Machine Learning Methods for Atmosphere, Ocean, and Climate Science

Lecture 4: Climate Research Applications of ML

Mathematical modeling of Climate, Ocean, and Atmosphere processes International Centre for Theoretical Sciences, TIFR, Bengaluru, India

Aman Gupta





Lecture 1

- Parametric estimation
- Introduction to deep neural networks
- The training algorithm

Lecture 2

- The PyTorch library
- Implementing Artificial Neural Nets in PyTorch



ecture 3

• Implementing Convolutional Neural Networks in PyTorch

• Applications of ML in climate science

Lecture 4

Updates on Model Hierarchies for Understanding and Simulating the Climate System: A Focus on Data-informed Methods and Usability

Laura A. Mansfield¹, Aman Gupta¹, Adam C. Burnett¹, Brian Green¹, Catherine Wilka¹ and Aditi Sheshadri¹

¹Department of Earth System Science, Stanford Doerr School of Sustainability, Stanford University, CA

Climate modeling has already adopted numerous ideas from the field of AI and has, within a short period of time, witnessed a meteoric rise in the application of ML methods. As discussed at the workshop, ML-assisted analyses have begun to pervade practically all aspects of the existing model hierarchy: from modeling fundamental partial differential equations (PDEs) and dynamical systems (Pathak et al., 2018a; Liu et al., 2022), to modeling and performing equation discovery for subgrid-scale (SGS) processes (e.g. Rasp et al., 2018; Gentine et al., 2018; Yuval & O'Gorman, 2020; Brenowitz & Bretherton, 2019; Zanna and Bolton, 2020), to full-blown efforts to completely replace complex weather prediction models with a single ML model (Pathak et al., 2022; Bi et al., 2022; Lam et al., 2022). Rather than just being used to build new models, ML is also helping modelers improve existing models by aiding calibration and uncertainty quantification, by providing emulators that approximate computationally expensive models.

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Interpretability

Generalizability

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Interpretability + Generalizability

Trustworthiness!

Data-driven Model Parameterizations Equation Discovery using ML ML in Weather Forecasting

Data-driven Model Parameterizations

Gravity Waves Significantly Influence Stratospheric Variability



- Tropical stratosphere dominated by oscillating wind patterns with a period of ~28 months, called the Quasi-Biennial Oscillation (QBO). Can have influence over tropical convective systems like ENSO, Madden-Julian Oscillation.
- Driven mostly by convectively generated gravity waves, which are not completely resolved in most climate models

Gravity Waves Significantly Influence Stratospheric Variability

Geophysical Research Letters^{*}

RESEARCH LETTER 10.1029/2022GL098174

Key Points:

- Neural networks trained on one annual cycle accurately emulate a physicsbased gravity wave parameterization (GWP) when coupled to a climate model
- Although trained on only one phase of the Quasi-Biennial Oscillation, the

Machine Learning Gravity Wave Parameterization Generalizes to Capture the QBO and Response to Increased CO₂

Zachary I. Espinosa¹, Aditi Sheshadri¹, Gerald R. Cain², Edwin P. Gerber³, and Kevin J. DallaSanta^{4,5}

¹Department of Earth System Science, Stanford University, Stanford, CA, USA, ²Department of Computer Science, Stanford University, Stanford, CA, USA, ³Courant Institute of Mathematical Sciences, New York University, New York, NY, USA, ⁴NASA Goddard Institute for Space Studies, New York, NY, USA, ⁵Universities Space Research Association, Columbia, MD, USA

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WaveNet: an ML Emulator for Atmospheric Gravity Waves



- Trained on just one year of atmospheric data (features) and GW parameterization data (labels) from an intermediate complexity climate model.
- Generalizes well to identify longer period signals and out-of-sample data points for four test years

Offline tests: comparable performance using less features and data



\longrightarrow [u,v, ω ,H,T, λ , φ ,ps]	—— [v]	—— [u, T]
─── [u,v]	── [v, T]	→ [u, H]
\longrightarrow [ω ,H,T, λ , ϕ ,ps]	—— [v, H]	[u, λ,φ]
—— [u]	<u> </u>	

