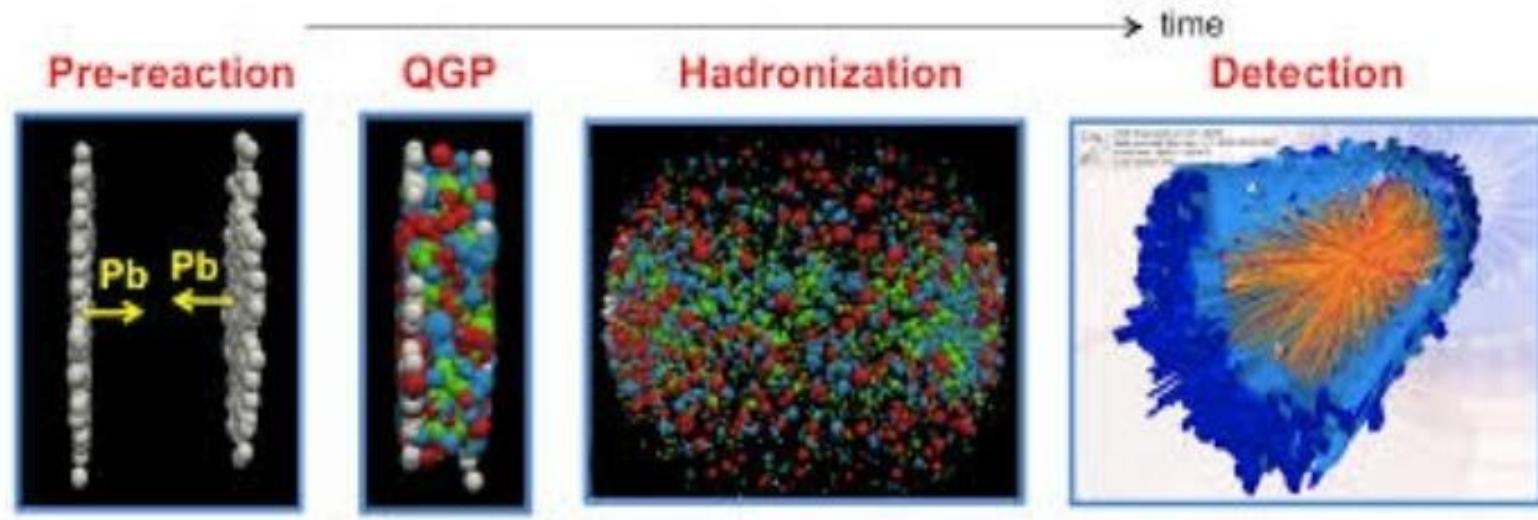


Heavy quark dynamics in QCD matter



Santosh Kumar Das

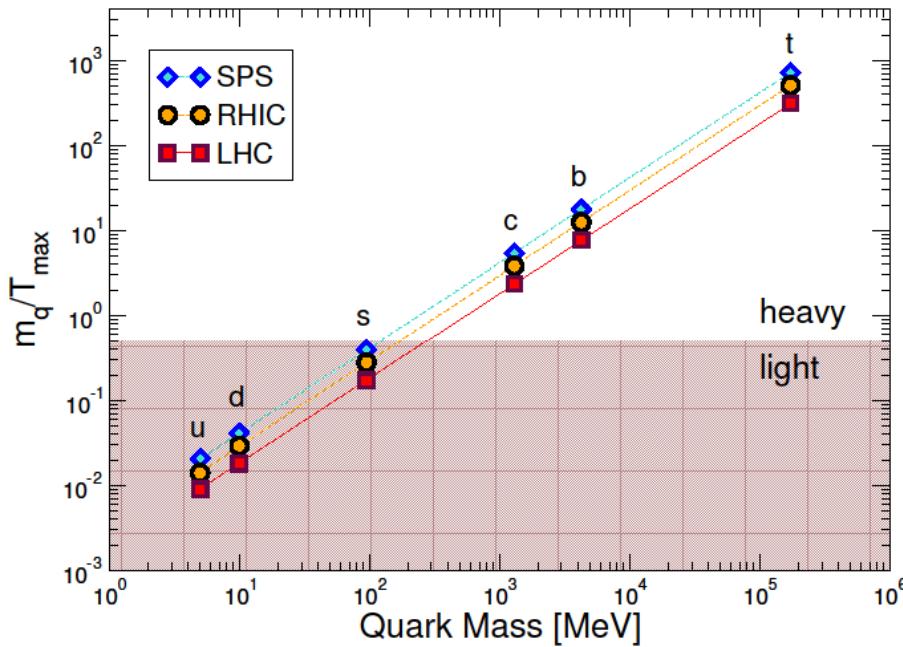
School of Physical Science
Indian Institute of Technology Goa
Goa, India



OUTLINE

- **Introduction**
- **Quark Gluon Plasma - the primordial fluid**
- **Heavy quark transport coefficients – R_{AA} and v_2**
- **Heavy quark momentum evolution and hadronization**
- **Initial stage effects – EM field, Angular momentum, Glasma**
- **Summary and outlook**

Heavy Quark & QGP



SPS to LHC

$\sqrt{s} = 17.3 \text{ GeV to } 2.76 \text{ TeV } \sim 100 \text{ times}$

$T_i = 200 \text{ MeV to } 600 \text{ MeV } \sim 3 \text{ times}$

τ relaxation time

$$M_{c,b} \gg \Lambda_{QCD}$$

Produced by pQCD process (before equilibrium)
(Early production)

$$\tau_{c,b} \gg \tau_{QGP}$$

They go through all the QGP life time

$$M_{c,b} \gg T_0$$

No thermal production

Boltzmann Kinetic equation

$$\left(\frac{\partial}{\partial t} + \frac{P}{E} \frac{\partial}{\partial x} + \mathbf{F} \cdot \frac{\partial}{\partial \mathbf{p}} \right) f(x, p, t) = \left(\frac{\partial f}{\partial t} \right)_{col}$$

- The plasma is uniform ,i.e., the distribution function is independent of \mathbf{x} .
- In the absence of any external force, $\mathbf{F}=\mathbf{0}$

$$R(p, t) = \left(\frac{\partial f}{\partial t} \right)_{col} = \int d^3k [\omega(p+k, k) f(p+k) - \omega(p, k) f(p)]$$

$$\omega(p, k) = g \int \frac{d^3q}{(2\pi)^3} f'(q) v_{q,p} \sigma_{p,q \rightarrow p-k,q+k} \rightarrow$$

is rate of collisions which change the momentum of the charmed quark from \mathbf{p} to $\mathbf{p}-\mathbf{k}$

$$\omega(p+k, k) f(p+k) \approx \omega(p, k) f(p) + \mathbf{k} \cdot \frac{\partial}{\partial \mathbf{p}} (\omega f) + \frac{1}{2} k_i k_j \frac{\partial^2}{\partial p_i \partial p_j} (\omega f)$$

$$\frac{\partial \mathbf{f}}{\partial \mathbf{t}} = \frac{\partial}{\partial \mathbf{p}_i} \left[\mathbf{A}_i(\mathbf{p}) \mathbf{f} + \frac{\partial}{\partial \mathbf{p}_j} [\mathbf{B}_{ij}(\mathbf{p}) \mathbf{f}] \right]$$

B. Svetitsky PRD 37(1987)2484

where we have defined the kernels

$$, \quad \mathbf{A}_i = \int d^3\mathbf{k} \omega(\mathbf{p}, \mathbf{k}) \mathbf{k}_i \quad \rightarrow \text{Drag Coefficient}$$

$$\mathbf{B}_{ij} = \int d^3\mathbf{k} \omega(\mathbf{p}, \mathbf{k}) \mathbf{k}_i \mathbf{k}_j \quad \rightarrow \text{Diffusion Coefficient}$$

Langevin Equation

The Fokker-Planck equation can be recast to Langevin equation:

$$d\mathbf{r} = \frac{p}{E} dt$$

$$\frac{dp}{dt} = -\gamma(p)p + \zeta \quad \text{with} \quad \langle \zeta_i(t)\zeta_k(t') \rangle = D\delta(t-t')\delta_{jk}$$

where γ is the deterministic friction (drag) force

ζ is stochastic force

For the bulk evolution: Hydrodynamics/Transport

Transport coefficients are connected by Fluctuation Dissipation Theorem.

Moore, Teaney, PRC 71 (2005) 064904

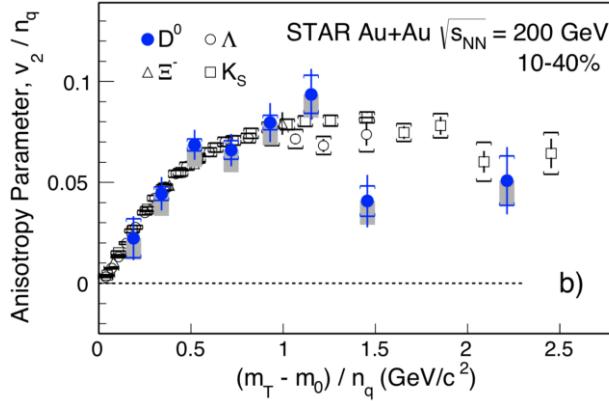
Van Hees, Greco, Rapp, PRC 73 (2006) 034913

Heavy quark initialization

- ✧ r-space: N_coll (Glauber mode)
- ✧ p-space: NLO (pQCD)

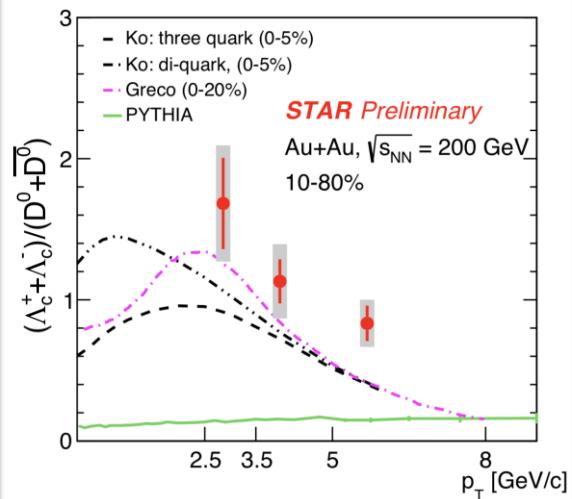
Heavy quark physics at different scales

low p_T



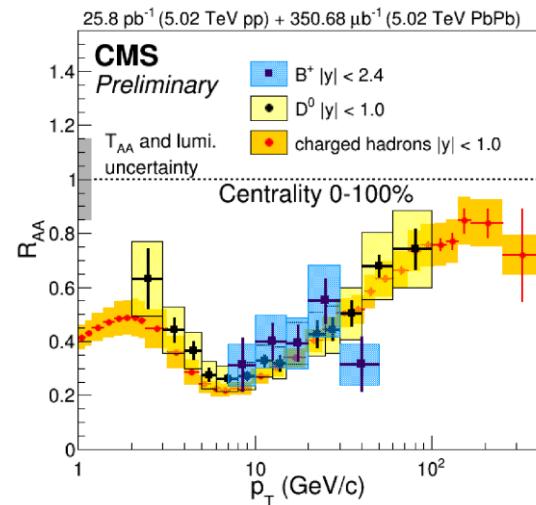
Study thermalization process of HQ
Constrain diffusion coefficient D_s

medium p_T



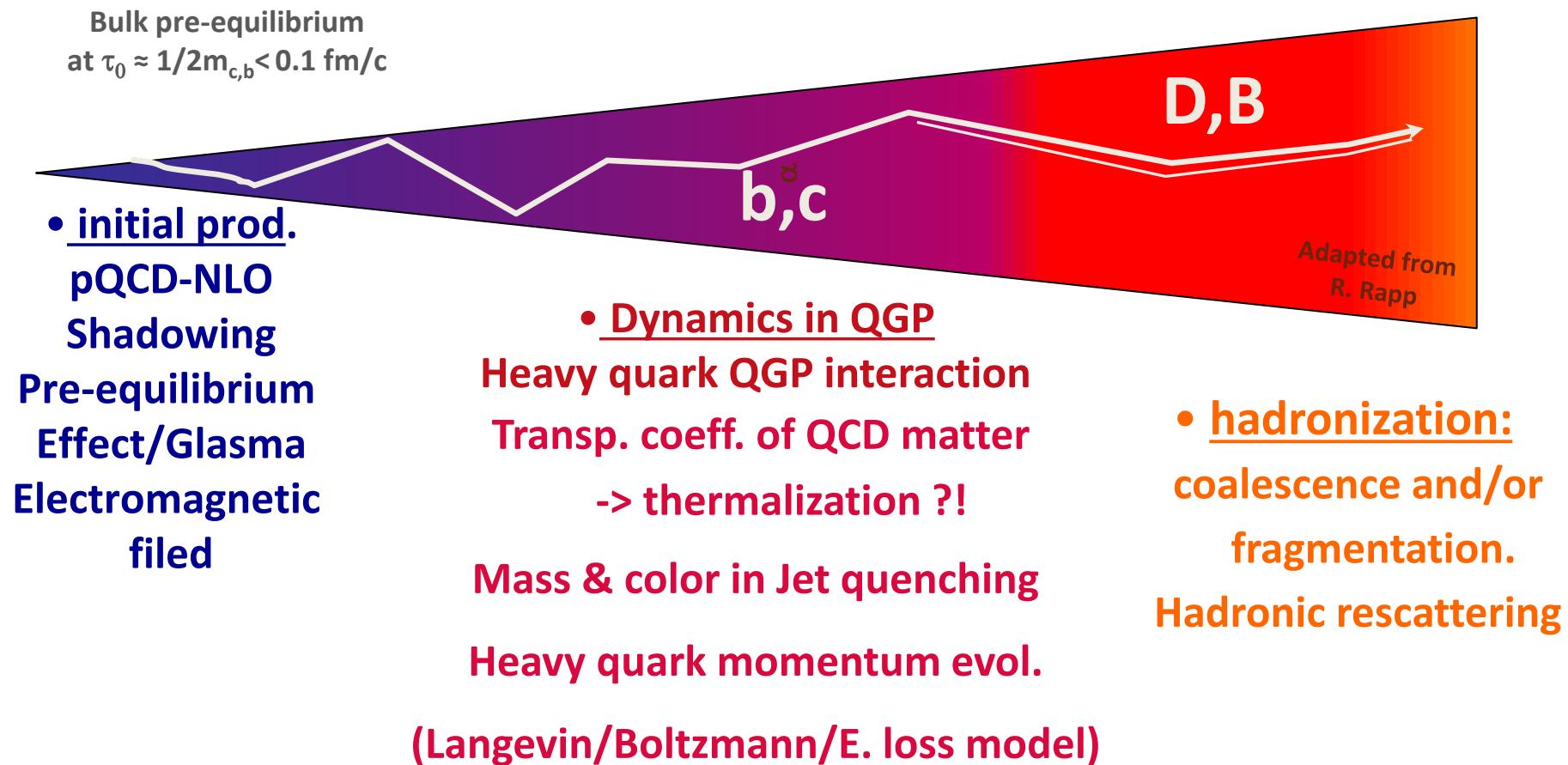
Study hadronization process of HQ
Constrain hadron wave-function

high p_T

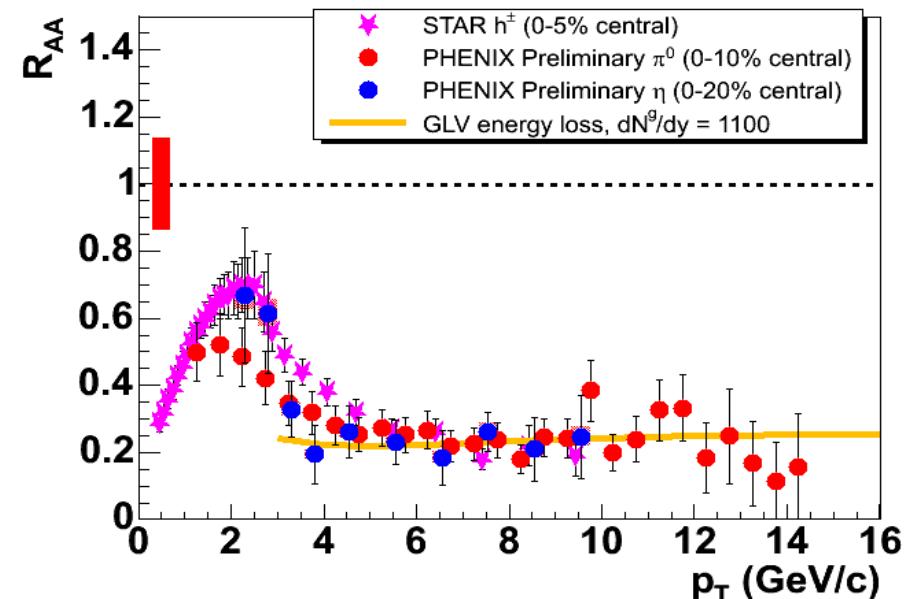
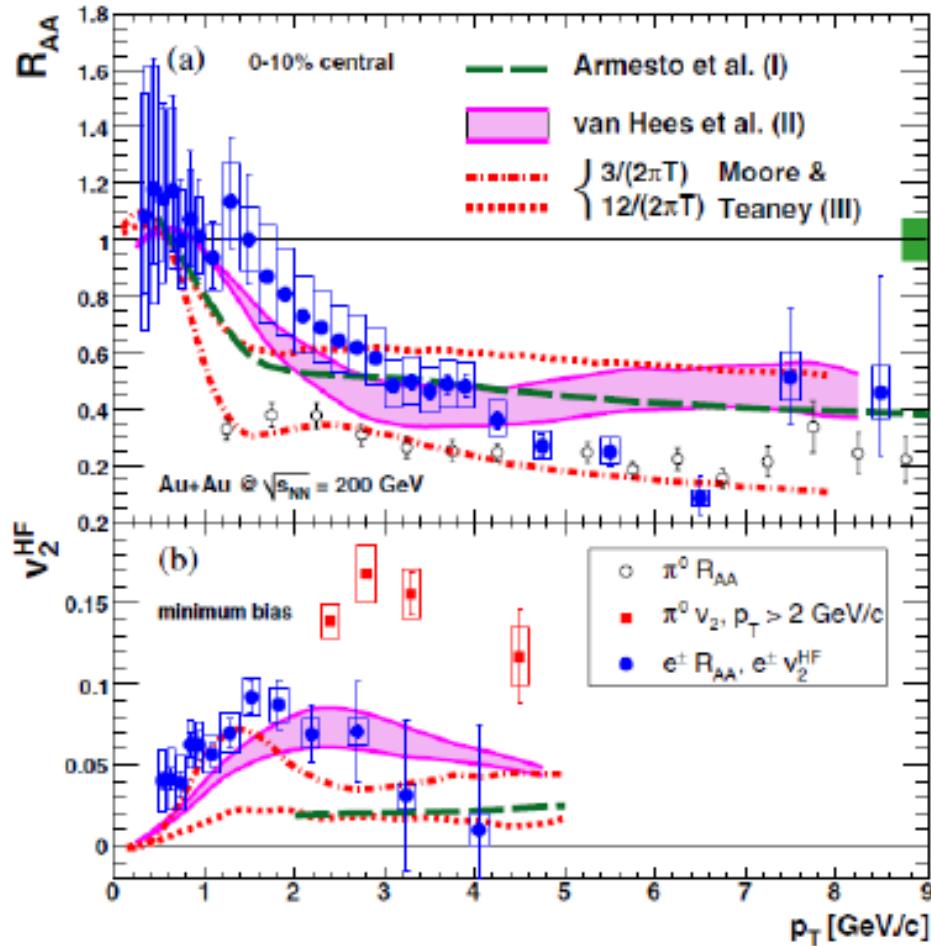


