

# *Studying the Longitudinal Spin Structure of the Proton at the EIC*

*Christine A. Aidala  
University of Michigan*

*International Workshop on Probing Hadron Structure  
at the Electron-Ion Collider  
ICTS, Bangalore, India  
February 5, 2024*



# *Studying the Longitudinal Spin Structure of the Proton at the EIC*

*\*EIC Physics with Longitudinally  
Polarized Hadron Beams*

*Christine A. Aidala  
University of Michigan*

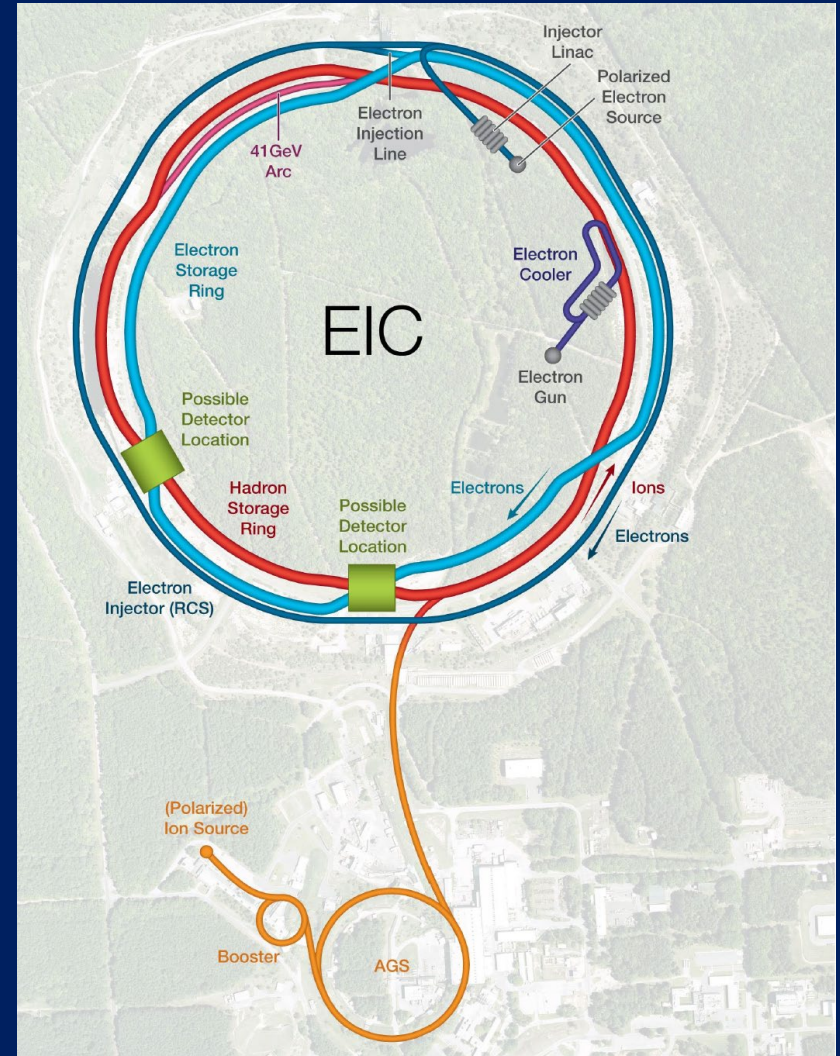
*International Workshop on Probing Hadron Structure  
at the Electron-Ion Collider  
ICTS, Bangalore, India  
February 5, 2024*



# The future Electron-Ion Collider

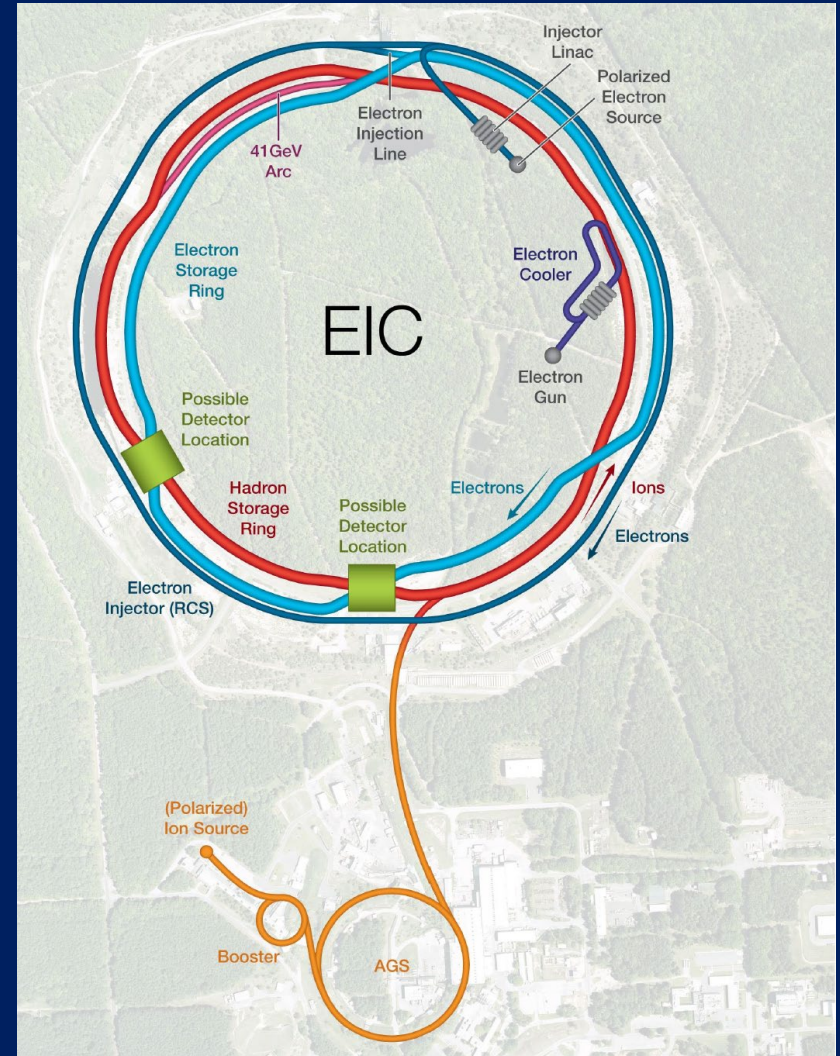
Key science questions:

- *How does a nucleon acquire mass?*
- *How does the spin of the nucleon arise from its elementary quark and gluon constituents?*
- *What are the emergent properties of dense systems of gluons?*



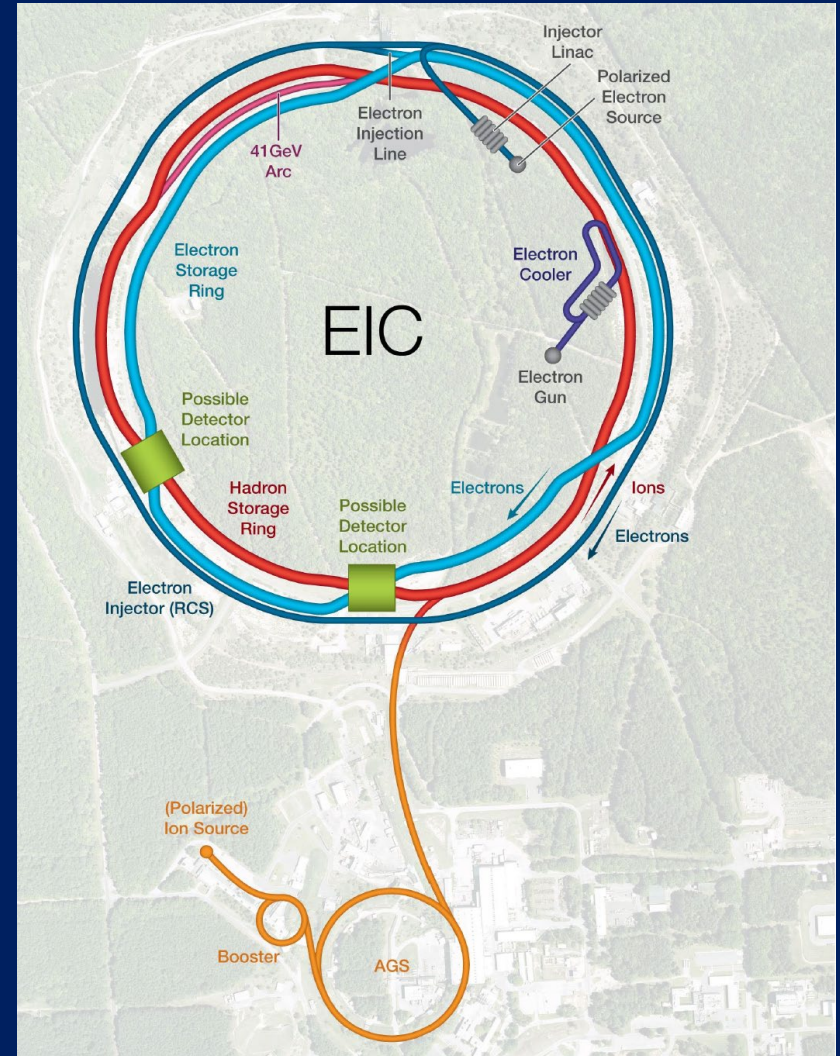
# The future Electron-Ion Collider

- Highly polarized electron (~70%) and proton (~70%) beams
- Ion beams from deuterons to heavy nuclei such as gold, lead, or uranium
- Variable  $e + p$  center-of-mass energies from 29-140 GeV
- $e + p$  luminosity  $10^{33} - 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$



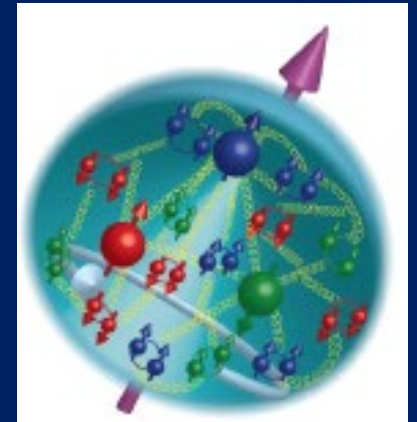
# The future Electron-Ion Collider

- Highly polarized electron (~70%) and proton (~70%) beams
- Ion beams from deuterons to heavy nuclei such as gold, lead, or uranium
  - Including polarized  $^3\text{He}$  and possibilities for polarized deuterons!
- Variable  $e + p$  center-of-mass energies from 29-140 GeV
- $e + p$  luminosity  $10^{33} - 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$



# *Proton helicity structure*

Can decompose total proton spin of  $\frac{1}{2}$  into contributions from quark spin, gluon spin, and quark and gluon orbital angular momentum (OAM)



Jaffe-Manohar spin decomposition

$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma(\mu^2) + \Delta G(\mu^2) + L_Q(\mu^2) + L_G(\mu^2)$$

$$\Delta\Sigma(\mu^2) = \int_0^1 dx \Delta\Sigma(x, \mu^2)$$

$$\Delta G(\mu^2) = \int_0^1 dx \Delta g(x, \mu^2)$$

NPB337, 509 (1990)

# *What have we already learned about proton helicity structure?*

- $\Delta\Sigma(\mu^2 = 10 \text{ GeV}^2) \approx 0.35$ 
  - I.e. total quark spin contributes  $\sim 35\%$  of proton spin
- $\Delta G(\mu^2 = 10 \text{ GeV}^2) \approx 0.2$ , still with large uncertainties

So there must be a significant contribution from orbital angular momentum, which is challenging to measure . . .



# *What have we already learned about proton helicity structure?*

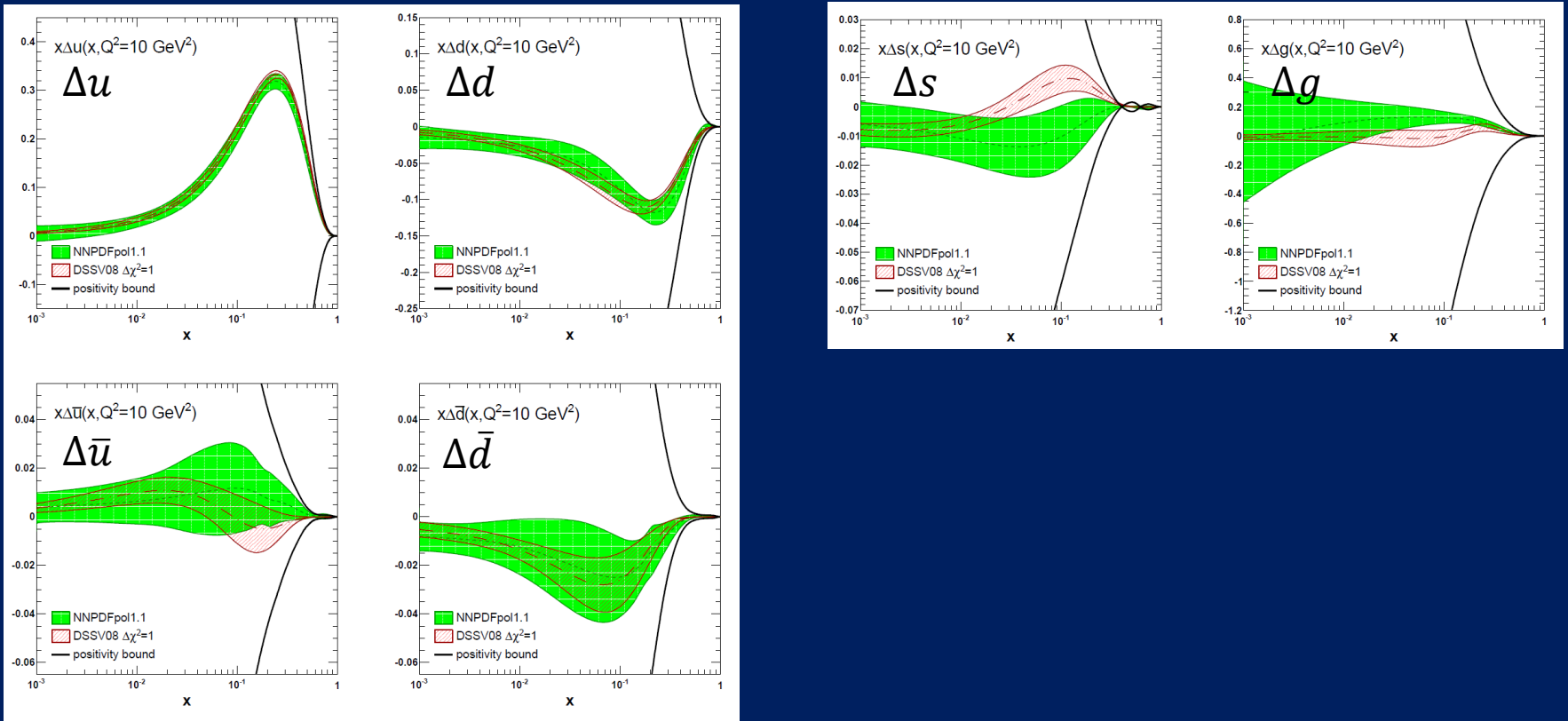
Breaking down  $\Delta\Sigma$ :

