

# PRIMORDIAL BLACK HOLES AS THE SOLUTION OF MANY COSMOLOGICAL CONUNDRAS



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ICTS (13/11/20)

# PBH FORMATION AND EVAPORATION

$$R_S = 2GM/c^2 = 3(M/M_O) \text{ km} \Rightarrow \rho_S = 10^{18}(M/M_O)^{-2} \text{ g/cm}^3$$

Small BHs can only form in early Universe

cf. cosmological density  $\rho \sim 1/(Gt^2) \sim 10^6(t/s)^{-2} \text{ g/cm}^3$

$$\begin{aligned} & 10^{-5} \text{ g at } 10^{-43} \text{ s} && \text{(minimum)} \\ \Rightarrow M_{\text{PBH}} \sim c^3 t / G = & 1 M_O \text{ at } 10^{-5} \text{ s} && \text{(QCD transition)} \\ & 10^5 M_O \text{ at } 1 \text{ s} && \text{(maximum?)} \end{aligned}$$

Black holes radiate thermally with temperature

$$T = \frac{hc^3}{8\pi GkM} \sim 10^{-7} \left[ \frac{M}{M_0} \right]^{-1} \text{ K}$$

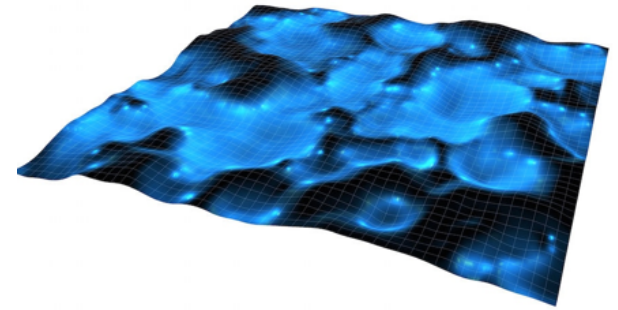
$$\Rightarrow \text{evaporate completely in time} \quad t_{\text{evap}} \sim 10^{64} \left[ \frac{M}{M_0} \right]^3 \text{ y}$$

$$M \sim 10^{15} \text{ g} \Rightarrow \text{final explosion phase today (} 10^{30} \text{ ergs)}$$

$$T > T_{\text{CMB}} = 3 \text{ K for } M < 10^{26} \text{ g} \Rightarrow \text{“quantum” black holes}$$

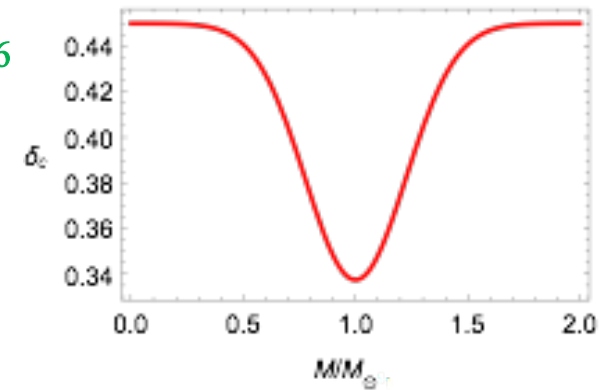
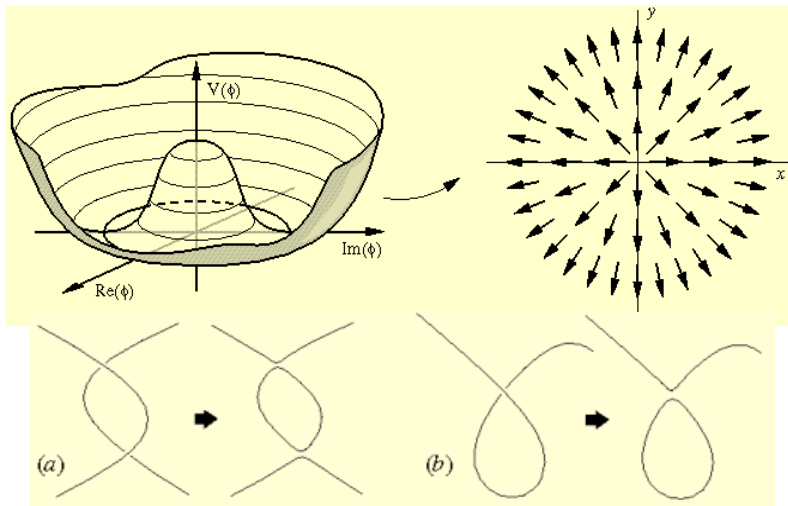
# FORMATION MECHANISMS

Primordial inhomogeneities Inflation



Pressure reduction Form more easily but need spherical symmetry

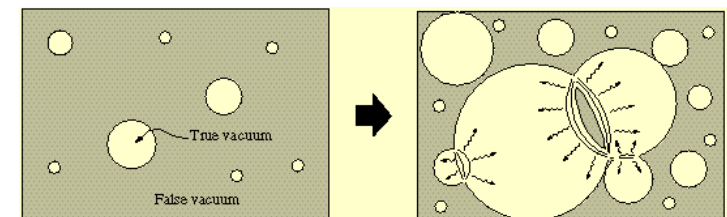
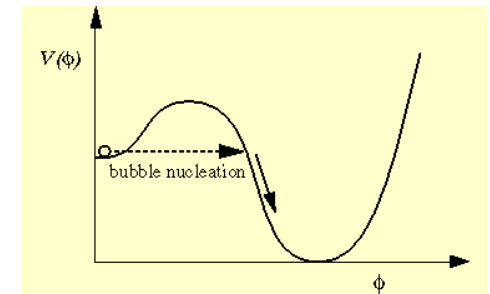
Cosmic strings PBH constraints  $\Rightarrow G\mu < 10^{-6}$



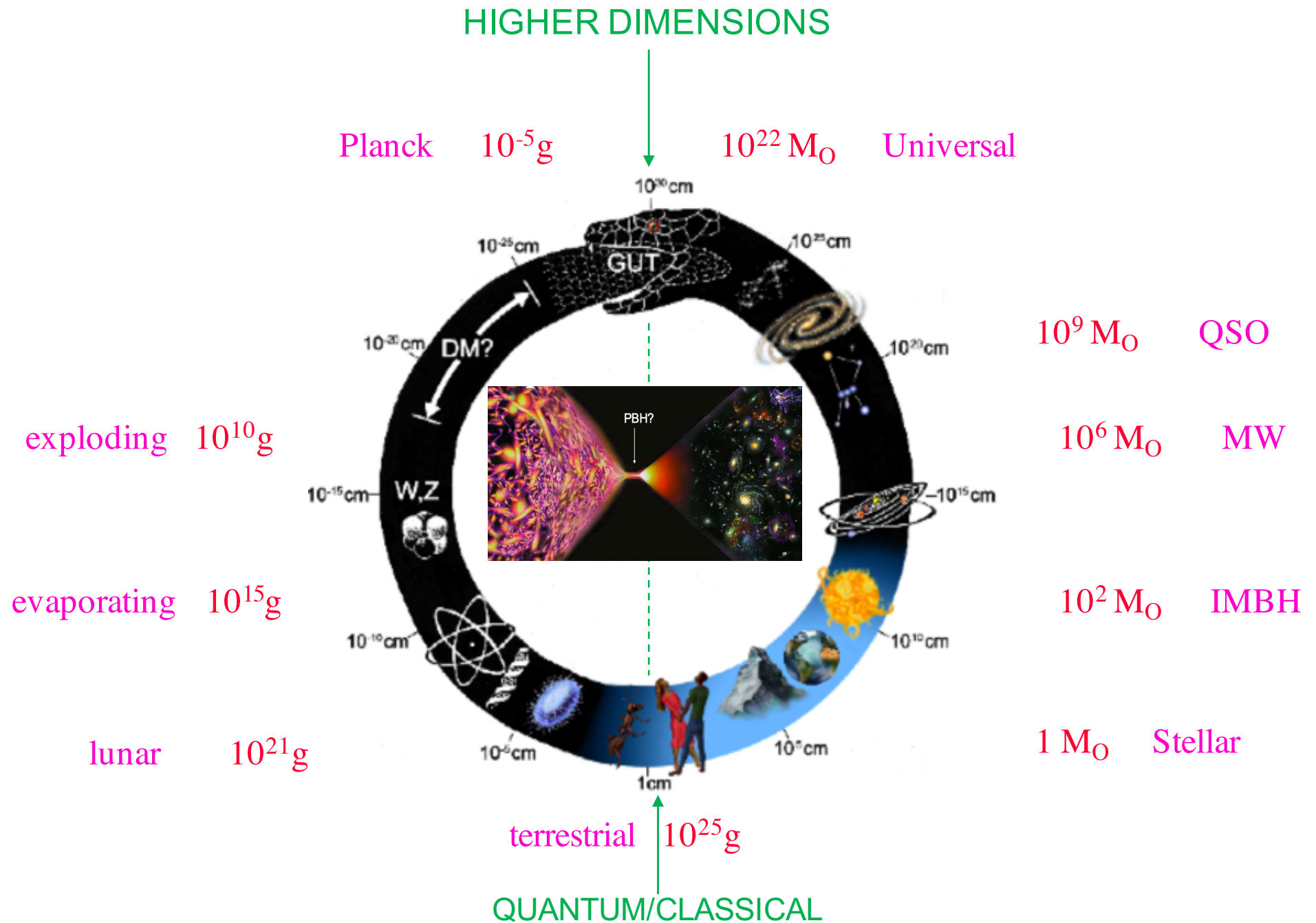
Bubble collisions

Need fine-tuning of bubble formation rate

Domain walls PBHs can be very large



# BLACK HOLES AS LINK BETWEEN MICRO AND MACRO PHYSICS





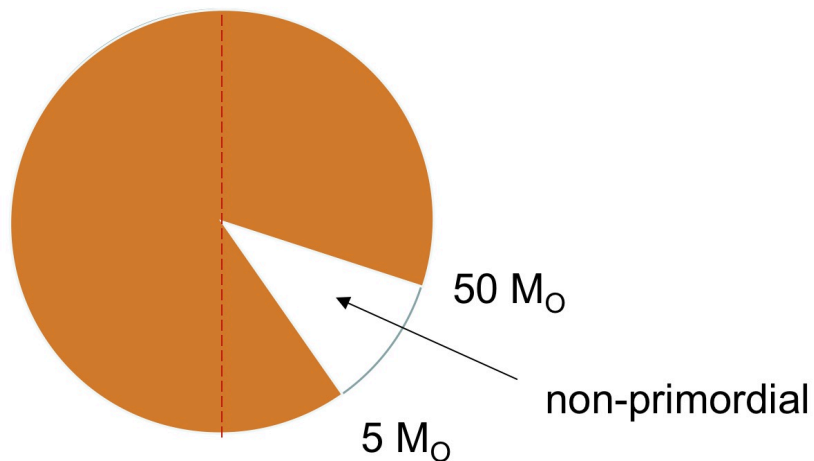
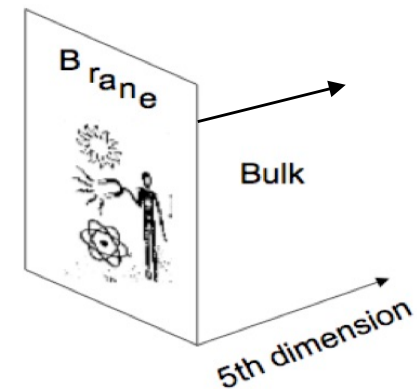
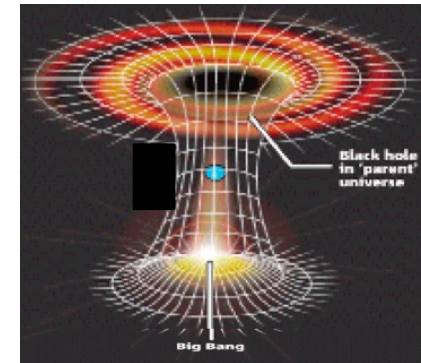
# IS THE UNIVERSE A PRIMORDIAL BLACK HOLE?

Collapse to black hole generates a baby Universe

Smolin (1997)

Brane cosmology => 5D Schwarzschild de Sitter model  
=> Universe emerges out of 5D black hole

Bowcock et al. (2000), Mukhoyama et al. (2000)



ARE MOST BLACK HOLES PRIMORDIAL?

# PBH FORMATION => LARGE INHOMOGENEITIES

To collapse against pressure, need (Carr 1975)

$$R > \sqrt{\alpha} \text{ ct} \quad \text{when } \delta \sim 1 \Rightarrow \delta_H > \alpha \quad (p = \alpha \rho c^2)$$

Gaussian fluctn's with  $\langle \delta_H^2 \rangle^{1/2} = \varepsilon(M)$

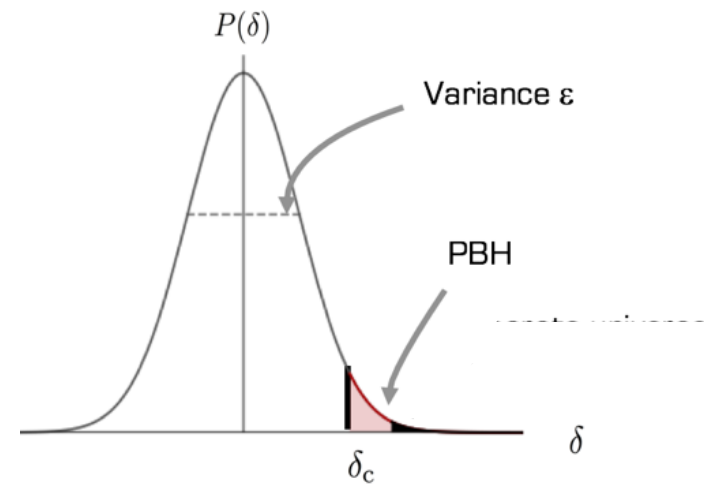
=> fraction of PBHs

$$\beta(M) \sim \varepsilon(M) \exp \left[ -\frac{\alpha^2}{2\varepsilon(M)^2} \right]$$

General limit

$$\frac{\rho_{PBH}}{\rho_{CBR}} \approx \frac{\Omega_{PBH}}{10^{-4}} \left[ \frac{R}{R_0} \right] \Rightarrow \beta \sim 10^{-6} \Omega_{PBH} \left[ \frac{t}{\text{sec}} \right]^{1/2} \sim 10^{-18} \Omega_{PBH} \left[ \frac{M}{10^{15} \text{ g}} \right]^{1/2}$$

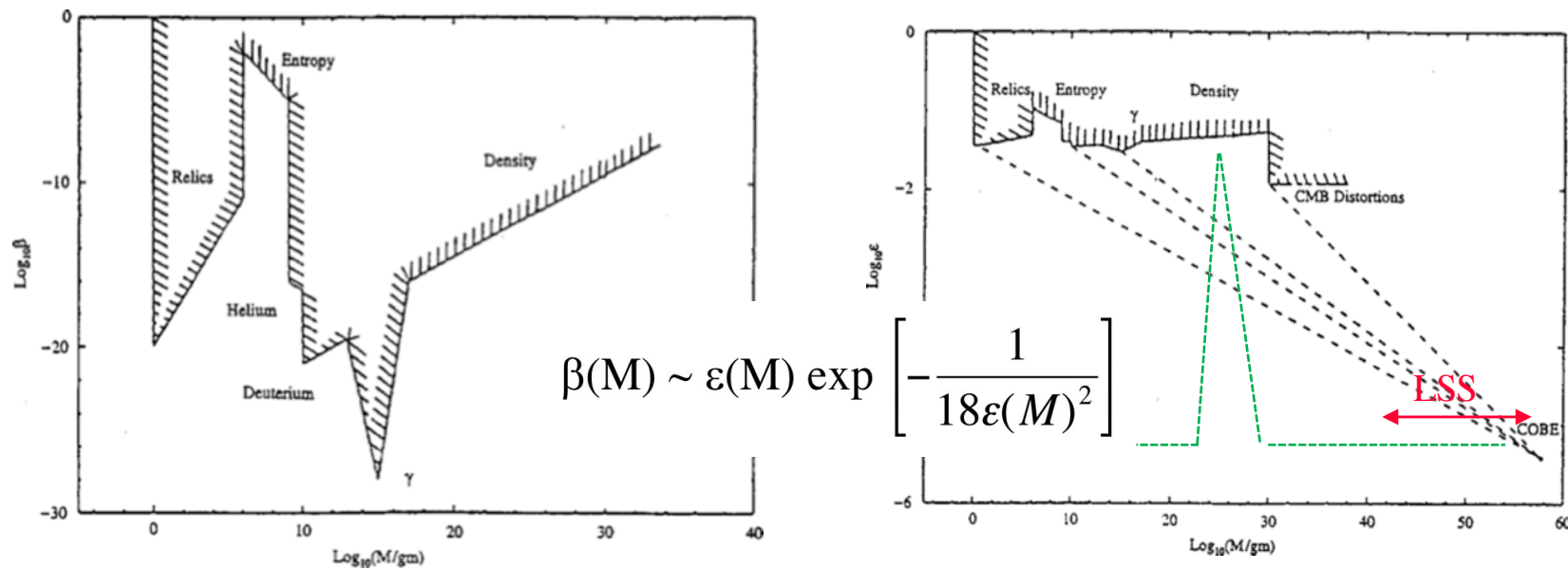
So both require and expect  $\beta(M)$  to be tiny



