

Distinguishing Integrable and Non-Integrable Systems using Quantum Quenches

Rajeev Singh

rajeevs.phy@itbhu.ac.in

Indian Institute of Technology (BHU), Varanasi



M. Tech. Project of
Abhishek Raj,
IIT(BHU)

Financial
Support
DST-SERB



*5th Indian Statistical
Physics Community
Meeting 2018*

ICTS, Bengaluru
February 18, 2018

Introduction

Loschmidt echo in
spin chains

System

Time evolution and
reversal

Entanglement at echo

Fluctuation in
entanglement

Entanglement
fluctuation at echo

Overview

Introduction

Loschmidt echo in spin chains

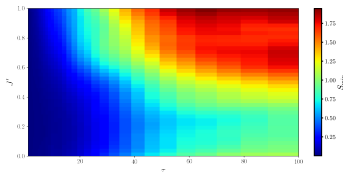
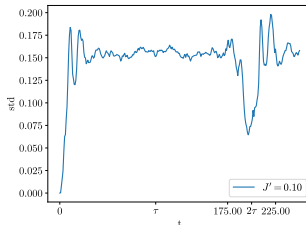
System

Time evolution and reversal

Entanglement at echo

Fluctuation in entanglement

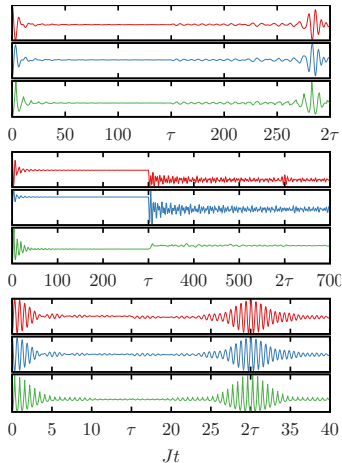
Entanglement fluctuation at echo



Effective time reversal and echo dynamics in the transverse field Ising model

MARKUS SCHMITT and STEFAN KEHREIN

Institute for Theoretical Physics, Georg-August-Universität Göttingen - Friedrich-Hund-Platz 1, Göttingen 37077, Germany



Schmitt, Kehrein (2016)

Introduction

Loschmidt echo in spin chains

System

Time evolution and
reversal

Entanglement at echo

Fluctuation in
entanglement

Entanglement
fluctuation at echo



System

Time evolution and
reversal
Entanglement at echo
Fluctuation in
entanglement
Entanglement
fluctuation at echo

$$H_{TFIM} = -J \sum_{i=1}^N S_i^z S_{i+1}^z + h \sum_{i=1}^N S_i^x$$

$$H_{ANNNI} = H_{TFIM} + J' \sum_{i=1}^N S_i^z S_{i+2}^z$$

$$2S_i^{\{x,y,z\}} = \sigma_i^{\{x,y,z\}} \text{ (Pauli matrices)}$$



System

Time evolution and
reversal
Entanglement at echo
Fluctuation in
entanglement
Entanglement
fluctuation at echo

Quench Protocol: $H(h) \rightarrow -H(h + \delta h)$

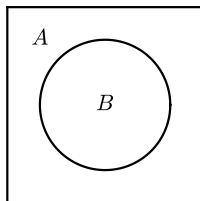
Observables:

$$\langle m_z \rangle = \frac{1}{N} \sum_{i=1}^N \langle S_i^z \rangle$$

$$\mathcal{F} = \langle \psi | S_{N/2}^z{}^2 | \psi \rangle - \langle \psi | S_{N/2}^z | \psi \rangle^2$$

$$\langle s_c \rangle = \langle S_i^z S_{i+2}^z \rangle$$

$$I = \frac{1}{N} \ln(|\langle \psi_0 | \psi_t \rangle|^2)$$



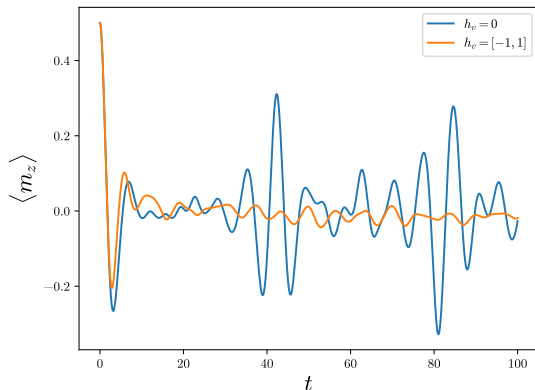
$$\rho_B = \text{Tr}_A |\psi\rangle\langle\psi|$$

