Rydberg atoms in Bose-Einstein condensed environments

from bubble chambers to controllable open quantum systems

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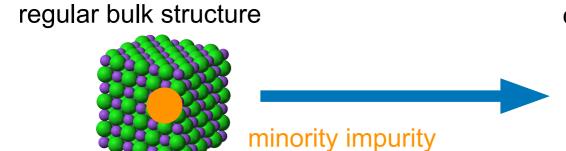










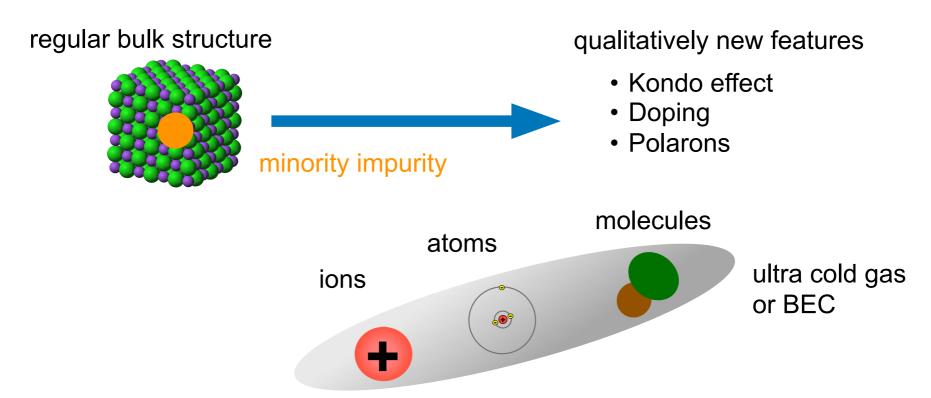


qualitatively new features

- Kondo effect
- Doping
- Polarons

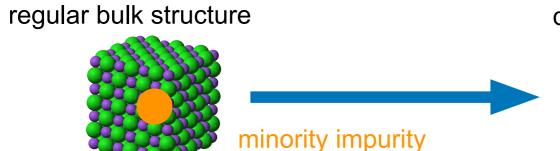






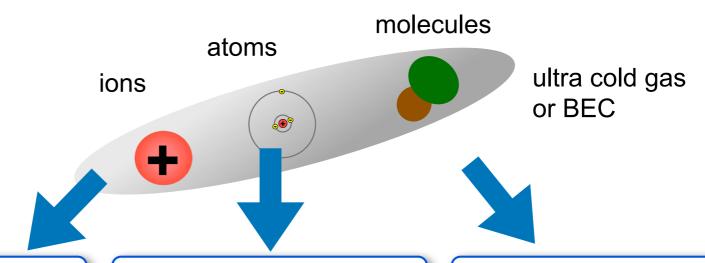






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- Kondo effect
- Doping
- Polarons



Cold ion-atom scattering

e.g. S. Dutta and S. Rangwala PRA(R) **97** (2018) 041401

Polaron formation

e.g. C. Kohstall et al. Nature **485** (2012) 615

Angular momentum dynamics

e.g. Schmidt and Lemeshko PRX 6 (2016) 011012







minority impurity

qualitatively new features

- Kondo effect
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Rydberg atoms ions ultra cold gas BEC

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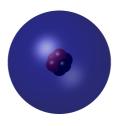




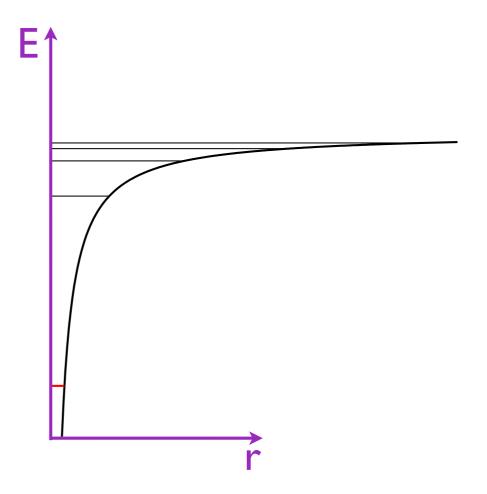
What are Rydberg atoms?

Electron quantum states (orbitals):

 $|nlm\rangle$



n=1

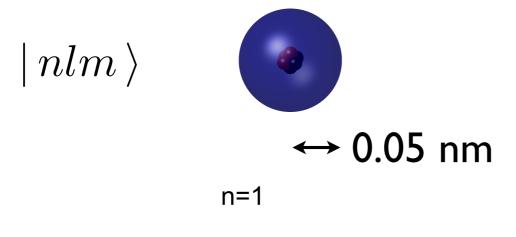




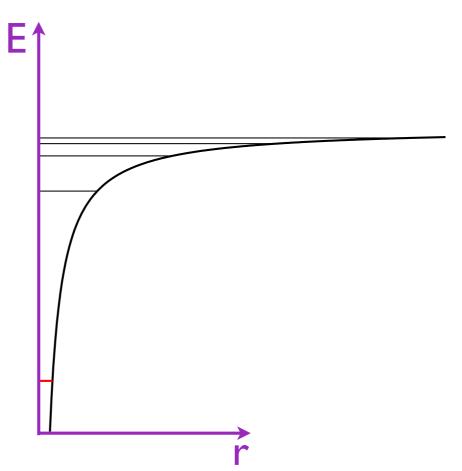


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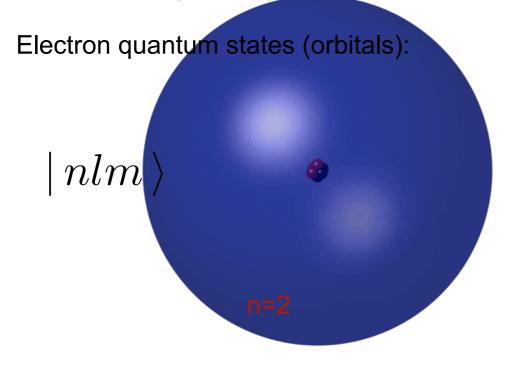
Orbital radius: $r_{rad} pprox rac{3}{2} a_0 n^2$



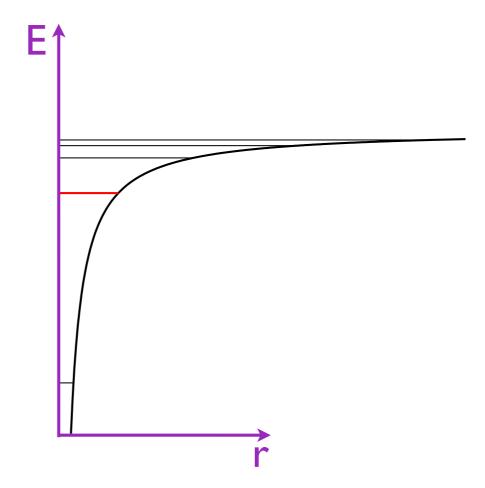




What are Rydberg atoms?



Orbital radius: $au_{
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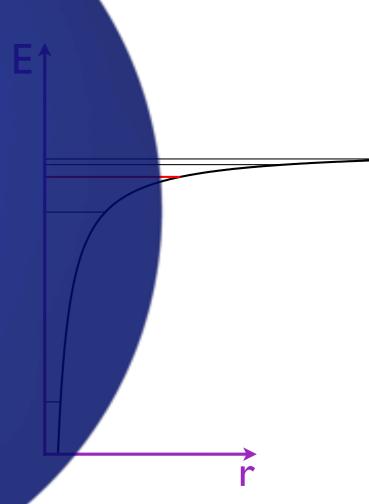
What are Rydberg atoms?

Electron quantum states (orbitals):

 $|nlm\rangle$

1 = 3

Orbital radius: $au_{
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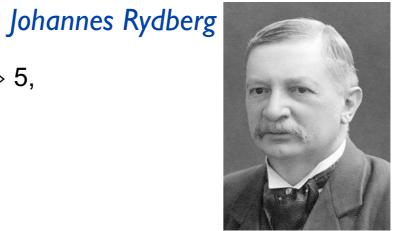






What are Rydberg atoms?

Very high principal quantum number $n \gg 5$, these are HUGE atoms...





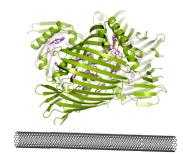


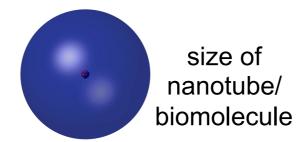
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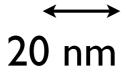
Johannes Rydberg

Very high principal quantum number $n \gg 5$, these are HUGE atoms...









n=20



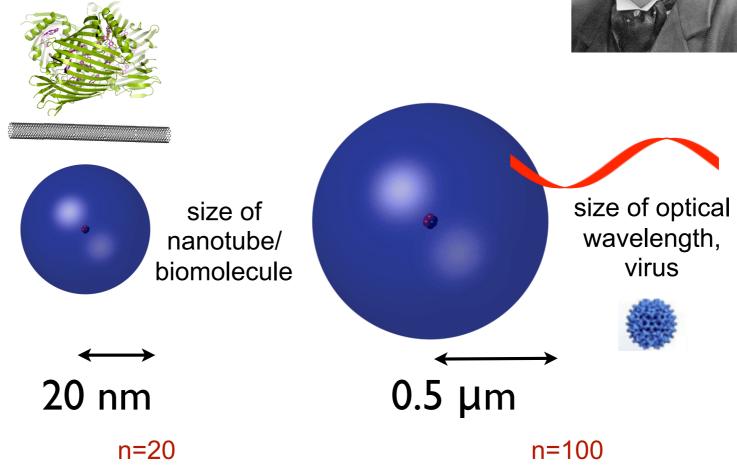


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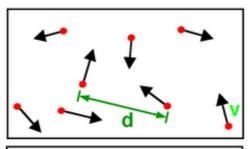












High Temperature T:

thermal velocity v density d⁻³

"Billiard balls"

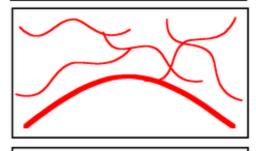


Low Temperature T:

De Broglie wavelength

 $\lambda_{dB}=h/mv \propto T^{-1/2}$

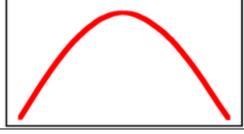
"Wave packets"



T=T_{Crit}: Bose-Einstein Condensation

 $\lambda_{dB} \approx d$

"Matter wave overlap"



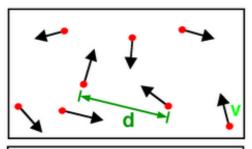
T=0: Pure Bose condensate

"Giant matter wave"

from: Durfee and Ketterle Opt. Express 2 (1998) 299.







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thermal velocity v density d⁻³

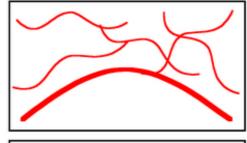
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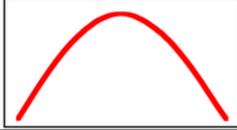
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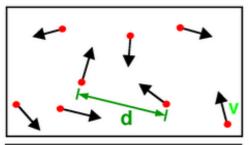
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$$\hat{\Psi}(\mathbf{R}) \to \langle \hat{\Psi}(\mathbf{R}) \rangle = \phi(\mathbf{R})$$







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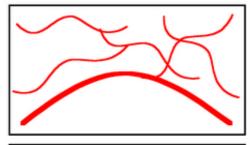
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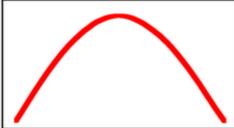
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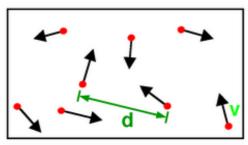
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Gross Pitaevskii equation

$$i\hbar \frac{\partial}{\partial t}\phi(\mathbf{R}) = \left(-\frac{\hbar^2}{2m}\nabla^2 + W(\mathbf{R}) + U_0 |\phi(\mathbf{R})|^2\right)\phi(\mathbf{R})$$







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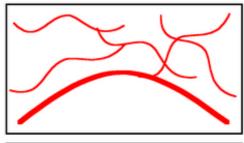


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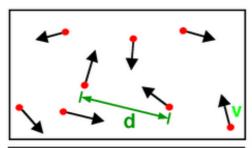
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BEC density



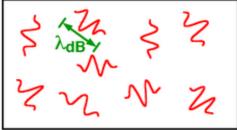




High Temperature T:

thermal velocity v density d⁻³

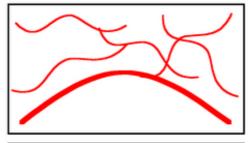
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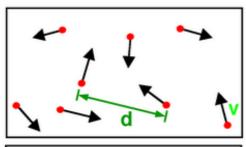
BEC density



s-wave scattering







High Temperature T:

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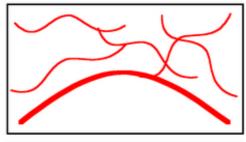


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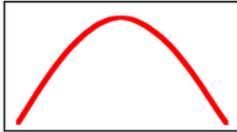
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BEC density



s-wave scattering

3D wavefunction (not 3N D)

Phase coherence

$$\phi(\mathbf{R}) \in \mathbb{C}$$

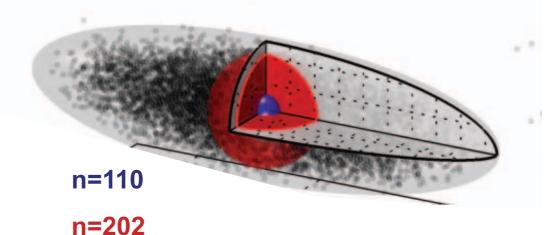


Rydberg atoms in BEC



Single large Rydberg atom in **BEC**

- Naturally excite Rydberg states in an ultracold gas or even BEC
- Extreme atoms in an extreme environment



J. Balewski *et al.*, Nature **502** (2013) 664.

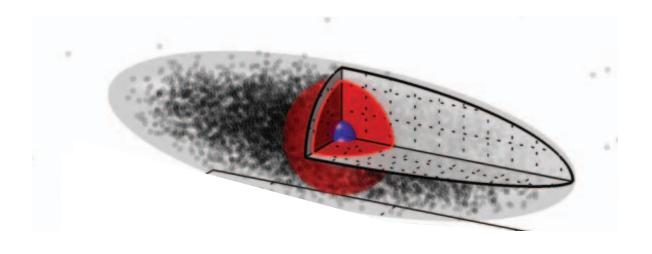
also:

Celistrino-Teixeira et al., Phys. Rev. Lett. **I I 5** (2015) 013001.