# Limit on fraction of Universe collapsing

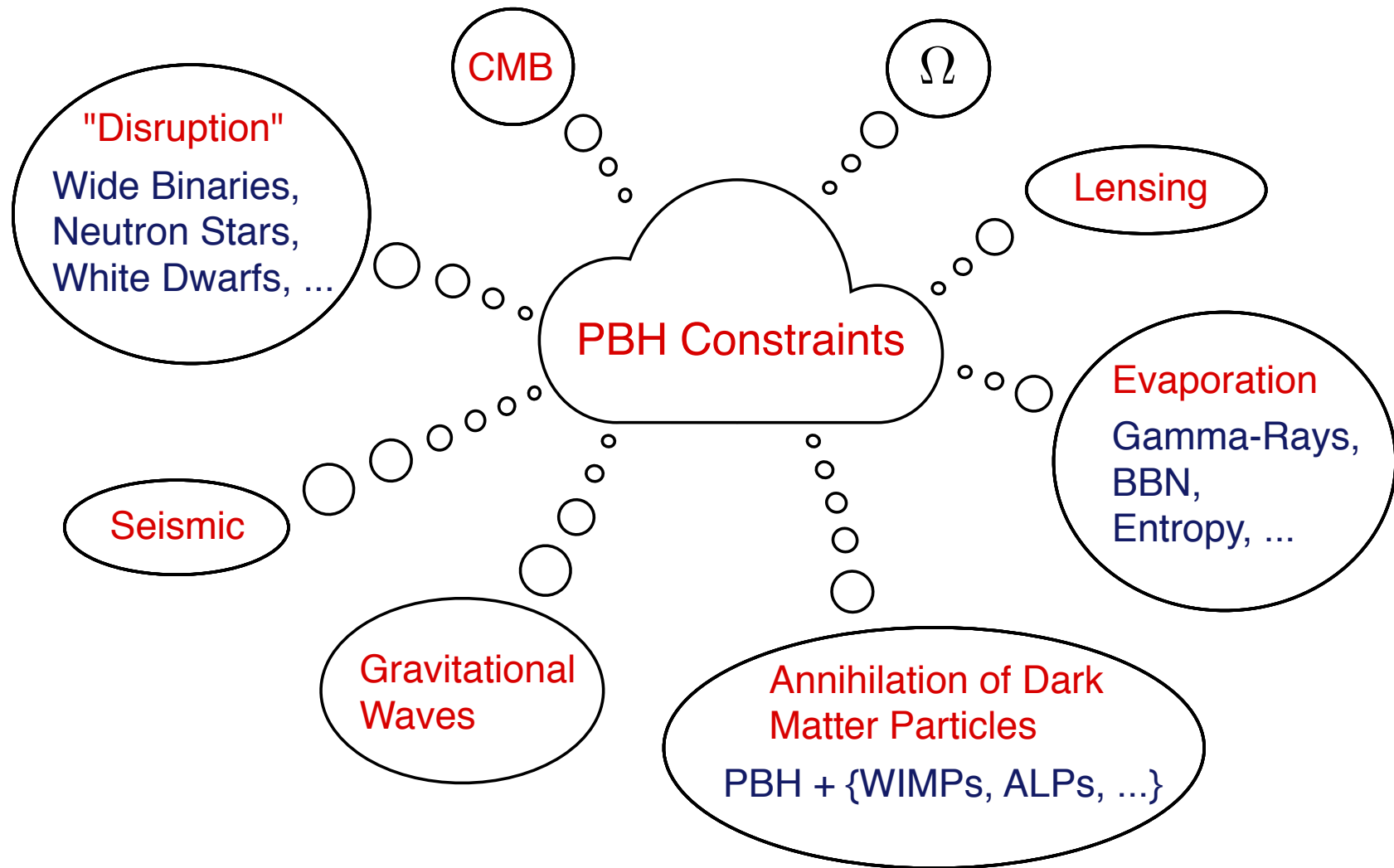
Unevaporated	$M > 10^{15} \text{g} \Rightarrow \Omega_{\text{PBH}} < 0.25$	(CDM)
Evaporating now	$M \sim 10^{15} \text{g} \Rightarrow \Omega_{\text{PBH}} < 10^{-8}$	(GRB)
Evaporated in past	$M < 10^{15} \text{g}$	

$\Rightarrow$  constraints from entropy,  $\gamma$ -background, BBNS



PBHs are unique probe of  $\epsilon$  on small scales.

Need blue spectrum or spectral feature to produce them.



# CONSTRAINTS FOR EVAPORATING PBHS

B. Carr, K. Kohri, Y. Sendouda &amp; J. Yokoyama PRD 81(2010) 104019

# Big bang nucleosynthesis

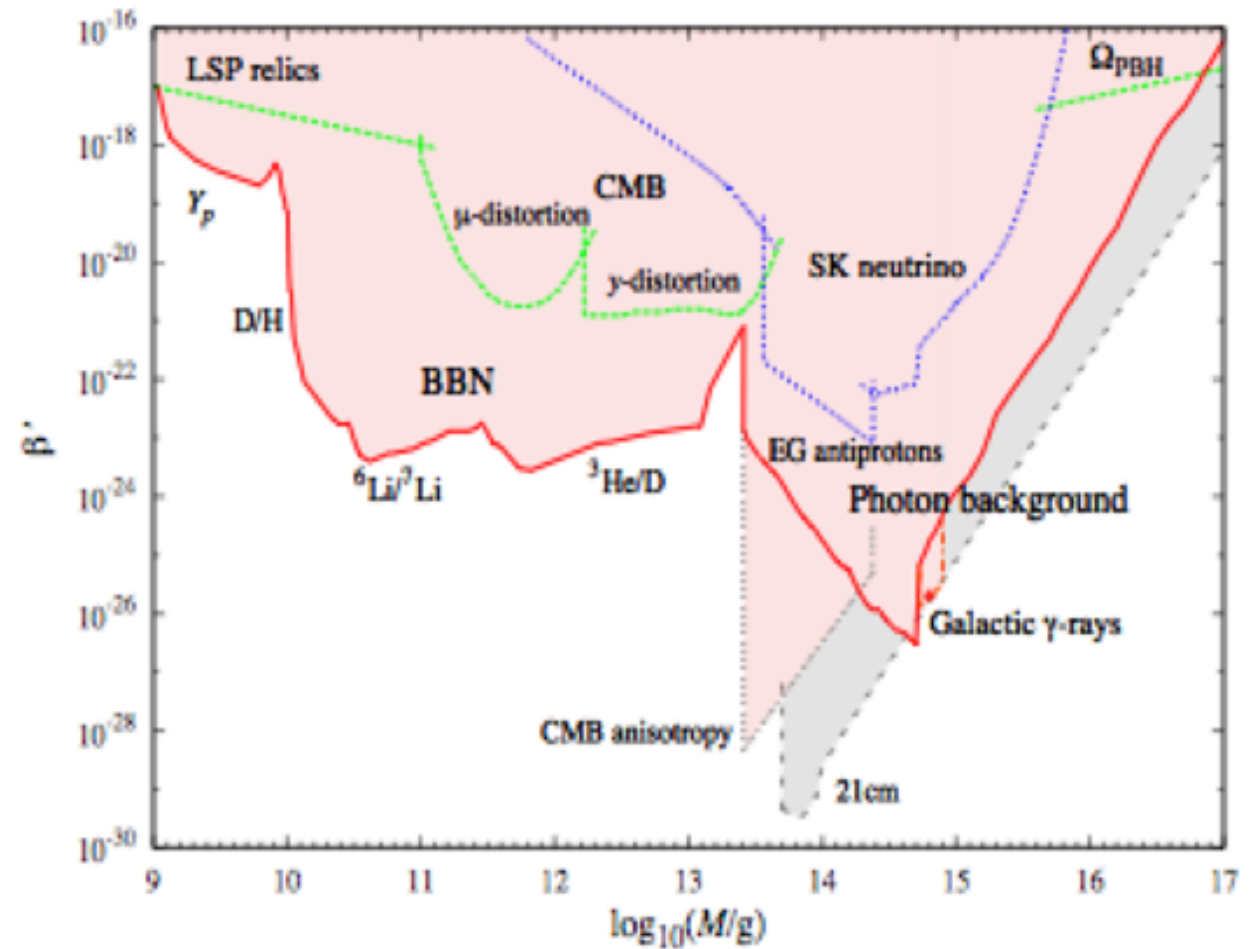
# Gamma-ray background

## Extragalactic cosmic rays

## Neutrino relics

## LSP relics

## CMB distortions



This assumes monochromatic mass function

# VOYAGER-1 $e^\pm$ further constrain Primordial Black Holes as Dark Matter

Mathieu Boudaud<sup>1</sup> and Marco Cirelli<sup>1</sup>

[arXiv:1807.03075](#)

## Direct Detection of Hawking Radiation from Asteroid-Mass Primordial Black Holes

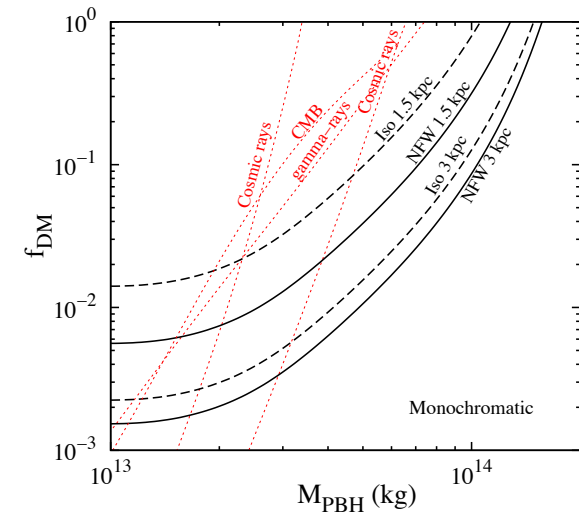
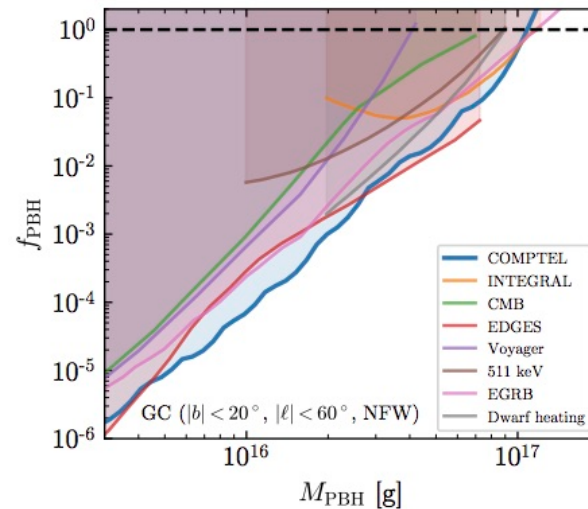
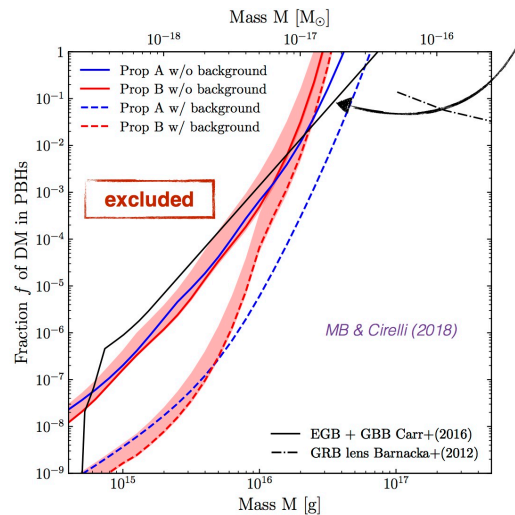
Adam Coogan,<sup>1,\*</sup> Logan Morrison,<sup>2,†</sup> and Stefano Profumo<sup>2,‡</sup>

[arXiv:2010.04797](#)

## PBHs as DM candidate are severely constrained by the Galactic Center 511 keV $\gamma$ -ray line

Laha

[arXiv:1906.09994](#)





# RECENT CONSTRAINTS ON EVAPORATING PBHS

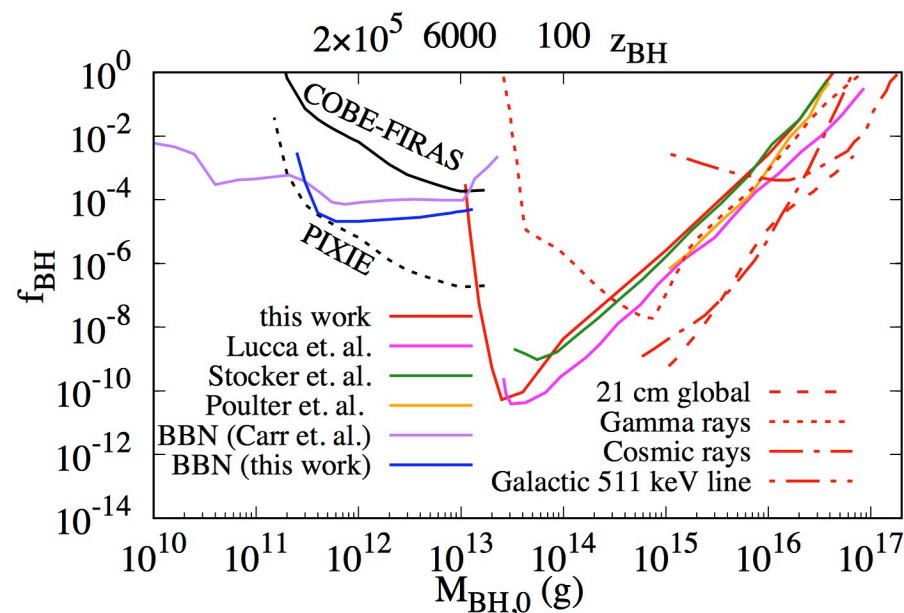
## *CMB anisotropies*

CKSY 2010

“CMB constraints on evaporating PBHs revisited”

Acharya & Khatri

2002.00898



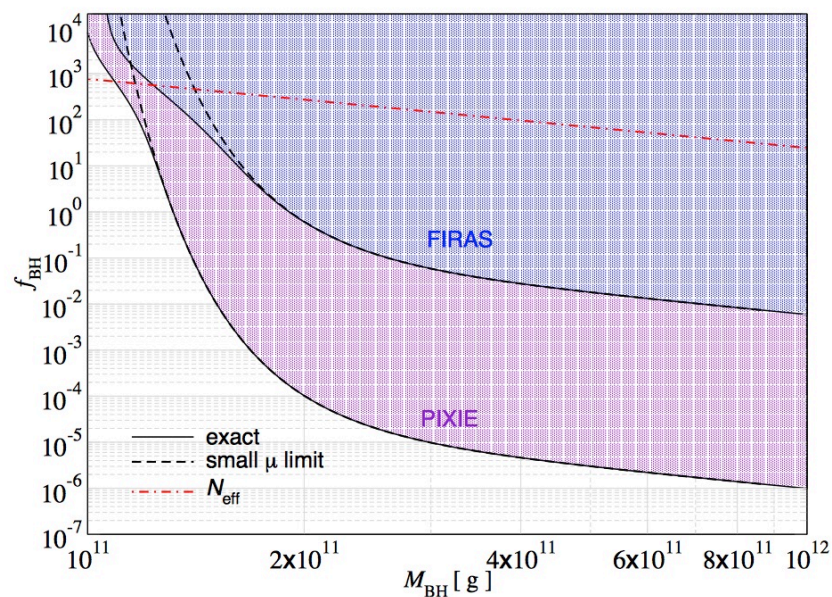
## *CMB spectral distortions*

Tashiro & Sugiyama (2008)

“Thermalization of large energy release in the early Universe”

