

# Precision Top Mass Determination at the LHC with Jet Grooming

**Aditya Pathak**

**Massachusetts Institute of Technology**

*In Collaboration with*

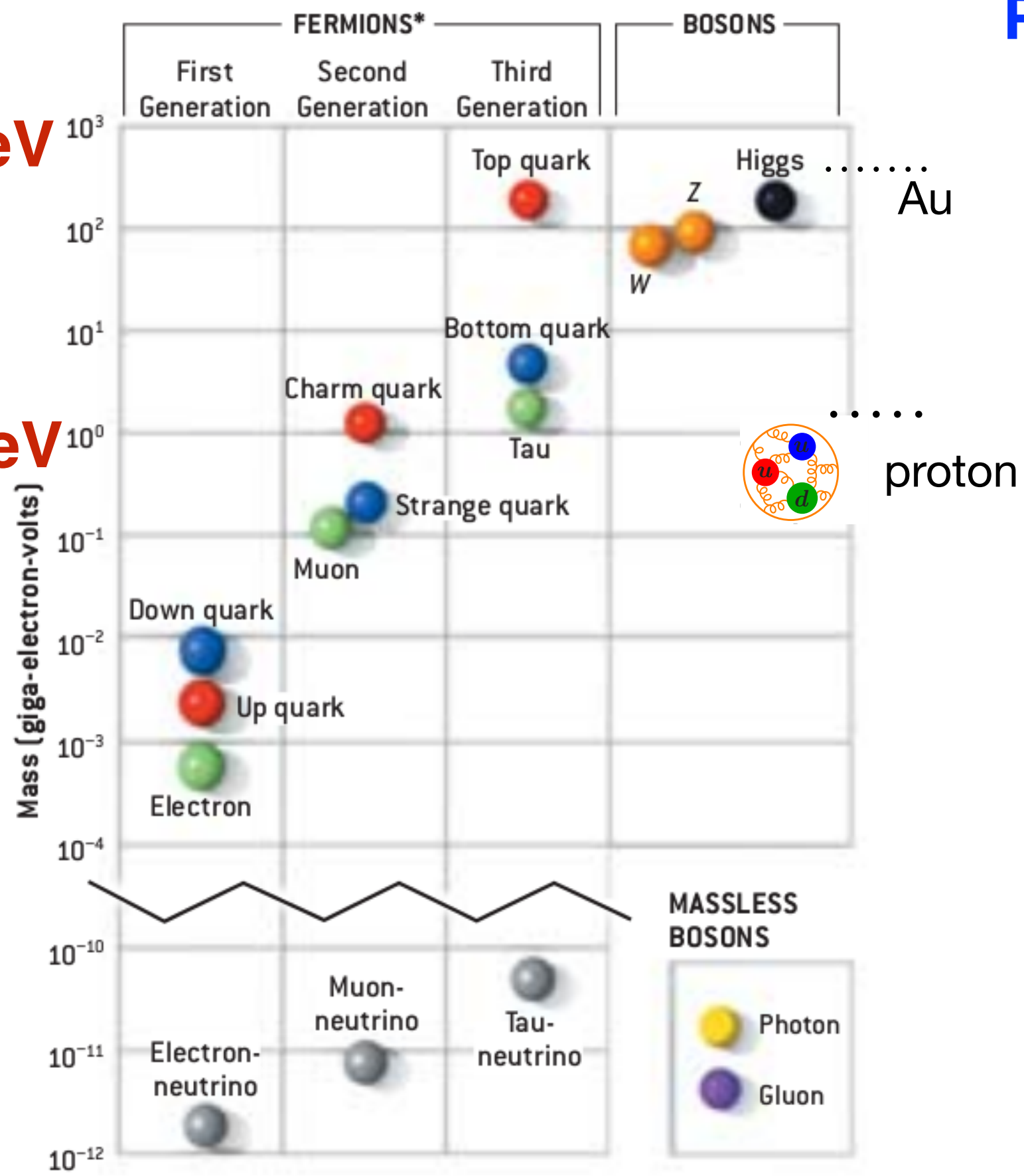
Andre Hoang, Sonny Mantry, Iain Stewart

January 2017  
ICTS-TIFR, Bangalore

# Particle Masses

1 TeV

1 GeV





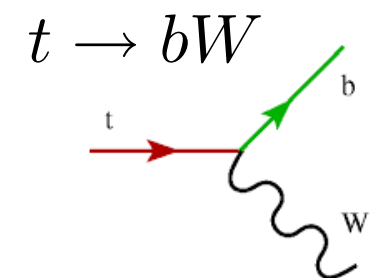
# Top Quark is special

Heaviest known elementary particle is the **top quark**

$$m_t = 173 \text{ GeV}$$

$$> m_H = 125 \text{ GeV}$$

The only quark that **decays before it binds** into a hadron



Largest Mass ->  
**Largest coupling to Higgs**

$$i \text{ --- } H \propto m_i$$

Dominant higgs production

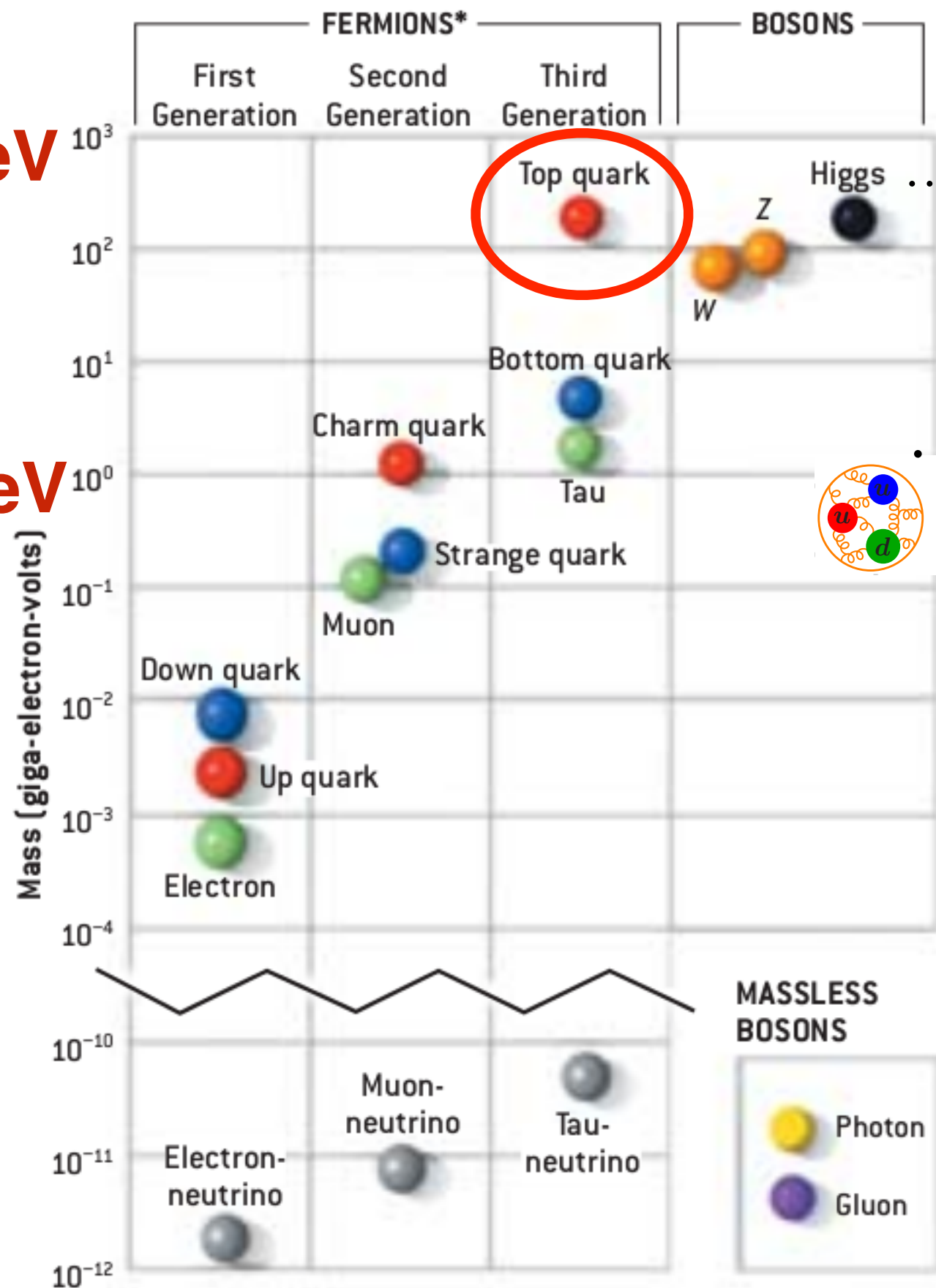
Plays key role in BSM searches  $Z' \rightarrow t\bar{t}$

Great exercise in jet tagging

$$t\bar{t} \rightarrow H, H \rightarrow b\bar{b}$$

1 TeV

1 GeV



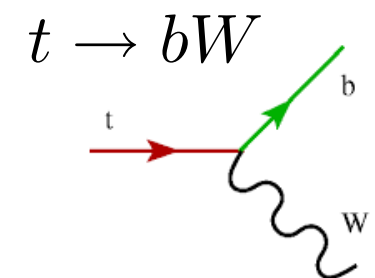
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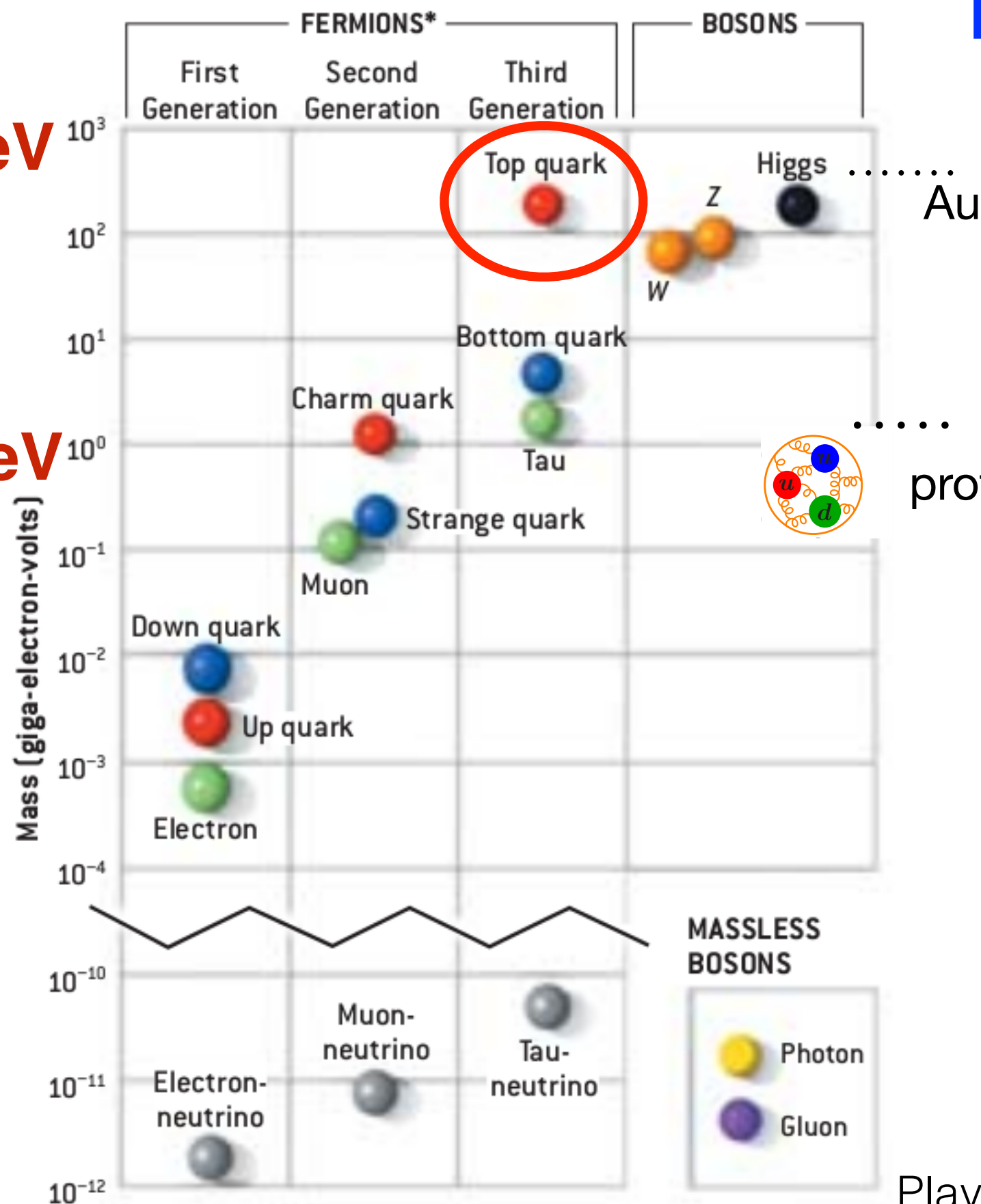
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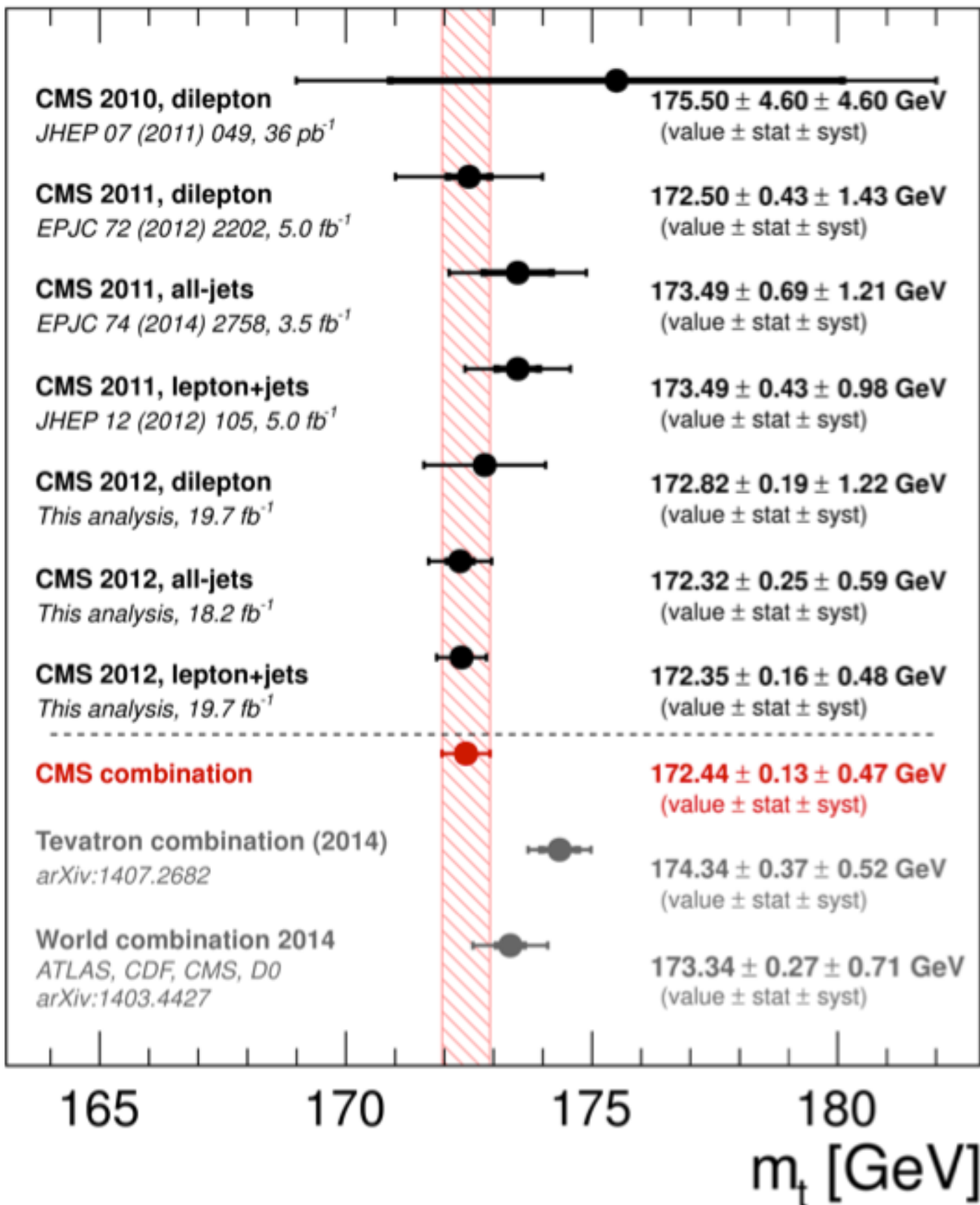
**This talk: exploiting jet grooming for precision top quark physics.**

# Precision Measurements

Tevatron (2014):  $m_t = 174.34 \pm 0.64 \text{ GeV}$

CMS Run 1 (2015):  $m_t = 172.44 \pm 0.49 \text{ GeV}$

ATLAS Run 1 (2016):  $m_t = 172.84 \pm 0.70 \text{ GeV}$



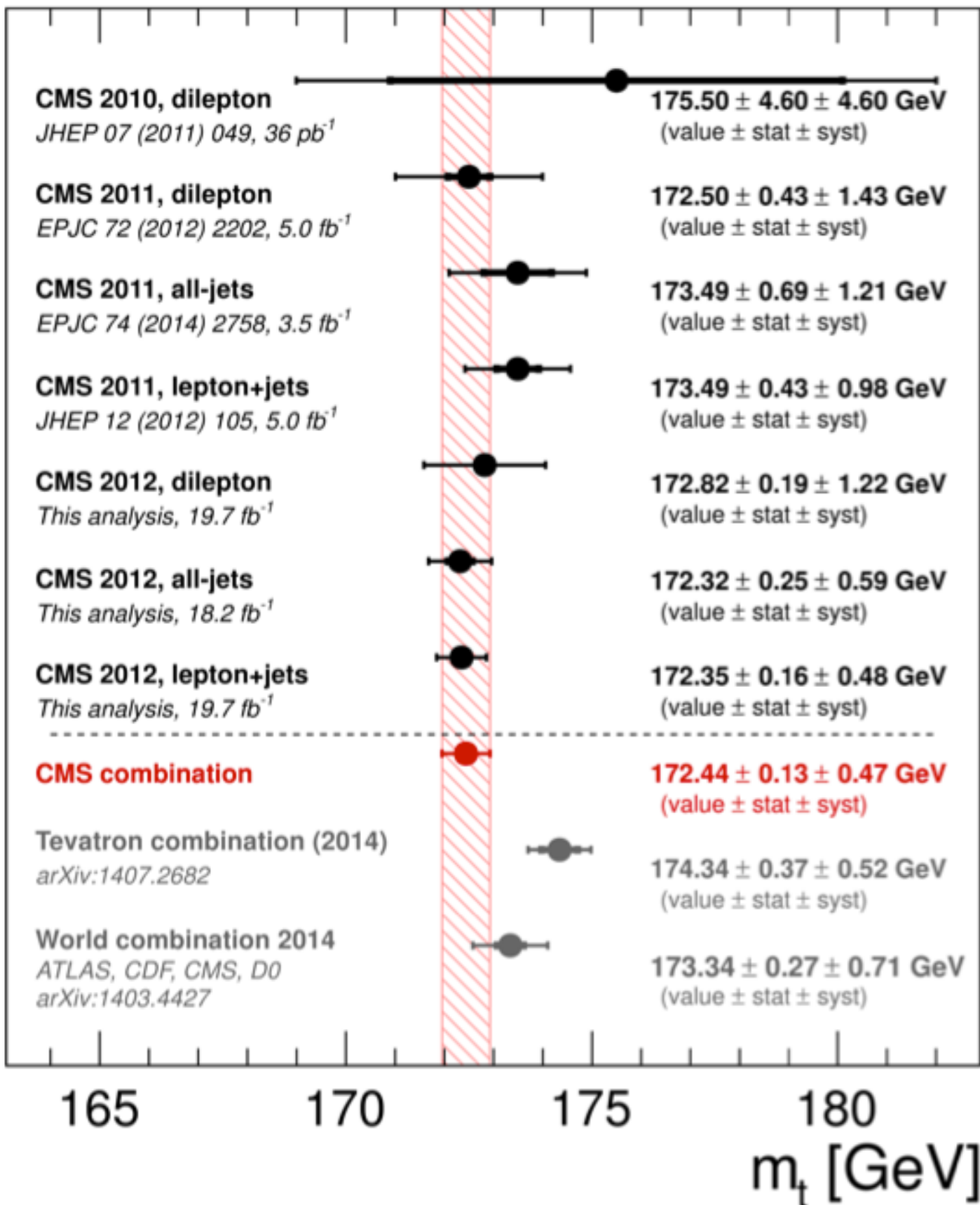
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0.3% sys + 0.07% stat!





# Precision Measurements

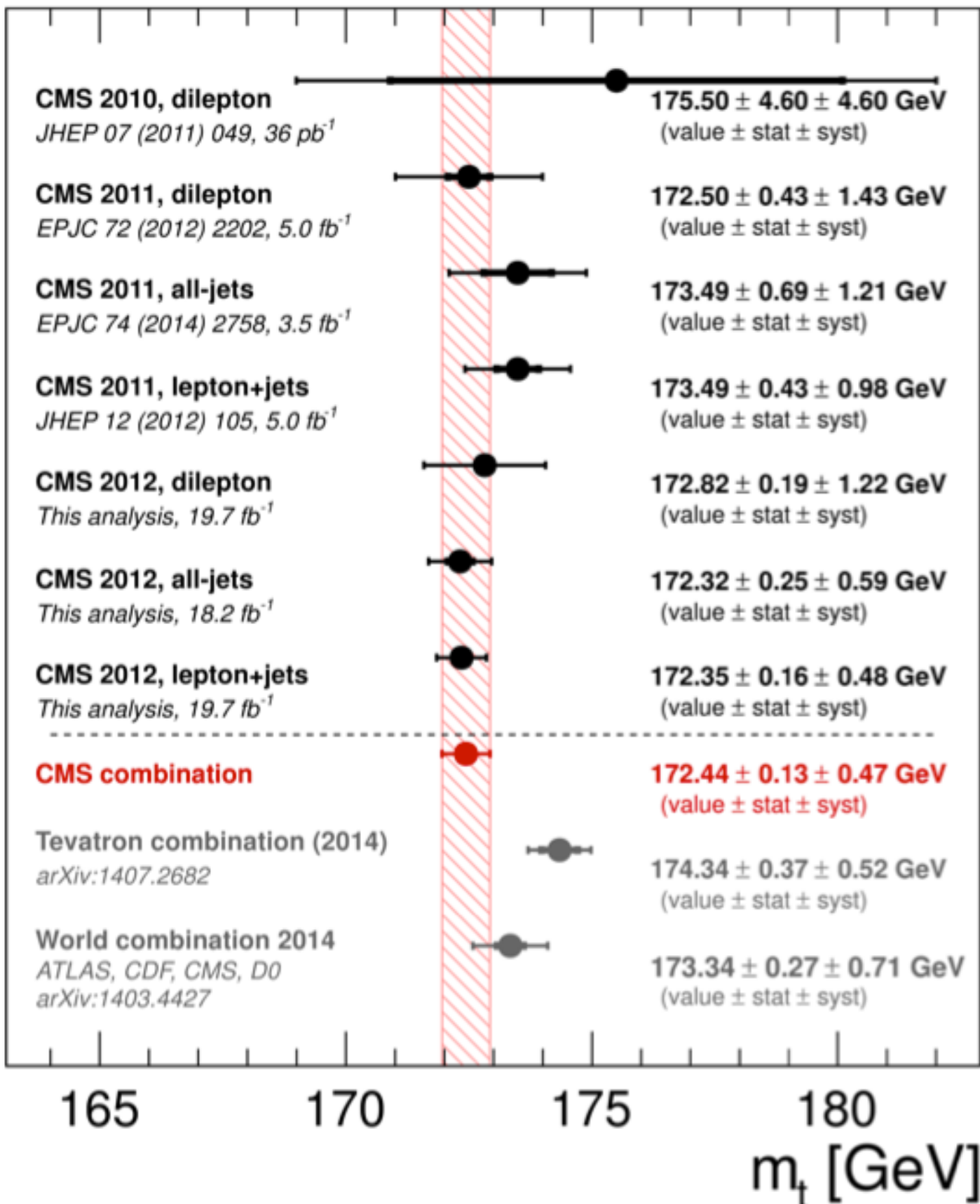
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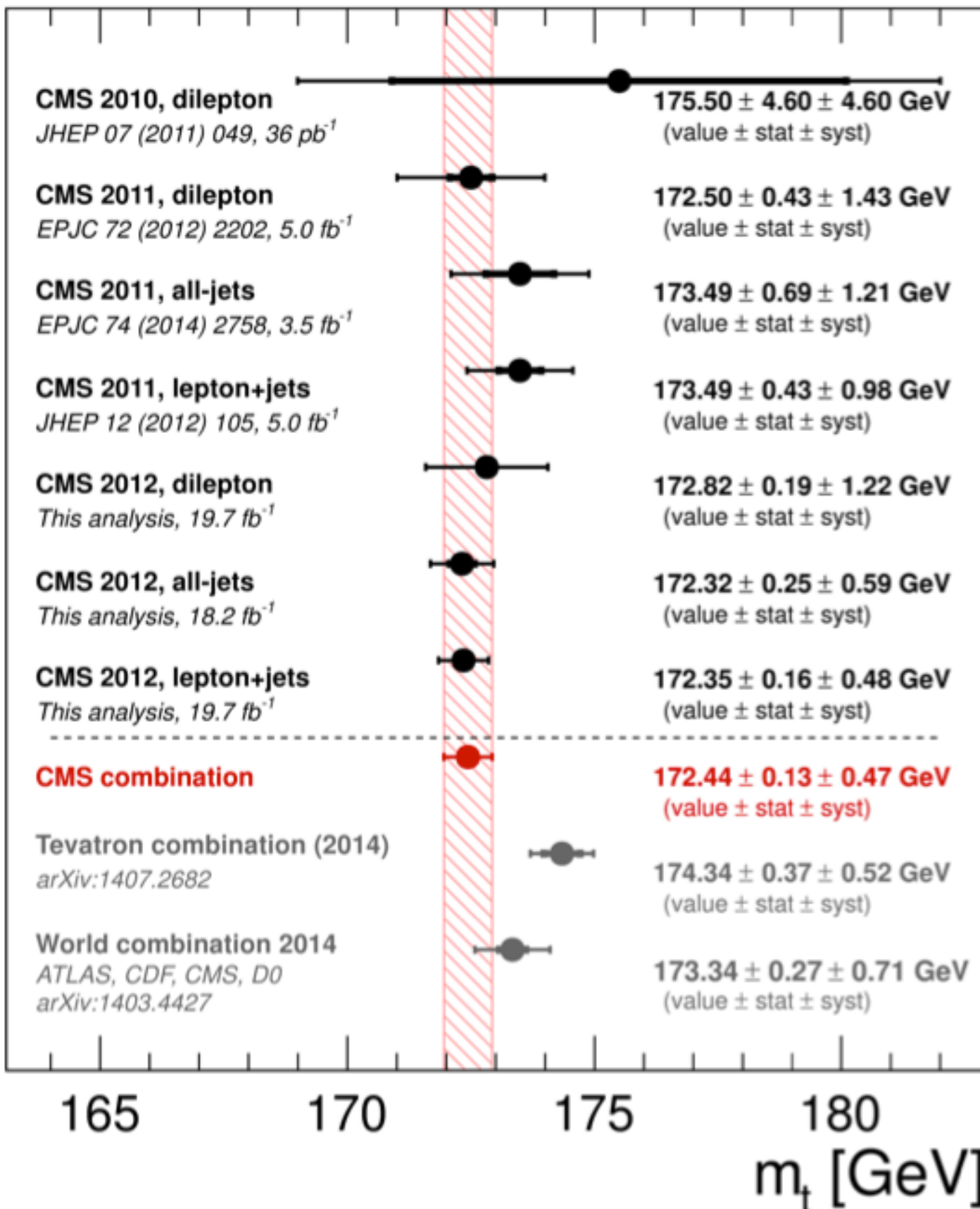
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What mass is it?