F. Carmargo et al., Phys. Rev. Lett. **120** (2018) 083401.





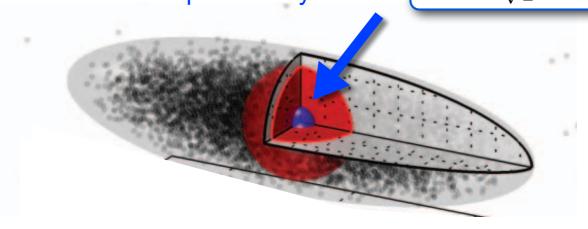






Well controlled simple quantum system

$$|\Psi\rangle = \frac{1}{\sqrt{2}} (|n = 55, s\rangle + |n = 55, p\rangle)$$

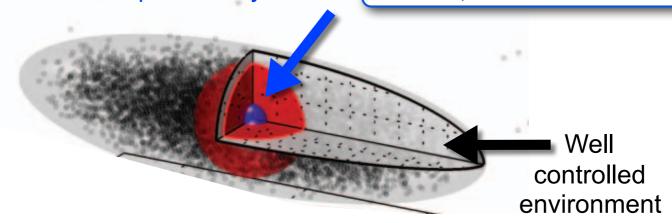






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Bose Einstein condensate: mean field and phonons

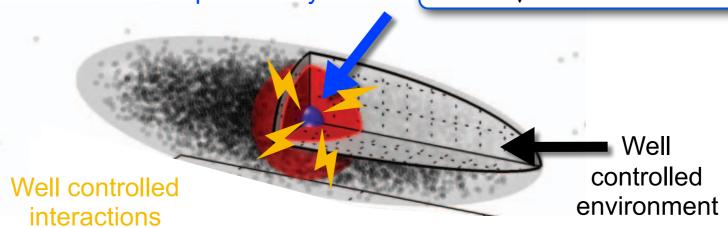
$$\hat{\Psi}(x) = \phi(x) + \sum_{q} (u_q(x)\hat{\alpha}_q - v_q^*(x)\hat{\alpha}_q^{\dagger})$$

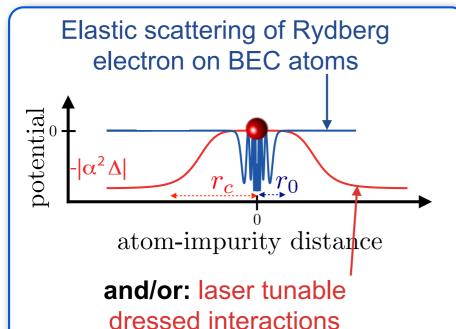




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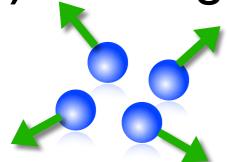
R. Mukherjee, C. Ates, Weibin Li and S. Wüster, PRL 115 040401 (2015)



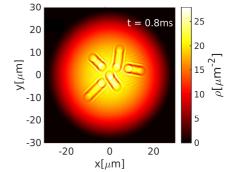
Outline



(I) Tracking of mobile Rydberg atoms in a BEC

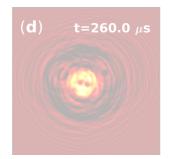


S. Tiwari and S. Wüster, PRA **99** 043616 (2019)



(II) BEC response to Rydberg insertion



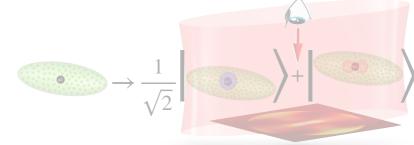


S. Tiwari et al. in preparation (2021).

(III) Decoherence of Rydberg qubits in a BEC

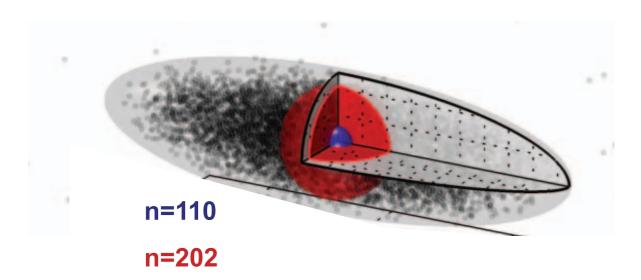


S. Rammohan *et al.* arXiv:2011.11022 (2020). arXiv:2006.15376 (2020).





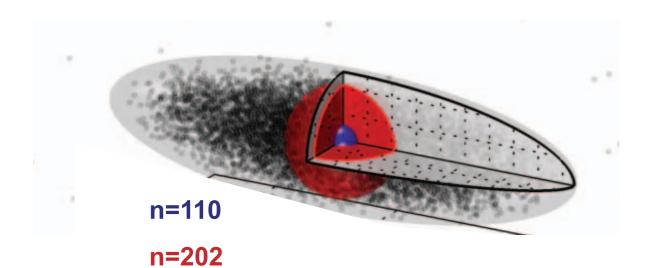




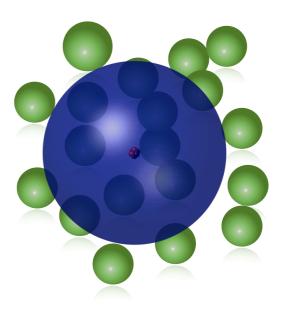
J. Balewski *et al.*, Nature **502** (2013) 664.





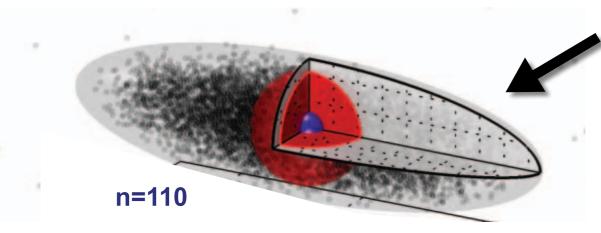


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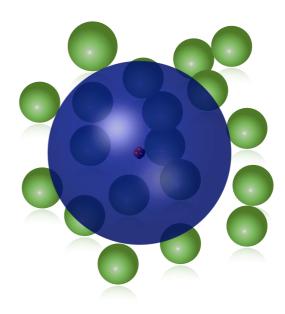




 $T \sim nK$

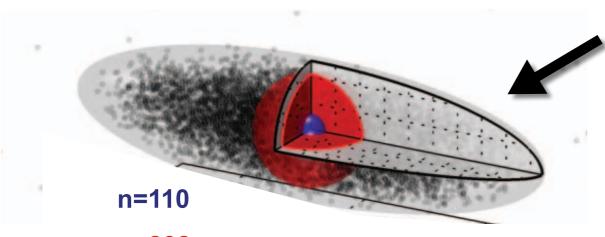
n=202

J. Balewski *et al.*, Nature **502** (2013) 664.









 $T \sim nK$

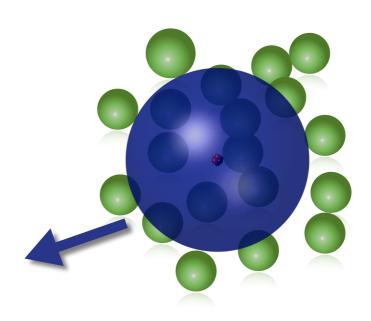
n=202

J. Balewski *et al.*, Nature **502** (2013) 664.

Intact Rydberg atom, with moderately reduced lifetime (1/2...1/10)

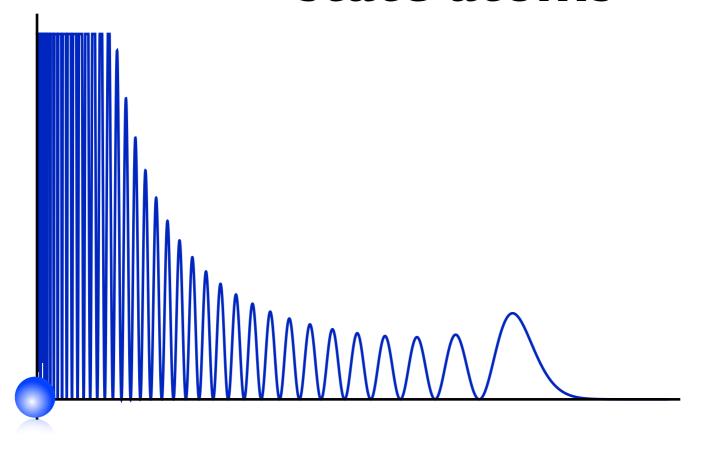
M. Schlagmüller et al., PRX 6 (2016) 031020.

S. Kanungo et al., PRA **102** (2020) 063317.





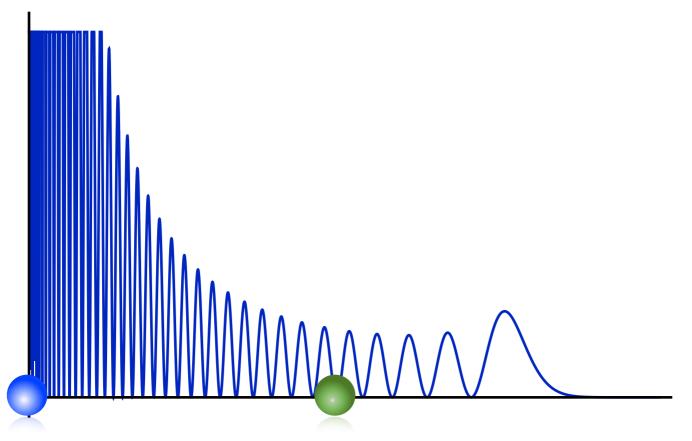








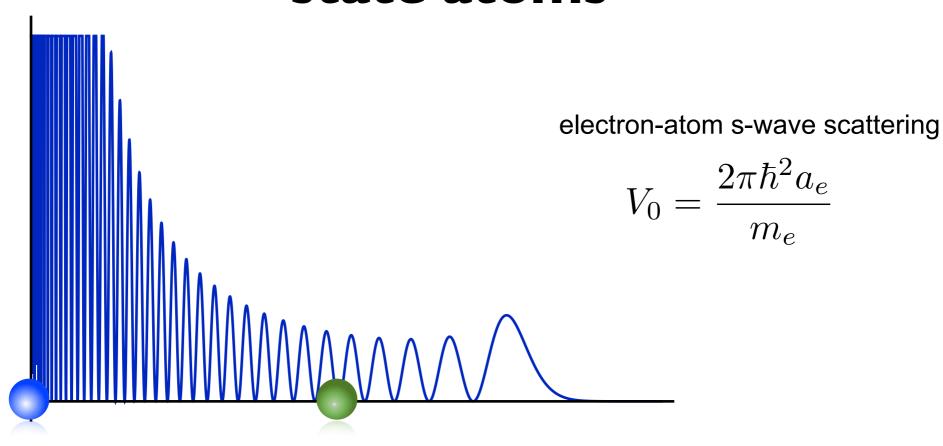




Ground-state atom within Rydberg orbit



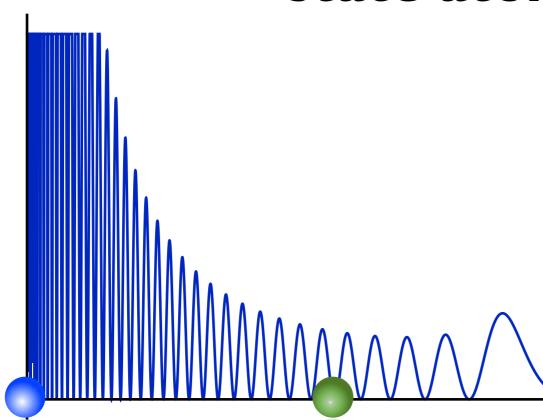




Ground-state atom within Rydberg orbit







electron-atom s-wave scattering

$$V_0 = \frac{2\pi\hbar^2 a_e}{m_e}$$

Fermi pseudo potential

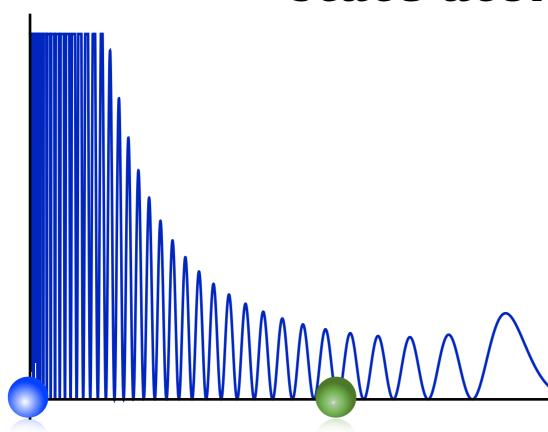
$$V(\mathbf{r}) = V_0 \delta(\mathbf{x}_e - \mathbf{r})$$

Ground-state atom within Rydberg orbit

see e.g. C.H. Greene et al. PRL **85** (2000) 2458







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Effective Rydberg-GS potential

$$V(\mathbf{r}) = V_0 |\Psi_e(\mathbf{r})|^2$$

$$a_e < 0$$





Ε

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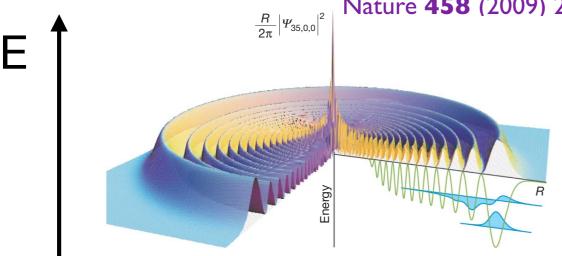
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Figure from: V. Bendkowsky et al. Nature **458** (2009) 2005.



