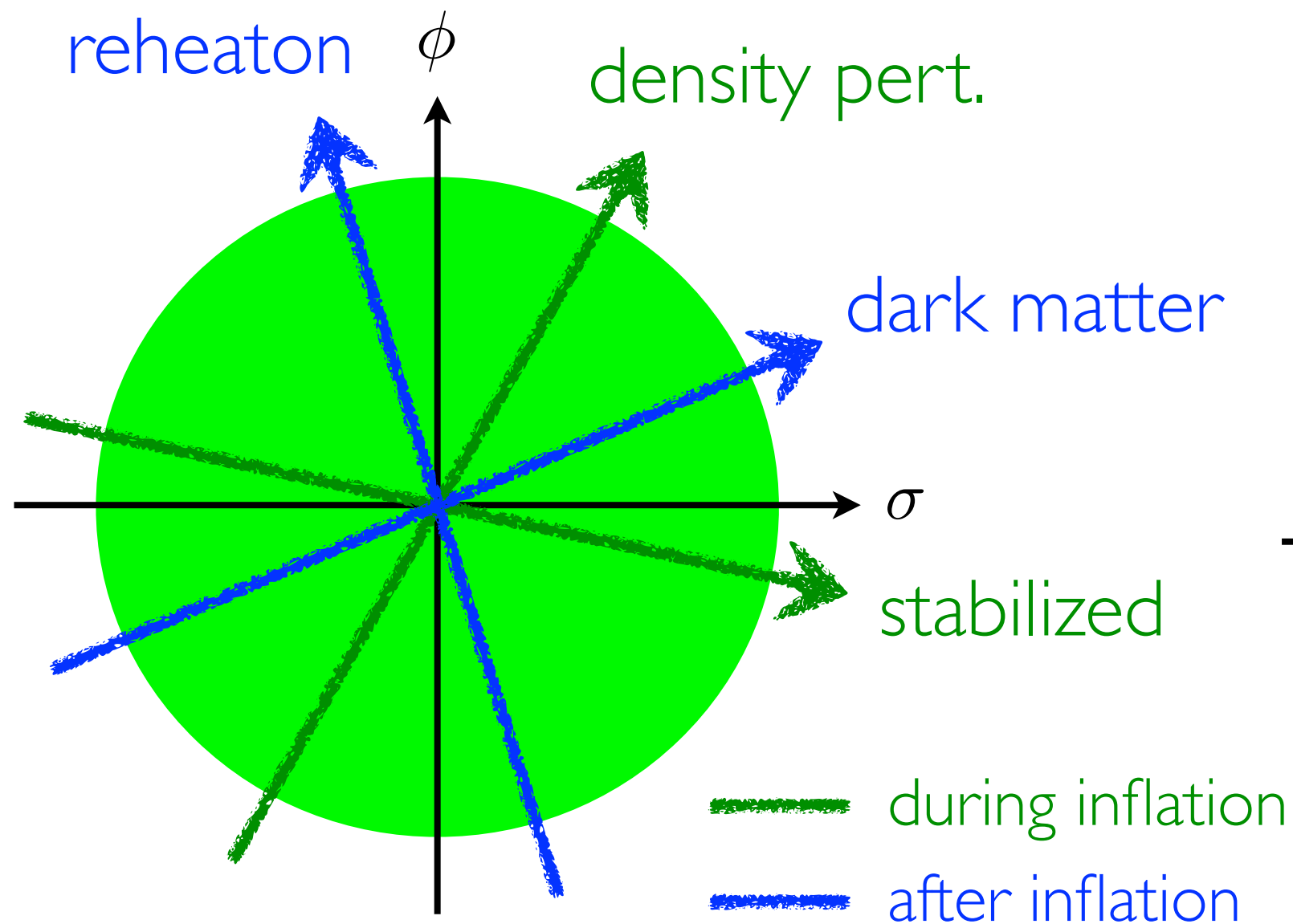


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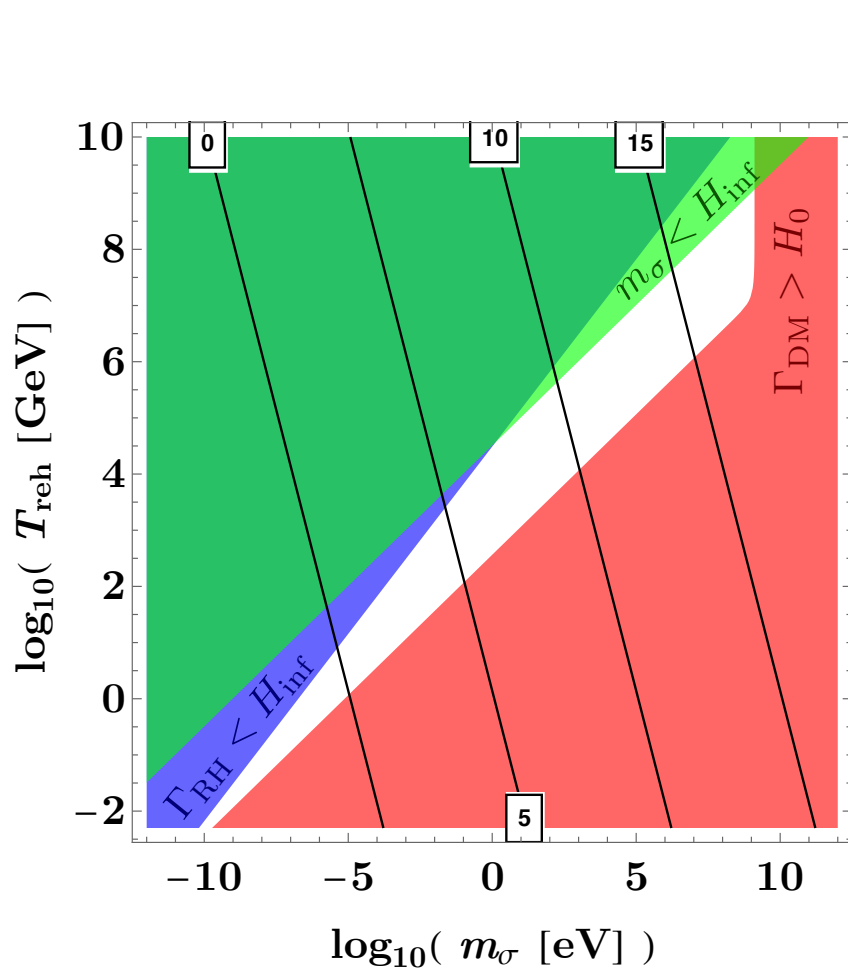


Different combinations of the inflaton and axion
(= **inflaxions**) play various cosmological roles.

