





Matrix Element Methods for particle and event identification

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Jets@LHC Workshop

ICTS Bangalore

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24.01.2014

Nature:

Symmetries, Forces, Particles

Result in measurable objects, e.g. Jets, stable leptons, photons

Experiments measure radiation

Theory assumption:

Symmetries, Forces, Particles

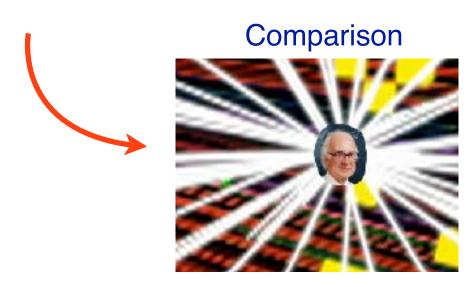


Encoded in Lagrangian Density

$$\mathcal{L} = \mathcal{L}_{\mathrm{EW}} + \mathcal{L}_{\mathrm{QCD}} + \mathcal{L}_{\mathrm{Higgs}}$$



Event Generators predict radiation



2

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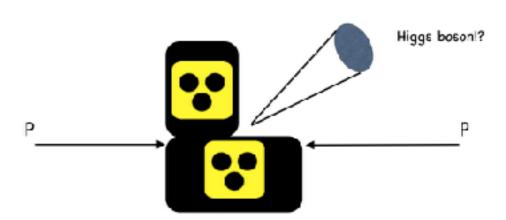
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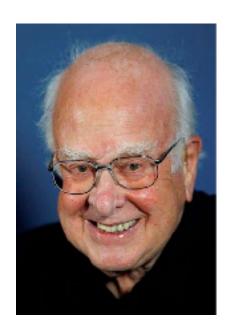


Identification exploits fact that quantum numbers of signal resonance different than backgrounds

Quantum numbers are:

mass, colour, spin, couplings (width)

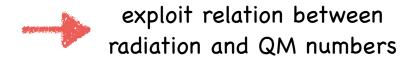


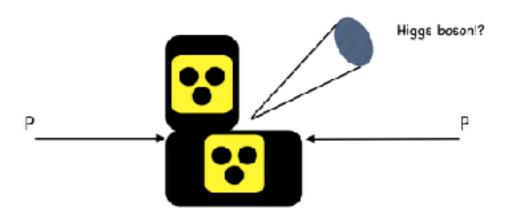


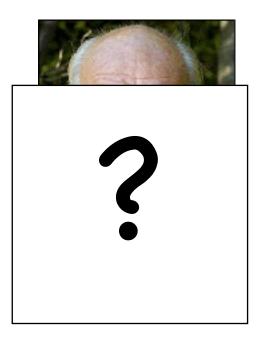
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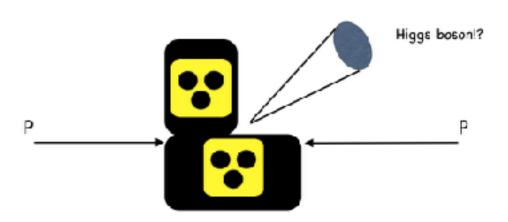


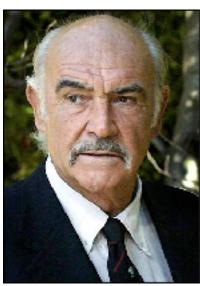


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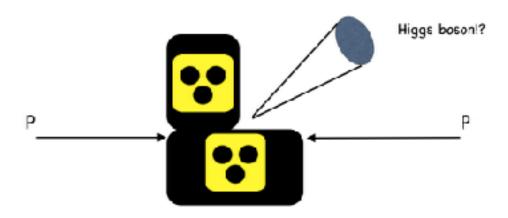


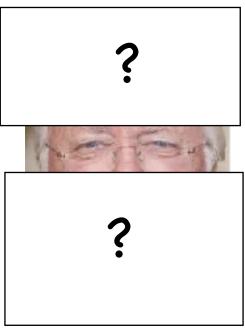
[Sean Connery]

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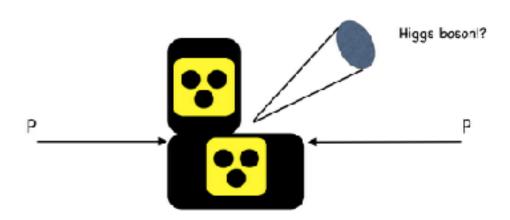


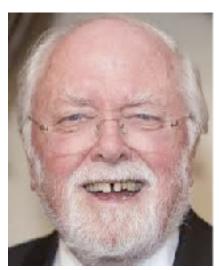


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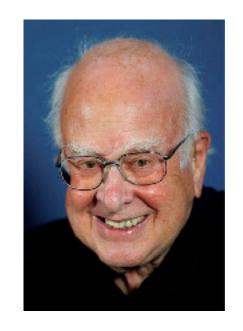
[Richard Attenborough]

Taking the full information simultaneously into account will give you the best chance to discriminate competing hypotheses

ICTS Bangalore



face recognition for object/event



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Result in measurable objects

Encoded in Lagrangian Density

$$\mathcal{L} = \mathcal{L}_{\mathrm{EW}} + \mathcal{L}_{\mathrm{QCD}} + \mathcal{L}_{\mathrm{Higgs}}$$

Matrix Enod Method Machine Learning

Experiments measure radiation

Event Generators predict radiation



"The strange death of theory"



Frankfurter Allgemeine Zeitung

23.01.2017

or is it?

Matrix Element Method vs Multi-variate Analysis (= pQCD = QFT)

Tilman's proposal from yesterday:

Matrix Element Method vs Multi-variate Analysis (= pQCD = QFT)

Tilman's proposal from yesterday:



- MVA well motivated to extract correlations without existing theory, i.e. stock trade
- In particle physics we established gauge theories, thus, we have existing theory to predict connection of 'input with output'
- Current pheno approach:

We take first-principle QFT: $\mathcal{L} = \mathcal{L}_{\mathrm{EW}} + \mathcal{L}_{\mathrm{QCD}} + \mathcal{L}_{\mathrm{Higgs}}$

Put it into an event generator to generate pseudo-data

Then a smart physicist or MVA comes up with way to access the Lagrangian we put in in the first place

Seems like an unnecessary detour...

Training MVAs on Monte Carlo

- MVAs will optimise for according to MC most sensitive exclusive phase space regions
 - → theory uncertainties difficult to control
- Full event generators are mashup of different parts that are partly tuned, i.e. hard interaction, UE, ISR,...
- Highly computationally intensive. If you want to template correlations of say 7 particles:
 - Time estimate:

7 microjets, each 4-momentum components divided into only 10 bins -> $10^{28}/7! \sim 10^{24}$ configurations

If MC takes 1 ms per event -> 10^{13} years to have 1 hit per config.

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We surrender to Tilman!

sensitive

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$$-> 10^{28}/7!$$

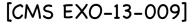
If MC takes 1 ms per event -> 1

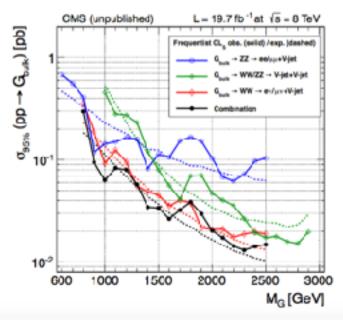


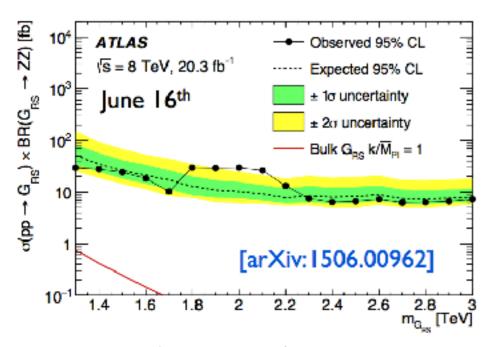
Training MVAs on data only

- Less plaqued by systematics
- But only possible if objects to reconstruct or events to measure already in data.
 - -> oxymoron for discovery of anything new, e.g. gluinotaq, axion-taq, pp->HH->4b,...
- Everything done purely on data without theory crosscheck has 0 safety margins...
- →2 TeV excess in ATLAS and CMS might be an example (though I am not saying that anything was done wrongly)

Brief interlude for the 2 TeV di-boson excess







- CMS sees small but consistently excesses in di-boson final states
- First excess in semileptonic final state using jet substructure from 2012

	CMS	ATLAS				
V _{jet} V _{jet}	1.3σ	3.4σ (2.5σ global)				
ℓℓ V _{jet}	2σ	=				
₹v V _{jet}	1.2σ	-				

 While masses seem consistent cross sections dont across channels

ATLAS VV excess

Most significant. Lets focus on this analysis

[Talk by C. Delitzsch at BOOST 2015]

Event Selection

- Compared to semileptonic analysis only boosted regime is considered
- Reject events with electron or muon candidate or $E_{\rm T}^{\rm miss} > 350$ GeV (orthogonal to other diboson resonance searches)
- Overlap between WW, WZ, ZZ selection due to chosen mass window
- Rapidity difference: $|y_1 y_2| < 1.2$
- ullet p_{T} asymmetry: $|(p_{\mathrm{T}_1}-p_{\mathrm{T}_2})|/(p_{\mathrm{T}_1}+p_{\mathrm{T}_2}) < 0.15$
- $m_{
 m JJ} > 1.05$ TeV: trigger plateau of large-R jet trigger



