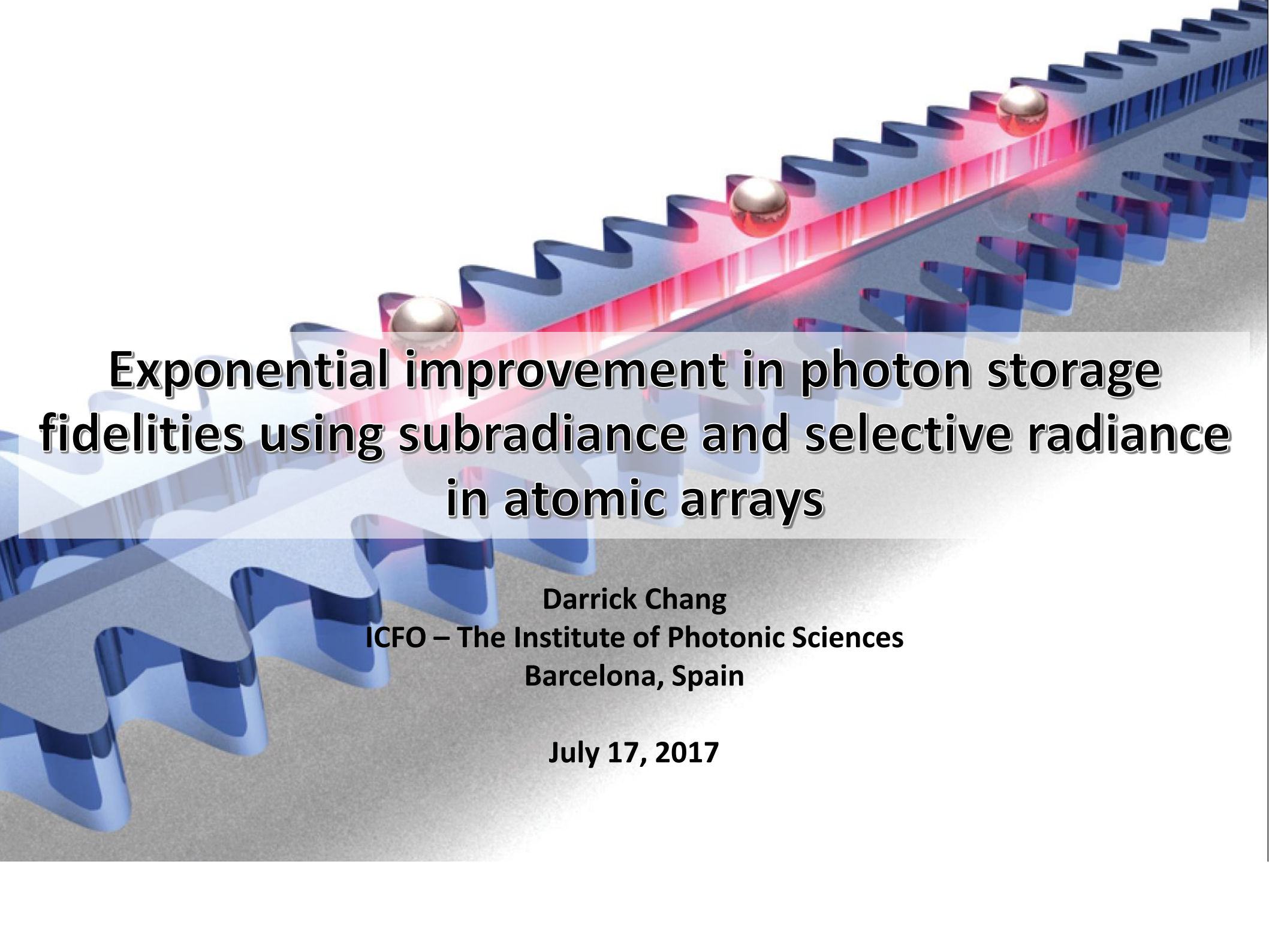




Exponential improvement in photon storage fidelities using subradiance and selective radiance in atomic arrays

Darrick Chang
ICFO – The Institute of Photonic Sciences
Barcelona, Spain

July 17, 2017

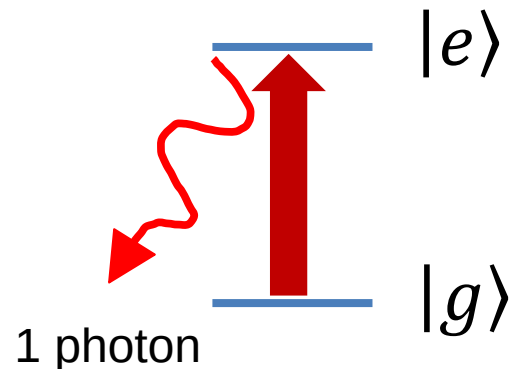
Acknowledgments



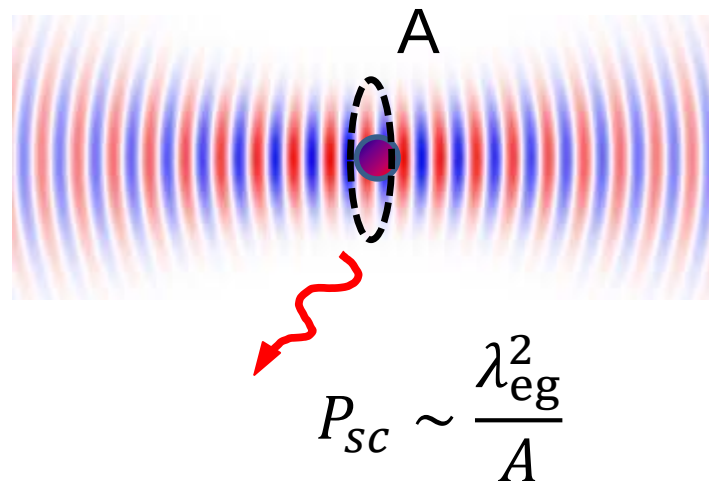
- In collaboration with Prof. Jeff Kimble (Caltech)

Atom-photon interactions

- Atoms constitute a natural quantum interface with light



- Route toward quantum information processing, or strong interactions between photons
- Problem: single atoms and photons don't like to talk to each other



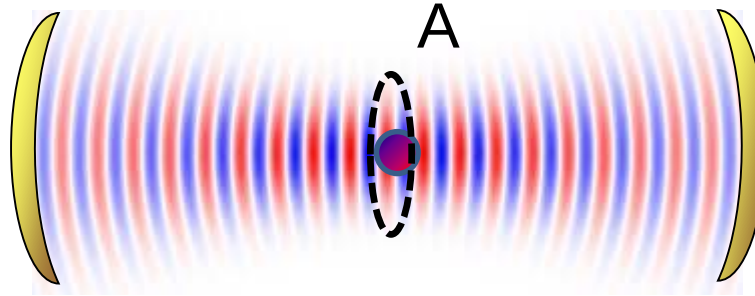
diffraction limit

$$A > \lambda_{eg}^2$$

Atom-photon interactions

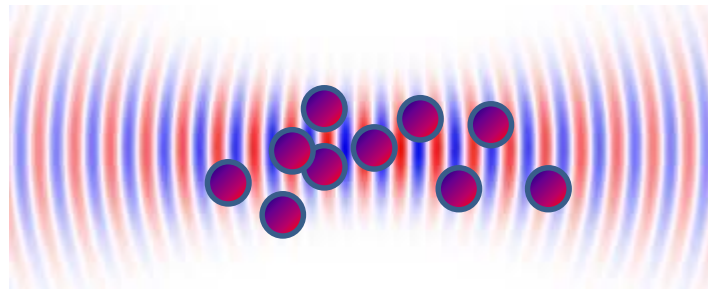
- Some fixes:

- Cavity QED



$$P_{sc} \sim \frac{\lambda_{eg}^2}{A} N_{\text{bounces}} \sim \frac{g^2}{\kappa\Gamma} \sim \text{Cooperativity}$$

- Atomic ensembles



$$P_{sc} \sim \frac{\lambda_{eg}^2}{A} N_{\text{atoms}} \sim \text{Optical depth}$$

A fundamental limit

- Cooperativity or optical depth viewed as a fundamental limit to applications of atom-light interfaces

A quantum gate between a flying optical photon and a single trapped atom

Andreas Reiserer¹, Norbert Kalb¹, Gerhard Rempe¹ & Stephan Ritter¹

In principle, the gate mechanism presented in this work is deterministic. In our experimental implementation, the photon is not back-reflected⁸ from the coupled system $|\uparrow^a \uparrow^p\rangle$ with a probability of 34(2)% (due to the finite cooperativity $C = \frac{g^2}{2\kappa\gamma} = 3$) and in the uncoupled

All-Optical Switch and Transistor Gated by One Stored Photon

Wenlan Chen,¹ Kristin M. Beck,¹ Robert Bücker,^{1,2} Michael Gullans,³ Mikhail D. Lukin,³ Haruka Tanji-Suzuki,^{1,3,4} Vladan Vuletić^{1*}

stood in a simple cavity QED model: One atom in state $|s\rangle$ reduces the cavity transmission (1, 4) by a factor of $T = (1 + \eta)^{-2}$, where η is the single-atom cooperativity (30). In the strong-coupling

Universal Approach to Optimal Photon Storage in Atomic Media

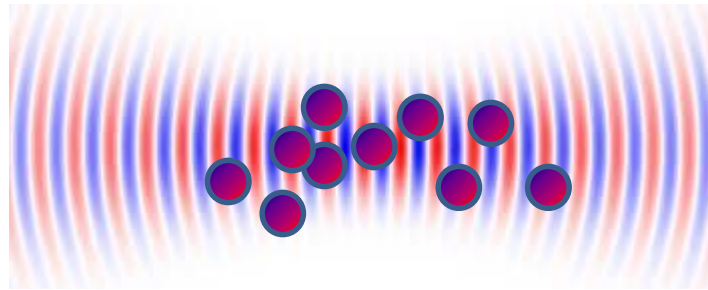
Alexey V. Gorshkov,¹ Axel André,¹ Michael Fleischhauer,² Anders S. Sørensen,³ and Mikhail D. Lukin¹

off-resonant Raman fields to photon-echo-based techniques. Furthermore, we derive an optimal control strategy for storage and retrieval of a photon wave packet of any given shape. All these approaches, when optimized, yield identical maximum efficiencies, which only depend on the optical depth of the medium.

- Errors decrease as $\frac{1}{C}$, $\frac{1}{OD}$ or slower

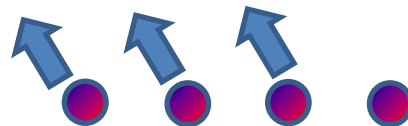
Is that the full story?

- Atomic ensembles



$$P_{sc} \sim \frac{\lambda_{eg}^2}{A} N_{atoms} \sim \text{Optical depth}$$

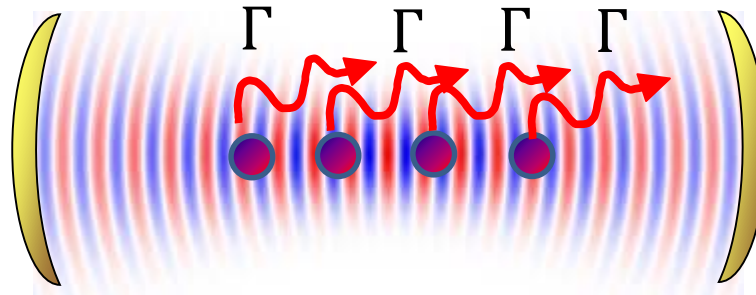
- **Important assumption:** atoms interact with light independently
 - Effectiveness is multiplied by # of attempts ($\propto N_{atoms}$)
- Cannot be true – atoms emit waves, which can interfere



Physics of super- and
sub-radiance

Is that the full story?

