

# On the broadcast of segmented messages in dynamic networks

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# Outline

- 1) Problem definition
- 2) Setup
- 3) Algorithms of Message Transfer
- 4) Deeper analysis of the algorithms
- 5) Conclusions

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# Problem Definition

- Consider a dynamic and a distributed system of agents
- Connections between any pair of agents are intermittent
- Information dissemination occurs through epidemic protocols due to its dynamic nature
- A piece of information can be passed on when two nodes meet (i.e., establish communication link)

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- A piece of information can be passed on when two nodes meet (i.e., establish communication link)
- **But what if the information is too large to be sent over in a single contact?**

# Split the Message

- A **simple solution** is to **split the message** into packets
- Hence, during a communication opportunity **transfer only a part** of the message
- But, how will message **splitting influence the speed** of dissemination?
- Will the underlying **topology have any effect**?
- Will it be possible to **control resource wastage** by devising efficient message spreading policy, especially, in a distributed environment?

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- Will it be possible to **control resource wastage** by devising efficient message spreading policy, especially, in a distributed environment?
- **We consider the case of broadcast and try to answer these questions**
- **We also propose an efficient broadcast algorithm**

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# Agent and Message Configuration

- Agent configuration

- A graph  $G=(V,E)$  represents a dynamic network

- A **node** in  $V$   $\rightarrow$  an **agent**, and
- An **edge** in  $E$   $\rightarrow$  a possible **link** between a pair of agents
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- A message is **split into a set of  $m$  packets** and the packets are grouped into  **$s$  segments**, s.t.,  $m \bmod s = 0$



A message

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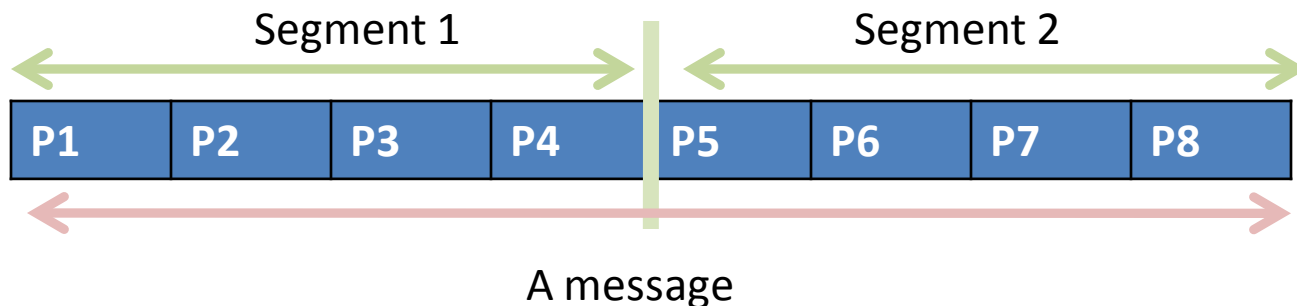
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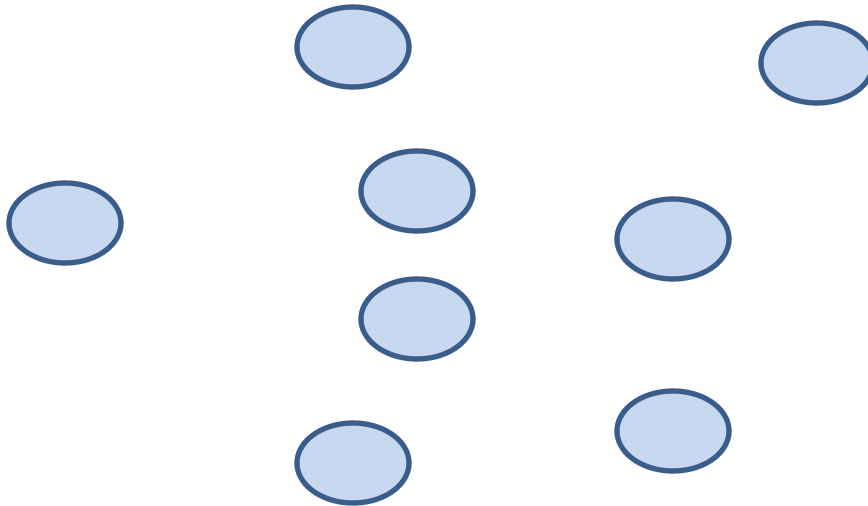
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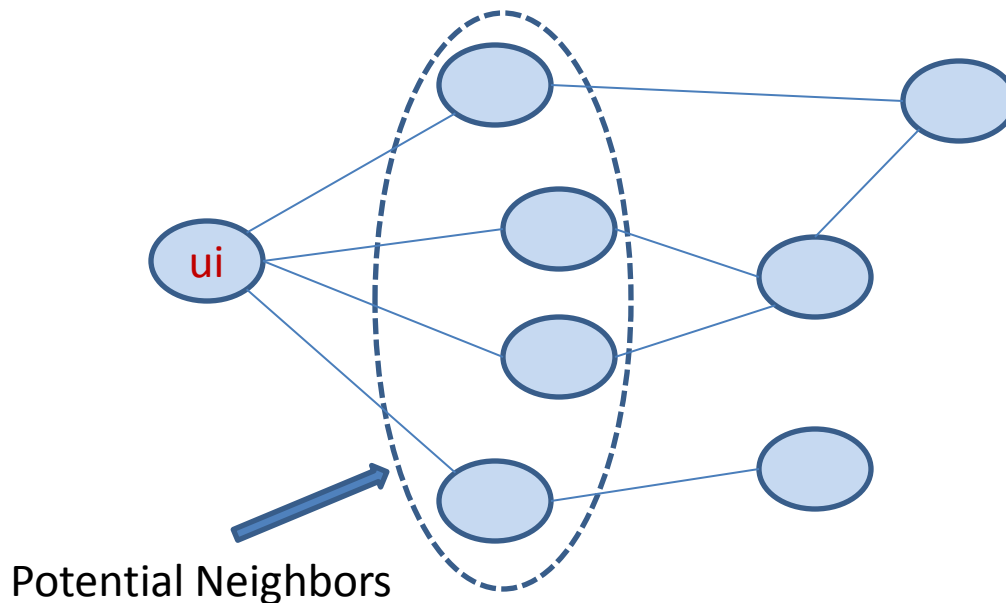
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- Topology specifies **potential neighbors** for each node
- At each time step, a node tries to **connect with one** of the neighbors selected randomly



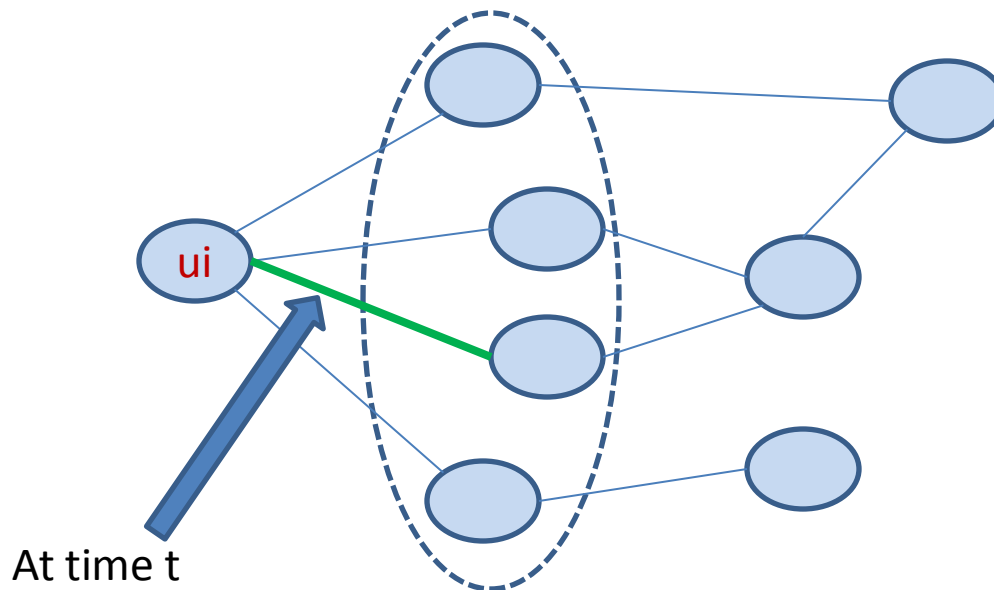
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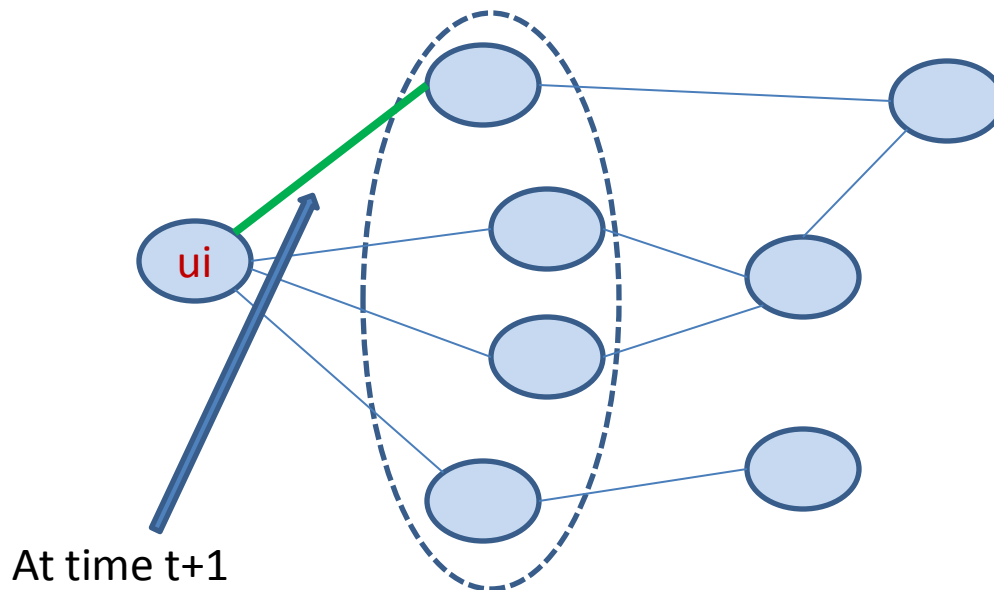
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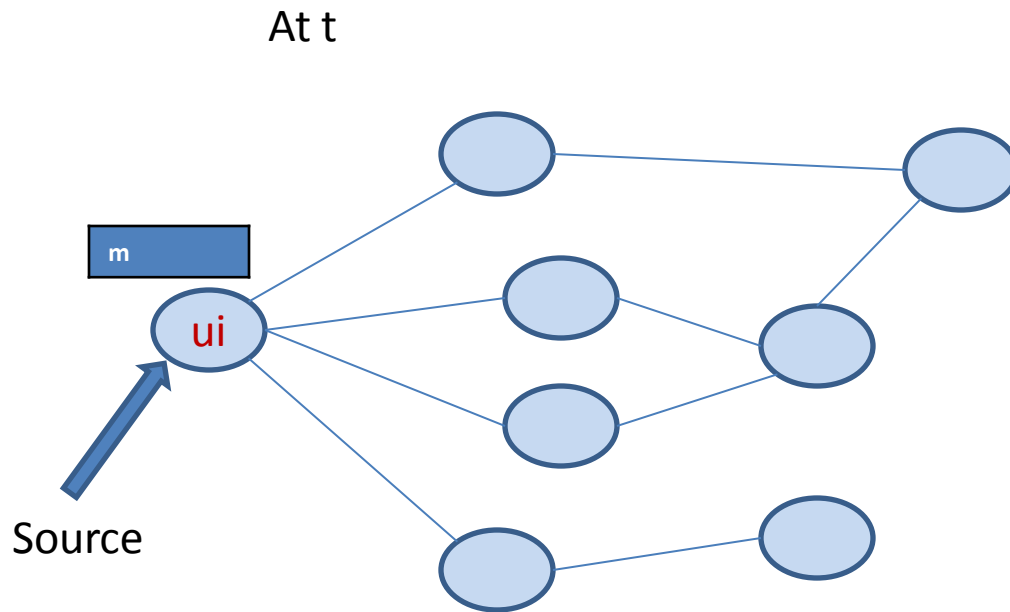




