

Chaotic Quarks in Holographic QCD

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The Myriad Colorful Ways of Understanding Extreme QCD Matter

ICTS, Bengaluru



Based on

Earlier Works

1. *A Bound on Chaos* (Maldacena , Shenker, Stanford)
2. *Stringy Effects in Scrambling* (Shenker, Stanford)
3. *Chaotic Strings in AdS/CFT* (Jan de Boer , E. Llabres, Juan Pedraza, D. Vegh)

Our Works

arXiv:1811.04977, arXiv:1809.02090 (AB , A. Kundu, R.Poojary)



Introduction and Motivation



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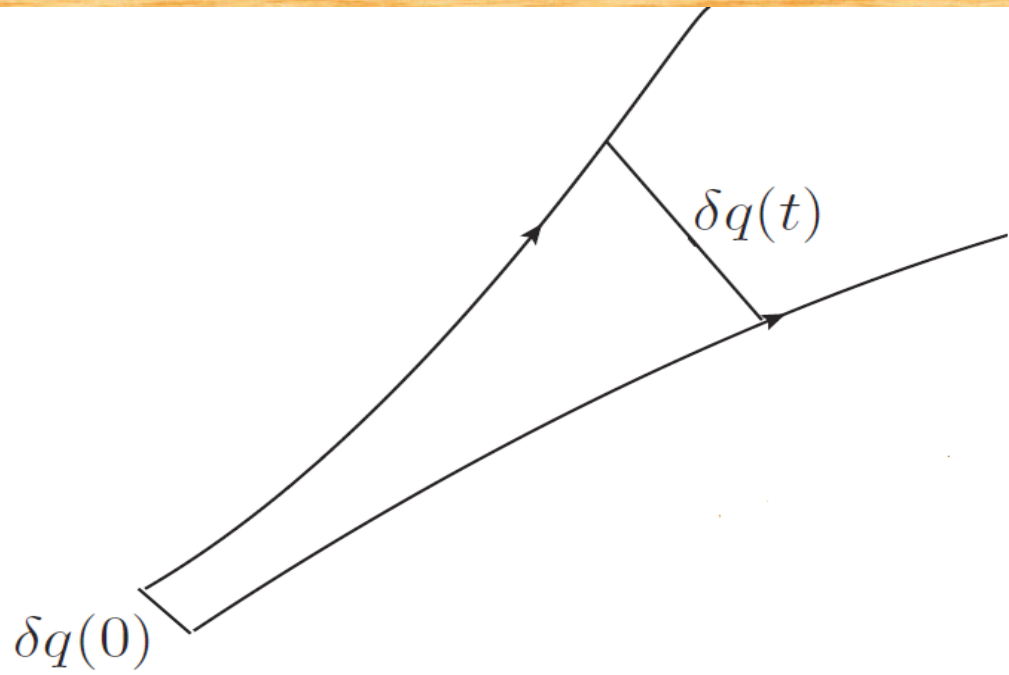
Holography provides a sharp upper bound on the rate of growth of chaos in the strongly coupled theories(gluonic sector). How does this bound translate to the flavor sector.

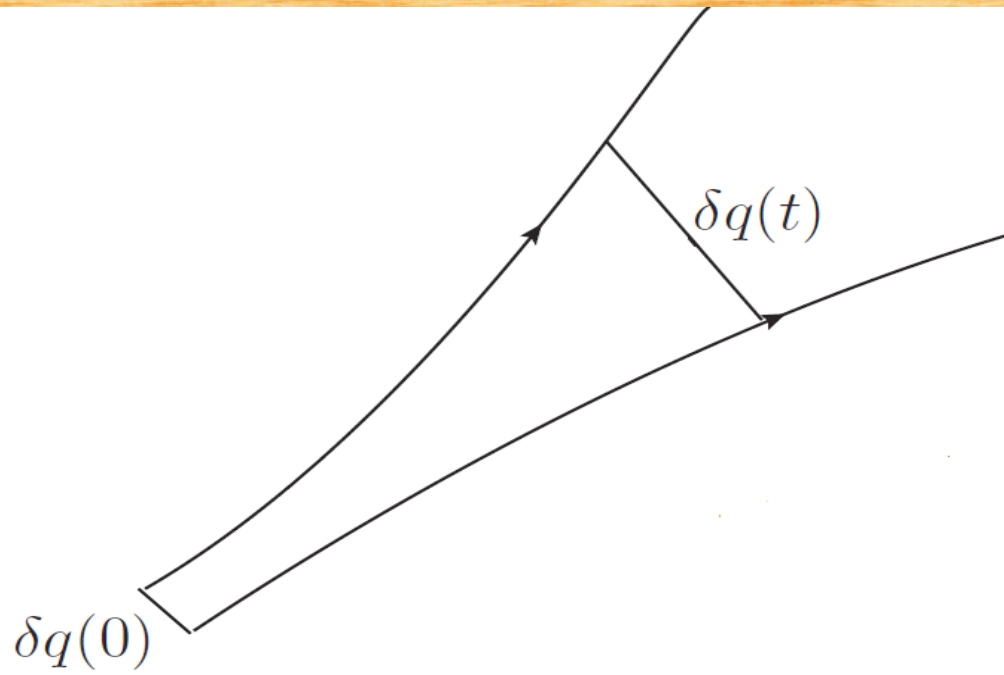


Outline

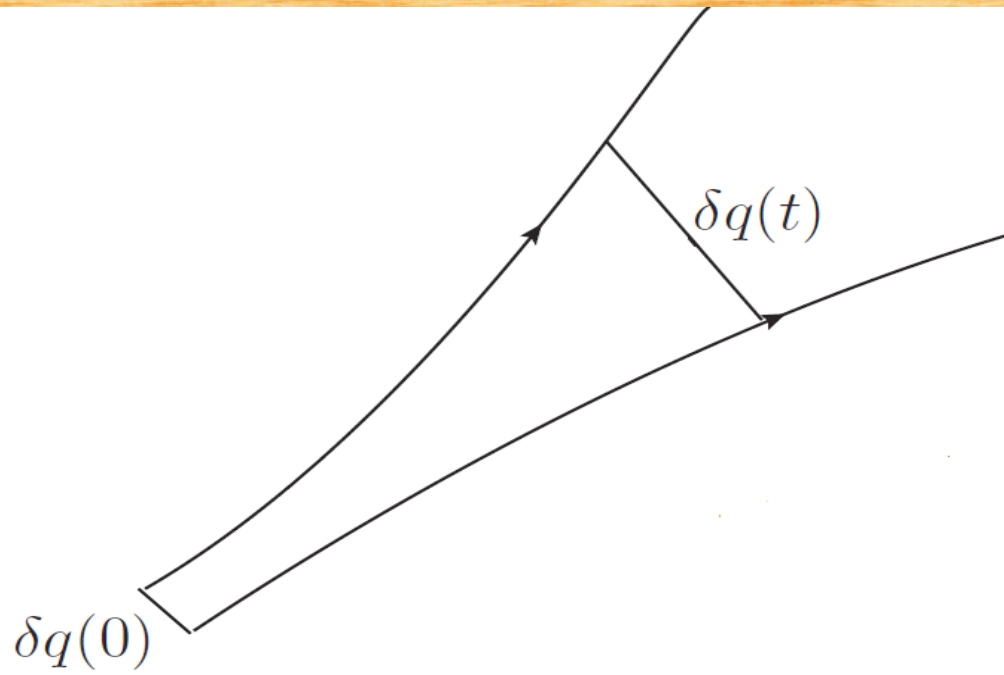
1. Chaos in Quantum Systems - Basic Idea
2. The Holographic Approach
3. Chaos in Flavor Sector
4. Concluding Remarks and Open Questions





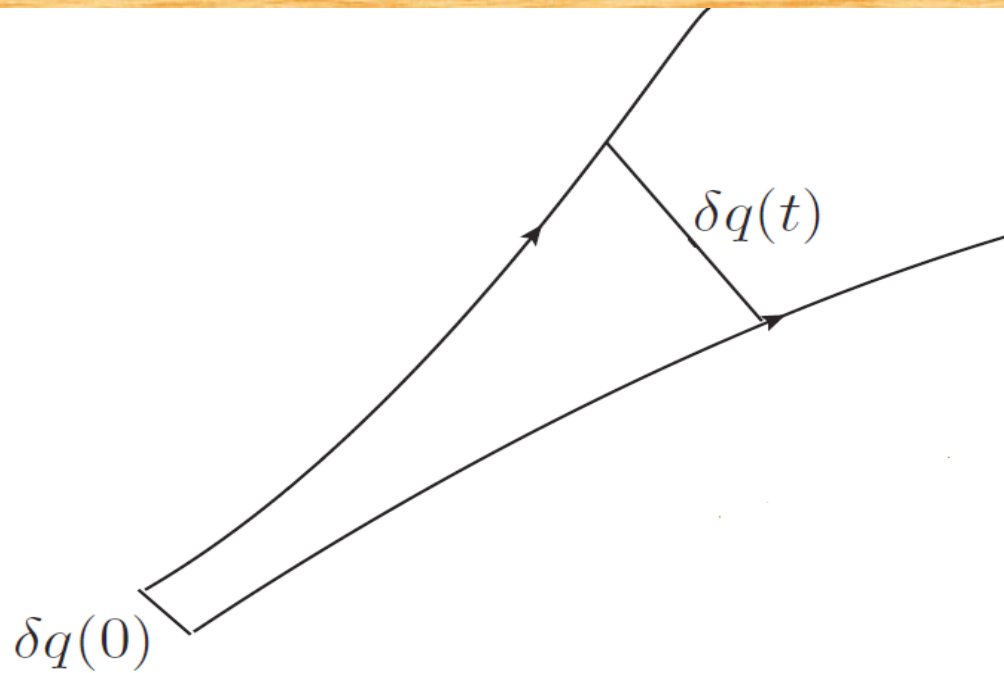


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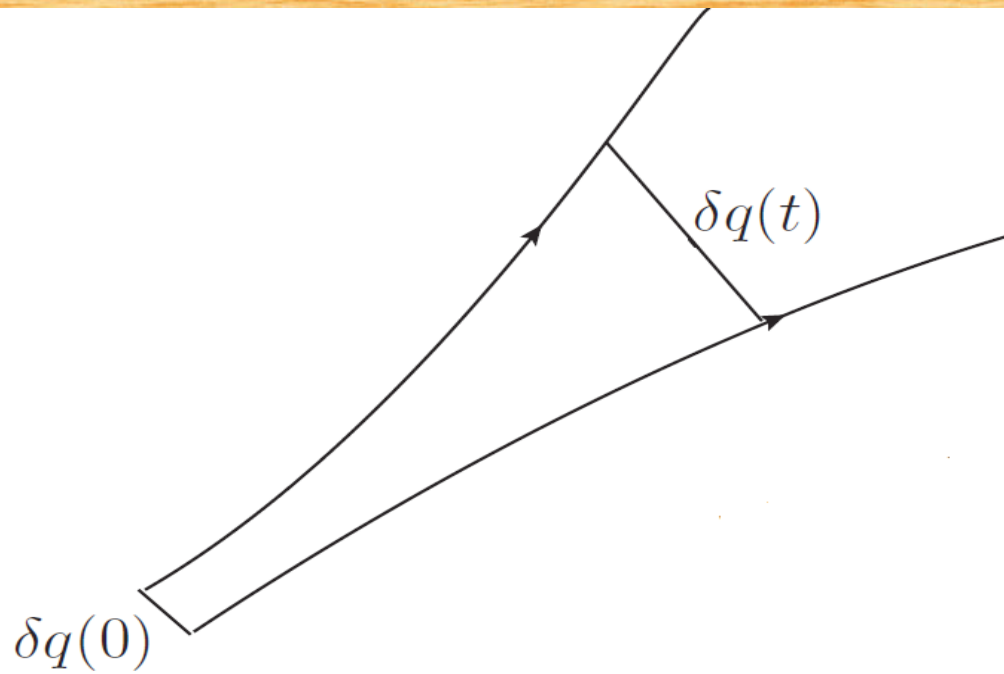
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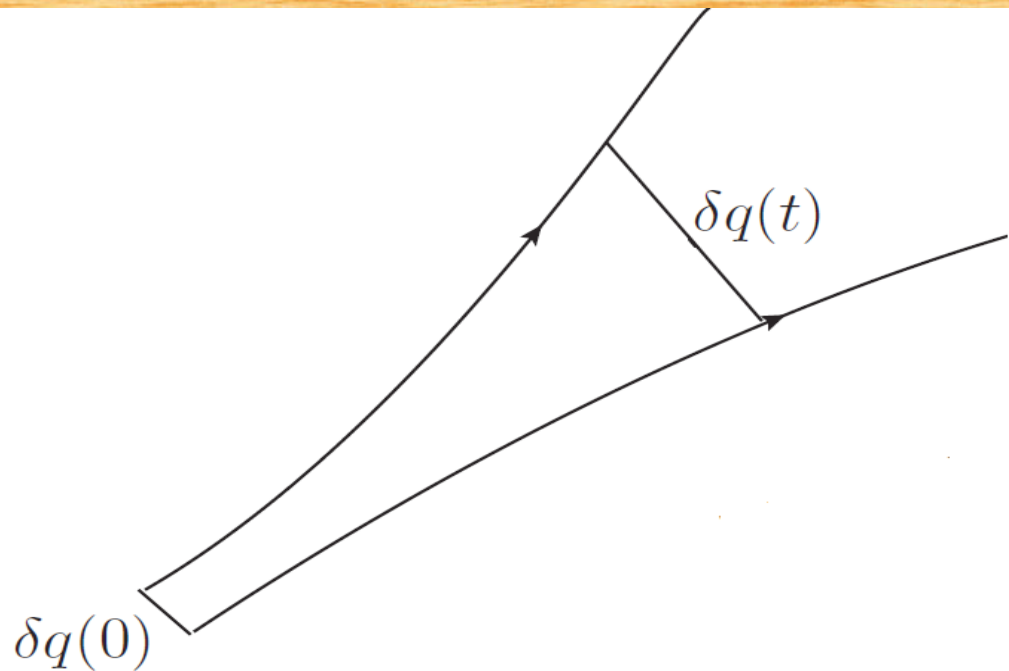
$$\{q(t), p(0)\}$$