*Higher R² means higher prediction score

Robustness to feature omission: only training on the winds sufficient to retain 96% of the prediction skill of the full model

Robustness to training data: training on 1/4th of the years retains 98% of the prediction skill of the full NN

Online tests: consistent results for QBO evolution under climate change



- WaveNet plugged into the Fortran climate model code. Model integrated for 50 years with original gravity wave parameterization and with WaveNet
- Both parameterizations and WaveNet predict a reduction in the QBO period and weakening of the maximum windspeeds

Properties desired:

1) Lateral propagation

2) Refraction

3) Transience

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1) Lateral propagation

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3) Transience

WaveNet

Trained on parameterizations Limited training data Incomplete wave

Nonlocal emulators

Trained on HighRes data Extend training periods Complete physics

Nonlocal emulators based on Recurrent Neural Networks

Trained on global 1km simulations from ECMWF Extended training periods Complete physics

Training using non-local columns

- ✓ Lateral propagation
- ✓ Refraction

Training using non-local columns

- ✓ Lateral propagation
- ✓ Refraction

Implement transience using Recurrent Networks

✓ Transience

Equation Discovery

Mesoscale Dynamics are Important, but are not Resolved in Ocean Models

- Subgrid-scale turbulent fluxes at scales 10-100 km important for global heat, oxygen, and tracer transport
- Interaction on small-scales with large-scales not well understood
- These scale not typically resolved in ocean models

- Parameterizations spuriously dissipate kinetic energy, affecting large-scale currents
- Use simple quadratic closures and hyperdiffusion to parameterize subgrid scales

$$\mathbf{S}_{\mathbf{u}} = \begin{pmatrix} S_x \\ S_y \end{pmatrix} = (\overline{\mathbf{u}} \cdot \overline{\nabla})\overline{\mathbf{u}} - \overline{(\mathbf{u} \cdot \nabla)\mathbf{u}},$$
$$S_T = (\overline{\mathbf{u}} \cdot \overline{\nabla})T - \overline{(\mathbf{u} \cdot \nabla)T},$$

u = (u,v): horizontal winds, T: temperature overbar: 30 km Gaussian filtering

"Given some spatiotemporal data set of the subgrid eddy forcing, we uncover an equation that could have produced that dataset."

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(a) Relevance Vector Machines (RVMs) iterative regression possible to physically interpret the results (b) Convolutional Neural Networks (CNNs)

Barotropic Model: highly idealized, 3.75 km, 10 years of data

Assume a library of basis functions: - Start with u and v and their gradients

- Obtain vorticity and divergence as a more reasonable basis

- Use vorticity, divergence, shear terms as the improved basis, ϕ_i s to create a library of funcitons (products and derivatives). Compute these quantities using the high resolution data

- Compute the weights w_i s for functions, and prune to get the basis that best captures the subgrid scale fluxes

- Obtain subgrid scale closures:

 $\Sigma_i w_i \phi_i(\bar{u}, \bar{v})$

RVM reveals the expression:

$$\mathbf{\hat{S}}_{\mathbf{u}}^{BT} = \begin{pmatrix} w_0(\zeta^2)_x - w_1(\zeta D)_x + w_2(\zeta \tilde{D})_y \\ w_3(\zeta^2)_y + w_4(\zeta D)_y + w_5(\zeta \tilde{D})_x \end{pmatrix},$$

 $w_0 = -4.096 \times 10^8 \text{ m}^2$ $w_1 = -5.483 \times 10^8 \text{ m}^2$ $w_2 = -4.384 \times 10^8 \text{ m}^2$ $w_3 = -4.100 \times 10^8 \text{ m}^2$ $w_4 = -6.332 \times 10^8 \text{ m}^2$ $w_5 = -4.815 \times 10^8 \text{ m}^2$