$$S = -\text{Tr}_B \rho_B \log \rho_B$$



System

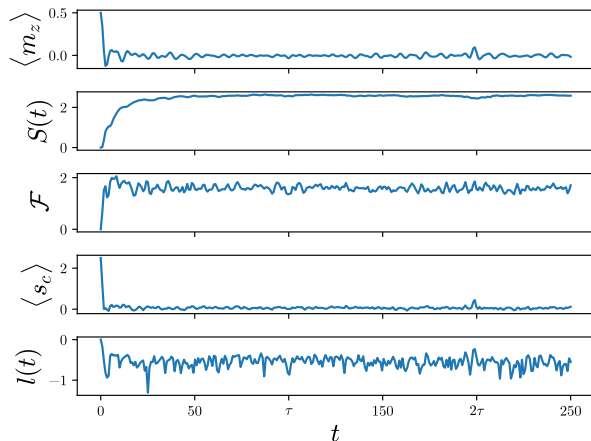
Time evolution and
reversal
Entanglement at echo
Fluctuation in
entanglement
Entanglement
fluctuation at echo



To suppress oscillations:
$$h_v = \sum_{i=1}^N h_i S_i^z$$



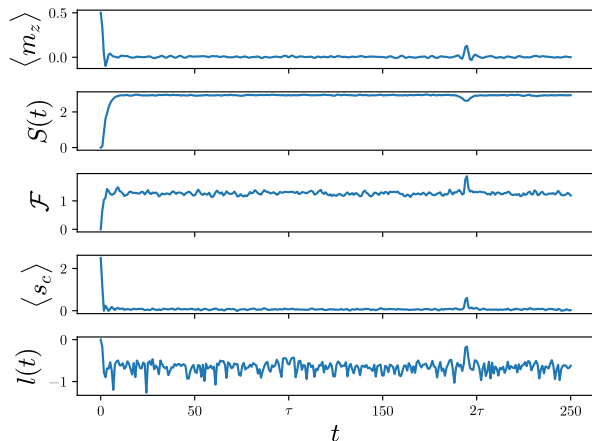
Time Evolution and Reversal



$N = 10, J = 1, h = 1, \delta h = 0.1, h_v = 1, \tau = 100, J' = 0$
fully polarized i.c., **single realization**



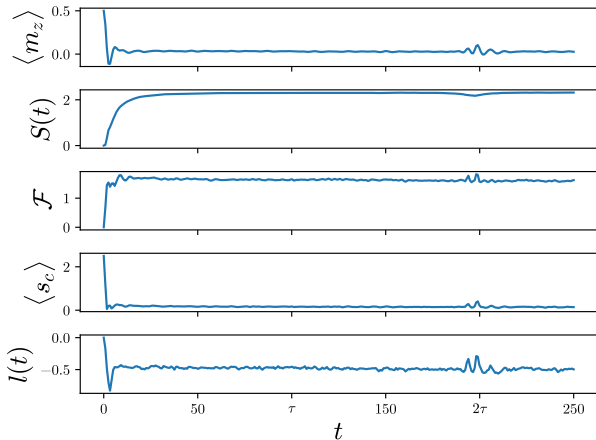
Time Evolution and Reversal



$N = 10, J = 1, h = 1, \delta h = 0.1, h_v = 1, \tau = 100, J' = 1$
fully polarized i.c., **single realization**



