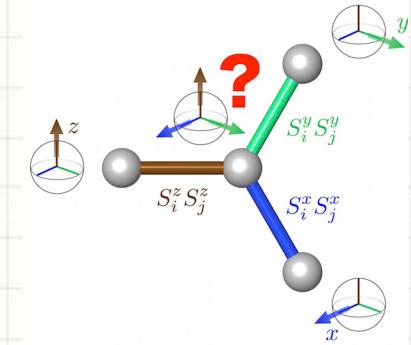
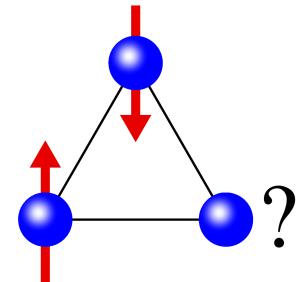


Realization of a Quantum Spin Liquid in a bilayer Kagome lattice $\text{Ca}_{10}\text{Cr}_7\text{O}_{28}$

Yogesh Singh
IISER Mohali



OUTLINE

- Spin Liquids : Geometrical Frustration, No LRO, Fractionalization, Spinons,....
- $\text{Ca}_{10}\text{Cr}_7\text{O}_{28}$, a new complex oxide
- Thermodynamic Measurements: Magnetism, Heat Capacity, AC chi
- Microscopic Measurements: μSR
- Magnetic Excitations: Inelastic neutron scattering
- The Hamiltonian
- FRG: SL ground state

Collaborators

C. Balz, A. T. M. N. Islam, Bella Lake
(Helmholtz Zentrum Berlin)

Crystal Growth, INS,
low temp. thermodynamics

Chris Baines and Hubertus Luetkens
(Paul Scherrer Institut, Switzerland)

μ SR

Elisa M. Wheeler
(ILL, Grenoble, France)

INS

J. A. Rodriguez-Rivera, T. Guidi, G. G. Simeoni
(NIST, ISIS, TU Muenchen)

INS

Rico Schoenemann, Thomas Herrmannsdoerfer
(Helmholtz-Zentrum Dresden)

AC Chi

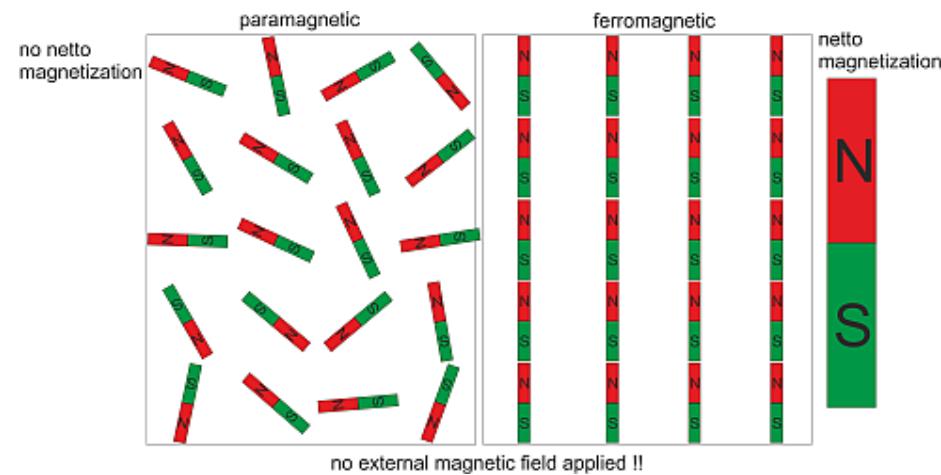
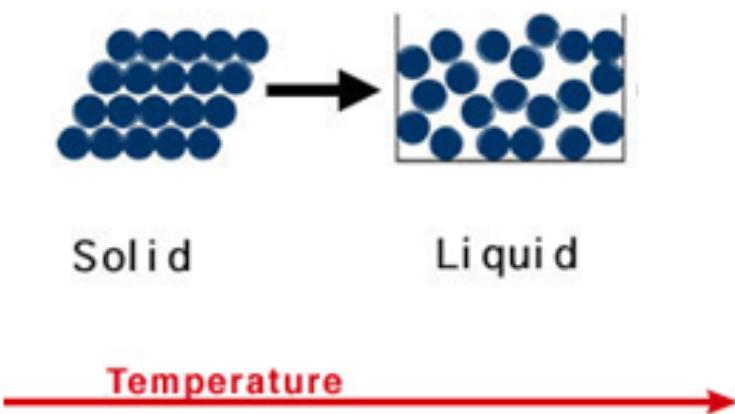
Hanjo Ryll
(Helmholtz Zentrum Berlin)

Low T heat capacity

J. Reuther
(Freie Universitaet Berlin, Germany)

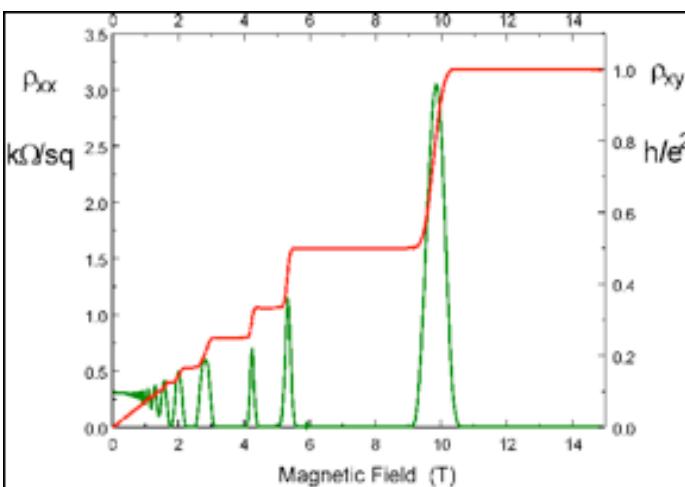
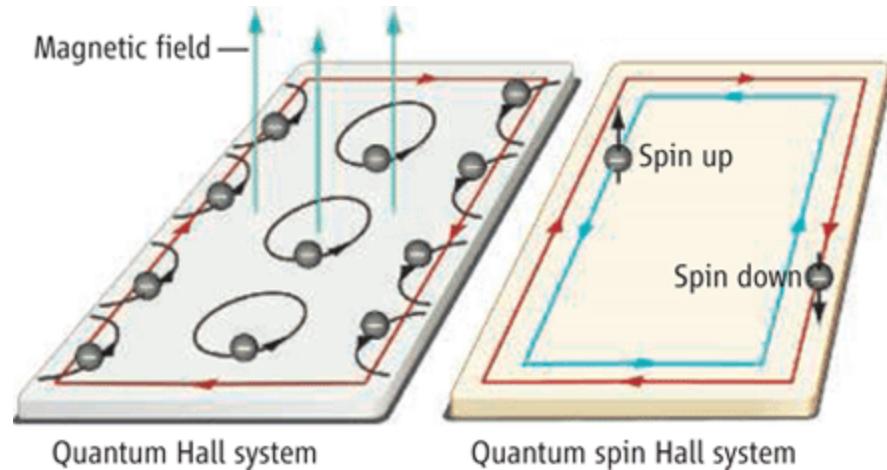
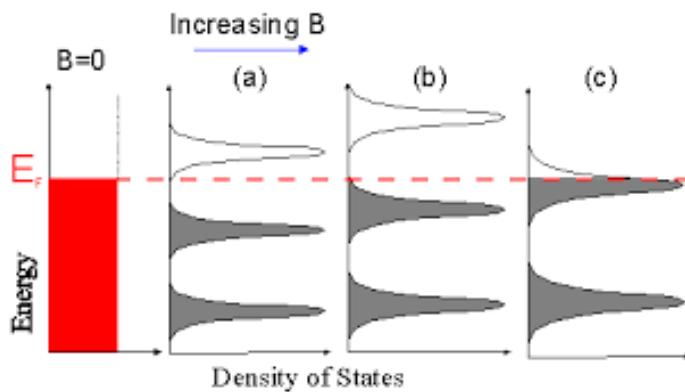
FRG calculations

Broken Symmetry -----> Phases/particles



Can one have phases with no broken symmetry or no order parameter ??