- $\Delta u > 0$
- $\Delta d < 0$
- Light quark sea shows evidence of flavor asymmetry
  - $\Delta\bar{u}(x) \neq \Delta\bar{d}(x)$
- Possible contribution from  $\Delta s(x)$  remains highly uncertain





# Helicity PDF extractions: NNPDFpol1.1.



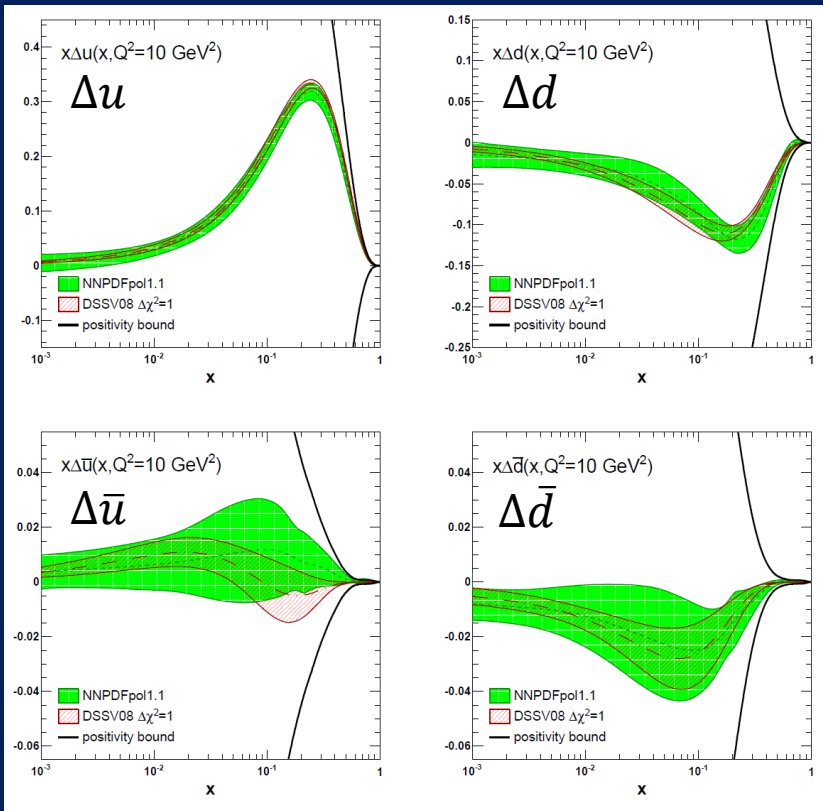
Note different y-axis scales!

NPB887, 276 (2014)

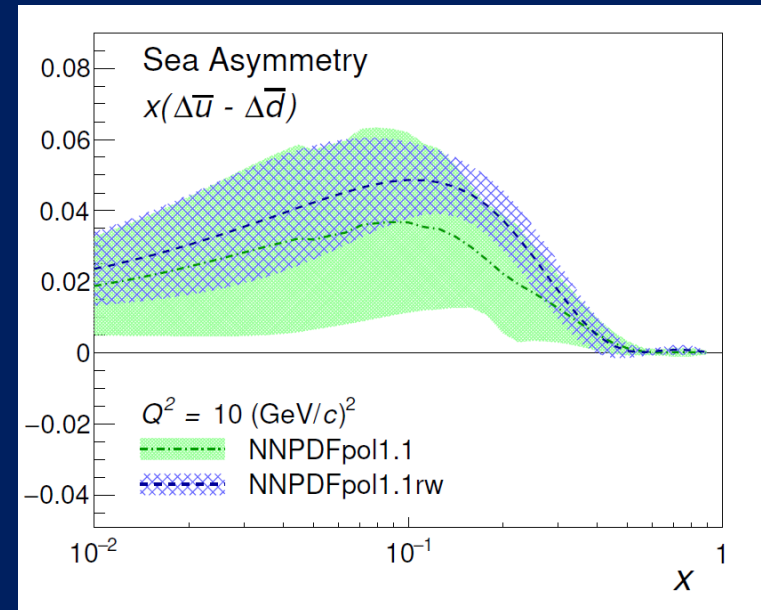


# Helicity PDF extractions: NNPDFpol1.1.

PRD102, 094018 (2020)



Note different y-axis scales!

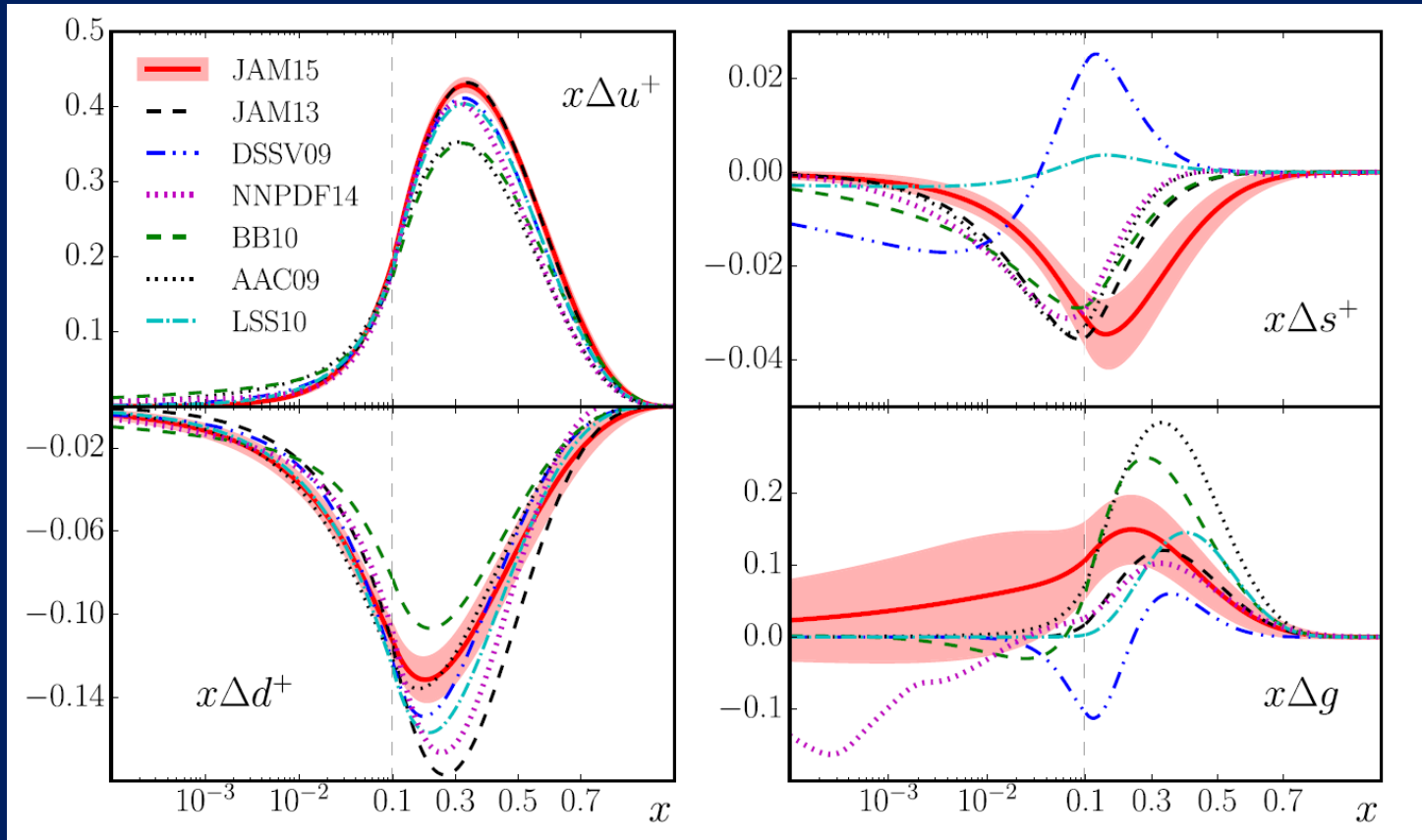


NNPDFpol1.1  $\Delta\bar{u} - \Delta\bar{d}$   
extraction and reweighted  
with 2013 W boson  $A_L$   
measurement from STAR

NPB887, 276 (2014)



# Helicity PDF extractions: JAM15

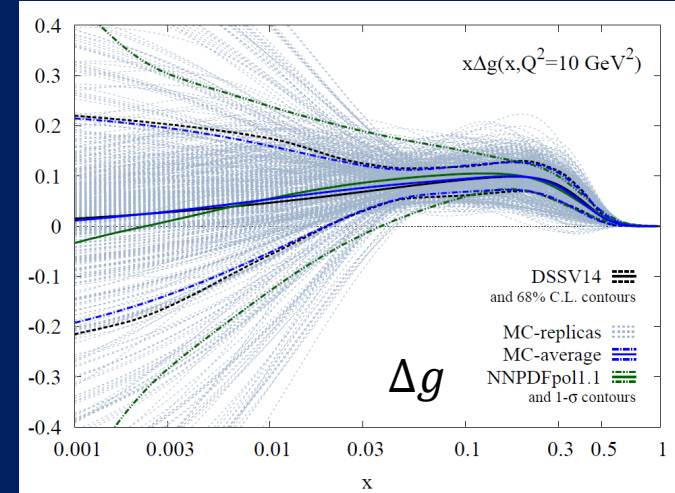
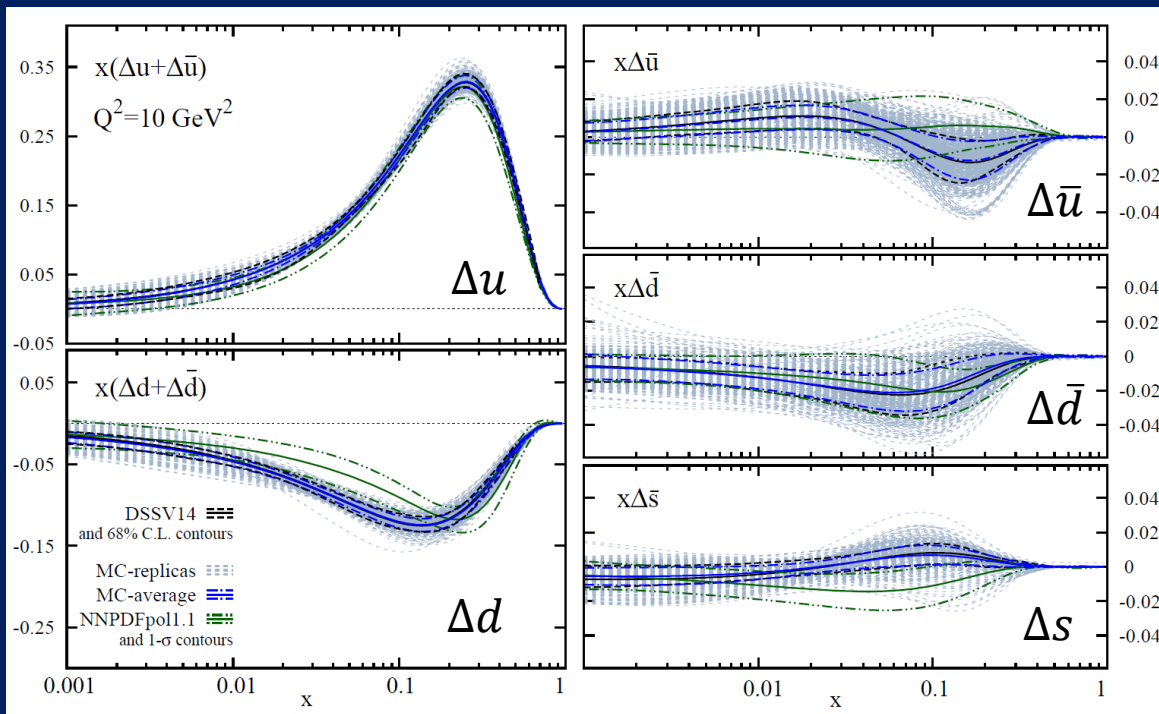


Note different y-axis scales!

PRD93, 074005 (2016)



# Helicity PDF extractions: DSSV14 with Monte Carlo sampling



Note different y-axis scales!

