



# Boosted 1D superconductors

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Current frontiers in condensed matter ICTS

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[arxiv:1603.09478](https://arxiv.org/abs/1603.09478)

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Landau critical velocity

$$v_c = \text{Min.} \left( v_s, \left( \left[ \sqrt{\Delta^2 + \mu^2} - \mu \right] / m \right)^{1/2} \right)$$

Sound velocity  
of bosonic collective  
mode

Fermionic (single-particle)  
excitations

Baym and Pethick, Phys. Rev. A 86 023602 (2012)

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What does a boost do to this kind of superconductor?

# What is known?

## Mean-field

Boost destroys superconductivity via  
Clogston-Chandrasekhar type mechanism.  
Critical velocity  $<$  Landau critical velocity

T.-C. Wei and P. M. Goldbart, *Phys. Rev. B* 80, 134507 (2009).

## Fluctuations

Interaction with walls can induce phase slips “dynamically”  
destroying superconductivity, finite  $\omega$  and  $T$

T. Eggel, M. A. Cazalilla and M. Oshikawa, *Phys. Rev. Lett.* 107,  
275302 (2011).



# Our calculations and results

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Bosonization treatment taking into account quantum  
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Superconductivity can be strengthened upon applying a boost

A boost can open or close gaps depending on whether the system has spinless or spin  $1/2$  fermions

# Bosonization

Low energy theory for interacting 1D spinless Fermi system

$$\mathcal{H} = \frac{v}{2} \int dx \left[ K \Pi(x)^2 + \frac{1}{K} (\nabla \phi(x))^2 \right]$$

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$K$  - Luttinger parameter

$$\langle O_{SU}(x) O_{SU}(x') \rangle \sim 1/|x - x'|^{1/K}$$

$$\langle O_{CDW}(x) O_{CDW}(x') \rangle \sim 1/|x - x'|^K$$

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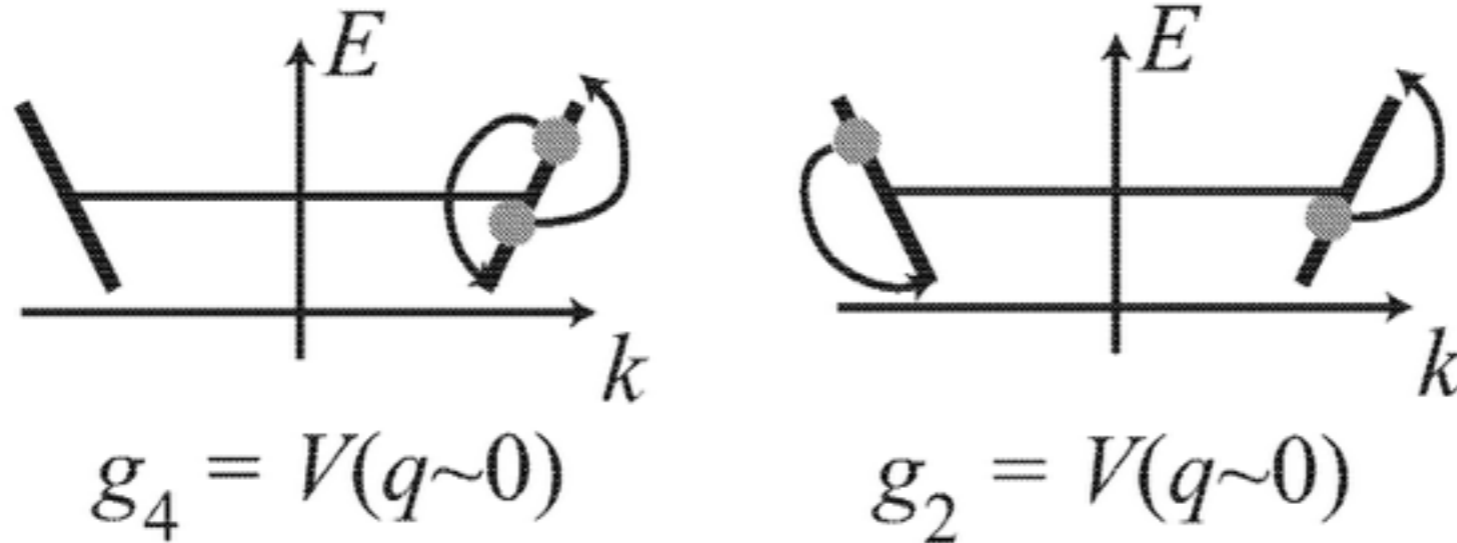
$$\langle O_{CDW}(x) O_{CDW}(x') \rangle \sim 1/|x - x'|^K$$

$K > 1$  attractive interactions (dominant SU order)

$K < 1$  repulsive interactions (dominant CDW order)



# Bosonization



$$v = \sqrt{\left(v_F + \frac{g_4}{2\pi}\right)^2 - \left(\frac{g_2}{2\pi}\right)^2}$$

$$K = \sqrt{\frac{v_F - \left(\frac{g_2}{2\pi} - \frac{g_4}{2\pi}\right)}{v_F + \left(\frac{g_2}{2\pi} + \frac{g_4}{2\pi}\right)}}$$

Ref: Quantum physics in one dimension, Giamarchi

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Different Fermi speeds for left and right movers

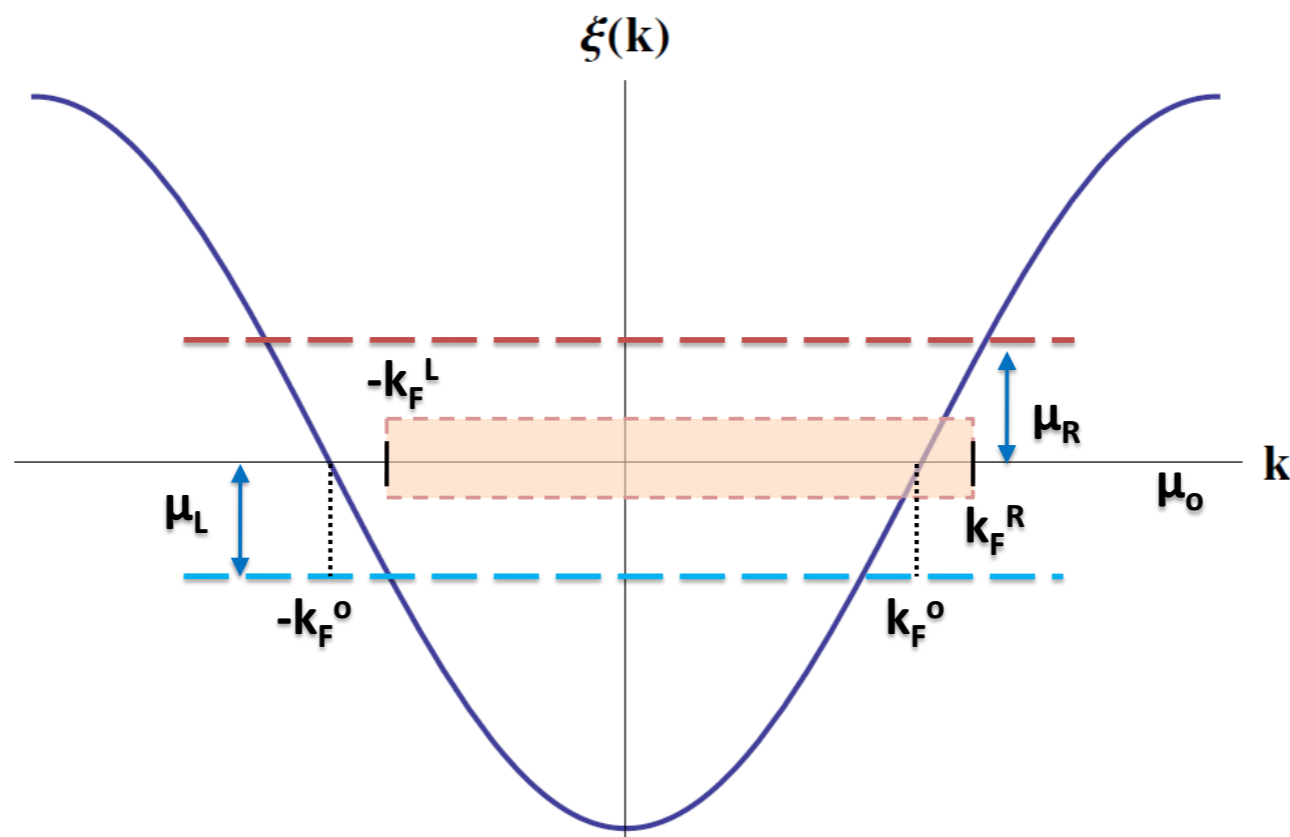
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$g$ 's unchanged by boost because they only depend on momentum differences