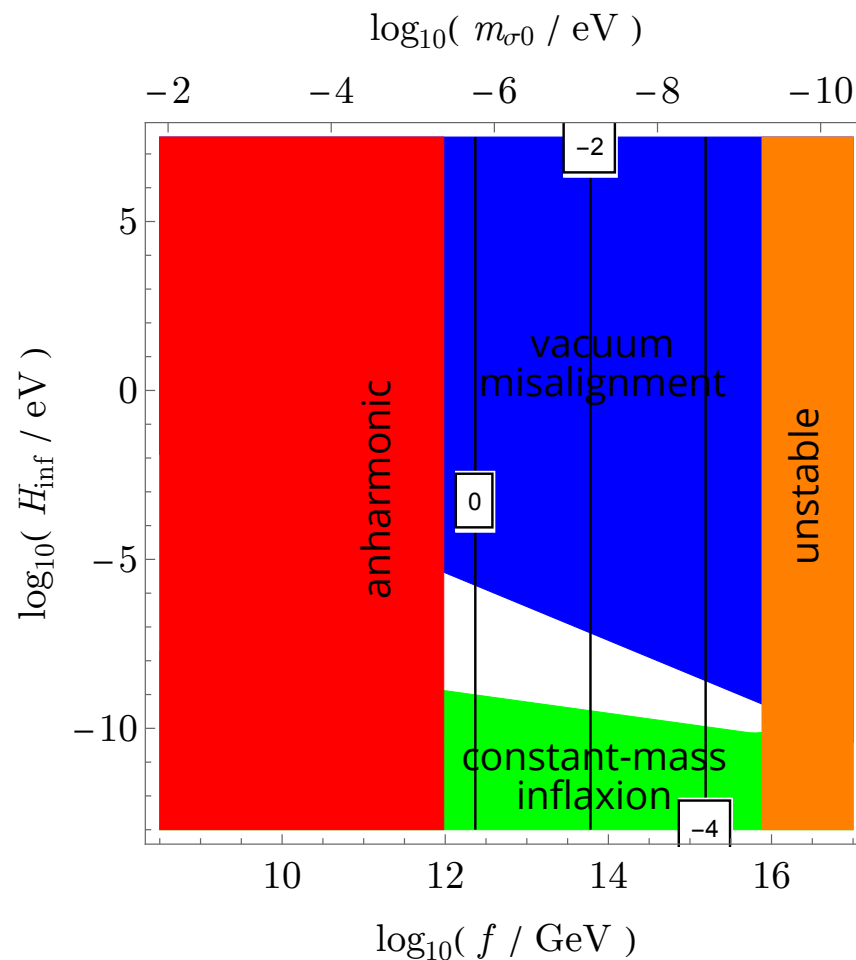


INFLAXION WINDOWS

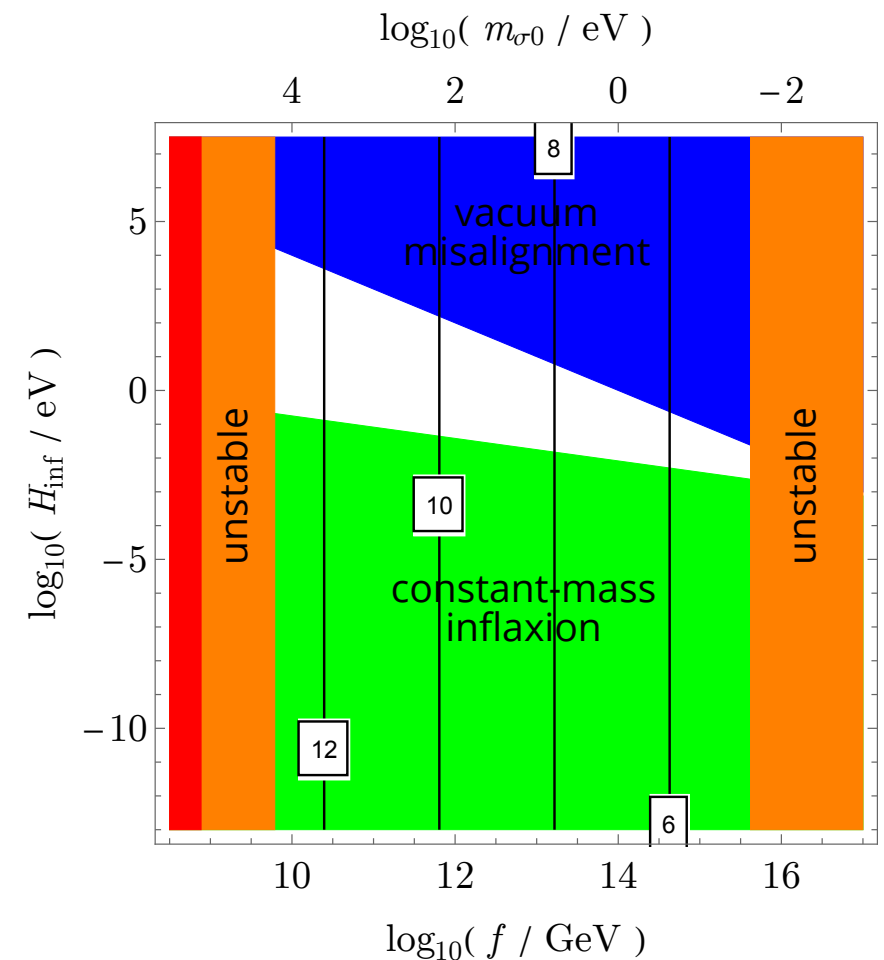
$$L_{\text{int}} = -\alpha \partial\sigma \cdot \partial\phi + \frac{\alpha_\gamma}{8\pi f} \sigma F \tilde{F} + g\phi\bar{\psi}i\gamma^5\psi \quad \alpha \sim 1/3 \quad g \sim 10^{-2}$$



constant-mass axion
($f = 10^{17} \text{ GeV}$)



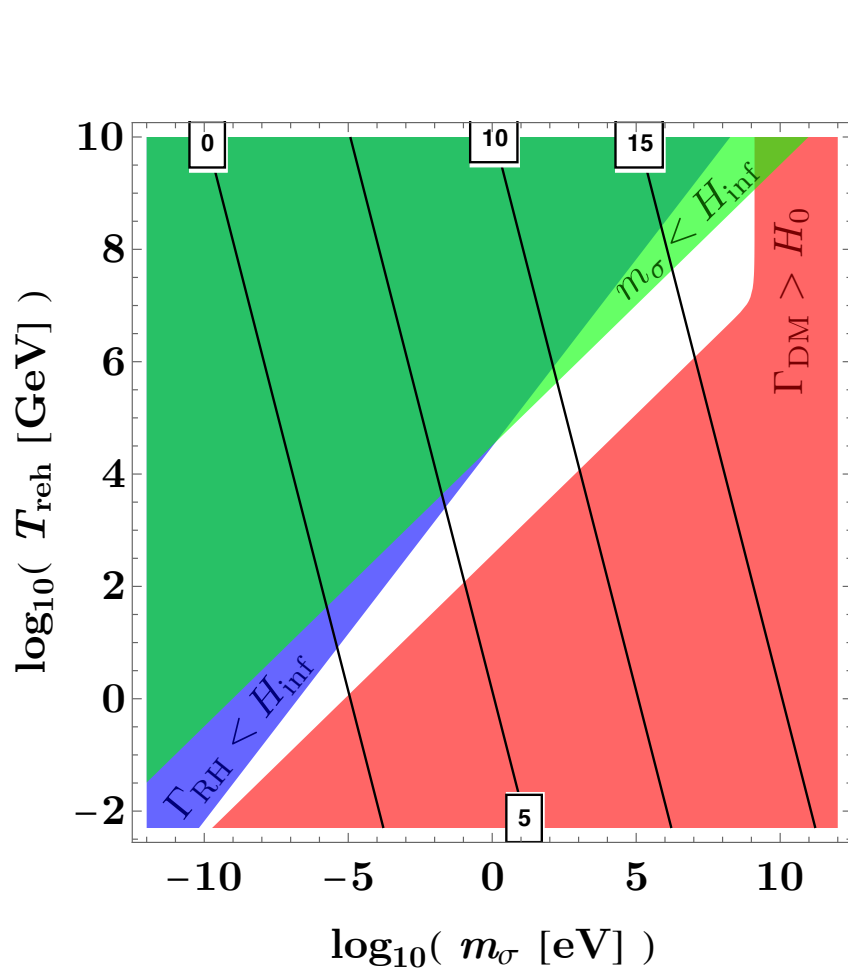
QCD axion
($T_{\text{max}} > \Lambda_{\text{QCD}}$)