PRD100, 114027 (2019)  
DSSV14: PRL113, 012001 (2014)

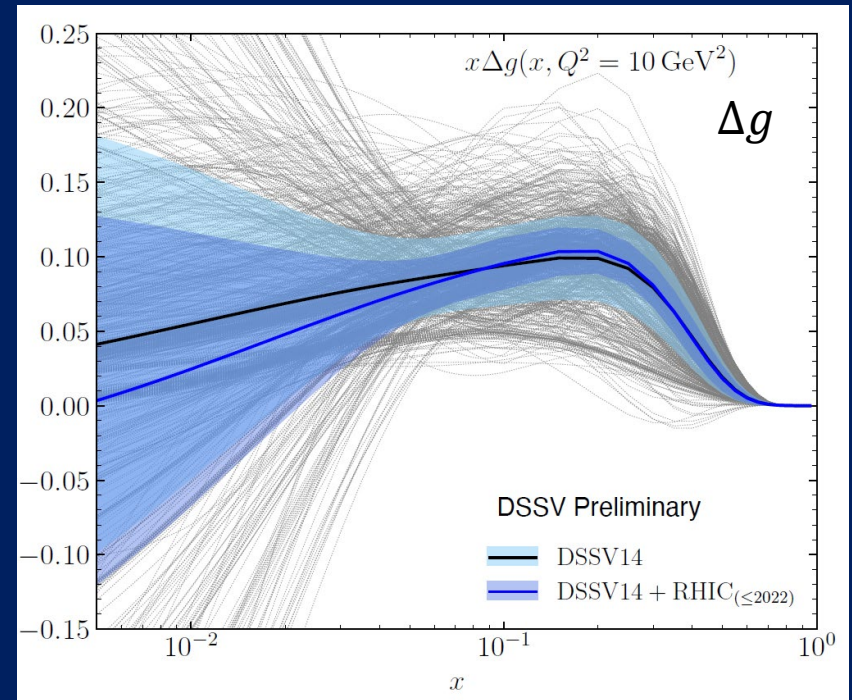
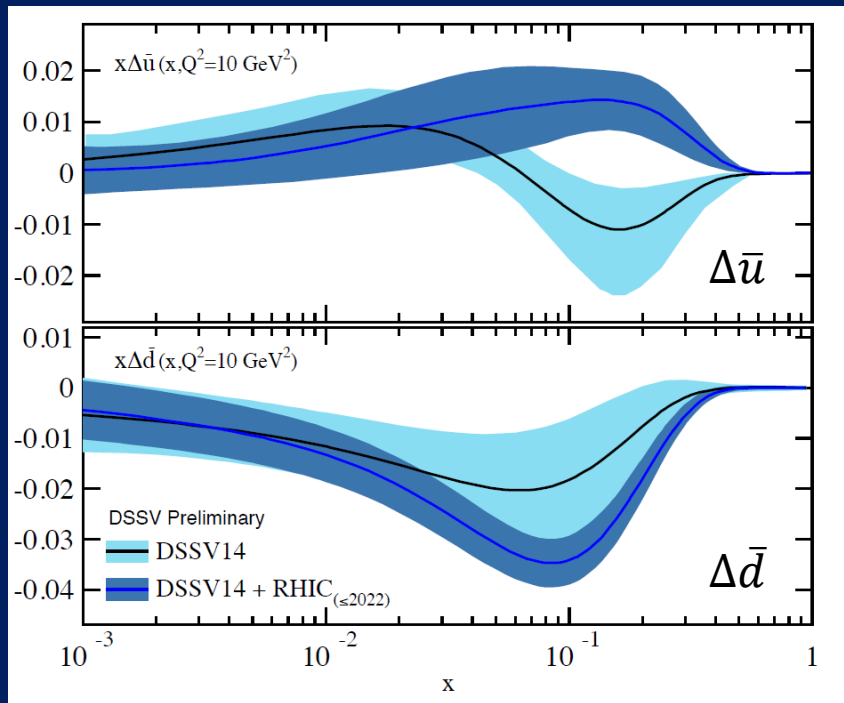


# Latest DSSV extraction of light sea and gluon

RHIC Cold QCD White Paper - arXiv:2302.00605

DSSV14: PRL113, 012001 (2014)

Note different y-axis scales!

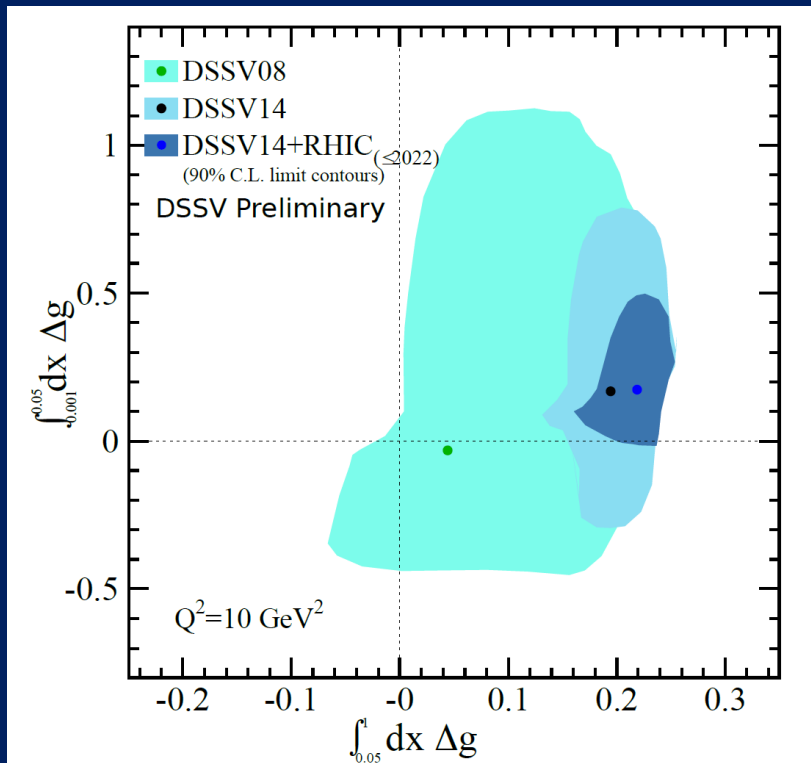


- Fit includes RHIC data released as of 2022:  $W$  boson  $A_L$  impacting light sea and jet, dijet, and pion  $A_{LL}$  impacting gluon distribution
- Asymmetry between  $\Delta\bar{u}(x)$  and  $\Delta\bar{d}(x)$  became more significant



# Could contributions from low-momentum gluons be large?

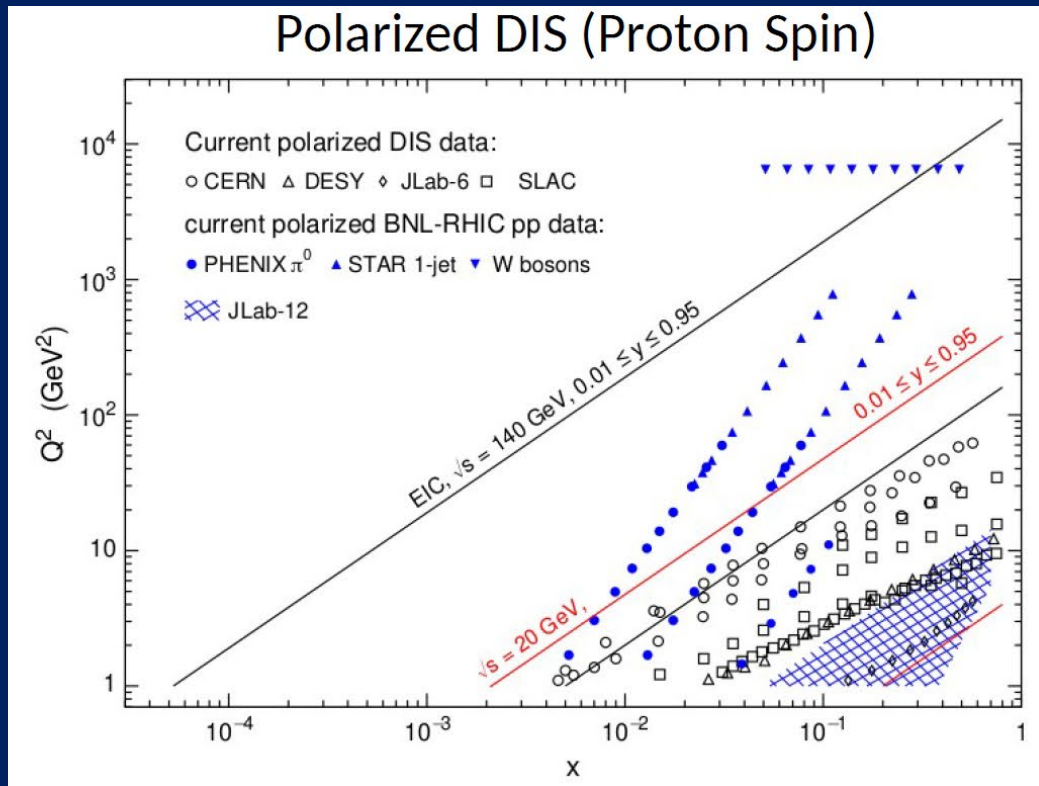
RHIC Cold QCD White Paper - arXiv:2302.00605



Note different horizontal and vertical axis scales!

- Inclusion of RHIC data released as of 2022 (jets, dijets, and pions) has constrained truncated first moment of  $\Delta g(x)$  from  $0.05 < x < 1$  relatively well
- Constraints for  $0.001 < x < 0.05$  improved, but still large uncertainties
- $\Delta g(x)$  remains  $\sim$ unconstrained for  $x < 0.001$

# Complementarity of EIC with ongoing and previous polarized experiments



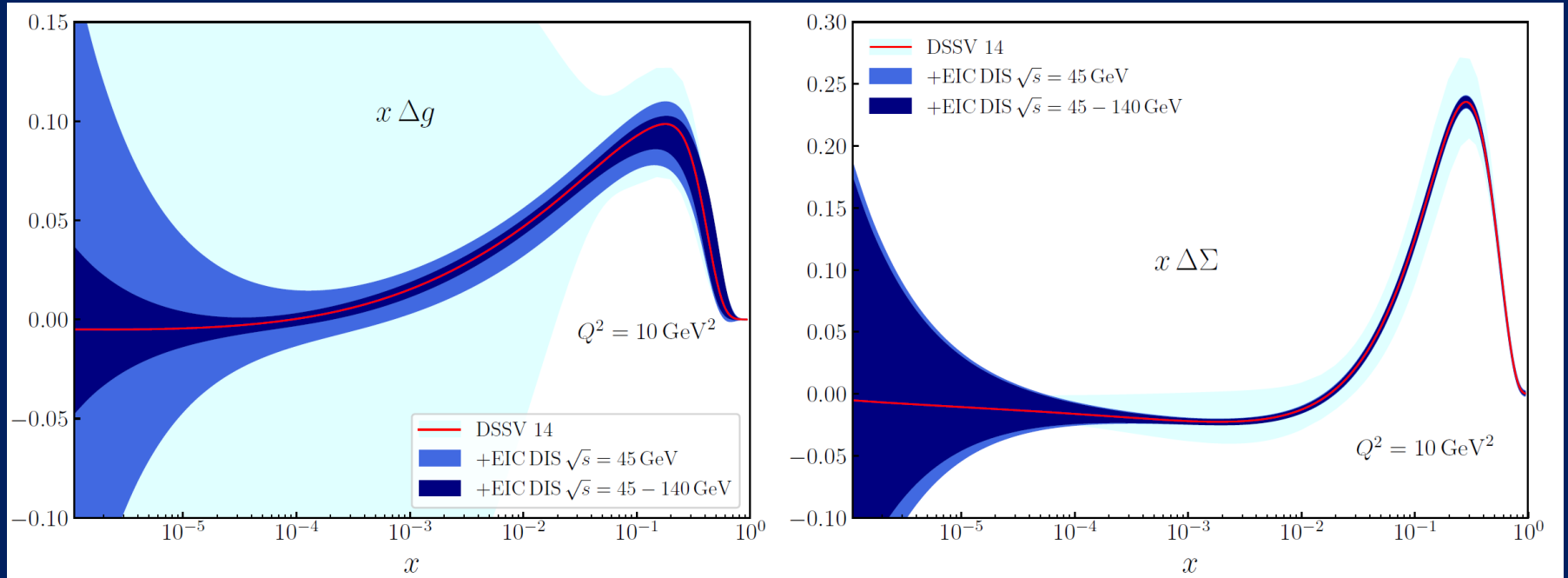
- EIC will greatly expand kinematic coverage for polarized measurements
- EIC at high energy will be critical to reach down to  $x \sim 10^{-4}$

# *EIC: Improving the gluon and quark singlet helicity distributions*

PRD102, 094018 (2020)

DSSV14: PRL113, 012001 (2014)

Note different y-axis scales!