Chluba, Ravenni & Acharya

2005.11325

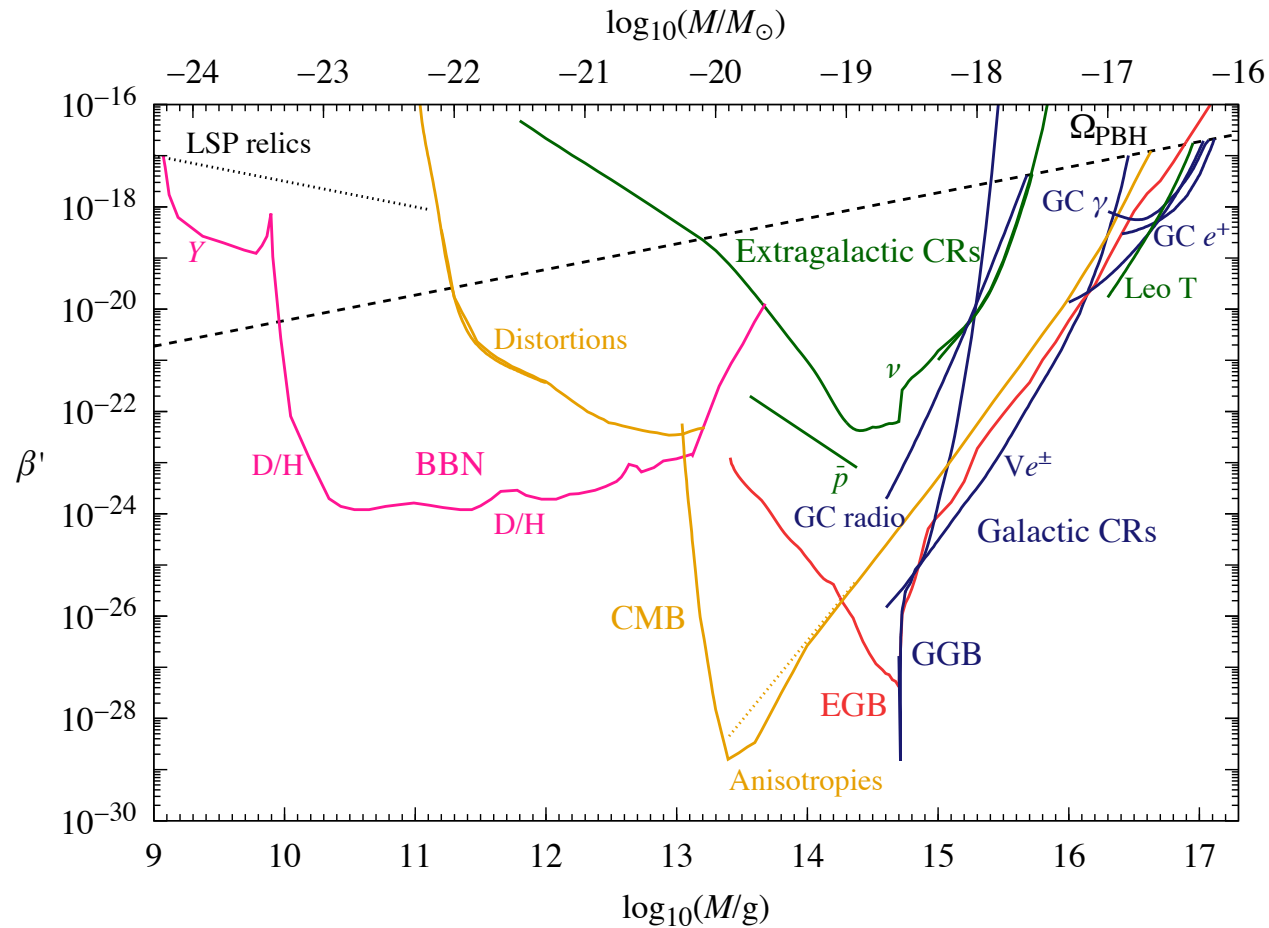




# CONSTRAINTS FOR EVAPORATING PBHS

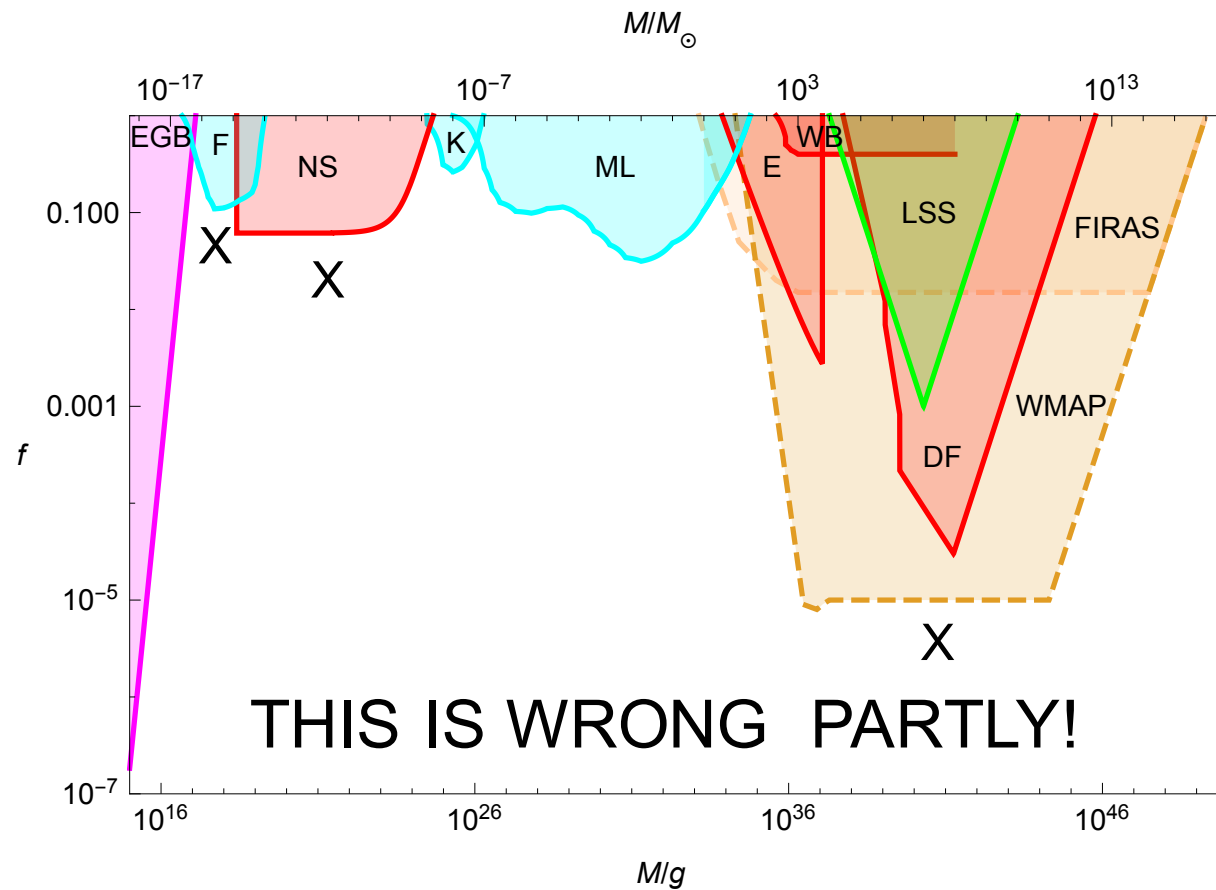
B. Carr, K. Kohri, Y. Sendouda & J. Yokoyama

Progress Theoretical Physics (2020), arXiv:2002.12778



# CONSTRAINTS ON NON-EVAPORATED PBHS

Carr, Kuhnel & Sandstad, arXiv:1607.06077



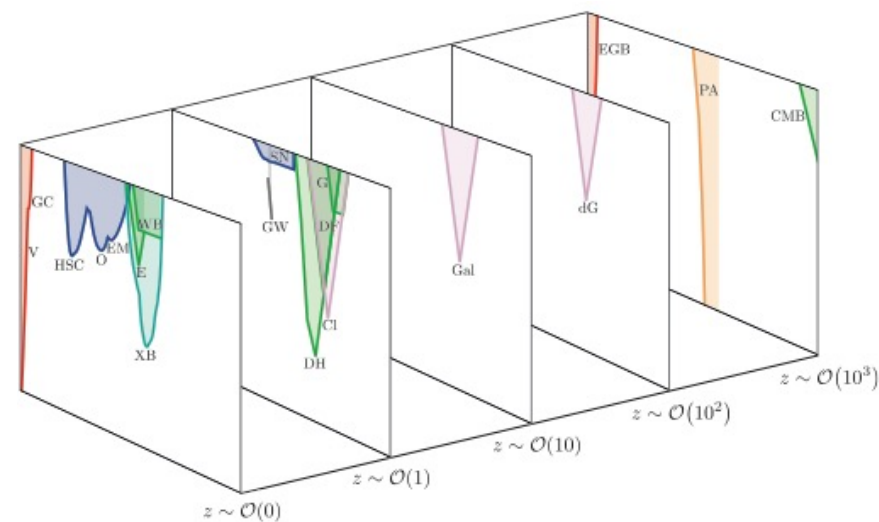
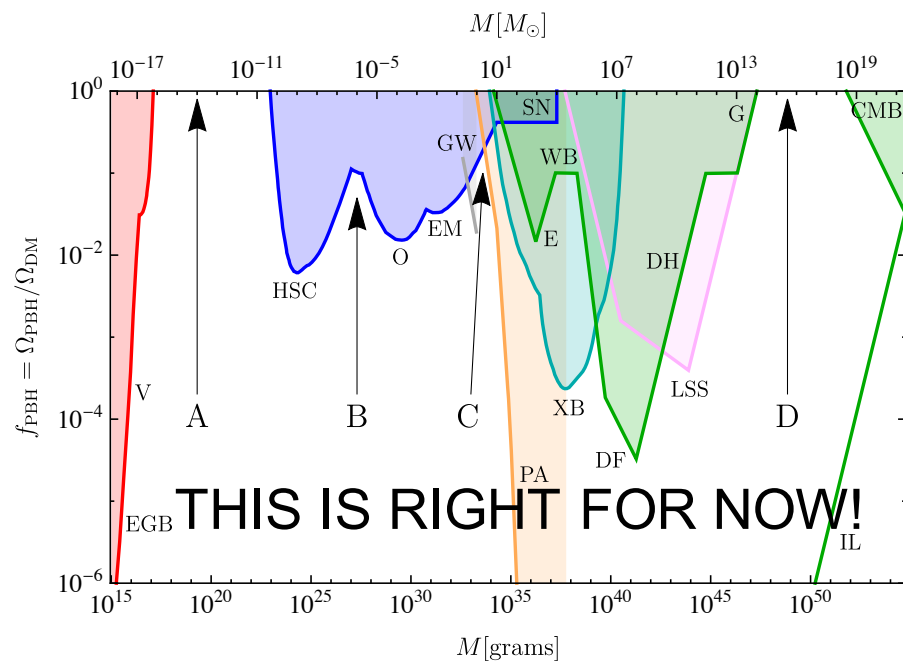
Some of these limits are now thought to be wrong

# Primordial Black Holes as Dark Matter: Recent Developments

Bernard Carr<sup>1,\*</sup> and Florian Kühnel<sup>2,†</sup>

Annu. Rev. Nucl. Part. Sci. 2020. 70:14.1–14.40

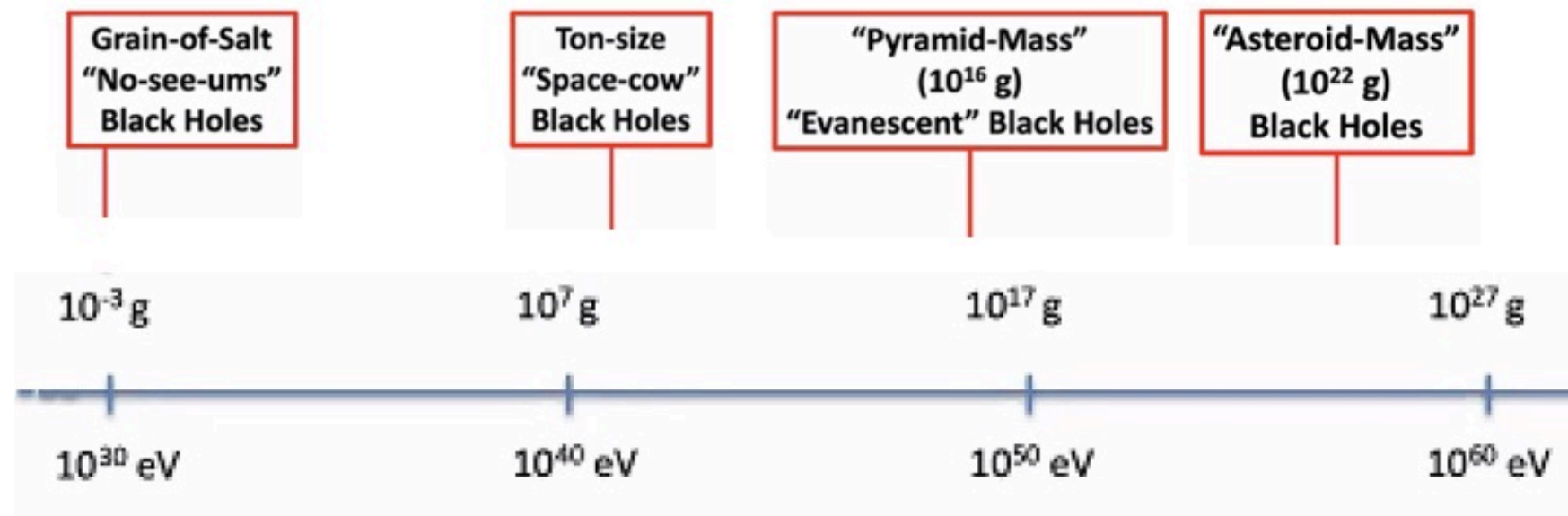
arXiv:2006.02838



(credit: based on JGB)

Three windows: (A) intermediate mass; (B) sublunar mass; (C) asteroid mass;  
(D) stupendously massive; (E) Planck mass relics

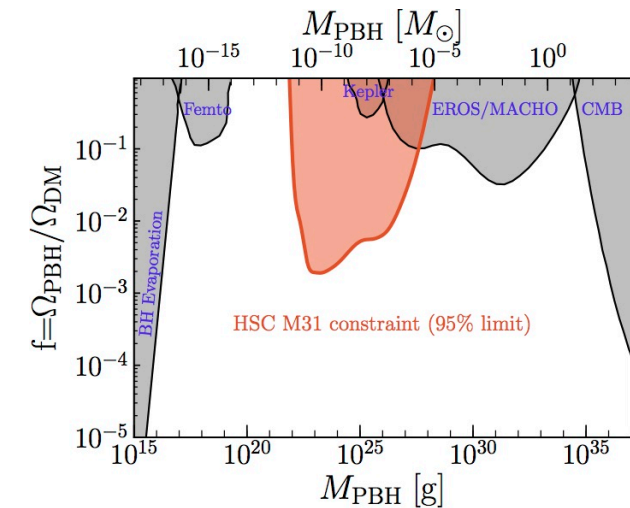
## Profumo talk



## Microlensing constraints on primordial black holes with the Subaru/HSC Andromeda observation

Hiroko Niikura<sup>1,2</sup>, Masahiro Takada<sup>1</sup>, Naoki Yasuda<sup>1</sup>, Robert H. Lupton<sup>3</sup>, Takahiro Sumi<sup>4</sup>,  
Surhud More<sup>1,5</sup>, Toshiki Kurita<sup>1,2</sup>, Sunao Sugiyama<sup>1,2</sup>, Anupreeta More<sup>1</sup>, Masamune Oguri<sup>1,2,6</sup>,  
Masashi Chiba<sup>7</sup>

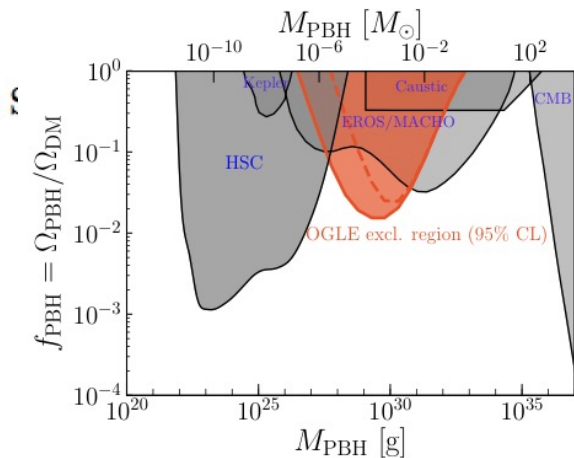
Nature Astronomy 3, 524 (2019),



## Earth-mass black holes? – Constraints on primordial black holes with 5-years OGLE microlensing events

Hiroko Niikura,<sup>1,2,\*</sup> Masahiro Takada,<sup>2,†</sup> Shuichiro Yokoyama,<sup>3,2</sup> Takahiro S

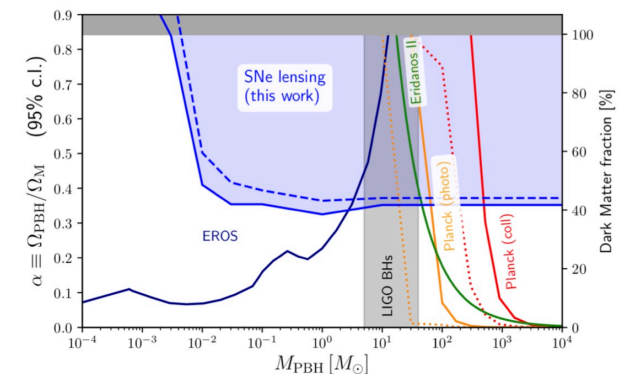
arXiv:1901.07120



## Limits on stellar-mass compact objects as dark matter from gravitational lensing of type Ia supernovae

Miguel Zumalacárregui<sup>1,2,3,\*</sup> and Uroš Seljak<sup>1,4,†</sup>

arXiv:1712.02240

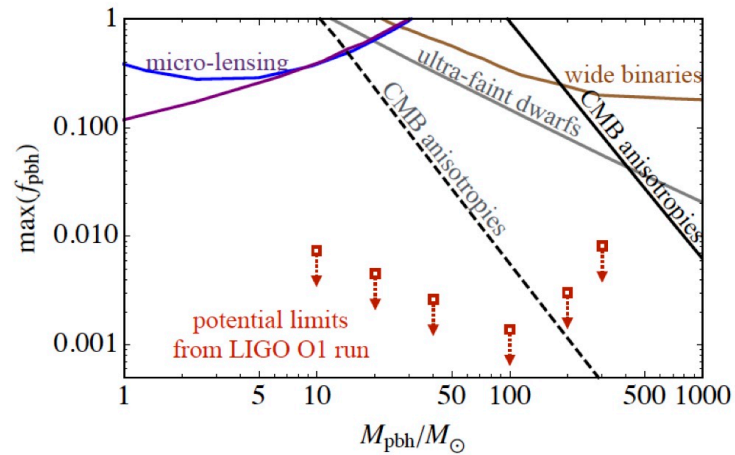


Can PBHs can evade these limits?