Topological States: Quantum Hall Effect



$$\sigma_{xy} = Ne^2/h.$$

σ has been measured to 1 part in 10^{19}

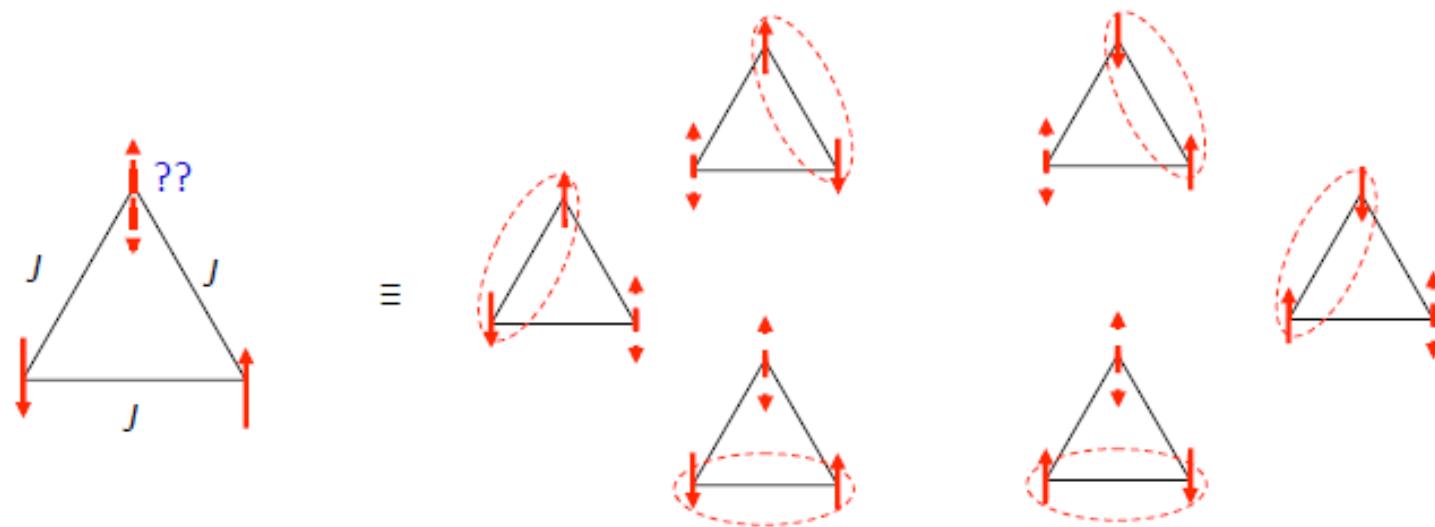
$$N = n_m = \frac{1}{2\pi} \int d^2k \mathcal{F}_m$$

Berry flux $F_m = \nabla \times \mathbf{A}_m$
 n_m = Chern #

This precision is a manifestation of the topological nature of σ_{xy}

Spin Liquids in Geometrically Frustrated Magnets

Huge degeneracy

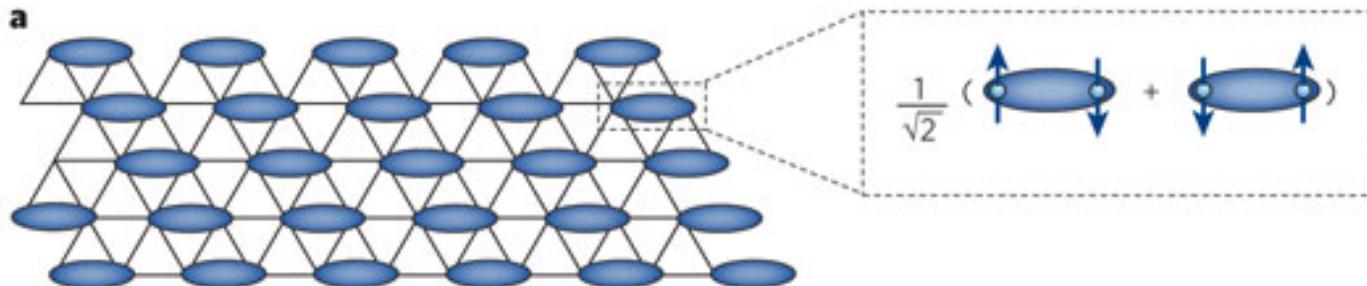


Spin-liquid: Quantum Disordered State of Strongly Interacting Spins
No “obvious” Order Parameter or Broken Symmetry

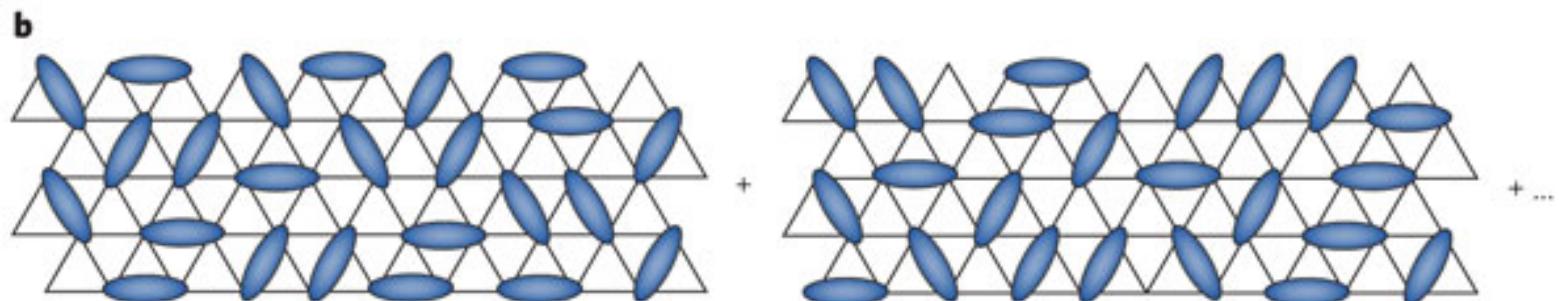
RVB state on a triangular lattice is a Z2 spin liquid

Anderson's Valence Bond States

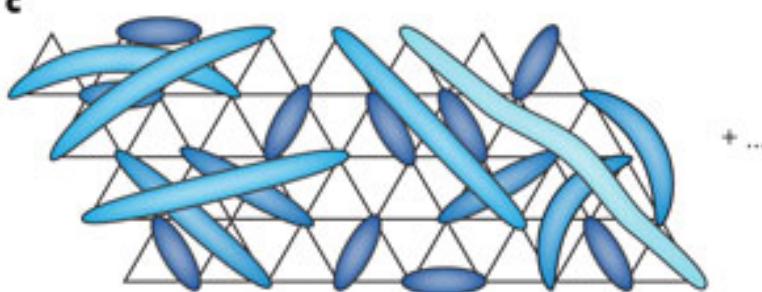
Valence
Bond Solid



Resonating
Valence
Bond : Short
Range



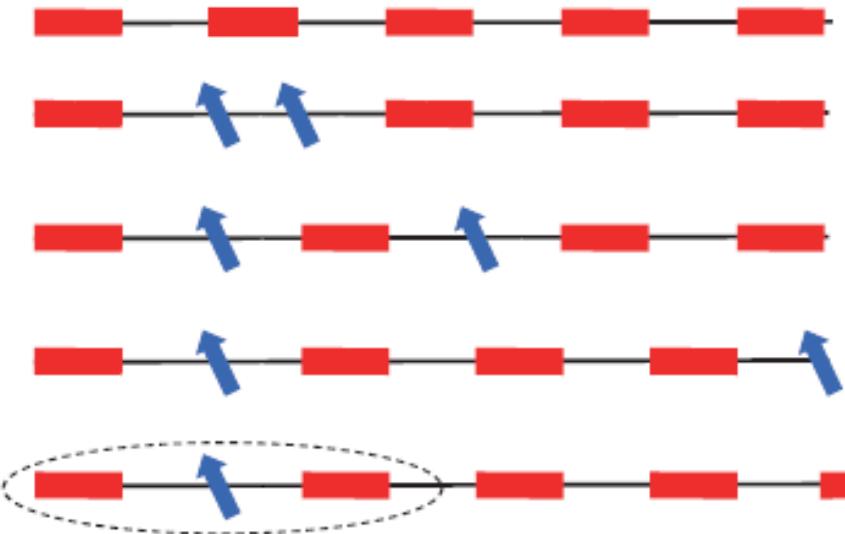
Resonating
Valence
Bond : Long
Range



L. Balents, "Spin liquids in frustrated magnets," Nature (2010).

Excitations in spin liquids: Fractional Particles

- Majumdar-Gosh chain (1D): $\mathcal{H} = J \sum_i \mathbf{S}_i \cdot \mathbf{S}_{i+1} + \frac{J}{2} \sum_i \mathbf{S}_i \cdot \mathbf{S}_{i+2}$ Federico Becca ('14)
- The exact ground state is known (two-fold degenerate), perfect dimerization



The “initial” $S = 1$ excitation can decay into **two** spatially separated spin-1/2 excitations (spinons)