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Galilean transformation with speed  $w(u)$

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$$\langle O_{\text{CDW}}(x, t) O_{\text{CDW}}(x', t') \rangle \sim \cos [2k_F(x-x')] \left( \frac{1}{\sqrt{[x-x'+w(u)(t-t')]^2 + [v^F(u)]^2(t-t')^2}} \right)^{K(u)}$$

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Conformal invariance restored in terms of  $\tilde{\phi}$

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Boost has no effect when the dispersion is parabolic

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The same effect for spin 1/2 fermions

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Superconducting pairing susceptibility

$$\chi_{\text{pair}} = \lim_{\omega \rightarrow 0} \frac{1}{\Omega} \sum_k \frac{f(\xi_k) - f(-\xi_{-k})}{\omega - \xi(k) - \xi(-k) + i\delta}$$

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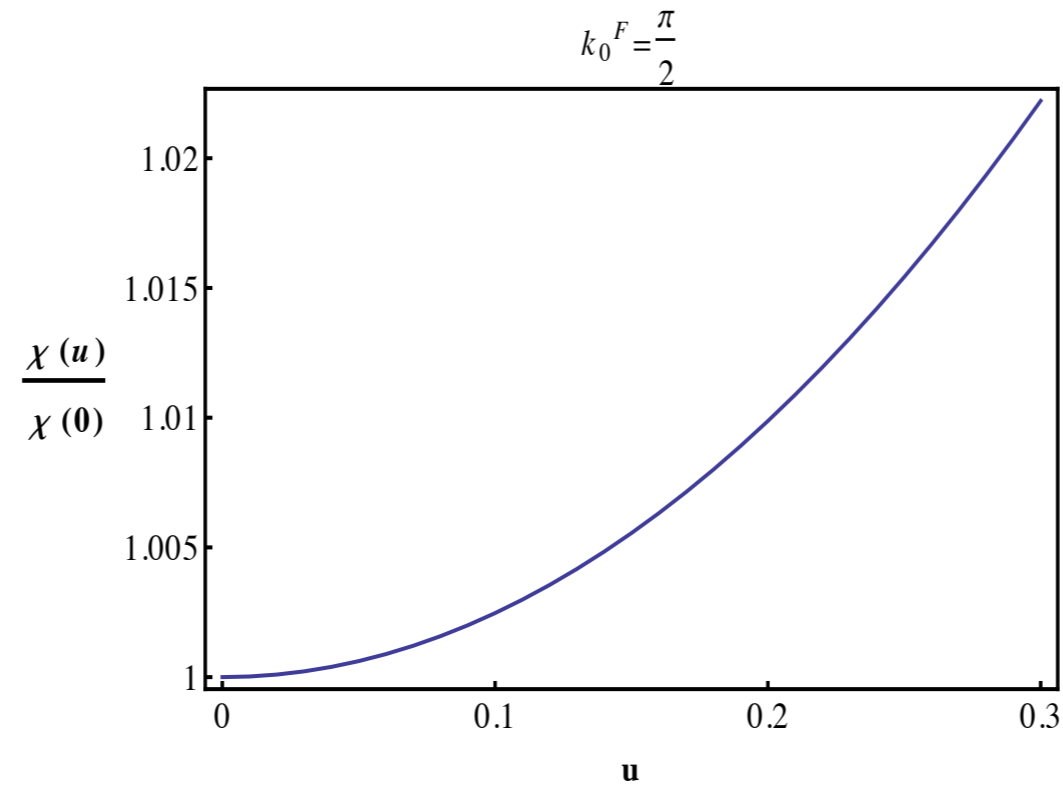
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Sine-Gordon Hamiltonian



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$$\mathcal{H} = \frac{v_\nu}{2} \int dx \left[ K_\nu \Pi_\nu^2 + \frac{1}{K_\nu} (\nabla \phi_\nu)^2 + \frac{2g_\nu}{2\pi a^2} \cos(\alpha_\nu \phi_\nu) \right]$$

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Renormalization group flows can be calculated for  $K$  and  $g$