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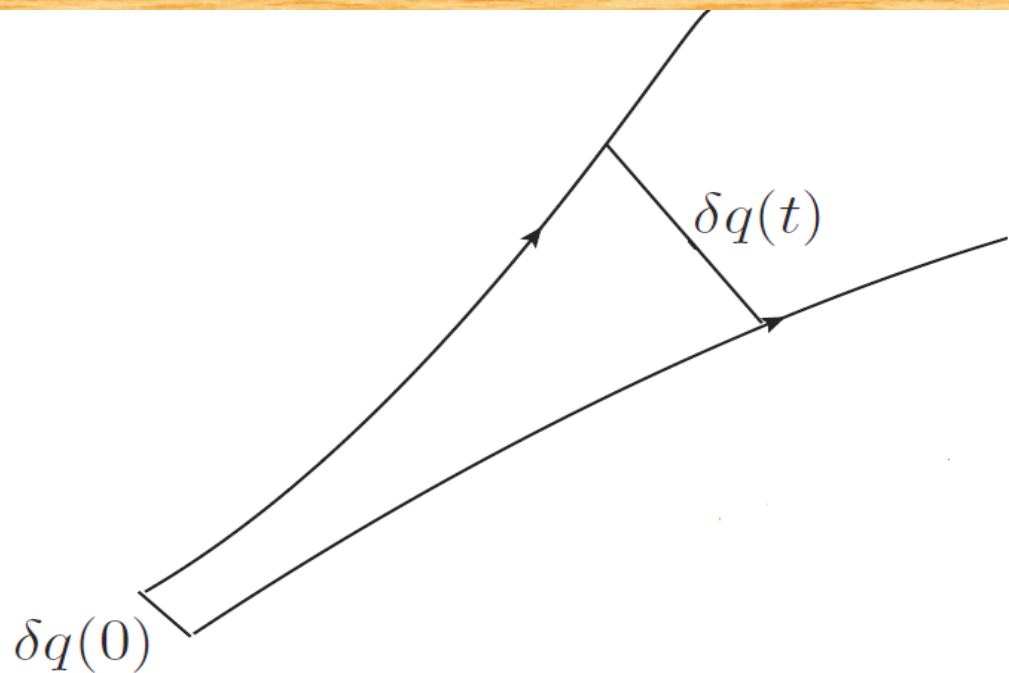


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(TOC)

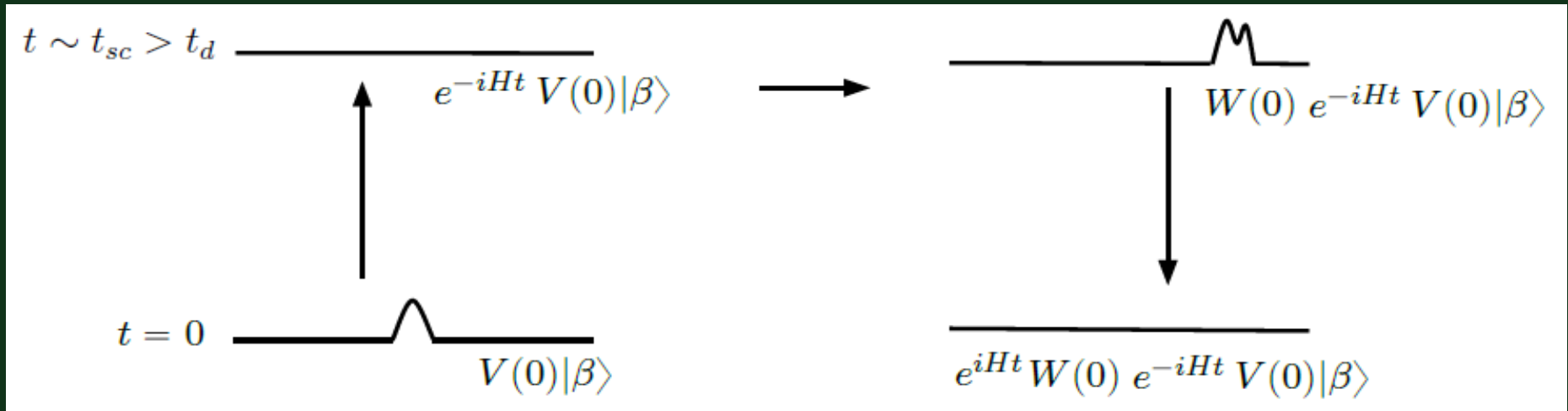
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(OTOC)

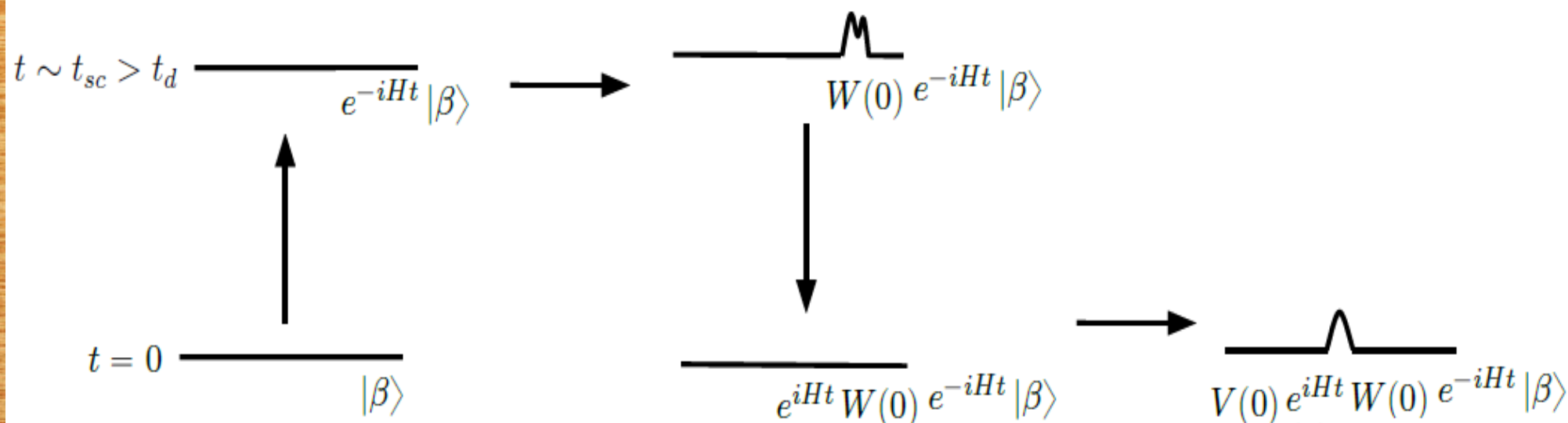
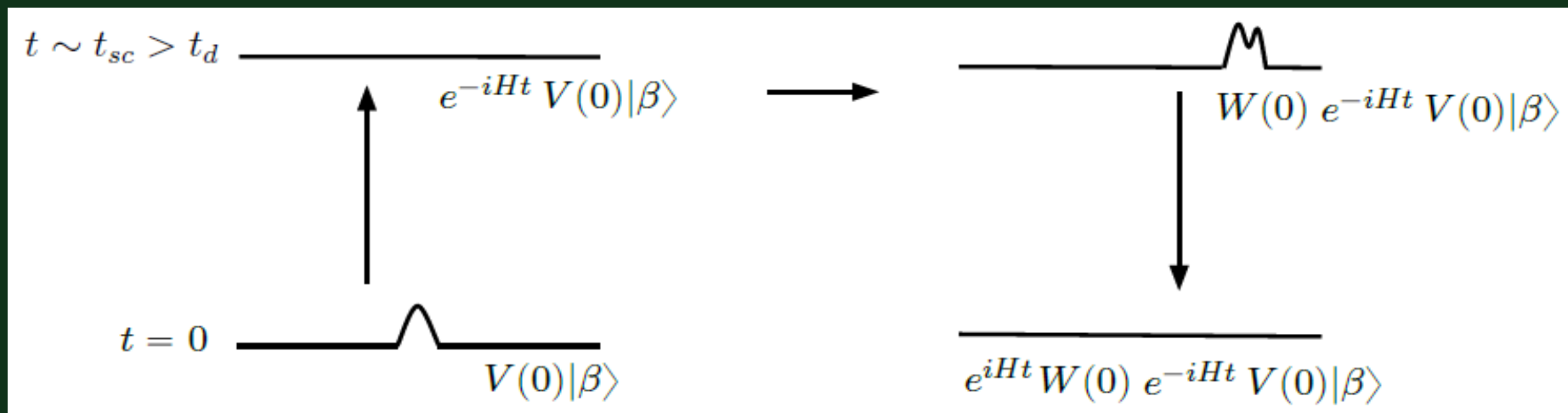
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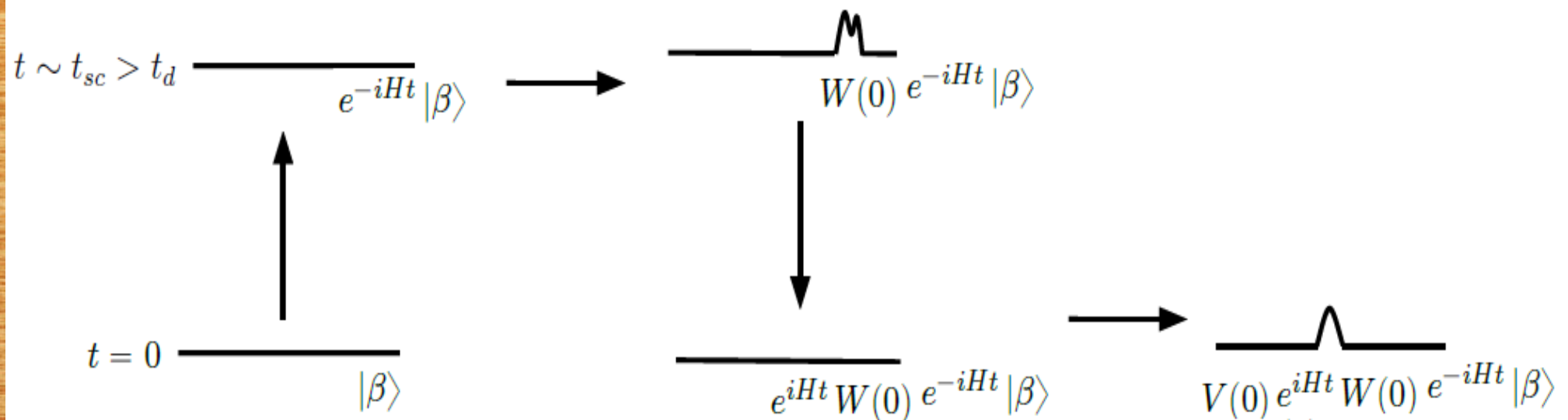
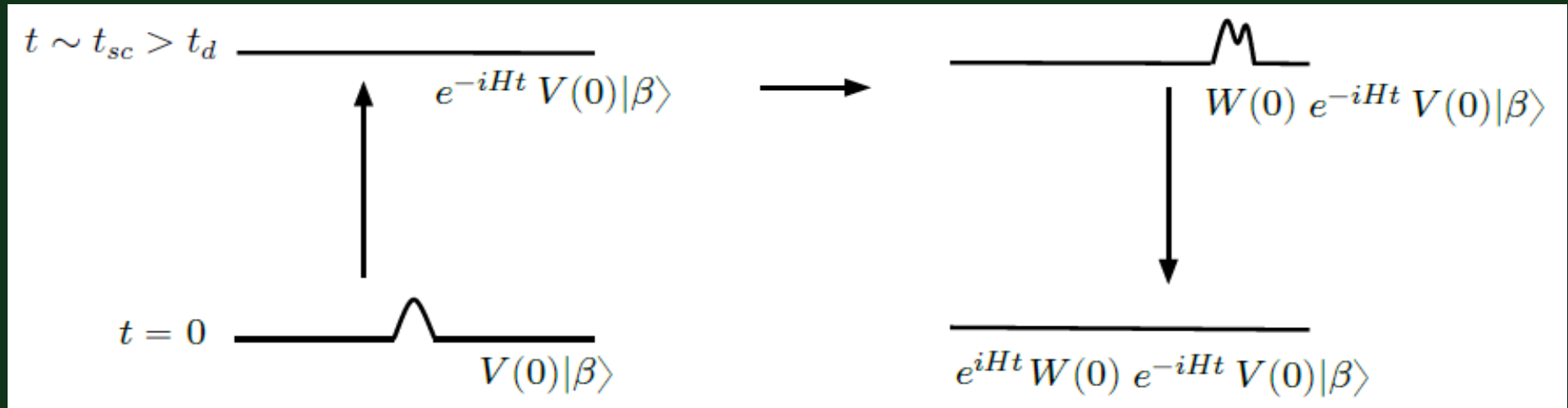
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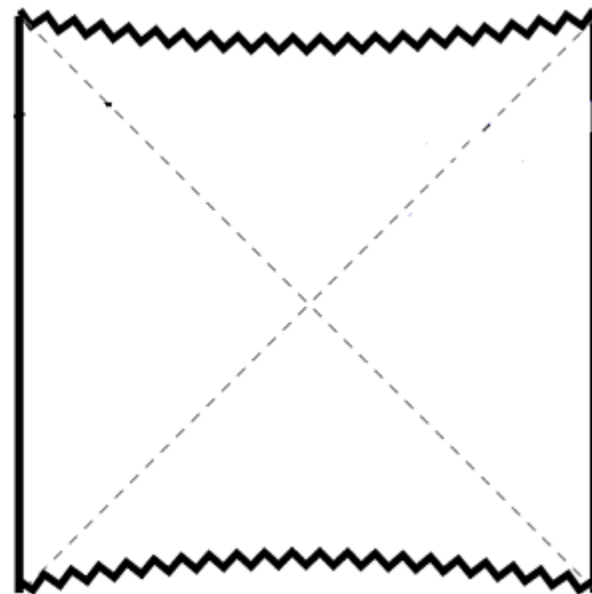
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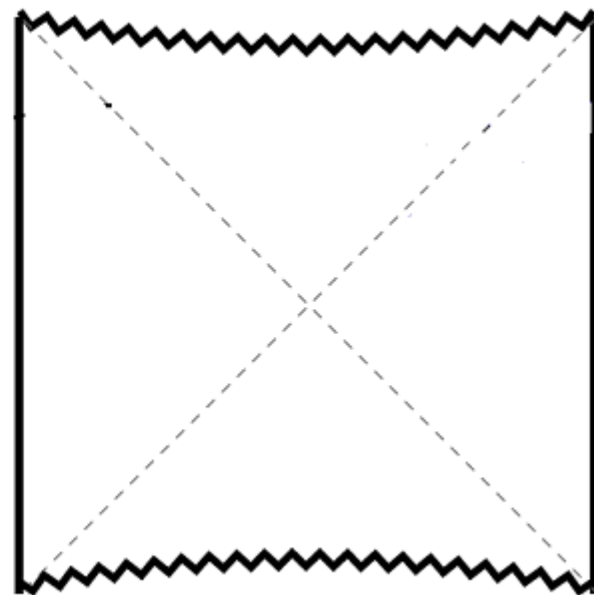
Such OTOCs in QFT are calculated using Schwinger-Keldysh techniques. Alternately, holography gives a simpler and elegant prescription