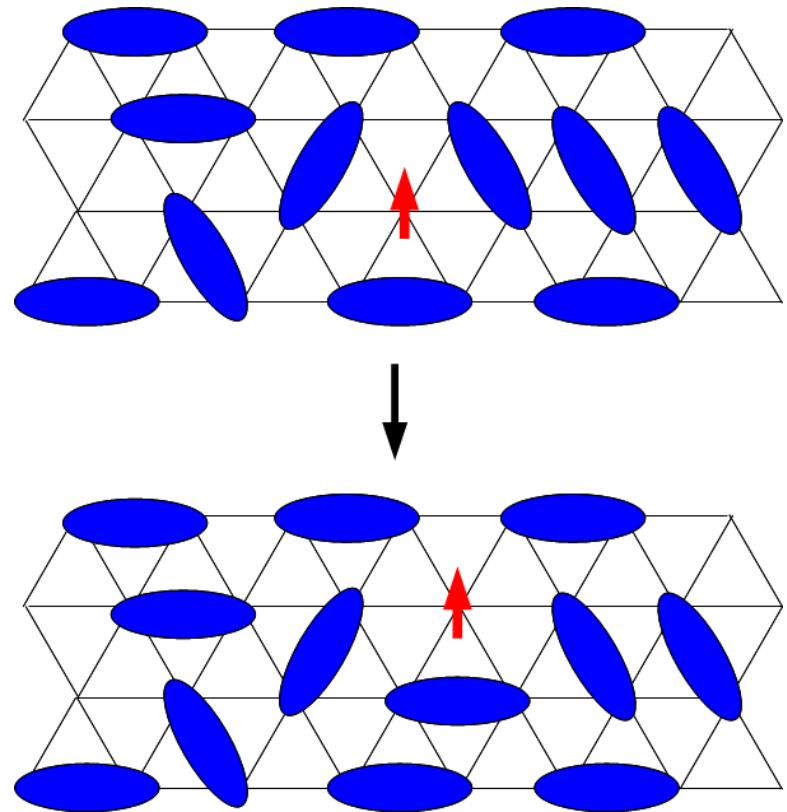
Finite-energy state with an **isolated** spinon (the other is far apart)
domain wall between two dimerization patterns

- A **spinon** is a neutral spin-1/2 excitation, “one-half” of a $S = 1$ spin flip.
(it has the same spin as the electron, but no charge)
- Spinons can only be created by **pairs** in finite systems
In one dimension, they can propagate at large distances, as **two elementary particles**

Excitations in spin liquids: Fractional Particles

In 2D a spinon is any unpaired spin which can move around the lattice “delocalize” with little or no energy cost

Experimental Signatures
 ρ = insulating
 C/T = metallic
 χ = metallic
 κ/T = metallic



Recipe for Quantum Fluctuations

- Small Spin : $S = \frac{1}{2}$
- Low Dimensionality or co-ordination
- Geometric Frustration: mostly AF on triangular motifs

Most Spin Liquid Candidates are $S = \frac{1}{2}$ Quasi-Low Dimensional Magnets with AF exchange

Some Examples

Table 1 | Some experimental materials studied in the search for QSLs

Material	Lattice	S	θ_{CW} (K)	R*	Status or explanation
κ -(BEDT-TTF) ₂ Cu ₂ (CN) ₃	Triangular†	$\frac{1}{2}$	-375‡	1.8	Possible QSL
EtMe ₃ Sb[Pd(dmit) ₂] ₂	Triangular†	$\frac{1}{2}$	-(375-325)‡	?	Possible QSL
Cu ₃ V ₂ O ₇ (OH) ₂ •2H ₂ O (volborthite)	Kagomé†	$\frac{1}{2}$	-115	6	Magnetic
ZnCu ₃ (OH) ₆ Cl ₂ (herbertsmithite)	Kagomé	$\frac{1}{2}$	-241	?	Possible QSL
BaCu ₃ V ₂ O ₈ (OH) ₂ (vesignieite)	Kagomé†	$\frac{1}{2}$	-77	4	Possible QSL
Na ₄ Ir ₃ O ₈	Hyperkagomé	$\frac{1}{2}$	-650	70	Possible QSL
Cs ₂ CuCl ₄	Triangular†	$\frac{1}{2}$	-4	0	Dimensional reduction
FeSc ₂ S ₄	Diamond	2	-45	230	Quantum criticality

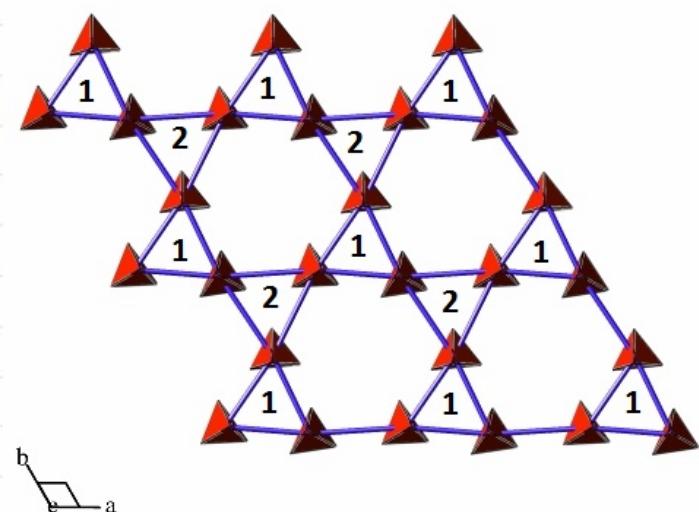
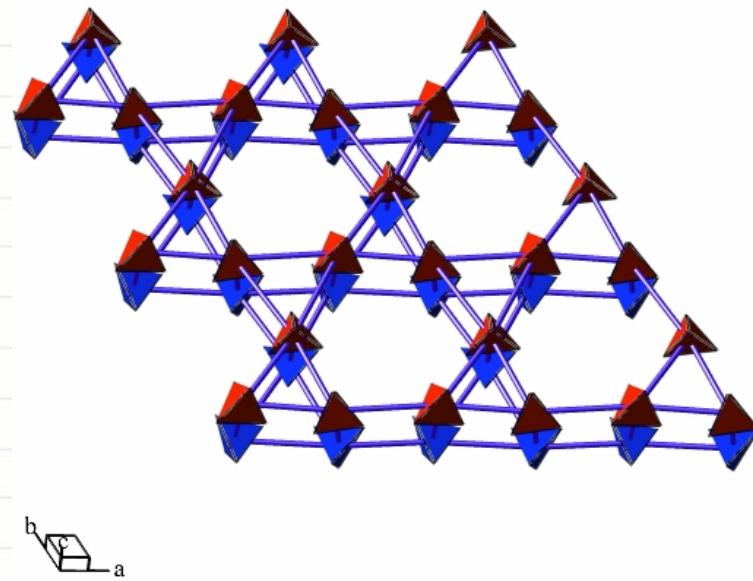
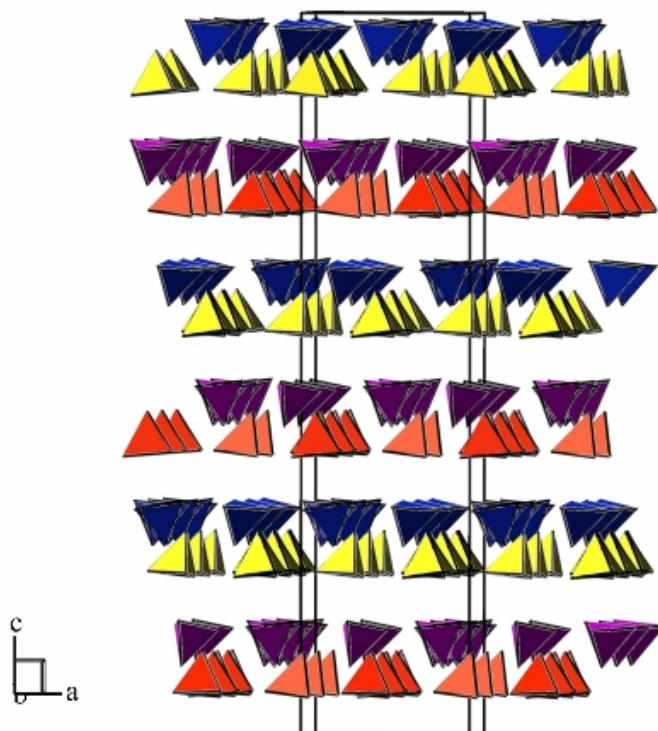
L. Balents, “Spin liquids in frustrated magnets,” Nature (2010).

