

# *Supersymmetry*

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*the high energy story*

*Tuhin S. Roy*

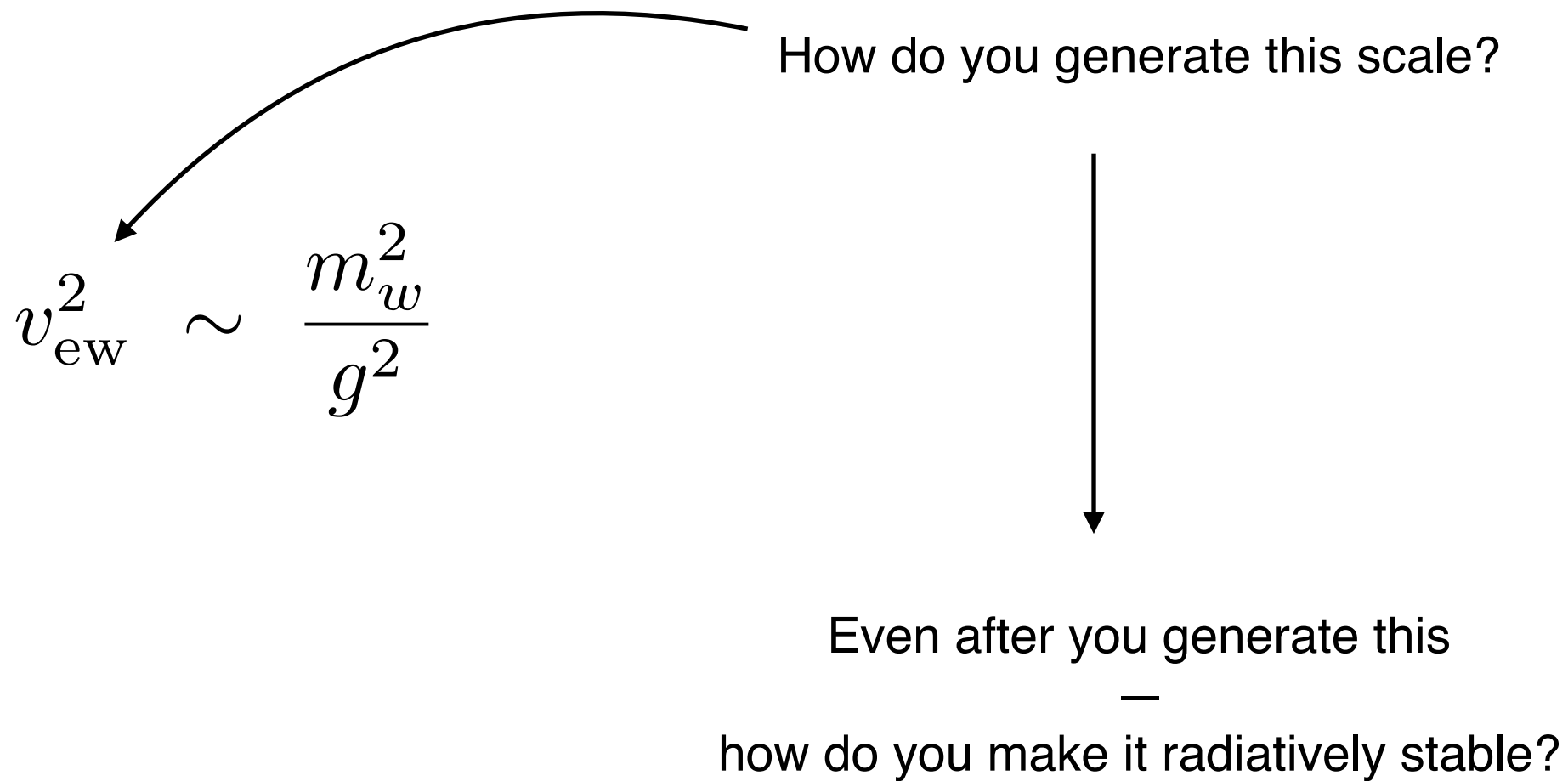
*Tata Institute of Fundamental Research*

# Outline

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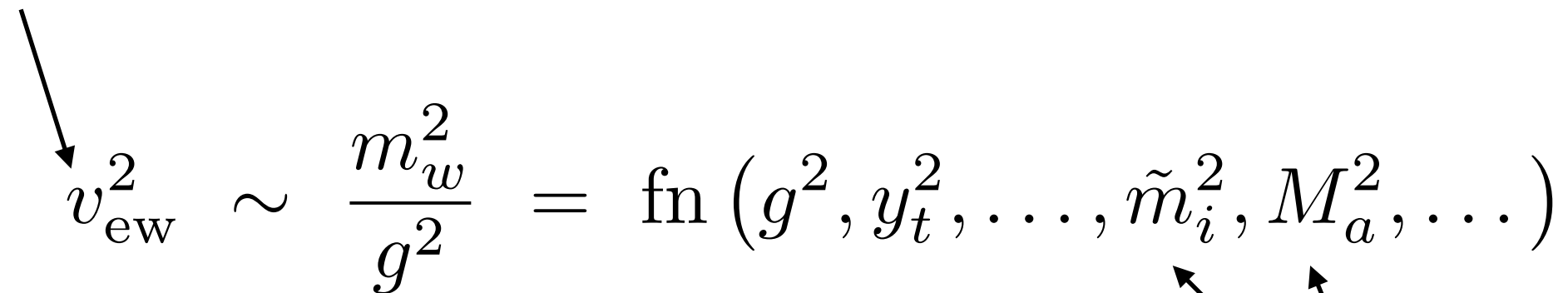
- Understanding electroweak scale
- Models of Supersymmetry in a nut-shell
- Physics of soft masses:
  - mediation mechanisms
  - renormalization
  - Dynamical supersymmetry breaking
- D-type susy breaking
  - the  $\mu$ -problem

# Understanding Electroweak Scale



# Understanding Electroweak Scale

mass scale we need to control

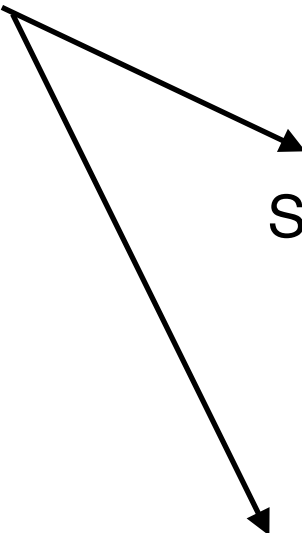

$$v_{\text{ew}}^2 \sim \frac{m_w^2}{g^2} = \text{fn} (g^2, y_t^2, \dots, \tilde{m}_i^2, M_a^2, \dots)$$

superpartner masses

In electroweak scale supersymmetry, you control  
electroweak scale by controlling superpartner masses

# Understanding Electroweak Scale

Control superpartner masses



SUSY rotates chirality into scalar sector — gives full control of radiative corrections on superpartner masses

How do we generate small (electroweak scale) superpartner masses?

# Understanding Electroweak Scale

$$\tilde{m}^2 \sim \frac{F^2}{M^2}$$

parameter of mass dimension 2

parametrizes susy breaking scale

mediation scale

For Planck mediation:

$$M = M_{\text{Pl}}$$

$$F \sim 10^{10-11} \text{ GeV}$$

# Understanding Electroweak Scale

$$\tilde{m}^2 \sim \frac{F^2}{M^2}$$

parameter of mass dimension 2

parametrizes susy breaking scale

mediation scale

Smallness of electroweak scale or smallness of superpartner masses  
raises the question

how do you generate

$$\begin{aligned} \sqrt{F} &\ll M && \text{if } M \sim M_{\text{Pl}} \\ \sqrt{F}, M &\ll M_{\text{Pl}} && \text{if } M \ll M_{\text{Pl}} \end{aligned}$$

# Understanding Electroweak Scale

Smallness of electroweak scale or smallness of superpartner masses  
raises the question