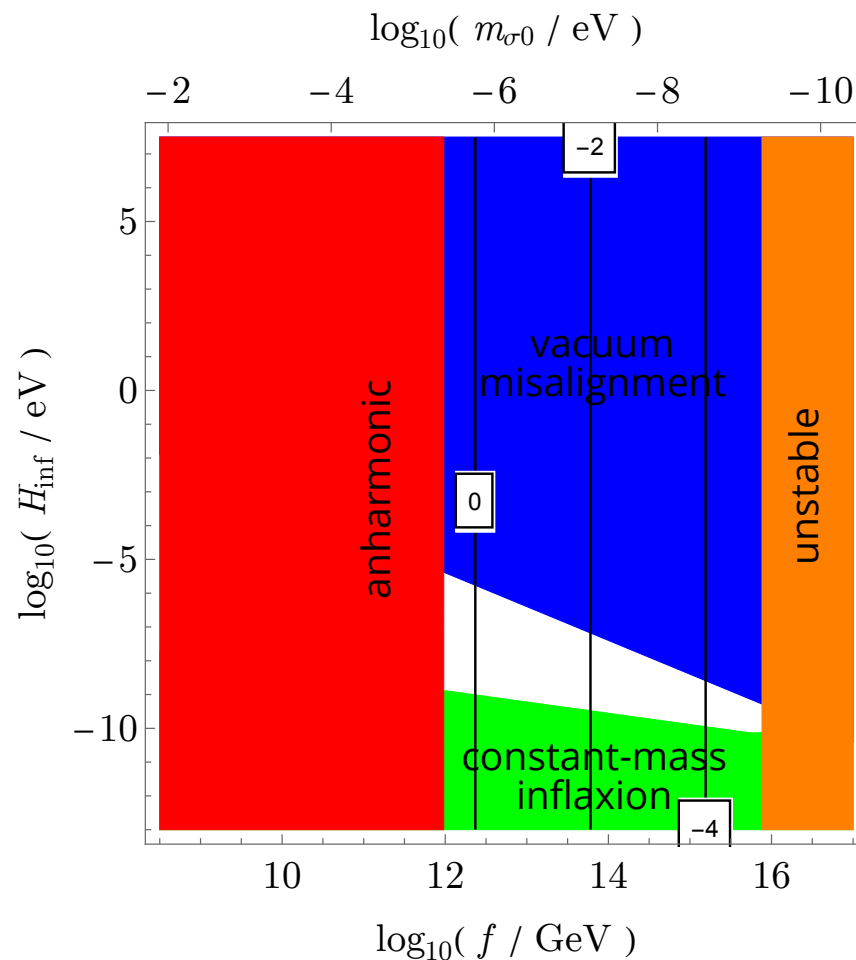
axion coupled to a
hidden strong group
($T_{\text{max}} > \Lambda = 10^3 \text{ GeV}$)

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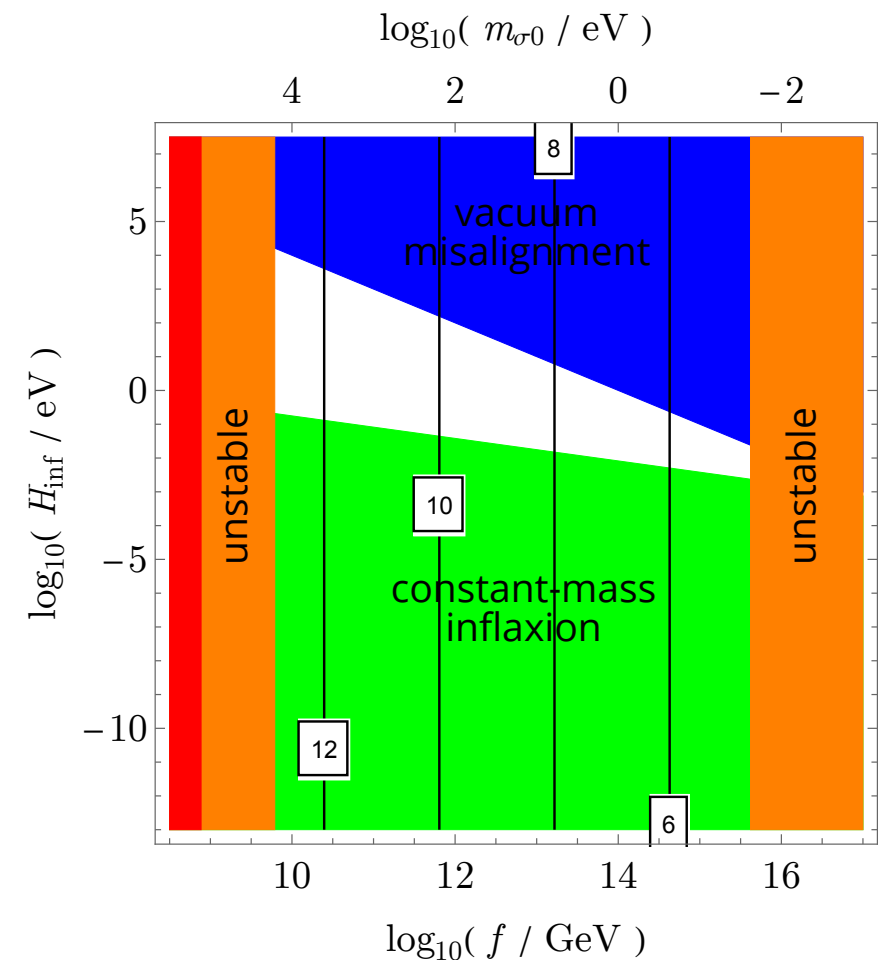
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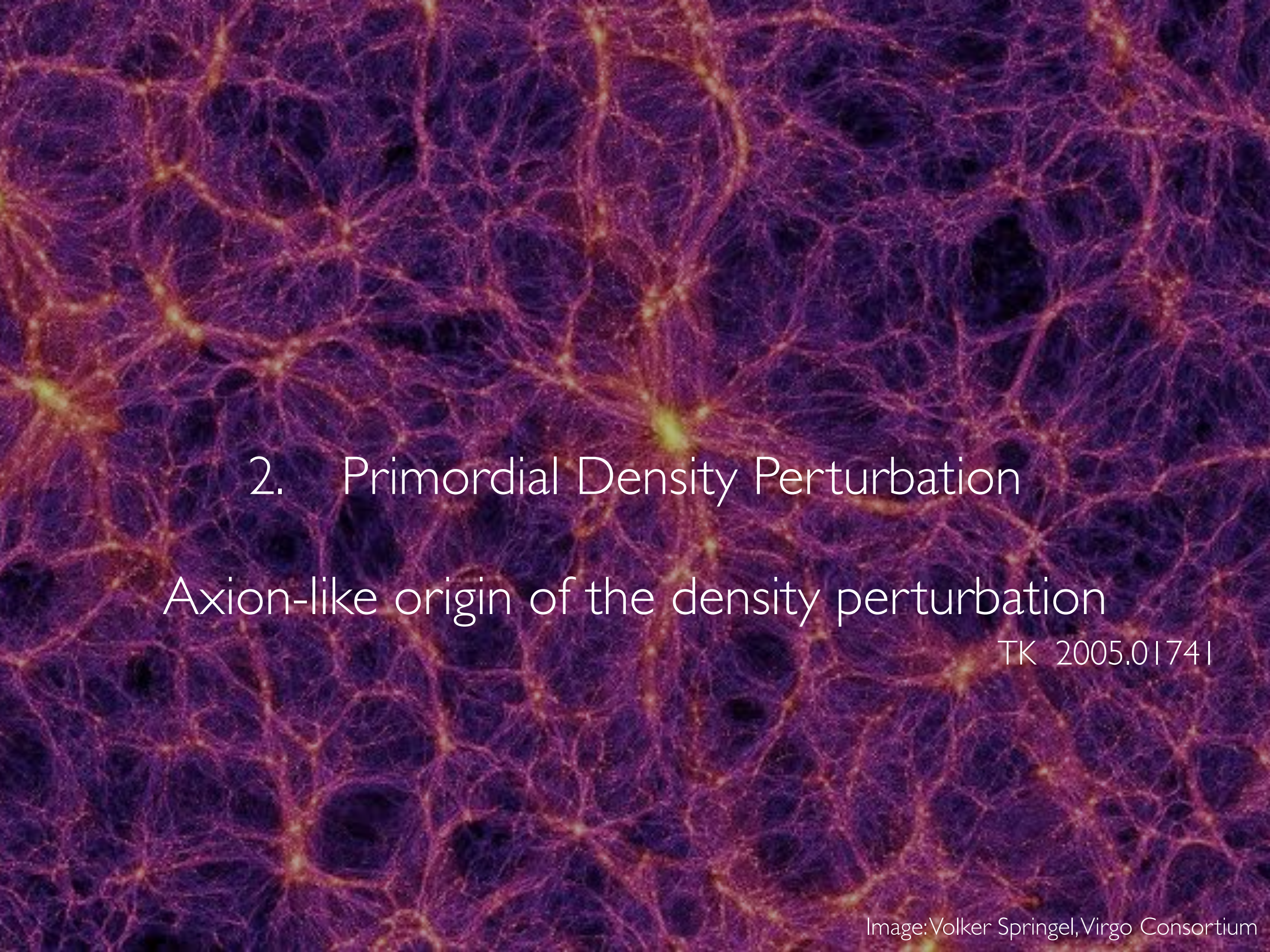


axion coupled to a
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Opens up new axion windows, especially large f regions.

