

**ICTS**

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TATA INSTITUTE OF FUNDAMENTAL RESEARCH

ICTS Seminar

Title : Moments of the Hurwitz zeta function with irrational shifts

Speaker : Anurag Sahay (Purdue University, USA)

Date : Friday, 07 November 2025

Time : 9:30 AM (IST)

Abstract : The Hurwitz zeta function is a shifted integer analogue of the Riemann zeta function, with a shift parameter $0 < \alpha \leq 1$. We will consider moments of the Hurwitz zeta function on the critical line with a focus on the case where the shift α is irrational. We will briefly review the deep literature on moments of the Riemann zeta function, before talking about the case of Hurwitz with rational α , which leads naturally into moments of products of Dirichlet L-functions. Heuristics involving random matrix theory can then be used to predict an asymptotic formula for all integer moments.

For irrational α , we will discuss recent work joint with Winston Heap investigating these moments, where we established that the fourth moment is of the order $T(\log T)^2$ assuming that α is not too well-approximable by rationals (concretely, when its irrationality exponent $\mu(\alpha)$ is less than 3).

Venue : Online

Zoom Link: <https://icts-res-in.zoom.us/j/93231938657?pwd=Jl8GbkIJTX7totWStWhCJMDKBLxYyn.1>

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