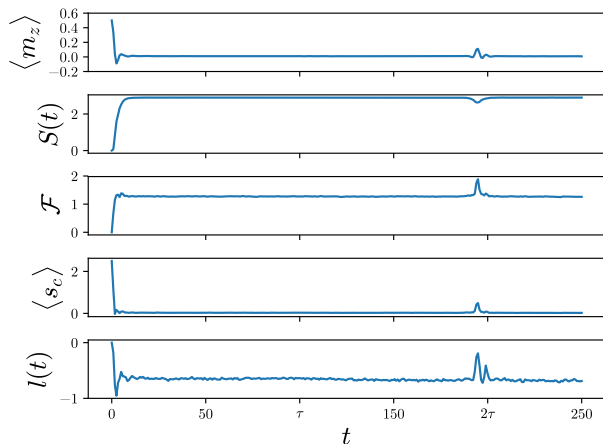
Time Evolution and Reversal



$N = 10, J = 1, h = 1, \delta h = 0.1, h_v = 1, \tau = 100, J' = 0$
fully polarized i.c., **disorder averaged**



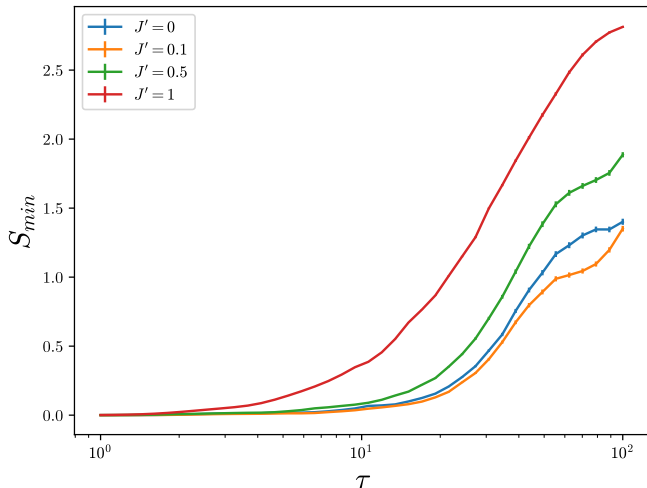
Time Evolution and Reversal



$N = 10, J = 1, h = 1, \delta h = 0.1, h_v = 1, \tau = 100, J' = 1$
fully polarized i.c., **disorder averaged**