OBSERVATIONAL CONSEQUENCES

- Link between reheating temperature and axion-matter couplings
 - DM lifetime can be short even with large f
 - Parts of the new axion window can be probed by upcoming experiments, e.g. ABRACADABRA
- QCD inflaxion with reheating into neutrinos
- No DM isocurvature

A visualization of the cosmic web, showing a dense network of filaments and nodes of matter in the universe. The filaments are colored in shades of purple and blue, with brighter yellow and orange spots indicating regions of higher density, such as galaxy clusters.

2. Primordial Density Perturbation

Axion-like origin of the density perturbation

TK 2005.01741

SEEDS OF COSMIC STRUCTURES

Observations have revealed that the primordial density perturbation was adiabatic, **red tilted**, and **nearly Gaussian**.

Was this generated by the inflaton, or something else?

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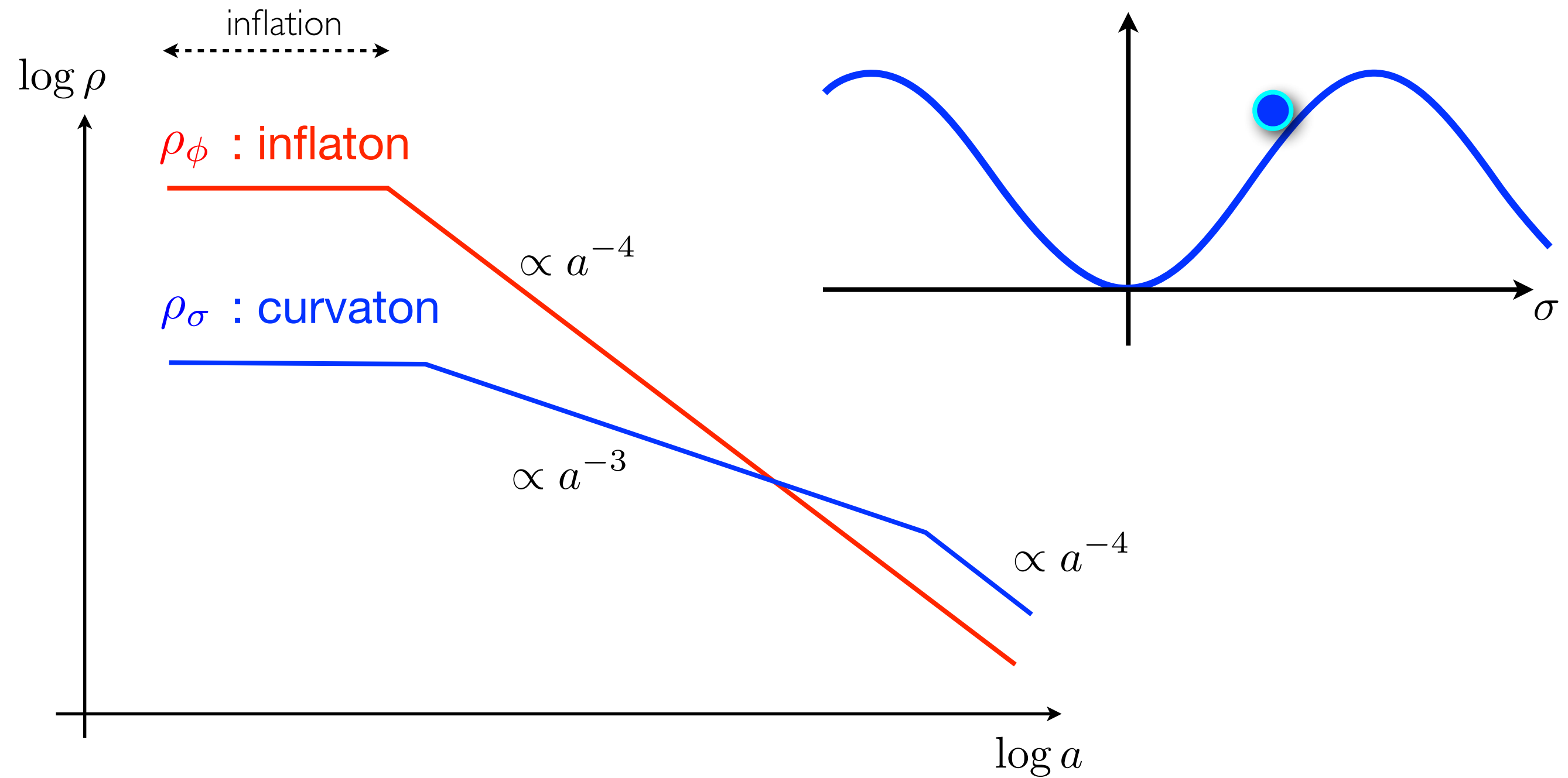
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An axion-like field coupled to a new confining sector can generate the perturbation à la curvaton.