New Quantum Magnet $\text{Ca}_{10}\text{Cr}_7\text{O}_{28}$

Crystal Structure of $\text{Ca}_{10}\text{Cr}_7\text{O}_{28}$

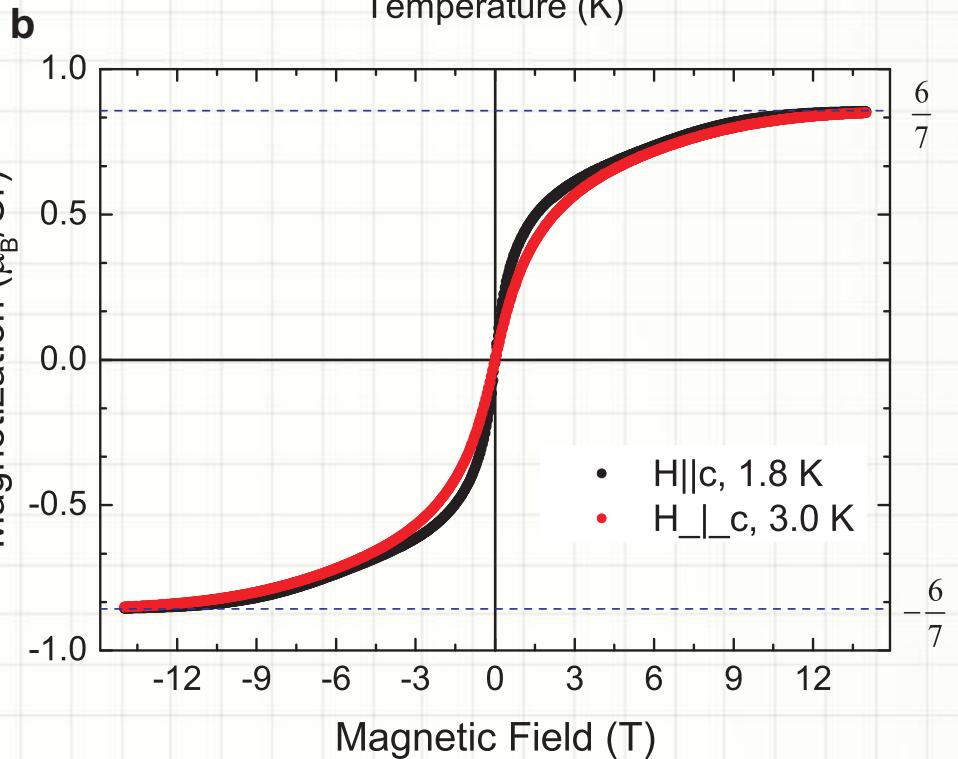
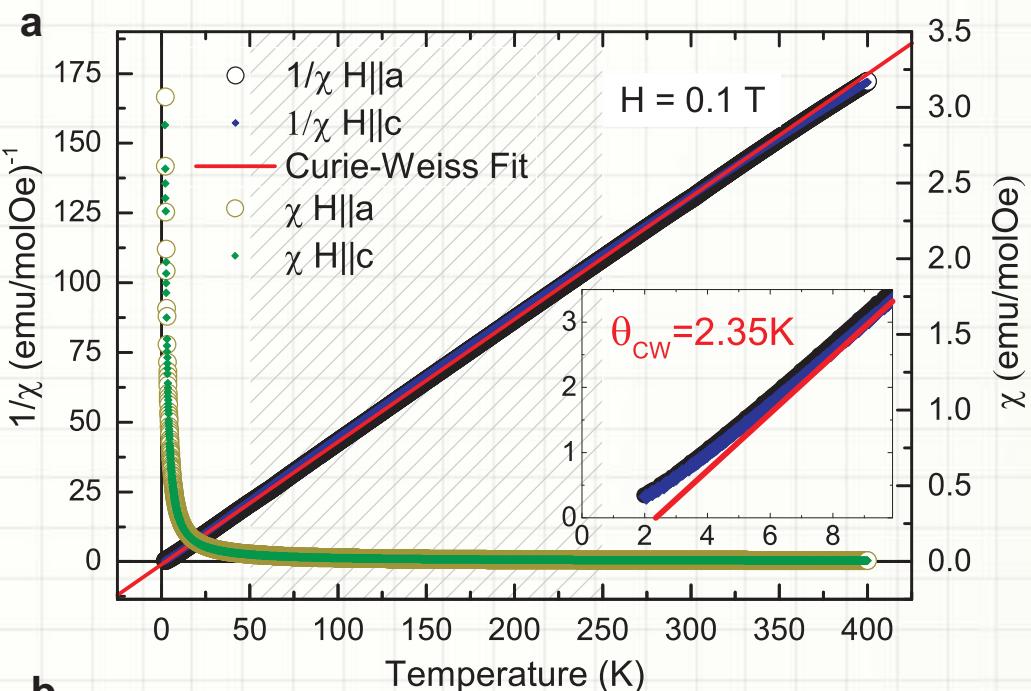
Lattice Parameters Space Group

$a = 10.76892(3) \text{ \AA}$ $R3c$
 $c = 38.09646(12) \text{ \AA}$

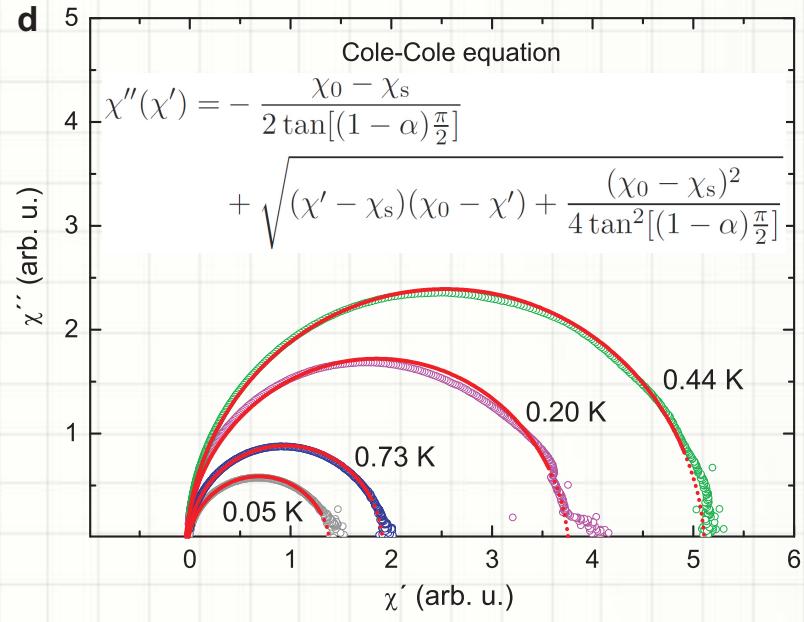
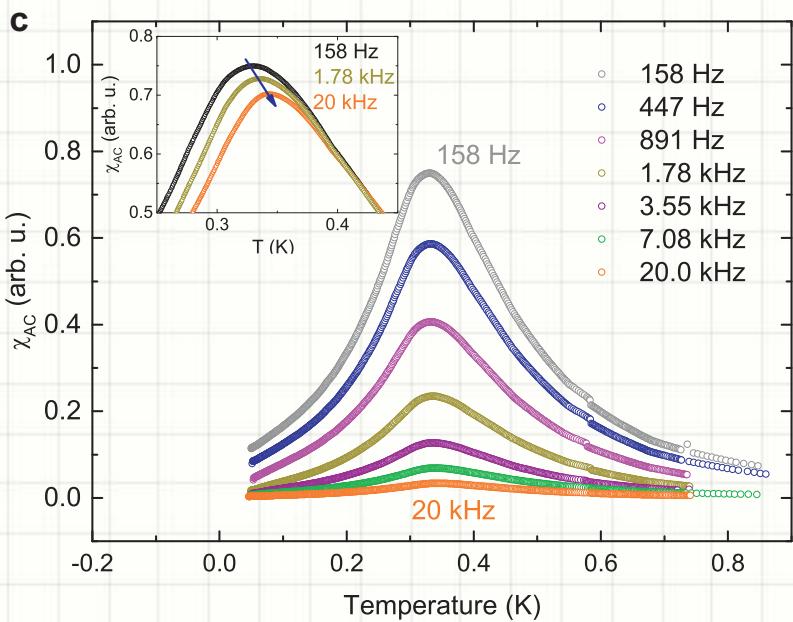
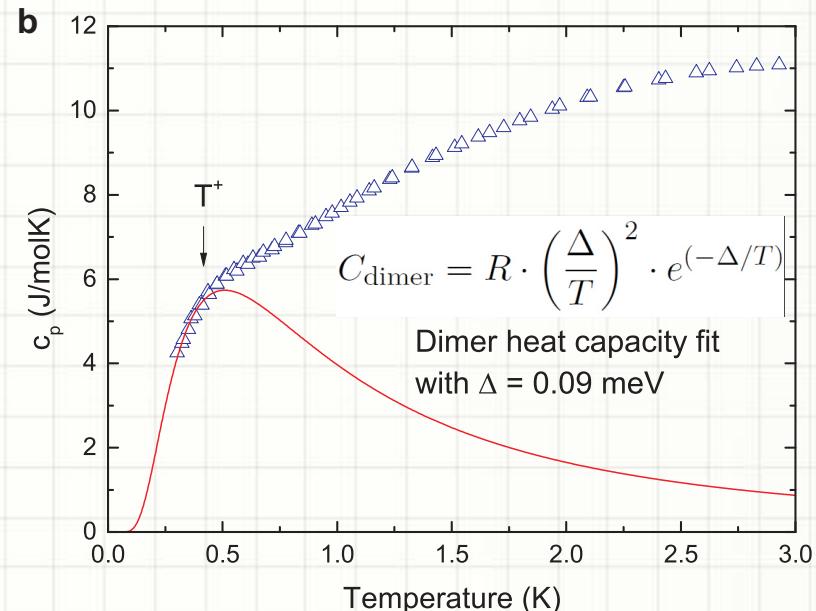
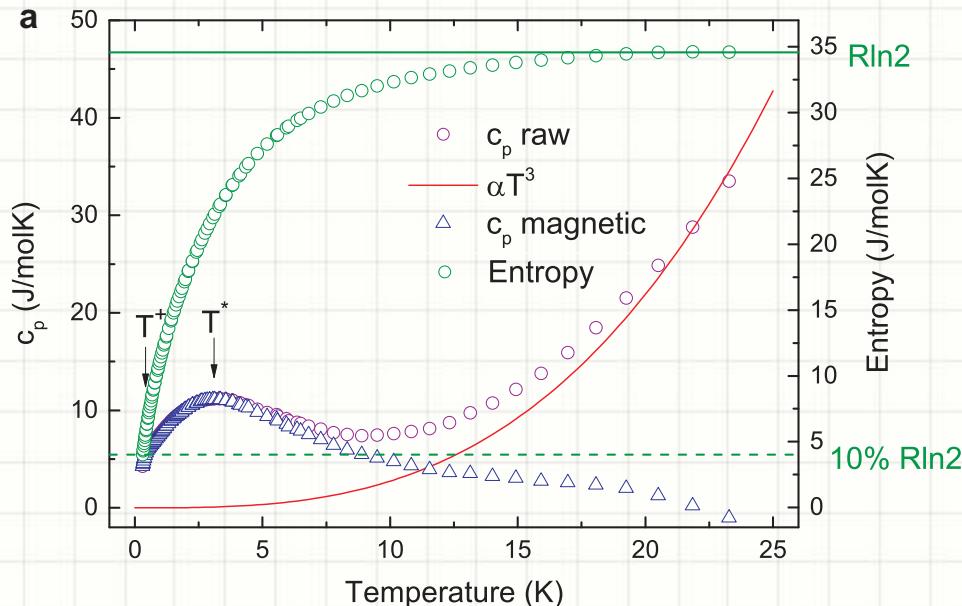