Pruning the basis – Just one basis function captures ~20% of the variance Three functions capture ~50% of the variance

approximate form

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Pruning the basis – Just one basis function captures ~20% of the variance Three functions capture ~50% of the variance Approximate form for subgrid scale momentum transport

$$\mathbf{\hat{S}}_{\mathbf{u}}^{BT} \approx \kappa_{BT} \overline{\nabla} \cdot \begin{pmatrix} \zeta^2 - \zeta D & \zeta \tilde{D} \\ \zeta \tilde{D} & \zeta^2 + \zeta D \end{pmatrix}.$$

$$\kappa_{BT} \approx \Sigma_i w_i = -4.87 \times 10^8 \text{ m}^2$$

approximate form

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Pruning the basis -

Just one basis function captures $\sim 20\%$ of the variance Three functions capture $\sim 50\%$ of the variance Approximate form for subgrid scale momentum transport

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$$\kappa_{BT} \approx \Sigma_i w_i = -4.87 \times 10^8 \text{ m}^2$$
Connect to the baroclinic form
$$\mathbf{\hat{S}}_{\mathbf{u}}^{BC} \approx \kappa_{BC} \overline{\nabla} \cdot \begin{pmatrix} -\zeta D & \zeta \tilde{D} \\ \zeta \tilde{D} & \zeta D \end{pmatrix} + \mathbf{I} \frac{1}{2} \kappa_{BC} \overline{\nabla} (\zeta^2 + D^2 + \tilde{D}^2),$$

Similarly for temperature,

$$\hat{S}_T = \kappa_T \overline{
abla} \cdot egin{pmatrix} -\overline{u}_y \overline{u}_z - \overline{
u}_y \overline{
u}_z \ \overline{u}_z \overline{u}_z + \overline{
u}_x \overline{
u}_z \end{pmatrix}.$$

ML in Weather Forecasting

FourCastNet: Data-driven Weather Forecasting

FOURCASTNET: A GLOBAL DATA-DRIVEN HIGH-RESOLUTION WEATHER MODEL USING ADAPTIVE FOURIER NEURAL OPERATORS

A PREPRINT **NVIDIA** Jaideep Pathak Shashank Subramanian Peter Harrington Sanjeev Raja University of Michigan NVIDIA Corporation Lawrence Berkeley Lawrence Berkeley Santa Clara, CA 95051 National Laboratory National Laboratory Ann Arbor, MI 48109 Berkeley, CA 94720 Berkeley, CA 94720 Ashesh Chattopadhyay Morteza Mardani Thorsten Kurth Rice University NVIDIA Corporation NVIDIA Corporation Houston, TX 77005 Santa Clara, CA 95051 Santa Clara, CA 95051 David Hall Zongyi Li Kamyar Azizzadenesheli NVIDIA Corporation California Institute of Technology Purdue University Santa Clara, CA 95051 Pasadena, CA 91125 West Lafavette, IN 47907 NVIDIA Corporation Santa Clara, CA 95051 Pedram Hassanzadeh Karthik Kashinath Animashree Anandkumar Rice University NVIDIA Corporation California Institute of Technology Houston, TX 77005 Santa Clara, CA 95051 Pasadena, CA 91125 NVIDIA Corporation Santa Clara, CA 95051

A complex semi-supervised ML model built using Fourier Neural Operators and Vision Transformer

FourCastNet: Data-driven Weather Forecasting

- Pre-training stage | Fine-tuning stage | Inference
- Trained on 6-hourly ERA5 reanalysis on pressure levels from 1979-2015. 0.25° resolution. 2016-17 validation data. 2018-2020 testing data.
- A separate AFNO model to forecast total precipitation: an additional convolutional layer and ReLU() activation to enforce non-negative outputs
- Model trained with cosine learning rates for a total of 130 epochs

Vertical Level	Variables
Surface	$U_{10}, V_{10}, T_{2m}, sp, mslp$
1000hPa	U, V, Z
850 hPa	T, U, V, Z, RH
500hPa	T, U, V, Z, RH
50hPa	Z
Integrated	TCWV

FourCastNet's Model Architecture

FourCastNet provides impressive Hurricane and AR forecasts over short lead times

Small-scales captured better than by CNNs

FourCastNet outperforms Weyn et al.'s DLWP model

ACC: Anomaly correlation coefficient. Higher ACC means higher skill

On 0-48 lead times, FourCastNet provides better total precipitation forecasts than IFS

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Brief outline of Weyn et al.'s DLWP