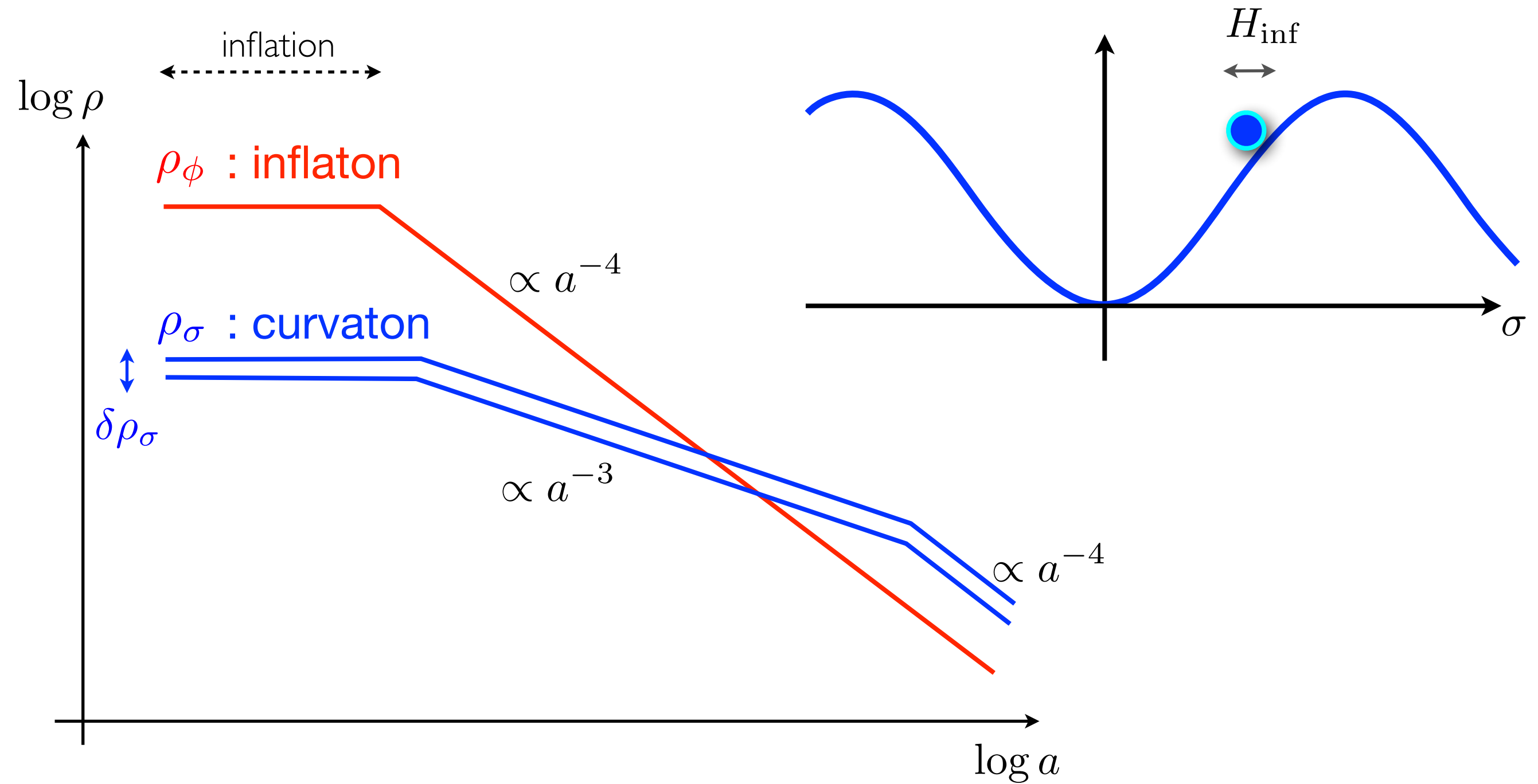
CURVATON PARADIGM

Mollerach '90 Linde, Mukhanov '96 Enqvist, Sloth '01 Lyth, Wands '01 Moroi, Takahashi '01



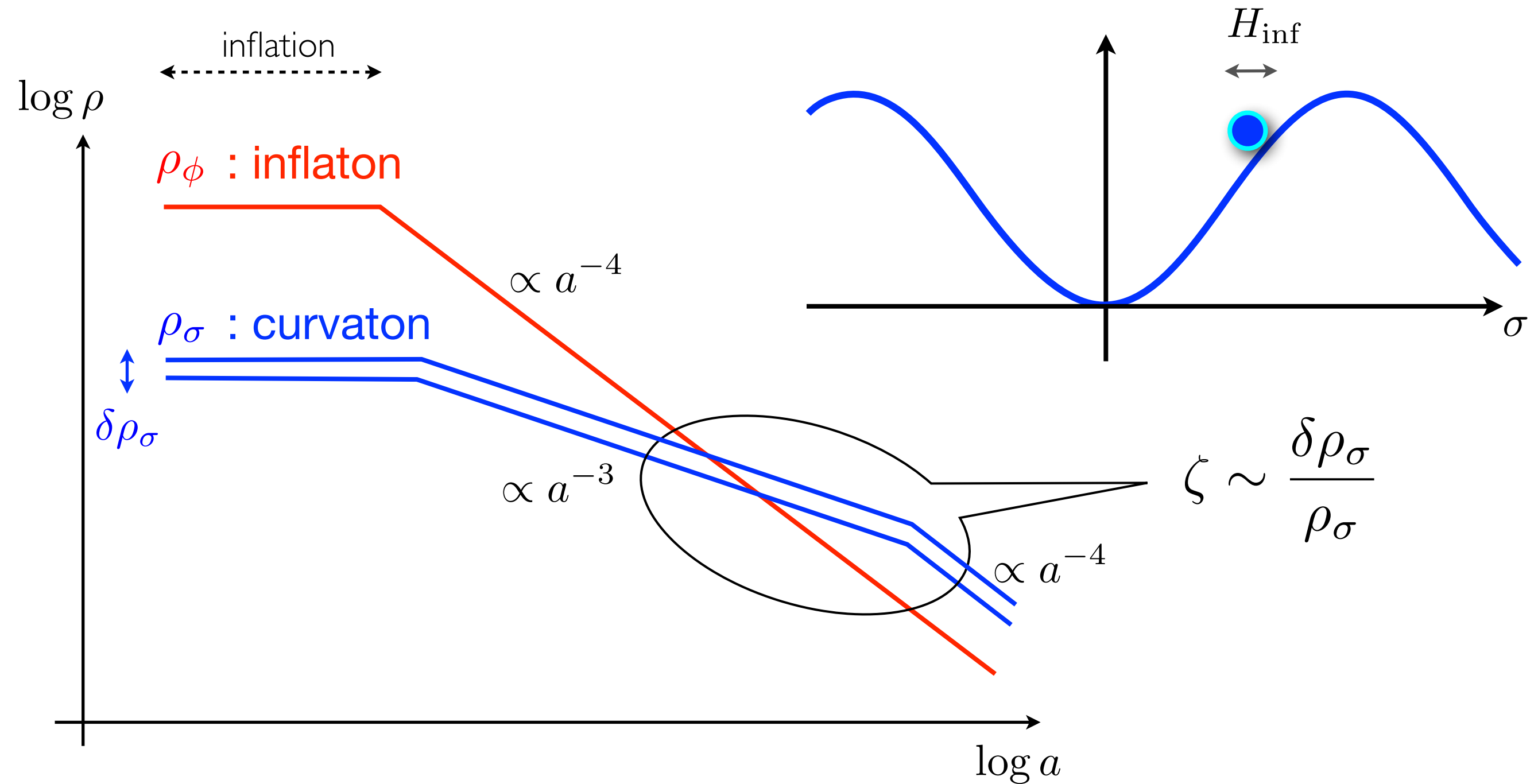
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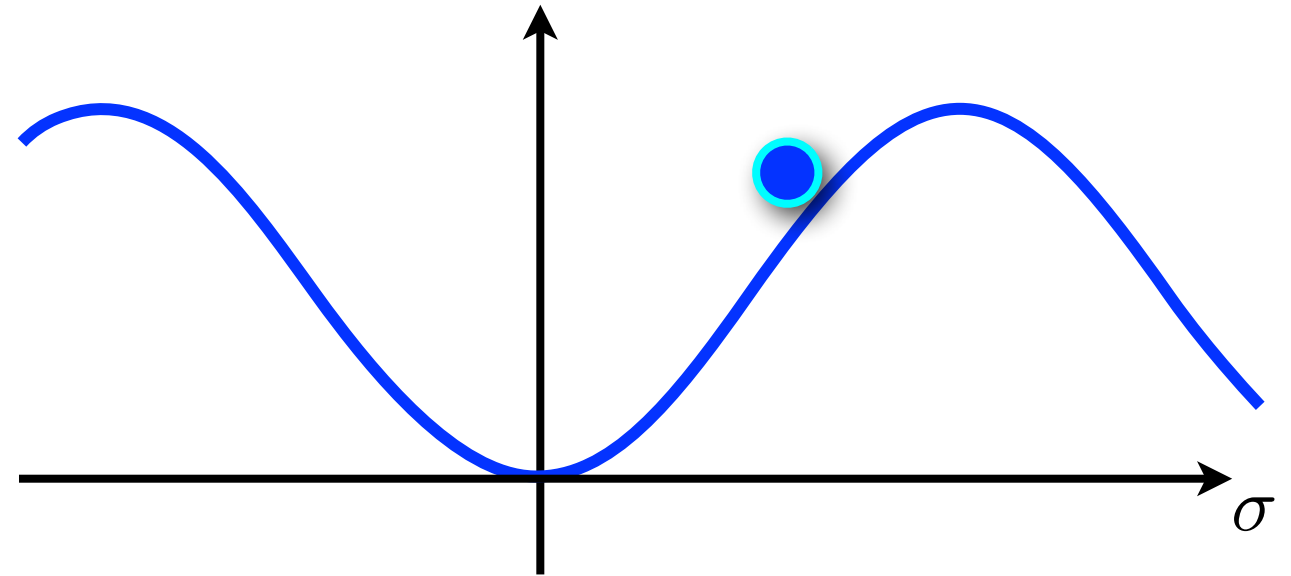
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SPECTRAL INDEX FROM CURVATON