- Starting equations for quantum optics already have an issue!
 - Jaynes-Cummings model for multiple emitters



$$H_{\text{eff}} = \sum_j g(x_j)(\sigma_{eg}^j a + h.c.) - \frac{i\kappa}{2} a^\dagger a - i \underbrace{\frac{\Gamma}{2} \sum_j \sigma_{ee}^j}_{\text{Independent emission}}$$

Independent emission

- Maxwell-Bloch equations for atomic ensembles

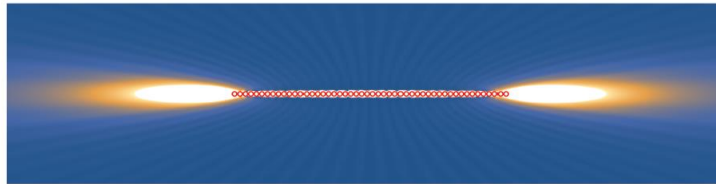
$$((1/c)\partial_t + \partial_z)E(z, t) \sim i \underbrace{P_{ge}(z, t)}_{\text{Continuous medium}}$$

$$dP_{ge}/dt = - \underbrace{(\Gamma/2)P_{ge}}_{\text{Independent emission}} + \dots$$

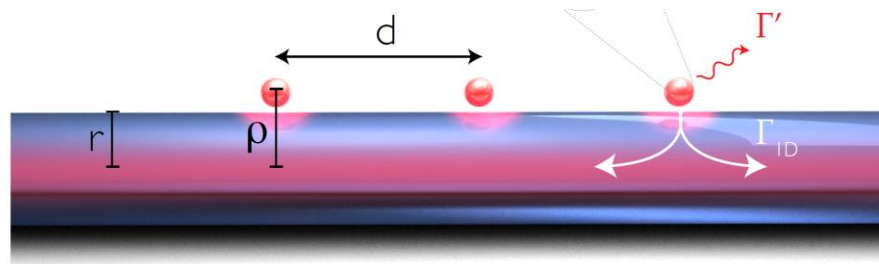
Independent emission

Outline

- **Big question:** can we exploit interference to enhance atom-light interfaces? **(Yes!)**
- Formalism to treat atom-light interfaces including subradiance
- Origin of subradiance in atomic arrays in free space



- “Selective” radiance: atoms coupled to a nanofiber



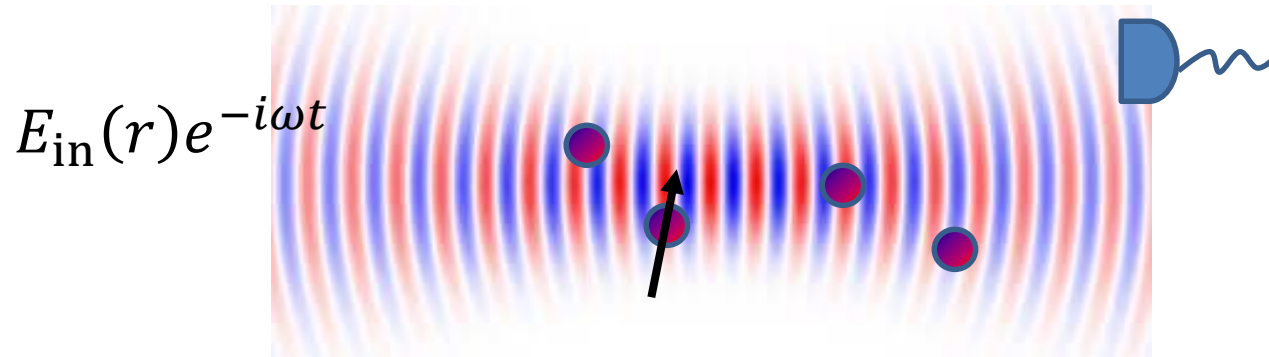
Light-matter interactions as a spin model

Electromagnetic Green's function

- Formal definition:
- G describes the electric field at point r , of a (normalized) oscillating dipole at r'
- Tensor quantity ($\alpha, \beta = x, y, z$): source dipole can have three orientations, and the electric field at r is a vector
- Simple case: free space

Getting rid of the light

- Scattering from polarizable particles



- Know the radiation pattern for a dipole
- Can formally write down the total field
- Generalized “input-output” equation for atoms

$$\hat{E}(r, t) = \hat{E}_{\text{in}}(r, t) + (3\pi\hbar c\Gamma_0/d_0\omega_{eg}) \sum_i G(r, r_i, \omega_{eg}) \sigma_{ge}^i(t)$$

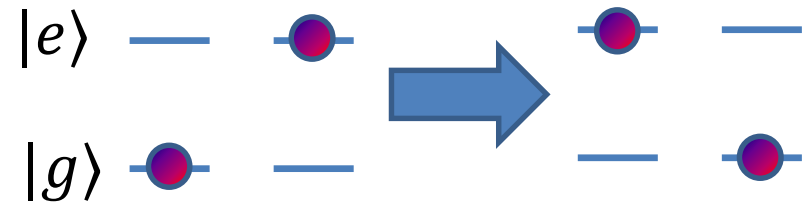
Field encoded in atoms!

- Quantum and classical fields propagate the same way

What about the atoms?

- Atoms interact with fields, but fields are dependent on the atoms themselves
- Effective “spin” Hamiltonian involving atoms alone

$$H_{\text{eff}} = -\left(3\pi\hbar\Gamma_0 c / \omega_{eg}\right) \sum_{i,j} G(r_j, r_i, \omega_{eg}) \sigma_{eg}^i \sigma_{ge}^j$$



What about the atoms?

- Atoms interact with fields, but fields are dependent on the atoms themselves
- Effective “spin” Hamiltonian involving atoms alone

$$H_{\text{eff}} = -\left(3\pi\hbar\Gamma_0 c / \omega_{eg}\right) \sum_{i,j} \underbrace{G(r_j, r_i, \omega_{eg})}_{\text{field propagation}} \sigma_{eg}^i \sigma_{ge}^j$$

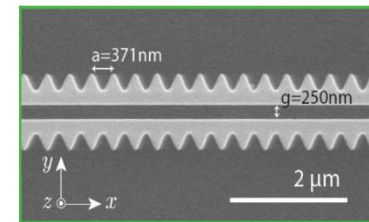
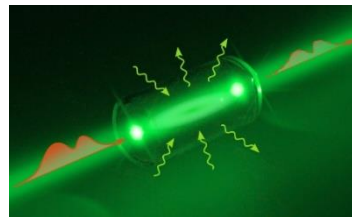
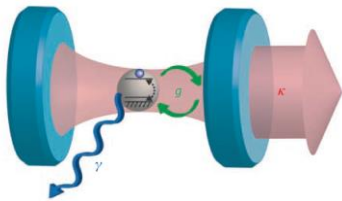
- Strength depends on how field propagates from j to i
- Non-Hermitian Hamiltonian – describes both coherent interactions and (collective) spontaneous emission

Quantum “spin model” of atom-light interactions

$$H_{\text{eff}} = -\left(3\pi\hbar\Gamma_0 c/\omega_{eg}\right) \sum_{i,j} G(r_j, r_i, \omega_{eg}) \sigma_{eg}^i \sigma_{ge}^j$$

$$\hat{E}(r, t) = \hat{E}_{in}(r, t) + \left(3\pi\hbar c\Gamma_0/d_0\omega_{eg}\right) \sum_i G(r, r_i, \omega_{eg}) \sigma_{ge}^i(t)$$

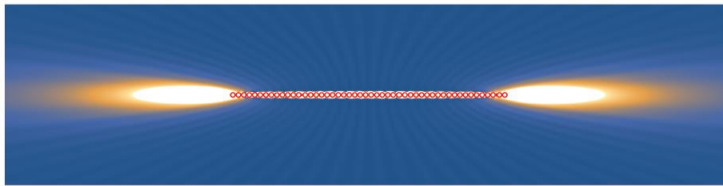
- Long history of these equations: Gross and Haroche (superradiance review, 1982); Kurizki (dipole-dipole interactions, 1990's); Welsch and Buhmann (quantization of dielectrics, 1990's); ...
- Equally captures **any system** of atoms interacting with light, and treats them on equal footing



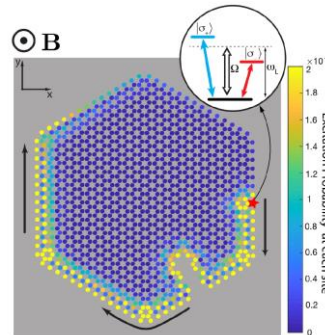
- All of atom-light interactions are formally encoded in a spin model!

Light-atom interactions as a spin model

- Subradiance, edge states in free-space atomic arrays

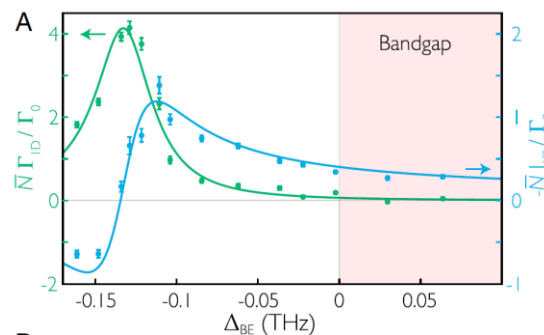
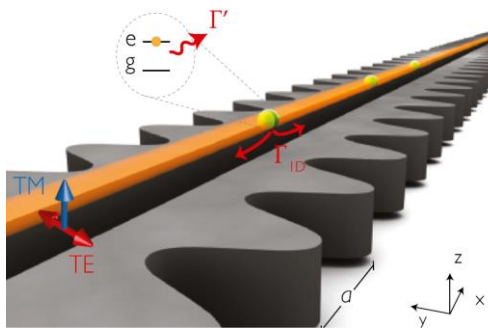


arXiv:1703.03382



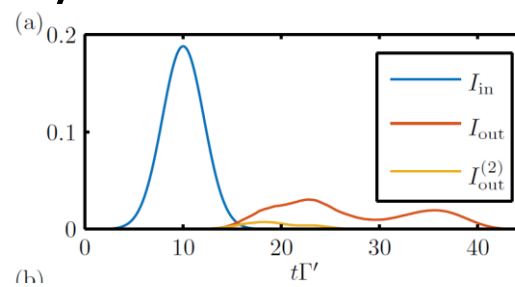
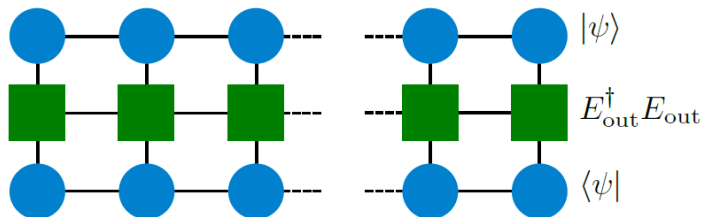
J Perzcel et al, PRL 119, 023603 (2017)

- Quantitative modeling of atoms near complex structures



JD Hood et al, PNAS 113, 10507 (2016)

- New techniques for dynamics of strongly interacting photons (e.g., matrix product states)