# Transfer Protocols

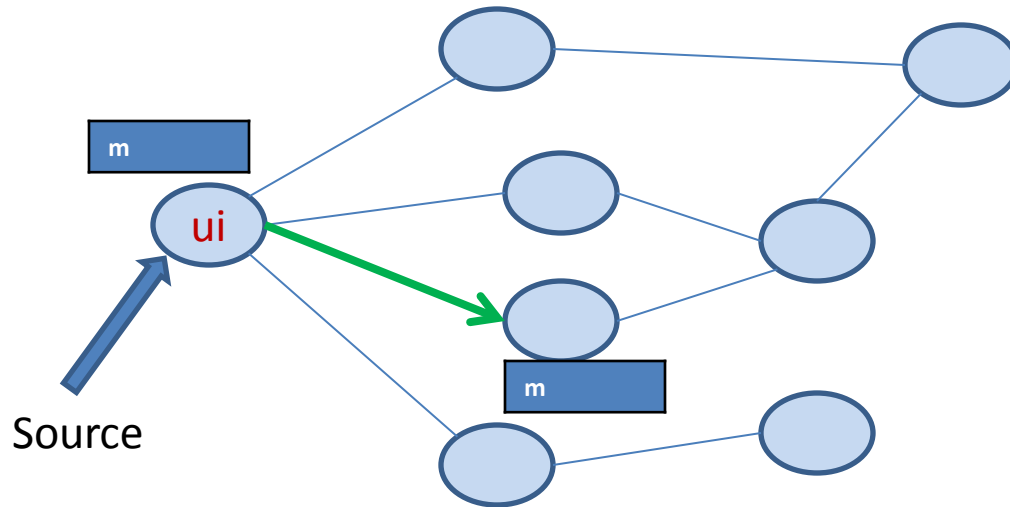
- Consider a node as a **sender** when it **has all the packets** of a message
  - Initially, **source is the only sender** having all the packets
- And, the other nodes as **non-senders** that has no or not all packets of the message
  - Hence, **non-senders won't start** forwarding any packet
  - They do forward only when they become sender
- Two basic forwarding techniques
  - **Push technique**
  - **Pull technique**

# Push Technique



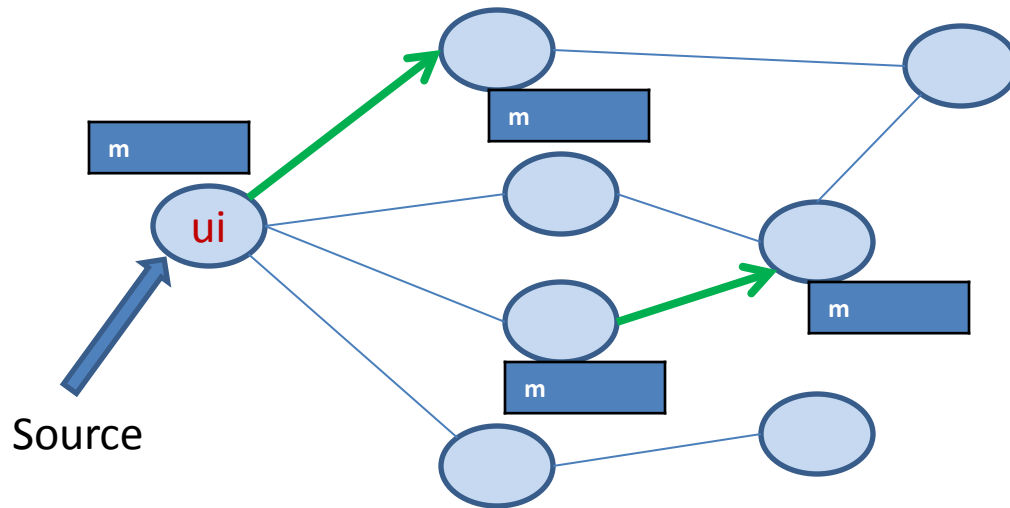
# Push Technique

At  $t+1$



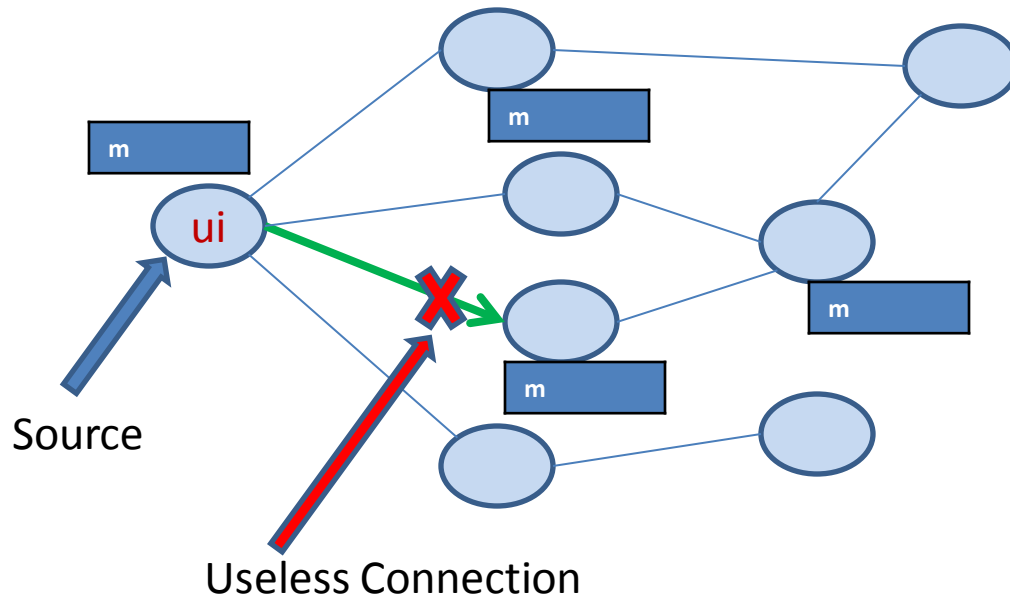
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At  $t+2$

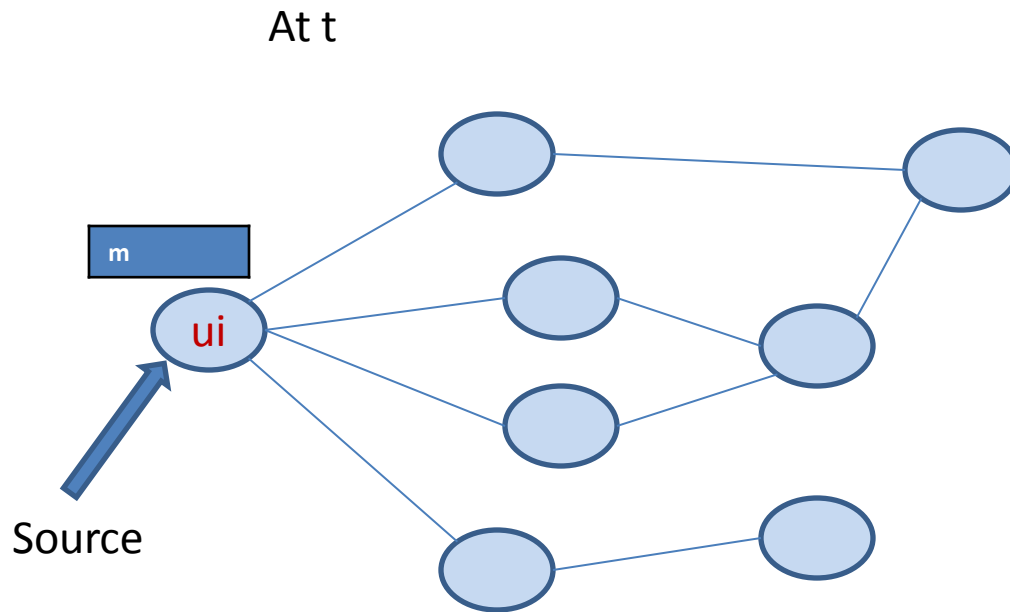


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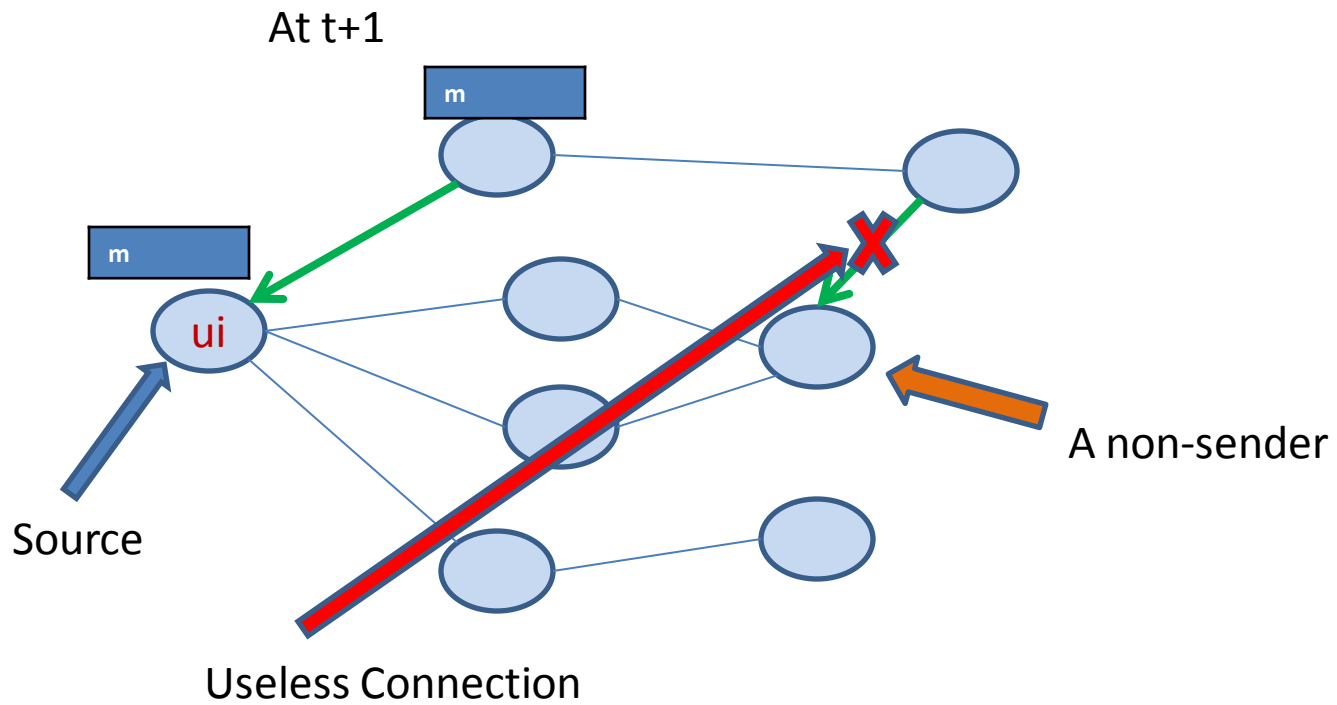
At t+3