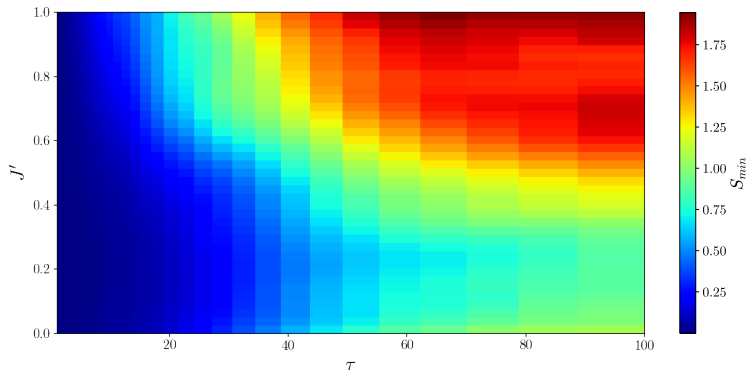
Entanglement at Echo



$$h = 1, \delta h = 0.1, h_v = 0.1, N = 10$$



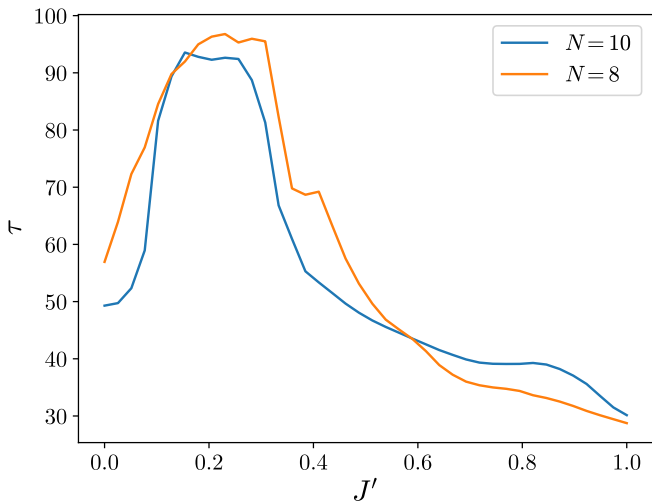
Entanglement at Echo



$$h = 1, \delta h = 0.1, h_v = 0.1, N = 8$$



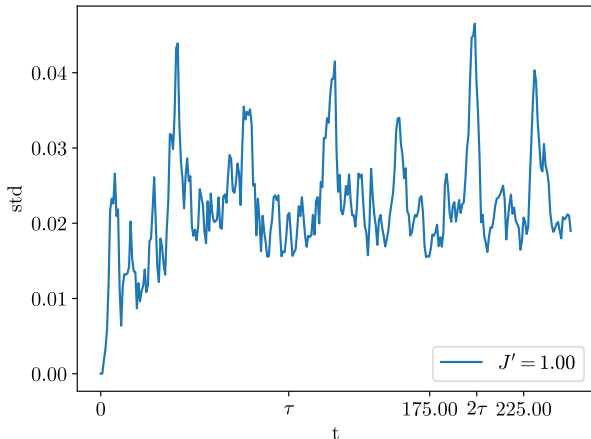
Entanglement at Echo



$$h = 1, \delta h = 0.1, h_v = 0.1$$



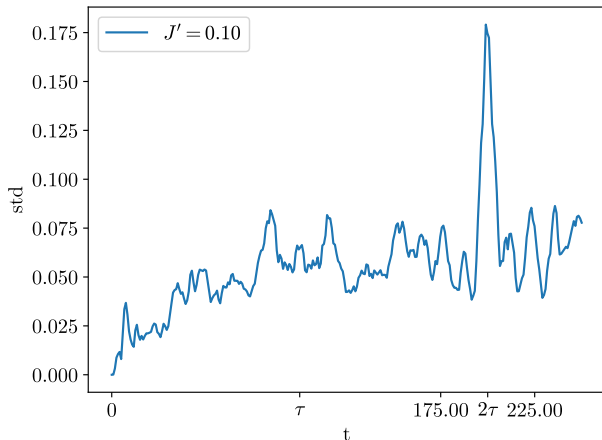
Fluctuation in Entanglement



$N = 10, J = 1, h = 1, \delta h = 0.1, \tau = 100$
fully polarized i.c. ($h_v = 0.1$)



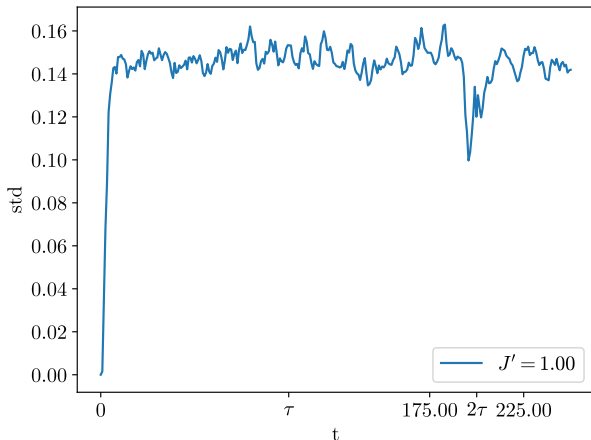
Fluctuation in Entanglement



$N = 10, J = 1, h = 1, \delta h = 0.1, \tau = 100$
fully polarized i.c. ($h_v = 0.1$)