Impact of projected EIC  $A_{LL}$  data on the gluon helicity and quark singlet helicity distributions, relative to DSSV14 global analysis

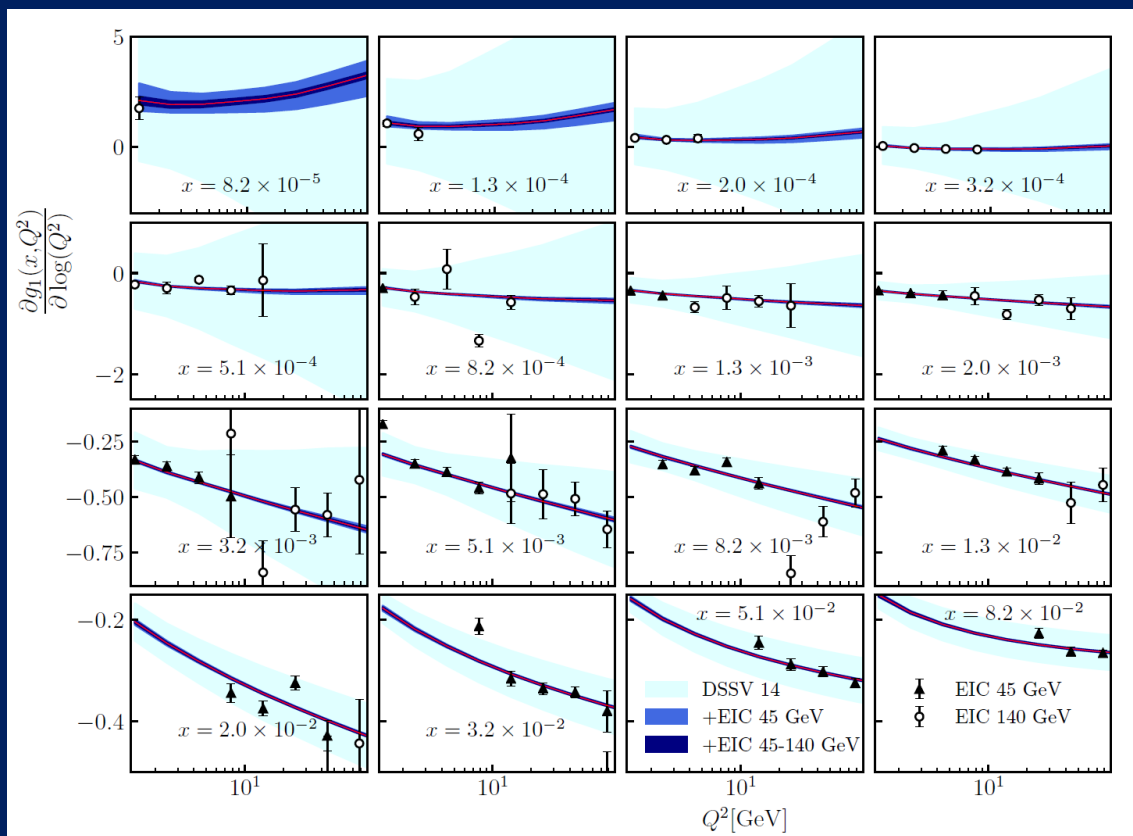




# *EIC: Accessing gluon helicity through scaling violations of $g_1$*

PRD102, 094018 (2020)

DSSV14: PRL113, 012001 (2014)



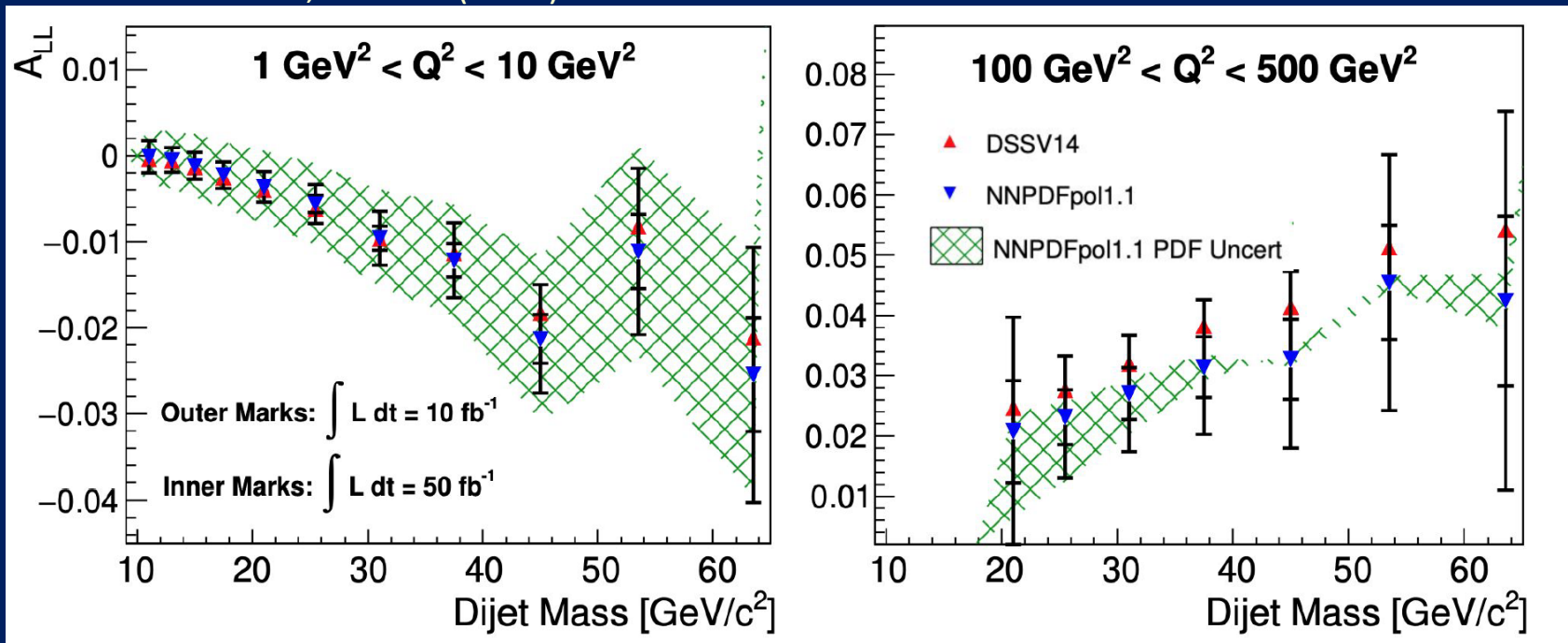
- Large kinematic coverage across  $x$  and  $Q^2$  at EIC
  - Scaling violations of polarized structure function  $g_1$  will be most powerful way to access  $\Delta g$
  - Inclusive DIS measurements

EIC pseudodata for scaling of  $g_1$  with  $Q^2$



# *EIC: Accessing gluon helicity through double-longitudinal asymmetry for dijets*

PRD101, 072003 (2020)



EIC pseudodata for dijets from QCD Compton scattering and photon-gluon fusion.  
Complementary measurement to inclusive polarized DIS structure function  $g_1$

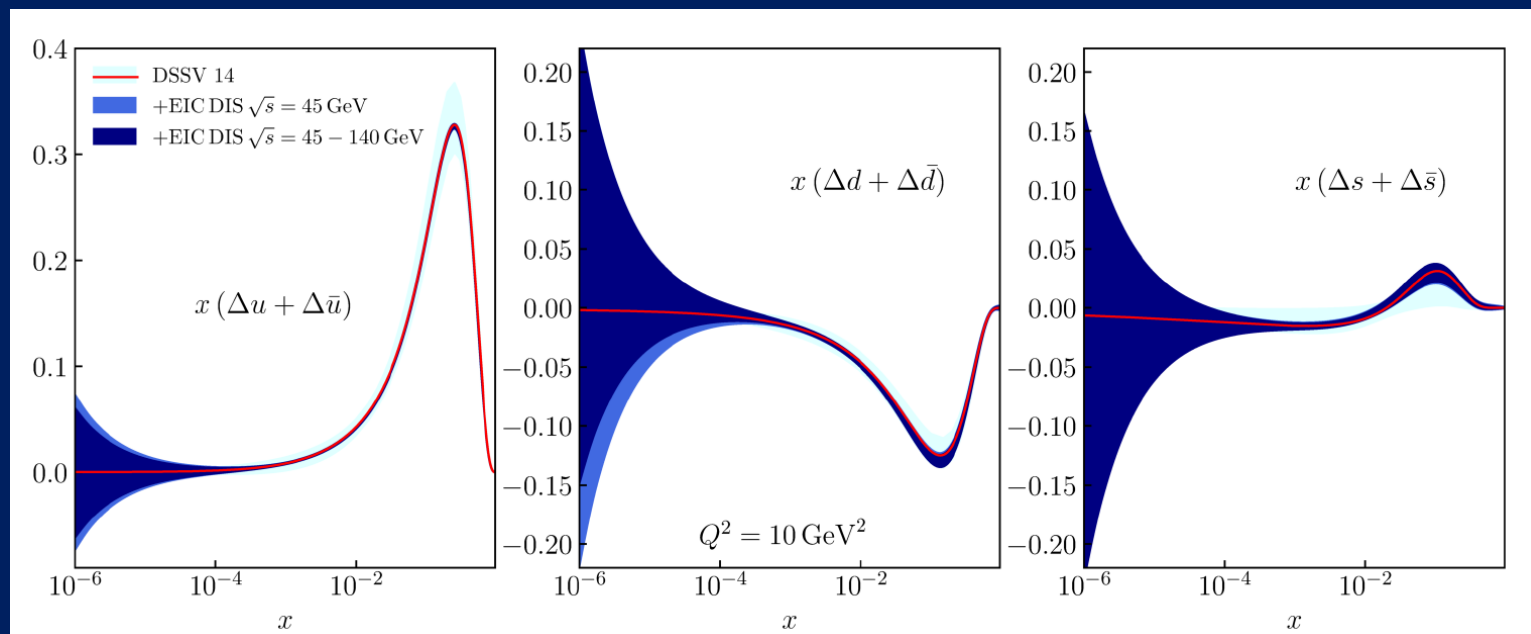


# *EIC: Improving the total quark helicity distributions*

PRD102, 094018 (2020)

DSSV14: PRL113, 012001 (2014)

Note different y-axis scales!



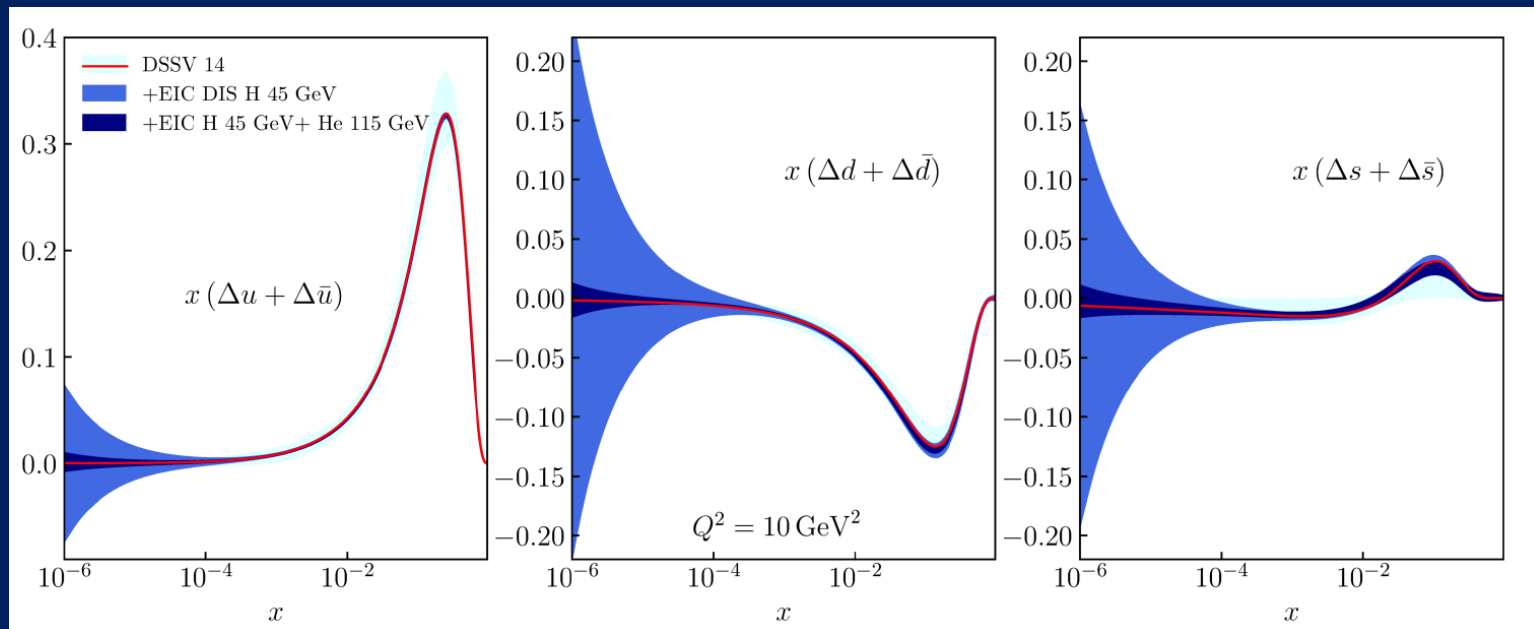
Impact of projected EIC  $A_{LL}$  data on the total quark helicity distributions, relative to DSSV14 global analysis



# *EIC: Improving the total quark helicity distributions, including $^3\text{He}$ data*

PRD102, 094018 (2020)

DSSV14: PRL113, 012001 (2014)



Impact on total quark helicity distributions using inclusive DIS measurements on polarized  $^3\text{He}$

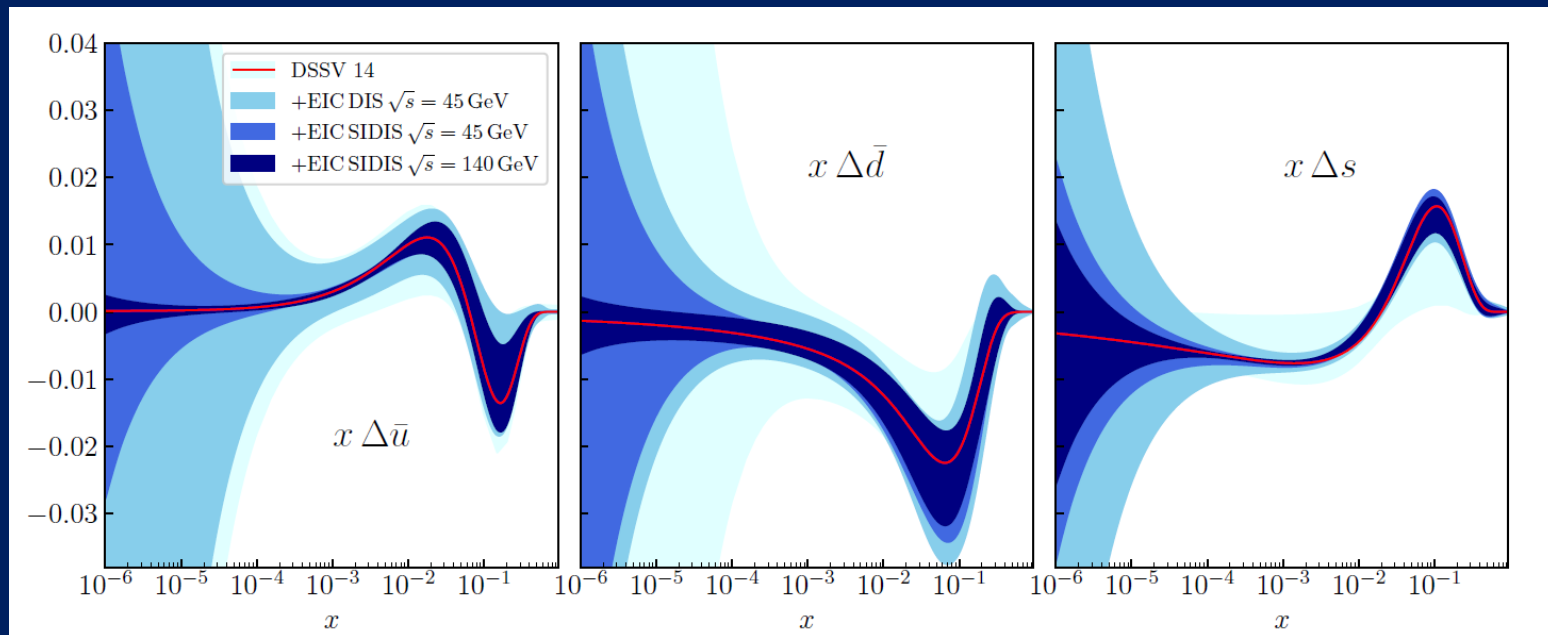


# *EIC: Improving the flavor-separated helicity distributions of the proton sea through SIDIS*

PRD102, 094018 (2020)

DSSV14: PRL113, 012001 (2014)

Note different y-axis scale  
w.r.t. plots on previous slide!