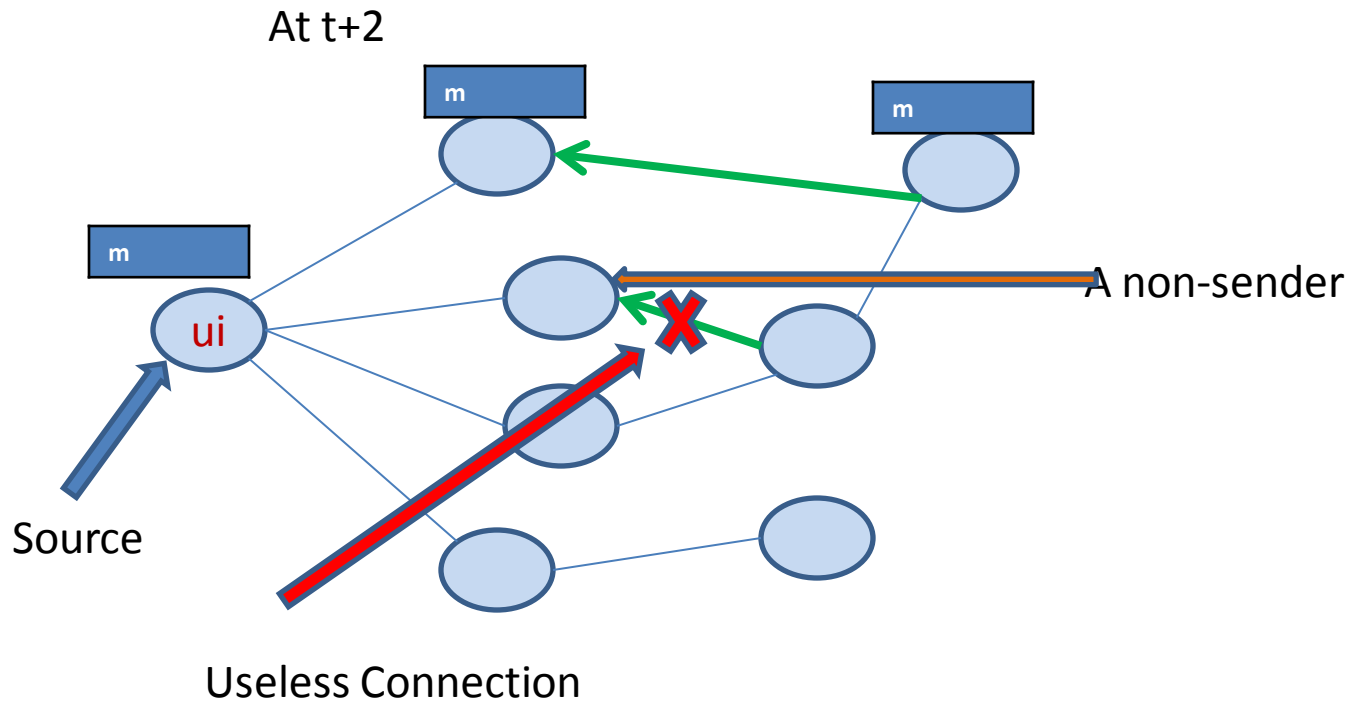
# Pull Technique



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# Metrics

- Broadcast Time  $T^*$

- Time from the point the source starts sending the first packet to the point when all the agents in the network have received the entire message
  - Expected broadcast time:  $E(T)$
- $T_i$ : minimum time at which the system has  $i$  senders

- Broadcast Wastage  $C_m^*$

- Measures the number of useless contacts, i.e., the contacts when no packet is transferred
- $C_m^* = (C_l - C_p)/C_l$ , where
  - $C_l \rightarrow$  the total number of links
  - $C_p \rightarrow$  the number of successful links

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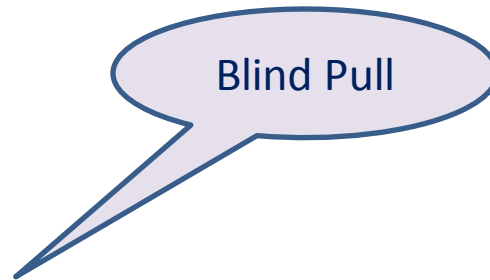
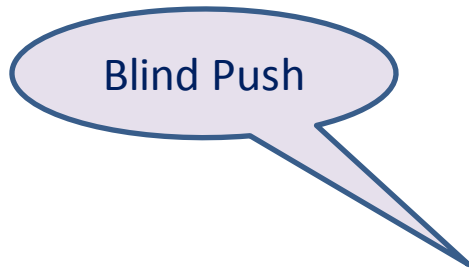
# Algorithms for Message Transfer

Blind Push

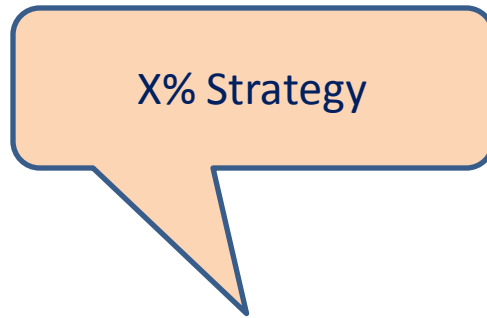
Blind Pull

Basic  
Strategies

# Algorithms for Message Transfer



Combine



Basic  
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A vertical blue line with a downward-pointing arrowhead, positioned to the left of the text "Basic Strategies".

# Algorithms for Message Transfer

Blind Push

Blind Pull

Basic Strategies

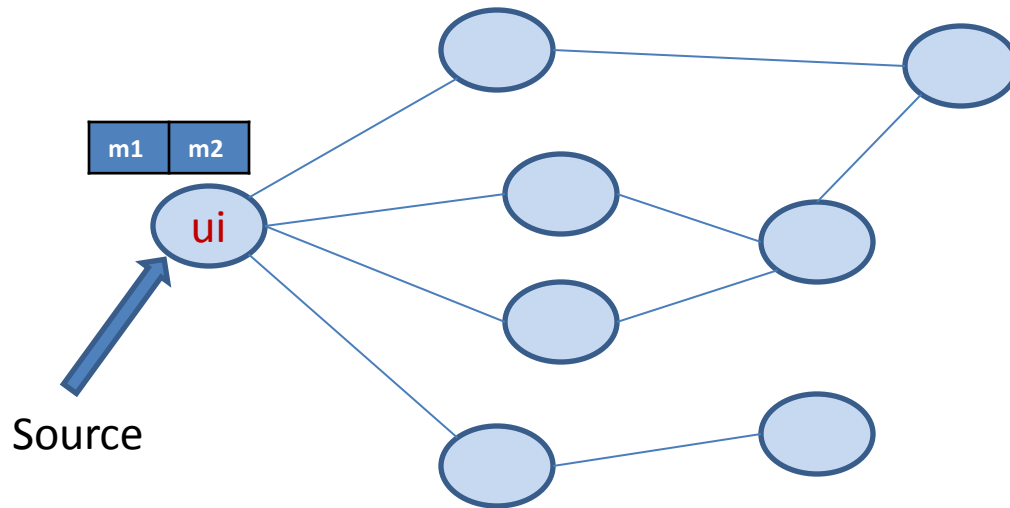
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X% Strategy