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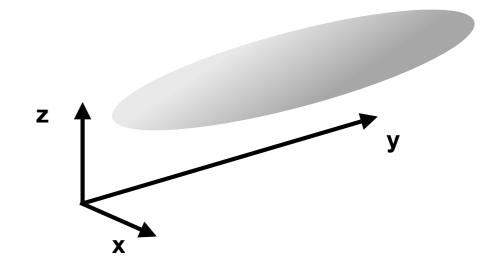
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Gross Pitaevskii equation

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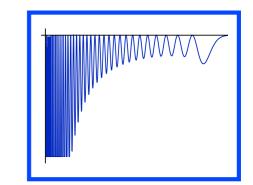


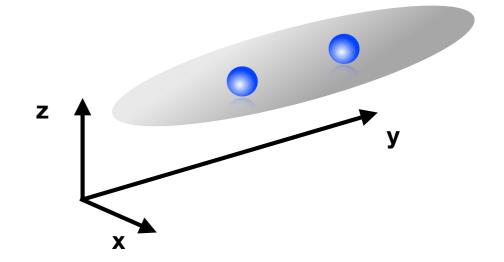




Gross Pitaevskii equation with impurities

$$i\hbar \frac{\partial}{\partial t} \phi(\mathbf{R}) = \left(-\frac{\hbar^2}{2m} \nabla^2 + W(\mathbf{R}) + g |\phi(\mathbf{R})|^2 + \sum_{n=0}^{N_{imp}} V_0 |\Psi(\mathbf{R} - \mathbf{x}_n)|^2 \right) \phi(\mathbf{R})$$



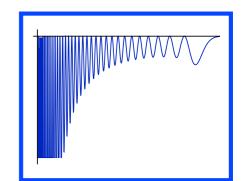






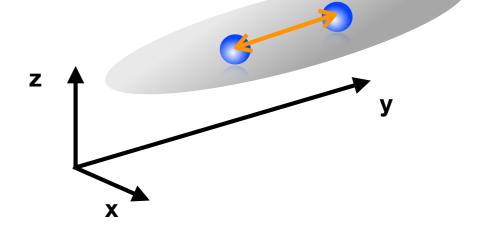
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Newton's equations with vdW interactions

$$m\frac{\partial^2}{\partial t^2}\mathbf{x}_n = -\nabla_{\mathbf{x_n}} \left[\sum_{n>m} \frac{C_6(\nu)}{|\mathbf{x}_n - \mathbf{x}_m|^6} \right]$$

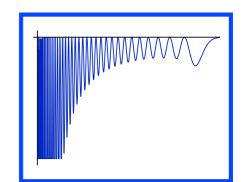






Gross Pitaevskii equation with impurities

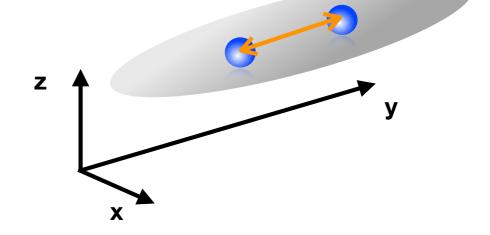
$$i\hbar \frac{\partial}{\partial t} \phi(\mathbf{R}) = \left(-\frac{\hbar^2}{2m} \nabla^2 + W(\mathbf{R}) + g |\phi(\mathbf{R})|^2 + \sum_{n=0}^{N_{imp}} V_0 |\Psi(\mathbf{R} - \mathbf{x}_n)|^2 \right) \phi(\mathbf{R})$$



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Initially: Phase imprinting



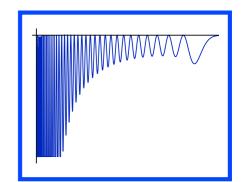




Gross Pitaevskii equation with impurities

$$i\hbar \frac{\partial}{\partial t} \phi(\mathbf{R}) =$$

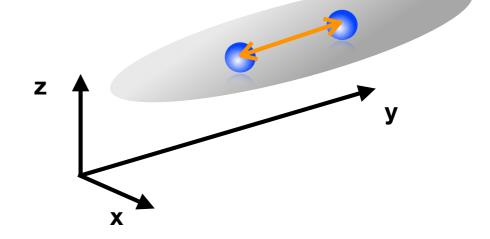
$$+\sum_{n}^{N_{imp}}V_{0}|\Psi(\mathbf{R}-\mathbf{x}_{n})|^{2}\bigg)\phi(\mathbf{R})$$



Newton's equations with vdW interactions

$$m\frac{\partial^2}{\partial t^2}\mathbf{x}_n = -\nabla_{\mathbf{x}_n} \left[\sum_{n>m} \frac{C_6(\nu)}{|\mathbf{x}_n - \mathbf{x}_m|^6} \right]$$

Initially: Phase imprinting



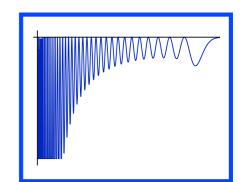




Gross Pitaevskii equation with impurities

$$i\hbar\frac{\partial}{\partial t}\phi(\mathbf{R}) =$$

$$+ \sum_{n}^{N_{imp}} V_0 |\Psi(\mathbf{R} - \mathbf{x}_n)|^2 \bigg) \phi(\mathbf{R})$$

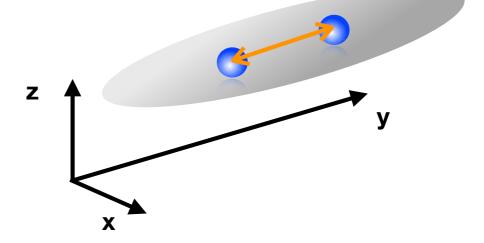


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Initially: Phase imprinting

$$\phi(\mathbf{R},t) = \phi(\mathbf{R},0) e^{-i\sum_{n}^{N_{imp}} V_0 |\Psi(\mathbf{R}-\mathbf{x}_n)|^2 t/\hbar}$$



see e.g.

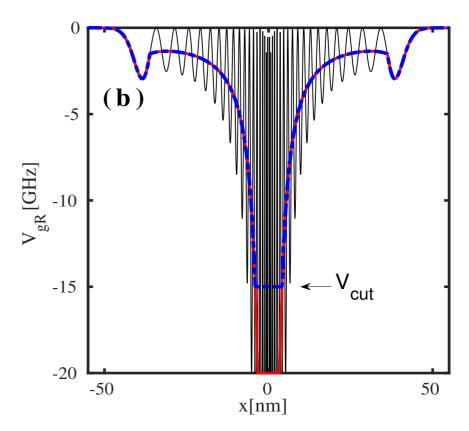
Dobrek et al. PRA **60** (1999) R3381, R. Mukherjee et al. PRL **115** (2015) 040401.



Phase imprinting tracks



$$i\hbar \frac{\partial}{\partial t} \phi(\mathbf{R}) = \left(-\frac{\hbar^2}{2m} \nabla^2 + W(\mathbf{R}) + g|\phi(\mathbf{R})|^2 + \sum_{m=1}^{N_{\text{imp}}} V_0 |\Psi(|\mathbf{R} - \mathbf{x}_m|)|^2 \right) \phi(\mathbf{R}).$$

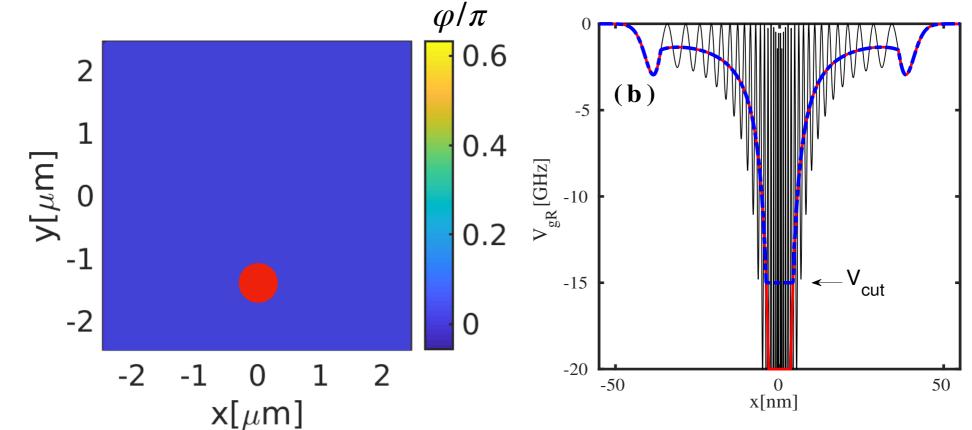




Phase imprinting tracks



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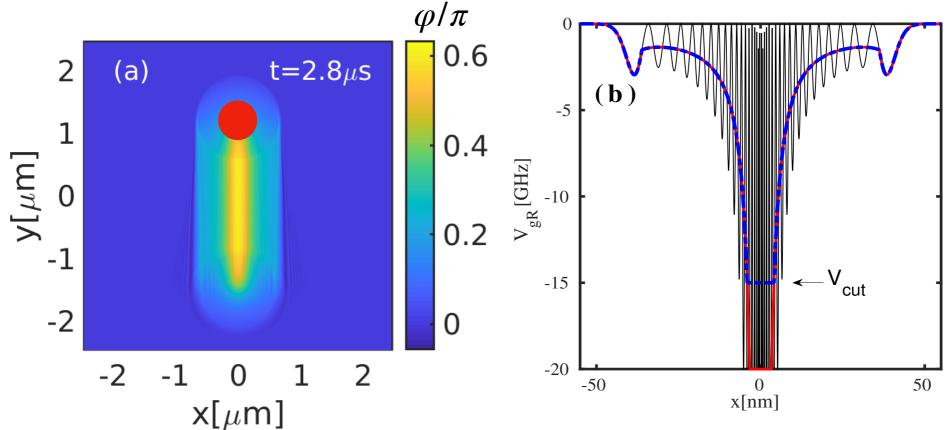




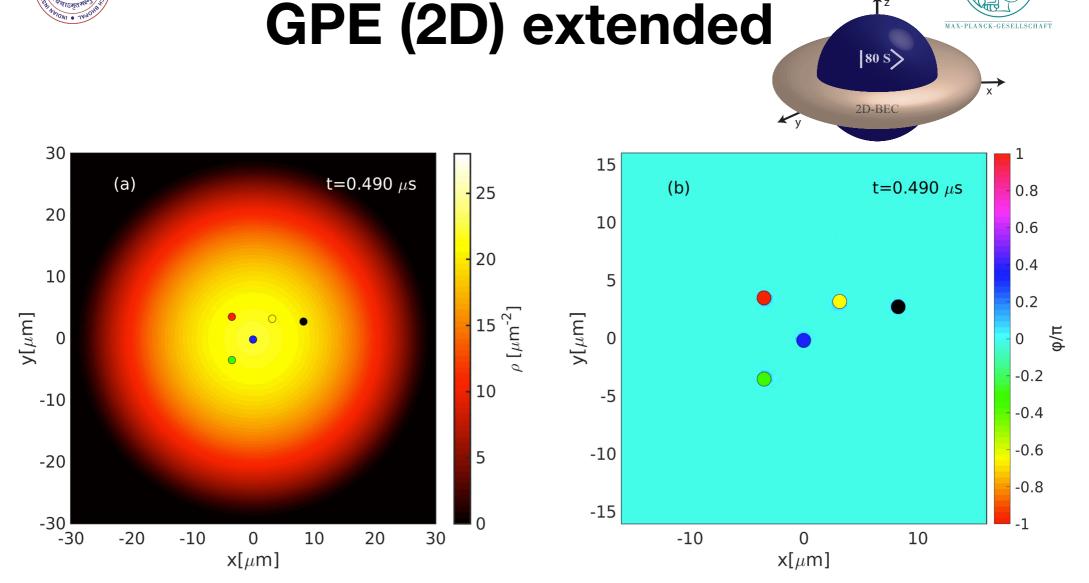
Phase imprinting tracks



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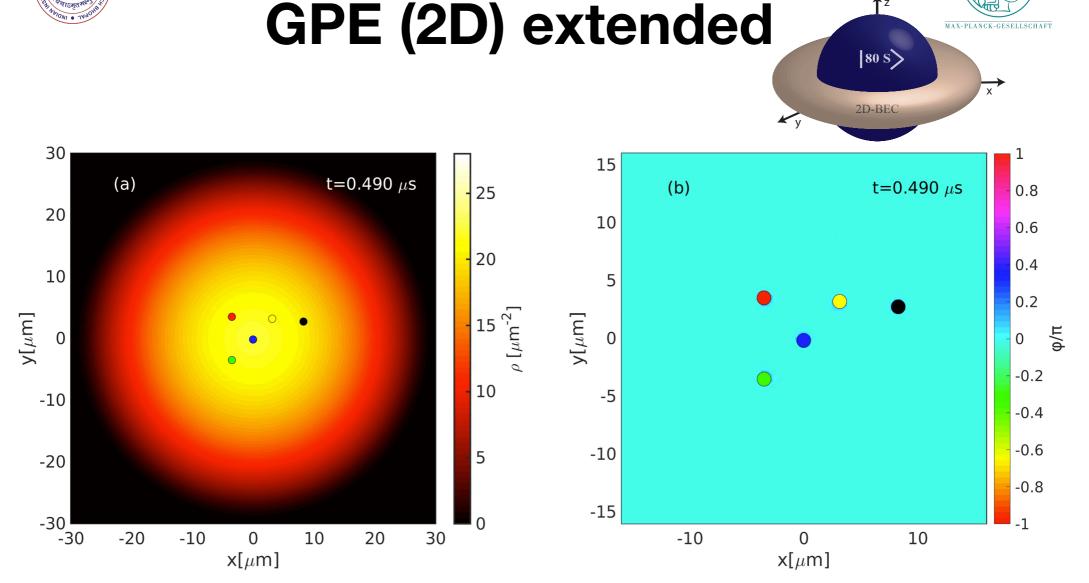






S. Tiwari and S. Wüster, PRA **99** 043616 (2019)



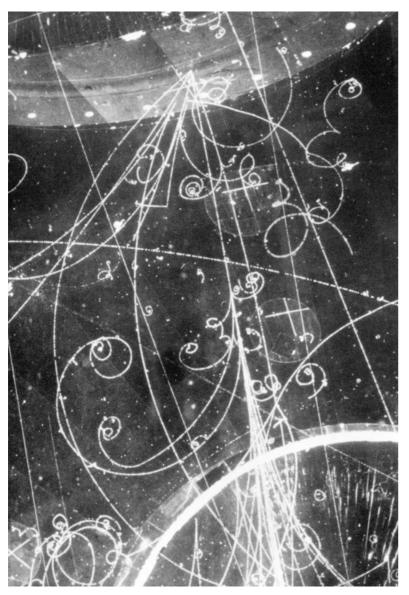


S. Tiwari and S. Wüster, PRA **99** 043616 (2019)

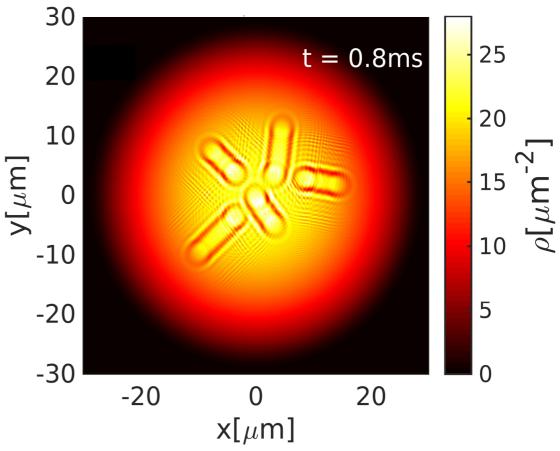


Rydberg "Bubble chamber"





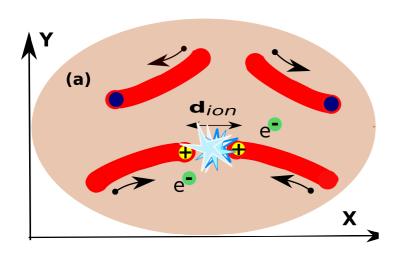
S. Tiwari and S. Wüster, PRA **99** 043616 (2019)





Rydberg "Bubble chamber"





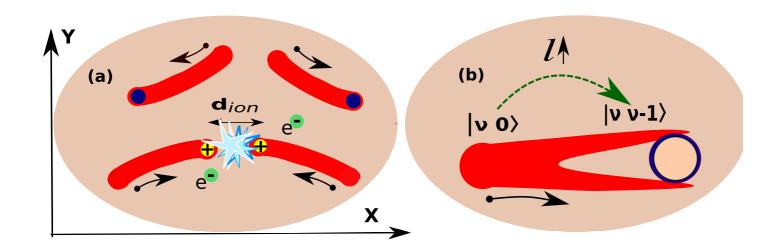
Ionizing collisions terminate tracks?