Study parton energy loss and mass effect
Constrain jet transport parameter \hat{q}

Studying the HF at RHIC and LHC



Heavy flavor at RHIC (2007)

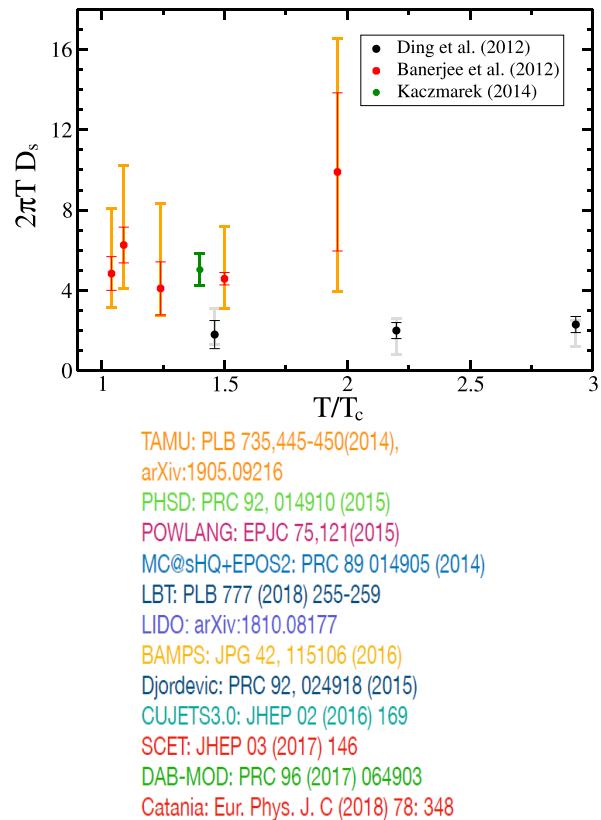
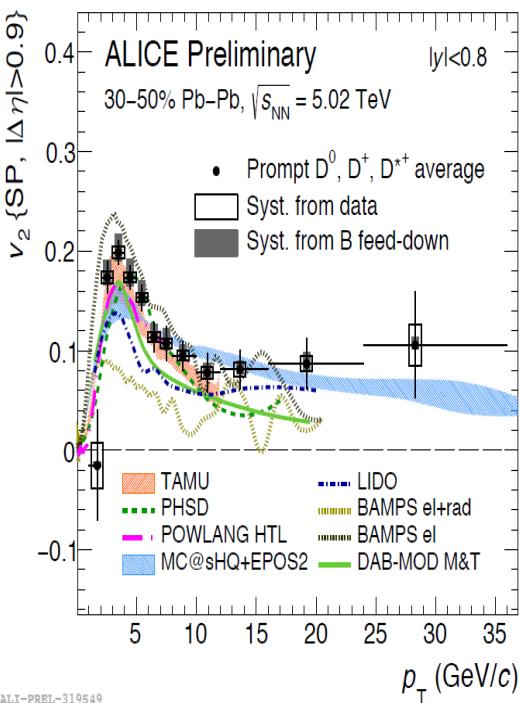
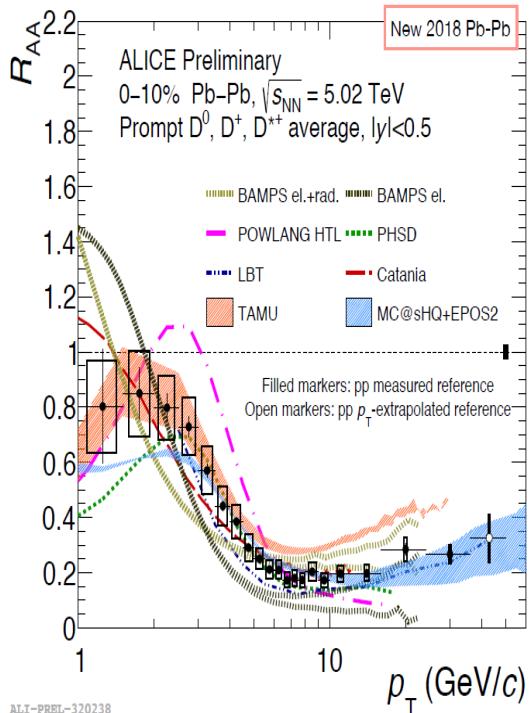


At RHIC energy heavy flavor suppression is similar to light flavor

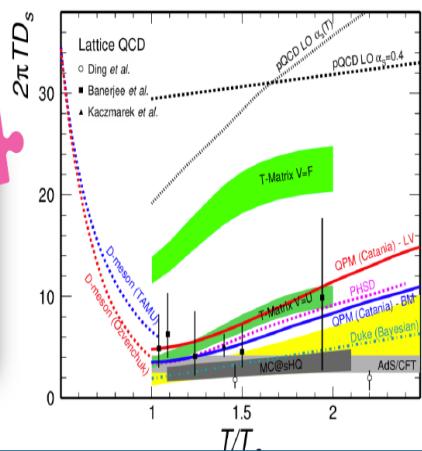
Simultaneous description of RAA and v_2 is a tough challenge for all the models.

R_{AA} and v_2

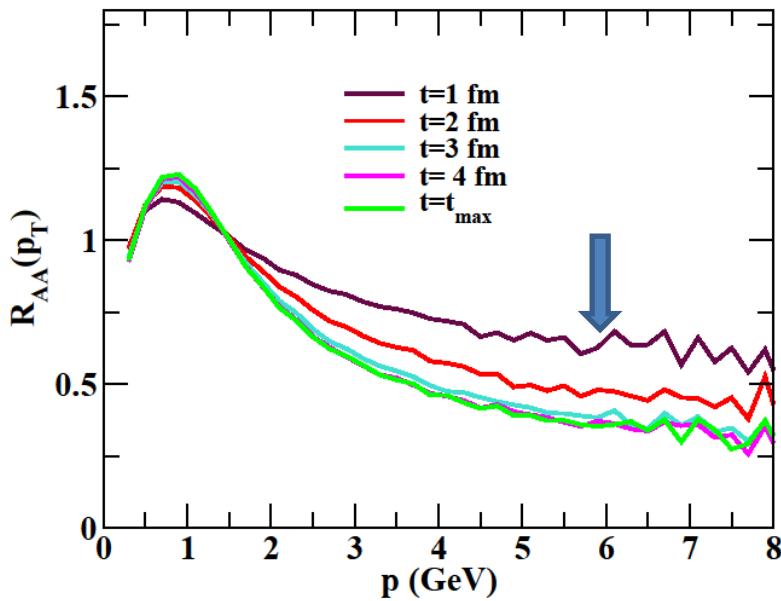
Comparison with models



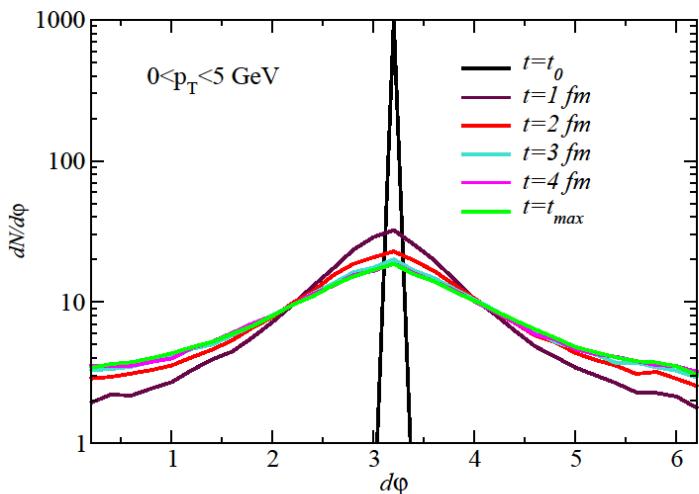
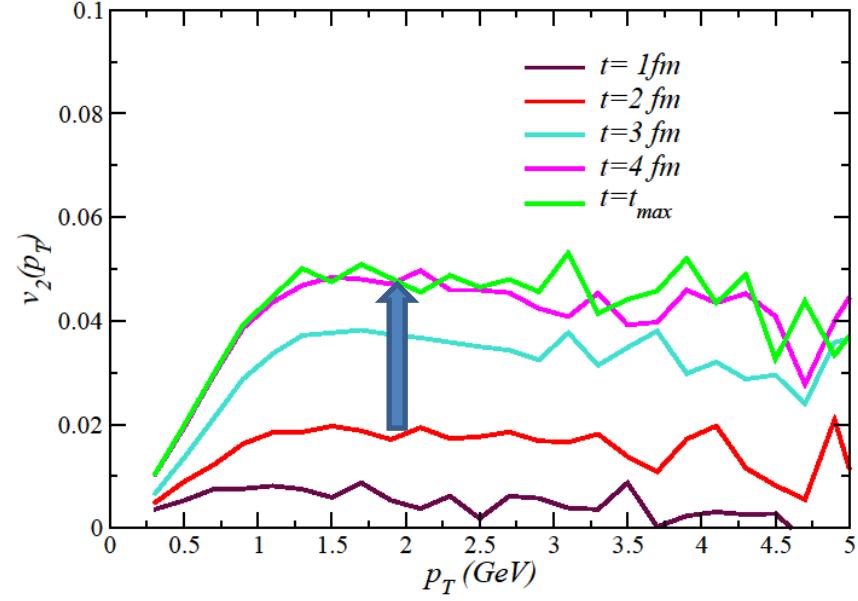
- Simultaneous description of R_{AA} and v_2 is challenging in the whole measured p_T range!
- Experimental measurements start to provide constraint to the models for the characterization of the charm and beauty interaction with the medium
- constraints on plasma transport parameters, such as the heavy-quark diffusion coefficient



Time evolution of Heavy quarks observables



Das, Scardina, Plumari, Greco
J. Phys. Conf. Ser. 668 (2016) 012051

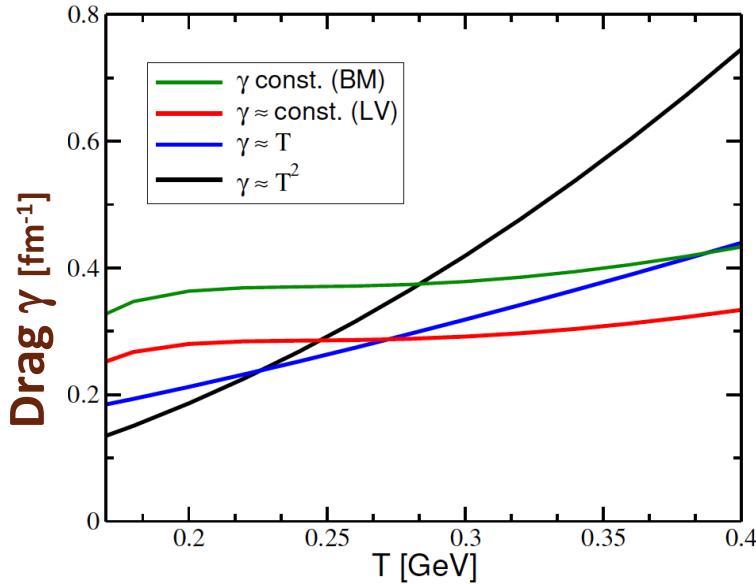


RAA and $dN/d\Phi$ developed during the early stage of the evolution → T_i

v_2 developed during the later stage of the evolution → T_c

T dependence of the interaction i.e the transport Coefficients are the essential ingradient for the simultanious description of HQ observables

Impact of T dep. interaction on $R_{AA} - v_2$



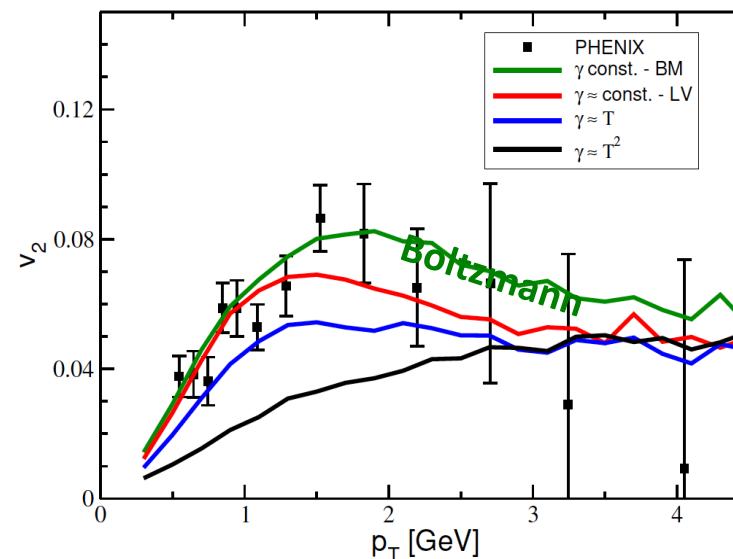
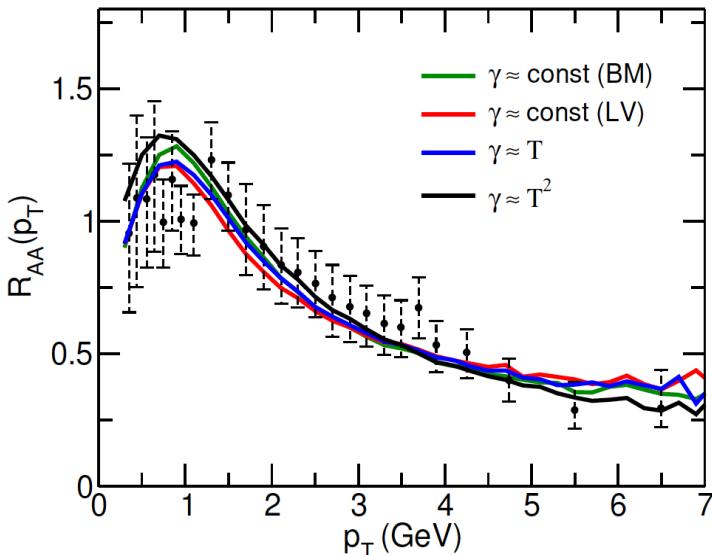
Looking at it beyond the specific modelings

➤ $\gamma \approx T^2$ [Ads/CFT, pQCD $\alpha_s = \text{const}$]

➤ $\gamma \approx T$ [pQCD strong α_s running]

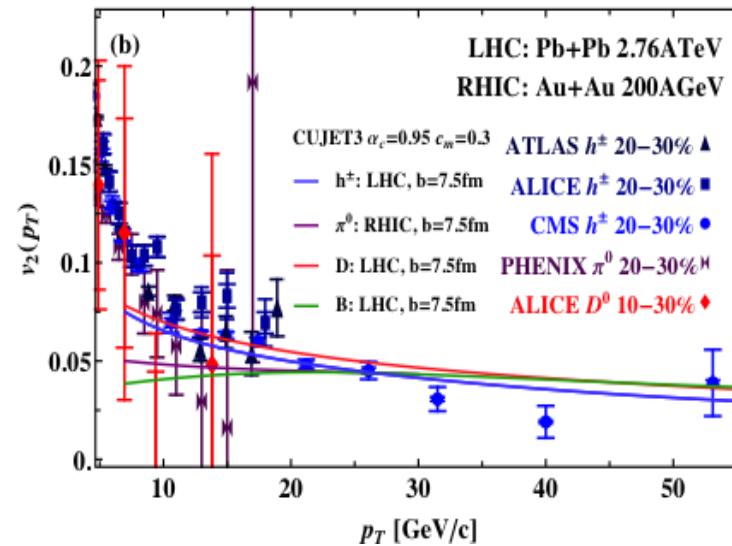
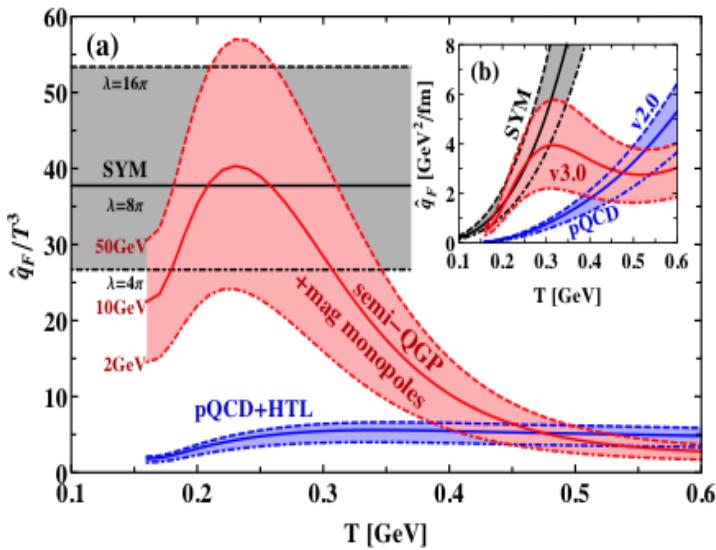
➤ $\gamma \approx \text{const.}$ [QPM, PHSD, T-matrix]

γ rescaled to fit $R_{AA}(p_T)$, D from FDT



R_{AA} vs. v_2 puzzle

Different temperature dependence of the interaction strength may lead to different v_2 for the same R_{AA} .



