



HOT TOPICS IN FLAVOR PHYSICS

ALEXANDER LENZ

SIEGEN UNIVERSITY

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Outline:

- The usual suggestions for hot topics
- Not so well known
- Underdogs/Surprise



The usual Suspects:

- Independent experimental check of **anomalies**: ATLAS, CMS, Belle II plus higher precision, R_X, \dots **flavour anomalies**



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See e.g. Fleischer et al. or

Artuso, Borissov, AL 1511.09466

Peng $\approx \pm 1^\circ = \pm 17$ mrad

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- CPV in charm **This is now the experimental precision!**
 - Direct CPV plus control measurements $\Delta A_{CP} = A_{CP}(D^0 \rightarrow K^+K^-) - A_{CP}(D^0 \rightarrow \pi^+\pi^-)$
 - CPV in mixing
 - Baryonic analogue of $D \rightarrow \pi^+\pi^-, K^+K^-$: e.g. $\Lambda_c \rightarrow p\pi^0, \Sigma K$

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LHCb 1903.08726

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All theorists agree:
 ΔA_{CP} is clearly governed by NP!

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What is NP?

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P/T can currently not be calculated from first principles
Additional assumptions (**ideologies**) needed - they might be wrong!

See e.g.

[Wilkinson, AL 2011.04443](#)

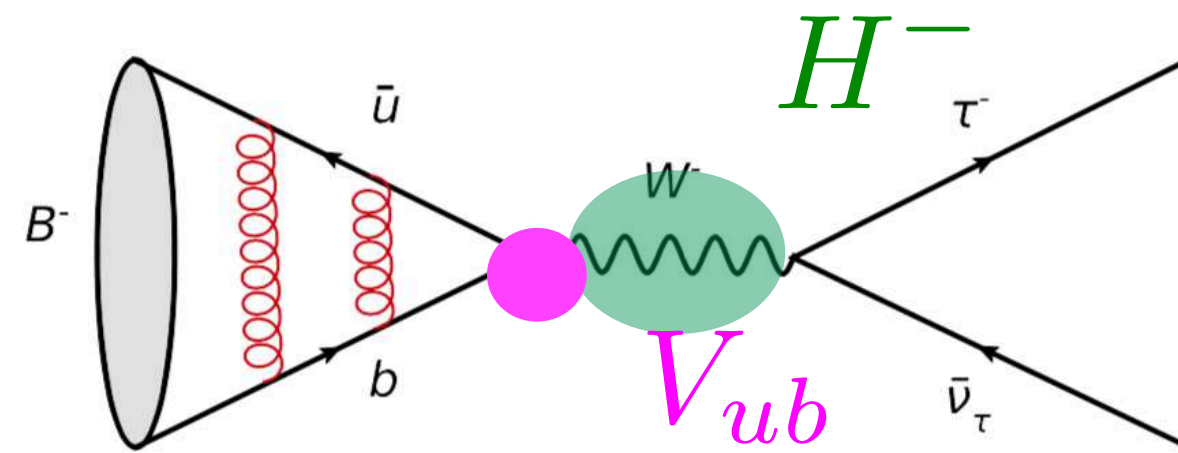
- **Ideology I:** NP = Non-perturbative physics
 - ◆ "Non-perturbative effects are known to be huge"
Analogy to the $\Delta I = 1/2$ rule
 - ◆ Good starting point for arguing:
 $\sin\phi \approx 1 \Rightarrow P/T = 1.3$ sufficient for $\Delta a_{CP} = -0.00329$
- **Ideology II:** NP = New physics
 - ◆ "Heavy quark expansion and factorisation are known to work well"
Analogy to the b -system
 - ◆ Good starting point for arguing:
 $\sin\phi \approx 1/10 \Rightarrow P/T = 13$ needed for $\Delta a_{CP} = -0.00329$



Control hadronic contributions in charm system

Hadronic Difficulty of Meson Decays

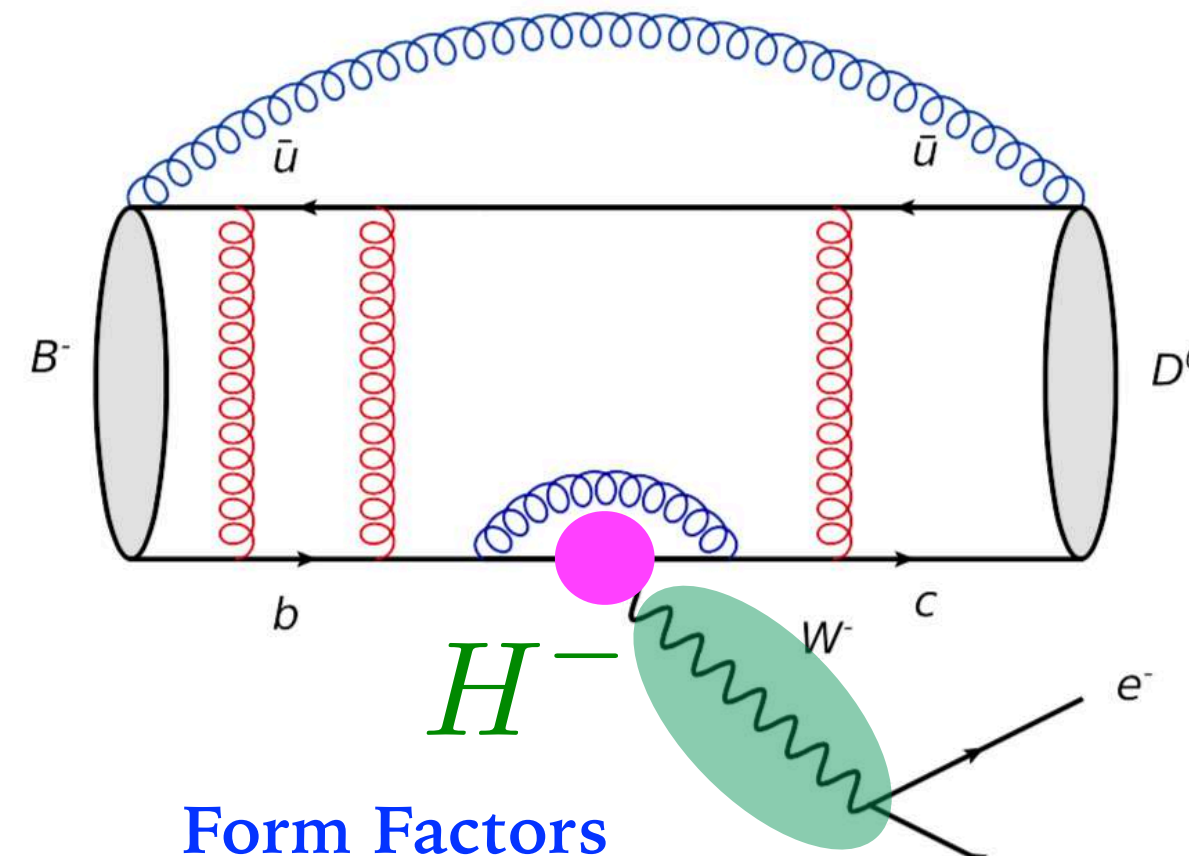
• Leptonic Decays



Decay constant

$$\langle 0 | \bar{b} \gamma^\mu \gamma_5 u | B_q(p) \rangle = i f_{B_q} p^\mu$$

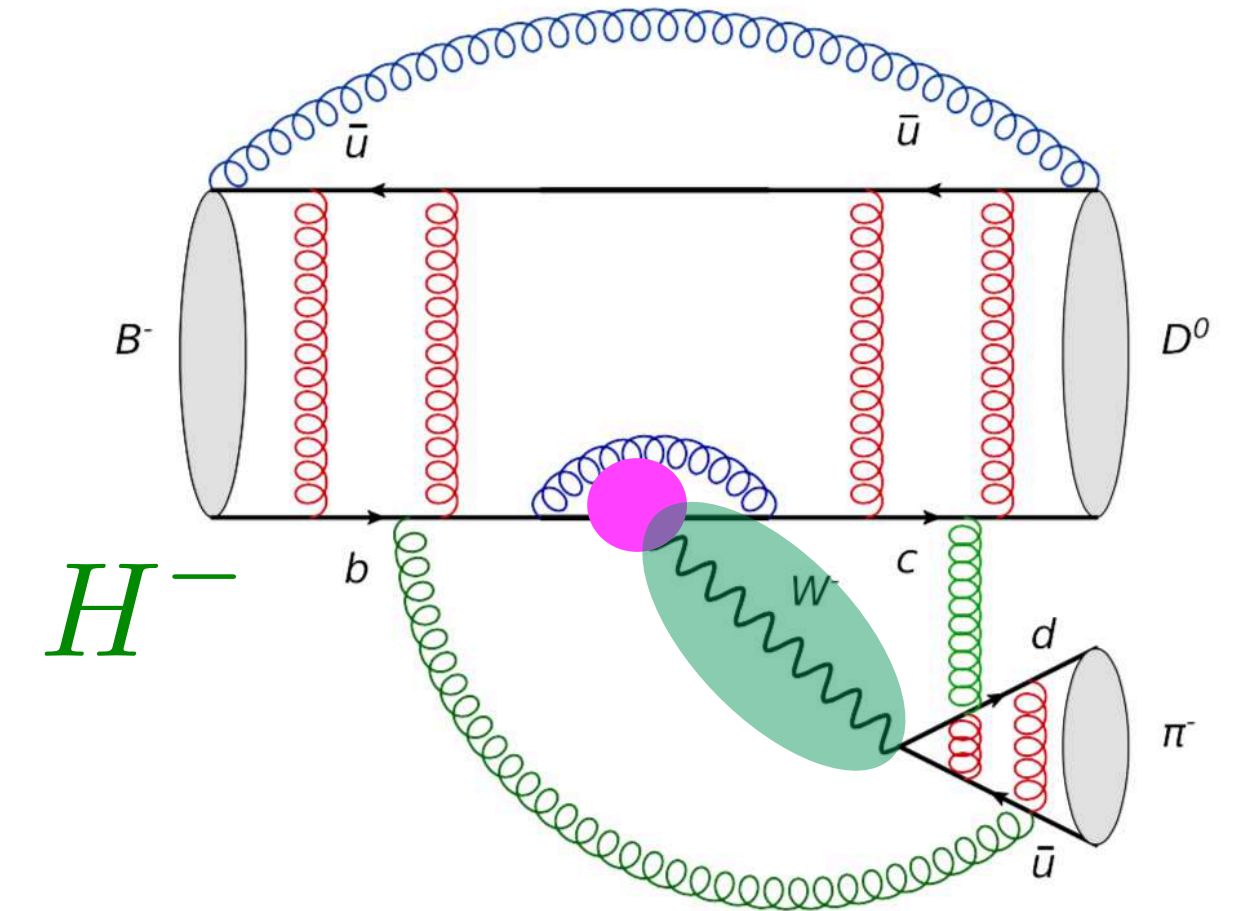
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Form Factors

$$\langle D^0(p_D) | \bar{c} \gamma_\mu b | B^-(p_B) \rangle = f_+^{B^- \rightarrow D^0}(q^2) \left(p_B^\mu + p_D^\mu - \frac{m_B^2 - m_D^2}{q^2} q^\mu \right)$$

• Non-leptonic Decays



Factorisation

$$\langle D^0 \pi^- | \bar{c} \gamma_\mu (1 - \gamma_5) b \cdot \bar{u} \gamma^\mu (1 - \gamma_5) d | B^- \rangle$$

$$\approx \langle D^0 | \bar{c} \gamma_\mu (1 - \gamma_5) b | B^- \rangle \cdot \langle \pi^- | \bar{u} \gamma^\mu (1 - \gamma_5) d | 0 \rangle$$

I) Imaginary part of CKM-elements = CP Violation

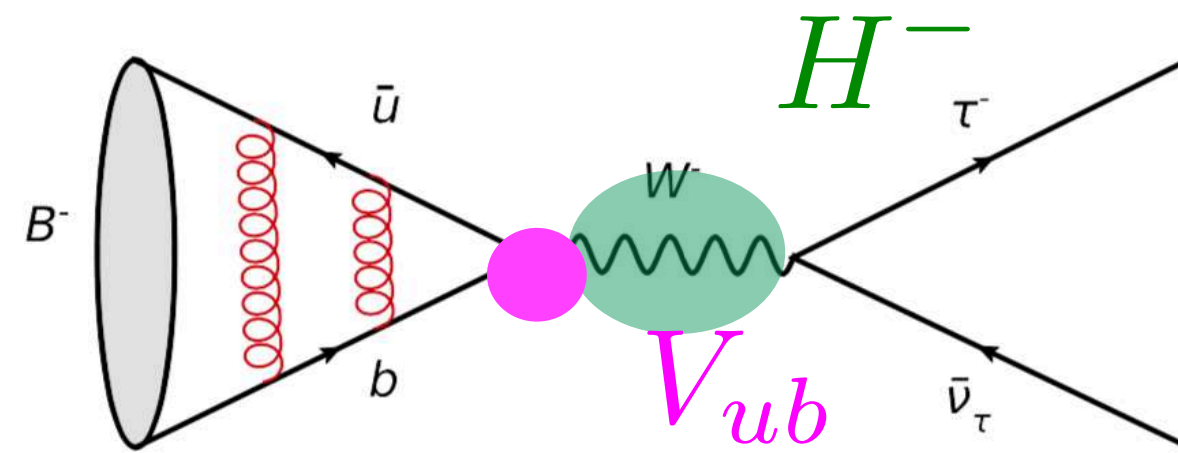
II) Instead of a W-Boson a charged Higgs particle could be exchanged

III) QCD effects are crucial! Perturbative QCD corrections
Non-perturbative: decay constants, form factors, factorisation

IV) Determination of SM-Parameter

Hadronic Difficulty of Meson Decays

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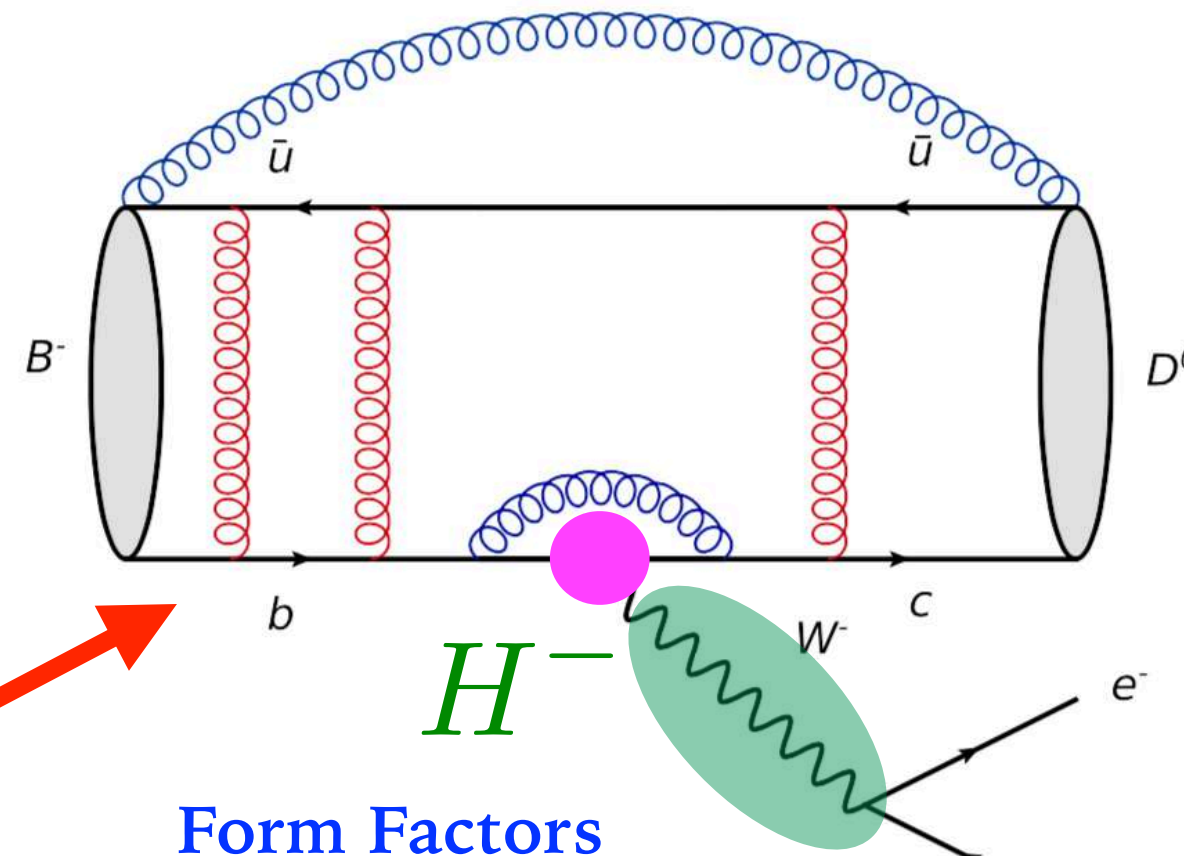
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Ancient B anomalies

Tree: V_{ub}, V_{cb}

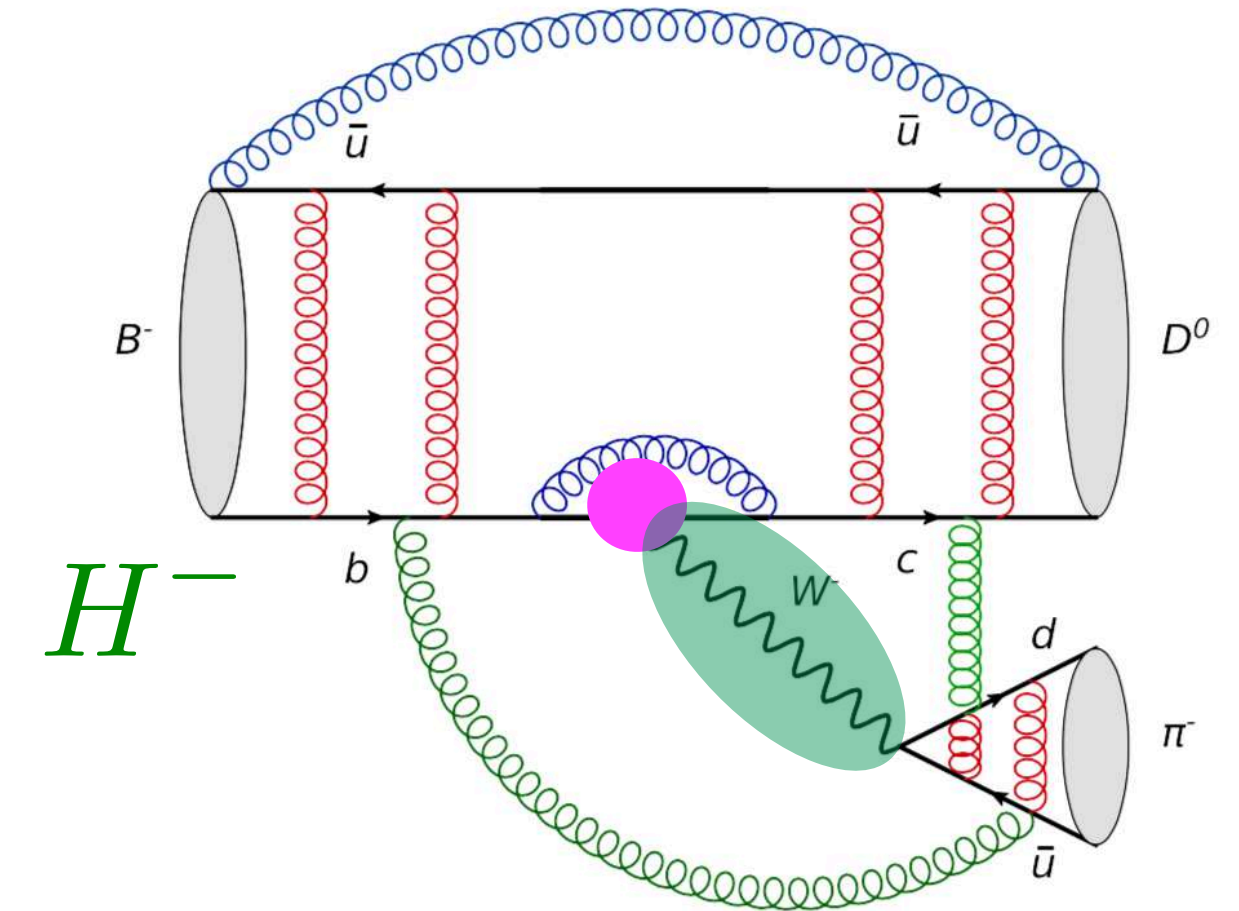
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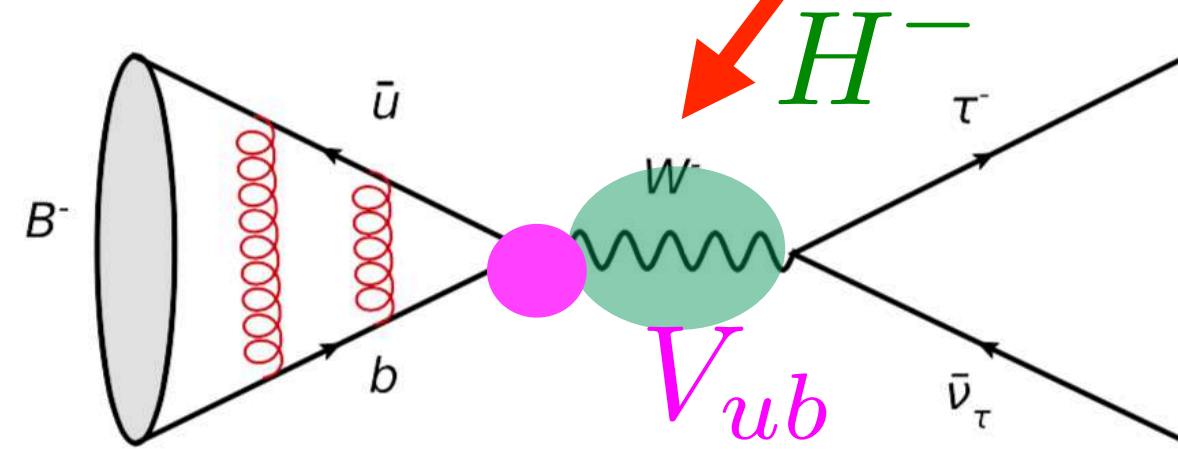
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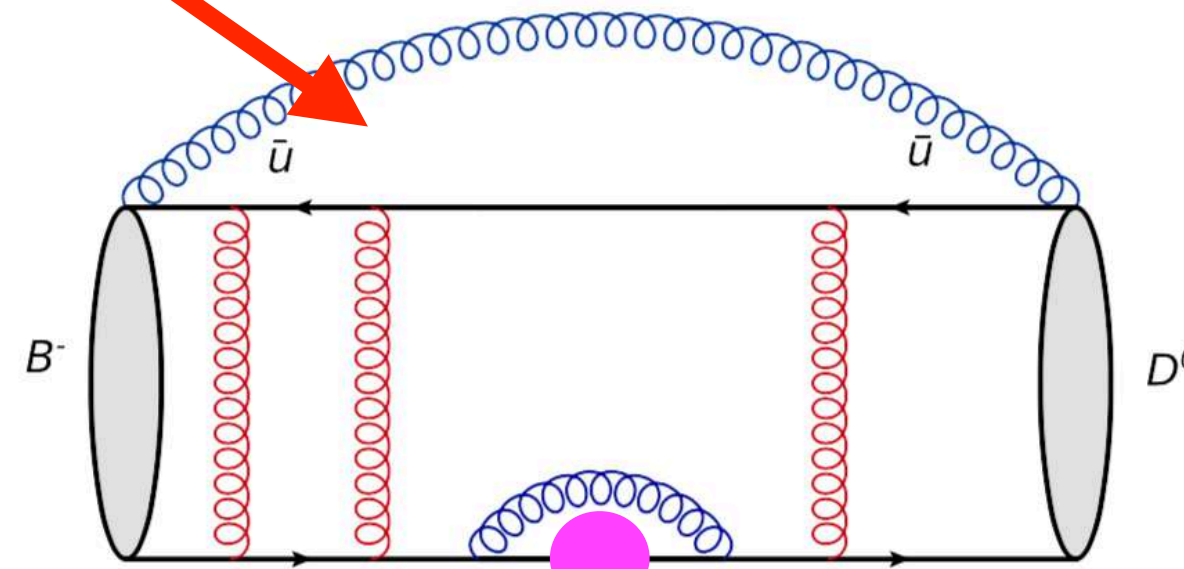
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$b \rightarrow sll$ anomalies
Loop

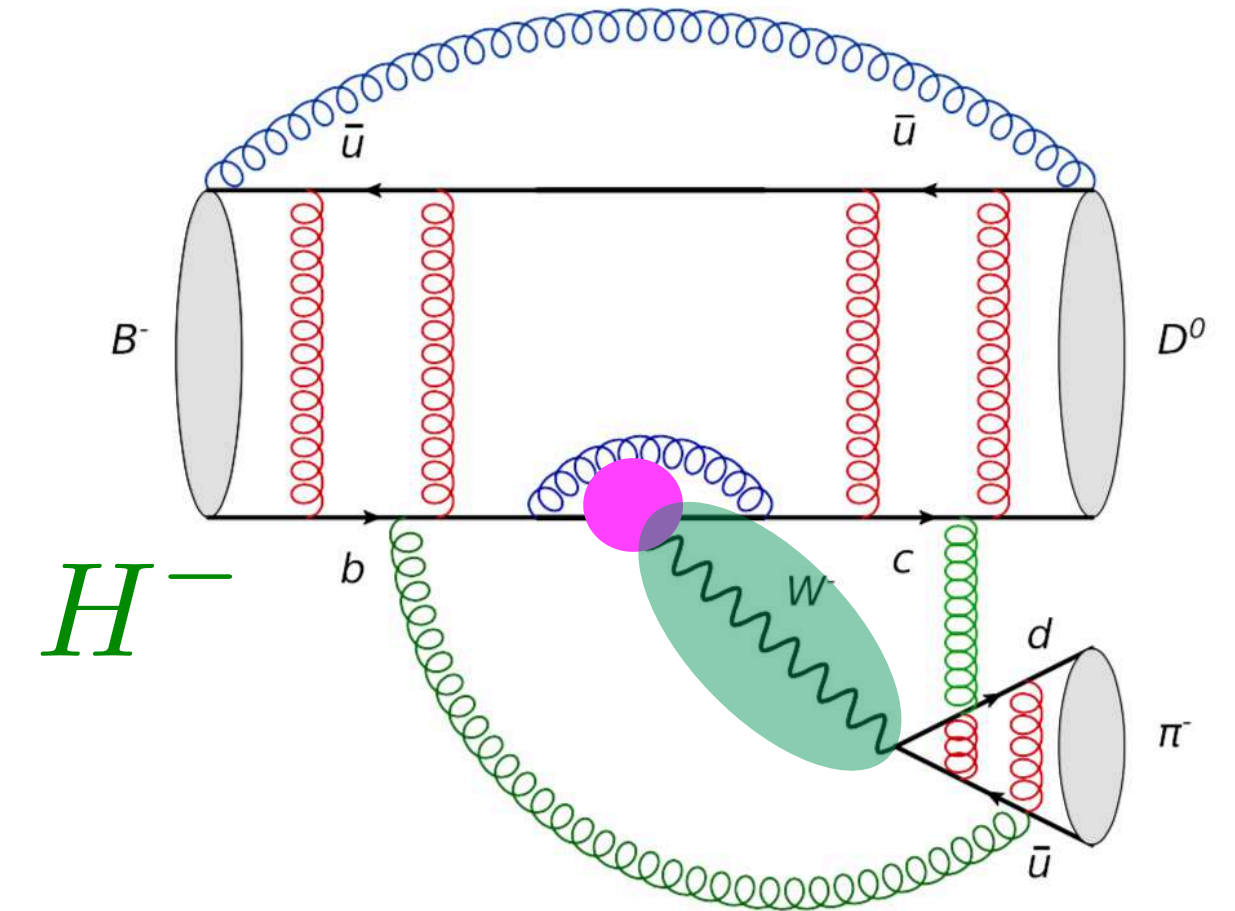
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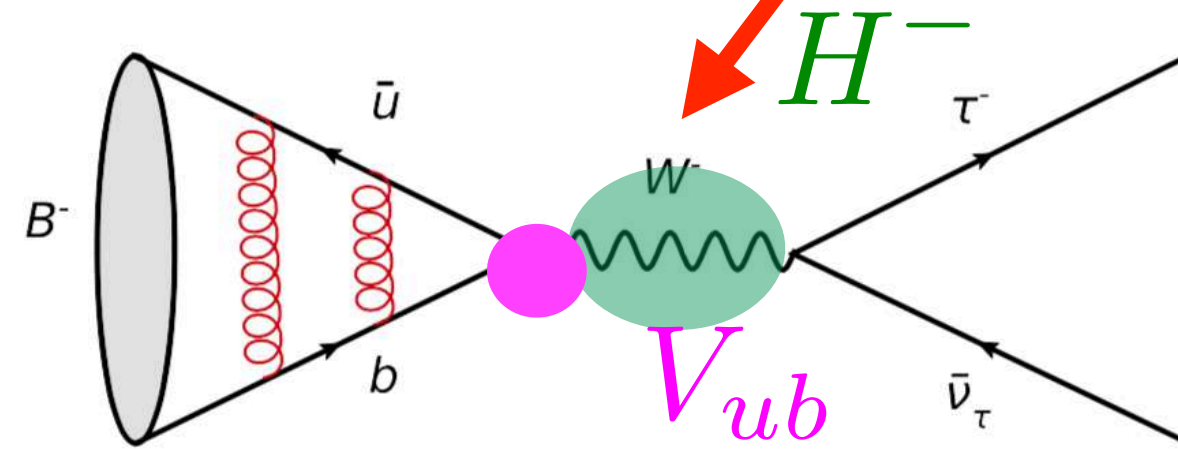
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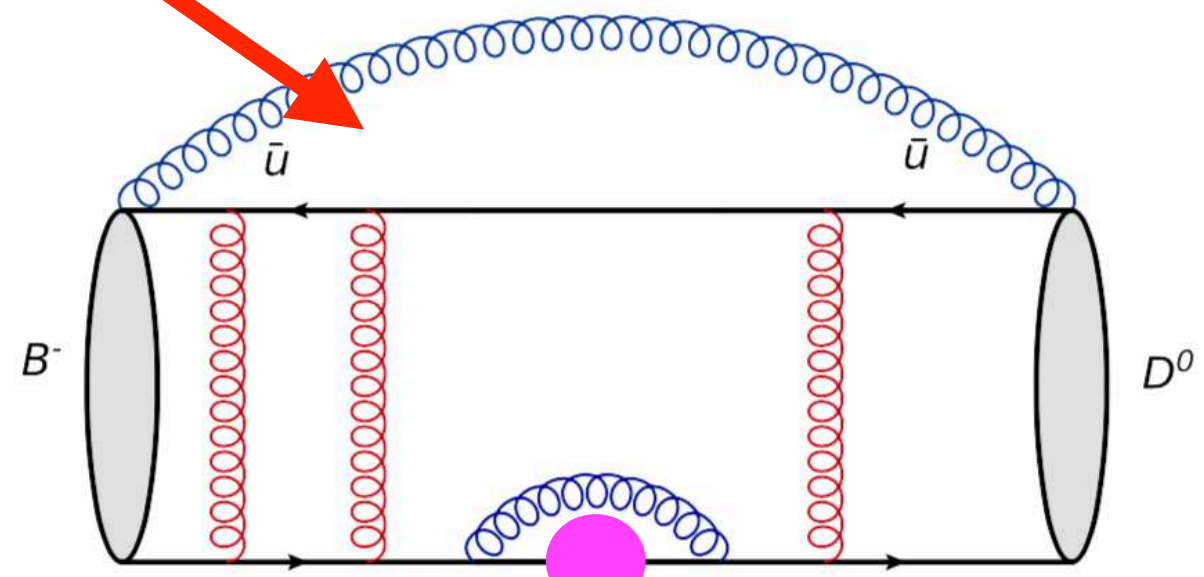