August 11, 2015

Searches for diboson resonances using boson tagging in ATLAS

1

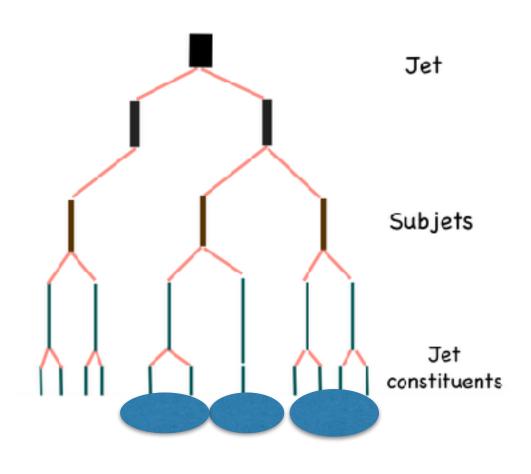
- For ungroomed fatjets pT,j > 540 GeV
- Reconstruction of VV final state follows same principles as discussed before

Resonance reconstruction

BDRS method

- Only y-cut applied when declustering
- y-cut fires, stop declustering and filter while keeping 1-3 subjets

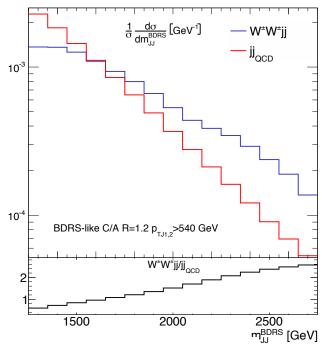
Filtering parameter	Value		
-√ y f	0.2		
$oldsymbol{\mu}_{ ext{f}}$	1		
$R_{\rm r}$	0.3		
$n_{\rm r}$	3		



[Goncalves, Krauss, MS '15]

Without theory background irrelevant in the control region can be significant in the signal region

there ELW backgrounds that have not been checked, but are in this case fortunately small!



cuts	$W' \to WZ$	jjąco	$t\bar{t}$	VV	Vj	Vjj_{EW}	jj_{EW}	$W^\pm W^\pm jj$	
	cross sections in fb								
BDRS $2J$ -tag, $p_{\perp}^{J} > 540 \text{ GeV}$	1.17	28302	45.6	5.34	370	50.8	119	0.50	
$\sqrt{y} > 0.45$	0.59	4290	9.7	0.67	44	5.4	10	0.1	
$ y_1 - y_2 < 1.2$	0.45	2791	8.0	0.52	24	3.2	5.8	0.06	
$ p_{T1} - p_{T2} /(p_{T1} + p_{T2}) < 0.15$	0.44	2776	7.8	0.51	24	3.2	5.74	0.054	
WZ selection	0.21	26.7	0.18	0.25	0.83	0.01	0.22	0.0005	
WZ selection, $1.9 < m_{JJ} < 2.1~{\rm TeV}$	0.14	0.33	0.002	0.04	0.01	0.0002	0.002	0.00001	

TABLE I: Cut-flow analysis for signal and SM background components. The selections follow the ATLAS publication and the cross-sections are given in fb.

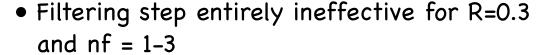
But reconstruction algorithm can also seize to work in signal region

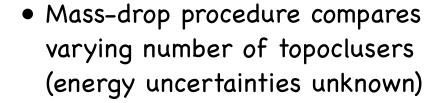
• Why start with R=1.2 jets when searching for W/Z with 1-2 TeV pT?

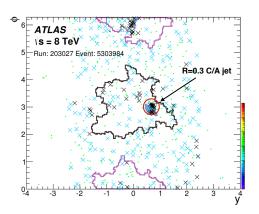
$$\Delta R_{q\bar{q}} \simeq \frac{2m_W}{p_T} \simeq 0.12 \cdots 0.4$$

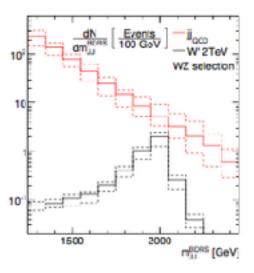
W/Z decay products in small area of detector

Jet absorbs lots of radiation from diff. sources



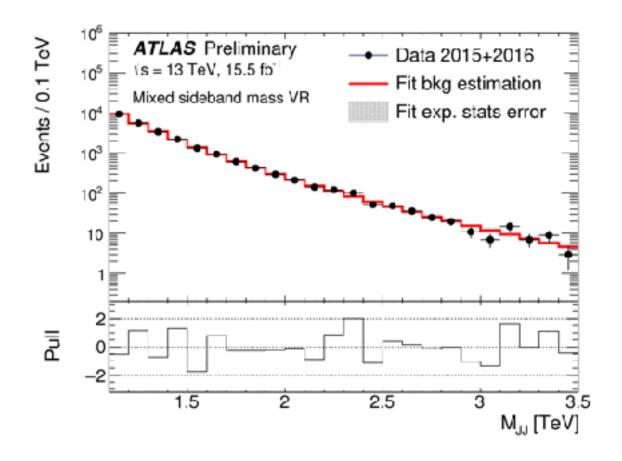




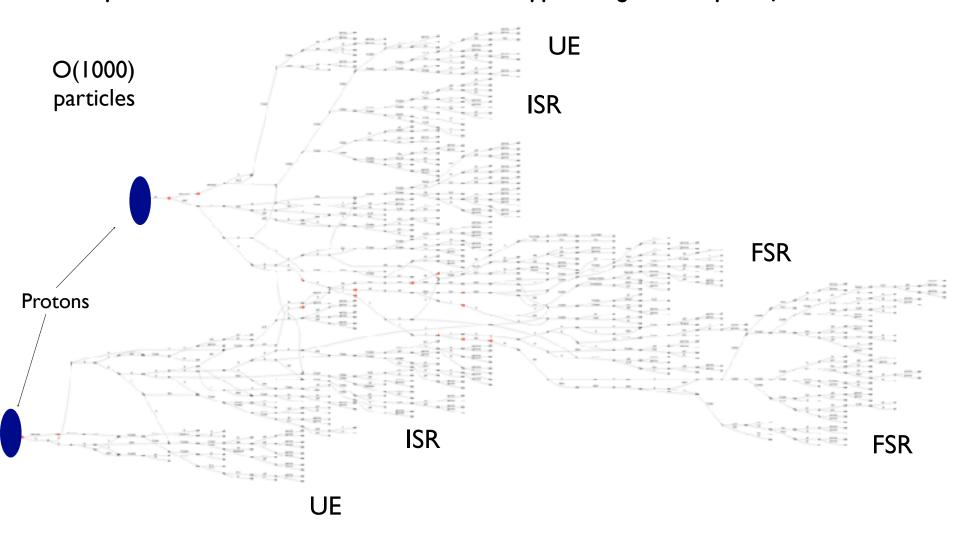


End of the story:

 Tagging algorithm changed to D2 and resonance was not seen in 13 TeV runs...

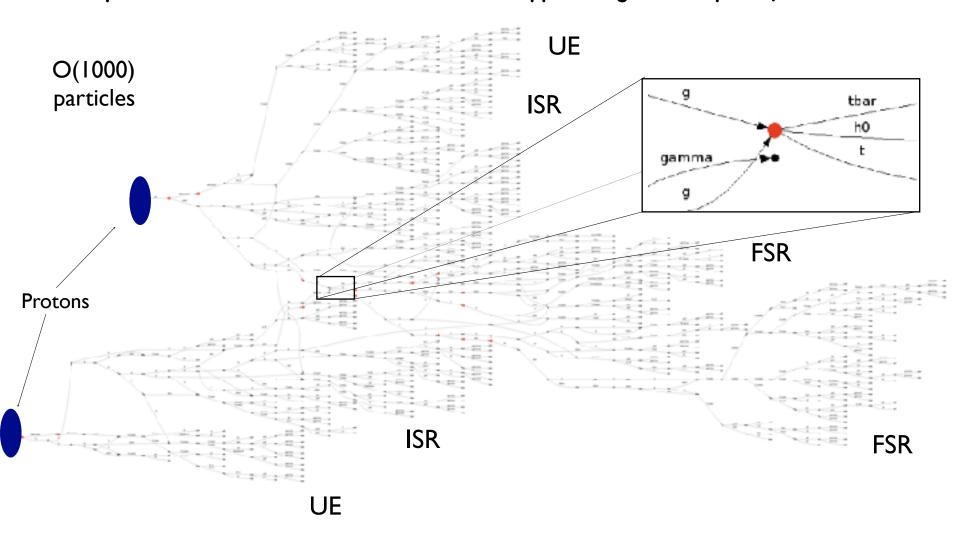


Is it possible to use matrix element methods approach given complexity of LHC events?