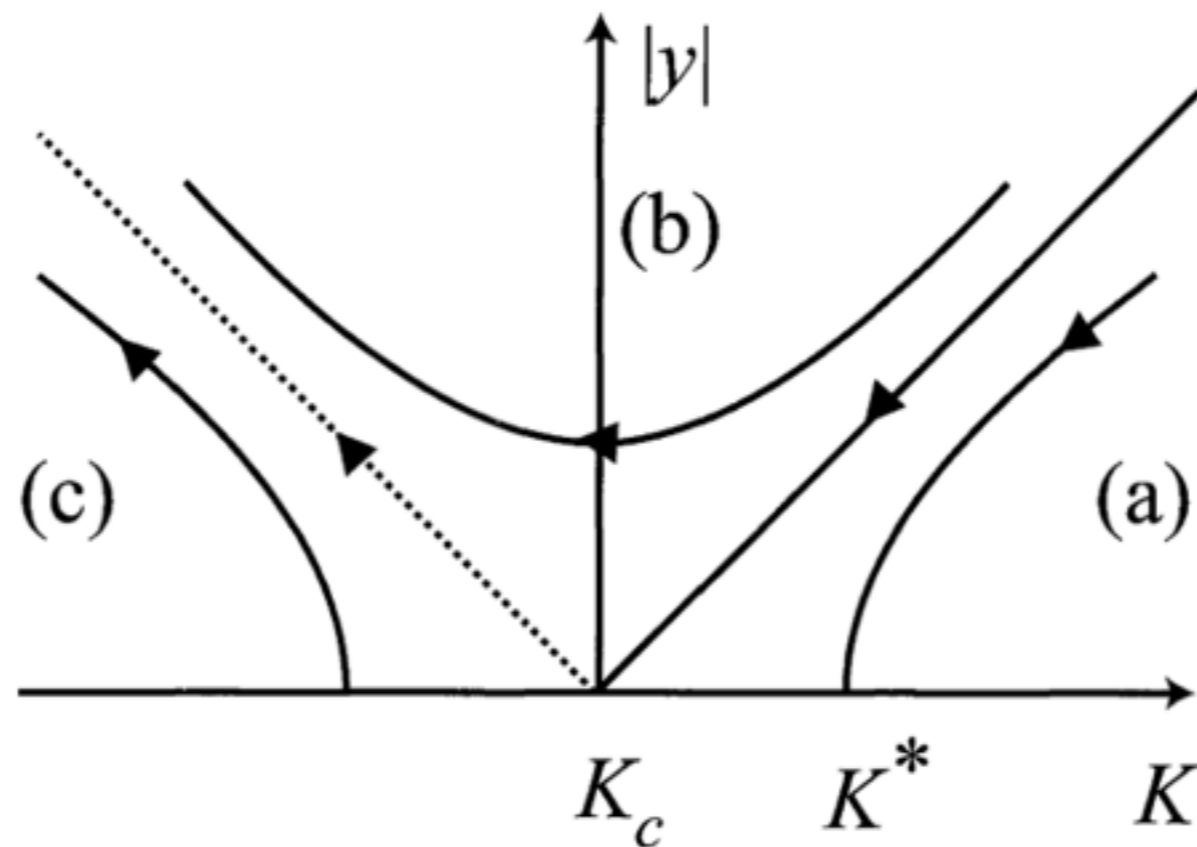
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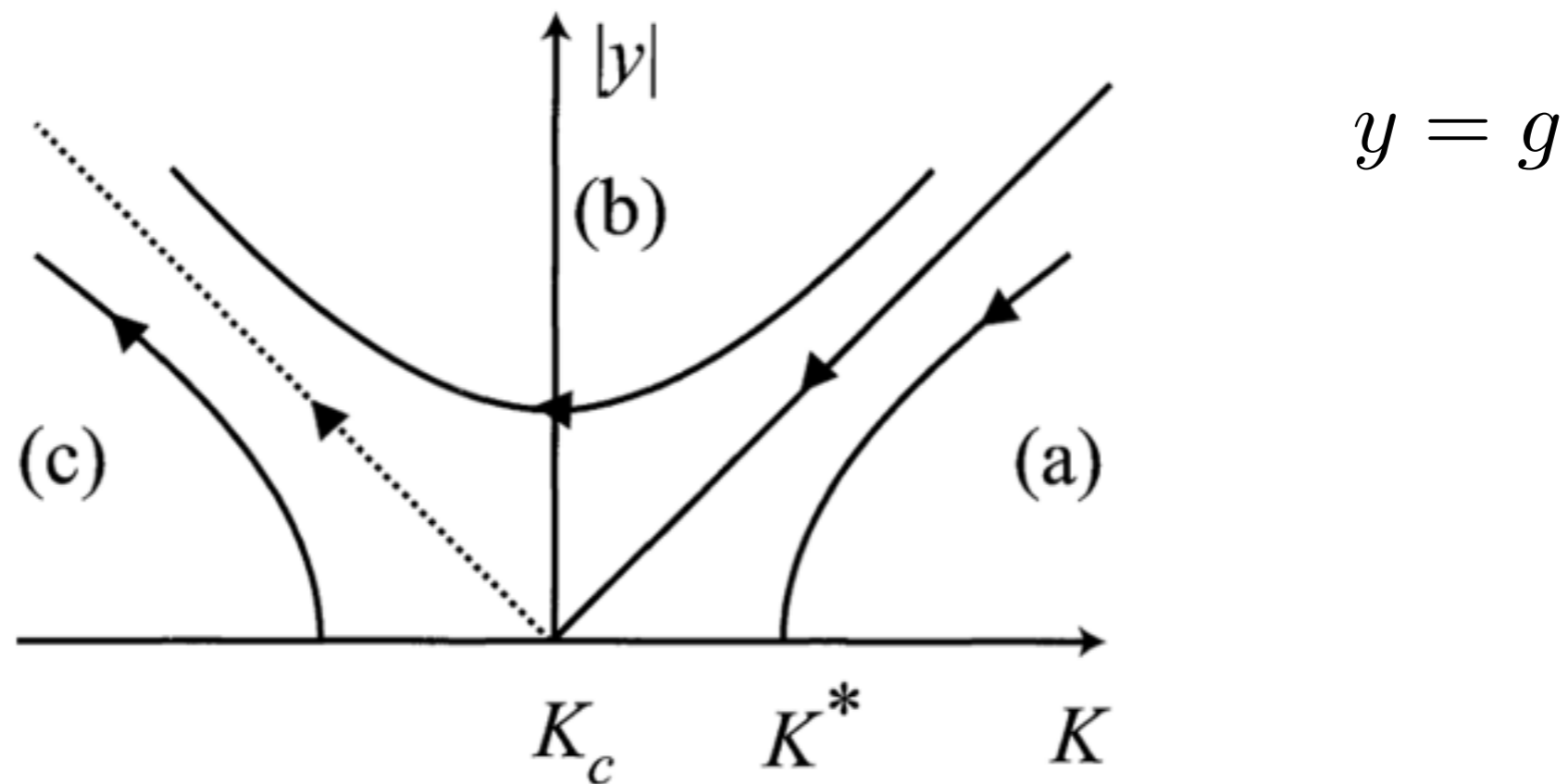
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$$K_\nu^c = \frac{8\pi}{\alpha_\nu^2}$$

$$h_\nu = 2 \left( \frac{K_\nu}{K_\nu^c} - 1 \right)$$

$$g_\nu^\perp = K_\nu^c g_\nu$$