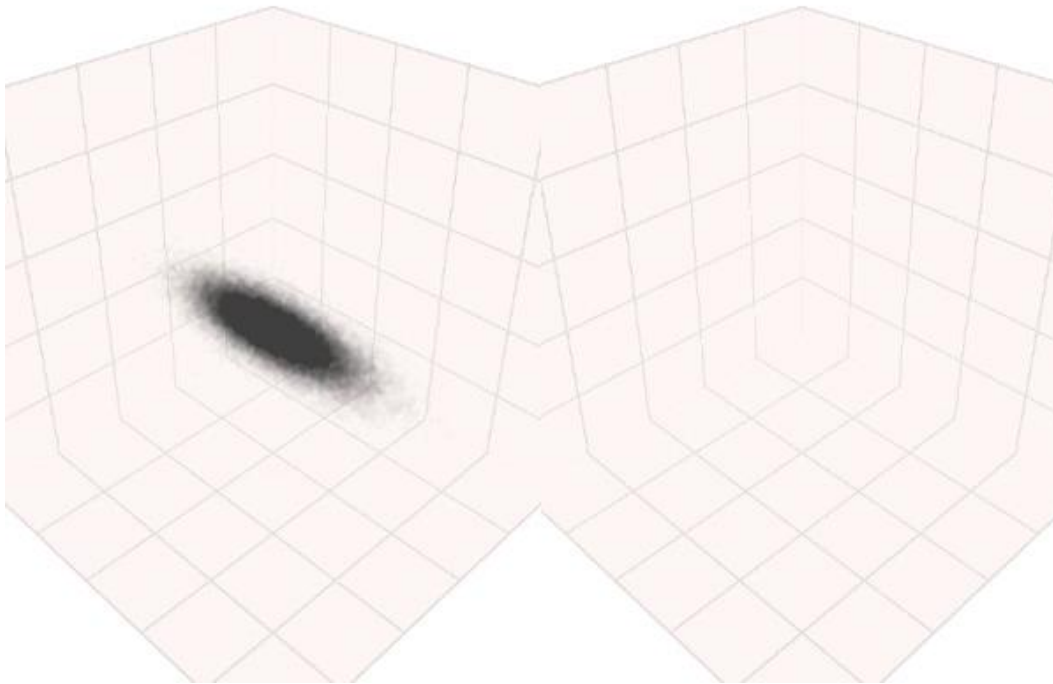


arXiv:1702.05954

Light-atom interactions as a spin model

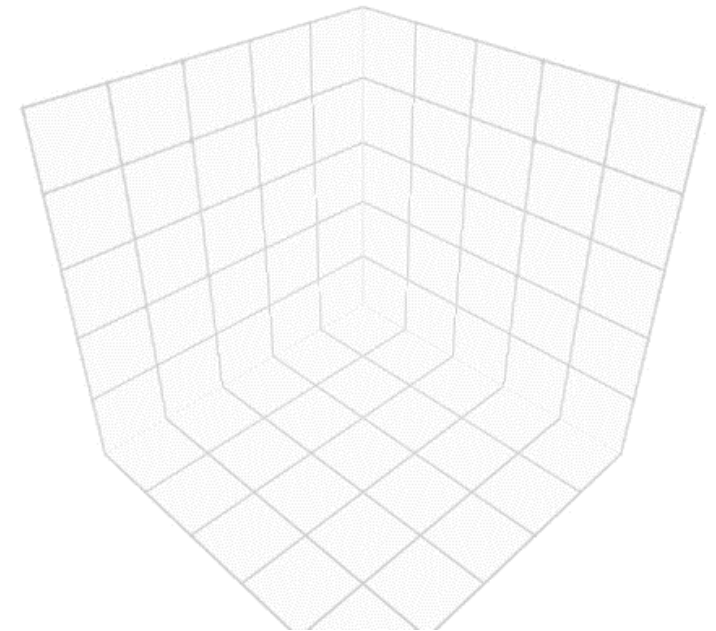
- Direct modeling of 3D atomic ensembles (James Douglas)

Electromagnetically induced transparency
 $N=50000$ atoms in Gaussian cloud, $OD \sim 50$



Atomic distribution

Field intensity



Spin population

1D chain of atoms in free space

Green's function for 1D atomic chain

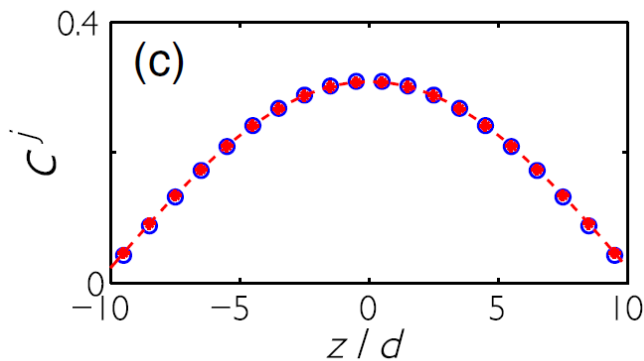
- Spin model in general:

$$H_{\text{eff}} = -\left(3\pi\hbar\Gamma_0 c / \omega_{eg}\right) \sum_{i,j} G(r_j, r_i, \omega_{eg}) \sigma_{eg}^i \sigma_{ge}^j$$

- Simple case: atoms in free space
- Must specify a geometry: 1D chain of atoms (but living in 3D)
- Considering just one excitation, there are N possible states
- Hamiltonian becomes N x N matrix in this subspace, $H_{ij} \propto G(r_j, r_i)$

Exact diagonalization

- Numerically diagonalize H
 - Each eigenstate α is a superposition of different atoms excited



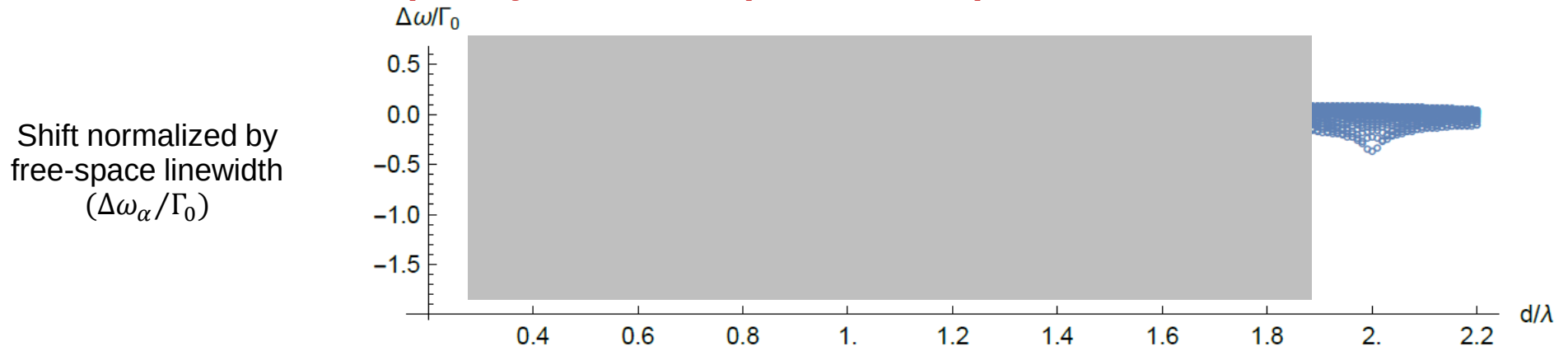
$$|\psi_\alpha\rangle = \sum_j c_\alpha^{(j)} |e_j\rangle$$

- Eigenvalues reveal:
 - Resonance frequency shift $\Delta\omega_\alpha$ away from bare atomic frequency ω_{eg}
 - Enhanced/suppressed decay rate Γ_α relative to single-atom rate Γ_0

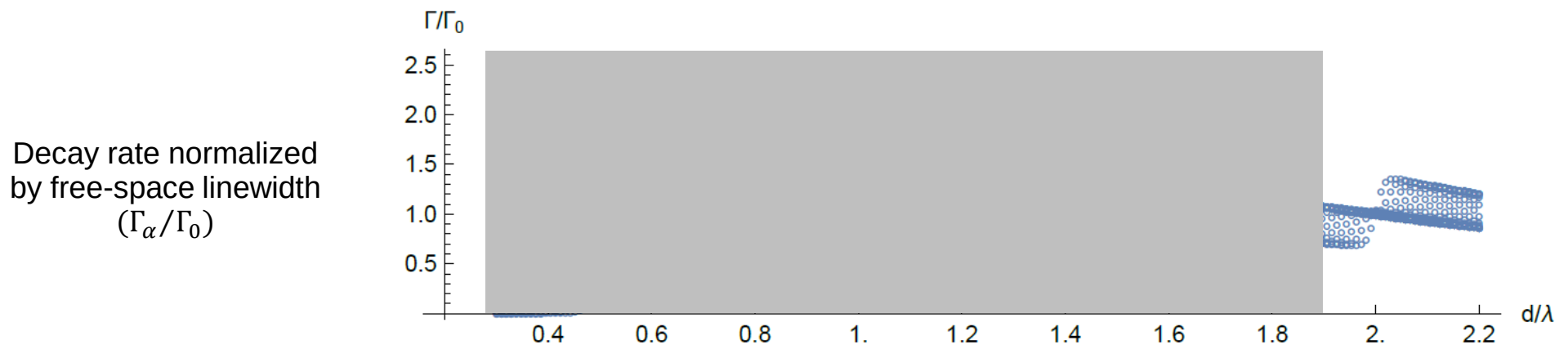
Energy shifts and decay rates

- Shifts and decay rates vs. lattice constant

Frequency shift vs. d ($N=30$ atoms)



Decay rate vs. d ($N=30$ atoms)