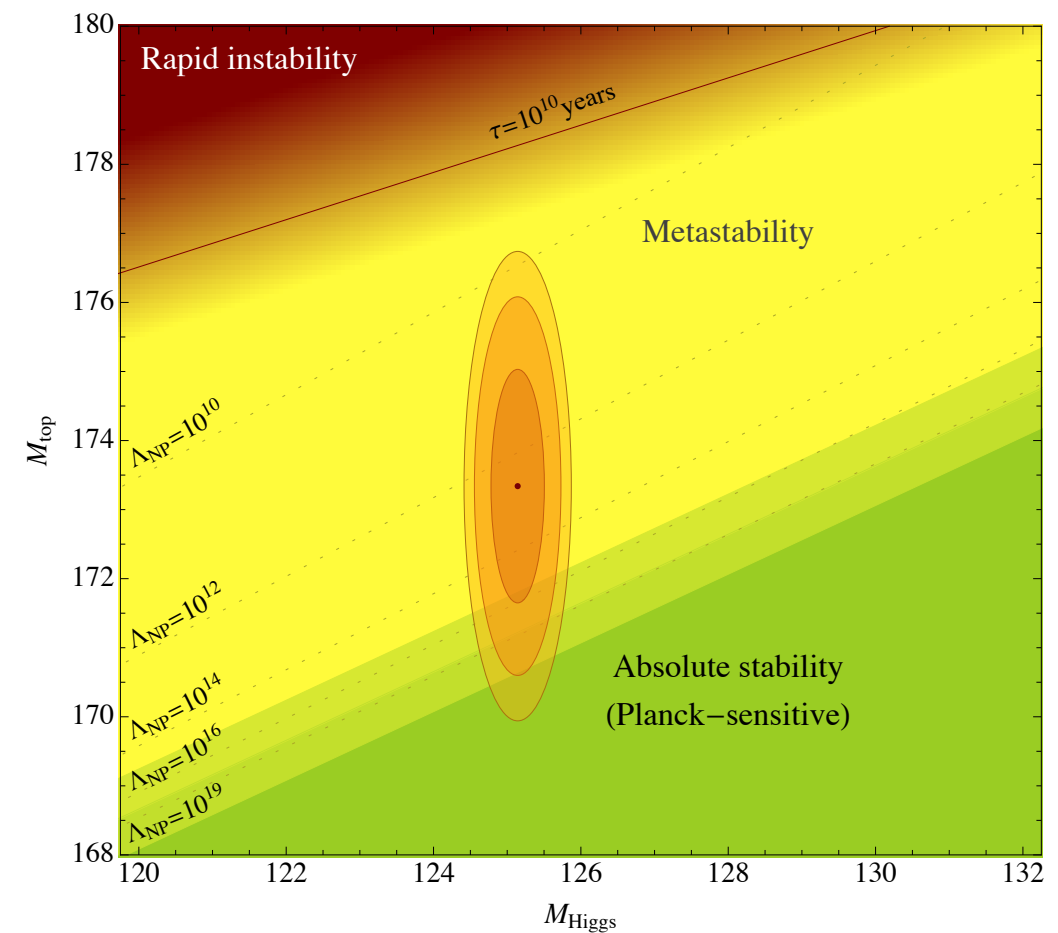
How precisely do we  
know the mass definition?

$$\delta m_t \sim 1 \text{ GeV}$$

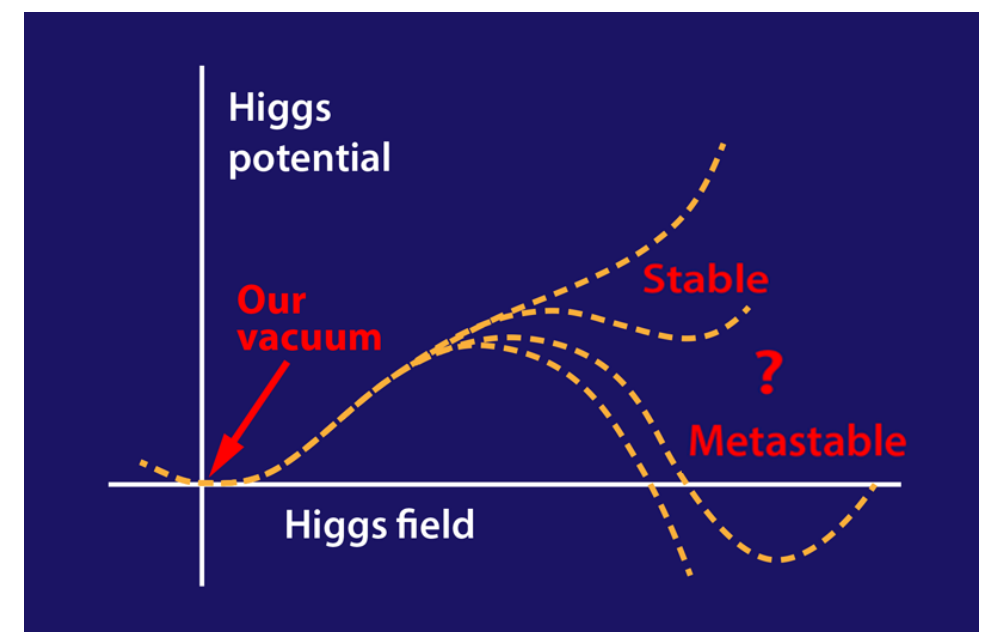


# Why should we care about a precision $m_t$ ?

- Stability of SM vacuum
- Precision electroweak measurements
- LHC searches



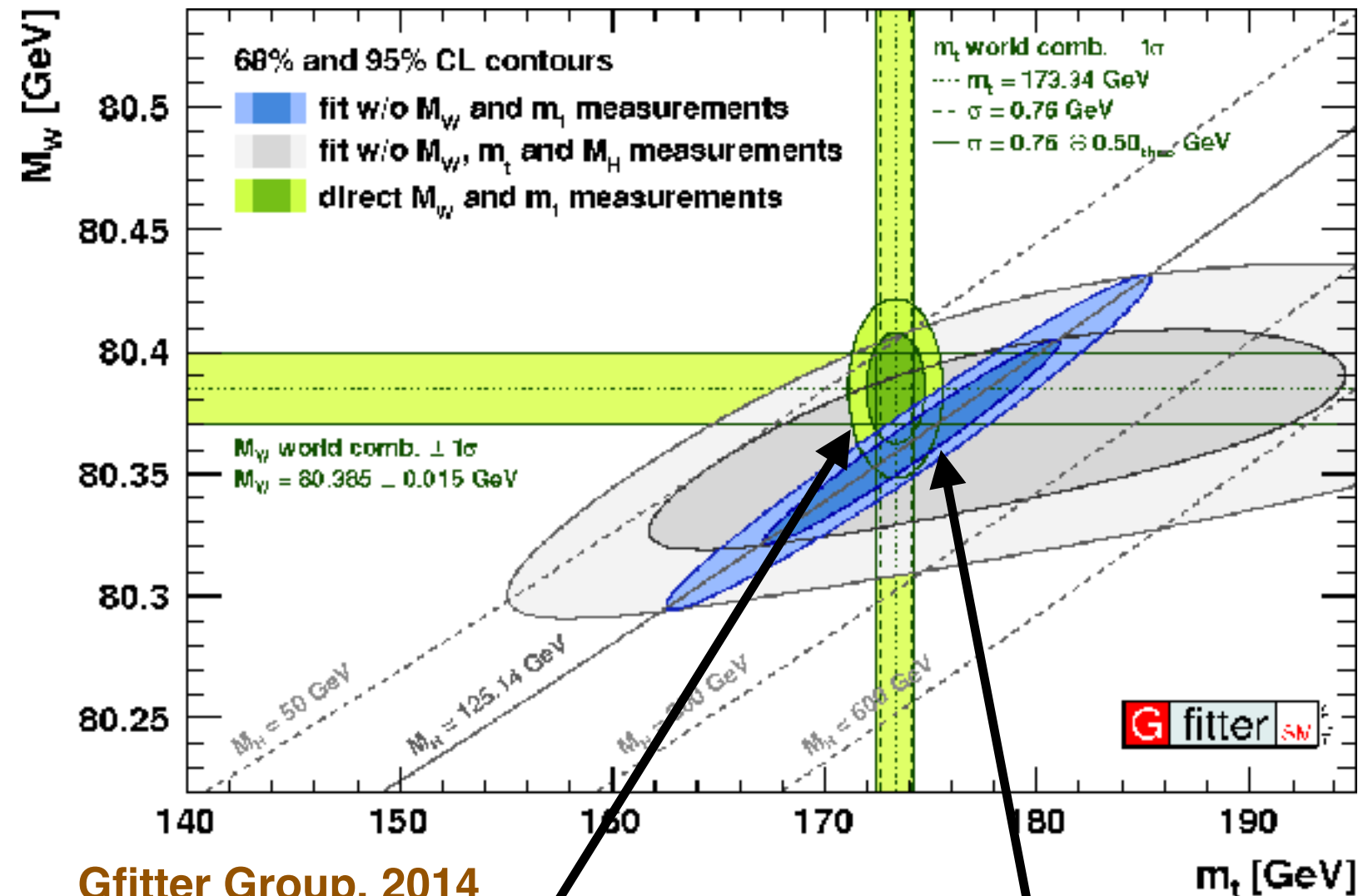
Andreassen, Frost, Schwartz



Butazzo, Degrassi, Giardinio, Giudice, Sala

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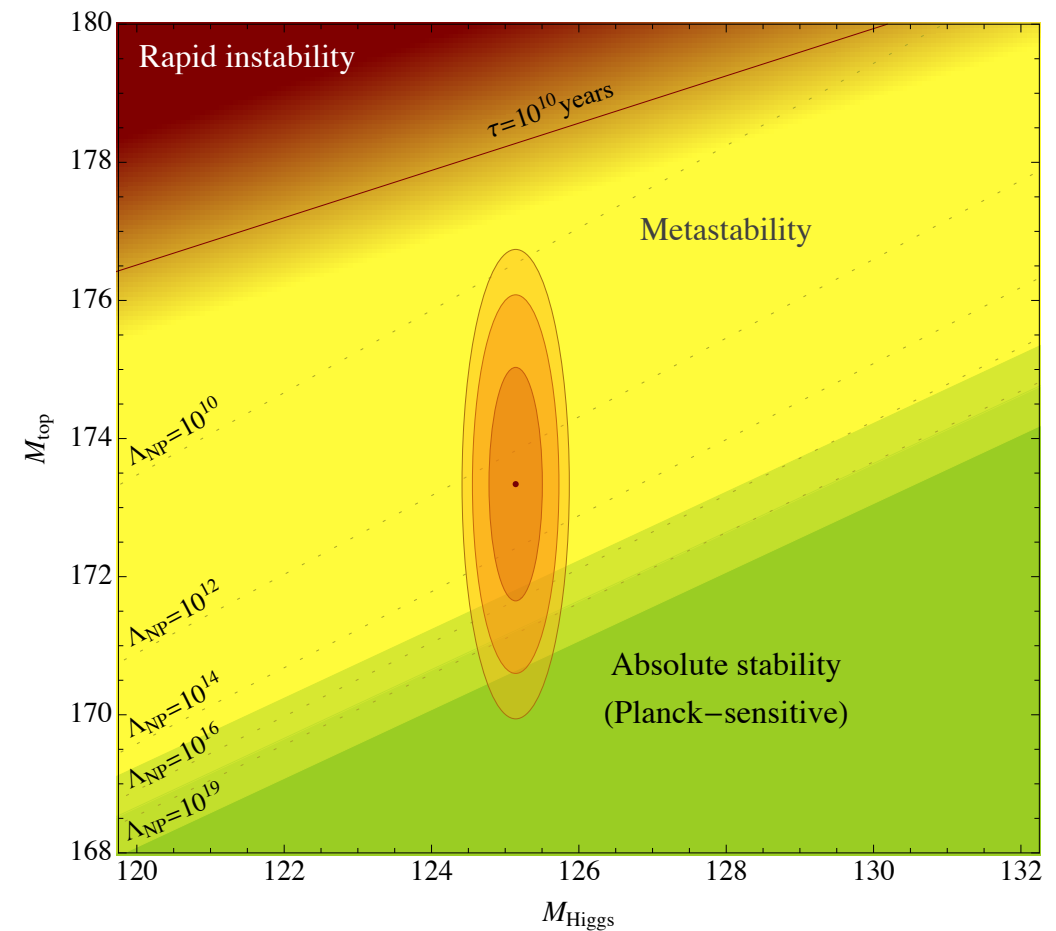


Gfitter Group, 2014

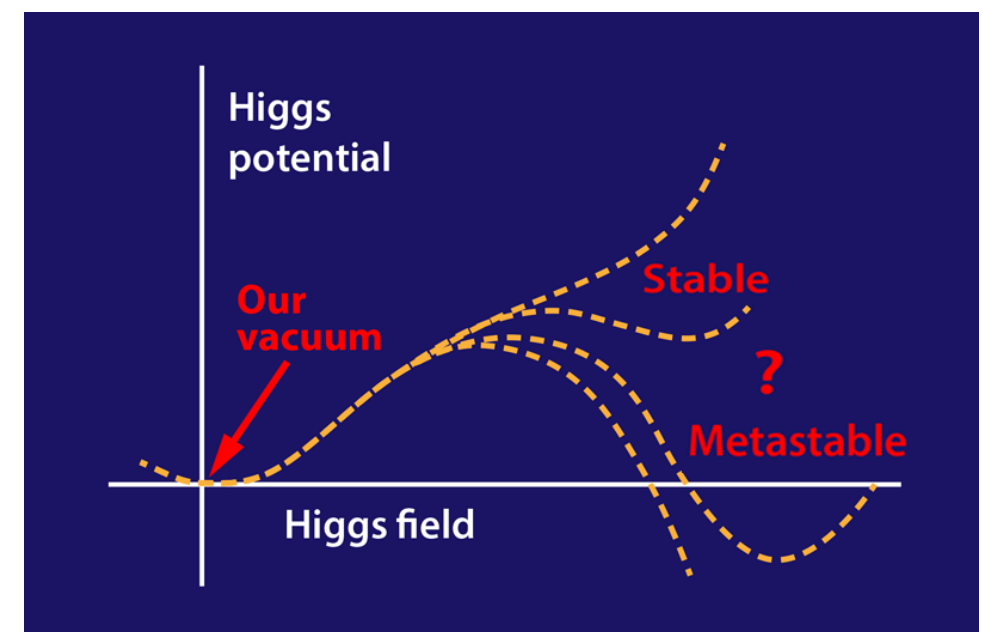
Direct measurements

Indirect Global fit

Significant contribution to uncertainty due to  $m_t$



Andreassen, Frost, Schwartz



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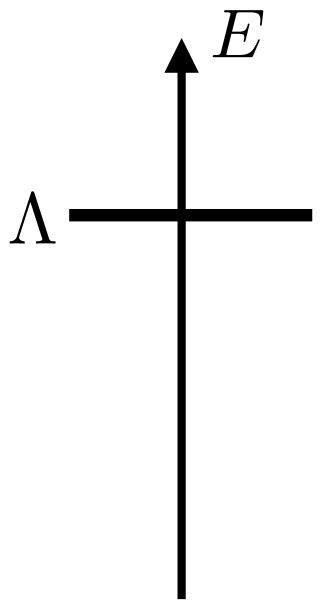
# Outline

- **Overview**
  - Mass renormalization schemes, Monte Carlo mass
  - Theory issues for top jets at the LHC
  - Effective field theories for top jets
- **Top mass determination at the LHC**
  - Soft Drop Grooming on top jets
  - Pythia Studies
  - Pythia and Theory Comparison

# Mass in Quantum Field Theory

Mass in quantum field theory  
gets renormalized and absorbs high  
energy divergences

$$\mathcal{L}^{\text{SM}}(m_t, \alpha_s, \dots, \Lambda)$$

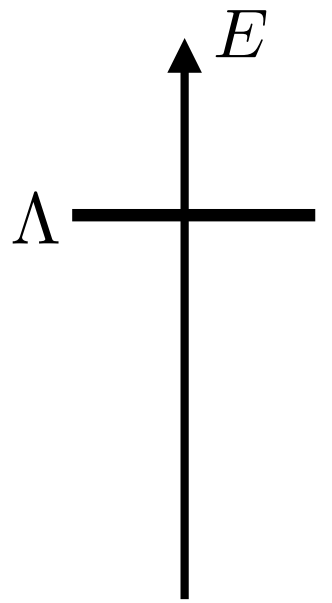


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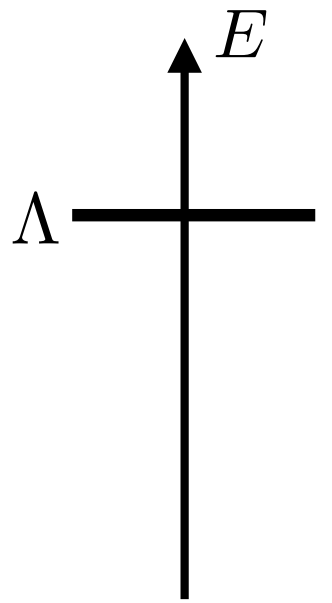
To be able to do more than one calculation and know we are talking about the same parameter requires **giving them a precise definition** (eg. “**top mass scheme**”).



# Mass in Quantum Field Theory

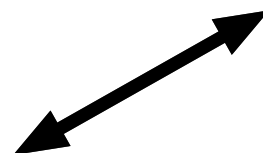
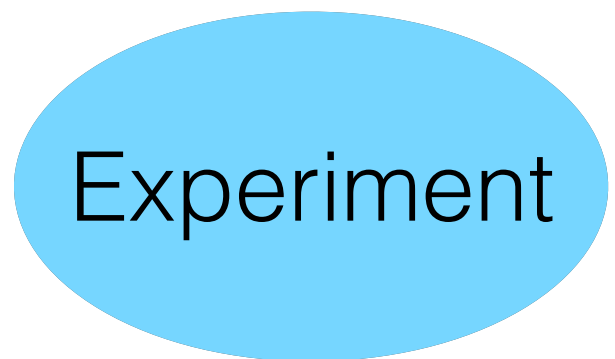
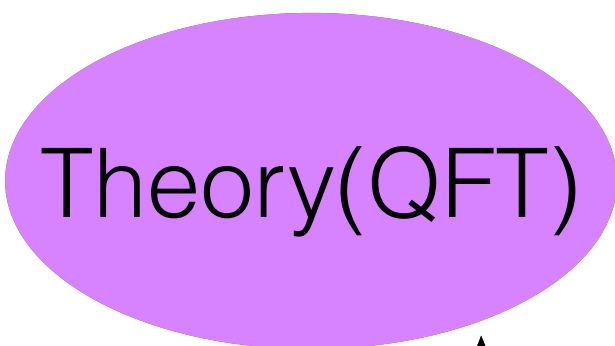
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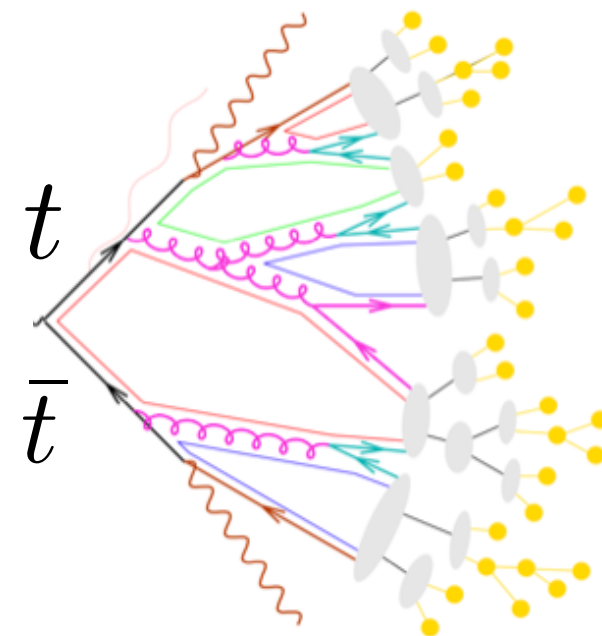


$\mathcal{L} :$   
 $m_t^{\text{pole}}, \bar{m}_t, m_t^{\text{MSR}}, \dots$

To be able to do more than one calculation and know we are talking about the same parameter requires **giving them a precise definition** (eg. “**top mass scheme**”).



Most precise measurements need simulations where it's hard to determine the  $m_t$  definition.

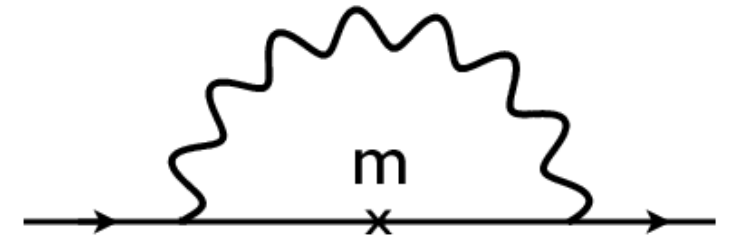


**Hadrons**

# Mass in Quantum Field Theory

$$m^{\text{bare}} \rightarrow m^{\text{bare}} + \Sigma(m^{\text{bare}})$$

$$\Sigma(m) = \frac{3}{4}C_F \frac{\alpha_s}{\pi} m \left( \frac{1}{\epsilon} + \text{finite} \right) + \mathcal{O}(\alpha_s^2)$$

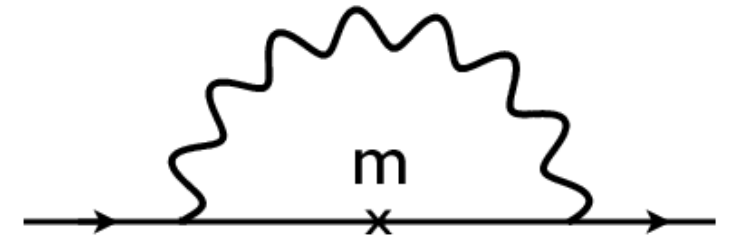


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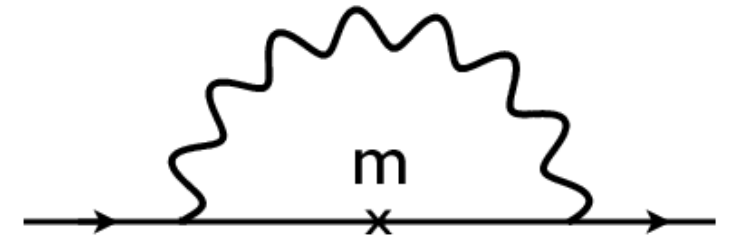
**Pick a renormalization scheme**  $m^{\text{bare}} = m^{\text{ren}} + \delta_m$

- Pole Mass - Remove the full one loop correction  $\Sigma$
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## Choice of scheme can affect accuracy: $b$ decay width example

$$\Gamma(b \rightarrow ue\bar{\nu}) = \frac{G_F^2 |V_{ub}|^2}{192\pi^3} m_b^5 \left[ 1 + \kappa_1 \frac{\alpha_s(m_b)}{\pi} \epsilon + \kappa_2 \frac{\alpha_s^2(m_b)}{\pi^2} \epsilon^2 + \dots \right]$$

$$\Gamma(b \rightarrow ue\bar{\nu}) = \frac{G_F^2 |V_{ub}|^2}{192\pi^3} (m_b^{\text{pole}})^5 \left[ 1 - 0.17\epsilon - 0.13\epsilon^2 + \dots \right]$$

$$\Gamma(b \rightarrow ue\bar{\nu}) = \frac{G_F^2 |V_{ub}|^2}{192\pi^3} (m_b^{\overline{\text{MS}}})^5 \left[ 1 + 0.30\epsilon + 0.19\epsilon^2 + \dots \right]$$

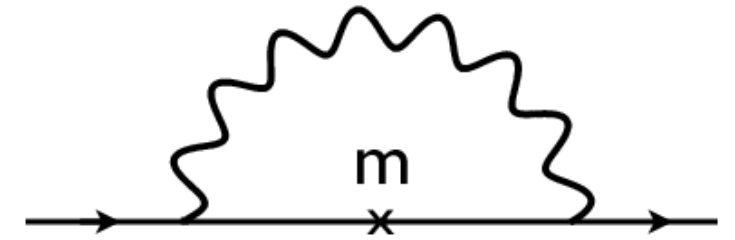
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Hoang, Ligeti, Manohar 1998

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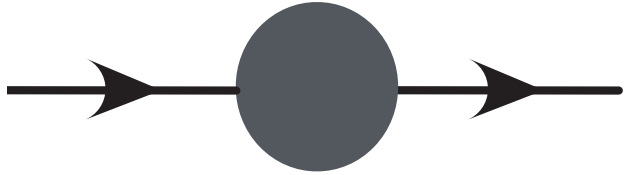
Significant improvement  
from using 1S scheme for  $m_b$   
defined using binding potential  
of bottomonium.

**Hoang, Ligeti, Manohar 1998**



# What makes certain schemes better (worse) than others?

- Pole Mass

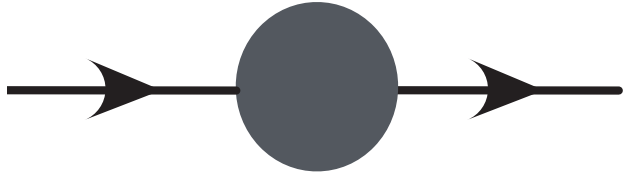
Full propagator:   $\propto \frac{1}{\not{p} - m_t^{\text{pole}}}$  pole at  $m_t$

Like a free particle

Compatible with Breit Wigner

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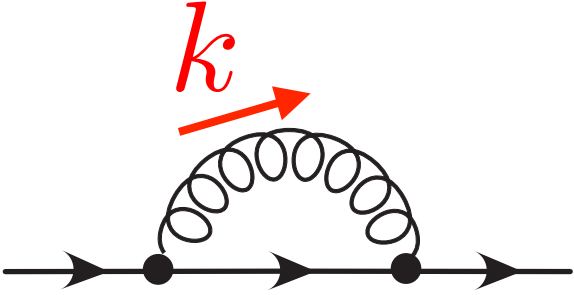
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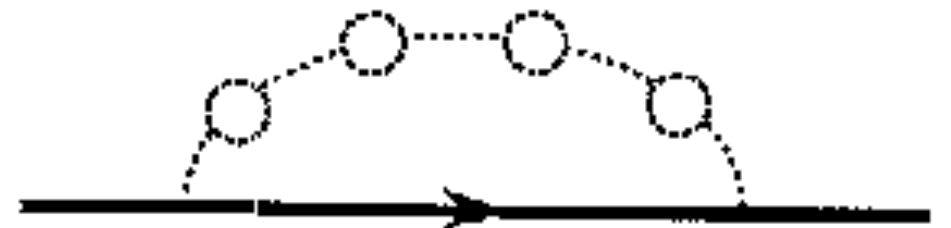
Like a free particle

Compatible with Breit Wigner

Good for electron in QED, but not for quarks.