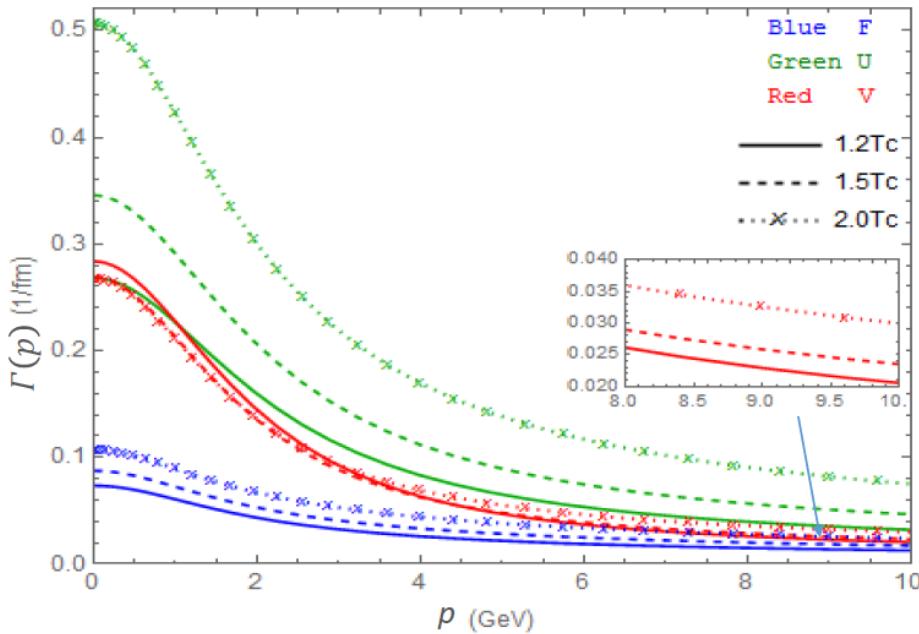
Semi-quark-gluon monopole plasma model increases \hat{q} around T_c and enhances hard probes' v_2 .

T-matrix developments [TAMU]:

❖ Relaxation rate (drag coefficient)

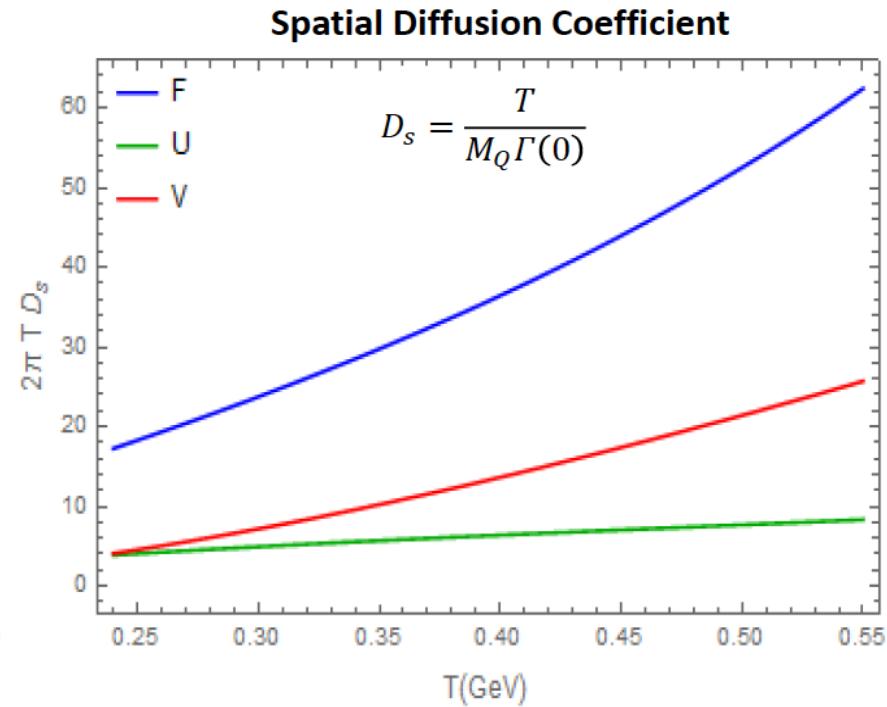
$$\Gamma(p) = \frac{1}{2\omega_Q(p)} \sum \int d^3\tilde{q} d^3\tilde{q}' d^3\tilde{p}' n_i(\omega_q) \cdot \frac{(2\pi)^4}{d_c} C_f |T(E_{cm} | \mathbf{p}_{cm}, \mathbf{p}'_{cm})|^2 \delta^4(p + q - p' - q') \left(1 - \frac{p \cdot p'}{p^2}\right)$$

Relaxation rate for F U V



❖ For V

- Infrared enhancement due to long range force
- Different (slightly reversed) T dependence at low p
- Recover usual T dependence at high p

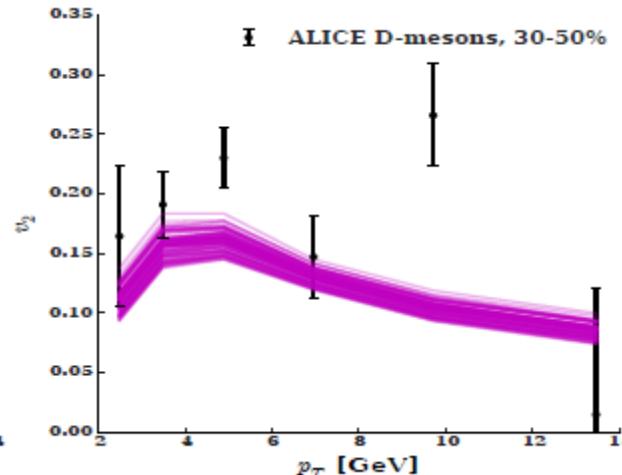
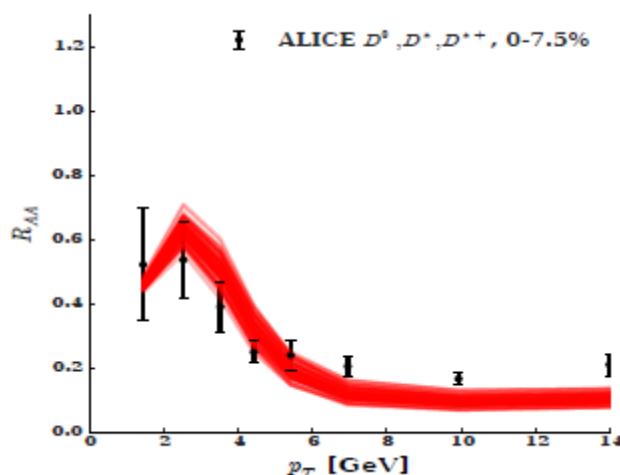


Radiative loss in T-matrix approach
Large suppression due to thermal mass
Impact on observables yet to see

Bayesian model to data analysis [Duke]:

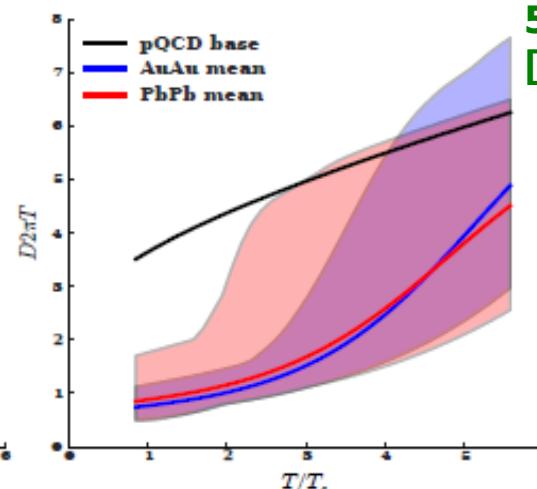
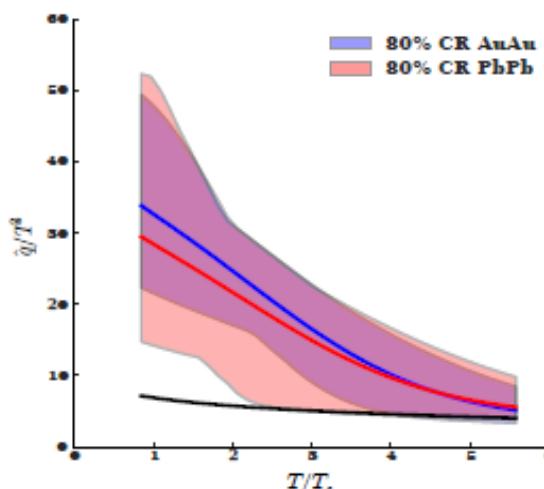
Simultaneously calibrate all model parameters through model-to-data comparison.

Extract the probability distribution of all parameters which best describe the data.



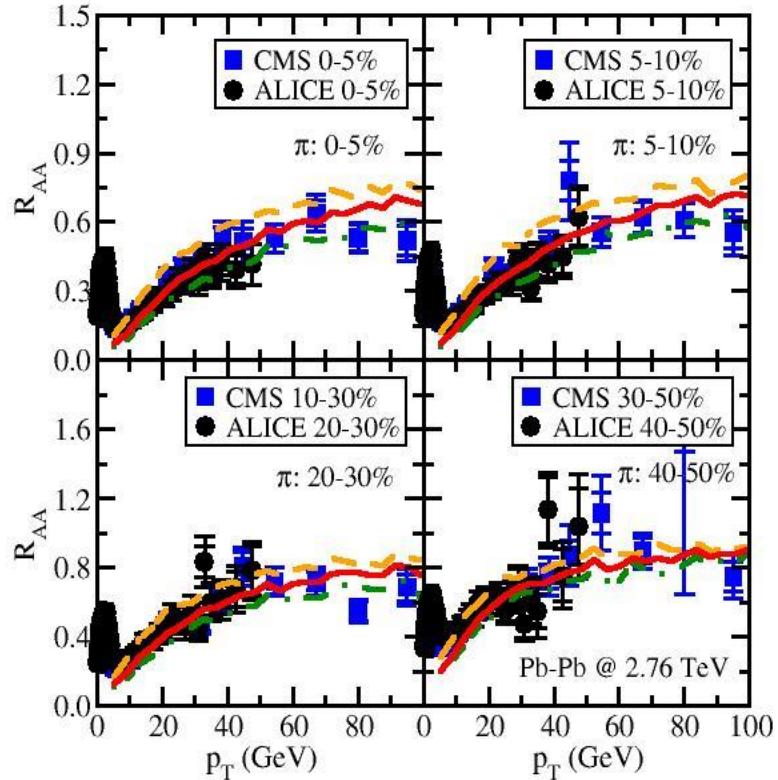
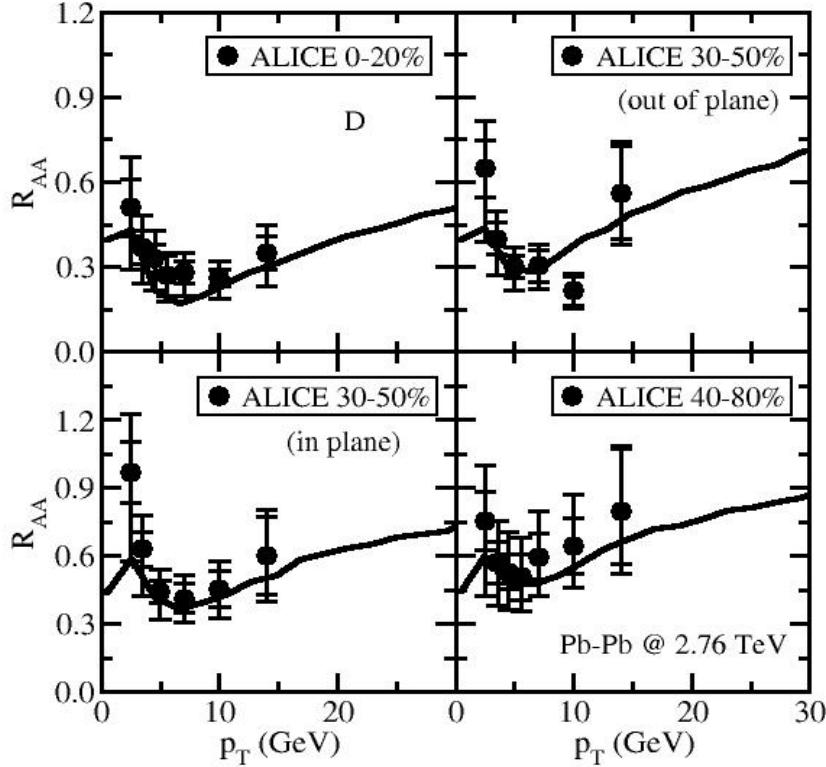
One can extract both the temperature and momentum dependence of heavy quark transport coefficients .

$$T, p\text{-dependence: } \hat{q} = \hat{q}_{pQCD} * preK * (1 + K_p e^{-\frac{|p|^2}{2\sigma_p^2}}) * (1 + K_T e^{-\frac{(T - T_c)^2}{2\sigma_T^2}}) \quad D_s = T^2 / \hat{q}$$



5 dimensional Parameter space:
[preK, K_p σ_p , K_T σ_T]

Approach from low to high p_T from heavy to light (high-pt) [LBL-CCNU]



Spectrum of medium-induced gluon (higher-twist formalism):

$$\frac{dN_g}{dx dk_\perp^2 dt} = \frac{2\alpha_s C_A P(x)}{\pi k_\perp^4} \hat{q} \left(\frac{k_\perp^2}{k_\perp^2 + x^2 M^2} \right)^4 \sin^2 \left(\frac{t - t_i}{2\tau_f} \right)$$

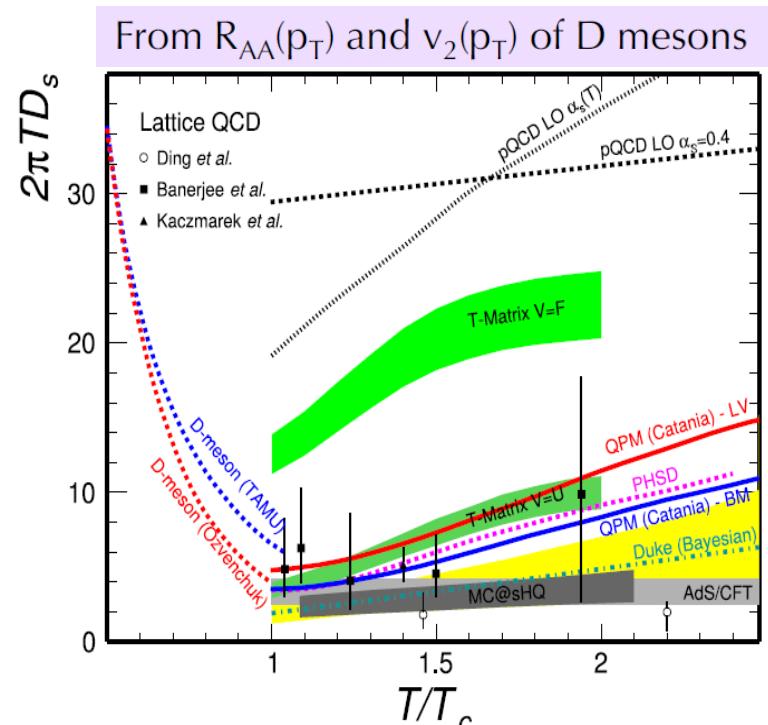
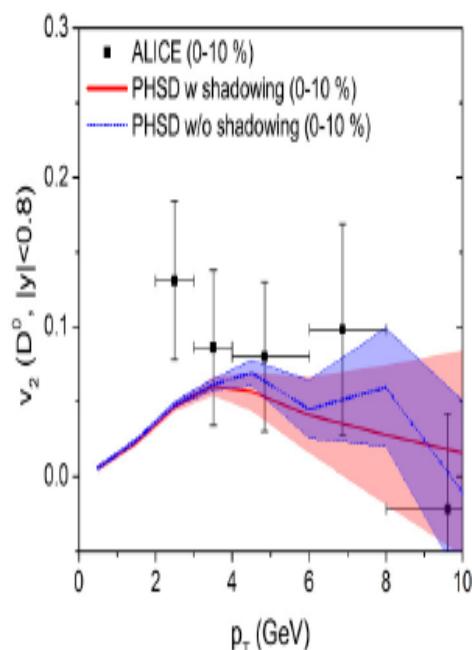
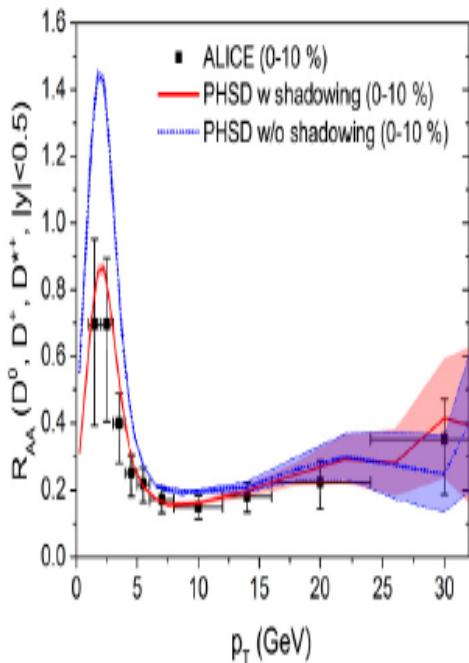
Linearized Boltzmann transport model
Both collisional and radiative loss

$$K_p = 1 + A_p e^{-|\vec{p}|^2/2\sigma_p^2}, \quad (\text{T-matrix like features})$$

$$K_T = 1 + A_T e^{-(T - T_c)^2/2\sigma_T^2} \quad (\text{Catania-QPM, PHSD, T-matrix})$$

T and p dependent K factor needed starting from pQCD

RAA and v_2 @PHSD



Dong, Greco, *PPNP* 104 (2019) 97-141

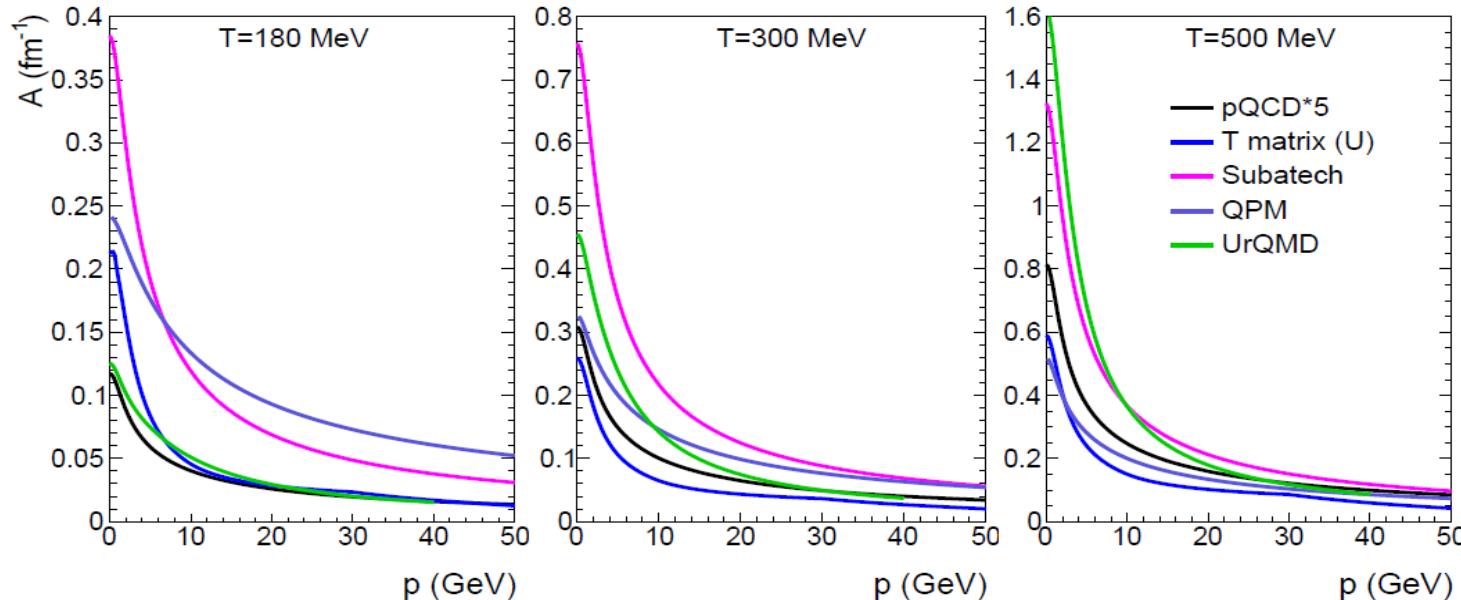
T. Song et al. *PRC* 93, 034906 (2016)