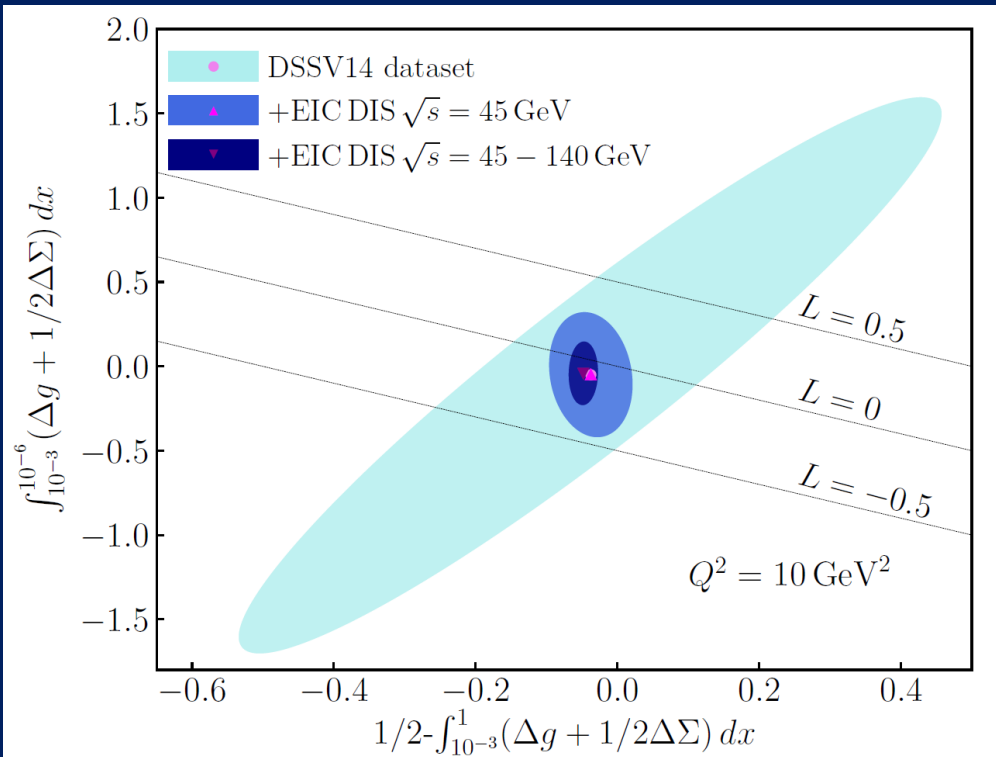
Access flavor through SIDIS measurements of identified charged pions and kaons. Current treatment of strangeness assumes  $\Delta s = \Delta \bar{s}$  and incorporates constraints from hyperon  $\beta$  decay. In the future could use positive and negative kaons to separate  $\Delta s$  and  $\Delta \bar{s}$ .



# *EIC: Spin sum rule, low- $x$ contributions, and OAM*

PRD102, 094018 (2020)

DSSV14: PRL113, 012001 (2014)



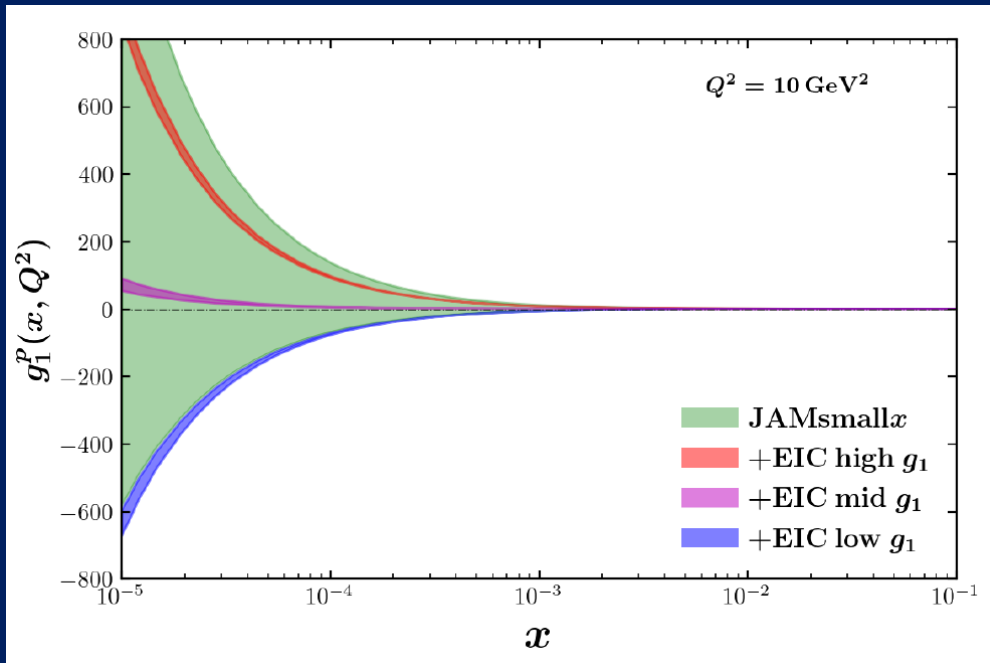
- Current polarized data cover  $x > \sim 10^{-3}$
- Could there be significant spin contributions for  $10^{-6} < x < 10^{-3}$ ?
- EIC data for  $\Delta g$  at low  $x$  will significantly improve uncertainty on the total quark and gluon contributions to proton spin
- Remainder must be orbital angular momentum!

Note different horizontal and vertical axis scales!



# *EIC: Pinning down $g_1^p$ at low $x$*

PRD108, 114007 (2023)



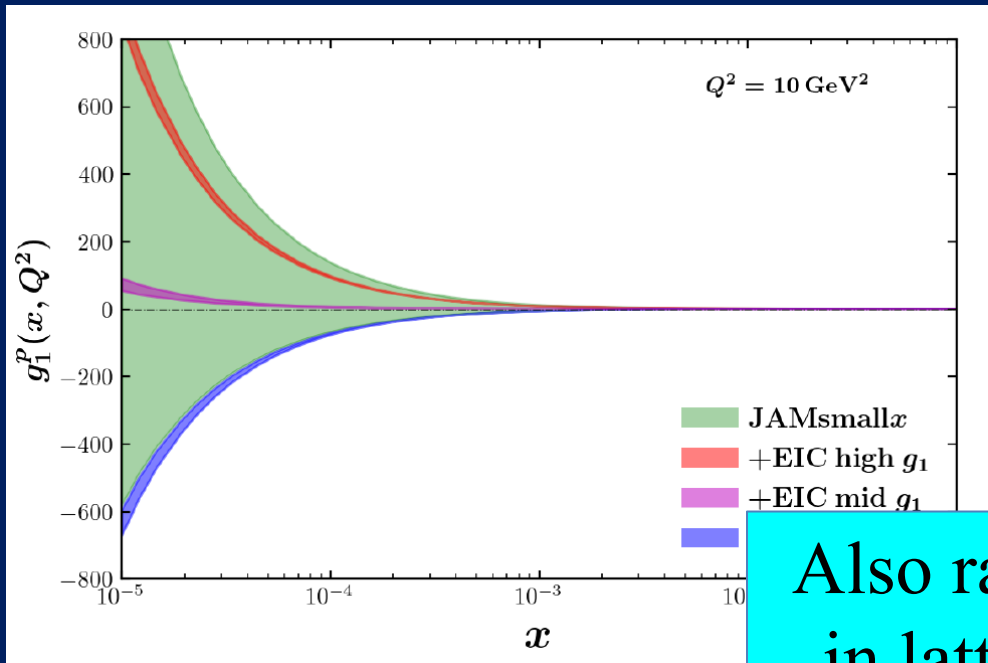
Impact of EIC pseudodata on  $g_1^p$  at low  $x$ ,  
assuming three different replicas

- Recent series of papers from Kovchegov and collaborators on small- $x$  helicity evolution has led to new phenomenology considering possible large spin contributions from  $x < \sim 10^{-4}$



# EIC: Pinning down $g_1^p$ at low $x$

PRD108, 114007 (2023)



Impact of EIC pseudodata on  $g_1^p$  at low  $x$  assuming three different replicas

- Recent series of papers from Kovchegov and collaborators on small- $x$  helicity evolution has led to new phenomenology

Also rapid theoretical progress in lattice QCD in calculating moments as well as  $x$  dependence of polarized PDFs!





# *Thinking more about polarized $^3\text{He}$ at the EIC*

- Polarized  $^3\text{He}$  can serve as a proxy for polarized neutrons
  - Already showed improvements in flavor separation from inclusive DIS measurements on  $^3\text{He}$
- We typically use isospin to map flavor-dependent distributions in the proton to those in the neutron
- As we reach the era of high-precision polarized data, might we be sensitive to differences in proton and neutron structure that break this isospin correspondence??



# *Thinking more about polarized $^3\text{He}$ at the EIC*

- Polarized  $^3\text{He}$  can serve as a proxy for polarized neutrons
  - Already showed improvements in flavor separation from inclusive DIS measurements on  $^3\text{He}$
- We typically use isospin to map flavor-dependent distributions in the proton to those in the neutron
- As we reach the era of high-precision polarized data, might we be sensitive to differences in proton and neutron structure that break this isospin correspondence??
- Mass difference between the proton and neutron only  $\sim 0.1\%$



# Thinking more about polarized $^3\text{He}$ at the EIC

- Polarized  $^3\text{He}$  can serve as a proxy for polarized neutrons
  - Already showed improvements in flavor separation from inclusive DIS measurements on  $^3\text{He}$
- We typically use isospin to map flavor-dependent distributions in the proton to those in the neutron
- As we reach the era of high-precision polarized data, might we be sensitive to differences in proton and neutron structure that break this isospin correspondence??
- Mass difference between the proton and neutron only  $\sim 0.1\%$
- But what about the quark *dynamics* in protons versus neutrons??  
Interplay between the helicity distributions and OAM??
  - Might naively expect different charges of the valence quarks in protons vs. neutrons to lead to different (and flavor-dependent) OAM

$$\text{Proton: } +\frac{2}{3}, +\frac{2}{3}, -\frac{1}{3}$$

$$\text{Neutron: } -\frac{1}{3}, -\frac{1}{3}, +\frac{2}{3}$$



# *Nuclear binding effects on helicity distributions*

- How does nuclear binding affect helicity distributions in nucleons?
- If want to understand potential isospin symmetry breaking in the polarized structure of protons vs. neutrons, will need to study and disentangle nuclear binding effects on the polarized structure of the neutron in  $^3\text{He}$

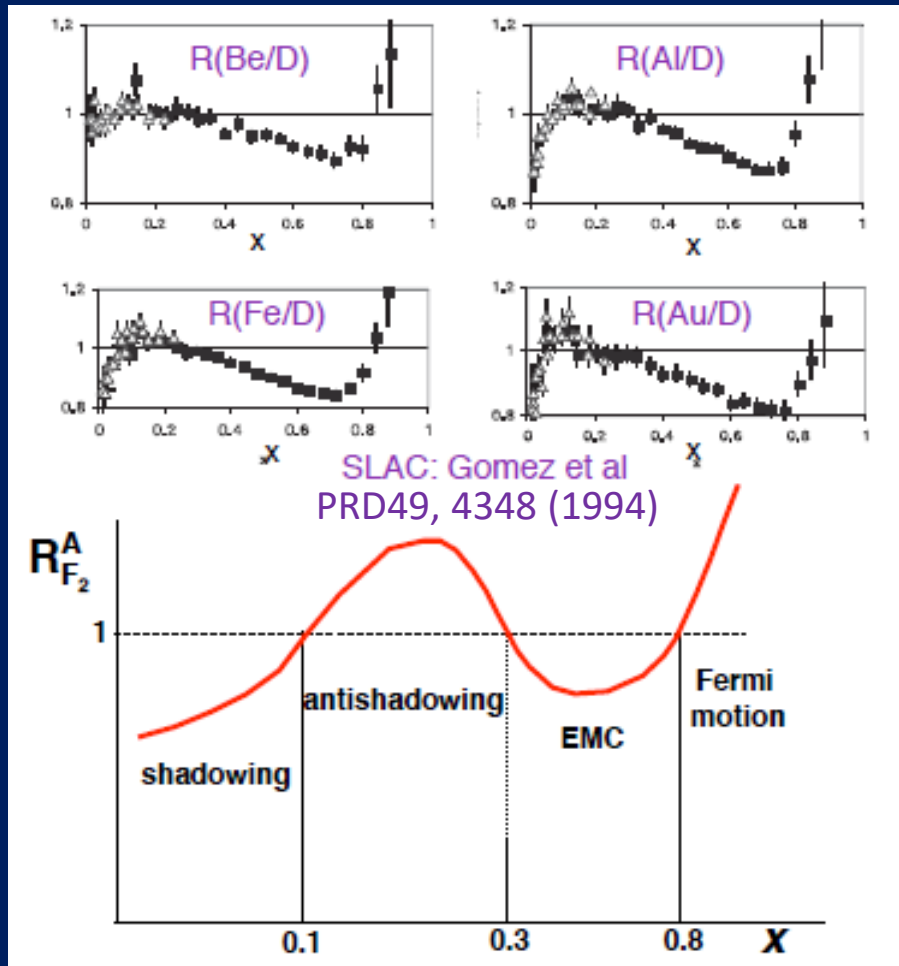


# *Nuclear binding effects on helicity distributions*

- How does nuclear binding affect helicity distributions in nucleons?
- If want to understand potential isospin symmetry breaking in the polarized structure of protons vs. neutrons, will need to study and disentangle nuclear binding effects on the polarized structure of the neutron in  $^3\text{He}$
- How does polarization affect the modification of nuclear PDFs w.r.t. the nucleon in different  $x$  ranges?
- Is there a polarized EMC effect in nuclei?
  - Some theoretical work has been done, see e.g. EIC Yellow Report (2021) and J.Phys.G 49, 03 (2022)
  - Polarized beams with nuclei heavier than  $^3\text{He}$  extremely challenging. Prospects for eventual fixed-target measurements with polarized heavier nuclei??