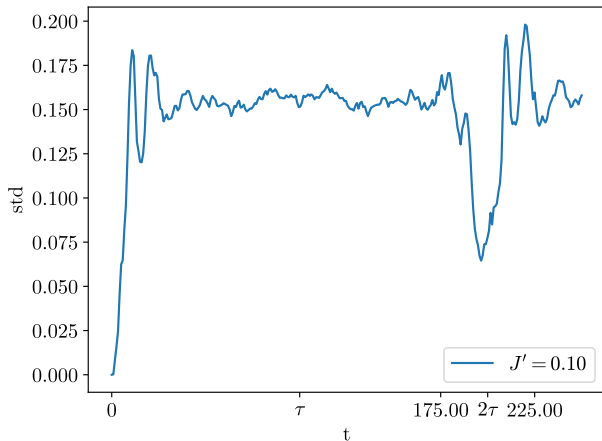
Fluctuation in Entanglement



$N = 10, J = 1, h = 1, \delta h = 0.1, \tau = 100$
random classical i.c. ($h_v = 0$)



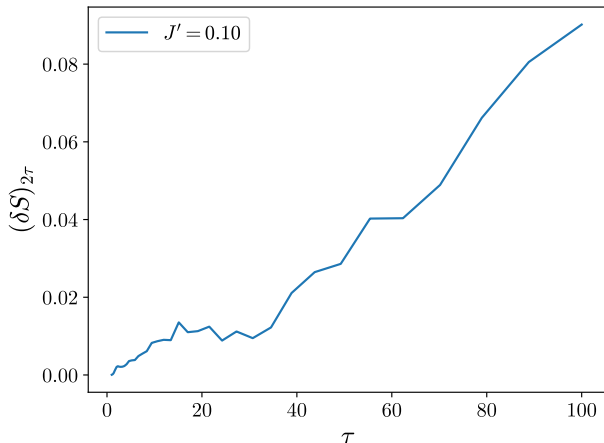
Fluctuation in Entanglement



$N = 10, J = 1, h = 1, \delta h = 0.1, \tau = 100$
random classical i.c. ($h_v = 0$)



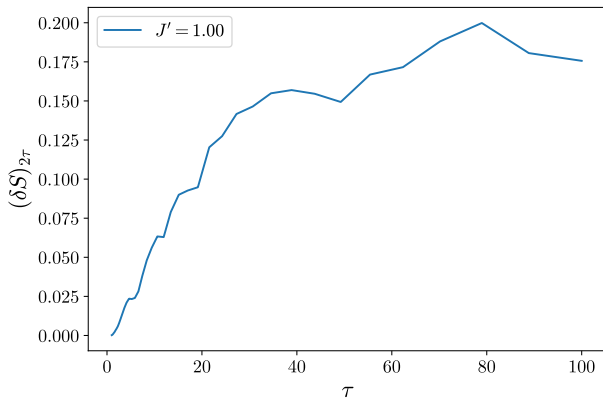
Entanglement Fluctuation at Echo



$N = 8, J = 1, h = 1, \delta h = 0.1$
random classical i.c. ($h_v = 0$)



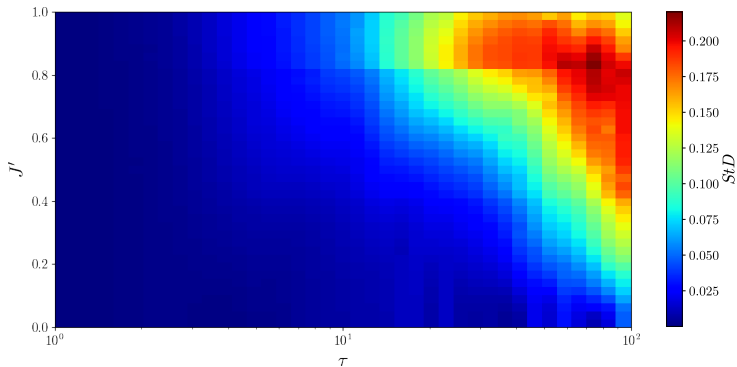
Entanglement Fluctuation at Echo



$N = 8, J = 1, h = 1, \delta h = 0.1$
random classical i.c. ($h_v = 0$)



Entanglement Fluctuation at Echo



$N = 8, J = 1, h = 1, \delta h = 0.1$
random classical i.c. ($h_v = 0$)



Overview

Introduction

Loschmidt echo in spin chains

System

Time evolution and reversal

Entanglement at echo

Fluctuation in entanglement

Entanglement fluctuation at echo