how do you generate

$$\frac{\sqrt{F}}{M_{\text{Pl}}} \ll 1$$

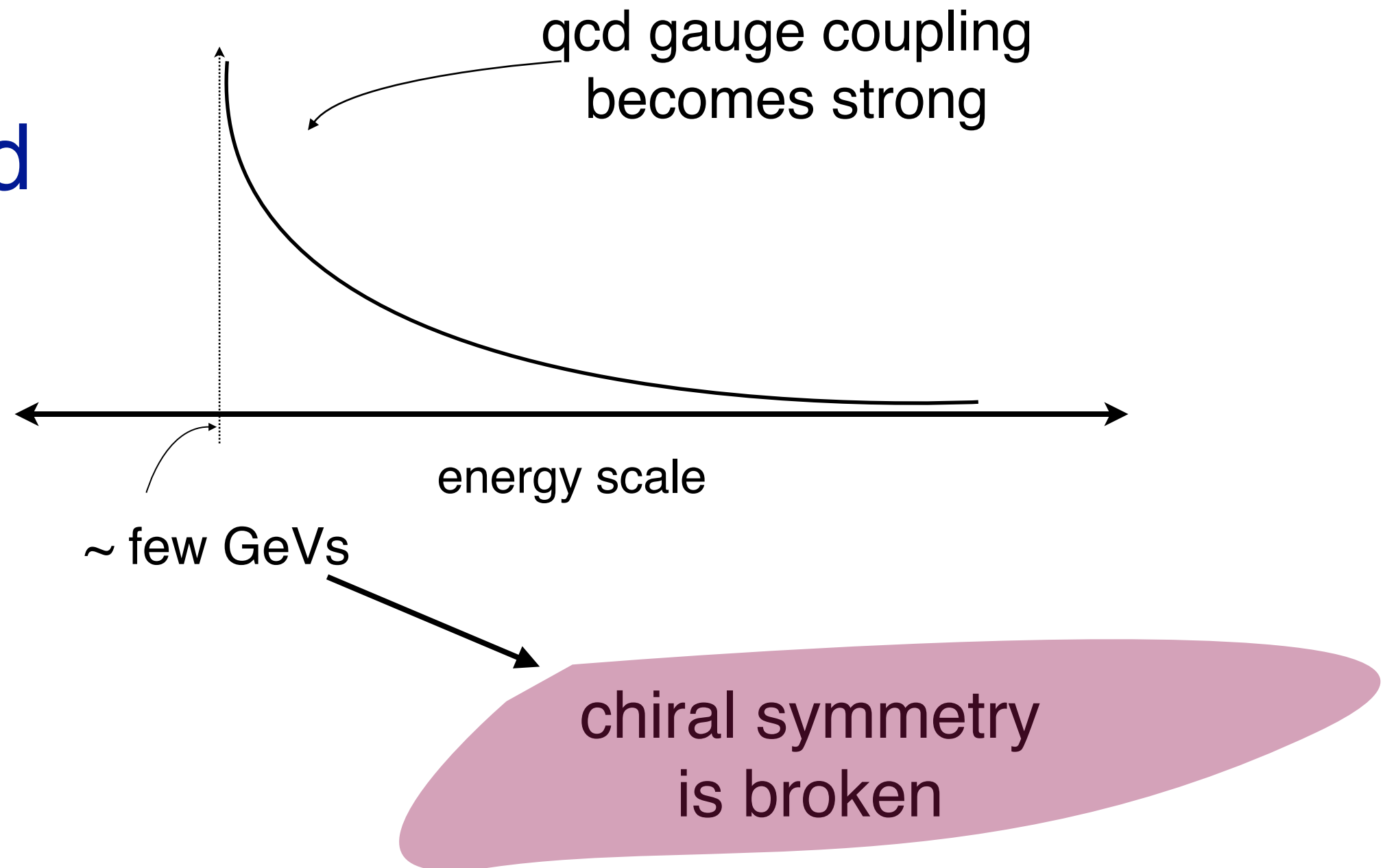
We know how nature does it with QCD

$$e^{-\frac{8\pi^2}{g^2}} \ll 1$$



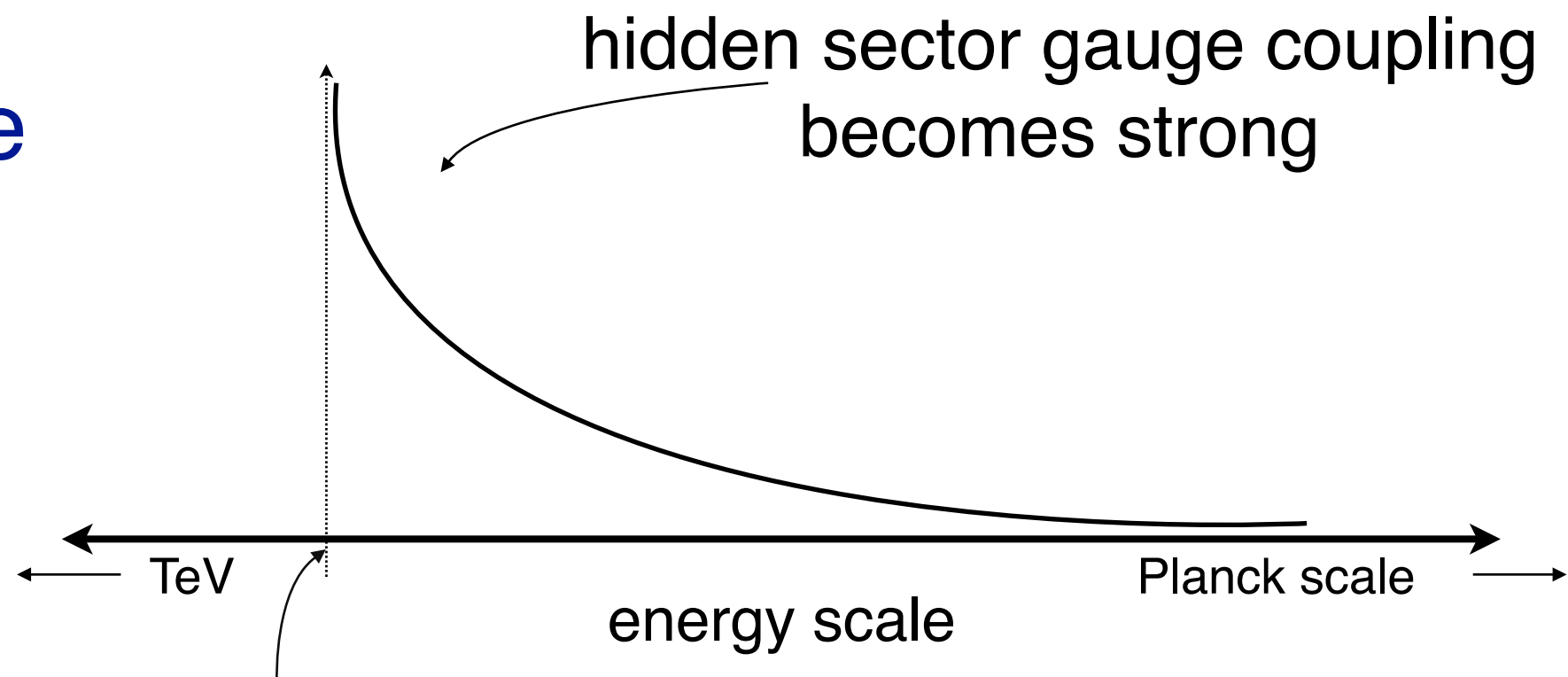
# Understanding Electroweak Scale

take qcd



# Understanding Electroweak Scale

just like  
qcd



intermediate  
scale

supersymmetry  
is broken

# Outline

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  - mediation mechanisms
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- D-type susy breaking
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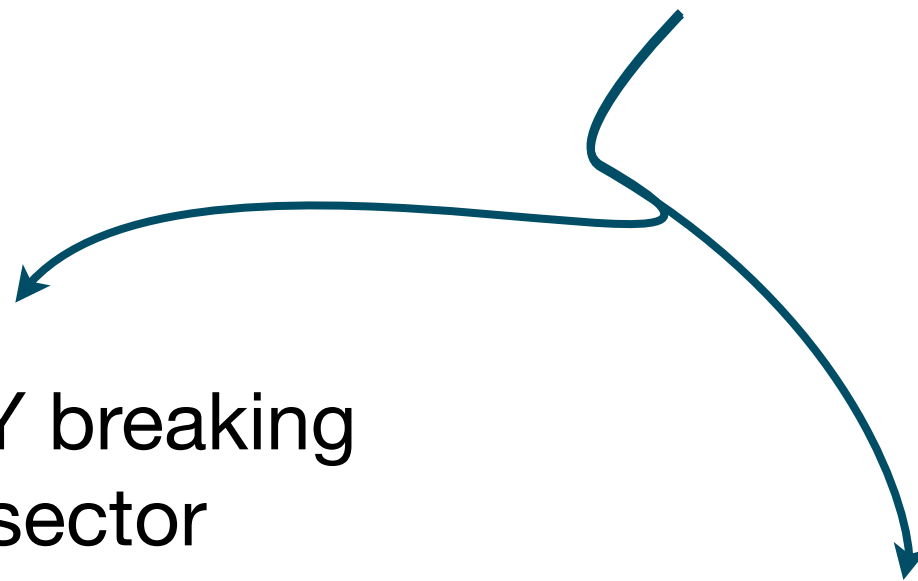
# *SUSY model in a nut-shell*

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Skeleton of a complete SUSY model

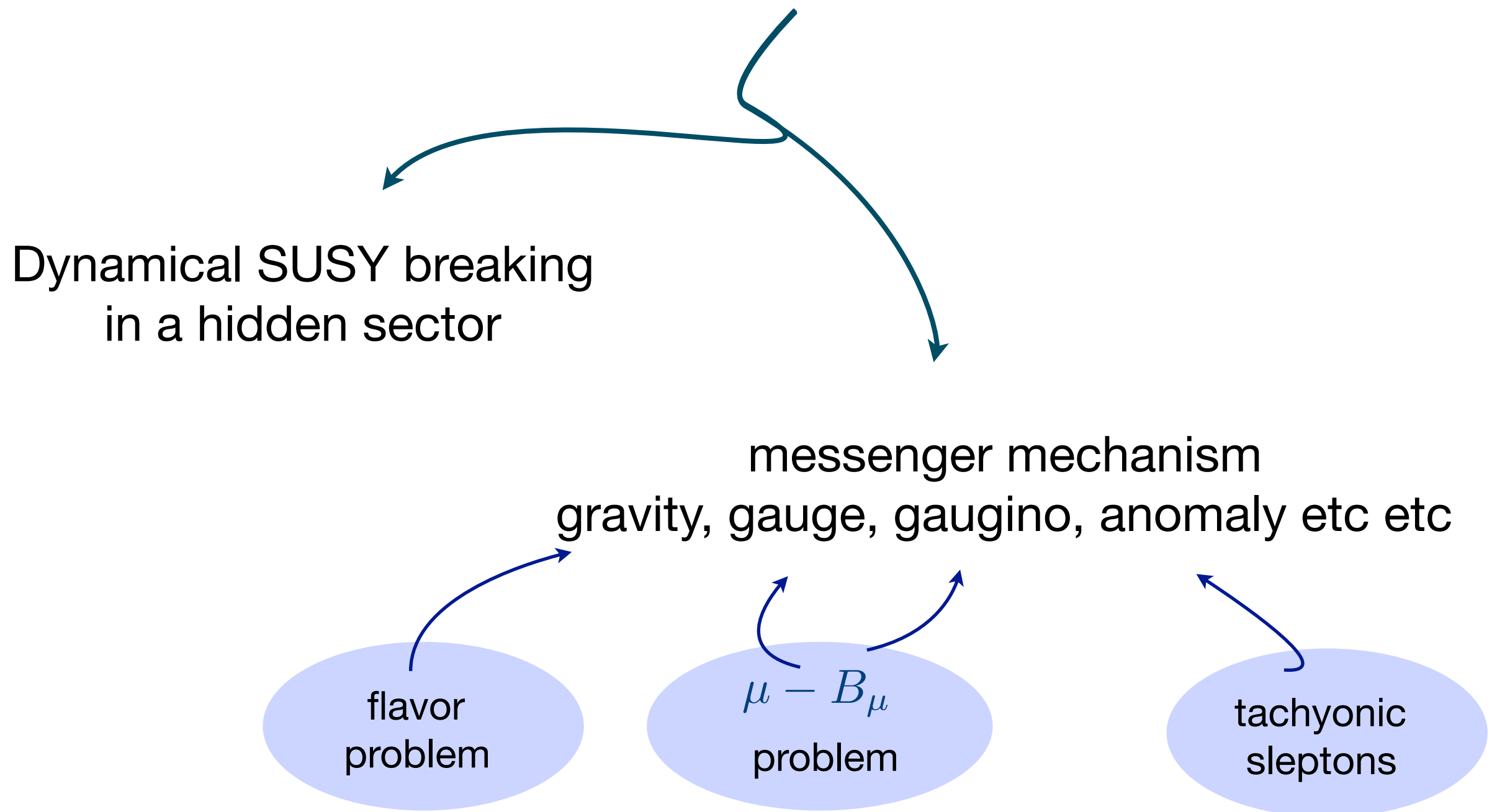
Dynamical SUSY breaking  
in a hidden sector

messenger mechanism  
gravity, gauge, gaugino, anomaly etc etc



# *SUSY model in a nut-shell*

Skeleton of a complete SUSY model



# *SUSY model in a nut-shell*

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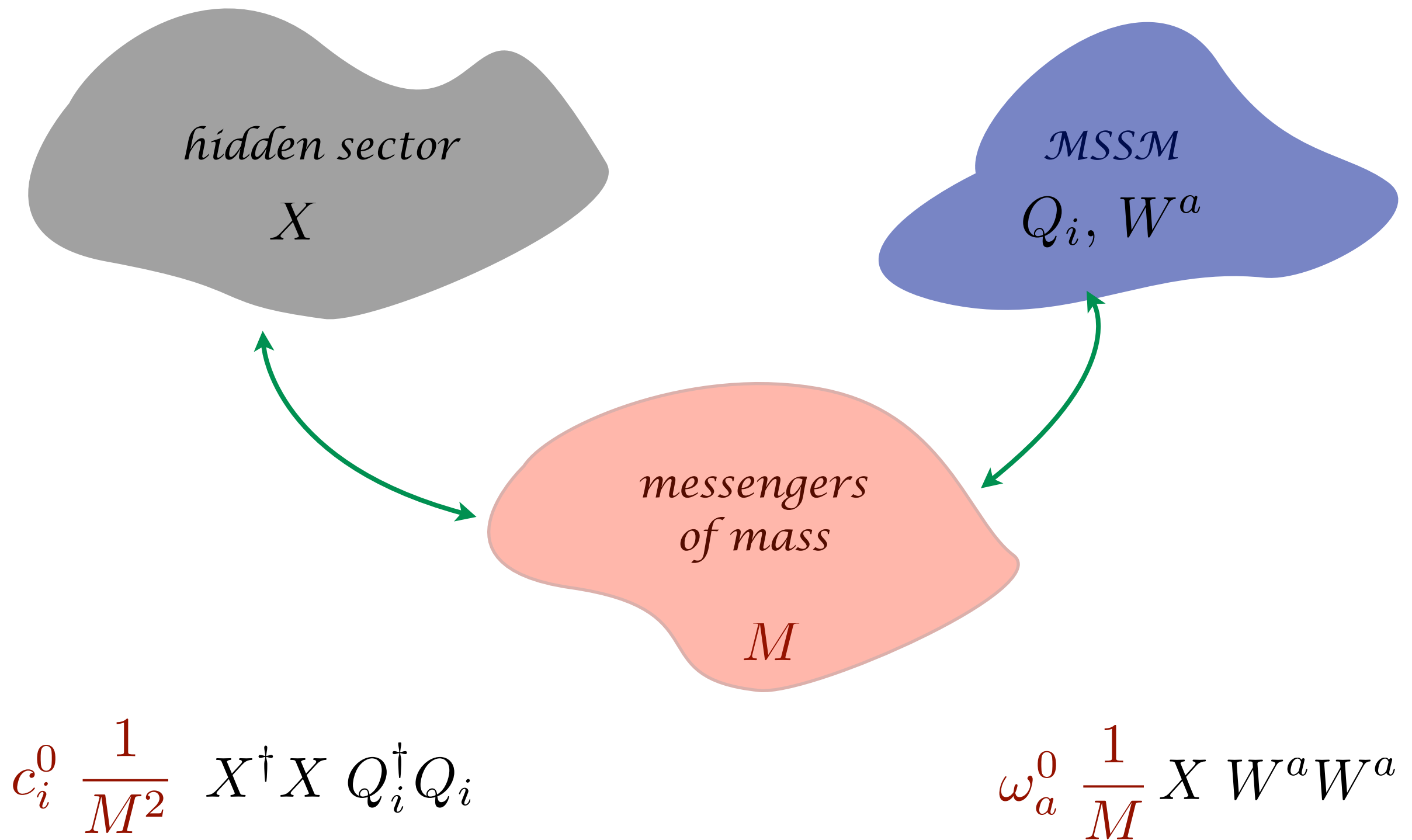
Skeleton of a complete SUSY model