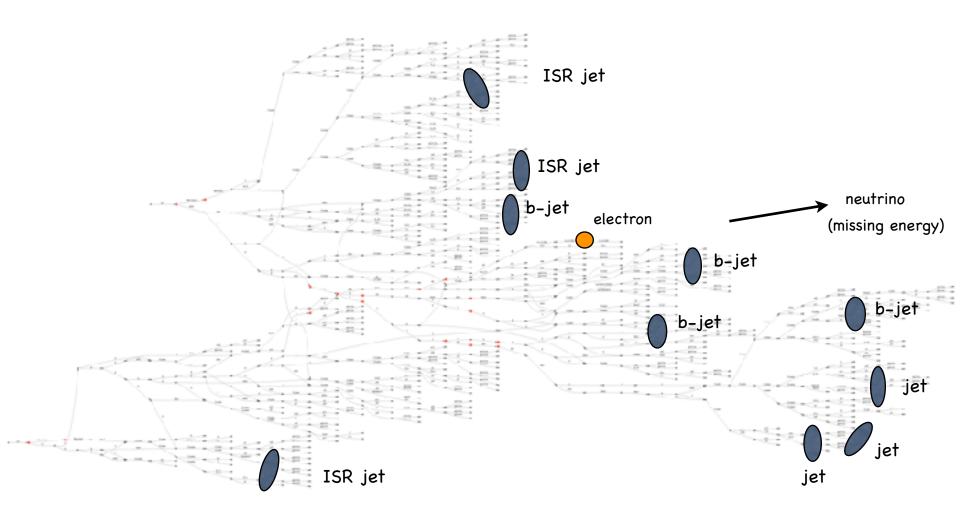
At least full event generators do a good job reproducing data...

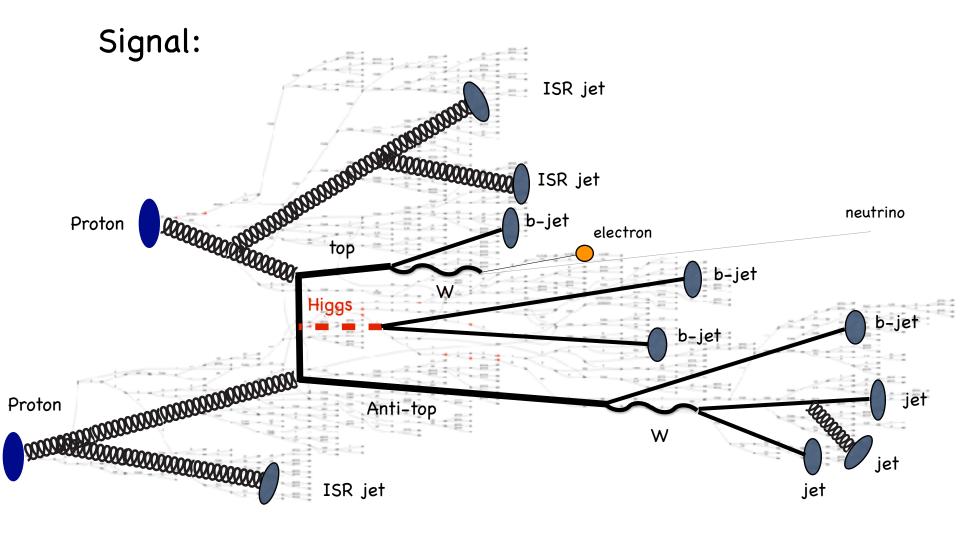
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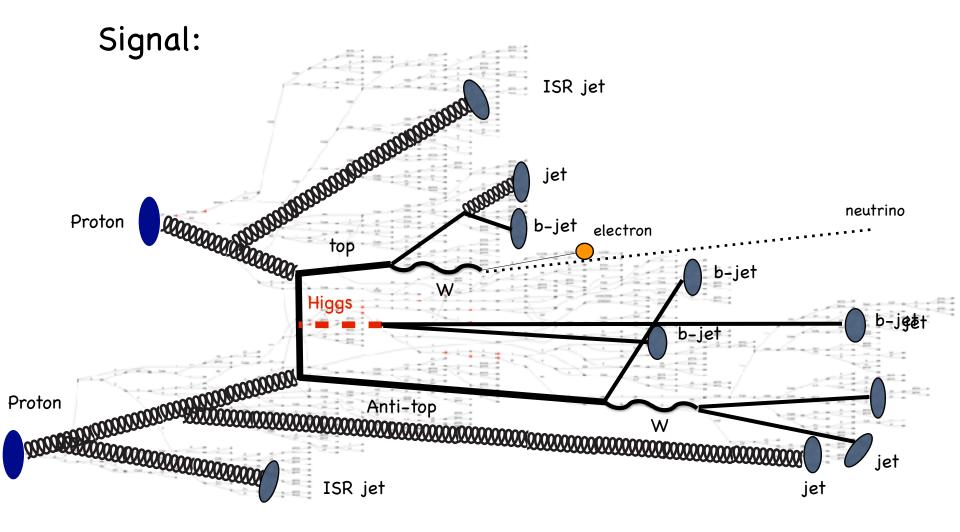


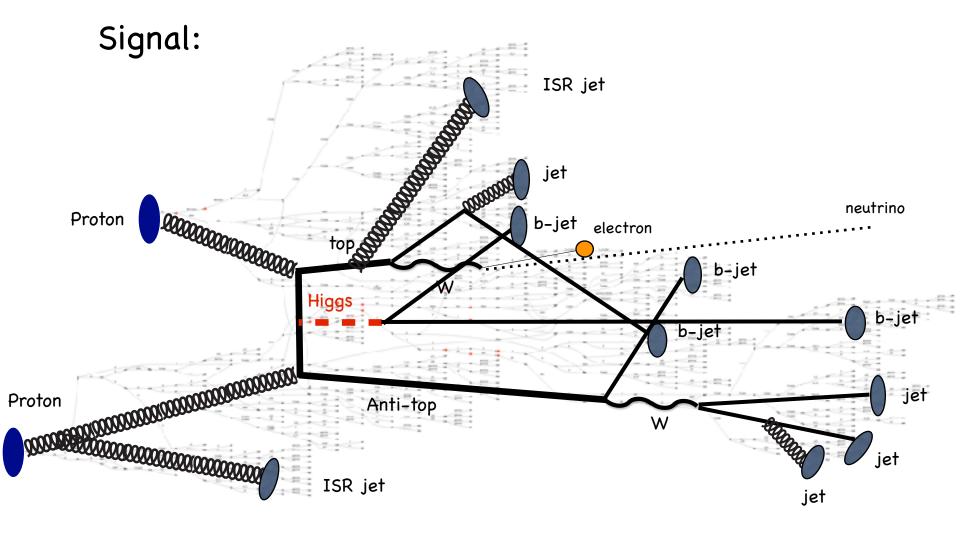
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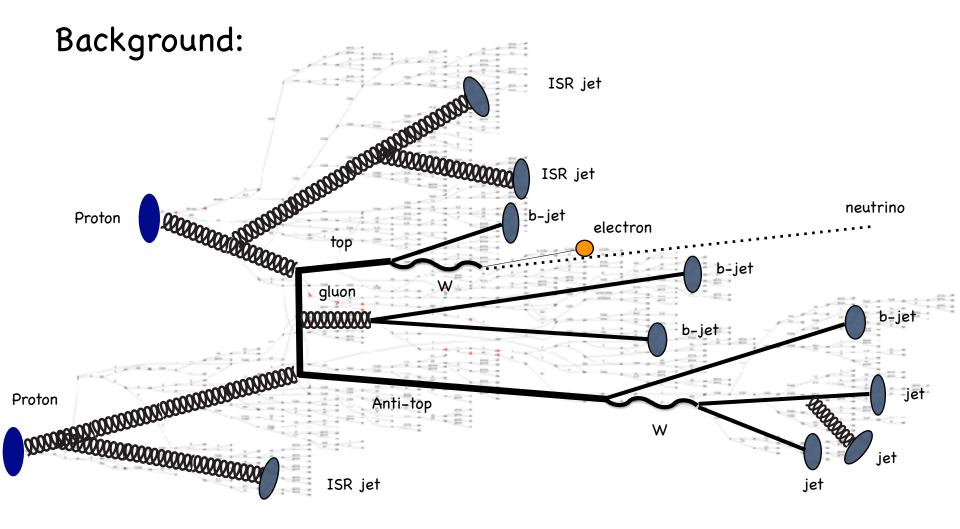
Inverse Problem: Final state measured ('phase space point chosen')



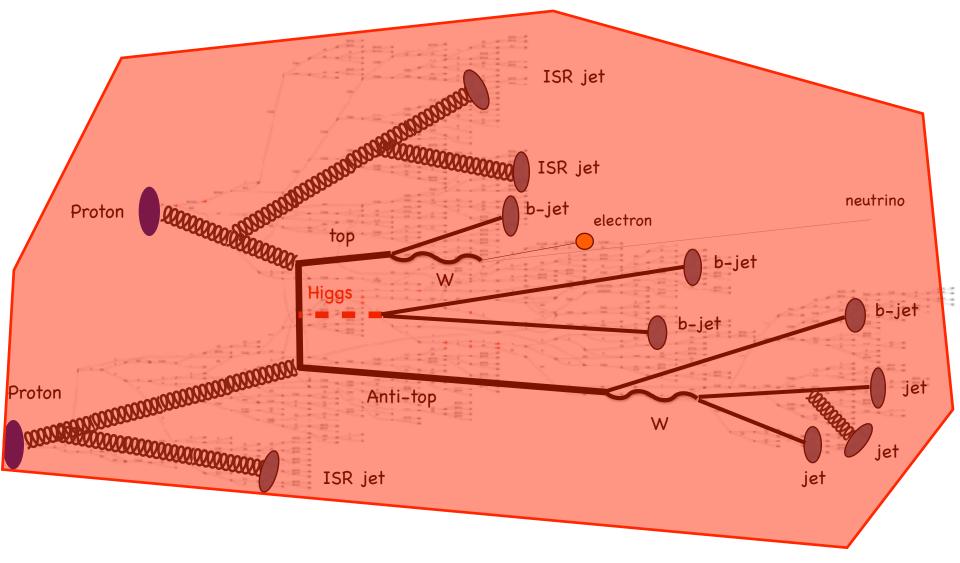








Ideally one would like to use all radiation related to hard process to discriminate signal from background



Applications of Matrix Element Method:

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Rec. of events with MET [Kondo, J.Phys.Soc.Jap. (1988)]

Anomalous gauge couplings [Diehl, Nachtmann Eur.
Phys. J. C1 (1998)]

top quark physics [Abazov et al., Nature (2004), D0 Collab.]