$|\beta\rangle$

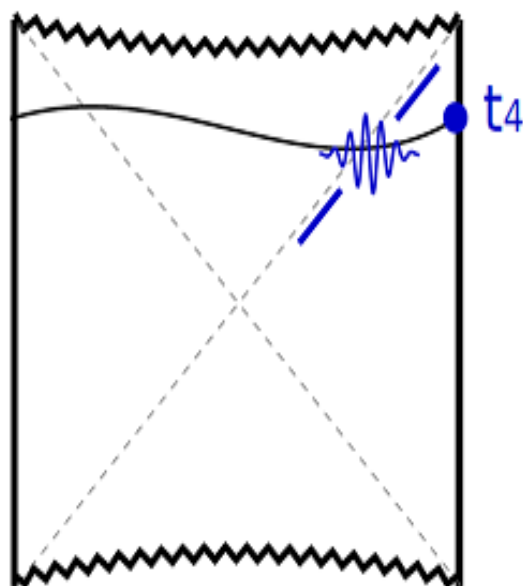
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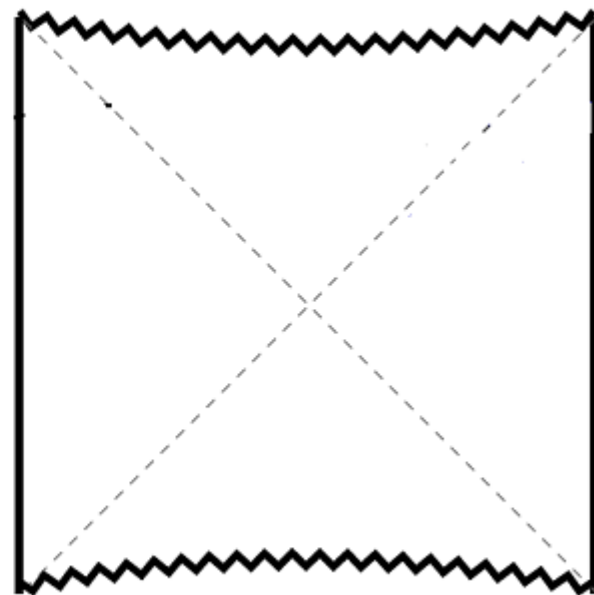
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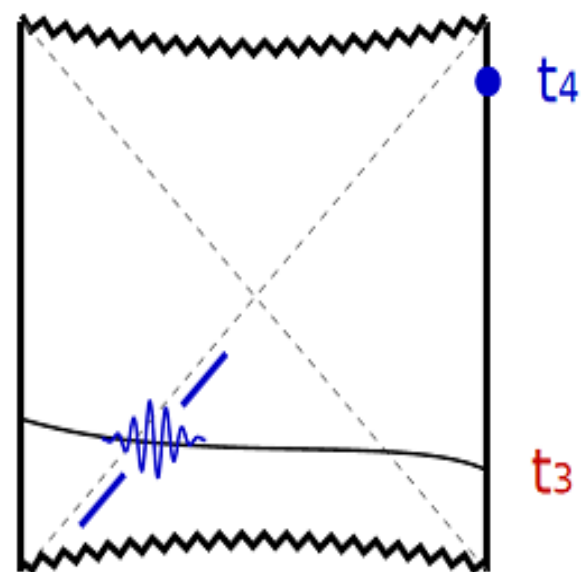
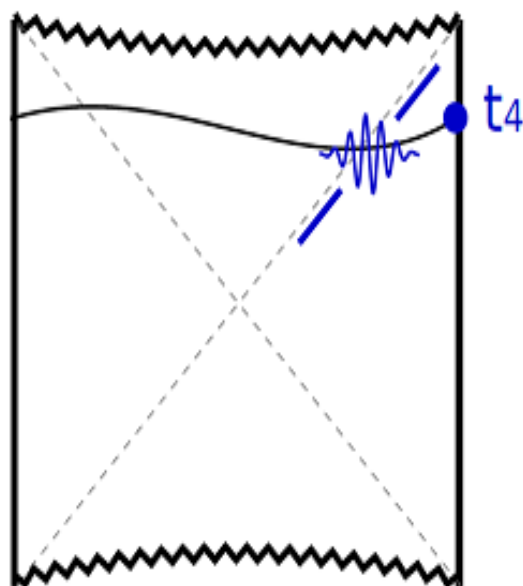
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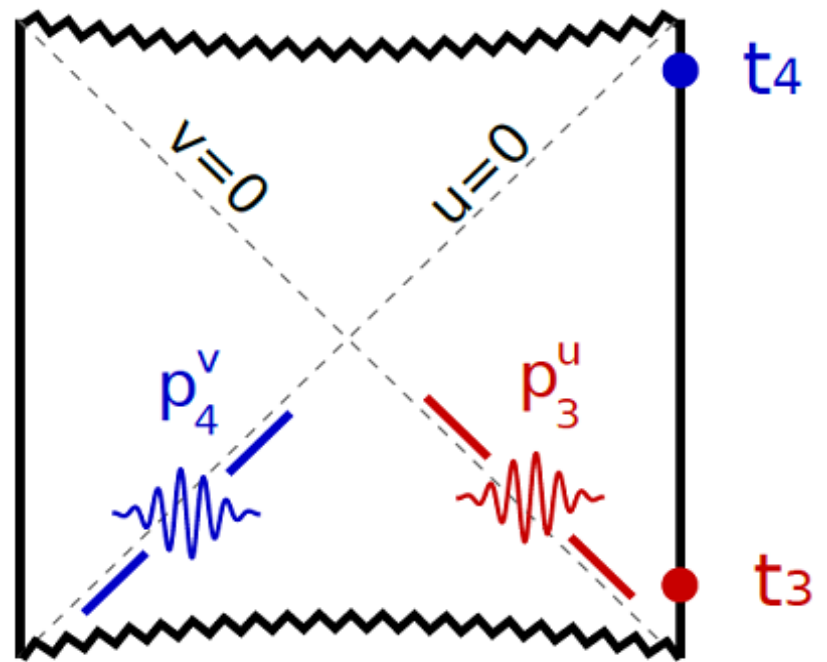
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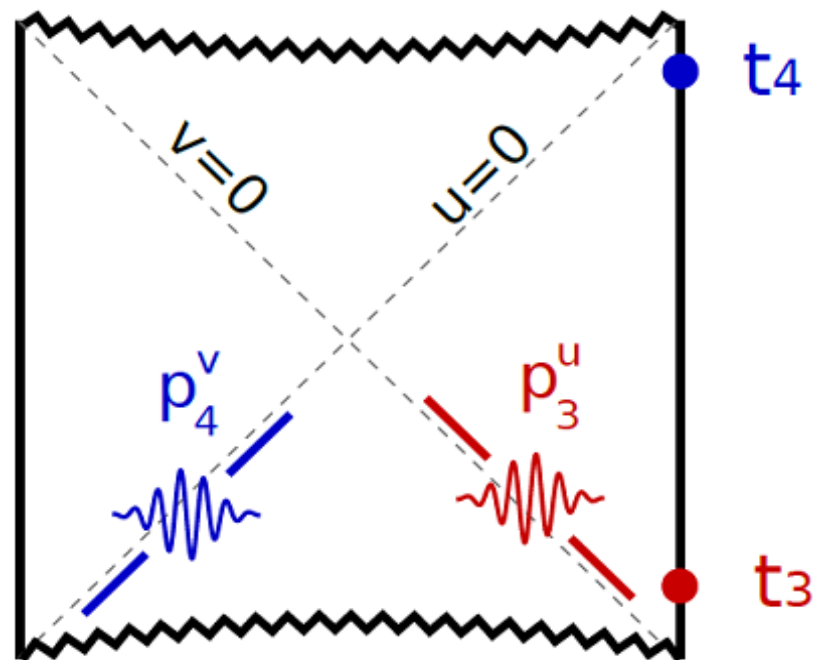
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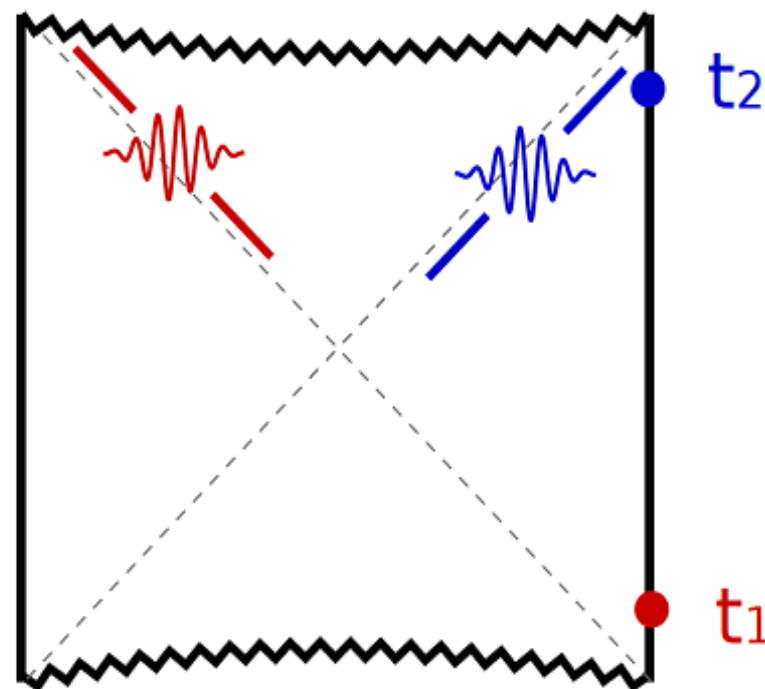
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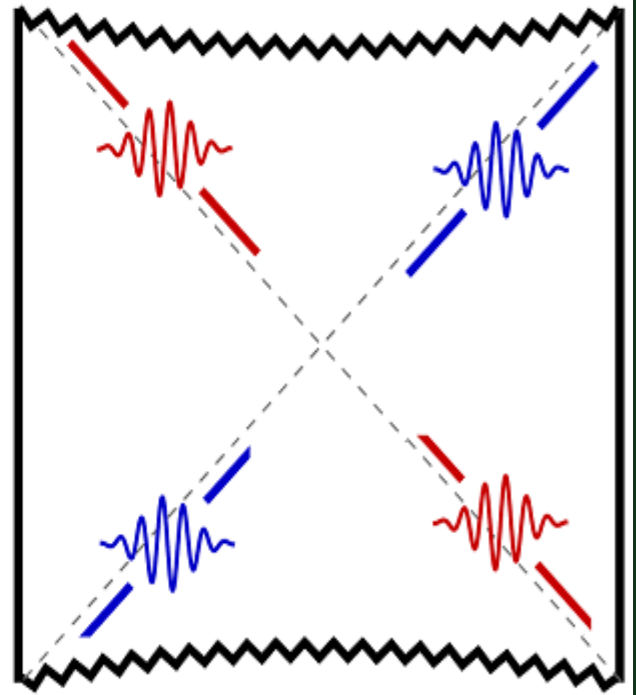
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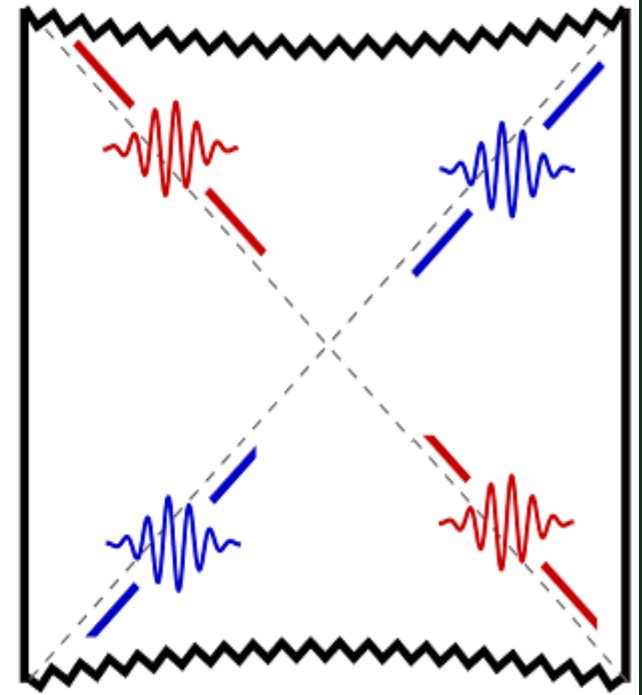
$$W(t_2)V(t_1)|\beta > \equiv$$