Dynamical SUSY breaking  
in a hidden sector

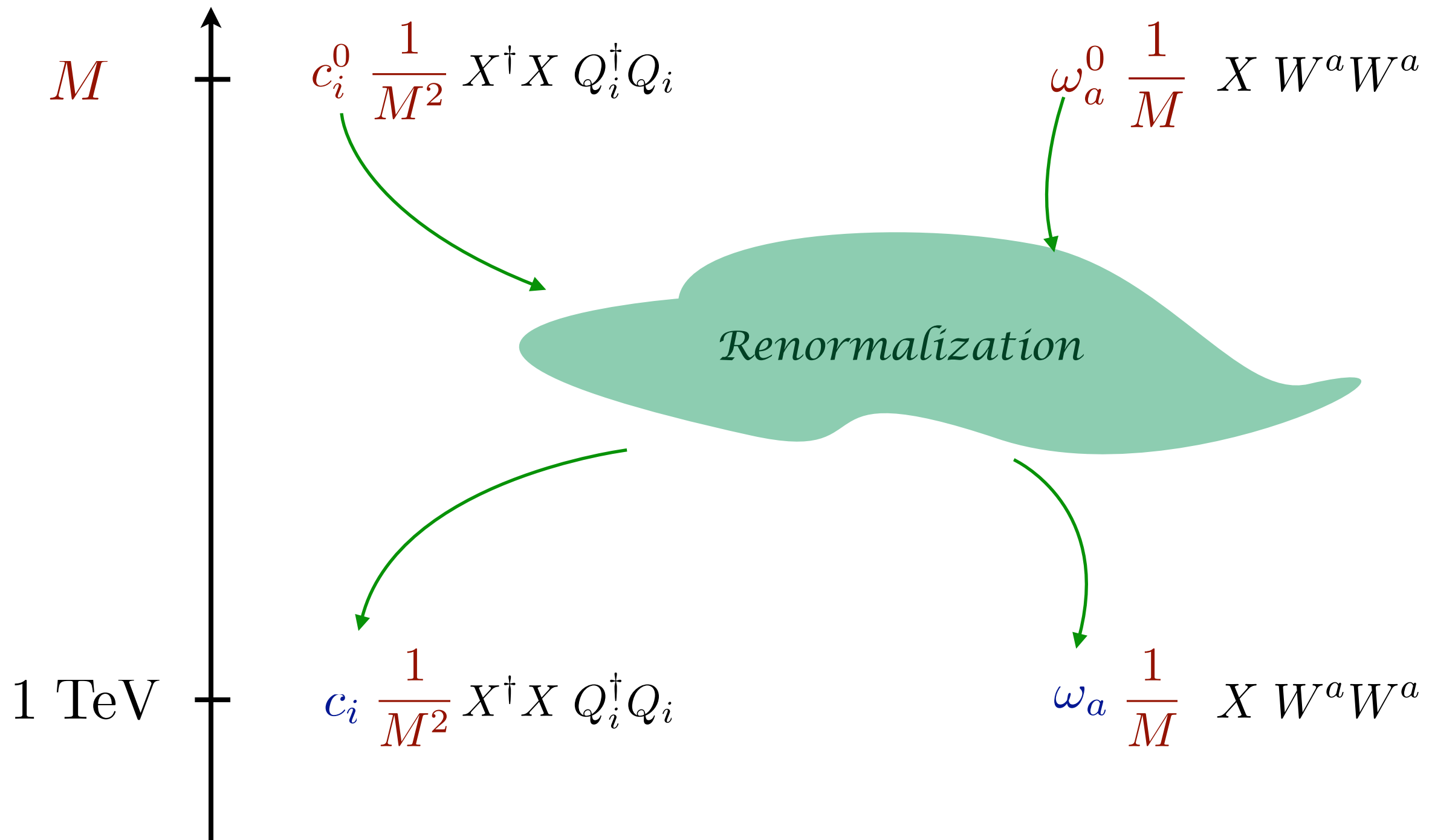
messenger mechanism  
gravity, gauge, gaugino, anomaly etc etc

Exploring various susy models and their nuances is a semester long course — can't do justice in 45 minutes