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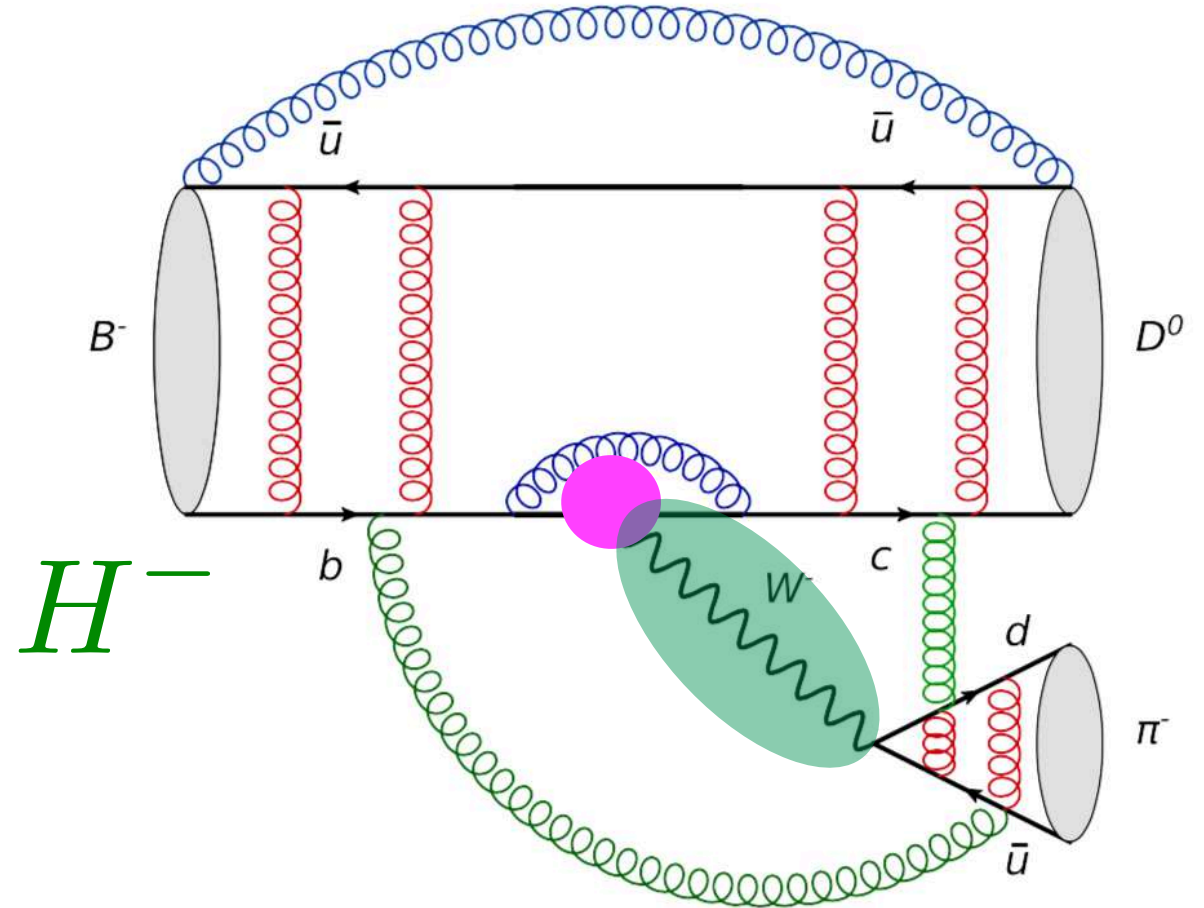
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$b \rightarrow sll$ anomalies
Loop

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$b \rightarrow cl\nu$ anomalies
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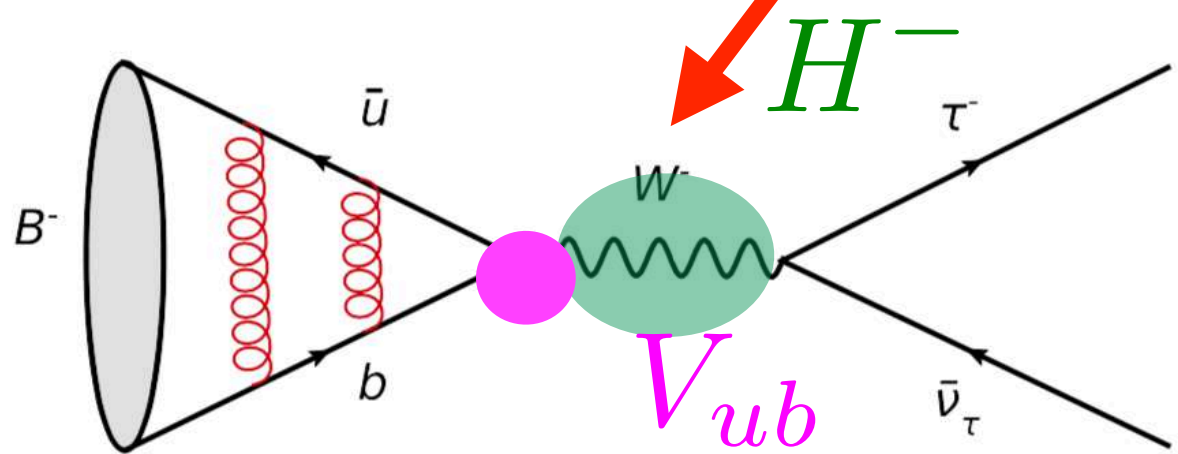
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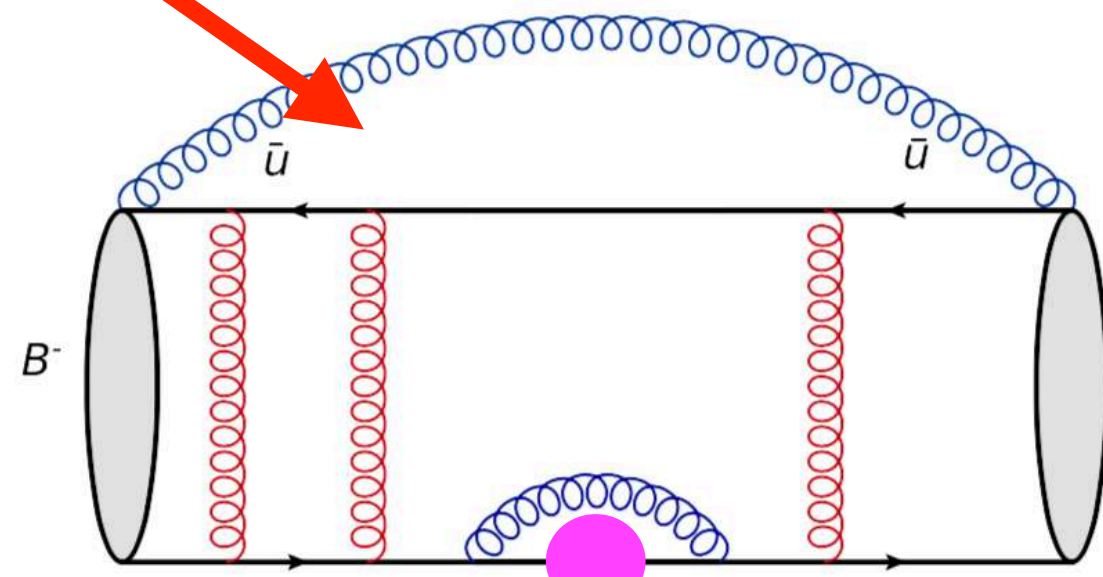


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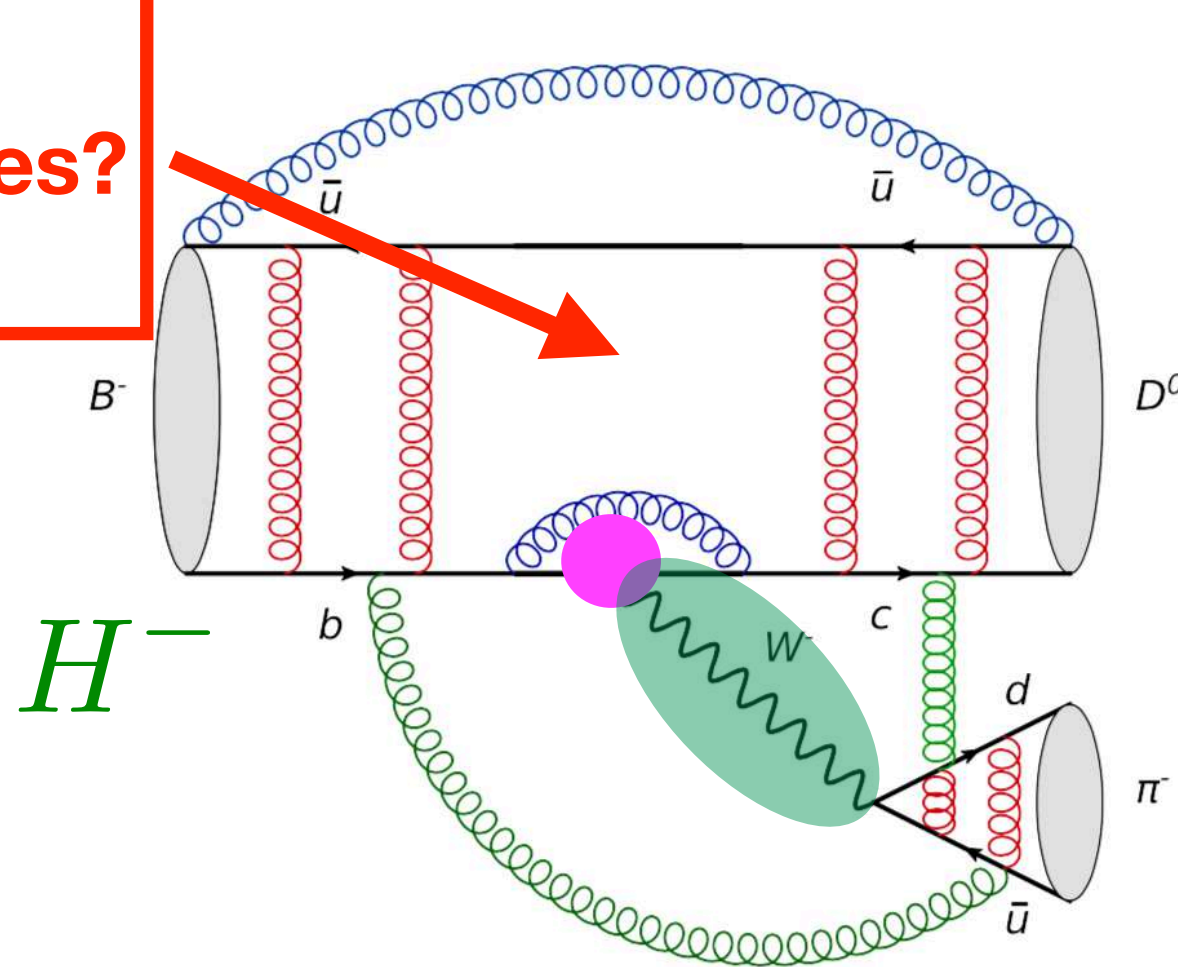


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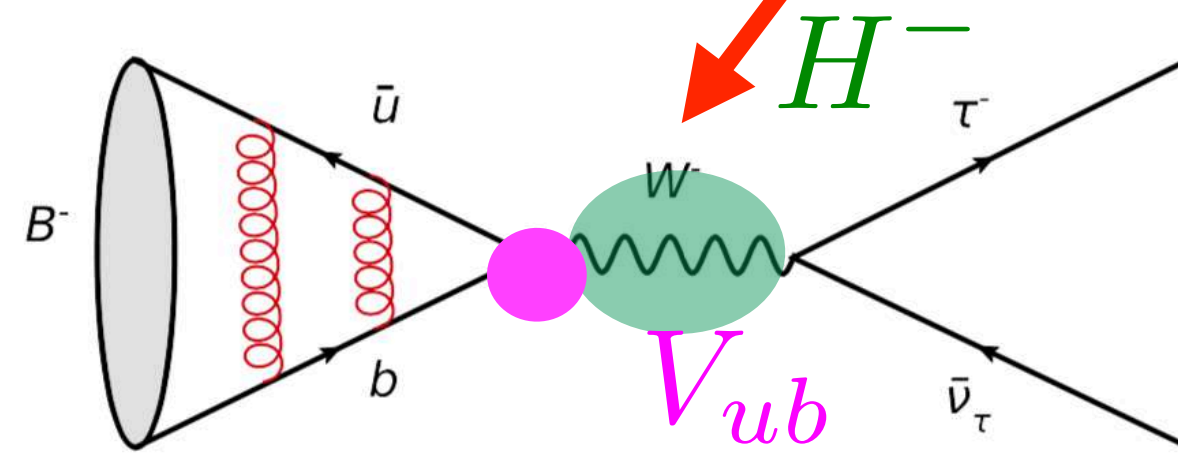
New B anomalies?
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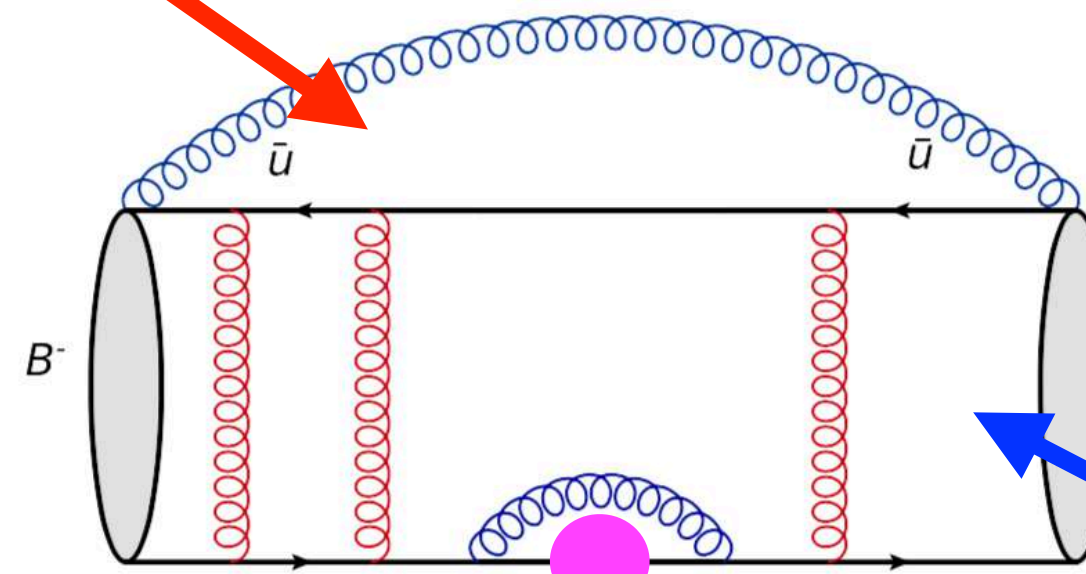


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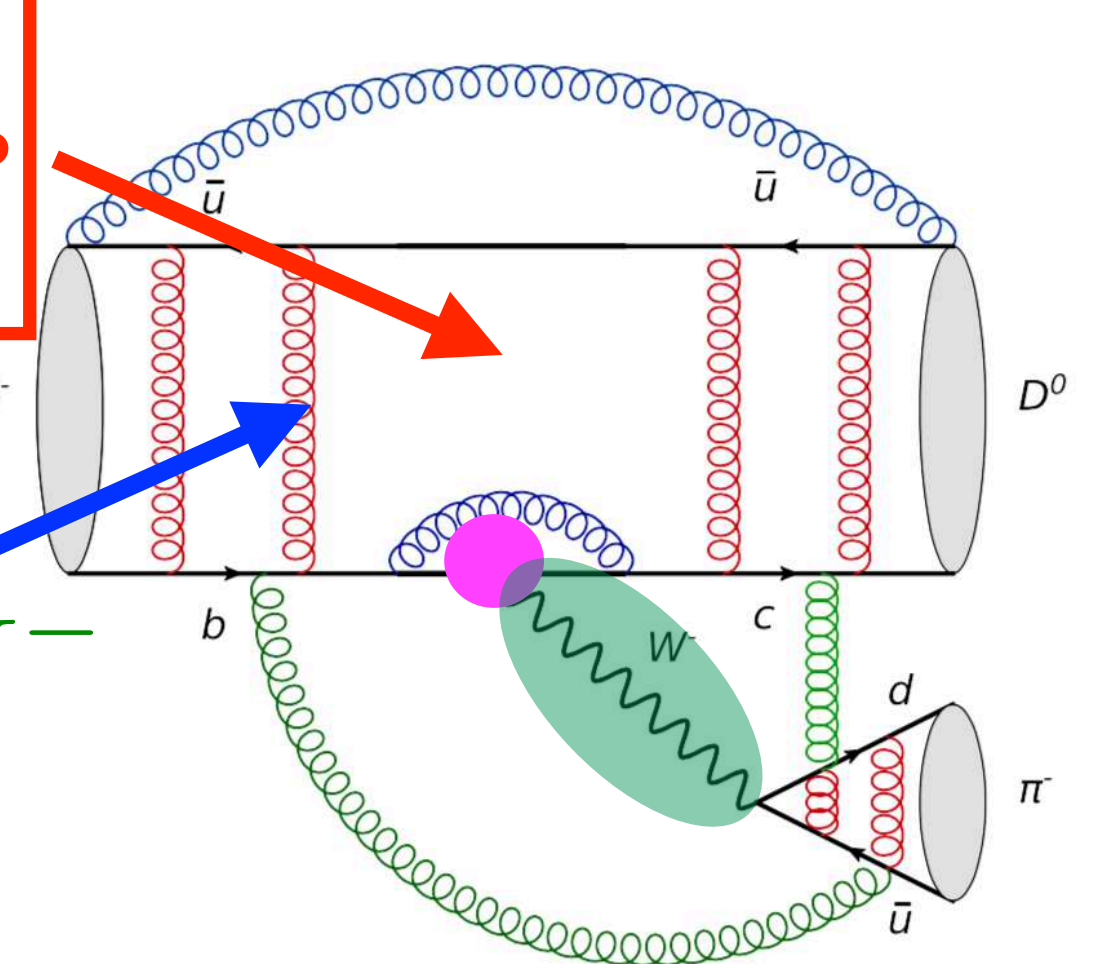


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QCdf

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Ancient Anomalies

V_{cb} : inclusive vs. exclusive

$$|V_{cb}|^{\text{incl.,2022}} = (42.16 \pm 0.51) \cdot 10^{-3}$$

Bordone, Caddevilla, Gambino 2107.00604

$$|V_{cb}|^{\text{excl.,PDG}} = (39.5 \pm 0.9) \cdot 10^{-3}.$$

Based on NNNLO-QCD!!!

Fael, Schönwald, Steinhauser 2011.13654

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$$|V_{cb}|^{\text{excl.}} = \left\{ \begin{array}{lll} (38.40 \pm 0.74) \cdot 10^{-3} & \text{FNAL/MILC} & B \rightarrow D^* l \nu, \\ (40.3 \pm 0.8) \cdot 10^{-3} & \text{LCSR2 and lattice} & B \rightarrow D^{(*)} l \nu, \\ (40.3 \pm 1.7) \cdot 10^{-3} & \text{LCSR1, BaBar} & B \rightarrow D l \nu, \\ (41.0 \pm 1.3) \cdot 10^{-3} & \text{LCSR1, Belle} & B \rightarrow D l \nu, \\ (41.0 \pm 1.2) \cdot 10^{-3} & \text{lattice + unitarity} & B \rightarrow D l \nu, \\ (42.2 \pm 2.3) \cdot 10^{-3} & \text{HPQCD} & B_s \rightarrow D_s^* l \nu. \end{array} \right.$$

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Study quark mass definitions

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Improved form factors

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Based on NNNLO-QCD!!!

Fael, Schönwald, Steinhauser 2011.13654

$$\Delta M_s^{\text{SM}} = 18.3^{+0.7}_{-1.2} \text{ ps}^{-1}$$

Perfect match

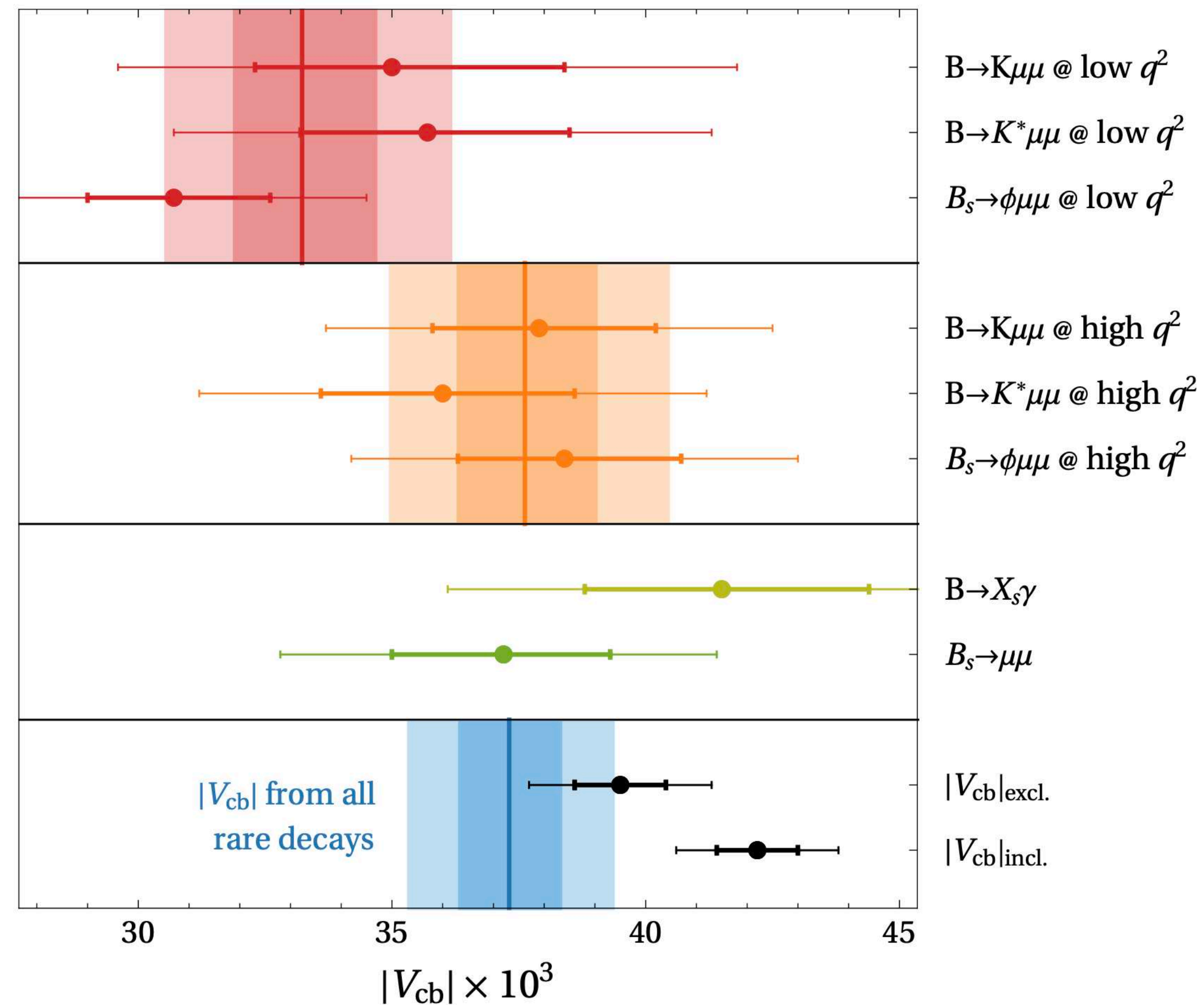
$$\Delta M_s^{\text{SM}} = 16.0^{+0.6}_{-1.0} \text{ ps}^{-1}$$

around 3σ deviation

$$\Delta M_s^{\text{Exp}} = 17.741(20) \text{ ps}^{-1}$$

B Anomalies

V_{cb} : inclusive vs. exclusive affects also the $b \rightarrow sll$ anomalies

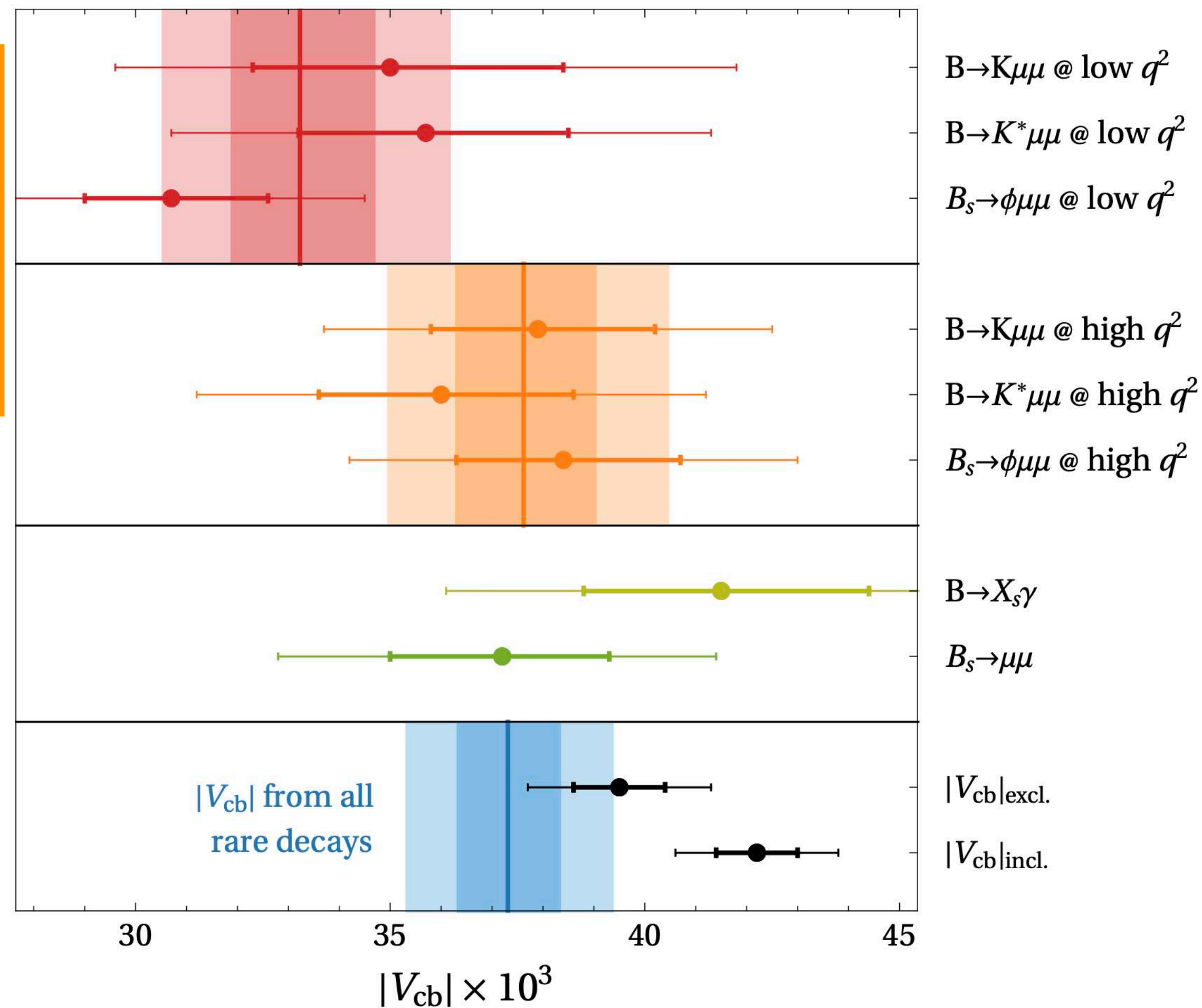


B Anomalies

V_{cb} : inclusive vs. exclusive affects also some of the $b \rightarrow sll$ anomalies

Interesting suggestion to determine inclusive B decays directly with Lattice-QCD

- [42] S. Hashimoto, *Inclusive semi-leptonic B meson decay structure functions from lattice QCD*, [PTEP 2017 \(2017\) 053B03](#), [arXiv:1703.01881](#).
- [43] M. Hansen, A. Lupo, and N. Tantalo, *Extraction of spectral densities from lattice correlators*, [Phys. Rev. D 99 \(2019\) 094508](#), [arXiv:1903.06476](#).
- [44] J. Bulava and M. T. Hansen, *Scattering amplitudes from finite-volume spectral functions*, [Phys. Rev. D 100 \(2019\) 034521](#), [arXiv:1903.11735](#).
- [45] P. Gambino and S. Hashimoto, *Inclusive Semileptonic Decays from Lattice QCD*, [Phys. Rev. Lett. 125 \(2020\) 032001](#), [arXiv:2005.13730](#).
- [46] J. Bulava *et al.*, *Inclusive rates from smeared spectral densities in the two-dimensional O(3) non-linear σ -model*, [arXiv:2111.12774](#).
- [47] P. Gambino *et al.*, *Lattice QCD study of inclusive semileptonic decays of heavy mesons*, [arXiv:2203.11762](#).