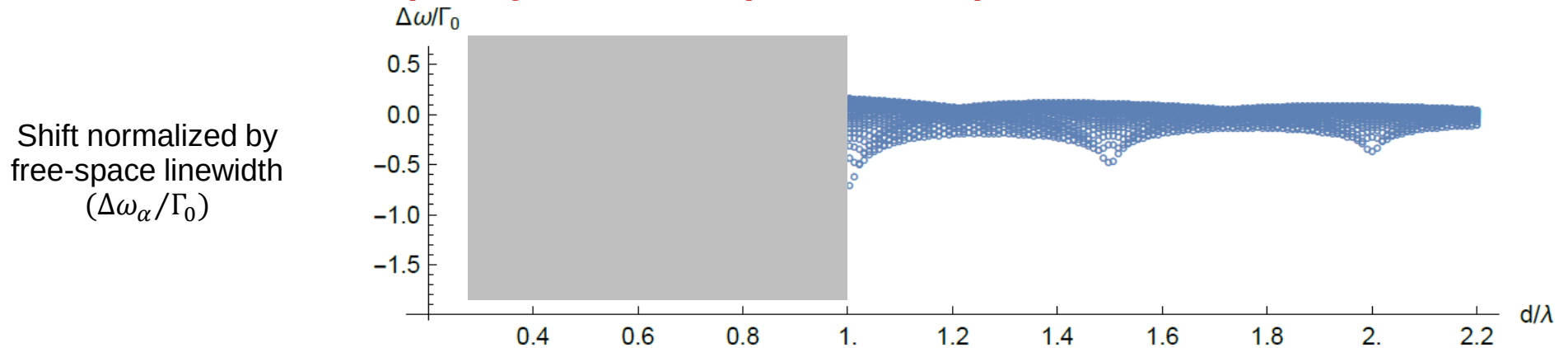


- Minimal effect of interactions at large distances

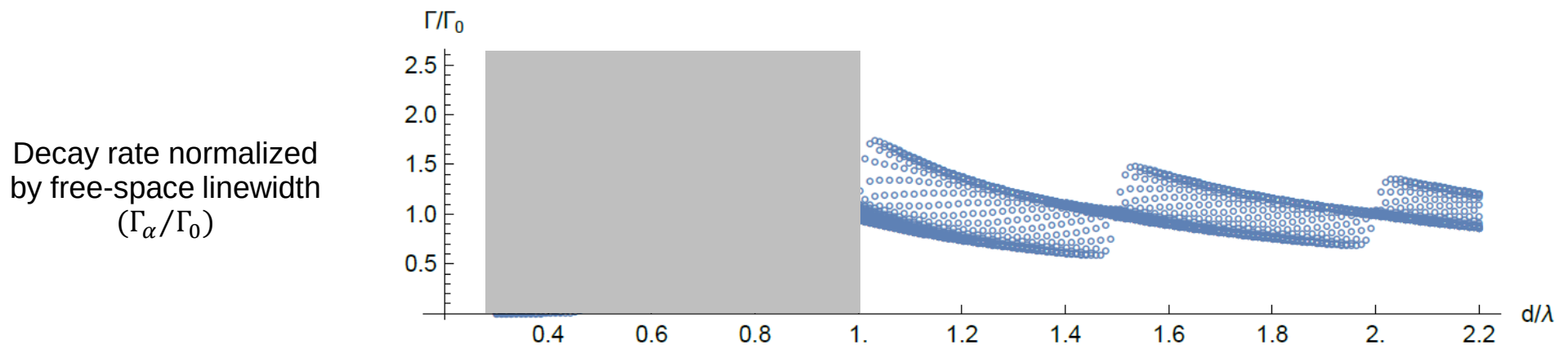
Energy shifts and decay rates

- Shifts and decay rates vs. lattice constant

Frequency shift vs. d ($N=30$ atoms)



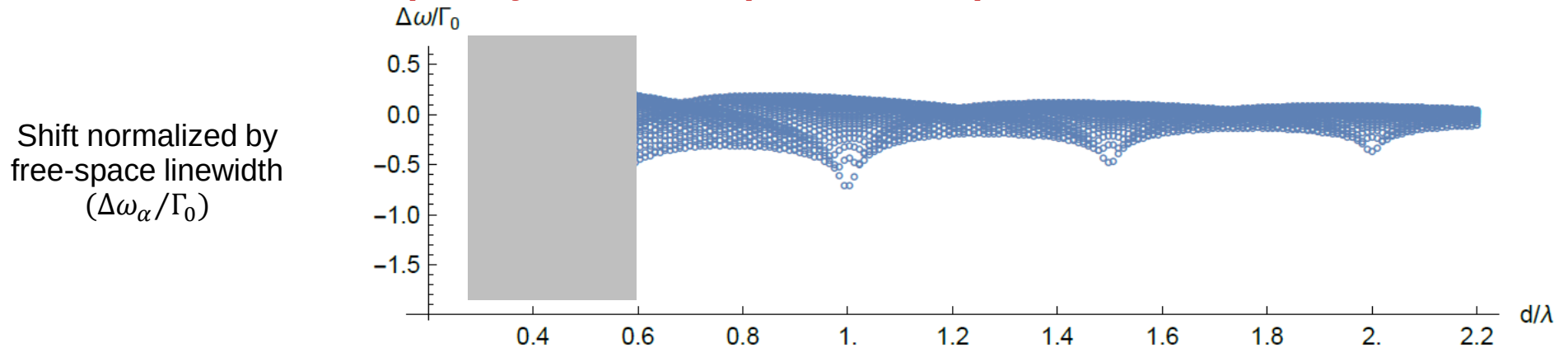
Decay rate vs. d ($N=30$ atoms)



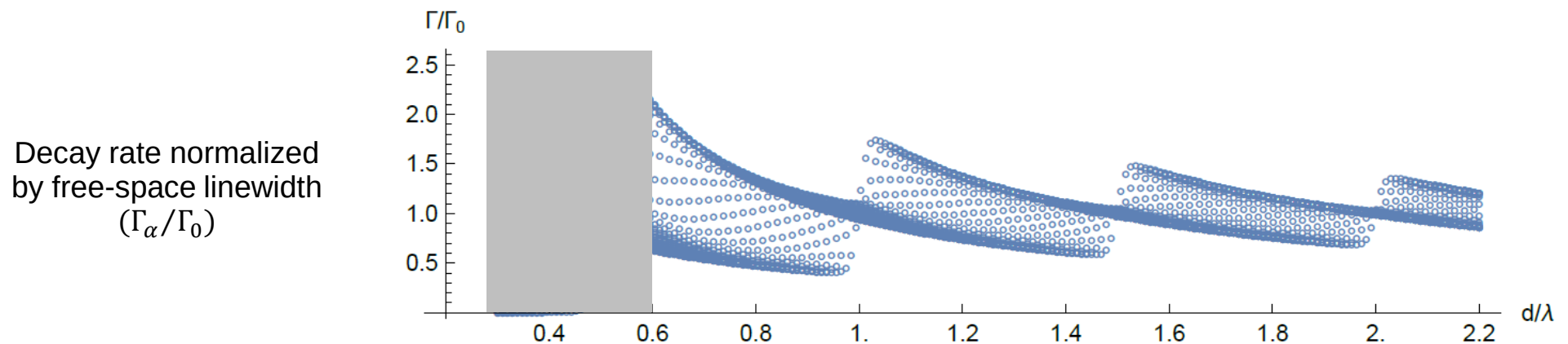
Energy shifts and decay rates

- Shifts and decay rates vs. lattice constant

Frequency shift vs. d (N=30 atoms)



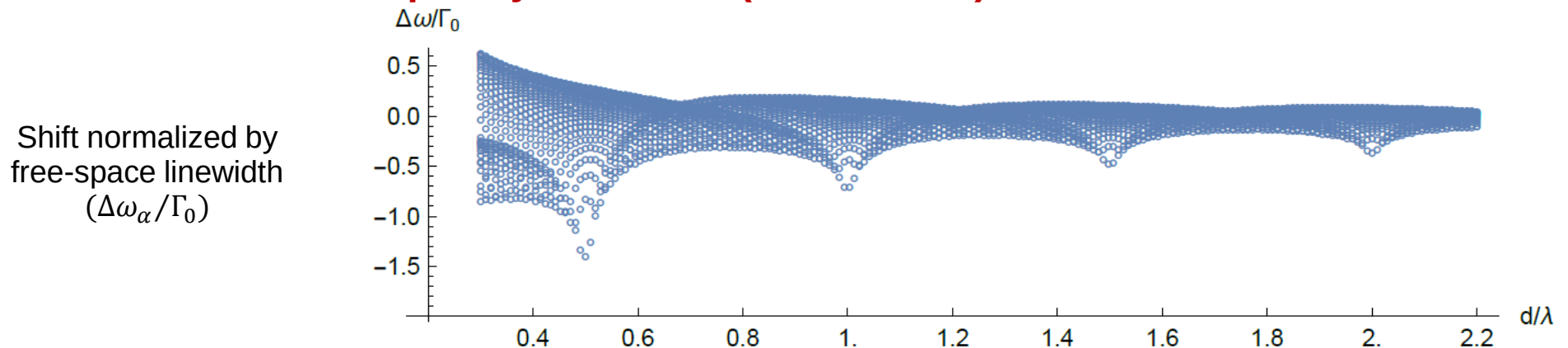
Decay rate vs. d (N=30 atoms)



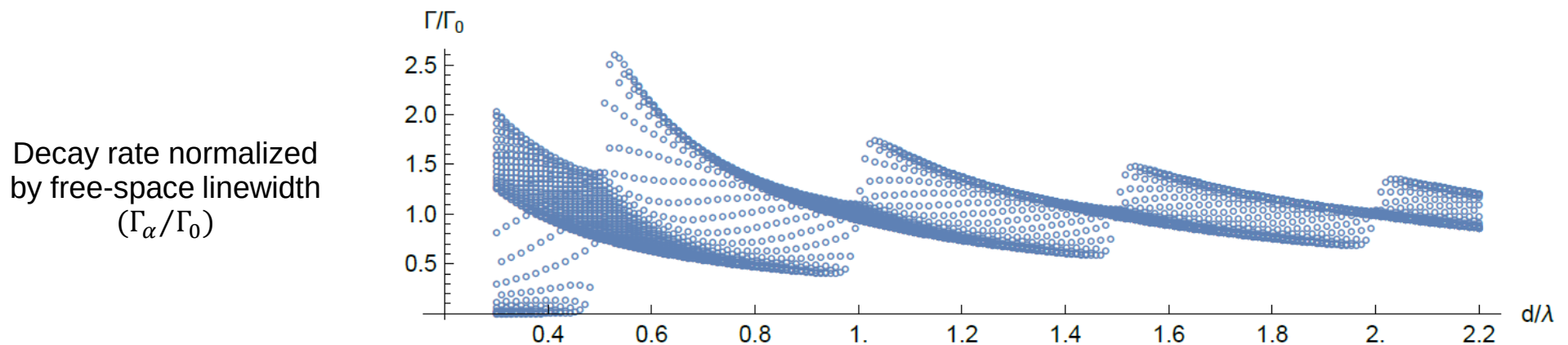
Energy shifts and decay rates

- Shifts and decay rates vs. lattice constant

Frequency shift vs. d ($N=30$ atoms)



Decay rate vs. d ($N=30$ atoms)

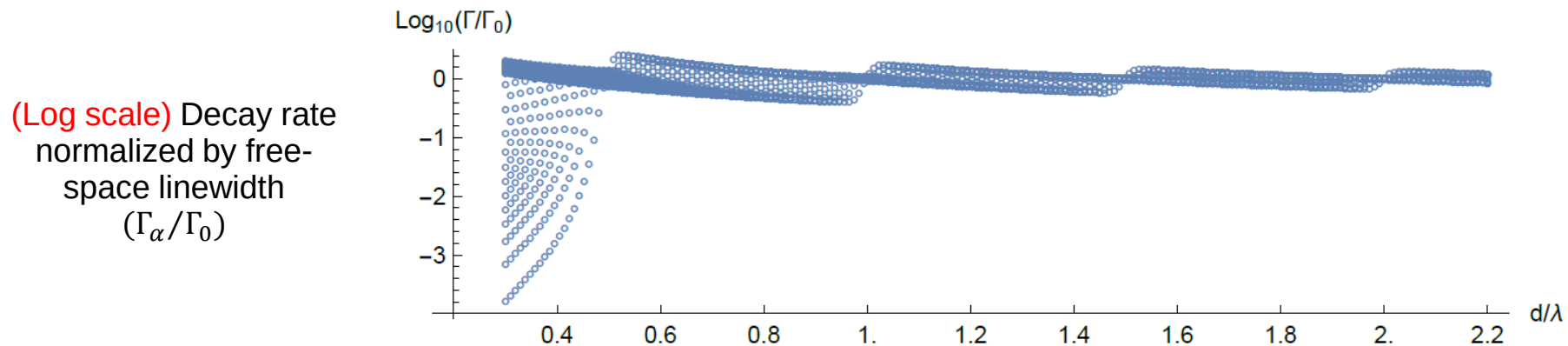


- States with **nearly zero decay rate** for $d < \frac{\lambda}{2}$!