# Physics of soft masses

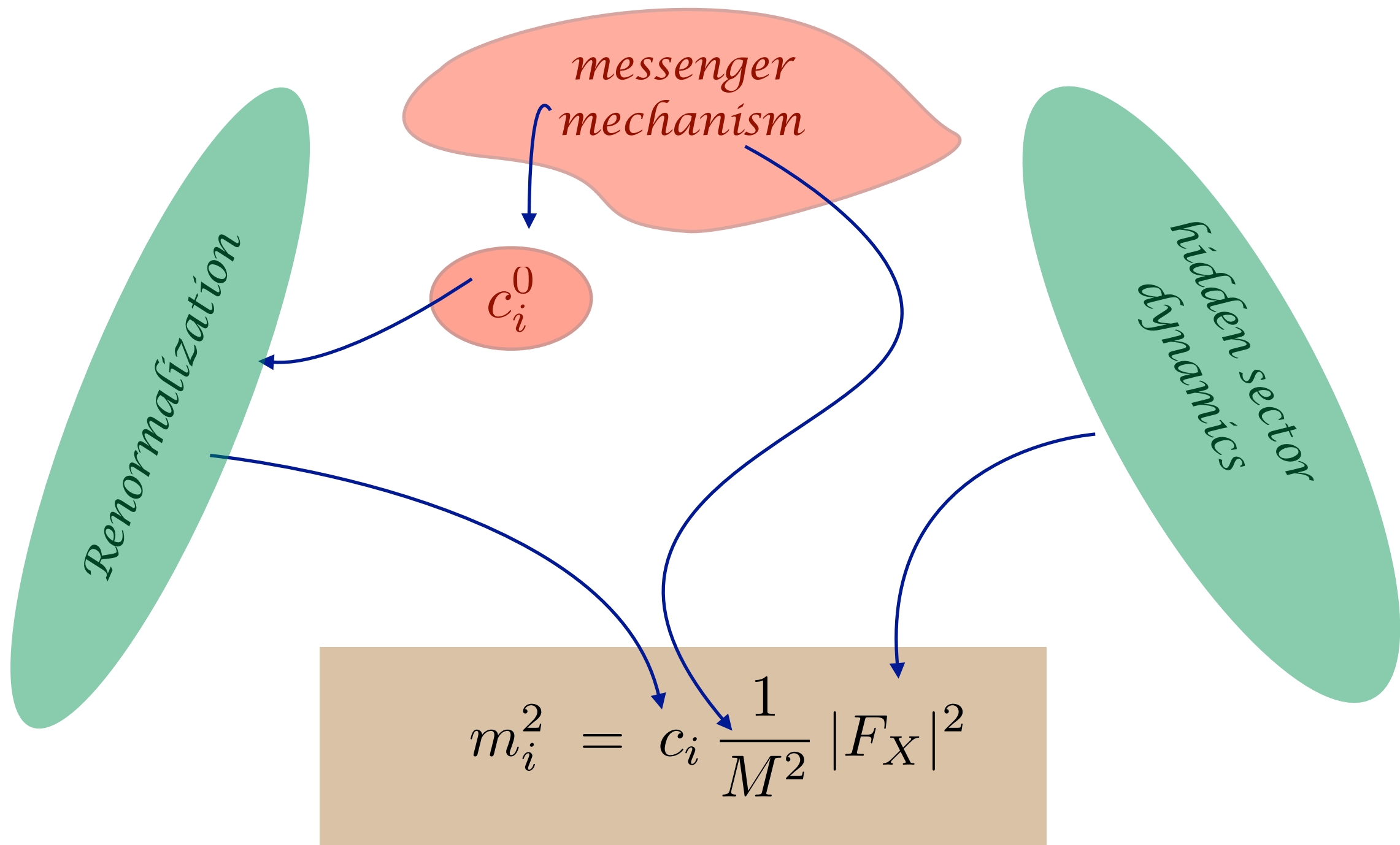


# Physics of soft masses

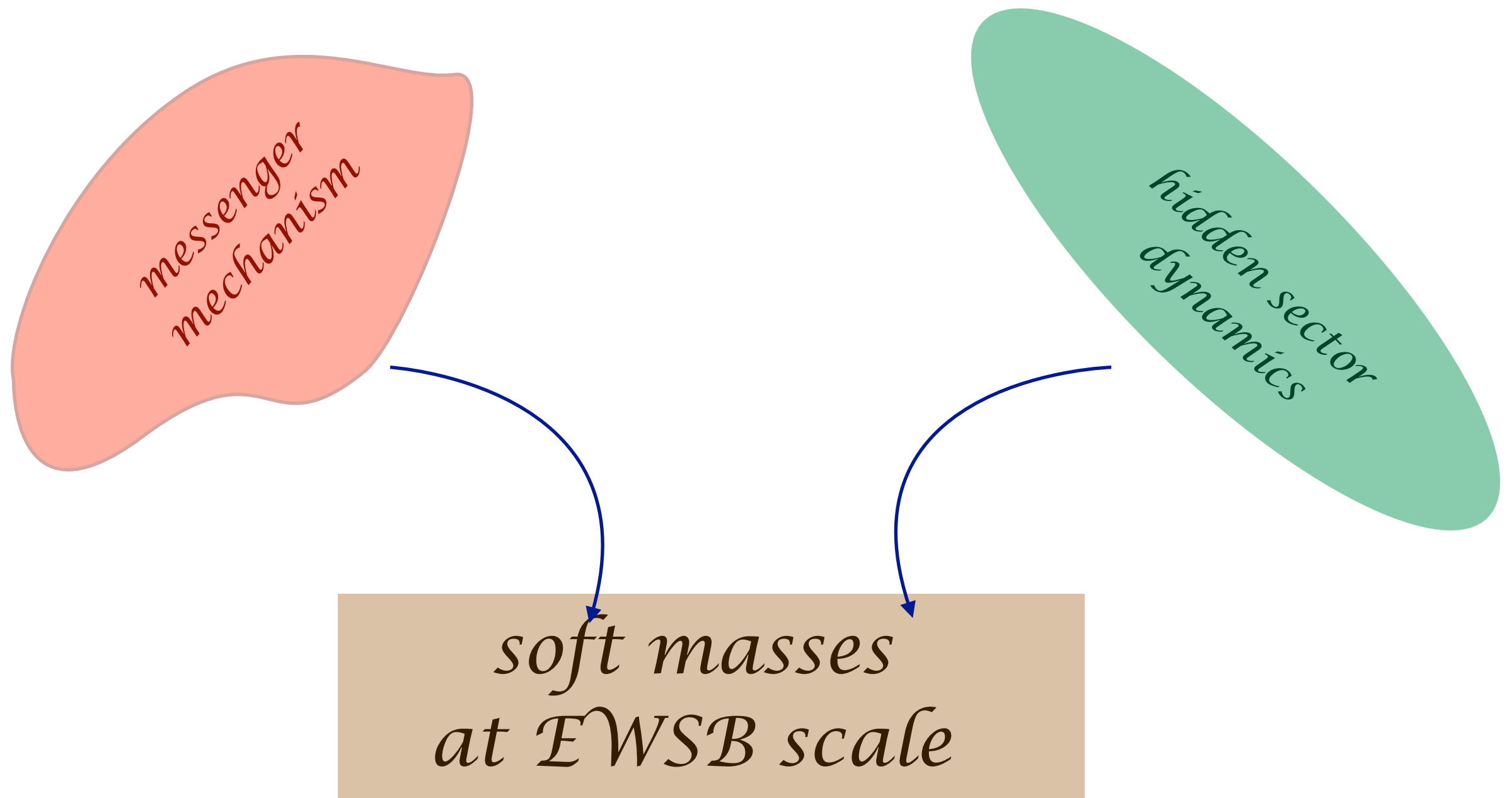




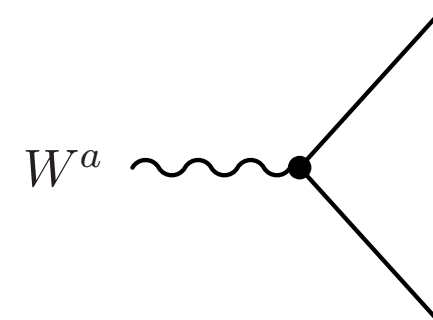
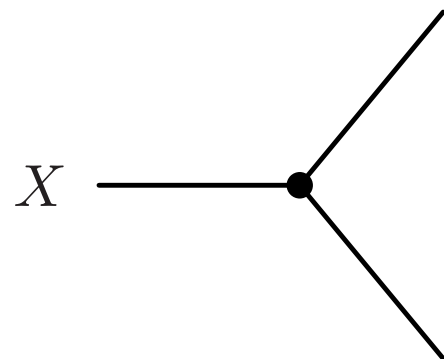
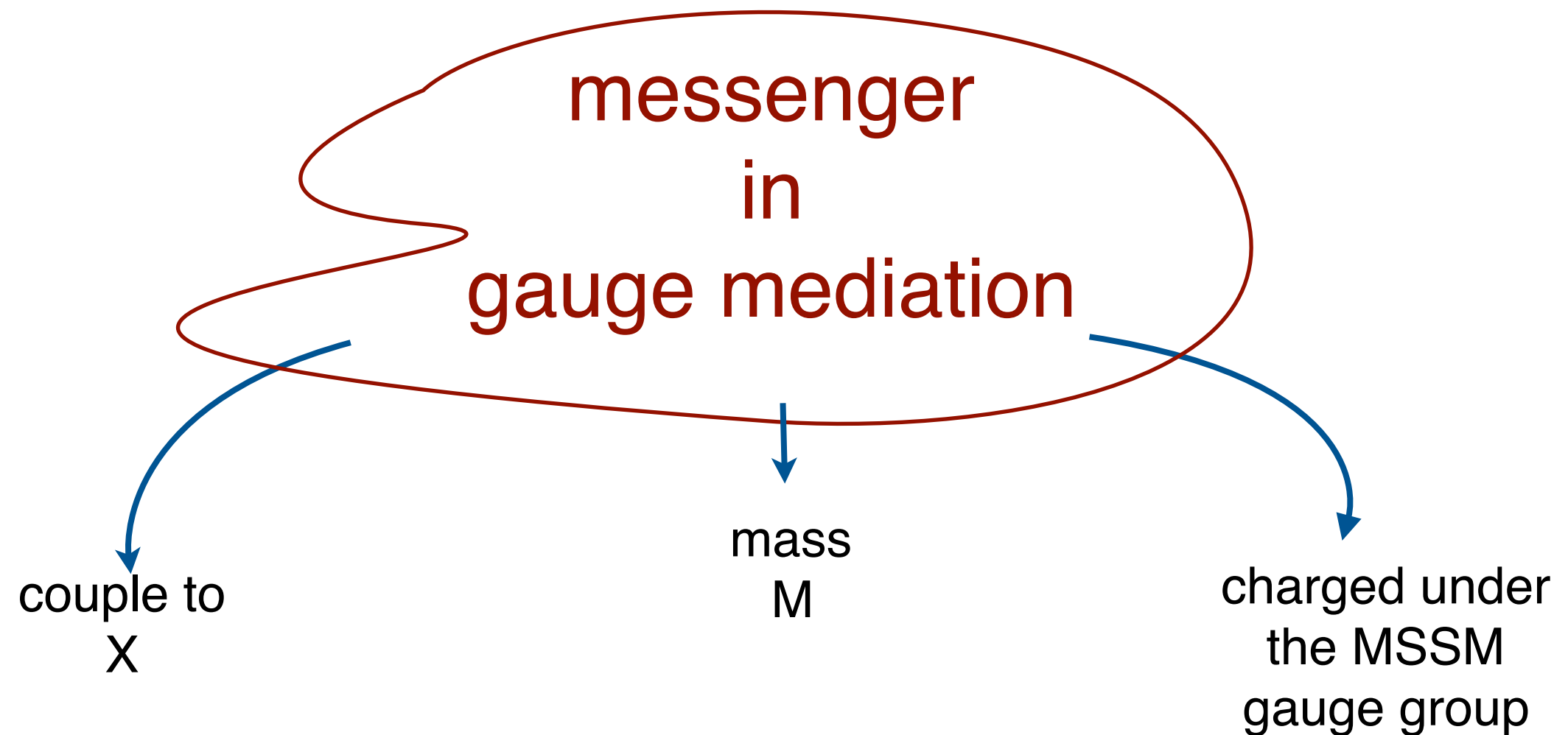
# Physics of soft masses



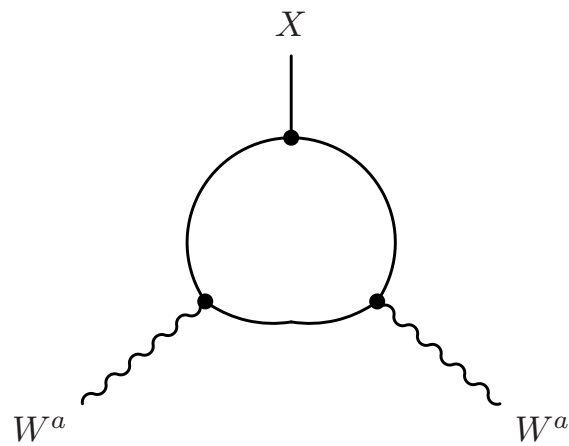
# Physics of soft masses



# example: gauge mediation

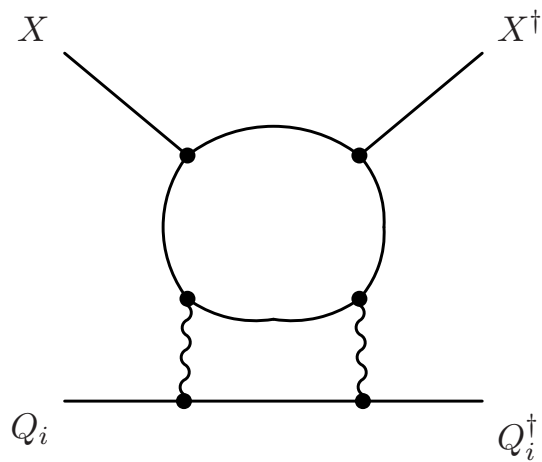


# example: gauge mediation



$$\sim \frac{1}{16\pi^2} \frac{X}{M} W^a W^a$$

$$\omega_a^0$$



$$\sim q_i \frac{g_i^4}{(16\pi^2)^2} \frac{X^\dagger X}{M^2} Q_i^\dagger Q_i$$

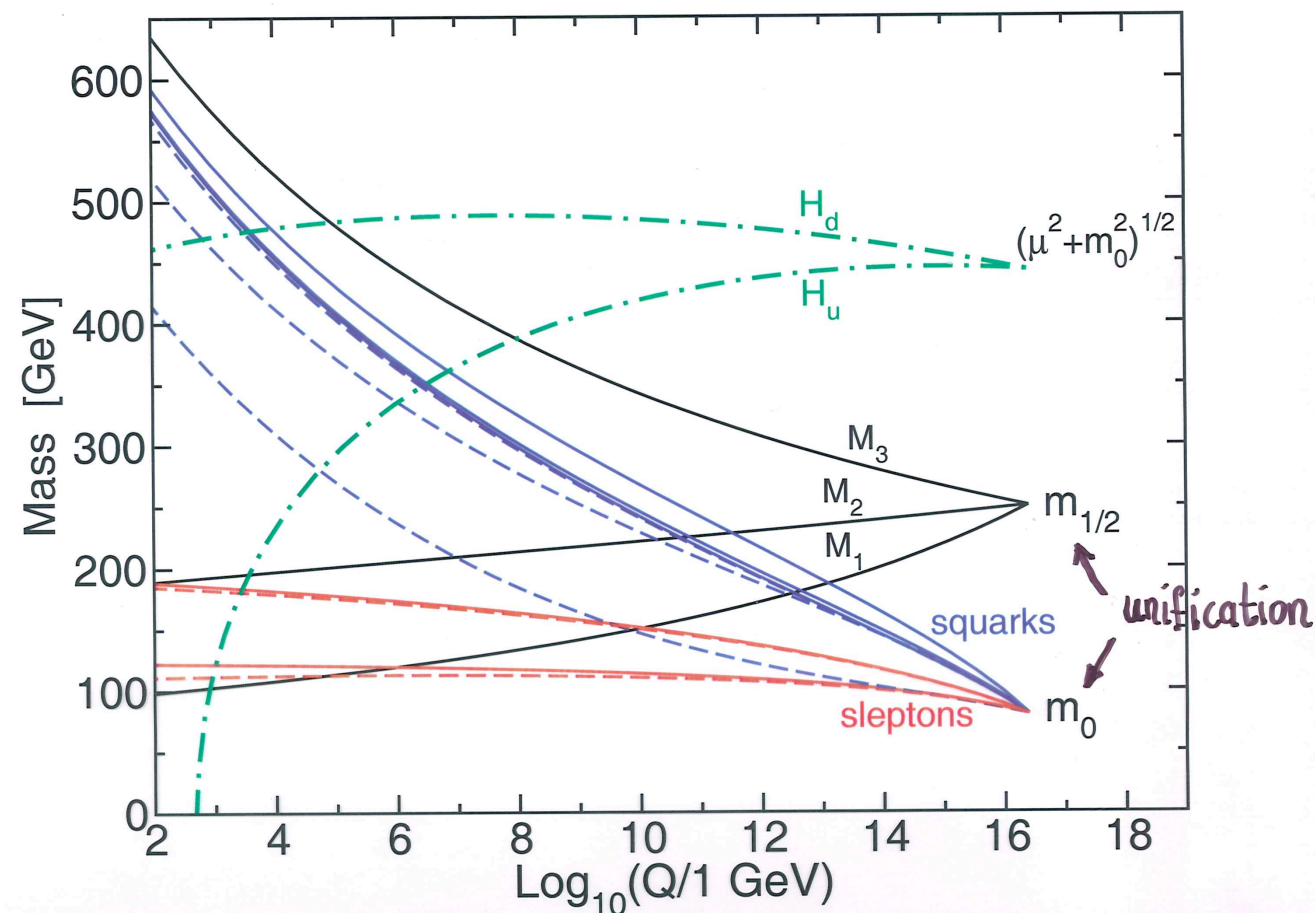
$$c_i^0$$

# Renormalization

*for example: take superpartner mass running in  
SO(10)*

## State of the art MSSM running

- 2 loop running
- 1 loop matching at 1 TeV and at GUT
- automated
  - Isajet
  - Softsusy
  - Suspect
  - -
  - -