The usual Suspects:

- High precision in γ^{CKM}

within the SM

$$\text{LHCb}$$
$$\gamma = (65.4^{+3.8}_{-4.2})^\circ$$

The ultimate theoretical error on γ from $B \rightarrow DK$ decays

Joachim Brod and Jure Zupan

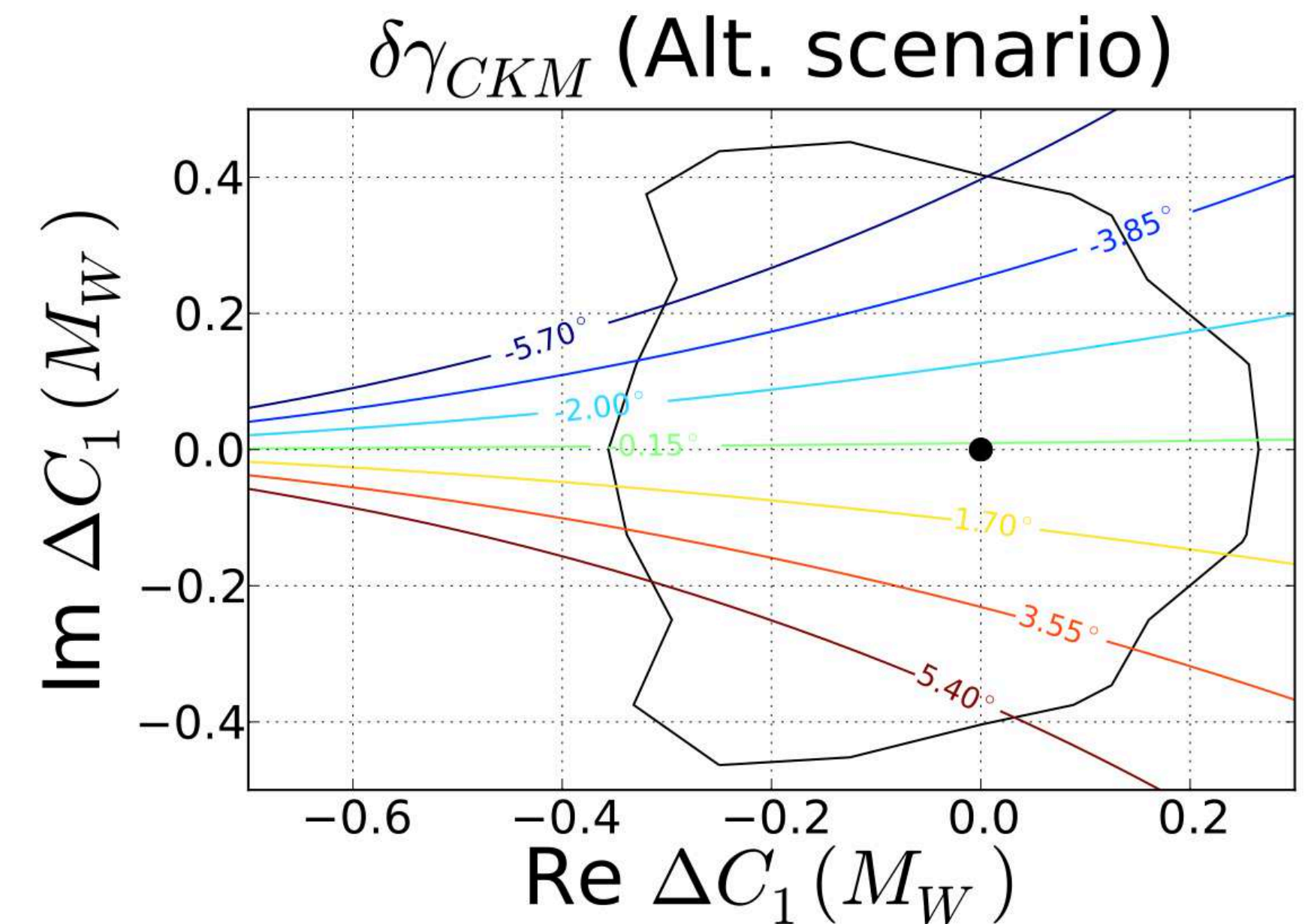
Department of Physics, University of Cincinnati,
Cincinnati, Ohio 45221, U.S.A.

E-mail: brodjm@ucmail.uc.edu, zupanje@ucmail.uc.edu

ABSTRACT: The angle γ of the standard CKM unitarity triangle can be determined from $B \rightarrow DK$ decays with a very small irreducible theoretical error, which is only due to second-order electroweak corrections. We study these contributions and estimate that their impact on the γ determination is to introduce a shift $|\delta\gamma| \lesssim \mathcal{O}(10^{-7})$, well below any present or planned future experiment.

Allow BSM effects in tree-level

$$C_1(M_W) := C_1^{\text{SM}}(M_W) + \Delta C_1(M_W),$$
$$C_2(M_W) := C_2^{\text{SM}}(M_W) + \Delta C_2(M_W),$$



Brod, AL, Tetlamatzi-Xolocotzi 1412.1446

AL, Tetlamatzi-Xolocotzi 1912.07621

Ancient Anomalies

The D0 dimuon anomaly is still not settled: 3.6σ

The New York Times

A New Clue to Explain Existence

By DENNIS OVERBYE MAY 17, 2010

Physicists at the [Fermi National Accelerator Laboratory](#) are reporting that they have discovered a new clue that could help unravel one of the biggest mysteries of cosmology: why the universe is composed of matter and not its evil-twin opposite, antimatter. If confirmed, the finding portends fundamental discoveries at the new [Large Hadron Collider](#) outside Geneva, as well as a possible explanation for our own existence.

$$A^{\text{Di-muon}} = C_s a_{sl}^s + C_d a_{sl}^d + \frac{1}{2} C_\Delta \Delta \Gamma_d$$

Experiment disagrees with the Standard Model predictions by 4σ

Evidence for an anomalous like-sign dimuon charge asymmetry

[V.M. Abazov et al \(D0 Collaboration\)](#)
Phys. Rev. Lett 105 (2010) 081801

Measurement of the anomalous like-sign dimuon charge asymmetry

[V.M. Abazov et al \(D0 Collaboration\)](#)
Phys. Rev. D 84 (2011) 052007

Study of CP violating charge asymmetry...

[V.M. Abazov et al \(D0 Collaboration\)](#)
Phys. Rev. D 89 (2014) 012002

Theoretical update of Bs mixing

[Alexander Lenz, Uli Nierste](#)
JHEP 0706(2007)072; hep-ph/0612167

Numerical update of lifetimes and mixing parameters

[Alexander Lenz, Uli Nierste](#)
hep-ph/1102.4274

CP violation in the Bs system

[Marina Artuso, Guennadi Borissov, Alexander Lenz](#)
Rev.Mod.Phys. 88 (2016) no.4,045002

New interpretation of experimental measurement

Understanding the anomalous like-sign dimuon charge asymmetry

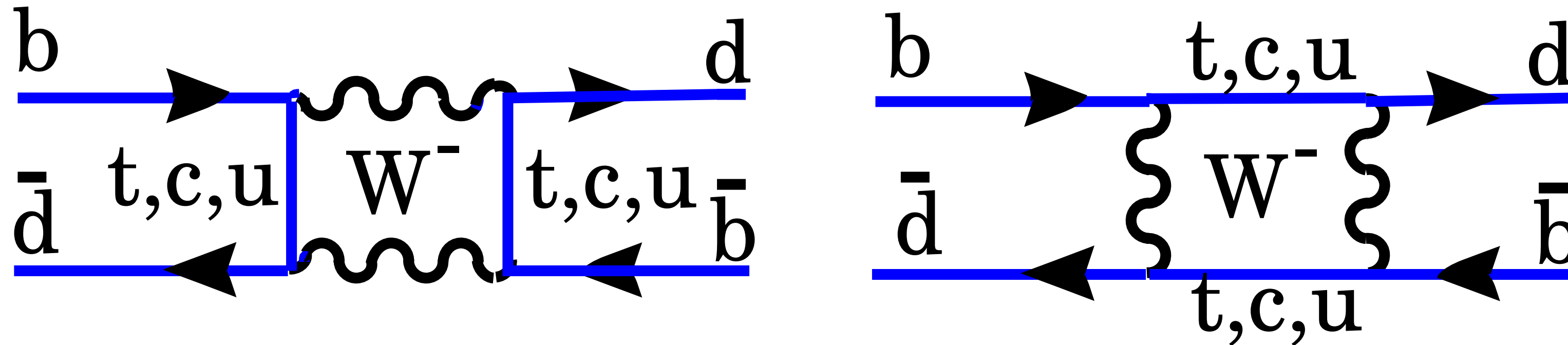
[Guennadi Borissov, Boris Hoeneisen](#)
Phys. Rev. D 87 (2013) 074020

Effect of Delta Gamma_d on the dimuon asymmetry

[Uli Nierste](#)
Talk at CKM 2014

Mixing

$$\begin{aligned} |B_{q,L}\rangle &= p|B_q\rangle + q|\bar{B}_q\rangle \\ |B_{q,H}\rangle &= p|B_q\rangle - q|\bar{B}_q\rangle \end{aligned}$$



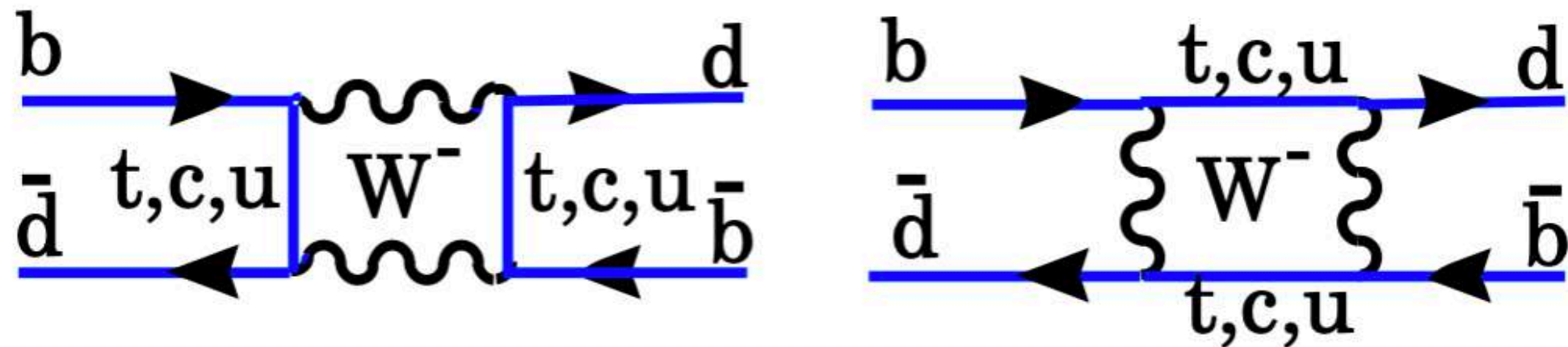
$|M_{12}|$, $|\Gamma_{12}|$ and $\phi = \arg(-M_{12}/\Gamma_{12})$ can be related to three observables:

- **Mass difference:** $\Delta M := M_H - M_L \approx 2|M_{12}|$ (off-shell)
 $|M_{12}|$: heavy internal particles: t, SUSY, ...
- **Decay rate difference:** $\Delta\Gamma := \Gamma_L - \Gamma_H \approx 2|\Gamma_{12}| \cos \phi$ (on-shell)
 $|\Gamma_{12}|$: light internal particles: u, c, ... (almost) no NP!!!
- **Flavor specific/semi-leptonic CP asymmetries:** e.g. $B_q \rightarrow Xl\nu$ (semi-leptonic)

$$a_{sl} \equiv a_{fs} = \frac{\Gamma(\bar{B}_q(t) \rightarrow f) - \Gamma(B_q(t) \rightarrow \bar{f})}{\Gamma(\bar{B}_q(t) \rightarrow f) + \Gamma(B_q(t) \rightarrow \bar{f})} = \left| \frac{\Gamma_{12}}{M_{12}} \right| \sin \phi$$

Status Quo: Mixing

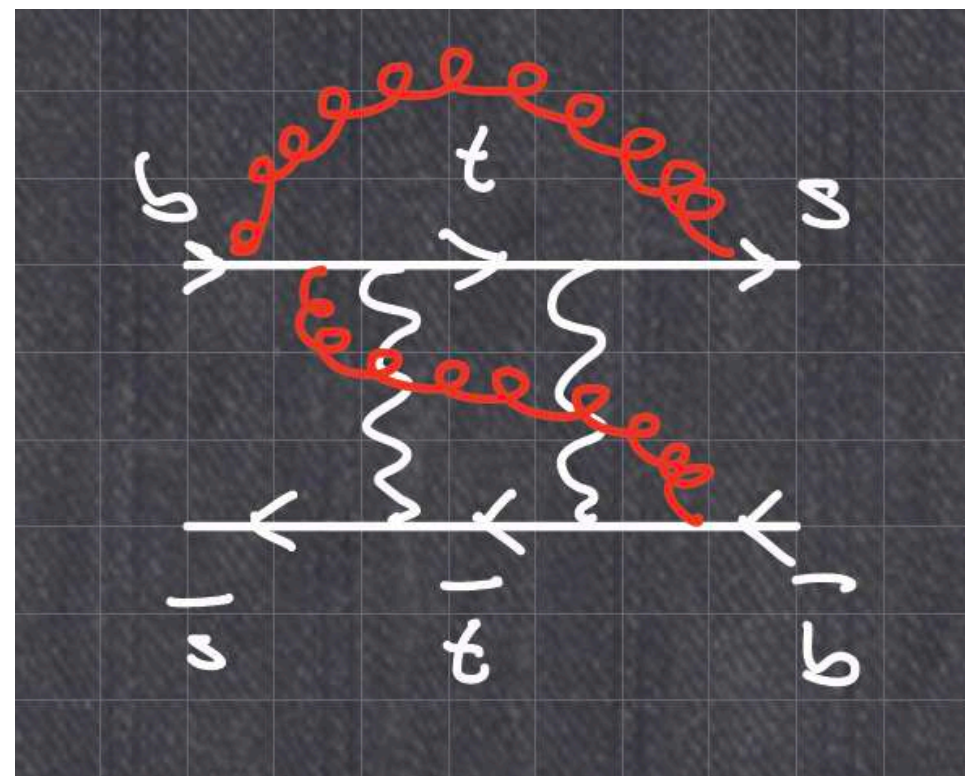
$$\Delta M_s = 2 |M_{12}^s|$$



$$M_{12}^q = \frac{G_F^2}{12\pi^2} \lambda_t^2 M_W^2 S_0(x_t) B f_{B_q}^2 M_{B_q} \hat{\eta}_B,$$

Significant CKM dependence

By far dominant uncertainty

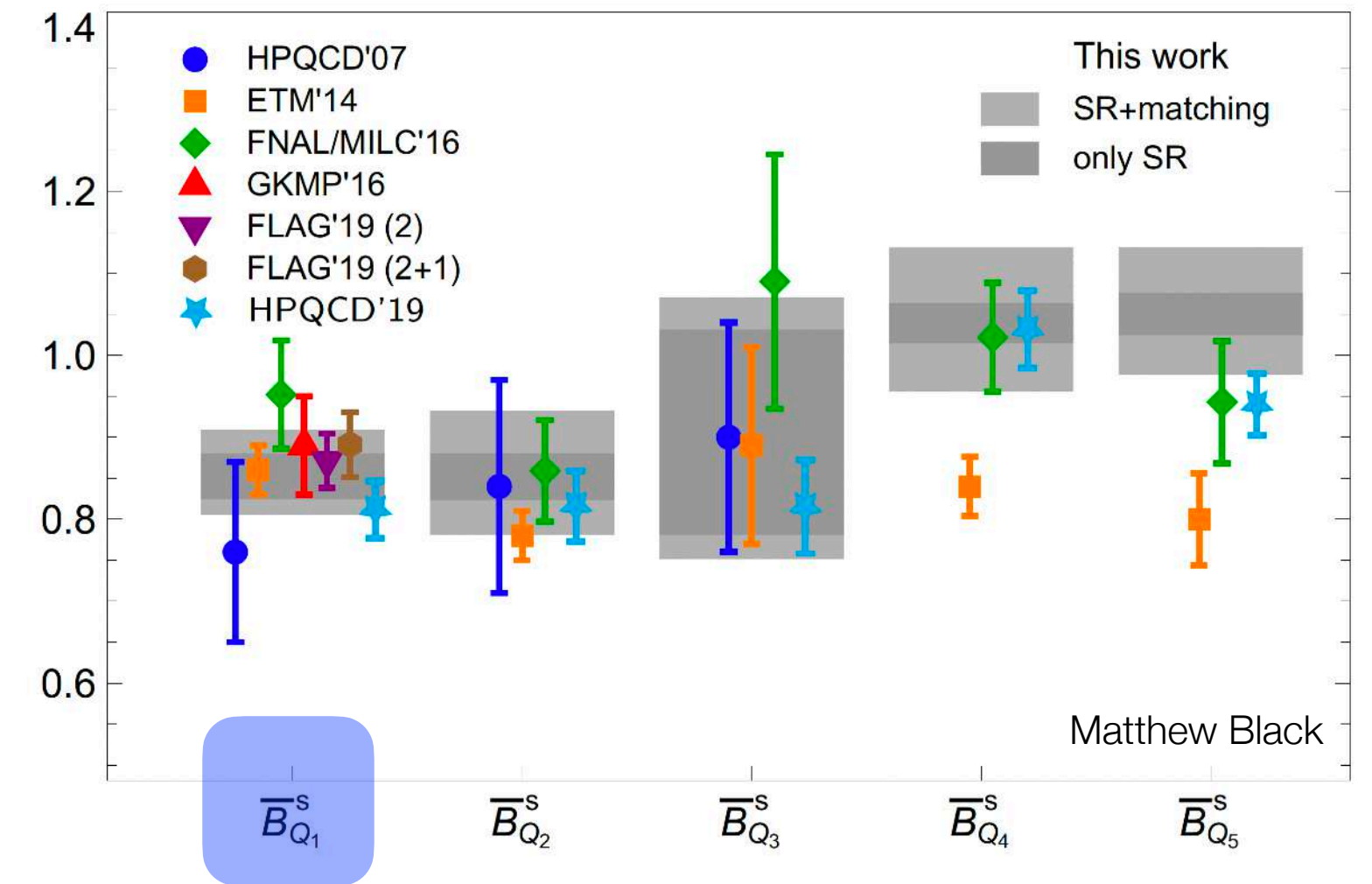


2-loop: Buras, Jamin, Weisz

3-loop: Gorbahn,...

$$Q = \bar{s}^\alpha \gamma_\mu (1 - \gamma_5) b^\alpha \times \bar{s}^\beta \gamma^\mu (1 - \gamma_5) b^\beta$$

$$\langle Q \rangle \equiv \langle B_s^0 | Q | \bar{B}_s^0 \rangle = \frac{8}{3} M_{B_s}^2 f_{B_s}^2 B(\mu)$$



Lattice

- * B_s, B_d and D mixing: [FNAL/MILC 1602.03560](#)
- * Ratio of B_s and B_d mixing: [RBC/UK QCD 1812.08791](#)
- * B_s and B_d mixing: [HQCD 19007.01025](#)

HQET-sum rules: 3-loop + part of NNLO matching:

* B_d mixing:

[Siegen: Grozin, Klein, Mannel, Pivovarov 1606.06054, 1706.05910, 1806.00253](#)

* B_d and D mixing, D^0, D^+, B_d and B^+ lifetimes

[Durham: Kirk \(Rome\), AL, Rauh \(Bern\) 1711.02100](#)

* B_s mixing

[Durham: King, AL, Rauh \(Bern\) 1904.00940](#)

* B_s and D_s^+ lifetimes

[Siegen: King \(Durham\), AL, Rauh \(Bern\) 2112.03691](#)

Status Quo: Mixing

<http://lhcb-public.web.cern.ch>

$$\Delta M_d = (0.5065 \pm 0.0019) \text{ ps}^{-1}$$

$$\Delta M_d = (0.533^{+0.022}_{-0.036}) \text{ ps}^{-1}$$

$$\Delta M_s = (17.741 \pm 0.020) \text{ ps}^{-1}$$

$$\Delta M_s = (18.4^{+0.7}_{-1.2}) \text{ ps}^{-1}$$

12 April 2021: Fascinating quantum mechanics.

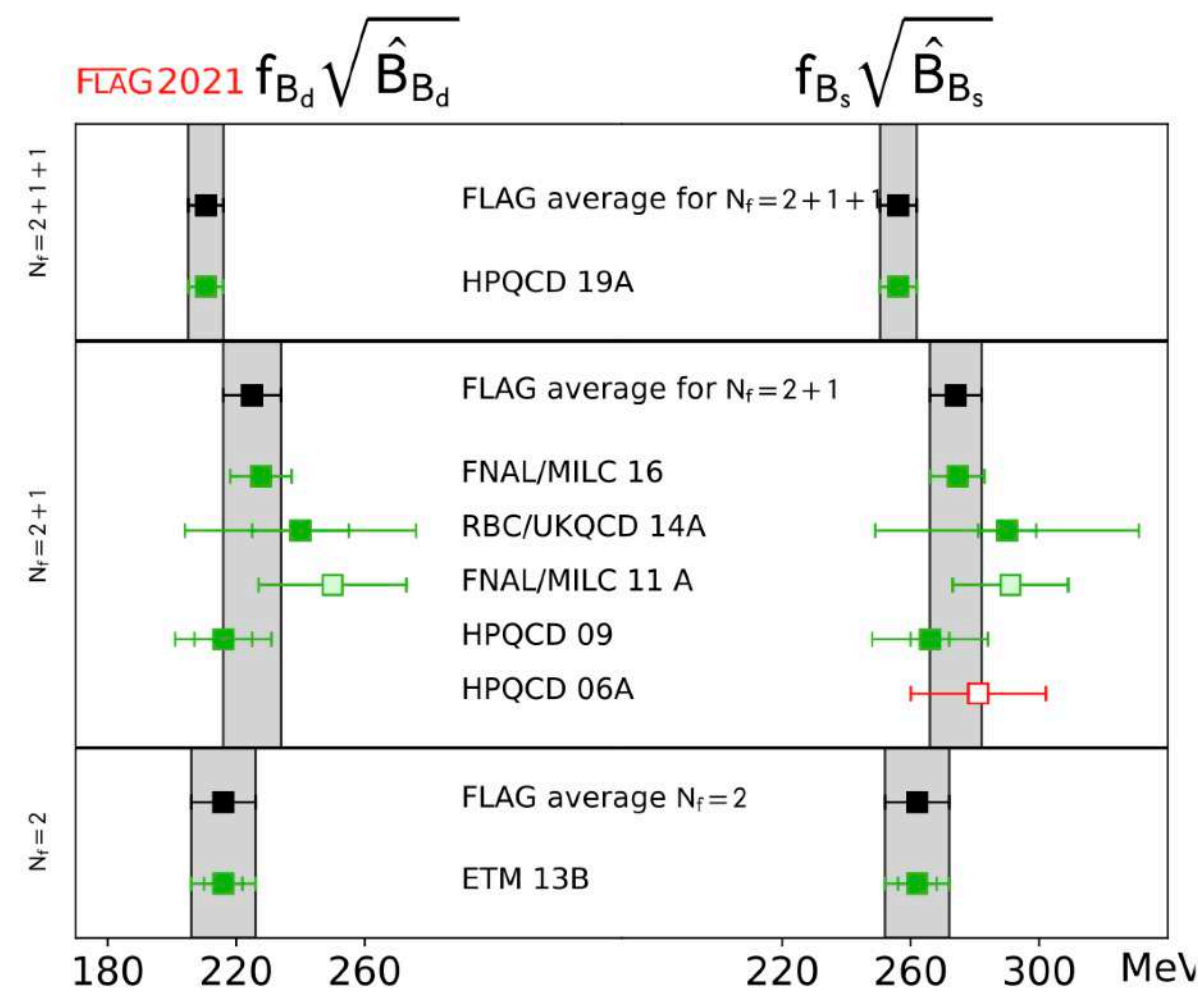
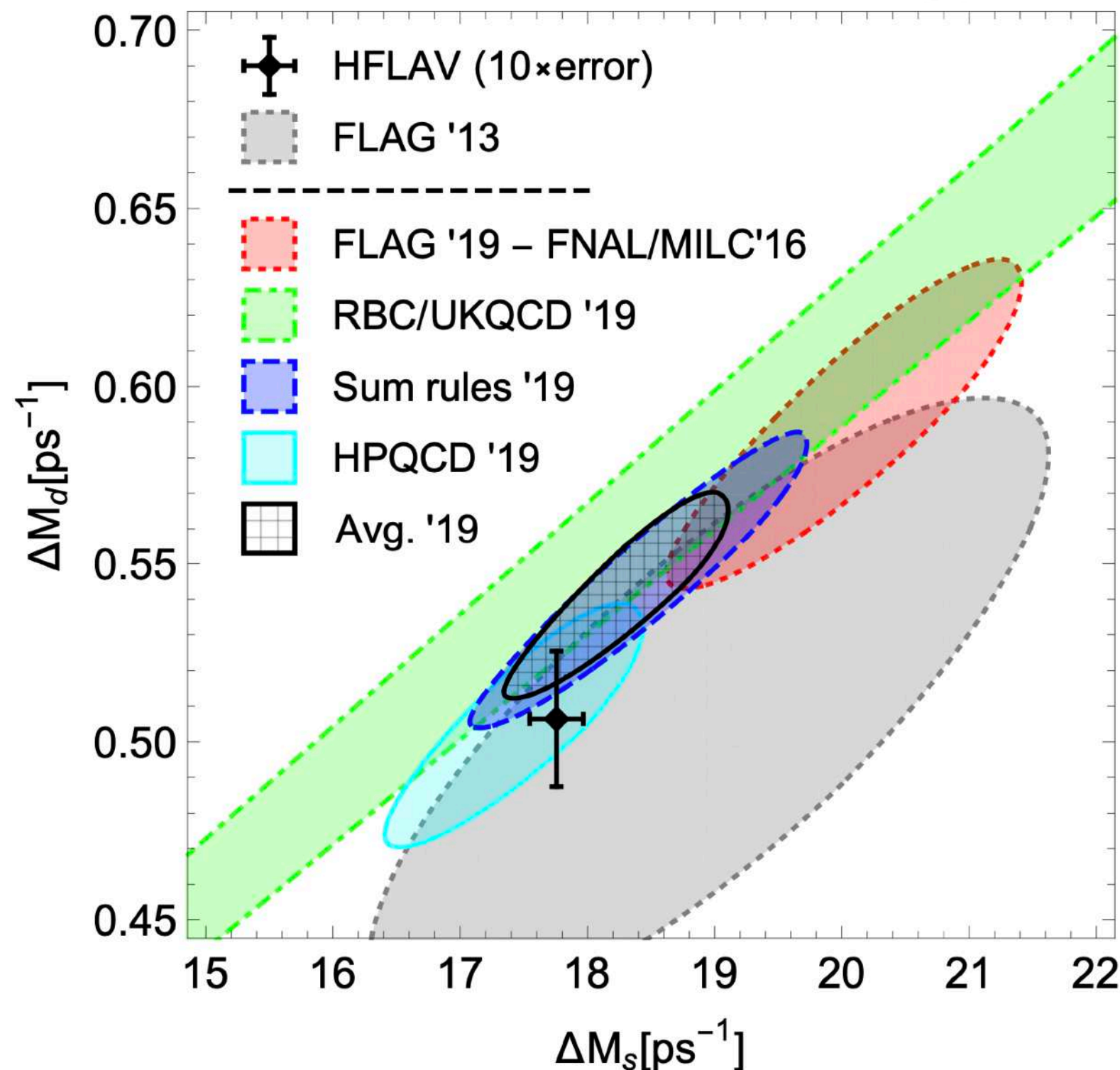
Precise determination of the $B_s^0 - \bar{B}_s^0$ oscillation frequency.