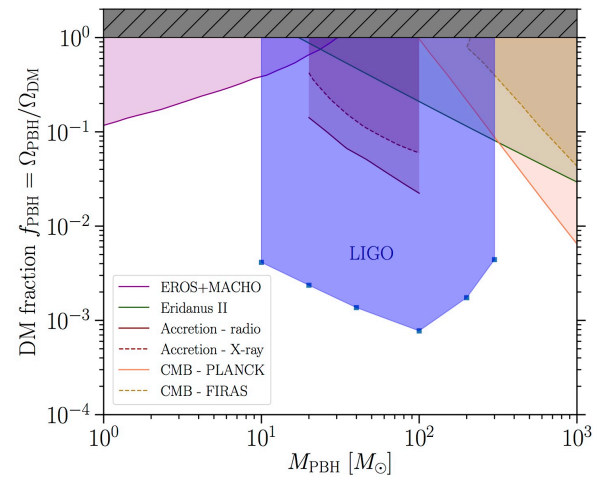
Garcia-Bellido et al, arXiv:1712.06574

# CONSTRAINTS ON $f(M)$ FROM LIGO

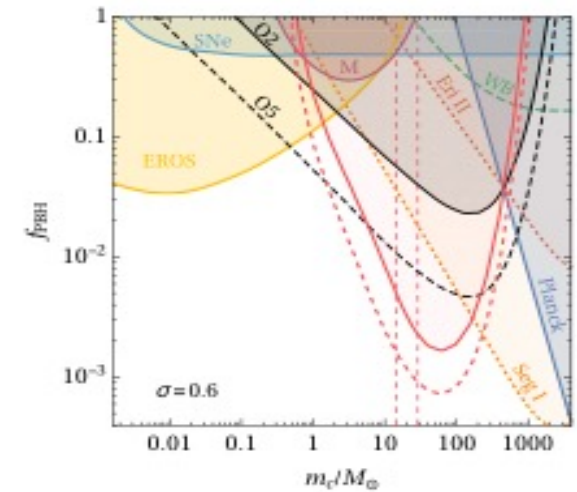
Ali-Haimoud et al. [1709.06576](#)



Kavanagh et al [1805.09034](#)



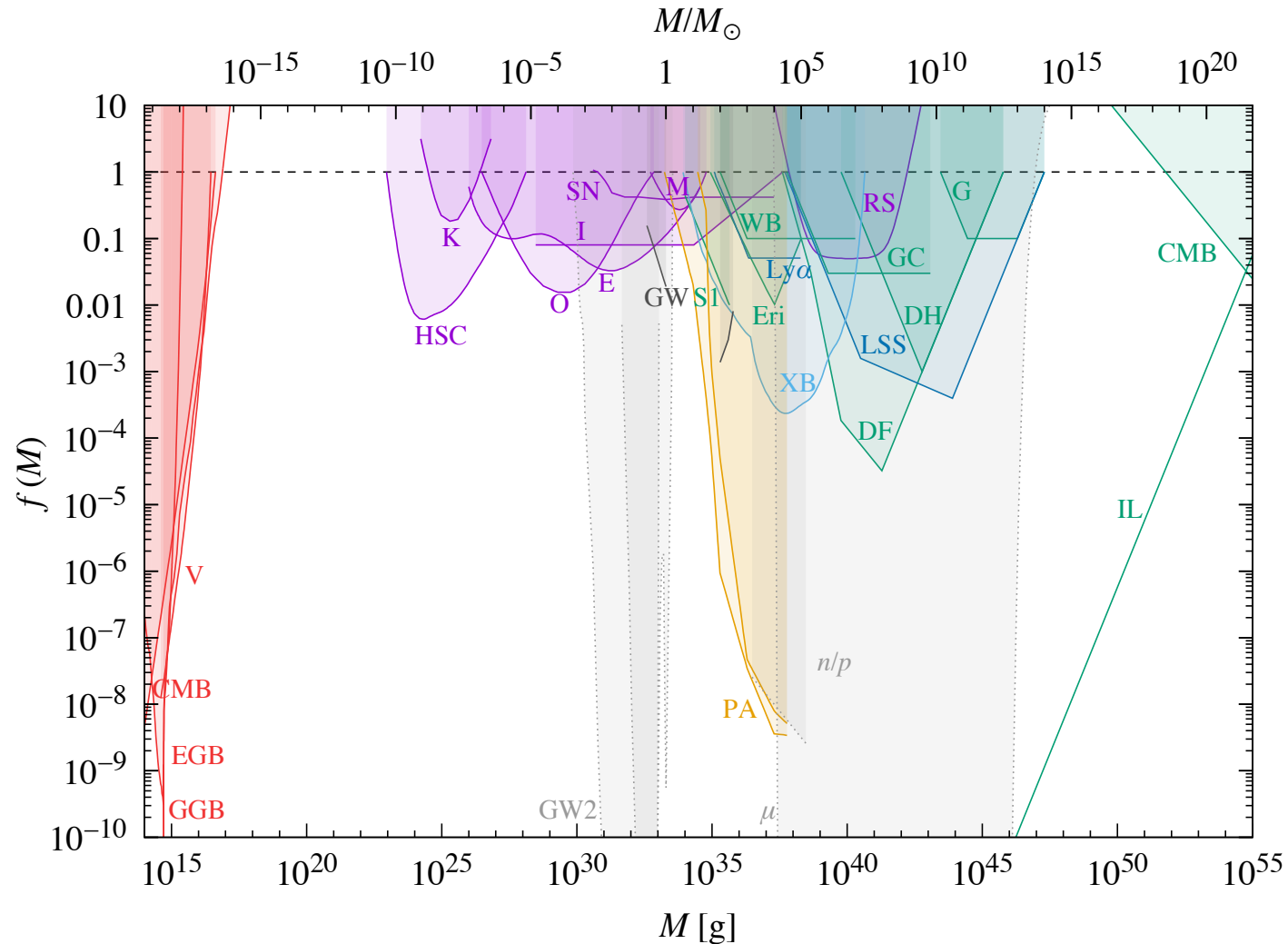
Raidal et al. [1812.01930](#)



# CONSTRAINTS ON PRIMORDIAL BLACK HOLES

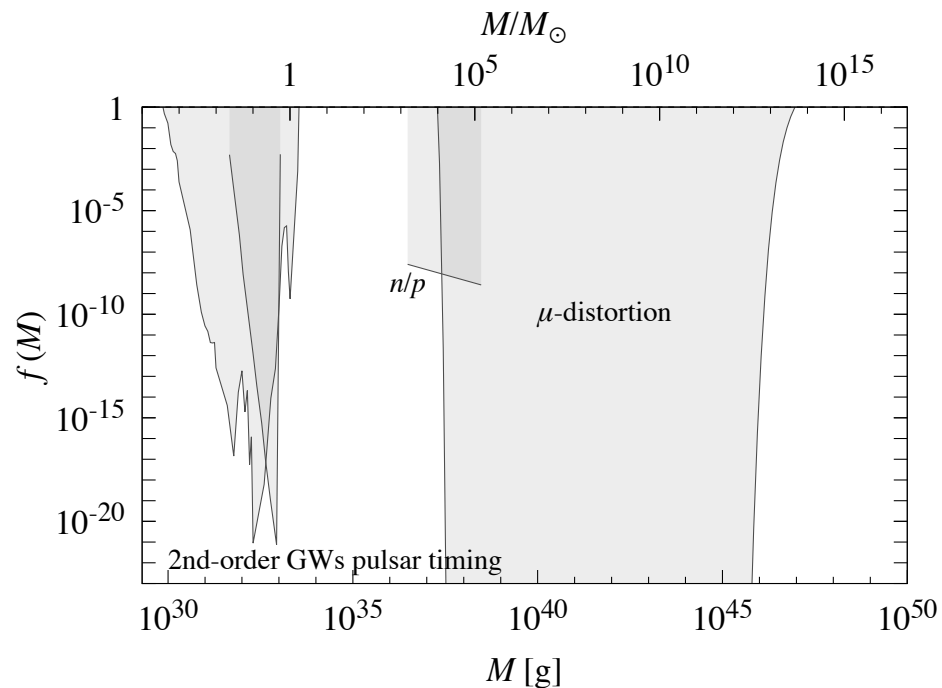
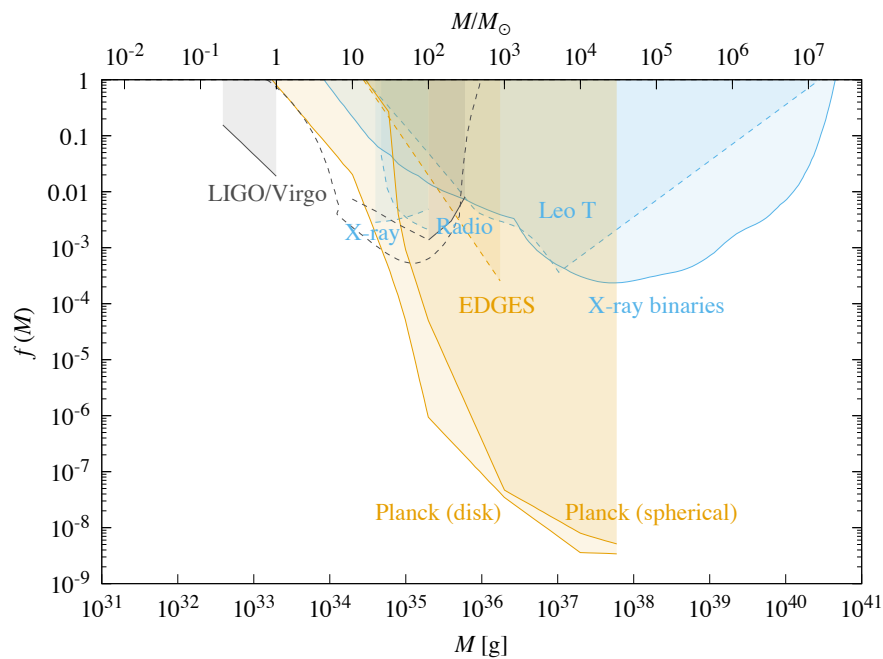
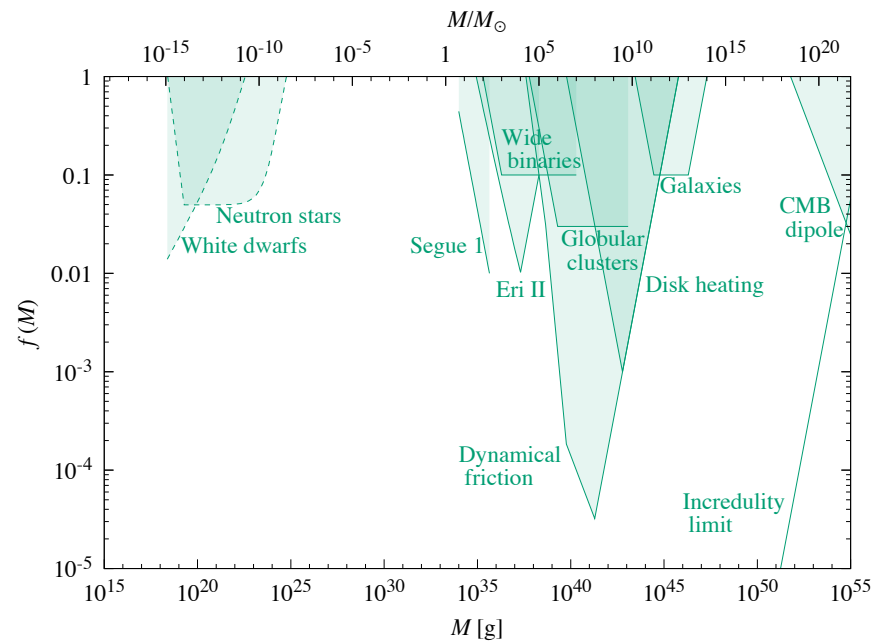
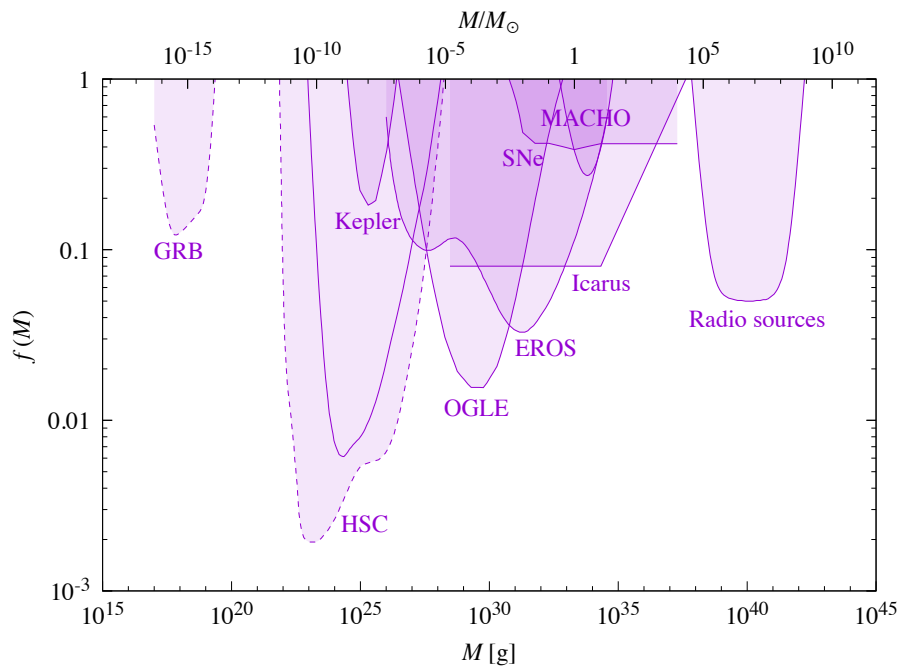
Bernard Carr,<sup>1, 2, \*</sup> Kazunori Kohri,<sup>3, †</sup> Yuuiti Sendouda,<sup>4, ‡</sup> and Jun'ichi Yokoyama<sup>2, 5, §</sup>

Progress Theoretical Physics (2020), arXiv:2002.12778

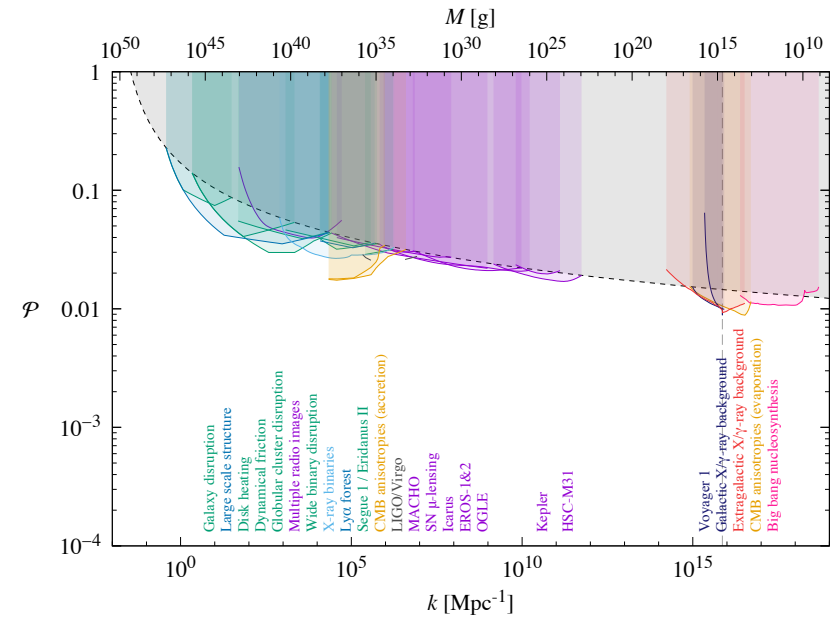
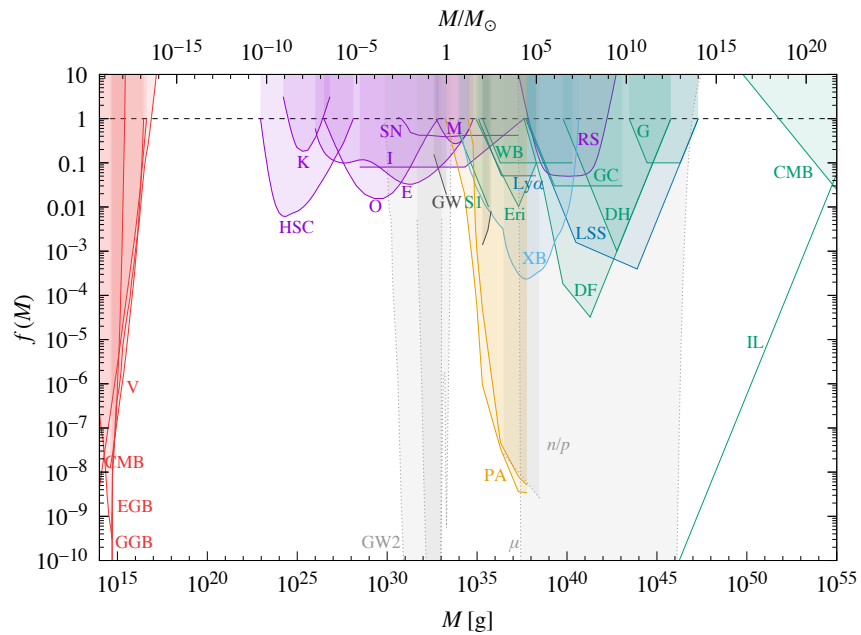
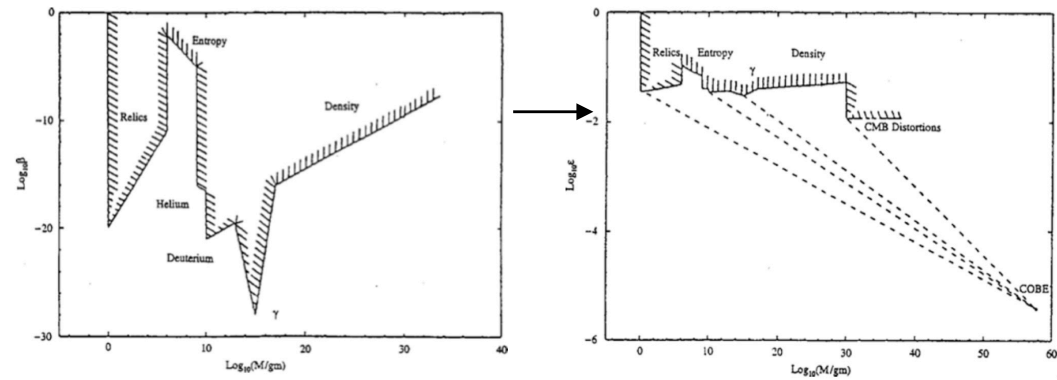




# LENSING, DYNAMICAL, ACCRETION AND COSMOLOGICAL LIMITS



# CONSTRAINTS ON POWER SPECTRUM



These constraints are not just nails in a coffin!