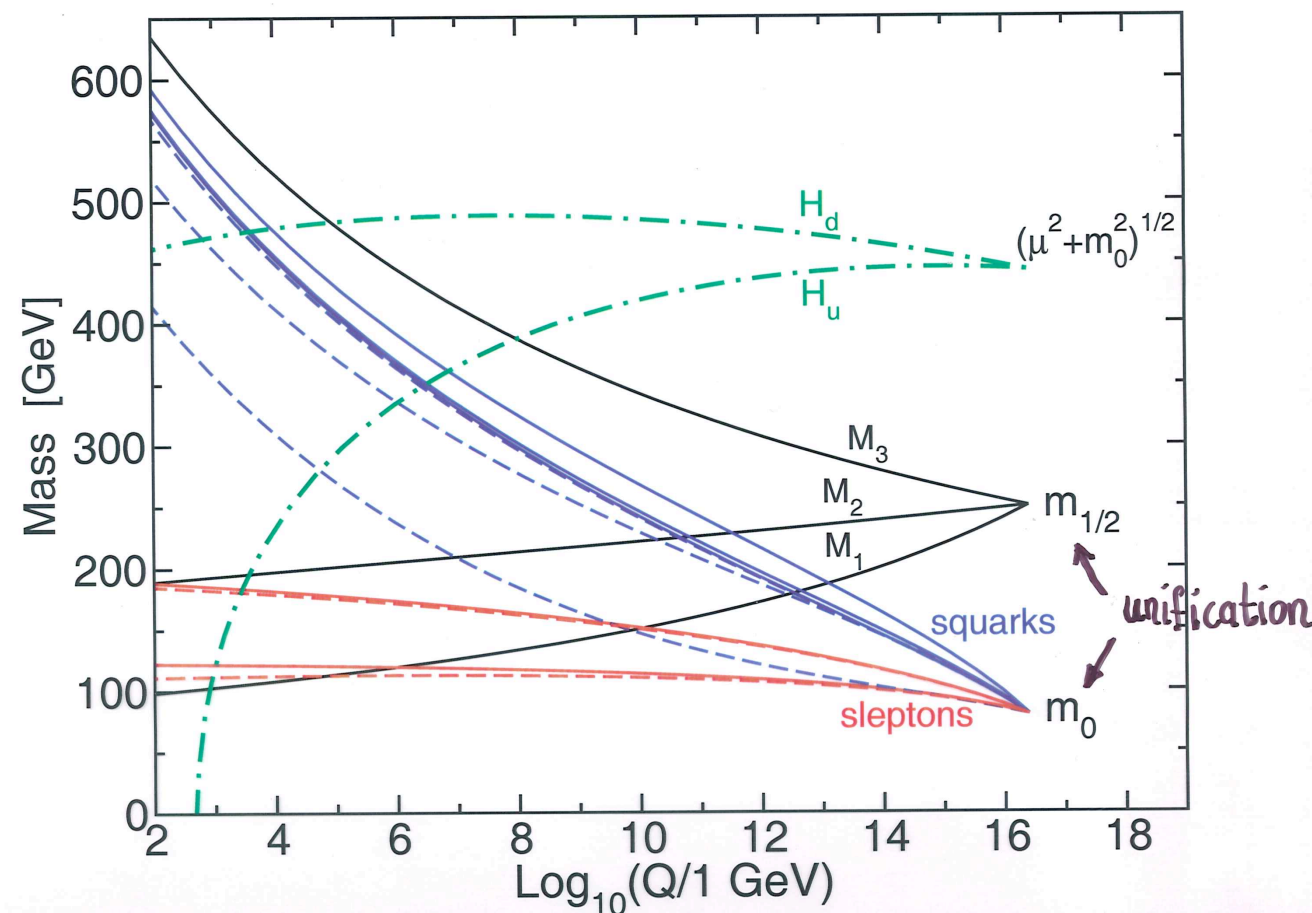


# Renormalization

*for example: take superpartner mass running in  
SO(10)*

## State of the art MSSM running

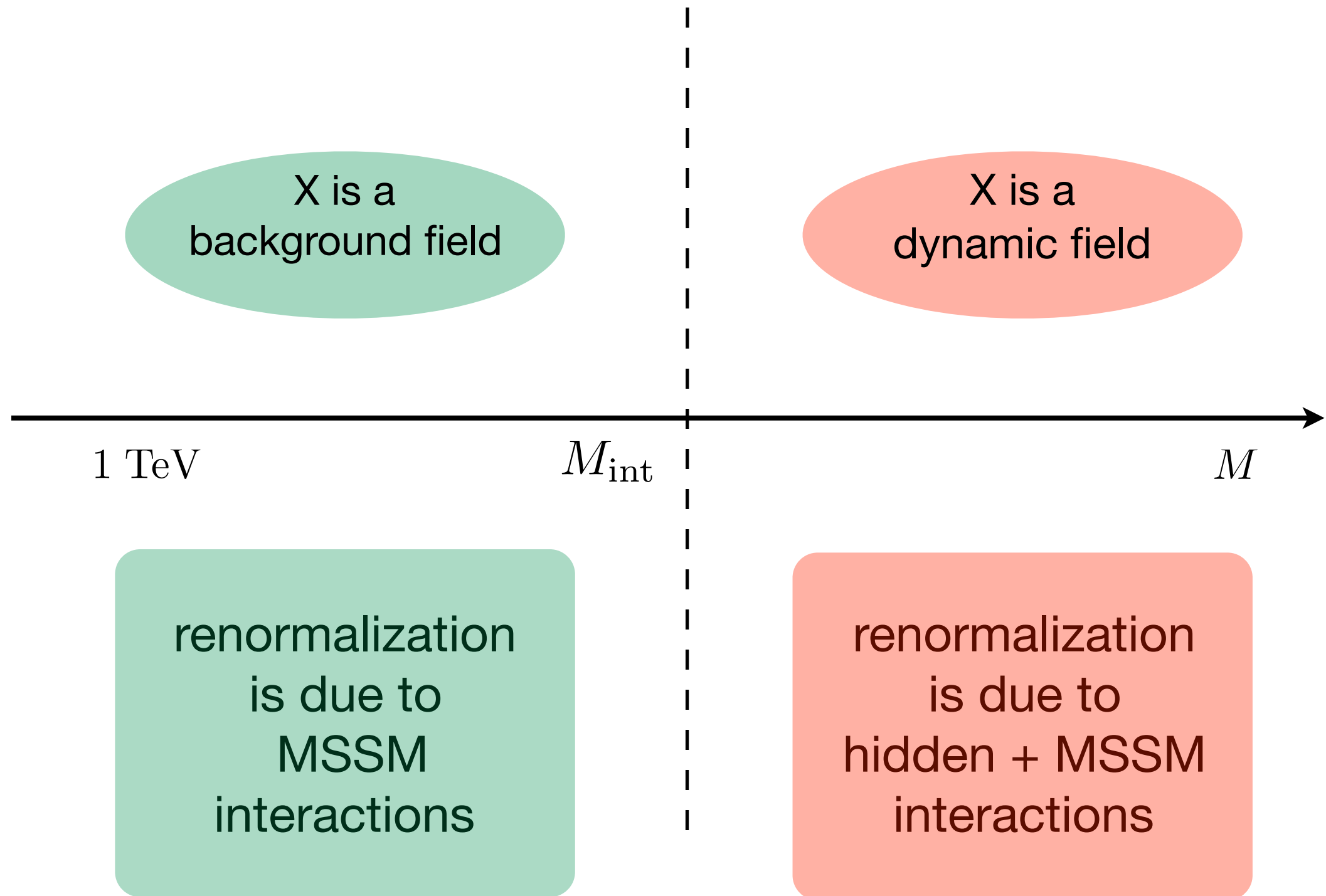
- 2 loop running
- 1 loop matching at 1 TeV and at GUT
- automated
  - Isajet
  - Softsusy
  - Suspect
  - -
  - -



zillions of papers have used/still use this renormalization — all wrong!

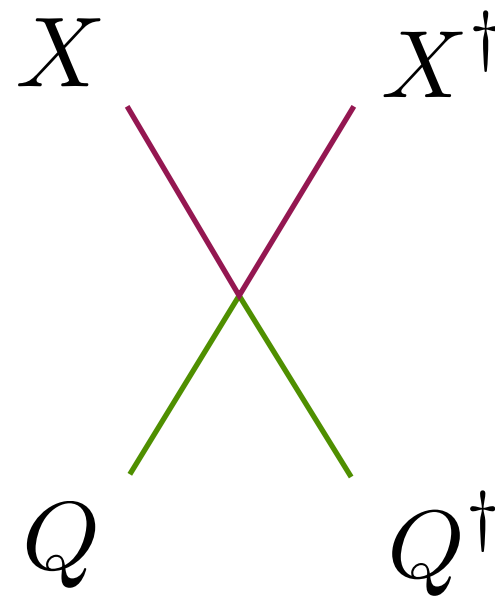
# *Scales in renormalization*

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# RGEs of SUSY breaking masses