Magnetic Susceptibility + Magnetization

- Local Moment behavior down to 1.8 K with $\mu_{\text{eff}} = 1.49 \mu_B = 6/7 \times 1.74(2) \mu_B$
- $\theta = 2.35$ K. No LRO.
- No anisotropy between $\chi_{||}$ and χ_{perp}
- Deviations below ~ 5 K of χ from CW fit suggest AF
- Magnetization saturates at 12 T ($= 17$ K) to $6/7 \mu_B = 6$ Cr⁵⁺ ($S = \frac{1}{2}$) and 1 Cr⁶⁺ (non-magnetic)



No LRO : Heat Capacity and AC chi



Other Examples of Cole-Cole plot analysis

How 'spin ice' freezes
NATURE 413 , (2001)

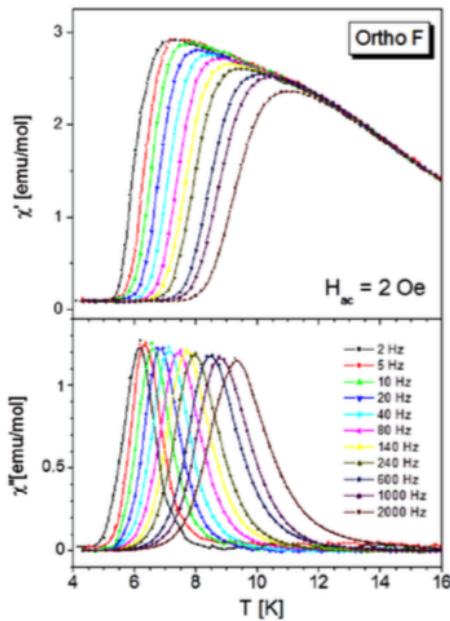
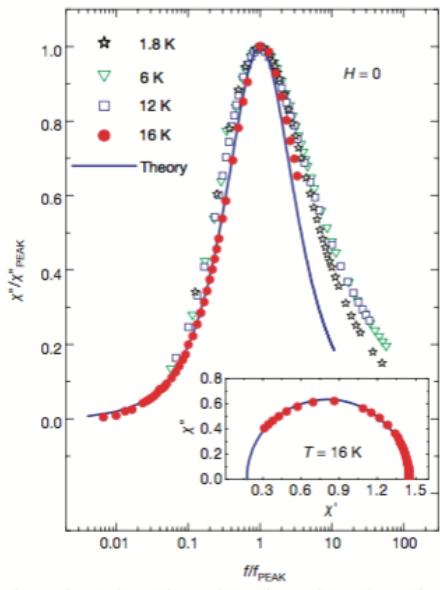
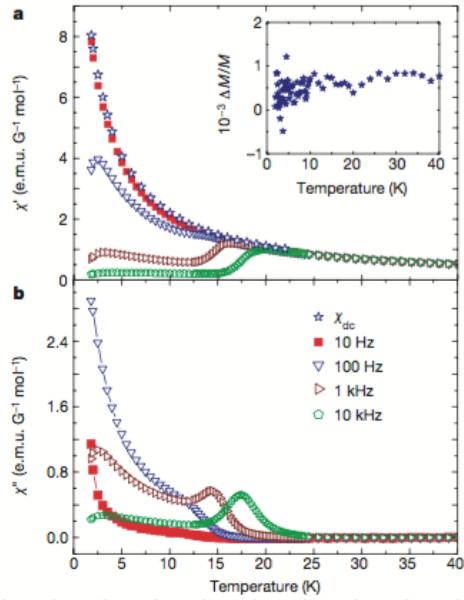


Fig. 12. Frequency dependent AC susceptibility of the $[\text{MnF}_4\text{TPP}][\text{TCNE}]$ single chain magnet; fluorine is substituted to porphyrin in the *ortho* position.

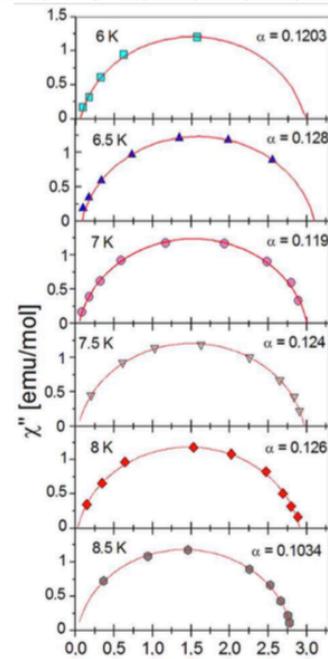


Fig. 13. Argand plots at several temperatures for the $[\text{MnF}_4\text{TPP}][\text{TCNE}]$ SCM obtained from the data shown in Fig. 12.

PHYSICAL REVIEW B 91, 054423 (2015)

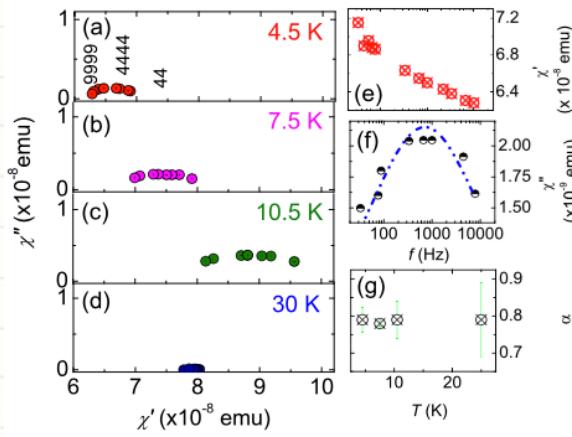
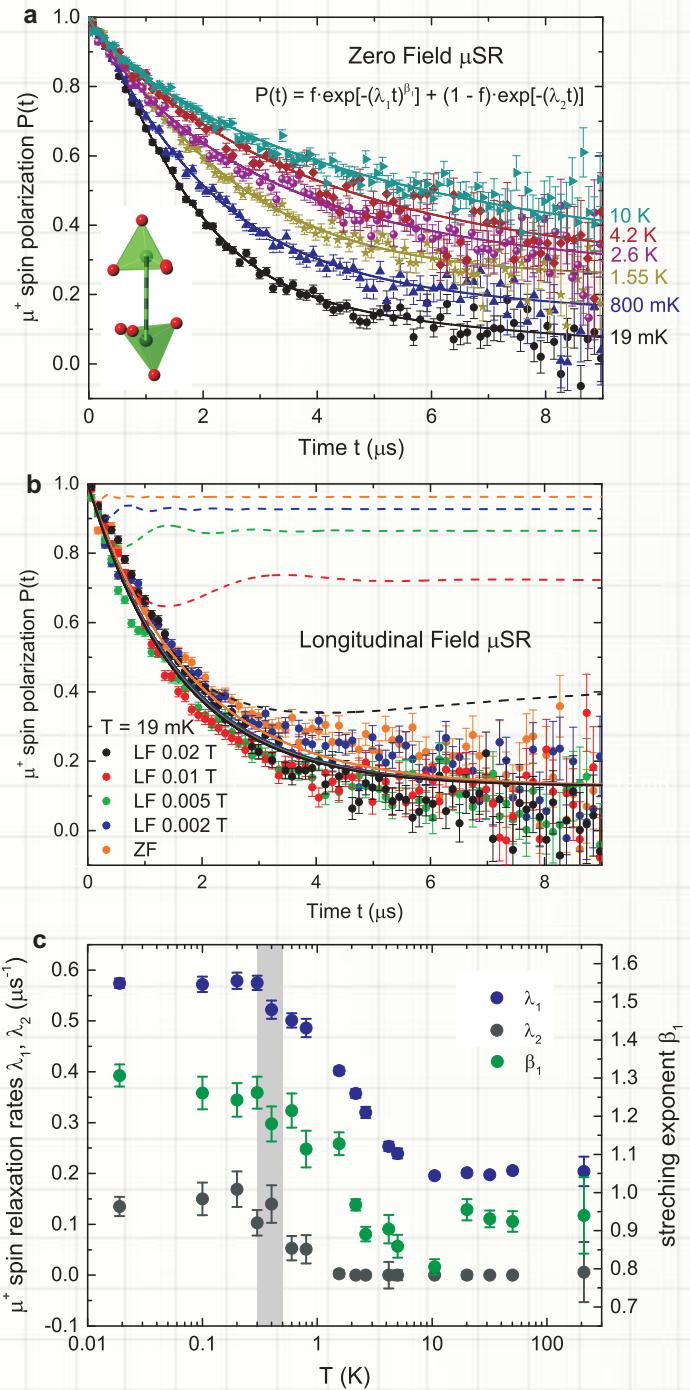