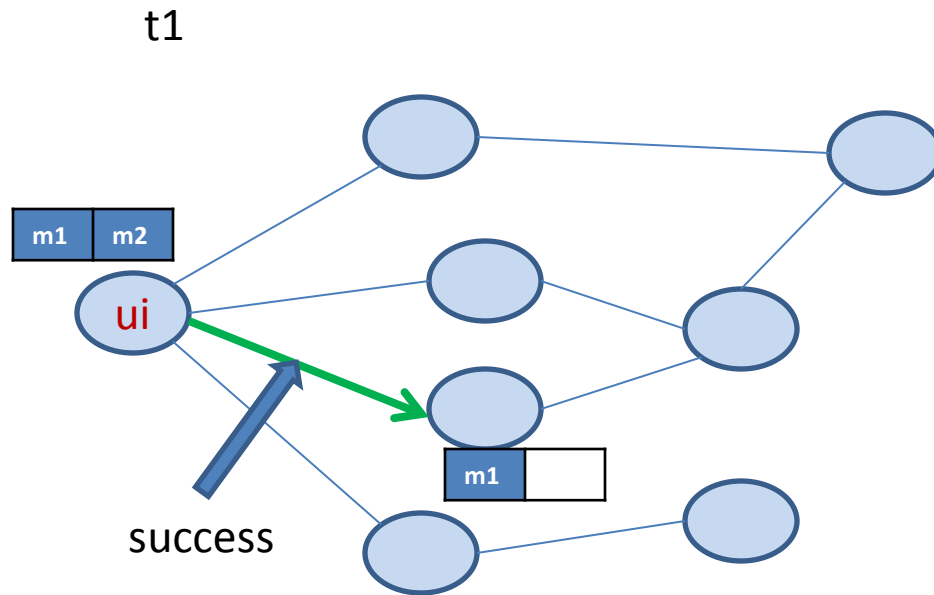
A distributed Version

Push – Pull – Give up

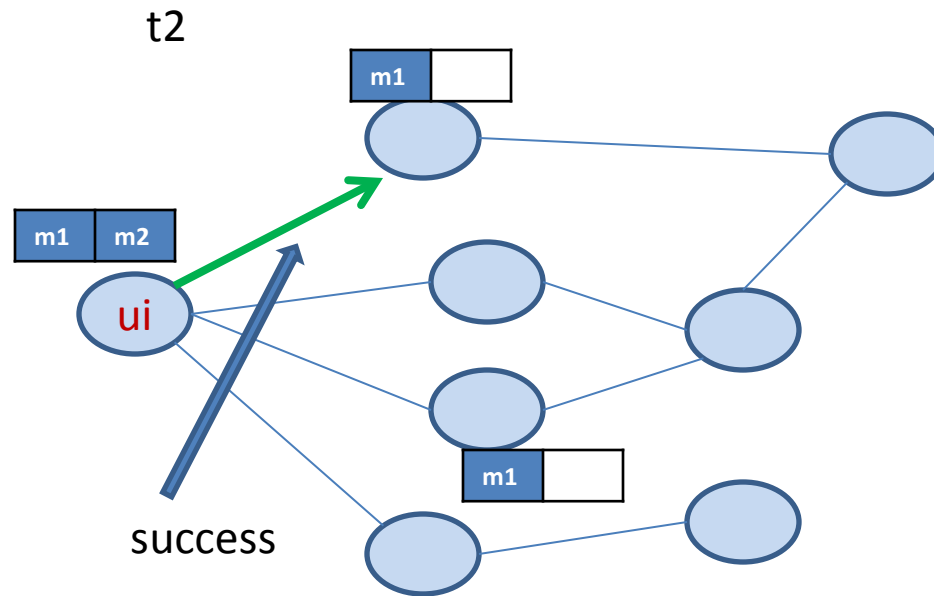
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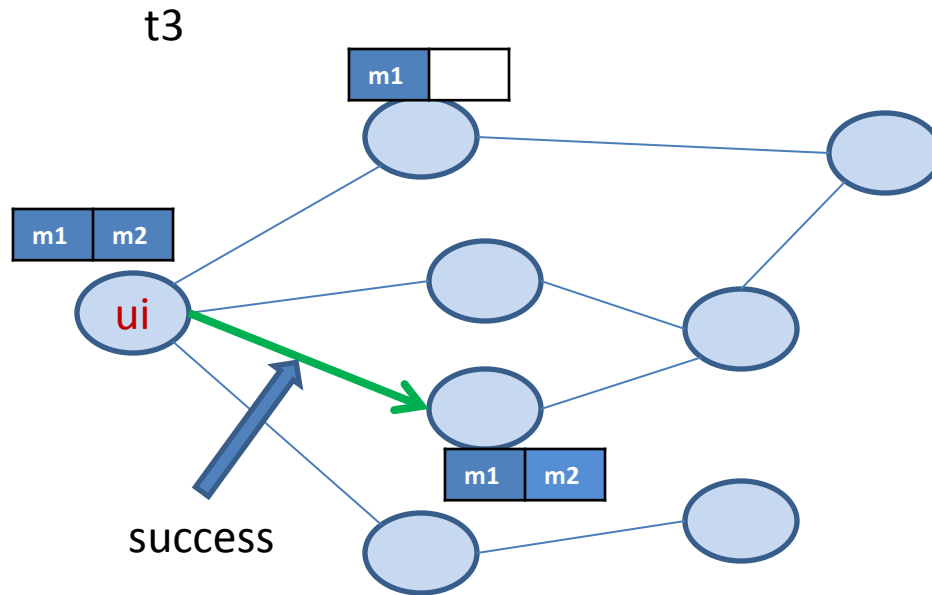


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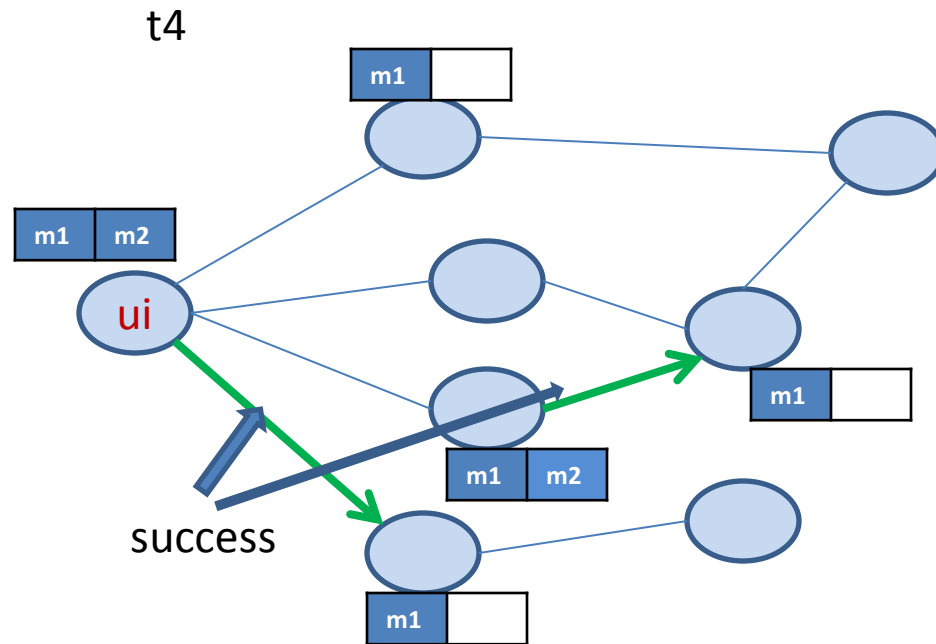




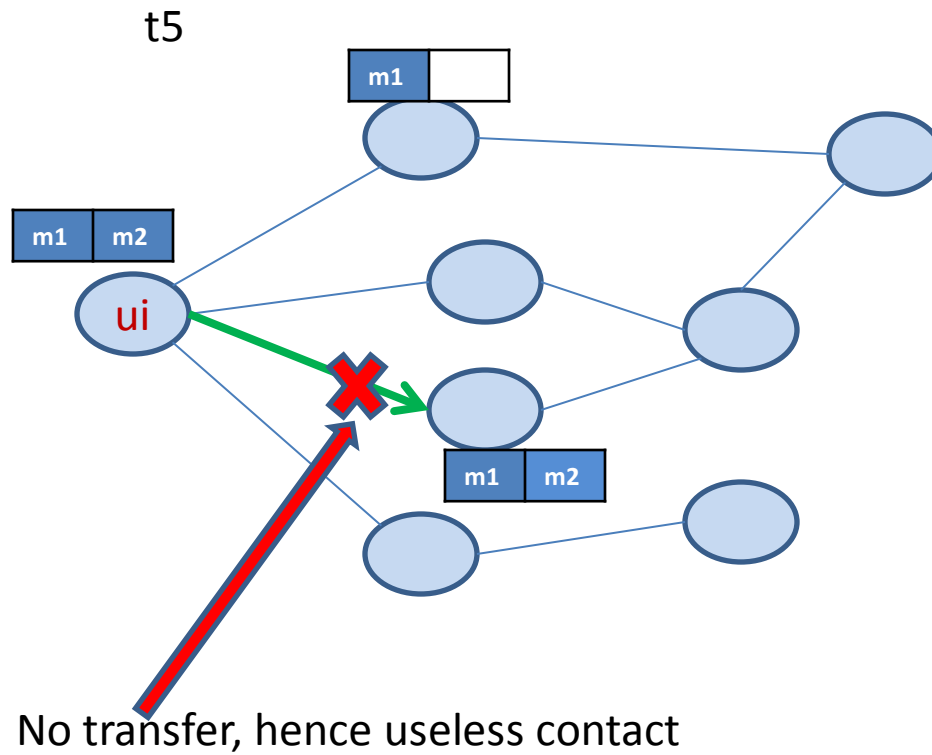
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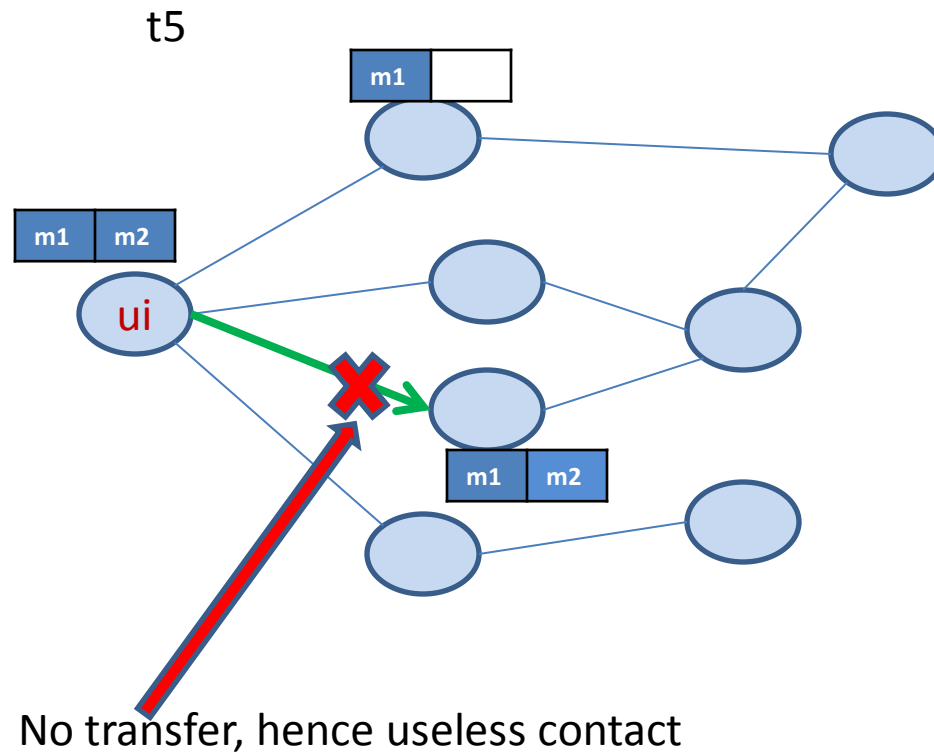
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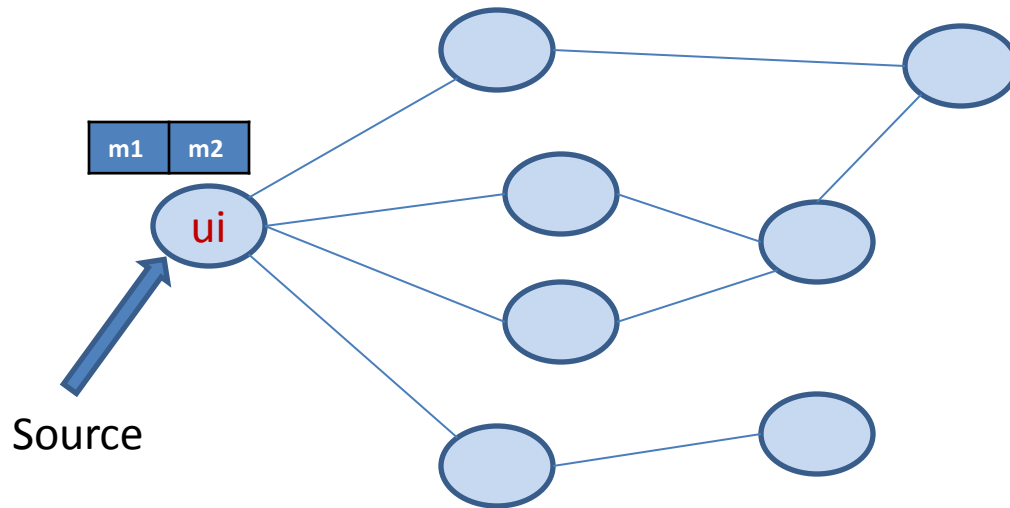


Such failures will be significant towards the end of the broadcast

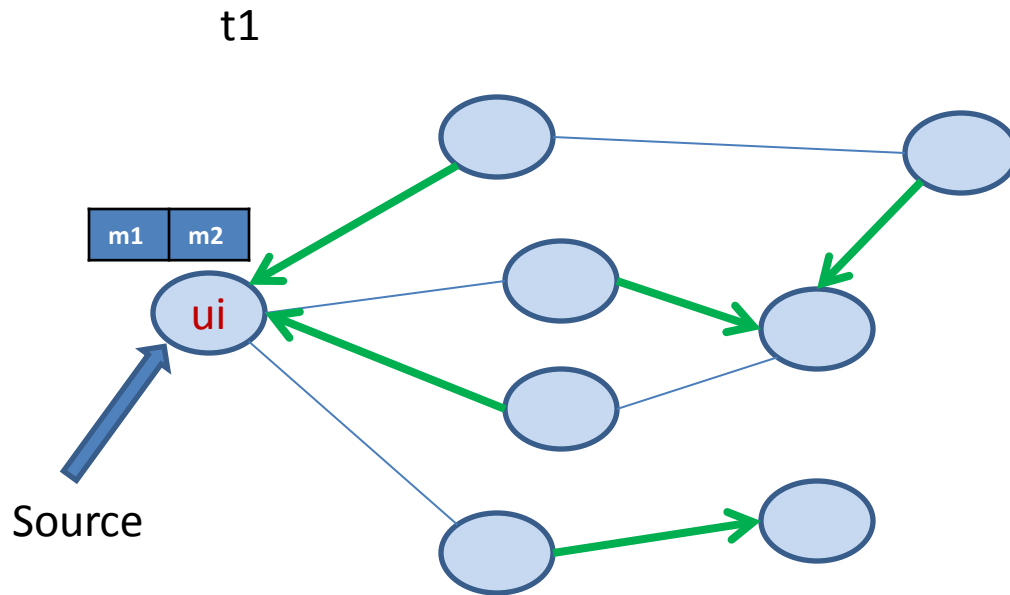
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How to reduce such failures towards the end?