Factorially diverging series (eg. bubble graphs) leads to an intrinsic uncertainty in the definition of pole mass.

$$\int_0 dk \quad \text{} \quad n! \alpha_s^{n+1}$$

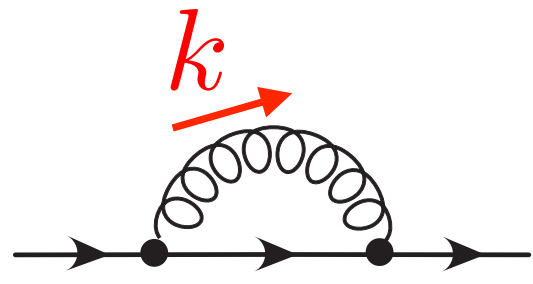


$$\Delta m_t^{\text{pole}} \sim \Lambda_{\text{QCD}}$$

Beneke 1998

# What makes certain schemes better (worse) than others?

- $\overline{\text{MS}}$  Mass  $\overline{m}_t$  No ambiguity ✓

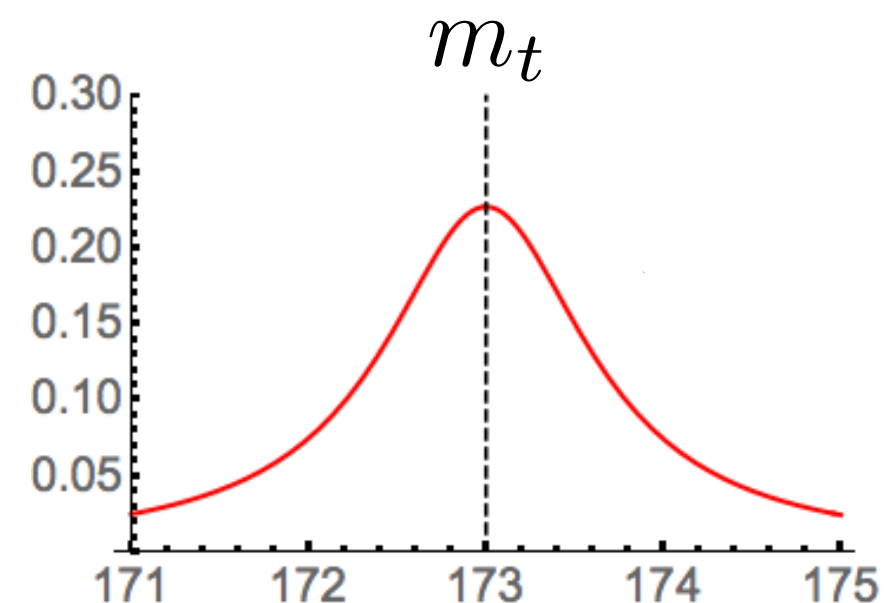
$$\int_{\mu=\overline{m}_t} dk$$


**NOT compatible with Breit Wigner** ✗

$$\frac{\Gamma_t}{[M^2 - m_t[\alpha_s]^2]^2 + \Gamma_t^2 m_t[\alpha_s]^2}$$

$$\sigma^{\text{th}}(m_t, \{Q\}) \rightarrow \int d\hat{s}_t \sigma^{\text{th}}(\hat{s}_t, \{Q\}) \times \frac{\Gamma_t}{[\hat{s}_t^2 - m_t^2]^2 + \Gamma_t^2 m_t^2}$$

$$\sigma^{\text{LO}} \rightarrow \sigma^{\text{NLO}}, \quad \overline{m}_t \rightarrow \overline{m}_t + \delta\overline{m}_t$$



**Need to expand BW in  $\delta m/m$**

$$m_t^{\text{pole}} = \overline{m}_t + \underbrace{0.4 \alpha_s \overline{m}_t}_{\text{shift}} + \dots$$

Swamps the Breit Wigner

$$7 \text{ GeV} \gg \Gamma_t = 1.4 \text{ GeV}$$

# What makes certain schemes better (worse) than others?

- MSR Mass

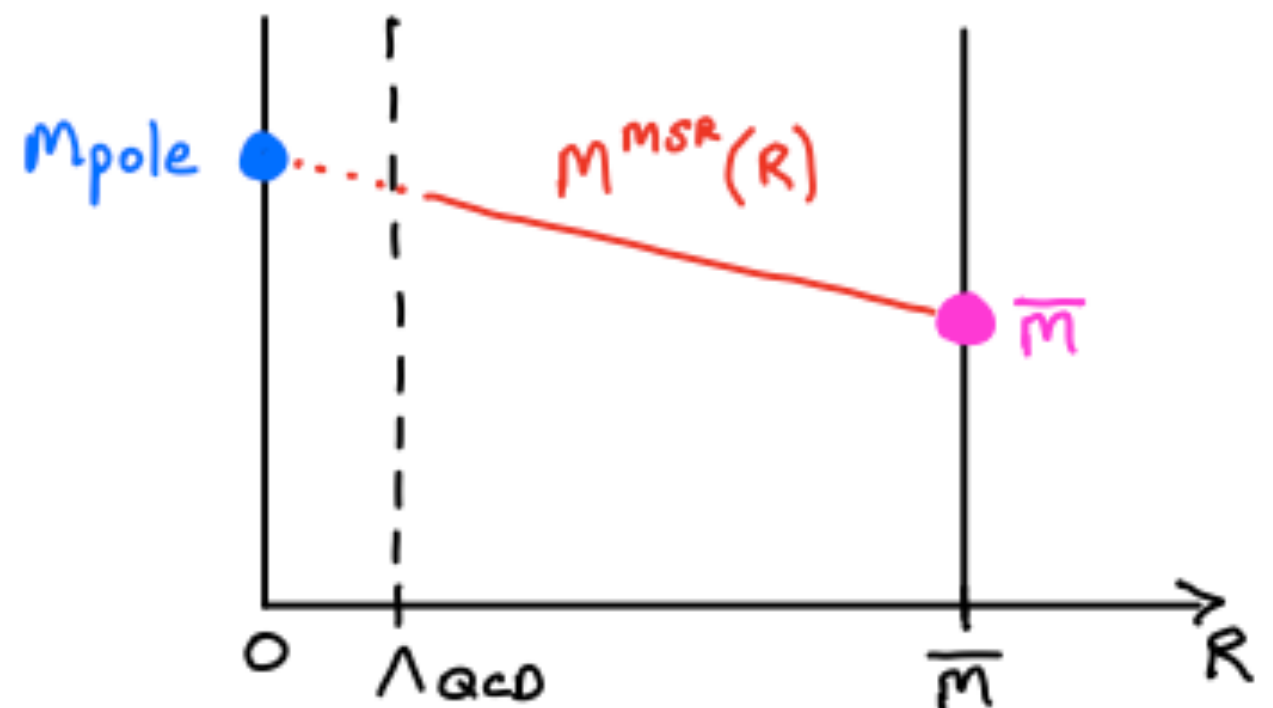
Define using  $\overline{\text{MS}}$  coefficients  $a_{nk}$   $m_t^{\text{pole}} = m_t(R, \mu) + \delta m_t(R, \mu)$

$$\delta m_t(R, \mu) = R \sum_{n=1}^{\infty} \sum_{k=0}^n a_{nk} \left[ \frac{\alpha_s(\mu)}{4\pi} \right] \ln^k \left( \frac{\mu}{R} \right)$$

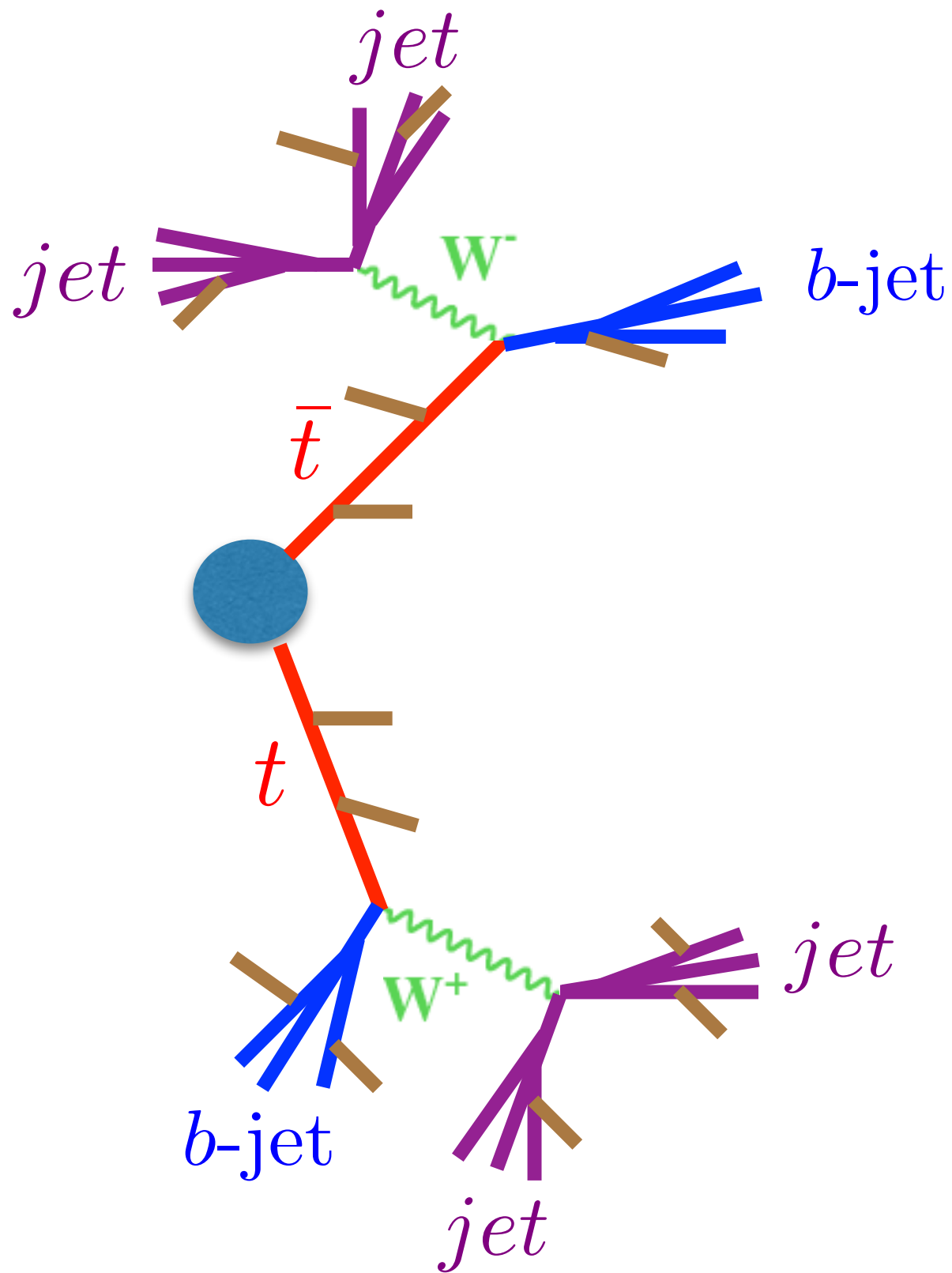
No ambiguity,  $R > \Lambda_{\text{QCD}}$  ✓

Compatible with Breit Wigner,  $R \sim \Gamma_t$  ✓

Nicely interpolates



# Direct Reconstruction Methods (Tevatron and LHC)



**Kinematic Fit:**

$$m_t^2 = p_t^2 = (p_{Jb} + p_{J1} + p_{J2})^2$$

# Direct Reconstruction Methods (Tevatron and LHC)

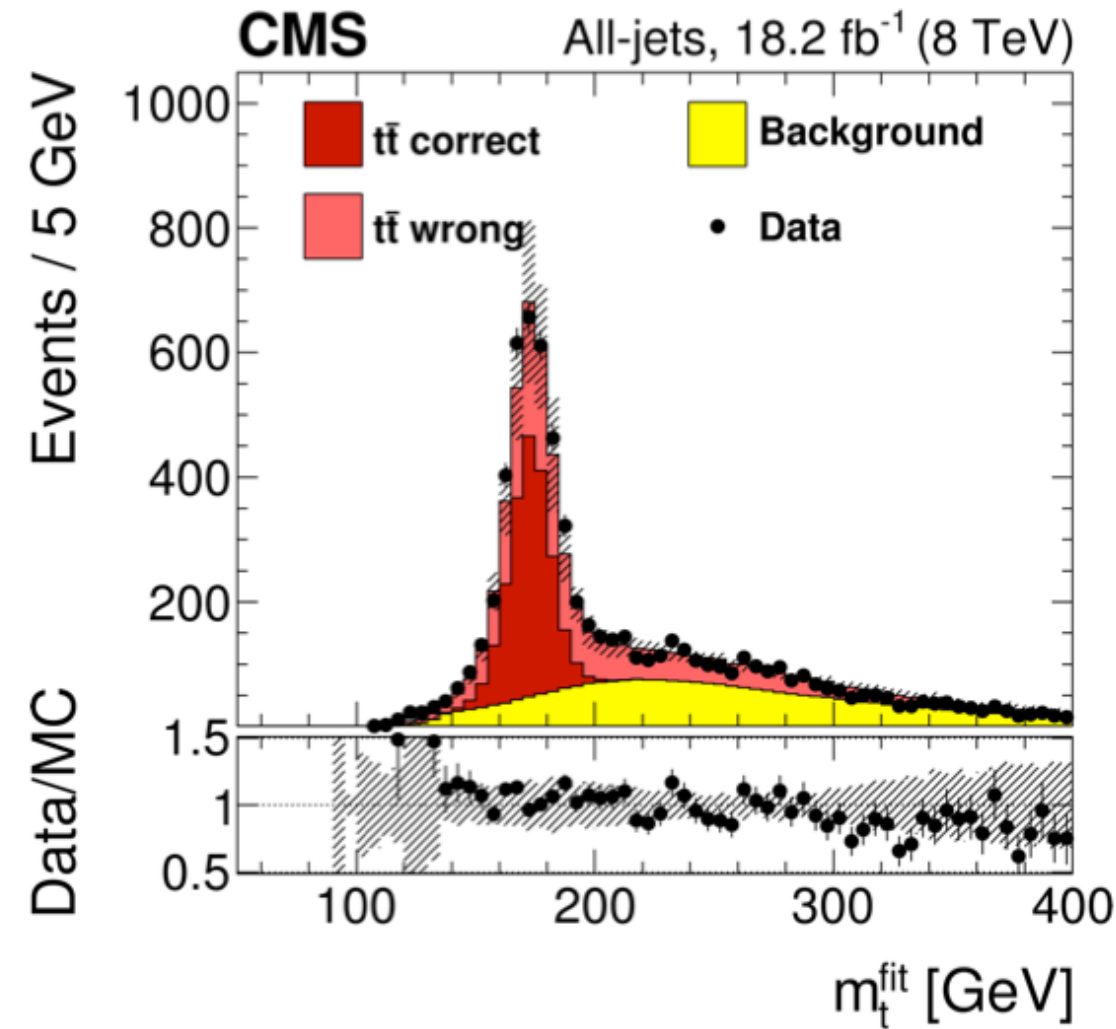
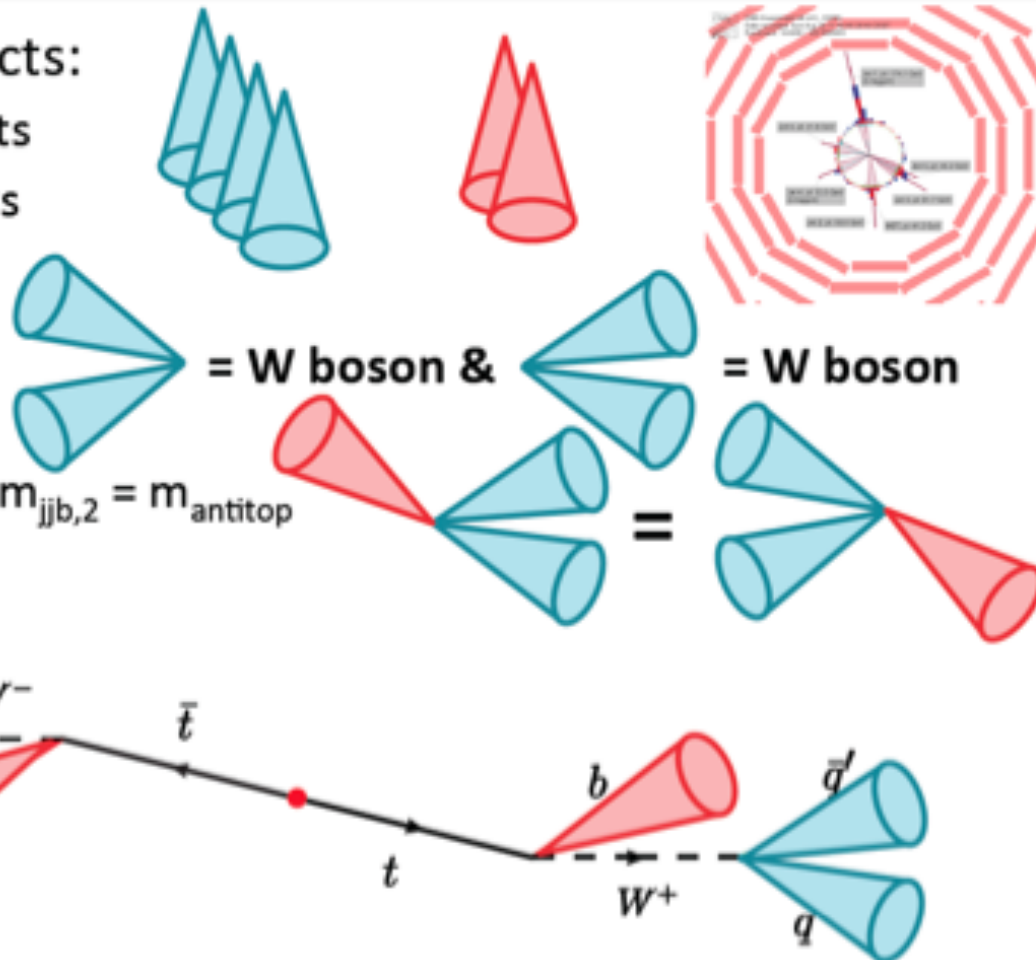
## Kinematic Fit

### Selected objects:

- 4 untagged jets
- 2 b-tagged jets

### Constraints:

- $2 \times m_{jj} = m_W$
- $m_{\text{top}} = m_{jjb,1} = m_{jjb,2} = m_{\text{antitop}}$



*all-jets channel at 8 TeV*

**Use Monte Carlo simulations for templates.**

**Determine the best fit value of MC top mass parameter:**

**CMS Run 1 (2015):  $m_t = 172.44 \pm 0.49$  GeV**

# Direct Reconstruction Methods (Tevatron and LHC)

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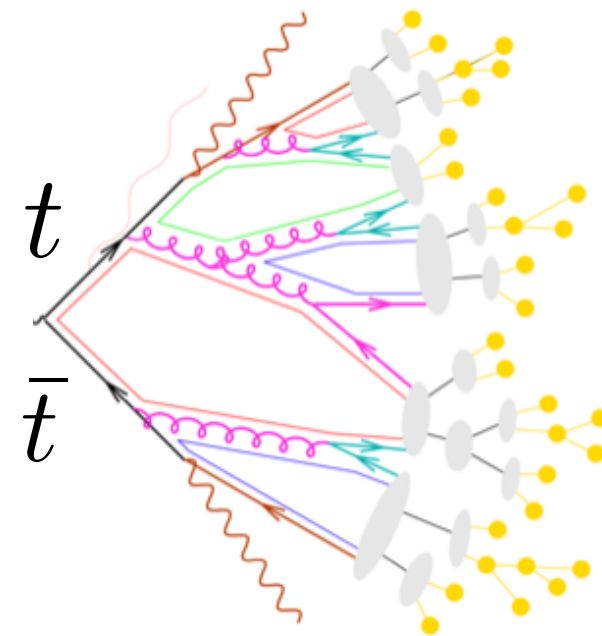
$$m_t^{\text{pole}}, \bar{m}_t, m_t^{\text{MSR}}, \dots$$

Theory(QFT)

Experiment

Simulation  
(Monte Carlo)

$$m_t^{\text{MC}}$$



Hadrons

$$\Lambda^{\text{shower}} = 1 \text{ GeV}$$

No ambiguity ✓

Compatible with Breit Wigner ✓

Definition?

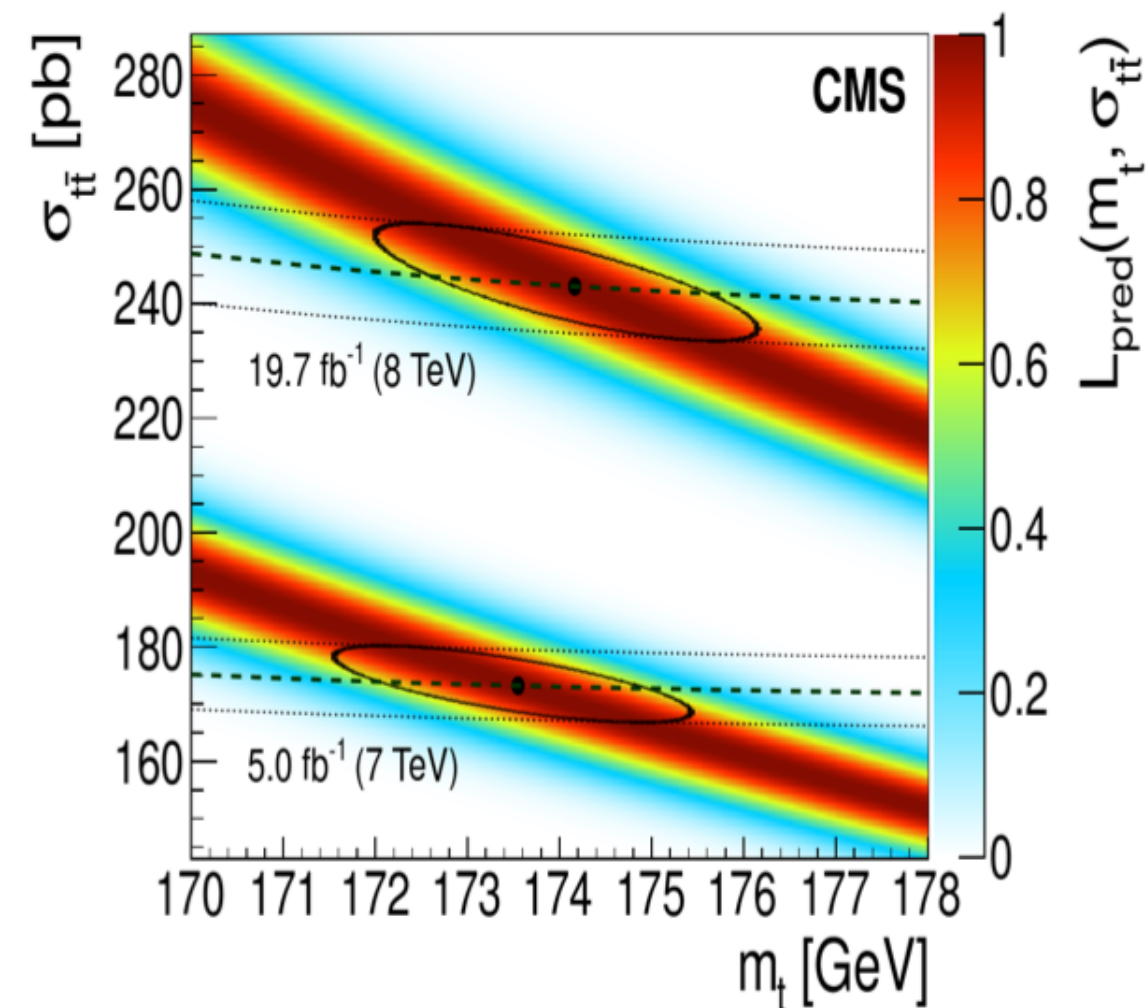


# Direct comparison of theory and experiment

eg. Pole mass from Total Cross Section

$$\sigma^{\text{exp}}(pp \rightarrow t\bar{t}) = \sigma_{t\bar{t}}^{\text{th}}(m_t)$$

CMS arXiv:1603.02303



	$m_t$ [ GeV ]
NNPDF3.0	$173.8^{+1.7}_{-1.8}$
MMHT2014	$174.1^{+1.8}_{-2.0}$
CT14	$174.3^{+2.1}_{-2.2}$

$m_t^{\text{pole}}, \bar{m}_t, m_t^{\text{MSR}}, \dots$

Czakon, Fielder, Mitov (13)

Theory(QFT)



Experiment

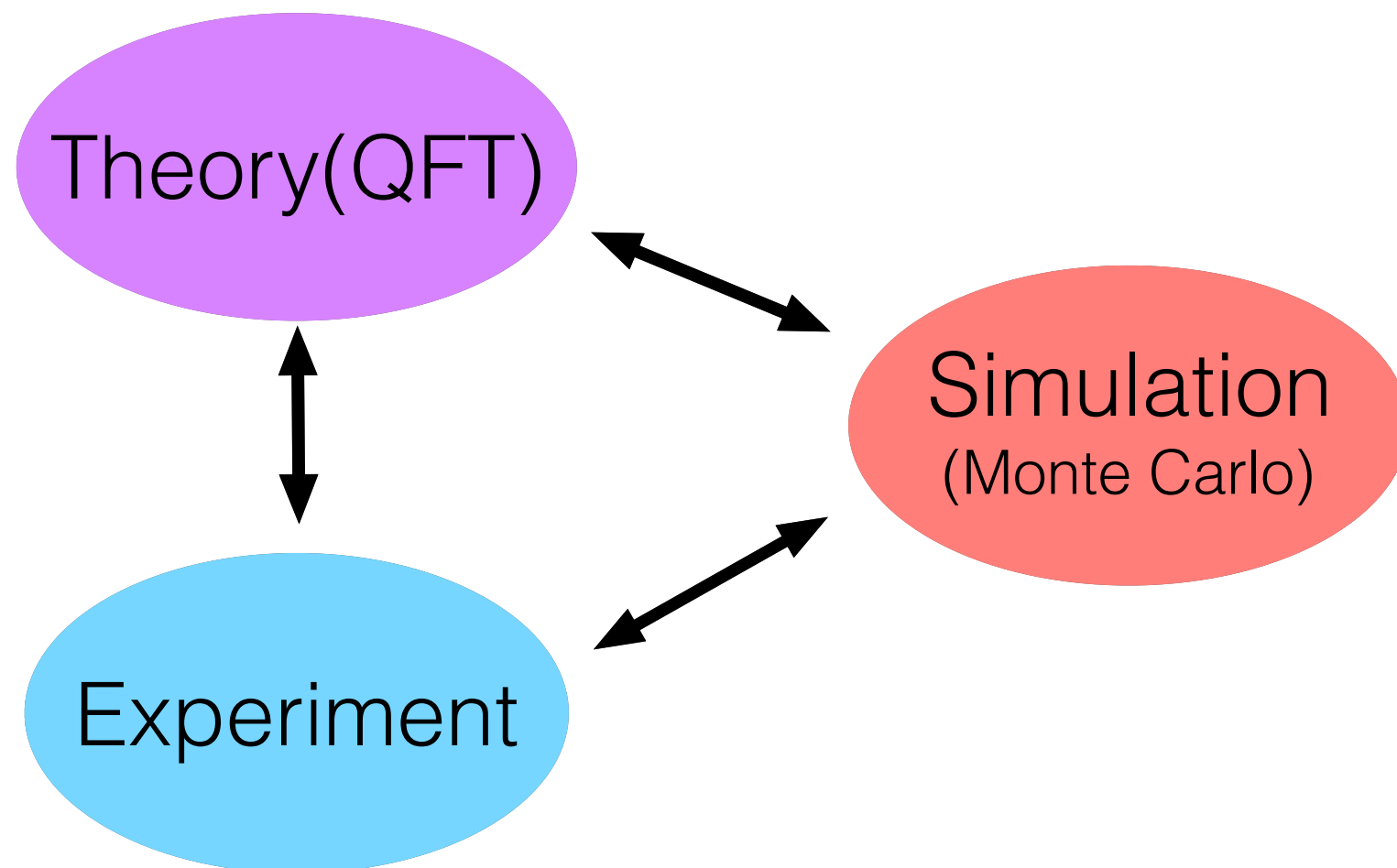
Simulation  
(Monte Carlo)



# Improving Top Mass Measurement at the LHC

- Use kinematically sensitive LHC observable
- Theoretically tractable in QFT
- Control Contamination

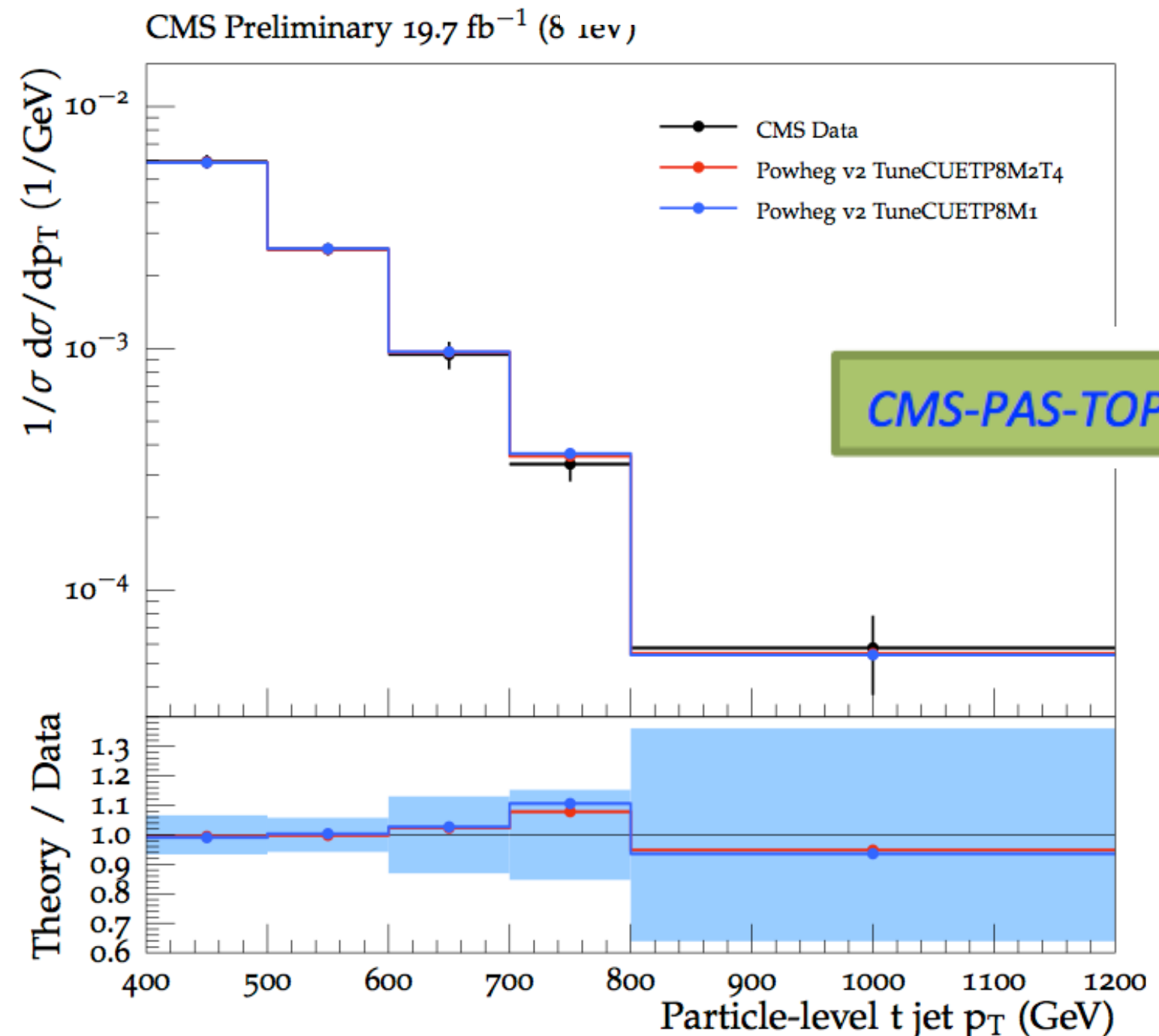
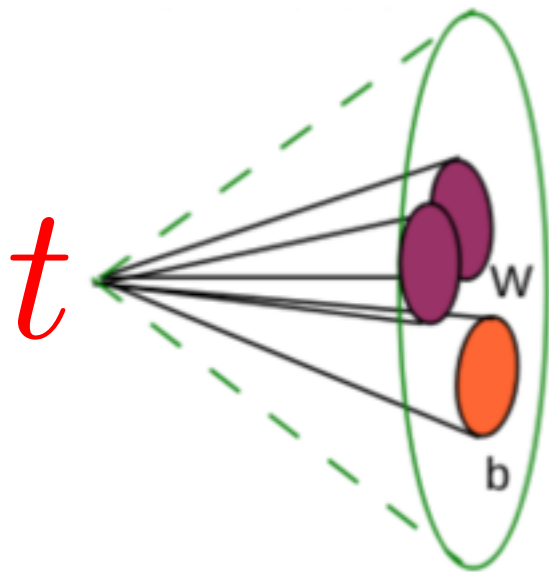
$$M_t^{\text{peak}} = m_t + (\text{nonperturbative effects}) + (\text{perturbative effects})$$



# First Simplification: Boosted Top Quarks

Enables us to be inclusive over decay products.