[Abulencia et al., PRD 73 (2005), CDF Collab.]

[Abazov et al., PLB 617 (2005), D0 Collab.]
```

2010 Automated implementation in MadWeight

[Artoisenet et al, JHEP 1012 (2010)]

Plenty of recent applications in Higgs physics:

```
H 
ightarrow \mu^+ \mu^- [Cranmer, Plehn EPJC 51 (2007)] H 
ightarrow b ar{b} [Soper, MS PRD 84 (2011)] H 
ightarrow \gamma \gamma [Andersen, Englert, MS PRD 84 (2013)] pp 
ightarrow t ar{t} H [Artoisenet et al. PRL 111 (2013)] H 
ightarrow ZZ^*/WW^*/Z\gamma [Campbell et al JHEP 1211 (2012)] [Freitas et al PRD 88 (2013)] [Campbell et al PRD 87 (2013)]
```

Spin/Parity [Avery, et al. PRD 87 (2013)] [Gao et al. PRD 81 (2010)]

The matrix element method in a nutshell:

Given a theoretical assumption α , attach a weight $P(\mathbf{x}, \alpha)$ to each experimental event \mathbf{x} quantifying the validity of the theoretical assumption α for this event.

$$P(\mathbf{x}, \alpha) = \frac{1}{\sigma} \int d\phi(\mathbf{y}) |M_{\alpha}|^{2}(\mathbf{y}) W(\mathbf{x}, \mathbf{y})$$

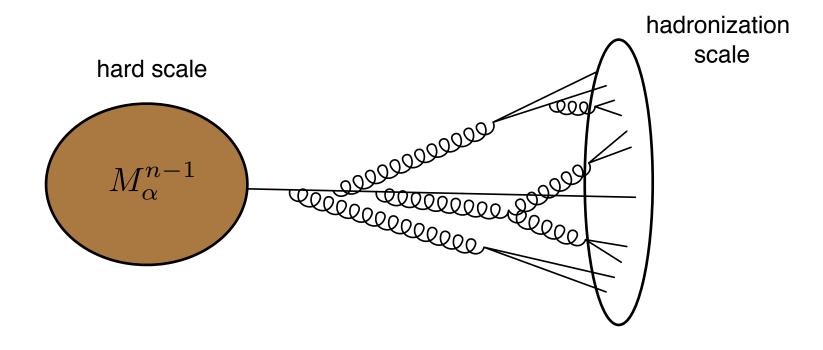
 $|M_{lpha}|^2$ is squared matrix element

 $W(\mathbf{x}, \mathbf{y})$ is the resolution or transfer function

 $d\phi(\mathbf{y})$ is the parton-level phase-space measure

The value of the weight $P(\mathbf{x}, \alpha)$ is the probability to observe the experimental event \mathbf{x} in the theoretical frame α

Purpose of the transfer function is to match jets to partons



Probability density function: $\int d\mathbf{y} \ W(\mathbf{x}, \mathbf{y}) = 1$

The form of the transfer function:

resolution in

$$W(\mathbf{x}, \mathbf{y}) \approx \Pi_i \frac{1}{\sqrt{2\pi}\sigma_{E,i}} e^{-\frac{(E_i^{rec} - E_i^{gen})^2}{2\sigma_{E,i}^2}}$$

Energy

$$\times \frac{1}{\sqrt{2\pi}\sigma_{\phi,i}} e^{-\frac{(\phi_i^{rec} - \phi_i^{gen})^2}{2\sigma_{\phi,i}^2}}$$

azimuthal angle

$$\times \frac{1}{\sqrt{2\pi}\sigma_{y,i}} e^{-\frac{(y_i^{rec} - y_i^{gen})^2}{2\sigma_{y,i}^2}}$$

rapidity

Complex, high-dimensional gaussian distribution!

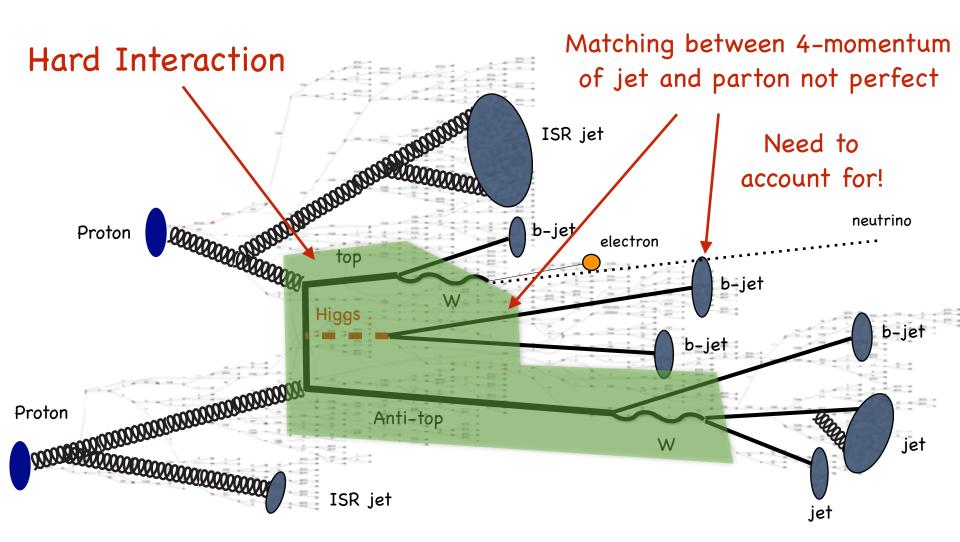
Transfer function introduces new peaks on top of propagators

Subtleties of the convolution $|M(y)|^2 \times W(y,x)$

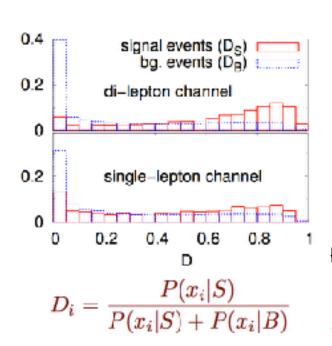
- 1) $|M(y)|^2$
 - Can be calculated at different order in pert. series (LO, NLO)