"A phenomenon in which quantum mechanics gives a most remarkable prediction" - Richard Feynman

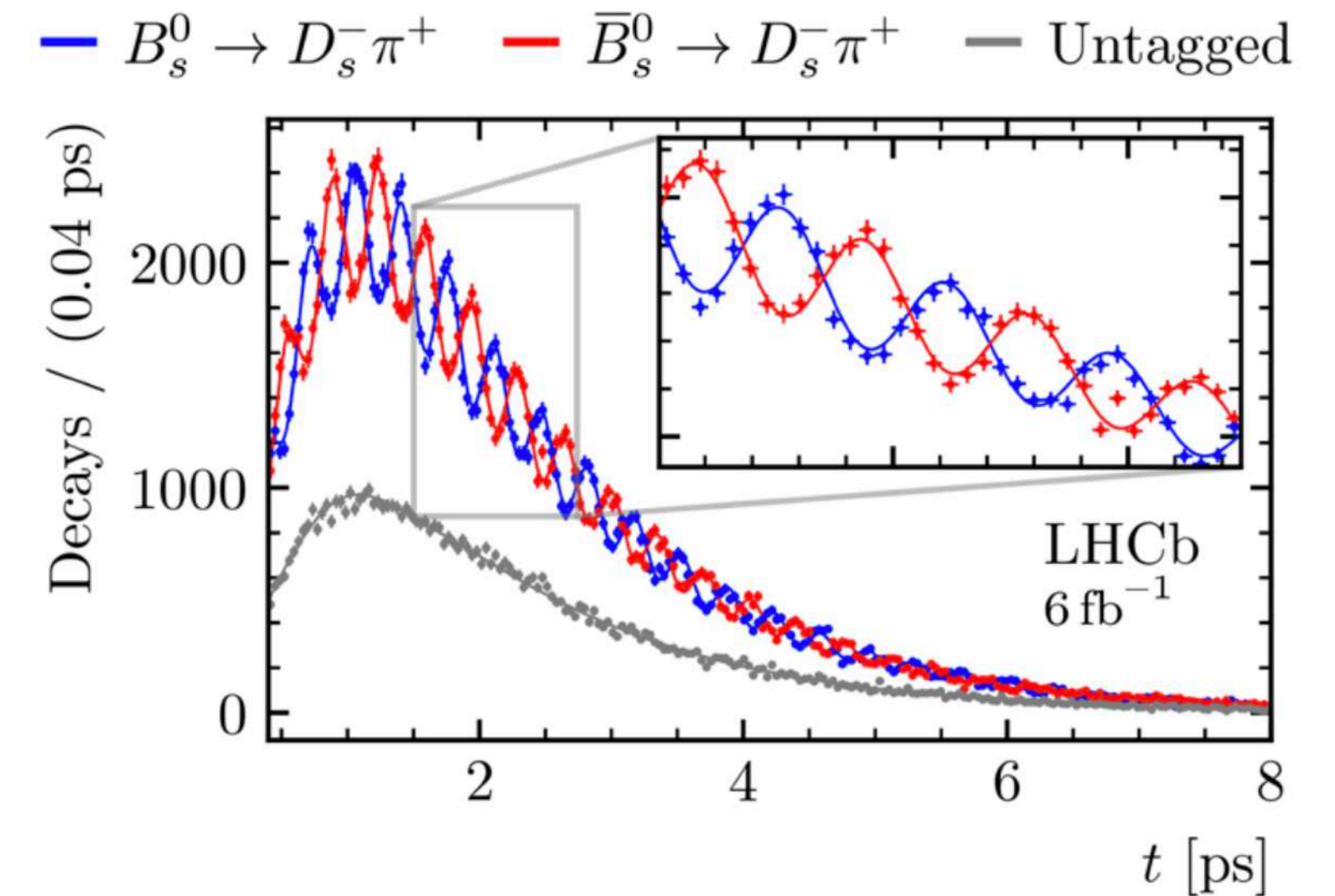
Today, the LHCb Collaboration submitted a paper for publication that reports a precise determination of the $B_s^0 - \bar{B}_s^0$ oscillation frequency. This result is presented also today at the joint [annual conference](#) of the UK Institute of Physics (IOP), organized by the University of Edinburgh. The $B_s^0 - \bar{B}_s^0$ oscillation is a spectacular and fascinating feature of quantum mechanics. The strange beauty particle B_s^0 composed of a [beauty](#) antiquark (\bar{b}) bound with a [strange](#) quark s turns into its antiparticle partner \bar{B}_s^0 composed of a b quark and an s antiquark (\bar{s}) about 3 million million times per second ($3 \cdot 10^{12}$) as seen in the image below.

HFLAV 2021

1909.11087
Average lattice & sum rules



Work in progress by
RBC/UKQCD+JLQCD 2111.11287

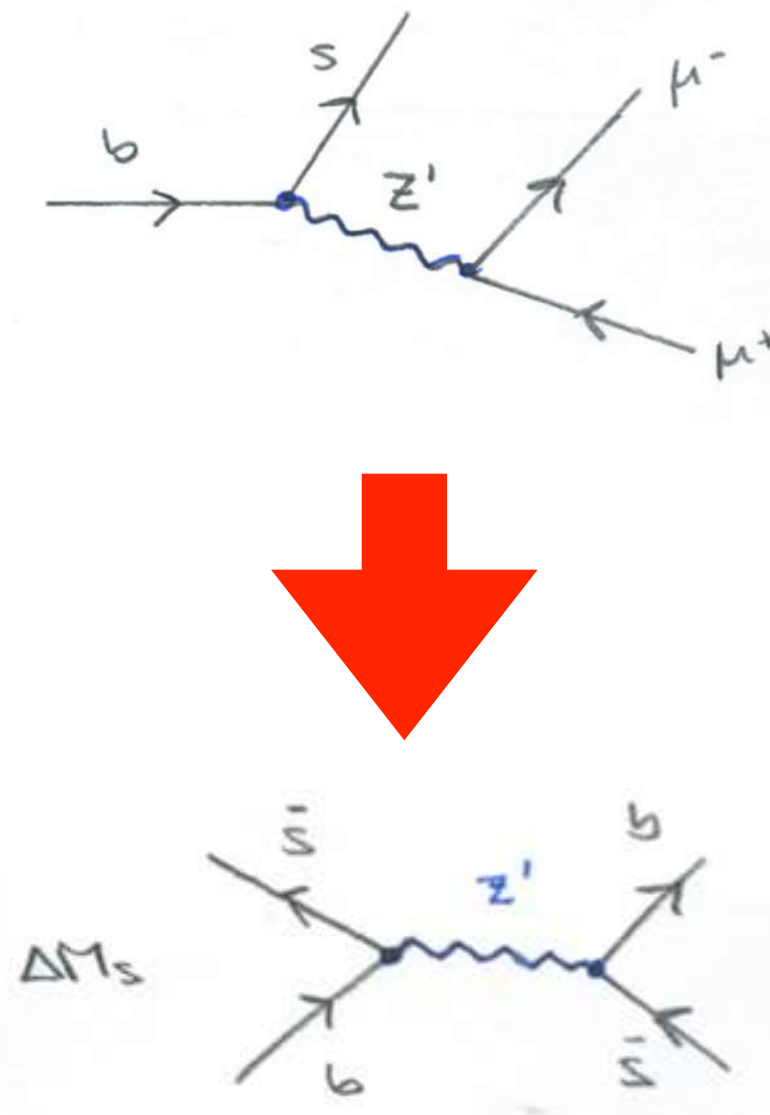
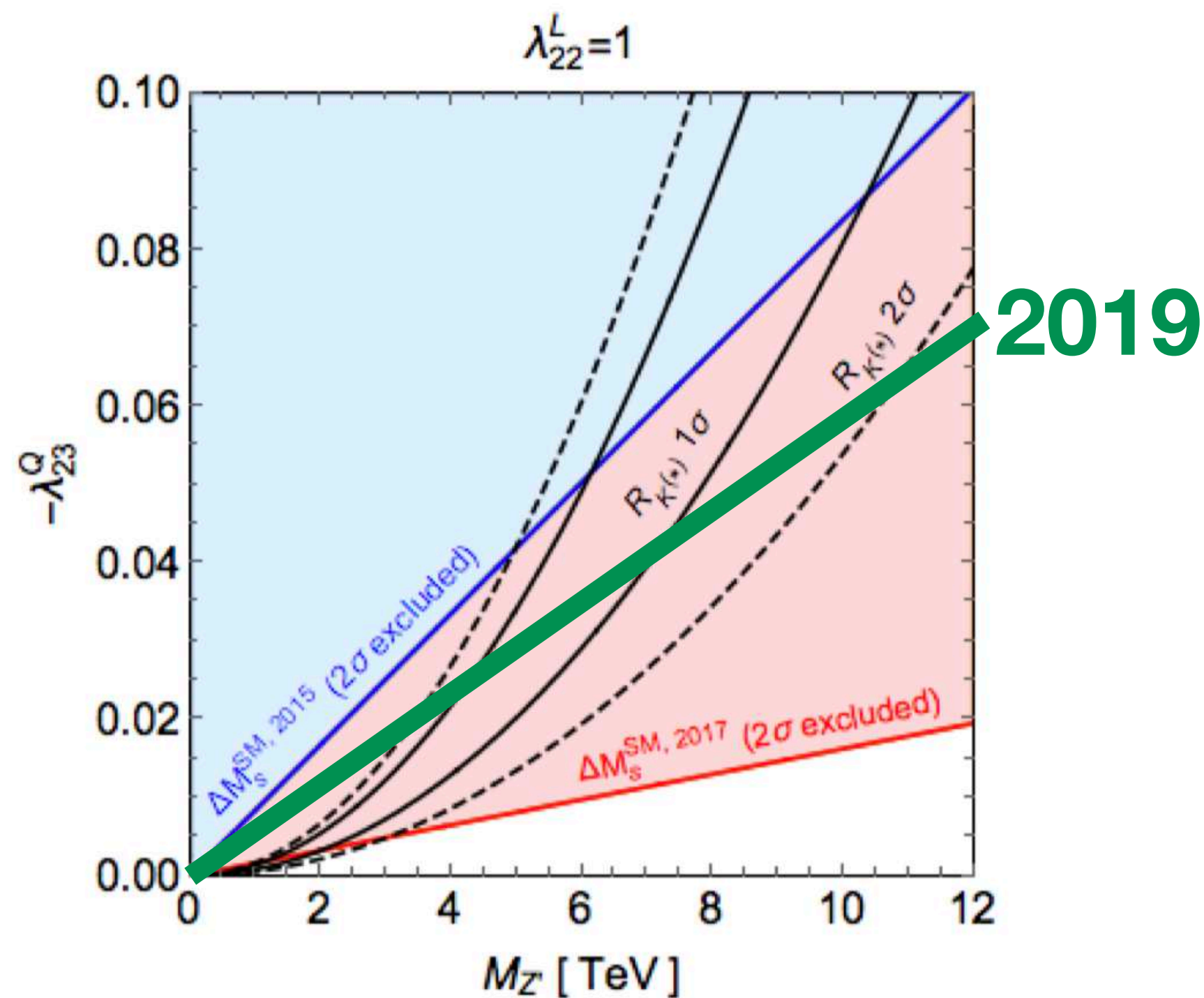


Higher precision for Bag

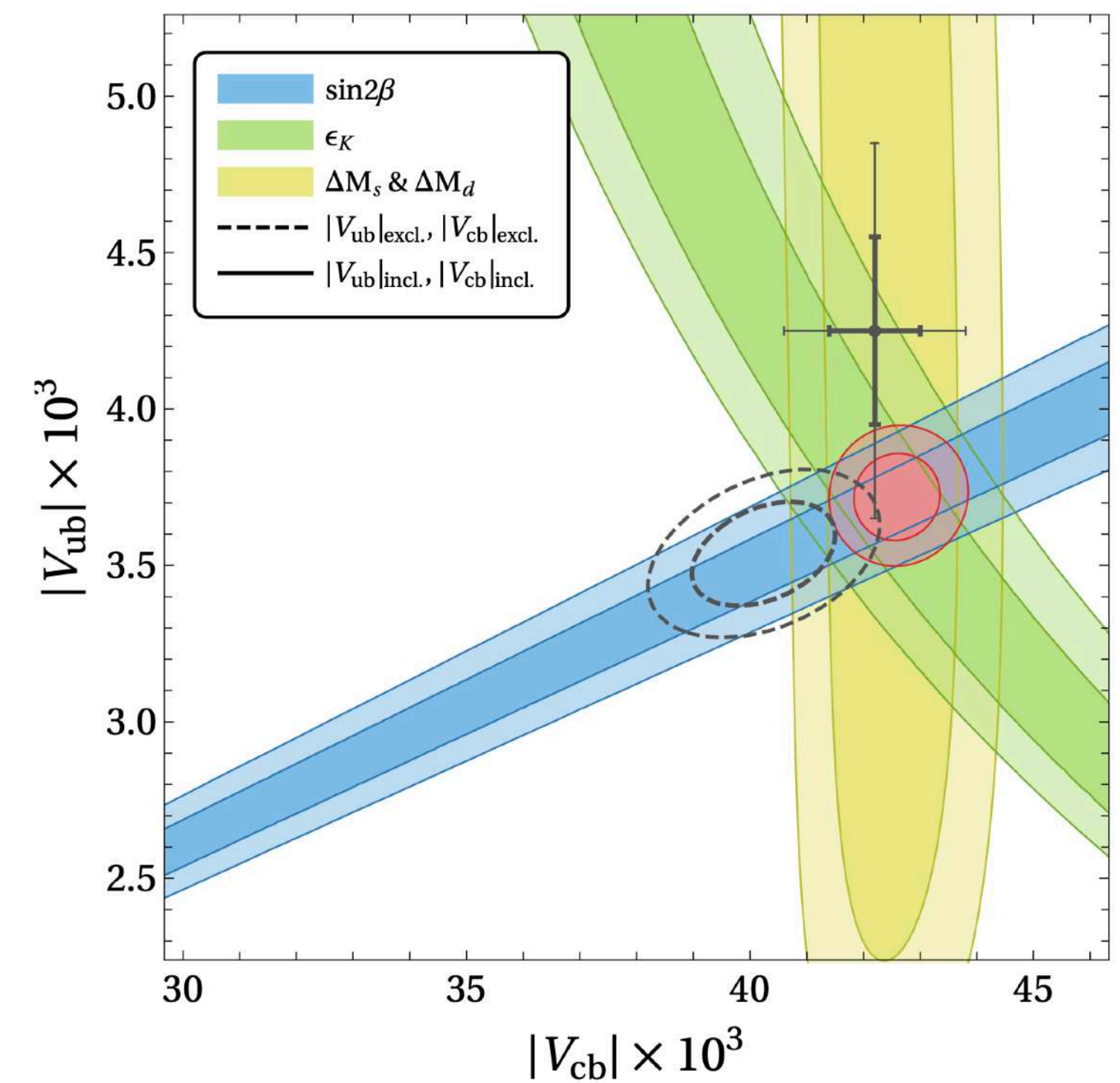
Status Quo: Mixing

The 2016 theory value for B-mixing has dramatic consequences for BSM models explaining the B anomalies

Direct determination of $V_{td}V_{tb}$, $V_{ts}V_{tb}$ and V_{ts}/V_{td}



Loopy determination of V_{cb} and V_{ub}



One constraint to kill them all?

Luca Di Luzio,^{1,*} Matthew Kirk,^{1,†} and Alexander Lenz^{1,‡}

1712.06572

Altmannshofer, Lewis 2112.03437

King, Kirk, AL, Rauh 1911.07856

The usual Suspects:

PHYSICAL REVIEW D **104**, 035028 (2021)

Editors' Suggestion

Collider signals of baryogenesis and dark matter from B mesons:
A roadmap to discovery

Gonzalo Alonso-Álvarez^{1,2,*}, Gilly Elor^{3,†} and Miguel Escudero^{4,‡}

- Semileptonic CP asymmetries a_{sl}^d, a_{sl}^s - Could explain Baryon asymmetry...

Semi-leptonic CP asymmetries

Relation to experiment

$$\Re \left(\frac{\Gamma_{12}^q}{M_{12}^q} \right) = - \frac{\Delta\Gamma_s}{\Delta M_q}$$

$$\Im \left(\frac{\Gamma_{12}^q}{M_{12}^q} \right) = a_{sl}^q$$

CP violating!

- Decay constants cancel completely
- Bag parameter cancel largely

Status Quo: Mixing

$$\Gamma_{12} = \frac{\Lambda^3}{m_b^3} \tilde{\Gamma}_6 \langle \tilde{Q}_6 \rangle + \frac{\Lambda^4}{m_b^4} \tilde{\Gamma}_7 \langle \tilde{Q}_7 \rangle + \dots$$

with $\langle \tilde{Q}_6 \rangle \propto f_B^2 B_{1,2,3}$ and $\langle \tilde{Q}_7 \rangle \propto f_B^2 R_{0,2,3}, m_s/m_b f_B^2 B_{4,5}$ and $\tilde{\Gamma}_i = \tilde{\Gamma}_i^{(0)} + \frac{\alpha}{4\pi} \tilde{\Gamma}_i^{(1)} + \dots$

$\tilde{\Gamma}_6^{(1)}$

- 1998 Beneke, Buchalla, Greub, AL, Nierste
- 2003 Franco, Lubicz, Mescia, Tarantino
- 2003 Beneke, Buchalla, AL, Nierste
- 2006 AL, Nierste

$\langle \tilde{Q}_6 \rangle$

- B_1 the same as for ΔM , $B_{2,3,4,5}$ new
- 2016 FNAL/MILC
- 2016-18 Grozin, Klein, Mannel, Pivovarov B_d
- 2017 Kirk, AL, Rauh B_d
- 2019 King, AL, Rauh B_s
- 2019 HPQCD 19007.01025

$\tilde{\Gamma}_6^{(2)}$

- 2017 partly: Asatrian, Hovhannisyanyan, Nierste, Yeghiazaryan
- 2020 partly: Asatrian, Asatryan, Hovhannisyanyan, Nierste, Tumasyan
- 2021 partly: Gerlach, Nierste, Shtabovenko, Steinhauser

$\langle \tilde{Q}_7 \rangle$

- So far only Vacuum insertion approximation
- 2019 HPQCD 1910.00970

$\tilde{\Gamma}_7^{(0)}$

- 1996 Beneke, Buchalla, Dunietz
- 2001 Dighe, Hurth, Kim

$\tilde{\Gamma}_7^{(1)}$

- 202x Nierste and friends

$\tilde{\Gamma}_8^{(0)}$

- 2007 Badin, Gabbiani, Petrov

$$R_2 = \frac{1}{m_b^2} (\bar{b}^\alpha \overleftarrow{D}_\rho \gamma^\mu (1 - \gamma^5) D^\rho s^\alpha) (\bar{b}^\beta \gamma_\mu (1 - \gamma^5) s^\beta)$$

$$R_3 = \frac{1}{m_b^2} (\bar{b}^\alpha \overleftarrow{D}_\rho (1 - \gamma^5) D^\rho s^\alpha) (\bar{b}^\beta (1 - \gamma^5) s^\beta)$$

This work

$$\Delta\Gamma_s^{HQE} = (0.091 \pm 0.013) \text{ ps}^{-1}$$

$$\Delta\Gamma_s^{HFLAV} = (0.082 \pm 0.005) \text{ ps}^{-1}$$

$$\Delta\Gamma_d^{HQE} = (2.6 \pm 0.4) \cdot 10^{-3} \text{ ps}^{-1}$$

$$\Delta\Gamma_d^{HFLAV} = (-1.3 \pm 6.6) \cdot 10^{-3} \text{ ps}^{-1}$$

1912.07621

HFLAV, ATLAS 1605.07485

Status Quo: CPV in Mixing

In the ratio Γ_{12}/M_{12} theory uncertainties are cancelling

$$\text{Re} \left(\frac{\Gamma_{12}^s}{M_{12}^s} \right) = -\frac{\Delta\Gamma_s}{\Delta M_s}, \quad \text{Im} \left(\frac{\Gamma_{12}^s}{M_{12}^s} \right) = a_{fs}^s.$$

$$-\frac{\Gamma_{12}^s}{M_{12}^s} = \frac{\lambda_c^2 \Gamma_{12}^{s,cc} + 2\lambda_c \lambda_u \Gamma_{12}^{s,uc} + \lambda_u^2 \Gamma_{12}^{s,uu}}{\lambda_t^2 \tilde{M}_{12}^s} = \frac{\Gamma_{12}^{s,cc}}{\tilde{M}_{12}^s} + 2 \frac{\lambda_u}{\lambda_t} \frac{\Gamma_{12}^{s,cc} - \Gamma_{12}^{s,uc}}{\tilde{M}_{12}^s} + \left(\frac{\lambda_u}{\lambda_t} \right)^2 \frac{\Gamma_{12}^{s,cc} - 2\Gamma_{12}^{s,uc} + \Gamma_{12}^{s,uu}}{\tilde{M}_{12}^s}$$

- No CKM dependence!
- No GIM suppression!
- No imaginary part!
- Small $\approx \mathcal{O}(5 \cdot 10^{-3})$
- Leading contribution to $\Delta\Gamma$

- CKM suppression
- GIM suppression
- Imaginary part via CKM
- Leading contribution to a_{fs}
- Tiny contribution to $\Delta\Gamma$

$$\frac{V_{ub}V_{ud}}{V_{tb}V_{td}} = \lambda^{0.8}$$

$$\frac{V_{ub}V_{us}}{V_{tb}V_{ts}} = \lambda^{2.8}$$

- Stronger CKM suppression
- Very strong GIM suppression
- Imaginary part via CKM
- Subleading contribution to a_{fs} and $\Delta\Gamma$

$$a_{sl}^{s,\text{Exp}} = (60 \pm 280) \cdot 10^{-5}, \quad a_{sl}^{s,\text{SM}} = (2.06 \pm 0.18) \cdot 10^{-5},$$

$$a_{sl}^{d,\text{Exp}} = (-21 \pm 17) \cdot 10^{-4}, \quad a_{sl}^{d,\text{SM}} = (-4.73 \pm 0.42) \cdot 10^{-4}.$$

HFLAV 1970?