$$\frac{dg_\nu^\perp}{dl} = -h_\nu g_\nu^\perp,$$

$$\frac{dh_\nu}{dl} = - (g_\nu^\perp)^2.$$

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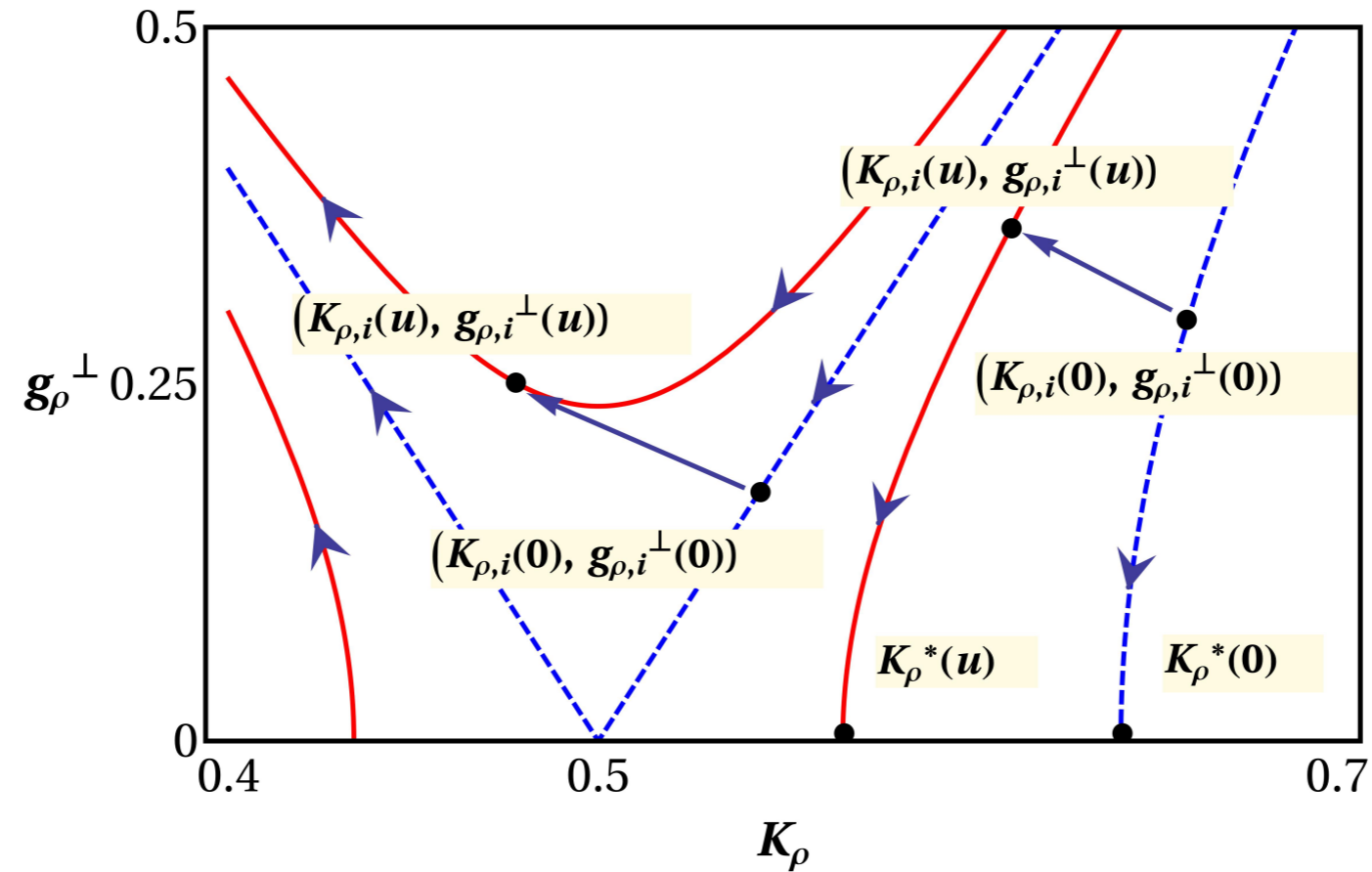
$$h_{\nu,i}(u) = 2 \left( \frac{K_{\nu,i}(0)}{K_{\nu}^c} - 1 \right) - \frac{v_i^F(0) f(u)}{v_{\nu}(0) K_{\nu}^c} \left[ (K_{\nu,i}(0))^2 - 1 \right]$$