 - Final state multiplicity fixed (exclusive process)
 - Some kinematic configurations induce large logs (need resummation)
- 2) W(y,x)
 - Number of final state objects limited to exclusive process
 - Integration very time consuming -> limits final state multiplicity
 - Transfer function fit dependent (input from experiment)

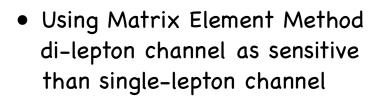
tth: di-lepton vs semileptonic channel

[Artoisenet et al. PRL 111 (2013)]



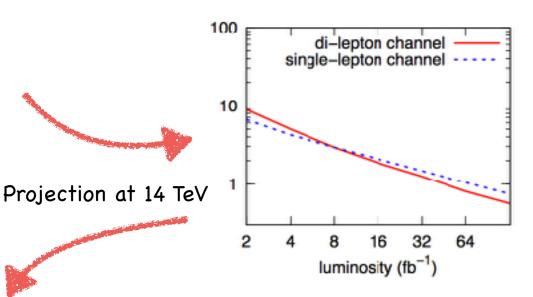
- Analysis with 4 b-jets and std reconstruction as input to MEM
- Full integration over invisible particles





[Artoisenet et al. PRL 111 (2013)]

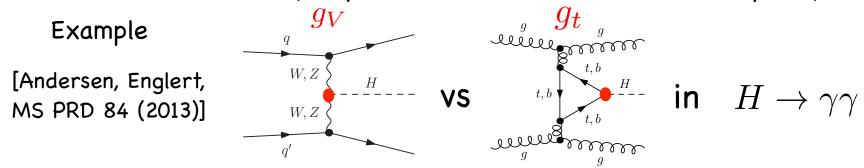
process	incl. σ	efficiency	$\sigma^{ m rec}$
$t\bar{t}h$, single-lepton	111 fb	0.0485	5.37 fb
$t\bar{t}h$, di-lepton	17.7 fb	0.0359	0.634 fb
tt+jets, single-lepton	$256~\mathrm{pb}$	0.463×10^{-3}	119 fb
$tar{t}+{ m jets},$ di-lepton	40.9 pb	0.168×10^{-3}	6.89 fb



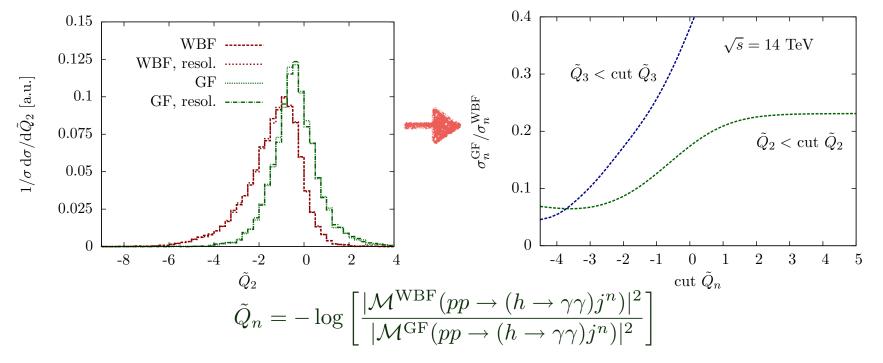
 However, single-lepton channel uses standard input,
 boosted region not captured [Plehn, Salam, MS PRL 104 (2009)]

We want to study more objects in final state -> Transfer function limits us. Do we always need it?

Transfer functions only important if matrix element varies quickly:

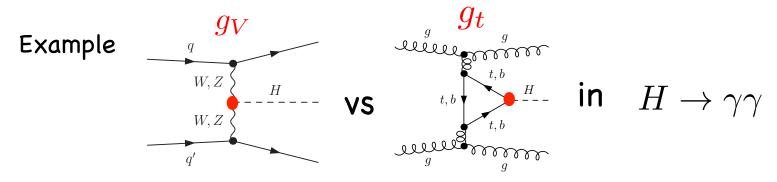


Higgs reconstructed, but no transfer function for jets:

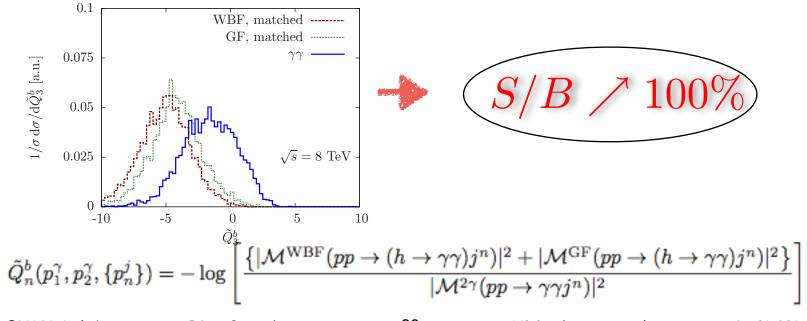


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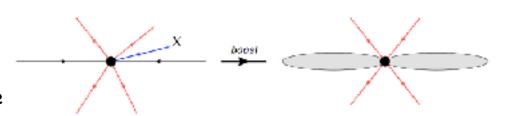
Higgs reconstructed, but no transfer function for jets:



After removing transfer function we can improve on precision of matrix element $|M(y)|^2$

Matrix element method at NLO: [Campbell, Giele, Williams JHEP 1211 (2012)]

Boost along transverse and longitudinal direction such that LO final state multiplicity momenta balance





Born phase space, but long. boost not unique, need longitud. integration

$$\mathcal{P}_{NLO}^{MEM}(\{Q_n\}) = \frac{1}{\sigma_{NLO}} \int_{x_{min}}^{x_{max}} dx_1 \mathcal{P}_{NLO}(\Phi_B)$$



Calculate virtual for born topology real for jet function

$$\eta^{lab,i} = \frac{1}{2} \log \left(\frac{x_a^2 s}{s_{ab}} \frac{s_{ib}}{s_{ai}} \right)$$

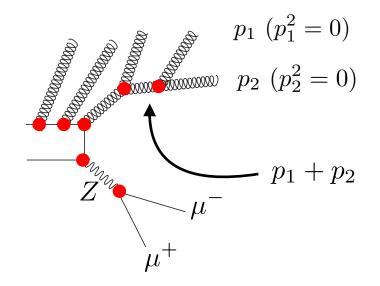