Brambilla et. al 2007.10078 [hep-lat]
Altenkort et al. 2009.13553 [hep-lat]

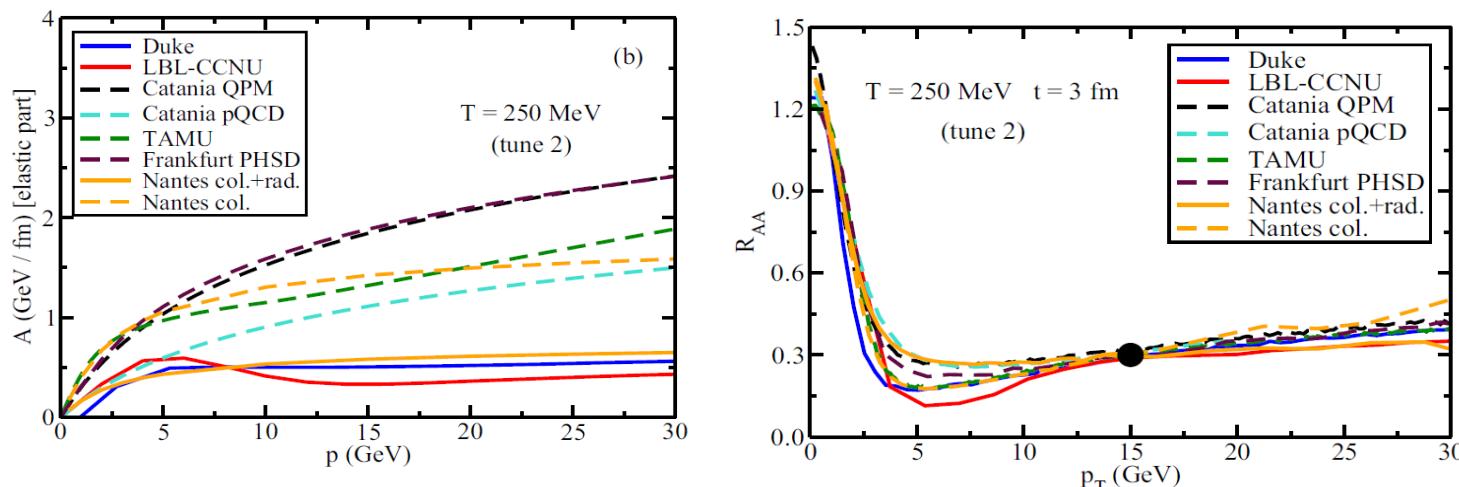
Heavy quark transport coefficients computed within Polyakov loop plasma showing similar T and p-dependence of heavy quark transport coefficients like T-matrix, QPM and PHSD.

Singh et al. *PRD* 100 (2019) 114019

A systematic attempts are going on within the EMMI-RRTF and “JET-HQ” working groups to find a common agreement between different groups:



R. Rapp et.al NPA 979 (2018) (EMMI-RRTF)

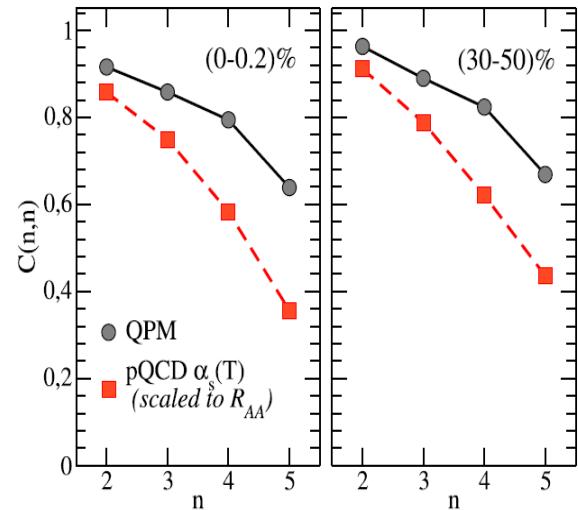
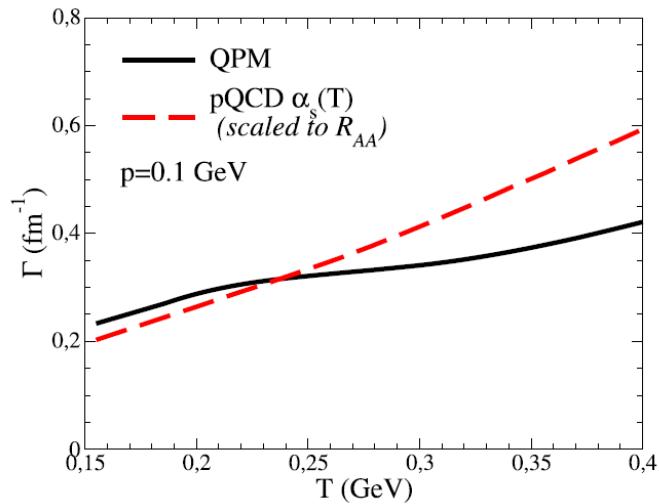
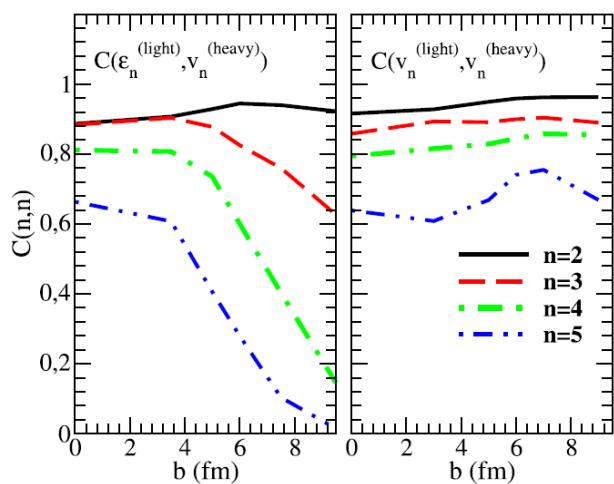


S. Cao et. al PRC 99, 054907 (2019) (JET-HQ)

New observables:

Heavy-light event-by-event correlation

$$C(n, m) = \frac{\sum_i (v_n^{L,i} - \langle v_n^L \rangle)(v_m^{H,i} - \langle v_m^H \rangle)}{\sqrt{\sum_i (v_n^{L,i} - \langle v_n^L \rangle)^2 \sum_i (v_m^{H,i} - \langle v_m^H \rangle)^2}}$$



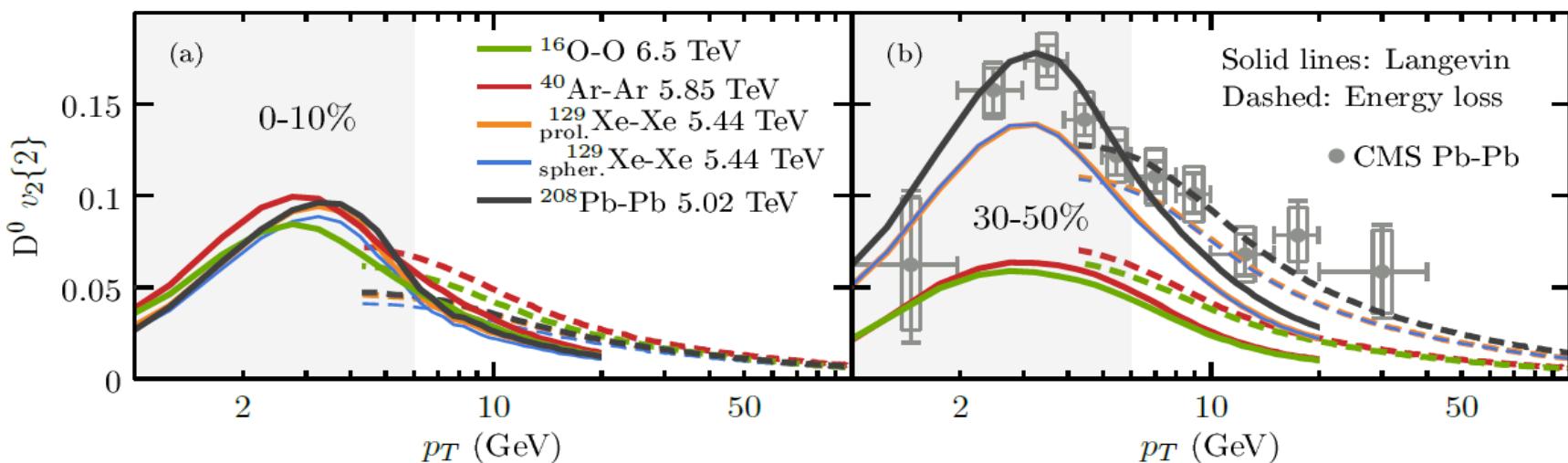
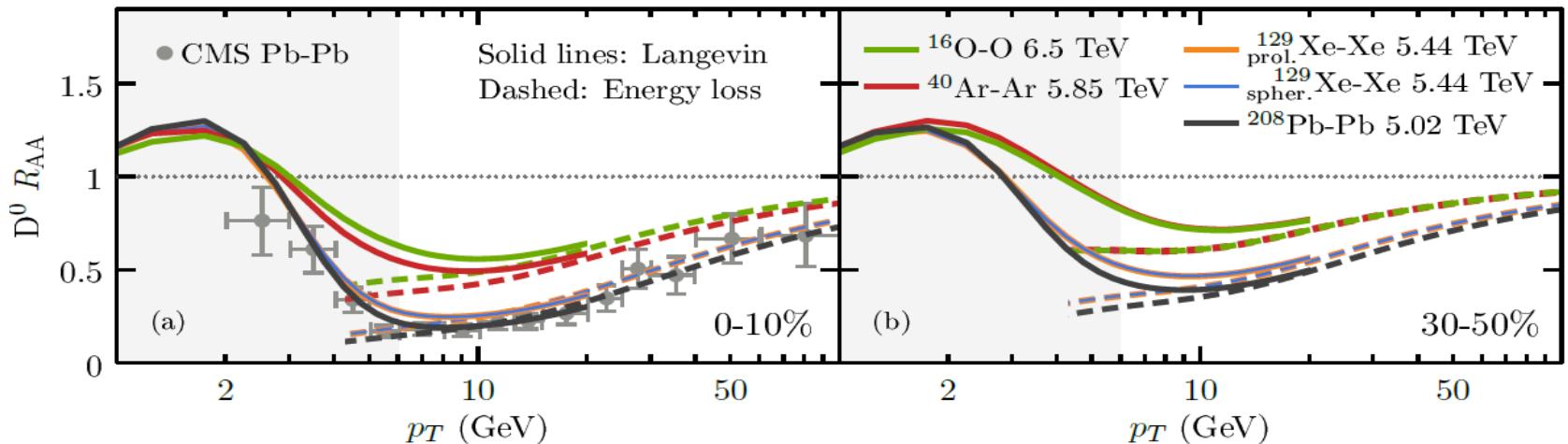
$v_n(D)$ more correlated to $v_n(N_{ch})$ than ϵ_n

Very large sensitivity to T dep. of Ds

This can put further constrain on heavy quark transport coefficients

Plumari Coci, Minissale, Das, Sun, Greco
PLB 805 (2020) 135460

System size scan of D meson R_{AA} and v_2



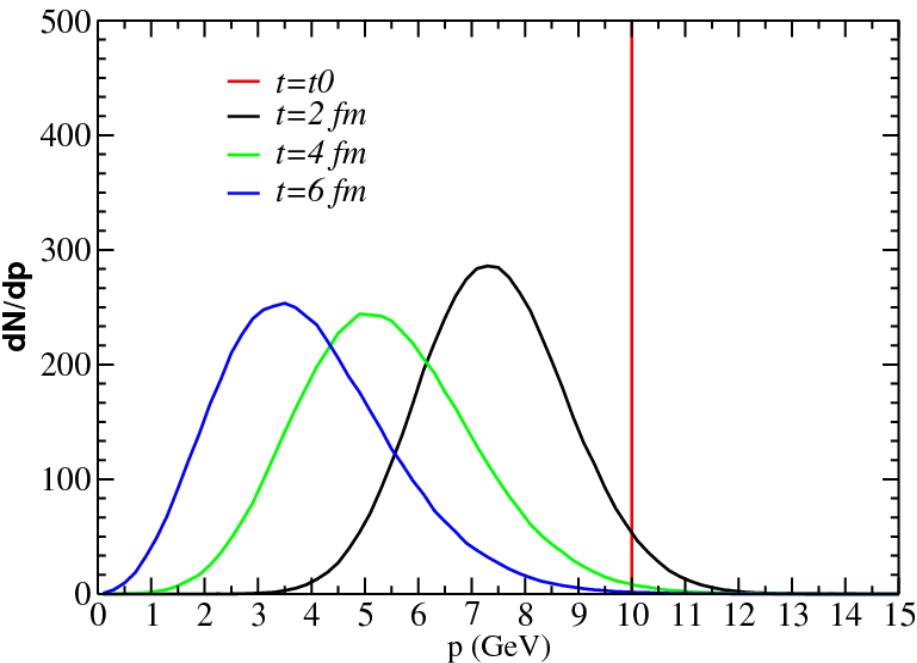
**In central collisions the v_2 is independent of system size.
System size vs Eccentricity**

Evolution: Boltzmann vs Langevin (Charm)

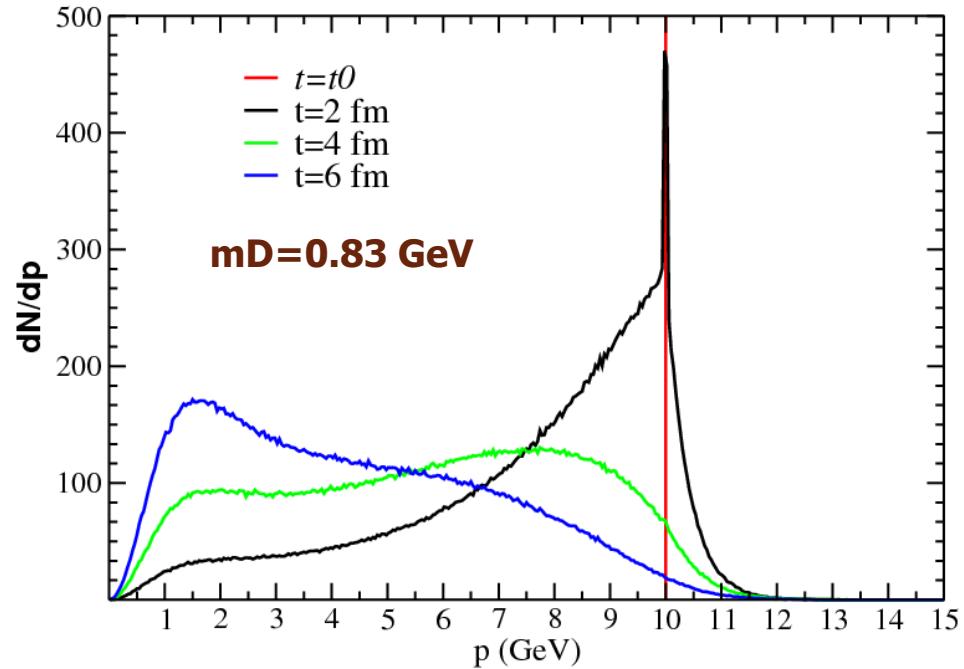
Momentum evolution starting from a δ (Charm) in a Box

$$\frac{dN}{d^3 p_{initial}} = \delta(p - 10\text{GeV})$$

Langevin



Boltzmann



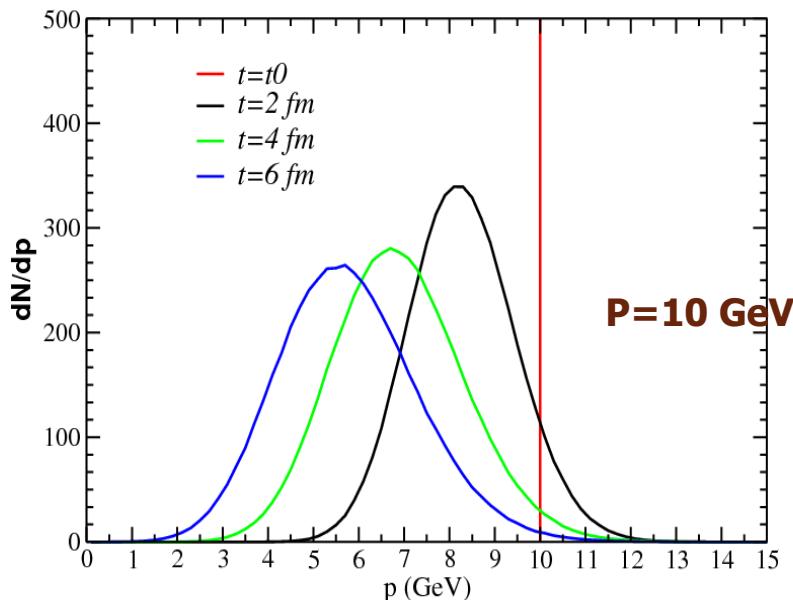
In case of Langevin the distributions are Gaussian as expected by construction

In case of Boltzmann the charm quarks does not follow the Brownian motion

Das, Scardina, Plumari and Greco
PRC,90,044901(2014)

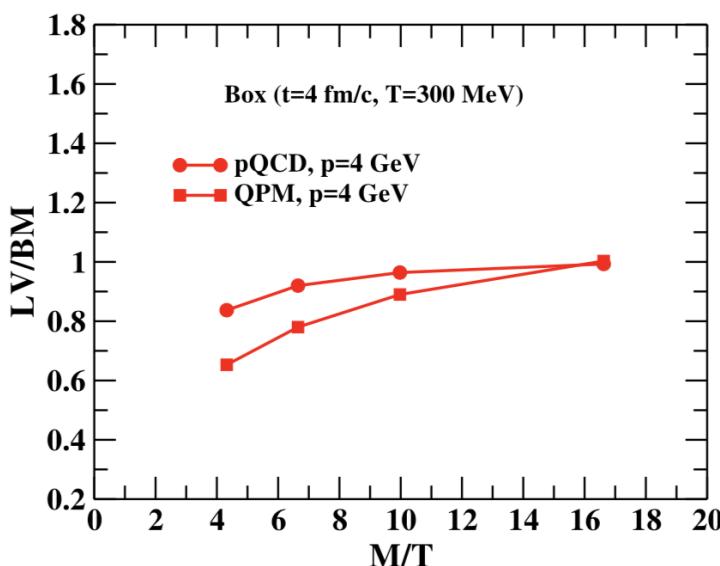
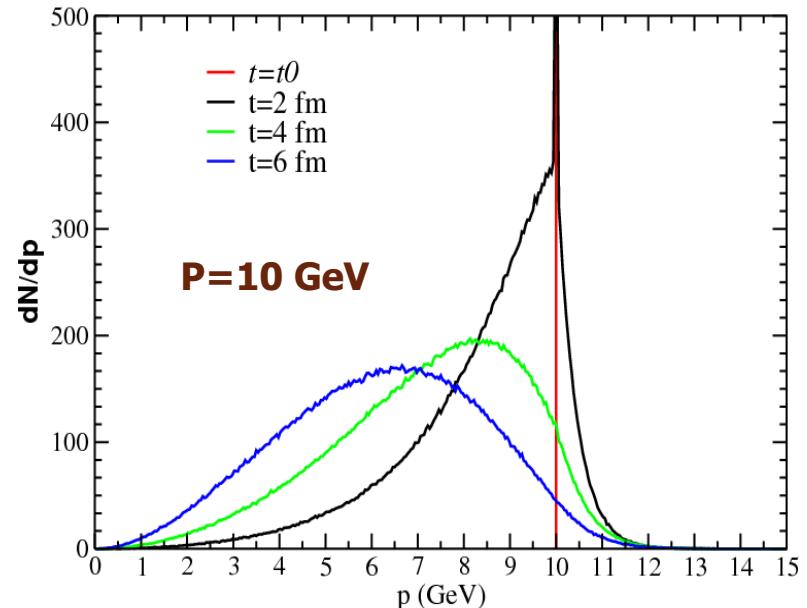
Momentum evolution starting from a δ (Bottom)

Langevin



In a Box

Boltzmann



Das, Scardina, Plumari and Greco
PRC,90,044901(2014)

Langevin dynamics overestimate the interaction
Boltzmann generate more v_2 for the same RAA.