$$g_{\nu,i}^{\perp}(u) = g_{\nu,i}^{\perp}(0) \left[ 1 - \frac{v_i^F(0) f(u)}{2v_{\nu}(0)} \left( K_{\nu,i}(0) + \frac{1}{K_{\nu,i}(0)} \right) \right].$$

$$f(u) = - \frac{v_i^F(0) - v_i^F(u)}{v_i^F(0)}$$

# Spinless fermions

$$\frac{v_v(0)}{v_i^F(0)} = 0.4 \text{ and } K_\rho^c = 1/2$$

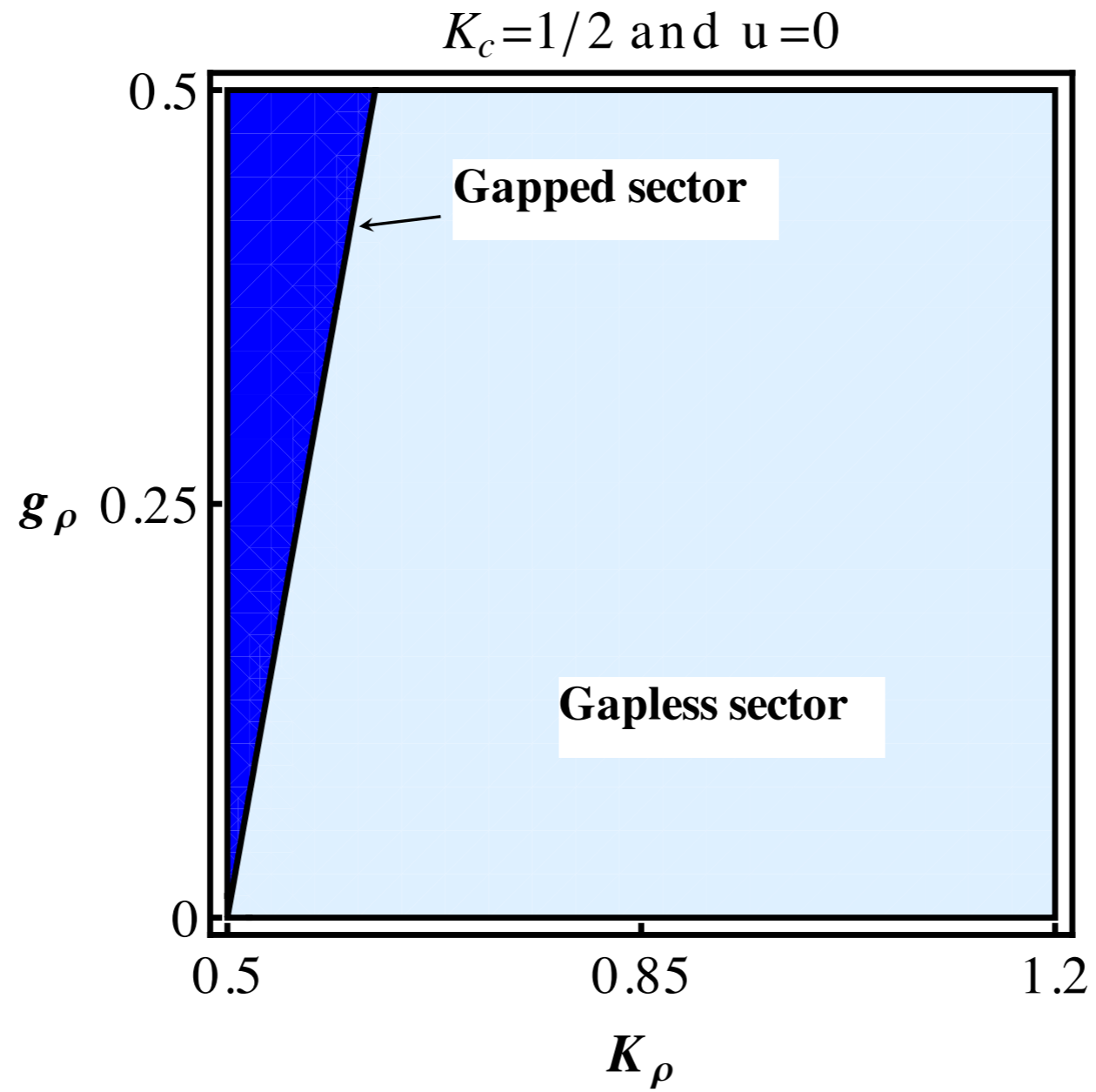


Spinless fermions

Boost can open a gap

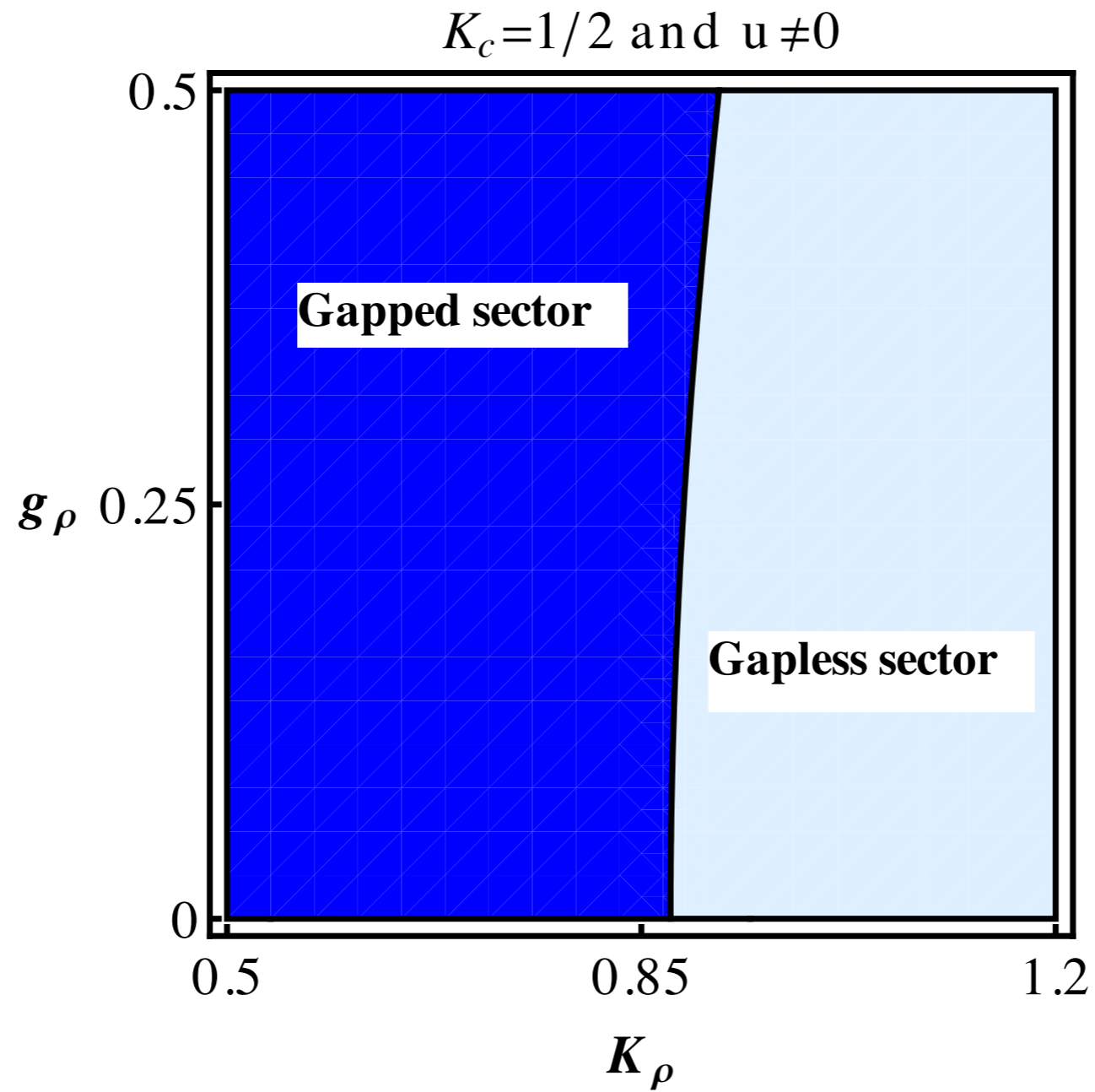
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# Spinless fermions