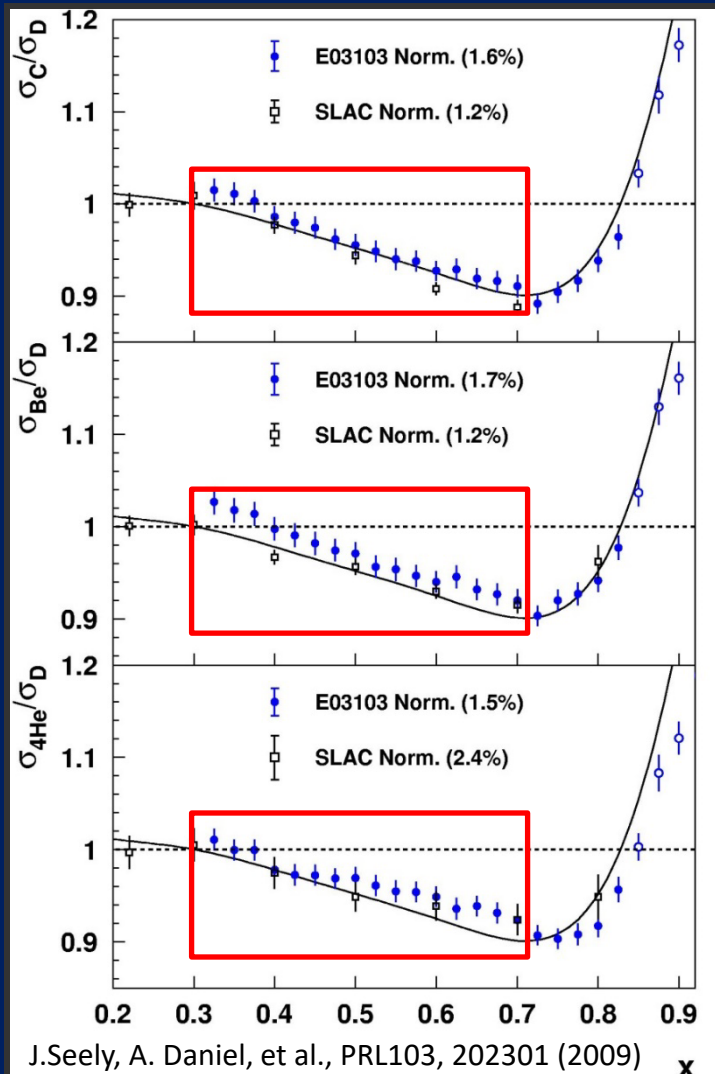
# Nuclear modification of PDFs and the EMC effect



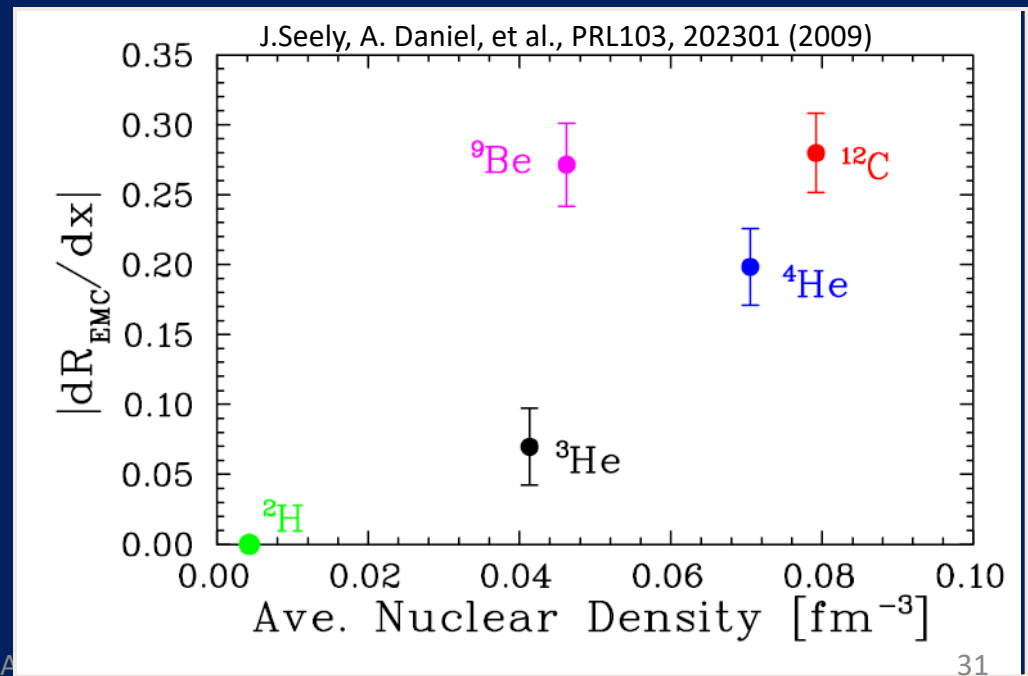
$$R_A \equiv \frac{1}{A} \frac{F_{2A}}{F_{2N}} \neq 1$$

- Ratio of cross section for  $e+A$  compared to scaled  $e+p$  collisions, shown vs. parton momentum fraction  $x$
- Regions of both enhancement and depletion—still lots to understand in detail!

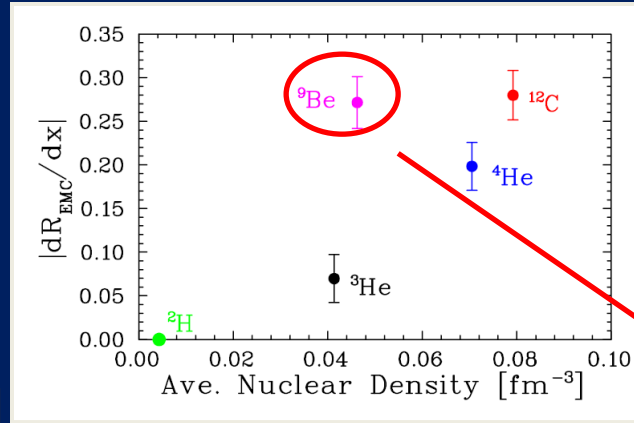
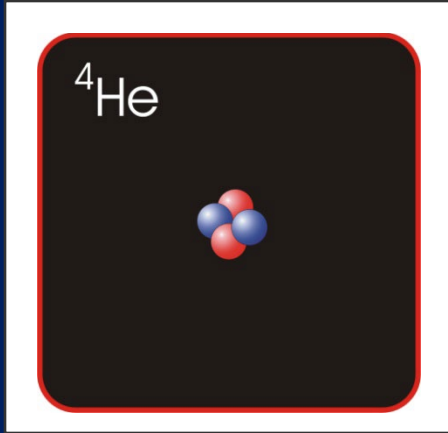
# Partonic momentum structure of nuclei: EMC effect and local density



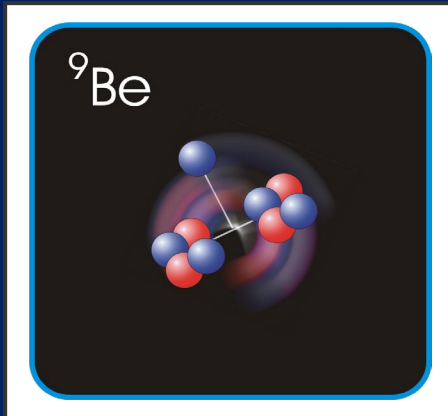
- Fit slope of ratios for  $0.3 < x < 0.7$ ; compare across nuclei
- EMC slope doesn't scale with  $A$  or with avg nuclear density...



# Partonic momentum structure of nuclei: EMC effect and local density

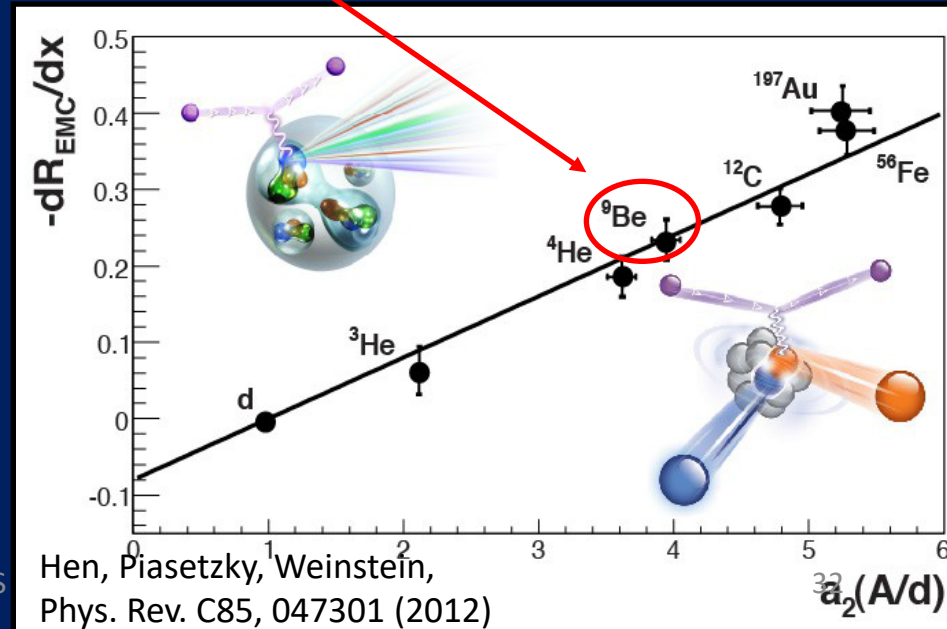


But appears to scale with local density!



Density determined from *ab initio* few-body calculation

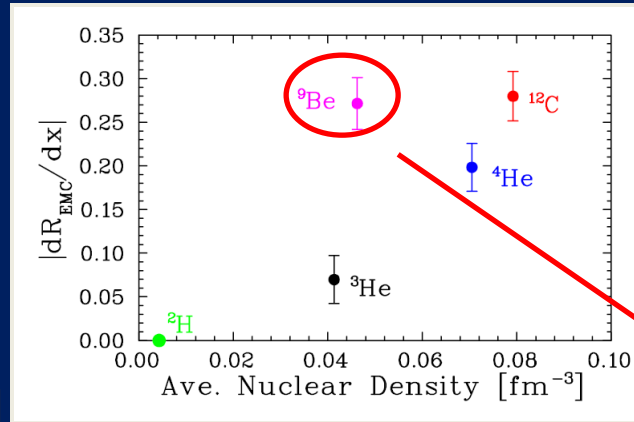
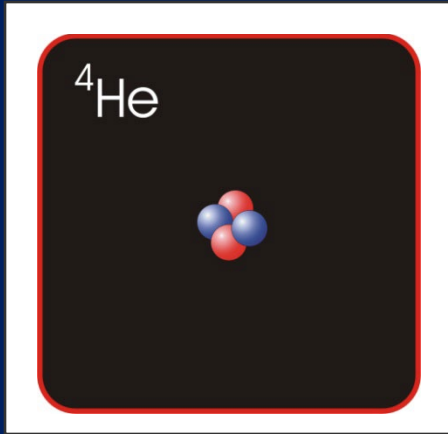
S.C. Pieper and R.B. Wiringa,  
*Ann. Rev. Nucl. Part. Sci* 51, 53 (2001)



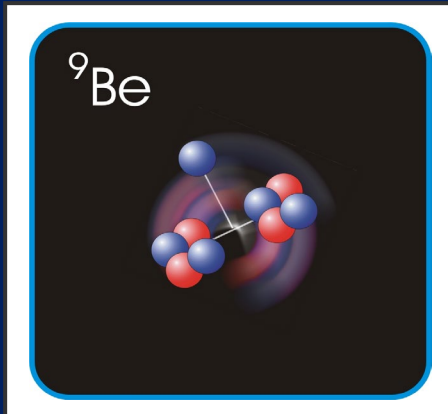
Hen, Piasezky, Weinstein,  
*Phys. Rev. C* 85, 047301 (2012)



# Partonic momentum structure of nuclei: EMC effect and local density



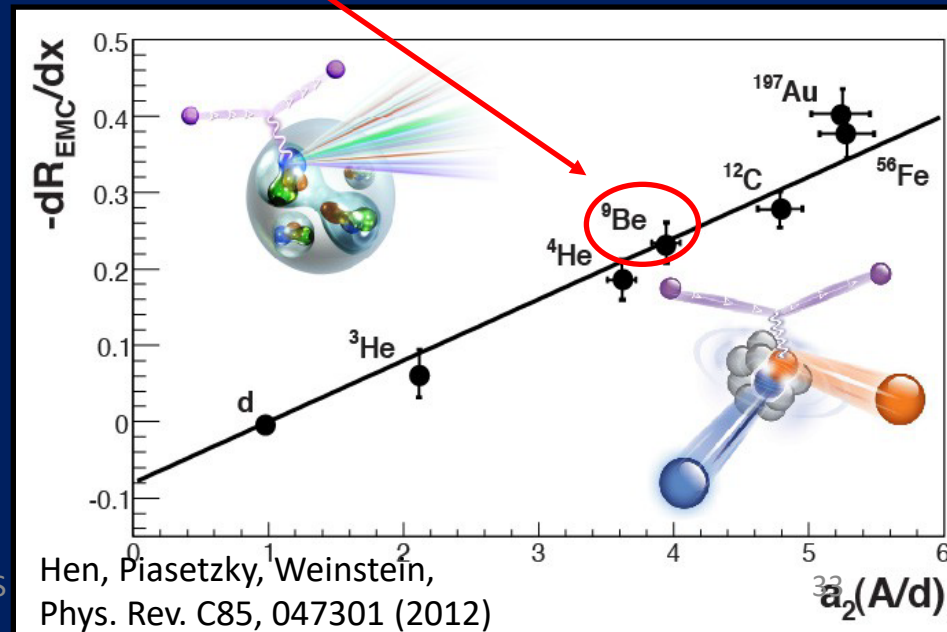
But appears to scale with local density!