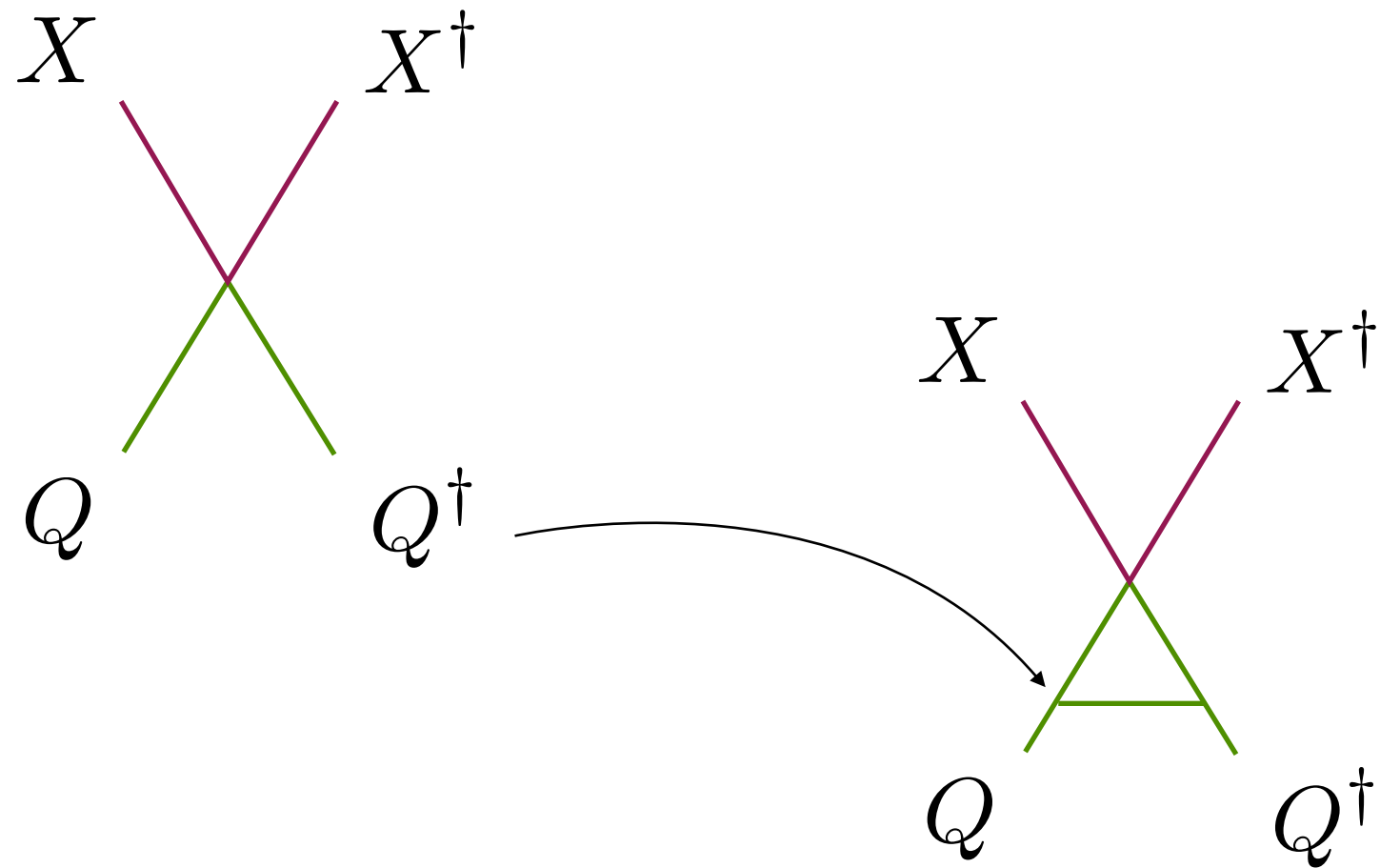
RGE of the operator





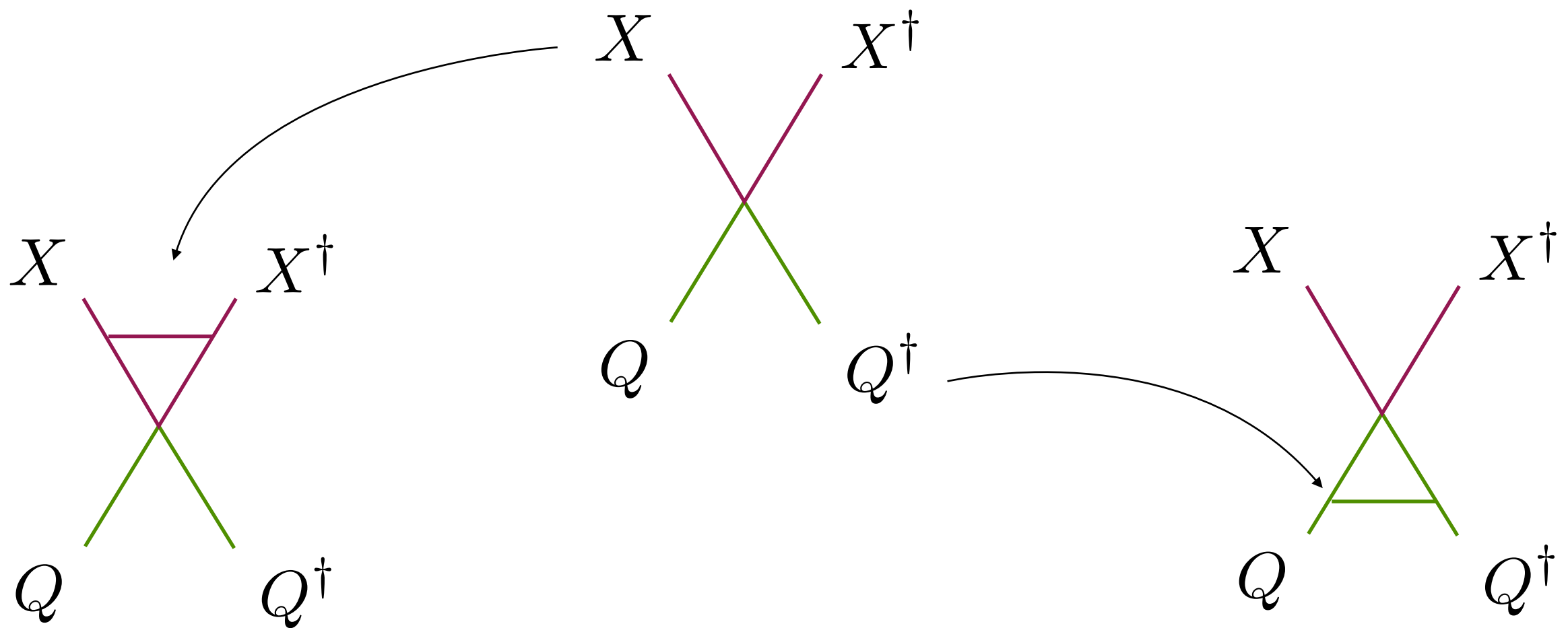
# RGEs of SUSY breaking masses

## RGE of the operator



# RGEs of SUSY breaking masses

## RGE of the operator



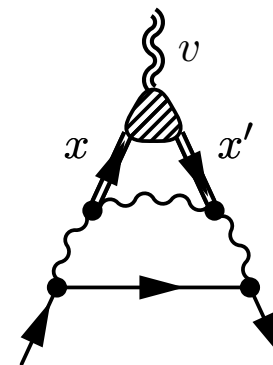
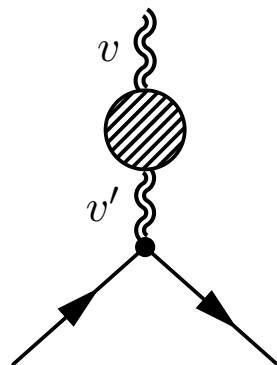
# *RGEs of SUSY breaking masses*

Cohen, Roy, Schmaltz

## A general hidden sector

Operators: 
$$\int d^4\theta \, k_{vi} \frac{V_v}{M^2} \Phi_i^\dagger \Phi_i + \int d^2\theta \, w_{xn} \frac{X_x}{M} W_n W_n$$

Diagrams:



RGEs


$$\frac{d}{dt} k_i = \gamma k_i - \frac{1}{16\pi^2} \sum_n 8 C_2^n(R_i) g_n^6 G_n$$

# RGEs of SUSY breaking masses

with MSSM interactions only

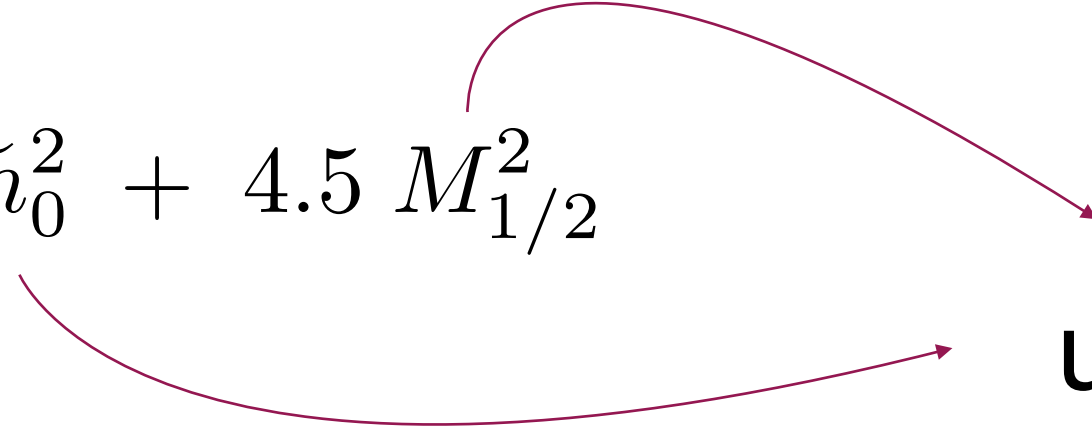
$$\frac{d}{dt} \tilde{m}_Q^2 = \frac{1}{16\pi^2} \sum_{a=1}^3 q_a g_a^2 M_a^2$$

$q_a \equiv \left\{ \frac{32}{3}, 6, \frac{2}{5} \right\}$



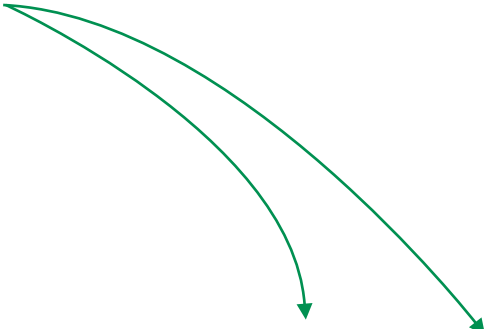
$$\tilde{m}_Q^2 = \tilde{m}_0^2 + 4.5 M_{1/2}^2$$

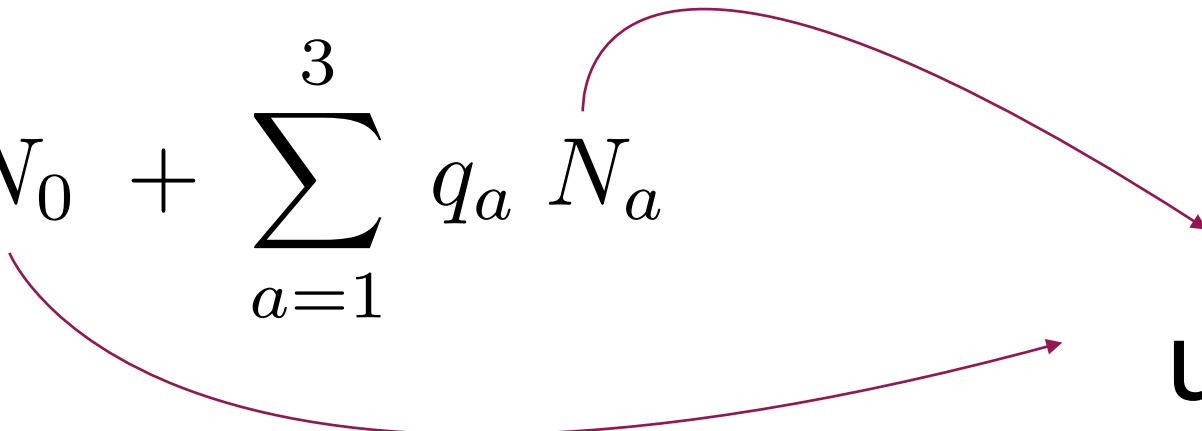
**2**  
**unknowns**



# RGEs of SUSY breaking masses

with MSSM + hidden interactions

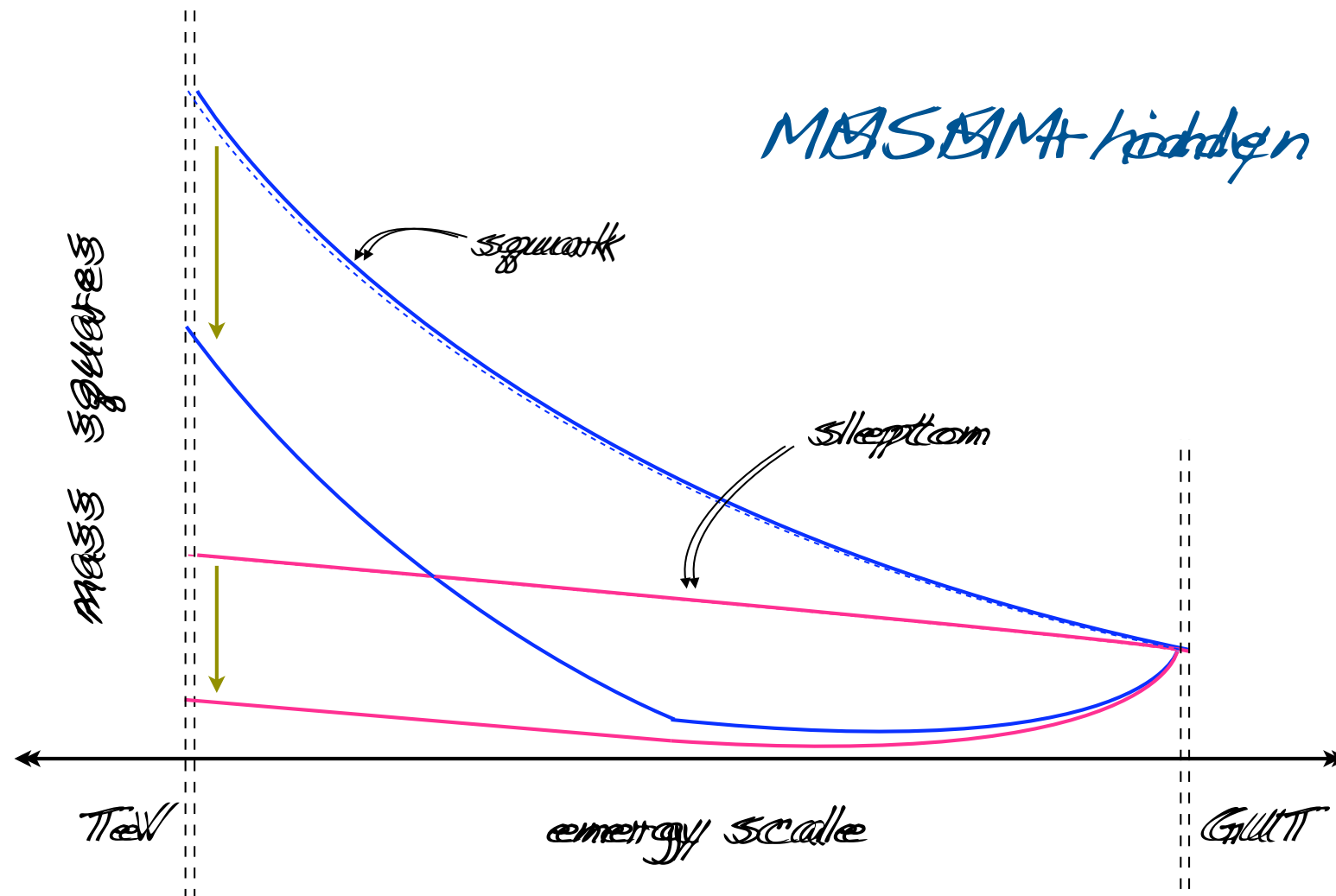
$$\frac{d}{dt} \tilde{m}_Q^2 = \frac{1}{16\pi^2} \sum_{a=1}^3 q_a g_a^2 M_a^2 G + \gamma \tilde{m}_Q^2$$


$$\tilde{m}_Q^2 = N_0 + \sum_{a=1}^3 q_a N_a$$


4

unknowns

# RGEs of SUSY breaking masses



# Hidden sector independent predictions

$$m_{\tilde{Q}}^2 - 2m_{\tilde{U}}^2 + m_{\tilde{D}}^2 - m_{\tilde{L}}^2 + m_{\tilde{E}}^2 = 0$$

holds for  
unification, MSUGRA,  
gauge mediation, gaugino mediation

# Hidden sector independent predictions

$$3 \left( \tilde{m}_U^2 - \tilde{m}_D^2 \right) + \tilde{m}_E^2 = 0$$

holds for  
gauge mediation, gaugino mediation



# Hidden sector independent predictions

all flavor universal models

e.g. MSUGRA, gauge/gaugino mediation

$$2\tilde{m}_{Q_3}^2 - \tilde{m}_{U_3}^2 - \tilde{m}_{D_3}^2 = 2\tilde{m}_{Q_1}^2 - \tilde{m}_{U_1}^2 - \tilde{m}_{D_1}^2$$