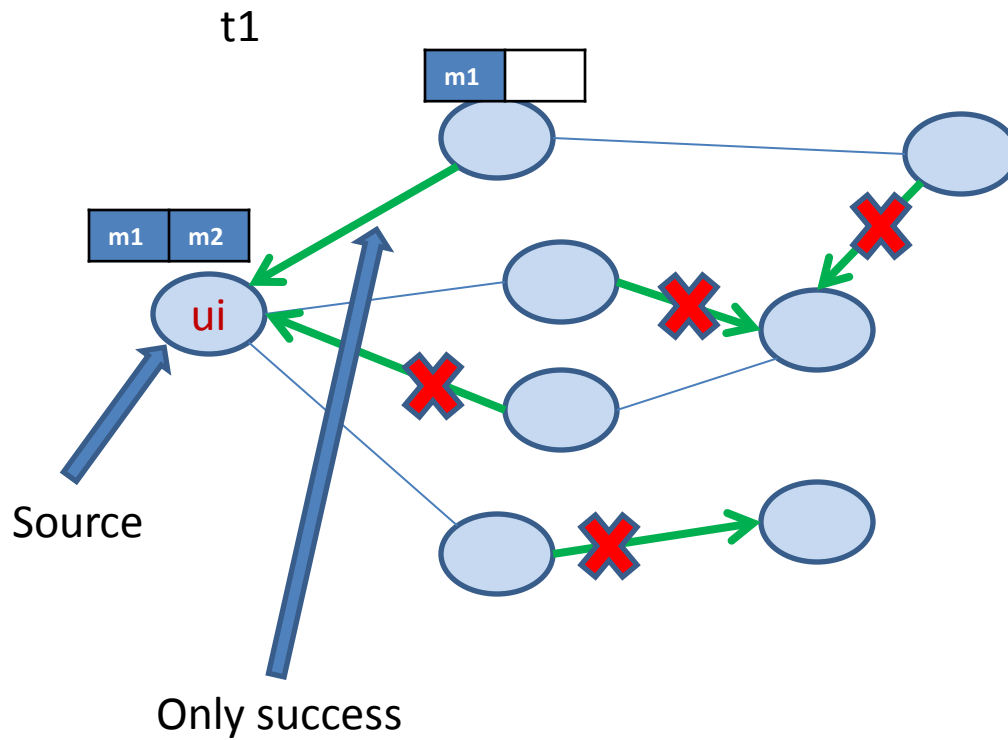
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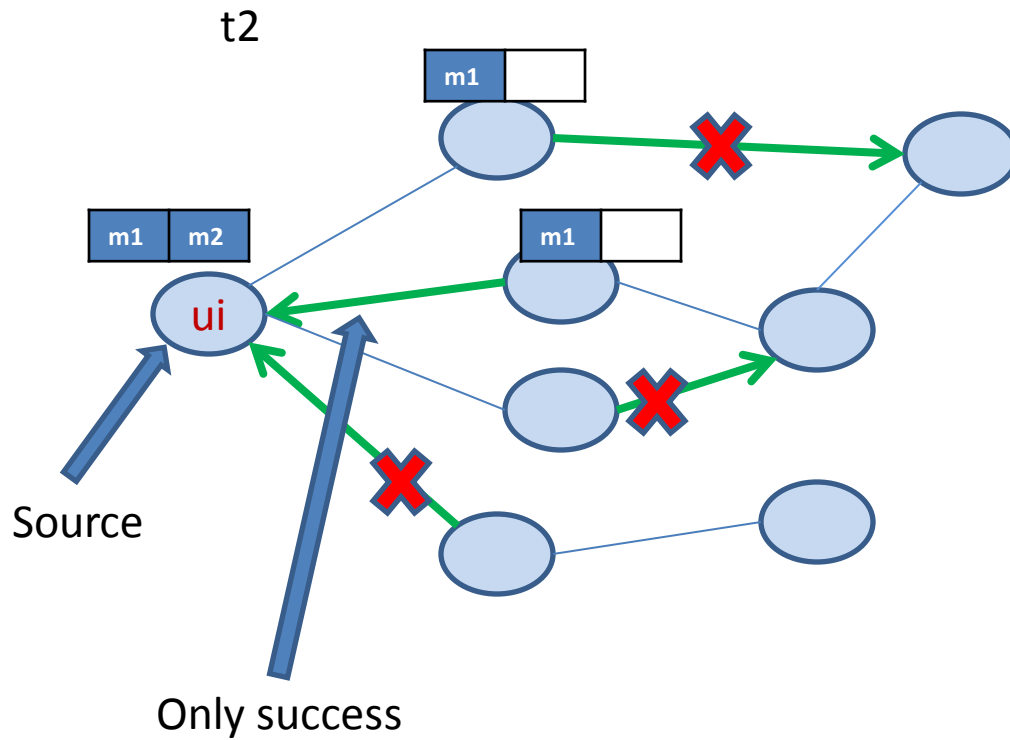


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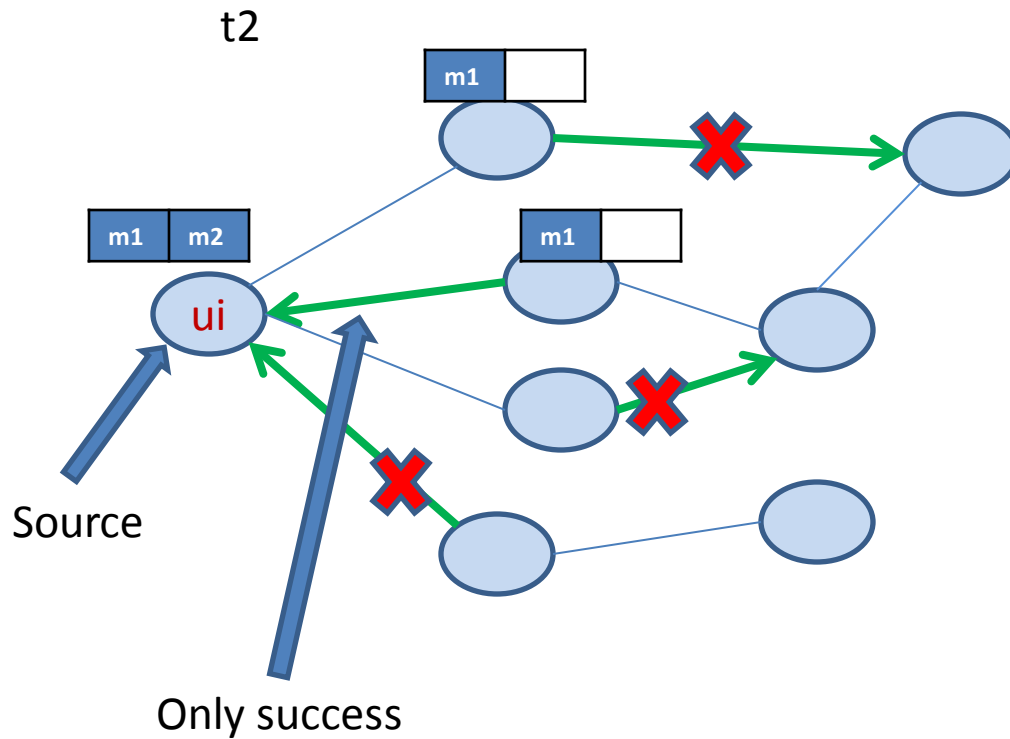




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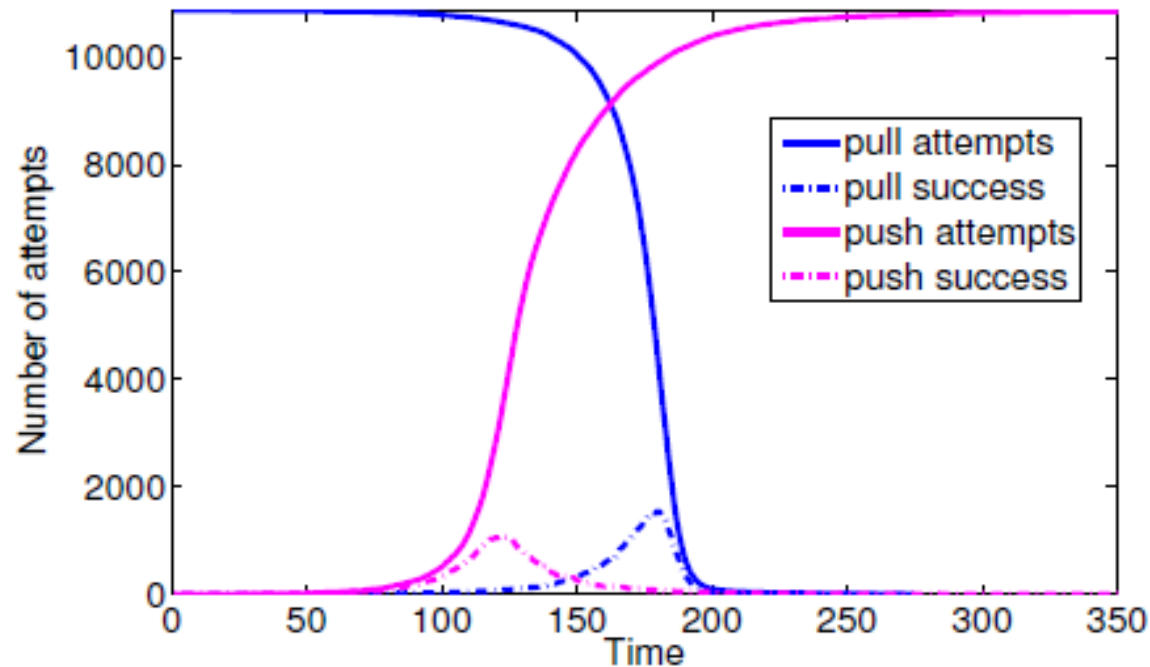


# Blind Pull Technique



How to reduce initial failures?

# Deeper analysis of the algorithms



- Blind push and blind pull are complementary to each other
- How to take advantages of them and combine?