1912.07621

Alternative Scale Setting

ϵ (GeV)	Γ_{12}^s/M_{12}^s	Γ_{12}^d/M_{12}^d
0.	-0.00499 + 0.000022I	-0.00497 - 0.00050I
0.2.	-0.00494 + 0.000023I	-0.00492 - 0.00053I
0.5.	-0.00484 + 0.000026I	-0.00482 - 0.00059I
1.0.	-0.00447 + 0.000037I	-0.00448 - 0.00084I
1.5.	-0.00287 + 0.000091I	-0.00309 - 0.0021I

Theory uncertainties might be larger, but this will only become relevant if the exp. precision reaches around

$$2 a_{fs}^{\text{SM}}$$

AL, Piscopo, Vlahos 2007.03022

CP Violation

1. **CP violation in Mixing**: Consider a **flavour specific** ($\mathcal{A}_{\bar{f}} = 0 = \bar{\mathcal{A}}_f$) **decay** $B \rightarrow f$

$$A_{\text{fs}}^q = \frac{\Gamma(\bar{B}_q(t) \rightarrow f) - \Gamma(B_q(t) \rightarrow \bar{f})}{\Gamma(\bar{B}_q(t) \rightarrow f) + \Gamma(B_q(t) \rightarrow \bar{f})} \quad \boxed{\bar{\mathcal{A}}_{\bar{f}} = \mathcal{A}_f} \\ = \text{No direct CP violation}$$

$$a_{\text{fs}}^q \approx \frac{|\Gamma_{12}^q|}{|M_{12}^q|} \sin \phi_{12}^q$$

e.g. $B \rightarrow Xl\nu$
 or $\bar{B}_s \rightarrow D_s^+ \pi^-$
 or $\bar{B}_d \rightarrow D^+ K^-$

2. **CP violation in interference of mixing and decay**

$$A_{\text{ind}}^q = \frac{\Gamma(\bar{B}_q(t) \rightarrow f) - \Gamma(B_q(t) \rightarrow f)}{\Gamma(\bar{B}_q(t) \rightarrow f) + \Gamma(B_q(t) \rightarrow f)}$$

e.g. $B_s \rightarrow J/\Psi \phi$
 or $B_d \rightarrow J/\Psi K_s$

See also
 1511.09466,
 hep-ph/0201071

3. **CP violation in decay**

$$A_{\text{dir}}^q = \frac{\Gamma(\bar{B}_q(t) \rightarrow \bar{f}) - \Gamma(B_q(t) \rightarrow f)}{\Gamma(\bar{B}_q(t) \rightarrow \bar{f}) + \Gamma(B_q(t) \rightarrow f)} = \frac{|\bar{\mathcal{A}}_{\bar{f}}|^2 - |\mathcal{A}_f|^2}{|\bar{\mathcal{A}}_{\bar{f}}|^2 + |\mathcal{A}_f|^2}$$

e.g. ΔA_{CP}
 or $D^0 \rightarrow \pi^- \pi^+, K^- K^+$

Time evolution

Time evolution of neutral B mesons (quantum mechanics on a macroscopic scale)

$$\Gamma [\bar{B}_q(t) \rightarrow f] = N_f |\mathcal{A}_f|^2 \frac{(1 + |\lambda_f|^2)}{2} (1 + a_{fs}^q) e^{-\Gamma_q t} \left\{ \cosh \left(\frac{\Delta\Gamma_q t}{2} \right) - \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2} \cos(\Delta M_q t) - \frac{2 \operatorname{Re}(\lambda_f)}{1 + |\lambda_f|^2} \sinh \left(\frac{\Delta\Gamma_q t}{2} \right) + \frac{2 \operatorname{Im}(\lambda_f)}{1 + |\lambda_f|^2} \sin(\Delta M_q t) \right\},$$

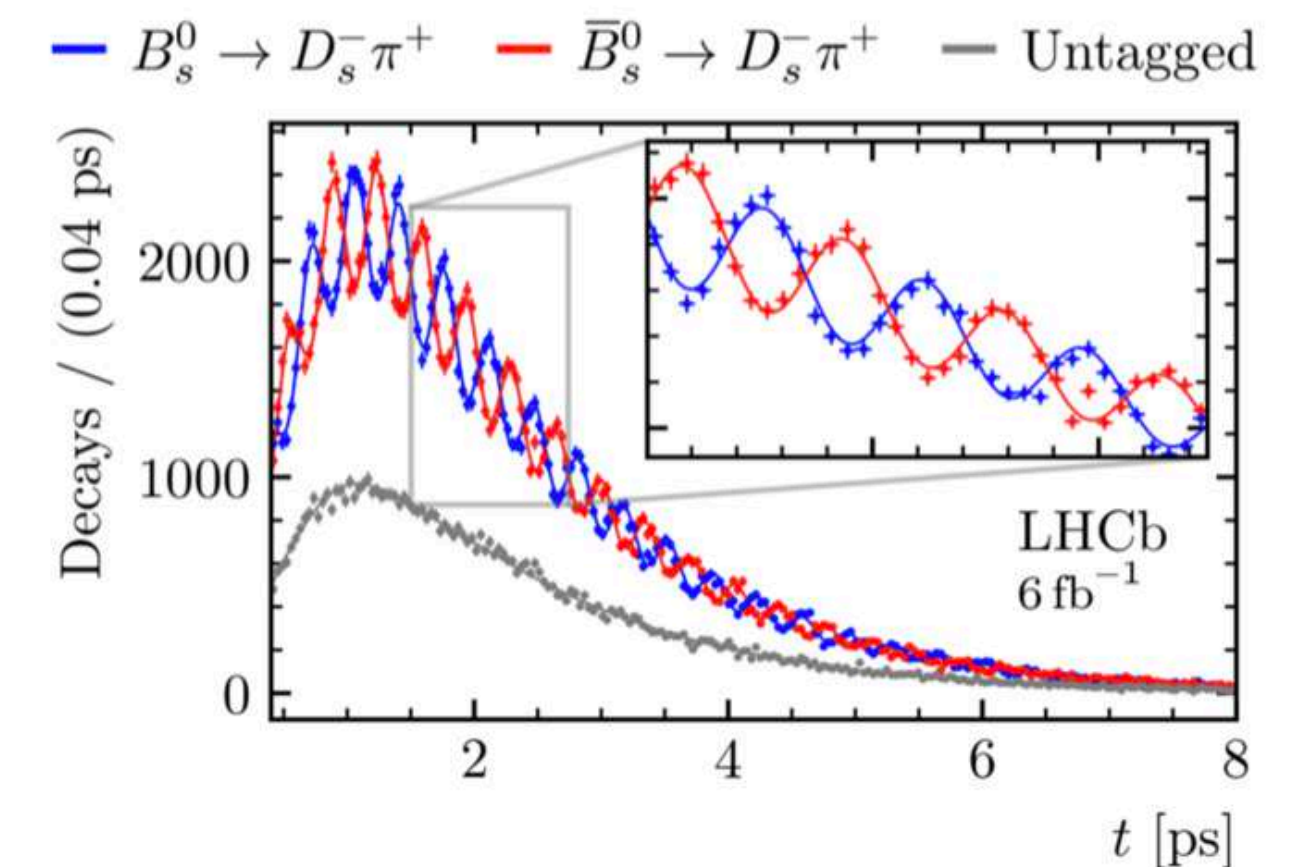
With

$$\mathcal{A}_f = \langle f | \mathcal{H}_{\text{eff}} | B_q \rangle,$$

$$\bar{\mathcal{A}}_f = \langle f | \mathcal{H}_{\text{eff}} | \bar{B}_q \rangle,$$

$$\lambda_f = \frac{q}{p} \frac{\bar{\mathcal{A}}_f}{\mathcal{A}_f}$$

and the tiny quantity a_{fs}^q to be defined below



Status Quo: CPV in Interference

$$A_{CP,f}(t) = \frac{\Gamma(\bar{B}_s^0(t) \rightarrow f) - \Gamma(B_s^0(t) \rightarrow f)}{\Gamma(\bar{B}_s^0(t) \rightarrow f) + \Gamma(B_s^0(t) \rightarrow f)} = -\frac{\mathcal{A}_{CP}^{\text{dir}} \cos(\Delta M_s t) + \mathcal{A}_{CP}^{\text{mix}} \sin(\Delta M_s t)}{\cosh(\frac{\Delta\Gamma_s t}{2}) + \mathcal{A}_{\Delta\Gamma} \sinh(\frac{\Delta\Gamma_s t}{2})}$$

$$\mathcal{A}_{CP}^{\text{dir}} = \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2},$$

$$\mathcal{A}_{CP}^{\text{mix}} = -\frac{2\Im(\lambda_f)}{1 + |\lambda_f|^2},$$

$$\mathcal{A}_{\Delta\Gamma} = -\frac{2\Re(\lambda_f)}{1 + |\lambda_f|^2}.$$

$$\lambda_f \approx -\frac{V_{ts}V_{tb}^*}{V_{ts}^*V_{tb}} \frac{\bar{A}_f}{A_f} \left[1 - \frac{a_{fs}^s}{2} \right]$$

$$\mathcal{A}_f = \langle f | \mathcal{H}_{eff} | B_s^0 \rangle$$

$$\bar{\mathcal{A}}_f = \langle f | \mathcal{H}_{eff} | \bar{B}_s^0 \rangle$$

CP violation in the B_s^0 system

[Marina Artuso \(Syracuse U.\)](#), [Guennadi Borissov \(Lancaster U.\)](#), [Alexander Lenz \(Durham U., IPPP\)](#) (Nov 30, 2015)

Published in: *Rev.Mod.Phys.* 88 (2016) 4, 045002, *Rev.Mod.Phys.* 91 (2019) 4, 049901 (addendum) • e-Print:

[1511.09466 \[hep-ph\]](#)

If there is **only one decay topology** contributing to the decay

$$\mathcal{A}_f = |\mathcal{A}_f^{\text{Tree}}| e^{i[\phi_{\text{Tree}}^{\text{QCD}} + \arg(\lambda_c)]}$$

$$\bar{\mathcal{A}}_{\bar{f}} = |\mathcal{A}_f^{\text{Tree}}| e^{i[\phi_{\text{Tree}}^{\text{QCD}} - \arg(\lambda_c)]}$$

$$\frac{\bar{\mathcal{A}}_{fCP}}{\mathcal{A}_{fCP}} = -\eta_{CP} e^{-2i\phi_j^{\text{CKM}}}$$

All hadronic uncertainties are cancelling exactly in the CP asymmetry!

Gold-plated modes

Status Quo: CPV in Interference

If there are **two decay topologies** contributing to the decay

$$\mathcal{A}_f = |\mathcal{A}_f^{\text{Tree}}| e^{i[\phi_{\text{Tree}}^{\text{QCD}} + \arg(\lambda_c)]} + |\mathcal{A}_f^{\text{Peng}}| e^{i[\phi_{\text{Peng}}^{\text{QCD}} + \arg(\lambda_u)]}$$
$$\bar{\mathcal{A}}_{\bar{f}} = |\mathcal{A}_f^{\text{Tree}}| e^{i[\phi_{\text{Tree}}^{\text{QCD}} - \arg(\lambda_c)]} + |\mathcal{A}_f^{\text{Peng}}| e^{i[\phi_{\text{Peng}}^{\text{QCD}} - \arg(\lambda_u)]}$$

Could also be BSM if there is only one SM amplitude

Then the CP asymmetry depends on

$$\frac{\bar{\mathcal{A}}_{\bar{f}}}{\mathcal{A}_f} = -e^{-2i \arg(\lambda_c)} \left[\frac{1 + r e^{-i \arg(\frac{\lambda_u}{\lambda_c})}}{1 + r e^{+i \arg(\frac{\lambda_u}{\lambda_c})}} \right]$$

$$\text{with } r = \left| \frac{\mathcal{A}_f^{\text{Peng}}}{\mathcal{A}_f^{\text{Tree}}} \right|$$

If penguins are small compared to tree-level, the hadronic corrections are cancelling to leading order and there is a correction proportional to r

Penguin pollution

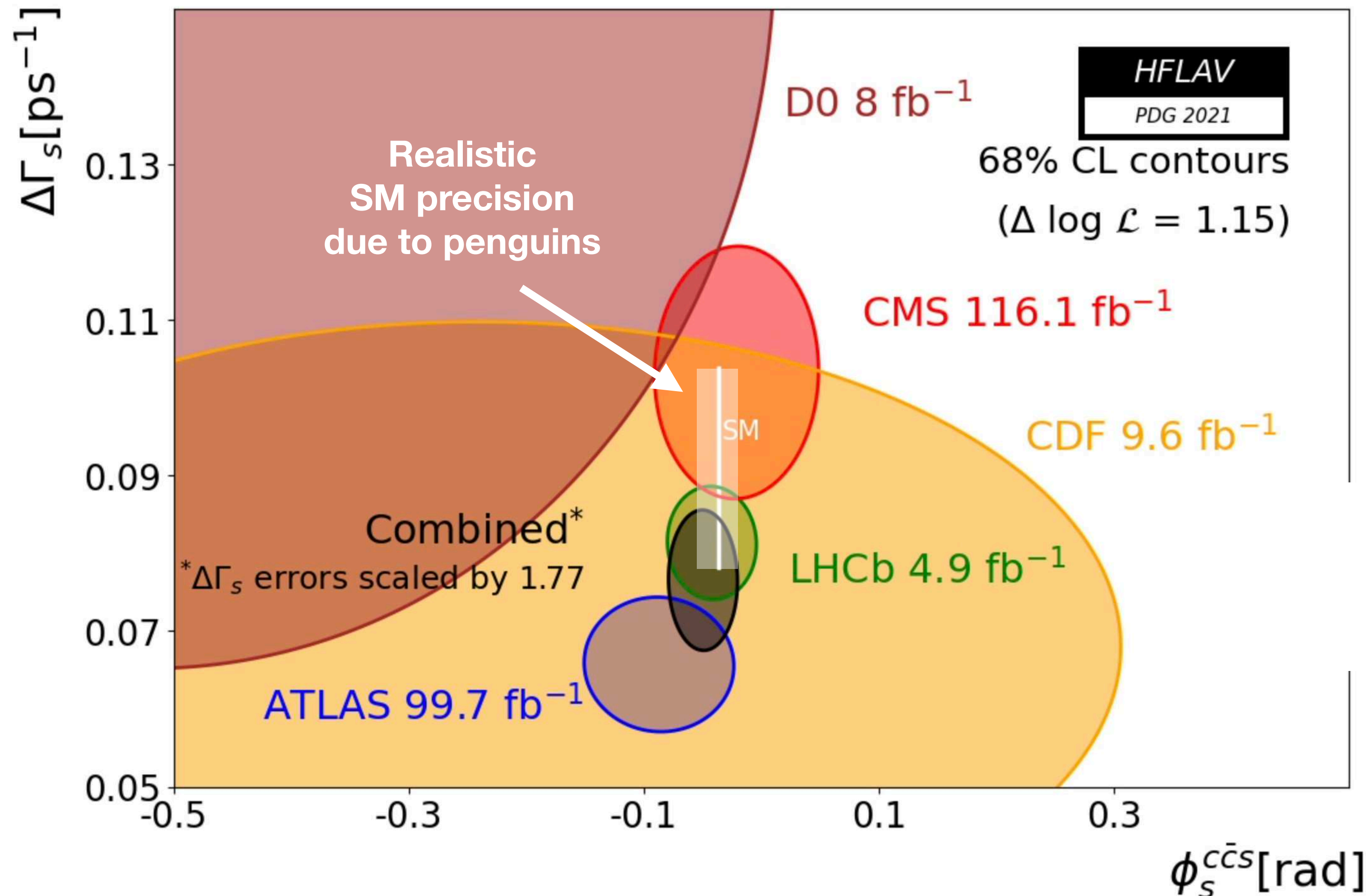
CP violation in the B_s^0 system

Marina Artuso (Syracuse U.), Guennadi Borissov (Lancaster U.), Alexander Lenz (Durham U., IPPP) (Nov 30, 2015)

Published in: *Rev.Mod.Phys.* 88 (2016) 4, 045002, *Rev.Mod.Phys.* 91 (2019) 4, 049901 (addendum) • e-Print: [1511.09466](https://arxiv.org/abs/1511.09466) [hep-ph]

Status Quo: CPV in Interference

Golden plated modes: $B_s \rightarrow J/\Psi\phi$



Modification due to **New Physics**

$$M_{12}^s = M_{12}^{s,\text{SM}} |\Delta_s| e^{i\phi_s^\Delta}$$

$$\Gamma_{12}^s = \Gamma_{12}^{s,\text{SM}} |\tilde{\Delta}| e^{-i\phi_s^{\tilde{\Delta}}}$$

$B_s \rightarrow J/\Psi\phi$

$$-2\beta_s^{\text{Exp}} = -2\beta_{s,\text{Tree}}^{\text{SM}} + \phi_s^\Delta + \beta_{s,\text{Peng}}^{\text{SM}} + \beta_{s,\text{Peng}}^{\text{BSM}},$$

$$\phi_{12}^{s,\text{Exp}} = \phi_{12}^{s,\text{SM}} + \phi_s^\Delta + \tilde{\phi}_s^{\tilde{\Delta}},$$

a_{fs}^s

not really constrained by $\phi_s^{c\bar{c}s}$

Status Quo: CPV in Decay

$$A_{\text{dir.CP},f}(t) = \frac{\Gamma(\bar{B}_s^0(t) \rightarrow \bar{f}) - \Gamma(B_s^0(t) \rightarrow f)}{\Gamma(\bar{B}_s^0(t) \rightarrow \bar{f}) + \Gamma(B_s^0(t) \rightarrow f)} = \frac{|\bar{\mathcal{A}}_{\bar{f}}|^2 - |\mathcal{A}_f|^2}{|\bar{\mathcal{A}}_{\bar{f}}|^2 + |\mathcal{A}_f|^2} = \frac{2|r| \sin(\phi_{\text{Peng}}^{\text{QCD}} - \phi_{\text{Tree}}^{\text{QCD}}) \sin[\arg(\lambda_u) - \arg(\lambda_c)]}{1 + |r|^2 + 2|r| \cos(\phi_{\text{Peng}}^{\text{QCD}} - \phi_{\text{Tree}}^{\text{QCD}}) \cos[\arg(\lambda_u) - \arg(\lambda_c)]}$$

$$\mathcal{A}_f = |\mathcal{A}_f^{\text{Tree}}| e^{i[\phi_{\text{Tree}}^{\text{QCD}} + \arg(\lambda_c)]} + |\mathcal{A}_f^{\text{Peng}}| e^{i[\phi_{\text{Peng}}^{\text{QCD}} + \arg(\lambda_u)]}$$

$$\bar{\mathcal{A}}_{\bar{f}} = |\mathcal{A}_f^{\text{Tree}}| e^{i[\phi_{\text{Tree}}^{\text{QCD}} - \arg(\lambda_c)]} + |\mathcal{A}_f^{\text{Peng}}| e^{i[\phi_{\text{Peng}}^{\text{QCD}} - \arg(\lambda_u)]}$$

The **leading contribution to the CP asymmetry is proportional to** $r = |\mathcal{A}_f^{\text{Peng}}| / |\mathcal{A}_f^{\text{Tree}}|$

Extremely hard to predict!

(In the case of CPV in interference the leading term was free of hadronic uncertainties and only the penguin corrections depended on r)



Direct CP asymmetries

- $B \rightarrow K\pi$ puzzle still present, see. e.g. 1507.03700

Updates: [2002.03262](#) complete 2-loop penguins

[2107.03819](#) QED corrections

[2104.14871](#) $A_{CP}(B^0 \rightarrow \pi^0 \bar{K}^0)$ Belle II

SU(3) symmetry e.g. [1806.08783](#), [2111.06418](#),...

comprehensive phenomenological study missing



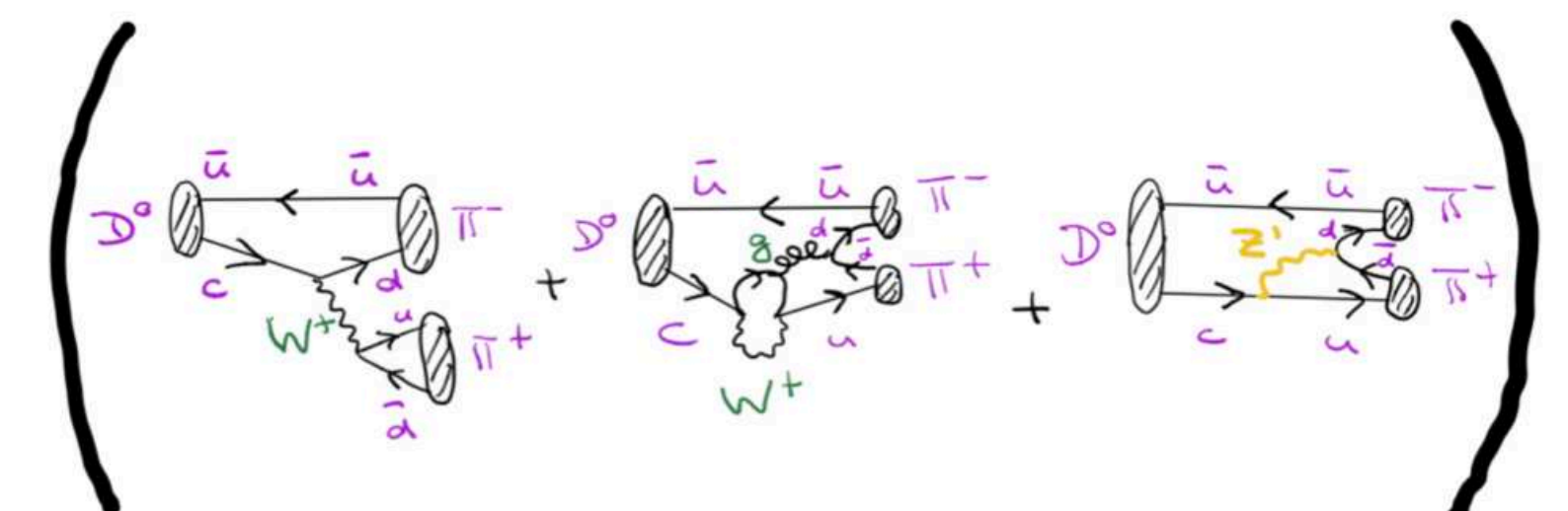
We need $r = | \mathcal{A}_f^{\text{Peng}} | / | \mathcal{A}_f^{\text{Tree}} |$

- ΔA_{CP} : direct CP violation in the charm system $D^0 \rightarrow K^+ K^-$ vs. $D^0 \rightarrow \pi^+ \pi^-$

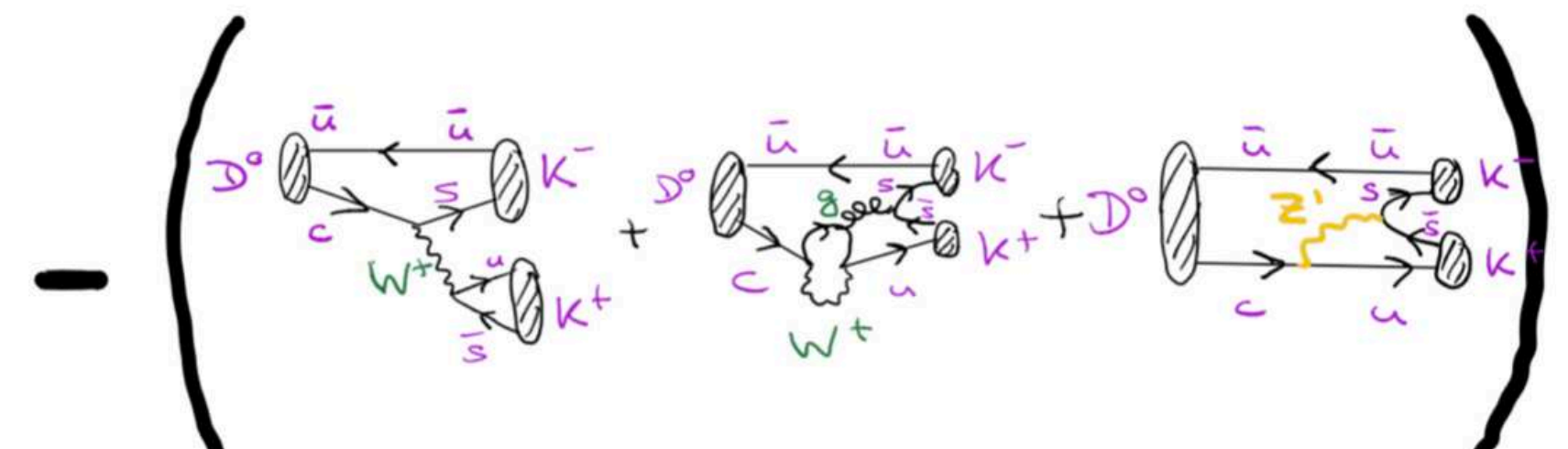
Experiment: LHCb 03/2019

Theory: SM or not SM?

E.g. [1903.10952](#), [1909.03063](#) vs. [1903.10490](#), [1909.11242](#)



We need $r = | \mathcal{A}_f^{\text{Peng}} | / | \mathcal{A}_f^{\text{Tree}} |$



Not so well-known:

Not so well-known:

- $\tau(B_s)/\tau(B_d)$ and $\Delta\Gamma_d$

$\Delta\Gamma_d$: A Forgotten Null Test of the Standard Model

Tim Gershon¹

Remember: D0 di muon asymmetry....



The ATLAS collaboration

E-mail: atlas.publications@cern.ch

ABSTRACT: This paper presents the measurement of the relative width difference $\Delta\Gamma_d/\Gamma_d$ of the $B^0-\bar{B}^0$ system using the data collected by the ATLAS experiment at the LHC in pp collisions at $\sqrt{s} = 7$ TeV and $\sqrt{s} = 8$ TeV and corresponding to an integrated luminosity of 25.2fb^{-1} . The value of $\Delta\Gamma_d/\Gamma_d$ is obtained by comparing the decay-time distributions of $B^0 \rightarrow J/\psi K_S$ and $B^0 \rightarrow J/\psi K^{*0}(892)$ decays. The result is $\Delta\Gamma_d/\Gamma_d = (-0.1 \pm 1.1 \text{ (stat.)} \pm 0.9 \text{ (syst.)}) \times 10^{-2}$. Currently, this is the most precise single measurement of $\Delta\Gamma_d/\Gamma_d$. It agrees with the Standard Model prediction and the measurements by other experiments.

- $b \rightarrow d\ell\ell$, e.g. differential q^2 distr. & CP asym. in $B \rightarrow \pi\ell\ell$, see e.g. **Rusov 1911.12819**, R_π

- $b \rightarrow s\tau\tau$ transitions, e.g. **Cornella, Isidori, König, Liechti, Owen 2001.04470**

- Inclusive $B \rightarrow X_s\ell\ell$, e.g. **Huber, Hurth, Jenkins, Lunghi, Qin, Vos 2007.04191**

- $B \rightarrow D^*\mu\nu$ - angular distribution, or even better $B \rightarrow D^*\tau\nu$ distribution q^2 distribution not enough, as effects of some NP operators can only be seen in particular angular observables

Rusa Mandal, Clara Murgui, Ana Peñuelas, Antonio Pich 2004.06726

- **for a complete LCSR analysis of nonlocal effects (charm loop etc.) in $B_s \rightarrow \phi\ell\ell$, accurate data on BR and amplitude decomposition are needed on hadronic B_s -decays such as $B_s \rightarrow \psi\phi$ where ψ are charmonia $J/\psi, \psi(2S)$ and above, also $B_s \rightarrow D^{(*)}\bar{D}\phi$ (for $B \rightarrow K$ and $B \rightarrow K^*$ channels this type of data is available)**

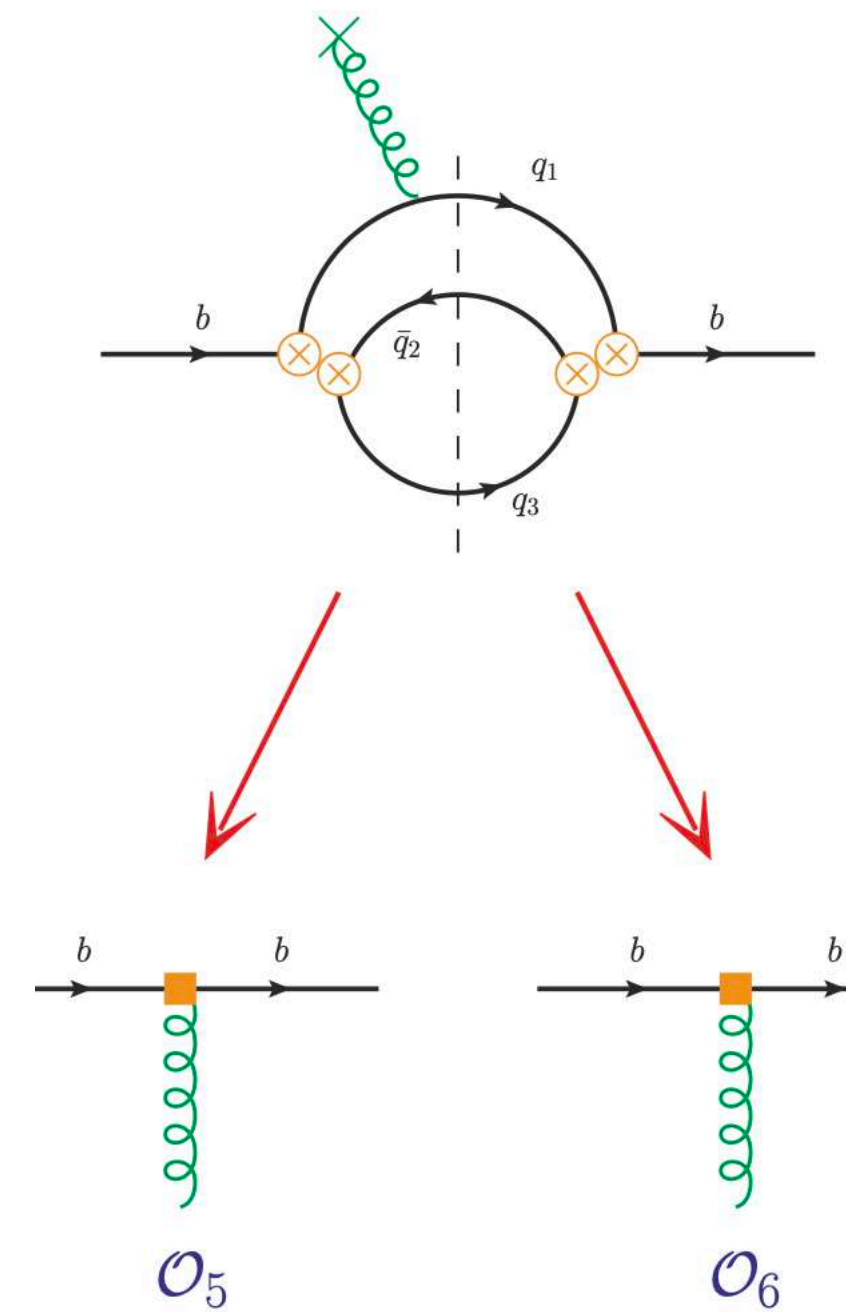
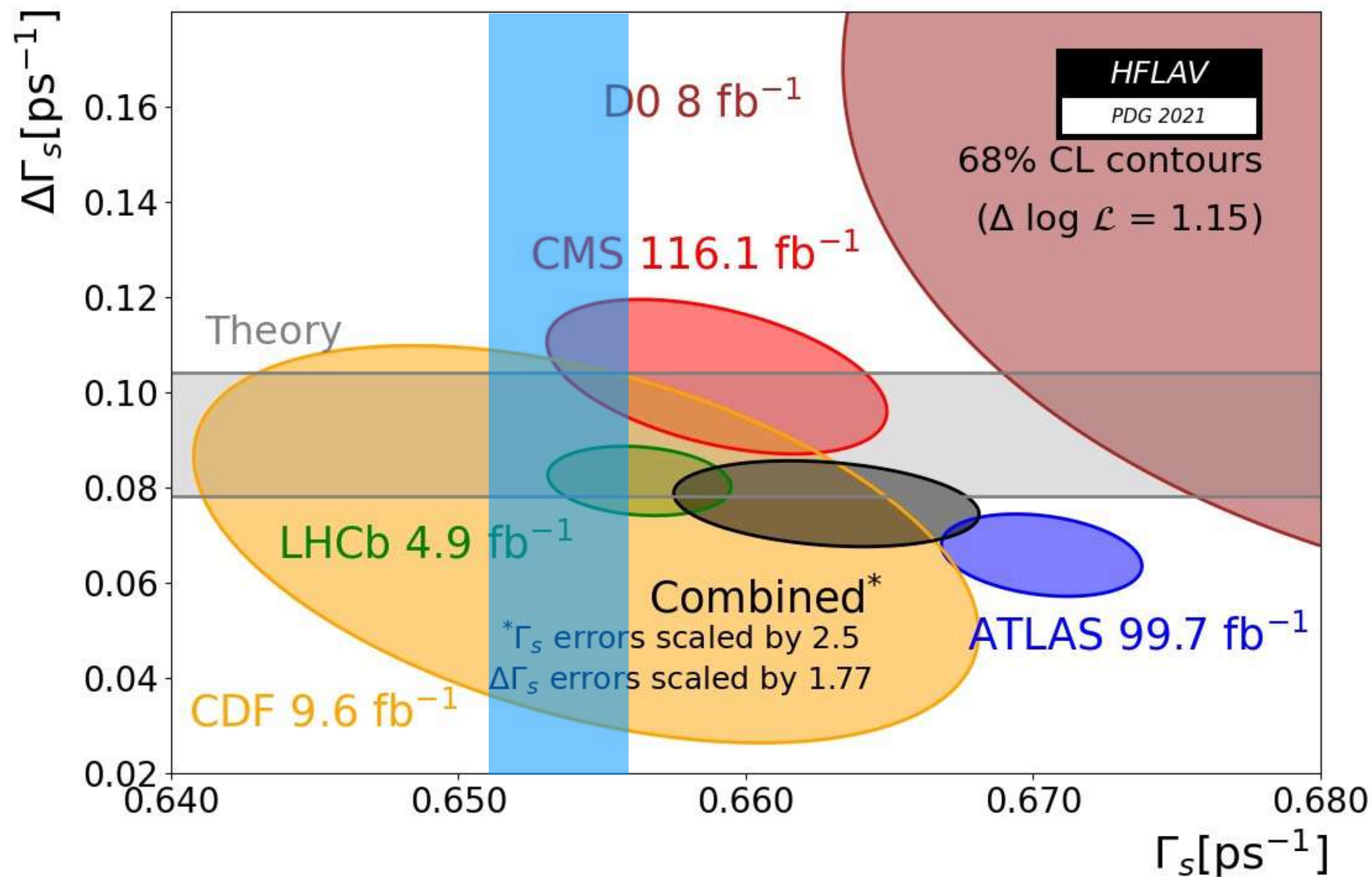
The BR and angular distributions of hadronic decays are needed as inputs (pole residues) in the dispersion relation for the $B_s \rightarrow \phi\ell\ell$ nonlocal amplitude to be matched to the LCSR calculation