FIG. 4. (Color online) (a)-(d) The Cole-Cole plot ($\chi''-\chi'$) at different temperatures below 30 K supports the claim of a broad distribution of relaxation times in FeAl_2O_4 . The numbers in (a) indicate the peak frequency in Hz. The numbers in (b)-(d) indicate the peak frequency in Hz.

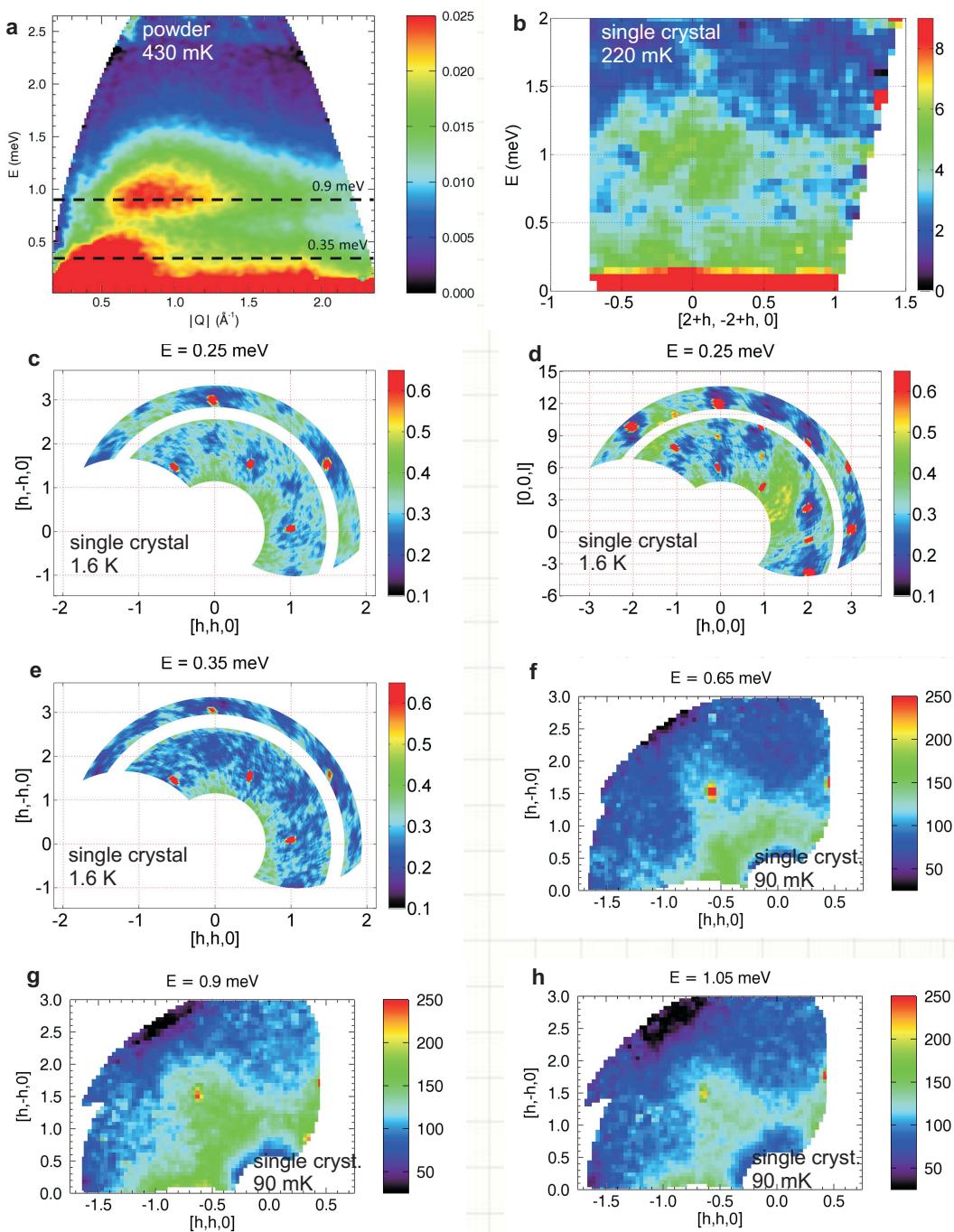
No LRO : μ SR

- No oscillations in $P(t)$ in ZF μ SR down to 19 mK = no static fields
- SG would also have no oscillations!!
- LF μ SR confirms absence of freezing
- Relaxation rates start to increase below about 3K and become constant below 0.3 – 0.5 K
- Persistent slow dynamics below 0.3 K



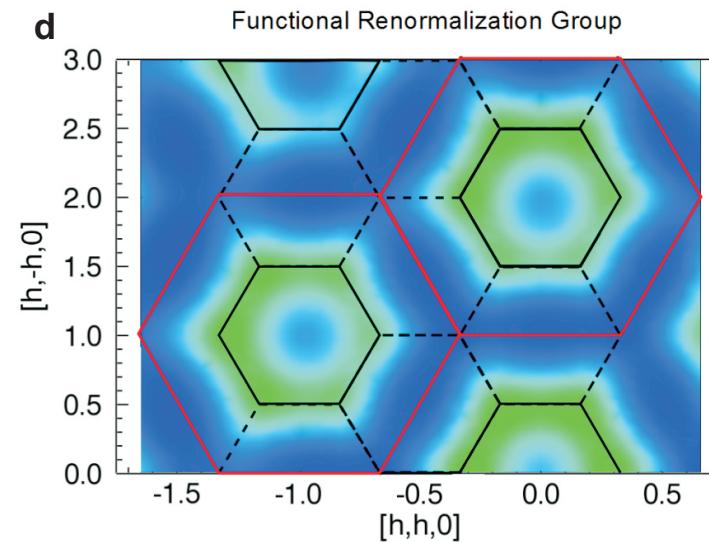
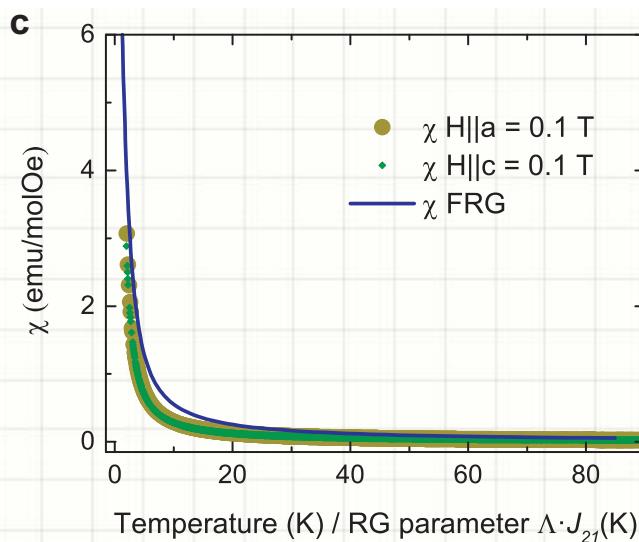
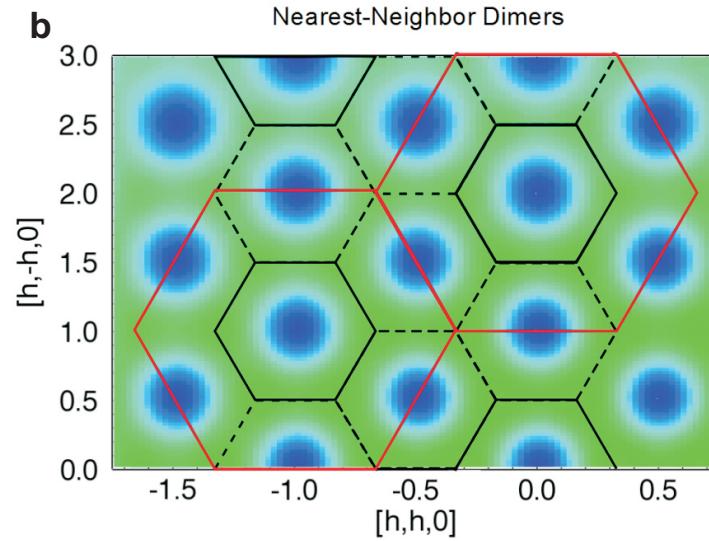
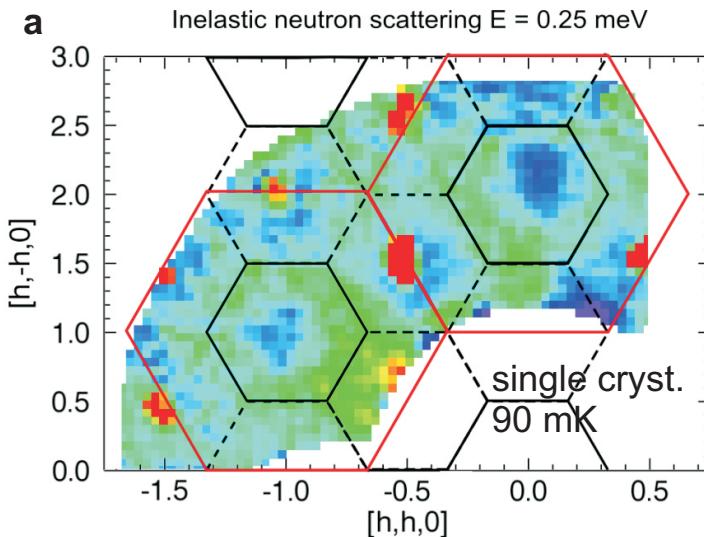
Inelastic Neutron Scattering