$$P_{\zeta}(k) = P_{\zeta}(k_*) \left(\frac{k}{k_*} \right)^{n_s - 1}$$

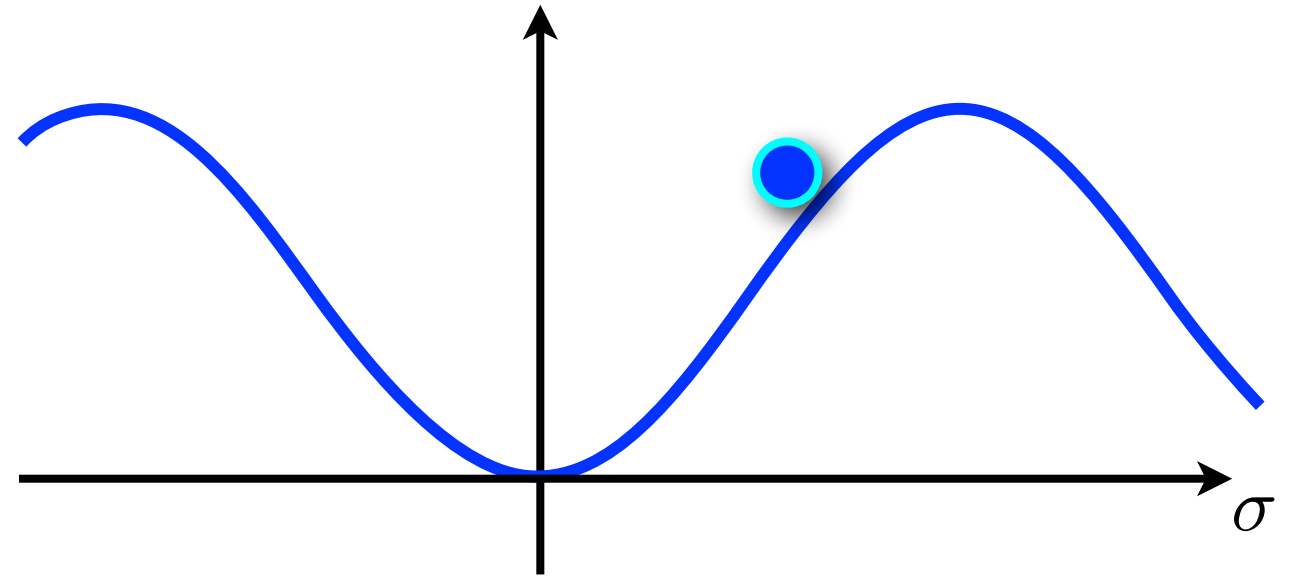
$$n_s - 1 = \frac{2}{3} \frac{V''}{H_{\text{inf}}^2} + 2 \frac{\dot{H}_{\text{inf}}}{H_{\text{inf}}^2}$$



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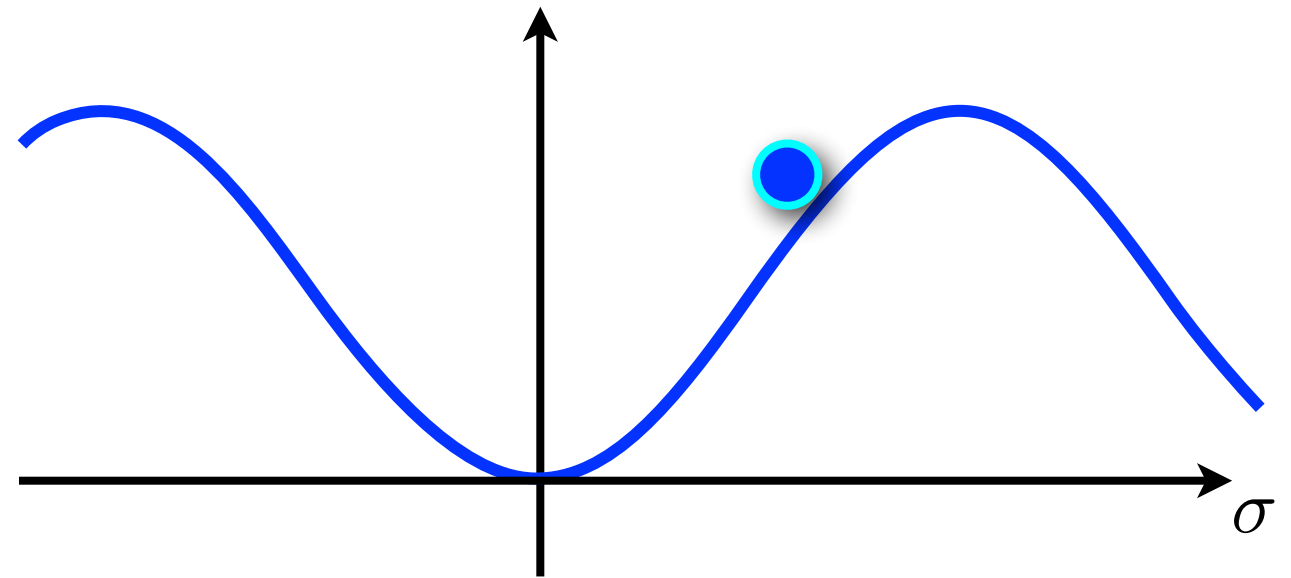
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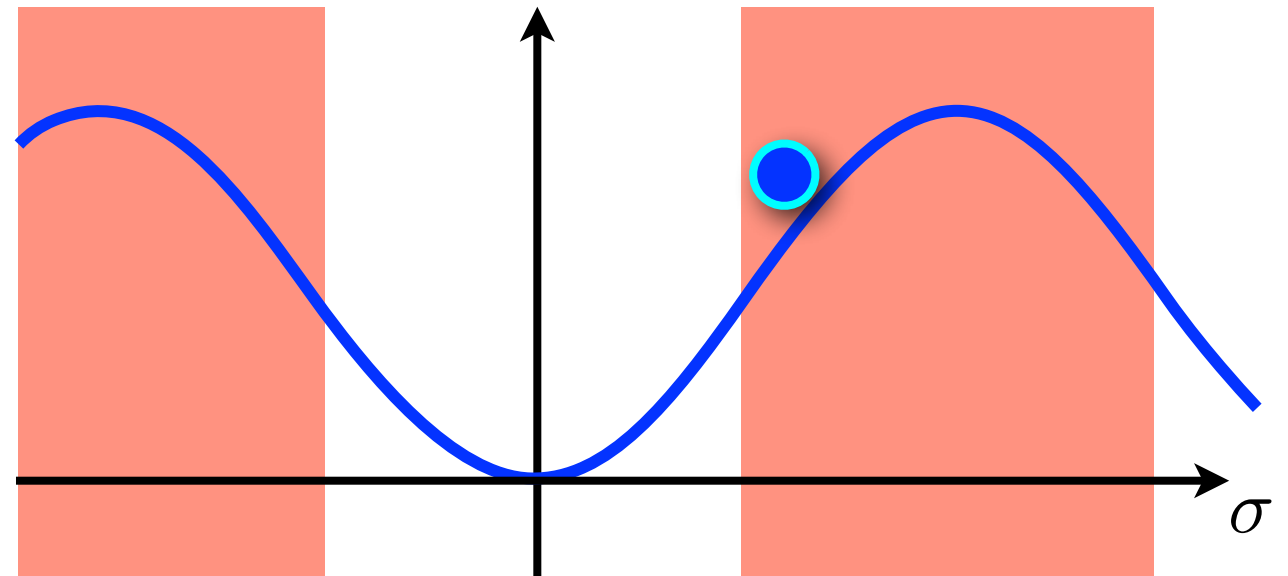
Two options for getting the red tilt:

- (i) $-\dot{H}/H^2 \sim 10^{-2}$, i.e. super-Planckian inflation
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Axion potentials (by definition) contain concave regions.