$\tau(B_s)/\tau(B_d)$

A less well known 4 sigma anomaly :-)

But be aware:

so far large Darwin term has not been included



AL, Piscopo, Rusov

2004.09527

Mannel, Moreno, Pivovarov 2004.09485

Dominant uncertainty

$$\rho_D^3(B_s) - \rho_D^3(B_d)$$

unknown

Known from inclusive V_{cb} determination

**SM based on 1711.02100,
based on hep-ph/0202106
and hep-ph/0203089 - obtained via**

$$\Gamma_s = 1/[\tau(B_s)/\tau(B_d)]^{HQE} * 1/\tau(B_d)^{EXP}$$

$$\tau(B_s)/\tau(B_d)$$

Precise lifetime ratio in Exp. and Theory can be used to constrain BSM effects

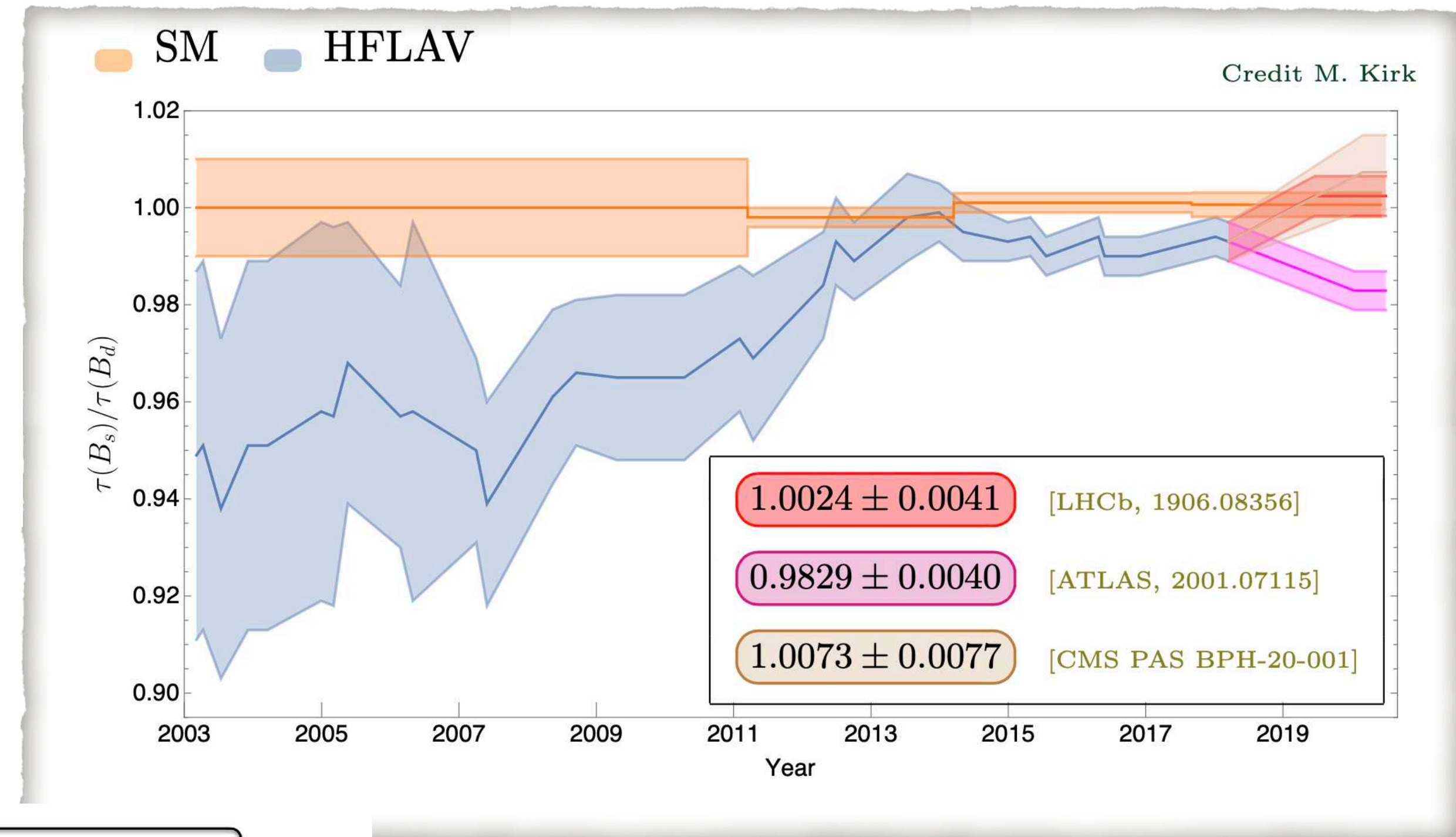
$$\underbrace{\frac{\tau(B_s)}{\tau(B_d)}}_{\text{exp.}} \approx 1 + \underbrace{\tau(B_s) (\delta\Gamma_{B_d}^{\text{SM}} - \delta\Gamma_{B_s}^{\text{SM}})}_{\text{theory}} + \underbrace{[\text{BR}(B_d \rightarrow X)^{\text{BSM}} - \text{BR}(B_s \rightarrow X)^{\text{BSM}}]}_{\text{indirectly constrained}}$$

Examples:

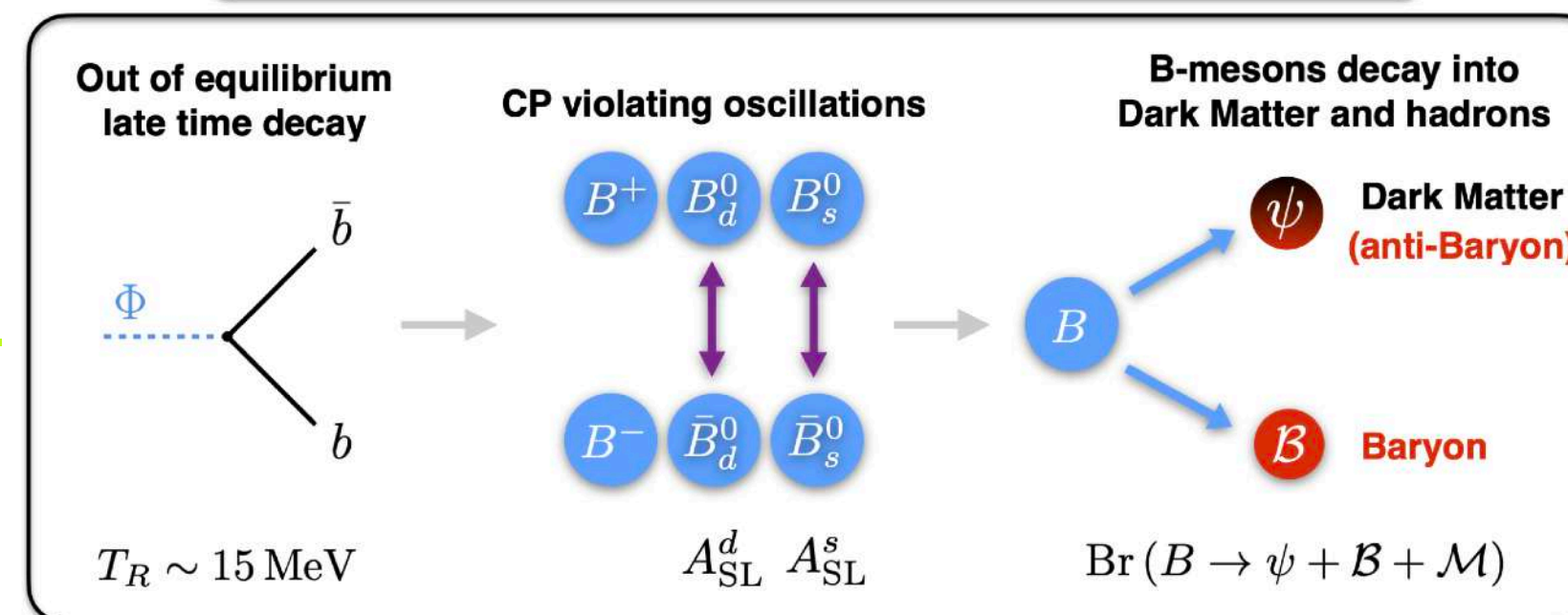
- $b \rightarrow s\tau\tau$, see **Bobeth, Haisch 1109.1826**
- New non-leptonic tree-level operators
- B meson baryogenesis

•

Still higher experimental precision needed



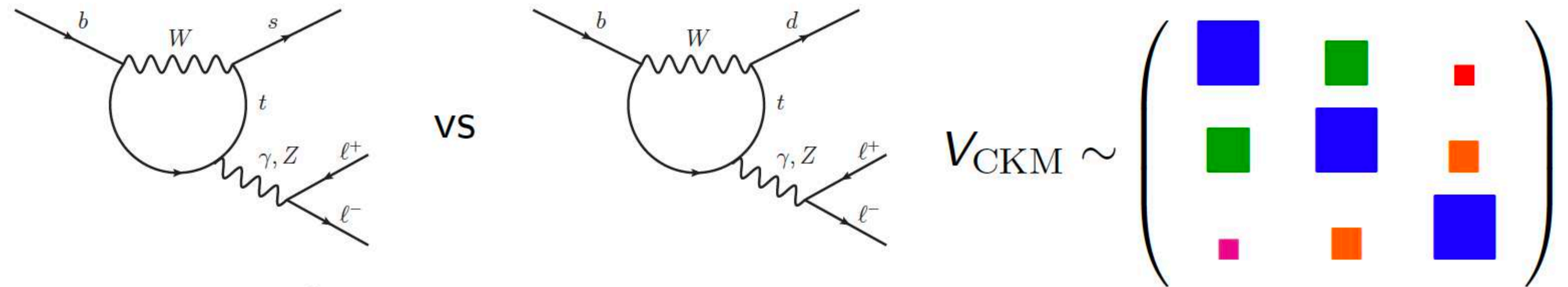
Baryogenesis and Dark Matter from B Mesons: *B-Mesogenesis*



Ann Nelson,....
Gonzalo-Alvarez, Elor, Escudero

$b \rightarrow d$ VS $b \rightarrow s$

$b \rightarrow d\ell\ell$



- Additionally CKM suppressed

$$\left| \frac{V_{tb} V_{td}^*}{V_{tb} V_{ts}^*} \right| \approx 0.22 \Rightarrow \left| \frac{V_{tb} V_{td}^*}{V_{tb} V_{ts}^*} \right|^2 \approx 0.05$$

- $b \rightarrow d$ transitions induce **non-vanishing** direct **CP-asymmetry**

▷ In $b \rightarrow s$:

$$|V_{tb} V_{ts}^*| \sim |V_{cb} V_{cs}^*| \sim \lambda^2 \gg |V_{ub} V_{us}^*| \sim \lambda^4$$

▷ In $b \rightarrow d$:

$$|V_{tb} V_{td}^*| \sim |V_{cb} V_{cd}^*| \sim |V_{ub} V_{ud}^*| \sim \lambda^3$$

- Also sensitive to contribution from **New Physics (NP)**

Study also decays like

$B \rightarrow (\pi, \rho, \omega)\ell\ell$ and $B_s \rightarrow (\eta, K^*)\ell\ell$

Surprise and/or Underdogs

Surprise and/or underdogs...:

- Inclusive semi-leptonic fit of moments in B_s decays at LHCb? Belle II?
Determine also non-perturbative matrix elements $\mu_G^2(B_s), \mu_\pi^2(B_s), \rho_D^3(B_s), \dots$
 - Inclusive semi-leptonic fit of moments of charm decays BESIII, Belle II?
Determine also non-perturbative matrix elements $\mu_G^2(D), \mu_\pi^2(D), \rho_D^3(D), \dots$
 - Non-leptonic tree-level decays: BSM in leading tree-level? $B \rightarrow K\pi$ puzzle
 - $B_c \rightarrow \tau\nu$: determination of V_{cb} depending only on decay constant f_{B_c}
 - Very rare to impossible decays: $B_{(s)} \rightarrow \tau\mu, B \rightarrow K\tau\mu, \dots$ and also D decays
 $\tau \rightarrow \mu\mu\mu$ and friends
 - measurement of V_{us} from τ decays with reasonable precision, Belle II?
Test Cabibbo anomaly, without any lattice input
-

Surprise and/or underdogs...:

Test of our theory tools:

Total inclusive quantities, like lifetimes or inclusive semi-leptonic branching ratios:

Theoretically well-behaved

compared to crazy GIM cancellations in D- mixing

Results

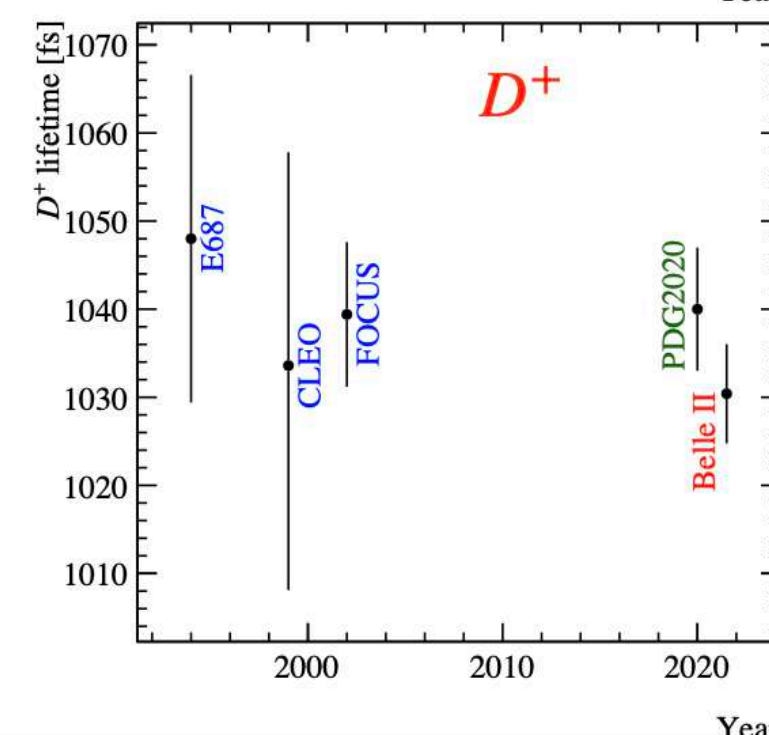
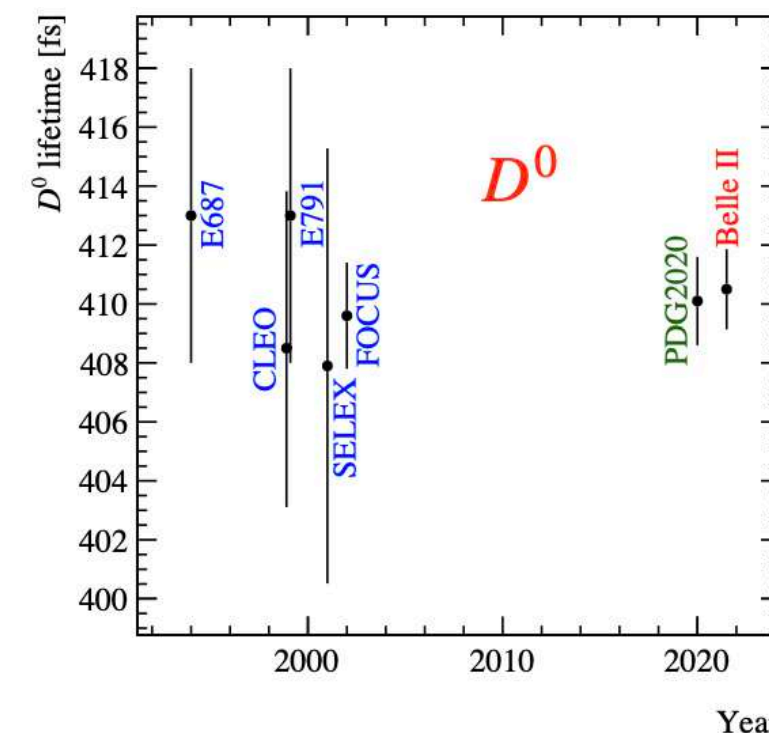
$$\tau(D^0) = 410.5 \pm 1.1 \pm 0.8 \text{ fs}$$

$$\tau(D^+) = 1030.4 \pm 4.7 \pm 3.1 \text{ fs}$$

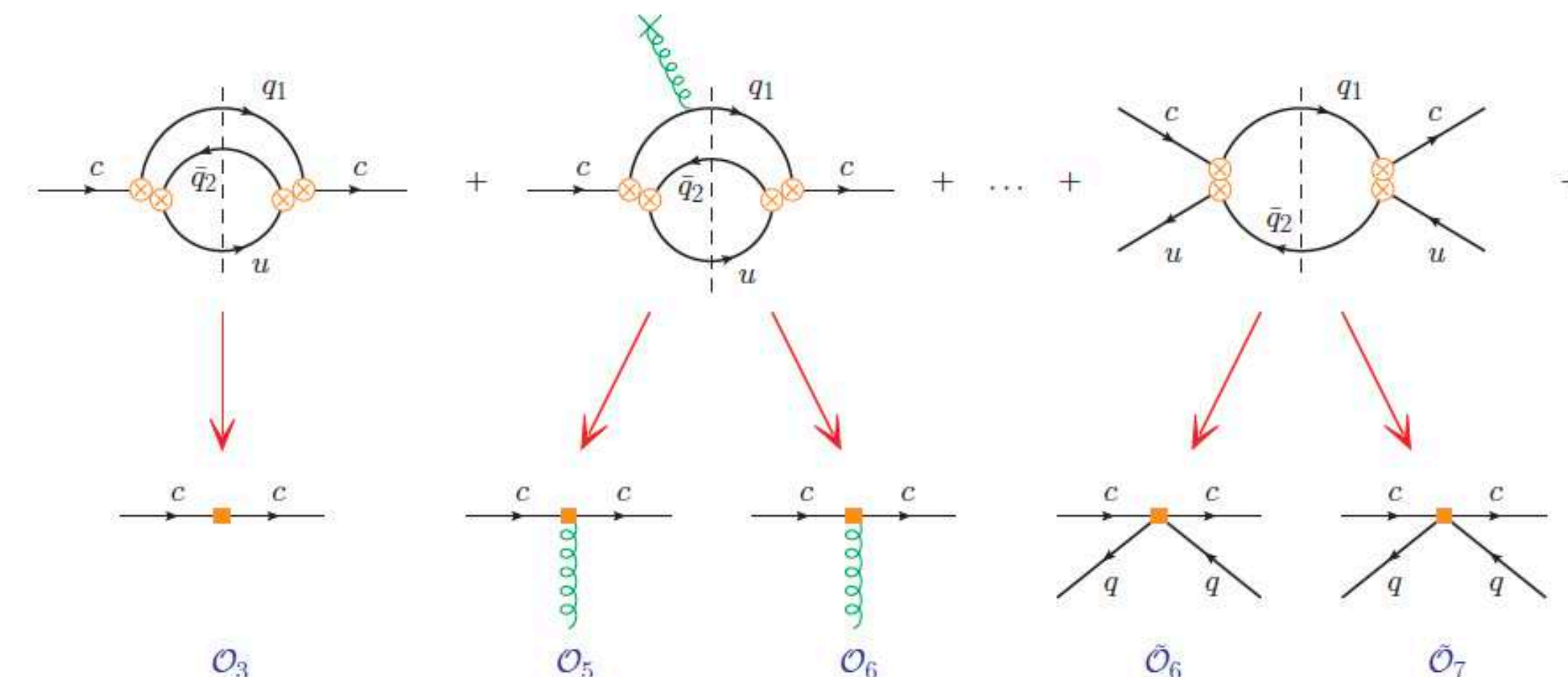
$$\tau(D^+)/\tau(D^0) = 2.510 \pm 0.015$$

determined considering correlations between (systematic) uncertainties

- Consistent with current world averages $410.1 \pm 1.5 \text{ fs}$ (D^0) and $1040 \pm 7 \text{ fs}$ (D^+).
- World's most precise measurements of the D^0 and D^+ lifetimes
- **Few ‰ accuracy** (3.5‰ for the D^0 and 5.4‰ for the D^+) **establishes excellent performance of our detector!**
- submitted to PRL, <https://arxiv.org/abs/2108.03216>



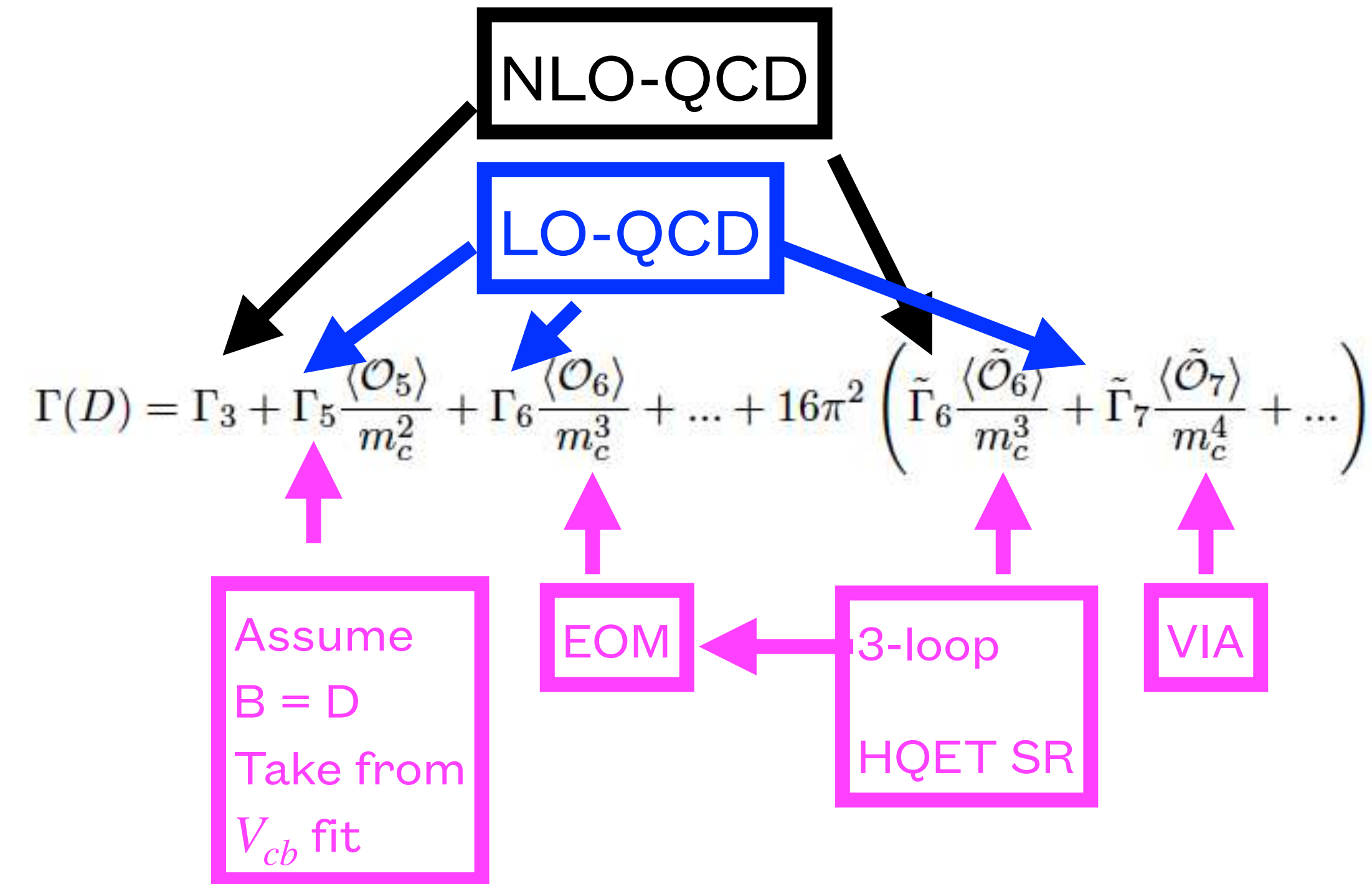
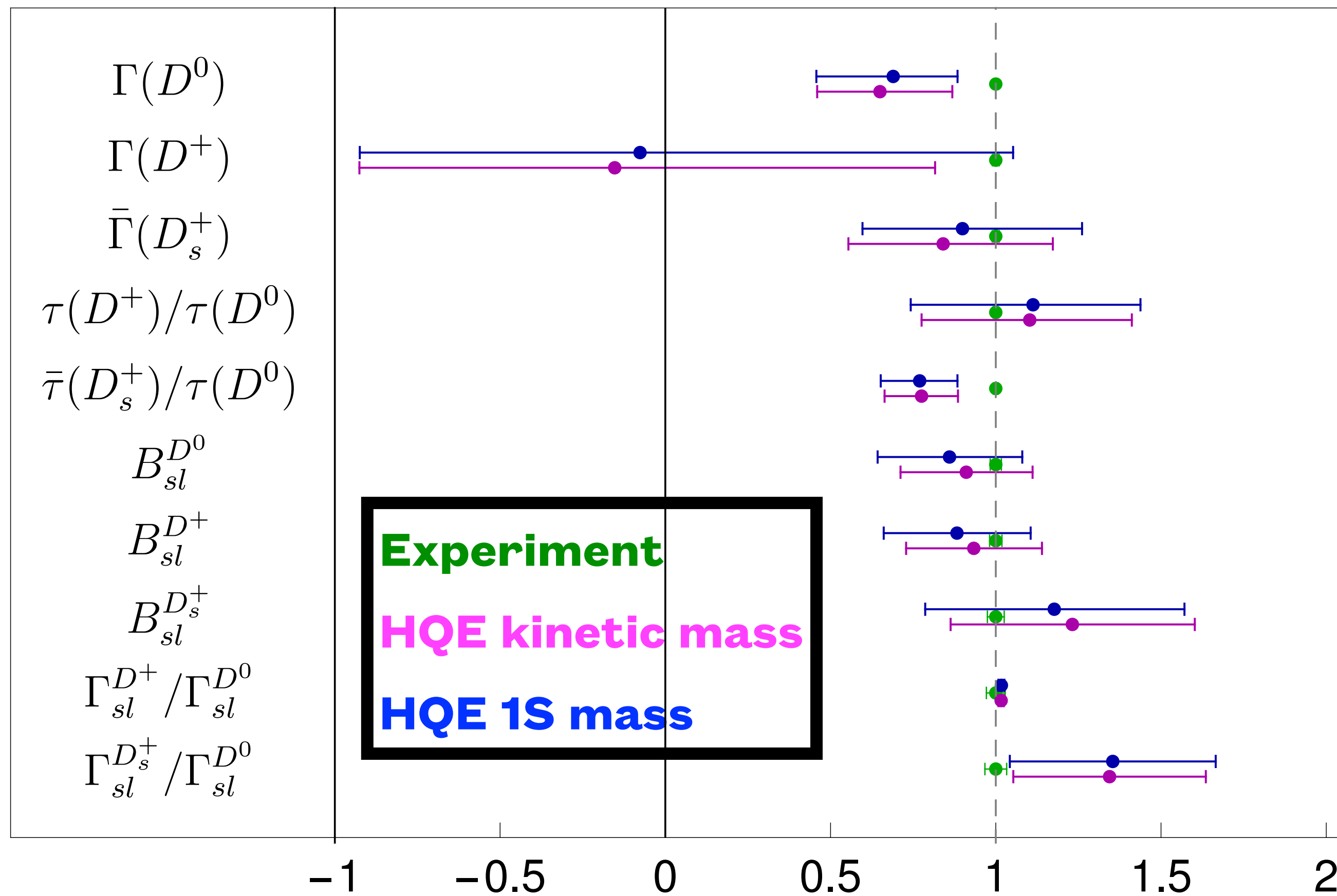
$$\Gamma(D) = \Gamma_3 + \Gamma_5 \frac{\langle \mathcal{O}_5 \rangle}{m_c^2} + \Gamma_6 \frac{\langle \mathcal{O}_6 \rangle}{m_c^3} + \dots + 16\pi^2 \left(\tilde{\Gamma}_6 \frac{\langle \tilde{\mathcal{O}}_6 \rangle}{m_c^3} + \tilde{\Gamma}_7 \frac{\langle \tilde{\mathcal{O}}_7 \rangle}{m_c^4} + \dots \right)$$



See also: charmed baryons **Gratrex, Melic, Nisandzic 2204.11935**

Surprise and/or underdogs...