T.Amthor et al., PRL **98** (2007) 023004.



Rydberg "Bubble chamber"





Ionizing collisions terminate tracks?

I-changing collisions reshape tracks?

T.Amthor et al., PRL **98** (2007) 023004.

M. Schlagmüller et al., PRX 6 (2016) 031020.

T. Niederprüm *et al.,* PRL **115** (2015) 013003.

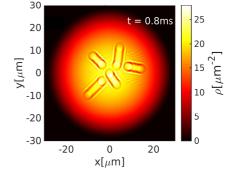


Outline

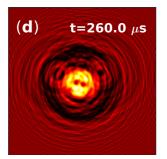


(I) Tracking of mobile Rydberg atoms in a BEC

S. Tiwari and S. Wüster, PRA **99** 043616 (2019)



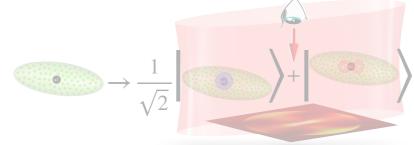
(II) BEC response to Rydberg insertion



S. Tiwari et al. in preparation (2021).

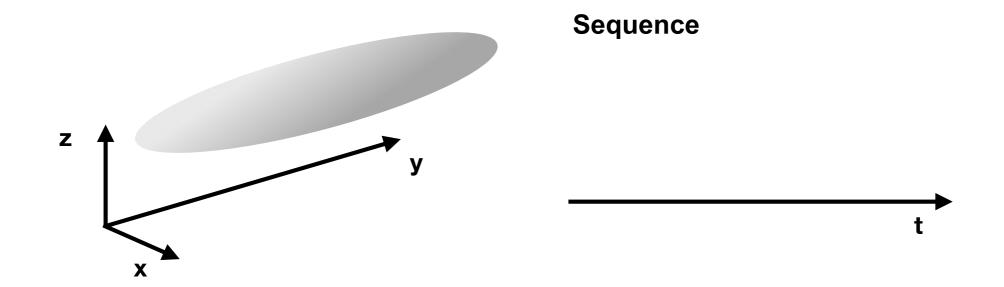
(III) Decoherence of Rydberg qubits in a BEC

S. Rammohan *et al.* arXiv:2011.11022 (2020). arXiv:2006.15376 (2020).



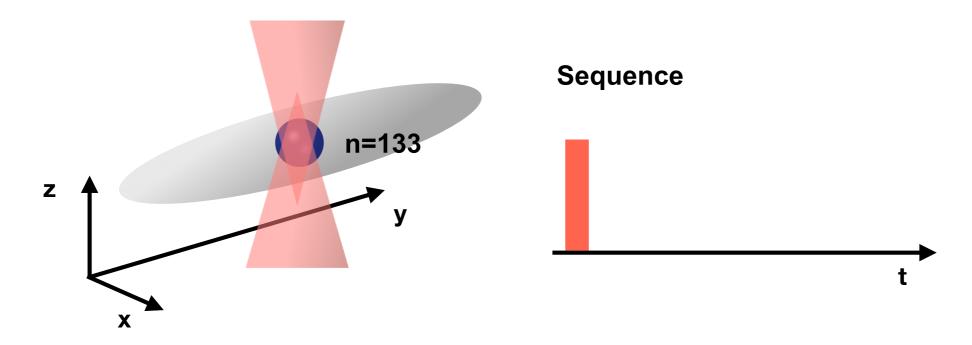






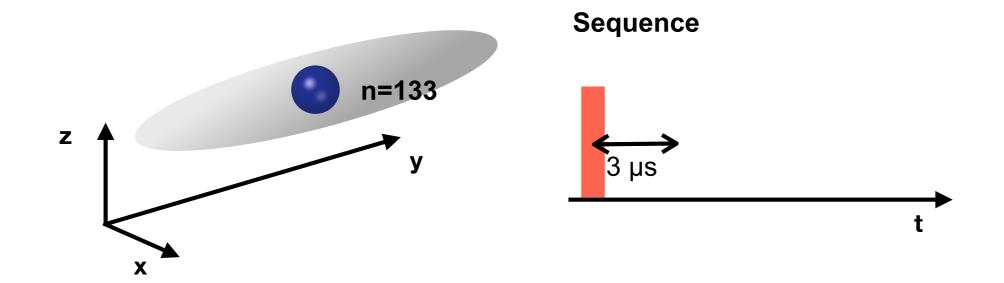






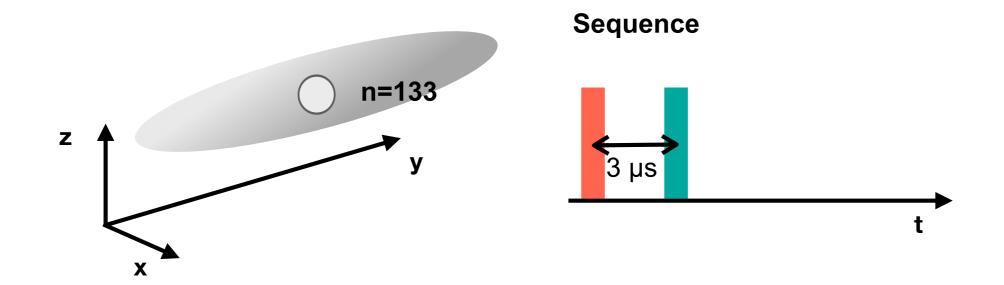






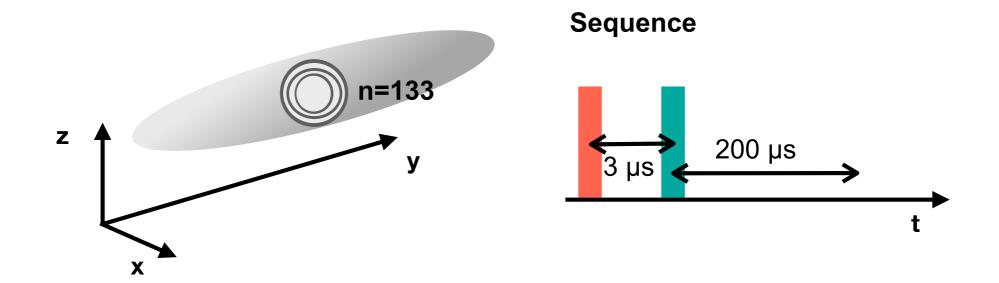






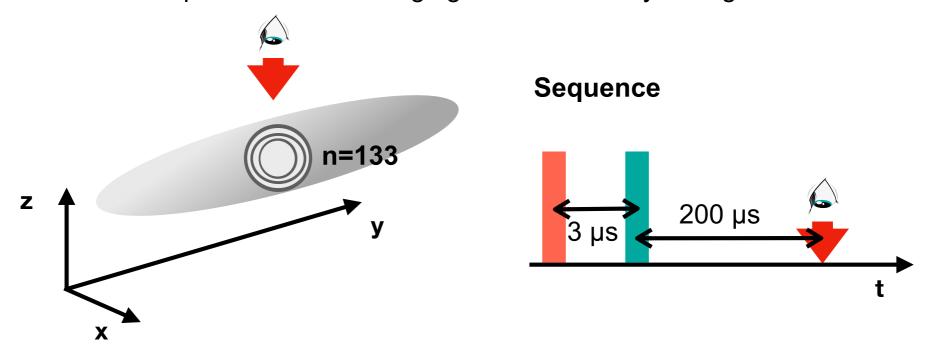






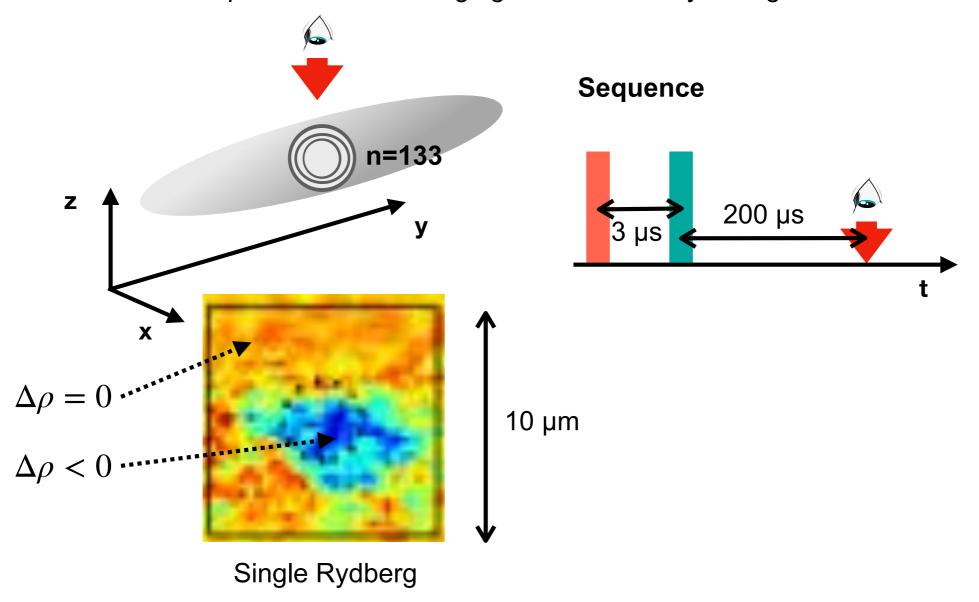






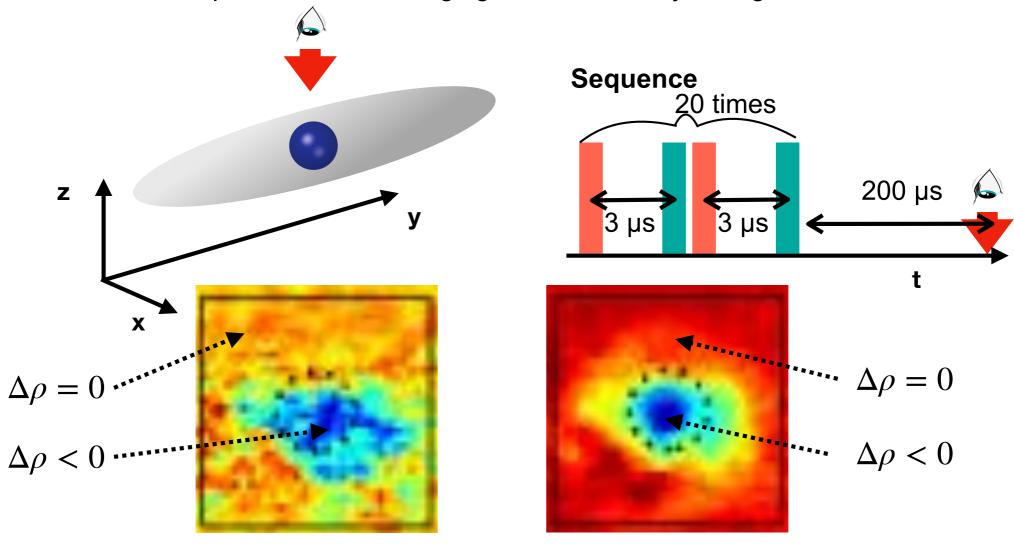












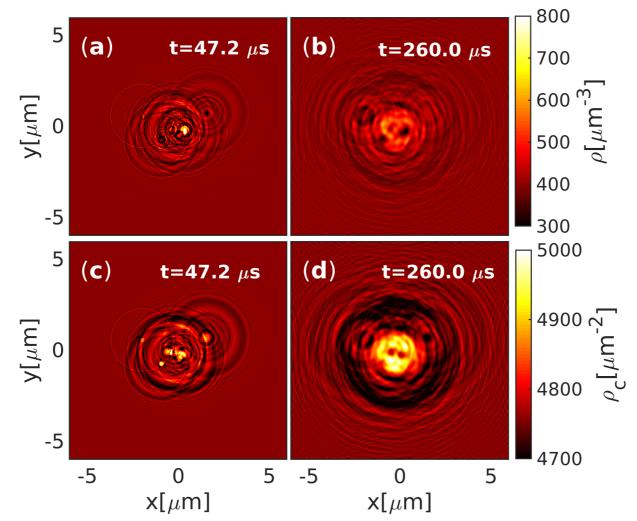
Single Rydberg for 3 μs Wait 200 μs

20 Rydbergs for 3 μs each Wait 200 μs





$$i\hbar \frac{\partial}{\partial t} \phi(\mathbf{R}) = \left(-\frac{\hbar^2}{2m} \nabla^2 + W(\mathbf{R}) + g |\phi(\mathbf{R})|^2 + V_0 |\Psi(\mathbf{R} - \mathbf{x}_n)|^2 \right) \phi(\mathbf{R})$$