Rapp et. al. EMMI-RRTF, NPA 979 (2018)

Hadronization: Coalescence plus Fragmentation

Fragmentation function gives the probability to get a hadron from a parton:

$$f_H(p_T) = \sum_p f_p(p_T / z) \otimes D_{p \rightarrow H}(z)$$

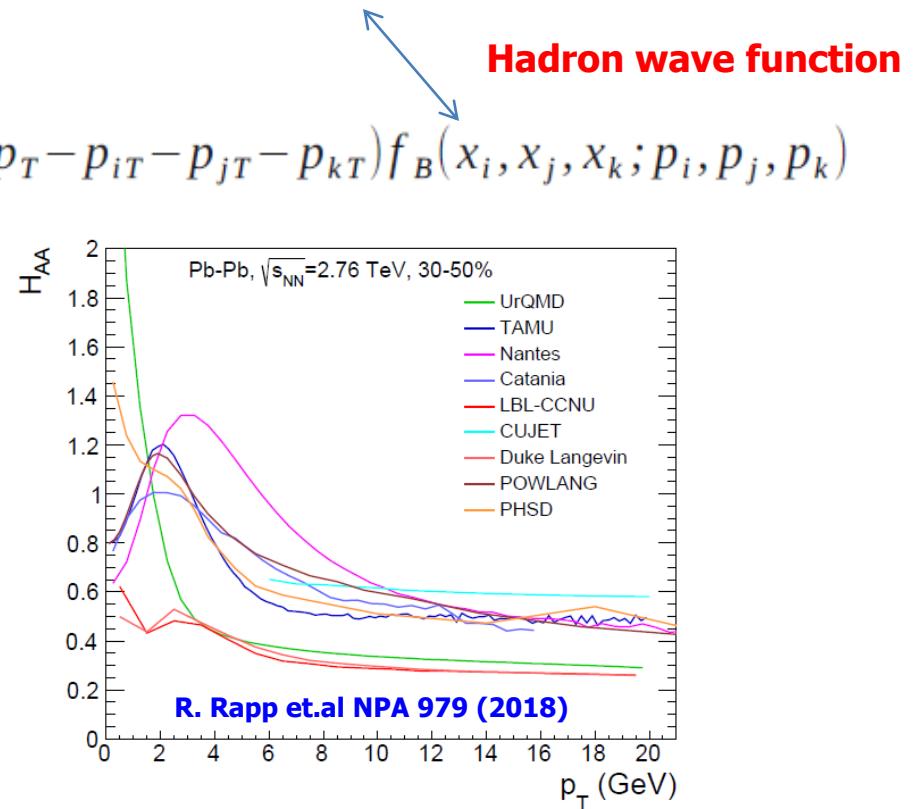
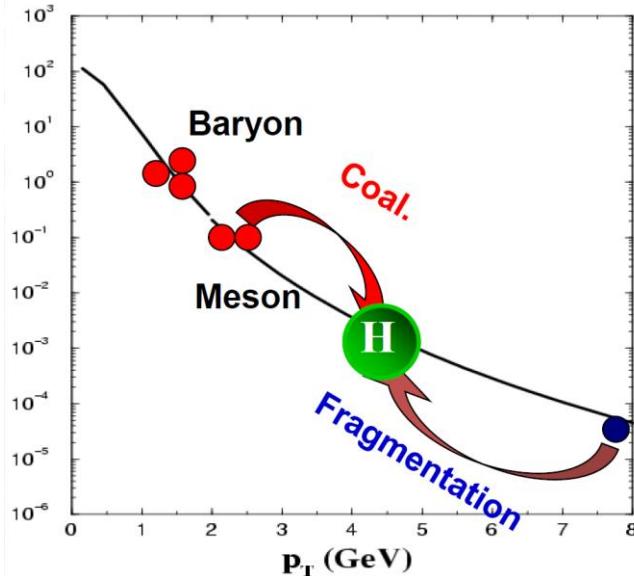
$\langle z \rangle \sim 0.9$ for charm quark and $\langle z \rangle \sim 0.5$ for light quark

Coalescence is the convolution of two /three parton distribution folded by a wave function:

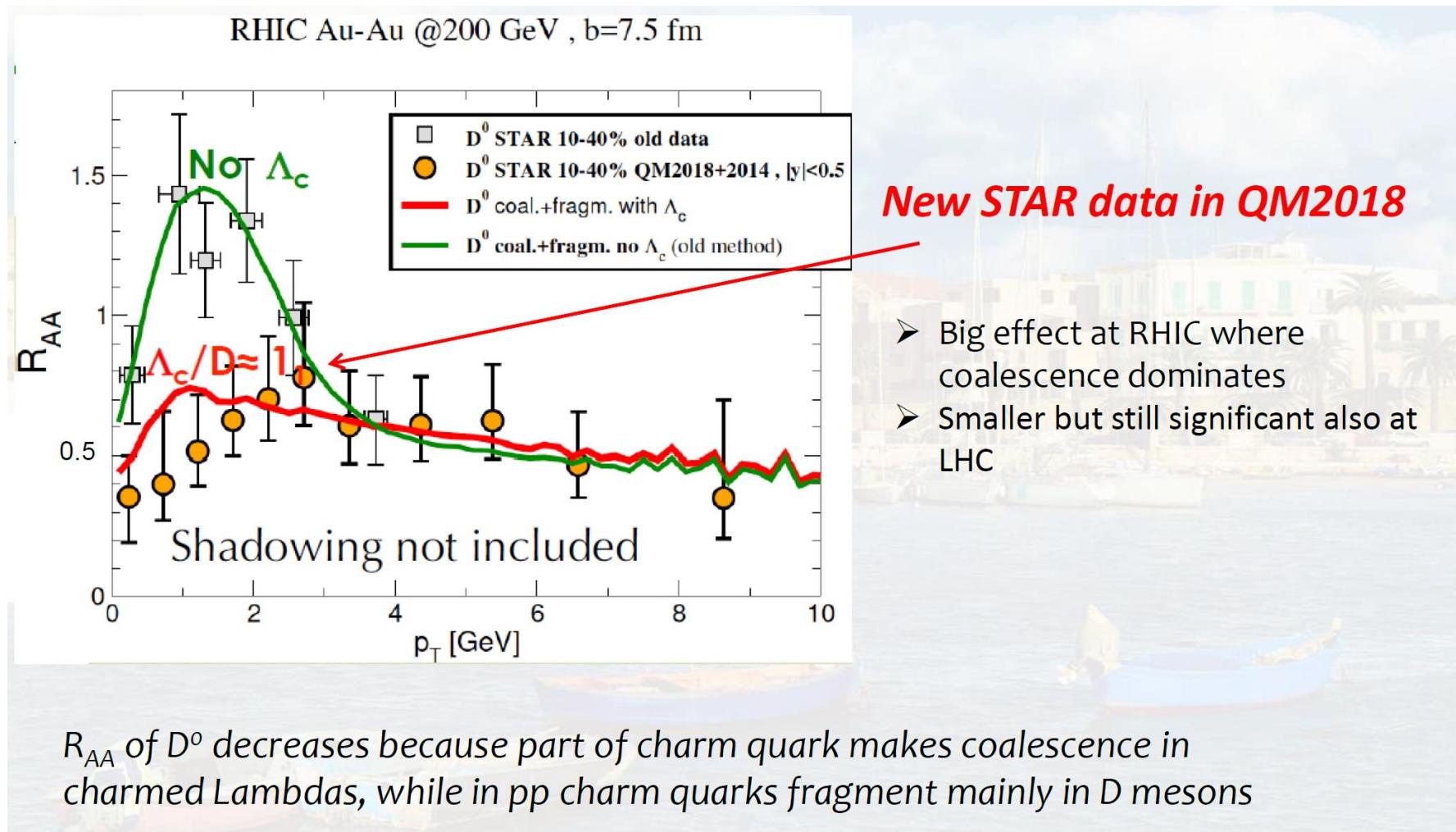
$$\frac{dN_{\text{Meson}}}{d^2 p_T} = g_M \sum_{i,j} P_q(i) P_q(j) \delta^{(2)}(p_T - p_{iT} - p_{jT}) f_M(x_i, x_j; p_i, p_j)$$

V. Greco, C.M. Ko, and P. L'evai
PRL 90, 202302 (2003)

$$\frac{dN_{\text{Baryon}}}{d^2 p_T} = g_B \sum_{i,j,k} P_q(i) P_q(j) P_q(k) \delta^{(2)}(p_T - p_{iT} - p_{jT} - p_{kT}) f_B(x_i, x_j, x_k; p_i, p_j, p_k)$$



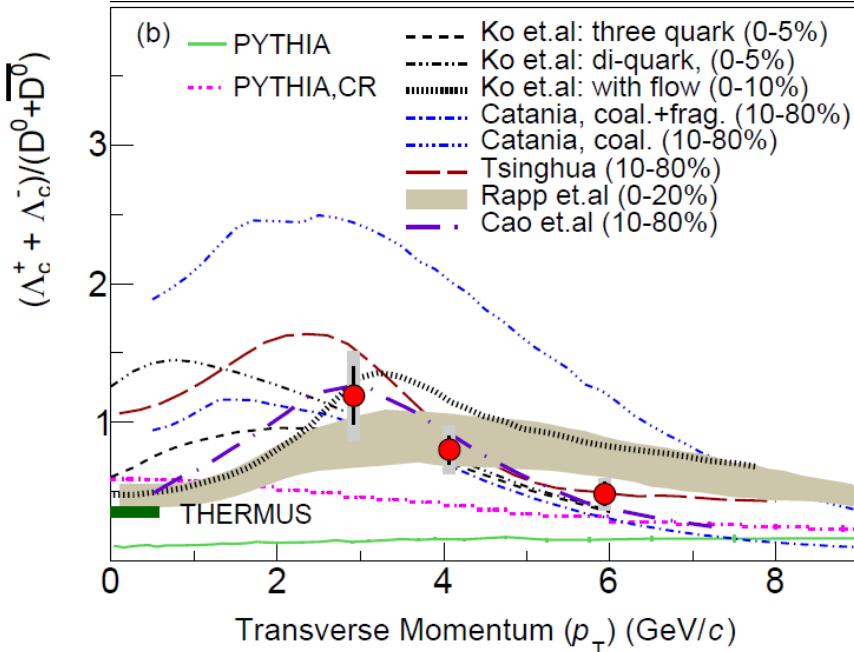
Impact of heavy baryon to meson ratio on heavy quark suppressions



Minissale at.al (SQM-2019)

Heavy Baryon to meson ratio

(Serve as a tool to disentangle different hadronization mechanisms)

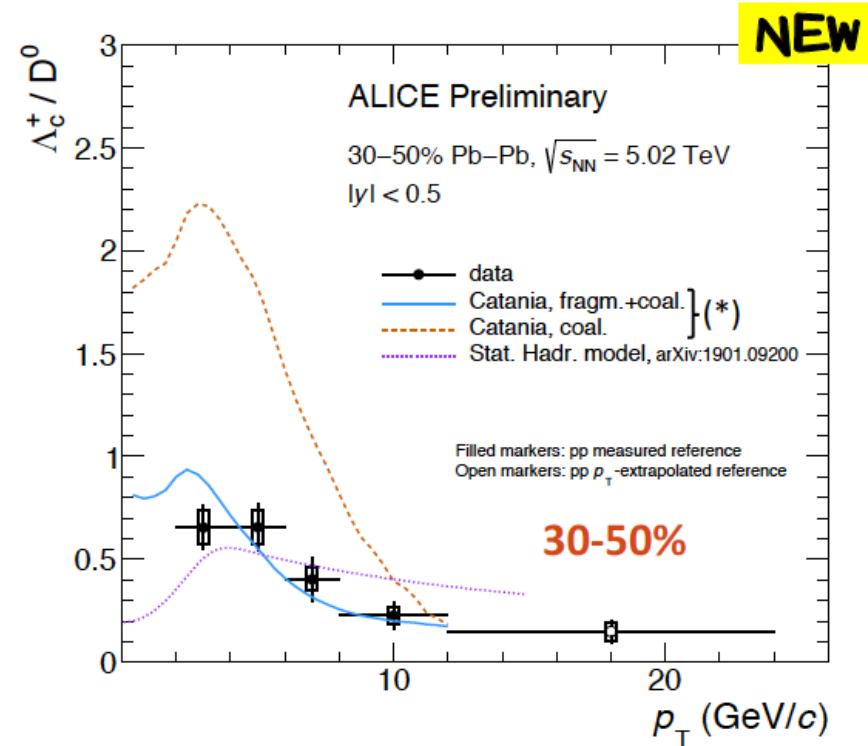


STAR, Phys. Rev. Lett. 124, 172301 (2020)

$P_{coal}=1$

to all hadron at $p \rightarrow 0$

Plumari et al. EPJC 78 (2018) 4, 348



Baryon in resonance recombination model

He, Rapp, PRL 124 (2020) 042301

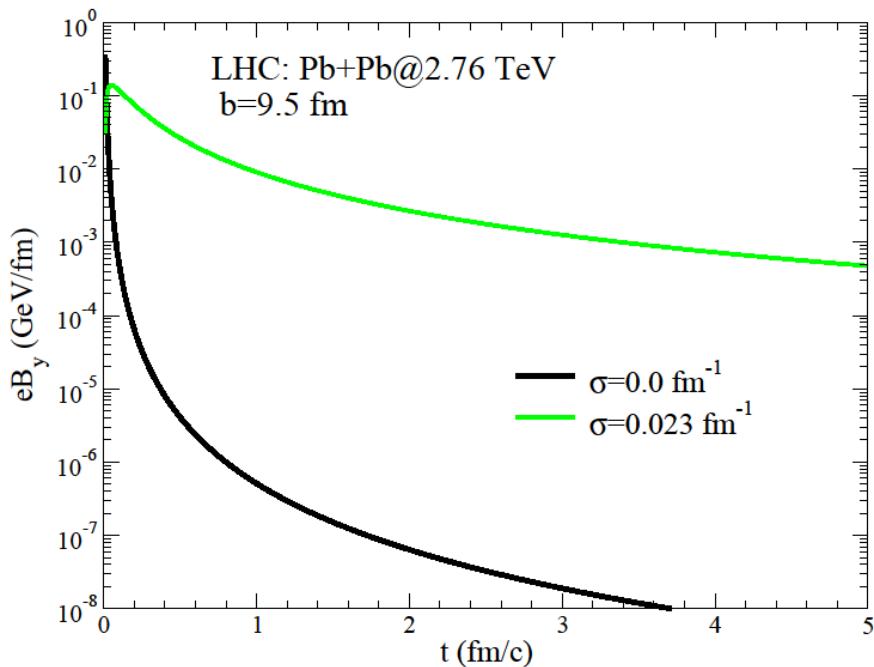
Impact of EM field on heavy quark dynamics at LHC

$$dp_j = -\Gamma p_j dt + \sqrt{dt} C_{jk}(t, p + \xi dp) \rho_k + F_{ext} dt$$

$$F_{ext} = q(E' + v \times B')$$

$$E' = \gamma (E + v \times B) - (\gamma - 1) (E \cdot \hat{v}) \hat{v}$$

$$B' = \gamma (B - v \times E) - (\gamma - 1) (B \cdot \hat{v}) \hat{v}$$



Gursoy, Kharzeev and Rajagopal
PRC 89, 054905 (2014)

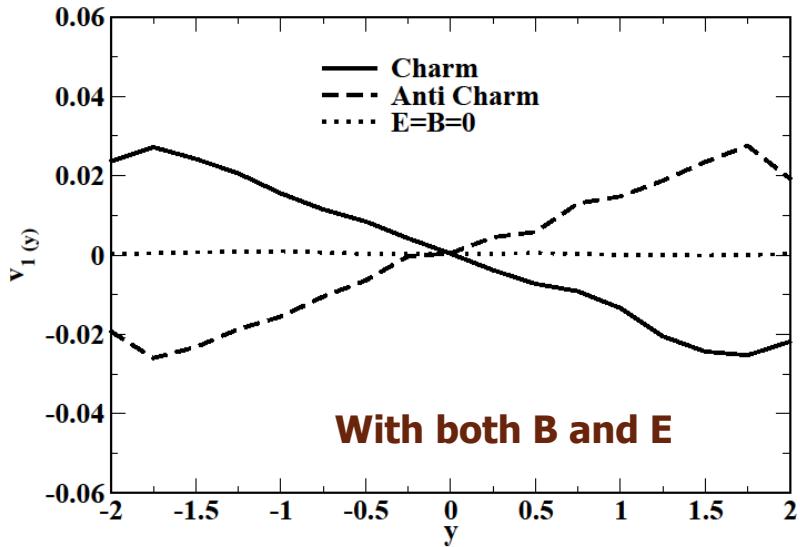
Electromagnetic field has been included in the Langevin equation as a external force.