# X% Push-Push Strategy (X-P-P)

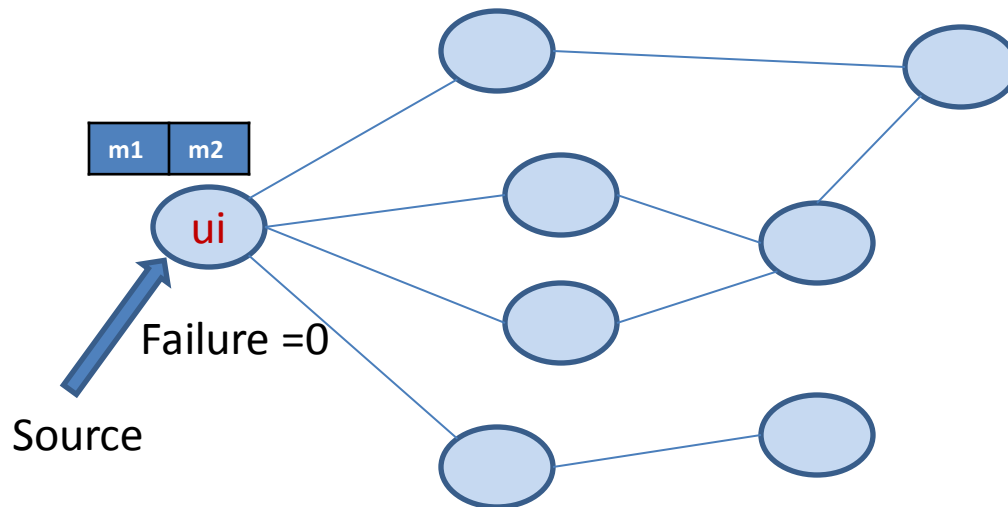
- X-P-P combines the advantages of blind push and blind pull
- The process
  - Starts with blind push (B-P)
    - to avoid potential wastage at the beginning
  - After some x% of agents becomes sender, the process converts to blind pull
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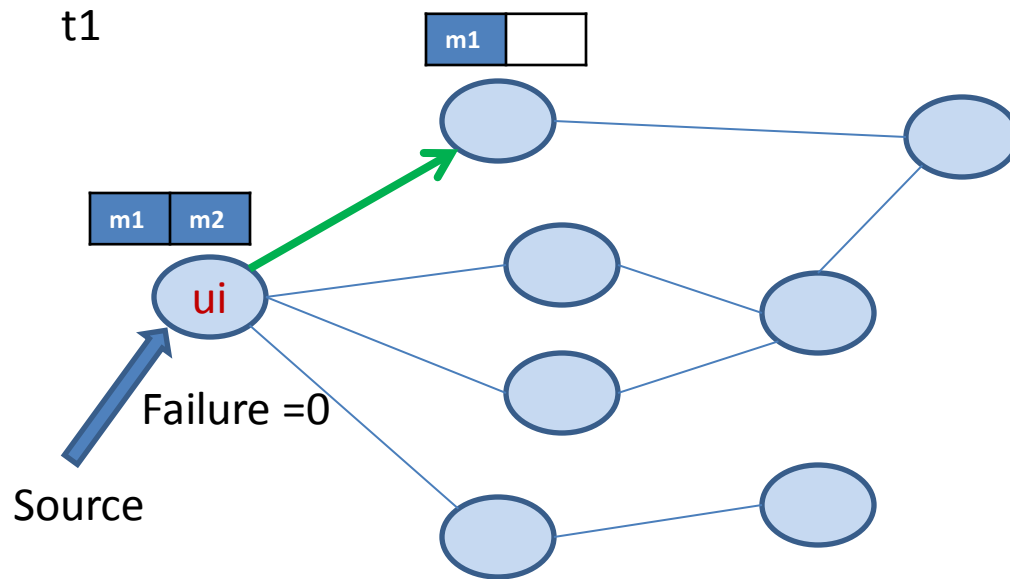
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- But, how to estimate x in X-P-P because the system is envisioned as distributed system?

# Push-Pull-with-Giveup (P-P-G)

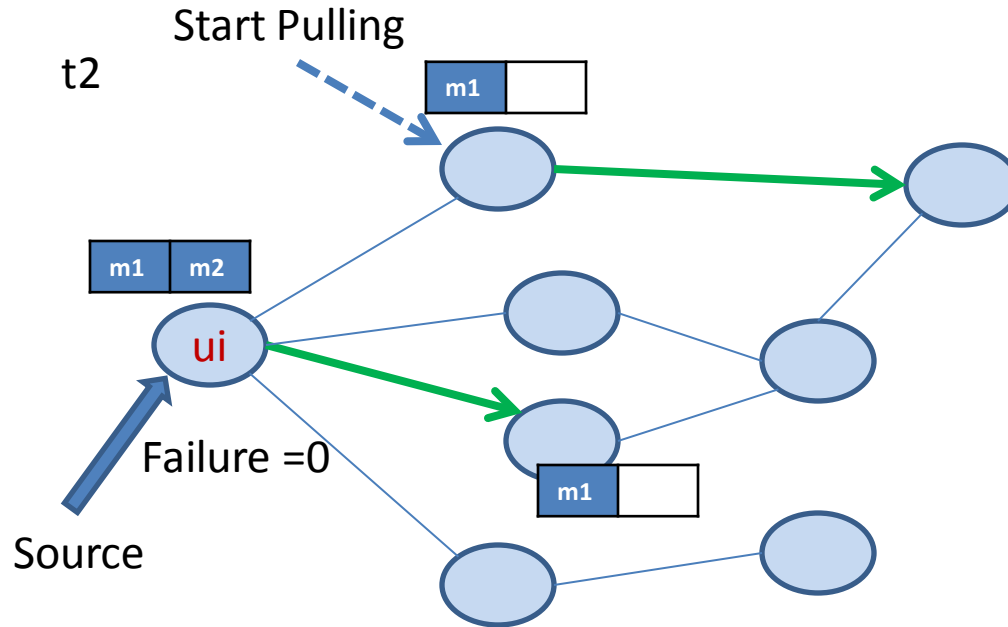
- An approximation of X-P-P to fit distributed environment
- Sender nodes stops “pushing” after a threshold number of failure “pushes”
- Receiving (i.e., non-sender) nodes starts pulling once a packet got received



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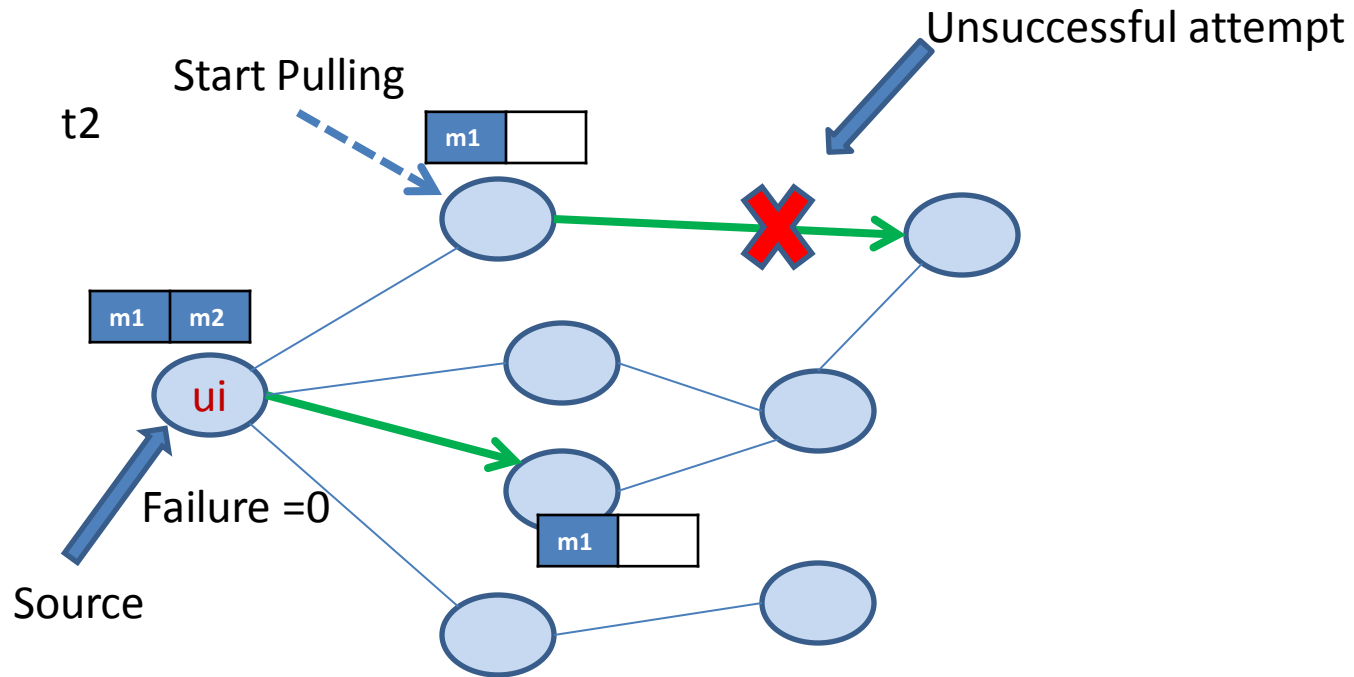


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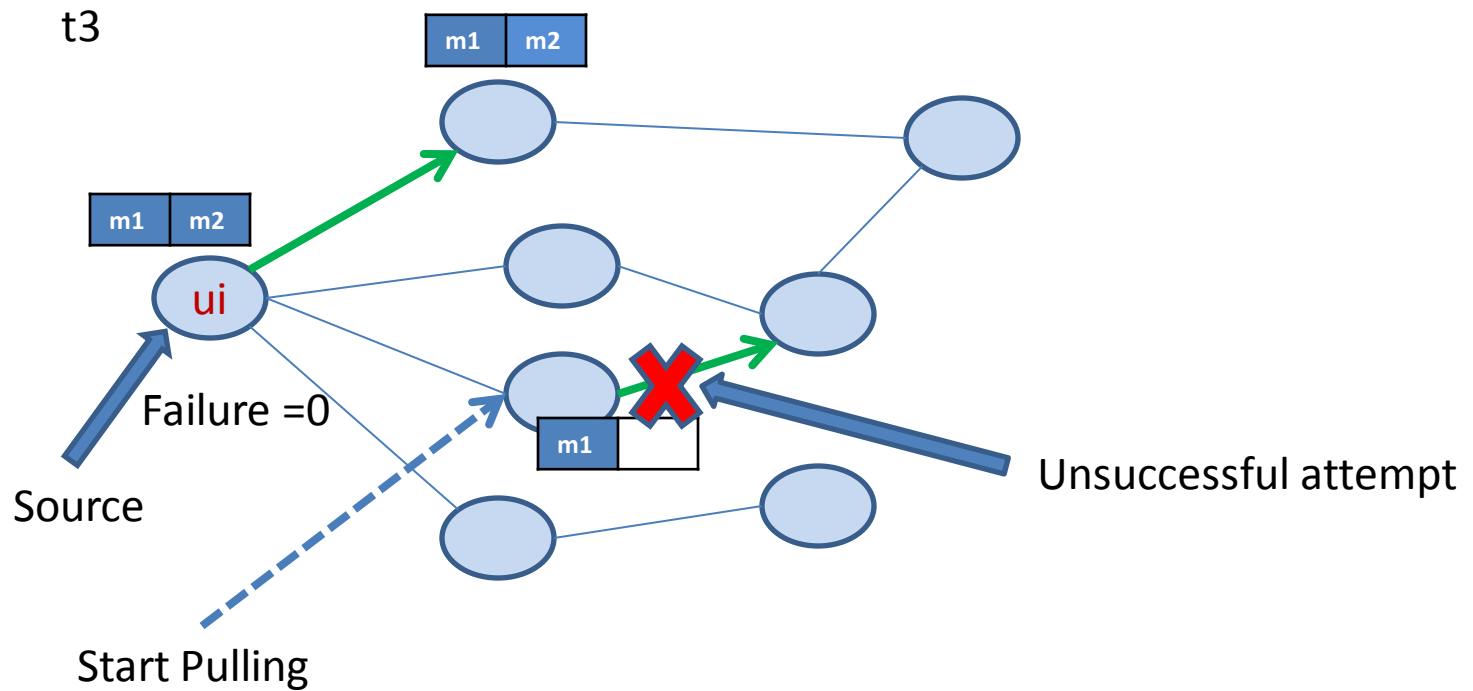