$$\langle \beta | V(t_1) W(t_2) V(t_3) W(t_4) | \beta \rangle \equiv$$

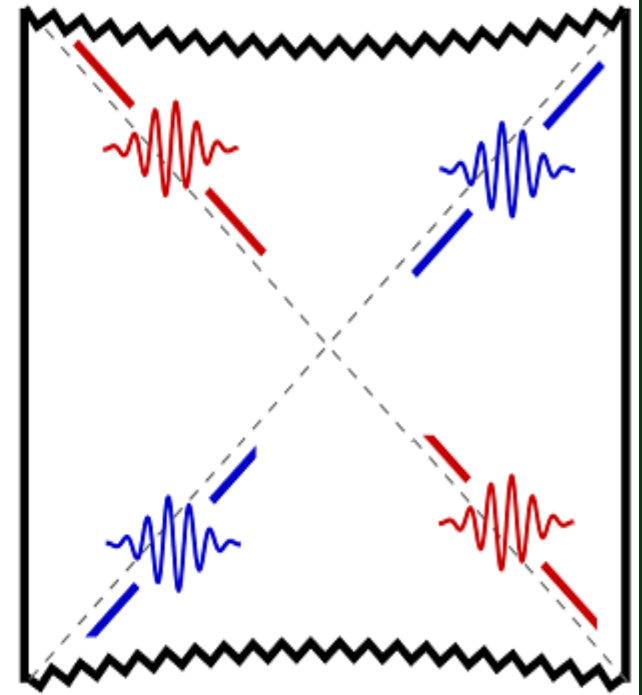


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$$= \int dp_1^u dp_2^v \ e^{i\delta(s)} \ p_1^u \ p_2^v \ \psi_1^* (p_1^u) \ \psi_2^* (p_2^v) \ \psi_3 (p_1^u) \ \psi_4 (p_2^v)$$

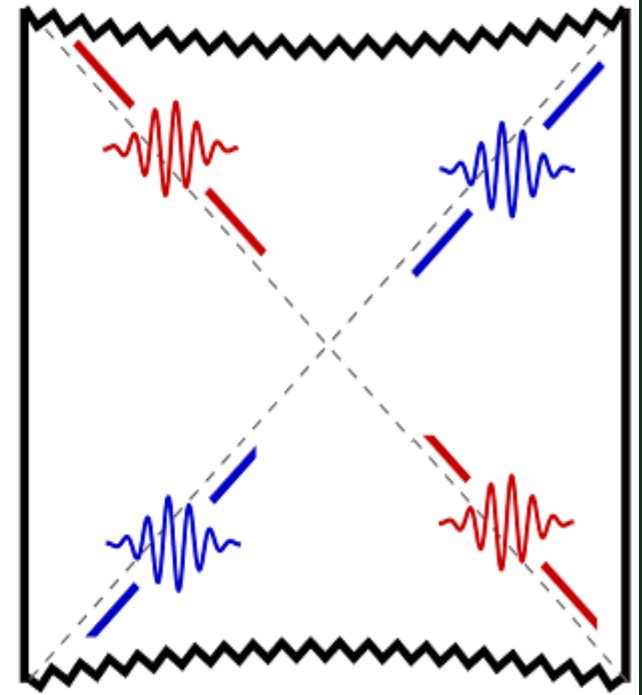
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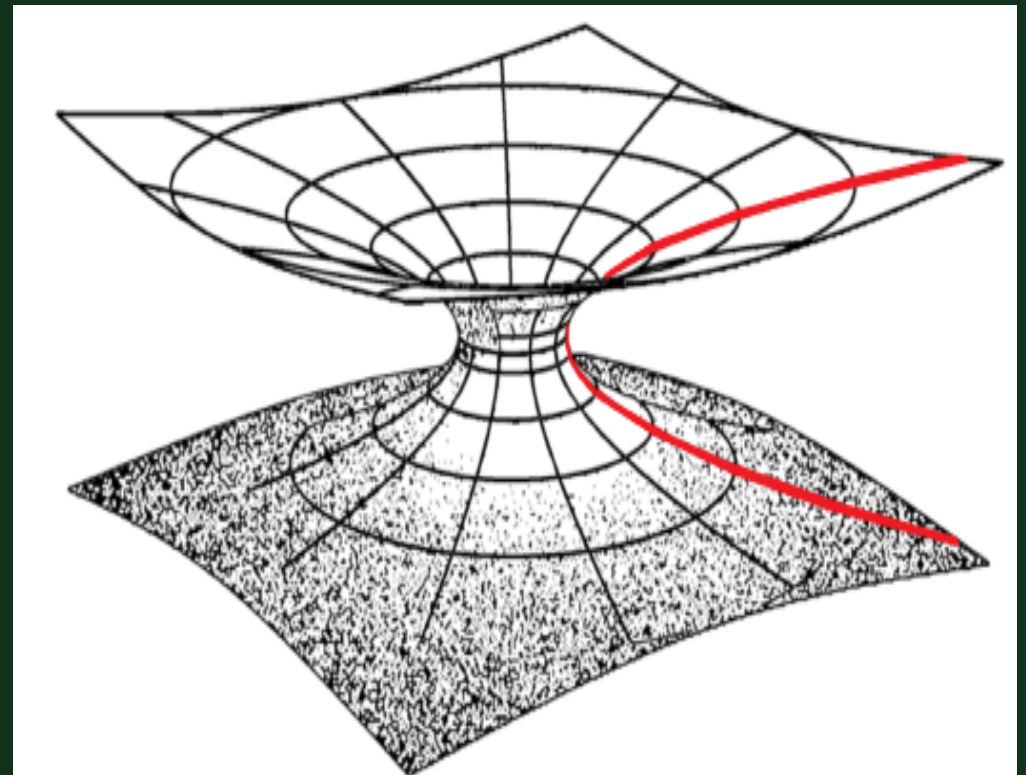
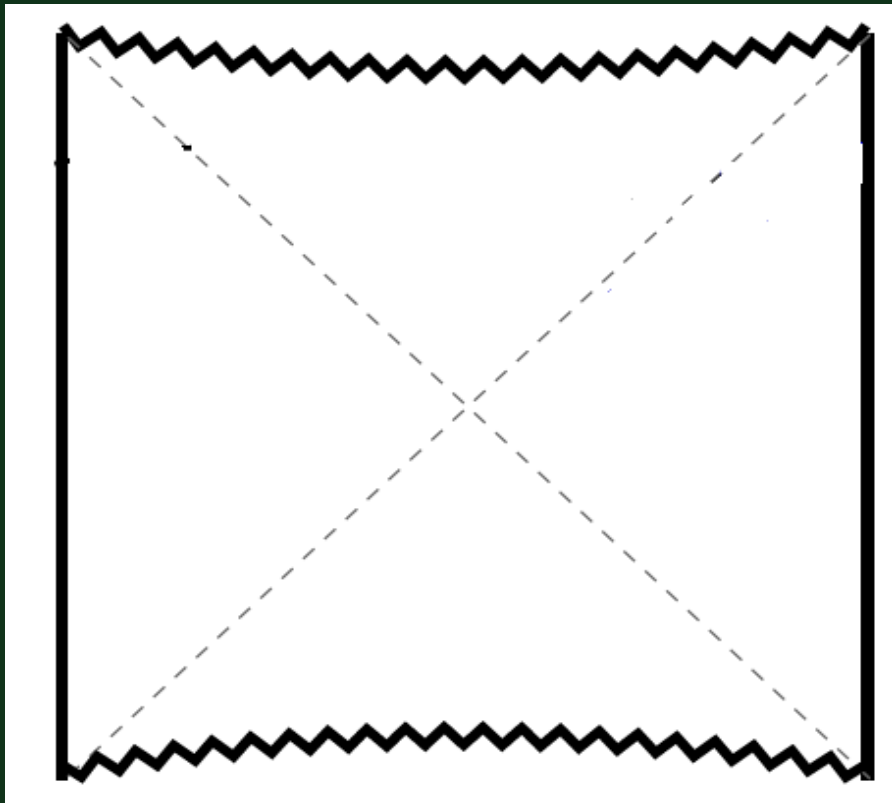
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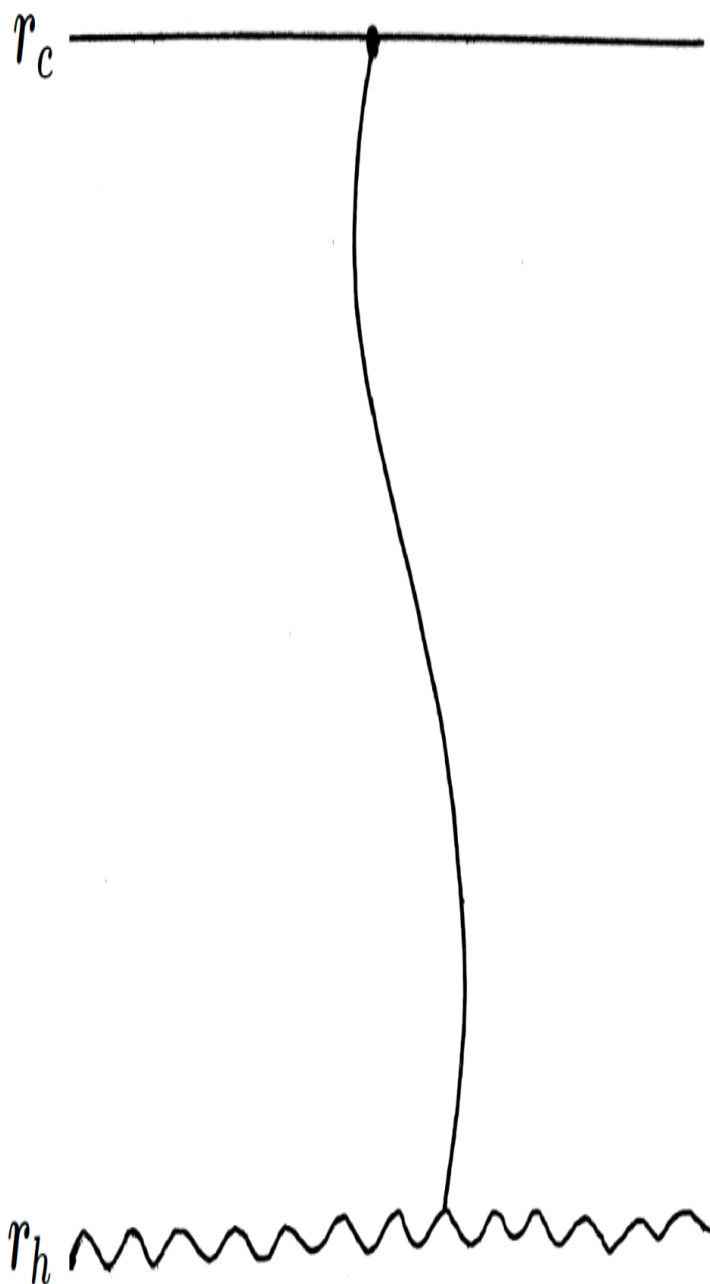
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r_c