We consider both E and B.
 $B_x = B_z = 0$
And $E_y = E_z = 0$

$$\nu_1 = \langle \frac{p_x}{p_T} \rangle$$

Das, Plumari, Chartarjee, Scardina, Greco, Alam
Phys. Lett. B, 768 (2017) 260

Heavy quark v_1 @LHC

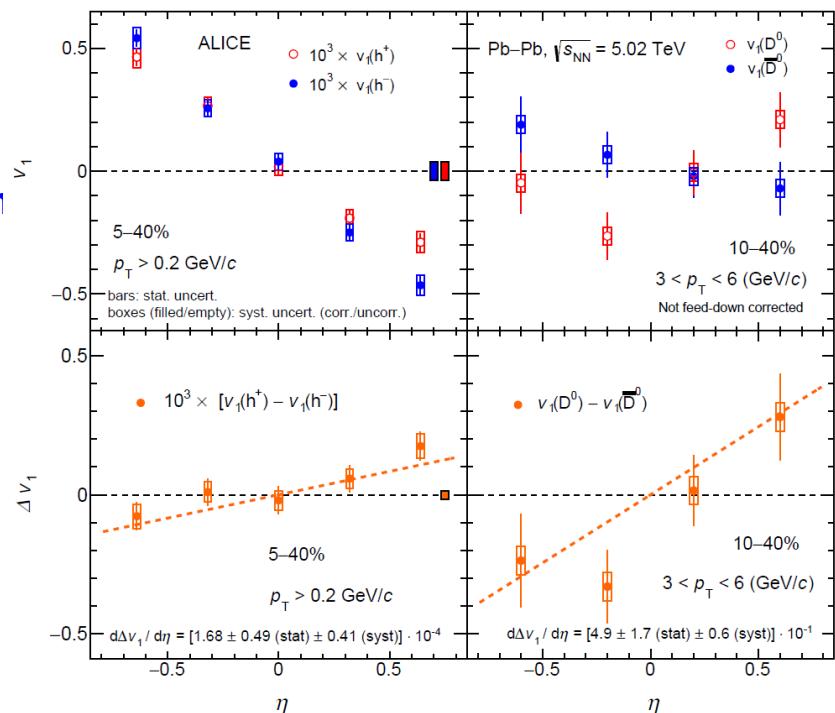
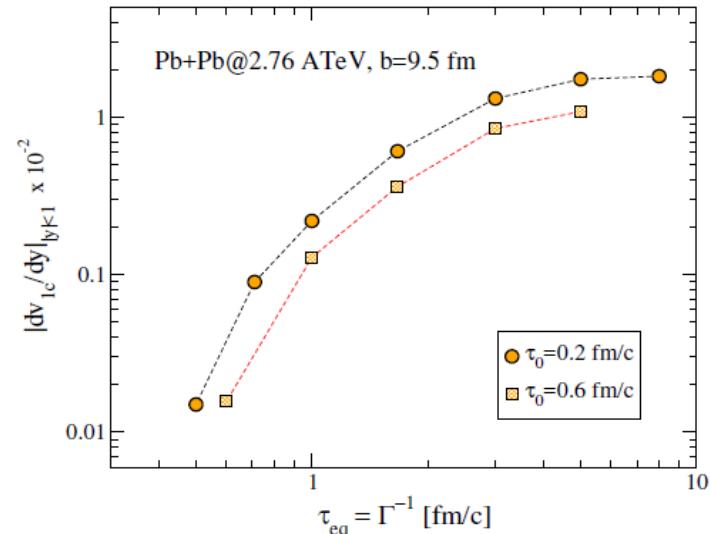


Das, Plumari, Chartarjee, Scardina, Greco, Alam
 Phys. Lett. B, 768 (2017) 260

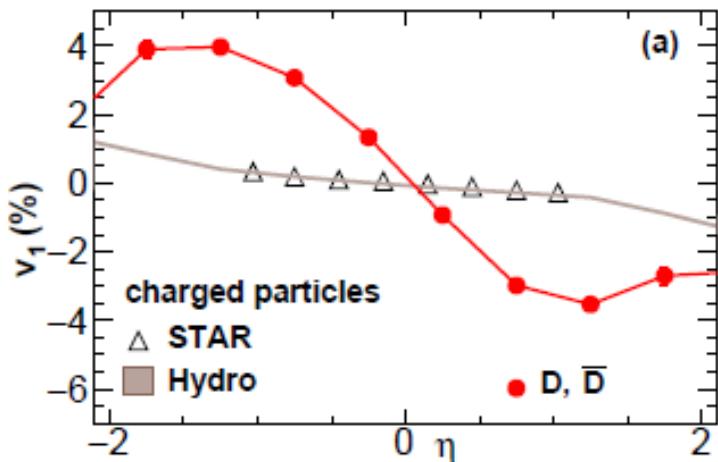
Heavy quark v_1 is larger than light quark v_1 .

Recent data from ALICE indicates splitting
 in D and Dbar v_1 .

ALICE Collaboration, PRL 125 (2020) 2, 022301

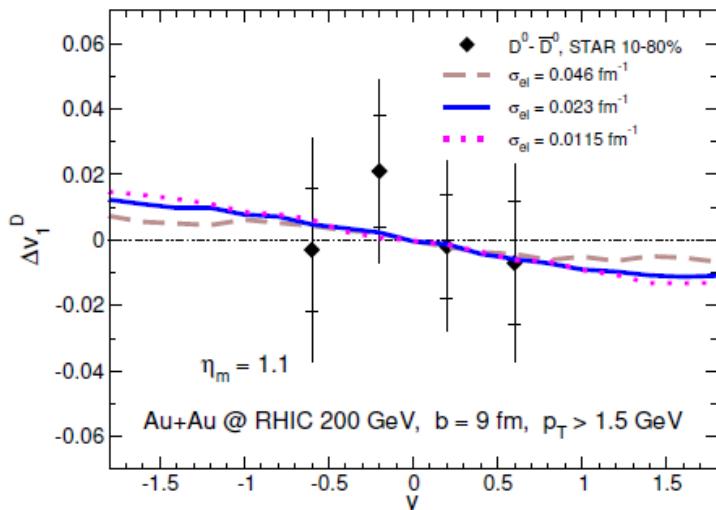


Initial vorticities and electromagnetic field

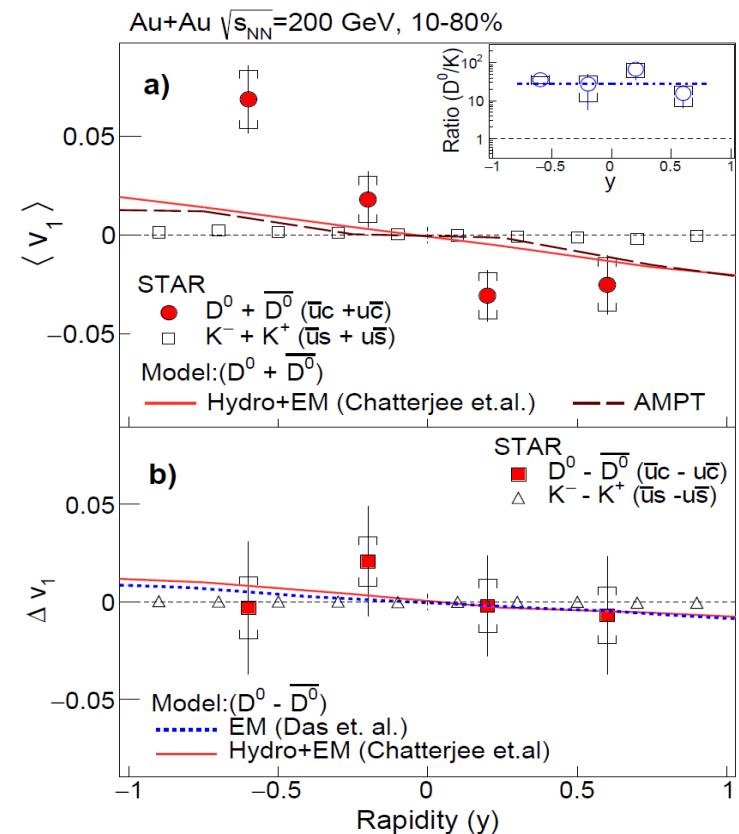


Impact of tilt bulk: Forward backward asymmetry

Chatterjee and Bozek, PRL 120 (2018) 192301



Oliva, Plumari, Greco, arxiv:2009.11077 [hep-ph]



STAR, PRL 123 (2019) 16, 162301

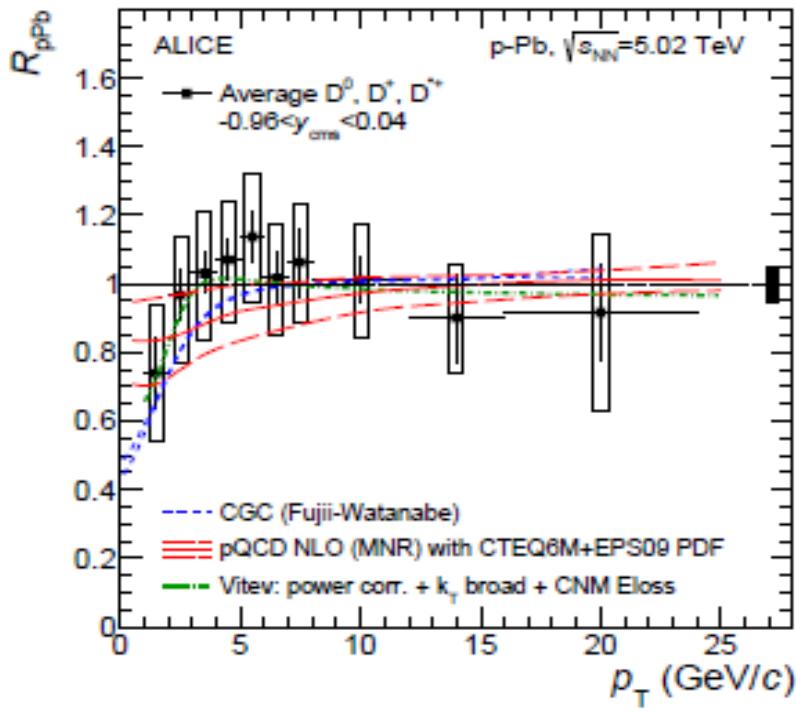
Heavy quark Transport coefficient in Magnetic field:

K. Fukushima et al. PRD, 93 (2016) 074028

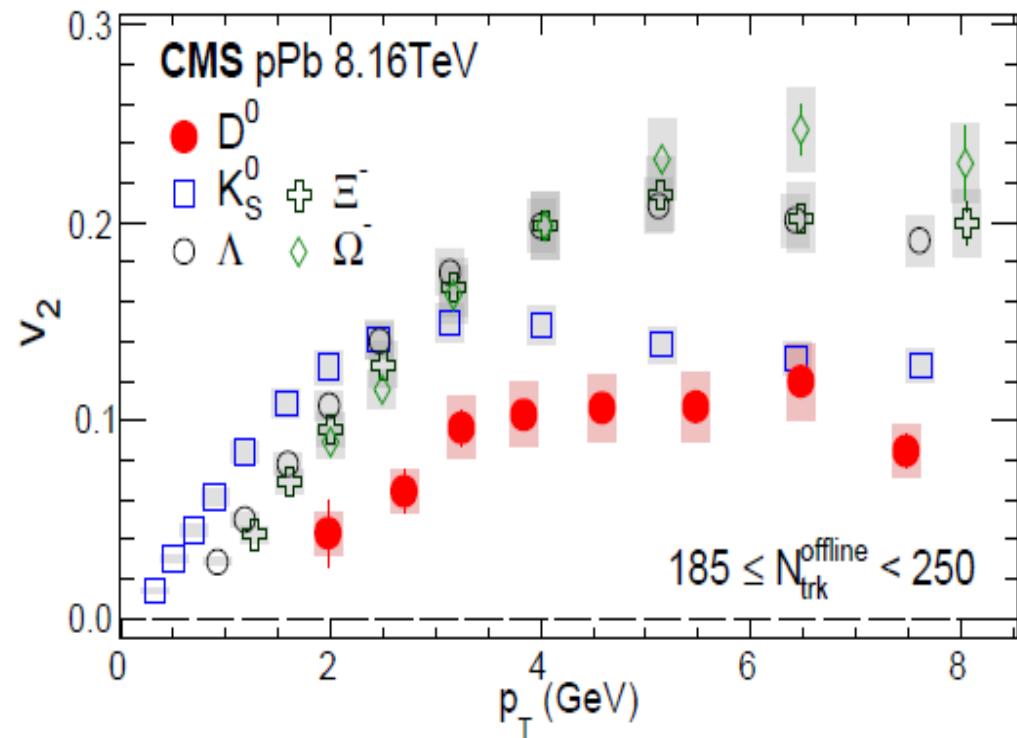
M. Kurin et al. PRD, 101 (2019) 074003

B. Singh et al. arXiv:2004.11092

Heavy quark in small system (p-nucleus)



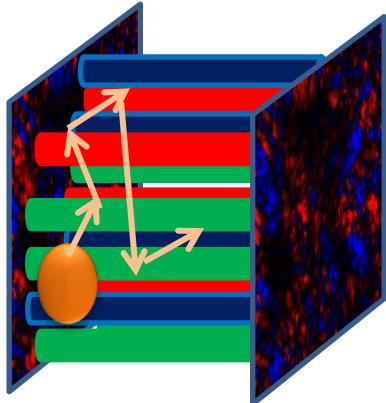
ALICE Collaboration
Phys. Rev. Lett. 113 (2014) 232301



CMS Collaboration
arXiv:1804.09767v2

What mechanism could build up v_2 without energy loss?

Heavy quarks as probes of the evolving Glasma



(Adapted from M. Ruggieri)

$$t_{\text{formation}} \approx \frac{1}{2m_c} \approx 0.06 \text{ fm/c}$$

[Talk by Mueller on Monday]

[Talk by Boguslavski on Tuesday]



HQs can probe the very early evolution of the Glasma fields

Hamilton equations of motion of c -quarks:

$$\frac{dx_i}{dt} = \frac{p_i}{E} \quad E = \sqrt{p^2 + m^2}$$

$$v \equiv \frac{p}{E} \quad \text{(Relativistic) Velocity}$$

$$E \frac{dp_i}{dt} = g Q_a F_{i\nu}^a p^\nu.$$

$$\frac{dp}{dt} = qE + q(v \times B) \quad \text{Lorentz force}$$

$$E \frac{dQ_a}{dt} = -g Q_c \varepsilon^{cba} A_b \cdot p$$

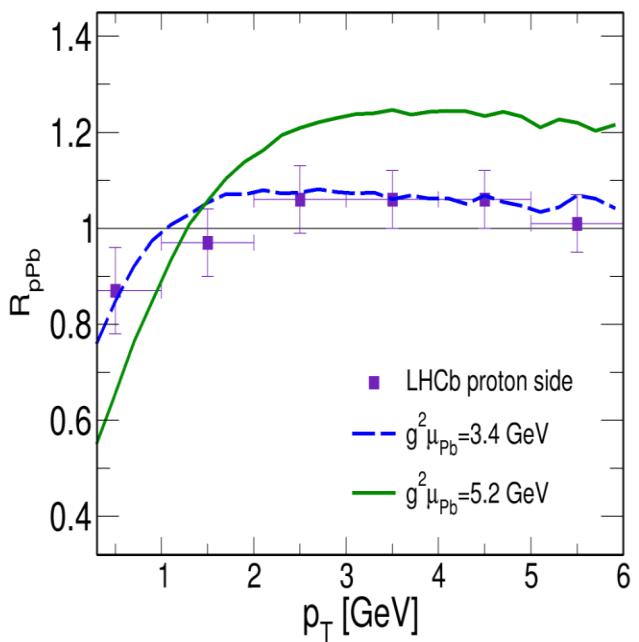
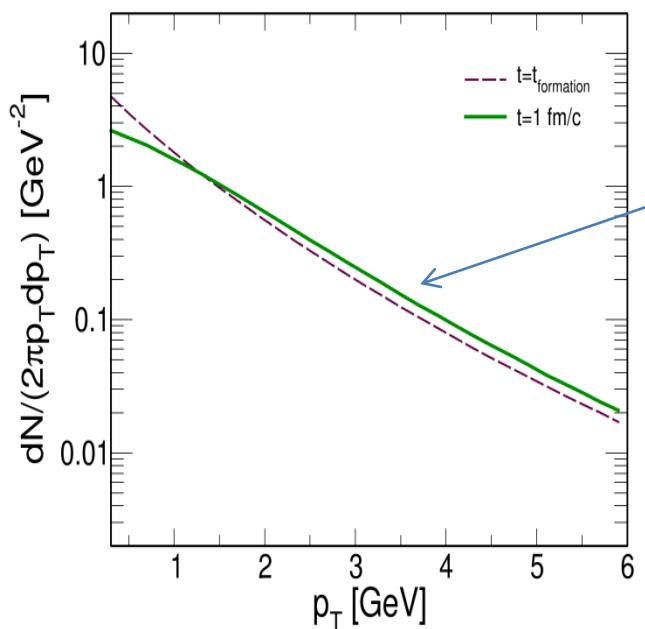
Wong (1979)

$$D_\mu J_a^\mu = 0$$

$$J_a^\mu = \bar{c} \gamma^\mu T_a c$$

Gauge-invariant conservation of the color Current carried by charm quarks + gluons

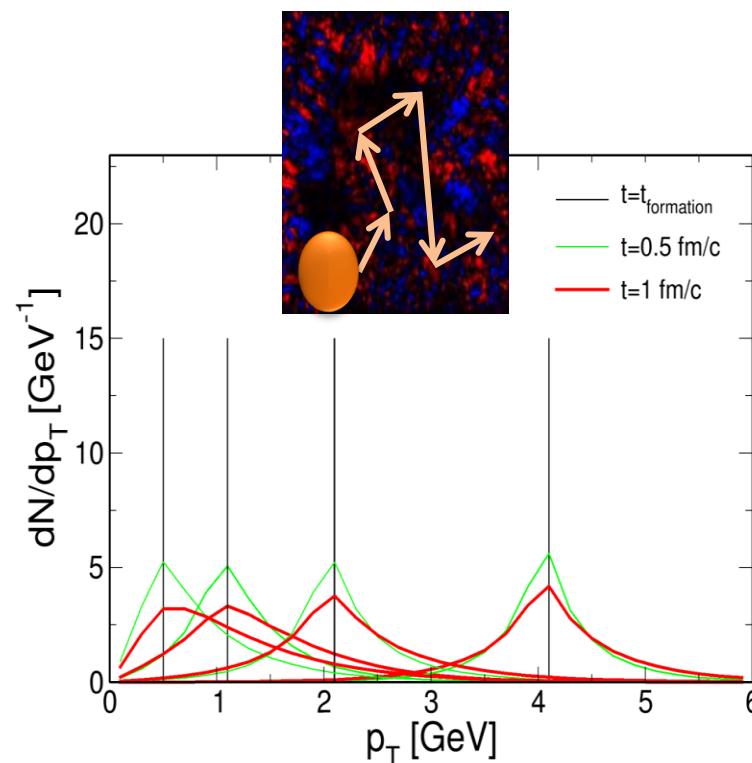
Equations of motion of heavy quarks are solved in the background given by the evolving Glasma fields