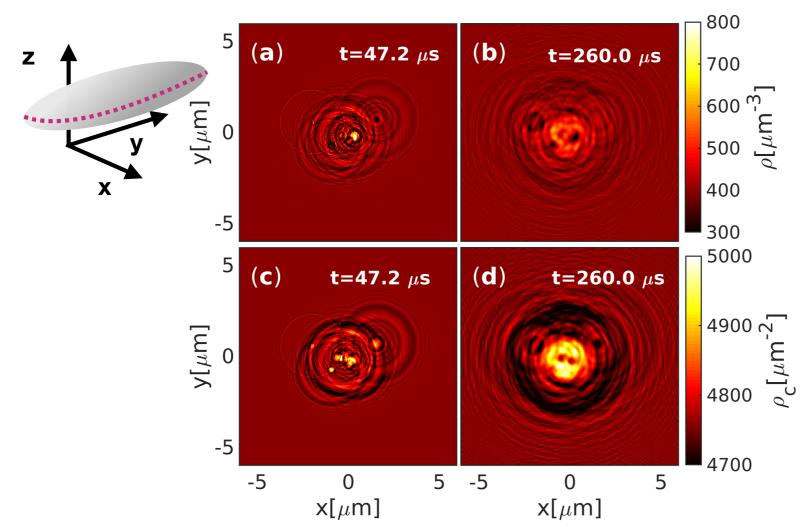


S. Tiwari *et al.* in preparation (2021).





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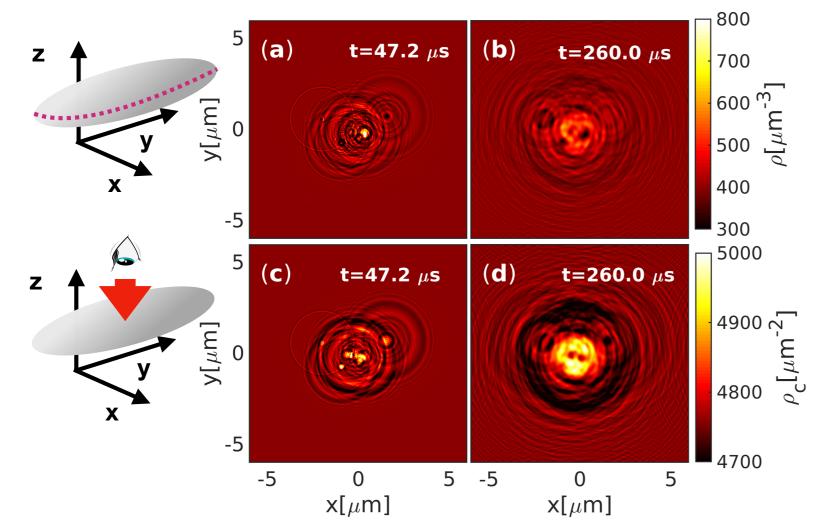


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S. Tiwari *et al.* in preparation (2021).

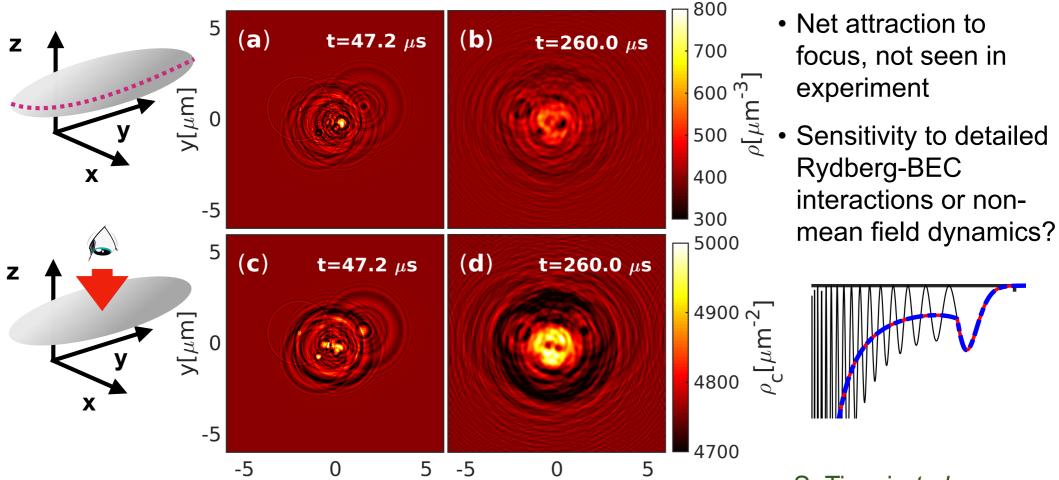




GPE (3D) with randomized Rydberg location

 $x[\mu m]$

$$i\hbar \frac{\partial}{\partial t} \phi(\mathbf{R}) = \left(-\frac{\hbar^2}{2m} \nabla^2 + W(\mathbf{R}) + g |\phi(\mathbf{R})|^2 + V_0 |\Psi(\mathbf{R} - \mathbf{x}_n)|^2 \right) \phi(\mathbf{R})$$



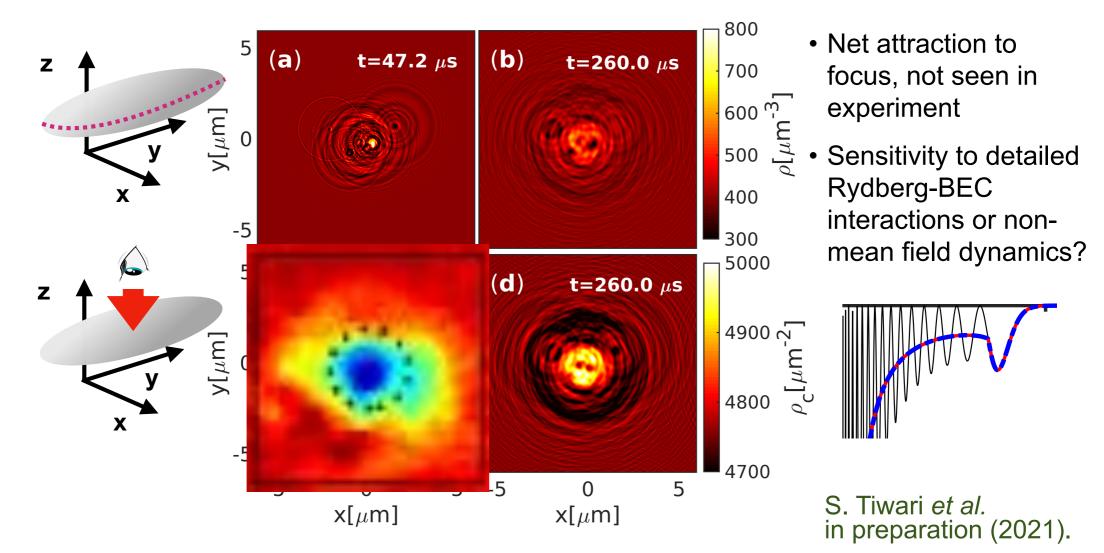
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S. Tiwari *et al.* in preparation (2021).





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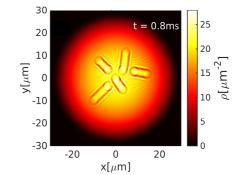


Outline

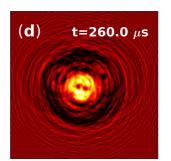


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S. Tiwari and S. Wüster, PRA **99** 043616 (2019)



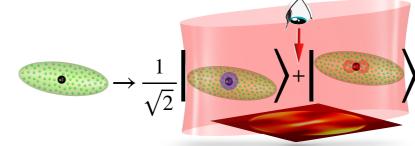
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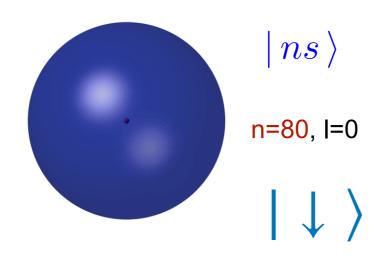
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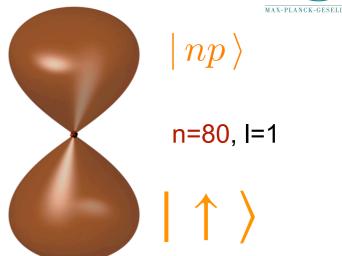
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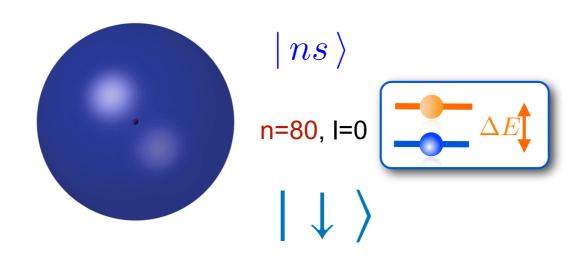


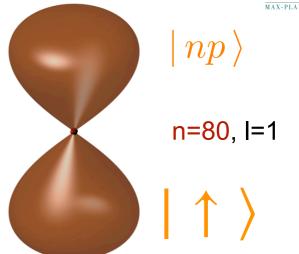






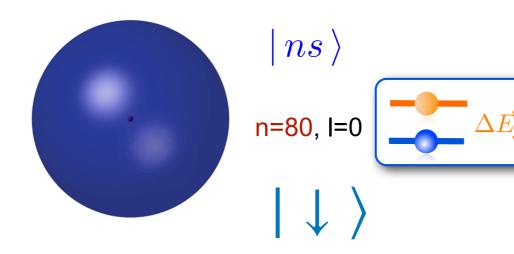


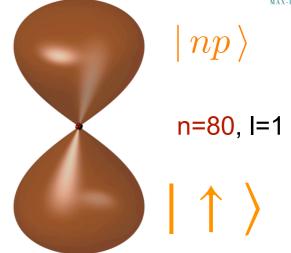








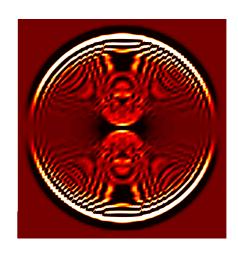




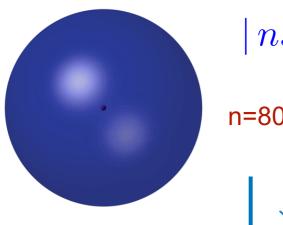


different Imprinted pattern

see also: Karpiuk et al. NJP **17** (2015) 053046

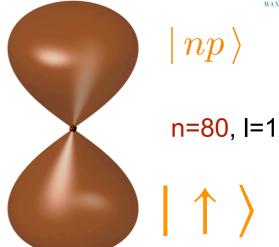


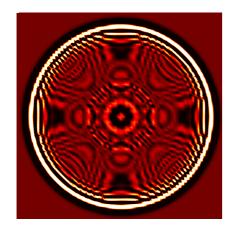




$$|\,ns\,
angle$$

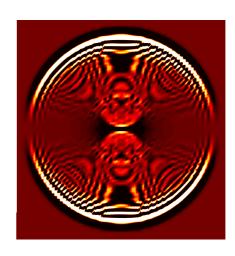






different **Imprinted** pattern

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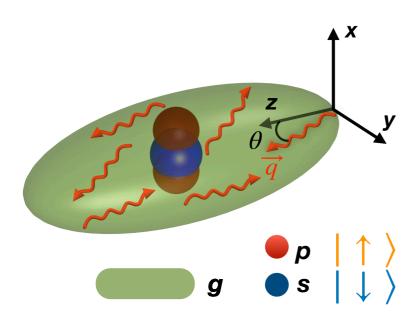


$$|\Psi\rangle = \frac{1}{\sqrt{2}} (|\downarrow\rangle + |\downarrow\rangle)?$$

 $|\Psi\rangle = \frac{1}{\sqrt{2}} (|\downarrow\rangle + |\downarrow\rangle)?$ • We only have **one** mean field, need to go beyond GRE? to go beyond GPE?







Many-body Hamiltonian

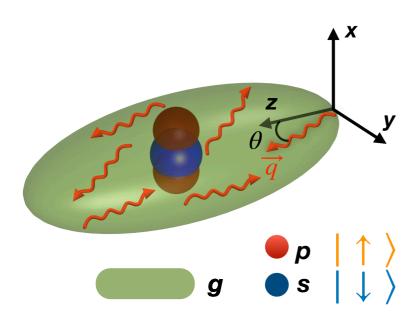
$$\hat{H} = \sum_{k} \int d^{3}\mathbf{x} \left[\hat{\Psi}_{k}^{\dagger}(\mathbf{x}) \left(-\frac{\hbar^{2}}{2m} \nabla^{2} + E_{k} \right) \hat{\Psi}_{k}(\mathbf{x}) \right]$$

$$+ \frac{1}{2} \sum_{i,j,s} \int d^{3}\mathbf{y} \hat{\Psi}_{k}^{\dagger}(\mathbf{x}) \hat{\Psi}_{i}^{\dagger}(\mathbf{y}) U_{kijs}(\mathbf{x} - \mathbf{y}) \hat{\Psi}_{j}(\mathbf{y}) \hat{\Psi}_{s}(\mathbf{x}) \right].$$
(1)

see also: Middelkamp et al. PRA 76 (2007) 022507.







Many-body Hamiltonian

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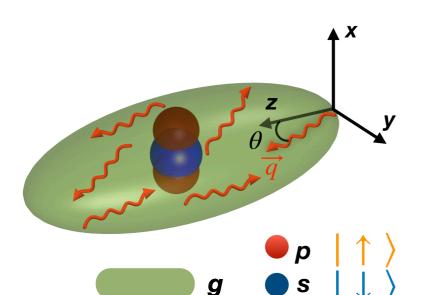
see also: Middelkamp et al. PRA 76 (2007) 022507.