$$Q = 2p_T \gg m_t$$

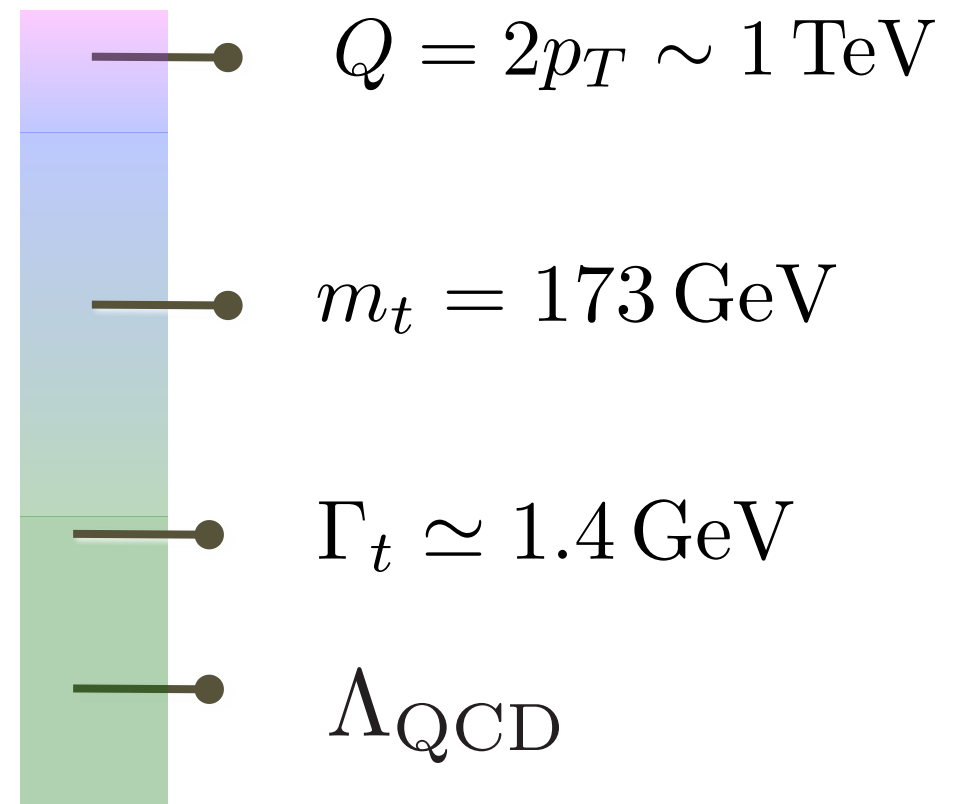


# Theory issues for $pp \rightarrow t\bar{t}$

- jet observable
- suitable top mass for jets
- initial state radiation
- final state radiation
- underlying event/ MPI
- color reconnection
- beam remnant
- parton distributions
- sum large logs

$$Q \gg m_t \gg \Gamma_t \gg \Lambda_{\text{QCD}}$$

Production Energy



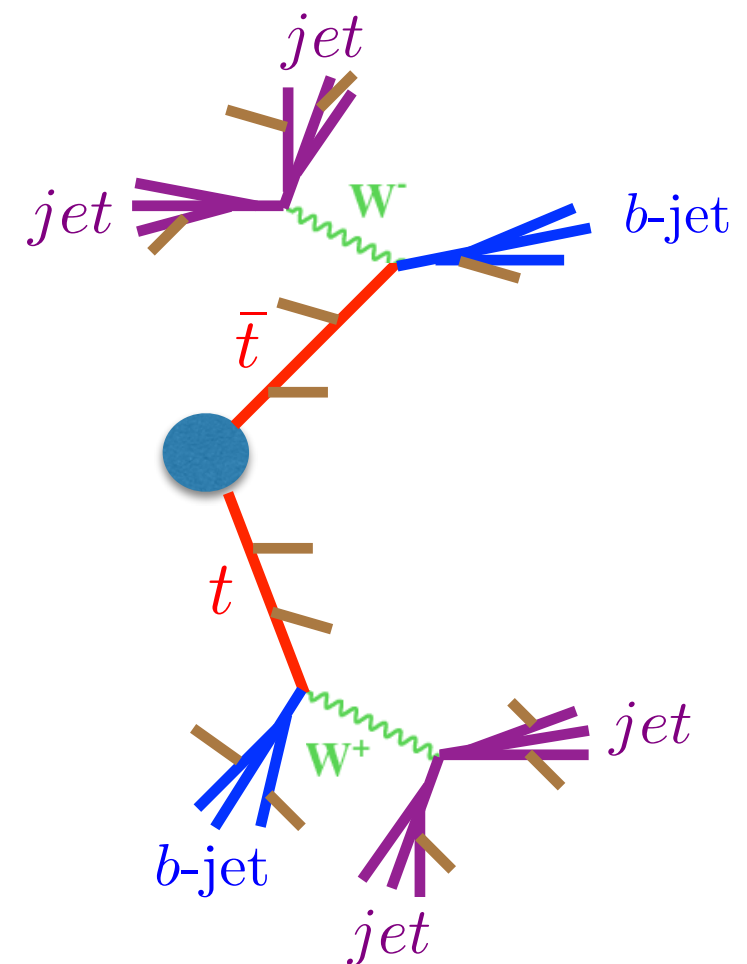
# Issues relevant for lepton colliders

- jet observable ★ ★
- suitable top mass for jets ★
- initial state radiation
- final state radiation ★
- underlying event/ MPI
- color reconnection
- beam remnant
- parton distributions
- sum large logs ★

$$Q \gg m_t \gg \Gamma_t \gg \Lambda_{\text{QCD}}$$

First

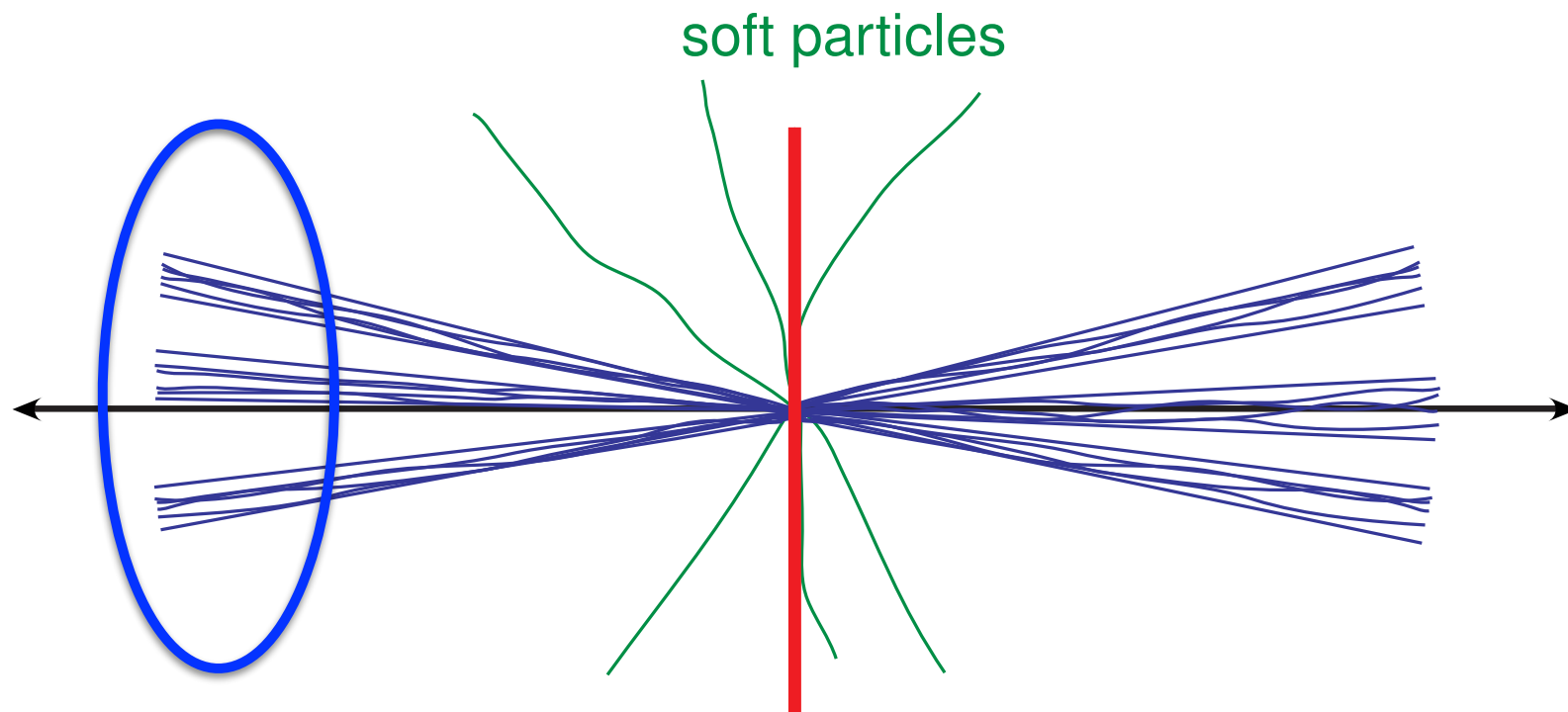
$e^+e^- \rightarrow t\bar{t}X$   
and the issues ★



# Measure what observable?

## Jet Invariant Mass

$$M_t^2 = \left( \sum_{i \in a} p_i^\mu \right)^2$$



**Jet of Radius R**

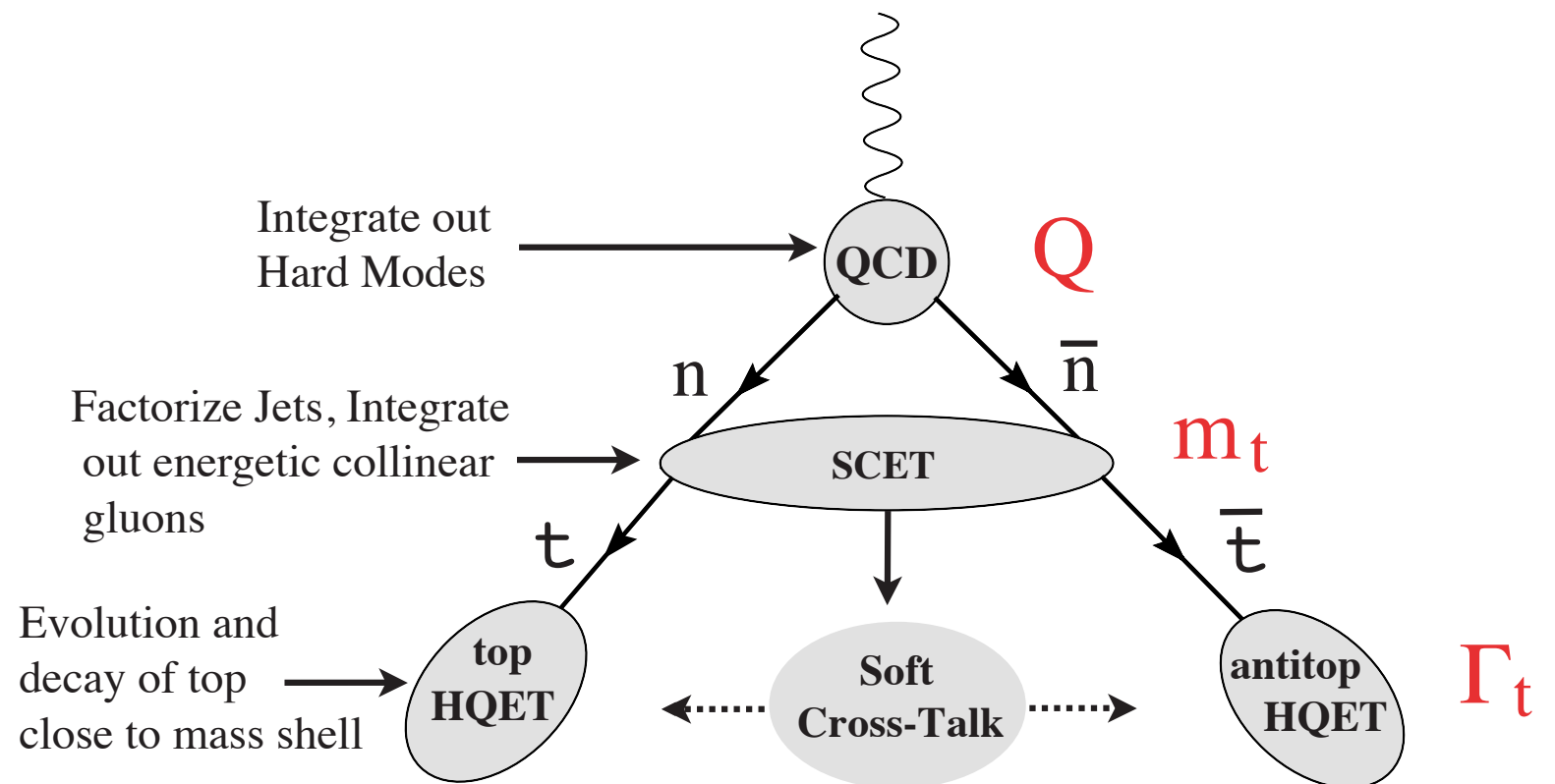
# EFTs for Boosted Tops in the Peak Region

$$e^+e^- \rightarrow t\bar{t}$$

$$\frac{d^2\sigma}{dM_t^2 dM_{\bar{t}}^2}$$

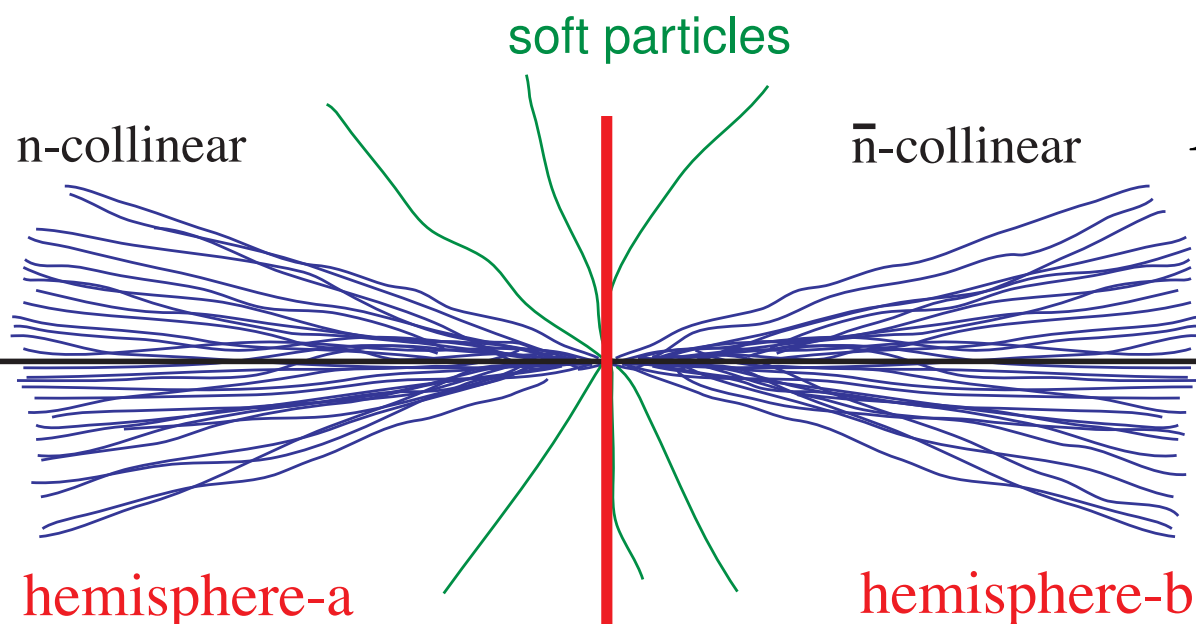
**Peak Region:**

$$M_{t,\bar{t}}^2 - m^2 \sim m\Gamma \ll m^2$$



**Fleming, Hoang, Mantry, Stewart 2007**

$$M_t^2 = \left( \sum_{i \in a} p_i^\mu \right)^2$$



$$M_{\bar{t}}^2 = \left( \sum_{i \in b} p_i^\mu \right)^2$$

# Factorized Cross Section

$$\left(\frac{d\sigma}{dM_t^2 dM_{\bar{t}}^2}\right)_{\text{hemi}} = \sigma_0 H_Q(Q, \mu_m) H_m\left(m_J, \frac{Q}{m_J}, \mu_m, \mu\right) \\ \times \int dl^+ dl^- J_B\left(\hat{s}_t - \frac{Ql^+}{m_J}, \Gamma_t, \delta m, \mu\right) J_B\left(\hat{s}_{\bar{t}} - \frac{Ql^-}{m_J}, \Gamma_{\bar{t}}, \delta m, \mu\right) \\ \times S_{\text{hemi}}(l^+ - k, l^- - k', \mu) F(k, k')$$

(boosted HQET)  
Jet Functions

Evolution and decay of top  
quark close to mass shell

Soft Function

Perturbative Cross talk

Hadronization

Control Over Mass Scheme

# Factorized Cross Section

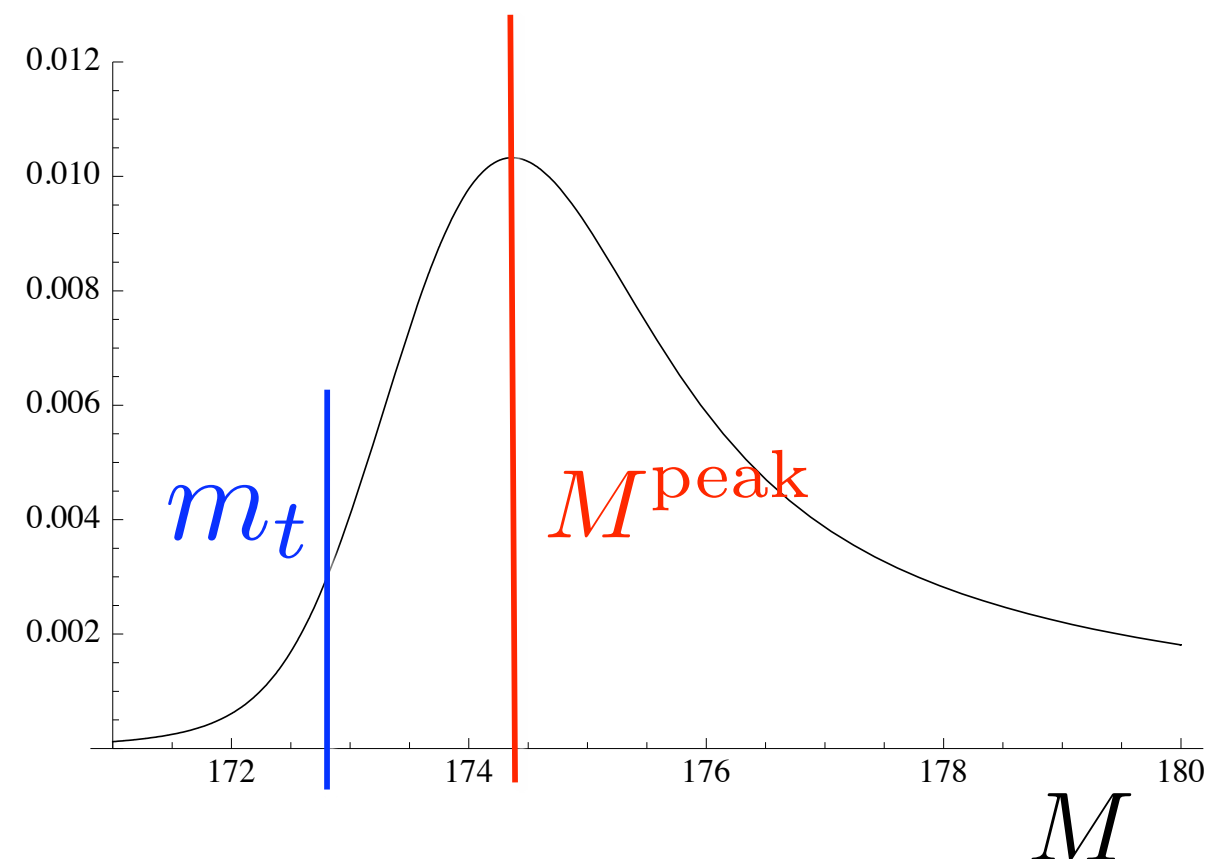
$$\left(\frac{d\sigma}{dM_t^2 dM_{\bar{t}}^2}\right)_{\text{hemi}} = \sigma_0 H_Q(Q, \mu_m) H_m\left(m_J, \frac{Q}{m_J}, \mu_m, \mu\right) \\ \times \int dl^+ dl^- J_B\left(\hat{s}_t - \frac{Ql^+}{m_J}, \Gamma_t, \delta m, \mu\right) J_B\left(\hat{s}_{\bar{t}} - \frac{Ql^-}{m_J}, \Gamma_t, \delta m, \mu\right) \\ \times S_{\text{hemi}}(l^+ - k, l^- - k', \mu) F(k, k')$$

$$M^{\text{peak}} = m_t + \Gamma_t(\alpha_s + \alpha_s^2 + \dots) + \frac{Q\Lambda_{\text{QCD}}}{m_t}$$

**measure this** **extract this**

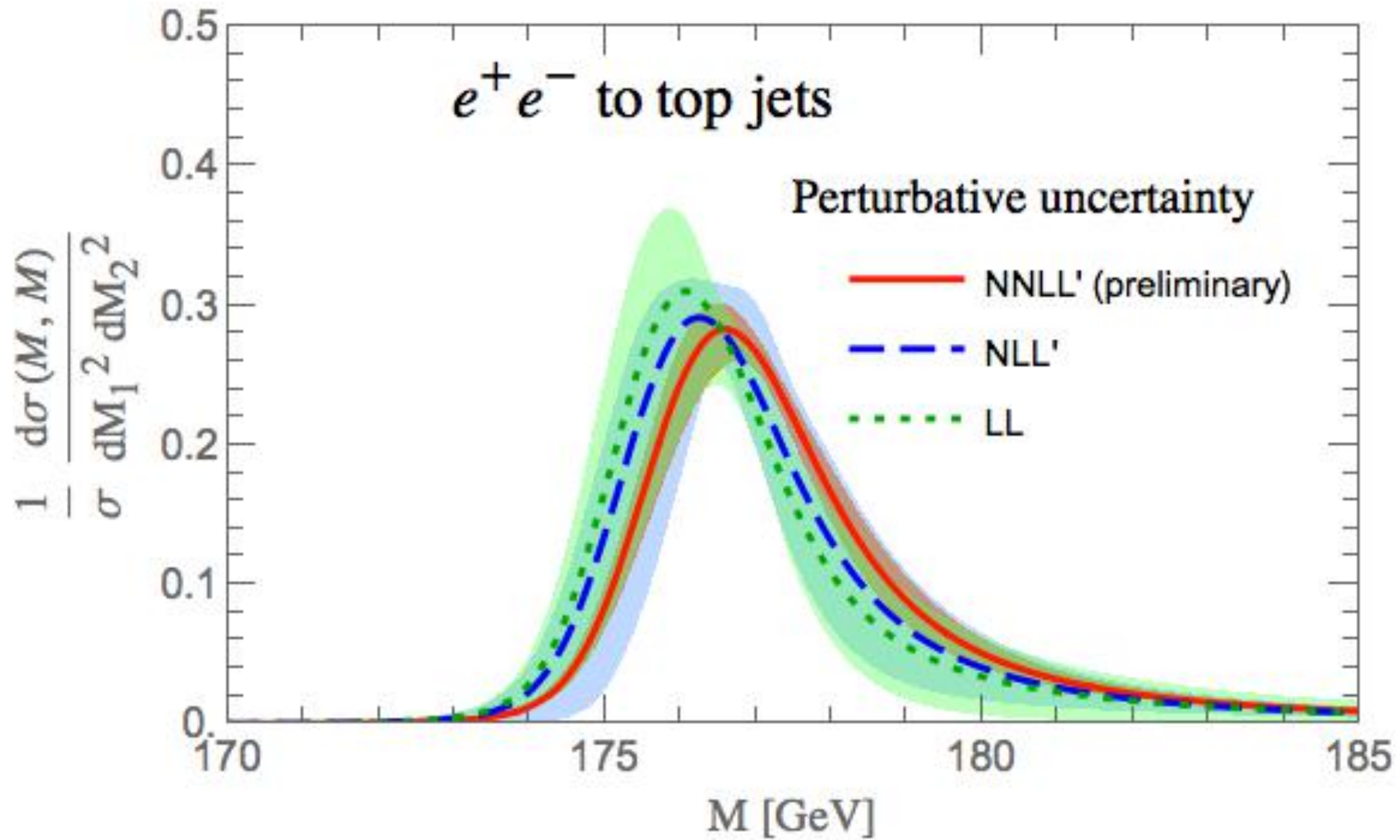
$$\hat{s}_t \equiv \frac{M_t^2 - m^2}{m} \sim \Gamma \ll m$$