Energy shifts and decay rates

- Shifts and decay rates vs. lattice constant

Decay rate (log scale) vs. d ($N=30$ atoms)



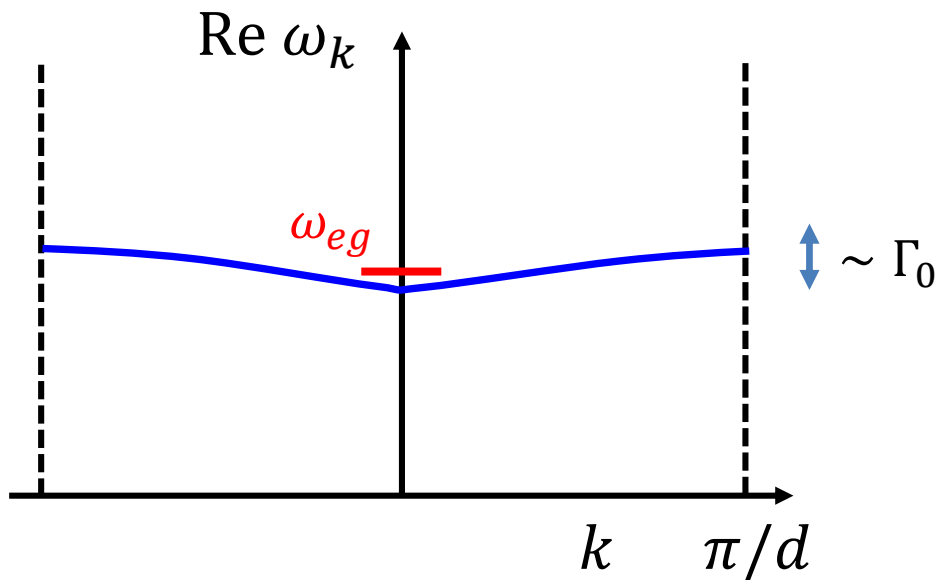
- Smallest decay rates go like $\Gamma_\alpha \sim \Gamma_0 \alpha^2 / N^3$
 $\alpha = 1, 2, 3, \dots$
- Interference of wave emission really matters at close distances!

Band structure of infinite lattice

- Infinite chain: single-excitation eigenstates are Bloch modes

$$|\psi_k\rangle = \sum_j e^{ikz_j} |e_j\rangle$$

- Diagonalize H, represent spectrum by band structure

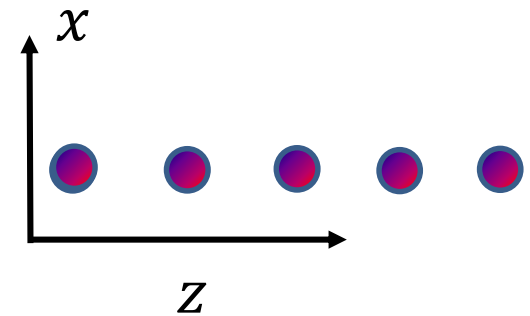
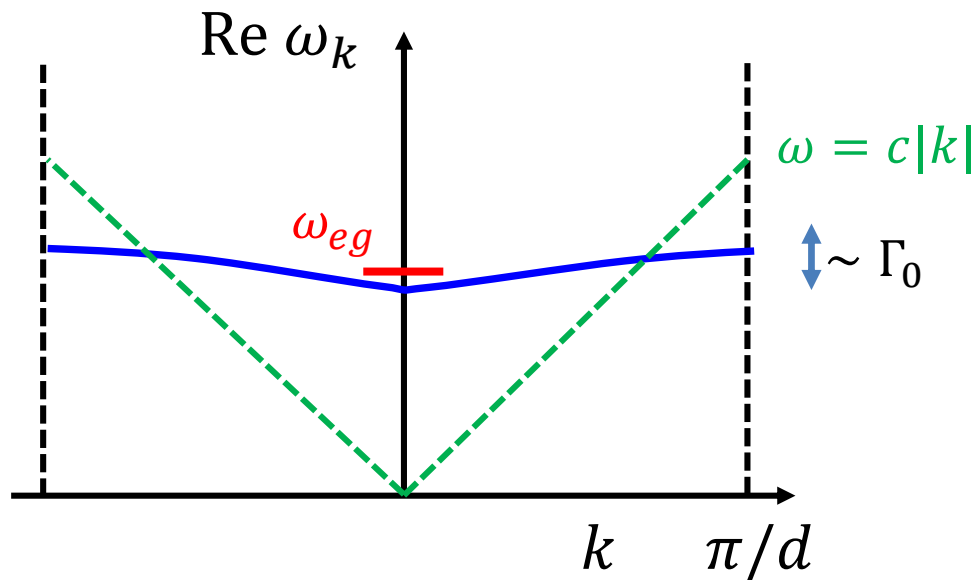


Band structure of infinite lattice

- Infinite chain: single-excitation eigenstates are Bloch modes

$$|\psi_k\rangle = \sum_j e^{ikz_j} |e_j\rangle$$

- Diagonalize H, represent spectrum by band structure



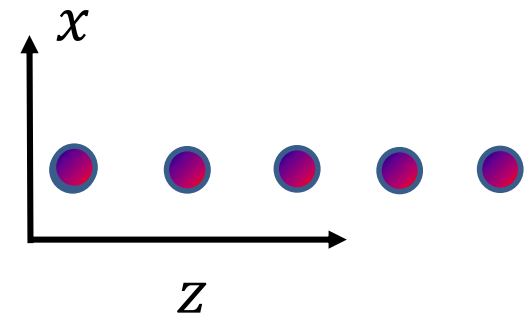
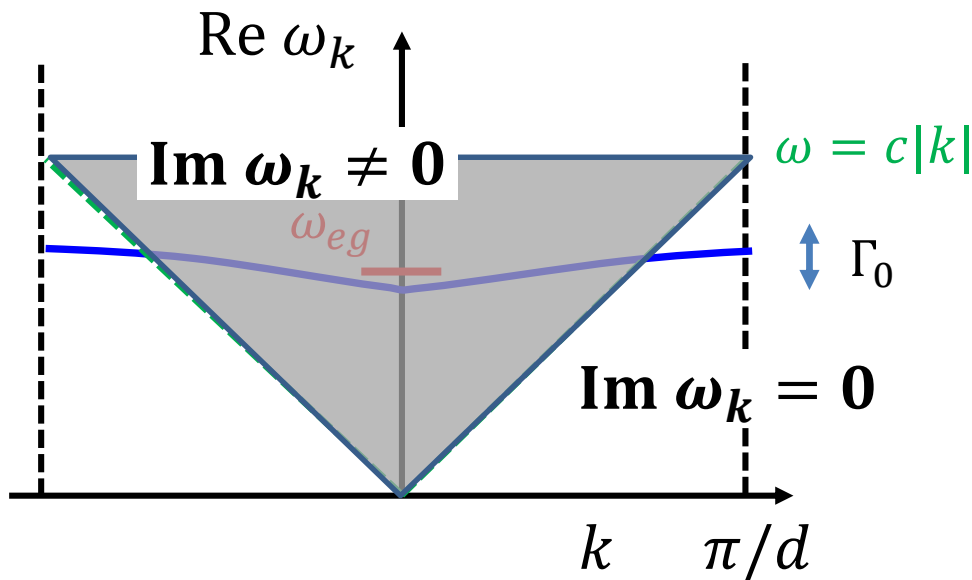
- Emitted light also has same wavevector: $E(r) \sim e^{ikz+ik_{\perp}x}$
 - Dispersion relation $k^2 + k_{\perp}^2 = (\omega/c)^2$
 - $|k| > \omega/c$ implies $k_{\perp} \in \text{Im}$ (evanescent or guided mode)

Band structure of infinite lattice

- Infinite chain: single-excitation eigenstates are Bloch modes

$$|\psi_k\rangle = \sum_j e^{ikz_j} |e_j\rangle$$

- Diagonalize H, represent spectrum by band structure

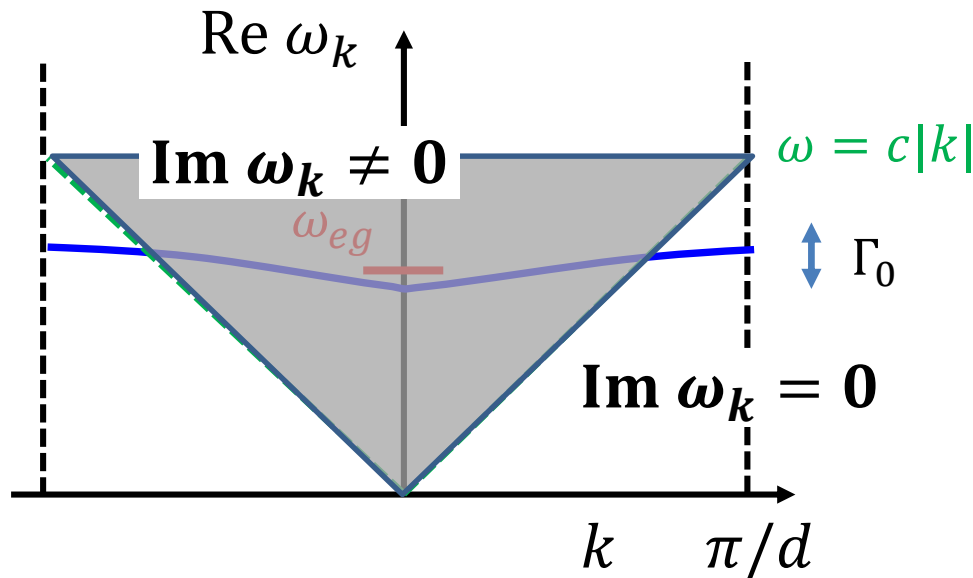


- Emitted light also has same wavevector: $E(r) \sim e^{ikz+ik_{\perp}x}$
 - Dispersion relation $k^2 + k_{\perp}^2 = (\omega/c)^2$
 - $|k| > \omega/c$ implies $k_{\perp} \in \text{Im}$ (evanescent or guided mode)

Subradiant states as guided modes

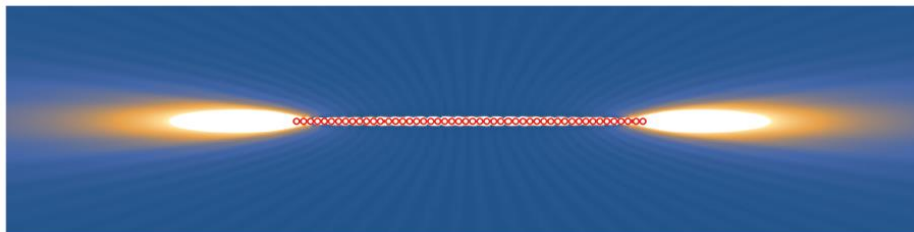
- In ordered arrays:

Subradiance = guided modes of an atomic “fiber”



- Condition: $\omega = c|k|$ intersects Brillouin zone above ω_{eg}
- Equivalent to $d < \frac{\lambda_{eg}}{2}$