Application to H->4l (boost easier to identify)

sensitivity LO vs NLO improvement ~ 10%

Parton shower in a nutshell

The parton shower bridges the gap from the hard interaction scale down to the hadronization scale O(1) GeV



partons from the hard interaction emit other partons (gluons and quarks)

These emissions are enhanced if they are collinear and/or soft with respect to the emitting parton

Probability enhanced in soft and collinear region due to ~ $1/(p_1+p_2)^2$

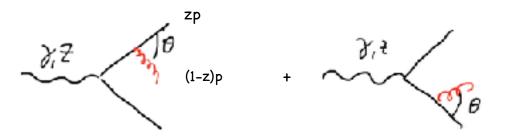
• If
$$p_1 \to 0$$
, then $1/(p_1 + p_2)^2 \to \infty$

$$ullet$$
 If $p_2 o 0$, then $1/(p_1+p_2)^2 o \infty$

• If
$$p_2 \to \lambda p_1$$
, then $1/(p_1 + p_2)^2 \to \infty$

Example

$$e^+e^- \to 3 \text{ jets}$$



Collinear limit:

$$d\sigma_{ee \to 3j} \approx \sigma_{ee \to 2j} \sum_{j \in \{q,\bar{q}\}} \frac{\alpha_s}{2\pi} \frac{d\theta_{jg}^2}{\theta_{jg}^2} P(z)$$

$$P_{q \to qg} = C_F \frac{1+z^2}{1-z}$$
 $P_{g \to gg} = C_A \frac{(1-z(1-z))^2}{z(1-z)}$ $P_{g \to q\bar{q}} = T_R n_f (z^2 + (1-z)^2)$

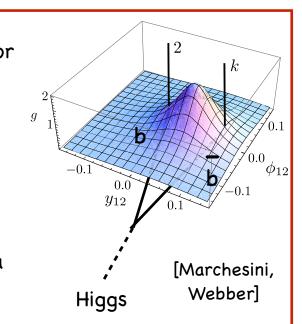
Soft limit: $E_g o 0$ $k^\mu \ll p_i^\mu$ the matrix element for

$$e^+e^- o \bar{q}qg$$
 factorizes (Eikonal Current)



$$|\mathcal{M}_{q\bar{q}g}|^2 = |\mathcal{M}_{q\bar{q}}|^2 g_s^2 C_F \frac{2p_1 \cdot p_2}{p_1 \cdot k \ p_2 \cdot k}$$

In the large Nc limit most radiation occurs in a cone between colour partners



Factorization of emissions and Sudakov factors allow semiclassical approximation of quantum process:

Sudakov form factor:

$$\mathcal{P}_{\text{nothing}}(0 < t \le T) = \lim_{n \to \infty} \Pi_{i=0}^{n-1} \mathcal{P}_{\text{nothing}}(T_i < t \le T_{i+1})$$

$$= \lim_{n \to \infty} \Pi_{i=0}^{n-1} \left(1 - \mathcal{P}_{\text{something}}(T_i < t \le T_{i+1})\right)$$

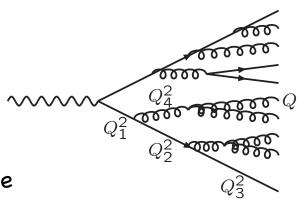
$$= \exp\left(-\int_0^T \frac{d\mathcal{P}_{\text{something}}(t)}{dt}dt\right)$$

$$\to d\mathcal{P}_{\text{first}}(T) = d\mathcal{P}_{\text{something}}(T) \exp\left(-\int_0^T \frac{d\mathcal{P}_{\text{something}}(t)}{dt}dt\right)$$

Sudakov form factor provides "time" ordering of shower:

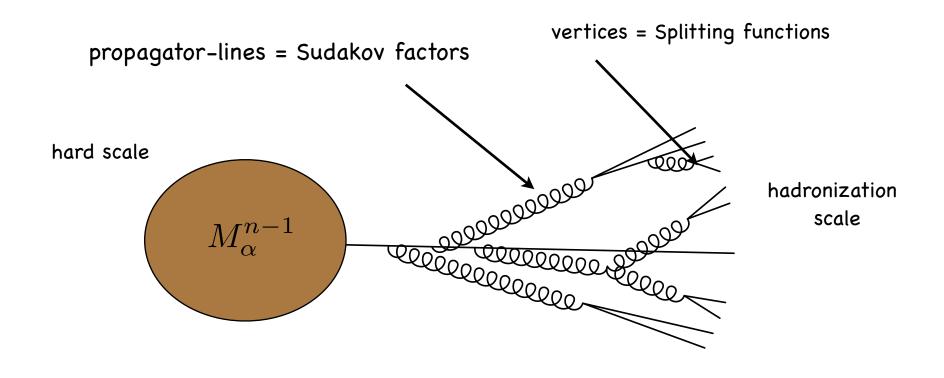
$$Q_1^2 > Q_2^2 > Q_3^2$$

 $low Q^2 \iff longer time$

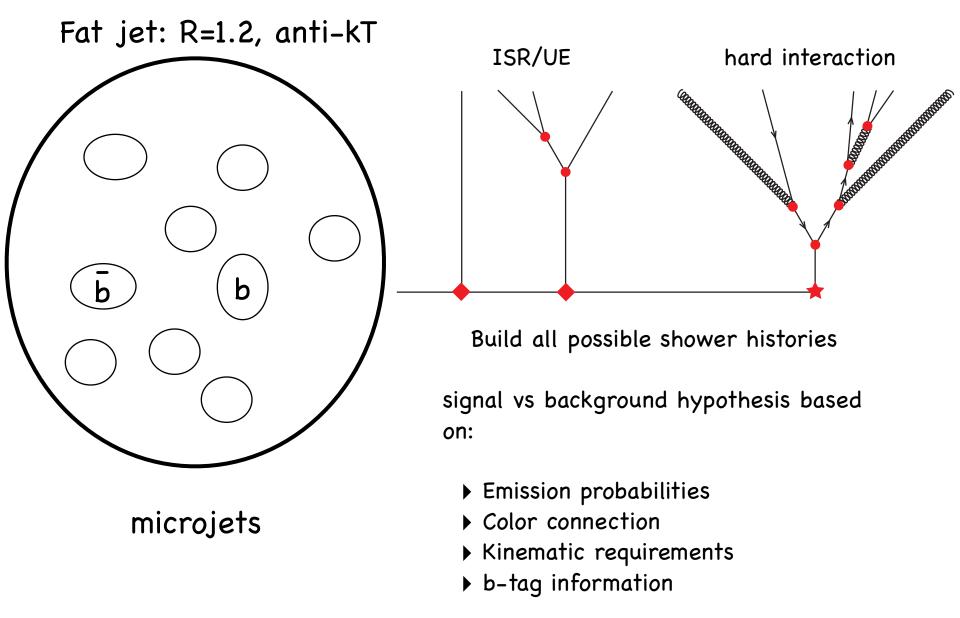