$$\frac{d\sigma}{dM}$$

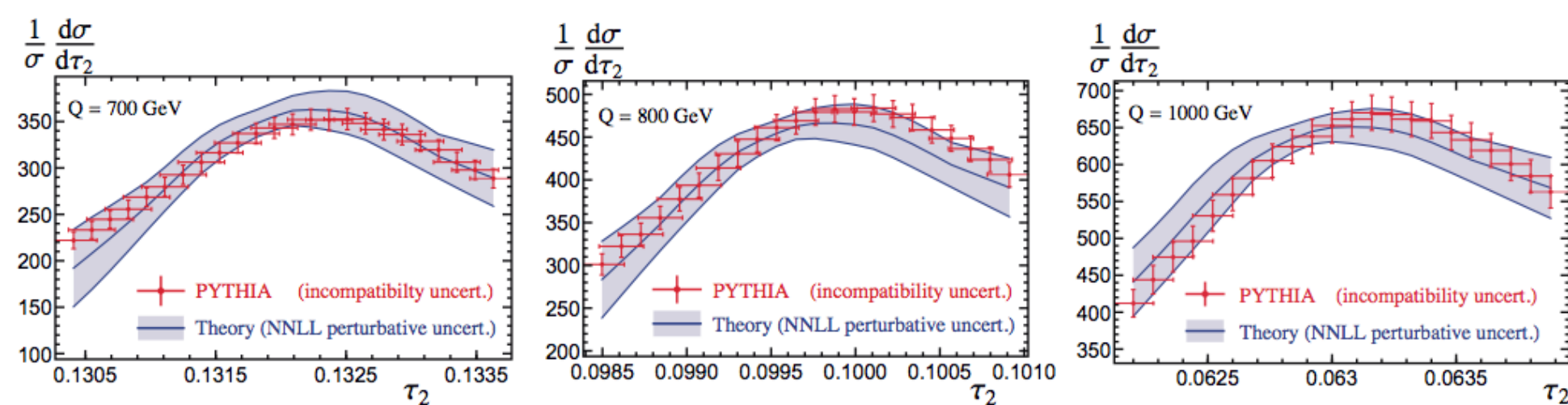




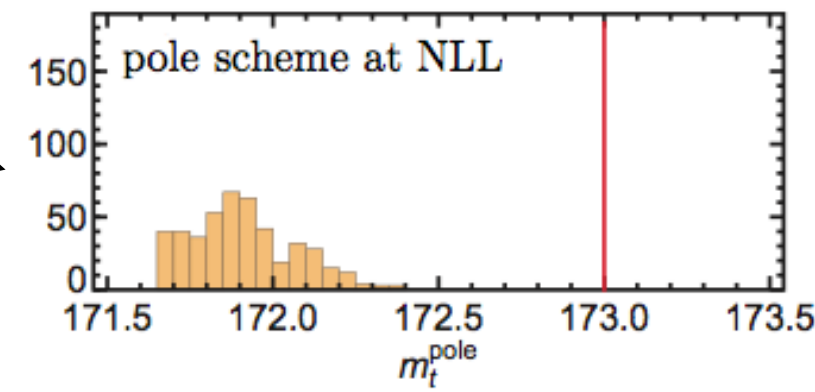
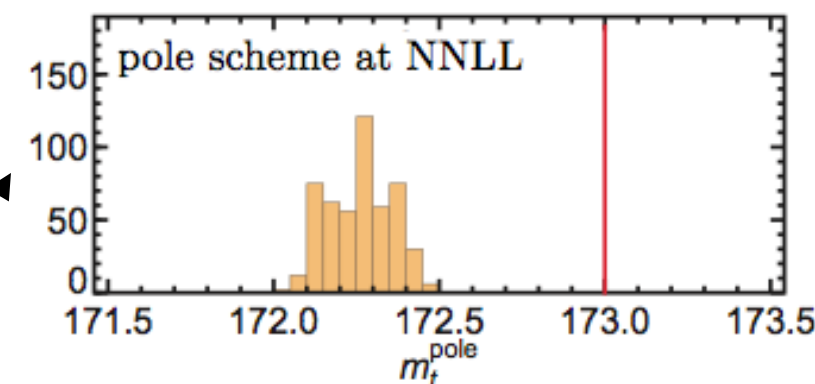
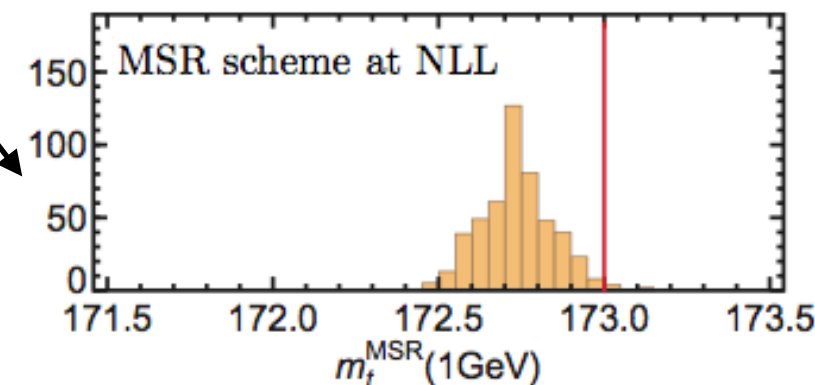
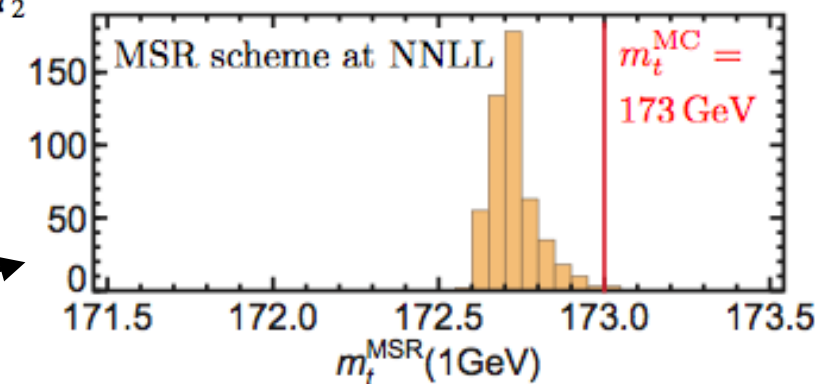
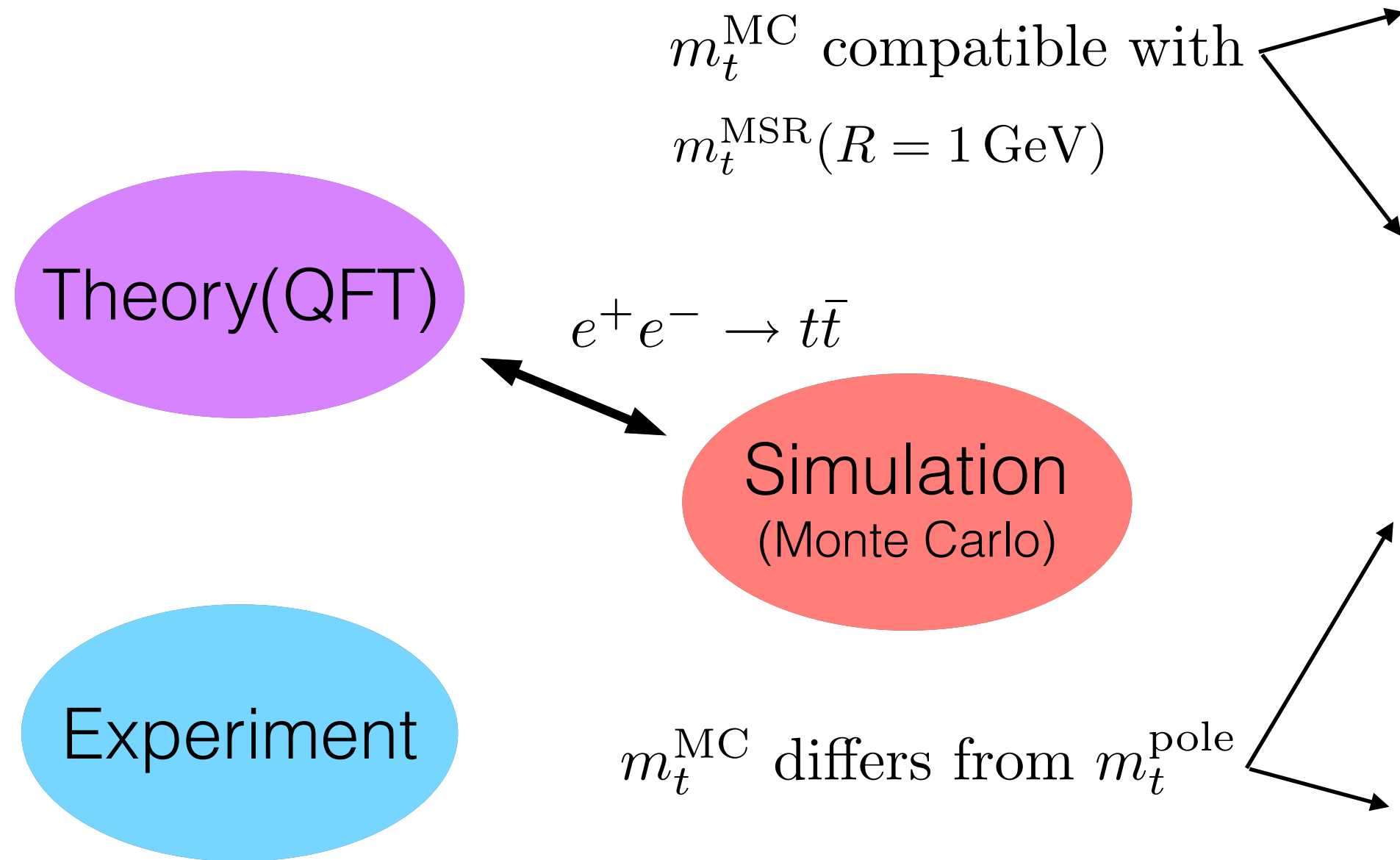
# Factorized Cross Section at NNLL+O( $\alpha_s^2$ )



To appear soon




# Top Mass Calibration of Monte Carlo



# Top Mass Determination at the LHC

**A. Hoang, S. Mantry, AP, I. Stewart**

# Theory issues for $pp \rightarrow t\bar{t}$

- jet observable ★ ★ **Jet Mass in Jet of Radius R**
  - suitable top mass for jets ★
  - initial state radiation ★
  - final state radiation ★
  - underlying event/ MPI  **“Contamination”**
  - color reconnection ★
  - beam remnant ★ **Jet Veto**
  - parton distributions ★ **Multiple Channels**
  - sum large logs  $Q \gg m_t \gg \Gamma_t \gg \Lambda_{\text{QCD}}$  ★
- Factorization for  $e^+ e^-$  can be extended to pp to account for issues with ★

# Factorization for $pp \rightarrow t\bar{t}$

Can be extended to pp using 2-jettiness. A. Hoang, S. Mantry, AP, I. Stewart

(Stewart, Tackmann, Waalewijn)

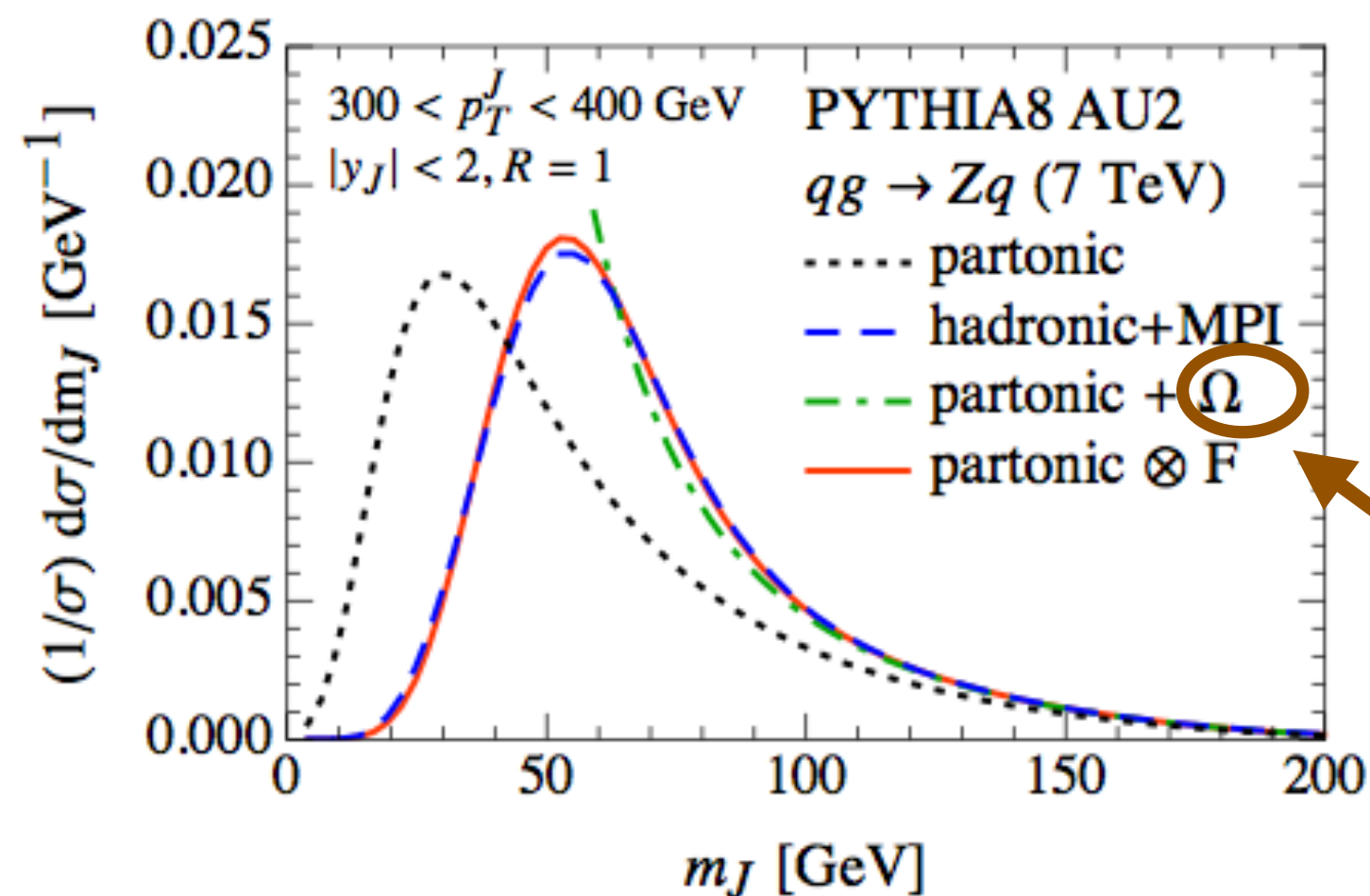
$$\frac{d^2\sigma}{dM_{J_1}^2 dM_{J_2}^2 d\mathcal{T}^{\text{cut}}} = \text{tr} \left[ \hat{H}_{Q_m} \hat{S}(\mathcal{T}^{\text{cut}}, R, \dots) \otimes F \right] \otimes J_B \otimes J_B \otimes \mathcal{I} \otimes f f$$

Jet Veto in  
Beam Region

Same Jet Functions!

Initial State Radiation

PDFs



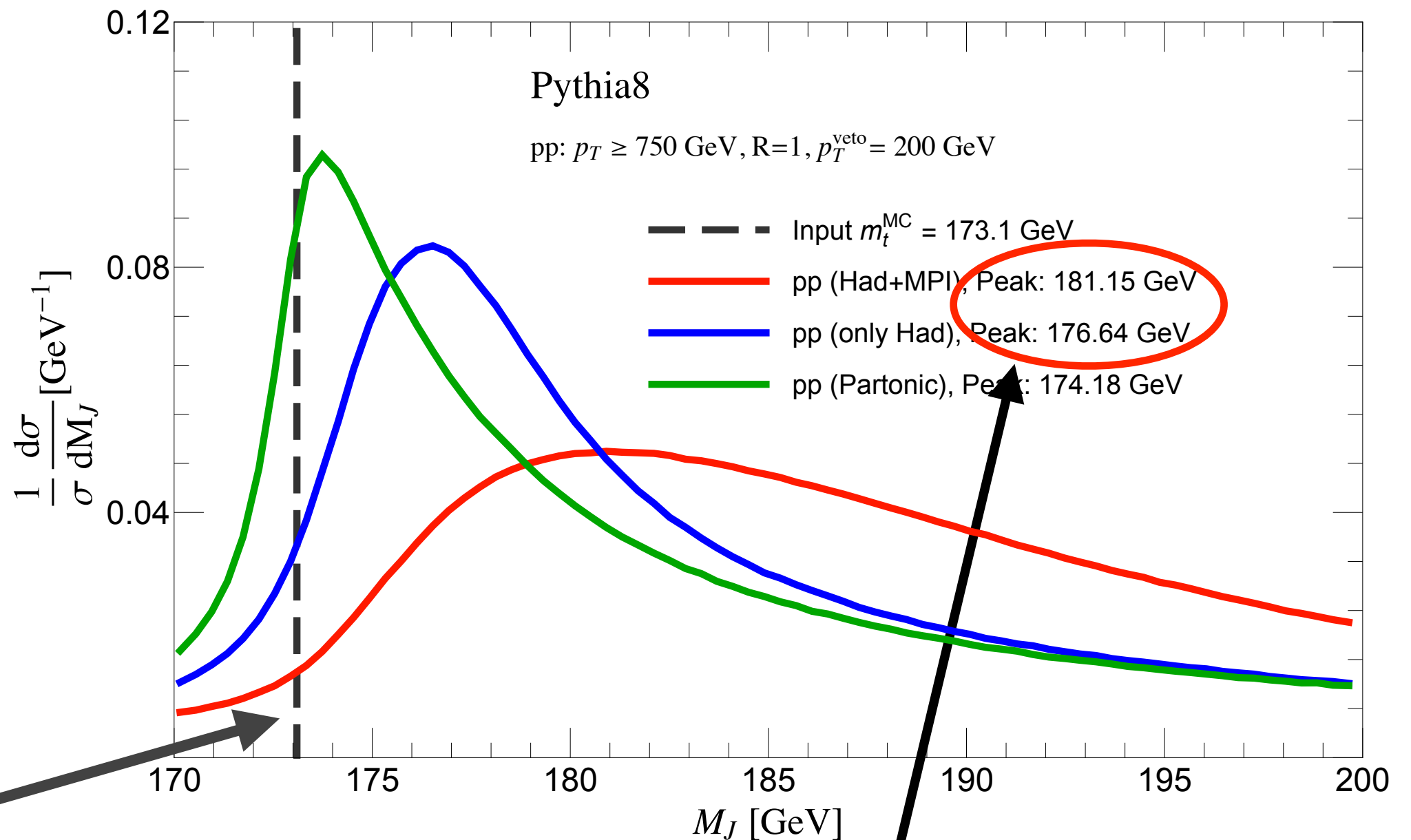
**BUT** control of **Underlying Event** is model dependent.

Same model used for **Hadronization** can describe **UE** by (primarily) tuning one parameter  $\Omega$ .

$$\Omega = \int dk k F(k)$$

Stewart, Tackmann, Waalewijn, 2015

# Effect of UE/MPI



Input mass in Pythia  
 $m_t = 173.1$  GeV

**Significant contamination**

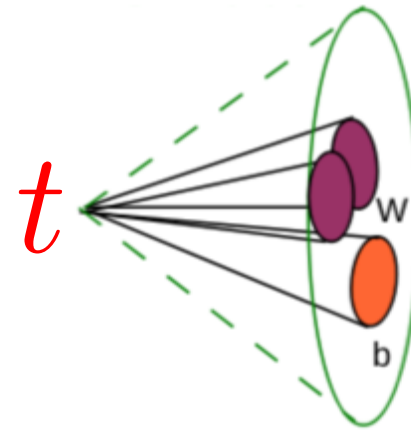
It is not ideal to have such a large shift from the contamination that needs to be modeled.



# Second Simplification: Jet Substructure Techniques

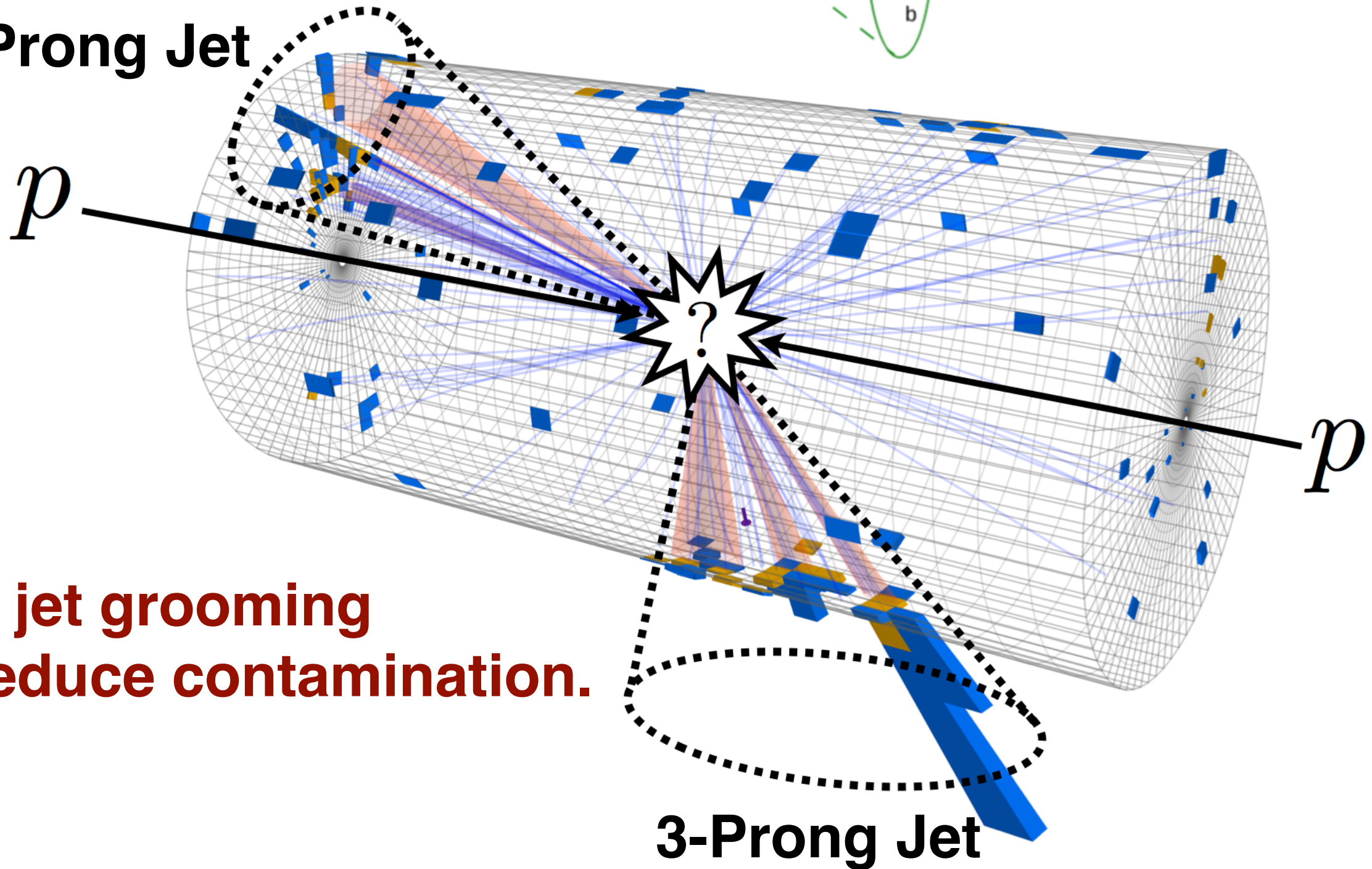


CMS Experiment at LHC, CERN  
Data recorded: Sun Jul 12 07:25:11 2015 CEST  
Run/Event: 251562 / 111132974  
Lumi section: 122  
Orbit/Crossing: 31722792 / 2253



$$pp \rightarrow t\bar{t}$$

**3-Prong Jet**



**Use jet grooming  
to reduce contamination.**

**3-Prong Jet**

# Soft Drop

Larkoski, Marzani, Soyez, Thaler 2014

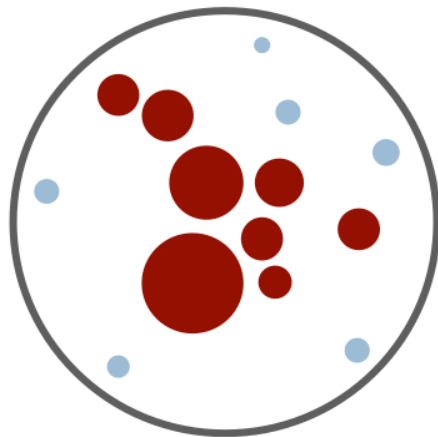
## Grooms soft radiation from the jet

$$\frac{\min(p_{Ti}, p_{Tj})}{p_{Ti} + p_{Tj}} > z_{\text{cut}} \left( \frac{\Delta R_{ij}}{R_0} \right)^\beta$$