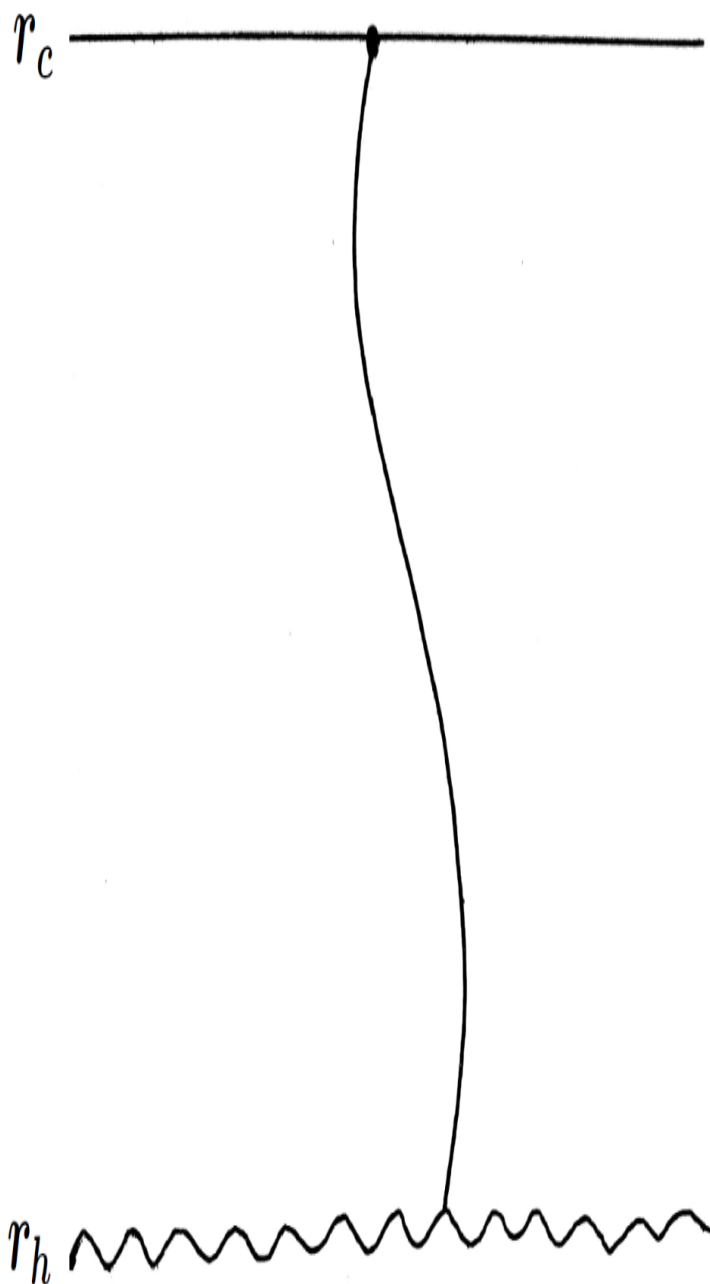


r_h



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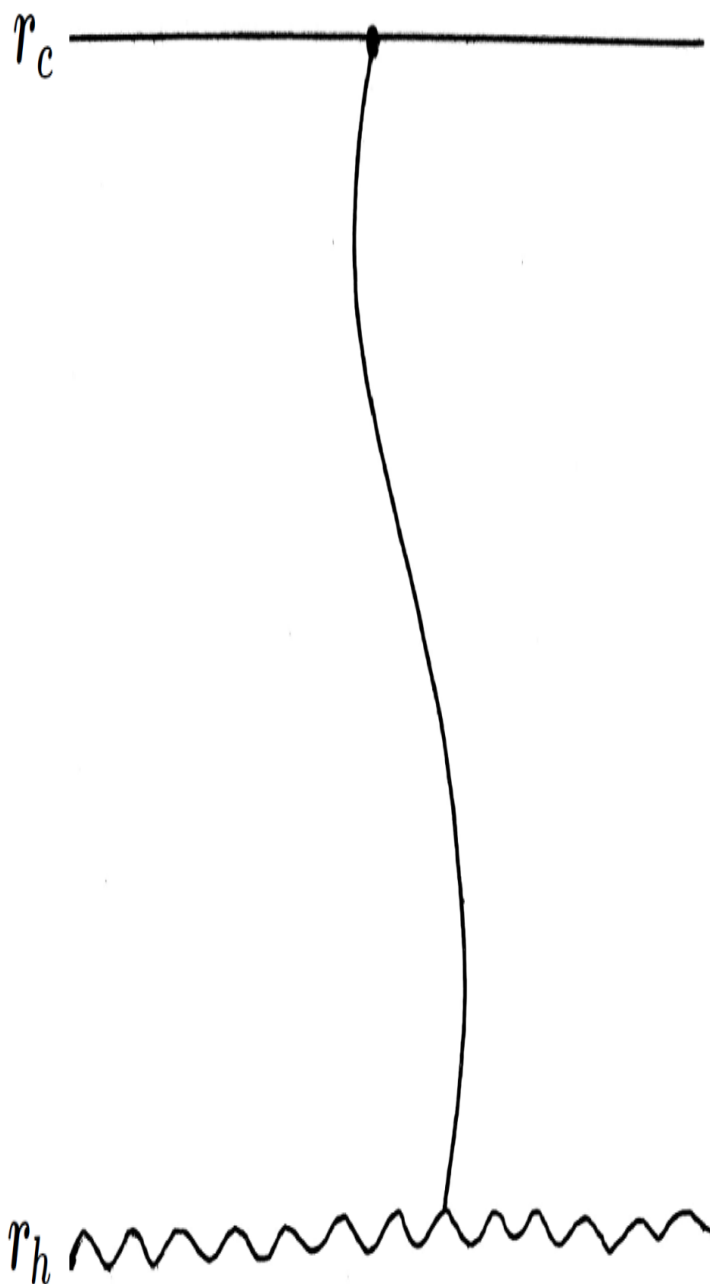
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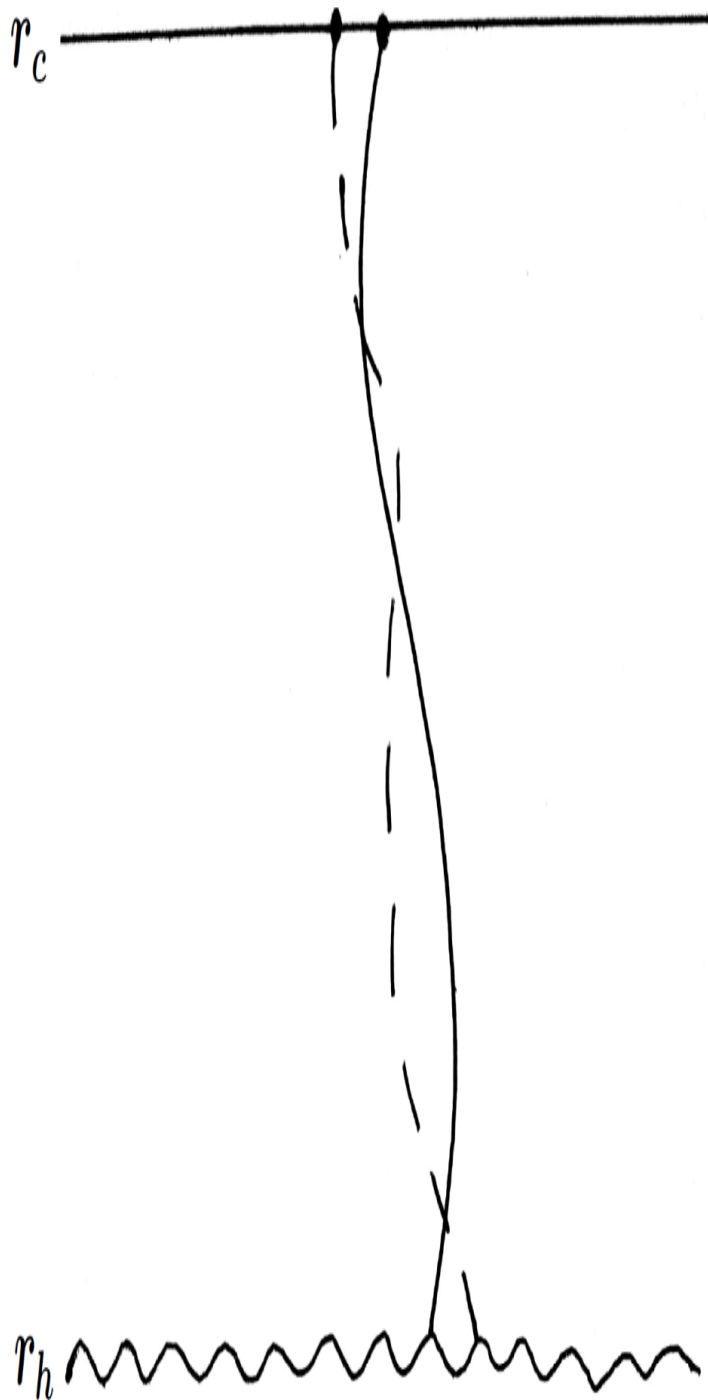
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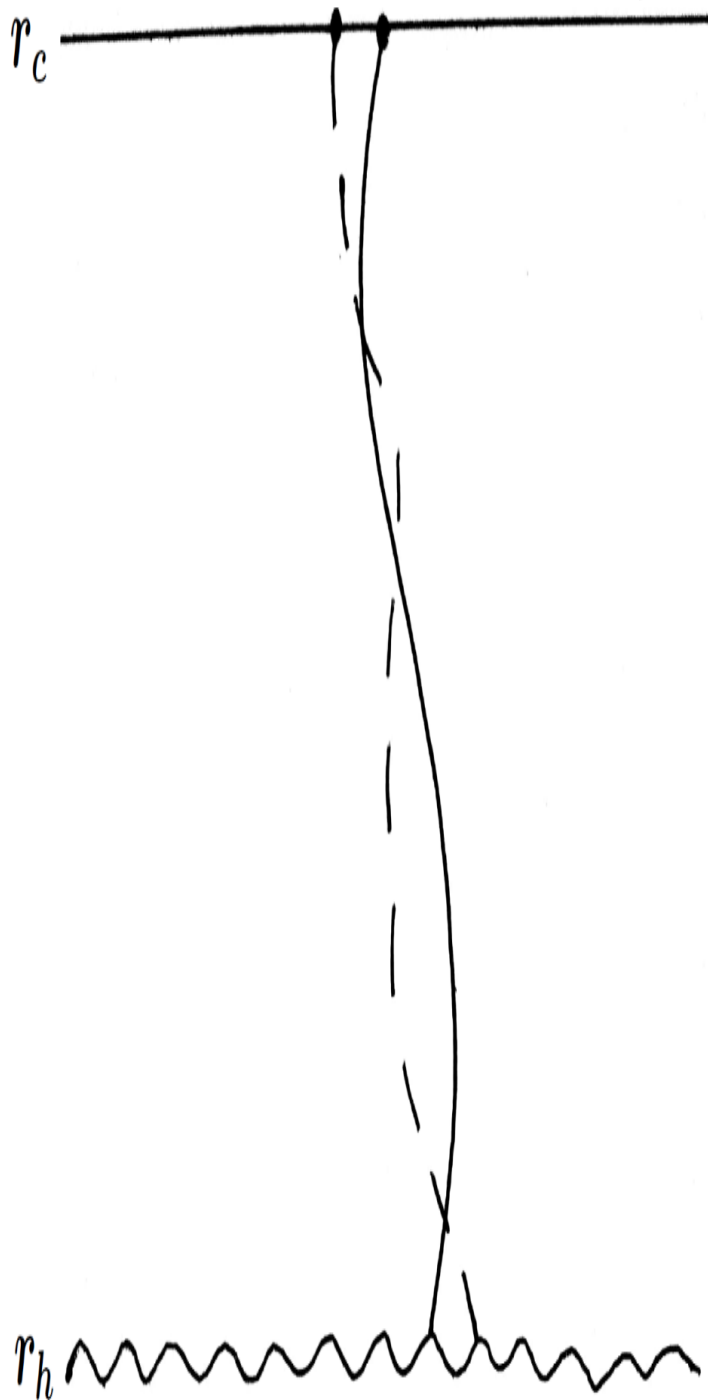
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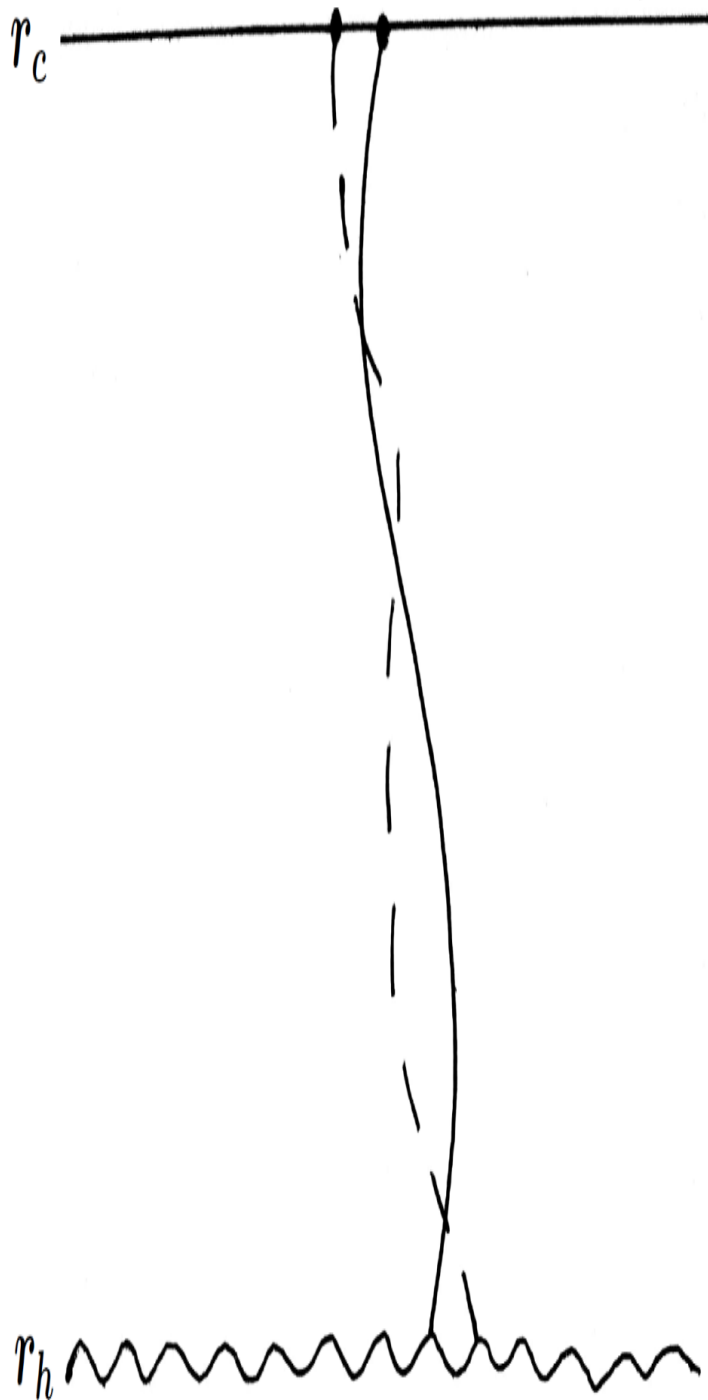