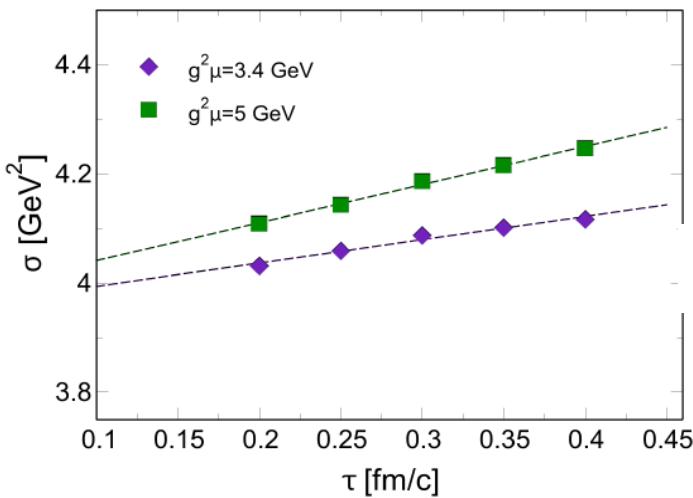
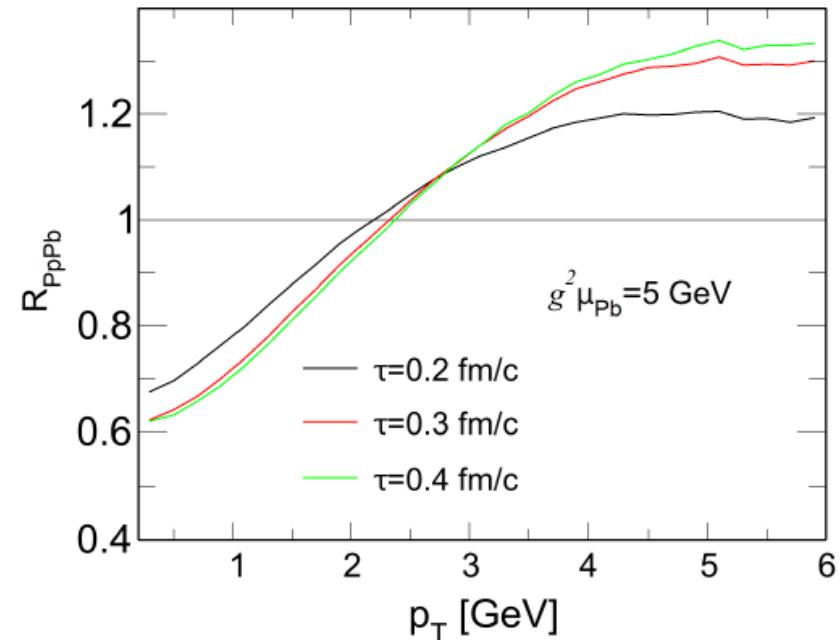
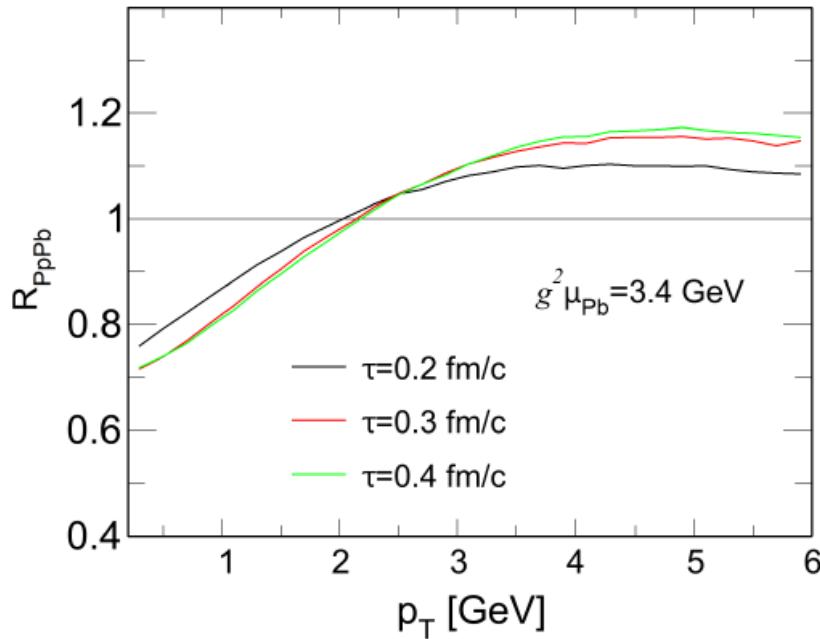
Initial distribution: from perturbative QCD
Evolution: interaction with the Glasma

$R_{p\text{Pb}} \neq 1$

*Interaction with the fields created
 by the collision*



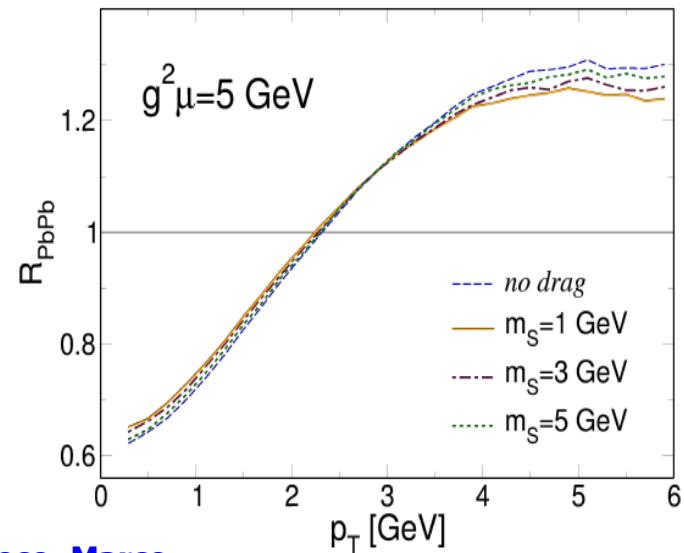
Heavy quark dynamics in Expanding Glasma



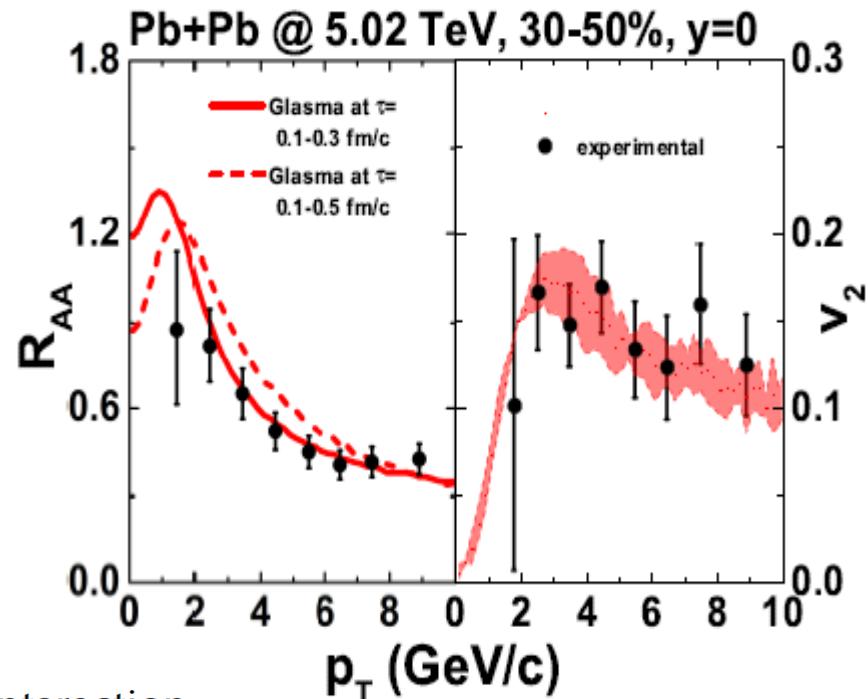
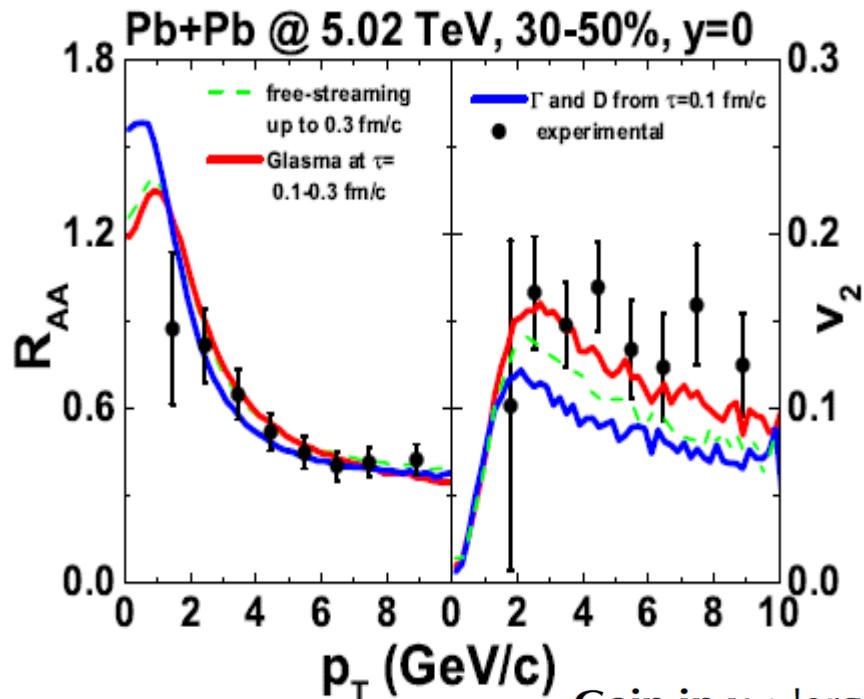
$$\sigma \equiv \langle (p_T - \langle p_T \rangle)^2 \rangle = 2D\tau + \text{constant}$$

$$E \frac{dp_i}{dt} = Q_a F_{i\nu}^a p^\nu - E \Gamma p_i$$

$$D = \Gamma E T$$



Impact of Glasma on a heavy quark observables at LHC (Heavy quark dynamics in Glasma plus Plasma)



Gain in v_2 : larger interaction
in QGP stage to have same $R_{AA}(p_T)$

This indicates an initial pre-thermal stage is unlikely to be described in terms of a standard drag and diffusion dynamics, because even if one tune such coefficients to reproduce the same $R_{AA}(p_T)$ this would imply a significantly smaller v_2 .

Few recent works on heavy quark diffusion in pre-equilibrium phase

S. Mrowczynski, EPJA 54 (2018) 3, 4

M. Carrington et al. NPA 1001 (2020) 121914

K. Boguslavski et. al. JHEP 09 (2020) 077

Talk by K. Boguslavski on Tuesday

A. IPP et al. 2009.14206 [hep-ph]

[Talk by D. Mueller on Monday]

Within Kinetic Theory:

S. K. Das et al. JPG, 44 (2017) 095112

T. Song et al. PRC, 101 (2020), 044901

Impact of pre-equilibrium phase is significant

Conclusions and Perspectives:

- ❖ **Open Heavy Flavor Physics at RHIC and LHC**

R_{AA} and $v_2 \rightarrow D_s(T) \rightarrow$ IQCD

- ❖ **More precision data and New Observables**

$V_n(HQ) - V_n(LQ)$, Λ_c , $dN/d\Phi$, System size scan and bottom quark observables, will allow significant advantage to understand the hot QCD matter

- ❖ **Heavy quark $V_1 \rightarrow$ EM field and Angular momentum**

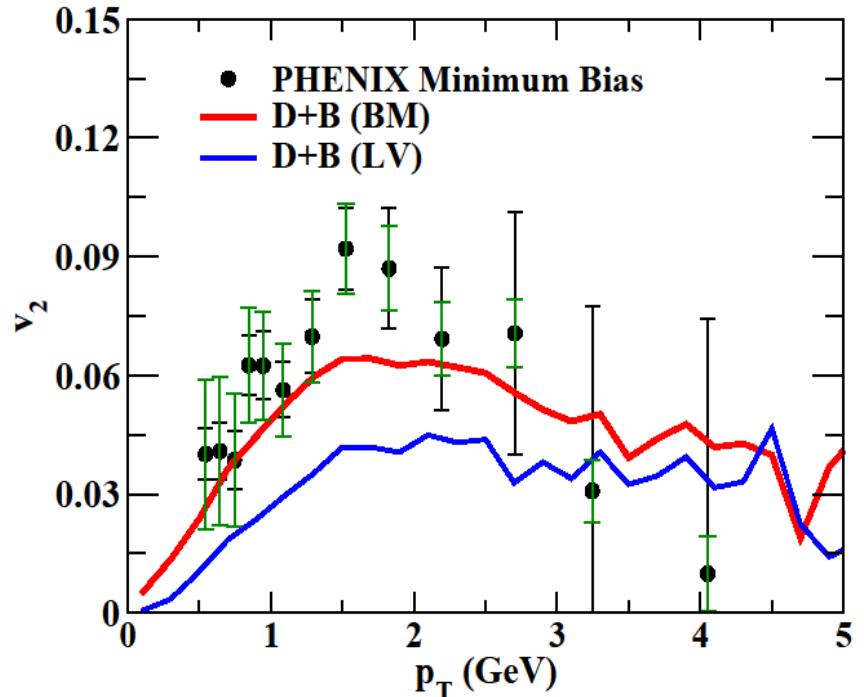
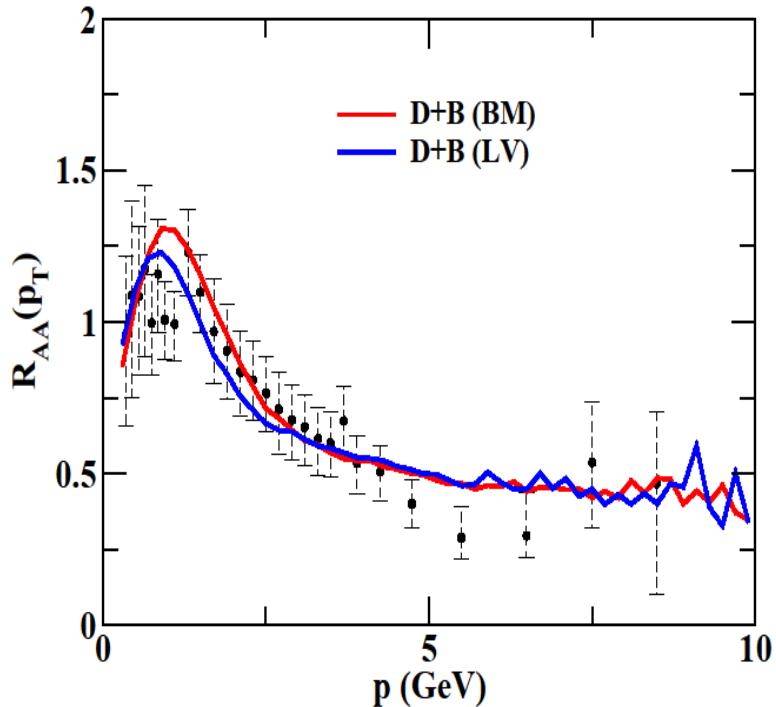
- ❖ **Heavy quark as a probe of the pre-equilibrium phase \rightarrow Glasma**

Thank You



R_{AA} and v₂ at RHIC

(With near isotropic cross-section)

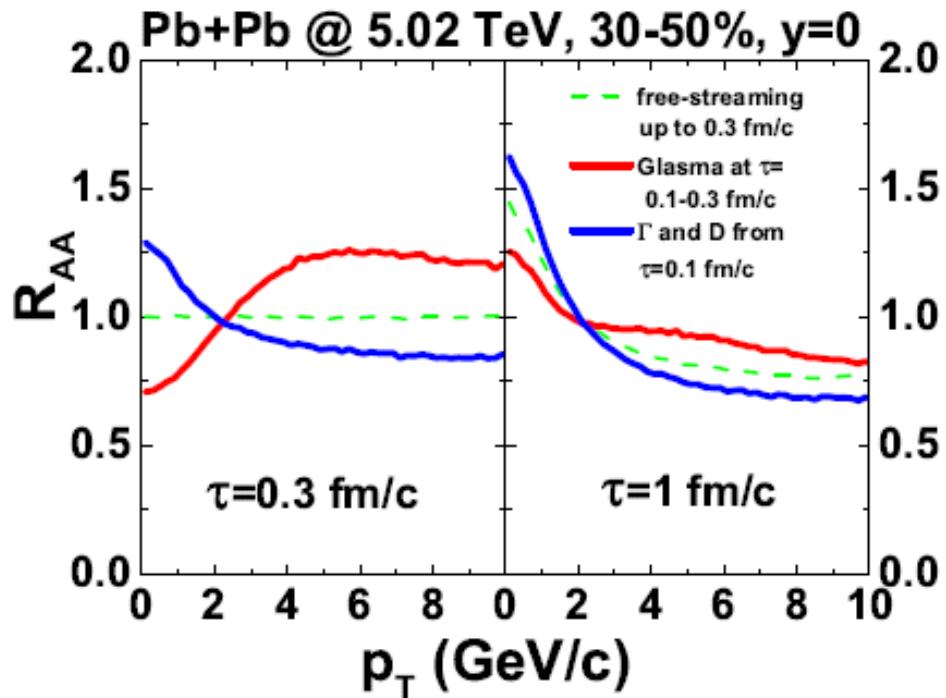
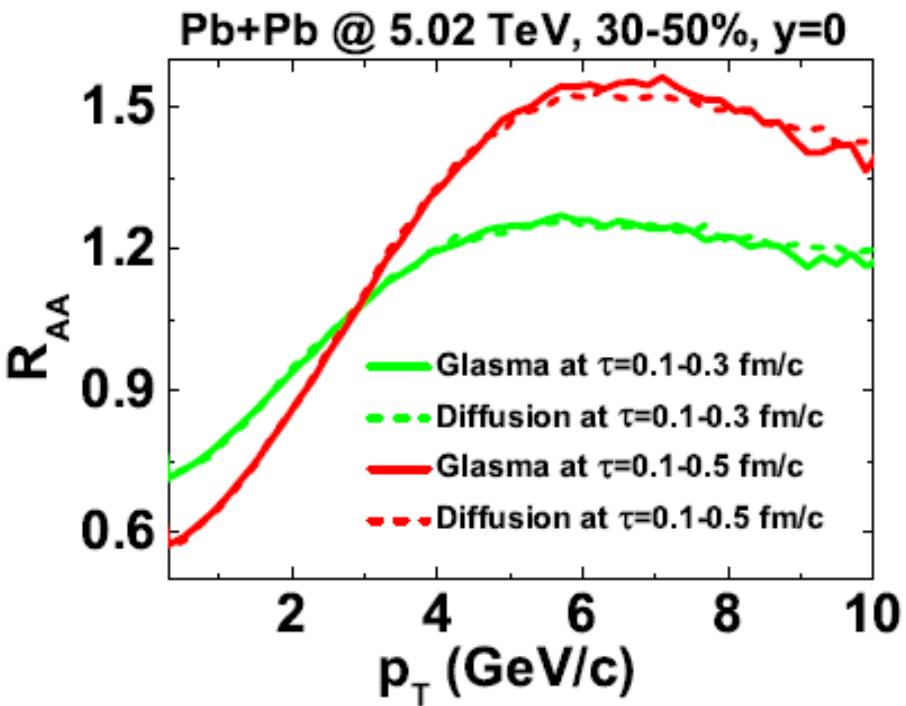