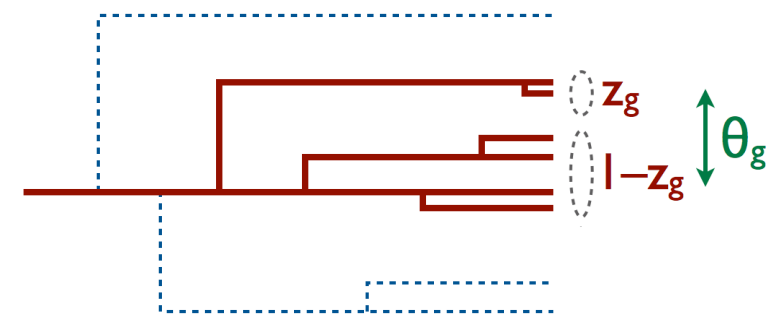
$$z > z_{\text{cut}} \theta^\beta$$

two grooming parameters

### Groomed jet

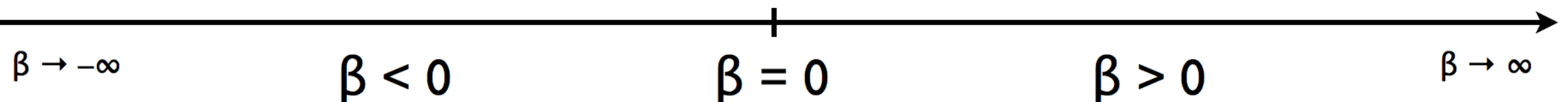


### Groomed Clustering tree



More Grooming

Less Grooming

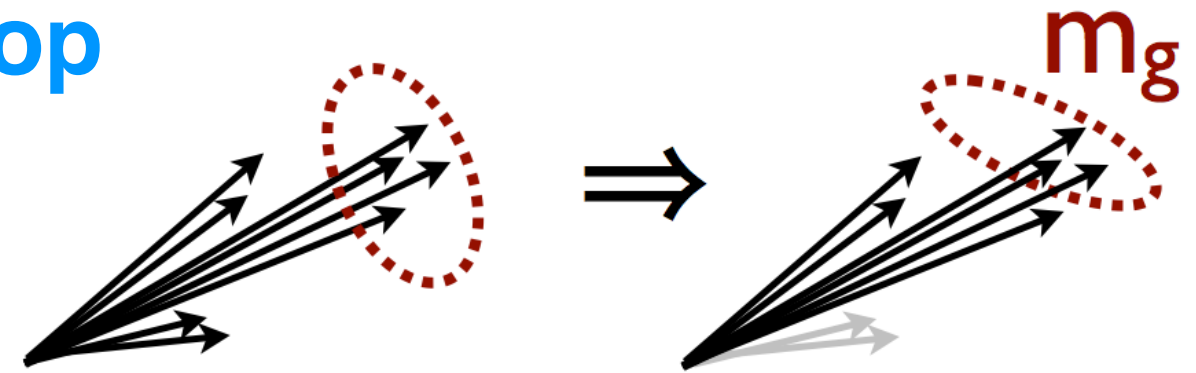




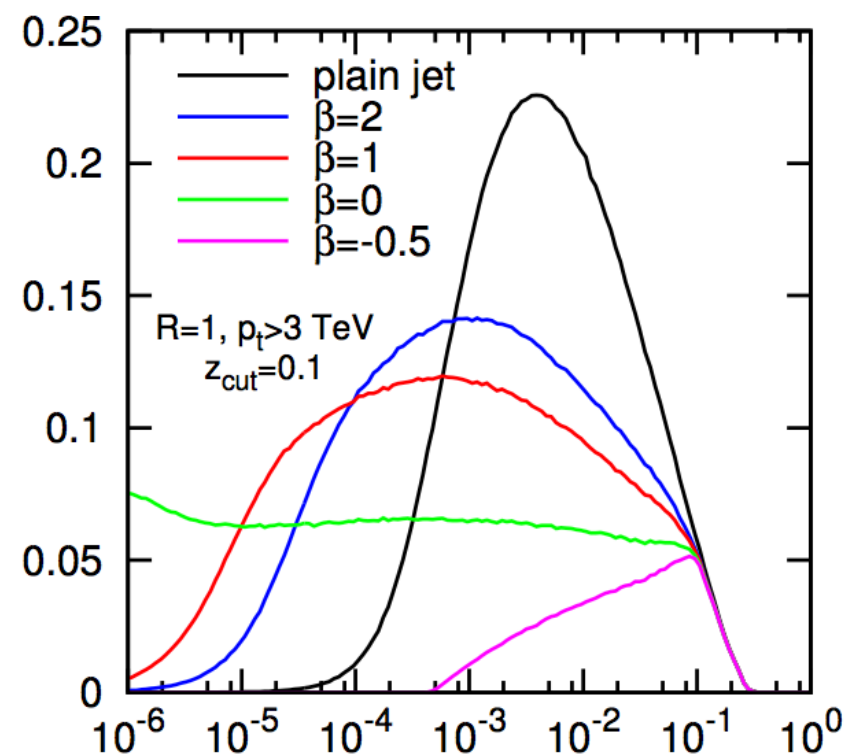
# Soft Drop

## Calculating Mass?

Larkoski, Marzani, Soyez, Thaler 2014

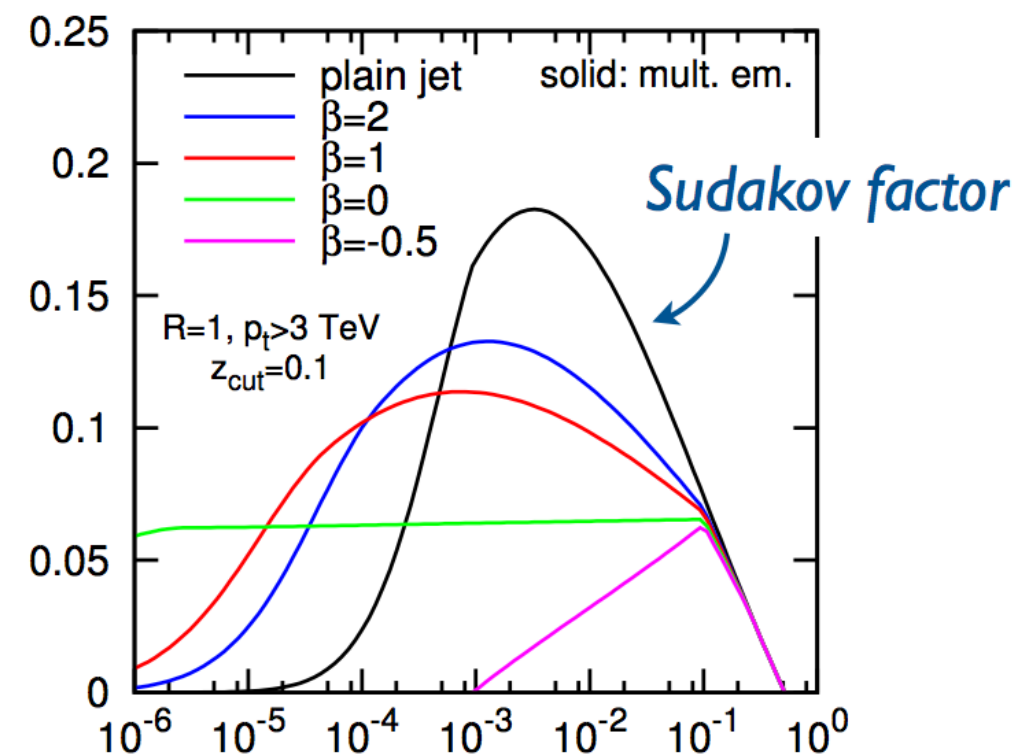


### Pythia8, partonic



$m^2/p_T^2$

### Pert QCD at $\sim$ NLL



$m^2/p_T^2$

More Grooming

$\beta \rightarrow -\infty$

$\beta < 0$

$\beta = 0$

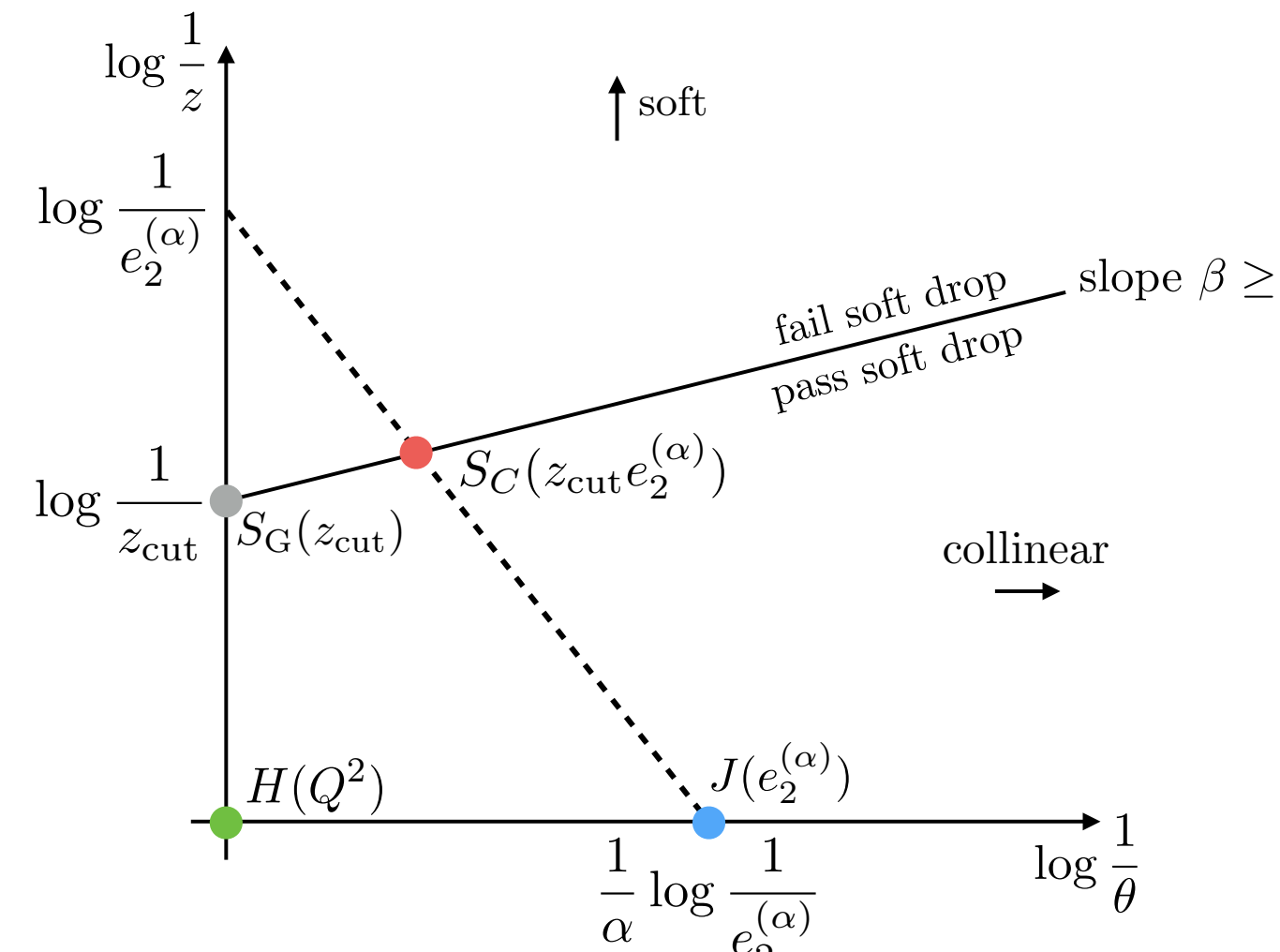
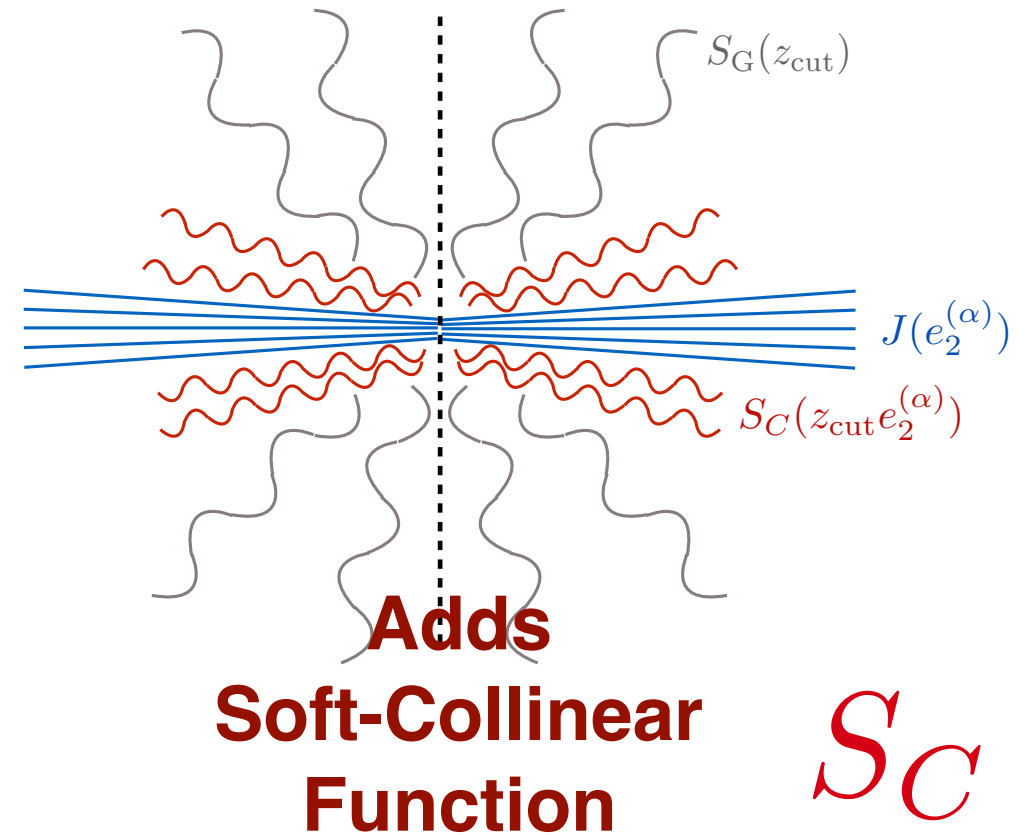
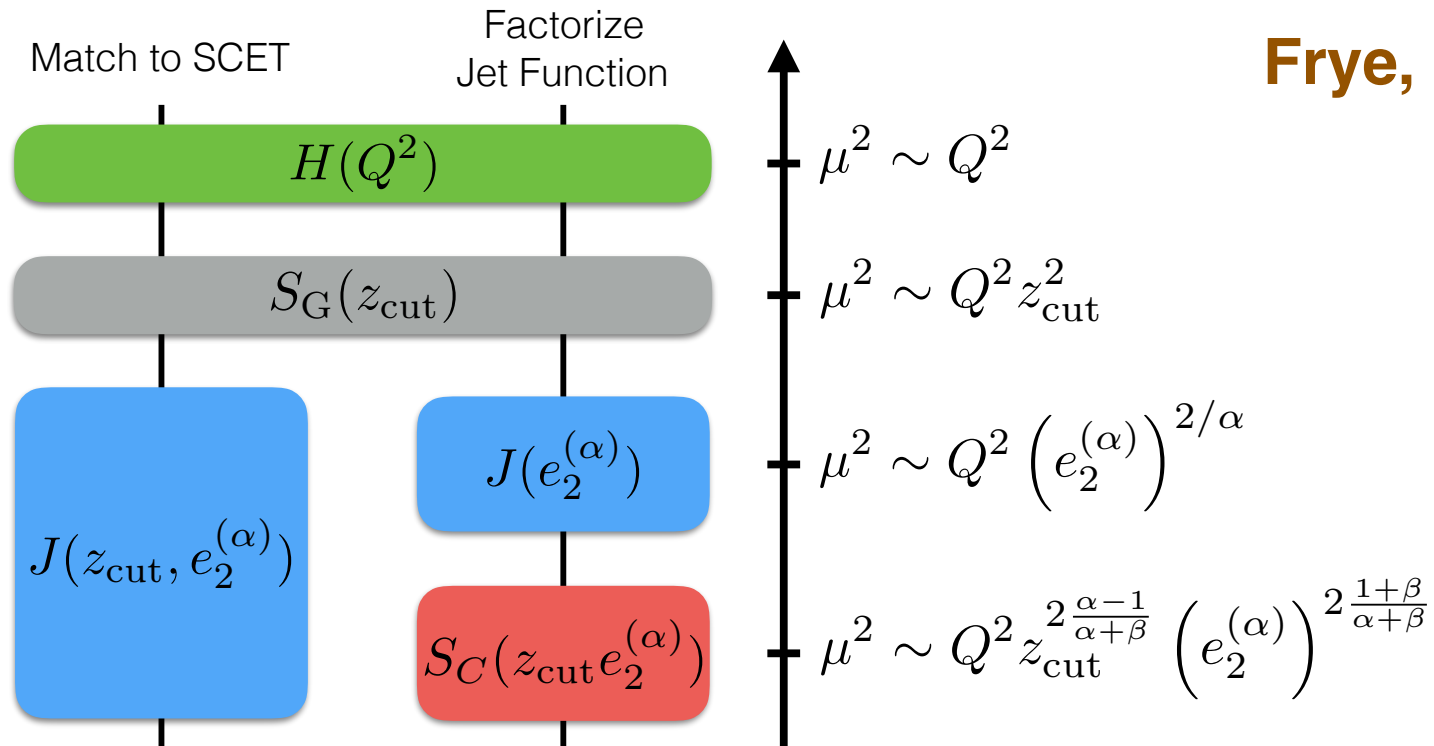
$\beta > 0$

Less Grooming

$\beta \rightarrow \infty$

# Soft Drop Factorization

Frye, Larkoski, Marzani, Schwartz, Yan 2016



$$\frac{d\sigma}{de_2 \dots} = H(Q^2) S_G(z_{\text{cut}}, \beta) \times \left[ S_C(e_2, z_{\text{cut}}, \beta) \otimes J(e_2) \right]$$

**isolates measurement**

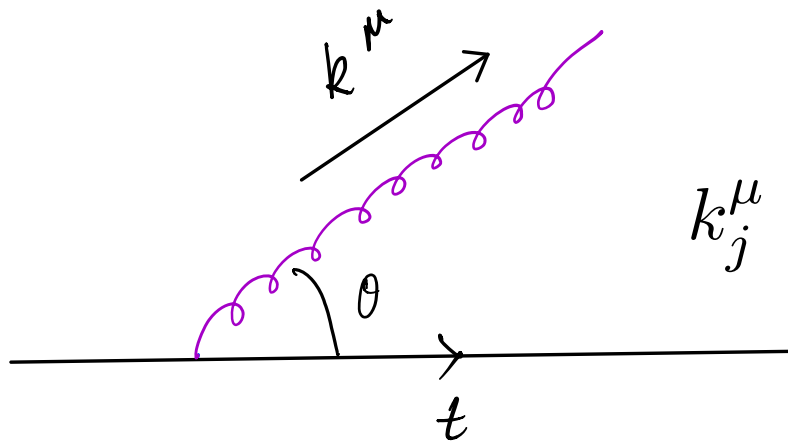
**achieve NNLL precision**

# Top Jet Mass with Soft Drop

$$pp \rightarrow t\bar{t}$$

# Top Jet Mass with Soft Drop

A. Hoang, S. Mantry, AP, I. Stewart



$$k_j^\mu = (k^+, k^-, k_\perp) = (E(1 - \cos \theta), E(1 + \cos \theta), k_\perp)$$

a) Peak Region Constraint:

$$z \left[ (1 - \cos \theta) + \frac{m^2}{Q^2} (1 + \cos \theta) \right] \sim \frac{2m\Gamma_t}{Q^2}$$

b) Soft Drop Constraint:

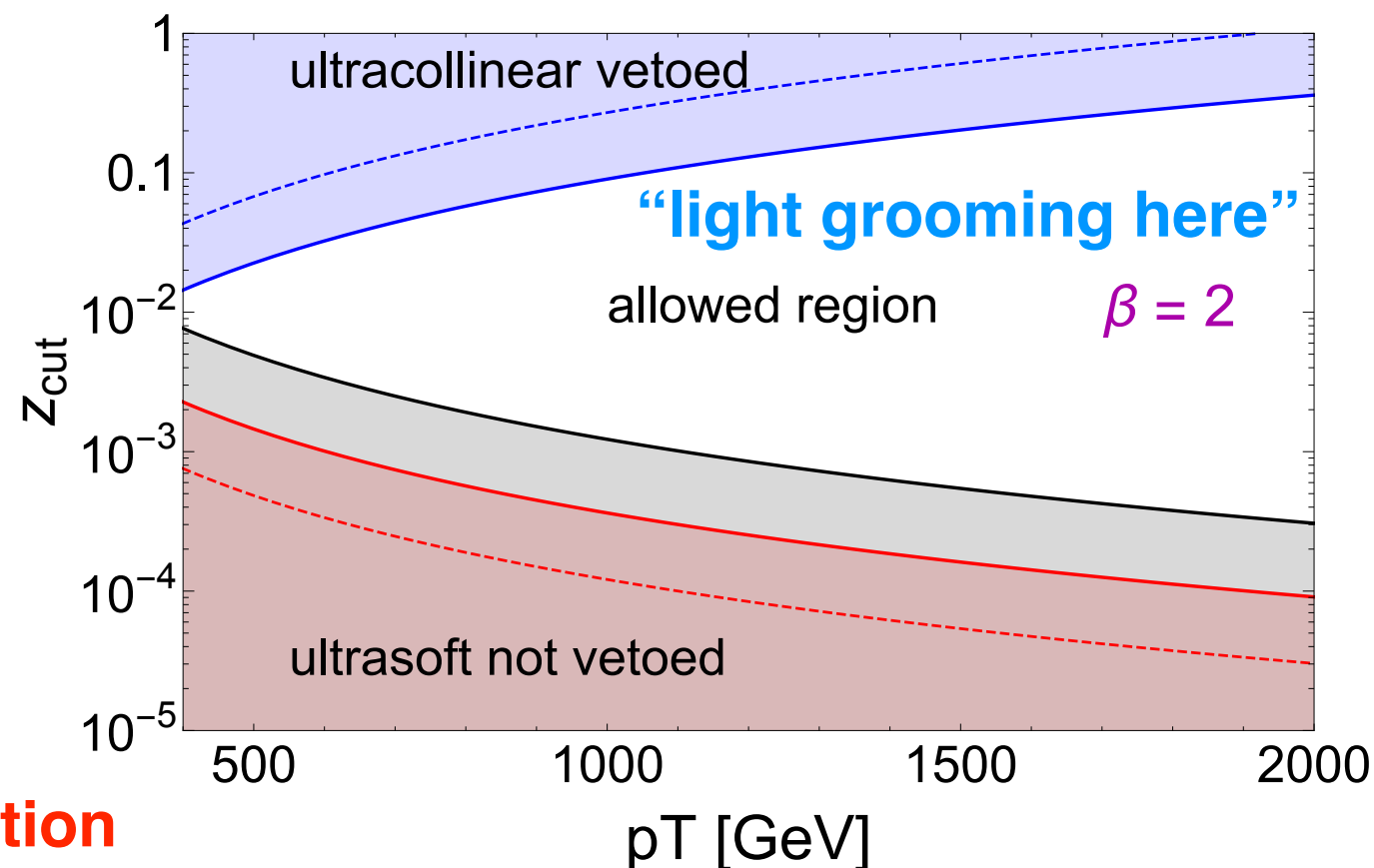
$$z > z_{\text{cut}} \theta^\beta$$

Constraints on  
Soft Drop parameters:

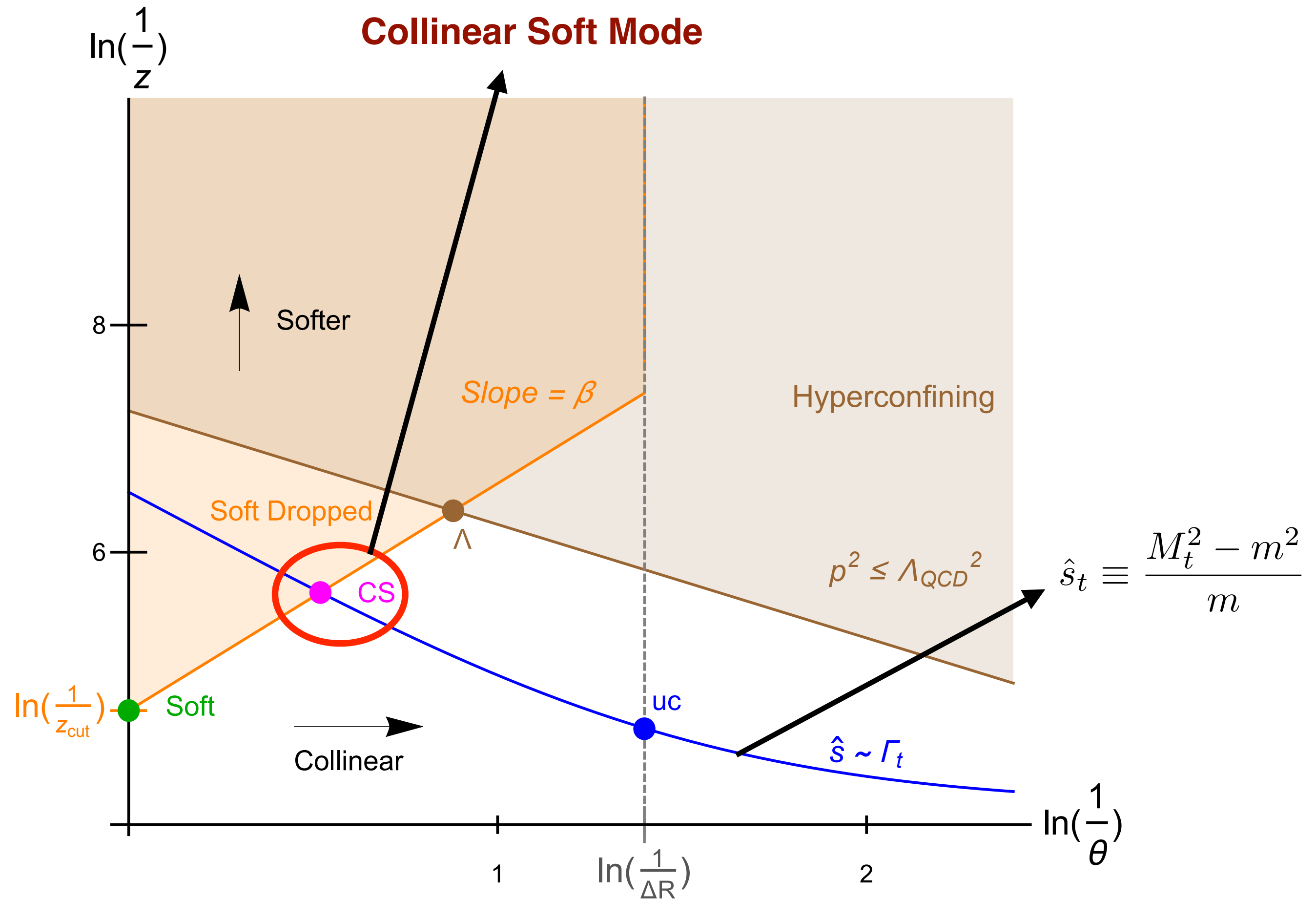
$$\frac{\Gamma_t}{m} \left( \frac{Q}{2m} \right)^\beta \gg z_{\text{cut}} \gg \frac{2m\Gamma_t}{Q^2}$$

Ensure soft drop  
does not touch mass

Ensure soft drop  
removes most contamination



# Top Jet Mass with Soft Drop

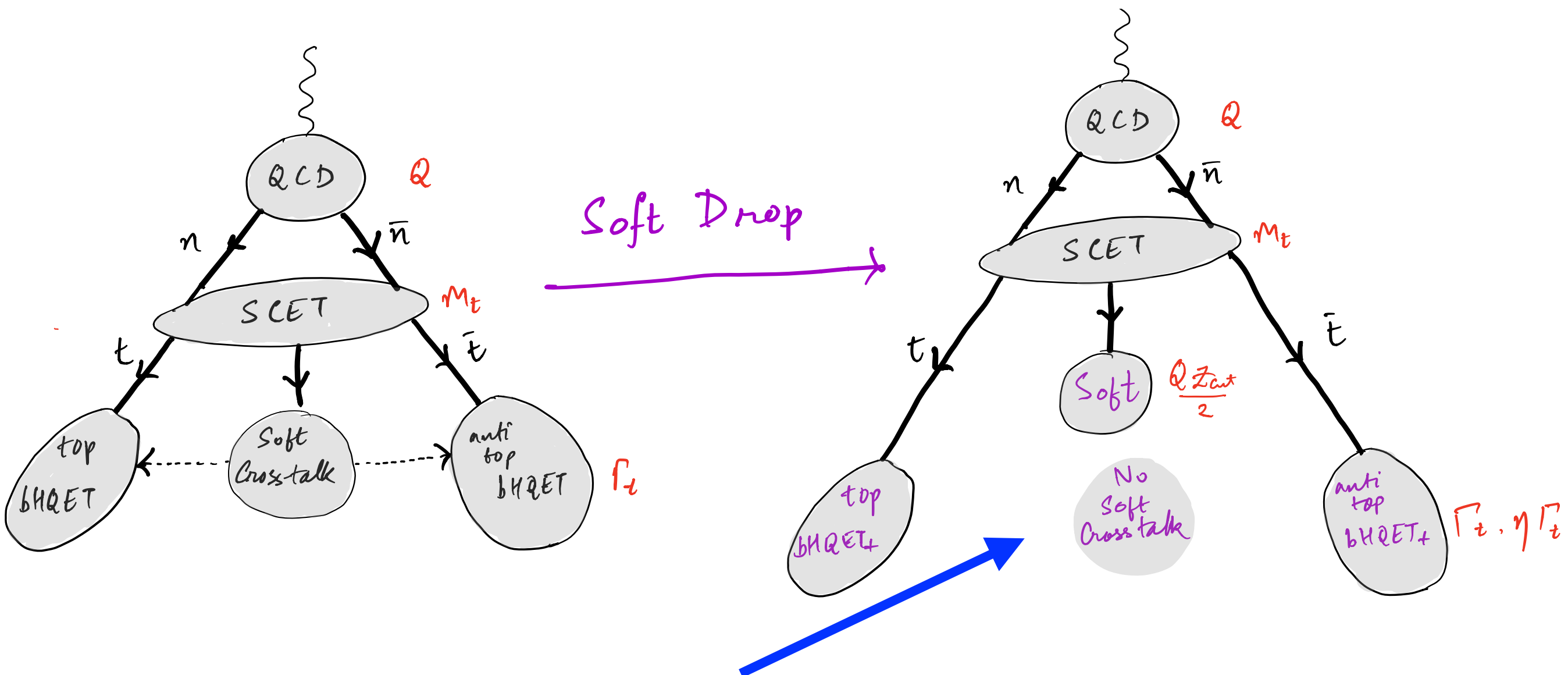


# Effective Theory for Groomed top jets

A. Hoang, S. Mantry, AP, I. Stewart

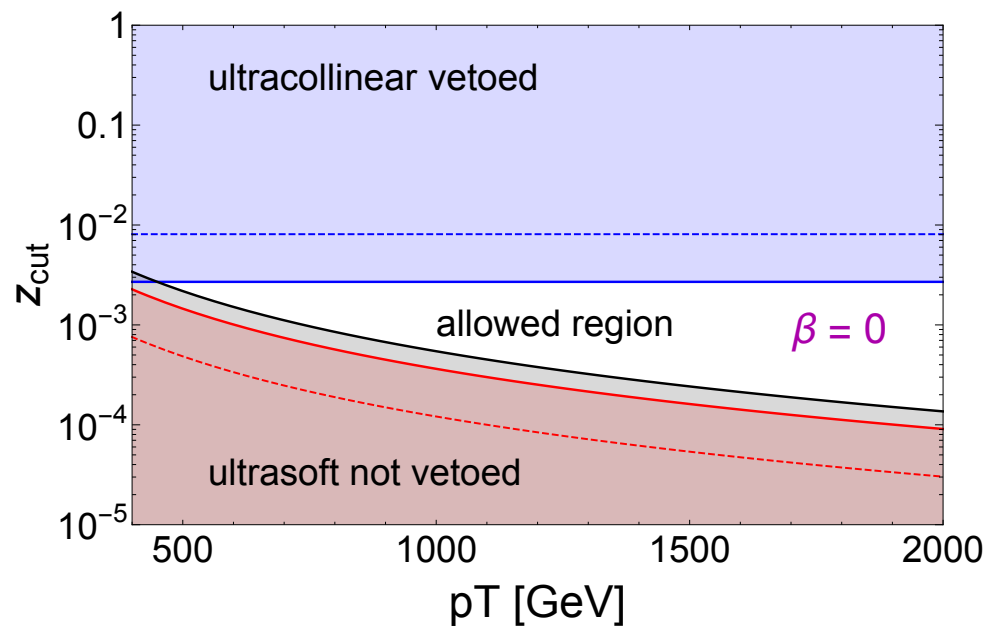
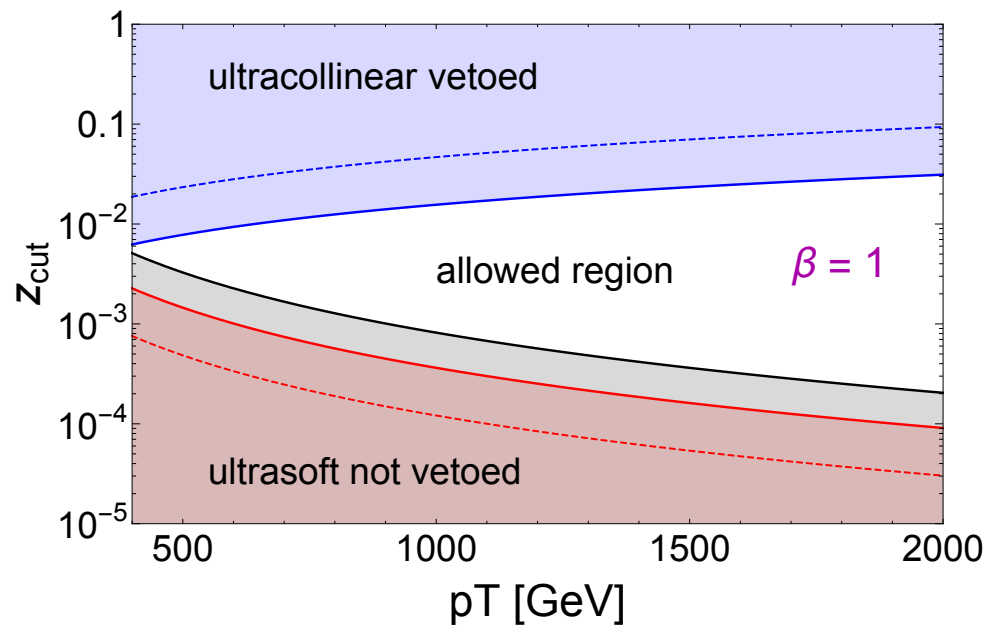
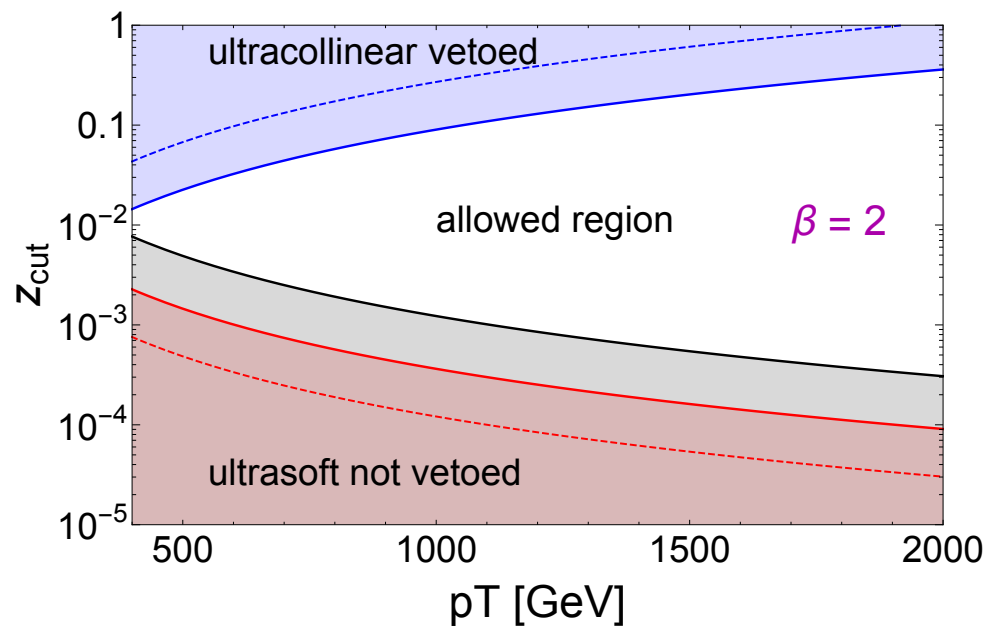
Factorization Theorem for Soft Dropped Top Jets:

$$\frac{d\sigma}{dM_J} = N \int d\ell dk J_B\left(\hat{s}_t - \frac{Q\ell}{m}, \Gamma_t, \delta m\right) S_C\left[\left(\ell - \frac{m}{Q}k\right)^{\frac{1+\beta}{2+\beta}} (2^\beta Q z_{\text{cut}})^{\frac{1}{1+\beta}}, \beta\right] F_C(k)$$