- Weyn et al (2020)'s Deep Learning Weather Prediction model uses convolutions (FCNN) on a cubed-sphere grid to predict weather on short and even sub-seasonal timescales. It is based on the U-Net architecture
- Trained on 2° resolution ERA5 data and four prognostic variables: 500 hPa geopotential height, 1000 hPa geopotential height, 300-700 hPa geopotential thickness, and 2m surface temperature.
- Improved to have 6 predicted variables and produce a 320-ensemble S2S forecast

FourCastNet outperforms Weyn et al.'s DLWP model

ACC: Anomaly correlation coefficient. Higher ACC means higher skill

On 0-48 lead times, FourCastNet provides better total precipitation forecasts than IFS

A factor 45,000 speedup and 12,000x lower energy footprint in generating forecasts using a larger ensemble size. 100 ensemble size vs traditional 50 used by ECMWF's IFS.

Scalable: model memory requirements ~10 GB for a batch size=1

Forecasts using the pre-trained model can be generated using a laptop

Additional Resources for Learning ML

BOOKS

DeepLearningAl

@Deeplearningai 228K subscribers 336 videos

Welcome to the official DeepLearning.AI YouTube channel! Here you can fi... >

3Blue1Brown ● @3blue1brown 5.25M subscribers 129 videos 3Blue1Brown, by Grant Sanderson, is some combination of math and enter... >

Patrick Loeber .

@patloeber 240K subscribers 204 videos
Free Python and Machine Learning Tutorials! >

Two Minute Papers 👁

@TwoMinutePapers 1.46M subscribers 794 videos

What a time to be alive! >

Jeremy Howard

@howardjeremyp 79.8K subscribers 182 videos

Deep learning is transforming the world. We are maki

YouTube

Auto-Encoding Variational Bayes

Generative Adversarial Nets

Diederik P. Kingma Machine Learning Group Universiteit van Amsterdam dpkingma@gmail.com

Max Welling Machine Learning Group Universiteit van Amsterdam welling.max@gmail.com Ian J. Goodfellow, Jean Pouget-Abadie, Mehdi Mirza, Bing Xu, David Warde-Farley, Sharill Ozairt Aaron Courville Vechus Bangiat

> **Unpaired Image-to-Image Translation** using Cycle-Consistent Adversarial Networks

Jun-Yan Zhu* Alexei A. Efros Taesung Park* Phillip Isola Berkeley AI Research (BAIR) laboratory, UC Berkeley

Robust flight navigation out of distribution with liquid neural networks

MAKRAM CHAHINE (10), RAMIN HASANI (10), PATRICK KAO (10), AARON RAY (10), RYAN SHUBERT, MATHIAS LECHNER (10), ALEXANDER AMINI (10), AND DANIELA RUS (10)

Data-driven discovery of partial differential equations

FOURIER NEURAL OPERATOR FOR PARAMETRIC PARTIAL DIFFERENTIAL EQUATIONS

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Attention Is All You Need

A shich Vacwan Jakob Uszkoreit **AN IMAGE IS WORTH 16x16 WORDS:** TRANSFORMERS FOR IMAGE RECOGNITION AT SCALE

> Alexe **Temporal Fusion Transformers** Xia for Interpretable Multi-horizon Time Series Forecasting

> > Bryan Lim^{a,1,*}, Sercan Ö. Arık^b, Nicolas Loeff^b, Tomas Pfister^b

^aUniversity of Oxford, UK ^bGoogle Cloud AI, USA

Data-driven Model Parameterizations

Using ANNs to create global emulators for gravity waves using parameterizationd or nonlocal high resolution climate data, and testing on new climate scenarios

Equation Discovery using ML

Relevance Vector Machines to obtain closed-form solutions for subgrid scale momentum and temperature fluxes for barotropic and baroclinic models that capture a bulk of the subgrid scale variance

ML in Weather Forecasting

Novel architectures using vision transformer + adaptive Fourier neural operators, and UNet CNN architecture to forecast surface weather with commendable skill

Thank You! I hope this helped. :)

Feel free to reach out: ag4680@stanford.edu

Source: Luccioni et al., 2022; Strubell et al., 2019 | Chart: 2023 Al Index Report