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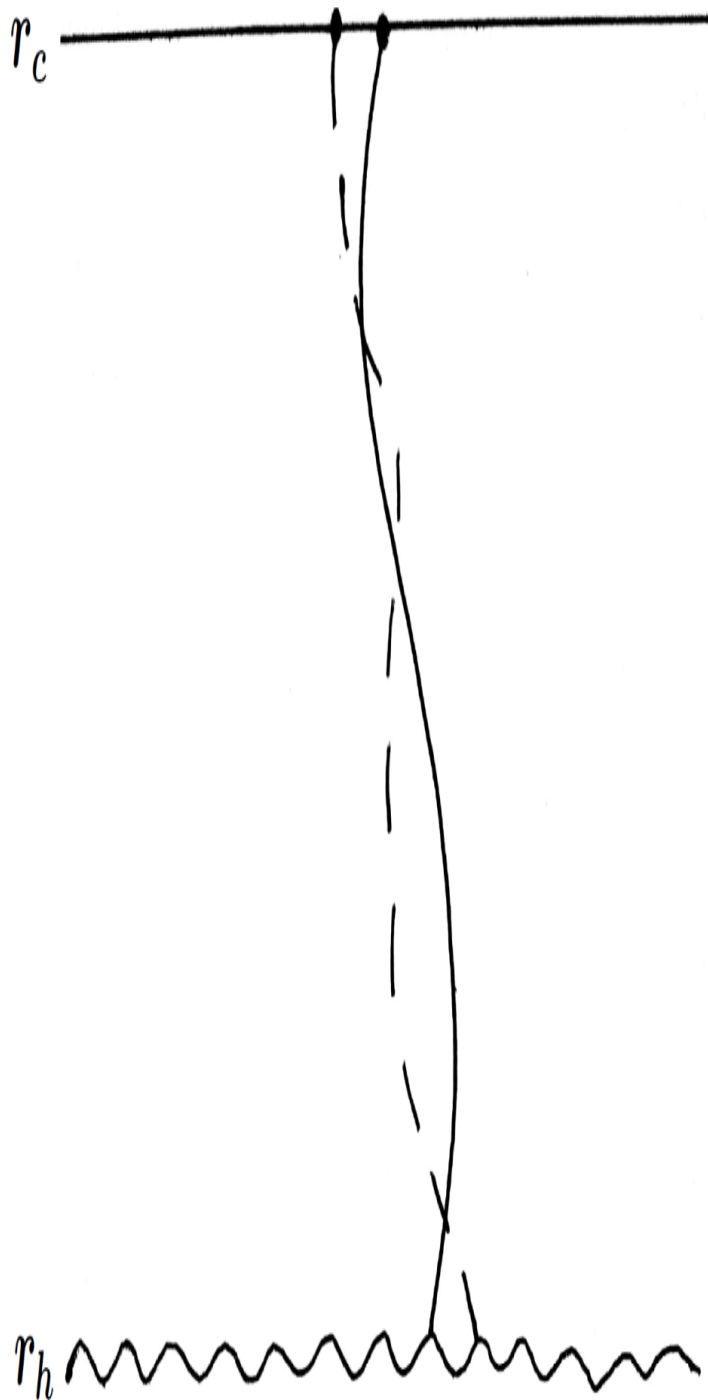
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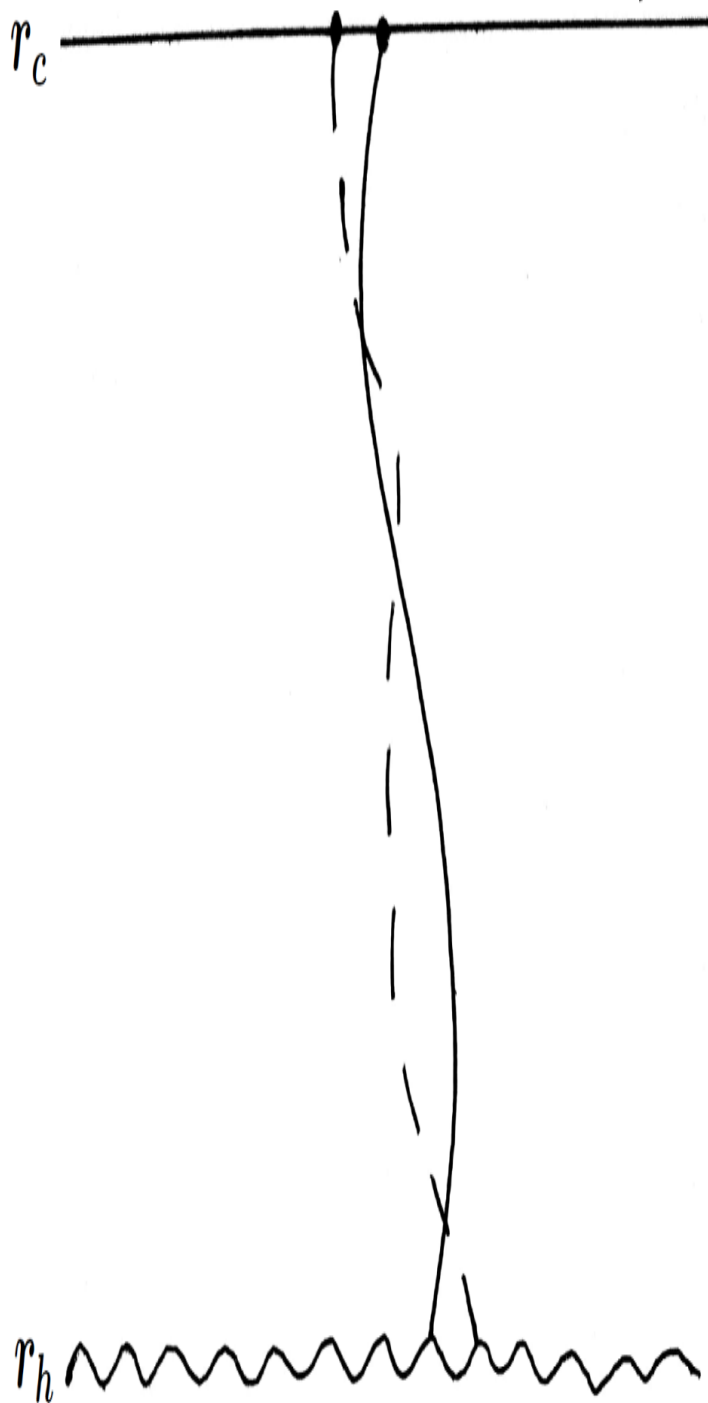
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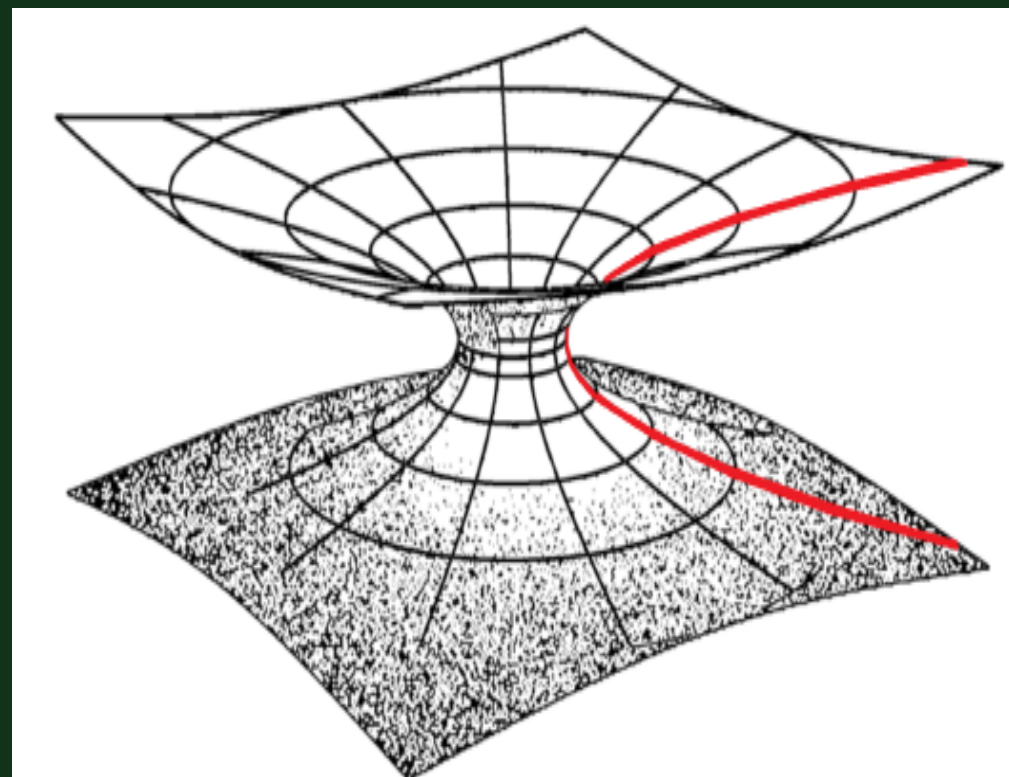
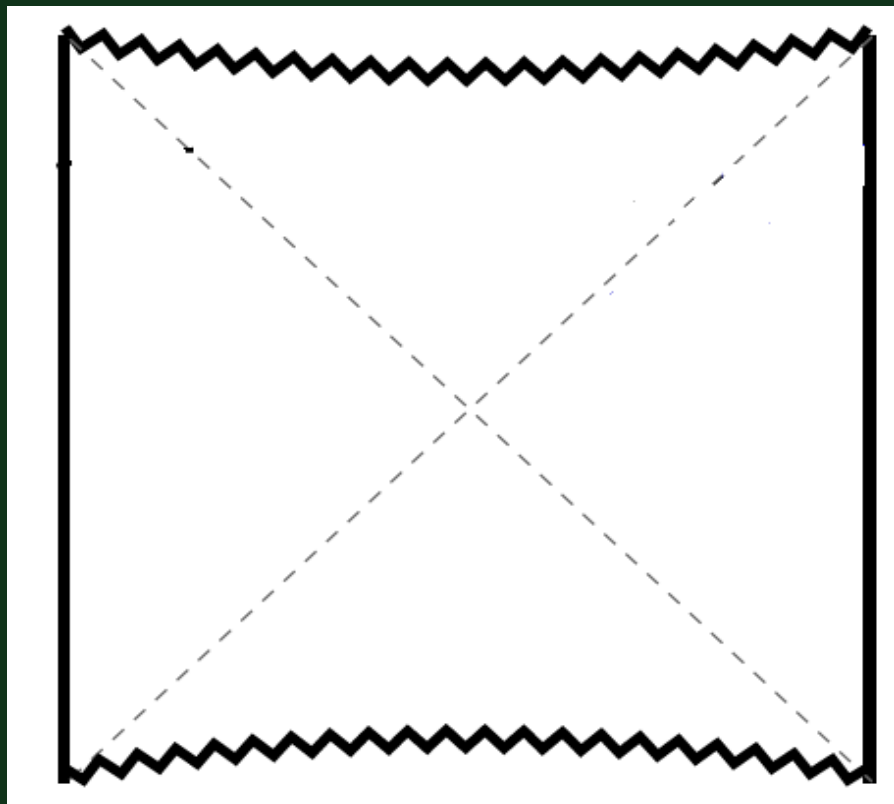
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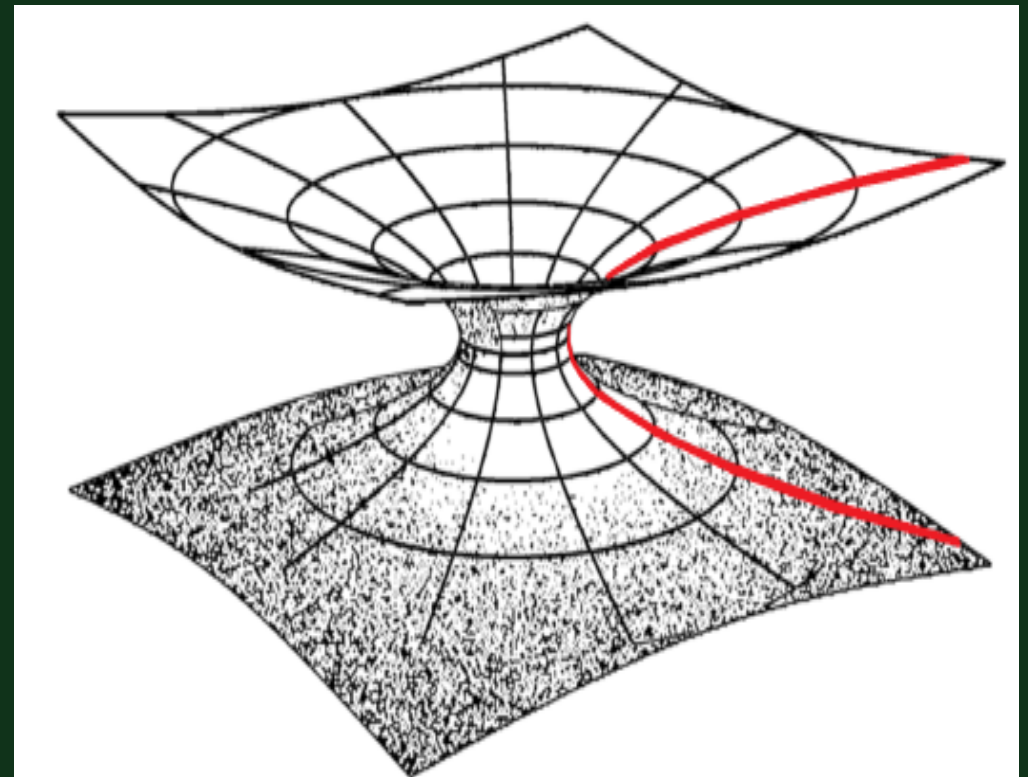
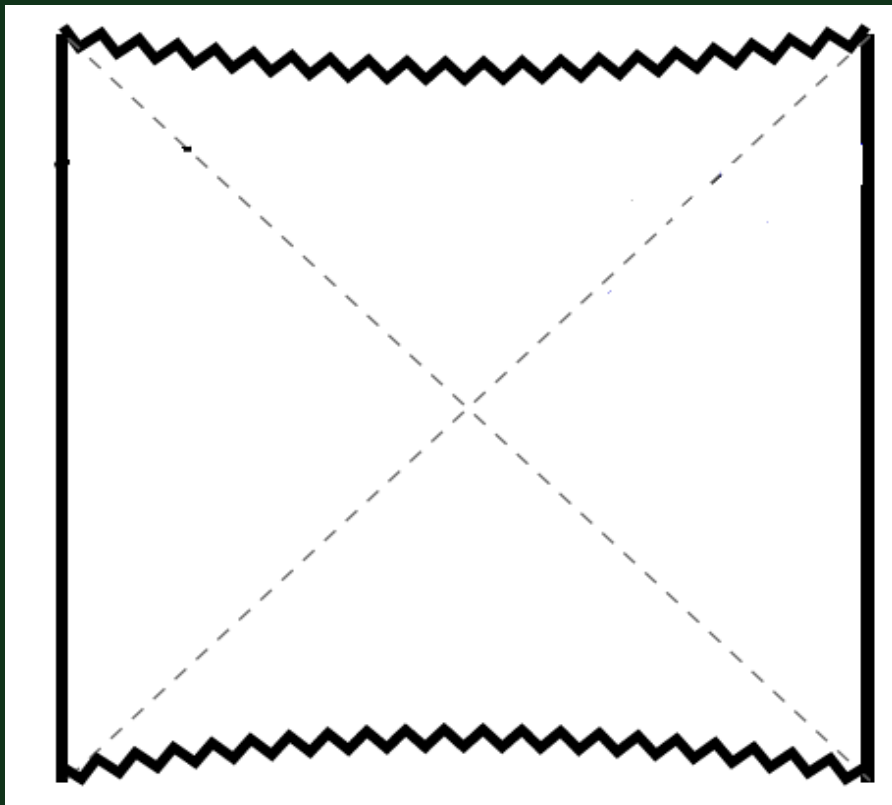
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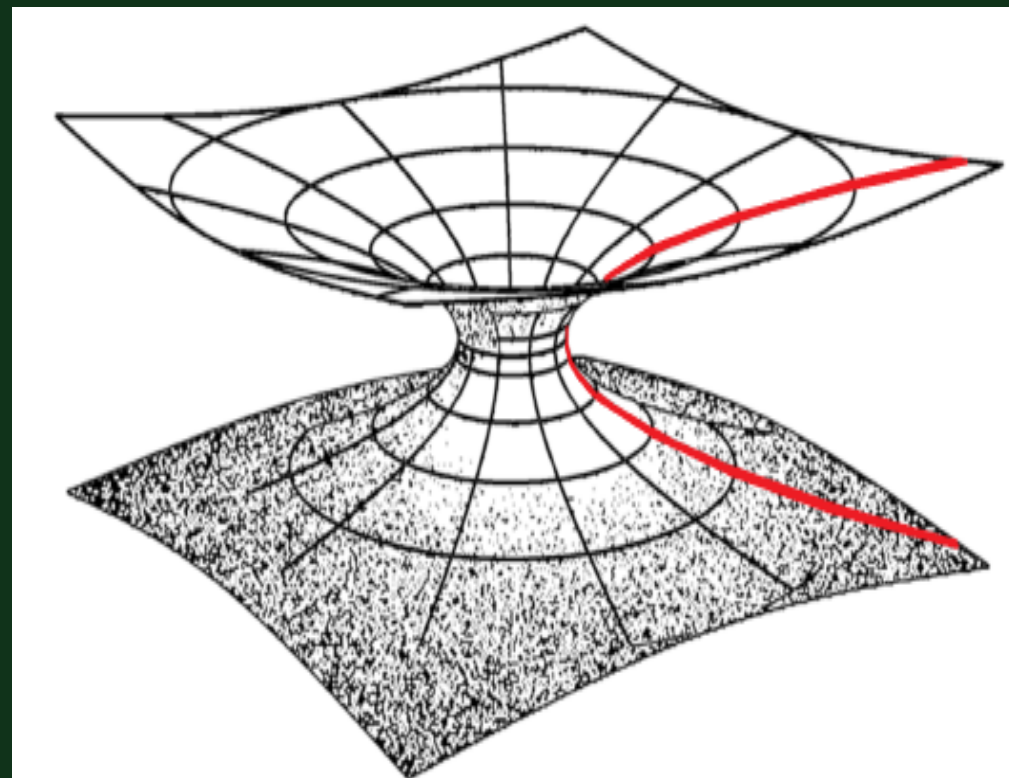
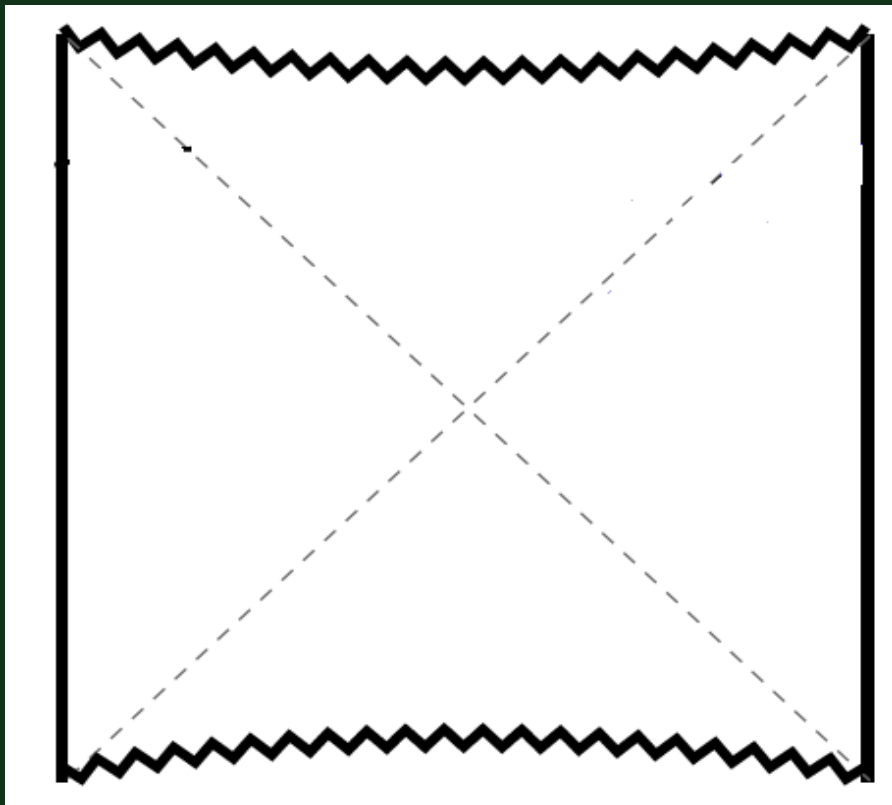
de Boer et al.