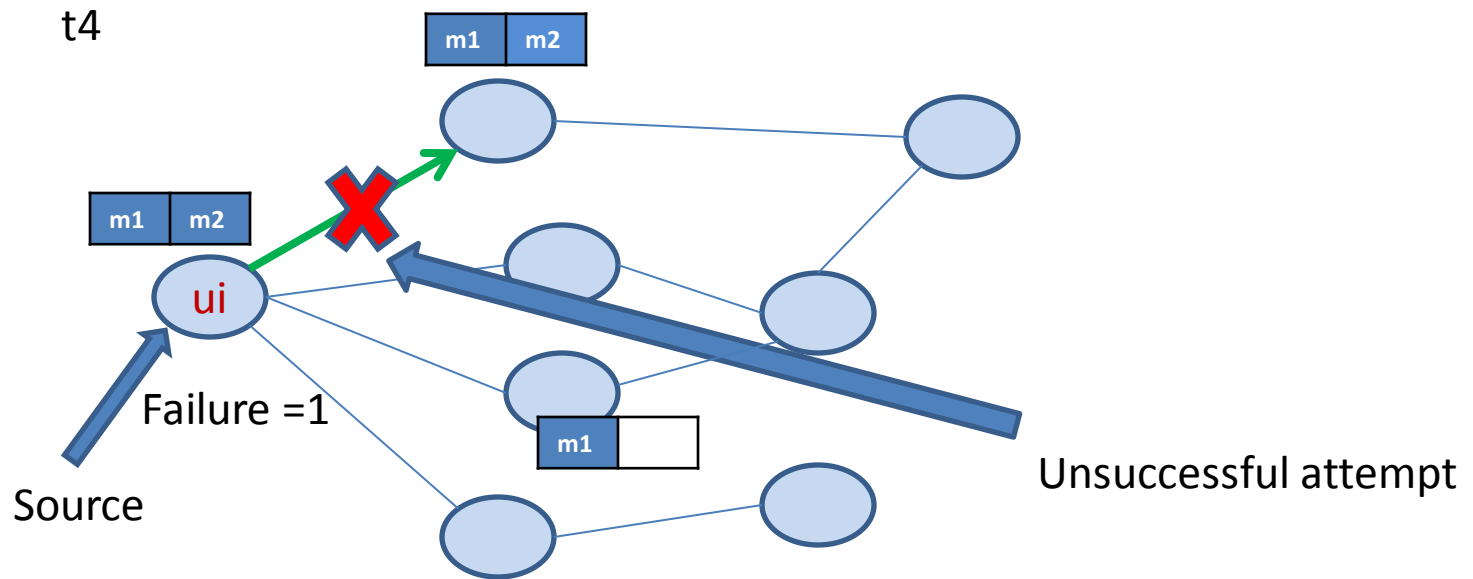
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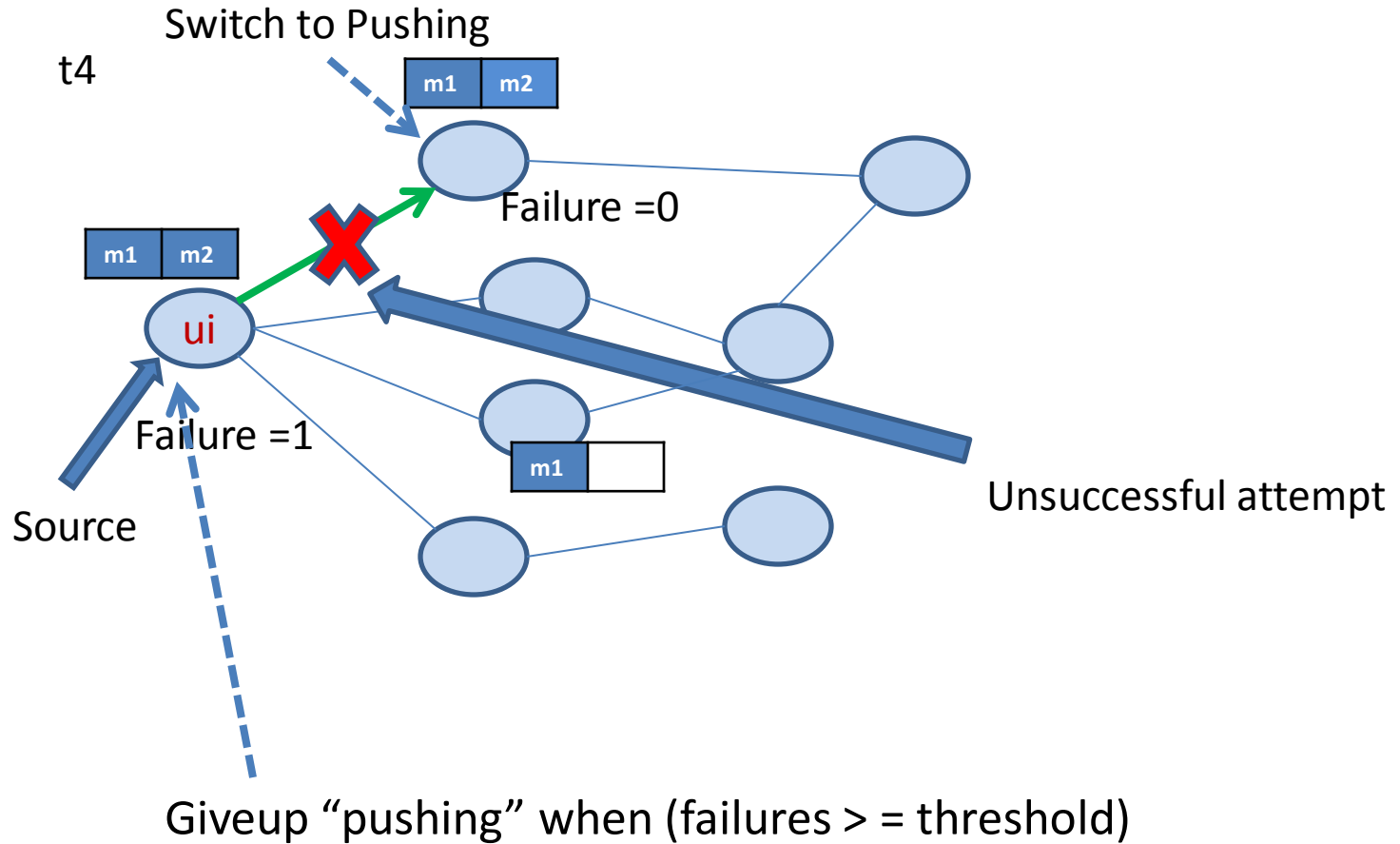
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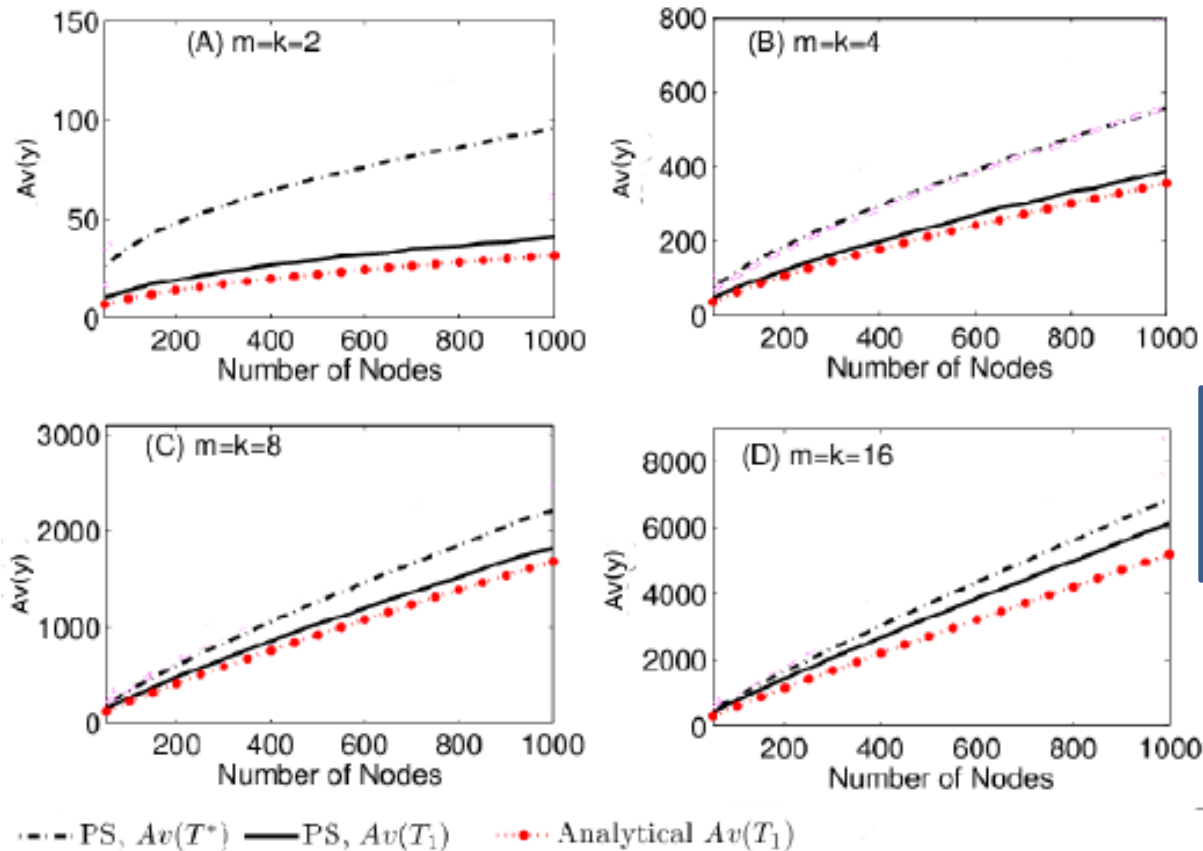
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# Deeper analysis of the algorithms

- Blind Push (B-P) is simple and analytically tractable
  - lets try to see analytical results
- Analyze B-P on a synthetic graph topology of dynamic graphs, like
  - Complete graph, regular graph, regular tree
- Then, find some simulation results on real network topologies, like
  - Gnutella network

# Blind Push (B-P) on Complete Graph

- For a complete graph topology we report
  - Expected broadcast time  $E(T)$
  - Expected time  $E(T_1)$  to get first sender other than source



Note:  $E(T_1)$  is an indicator of  $E(T)$

# Estimation of $T_1$

- Ratio of  $T^*$  and  $T_1$  converges to a constant
- Estimation of  $T_1$

Estimate  $T_1$  as:

$$\Pr\{T_1 = t\} = \frac{t-1}{n} \prod_{l=1}^{t-2} \left(1 - \frac{l}{n}\right), t \geq 2$$

