

THE FLUID DYNAMICS OF CUMULUS CLOUDS

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THE GRAND CHALLENGE IN ATMOSPHERIC SCIENCE

CLIMATE SCIENCE

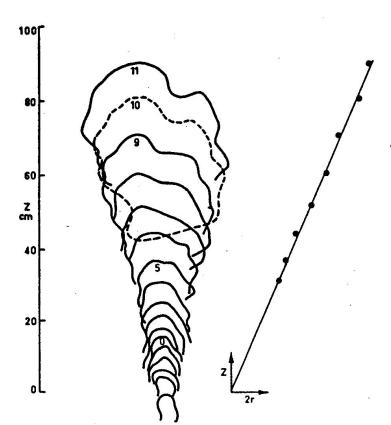
Physicists, your planet needs you

Climatologists highlight cloud mysteries in an attempt to lure physicists to their field.

BY QUIRIN SCHIERMEIER



MODELLING CLOUDS



... large convective clouds ... which are not adequately described by similarity theory but for which there is at present no alternative model.

J S Turner 1973 Buoyancy Effects in Fluids



BOTANIZING CLOUD TYPES

♦ WMO (1956):

Cloud: A visible aggregate of minute particles of water or ice, or both, in the free air

Luke Howard 1772-1864: 10 genera

Cumulus¹ Cumulo-nimbus Fog added later as 11th Stratus² Stratocumulus genus.

Nimbo-stratus Altostratus

Altocumulus Cirrus³

Cirrostratus Cirrocumulus

Nimbo: rain-bearing Alto: high

¹3D; heap ²2D, sheet ³1D, filament

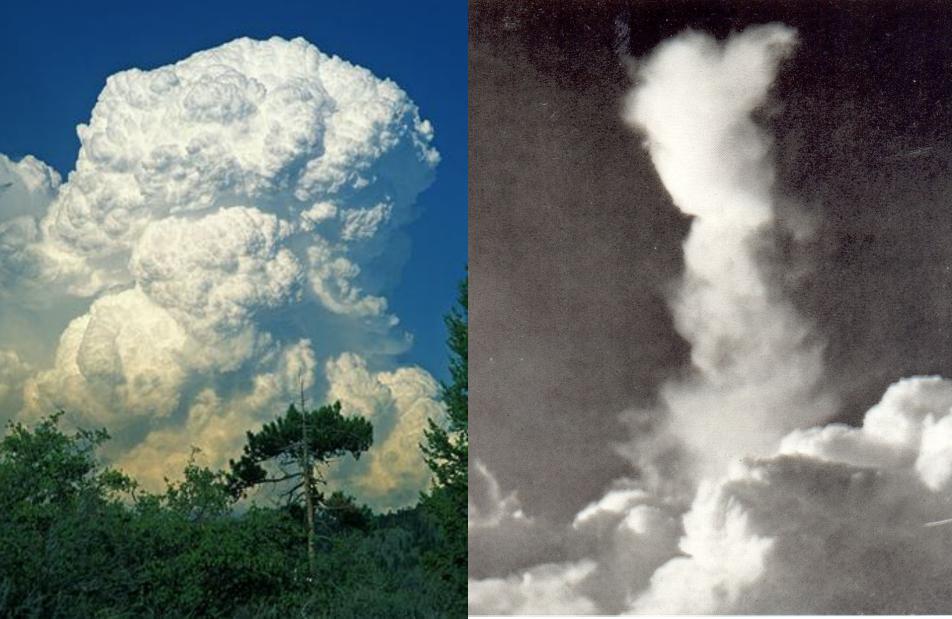
 $\# \rightarrow 3$ etages $\rightarrow 26$ species $\rightarrow 31$ varieties

Marker becomes Player in 1950s: (contra David Brunt 1941)





CUMULUS SHAPES: FLUFFY BALLS, OR SHOOTING PLUMES?...





BACKGROUND 1

- Clouds are complex flows involving multiple phases, thermodynamics, microphysics, radiation . . . ? ?
- A central problem in the fluid dynamics of clouds concerns their entrainment characteristics; entrainment is also the dynamic behind shape
- Taylor's entrainment hypothesis (1945) for free turbulent shear flows (Morton, Taylor, Turner 1956): entrainment velocity V_e ∝ characteristic mean velocity U_c Later refinements: replace U_c by u'_c, (u' w ')^{1/2} etc.