Gravity Side

Field theory side

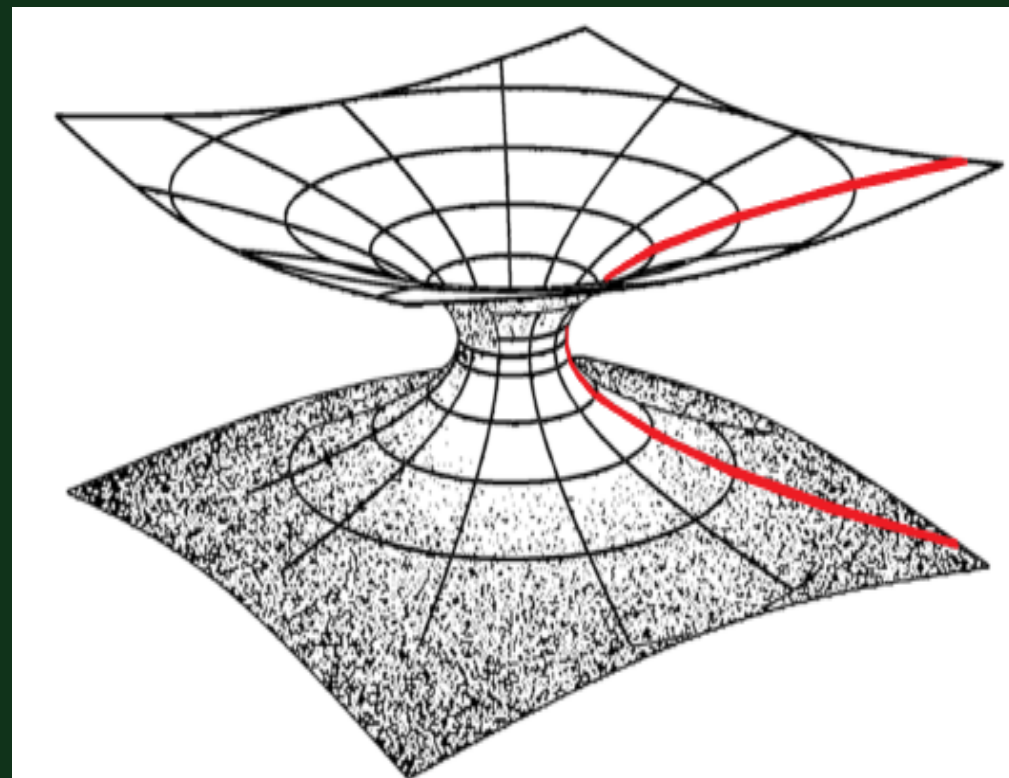
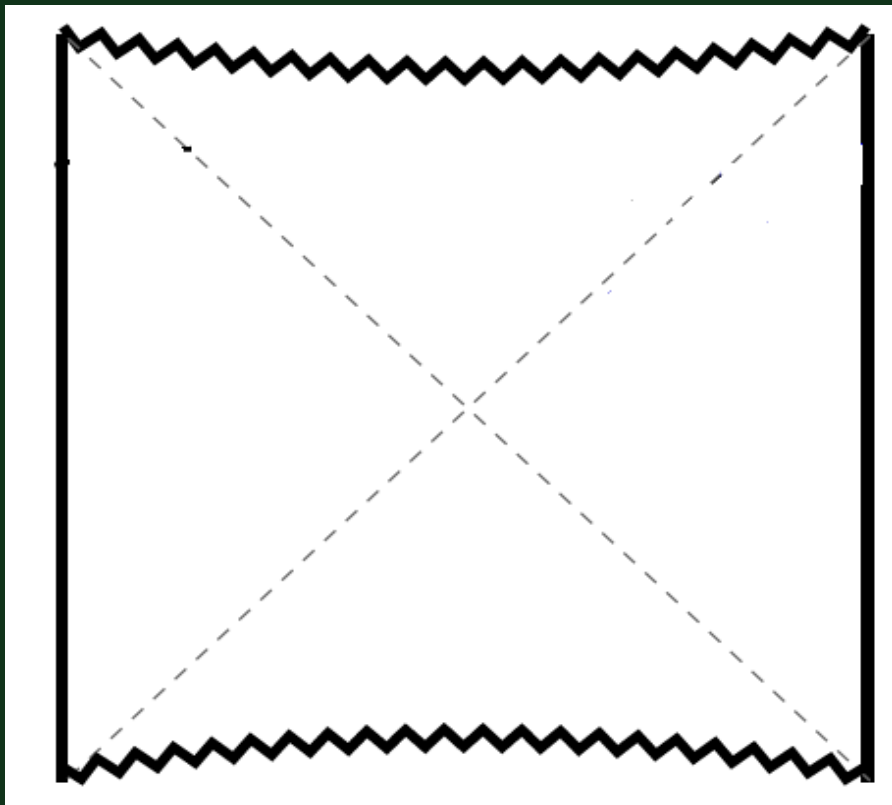


Gravity Side

Is black hole background essential?

Field theory side

What if the background plasma is at zero temperature



Gravity Side

Is black hole background essential?

Do vectors fluctuations saturate the bound as well?