Das, Scardina, Plumari and Greco
PRC,90,044901(2014)

At fixed R_{AA} Boltzmann approach generate larger v₂ .
(depending on m_D and M/T)

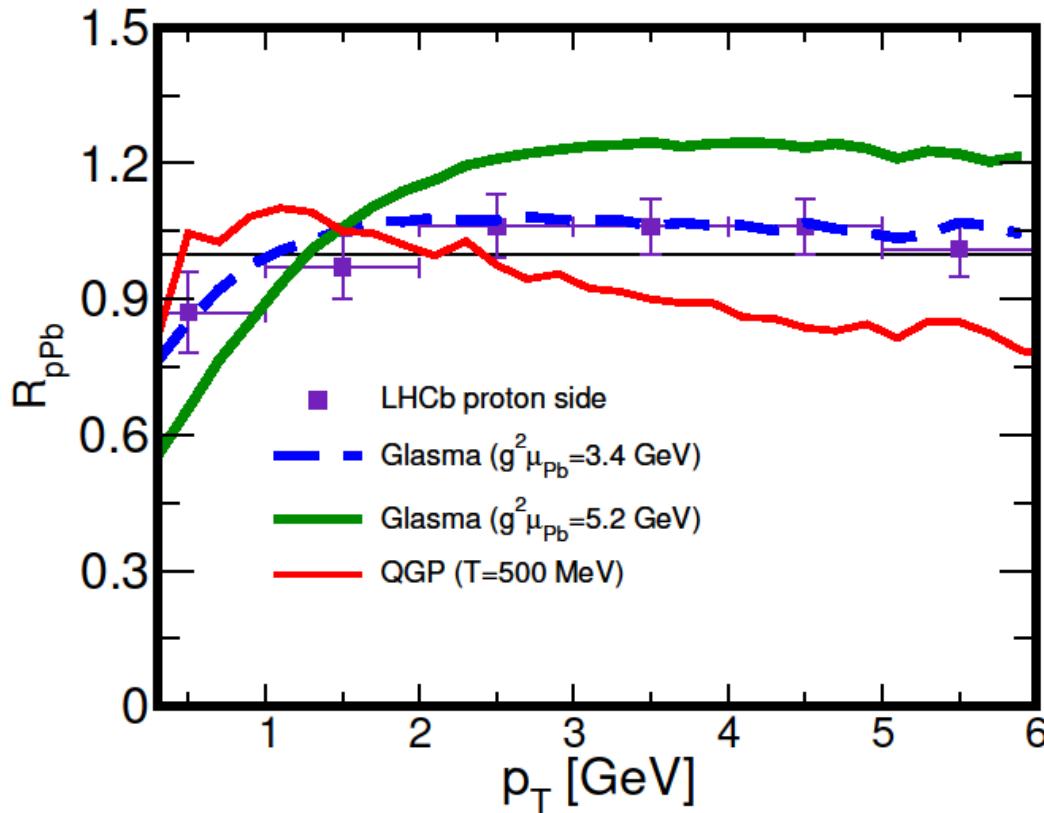
With isotropic cross section one can describe both R_{AA} and V₂
simultaneously within the Boltzmann approach

Impact of Glasma on a heavy quark observables at LHC (Glasma vs Plasma)



Glasma induce a diffusion of charm quarks in momentum space resulting in a tilt of their spectrum without a significant drag.

Heavy quark suppression in pPb: Glasma vs Plasma



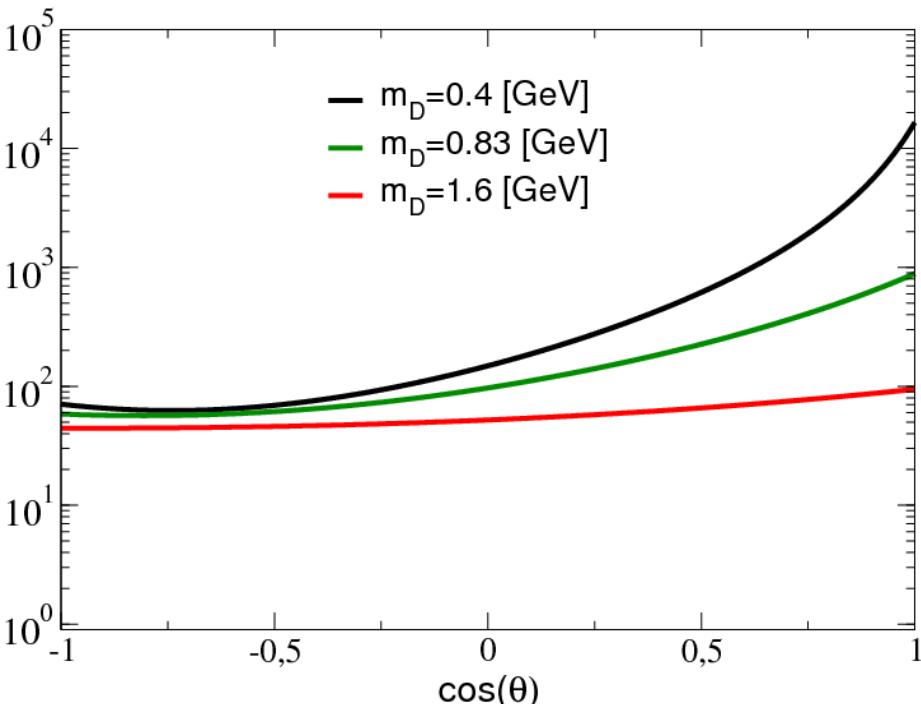
In Plasma: high momentum particle loose energy shifted to low momentum domain.

In Glasma: low momentum particle get accelerated and shifted to high momentum domain

Boltzmann vs Langevin (Charm)

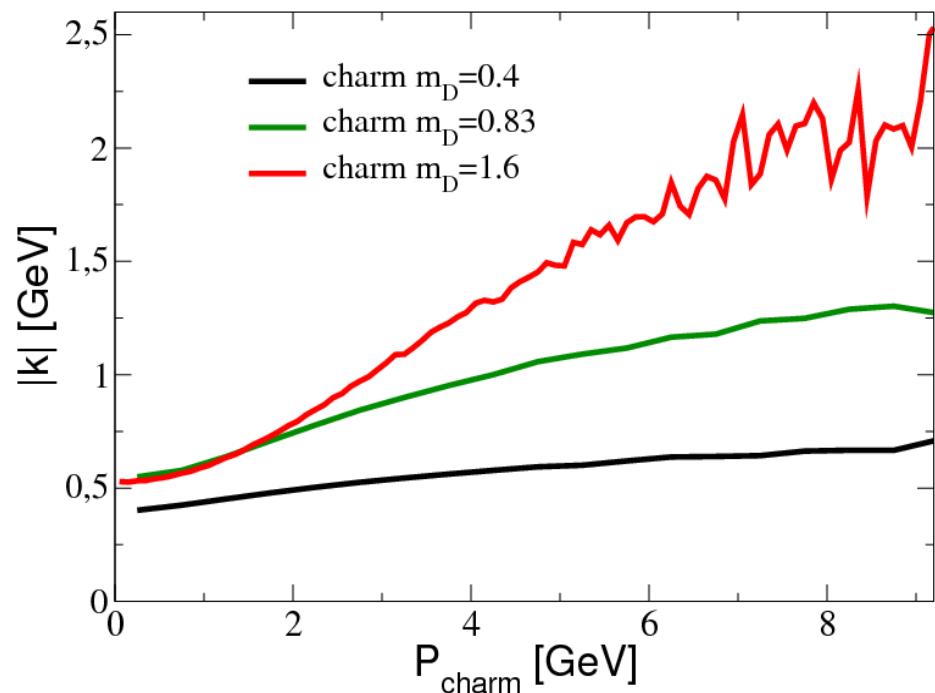
T=400 MeV

Angular dependence of σ



Decreasing m_D makes the σ more anisotropic

Momentum transfer vs P

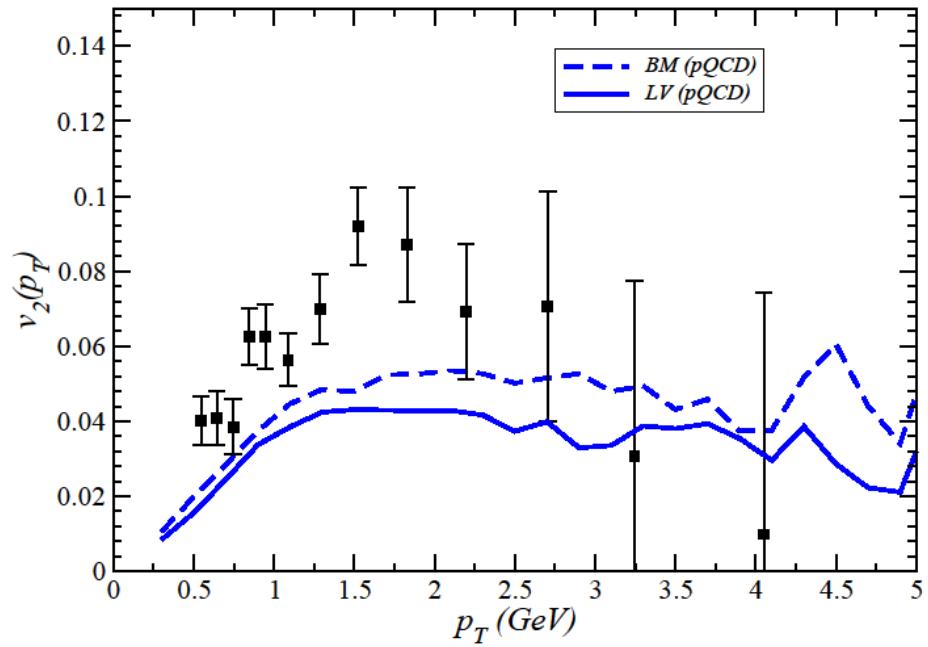
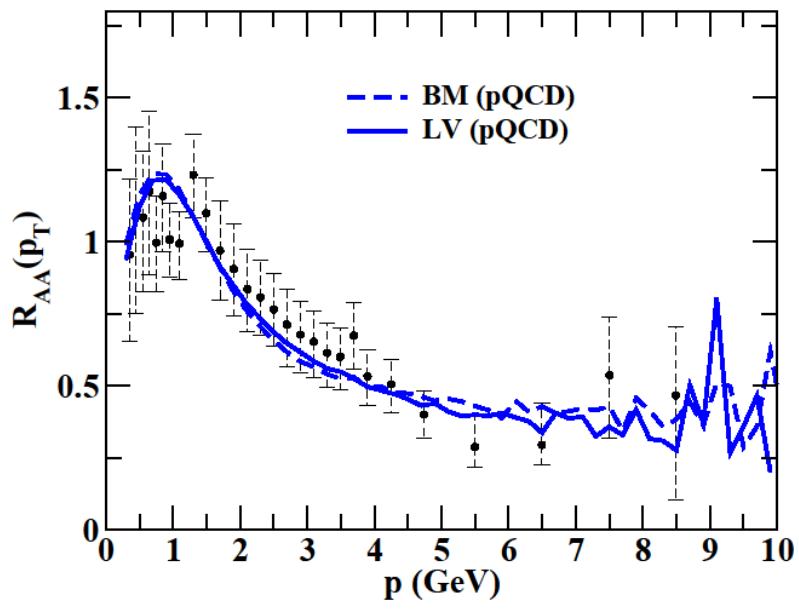


Smaller average momentum transfer

Hees, Greco, Rapp, PRC, 73, 034913 (2006)

Das, Scardina, Plumari and Greco
PRC, 90, 044901 (2014)

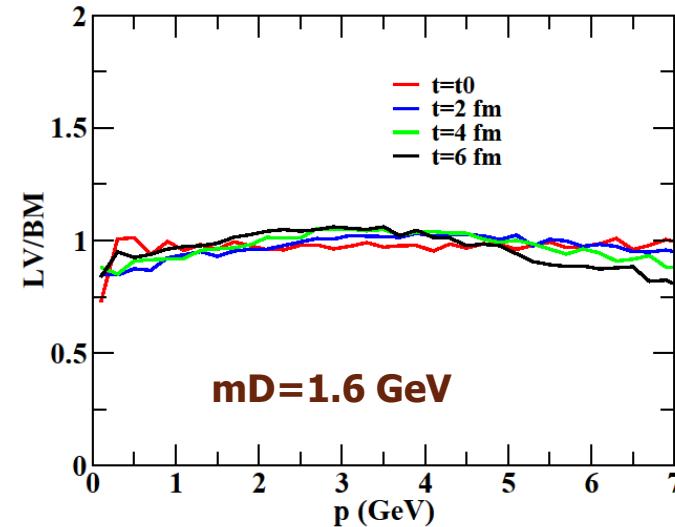
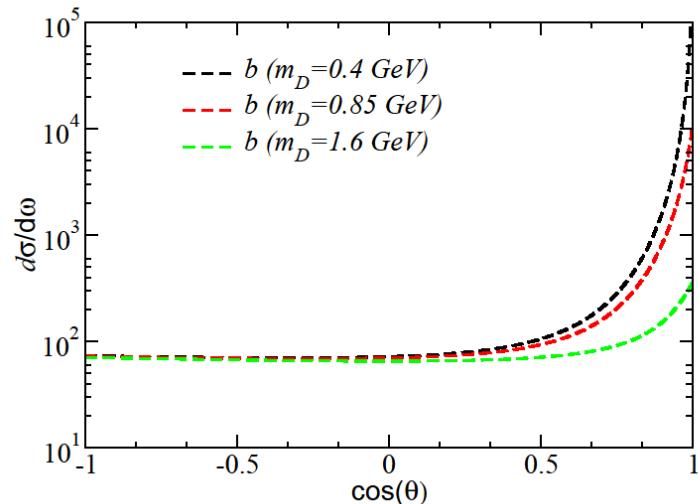
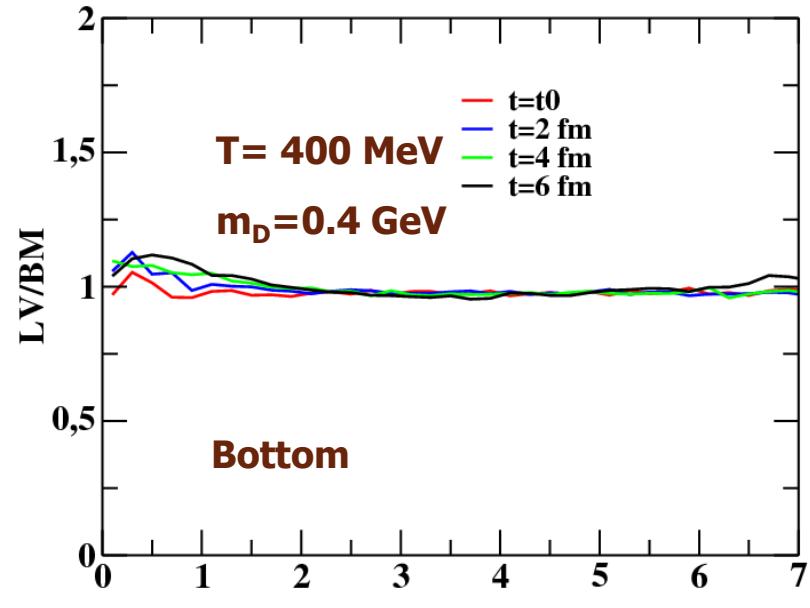
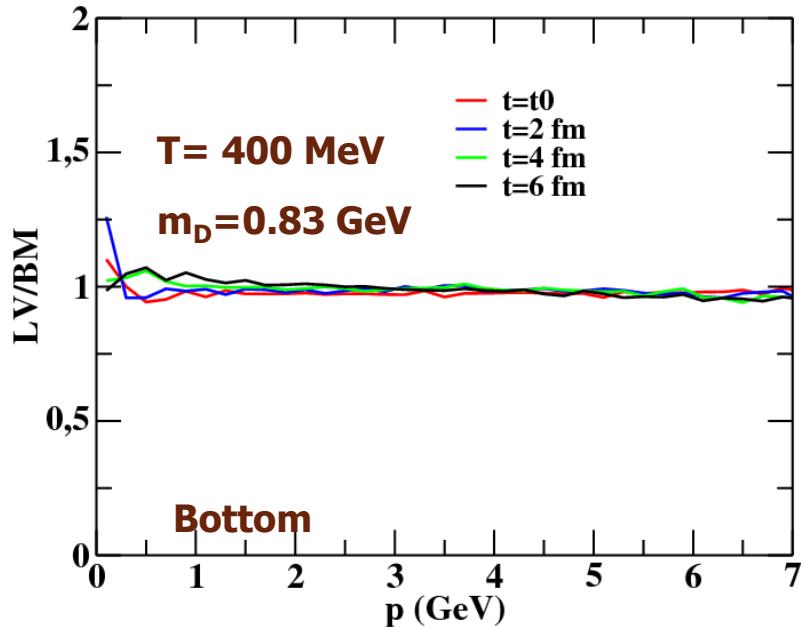
R_{AA} and v2 at RHIC at mD=gT



Das, Scardina, Plumari and Greco
PRC,90,044901(2014)

**At fixed RAA Boltzmann approach generate larger v2 .
(depending on mD and M/T)**

Bottom: Boltzmann = Langevin



But Larger M_b/T (≈ 10) the better Langevin approximation works

Boltzmann vs Langevin (Charm)