Plume

Often works well (Turner 1973, 1986 JFM)



BACKGROUND 2

- Does not work for cumulus clouds which are not fans or cones, but heaps and the hot cumulus towers of Riehl (58).
- Telford (1975):

 Liquid water content remarkably constant across cloud, decreases monotonically from cloud base
 "The problem of explaining infinite horizontal diffusion and zero vertical diffusion"
- Or (from present work on momentum) the other way round?
- Emanuel (1994): "Early cloud parameterization schemes based on the similarity plume model . . . [were] thoroughly discredited by observations".

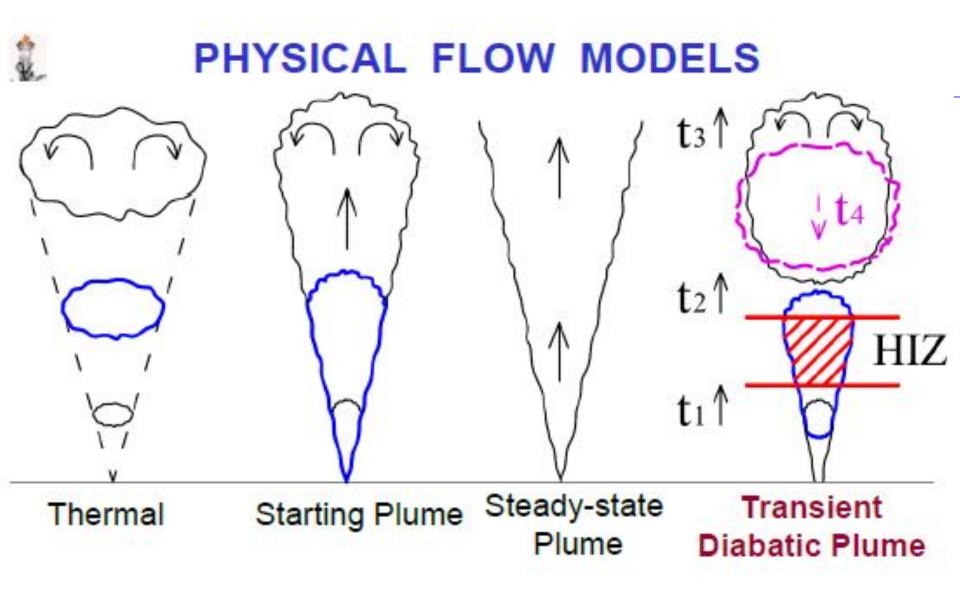


CUMULUS CLOUDS

can be

shallow / deep fluffy / smooth boiling / fading loners /crowded chaotic / ordered

BUT THEY ARW ALL FLOW CLOUDS

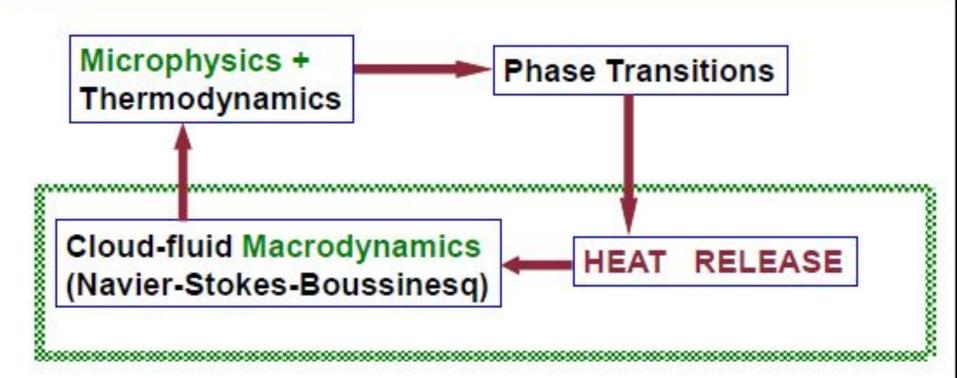


Turner's proposals

RN ++ 2011 *PNAS*



FIRST ORDER NON-PRECIPITATING CUMULUS SYSTEM





EQUATIONS FOR A 'BOUSSINESQ CLOUD'

$$\nabla \cdot u = 0,$$
 (mass)

$$\frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla)\mathbf{u} = -\frac{1}{\rho} \nabla p + v \nabla^2 \mathbf{u} - \mathbf{g} \alpha T,$$
(momentum)

$$\frac{\partial T}{\partial t} + (\mathbf{u} \cdot \nabla)T = \kappa \nabla^2 T + \frac{J}{\rho c_p} H$$
(energy)

Basu, RN 1999 J. Fluid Mech.