# Hidden sector independent predictions

all flavor universal models

e.g. MSUGRA, gauge/gaugino mediation

$$2\tilde{m}_{L_3}^2 - \tilde{m}_{E_3}^2 = 2\tilde{m}_{L_1}^2 - \tilde{m}_{E_1}^2$$

# Hidden sector independent predictions

all flavor universal models

e.g. MSUGRA, gauge/gaugino mediation

$$2\tilde{m}_{L_3}^2 - \tilde{m}_{E_3}^2 \neq 2\tilde{m}_{L_1}^2 - \tilde{m}_{E_1}^2$$

right handed neutrinos  
with large Yukawa coupling

# Hidden sector independent predictions

all flavor universal models

e.g. MSUGRA, gauge/gaugino mediation

$$2\tilde{m}_{Q_3}^2 - \tilde{m}_{U_3}^2 = 2\tilde{m}_{Q_1}^2 - \tilde{m}_{U_1}^2$$

$$\tilde{m}_{E_3}^2 = \tilde{m}_{E_1}^2$$

# Hidden sector independent predictions

all flavor universal models

e.g. MSUGRA, gauge/gaugino mediation

$$2\tilde{m}_{Q_3}^2 - \tilde{m}_{U_3}^2 \neq 2\tilde{m}_{Q_1}^2 - \tilde{m}_{U_1}^2$$

$$\tilde{m}_{E_3}^2 \neq \tilde{m}_{E_1}^2$$

large  $\tan \beta$

# Hidden sector independent predictions

all flavor universal models

e.g. MSUGRA, gauge/gaugino mediation

$$3\tilde{m}_{D_3}^2 + \tilde{m}_{E_3}^2 - 2m_{\bar{H}}^2 = 3\tilde{m}_{D_1}^2 + \tilde{m}_{E_1}^2 - 2\tilde{m}_{L_1}^2$$

$$3\tilde{m}_{U_3}^2 - 3\tilde{m}_{D_3}^2 + 2\tilde{m}_{L_3}^2 - 2\tilde{m}_{E_3}^2 + 2m_{\bar{H}}^2 = 3\tilde{m}_{U_1}^2 - 3\tilde{m}_{D_1}^2 + 2\tilde{m}_{L_1}^2 - 2\tilde{m}_{E_1}^2 + 2m_H^2$$

# Hidden sector independent predictions

all flavor universal models

e.g. MSUGRA, gauge/gaugino mediation

$$3\tilde{m}_{D_3}^2 + \tilde{m}_{E_3}^2 - 2m_{\bar{H}}^2 \neq 3\tilde{m}_{D_1}^2 + \tilde{m}_{E_1}^2 - 2\tilde{m}_{L_1}^2$$

$$3\tilde{m}_{U_3}^2 - 3\tilde{m}_{D_3}^2 + 2\tilde{m}_{L_3}^2 - 2\tilde{m}_{E_3}^2 + 2m_{\bar{H}}^2 \neq 3\tilde{m}_{U_1}^2 - 3\tilde{m}_{D_1}^2 + 2\tilde{m}_{L_1}^2 - 2\tilde{m}_{E_1}^2 + 2m_H^2$$

$\mu$  term is not fundamental

# Hidden sector independent predictions

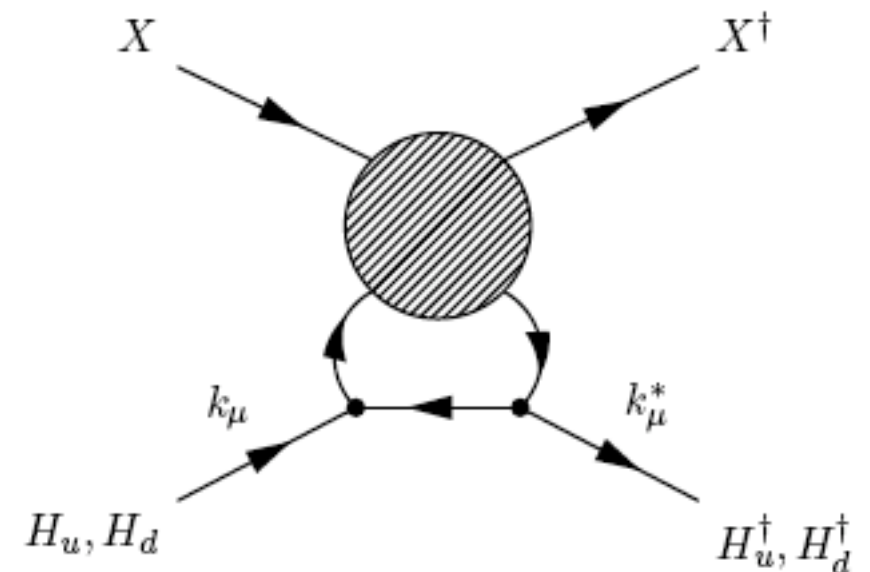
all flavor universal models

e.g. MSUGRA, gauge/gaugino mediation

$$3\tilde{m}_{D_3}^2 + \tilde{m}_{E_3}^2 - 2m_{\bar{H}}^2 \neq 3\tilde{m}_{D_1}^2 + \tilde{m}_{E_1}^2 - 2\tilde{m}_{L_1}^2$$

$$3\tilde{m}_{U_3}^2 - 3\tilde{m}_{D_3}^2 + 2\tilde{m}_{L_3}^2 - 2\tilde{m}_{E_3}^2 + 2m_{\bar{H}}^2 \neq 3\tilde{m}_{U_1}^2 -$$

$\mu$  term is not funda





# Example of DSB

$$W = \lambda S^{ij} Q_i Q_j$$

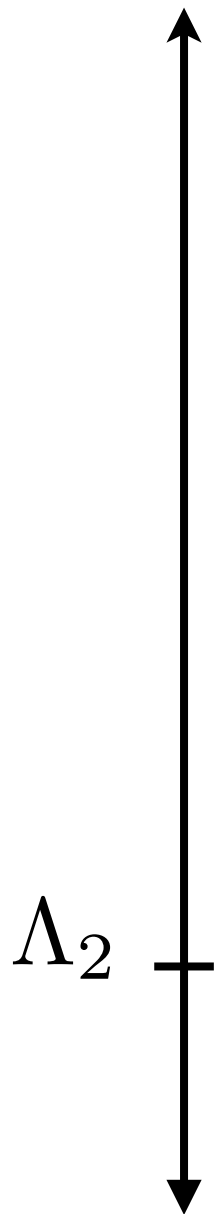
$$\frac{\partial W}{\partial S^{ij}} = \lambda Q_i Q_j$$

$$\text{Pf}(QQ) = \Lambda_2^4$$

	SU(2)	SU(4)
$Q$	$\square$	$\square$
$S$	1	$\boxplus$

Take the limit of large field value ( $\lambda S$ )

$$W_{\text{eff}} = 2 \Lambda_2^2 \lambda S$$



# *Example of DSB*

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We can provide many more examples of DSB

all share the same feature

there is no elementary singlet field in the UV

gaugino masses are naturally suppressed wrt scalar masses

# Example of DSB

SU(4) X U(1)

$X_1$	$\square$	-3
$X_2$	$\bar{\square}$	-1
$X_3$	$\boxplus$	2
$X_4$	1	4

(Dine, Nelson, Nir, Shirman, '95)

$$g_4 \gg \lambda \gg g_1$$

$$W = \lambda X_1 X_2 X_4$$



$$W_{np} = \frac{\Lambda_4^5}{X_1 X_2 X_3^2}$$

susy breaking vev at

$$D_1 = 1.4 F_{X_4} \neq 0$$

# Superpartner masses from $\mathcal{D}$ -term

$$\mathbf{W}_{\text{eff}} \supset w_a \frac{X}{M_{\text{Pl}}} W_a W_a + \sqrt{2} \Omega_a \frac{W'}{M_{\text{Pl}}} W_a \Phi_a$$



majorana  
mass



Dirac  
mass

# Superpartner masses from D-term

$$\mathbf{W}_{\text{eff}} \supset w_a \frac{X}{M_{\text{Pl}}} W_a W_a + \sqrt{2} \Omega_a \frac{W'}{M_{\text{Pl}}} W_a \Phi_a$$

Dirac mass

These interactions preserve an

$U(1)_R$

$$\begin{aligned} R[Q_i] &= 1 \\ R[W_a] &= 1 \\ R[\Phi_a] &= 0 \end{aligned}$$

# Dirac Gaugino Masses

gaugino  
contribution to  
scalar masses

$$\int d^4\theta \frac{1}{\Lambda^6} |W'W'|^2 Q^\dagger Q$$

gaugino  
mass

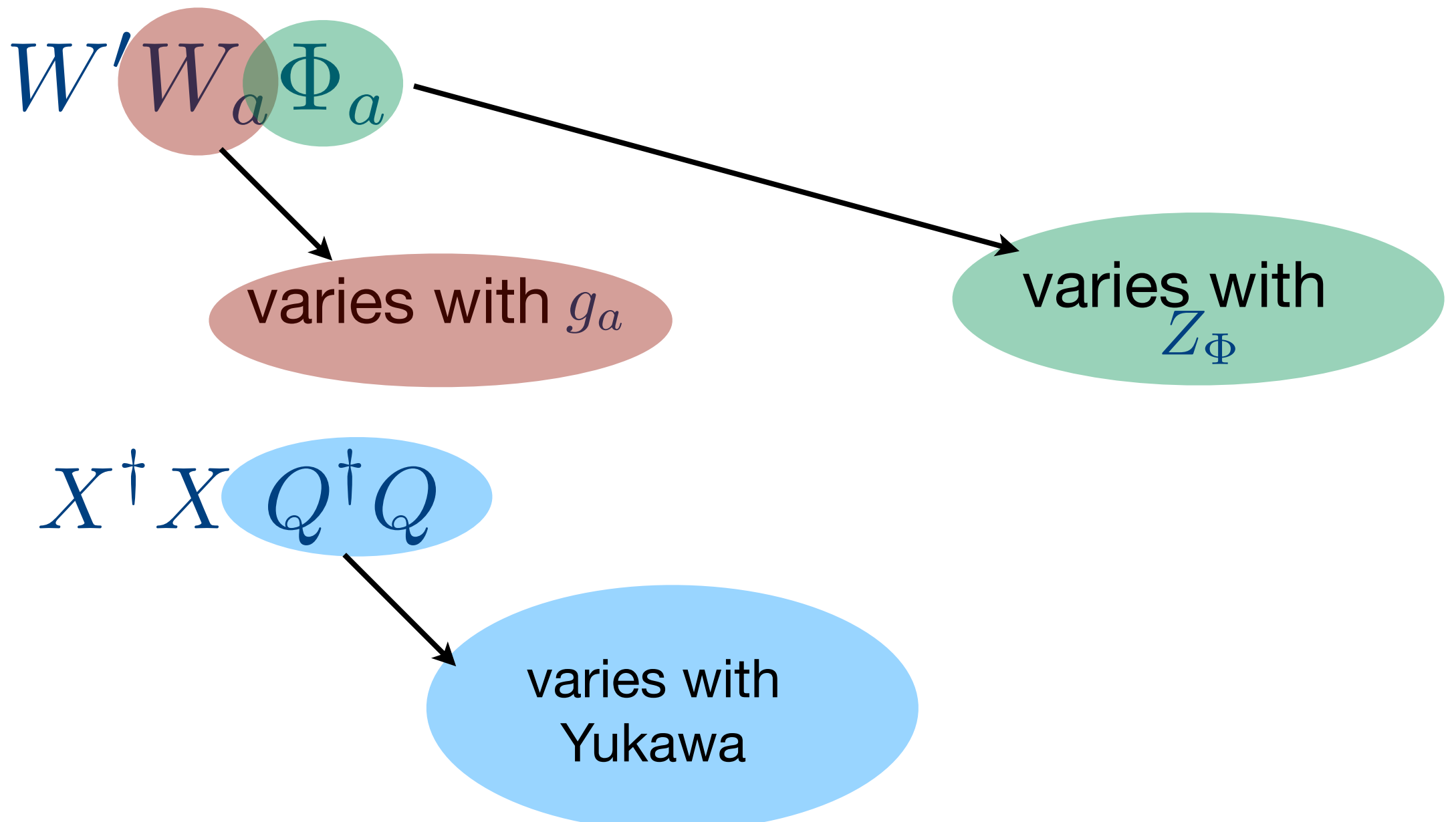
$$\frac{M^4}{\Lambda^2} \tilde{Q}^\dagger \tilde{Q}$$