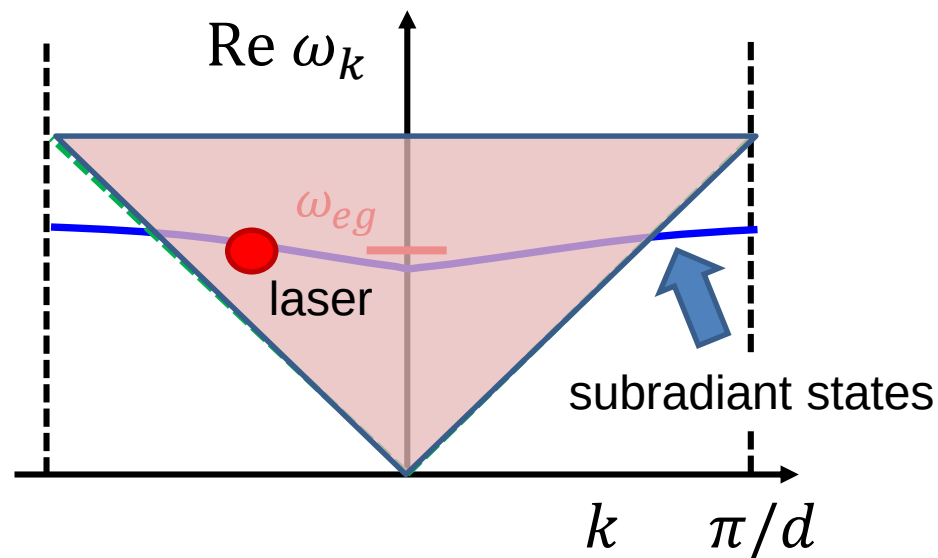
- Finite chain: non-zero decay rate $\Gamma_\alpha \propto \Gamma_0 \alpha^2 / N^3$ due to end-fire emission off the “fiber” ends



Emission pattern for most subradiant state, $N=30$ atoms

Accessing subradiant states

- Hard to couple to subradiant states from free space

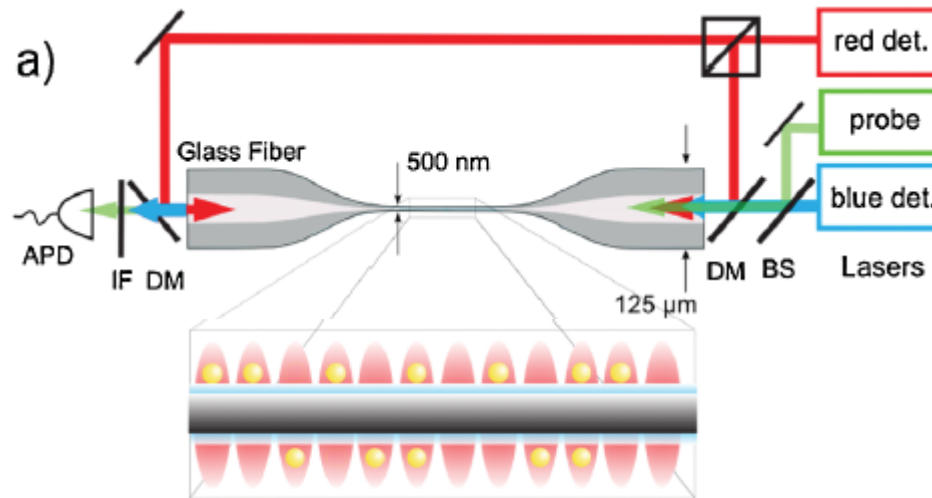


- First experimental observation in extended atomic ensembles just last year (Robin Kaiser, Nice)
- More efficient approach: excite with another set of guided modes (optical nanofiber!)

Atom-nanofiber interfaces

Atom-nanofiber interface

- Trap atoms in lattice with far off-resonant guided modes



Vetsch et al, PRL 104, 203603 (2010)

- Efficient coupling of atoms with near-resonant photons



Single atom:

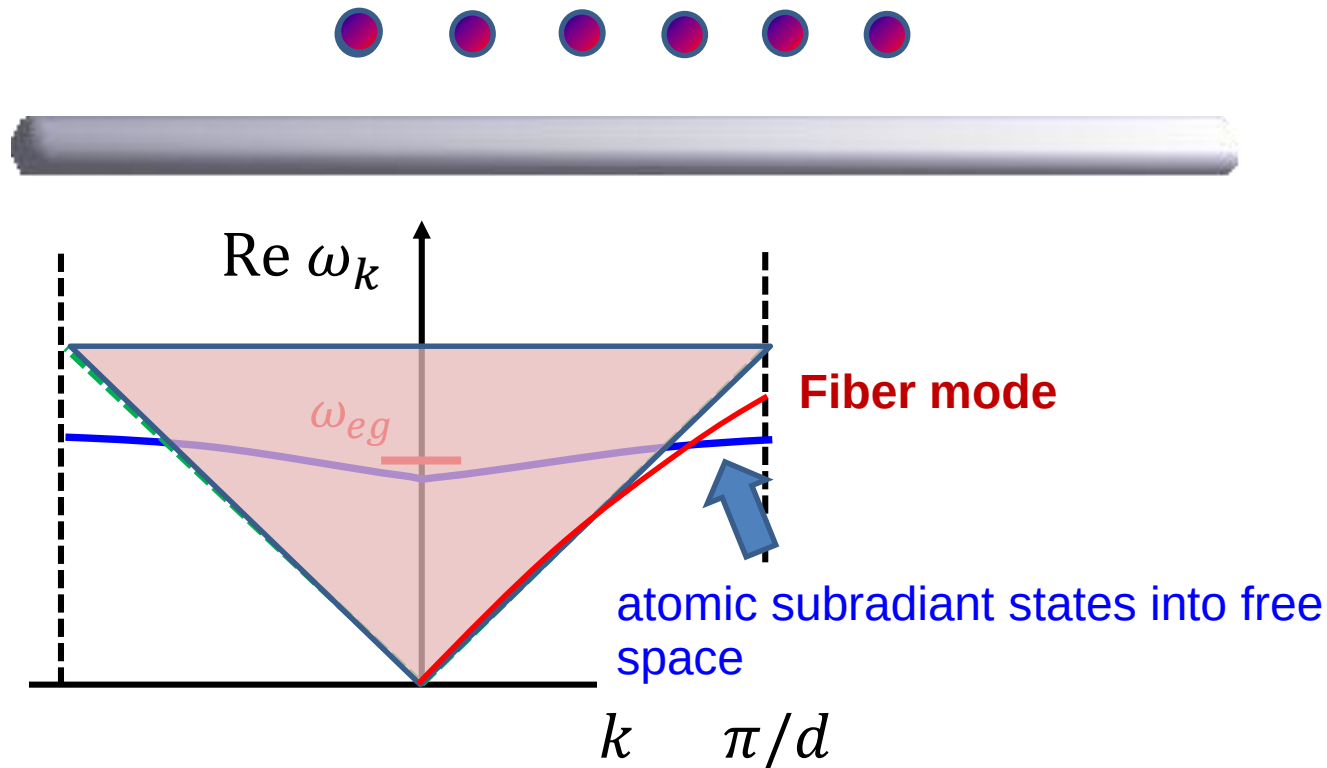


Emission into guided modes $\Gamma_{1D} \sim 0.1\Gamma_0$

- Expts: Hakuta (Tokyo), Rauschenbeutel (TU Vienna), Kimble (Caltech), Orozco (JQI), Laurat (Paris), Polzik (NBI), Nic Chormaic (OIST), ...

“Selective” radiance

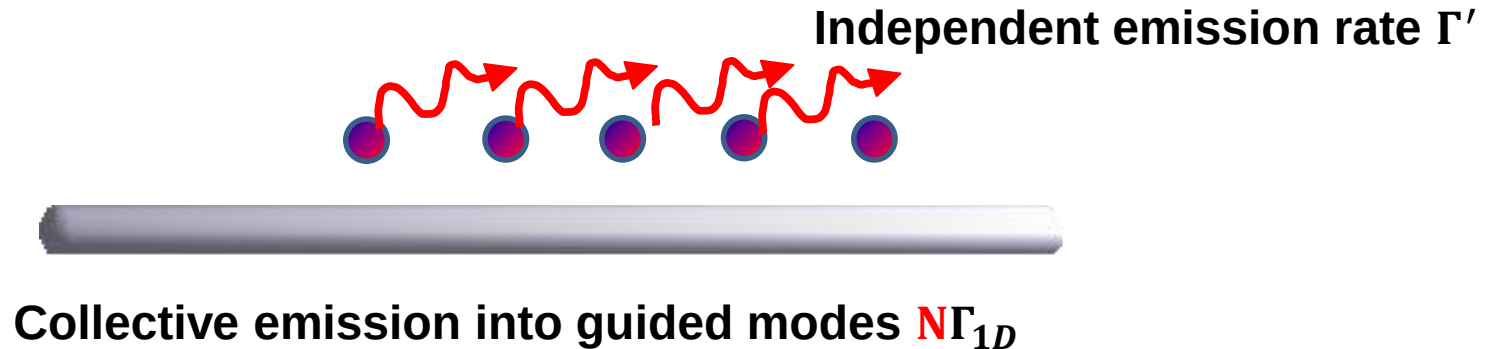
- Previously subradiant states can now couple to guided modes of the fiber



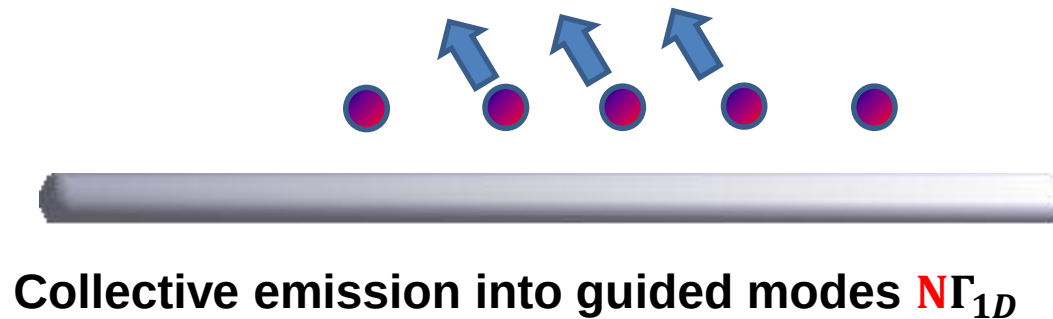
- Not subradiant, but “selectively” radiant... **perfect!**
- Efficient atom-light interface: atoms talk very well to modes of interest, but not to free space
 - Use this to beat the “optical depth” limit

Model of atom-light interactions

- “Independent emission model”

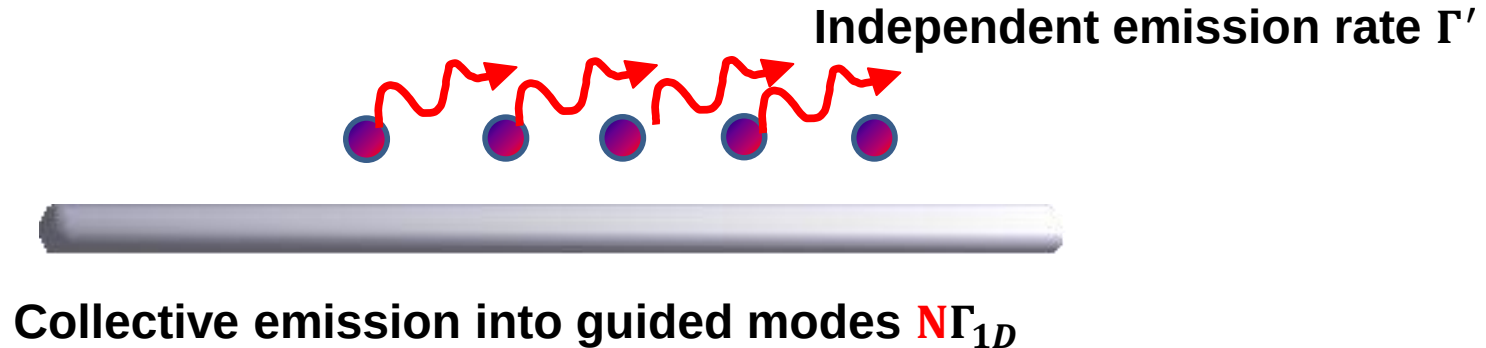


- Collective emission model



Model of atom-light interactions

- “Independent emission model”