All constraints have caveats and may change

Each constraint is a potential signature

PBHs are interesting even if  $f \ll 1$

# PRIMORDIAL BLACK HOLES AS DARK MATTER

## PRO

- \* Black holes exist
- \* No new physics needed
- \* LIGO results

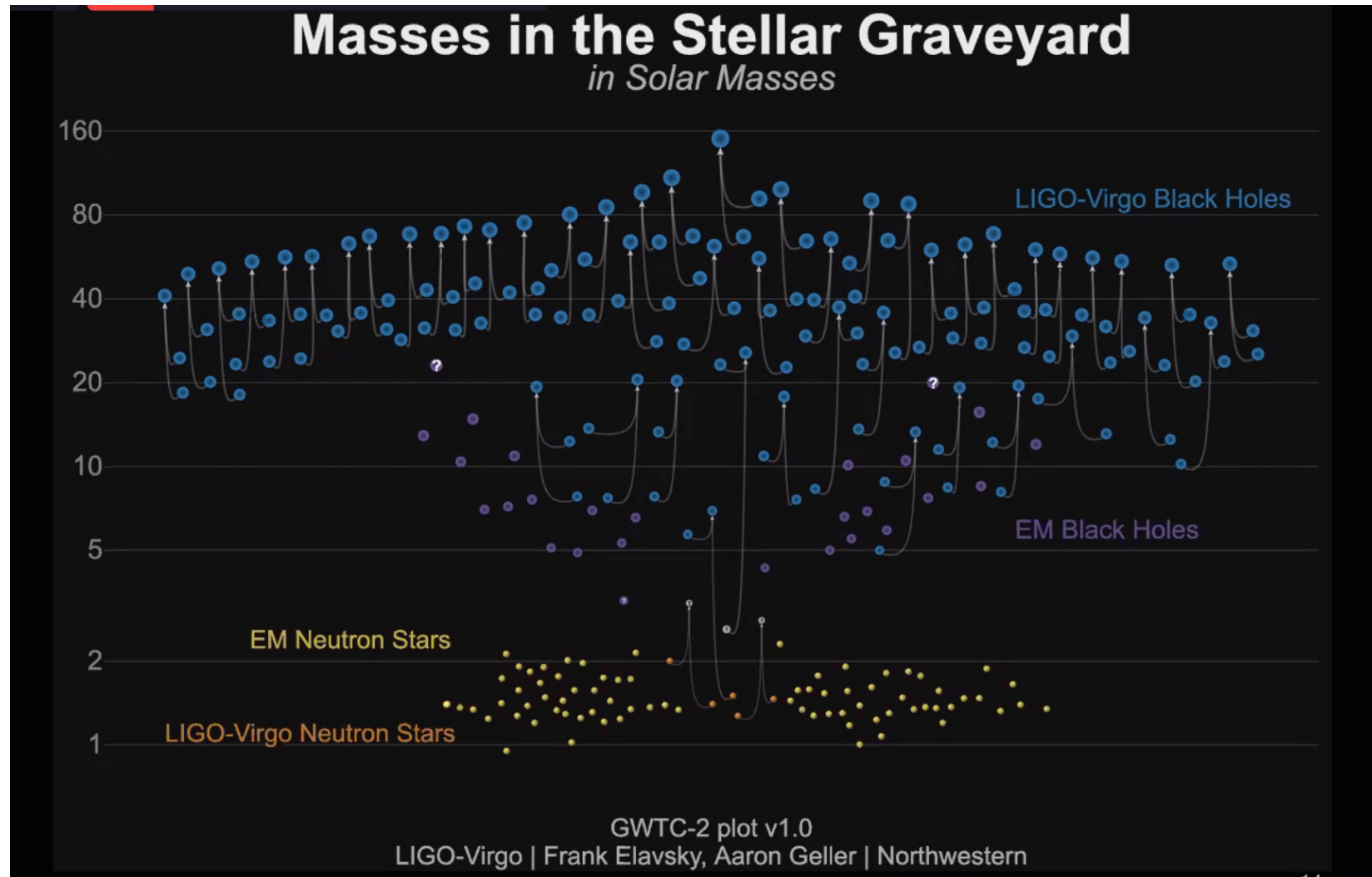
## CON

- \* Requires fine-tuning

**PBH can do it!**



# PBHS AND LIGO/Virgo/KAGRA



Do we need Population III or primordial BHs?

## RECENT PBH PAPERS

### **PBHs, dark matter and hot-spot electroweak baryogenesis at the QCD epoch**

Bernard Carr,<sup>1\*</sup> Sebastien Clesse,<sup>2,3</sup> and Juan García-Bellido<sup>4</sup>

[arXiv:1904.02129](#)

A common origin of baryons and dark matter via the gravitational collapse of black holes in the early universe

Juan García-Bellido<sup>a,\*</sup> Bernard Carr<sup>b,c,†</sup> and Sébastien Clesse<sup>d,e‡</sup>

[arXiv:1904.11482](#)

### **Cosmic Conundra Explained by Thermal History and Primordial Black Holes**

Bernard Carr,<sup>1,2,\*</sup> Sébastien Clesse,<sup>3,4,†</sup> Juan García-Bellido,<sup>5,‡</sup> and Florian Kühnel<sup>6,§</sup>

[arXiv:1906.08217](#)

### **Constraints on Stupendously Large Black Holes**

Bernard Carr,<sup>1,2,\*</sup> Florian Kühnel,<sup>3,†</sup> and Luca Visinelli<sup>4,‡</sup>

[arXiv:2008.08077](#)

### **Black Holes and WIMPs: All or Nothing or Something Else**

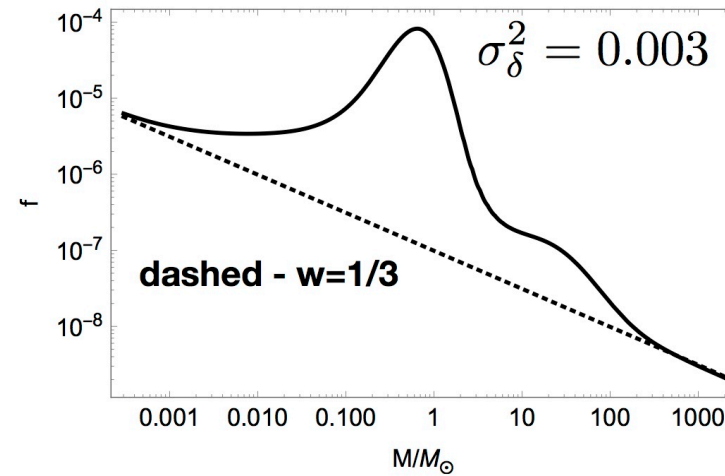
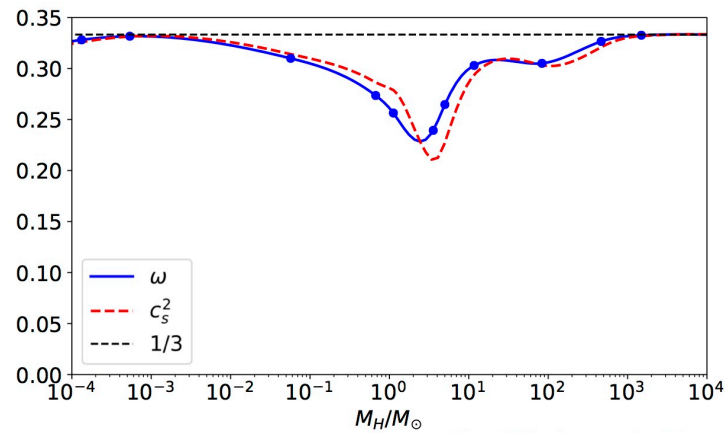
Bernard Carr,<sup>1,2,\*</sup> Florian Kühnel,<sup>3,†</sup> and Luca Visinelli<sup>4,5,‡</sup>

[arXiv:2011.01930](#)

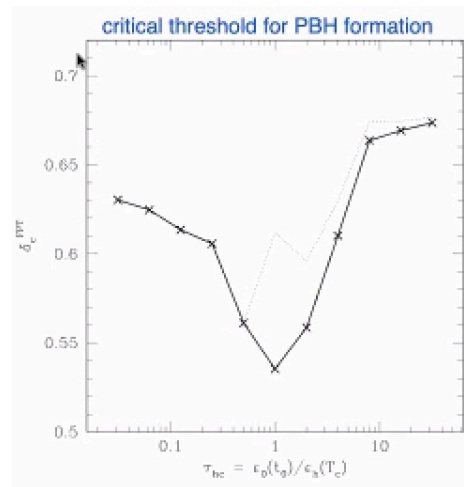
# Primordial black holes with an accurate QCD equation of state

Christian T. Byrnes,<sup>1,\*</sup> Mark Hindmarsh,<sup>1,2,†</sup> Sam Young,<sup>1,‡</sup> and Michael R. S. Hawkins<sup>3,§</sup>

arXiv:1801.06138



Jedamzik (1996)



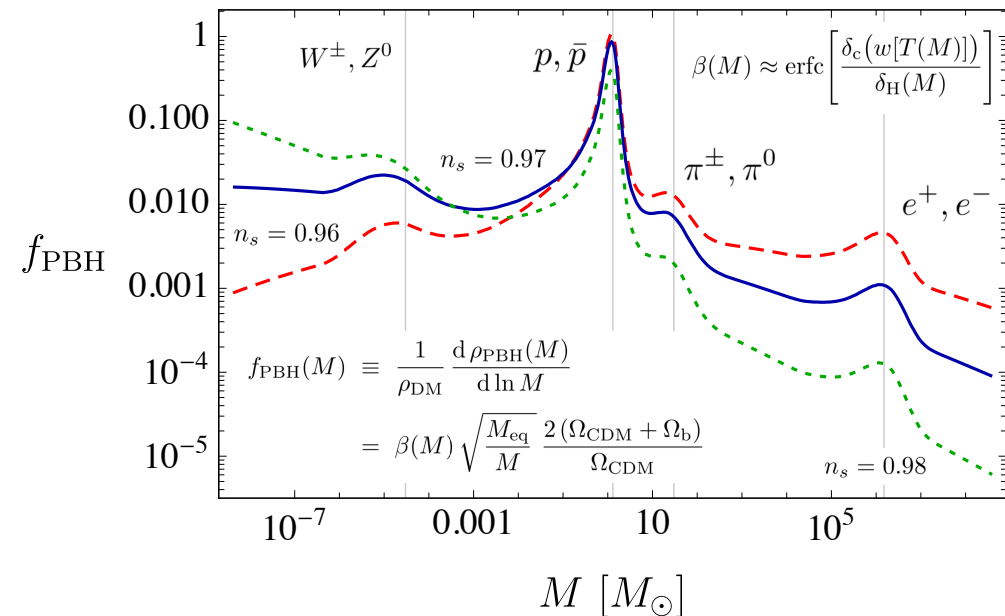
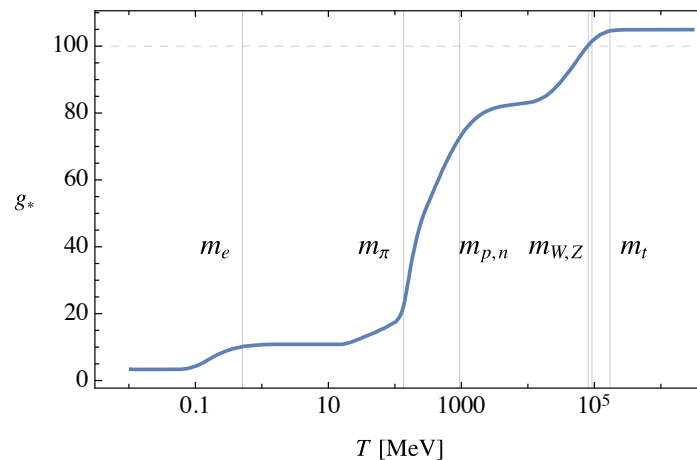
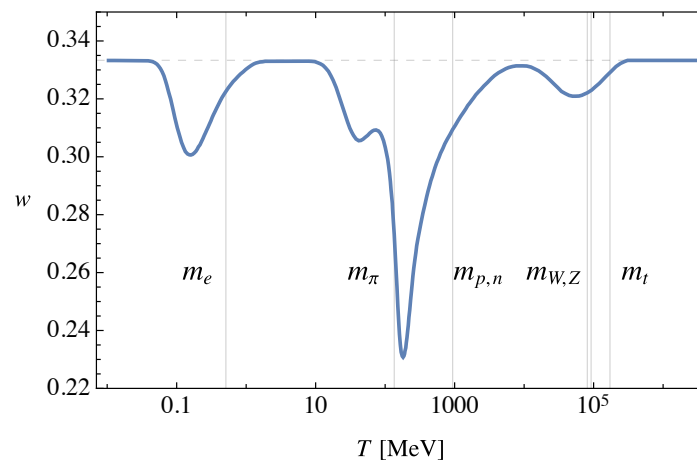


# Cosmic Conundra Explained by Thermal History and Primordial Black Holes

Bernard Carr,<sup>1,2,\*</sup> Sébastien Clesse,<sup>3,4,†</sup> Juan García-Bellido,<sup>5,‡</sup> and Florian Kühnel<sup>6,§</sup>

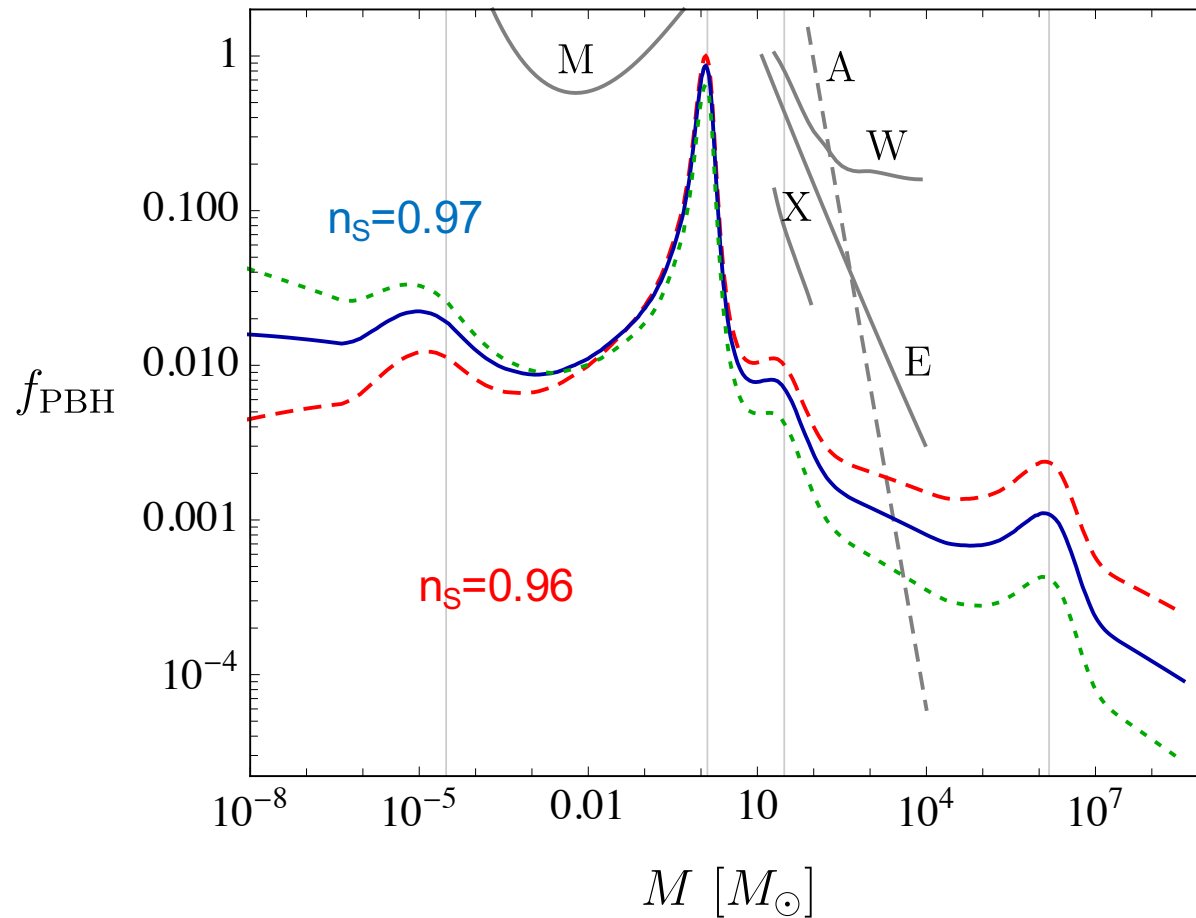
arXiv:1906.08217

Extend this to include other stages in thermal history



- ▶ Nearly scale-invariant PS
- ▶ Spectral index:  $n_s = 0.97$
- ▶ Peak at  $\sim 2 M_\odot$
- ▶ Second peak at  $\sim 30 M_\odot$
- ▶ Two bumps at  $10^{-6}$  and  $10^6 M_\odot$