Bose gas beyond mean field (Bogoliubov)

$$\hat{\Psi}_g(\mathbf{x}) = \phi_0(\mathbf{x}) + \sum_{\mathbf{q}} \left(u_{\mathbf{q}}(\mathbf{x}) \hat{b}_{\mathbf{q}} - v_{\mathbf{q}}^*(\mathbf{x}) \hat{b}_{\mathbf{q}}^{\dagger} \right)$$







Many-body Hamiltonian

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Spin-Boson Hamiltonian

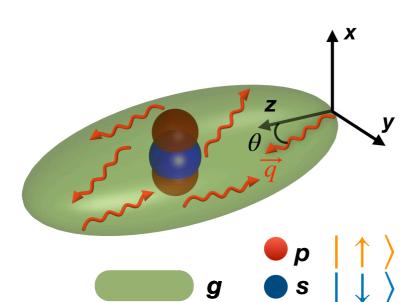
$$\hat{H}_{\text{syst}} = \frac{\Delta E(t)}{2} \hat{\sigma}_z, \quad \hat{H}_{\text{env}} = \sum_{\mathbf{q}} \hbar \omega_{\mathbf{q}} \, \tilde{b}_{\mathbf{q}}^{\dagger} \tilde{b}_{\mathbf{q}}$$

$$\hat{H}_{\mathrm{int}} = \sum_{\mathbf{q}} \frac{\Delta \kappa_{\mathbf{q}}}{2} \left(\tilde{b}_{\mathbf{q}} + \tilde{b}_{\mathbf{q}}^{\dagger} \right) \hat{\sigma}_{z}.$$
 +

S. Rammohan et al. arXiv:2006.15376 (2020).







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$$\hat{\Psi}_g(\mathbf{x}) = \phi_0(\mathbf{x}) + \sum_{\mathbf{q}} \left(u_{\mathbf{q}}(\mathbf{x}) \hat{b}_{\mathbf{q}} - v_{\mathbf{q}}^*(\mathbf{x}) \hat{b}_{\mathbf{q}}^{\dagger} \right)$$

Spin-Boson Hamiltonian

$$\hat{H}_{\text{syst}} = \frac{\Delta E(t)}{2} \hat{\sigma}_z, \quad \hat{H}_{\text{env}} = \sum_{\mathbf{q}} \hbar \omega_{\mathbf{q}} \, \tilde{b}_{\mathbf{q}}^{\dagger} \tilde{b}_{\mathbf{q}}$$

$$\hat{H}_{\rm int} = \sum_{\mathbf{q}} \frac{\Delta \kappa_{\mathbf{q}}}{2} \left(\tilde{b}_{\mathbf{q}} + \tilde{b}_{\mathbf{q}}^{\dagger} \right) \hat{\sigma}_{z}. \quad + \quad \blacksquare$$

S. Rammohan et al. arXiv:2006.15376 (2020).

For g-impurities:

Jaksch group and Lewenstein group





Spin-phonon coupling:

$$\Delta \kappa_{\mathbf{q}} = V_0 \sqrt{\rho} \int d^3 \mathbf{x} \left(|\psi^{(p)}(\mathbf{x})|^2 - |\psi^{(s)}(\mathbf{x})|^2 \right) \left(u_{\mathbf{q}} e^{i\mathbf{q}x} - v_{\mathbf{q}}^* e^{-i\mathbf{q}x} \right)$$





Spin-phonon coupling:

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Block diagonal Hamiltonian:

$$H = \begin{bmatrix} H_{\uparrow} & 0 \\ 0 & H_{\downarrow} \end{bmatrix}$$





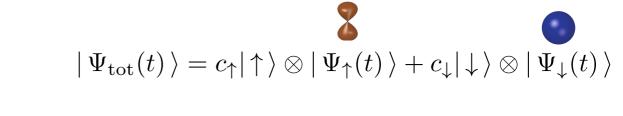
Spin-phonon coupling:

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$$|\Psi_{
m tot}(t)\rangle=c_{\uparrow}|\!\uparrow
angle\otimes|\Psi_{\uparrow}(t)
angle+c_{\downarrow}|\!\downarrow
angle\otimes|\Psi_{\downarrow}(t)
angle$$

Spin coherence

$$\hat{\rho}_{red} = \mathbf{Tr}_{\mathscr{E}}[|\Psi_{tot}\rangle\langle\Psi_{tot}|]$$

$$\rho_{\downarrow\uparrow}(t) = c_{\downarrow}^* c_{\uparrow} \langle \Psi_{\uparrow}(t) | \Psi_{\downarrow}(t) \rangle$$





Spin-phonon coupling:

$$\Delta \kappa_{\mathbf{q}} = V_0 \sqrt{\rho} \int d^3 \mathbf{x} \left(|\psi^{(p)}(\mathbf{x})|^2 - |\psi^{(s)}(\mathbf{x})|^2 \right) \left(u_{\mathbf{q}} e^{i\mathbf{q}x} - v_{\mathbf{q}}^* e^{-i\mathbf{q}x} \right)$$

Block diagonal Hamiltonian:

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Many-body wavefunction:

$$|\Psi_{\mathrm{tot}}(t)\rangle = c_{\uparrow}|\uparrow\rangle\otimes|\Psi_{\uparrow}(t)\rangle + c_{\downarrow}|\downarrow\rangle\otimes|\Psi_{\downarrow}(t)\rangle$$

Spin coherence

$$\hat{\rho}_{red} = \mathbf{Tr}_{\mathscr{E}}[\,|\,\Psi_{tot}\rangle\langle\Psi_{tot}|\,]$$

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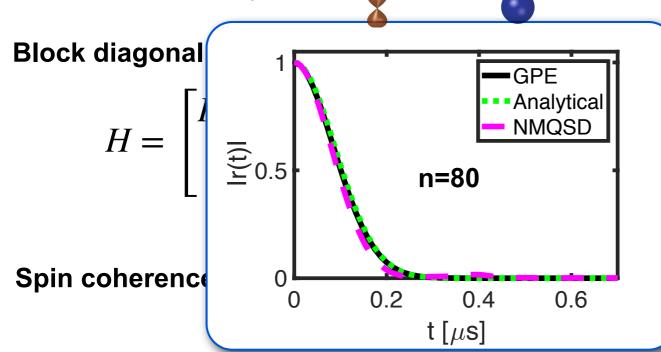
$$\Psi(\mathbf{R}_1, \dots, \mathbf{R}_N) = \prod_k \left(\frac{\phi(\mathbf{R}_k)}{\sqrt{N}}\right)^N$$

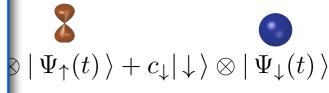




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$$\begin{split} \mathbf{SBM}_{l_{\mathrm{syst}}} & \underline{\underline{\underline{\Omega}_{\mathrm{mw}}}}_{\underline{\underline{q}}} \underline{\hat{\sigma}_{x}} + \frac{\Delta E(t)}{2} \hat{\sigma}_{z}, \quad \hat{H}_{\mathrm{env}} = \sum_{\mathbf{q}} \hbar \omega_{\mathbf{q}} \, \hat{b}_{\mathbf{q}}^{\dagger} \hat{b}_{\mathbf{q}} \\ & \hat{H}_{\mathrm{int}} = \sum_{\mathbf{q}} \frac{\Delta \kappa_{\mathbf{q}}}{2} \Big(\hat{b}_{\mathbf{q}} + \bar{b}_{\mathbf{q}}^{\dagger} \Big) \hat{\sigma}_{z}. \end{split}$$

$$\rho_{\downarrow\uparrow}(t) = c_{\downarrow}^* c_{\uparrow} \langle \Psi_{\uparrow}(t) | \Psi_{\downarrow}(t) \rangle$$



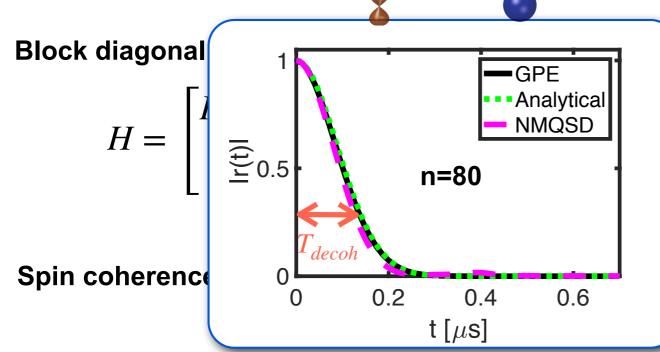
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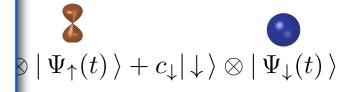


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unction:



$$\begin{aligned} \mathbf{S} \mathbf{B}_{\mathbf{H}_{\text{syst}}}^{\mathbf{M}} &= \frac{\Omega_{\text{mw}}}{2} \hat{\sigma}_x + \frac{\Delta E(t)}{2} \hat{\sigma}_z, \quad \hat{H}_{\text{env}} = \sum_{\mathbf{q}} \hbar \omega_{\mathbf{q}} \, \tilde{b}_{\mathbf{q}}^{\dagger} \tilde{b}_{\mathbf{q}} \\ \hat{H}_{\text{int}} &= \sum_{\mathbf{q}} \frac{\Delta \kappa_{\mathbf{q}}}{2} \Big(\tilde{b}_{\mathbf{q}} + \tilde{b}_{\mathbf{q}}^{\dagger} \Big) \hat{\sigma}_z. \end{aligned}$$

$\rho_{\downarrow\uparrow}(t) = c_{\downarrow}^* c_{\uparrow} \langle \Psi_{\uparrow}(t) | \Psi_{\downarrow}(t) \rangle$

Decoherence times

$$T_{decoh} \approx 20 \text{ ns} \text{ n=40}$$

$$T_{decoh} \approx 20 \text{ ns } \text{n=40}$$
 $T_{decoh} \approx 0.9 \mu s \text{ n=120}$

$$\Psi(\mathbf{R}_1, \dots, \mathbf{R}_N) = \prod_k \left(\frac{\phi(\mathbf{R}_k)}{\sqrt{N}}\right)^N$$

GPE

S. Rammohan et al., arXiv:2011.11022 (2020).

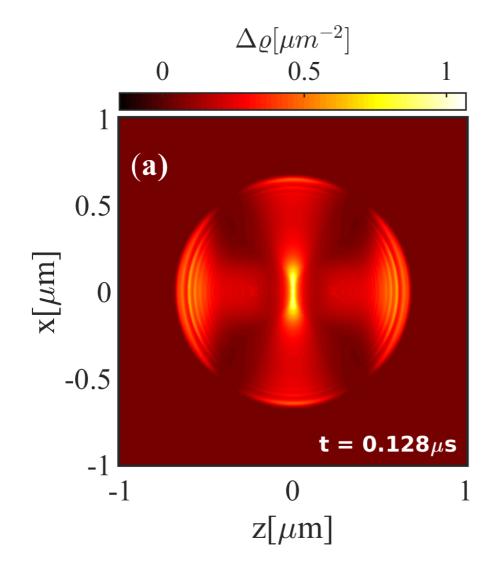


Imaging decohering environment



BEC column densities in

$$|\Psi_{\mathrm{ms}}(t)\rangle = A[|\Psi_{\uparrow}(t)\rangle + |\Psi_{\downarrow}(t)\rangle]$$
 (minus) $\hat{\rho} = (|\Psi_{\uparrow}\rangle\langle\Psi_{\uparrow}| + |\Psi_{\downarrow}\rangle\langle\Psi_{\downarrow}|)/2$



S. Rammohan et al., arXiv:2011.11022 (2020).



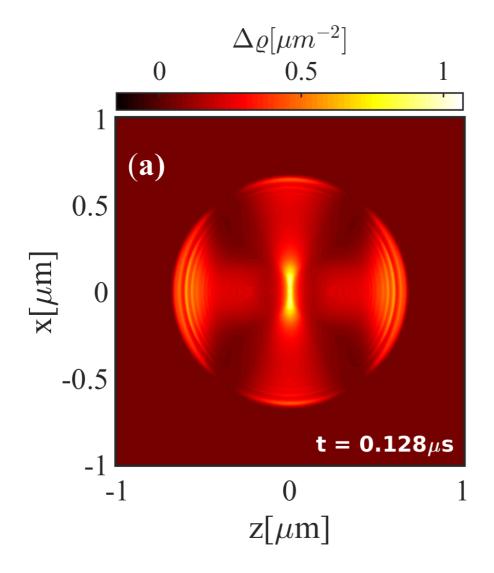
Imaging decohering environment

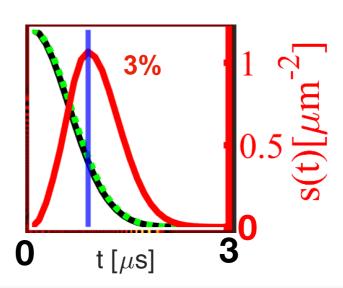


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ho} = (|\Psi_{\uparrow}\rangle\langle\Psi_{\uparrow}| + |\Psi_{\downarrow}\rangle\langle\Psi_{\downarrow}|)/2$$





 Transient glimpse at many-body entanglement at the root of decoherence:

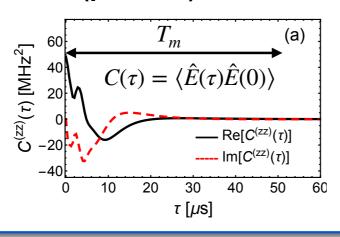
$$|\Psi_{\text{tot}}(t)\rangle = c_{\uparrow}|\uparrow\rangle \otimes |\Psi_{\uparrow}(t)\rangle + c_{\downarrow}|\downarrow\rangle \otimes |\Psi_{\downarrow}(t)\rangle$$

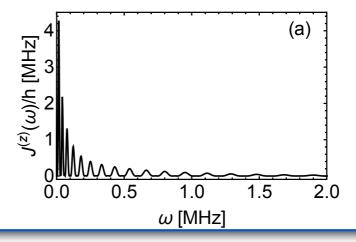
S. Rammohan et al., arXiv:2011.11022 (2020).



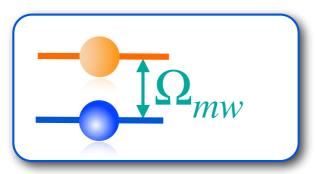


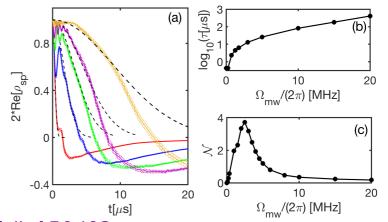
Environment (phonon) correlation functions and spectral densities





Non-Markovian Rydberg qubit dynamics



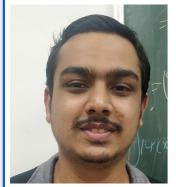


using **NMQSD:** Suess et al. PRL **113** (2014) 150403.