- Collective emission model
- Use our “spin model”

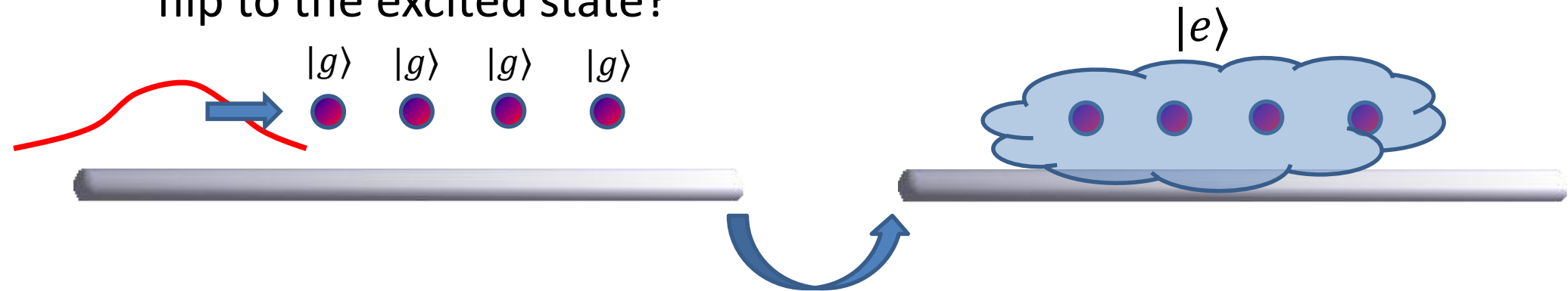
$$H_{\text{eff}} = -\mu_0 d_0^2 \omega_{eg}^2 \sum_{i,j} \underbrace{G(r_j, r_i, \omega_{eg})}_{\text{Exact for cylindrical fiber}} \sigma_{eg}^i \sigma_{ge}^j$$

- Field propagation

$$\hat{E}(r, t) = \hat{E}_{in}(r, t) + (3\pi\hbar c\Gamma_0/d_0\omega_{eg}) \sum_i G(r, r_i, \omega_{eg}) \sigma_{ge}^i(t)$$

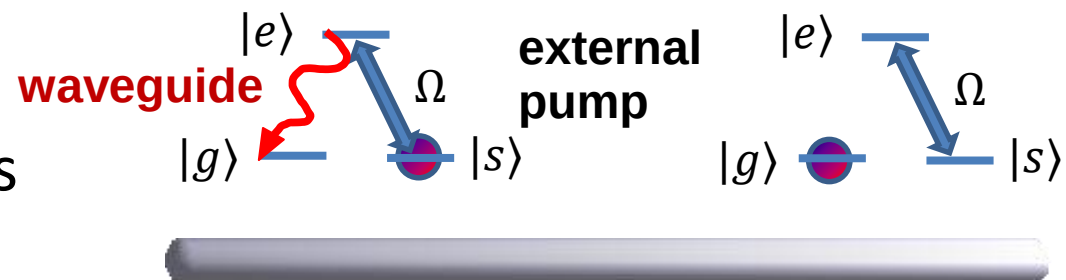
Quantum memory for light

- How well can one store an incoming photon as a collective spin flip to the excited state?



- By time reversal symmetry, can study the reverse problem of mapping an initial spin excitation into a photon

- Use three-level systems

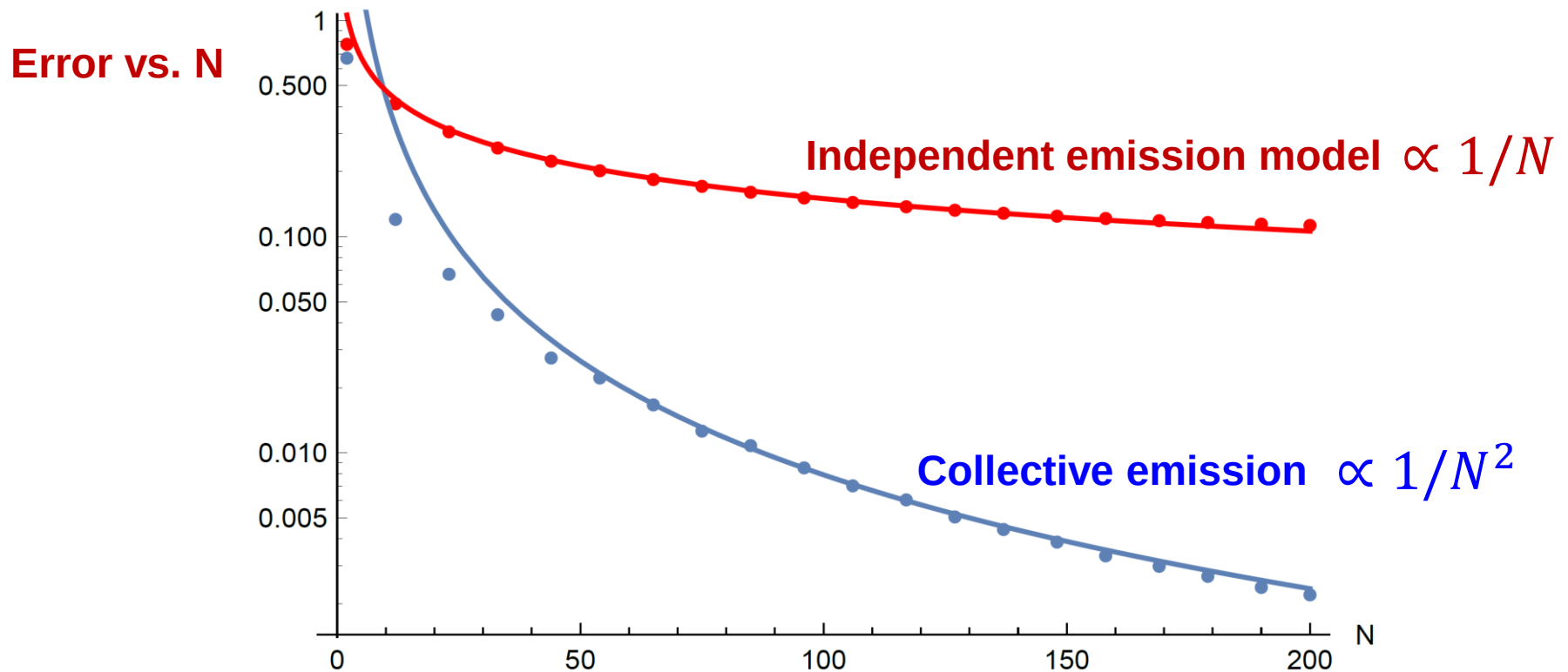


- Independent emission model: error $\sim \frac{5.8\Gamma'}{N\Gamma_{1D}} = \frac{5.8}{OD}$

Same scaling as free space: AV Gorshkov et al, PRL 98, 123601 (2007)

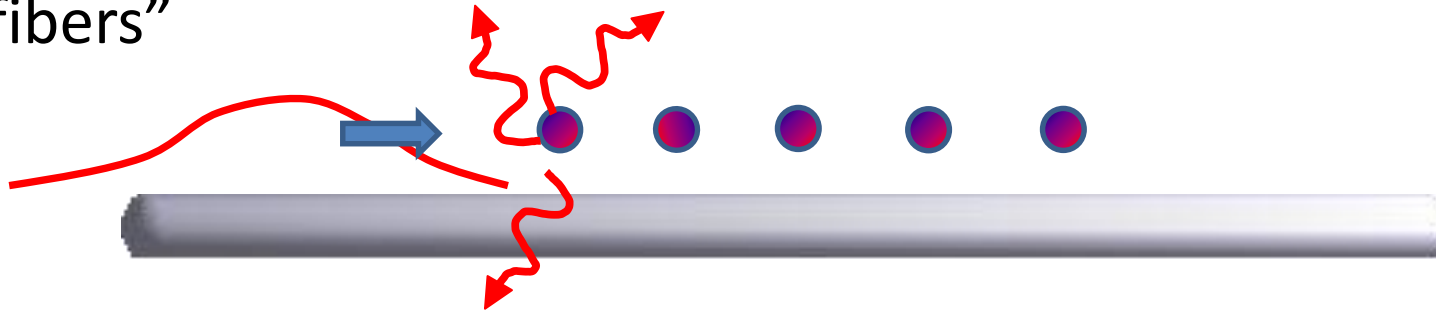
Photon storage/generation

- Collective emission:
 - Numerically diagonalize H_{eff} within manifold of single $|s\rangle$ excitation
 - Look for eigenstate with highest emission probability into waveguide



What limits the process?

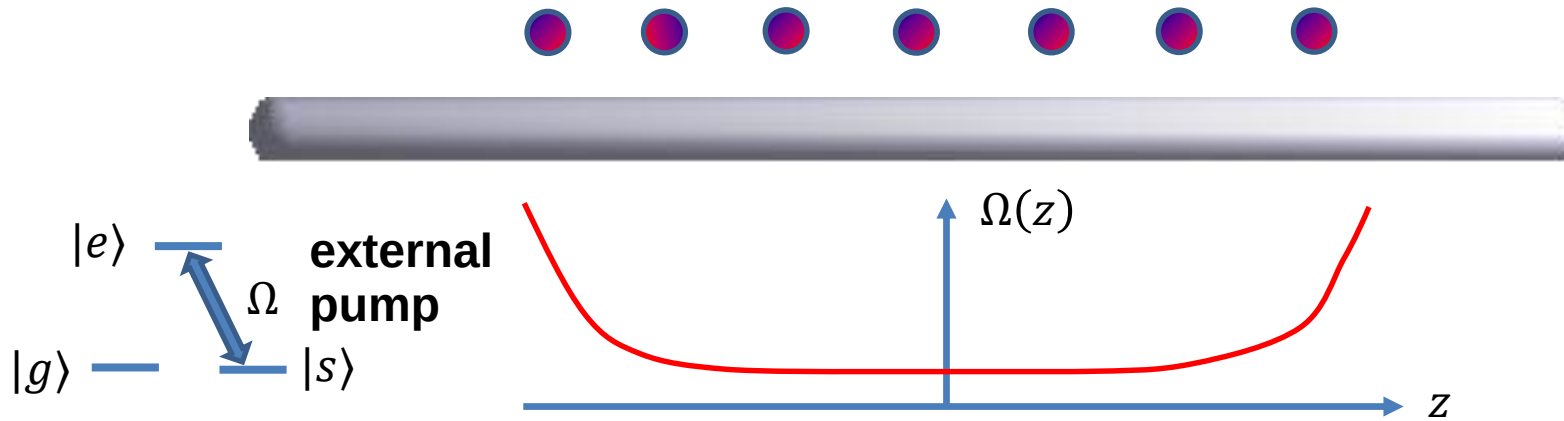
- $1/N^2$ error seems less than ideal
 - $\frac{1}{N}$ from collective enhancement into guided mode
 - “Only” $\frac{1}{N}$ suppression of emission into free space
- Origin: scattering losses at interface between two different “fibers”