# CONSTRAINTS



$$\delta_{\text{rms}}(M) = A \left( \frac{M}{M_\odot} \right)^{(1-n_s)/4}$$

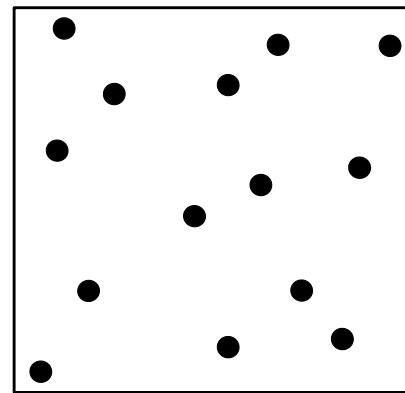
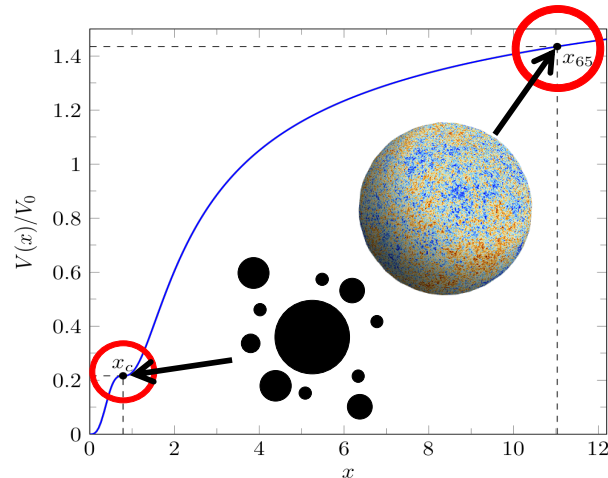
$$f_{\text{PBH}}^{\text{max}} = \left( \int d \ln M \frac{f_{\text{PBH}}(M)}{f_p^{\text{mon}}(M)} \right)^{-1}$$

Overproduce light PBHs for  $n_s > 0.975$

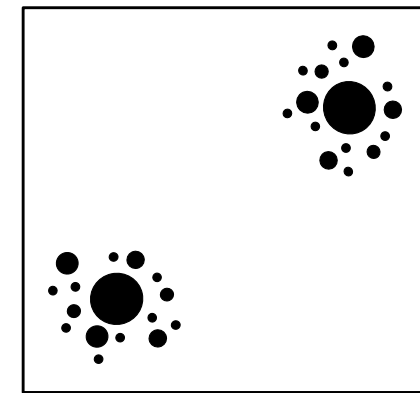
Overproduce heavy PBHs for  $n_s < 0.965$

# ARE PBHS CLUSTERED?

- Inflation =>
- Lognormal wide-mass distribution JGB & Clesse (2017)
  - Clusters of PBH:  $N_{cl} \sim 100-1000$  , comoving size  $\sim 1\text{ mpc}$



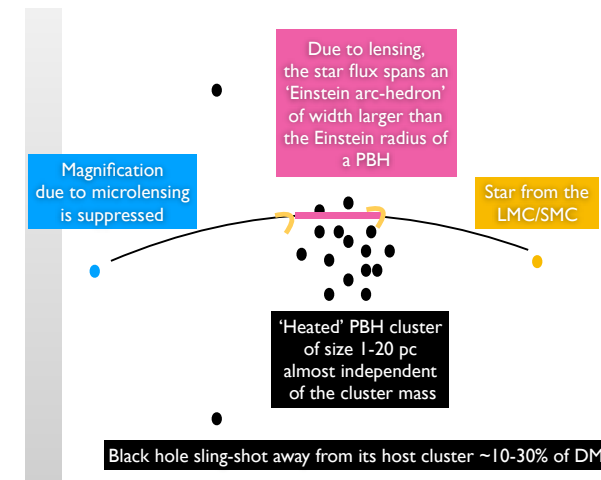
uniform single-mass  
is already ruled out



clustered wide-mass  
is still viable

[slide credit: JGB]

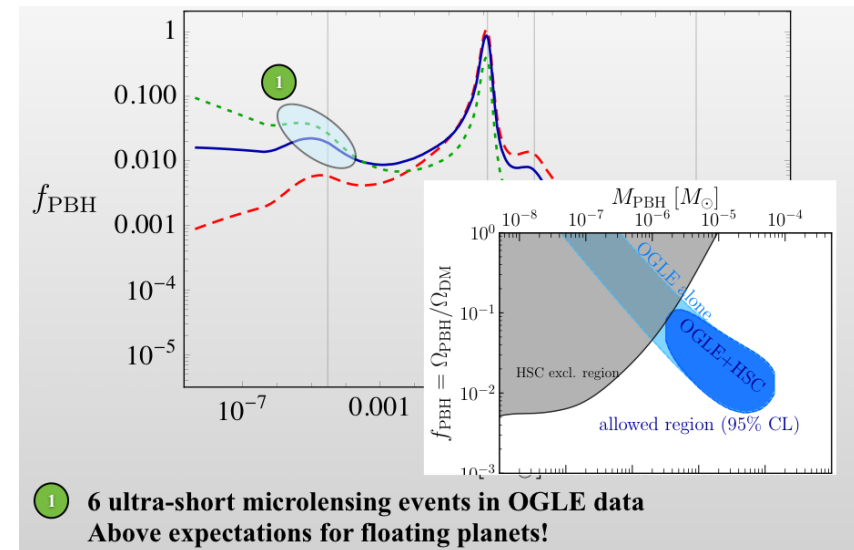
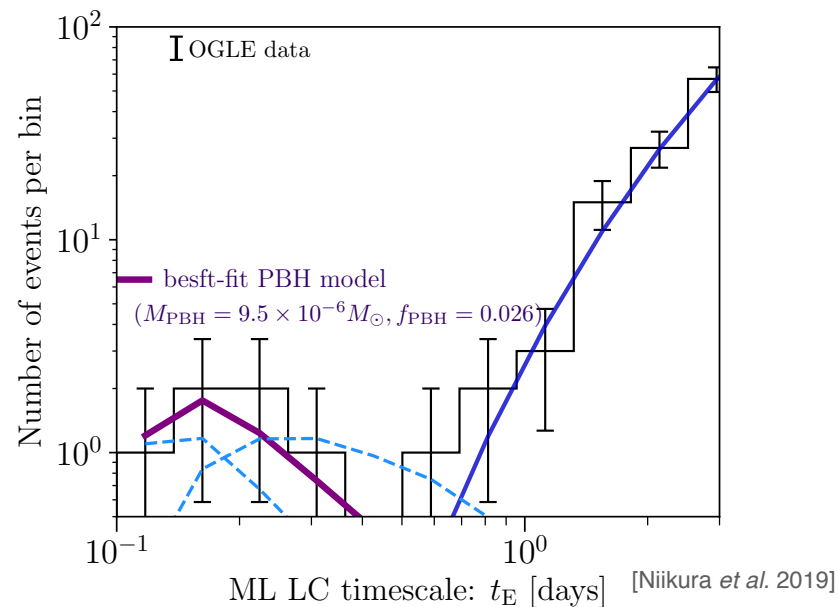
But controversial....



# Planetary-mass microlenses

OGLE detected microlenses on 0.1-0.3 day timescale of unknown origin – free-floating planets or PBHs?

Niikura et al. (2019)



# Quasar microlensing

## Evidence for dark matter in the form of compact bodies

Michael Hawkins  
University of Edinburgh

### Evidence for Microlensing

- Lack of time dilation.
- Symmetry of variation.
- Achromatic variation.
- Microlensing in multiply lensed quasars
- Caustic features in light curves
- Slope of structure function

The timescale of variation implies that the mass of the microlensing bodies is around  $0.1 M_{\odot}$

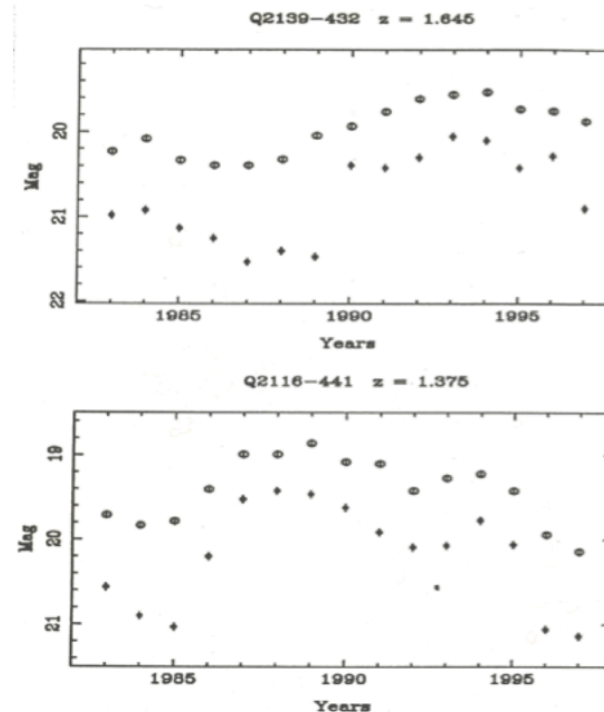
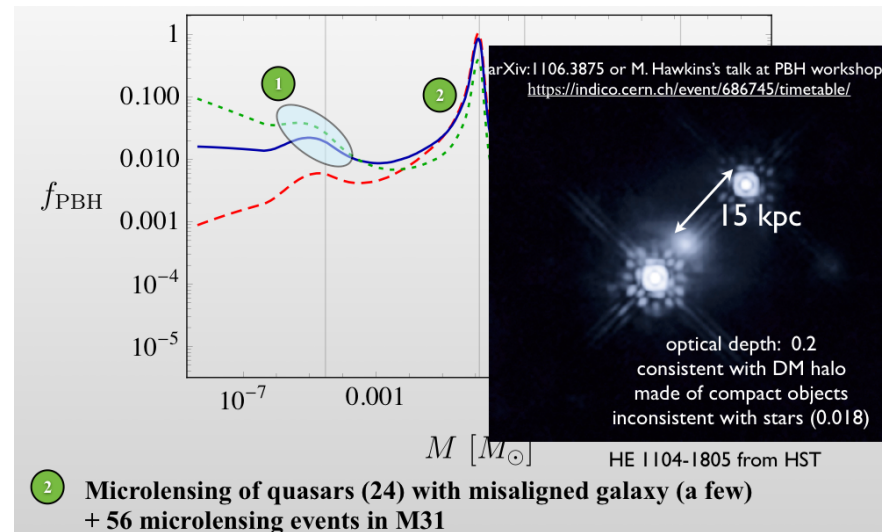
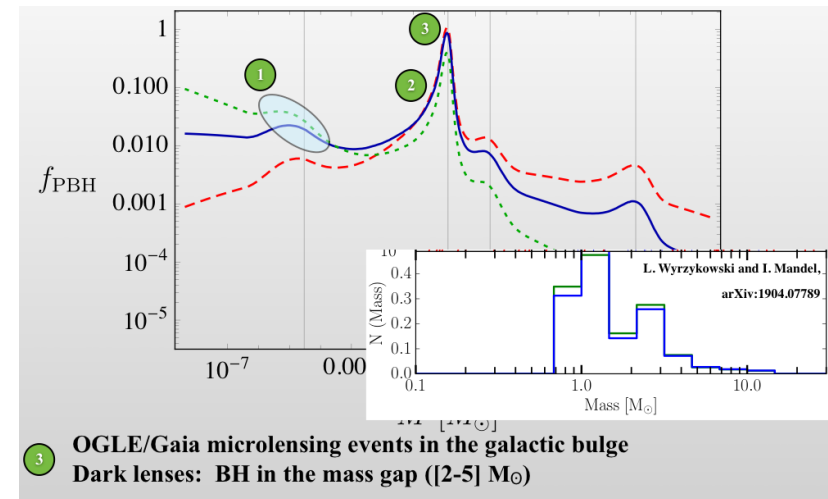
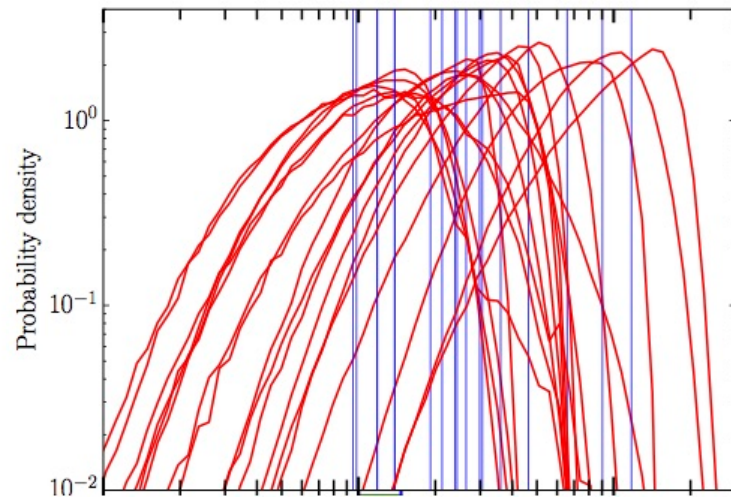


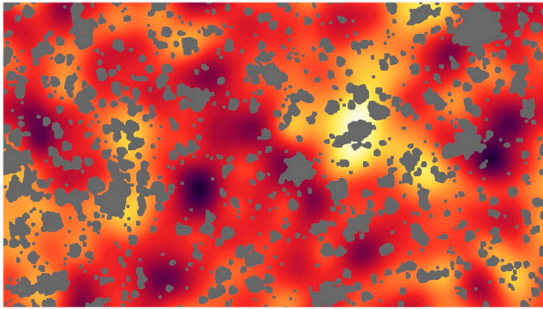
Fig. 3. Light curves for two quasars showing all the characteristic expected of caustic crossing events. Symbols as for Fig. 1.

# OGLE/GAIA excess of lenses in Galactic bulge

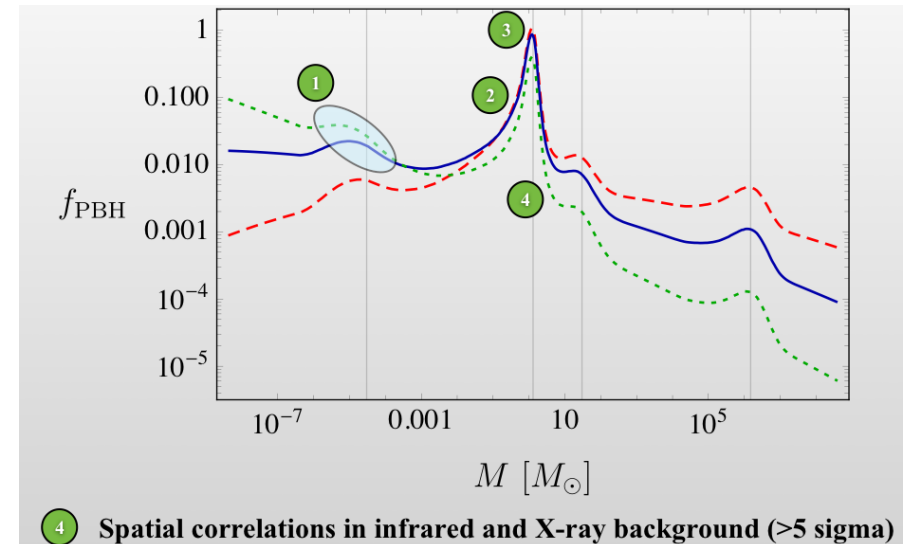


# Cosmic infrared/X-ray backgrounds

PBHs generate early structure  
and infrared background



Kashlinsky  
arXiv:1605.04023

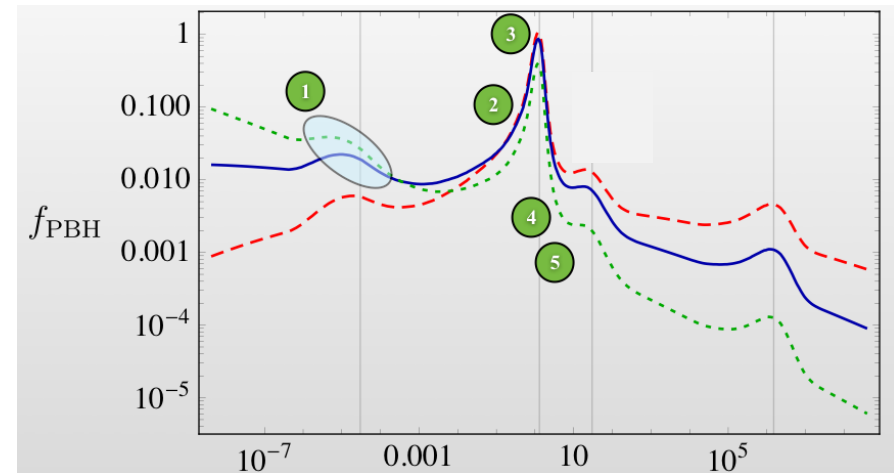
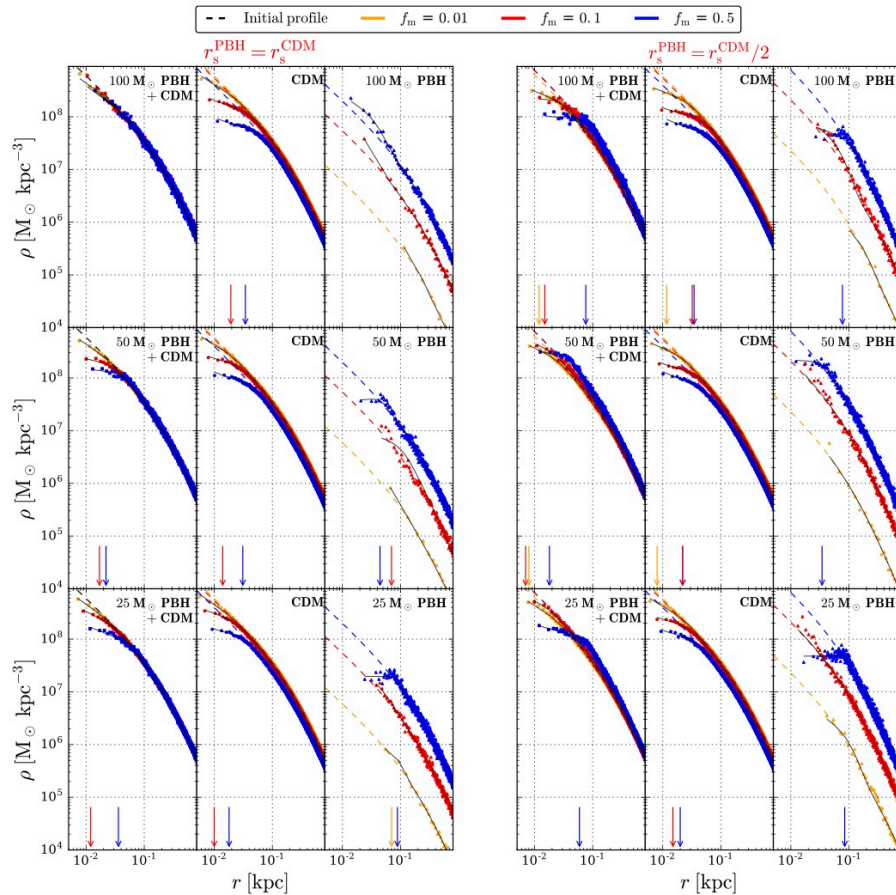