AXION-LIKE CURVATON COUPLED TO A NEW CONFINING GAUGE GROUP

$$m_0 \sim \frac{\Lambda^2}{f}$$

$$P_\zeta \sim \left(\frac{H_{\text{inf}}}{3\pi f} \right)^2 \approx 2 \times 10^{-9} \quad n_s - 1 \sim -\frac{2}{3} \left(\frac{m_0}{H_{\text{inf}}} \right)^2 \approx -0.04$$

$$f \sim 2000 H_{\text{inf}} \quad \Lambda \sim 20 H_{\text{inf}}$$

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Assuming instantaneous inflaton decay, the
max. temperature after inflation $T_{\text{max}} \sim (M_p H_{\text{inf}})^{1/2}$ obeys

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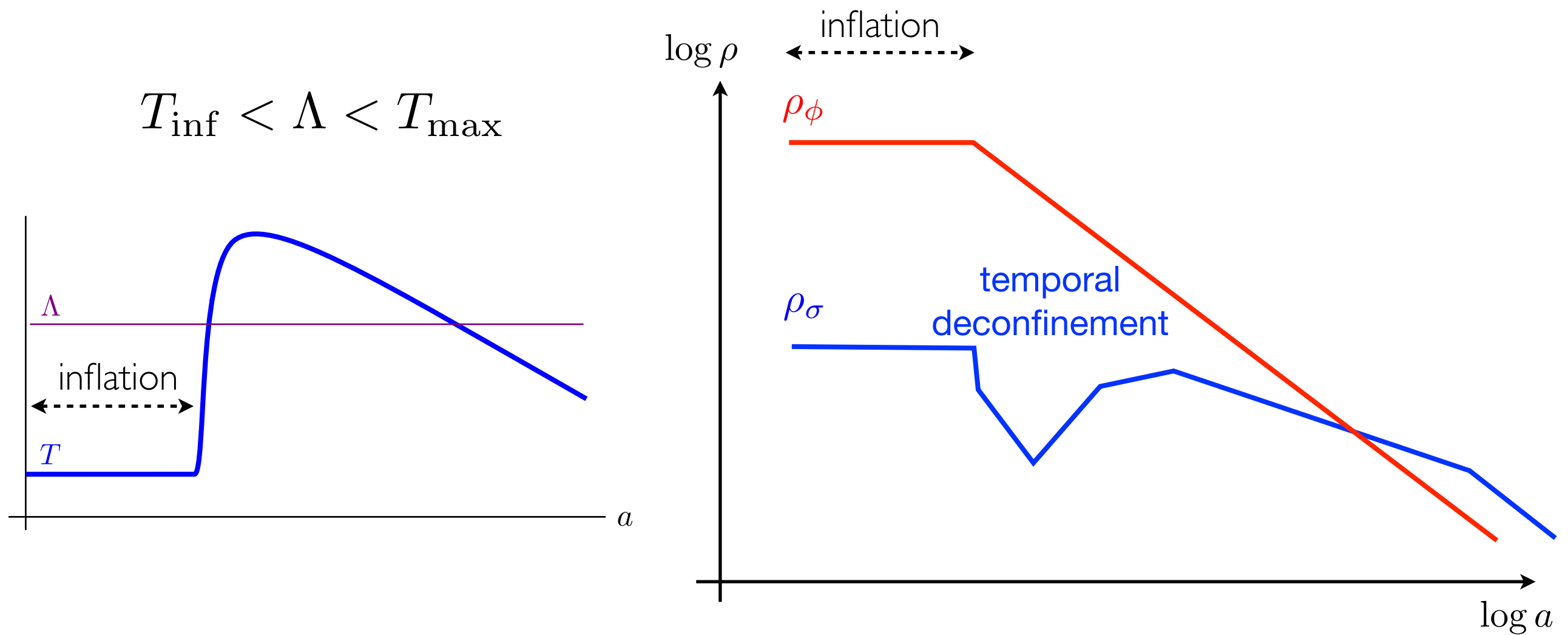
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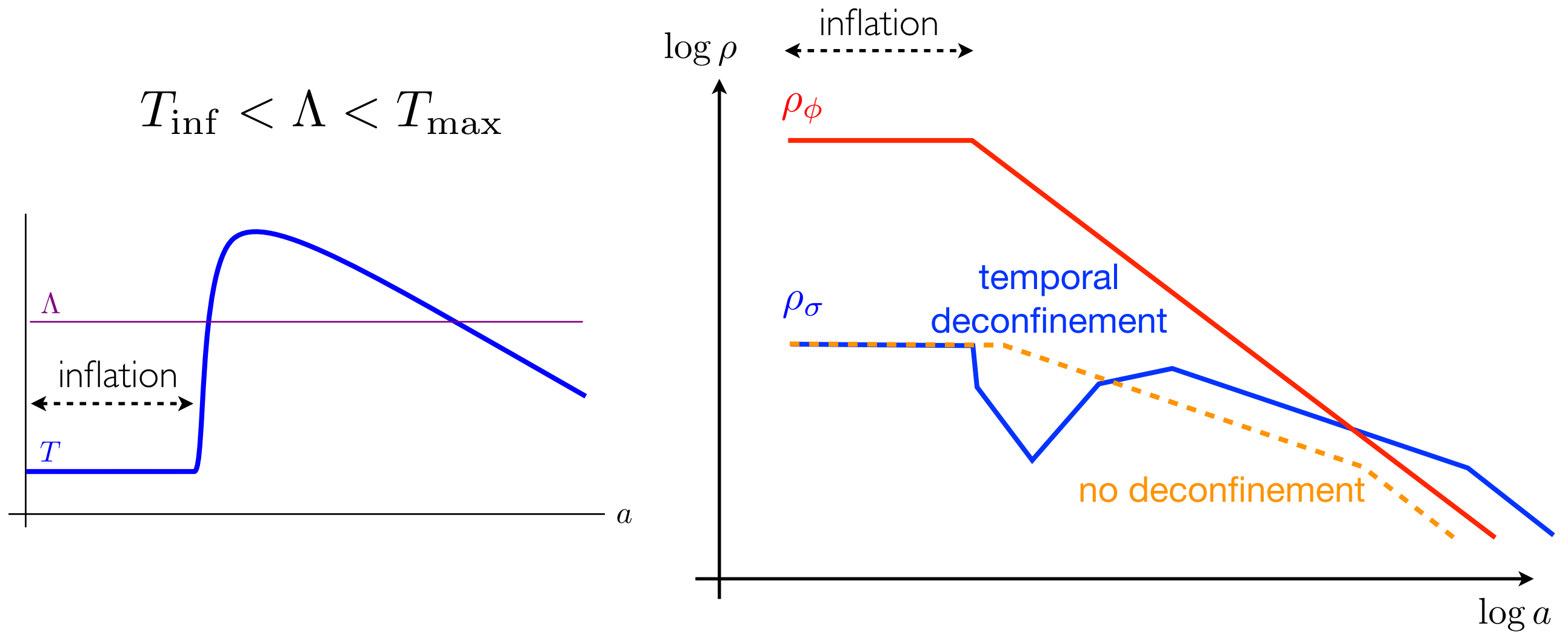
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→ temporal deconfinement after inflation