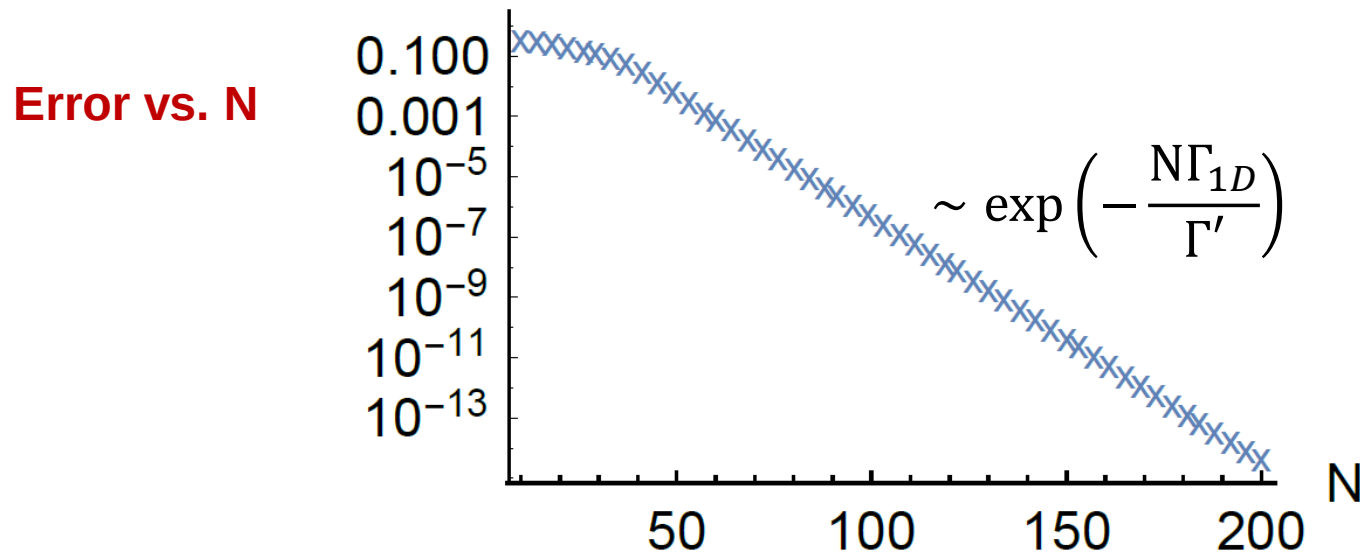
- Need a fiber “connector!”

Photon storage with impedance matching

- Spatially vary the pump field profile, so that atoms at the ends “gradually” couple to fiber

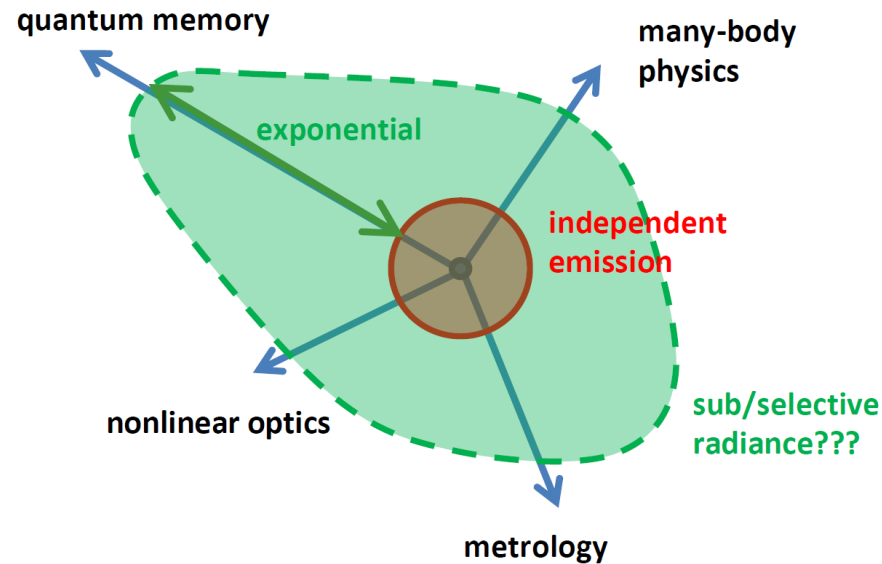


- Exponential suppression of error!



Outlook

- What is the new ceiling if one exploits subradiance?



- Atom-light interactions as a quantum spin model

$$H_{\text{eff}} = -\left(3\pi\hbar\Gamma_0 c/\omega_{eg}\right) \sum_{i,j} G(r_j, r_i, \omega_{eg}) \sigma_{eg}^i \sigma_{ge}^j$$

$$\hat{E}(r, t) = \hat{E}_{in}(r, t) + \left(3\pi\hbar c\Gamma_0/d_0\omega_{eg}\right) \sum_i G(r, r_i, \omega_{eg}) \sigma_{ge}^i(t)$$

- New insights or numerical tools for AMO physics?

Multiple excitations

- Single-excitation physics is classical
- Can we encode many excitations in sub-radiant states?
- Most sub-radiant single excitation $\Gamma_1 \propto \Gamma_0/N^3$

$$|\psi\rangle = s_1^\dagger |g\rangle^{\otimes N} = \sum_j c_j^{(1)} |e_j\rangle$$

- Example: two excitations

- What if we create same excitation twice: $|\psi\rangle = (s_1^\dagger)^2 |g\rangle^{\otimes N}$

Eigenstate?

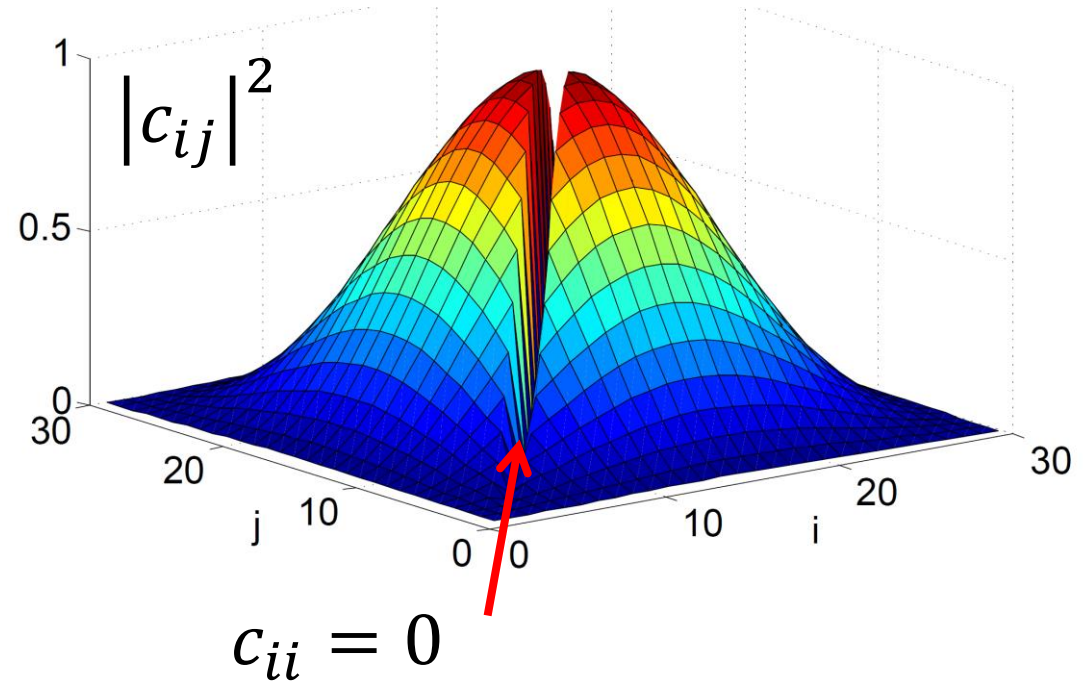
- Bosons: yes! Decay rate $2\Gamma_1$
- Spins: no!

Two-excitation wavefunction

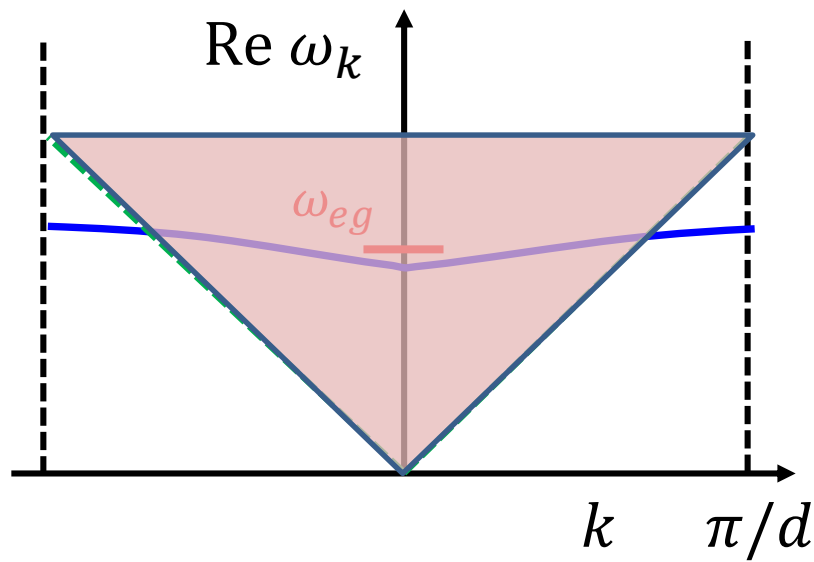
- Wave function:

$$|\psi\rangle = (S_1^\dagger)^2 |g\rangle^{\otimes N}$$

$$= \sum_{i,j} c_{ij} |e_i e_j\rangle$$



- State contains many momentum components within light cone



- Only weakly subradiant

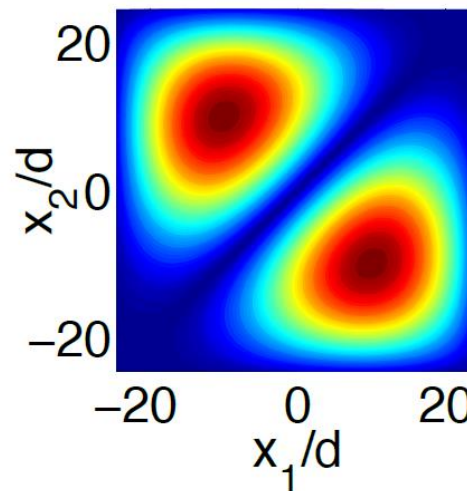
$$\langle \Gamma \rangle \sim \Gamma_0 / N$$

Multiple excitations

- How to construct many-excitation subradiant states?
- Single-particle eigenstates
$$\Gamma_\alpha \propto \alpha^2 \Gamma_0 / N^3, \quad |\psi_\alpha\rangle = \sum_j c_j^{(\alpha)} |e_j\rangle$$
- Sub-radiant states should satisfy:
 - Wavevectors beyond the light line, *and* spatially non-overlapping
- Create a *fermionized* wave function (Pauli exclusion!)

- Example: two excitations

$$|\psi\rangle = \sum_{i>j} c_{ij} |e_i e_j\rangle$$
$$c_{ij} = c_i^{(1)} c_j^{(2)} - c_i^{(2)} c_j^{(1)}$$



$$\Gamma \sim \Gamma_1 + \Gamma_2 \propto \frac{1}{N^3}$$

- Subradiance itself is a rich many-body problem!