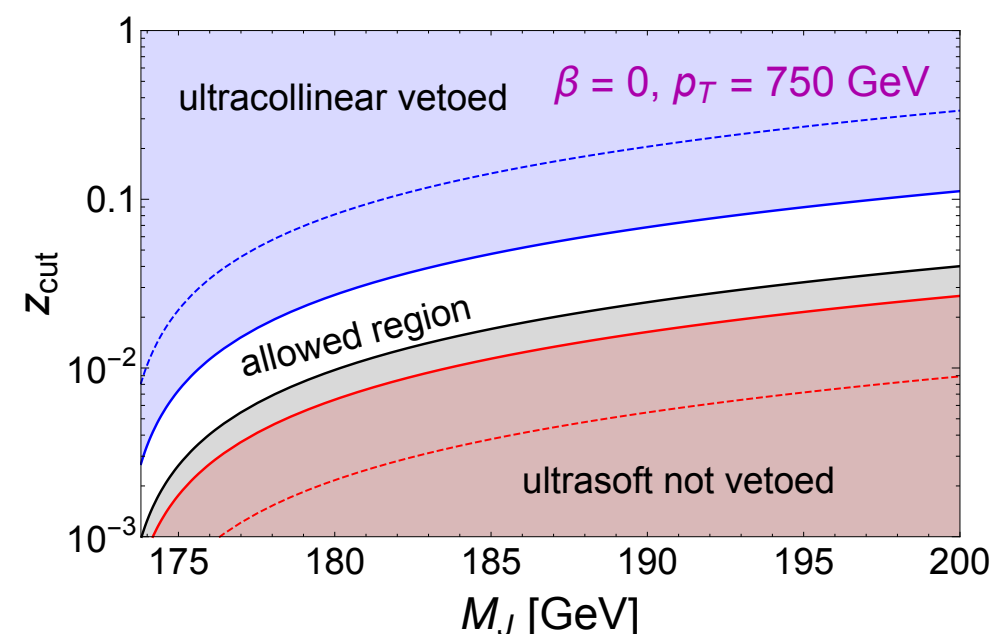
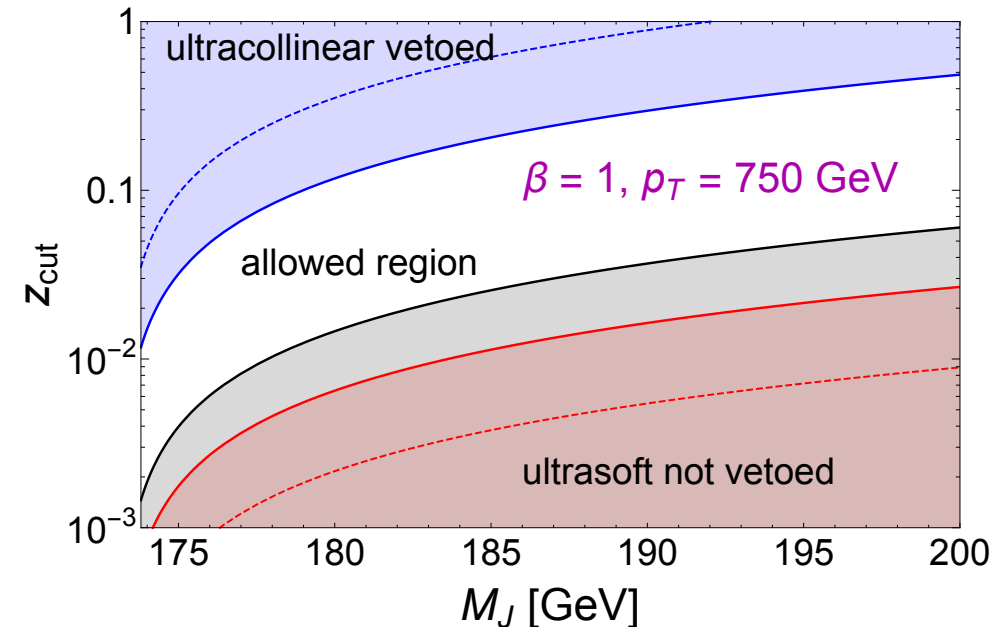
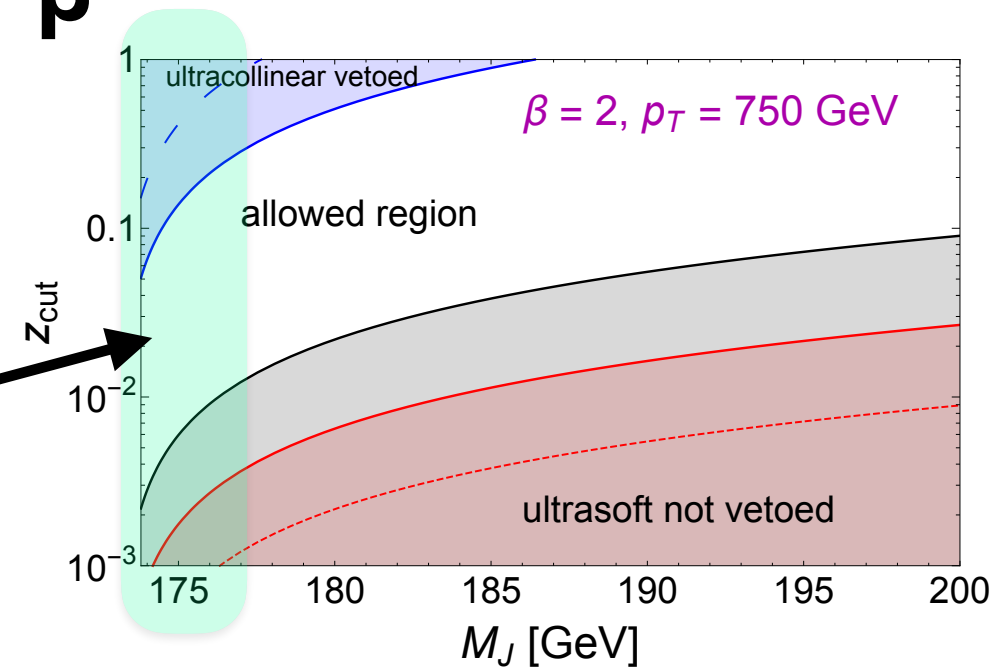
**Now includes semi leptonic decays!**

# Constraints: Vary $\beta$



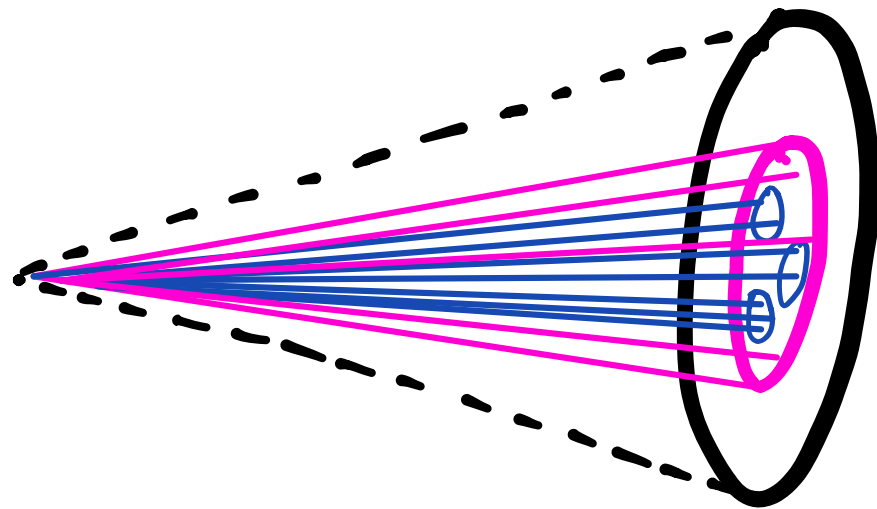
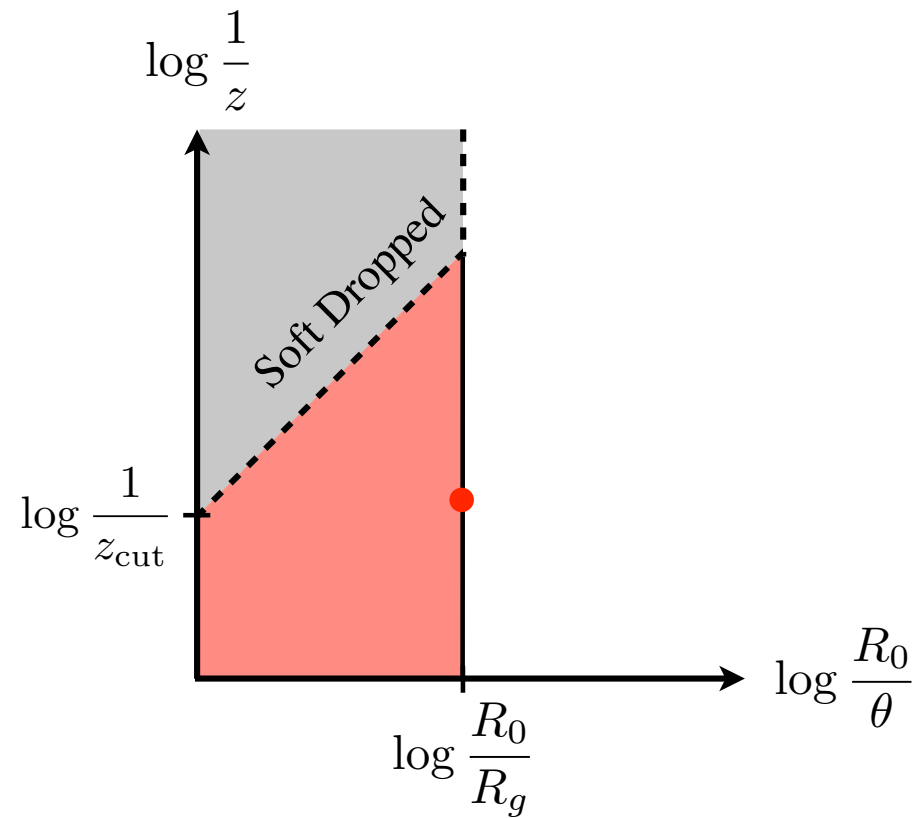
Peak Region

More grooming



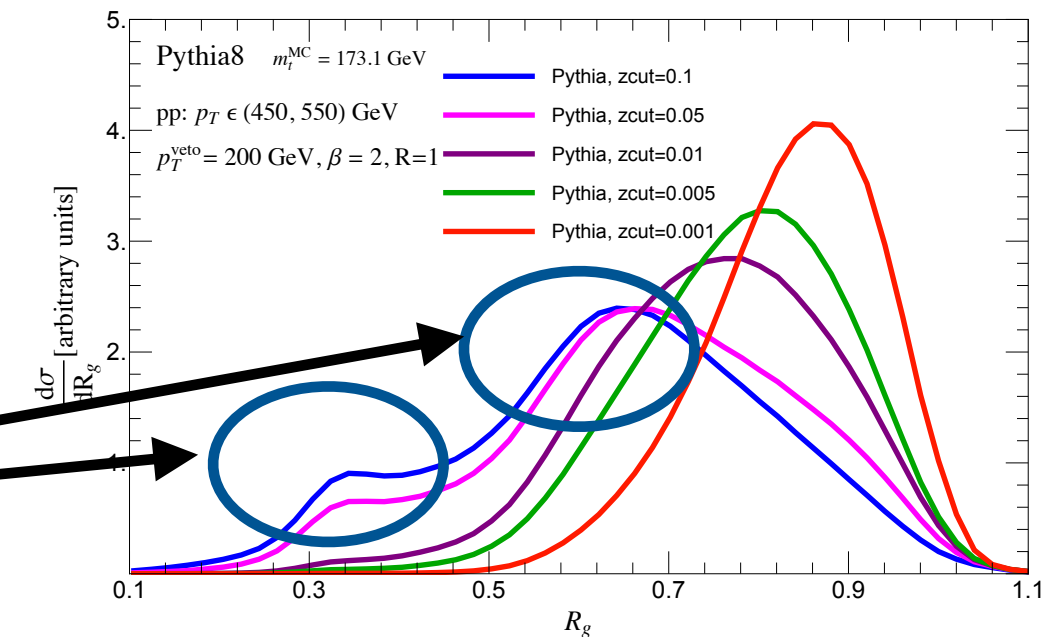
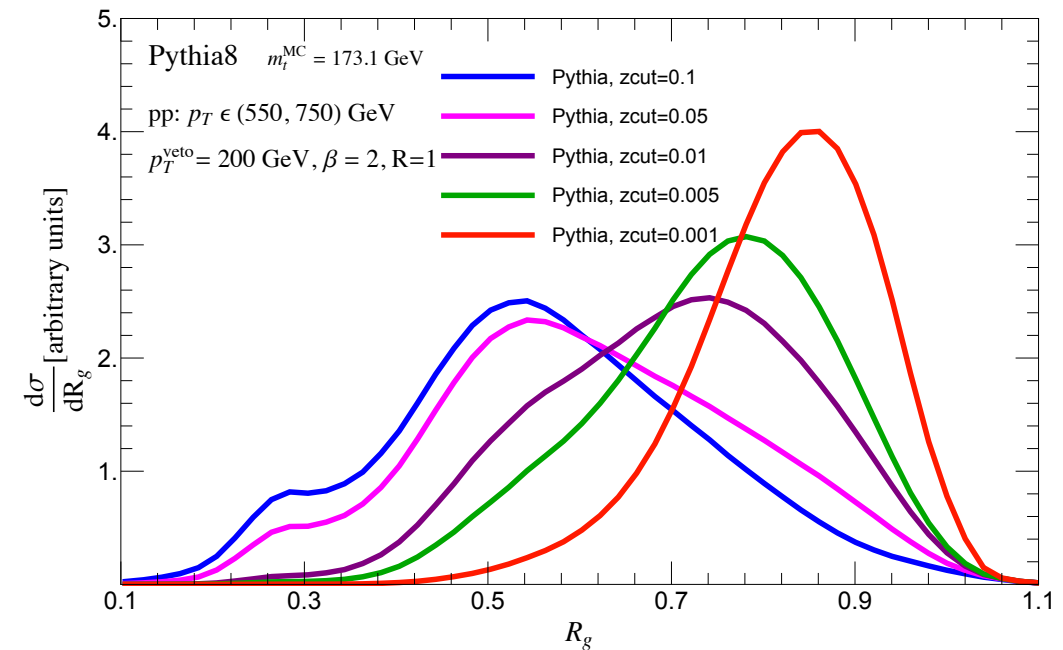
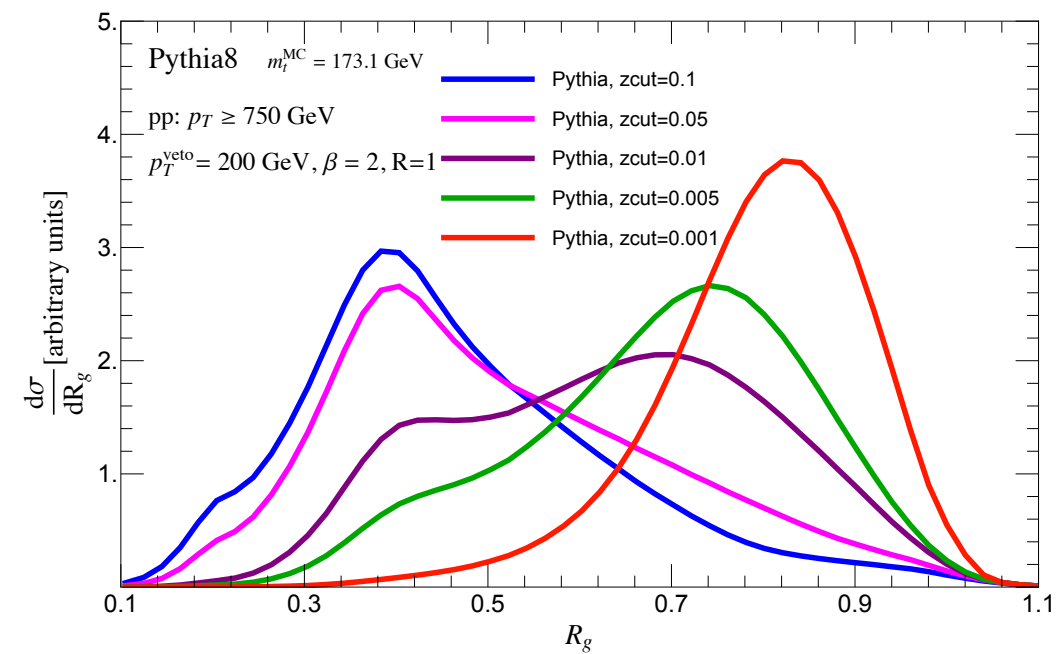
# Groomed Jet Radius: $R_g$

Larkoski, Marzani, Soyez, Thaler 2014



from decay products

Lower  
 $p_T$





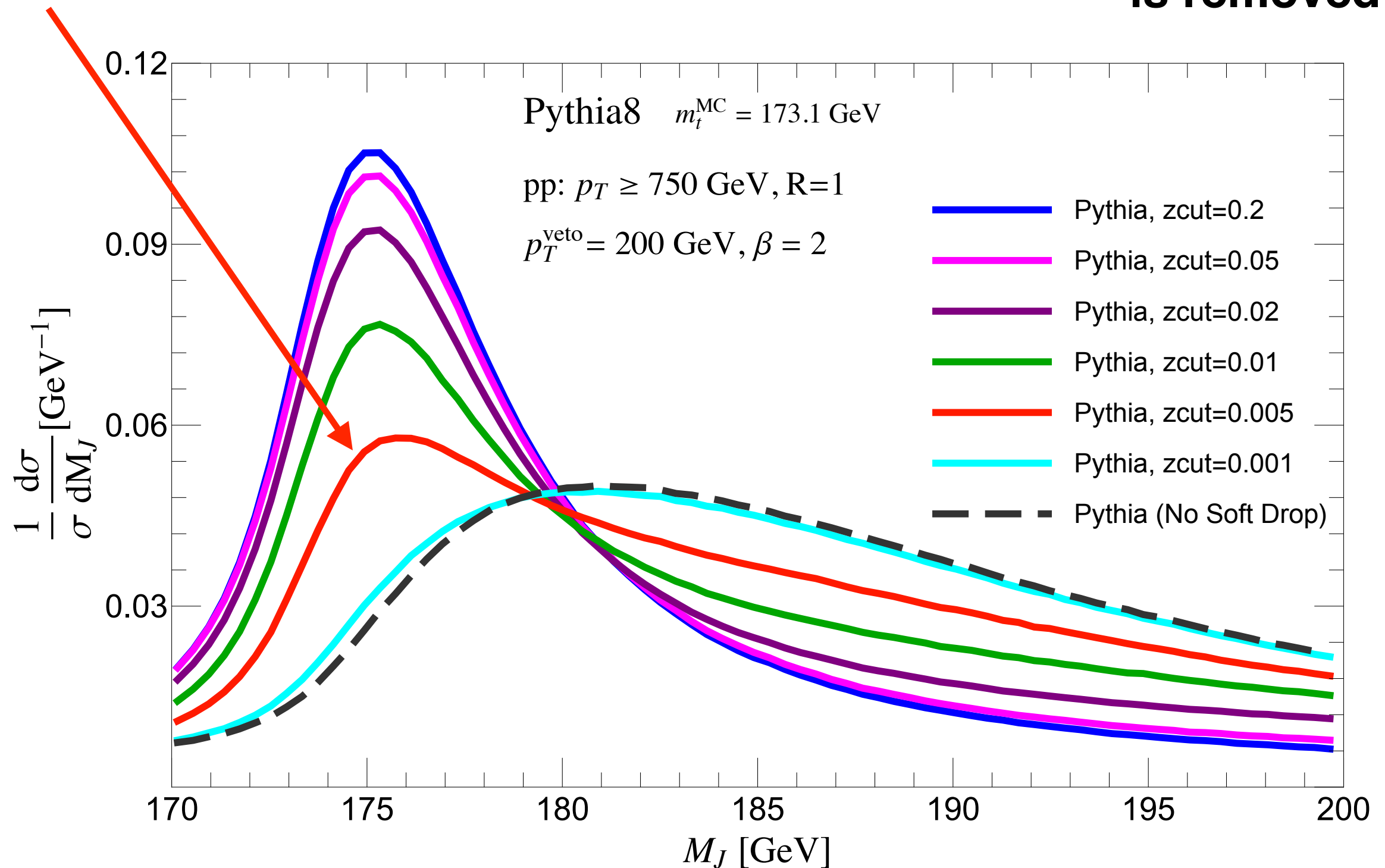
# **Pythia Studies**

Test Theory Predictions with Simulations

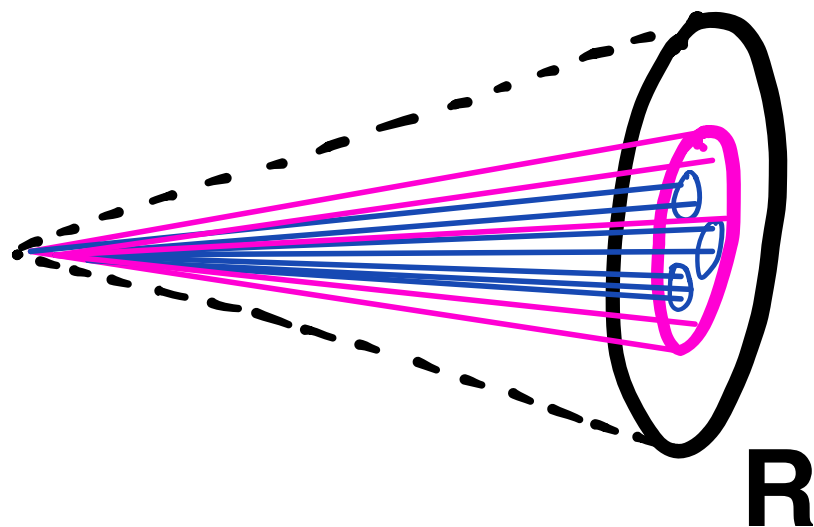
# $z_{\text{cut}}$ dependence

predict transition for “light Soft Drop” ✓

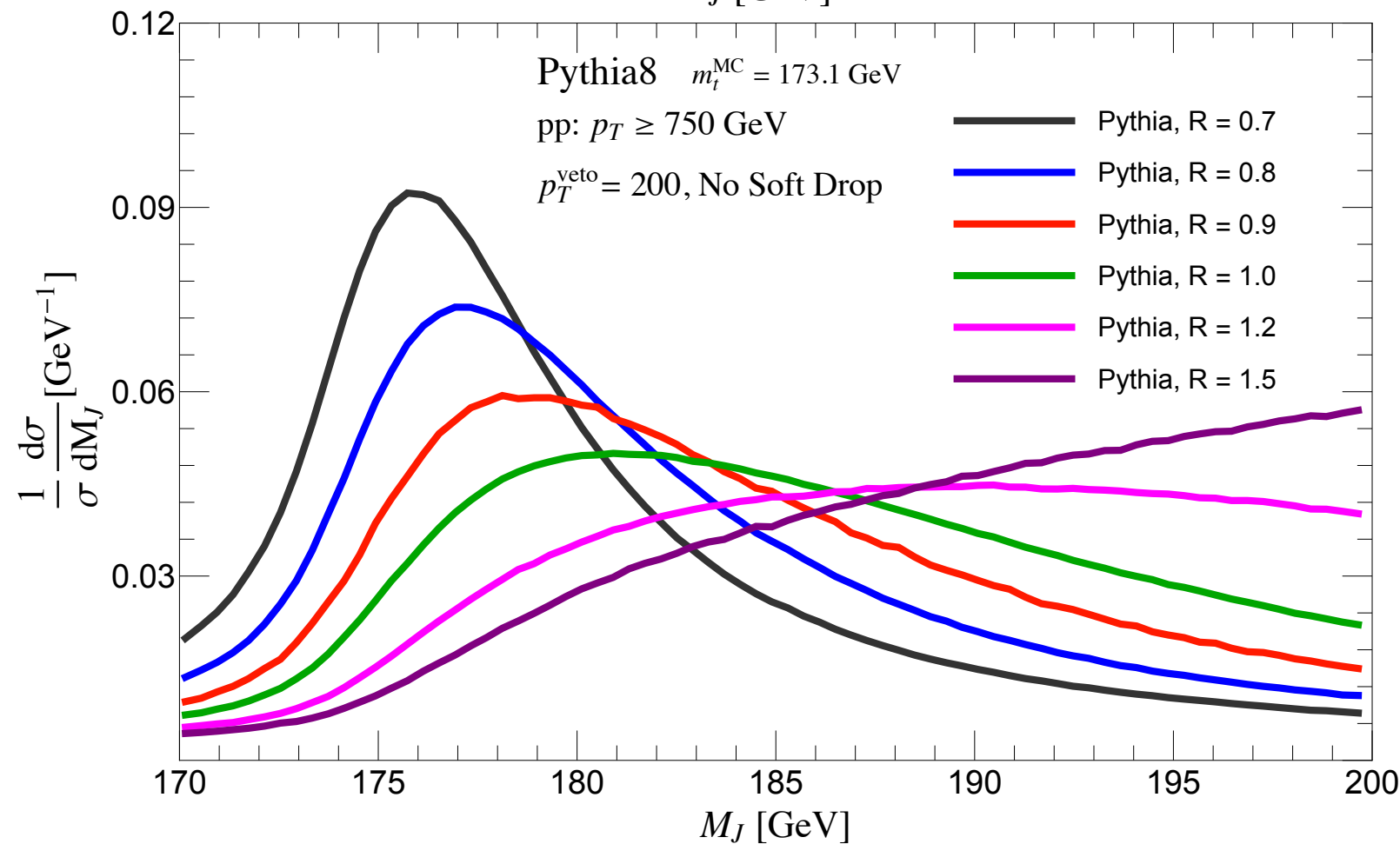
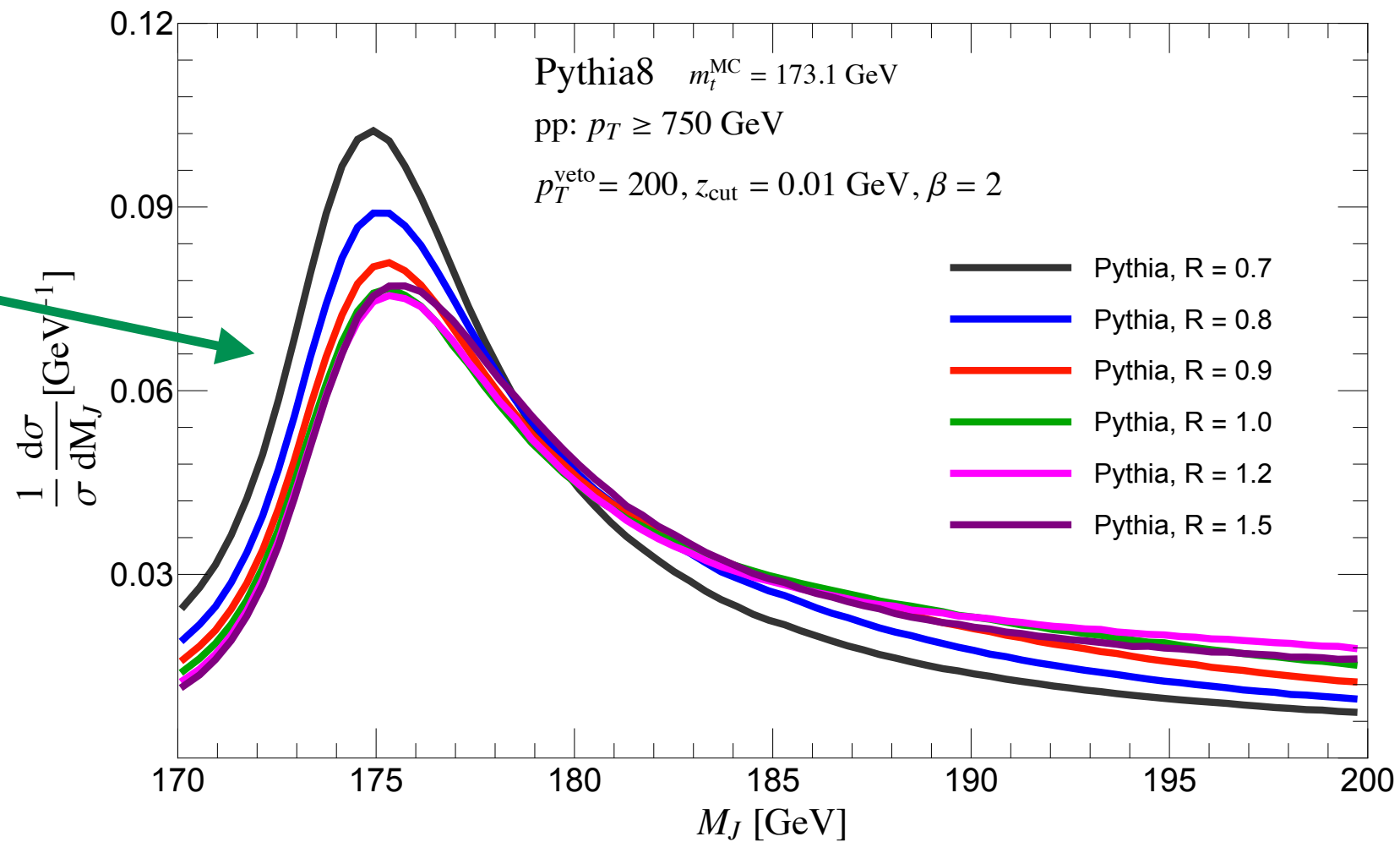
most contamination  
is removed



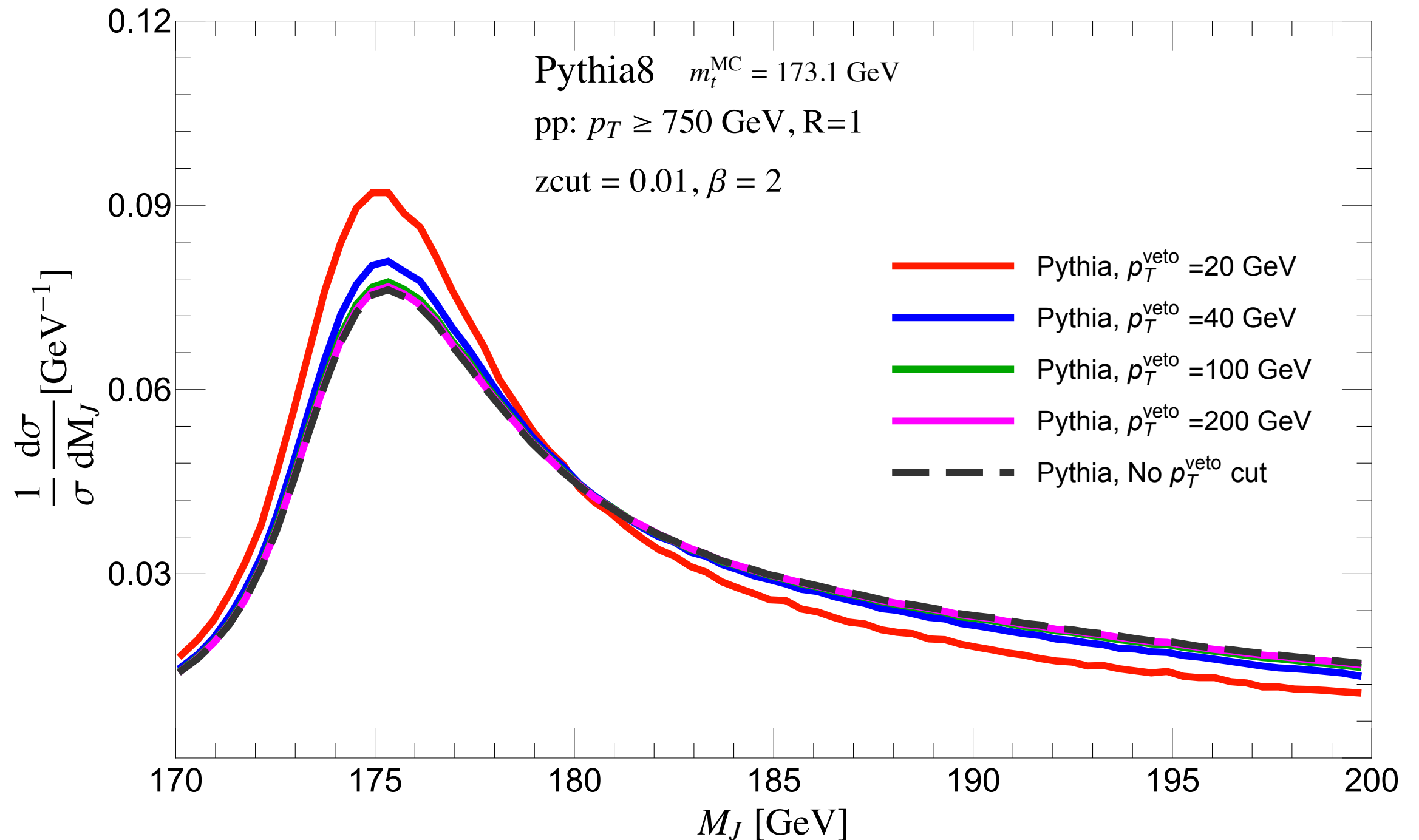
**predict:  
independent of  
Jet Radius**