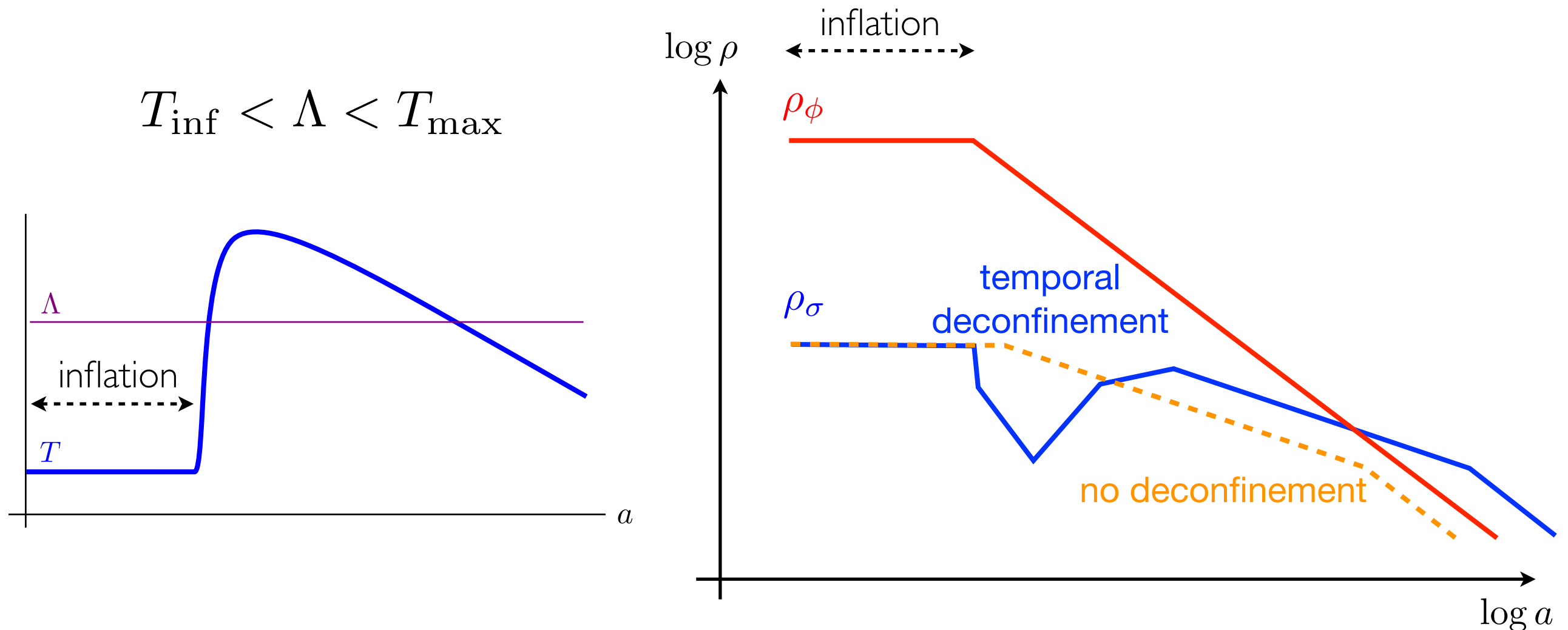
THE IMPORTANCE OF DECONFINING



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A temporal deconfinement delays the axion oscillation, which helps the axion dominate the universe before decaying.

(Alternatively the axion can be initially placed close to the hilltop, but this produces $f_{\text{NL}} \sim 10$ and thus is ruled out. Kawasaki, TK, Takahashi '11)

OBSERVATIONAL CONSEQUENCES

- **Positive local-type non-Gaussianity of $f_{\text{NL}} \sim 1$**
(cf. single-field inflation $|f_{\text{NL}}| \ll 1$, vanilla curvaton $f_{\text{NL}} \sim -1$):
testable with upcoming LSS surveys, e.g. SPHEREx
- **Blue tilt on small scales:** enhanced perturbations can form ultracompact minihalos (but probably no PBHs in the minimal model)
- **Running non-Gaussianity:** $f_{\text{NL}} \rightarrow -1$ towards small scales

SUMMARY

- Inflation dark matter
 - An axion-inflaton kinetic mixing allows for a production of axion DM even with low-scale inflation ($H_{\text{inf}} < m_\sigma$)
 - Inflatons integrate a single-field inflaton, reheaton, DM, and opens up new windows (e.g. low H_{inf} , $f \gtrsim 10^{16} \text{ GeV}$)
- Axion-like curvaton coupled to a new confining sector
 - Parameters are fixed by observations, which suggest a temporal deconfinement of the gauge group after inflation
 - Temperature-dependent and periodic axion potential gives rise to the red tilt as well as $f_{\text{NL}} \sim 1$

BACKUP SLIDES

AXION-LIKE CURVATON: PARAMETERS

$$\frac{\mathcal{L}}{\sqrt{-g}} = \frac{1}{2}f^2(\partial\theta)^2 - m(T)^2 f^2 (1 - \cos\theta) + \frac{\alpha}{8\pi}\theta F\tilde{F} \quad m_0 \sim \frac{\Lambda^2}{f}$$

$$P_\zeta \sim \left(\frac{H_{\text{inf}}}{3\pi f}\right)^2 \approx 2 \times 10^{-9} \quad n_s - 1 \sim -\frac{2}{3} \left(\frac{m_0}{H_{\text{inf}}}\right)^2 \approx -0.04 \quad f_{\text{NL}} \sim 1$$

$$f \sim 2000 H_{\text{inf}} \quad \Lambda \sim 20 H_{\text{inf}}$$

$$T_{\text{inf}} < \Lambda < T_{\text{max}} < f$$

$$T_{\text{max}} \sim (M_p H_{\text{inf}})^{1/2}$$

$$10^{11} \text{ GeV} \lesssim H_{\text{inf}} \lesssim 10^{14} \text{ GeV}$$

$$10^{-11} \text{ (} 10^{-13} \text{)} \lesssim \alpha \lesssim 10^{-2} \text{ (} 10^3 \text{)} \quad \text{for } H_{\text{inf}} = 10^{11} \text{ (} 10^{14} \text{)} \text{ GeV}$$

decay before BBN

curvaton domination

AXION-LIKE CURVATON: PERTURBATION

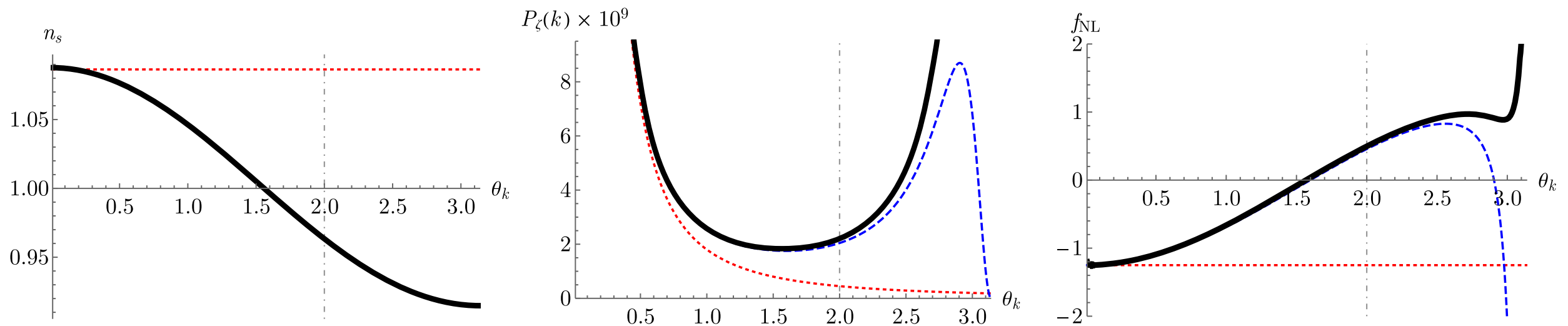


FIG. 1. Curvature perturbation as a function of the axion angle when the pivot scale exits the horizon during inflation. The axion decay constant and strong coupling scale are taken as $f = 2500H_{\text{inf}}$ and $\Lambda = 30H_{\text{inf}}$, so that the power spectrum amplitude and the spectral index match with observations at $\theta_k \approx 2.0$. The black solid lines show the numerical results, while the blue dashed lines are analytic approximations. Results for vanilla curvatons are shown as the red dotted lines.

$$P_\zeta(k) \simeq \left(\frac{R}{3R+4} \frac{1 + \cos \theta_{\text{end}}}{\sin \theta_k} \frac{H_k}{2\pi f} \right)^2 \quad R \equiv \left(\frac{\rho_\theta}{\rho_r} \right)_{\text{dec}}$$

$$f_{\text{NL}} \simeq \frac{5}{6} \left\{ \frac{4}{R} + \frac{4}{3R+4} - \left(3 + \frac{4}{R} \right) \frac{1 - \cos \theta_{\text{end}} + \cos \theta_k}{1 + \cos \theta_{\text{end}}} \right\}$$

$$n_s - 1 \simeq \frac{2}{3} \frac{m_0^2}{H_k^2} \cos \theta_k + 2 \frac{\dot{H}_k}{H_k^2}$$