In summary:

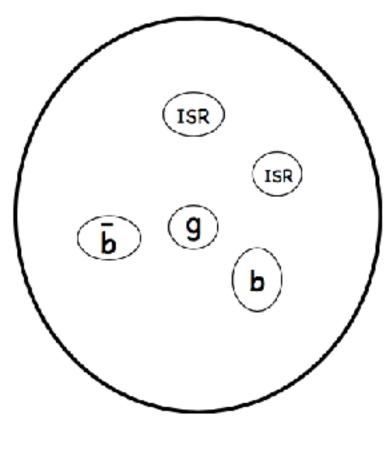
The probability weights in the evolution from the hard interaction scale to the hadronization scale are given by Sudakov factors and splitting functions.



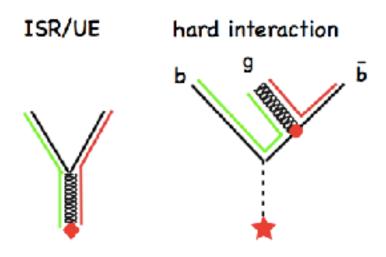
Shower deconstruction = first-principal calculation for resummed MEM



Fat jet: R=1.2, anti-kT



microjets

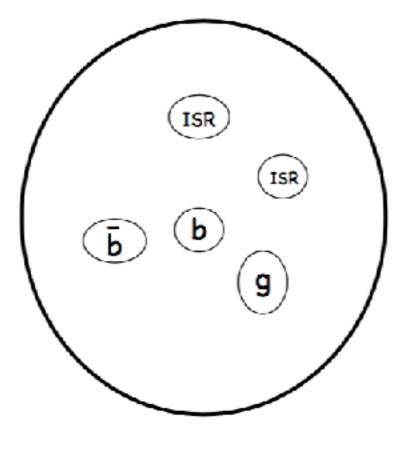


Build all possible shower histories

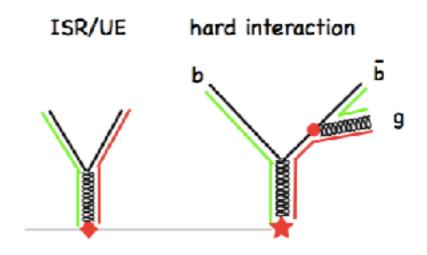
signal vs background hypothesis based on:

- ▶ Emission probabilities
- Color connection
- Kinematic requirements
- ▶ b-tag information

Fat jet: R=1.2, anti-kT



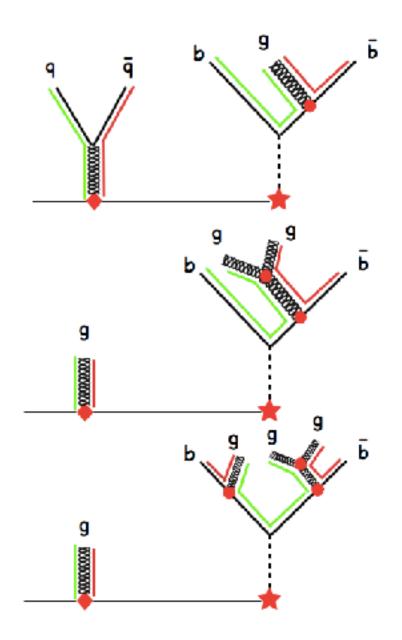
microjets

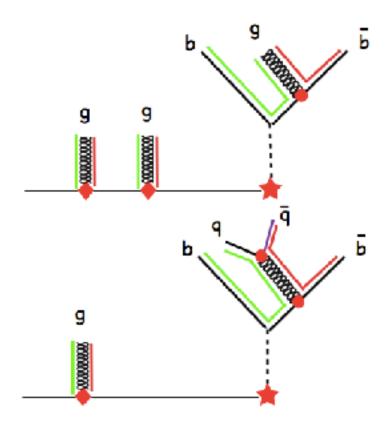


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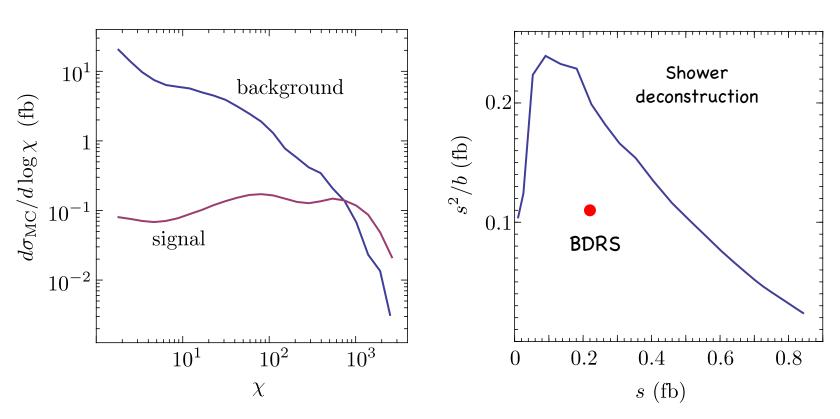




- And many more...
- And for all backgrounds...

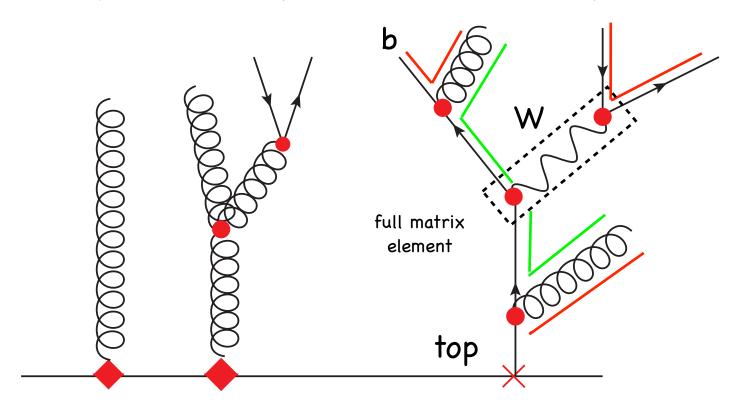
Results for Higgs boson:

$$\chi(\{p, t\}_N) = \frac{P(\{p, t\}_N | S)}{P(\{p, t\}_N | B)}$$



imperfect b-tagging (60%,2%) no b-tag required

Analogously for the top decay (more involved as top colored)

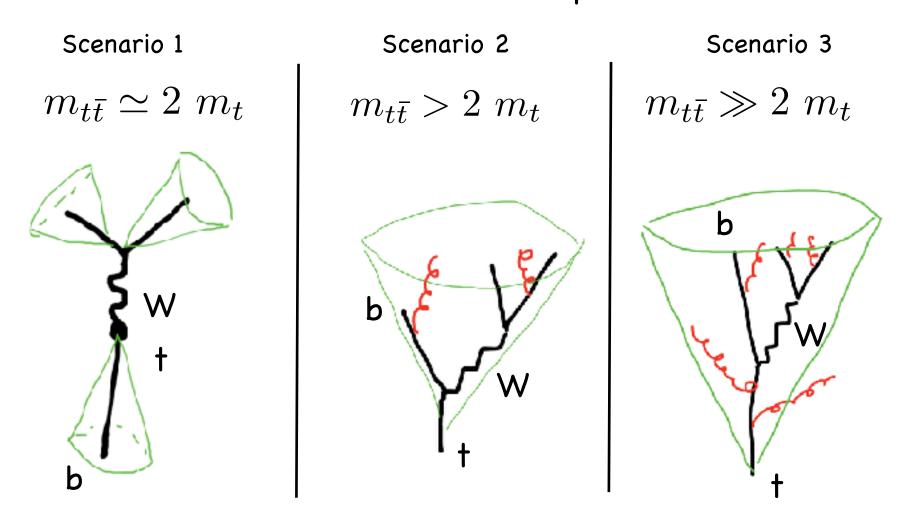


Conceptional difference compared to Higgs from last year:

- Splitting functions for massive emitter and spectator
- Full matrix element for top decay

$$\chi(\{p,t\}_N) = \frac{P(\{p,t\}_N|\mathbf{S})}{P(\{p,t\}_N|\mathbf{B})} = \frac{\sum_{\text{histories}} H_{ISR} \cdots \sum_{\text{histories}} |\mathcal{M}|^2 H_{\text{top}} e^{-S_{t_1}} H_{tg}^s e^{-S_g} \cdots}{\sum_{\text{histories}} H_{ISR} \cdots \sum_{\text{histories}} H_g^b e^{S_g} H_{ggg} \cdots}$$

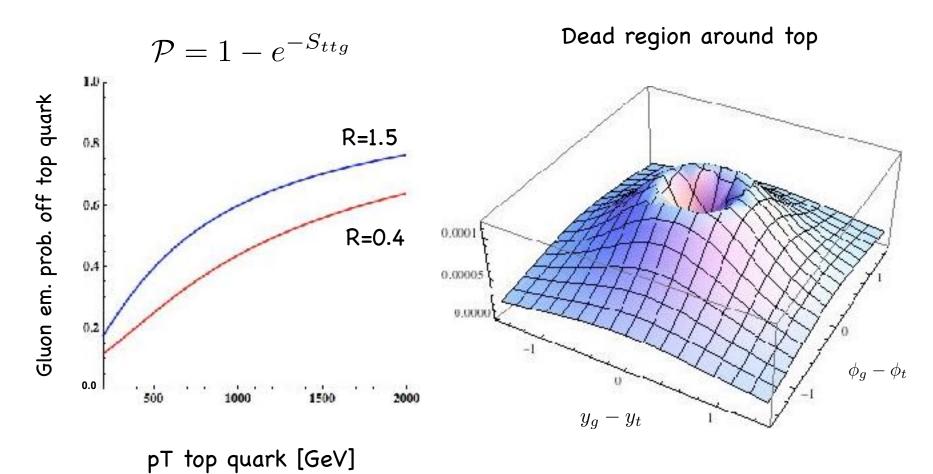
Different scenarios based on pT vs mass



Standard (resolved) reconstruction focuses on Scenario 1
Physics cases require Scenarios 2 and 3 -> tagging for accelerated charges

Top 2015 Ischia

Characteristic radiation profiles for gluon emissions from tops

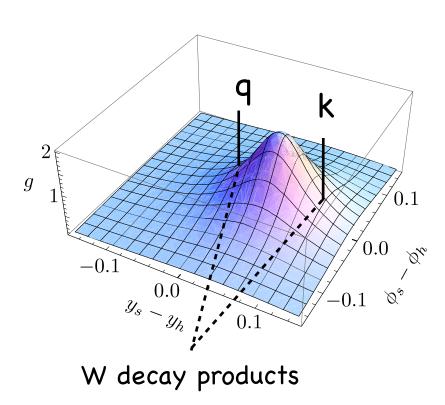


pT top 500 GeV, pT gluon 20 GeV

Radiation off bottom quark down to hadronization scale

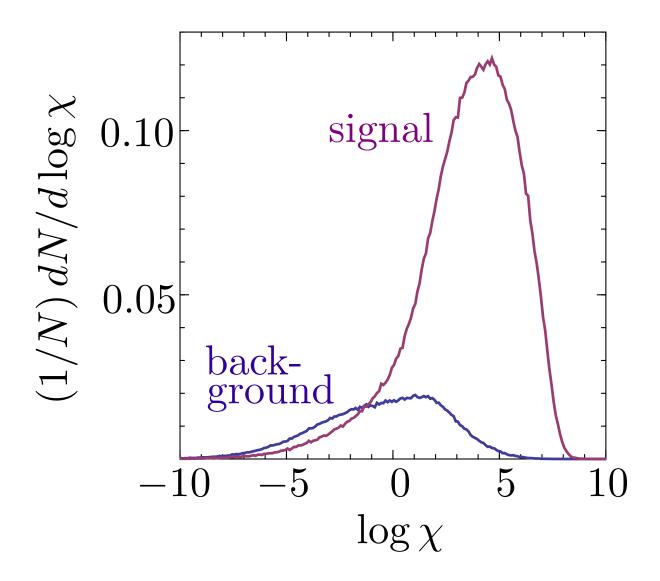
$\mathcal{P} = 1 - e^{-S_{bbg}}$ Gluon em. prob. off b quark 1.0 0.8 0.6 0.4 0.2 0.0 pT top quark [GeV] pT bottom = pT top / 3