Small but nonzero effect for  ${}^3\text{He}$

Density determined from *ab initio* few-body calculation

S.C. Pieper and R.B. Wiringa,  
*Ann. Rev. Nucl. Part. Sci* 51, 53 (2001)



Hen, Piasezky, Weinstein,  
*Phys. Rev. C* 85, 047301 (2012)

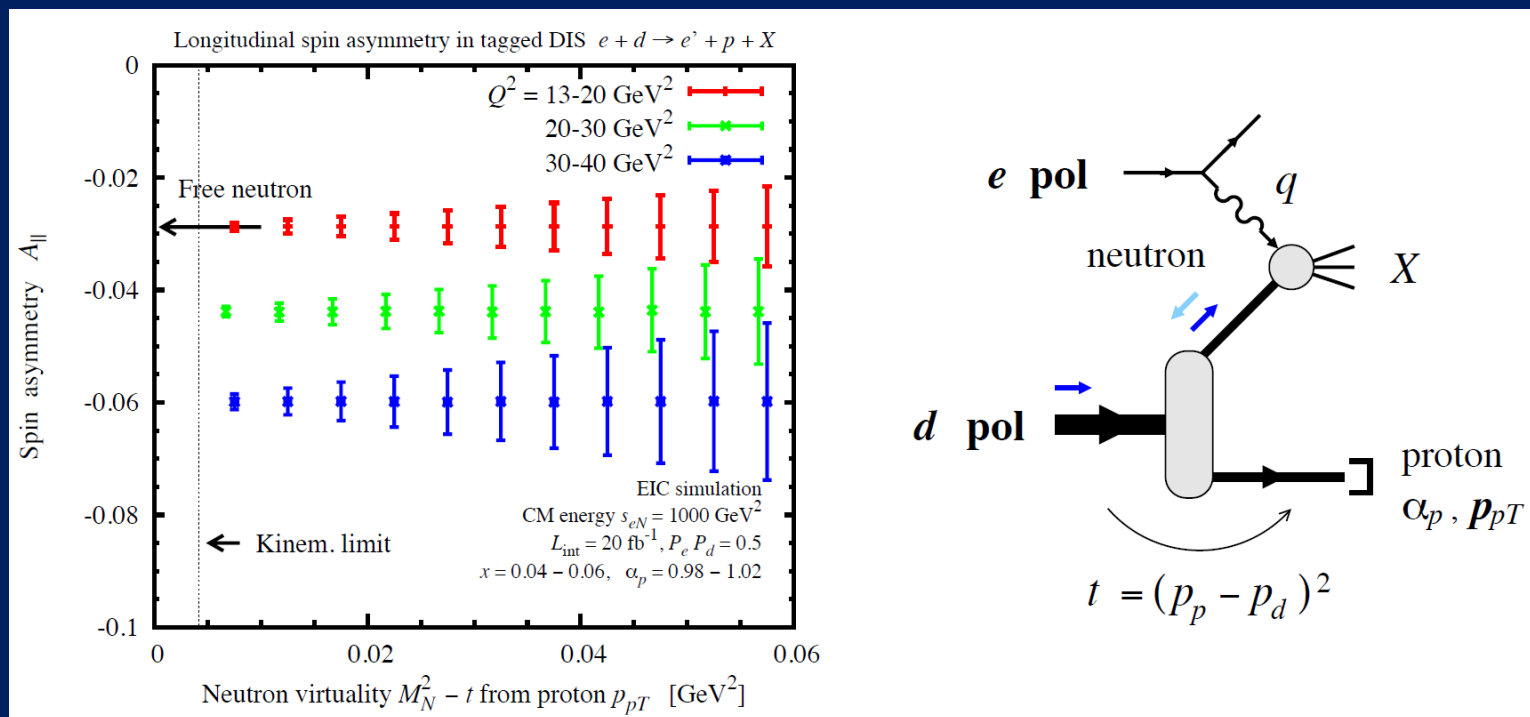
# *Possibility of polarized deuteron beams at the EIC*

- Polarized deuteron beams at the EIC much more challenging than polarized  $^3\text{He}$  but would offer a number of interesting opportunities
- Reduced nuclear effects compared to  $^3\text{He}$
- Spectator tagging would allow measurement on a nearly free neutron
- Deuterons also allow us to study *tensor polarization*
  - See discussion in EIC Yellow Report (2021)
- Much less work has been done on spin-1 systems, but there is increasing interest . . .



# EIC: Spectator tagging with deuteron beam

EIC Yellow Report, 2021



- Measure spectator proton in the far forward region, including its  $p_T$ , for sensitivity to neutron virtuality

# *Exploring polarized deuterons*

- Speculation – knowing unpolarized or polarized partonic structure of light nuclei someday helpful to improve efficiency of fusion reactions???
- E.g. arXiv:2312.16777 – *Multiphoton fusion of light nuclei in intense laser fields*
  - “Future investigations should contemplate the utilization of a more realistic optical potential featuring a rigid core and nuclear spin”



# Longitudinally polarized protons and transverse-momentum-dependent PDFs

Unpolarized

$$f_1 = \text{circle with dot}$$

Spin-spin correlations

$$g_{1L} = \text{circle with dot and right arrow} - \text{circle with dot and left arrow} \quad \text{Helicity}$$

$$h_{1T} = \text{circle with dot and up arrow} - \text{circle with dot and down arrow} \quad \text{Transversity}$$

Spin-momentum correlations

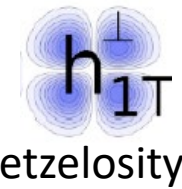
$$f_{1T}^\perp = \text{circle with up arrow} - \text{circle with down arrow} \quad \text{Sivers}$$

$$h_1^\perp = \text{circle with dot and up arrow} - \text{circle with dot and down arrow} \quad \text{Boer-Mulders}$$

$$h_{1L}^\perp = \text{circle with dot and right arrow} - \text{circle with dot and left arrow} \quad \text{Worm-gear} \quad h_{1T}^\perp = \text{circle with dot and up arrow} - \text{circle with dot and down arrow}$$

Worm-gear  
(Kotzinian-Mulders)

$$g_{1T} = \text{circle with dot and right arrow} - \text{circle with dot and left arrow}$$



# Longitudinally polarized protons and transverse-momentum-dependent PDFs

Unpolarized


$$f_1 = \text{circle with dot}$$

Spin-spin correlations

$$g_{1L} = \text{circle with dot and right arrow} - \text{circle with dot and left arrow} \quad \text{Helicity}$$

$$h_{1T} = \text{circle with dot and up arrow} - \text{circle with dot and down arrow} \quad \text{Transversity}$$

Worm-gear (Kotzinian-Mulders)

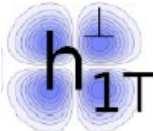
$$g_{1T} = \text{circle with dot and right arrow} - \text{circle with dot and left arrow}$$


Spin-momentum correlations

$$f_{1T}^\perp = \text{circle with up arrow} - \text{circle with down arrow} \quad \text{Sivers}$$

$$h_1^\perp = \text{circle with dot and up arrow} - \text{circle with dot and down arrow} \quad \text{Boer-Mulders}$$

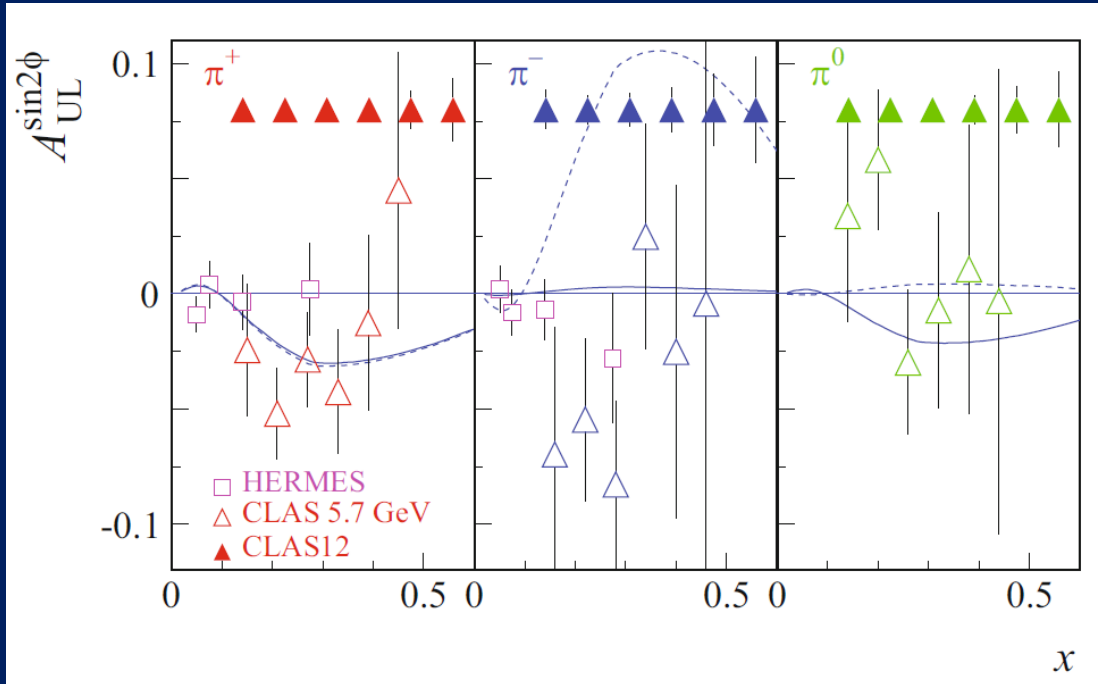
$$h_{1L}^\perp = \text{circle with dot and right arrow} - \text{circle with dot and left arrow} \quad \text{Worm-gear}$$



Pretzelocity

$$h_{1T}^{\perp\perp} = \text{circle with dot and up arrow} - \text{circle with dot and down arrow}$$

# Worm-gear TMD PDF $h_{1L}^\perp$



EPJA 52, 150 (2016)

- $h_{1L}^\perp$  sensitive to transversely polarized quarks in a longitudinally polarized proton
  - A spin-spin-momentum correlation
- So far no evidence for a nonzero asymmetry, but higher-precision data expected from CLAS12

# *Ji spin sum rule, Generalized Parton Distributions, and OAM*

- Ji spin decomposition:  $\frac{1}{2} = \frac{1}{2} \Delta\Sigma + L_q + J_g$  PRL78, 610 (1997)
  - Only in terms of gluon *total* angular momentum
  - Different definition of  $L_q$  than in Jaffe-Manohar sum rule – matter and gauge degrees of freedom can't be unambiguously separated in a gauge theory
- Moments of some generalized parton distributions (GPDs) for longitudinally polarized protons can be related to quark orbital angular momentum
  - GPDs measurable via exclusive processes, e.g. deeply virtual Compton scattering to access quarks





# *Orbital angular momentum and generalized transverse-momentum-dependent distributions*

- The formulation of *generalized transverse-momentum-dependent* distributions (GTMDs) encompasses both Jaffe-Manohar and Ji decompositions
  - See e.g. JHEP08, 056 (2009), PRD84, 014015 (2011), Phys. Rep. 541, 163 (2014)
  - Relating Ji and Jaffe-Manohar OAM using GTMD approach on the lattice –PRD102, 074505 (2020)
- Also recent proposals to access gluon orbital angular momentum at EIC via single and double spin asymmetry in diffractive dijet production, using the framework of Generalized TMDs: PRL118, 192004 (2017), PRL128, 182002 (2022)



# Summary

- The EIC will open up a great wealth of new opportunities to study the longitudinal spin structure of the proton and neutron as well as many other spin-dependent (and unpolarized) observables
- The more we learn in the upcoming years from theoretical developments as well as existing and near-term data, the more fully we will be able to exploit the EIC's powerful and unique capabilities once it turns on!