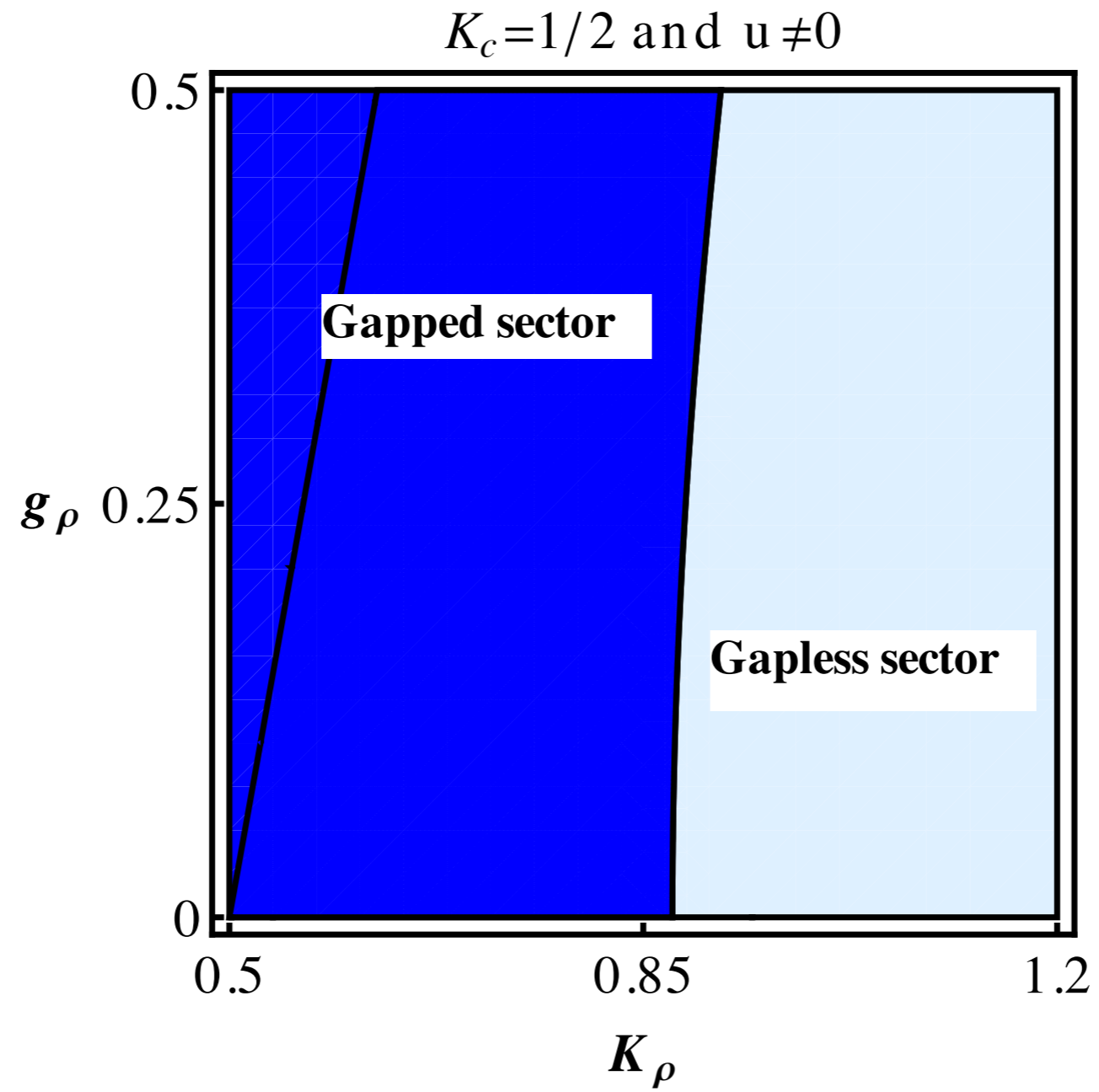
# Spinless fermions



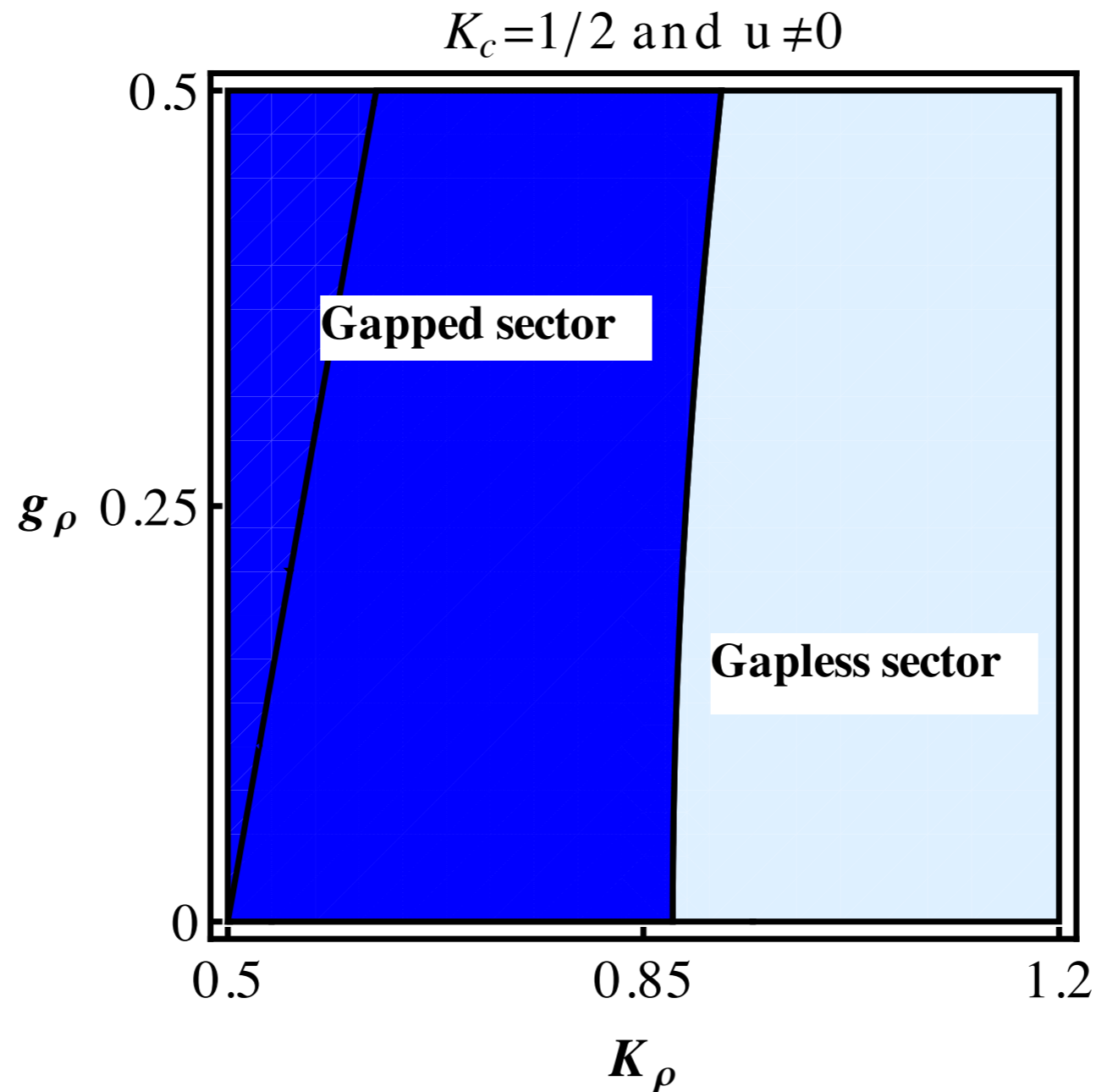
# Spinless fermions



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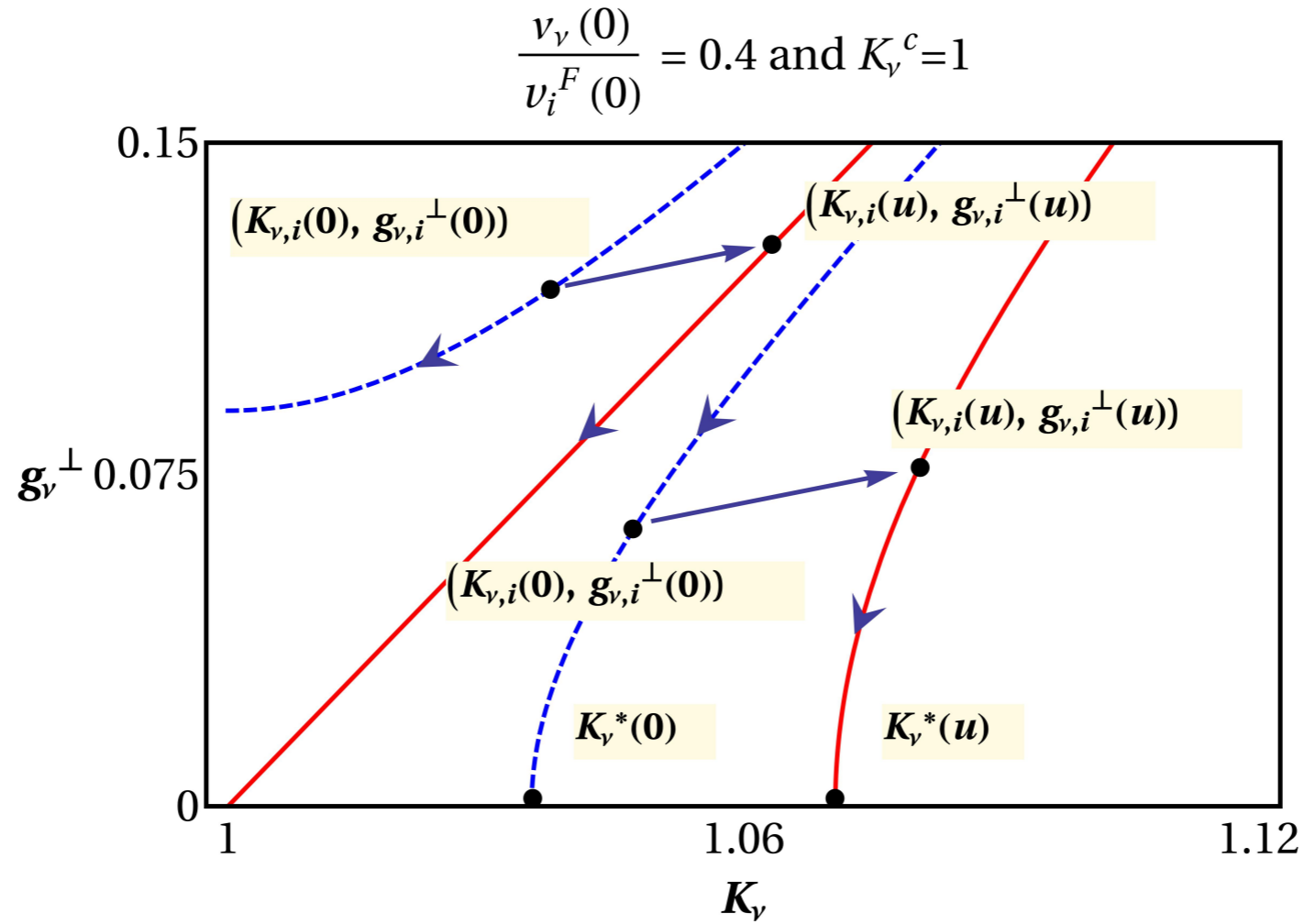


# Spinless fermions



The boost can open a gap for  $K < 1$   
Possibly algebraic CDW to long-ranged CDW