Convergence of HQE in the charm system?



- **Huge uncertainties**
- **HQE covers experiment**
- **$< 1\sigma$ deviation for SU(3)F breaking in sl**

Surprise and/or underdogs...

How to improve the precision of the HQE in the charm system?

$$\begin{aligned}
 \frac{\Gamma_{sl}^{D_s^+}}{\Gamma_{sl}^{D^0}} &= 1 - 0.40 [\mu_\pi^2(D_s) - \mu_\pi^2(D)] - 1.21 [\mu_G^2(D_s) - \mu_G^2(D)] + 3.13 [\rho_D^3(D_s) - \rho_D^3(D)] \\
 &\quad - 8.84 \tilde{B}_1^s + 8.84 \tilde{B}_2^s - 3.02 \tilde{\epsilon}_1^s + 2.79 \tilde{\epsilon}_2^s \underbrace{+ 0.00}_{\text{dim-7, VIA}} \\
 &\quad + 0.35 \tilde{\delta}_1^{qq} - 0.35 \tilde{\delta}_2^{qq} + 6.60 \tilde{\delta}_1^{qs} - 6.60 \tilde{\delta}_2^{qs} - 0.52 \tilde{\delta}_1^{sq} + 0.52 \tilde{\delta}_2^{sq} + 9.68 \tilde{\delta}_1^{ss} - 9.68 \tilde{\delta}_2^{ss} \\
 &= 1 - 0.04 \frac{\mu_\pi^2(D_s) - \mu_\pi^2(D)}{0.1 \text{ GeV}^2} - 0.02 \frac{\mu_G^2(D_s) - \mu_G^2(D)}{0.02 \text{ GeV}^2} + 0.11 \frac{\rho_D^3(D_s) - \rho_D^3(D)}{0.035 \text{ GeV}^2} \\
 &\quad \underbrace{+ 0.00}_{\text{dim-6,7, VIA}} - 0.09 \delta \tilde{B}_1^s + 0.09 \delta \tilde{B}_2^s + 0.06 \frac{\tilde{\epsilon}_1^s}{-0.02} - 0.06 \frac{\tilde{\epsilon}_2^s}{-0.02} \\
 &\quad + 0.0009 r_1^{qq} + 0.0006 r_2^{qq} + 0.0112 r_1^{qs} + 0.0079 r_2^{qs} \\
 &\quad - 0.0013 r_1^{sq} - 0.0009 r_2^{sq} + 0.0223 r_1^{ss} + 0.0165 r_2^{ss}
 \end{aligned}$$

Could probably be extracted from momentum analysis of inclusive semileptonic D meson decays by BESIII, Belle II,...

Bag parameter determined with 3-loop HQET sum rules: 1711.02100
New: ms corrections King, AL, Rauh, to appear

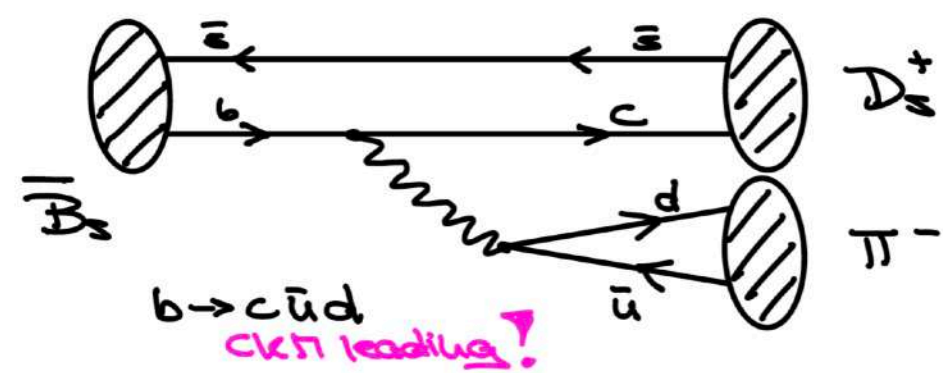
New: first ever determination of eye-contractions King, AL, Rauh, to appear

Non-leptonic decays

3 σ to 9 σ deviation of experiment from QCDf predictions with standard error estimates

N. Skidmore

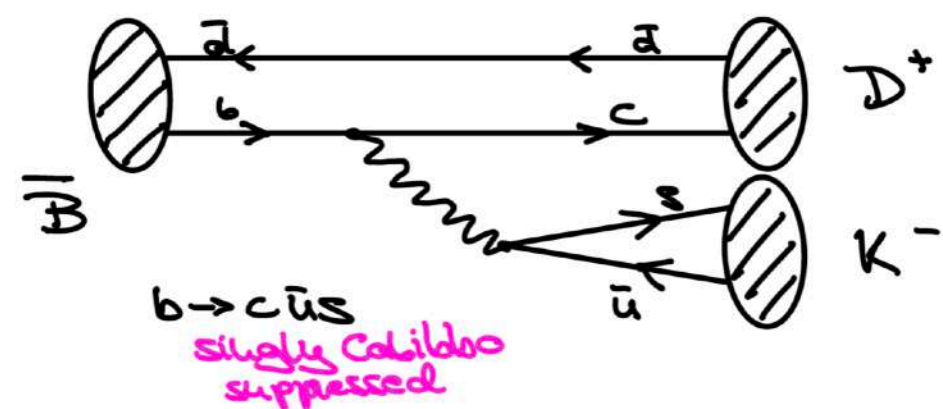
Colour-allowed Tree-level Decays



- CKM leading decays
- There are no annihilation, penguins, ...
- QCDf should work at its best!

Beneke, Buchalla, Neubert, Sachrajda 1999...

$$\langle D_q^{(*)+} L^- | Q_i | \bar{B}_q^0 \rangle = \sum_j F_j^{\bar{B}_q^0 \rightarrow D_q^{(*)+}}(M_L^2) \times \int_0^1 du T_{ij}(u) \phi_L(u) + \mathcal{O}\left(\frac{\Lambda_{\text{QCD}}}{m_b}\right)$$



$$\mathcal{B}(\bar{B}^0 \rightarrow D^+ K^-)$$

(Belle 2111.04978)

$$\mathcal{B}(\bar{B}^0 \rightarrow D^+ K^-)$$

$$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} K^-)$$

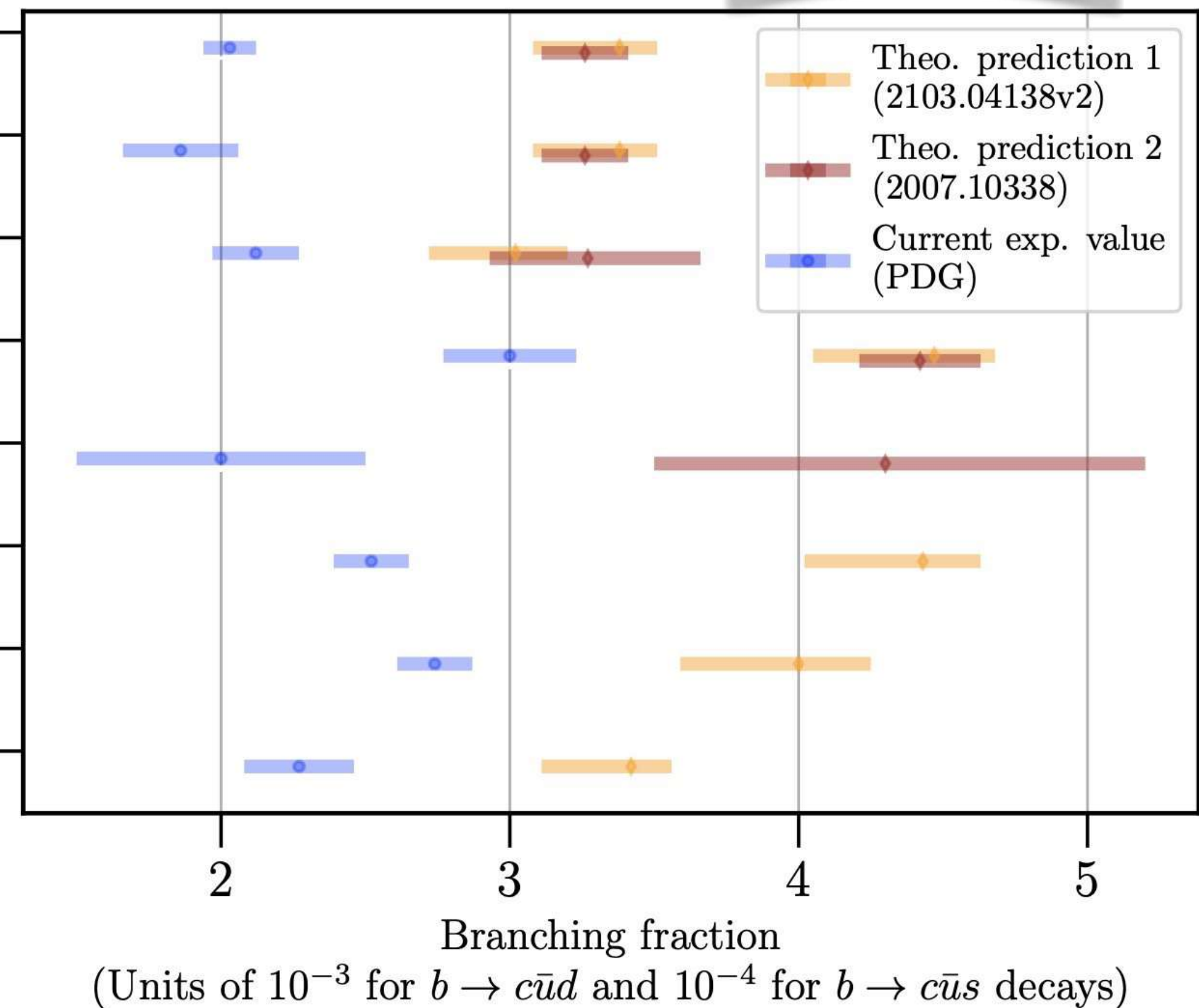
$$\mathcal{B}(\bar{B}_s^0 \rightarrow D_s^+ \pi^-)$$

$$\mathcal{B}(\bar{B}_s^0 \rightarrow D_s^{*+} \pi^-)$$

$$\mathcal{B}(\bar{B}^0 \rightarrow D^+ \pi^-)$$

$$\mathcal{B}(\bar{B}^0 \rightarrow D^{*+} \pi^-)$$

$$\mathcal{B}(\bar{B}_s^0 \rightarrow D_s^+ K^-)$$



Non-leptonic decays

What could go wrong?

Non-leptonic decays

What could go wrong?



Alexander Lenz

@alexlenz42



According to the new Belle measurement in 2111.04978, the decay \bar{B}_d to $D^+ K^-$ is around 7 sigma of the QCD factorisation prediction in 2007.10338. Where is this discrepancy rooted?



33 votes · Final results

9:47 AM · Nov 10, 2021 · Twitter Web App

Non-leptonic decays

What could go wrong?



Alexander Lenz
@alexlenz42



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- Huber, Kränkl 1606.02888
- Bordone, Gubernari, Huber, Jung, vanDyk 2007.10338
- Iguro, Kitahara 2008.01086
- Cai, Deng, Li, Yang 2103.04138
- Bordone, Greljo, Maryocca 2103.10332
- Beneke, Böer, Finauro, Vos 2107.03819

Similar for $B_s \rightarrow D_s^\mp K^\pm$

- Fleischer, Malami 2110.04240, 2109.04950

Non-leptonic decays

What could go wrong?



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Similar for $B_s \rightarrow D_s^\mp K^\pm$

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In the SM the determination of γ is super precise

The ultimate theoretical error on γ from $B \rightarrow DK$ decays

Joachim Brod^{1,*} and Jure Zupan^{1,†}

¹Department of Physics, University of Cincinnati, Cincinnati, Ohio 45221, USA

Abstract

The angle γ of the standard CKM unitarity triangle can be determined from $B \rightarrow DK$ decays with a very small irreducible theoretical error, which is only due to second-order electroweak corrections. We study these contributions and estimate that their impact on the γ determination is to introduce a shift $|\delta\gamma| \lesssim \mathcal{O}(10^{-7})$, well below any present or planned future experiment.

If there are BSM effects in non-leptonic decays, the determination of γ can be modified by $\mathcal{O}(5^\circ)$

PHYSICAL REVIEW D **92**, 033002 (2015)

New physics effects in tree-level decays and the precision in the determination of the quark mixing angle γ

Joachim Brod

PRISMA Cluster of Excellence and Mainz Institute for Theoretical Physics,
Johannes Gutenberg University, 55099 Mainz, Germany

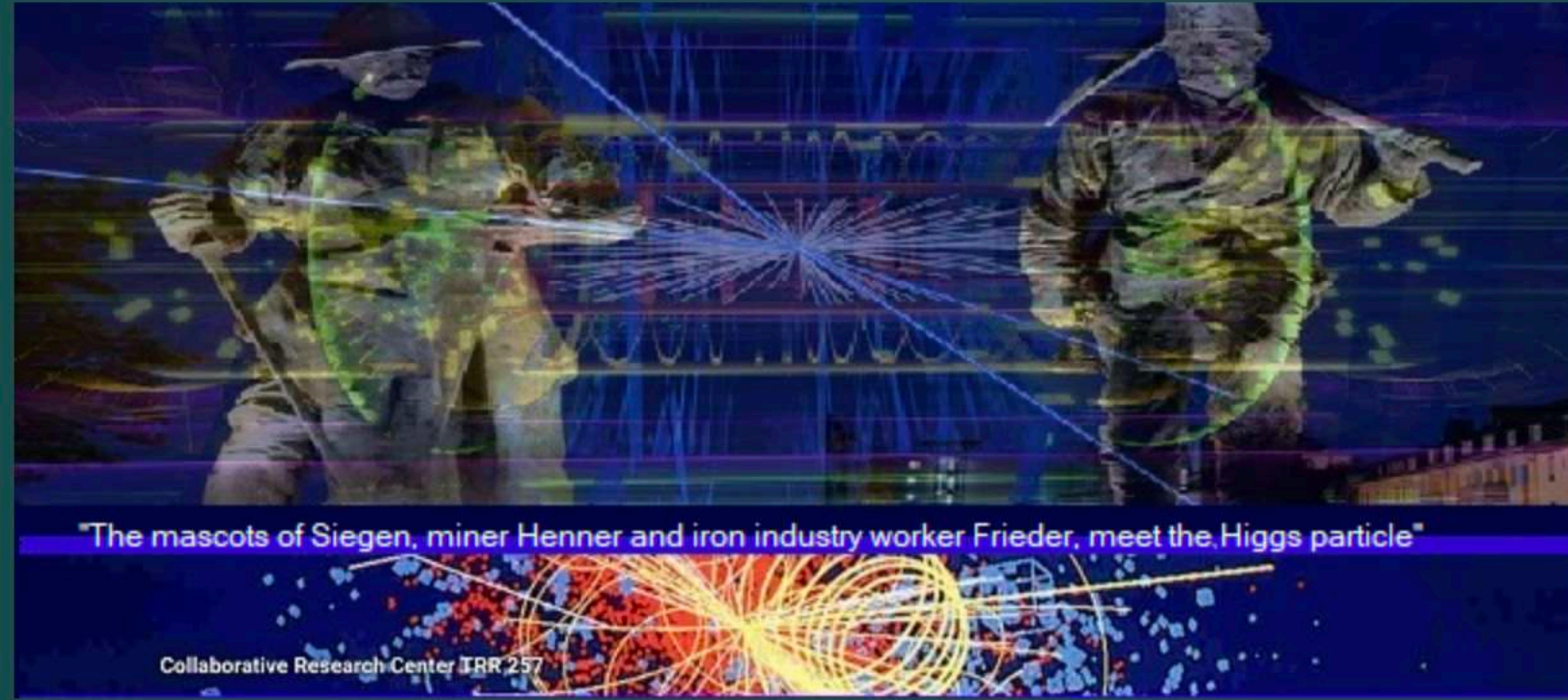
Alexander Lenz, Gilberto Tetlalmatzi-Xolocotzi, and Martin Wiebusch
Institute for Particle Physics Phenomenology, Department of Physics, Durham University,
South Road, Durham DH1 3LE, United Kingdom

update
AL, Tetlalmatzi-Xolocotzi
1912.07621

Non-leptonic decays

Things to check

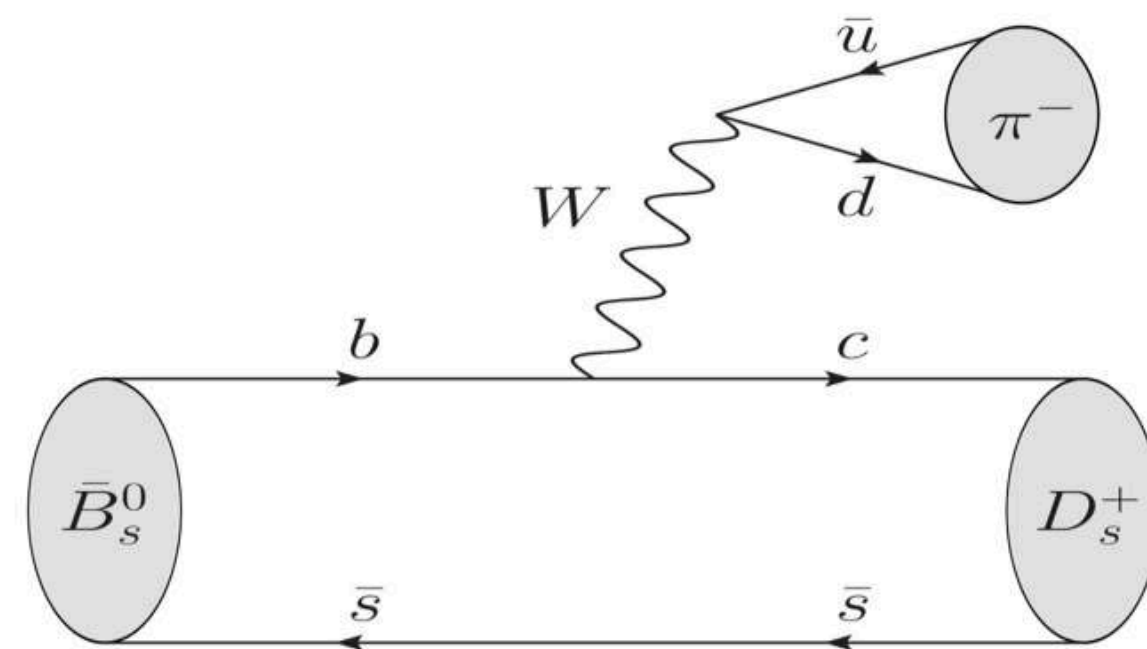
- Reconsidering QCDf uncertainty estimates: **Khodjamirian, Piscopo, Rusov** if new effects will be found, then this might also affect the estimate of charm loops
- **BSM** in $b \rightarrow c\bar{u}d$ would also affect $\tau(B^+)/\tau(B_d)$ **AL, Müller, Piscopo, Rusov**
- Consider CP asymmetries in colour allowed tree-level decays there is only one amplitude in the SM



Status and prospects of Non-leptonic B meson decays

31 May 2022 to 2 June 2022
Europe/Berlin timezone

The aim of this event is to discuss the current status in theory and experiment of non-leptonic B meson decays. This entails talks on calculation techniques, including QCD factorization and perturbative QCD with special emphasis on the current status of estimating power corrections. Moreover, this workshop will include sessions devoted to the discussion of different puzzles, old and new, arising within the context of purely hadronic B meson processes. Here, discrepancies between the theoretical and the experimental determinations may indicate either potential physics beyond the SM or a critical reassessment of our theory tools. Finally, future experimental prospects on the expected precision and the measurement of different non-leptonic channels will also be addressed.



The University of Siegen has around 18.000 students and it has a large theoretical flavour physics group with around 40 members. Downtown Siegen offers many pubs, restaurants and cafes, but also theaters, cinemas and concert halls.



<https://indico.scc.kit.edu/event/2641/>

Flavour specific decays

- a_{fs}^q is typically measured with semi-leptonic B_q decays

$$a_{sl}^{s,Exp} = (60 \pm 280) \cdot 10^{-5},$$
$$a_{sl}^{d,Exp} = (-21 \pm 17) \cdot 10^{-4}.$$

HFLAV 1970?

Flavour specific decays

- a_{fs}^q is typically measured with semi-leptonic B_q decays
- One could also use the flavour specific $\bar{B}_s \rightarrow D_s^+ \pi^-$ decay

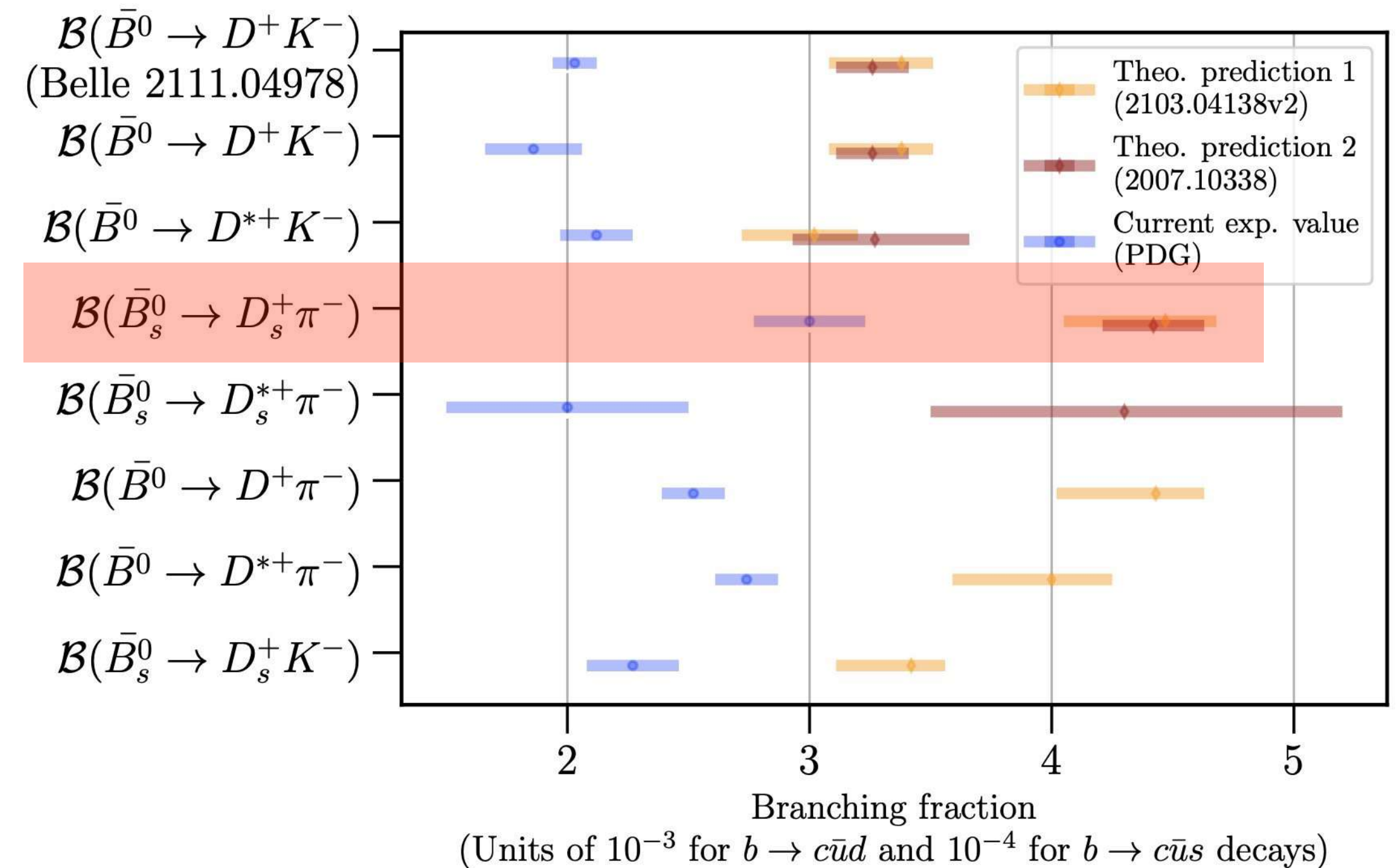
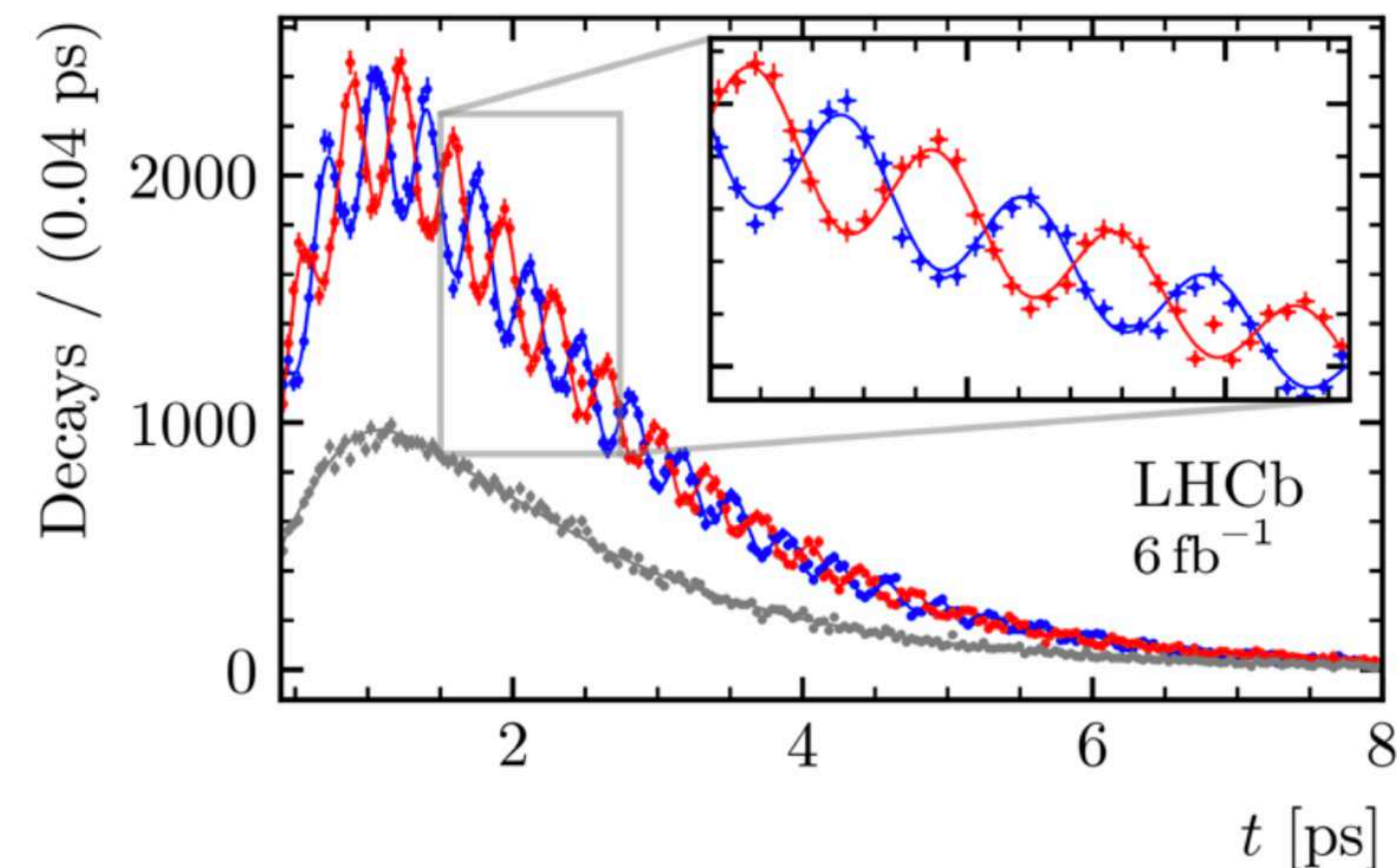
12 April 2021: Fascinating quantum mechanics.