- Sketch: **consider a message has 2 packets (for simplicity)**
  - Minimum time required to create first sender = 2
  - $\Pr(T_1 = t)$  implies that up to  $t-1$  time only those nodes are selected that has no packet, and at  $t$ , a node out of  $t-1$  nodes are selected



# Estimation of $T_1$


- Thus,

$$\Pr\{T_1 = t\} = \underbrace{\left(1 - \frac{1}{n}\right)\left(1 - \frac{2}{n}\right)\left(1 - \frac{3}{n}\right)\dots\left(1 - \frac{t-2}{n}\right)}_{\text{This part ensures that none of } t-1 \text{ nodes got selected up to time } t-1} \left(\frac{t-1}{n}\right)$$

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- Generalized for k-packets message

$$\begin{aligned}\Pr(T_1 = t) &\sim \frac{t^{k-1}}{(k-1)!n^{k-1}} \prod_i^t \left(1 - \frac{i^{k-1}}{(k-1)!n^{k-1}}\right) \\ &\sim \frac{t^{k-1}}{(k-1)!n^{k-1}} e^{-\frac{t^k}{k!n^{k-1}}}\end{aligned}$$

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$$E(T_1) = \sum t * \frac{t^{k-1}}{(k-1)!n^{k-1}} e^{-\frac{t^k}{k!n^{k-1}}} \quad \Rightarrow \quad n^{\frac{k-1}{k}}$$

# Blind Push on Sparse Networks

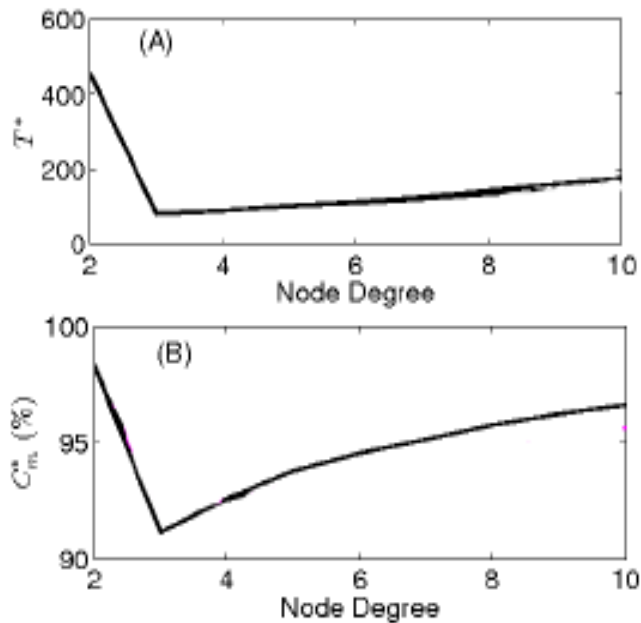


Figure : Regular tree

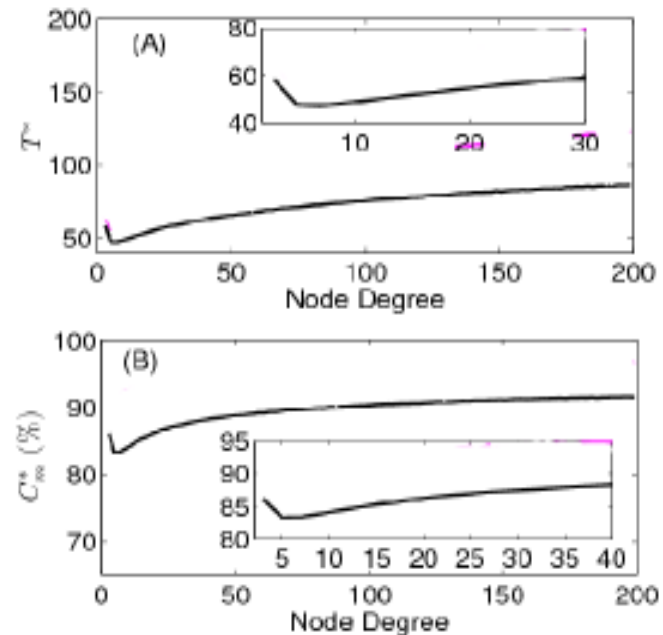


Figure : Regular graph

- An optimal degree  $d$  can be found where broadcast delay and wastage can be minimum

# B-P, X-P-P, & P-P-G on Real Network Topology

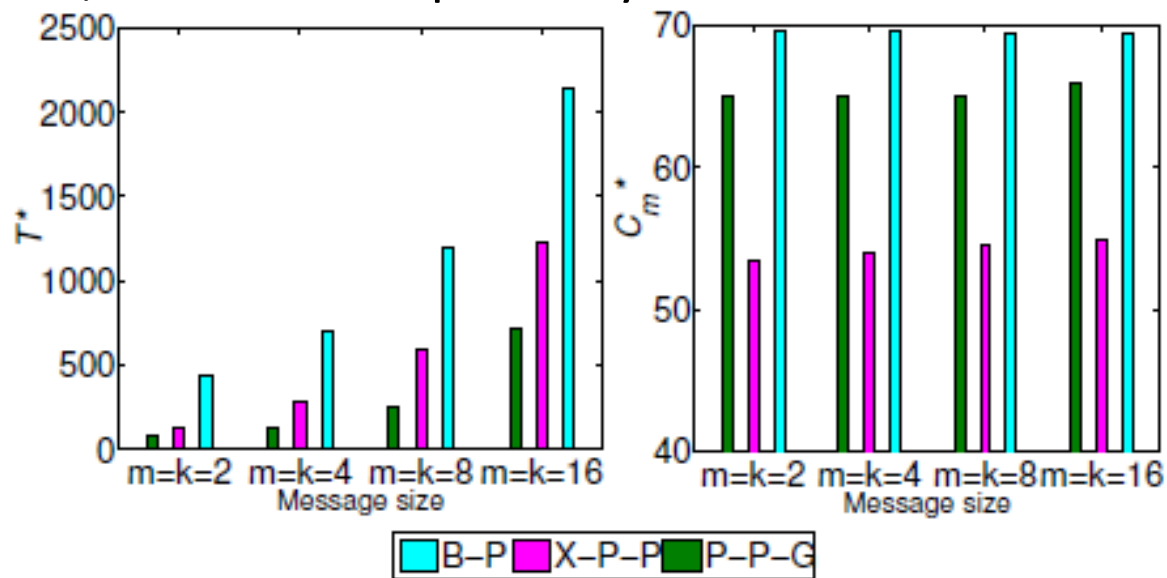
- Three snapshots of Gnutella network (taken in 2002)

Data set	#Nodes	#Edges	Avg. degree
Gnutella_1	10876	39994	7.34
Gnutella_2	8717	31525	7.24
Gnutella_3	22663	54693	5.82



# Comparison of the Broadcast Algorithms

- The optimal  $X$  (point where the system switches to Pull) for the three networks are 50, 50 and 60 respectively



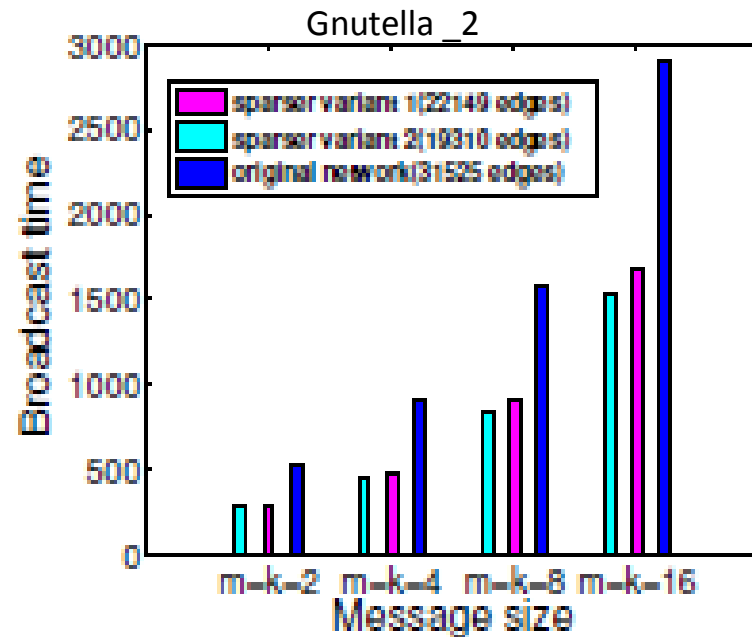
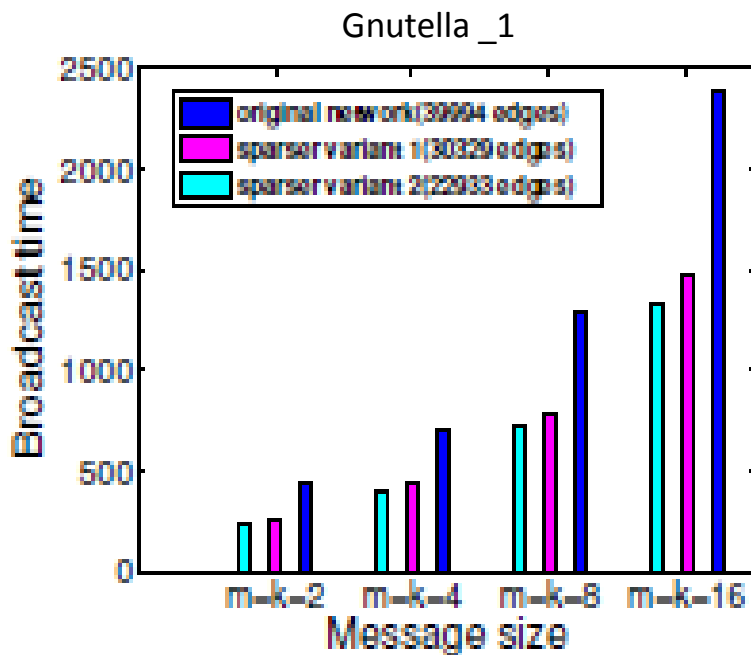
	Gain of P-P-G in Delay		Gain of P-P-G in Wastage	
	Over B-P	Over X-P-P	Over B-P	Over X-P-P
Gnutella_1	5.45	1.5	1.10	0.75
Gnutella_2	5.9	1.6	1.06	0.72

# Observations

- With respect to B-P, we gain in both broadcast time and wastage while with respect to X-P-P we gain only in broadcast time
- X-P-P provides optimal trade-o between time and wastage but is not practically implementable
- P-P-G gives best trade-o and can be implemented in distributed fashion with negligible computational overhead

# Effect of Sparsity on Broadcast Delay on Real Data Set

- Already **observed presence of an optimal degree** in case of synthetic networks
- To perform simulations on the sparser variants of the Gnutella networks
  - removed a set of the network edges keeping the network connected



The broadcast time reduces significantly for the sparser variants

- 1) Problem definition
- 2) Setup
- 3) Algorithms of Message Transfer
- 4) Deeper analysis of the algorithms
- 5) **Conclusions**

# Conclusion

- Define **a new problem** in the space of information dissemination and broadcast in dynamic networks
- The **speed of broadcast** for segmented message **differs** from single message case
- **Presence of an optimal  $d$**  (average degree) irrespective of topology where the broadcast is most efficient
- **Sparseness** leads to faster broadcast

Thank You