VORTICITY IN BOUSSINESQ CLOUD

$$\frac{\partial \boldsymbol{\omega}}{\partial t} + (\boldsymbol{u} \cdot \nabla)\boldsymbol{\omega} - (\boldsymbol{\omega} \cdot \nabla)\boldsymbol{u} - \boldsymbol{v}\nabla^2\boldsymbol{\omega} = \alpha \boldsymbol{g} \times \nabla T$$
advect tilt, stretch diffuse create

$$u(x,t) = u(x + Le_i,t), \quad p(x,t) = p(x + Le_i,t),$$

 $T(x,t) = T(x + Le_i,t), \quad i = 1,2,3.$



NON-DIMENSIONAL (GLOBAL) HEAT RELEASE PARAMETER

$$G \sim \frac{g\beta}{\rho_o C_p} \frac{Q}{bU^3}$$
 (global)

 β : thermal coefficient of expansion of the cloud fluid (1/K)

g: acceleration due to gravity (m/s²)

 ρ and C_{ρ} : density (kg/m3) and specific heat (J/kg K) at constant pressure of the ambient fluid

Q: total off-source heating rate (W)

b and U: length and velocity scales (m and m/s)

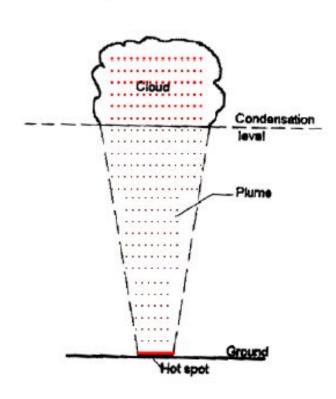
Heat release in general varies in space and time, so define a 'local' heat release number

$$G'(\mathbf{x},t) = \frac{g\beta}{\rho_o C_n} \frac{b^2}{U^3} J(\mathbf{x},t)$$



Simulation of cumulus clouds in laboratory

Principle



Physical model:

Transient turbulent plume/jet of a single-phase 'cloud fluid', with off-source addition of heat to simulate latent heat release due to condensation in natural cumulus clouds

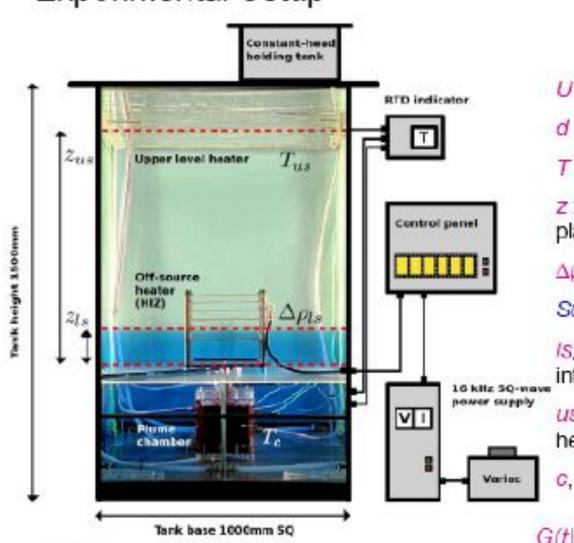
- We work with water, not moist air.
- Shape primarily determined by largescale entrainment processes.

Recent work shows (Narasimha et al., PNAS, 2011) "Clouds are transient diabatic plumes"



EXPERIMENTAL SETUP

Experimental Setup



RTD: Resistance Temperature Detector

 $Re = \frac{Ud}{v}$

U: nozzle-exit velocity

d: nozzle diameter

T: Averaged temperature

z : Height measured from plane of nozzle exit

Δp : Density difference;

Subscripts:

Is, lower density stratification interface (dash-dot lines);

us, plane of free-surface heater;

c, chamber exit.

G(t) and G(z) possible to obtain



Dynamical similarity: Cloud-like flows in a water tank

Heat release into the cloud fluid:

~ 1 W/m3 in the atmosphere

What matters: The ratio G

~ (Heat release) / (Energy flux)

- To get same value of G in a water tank as in clouds, we need heat release of O(1 kW) in 5 cm x 5 cm x 10 cm = 250 cm³ = 250 x 10⁻⁶ m³.
- This idea forms the basis for design of the off-source heating mechanism.