Precise determination of the $B_s^0 - \bar{B}_s^0$ oscillation frequency.

"A phenomenon in which quantum mechanics gives a most remarkable prediction" - Richard Feynman

Today, the LHCb Collaboration submitted a paper for publication that reports a precise determination of the $B_s^0 - \bar{B}_s^0$ oscillation frequency. This result is presented also today at the joint [annual conference](#) of the UK Institute of Physics (IOP), organized by the University of Edinburgh. The $B_s^0 - \bar{B}_s^0$ oscillation is a spectacular and fascinating feature of quantum mechanics. The strange beauty particle B_s^0 composed of a [beauty](#) antiquark (\bar{b}) bound with a [strange](#) quark s turns into its antiparticle partner \bar{B}_s^0 composed of a b quark and an s antiquark (\bar{s}) about 3 million million times per second (3×10^{12}) as seen in the image below.

— $B_s^0 \rightarrow D_s^- \pi^+$ — $\bar{B}_s^0 \rightarrow D_s^- \pi^+$ — Untagged



Flavour specific decays

- a_{fs}^q is typically measured with semi-leptonic B_q decays
- One could also use the flavour specific $\bar{B}_s \rightarrow D_s^+ \pi^-$ decay
- Assume: there is **new physics** in these decays, potentially CP violating

$$\begin{aligned} \mathcal{A}_f &= |\mathcal{A}_f^{\text{SM}}| e^{i\phi^{\text{SM}}} e^{i\varphi^{\text{SM}}} + |\mathcal{A}_f^{\text{BSM}}| e^{i\phi^{\text{BSM}}} e^{i\varphi^{\text{BSM}}} \\ &=: |\mathcal{A}_f^{\text{SM}}| e^{i\phi^{\text{SM}}} e^{i\varphi^{\text{SM}}} (1 + r e^{i\phi} e^{i\varphi}), \end{aligned}$$

Discrepancy QCDf vs Exp. suggests $r \approx 0.1 - 0.2$

Flavour specific decays

- a_{fs}^q is typically measured with semi-leptonic B_q decays
- One could also use the flavour specific $\bar{B}_s \rightarrow D_s^+ \pi^-$ decay
- Assume: there is new physics in these decays, potentially CP violating
- Derive CP asymmetry

$$A_{fs}^q = \frac{a_{fs}^q - 2r \sin \phi \sin \varphi + 2a_{fs}^q r \cos \phi \cos \varphi + a_{fs}^q r^2}{1 + 2r \cos \phi \cos \varphi + r^2 - 2a_{fs}^q r \sin \phi \sin \varphi} \approx a_{fs}^q - A_{dir}^q$$

$$\approx 2r \sin \phi \sin \varphi < 0.40$$

Constrained by
semi-leptonic
Measurements

$$a_{sl}^{s,Exp} = (60 \pm 280) \cdot 10^{-5},$$

$$a_{sl}^{d,Exp} = (-21 \pm 17) \cdot 10^{-4}.$$

HFLAV 1970?

Flavour specific decays

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Gershon, AL, Rusov, Skidmore
2111.04478

$$A_{fs}^q = \frac{a_{fs}^q - 2r \sin \phi \sin \varphi + 2a_{fs}^q r \cos \phi \cos \varphi + a_{fs}^q r^2}{1 + 2r \cos \phi \cos \varphi + r^2 - 2a_{fs}^q r \sin \phi \sin \varphi} \approx a_{fs}^q - A_{dir}^q$$

$$\approx 2r \sin \phi \sin \varphi < 0.40$$

**Significant exp. deviation of A_{fs}^q from a_{sl}^q
= unambiguous and theory independent
signal for BSM**

Constrained by
semi-leptonic
Measurements

$$a_{sl}^{s,Exp} = (60 \pm 280) \cdot 10^{-5},$$

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HFLAV 1970?



Conclusion

Many, many interesting topics ahead of us
also besides the very important and interesting B anomalies

Additional Material

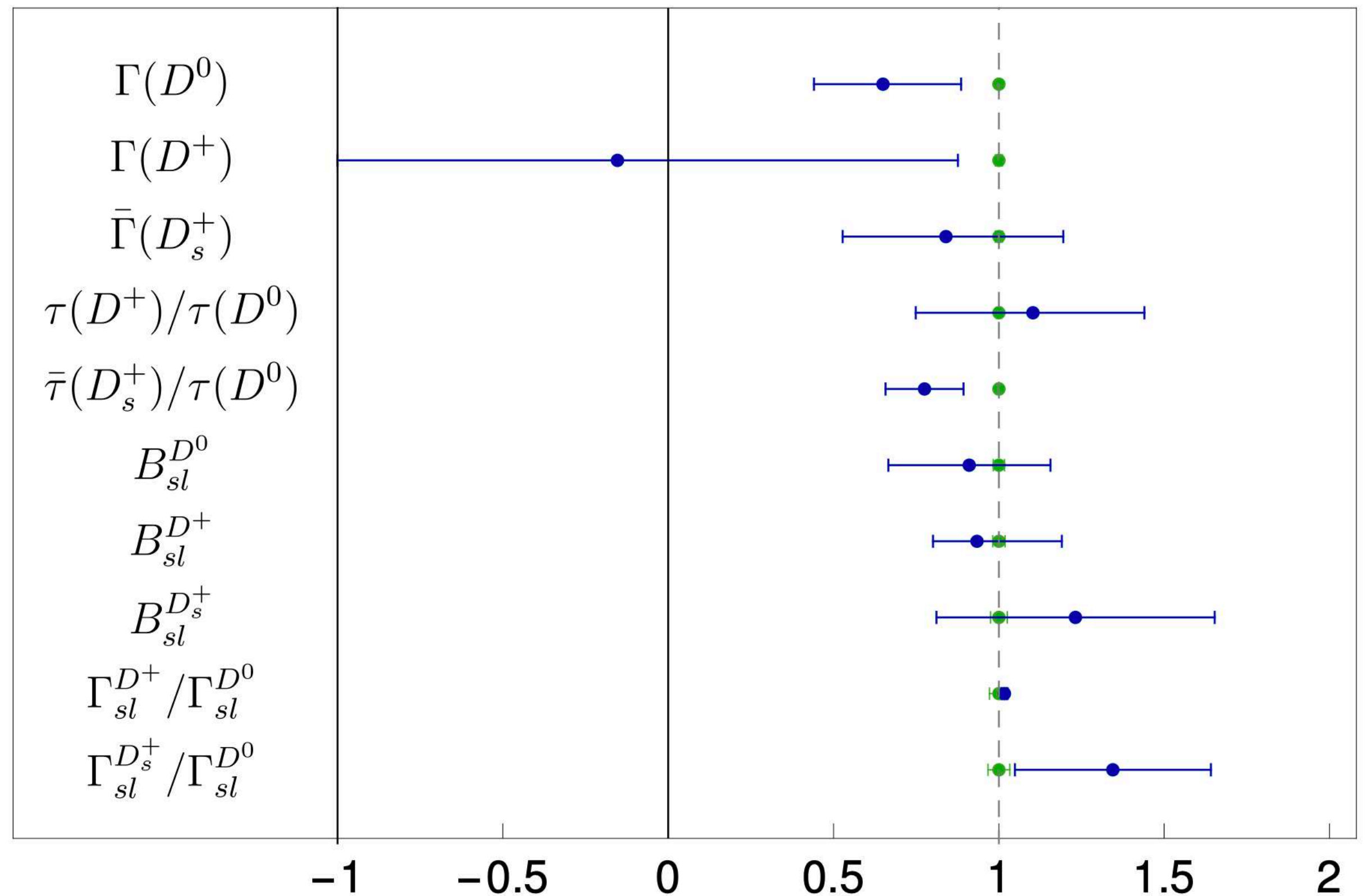
Status Quo: Charm Mixing

The charm system is theoretically more difficult than the b system since

- $\alpha_s(m_c) \approx 0.34$

- $\frac{\Lambda_{QCD}}{m_c} \approx 3 \frac{\Lambda_{QCD}}{m_b}$

Nevertheless the Heavy Quark Expansion might still converge in the charm system



Mixing and CP violation in the charm system

Alexander Lenz (Siegen U.), Guy Wilkinson (Oxford U.) (Nov 9, 2020)

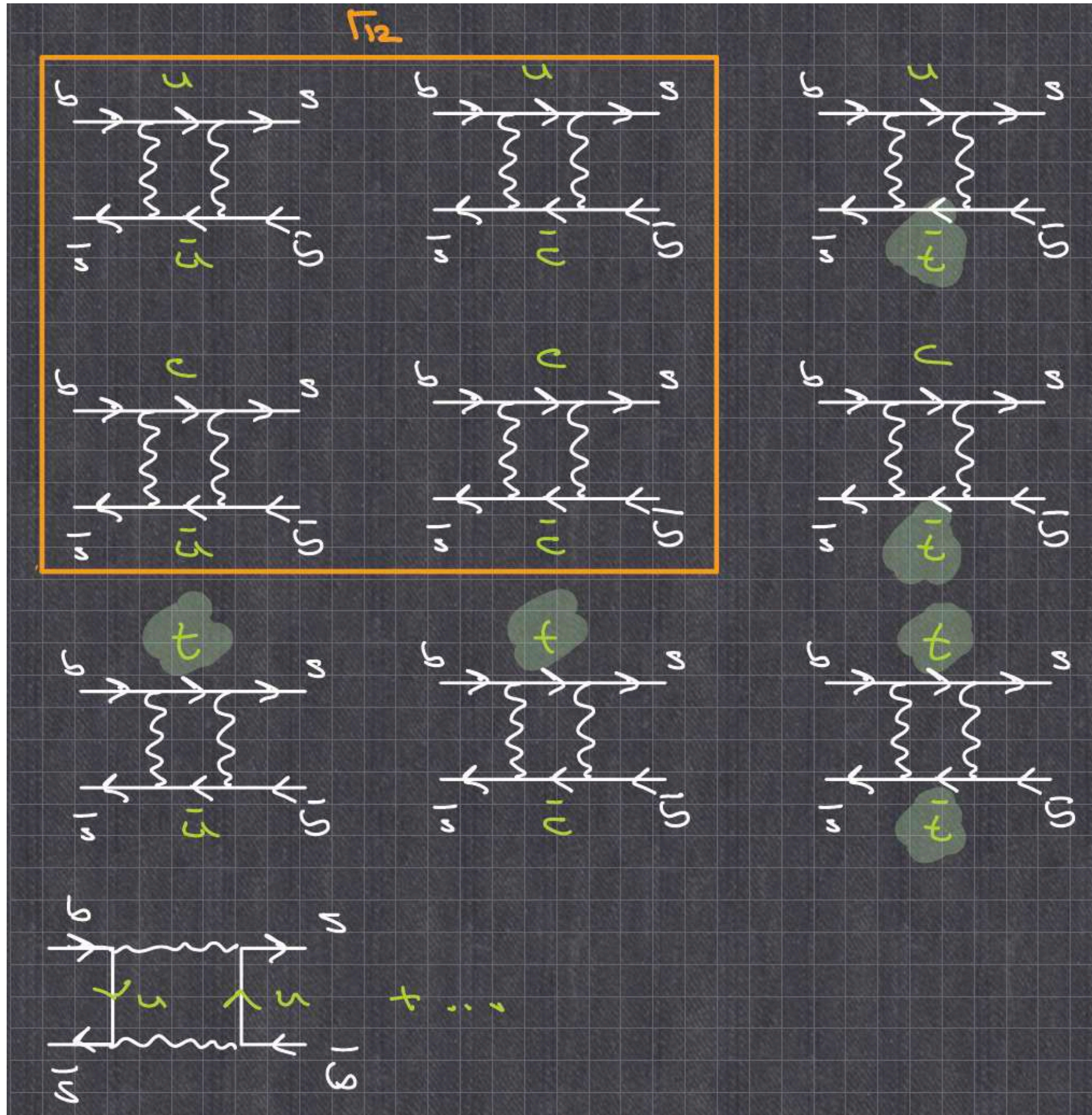
e-Print: 2011.04443 [hep-ph]

King, AL, Piscopo, Rauh, Rusov, Vlahos
2109.13219

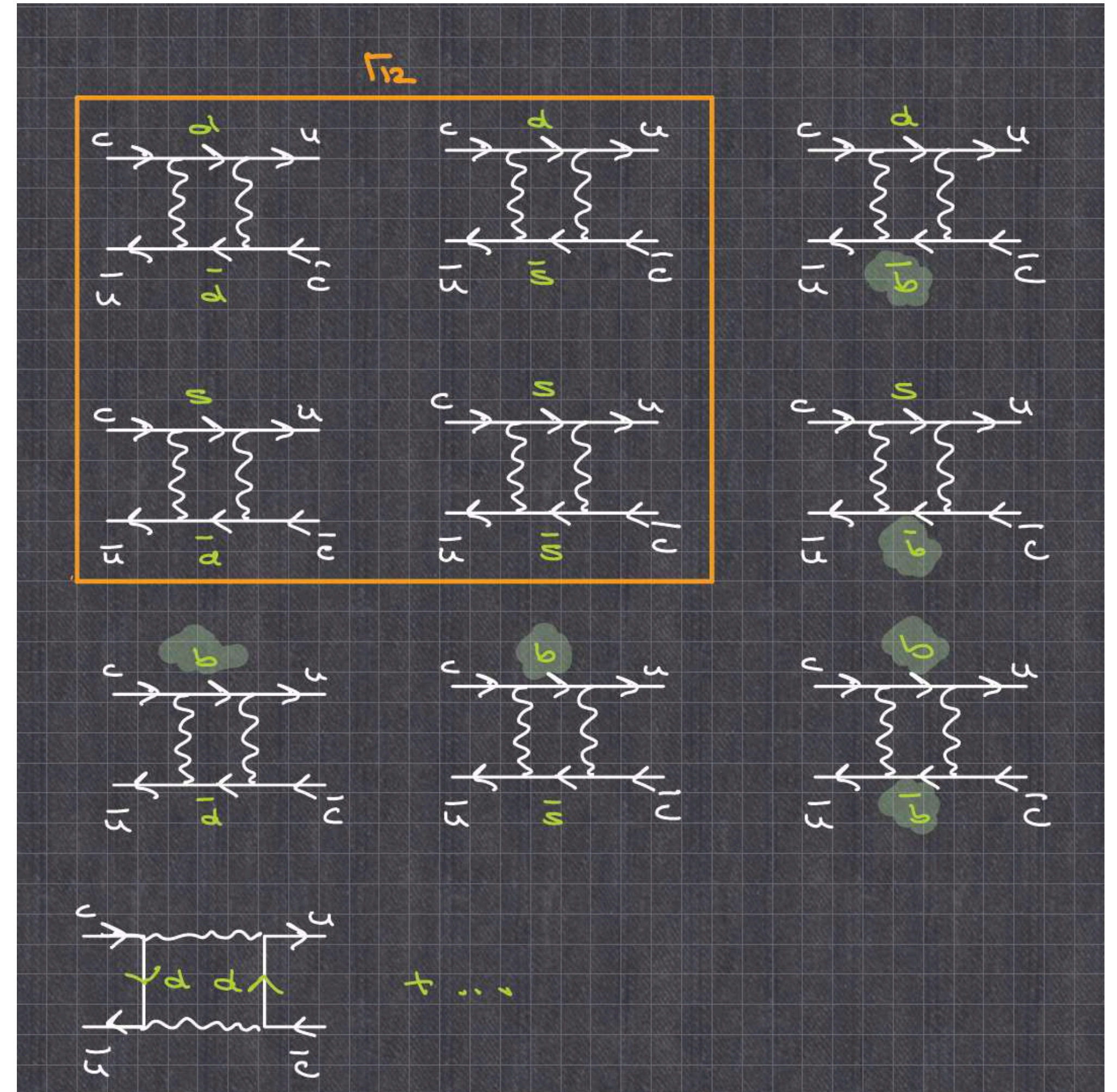
But for mixing it gets much worse

Status Quo: Charm Mixing

B-mixing



D-mixing



Status Quo: Charm Mixing

B-mixing



$$\begin{aligned}
 M_{12} = & \lambda_u^2 F(u,u) + \lambda_u \lambda_c F(u,c) + \lambda_u \lambda_t F(u,t) \\
 & + \lambda_c \lambda_u F(c,u) + \lambda_c^2 F(c,c) + \lambda_c \lambda_t F(c,t) \\
 & + \lambda_t \lambda_u F(t,u) + \lambda_t \lambda_c F(t,c) + \lambda_t^2 F(t,t)
 \end{aligned}$$

$\lambda_u + \lambda_c + \lambda_t = 0$

$$\begin{aligned}
 = & \lambda_u^2 [F(c,c) - 2F(u,c) + F(u,u)] \\
 & + 2\lambda_u \lambda_t [F(c,c) - F(u,c) + F(u,t) - F(c,t)] \\
 & + \lambda_t^2 [F(c,c) - 2F(c,t) + F(t,t)]
 \end{aligned}$$

	B_d	B_s	
λ_u	$\lambda^{3.8}$	$\lambda^{4.8}$	$m_u^2/m_\tau^2 \approx 0$
λ_c	λ^3	λ^2	$m_c^2/m_\tau^2 \approx 2.5 \cdot 10^{-4}$
λ_t	λ^3	λ^2	$m_t^2/m_\tau^2 \approx 4.5$

CKM dominant \equiv GIM dominant

CKM suppressed \equiv GIM suppressed

D-mixing



$$\begin{aligned}
 M_{12} = & \lambda_d^2 F(d,d) + \lambda_d \lambda_s F(d,s) + \lambda_d \lambda_b F(d,b) \\
 & + \lambda_s \lambda_d F(s,d) + \lambda_s^2 F(s,s) + \lambda_s \lambda_b F(s,b) \\
 & + \lambda_b \lambda_d F(b,d) + \lambda_b \lambda_s F(b,s) + \lambda_b^2 F(b,b)
 \end{aligned}$$

$\lambda_d + \lambda_s + \lambda_b = 0$

$$\begin{aligned}
 = & \lambda_d^2 [F(d,d) - 2F(d,s) + F(s,s)] \\
 & + 2\lambda_s \lambda_b [F(s,s) - F(d,s) + F(d,b) - F(s,b)] \\
 & + \lambda_b^2 [F(s,s) - 2F(s,b) + F(b,b)]
 \end{aligned}$$

	D	
λ_d	λ'	$m_d^2/m_\tau^2 \approx 0$
λ_s	λ'	$m_s^2/m_\tau^2 \approx 1.3 \cdot 10^{-6}$
λ_b	$\lambda^{5.8}$	$m_b^2/m_\tau^2 \approx 2.8 \cdot 10^{-3}$

CKM suppressed \equiv GIM dominant

CKM dominant \equiv GIM suppressed

Status Quo: Charm Mixing

The HQE is successful in the B system and for D meson lifetimes
=> apply it for D-mixing

$$y_D^{\text{HQE}} \approx \lambda_s^2 (\Gamma_{12}^{ss} - 2\Gamma_{12}^{sd} + \Gamma_{12}^{dd}) \approx 10^{-5} y_D^{\text{Exp.}}$$

How can this be?

Look only at a single diagram:

$$y_D^{\text{HQE}} \neq \lambda_s^2 \Gamma_{12}^{ss} \tau_D = 3.7 \cdot 10^{-2} \approx 5.6 y_D^{\text{Exp.}}$$

pert. calculation: **Bobrowski et al 1002.4794**

lattice input: **ETM 1403.7302; 1505.06639; FNAL/MILC 1706.04622**

HQET sum rules: **Kirk, AL, Rauh 1711.02100**

The problem seems to originate in the extreme GIM cancellations

Status Quo: Charm Mixing

1. Duality violations - break down of HQE

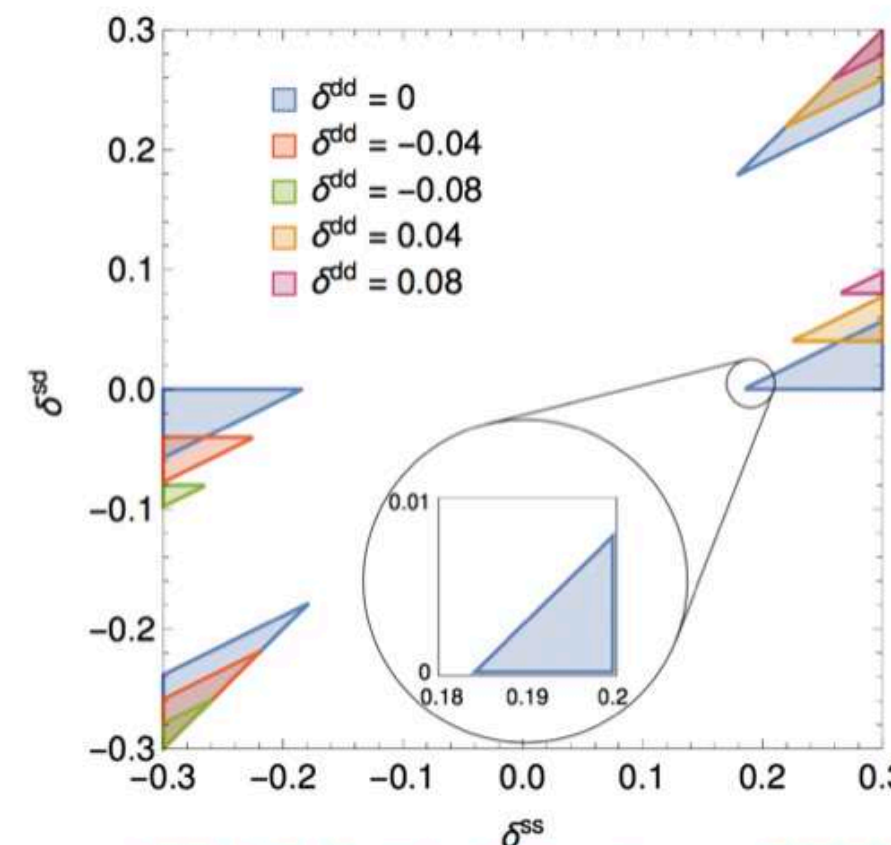
$$\Gamma_{12}^{ss} \rightarrow \Gamma_{12}^{ss}(1 + \delta^{ss}),$$

$$\Gamma_{12}^{sd} \rightarrow \Gamma_{12}^{sd}(1 + \delta^{sd}),$$

$$\Gamma_{12}^{dd} \rightarrow \Gamma_{12}^{dd}(1 + \delta^{dd}),$$

20% of duality violation is sufficient to explain experiment

Jubb, Kirk, AL, Tetlalmatzi-Xolocotzi 2016



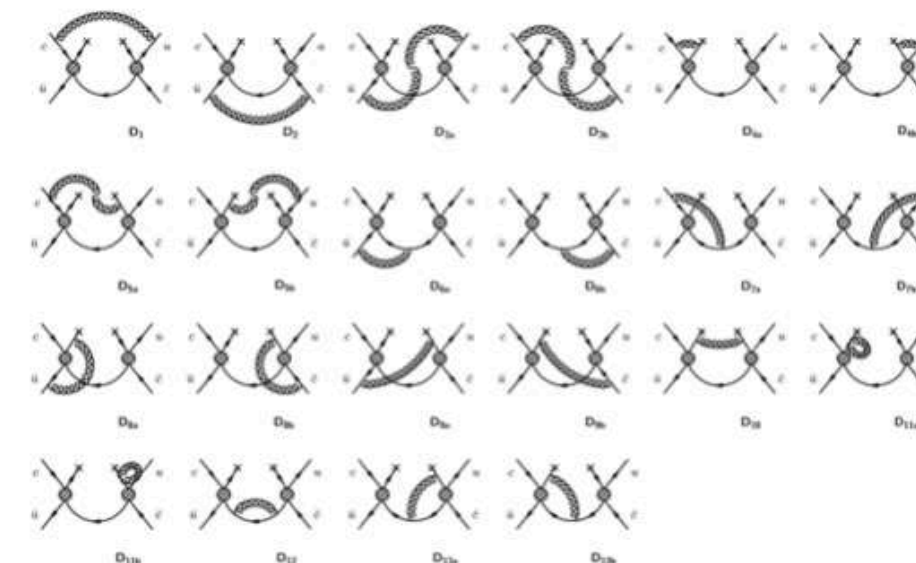
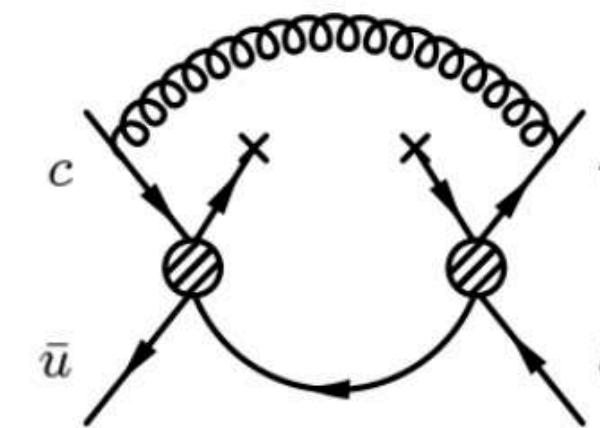
2. Higher dimensions

Georgi 9209291; Ohi, Ricciardi, Simmons 9301212; Bigi, Uraltsev 0005089

Idea: GIM cancellation is lifted by higher orders in the HQE - overcompensating the 1/mc suppression.

Partial calculation of D=9 yields an enhancement - but not to the experimental value

Bobrowski, AL, Rauh 2012



3. Renormalisation scale setting:

AL, Piscopo, Vlahos 2020

$$\mu_x^{ss} = \mu_x^{sd} = \mu_x^{dd}$$

Implicitly assumes a precision of 10^-5!

4. New Physics is present and we cannot prove it yet:-)

- 1) Vary $\mu^{ss,dd}$ and μ^{ds} independently between 1 GeV and $2 m_c$
 \Rightarrow uncertainty increases and exp. value is covered
- 2) Choose scales somehow phase space inspired as

$$\begin{aligned} \mu^{ss} &= m_c - 2\epsilon \\ \mu^{sd} &= m_c - \epsilon \\ \mu^{dd} &= m_c \end{aligned}$$

\Rightarrow exp. value is covered

Exclusive and inclusive approaches can cover the experimental regions



No precision determination possible