- Diffuse magnetic excitations
- excitations appear gapless
- two distinct bands with energy ranges 0.0-0.6 meV and 0.7-1.5 meV
- No magnetic scattering above 1.6 meV \sim 18 K
- Ring-like features in lower band (c & e)
- Block-like features in higher band (f-h)
- Fig.d: spectrum perp. to the kagome bilayers at 0.25 meV, no dispersion along the $[(0,0,l)]$ = 2D-magnetism

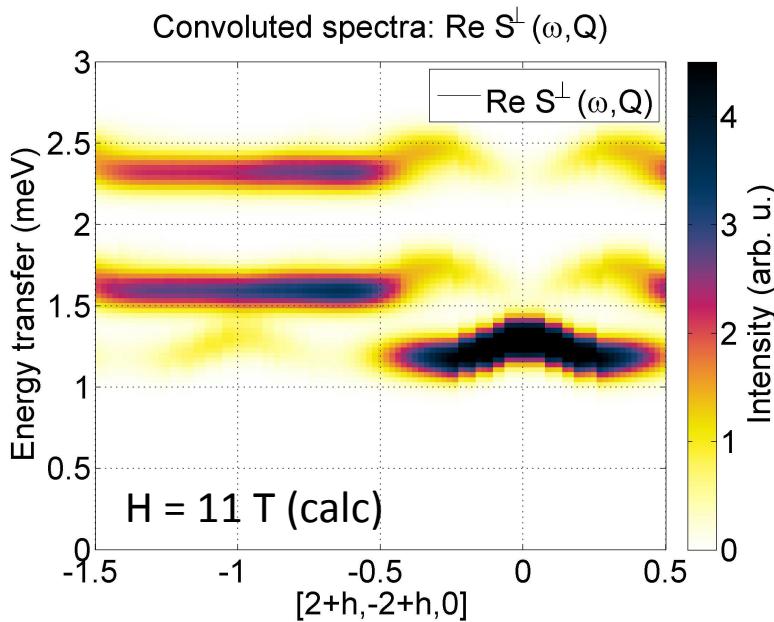
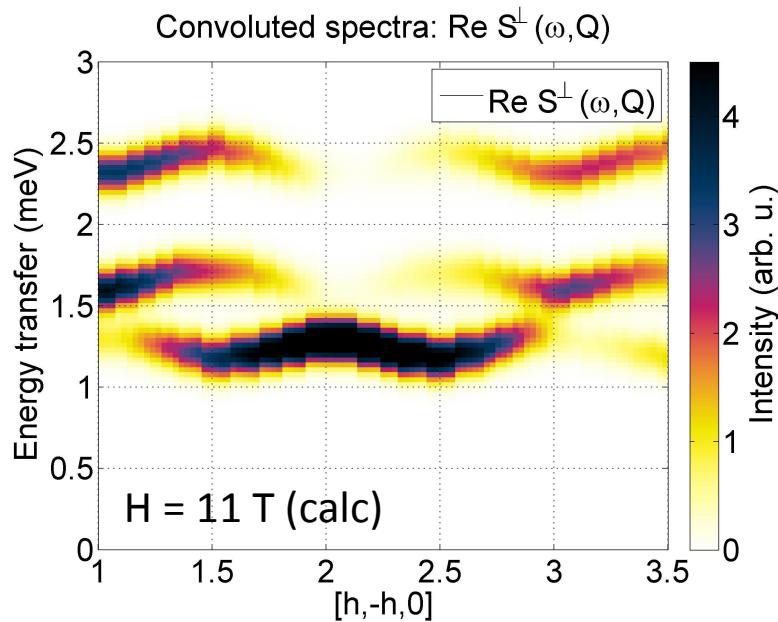
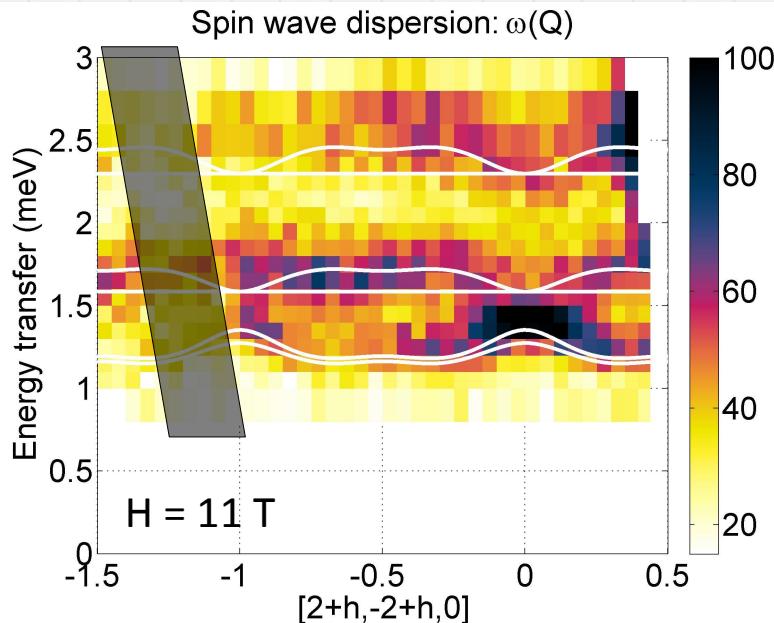
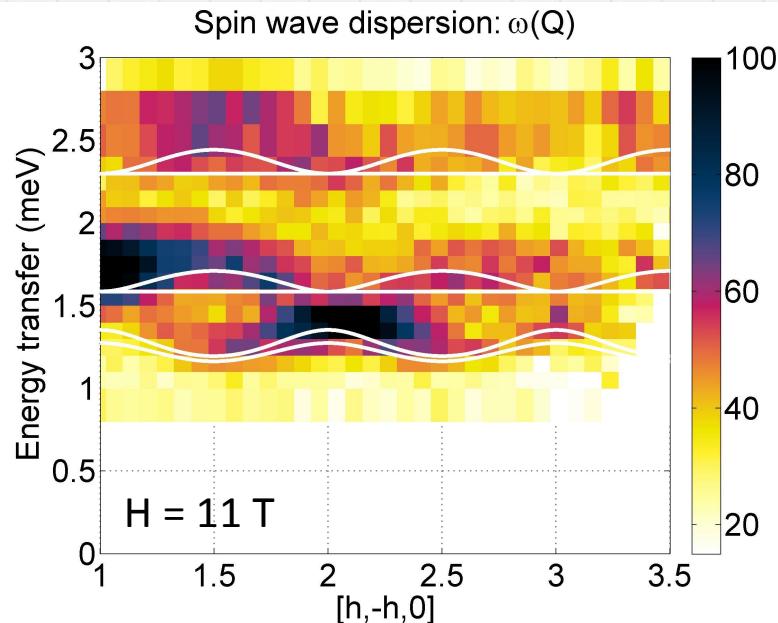