angular distribution for radiation off W decay products

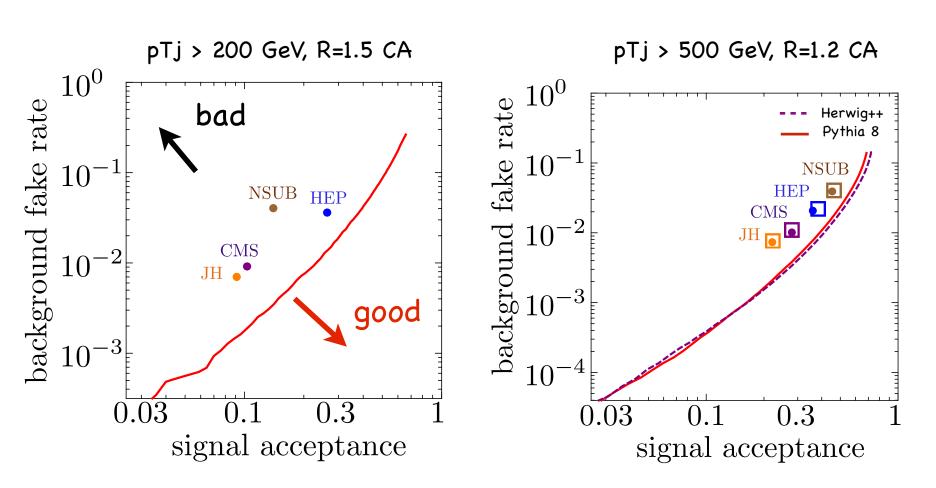


All calculated and build-in into shower/event deconstruction

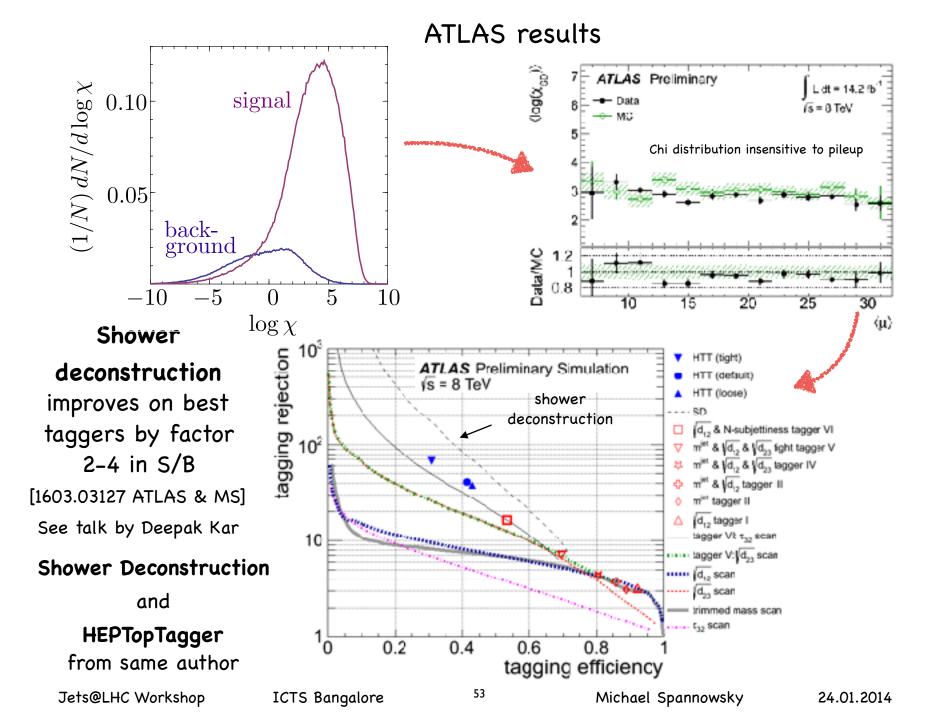
chi distribution for top vs QCD



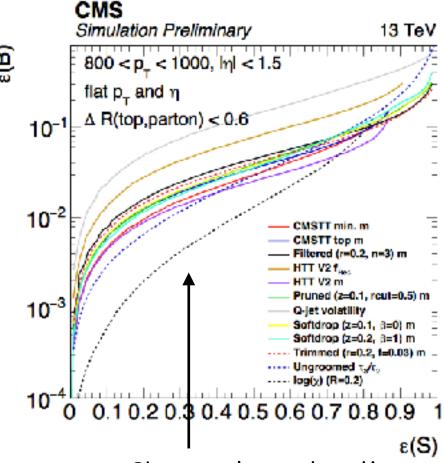
Results for top quark tagging:



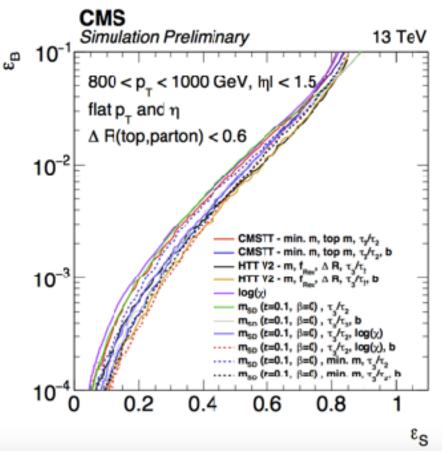
microjets: kT, R=0.2, pT>5 GeV



Results by CMS



 Shower deconstruction best single variable

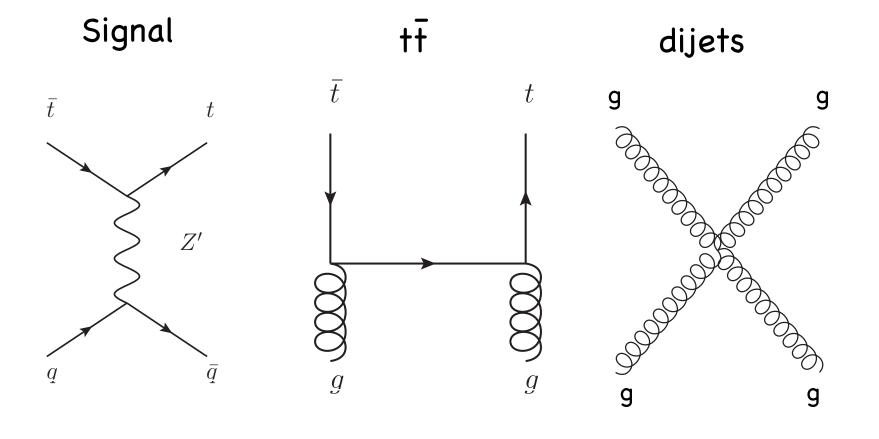


 Efficiencies matched if taggers combined

First application of Event Deconstruction = full event MEM + parton shower resummation

fully hadronic Z' -> tt

[Soper, MS '14]



Model: mass Z' = 1500 GeV with width = 65 GeV

Event selection:

2 fat jets with pT > 400 GeV jet algorithm CA R=1.5

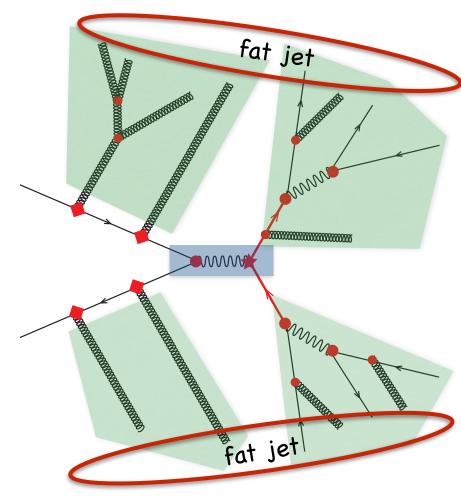
Cross section after ES:

dijets 1.73 nb

ttbar 2.27 pb

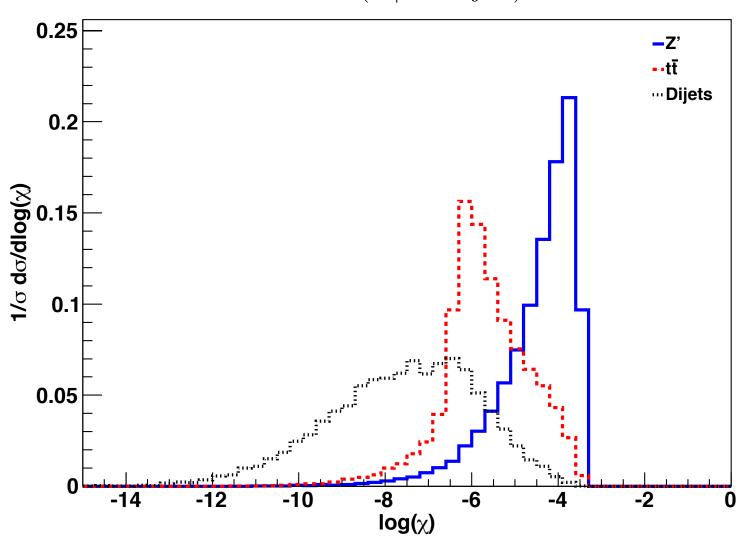
Recluster fatjet constituents using microjets kT R=0.2 pT>10 GeV

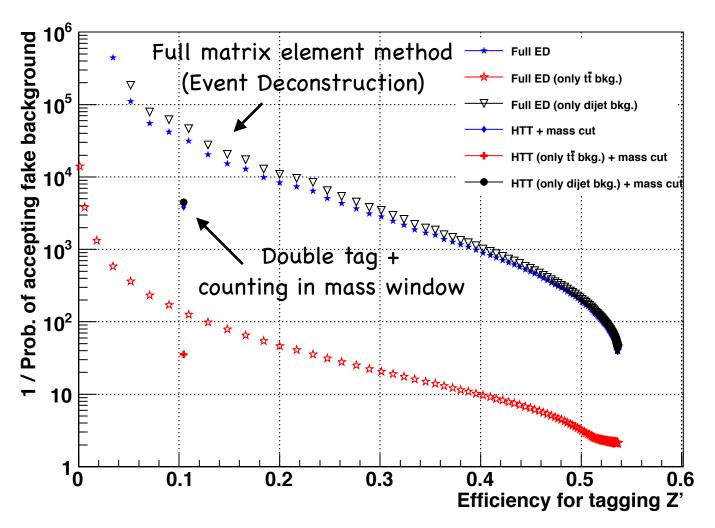
Z' width in Event Dec. 130 GeV



Hard matrix element generated with MadGraph5

$$\chi = \frac{P(X|Z')}{P(X|t\bar{t} + \text{dijets})}$$





Event Dec: eff: 0.109538

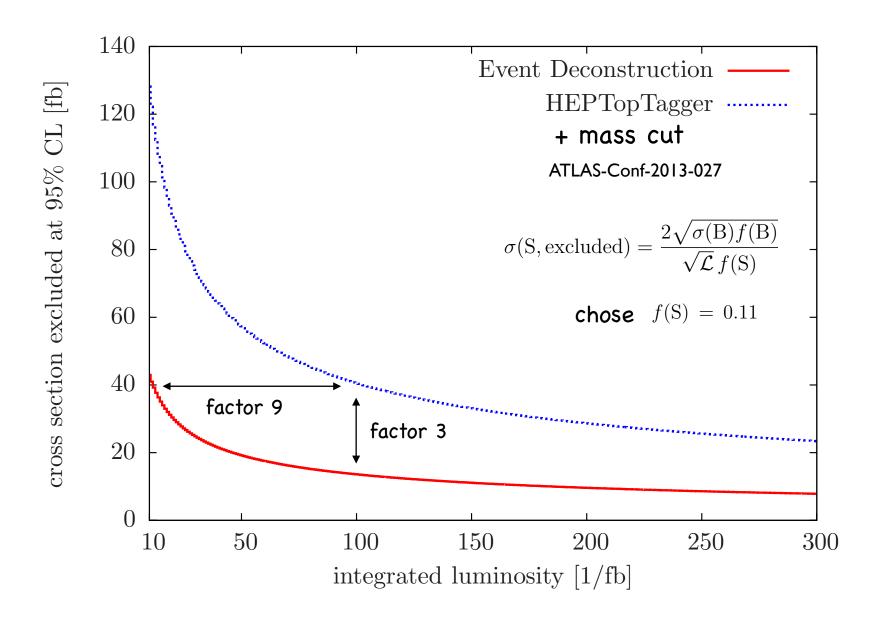
fkr: 3.20063e-05

1/fkr: 31243.8

HTT: eff: 0.104659

fkr: 0.000259946

1/fkr: 3846.95



Brief comment on Tilman's 'challenge'

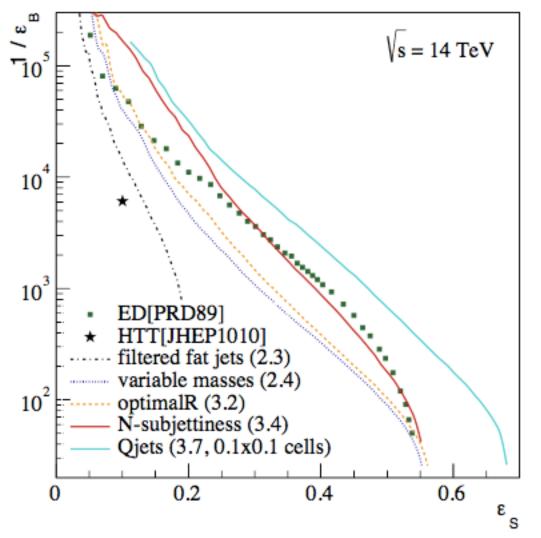
3 theorists and 2 CMS postdocs worked for 1 year vs

1 week unoptimised implementation of Event Deconstruction by 1 person

ED includes mimic of detector response using imperfect width measurement in matrix element

huge improvement due to QJets rather peculiar...

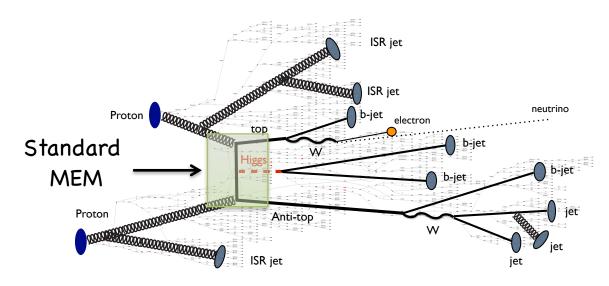
[Kasieczka, Plehn, Schell, Strebler, Salam '15]



Summary

- Matrix Element Method is active field of research
 [see also MEM Workshops in Louvain (2013) and Zurich (2014)]
- Current interest in machine-learning is not taking matrix element methods out of the picture! MEM can help to check MVAs
- My personal view:

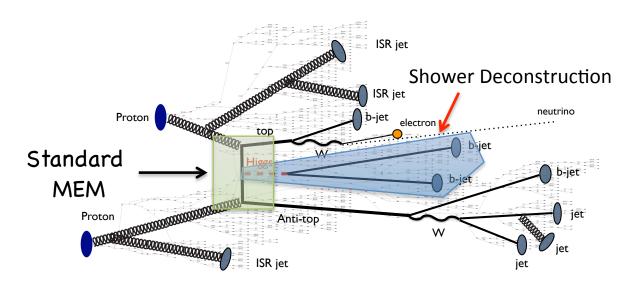
MEM is much more than object identification!



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- My personal view:
 Event Deconstruction, i.e. Pattern Recognition for full event