# Ultra-faint dwarf galaxies

5

## Minimum radius of (ultra-faint) dwarf galaxies and cored DM profiles

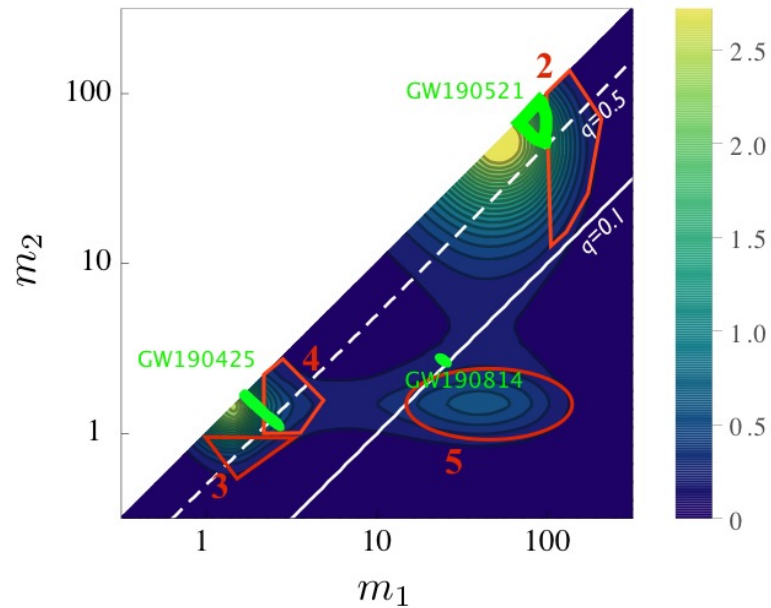


PBHs as dark matter: cusp-to-core  
transition in low-mass dwarf galaxies

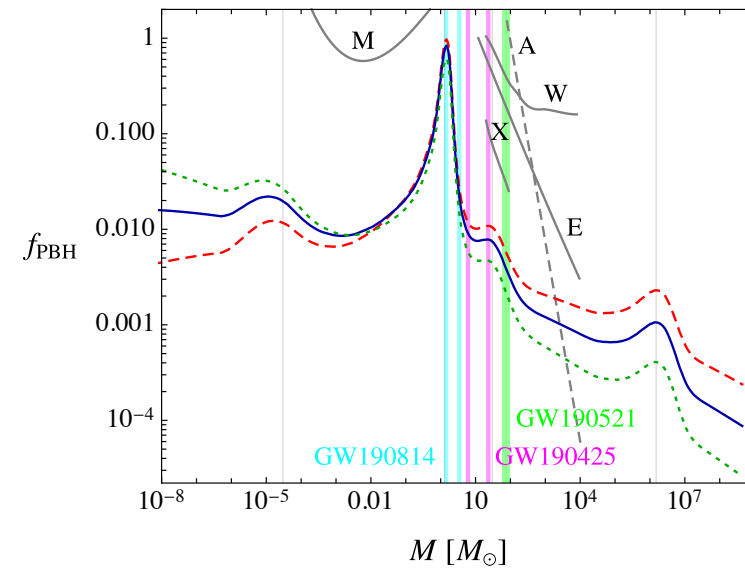
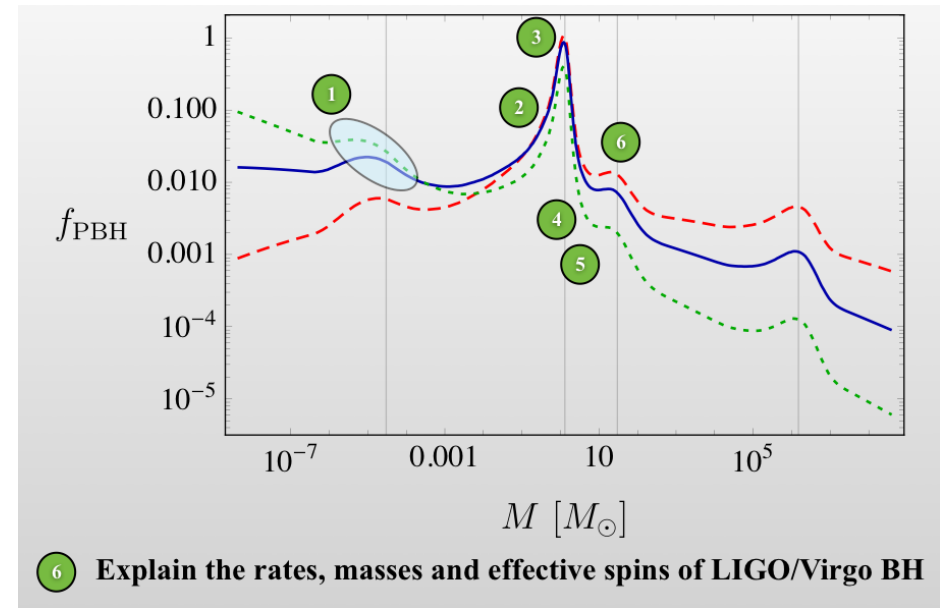
Boldrini et al.

arXiv:1909.07395

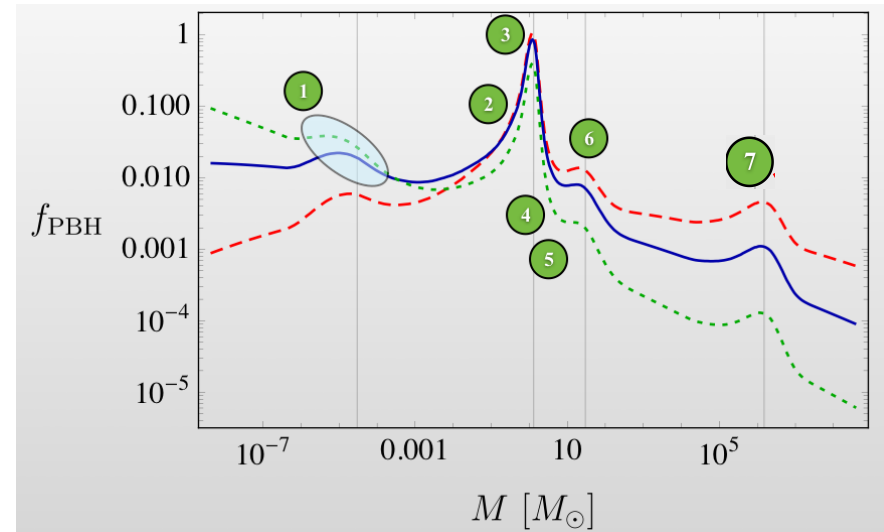
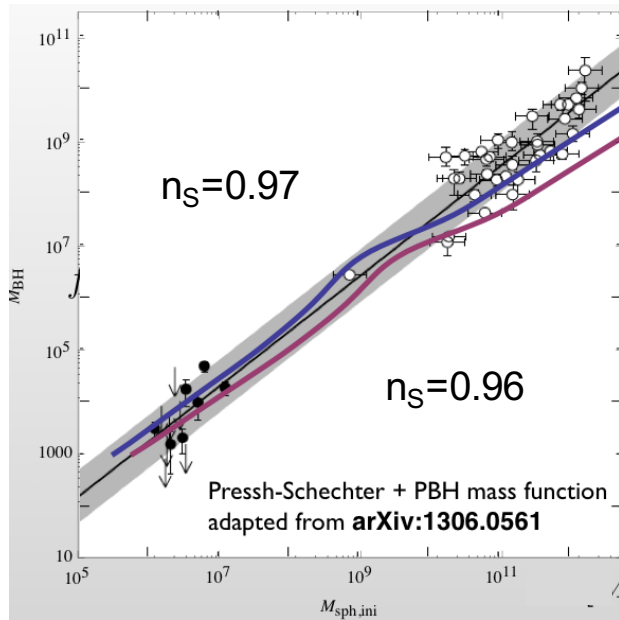
# LIGO/Virgo black holes



Successful prediction!

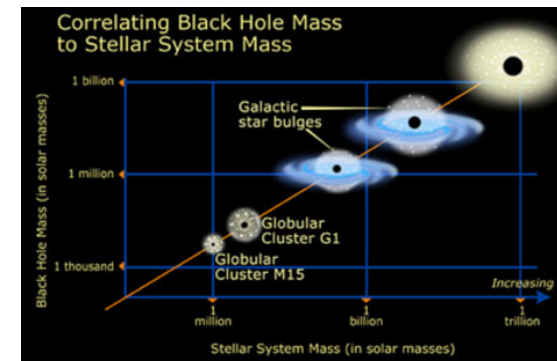


# Intermediate and supermassive black holes



7 Right number of intermediate and supermassive black holes

$n_s = 0.97 \Rightarrow$  observed ratio of BH and halo mass if  $f_{\text{PBH}} \sim 1$ .



# ADDRESSING FINE-TUNING PROBLEM AT QCD EPOCH \*

Carr, Clesse & Garcia-Bellido

arXiv:1904.02129

PBHs forming at time  $t$  have mass and collapse fraction

$$M \sim 10^5 (t/s) M_{\odot}, \quad \beta(M) \sim 10^{-9} f(M) (M/M_{\odot})^{1/2}$$

So  $\beta$  appears fine-tuned and we must also explain why

$$\chi = \rho_{\text{PBH}}/\rho_B = f \rho_{\text{DM}}/\rho_B = 6 f \text{ is } O(1).$$

$\chi \gg 1 \Rightarrow t_{\text{eq}} \ll t_{\text{dec}} \Rightarrow$  not enough baryons to make galaxies

$\chi \ll 1 \Rightarrow t_{\text{deq}} \gg t_{\text{dec}} \Rightarrow$  fluctuations too small to make galaxies

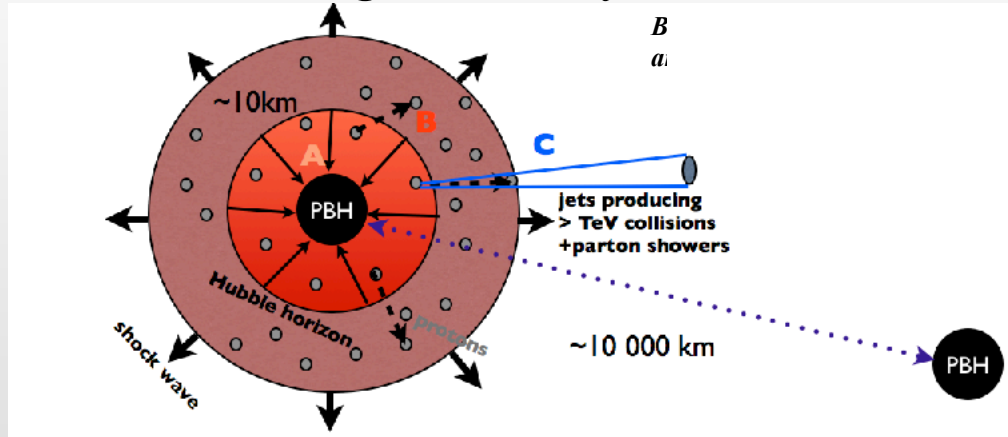
QCD epoch  $\Rightarrow M \sim M_{\text{C}} \sim 1 M_{\odot}$ ,  $\beta(M) \sim \eta = n_B/n_{\gamma} \sim 10^{-9}$  **anthropic selection?**

$\Rightarrow$  dark matter and visible baryons have similar mass  
PBHs may *generate* baryon asymmetry

\* PBHs from the QCD epoch: Linking dark matter, baryogenesis and anthropic selection

# Primordial Black Holes

as a common origin of baryons and dark matter



Garcia-Bellido,  
Carr & Clesse

arXiv:1904.114827

- C and CP violation of the standard model (CKM matrix)
- Baryon number violation: sphaleron transitions from  $> \text{TeV}$  collisions
- Out of thermal equilibrium (PBH collapse)

$$\Delta K \simeq \left( \frac{1}{\gamma} - 1 \right) M_H \quad E_0 = \frac{\Delta K}{n_p \Delta V} \quad k_B T_{\text{eff}} = \frac{2}{3} E_0 \simeq 5 \text{ TeV}$$

$$\delta_{\text{CP}}(T) = 3 \times 10^{-5} (20.4 \text{ GeV}/T)^{12} \quad \text{above sphaleron barrier}$$

$$\chi \approx \gamma/(1 - \gamma) \approx 5 \text{ if } \gamma \approx 0.8$$

$$\eta_{\text{loc}} \sim 1 \Rightarrow \eta \sim \beta \text{ and } \chi \sim 1 \text{ after diffusion of baryon asymmetry}$$

# Curvature perturbation scenario

Natural peak in PBH mass function but need to fine-tune pert' amp'

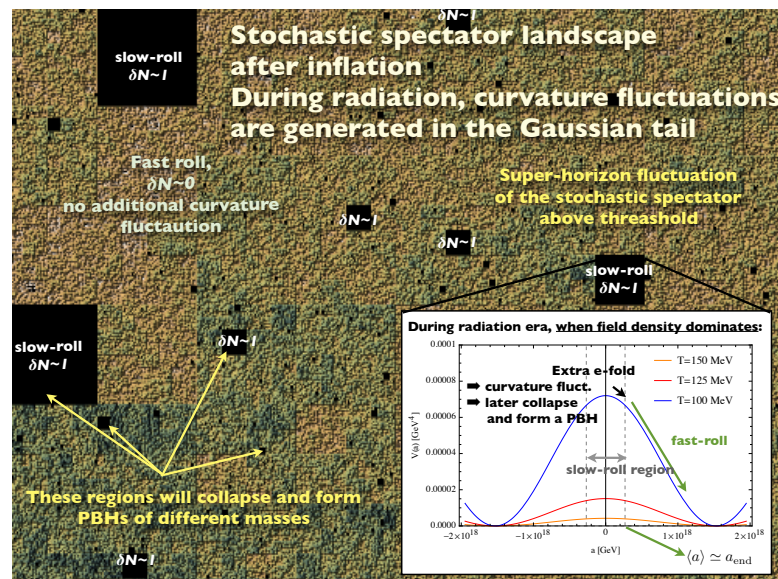
Stochastic fluct'ns in spectator field during inflation

⇒ different values in different patches

⇒ frozen until pot' energy dominates density long after inflation

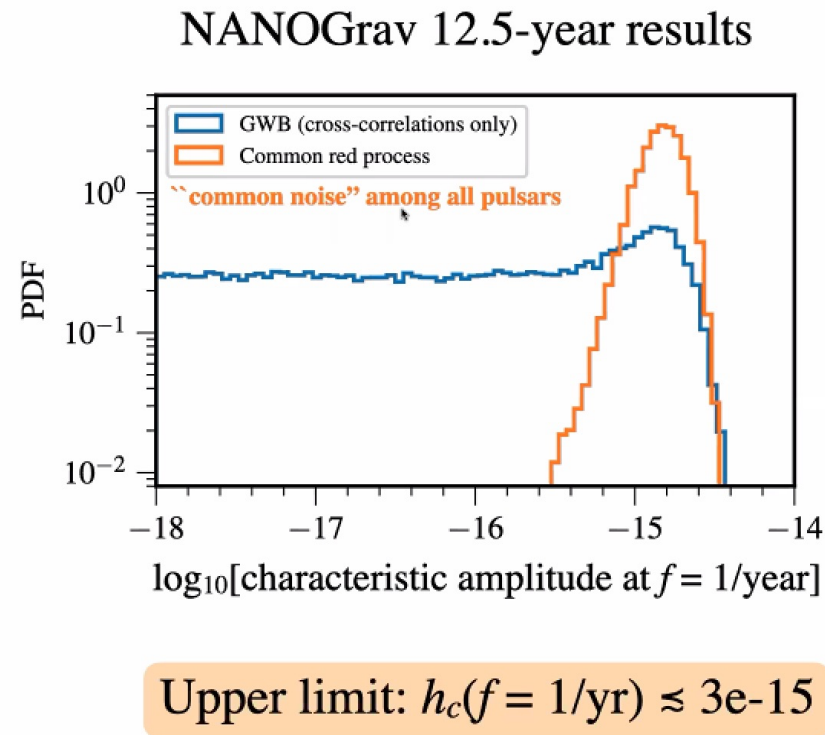
⇒ 2<sup>nd</sup> inflation phase within region (few e-folds)

⇒ non-linear perturbations => PBHs.