Broad, diffuse excitations
consistent with spinons

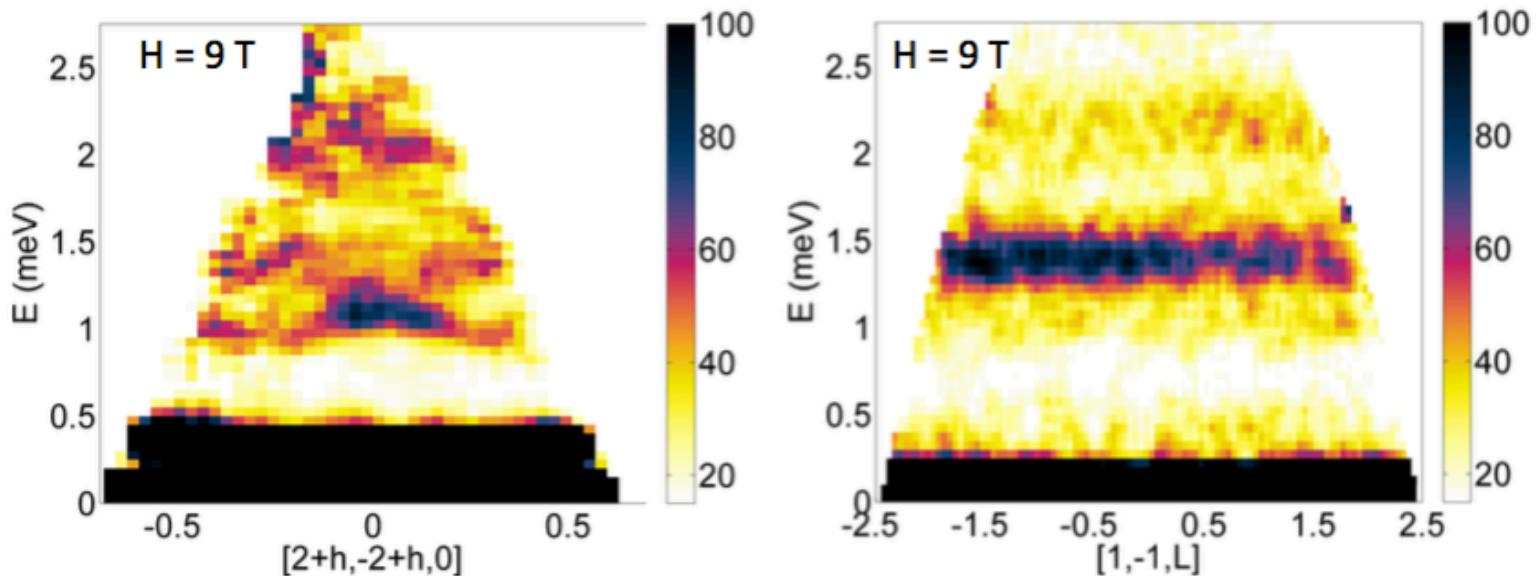
Inelastic Neutron Scattering at H =0



Spin Waves: INS at $H = 11\text{T}$, $T = 90\text{ mK}$

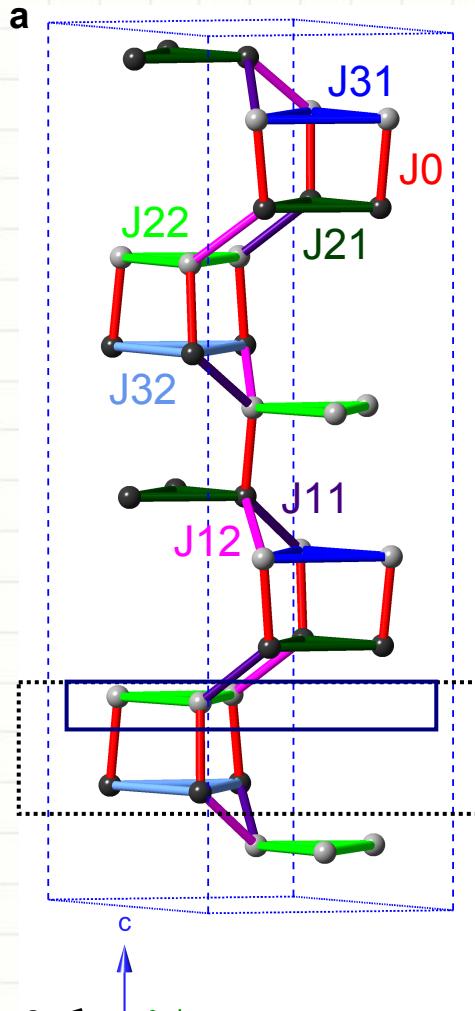


Spin Waves: INS at $H = 9\text{ T}$, $T = 2\text{ K}$



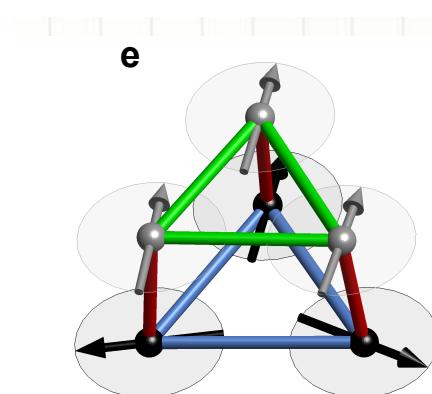
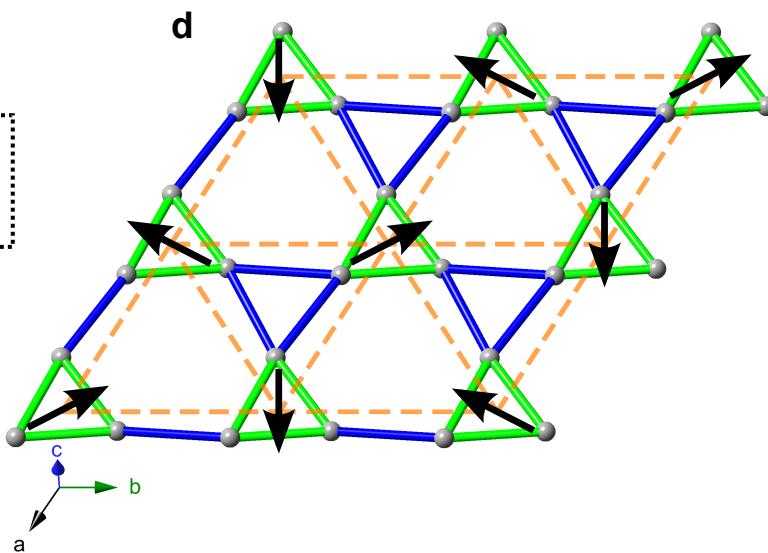
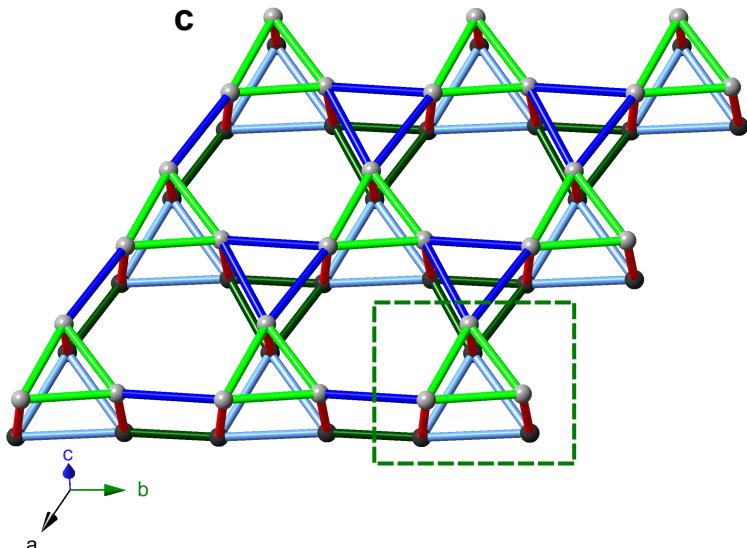
- Sharp spin-wave dispersion within Kagome bilayers
- Absence of dispersion along $(0,0,L)$ direction (perpendicular to Kagome bilayers) indicates 2D magnetic interactions

Magnetic Interactions : Novel Frustration Mechanism



b

exchange	coupling [meV]	type
J_0	-0.08(4)	FM
J_{11}	0	
J_{12}	0	
J_{21}	-0.76(5)	FM
J_{22}	-0.27(3)	FM
J_{31}	0.09(2)	AFM
J_{32}	0.11(3)	AFM
ΣJ	-0.91(17)	



Summary

- A new QSL candidate discovered in the complex oxide $\text{Ca}_{10}\text{Cr}_7\text{O}_{28}$ with a bilayer Kagome lattice of $S = \frac{1}{2}$ Cr^{5+} moments
- No LRO or freezing down to 19 mK
- Gapless, dispersionless, diffuse magnetic excitations: spinons
- Unusual combination of magnetic interactions with dominant FM interactions leads to frustration
- PFFRG for the extracted Hamiltonian confirms absence of LRO

C. Balz, et al. arxiv:1606.06463,
Nature Physics (2016)

Herbertsmithite