Thanks to coworkers...







Sidharth Shiva Kant Abhijit Rammohan Tiwari



Pendse



Aritra Mishra



Anil Kumar



Rejish Nath



Alexander Eisfeld

...collaborators...

Felix Engel, Florian Meinert, Marcel Wagner, Richard Schmidt

...and funding:









Thanks to current group



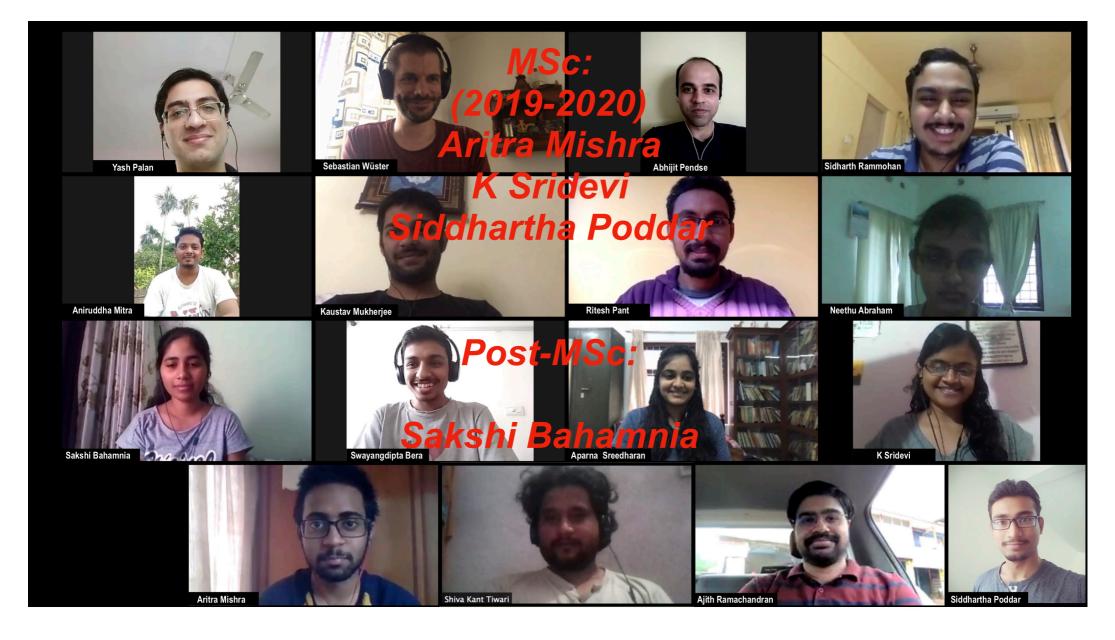


Shivakant Tivari Sidharth Rammohan



Thank Sweethu Abraham Thank Sweethu Abraham





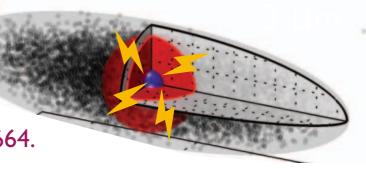


Summary



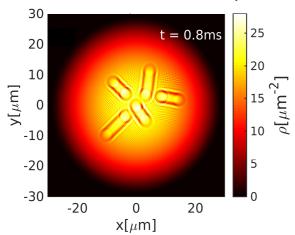
 Combination of two extreme systems: Rydberg atoms and BEC:

J. Balewski *et al.*, Nature **502** (2013) 664.



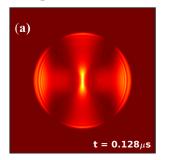
Tracking of Rydberg motion by BEC

S. Tiwari and S. Wüster, PRA **99** 043616 (2019)

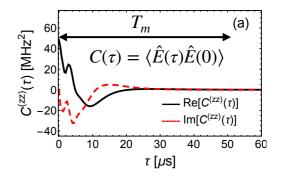


Imaging the decohering interface

S. Rammohan *et al.* arXiv:2011.11022 (2020). arXiv:2006.15376 (2020).



Tunable open quantum system



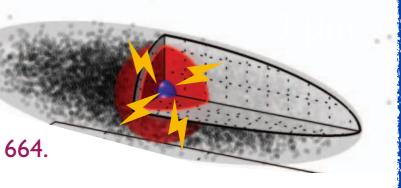


Summary



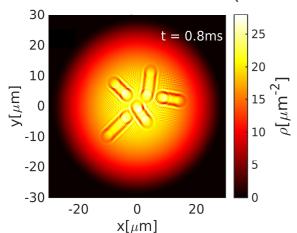
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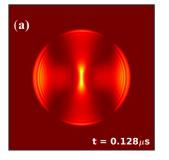
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Thanks for your attention

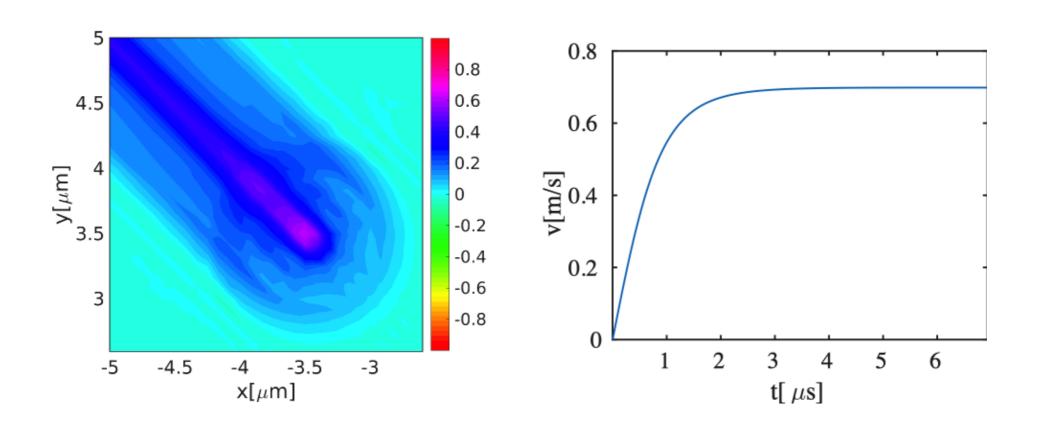




Appendix

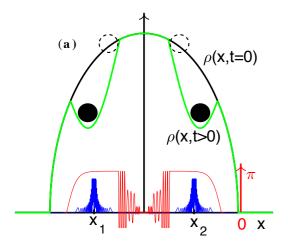
Velocity dependence



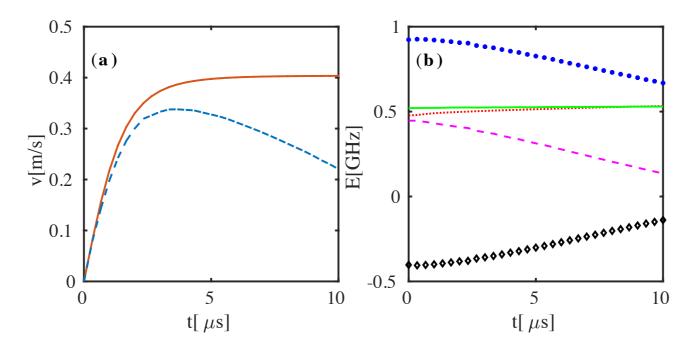


Condensate backaction

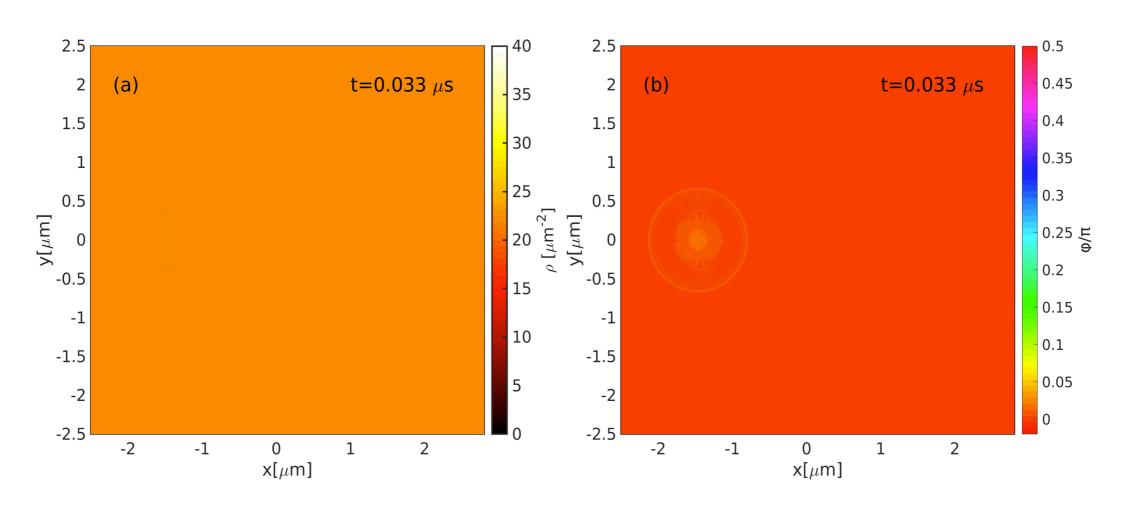




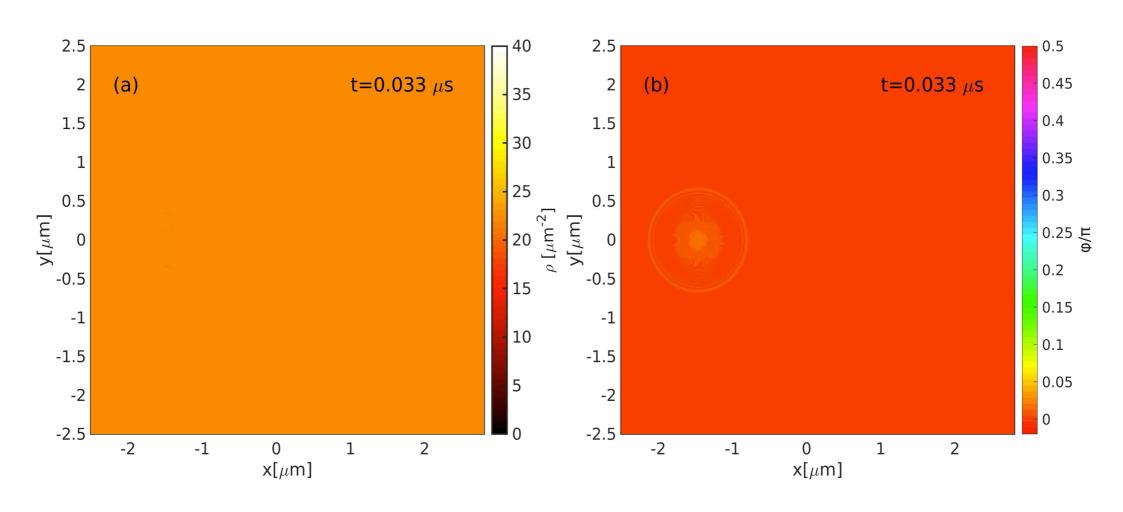
$$m \frac{\partial^2}{\partial t^2} \mathbf{x}_n = -\nabla_{\mathbf{x}_n} \left[V_{RR}(\mathbf{X}) + \bar{V}(\mathbf{x}_n) \right]$$
$$\bar{V}(\mathbf{x}_n) = \int d^2 \mathbf{R} |V_0| \Psi(\mathbf{R} - \mathbf{x}_n)|^2 |\phi(\mathbf{R})|^2$$





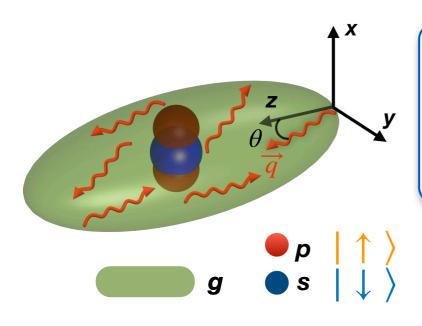








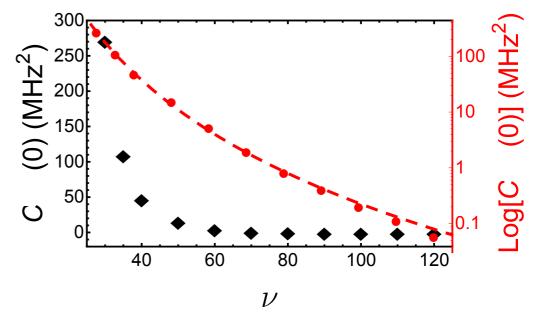




$$\hat{H}_{\text{syst}} = \frac{\Omega_{\text{mw}}}{2} \hat{\sigma}_x + \frac{\Delta E(t)}{2} \hat{\sigma}_z, \quad \hat{H}_{\text{env}} = \sum_{\mathbf{q}} \hbar \omega_{\mathbf{q}} \, \tilde{b}_{\mathbf{q}}^{\dagger} \tilde{b}_{\mathbf{q}}$$

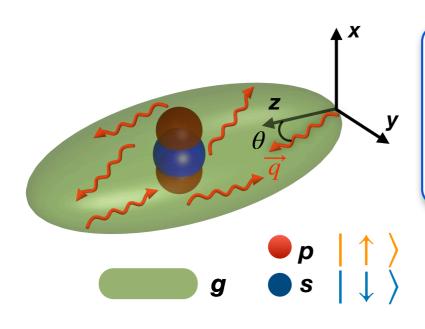
$$\hat{H}_{\mathrm{int}} = \sum_{\mathbf{q}} \frac{\Delta \kappa_{\mathbf{q}}}{2} \left(\tilde{b}_{\mathbf{q}} + \tilde{b}_{\mathbf{q}}^{\dagger} \right) \hat{\sigma}_{z}.$$