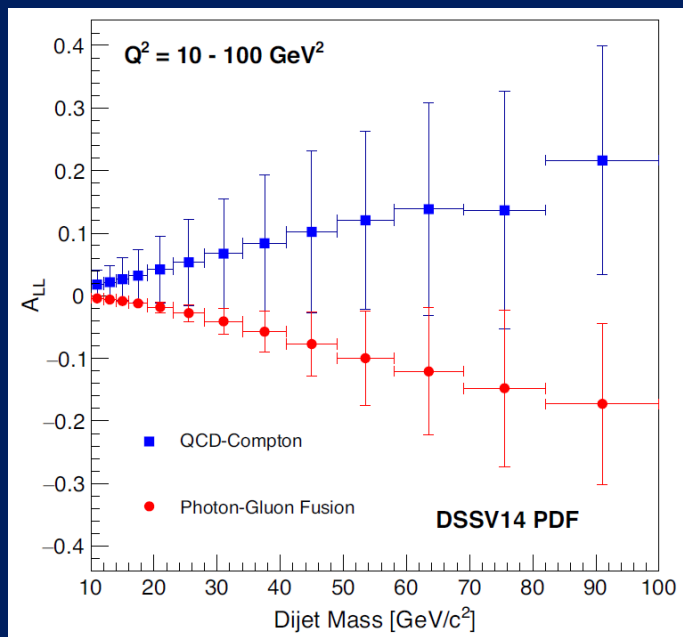


# *Extra*

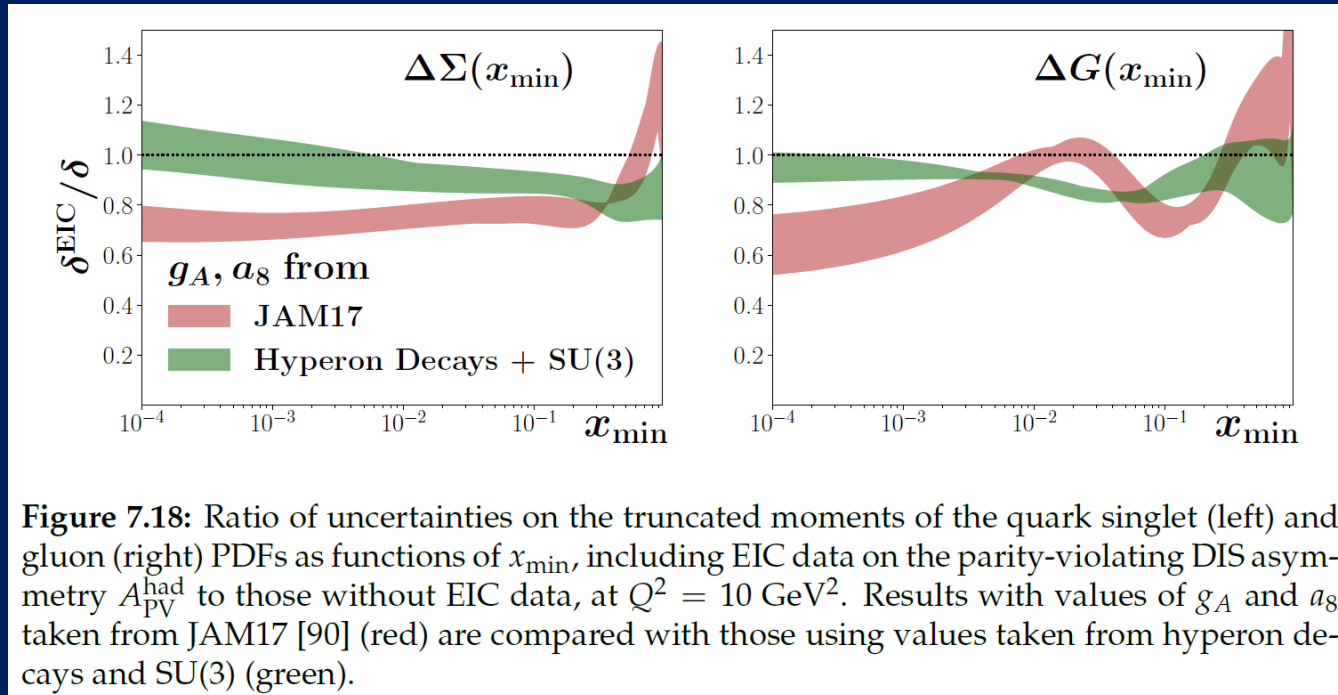


# *EIC: Accessing gluon helicity through double-longitudinal asymmetry for dijets*

PRD101, 072003 (2020)



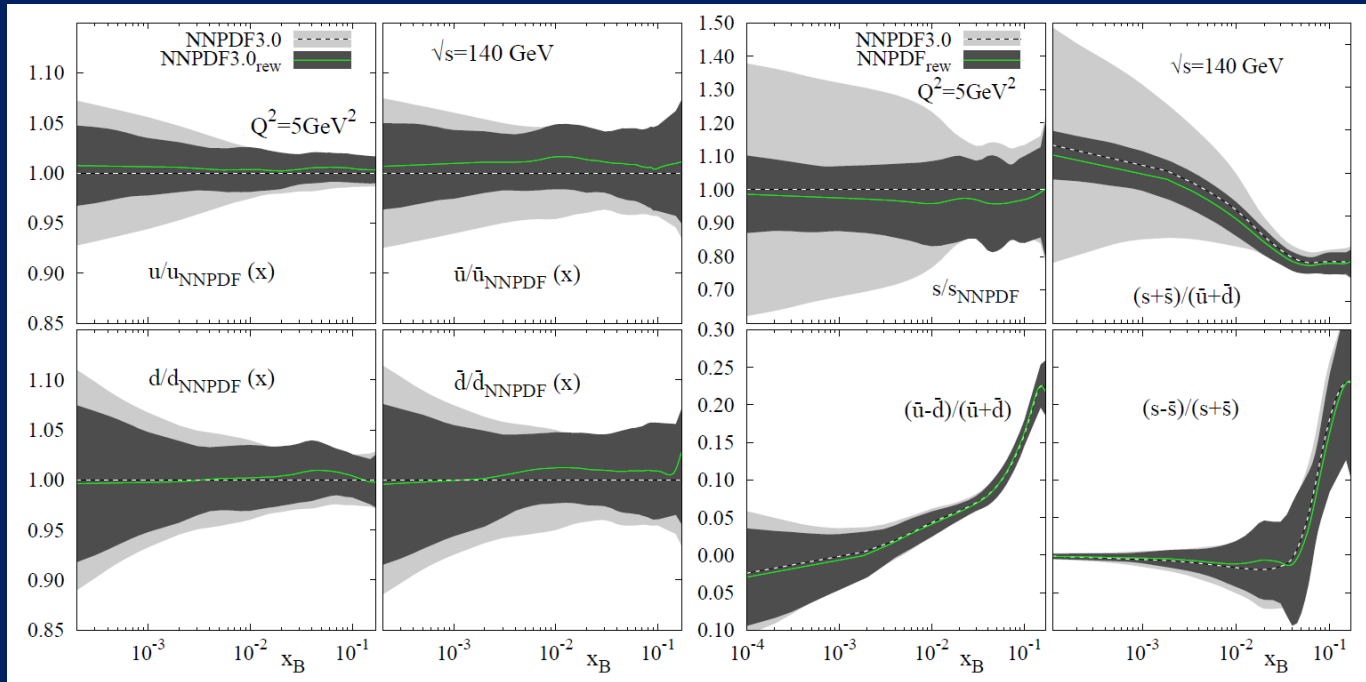
# EIC: Parity-violating DIS for flavor-dependent helicity PDFs



EIC Yellow Report, 2021



# *SIDIS to probe flavor-separated unpolarized PDFs*



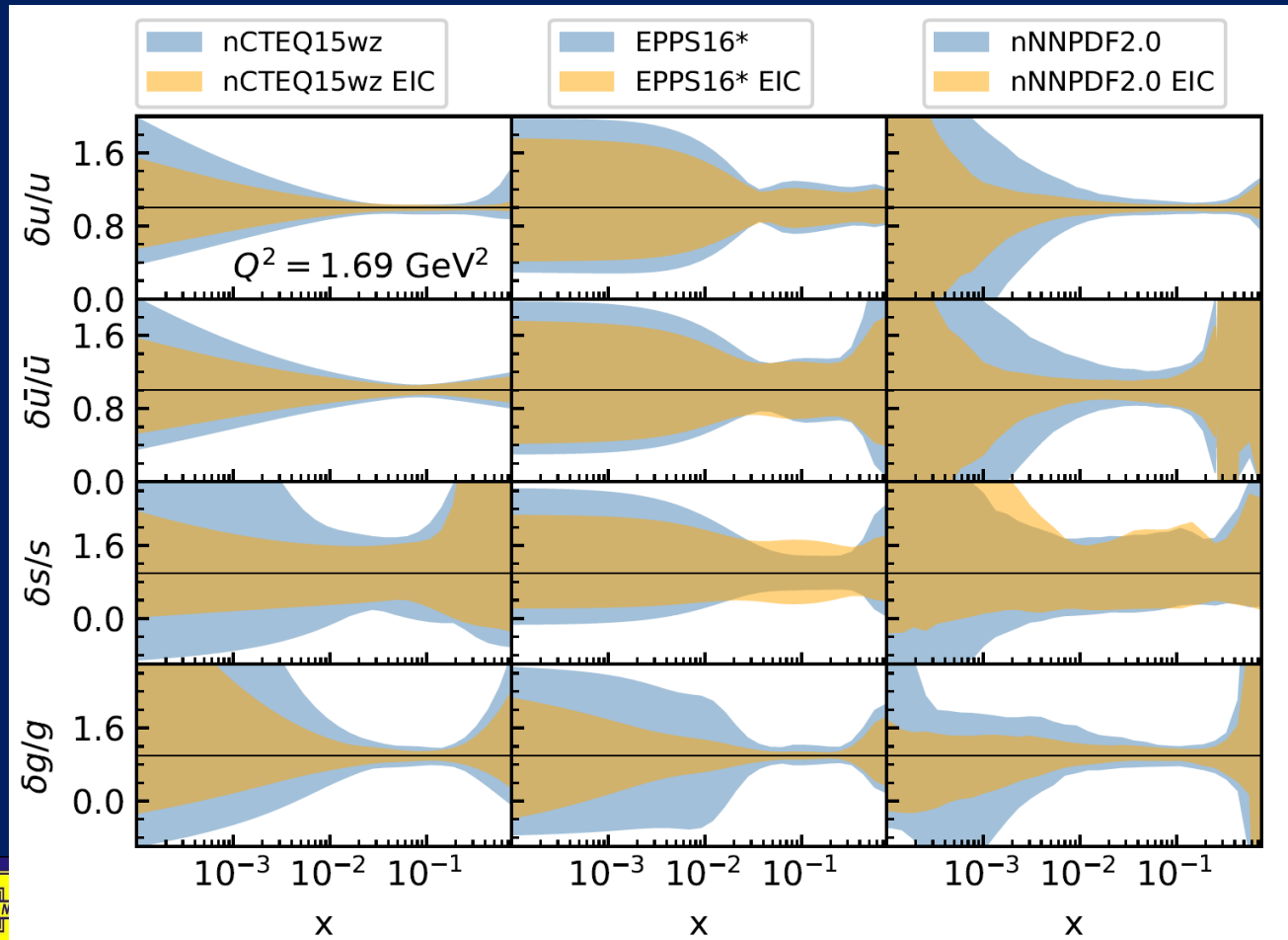
Projected impact on the **unpolarized** (sea) quark PDFs from identified charged pion and kaon SIDIS data at the EIC

EIC Yellow Report  
Baseline PDFs from JHEP 04, 040 (2015)



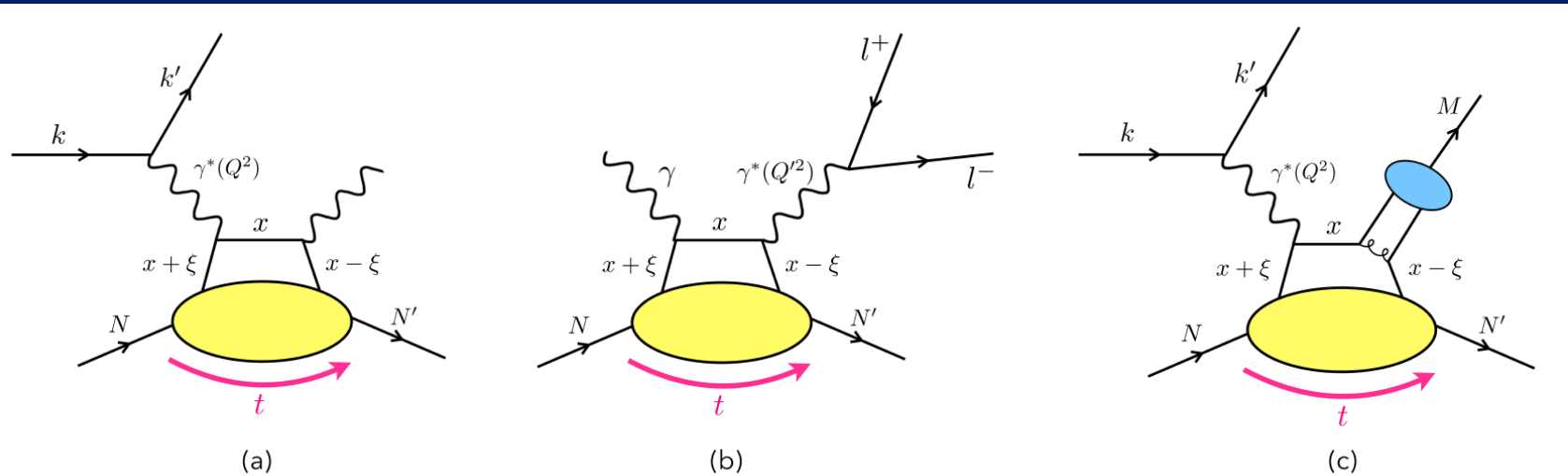
# Partonic momentum structure of nuclei: Nuclear parton distribution functions

(Traditional collinear, unpolarized) Nuclear PDFs



Expected improvement  
on uncertainty in  
nuclear PDFs - from  
Yellow Report

# Processes sensitive to GPDs



**Figure 7.43:** Illustrations of three main processes which are sensitive to GPDs: (a) exclusive electroproduction of a real photon, (b) TCS and (c) exclusive electroproduction of a meson.

From EIC Yellow Report (2021)



# *Twist-3 multiparton correlation functions*

- Interference between higher Fock components in the hadron wave functions
- No probabilistic partonic interpretation, but provide information on partons involved in hard scattering interacting with color fields in the initial-state hadron



# *Nucleon-to-meson transition distribution amplitudes*

- 3-parton exchange between the TDA and the hard part
- Potential access to helicity of correlated quarks in the nucleon
- See discussion in EIC Yellow Report



# *Long-term: Synthesizing what we learn*

- Eventually want a unified picture linking these nonperturbative functions coming from a “hard” factorized regime to a “soft” regime where this kind of partonic language isn’t necessarily suitable.
  - Could thinking about multiparton correlation functions potentially be a step towards useful “nonperturbative color blob” descriptions of some sort???
- What might nonperturbative theoretical tools such as lattice QCD, low-energy models, or possibly future quantum computers tell us about how to fruitfully link perturbative/partonic and nonperturbative/nonpartonic descriptions of hadron structure?