Field theory side

What if the background plasma is at zero temperature

Fluctuations of vector mesons?


$$\underline{D3_N - D5_M (N \gg M)}$$

$D3_N - D5_M (N \gg M)$

	r	t	x^1	x^2	x^3	ψ	θ	ϕ	χ	ζ
D3	\times	\checkmark	\checkmark	\checkmark	\checkmark	\times	\times	\times	\times	\times
D5	\checkmark	\checkmark	\checkmark	\checkmark	\times	\times	\checkmark	\checkmark	\times	\times

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D3	\times	\checkmark	\checkmark	\checkmark	\checkmark	\times	\times	\times	\times	\times
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$$ds^2 = \frac{r^2}{R^2} (-dt^2 + d\bar{x}^2) + \frac{R^2}{r^2} dr^2 + R^2 d\Omega_5^2$$

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D3	\times	\checkmark	\checkmark	\checkmark	\checkmark	\times	\times	\times	\times	\times
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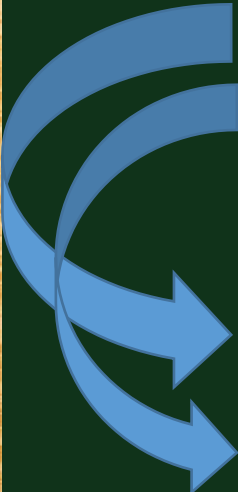
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D3	\times	\checkmark	\checkmark	\checkmark	\checkmark	\times	\times	\times	\times	\times
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D3	\times	\checkmark	\checkmark	\checkmark	\checkmark	\times	\times	\times	\times	\times
D5	\checkmark	\checkmark	\checkmark	\checkmark	\times	\times	\checkmark	\checkmark	\times	\times

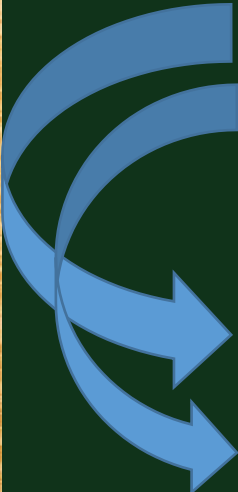


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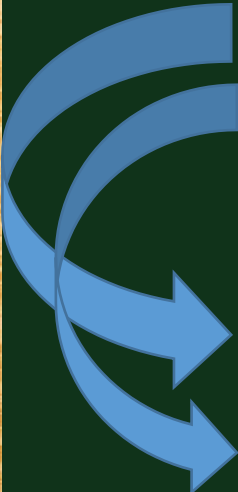
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Fluctuation on the brane perceive an effective geometry $S_{ab} = P[g]_{ab} - (F.P[g]^{-1}.F)_{ab}$

$D3_N - D5_M (N \gg M)$

	r	t	x^1	x^2	x^3	ψ	θ	ϕ	χ	ζ
D3	\times	\checkmark	\checkmark	\checkmark	\checkmark	\times	\times	\times	\times	\times
D5	\checkmark	\checkmark	\checkmark	\checkmark	\times	\times	\checkmark	\checkmark	\times	\times



$$ds^2 = \frac{r^2}{R^2} (-dt^2 + d\bar{x}^2) + \frac{R^2}{r^2} dr^2 + R^2 d\Omega_5^2 \longrightarrow \boxed{T = 0}$$

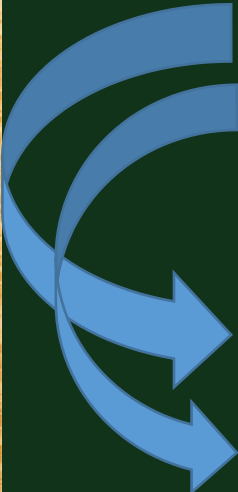
$$S_{D5} = -\tau_5 \int d^6 y \sqrt{-\det (P[g] + F)} \longrightarrow \{X, A_\mu\}$$

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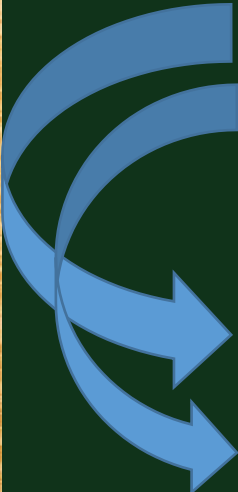
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D3	\times	\checkmark	\checkmark	\checkmark	\checkmark	\times	\times	\times	\times	\times
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T_{eff}

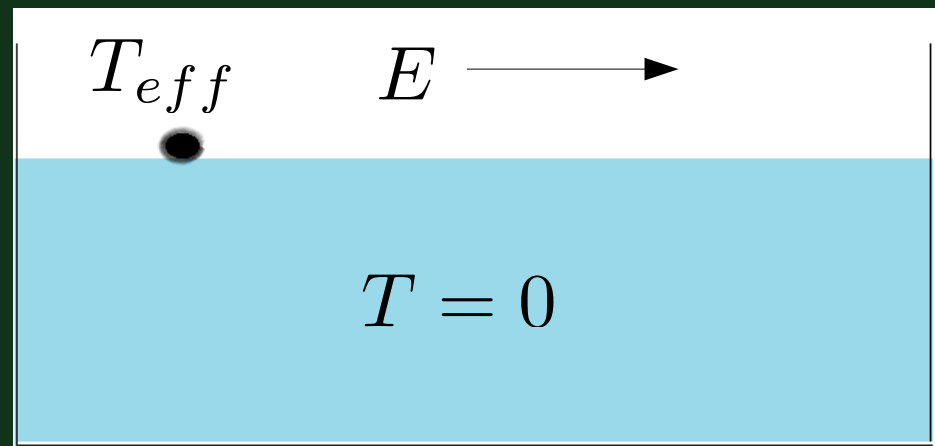


E



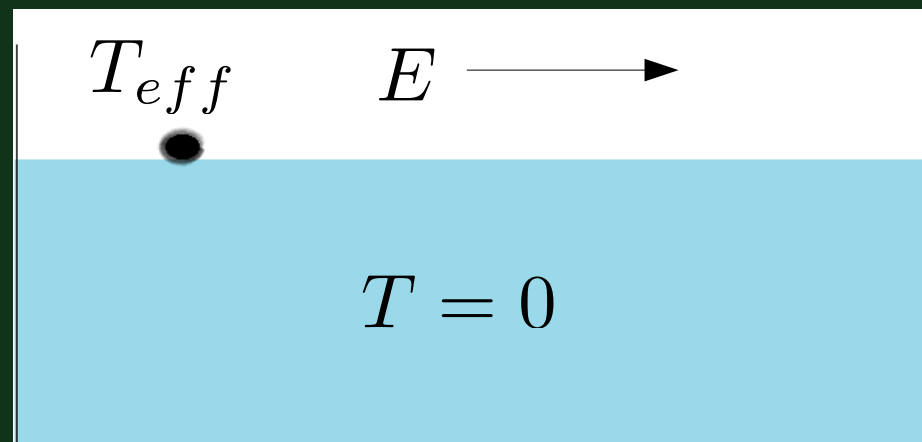
$T = 0$

$$A(r, t) = A_{cl}(r, t) + \delta A(r, t)$$

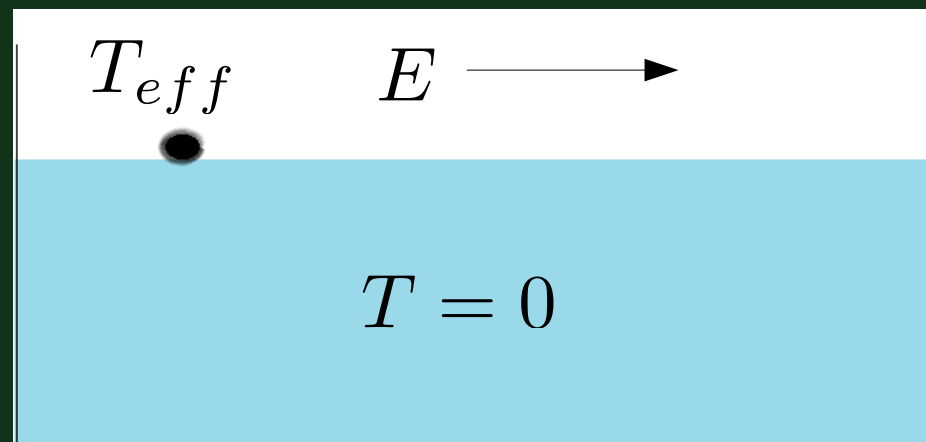


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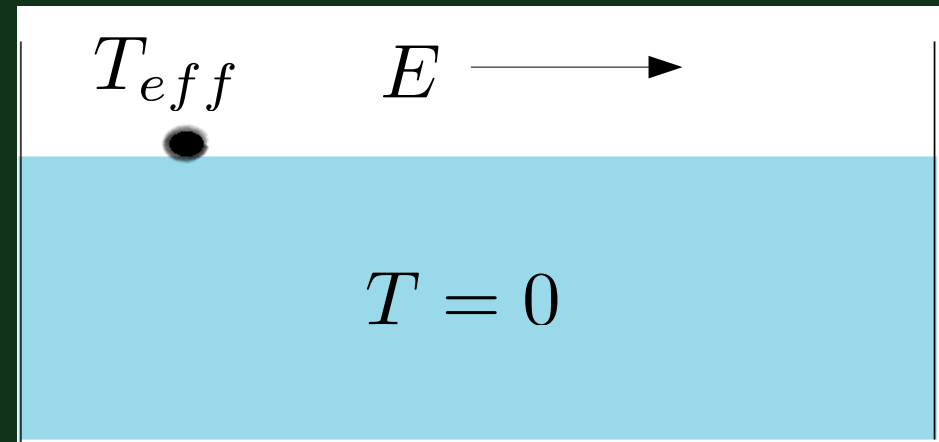


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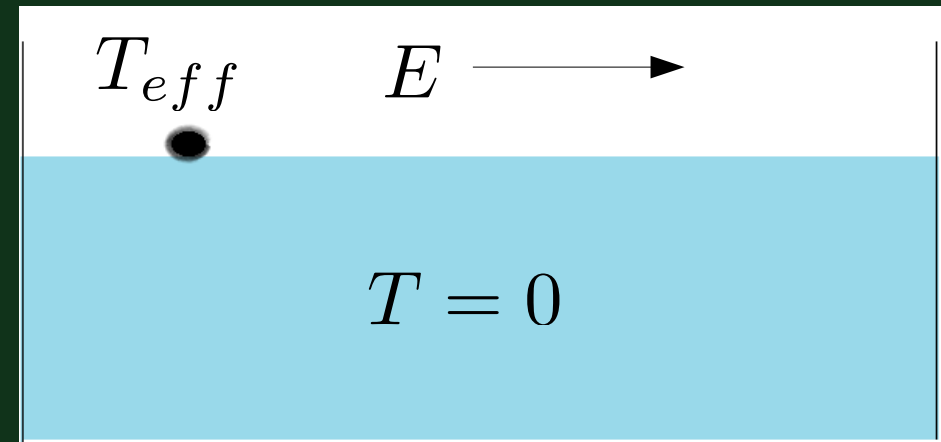
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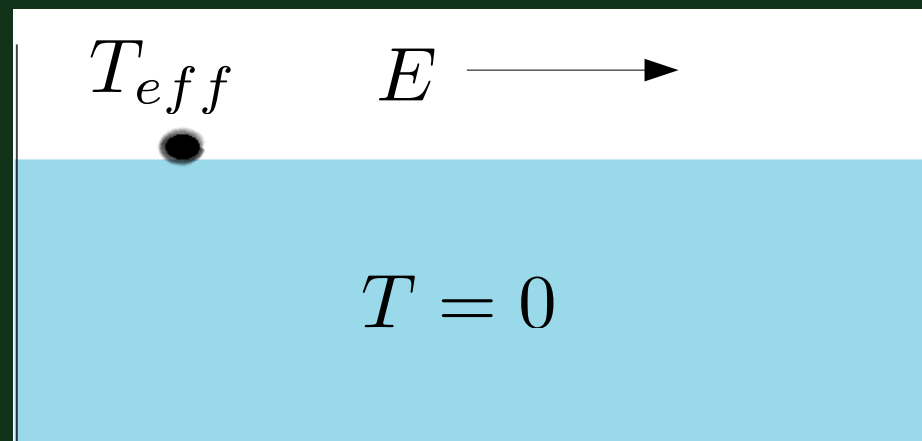


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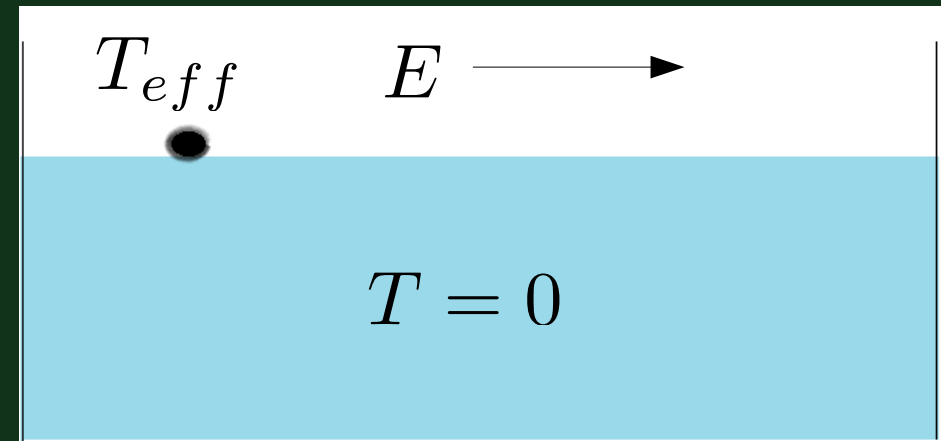
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In presence of non-extremal background

whereas $\lambda_{gravity} = 2\pi T$

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□ Einstein gravity not essential. Even if the gluon bath is at zero temperature, flavor fluctuations independently saturate the bound.

Fluctuations

Scrambling Time (t_{sc})

Gravity (gluons)

$$\beta \log(N_c^2)$$

Scalar (scalar mesons)

$$\beta \log(\sqrt{\lambda})$$

Vector (vector mesons)

$$\beta \log(N_c N_f \lambda^{\frac{p-3}{4}})$$

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4. Baryonic Fluctuations ?!
5. Effect conserved charges added to the system. So far it has turned out that, only spacetime symmetry charges lead to violation of the bound, internal symmetry charges do not.



Thank you!