# Spin 1/2 fermions

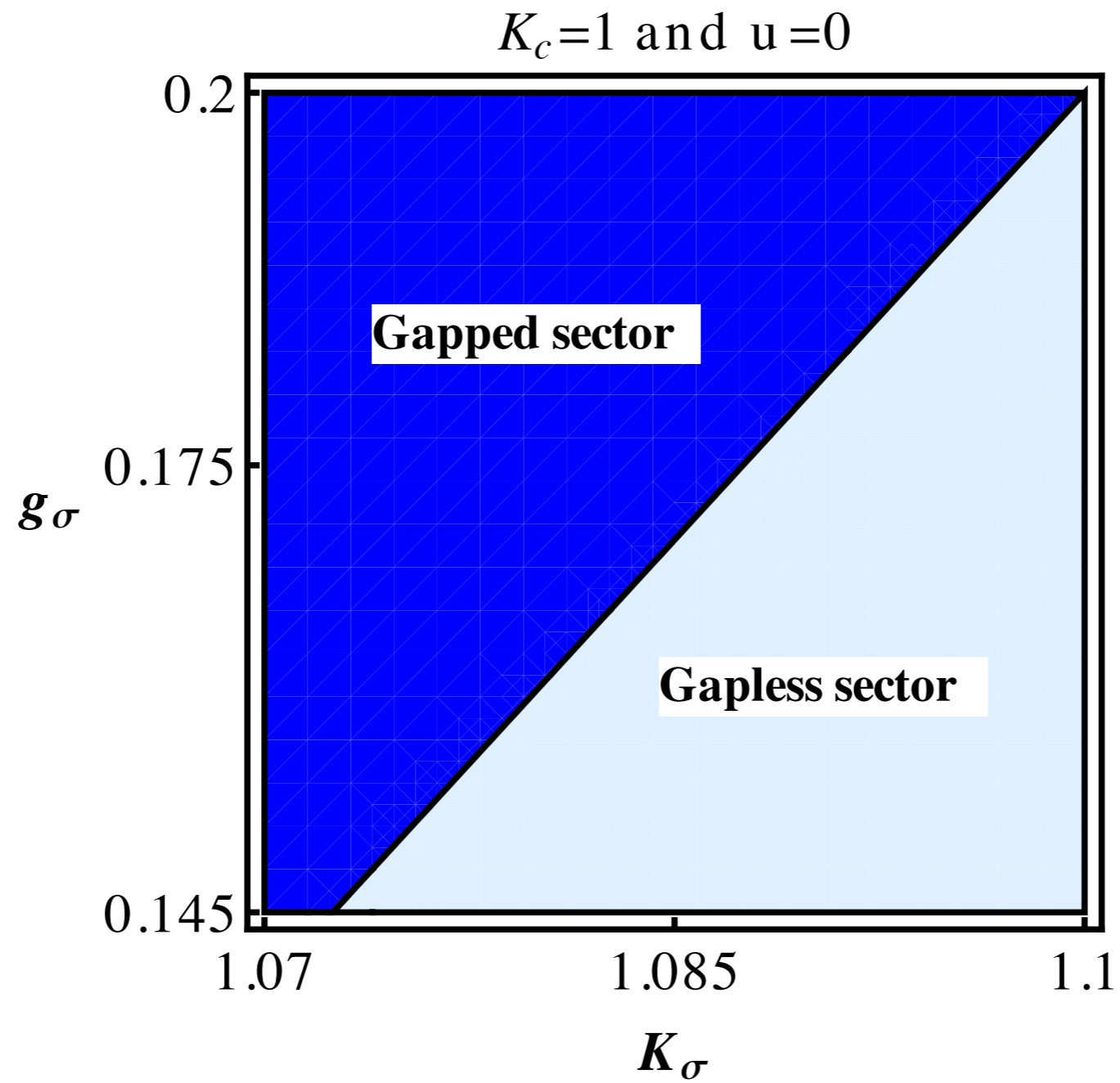


Spin 1/2 fermions

Boost can close gap

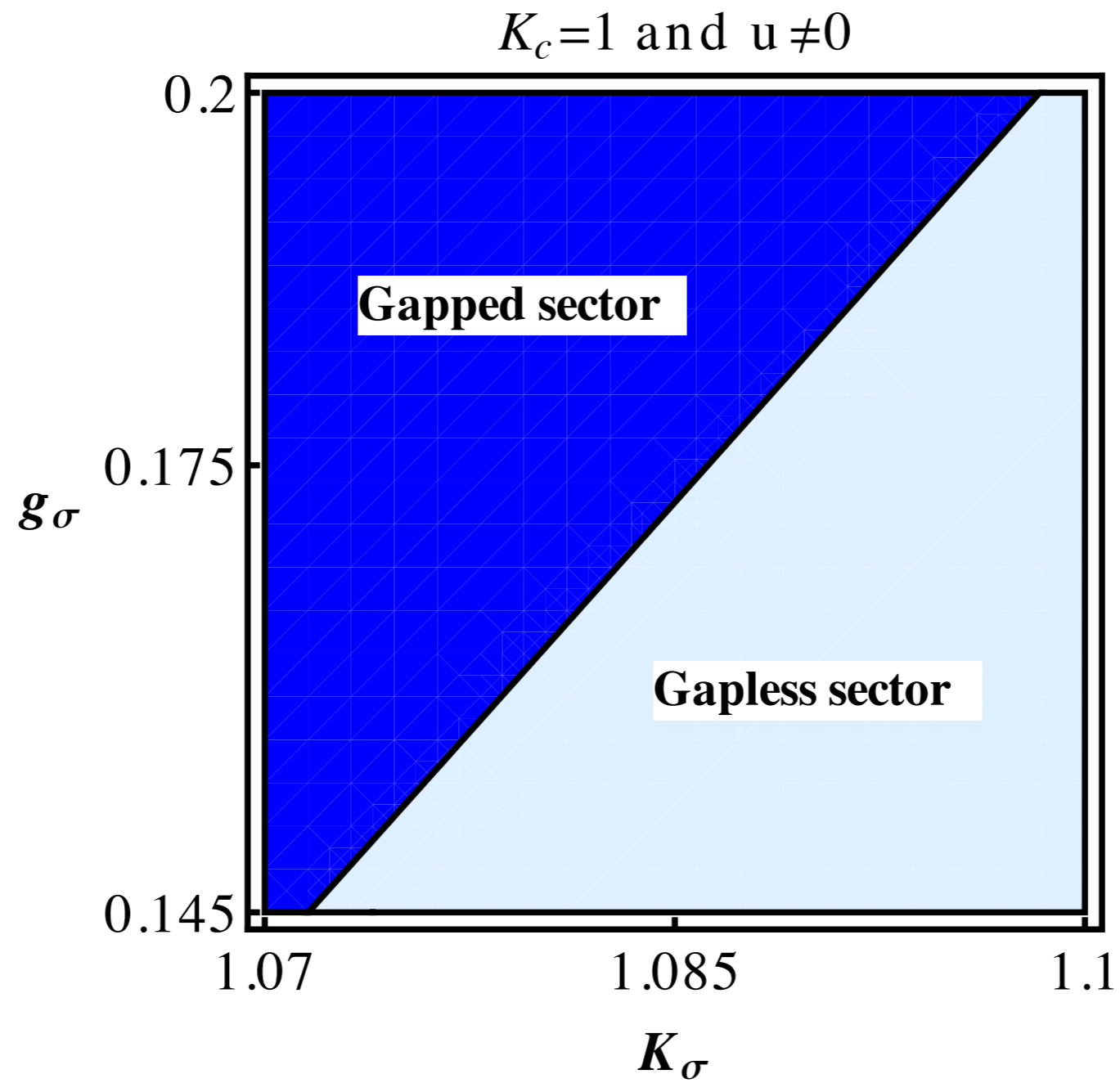
Spin  $1/2$  fermions

# Spin 1/2 fermions



Spin  $1/2$  fermions

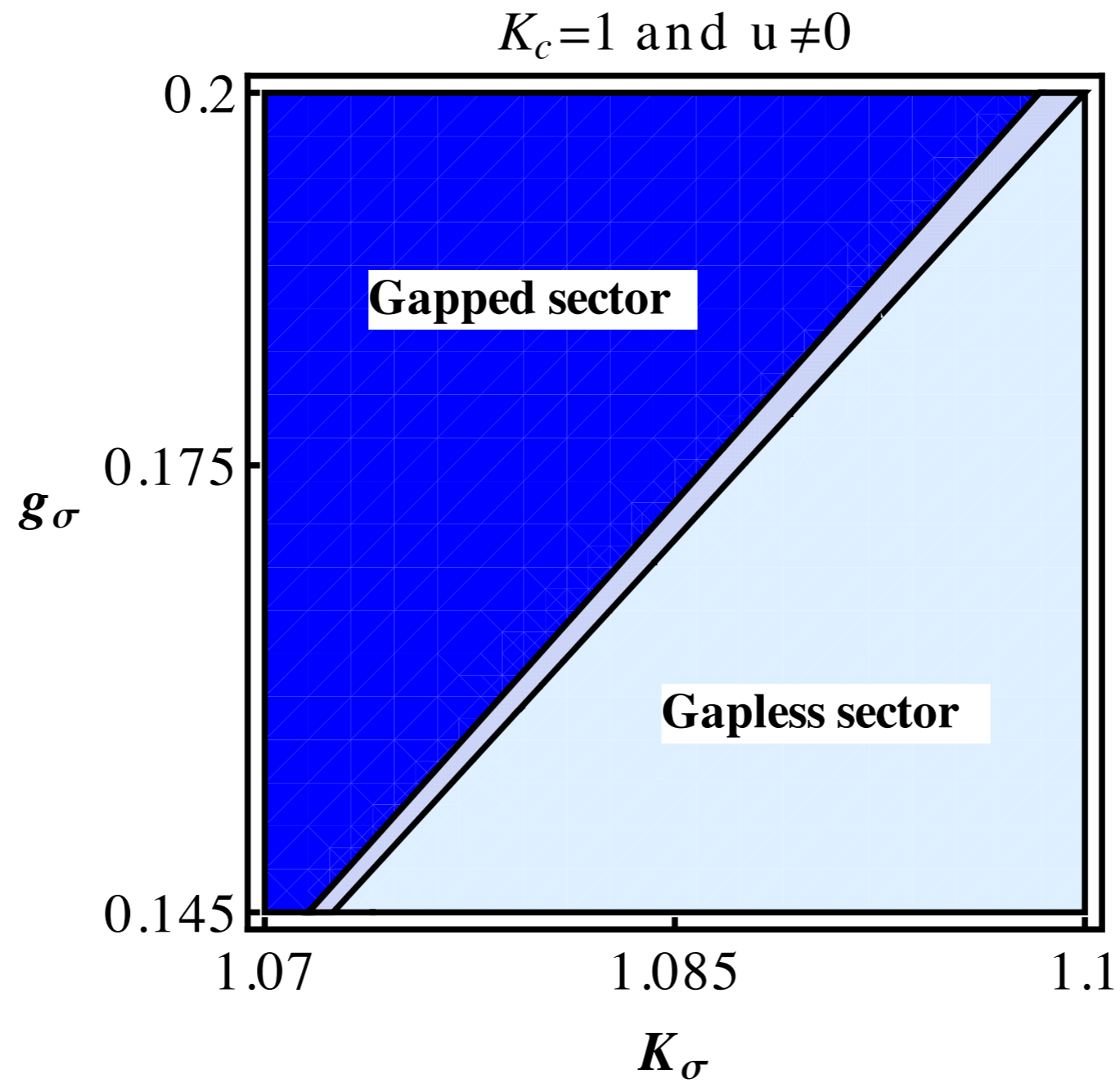
# Spin 1/2 fermions



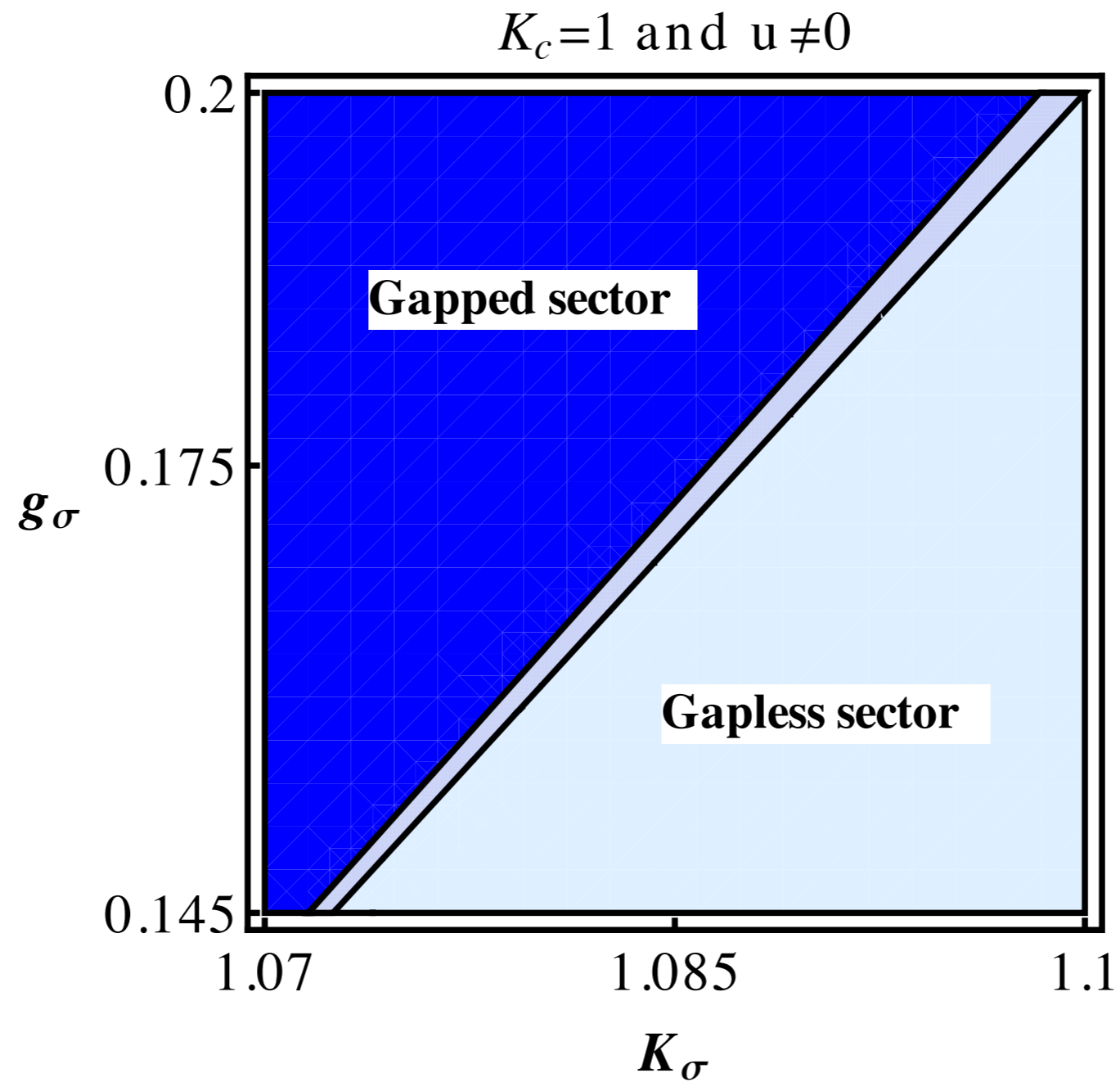
Spin  $1/2$  fermions



# Spin 1/2 fermions



# Spin 1/2 fermions



The boost can close a gap for  $K > 1$

Spin  $1/2$  fermions

Interesting possibility

Unboosted system with charge and spin gap

Boost closes one of the gaps

Close charge gap but not spin gap - Luther-Emery fluid

# Conclusions

- A boost has a non-trivial effect on algebraic order in 1D only for non-parabolic bands
- For a simple lattice dispersion, a boost can strengthen superconductivity (and CDW order)
- At commensurate filling, a boost can open or close gaps depending on whether the fermions are spinless or spinful
- Possible to obtain a Luther-Emery fluid by boosting starting from fully gapped state