**Without  
Soft Drop  
(huge):**

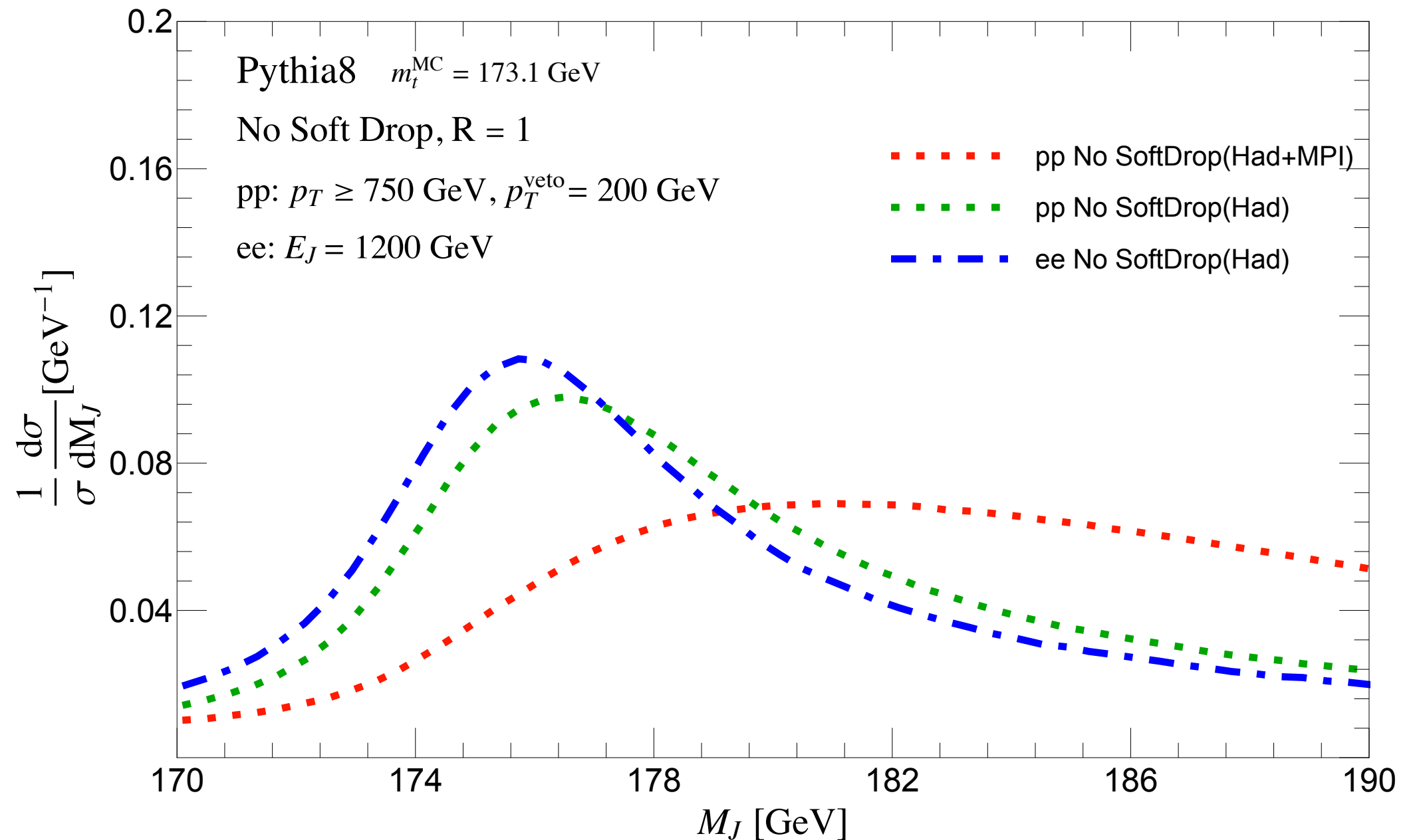


**Predict independent of cutoff  
on radiation outside the jet (“jet veto”):**



# Soft Drop prediction: Same Result for $e^+e^-$ and $pp$ collisions

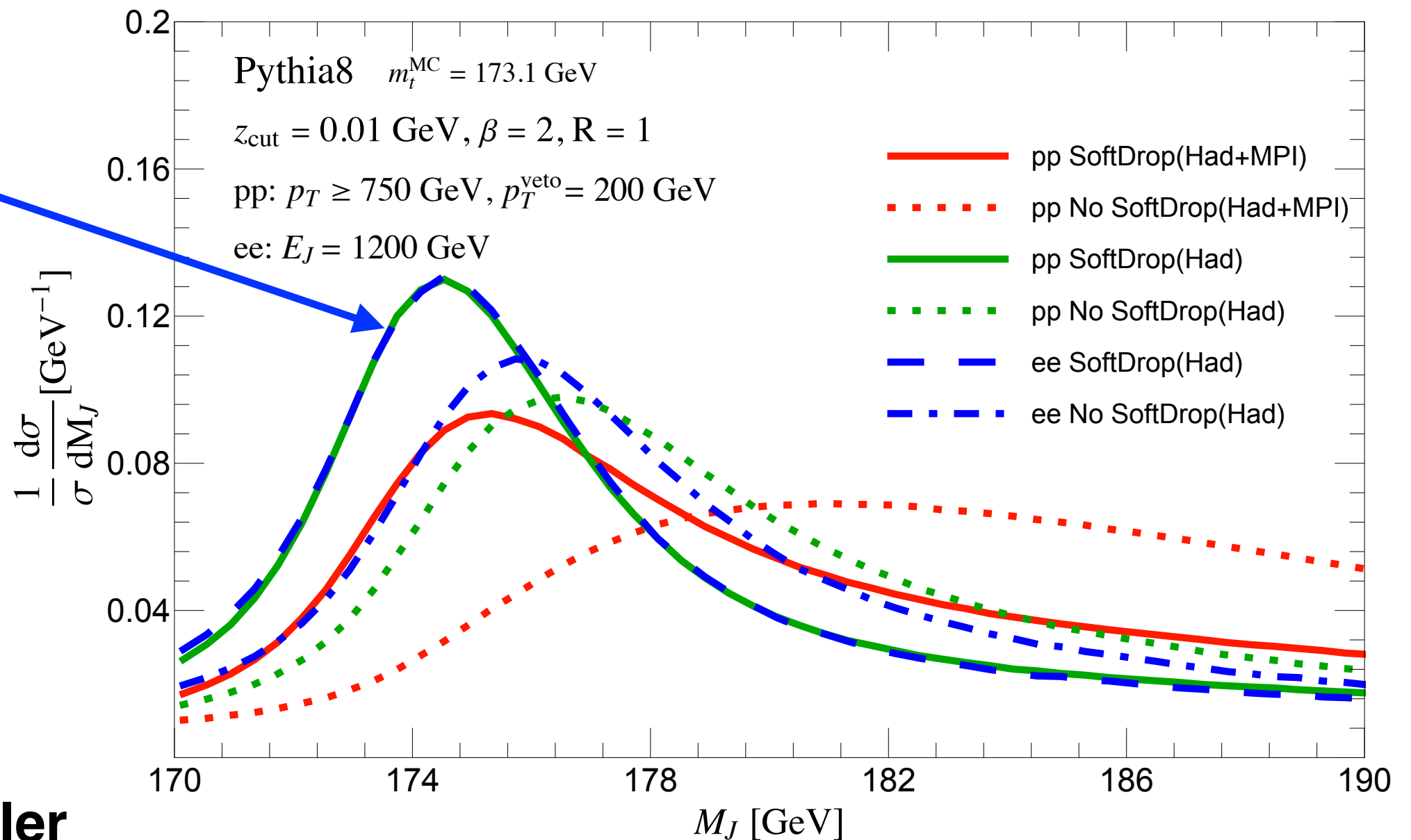
**Without  
Soft Drop  
(differ):**



# Soft Drop prediction: Same Result for $e^+e^-$ and $pp$ collisions

With  
Soft Drop:

Great!



much smaller  
contamination

# Compare Simulations to Our Theory

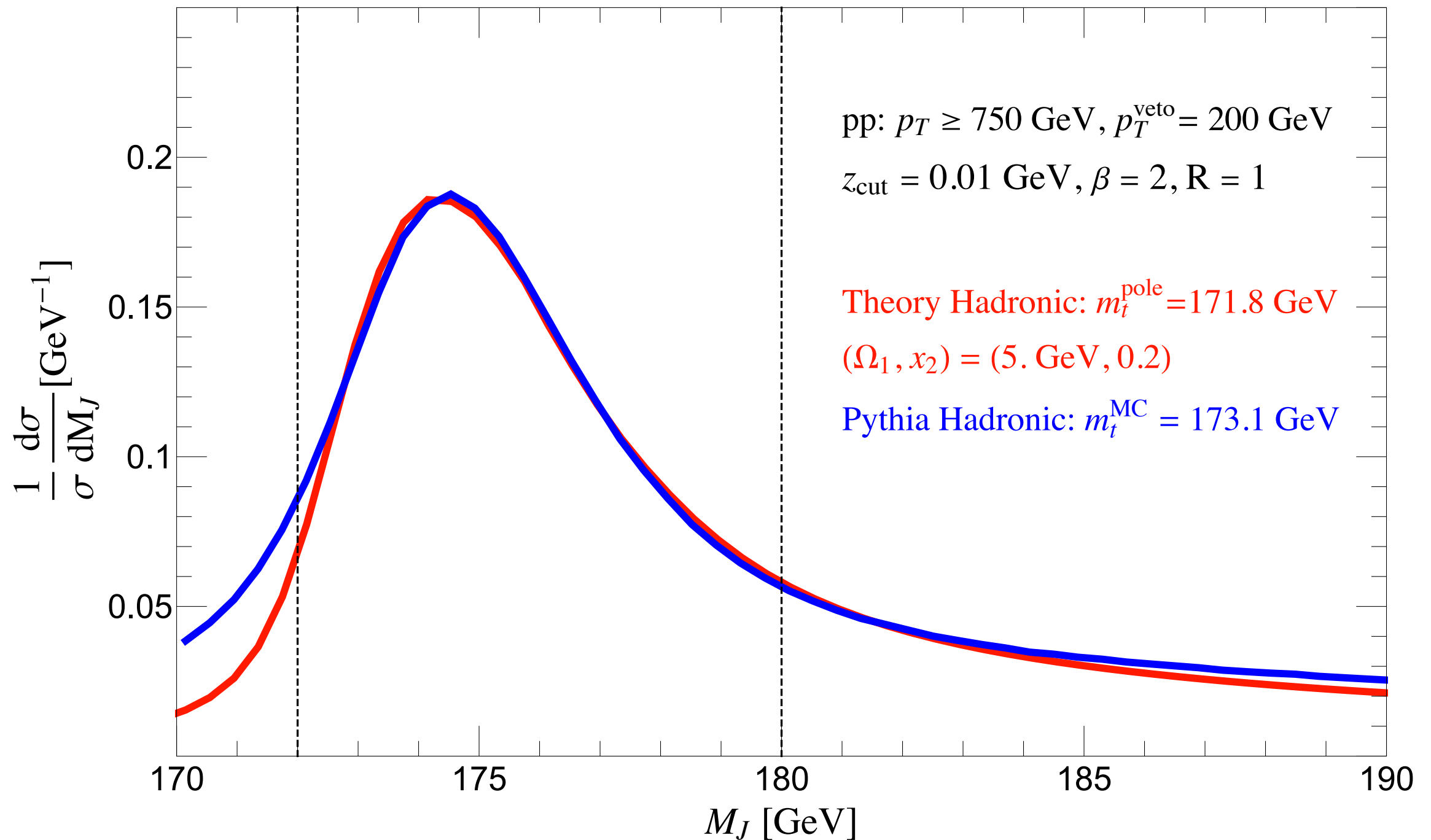
(preliminary)

# Pythia Simulation vs. Theory (with Soft Drop)

**without  
contamination:**

$$m_t^{\text{pole}} = 171.8 \text{ GeV}$$

$$m_t^{\text{MC}} = 173.1 \text{ GeV}$$





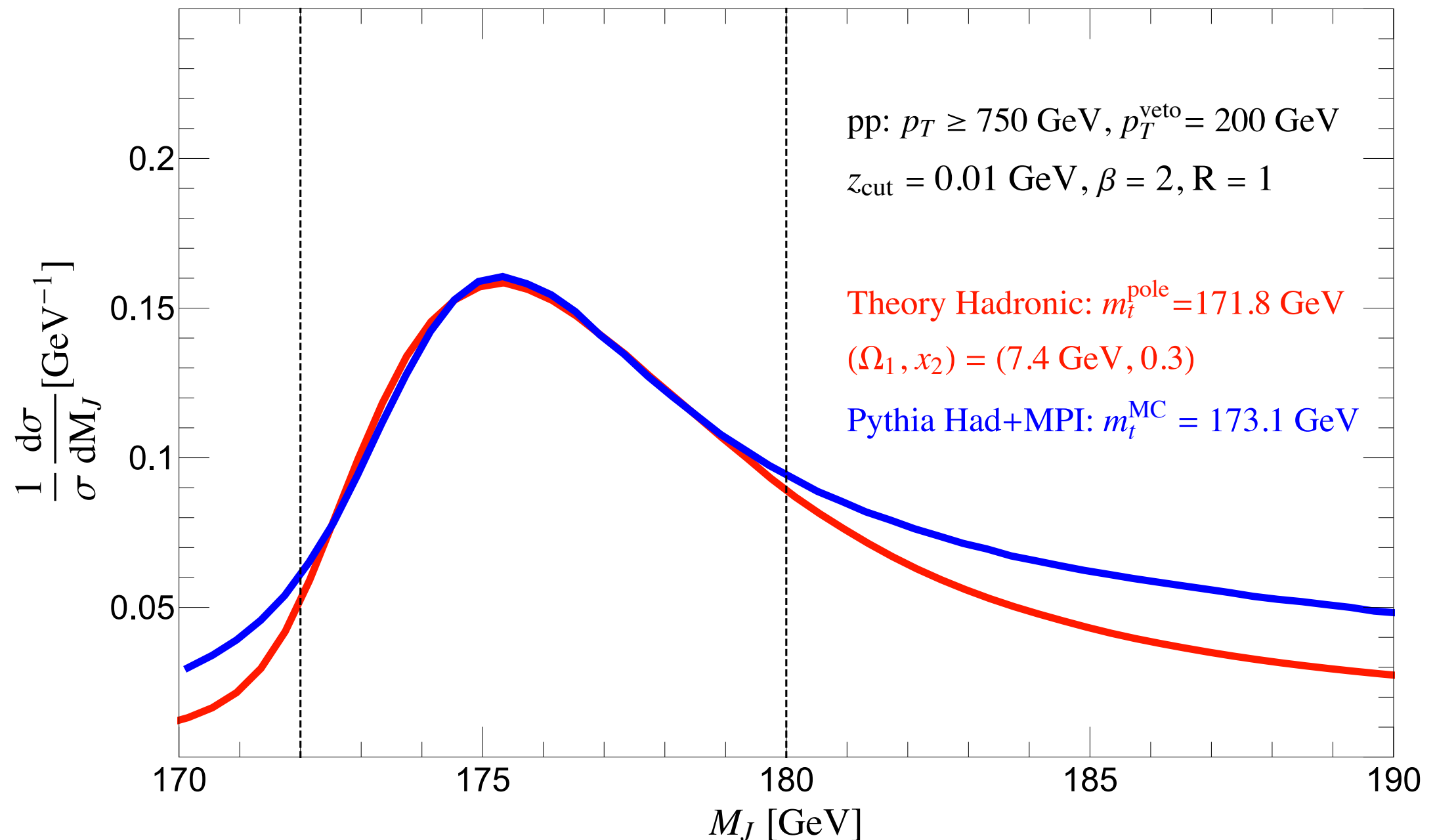
# Pythia Simulation vs. Theory (with Soft Drop)

with  
contamination:

$$m_t^{\text{pole}} = 171.8 \text{ GeV}$$

Same!

$$m_t^{\text{MC}} = 173.1 \text{ GeV}$$

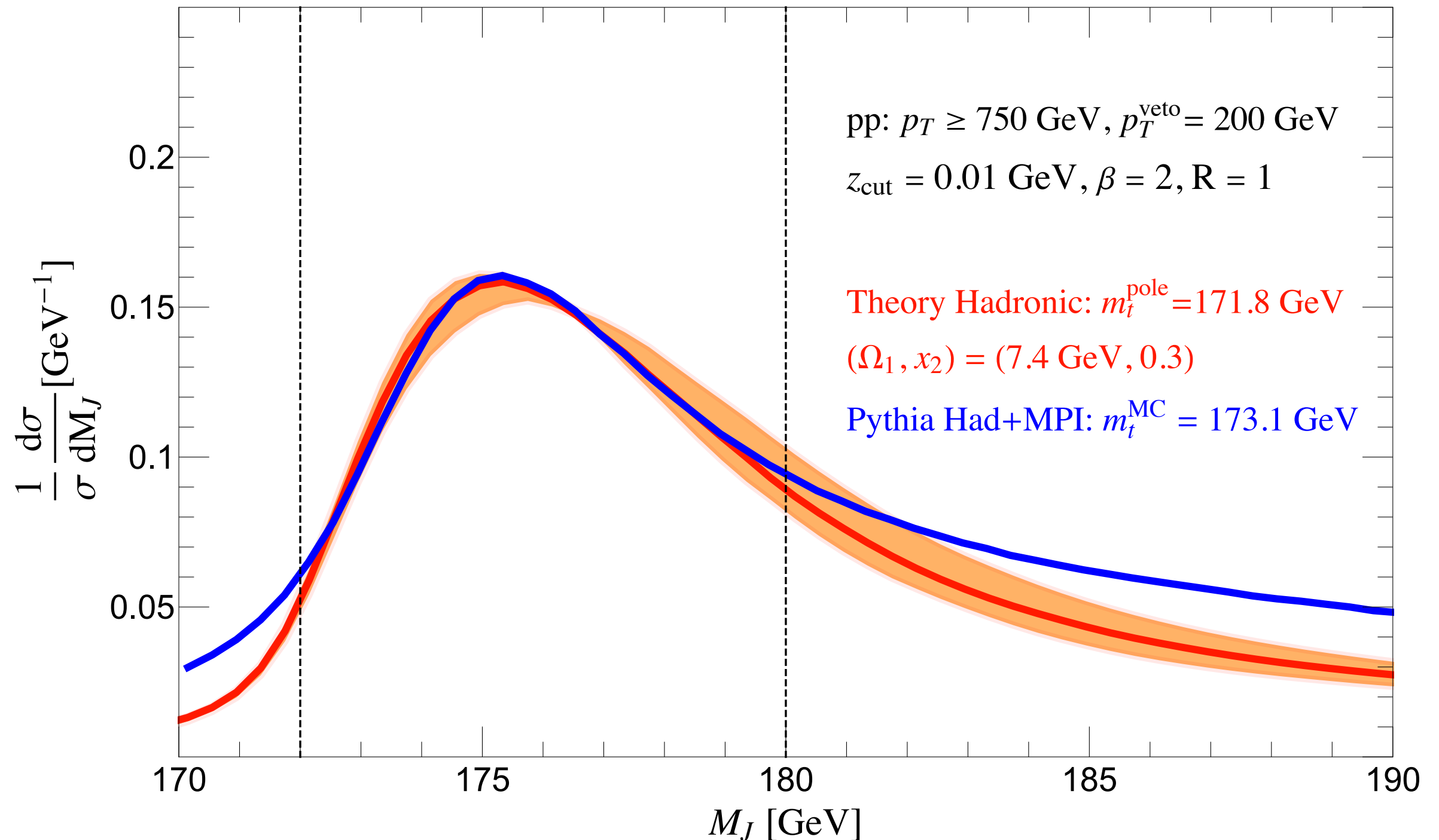


**Dominant change is expected:**  $\Omega_1$  (hadronization)

# Pythia Simulation vs. Theory (with Soft Drop)

**Add uncertainties from  
scale variation:**

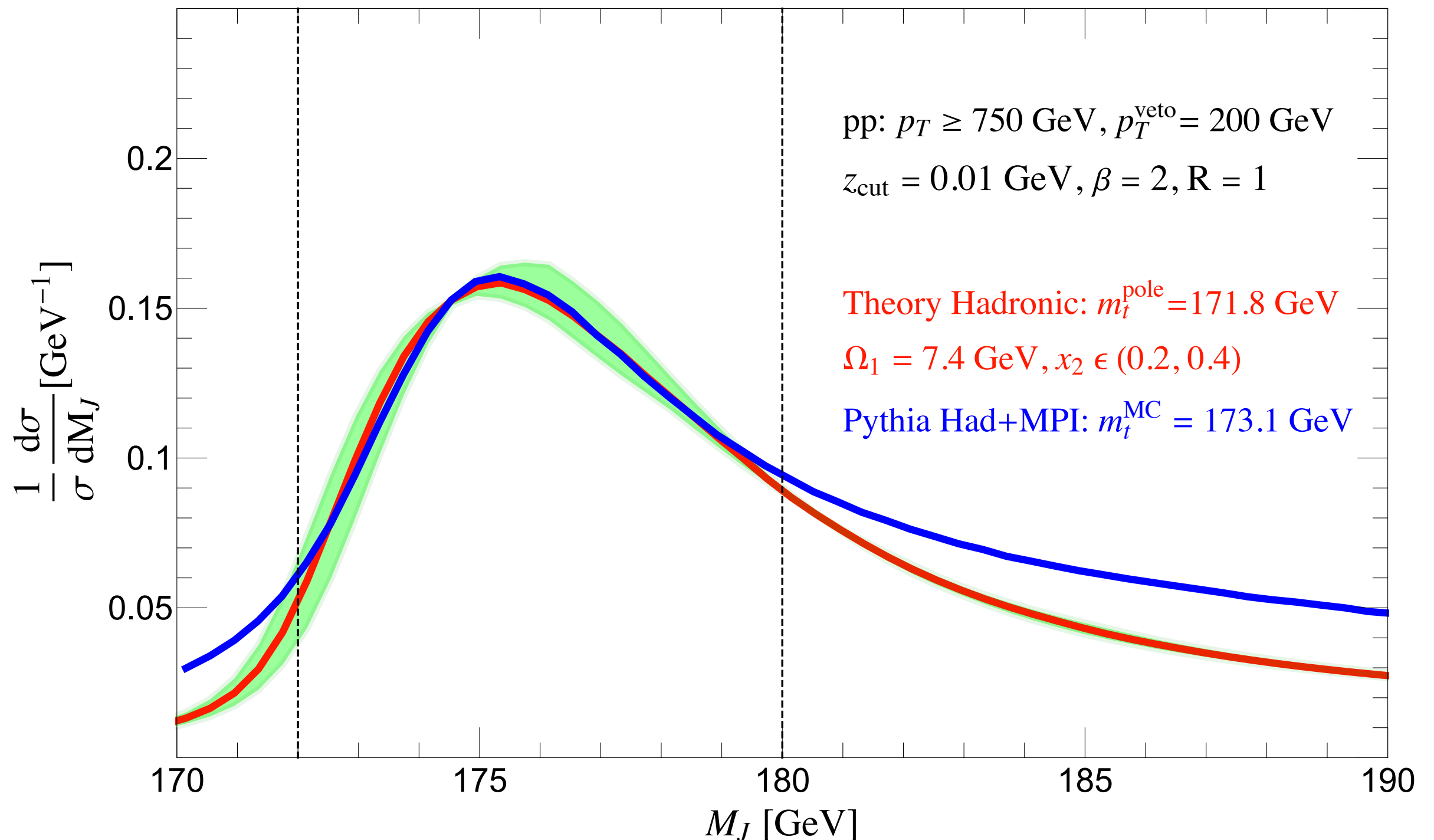
Translation of theory uncertainties to  
the fit parameters is in progress.



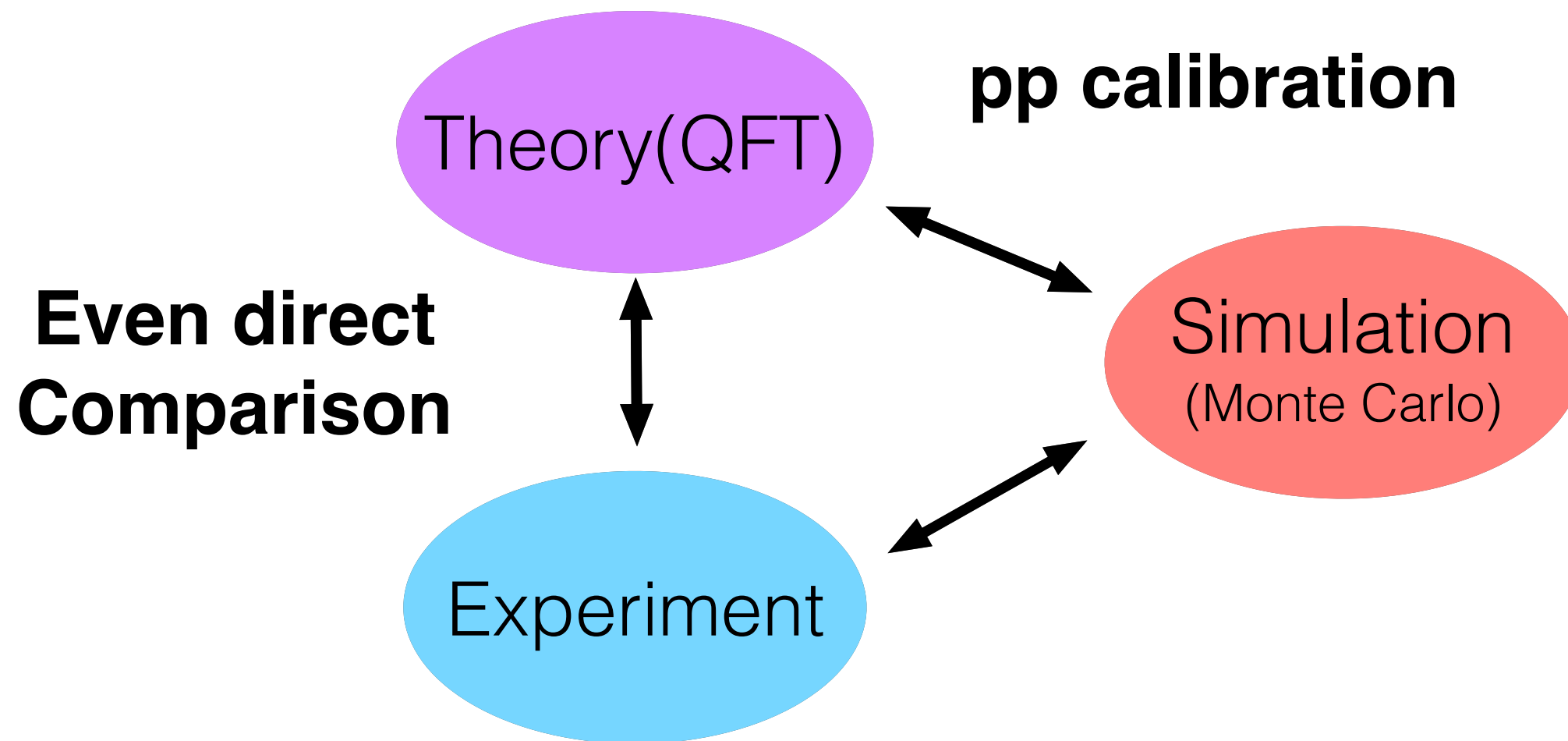
# Pythia Simulation vs. Theory (with Soft Drop)

**Testing sensitivity to higher moments:**

$$\Omega_1 = \int dk k F^{\text{model}}(k) \quad x_n = \frac{\Omega_n^c}{(\Omega_1)^n}$$



Looks very promising:



# Summary

- Probing the question: “What mass are we measuring?”
- Answers from connecting theory (QFT) to Simulations or Data.
- A promising new method to measure Top Quark Mass exploiting a light Soft Drop