In the stochastic spectator scenario: no parameter tuning,  
but unavoidable **anthropic selection** due to the field **stochasticity**

# Pulsar Timing Array Constraints on PBHs with NANOGrav

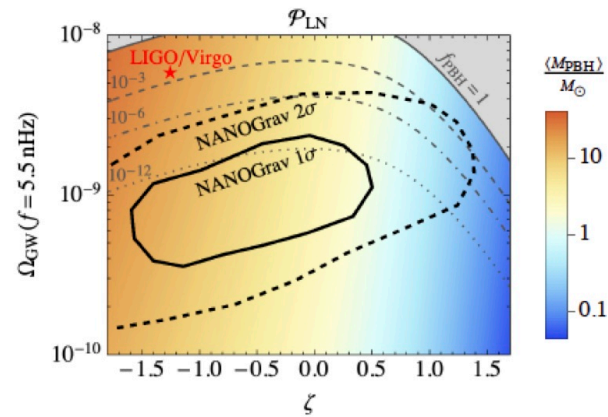


Kapadia et al. [arXiv:2009.05514](https://arxiv.org/abs/2009.05514)

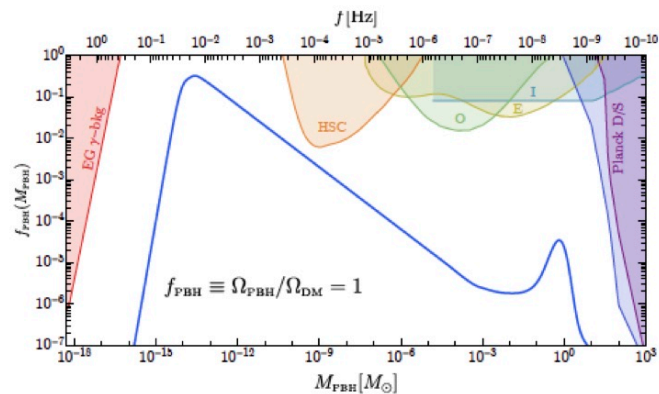
Four recent claims of positive detection?



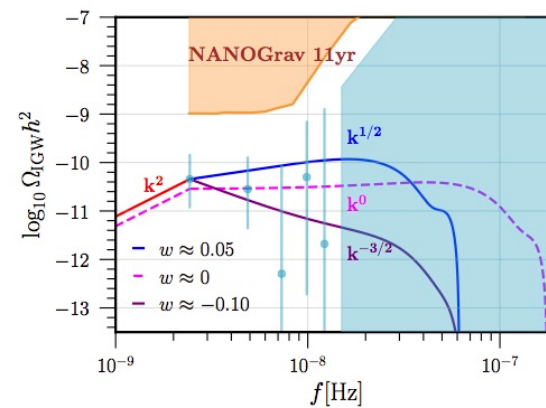
Vaskonen & Veermae  
2009.07832  
 $M \sim 10^3 - 10^6 M_\odot, f < 10^{-4}$



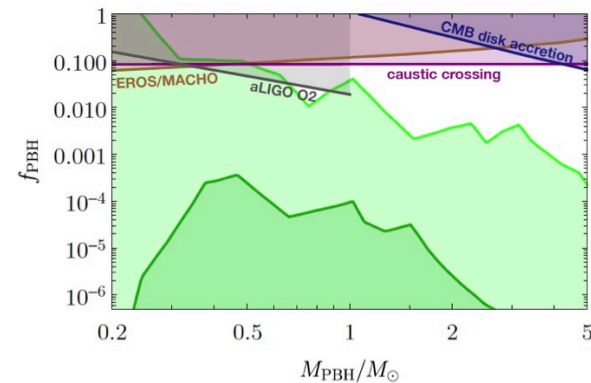
De Luca et al.  
2009.08268  
 $M \sim 10^{-15} - 10^{-11} M_\odot, f \sim 1$



Domenech & Shi Pi  
2010.03976  
 $M \sim 10^3 - 10^6 M_\odot, f < 10^{-4}$



Kohri & Terada  
2009.11853  
 $M \sim 1 M_\odot, f = 10^{-3}$

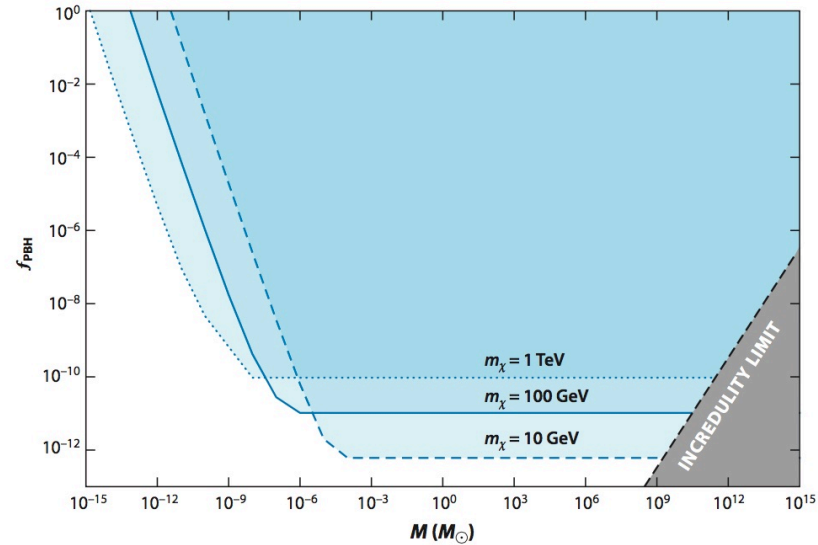
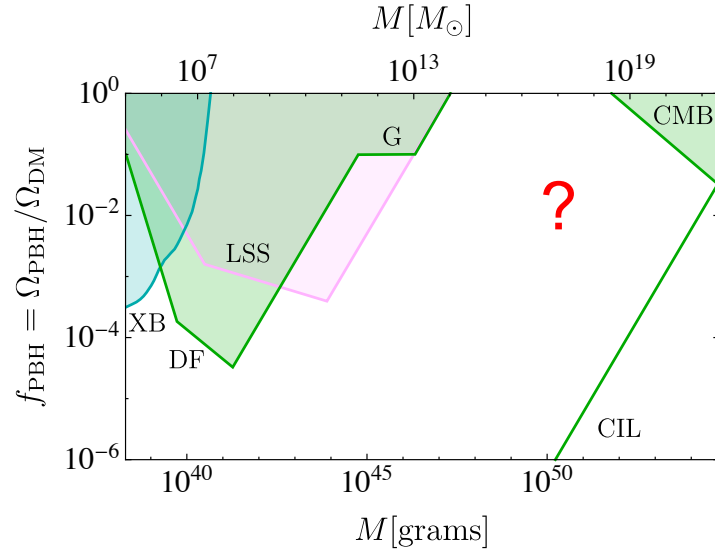


# Constraints on Stupendously Large Black Holes

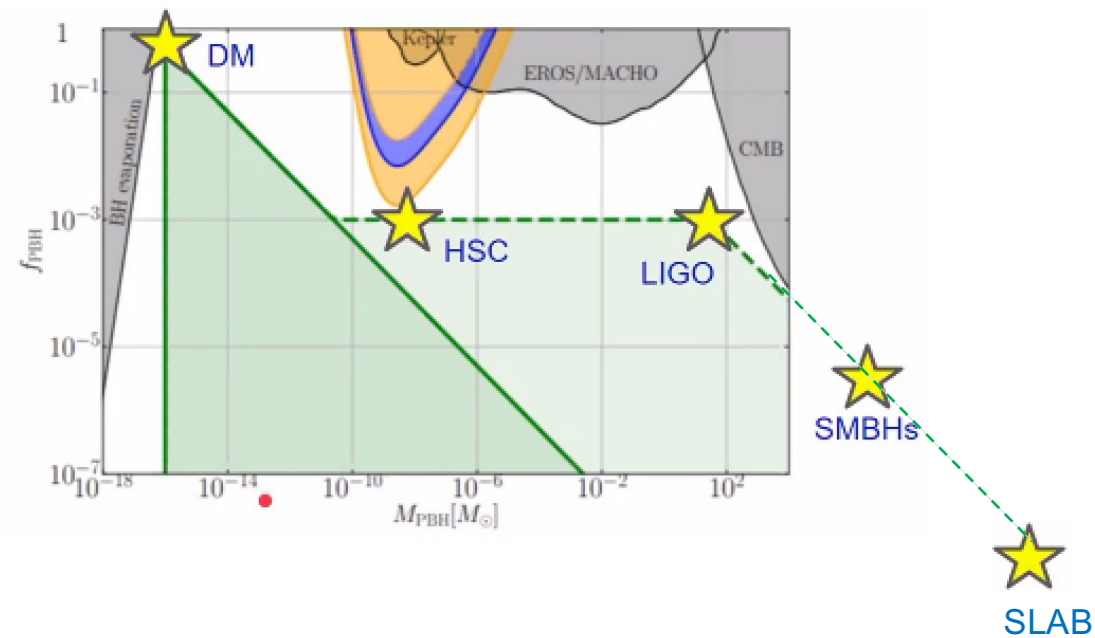
Bernard Carr,<sup>1,2,\*</sup> Florian Kühnel,<sup>3,†</sup> and Luca Visinelli<sup>4,‡</sup>

arXiv:2008.08077

We consider the observational constraints on stupendously large black holes (SLABs) in the mass range  $M \gtrsim 10^{11} M_\odot$ . These have attracted little attention hitherto and we are aware of no published constraints on a SLAB population in the range  $(10^{12} - 10^{18}) M_\odot$ . However, there is already evidence for black holes of up to nearly  $10^{11} M_\odot$  in galactic nuclei, so it is conceivable that SLABs exist and they may even have been seeded by primordial black holes. We focus on limits associated with (i) dynamical and lensing effects, (ii) the generation of background radiation through the accretion of gas during the pregalactic epoch, and (iii) the gamma-ray emission from the annihilation of the halo of weakly interacting massive particles (WIMPs) expected to form around each SLAB if these provide the dark matter. Finally, we comment on the constraints on the mass of ultra-light bosons from future measurements of the mass and spin of SLABs.



## PBH DM from Bubble Multiverse



Generalized model for everything



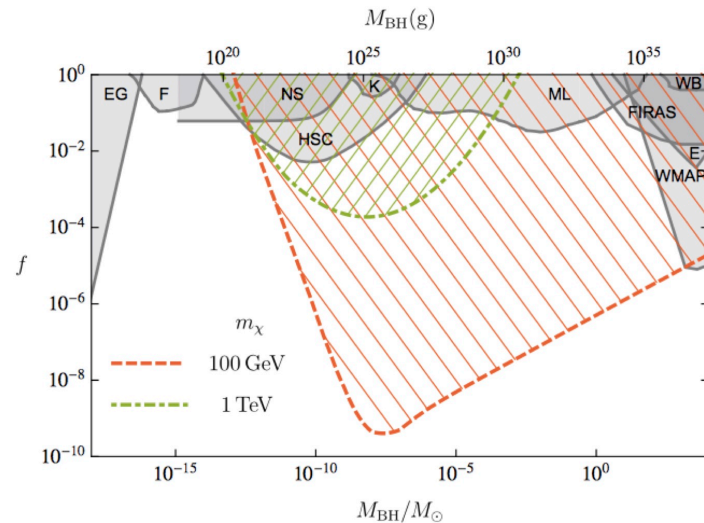
# Black Holes and WIMPs: All or Nothing or Something Else

Bernard Carr,<sup>1,2,\*</sup> Florian Kühnel,<sup>3,†</sup> and Luca Visinelli<sup>4,5,‡</sup>

arXiv:2011.01930

We consider constraints on primordial black holes (PBHs) in the mass range  $(10^{-18}-10^{15}) M_{\odot}$  if the dark matter (DM) comprises weakly interacting massive particles (WIMPs) which form halos around them and generate  $\gamma$ -rays by annihilations. The observed extragalactic  $\gamma$ -ray background then implies that the PBH DM fraction is  $f_{\text{PBH}} \lesssim 10^{-10} (m_{\chi}/\text{TeV})^{1.1}$  in the mass range  $2 \times 10^{-11} M_{\odot} (m_{\chi}/\text{TeV})^{-3.2} \lesssim M \lesssim 3 \times 10^{11} M_{\odot} (m_{\chi}/\text{TeV})^{1.1}$ , where  $m_{\chi}$  and  $M$  are the WIMP and PBH masses, respectively. This limit is independent of  $M$  and therefore applies for any PBH mass function. For  $M \lesssim 2 \times 10^{-11} M_{\odot} (m_{\chi}/\text{TeV})^{-3.2}$ , the constraint on  $f_{\text{PBH}}$  is a decreasing function of  $M$  and PBHs could still make a significant DM contribution at very low masses. We also consider constraints on WIMPs if the DM is mostly PBHs. If the merging black holes recently discovered by LIGO/Virgo are of primordial origin, this would rule out the standard WIMP DM scenario. More generally, the WIMP DM fraction cannot exceed  $10^{-4}$  for  $M > 10^{-9} M_{\odot}$  and  $m_{\chi} > 10 \text{ GeV}$ . There is a region of parameter space, with  $M \lesssim 10^{-11} M_{\odot}$  and  $m_{\chi} \lesssim 100 \text{ GeV}$ , in which WIMPs and PBHs can both provide some but not all of the DM, so that one requires a third DM candidate.

## WIMPs and PBHs are incompatible



Hybrid models with PBHs and WIMPs  
=> clumping of WIMPs around PBHs  
=> enhanced annihilations  
=>  $\gamma$ -ray signals which should be seen.

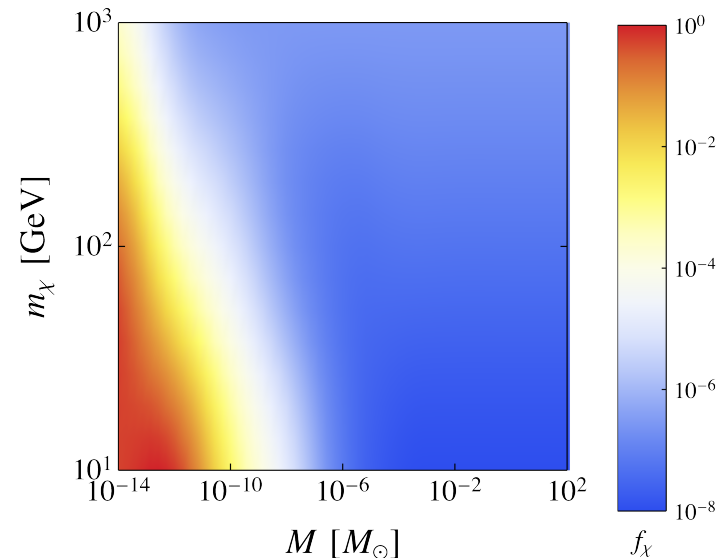
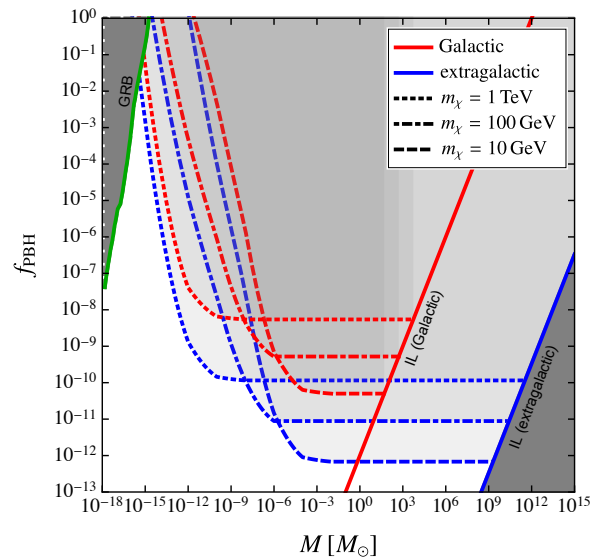
Lacki & Beacom 2010, Eroshenko 2016, Boucenna, Kuhnel & Visinelli 2017;  
Adamek, Byrnes, Gosenca & Hotchkiss 2019; Cai, Yang & Zhou 2020.

Consider as wide a range of masses for the two components as possible.

PBH mass  $10^{-18} - 10^{15} M_{\odot}$  , WIMP mass 10 GeV - 1 TeV

Distinguish between Galactic and extragalactic  $\gamma$ -ray backgrounds.

$m_\chi$ (GeV)	$f_{\text{PBH}}^{\text{gal}}$	$f_\chi^{\text{gal}}$	$f_{\text{PBH}}^{\text{eg}}$	$f_\chi^{\text{eg}}$
$10^1$	$5 \times 10^{-11}$	$6 \times 10^{-7}$	$7 \times 10^{-13}$	$5 \times 10^{-8}$
$10^2$	$5 \times 10^{-10}$	$3 \times 10^{-6}$	$9 \times 10^{-12}$	$2 \times 10^{-7}$
$10^3$	$5 \times 10^{-9}$	$1 \times 10^{-5}$	$1 \times 10^{-10}$	$1 \times 10^{-6}$
$10^4$	$6 \times 10^{-8}$	$4 \times 10^{-5}$	$2 \times 10^{-9}$	$5 \times 10^{-6}$



For most of parameter space, one component completely dominates

$f_{\text{PBH}} > 0.01$  above  $10^{-9} M_\odot \Rightarrow$  canonical WIMP scenario excluded

LIGO/Virgo PBHs  $\Rightarrow$  WIMPs and PBHs have  $f_{\text{DM}} < 1 \Rightarrow$  third DM candidate

## CONCLUSIONS

PBH studies have already led to profound insights into cosmology and fundamental physics, even if they never formed.

Until recently most work focused on PBH constraints but now they have been invoked for numerous cosmological purposes:

Cosmic rays

Dark matter

LIGO/Virgo

Other conundra

These are distinct roles but PBHs with extended mass function could play all of them with fine-tuning of collapse fraction.

PBHs naturally form at QCD epoch and could explain both dark matter and baryon asymmetry with anthropic fine-tuning.