extra  
suppression

no counterterm is needed and hence Dirac  
gauginos induce **finite** contributions to the scalars

*A sample point*

RGE evolution



# *A sample point*

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TeV scale outputs

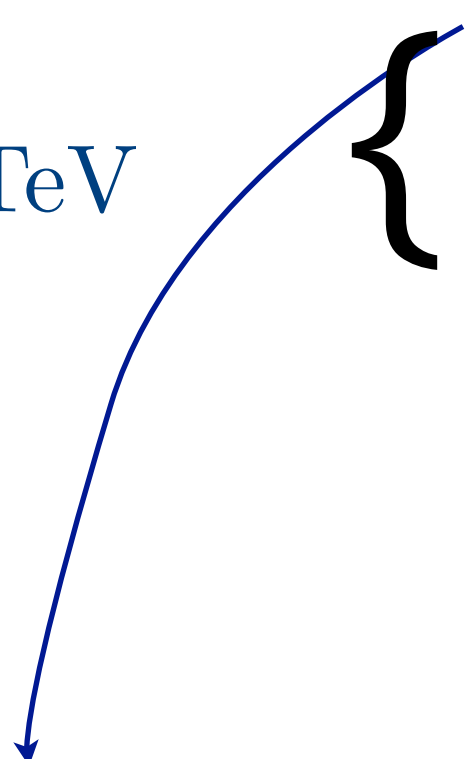
$$M_a(M_{\text{Pl}}) = 1 \text{ TeV} \quad \left\{ \begin{array}{lll} M_3(\text{TeV}) & \sim & 5.4 \text{ TeV} \\ M_2(\text{TeV}) & \sim & 1 \text{ TeV} \\ M_1(\text{TeV}) & \sim & 600 \text{ GeV} \end{array} \right.$$



# *A sample point*

TeV scale outputs

$$M_a(M_{\text{Pl}}) = 1 \text{ TeV}$$



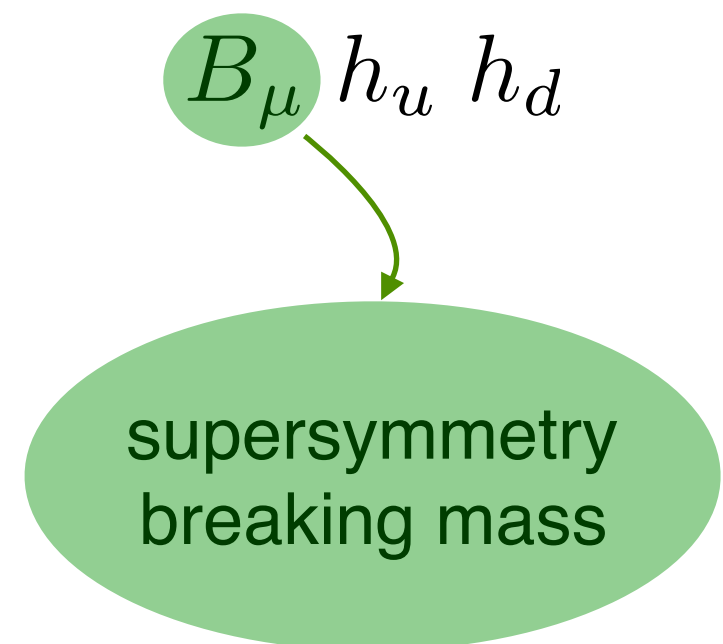
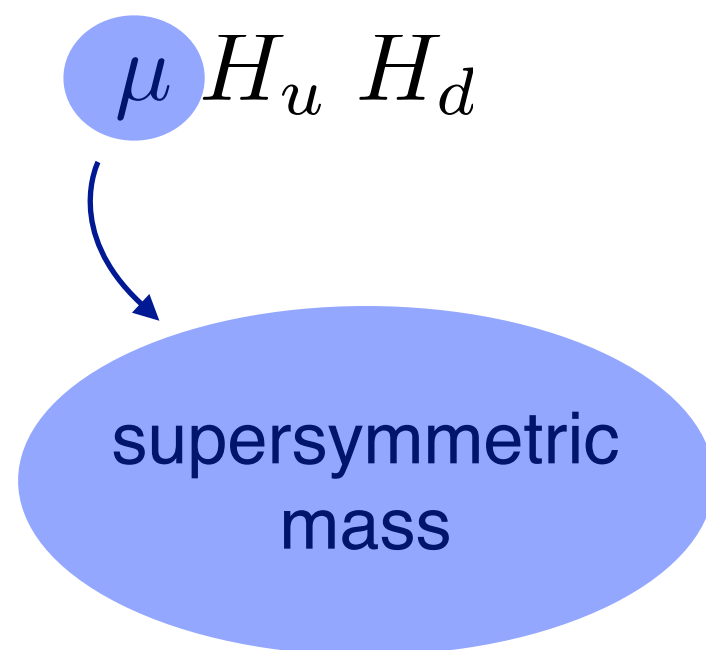
$M_3(\text{TeV})$	$\sim$	5.4 TeV
$M_2(\text{TeV})$	$\sim$	1 TeV
$M_1(\text{TeV})$	$\sim$	600 GeV

$$m_{\tilde{q}}^2(\text{TeV}) \sim (1.3 \text{ TeV})^2 \times \text{flavor diagonal}$$

# *A deep problem in the Higgs sector*


$$H_u \equiv H_u(h_u, \psi_{H_u}, F_{H_u})$$

$$H_d \equiv H_d(h_d, \psi_{H_d}, F_{H_d})$$



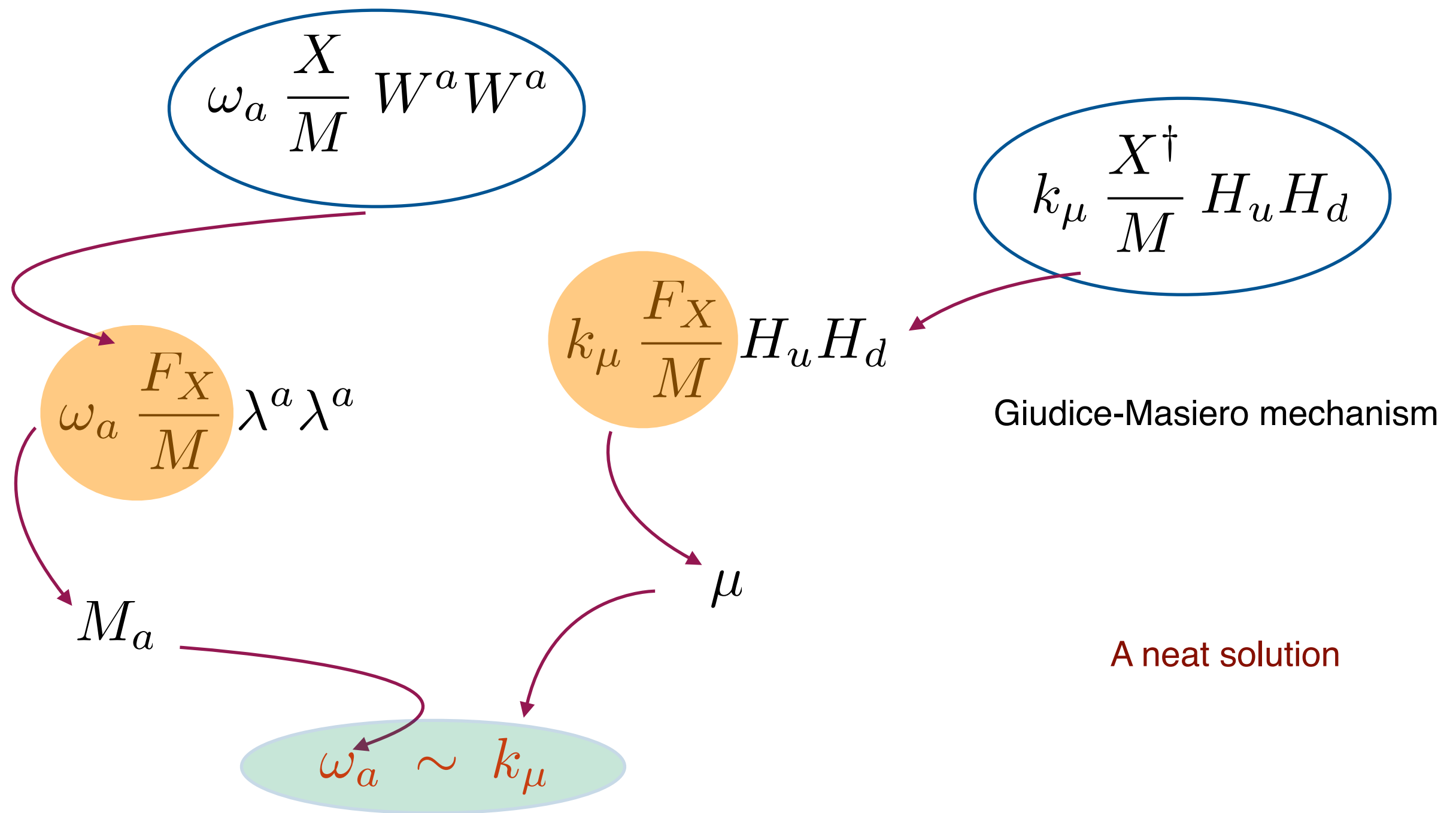
# *A deep problem in the Higgs sector*

Natural electroweak  
symmetry breaking  
requires

$$\begin{aligned}\mu &\sim M_a \\ B_\mu &\sim |\mu|^2\end{aligned}$$


μ problem

# A deep problem in the Higgs sector



# *A deep problem in the Higgs sector*

Nelson-Roy

We need a slightly more complicated operator  
for D-term susy breaking

Operator: 
$$\int d^2\theta \frac{1}{4} w_{2,\Phi_1,\Phi_2} \frac{\bar{D}^2 (D^\alpha V' D_\alpha \Phi_1)}{M_m} \Phi_2.$$

$$\frac{\mu_{\Phi_2}}{2} (\tilde{\phi}_1 \tilde{\phi}_2 - 2F_{\phi_1} \phi_2) \rightarrow \frac{\mu_{\phi_2}}{2} \tilde{\phi}_1 \tilde{\phi}_2 + |\mu_{\phi_2}|^2 |\phi_2|^2,$$

where

$$\mu_{\phi_2} = 2w_{2,\Phi_1,\Phi_2} \frac{\mathcal{D}}{M_m}.$$

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Let's not conclude — since another SUSY talk is approaching