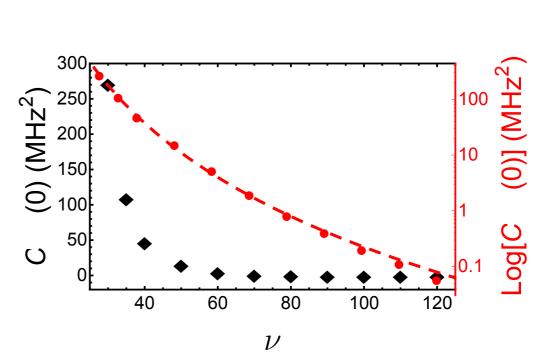






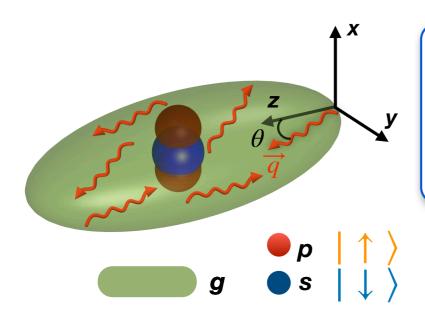
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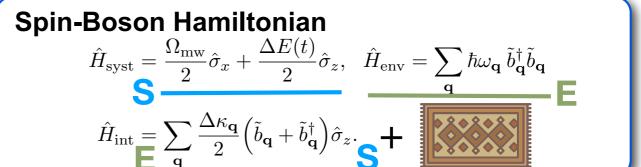
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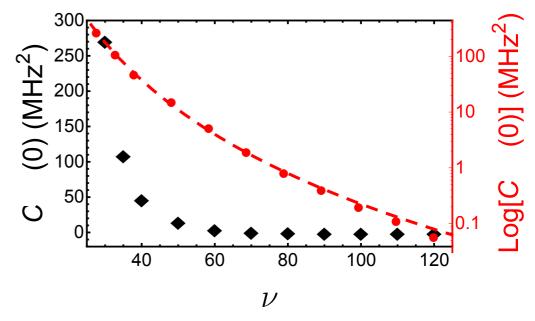






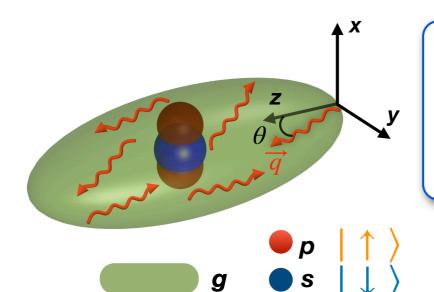








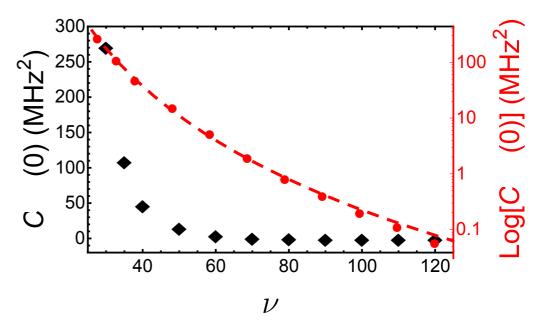




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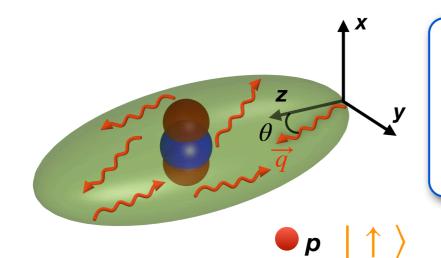
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$$\hat{H}_{int} = \hat{E} \otimes \hat{S}$$





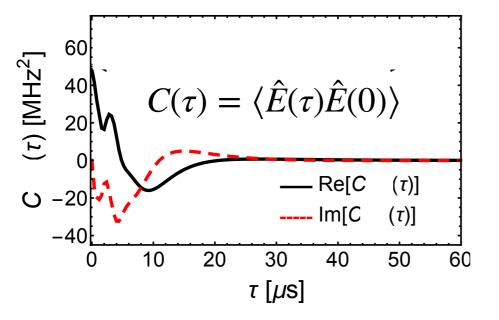


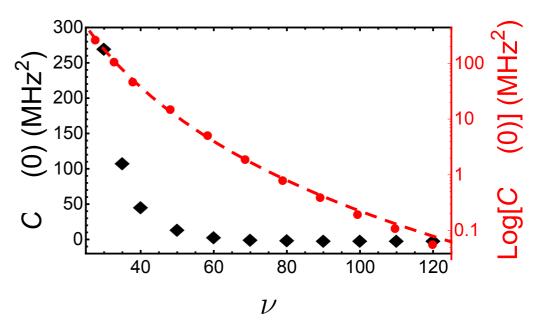


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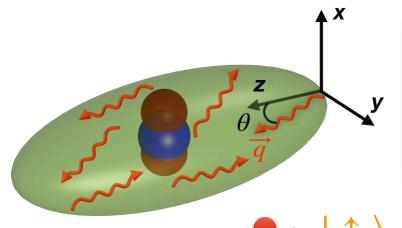




S. Rammohan et al. arXiv:2006.15376 (2020).





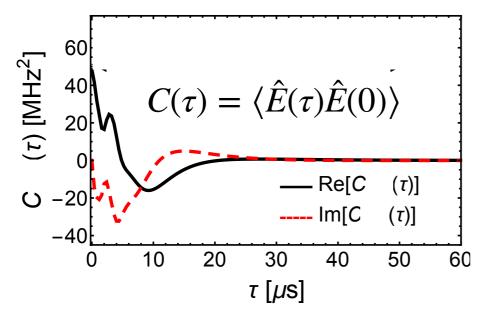


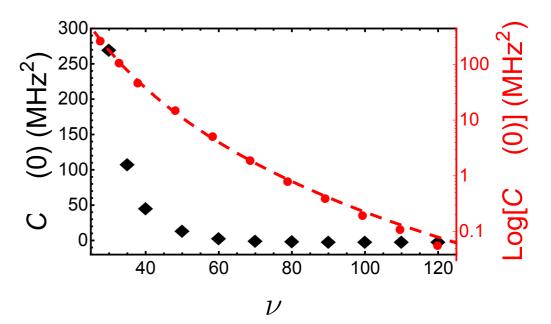
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$$\hat{H}_{int} = \hat{E} \otimes \hat{S}$$

$$T_{decoh} \approx 1/\sqrt{2C(0)}$$

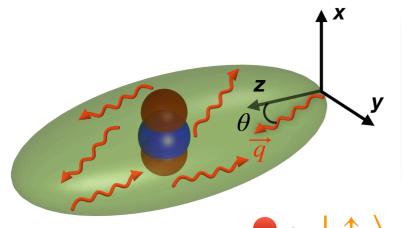




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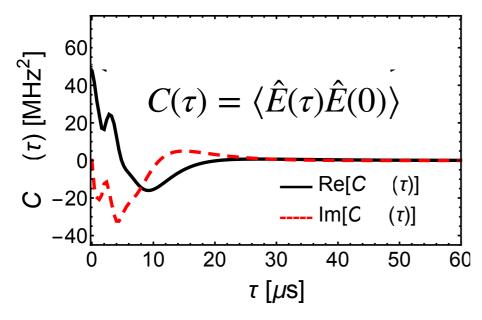


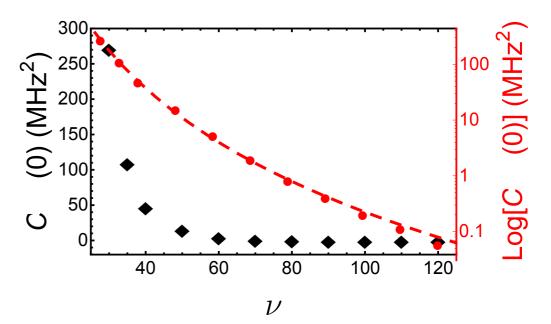
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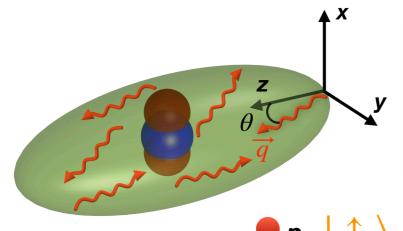




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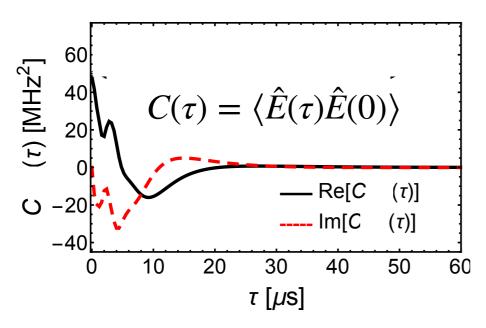


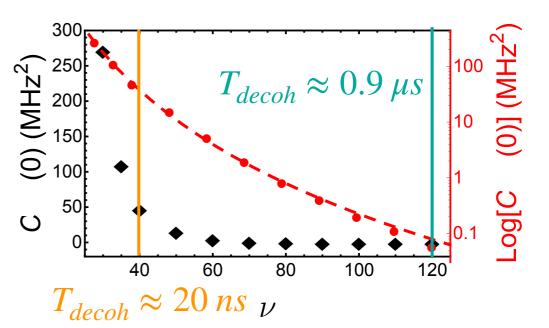
$$\hat{H}_{\rm syst} = \frac{\Omega_{\rm mw}}{2} \hat{\sigma}_x + \frac{\Delta E(t)}{2} \hat{\sigma}_z, \quad \hat{H}_{\rm env} = \sum_{\bf q} \hbar \omega_{\bf q} \, \tilde{b}_{\bf q}^{\dagger} \tilde{b}_{\bf q}$$

$$\hat{H}_{\rm int} = \sum_{\bf q} \frac{\Delta \kappa_{\bf q}}{2} \left(\tilde{b}_{\bf q} + \tilde{b}_{\bf q}^{\dagger} \right) \hat{\sigma}_z.$$

$$\begin{array}{c|c} \bullet & \uparrow \\ \bullet & s \\ \hline \end{array} \begin{array}{c} \uparrow \\ \downarrow \end{array} \begin{array}{c} \hat{H}_{int} = \hat{E} \otimes \hat{S} \end{array}$$

$$T_{decoh} \approx 1/\sqrt{2C(0)}$$





S. Rammohan et al. arXiv:2006.15376 (2020).

Full Spin-Boson Model



$$\epsilon_q = \hbar\omega_q = \sqrt{\frac{\hbar^2 q^2}{2m} \left(\frac{\hbar^2 q^2}{2m} + 2U_0 \rho\right)}$$

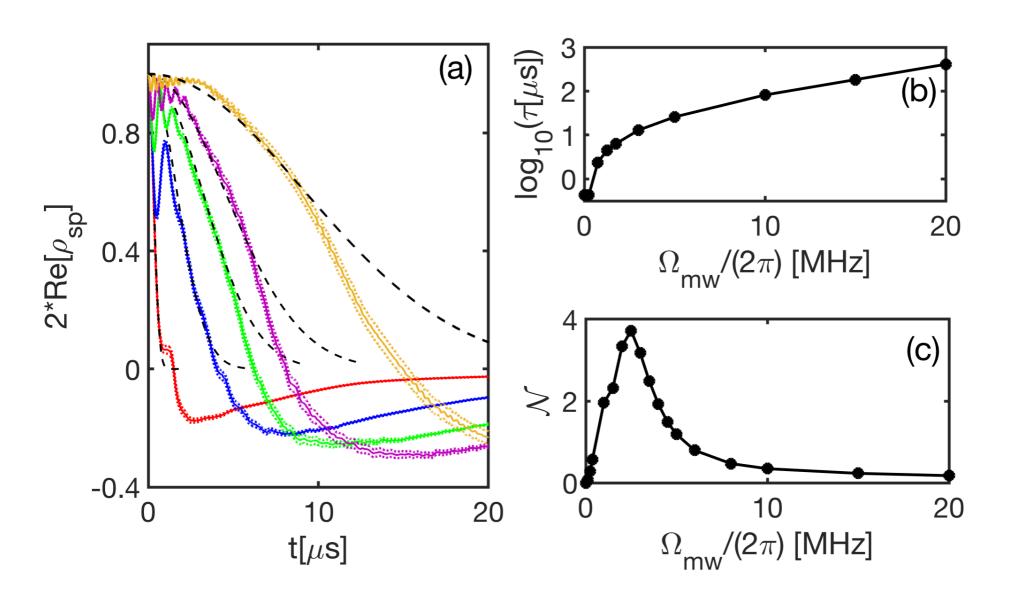
$$\hat{H}_{\text{tot}} = \hat{H}'_{\text{syst}} + \sum_{\mathbf{q}} \hbar \omega_{q} \, \tilde{b}_{\mathbf{q}}^{\dagger} \tilde{b}_{\mathbf{q}} + \sum_{\mathbf{q}} \frac{\Delta \kappa_{\mathbf{q}}}{2} \left(\tilde{b}_{\mathbf{q}} + \tilde{b}_{\mathbf{q}}^{\dagger} \right) \hat{\sigma}_{z}$$

$$+ i \sum_{\mathbf{q}} \kappa_{\mathbf{q}}^{(sp)} \left(\tilde{b}_{\mathbf{q}} - \tilde{b}_{\mathbf{q}}^{\dagger} \right) \hat{\sigma}_{y} + const, \qquad (21)$$

$$\hat{H}'_{\text{syst}} = \left[\frac{\Delta E}{2} + \sum_{\mathbf{q}} \frac{\Delta \kappa_{\mathbf{q}} \,\bar{\kappa}_{\mathbf{q}}}{2\hbar\omega_{q}} \left(\cos(\omega_{q} t) - 1 \right) \right] \hat{\sigma}_{z}$$

Non-Markovian Rydberg qubit dynamics





NMQSD



$$\frac{\partial}{\partial t} f^{(\mathbf{k})}(t) = \left(-i\hat{H}_{\text{syst}} - \mathbf{k} \cdot \mathbf{w} + \hat{L}\tilde{z}_t \right) f^{(\mathbf{k})}(t)$$

$$+ \sum_{j} k_j g_j f^{(\mathbf{k} - \mathbf{e}_j)}(t) - \sum_{j} (\hat{L}^{\dagger} - \langle \hat{L}^{\dagger} \rangle) f^{(\mathbf{k} + \mathbf{e}_j)}(t)$$

$$\overline{z_t z_s^*} = C(t - s)$$

$$\tilde{z}_t = z_t^* + \int_0^t ds \ C^*(t-s)\langle \hat{L}^\dagger \rangle$$