Dynamical similarity: Cloud-like flows in a water tank

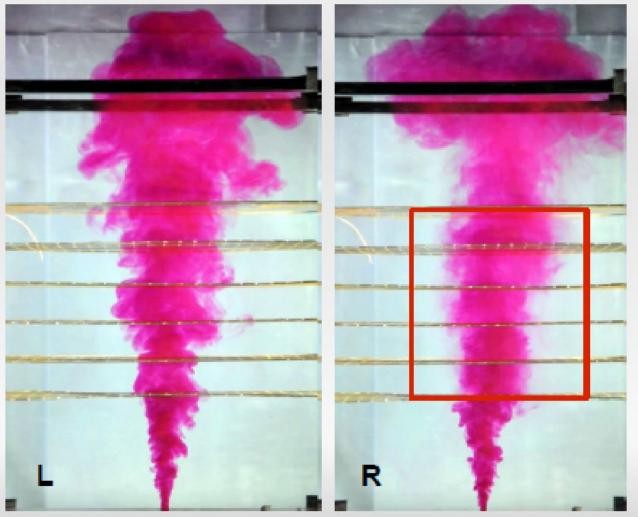
Flow	Width b (m)	Centre-line velocity U (m/s)	$\mathbf{G'} = \frac{\alpha g}{\rho c_p} \frac{Q}{b_b U_b^3}$
Cumulus	500	3 - 4	0.11 - 0.53
Cumulonimbus	1200 - 2500	10 - 25	0.14 - 0.46
Jet/Plume d = 4 mm, z/d = 50, Q = 600 W	21 x 10 ⁻³	38 x 10 ⁻³	0.25

Venkatakrishnan et al. - 1998 Current Science

Re in the experiments is much lower, but jets and plumes are relatively insensitive to Re, for $Re > 10^3 - 10^4$

Y.

Whole-field visualisation: Temporal evolution of a starting plume



- Re = 1900
- Exit velocity at nozzle = 0.28 m/s
- ΔT = 25° C (heating chamber)
- L) Q = 0, G = 0
- R) Q = 800 WG = 8.18

Heat injection zone



Classification as per the International Cloud Atlas (WMO)

Based mainly on appearance

Three genera and three species simulated

Genera: Cumulus

Alto- / Strato- cumulus

Species: Congestus

Mediocris

Fractus

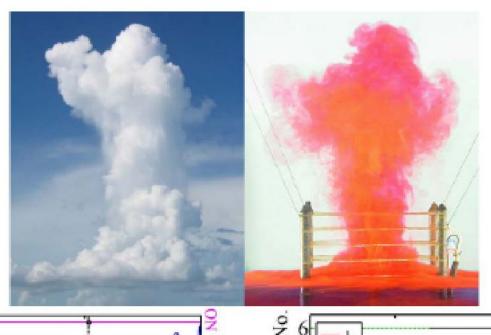


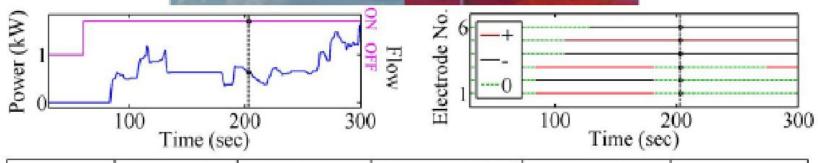
COMPARISON WITH REAL CLOUDS Towers and Flowers

Comparison

Cumulus Congestus

Tall, narrow, tower-like





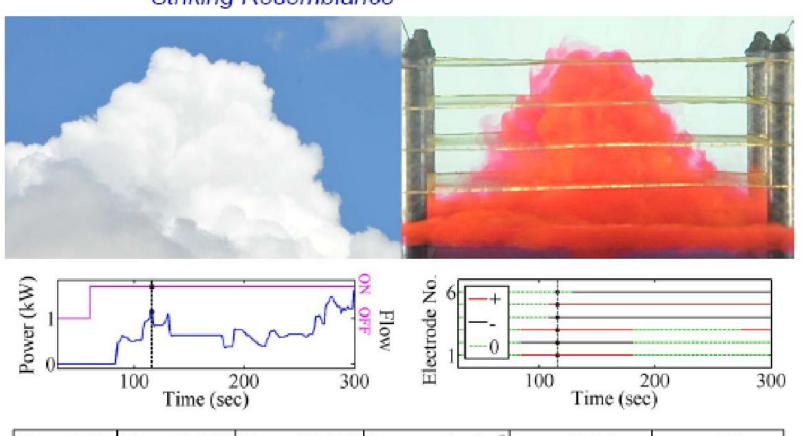
 $|Re \approx 3000|T_c = 30.8^{\circ} \text{C}|T_{us} = 33.9^{\circ} \text{C}|\Delta \rho_{ls} \approx 1 \text{kg/m}^3|z_{ls} = 126.5 \text{mm}|z_{us} = 869 \text{mm}|$



Comparison

Cumulus Congestus

Striking Resemblance



$$Re \approx 3000 | T_c = 30.8^{\circ} \text{C} | T_{us} = 33.9^{\circ} \text{C} | \Delta \rho_{ls} \approx 1 \text{kg/m}^3 | z_{ls} = 126.5 \text{mm} | z_{us} = 869 \text{mm}$$

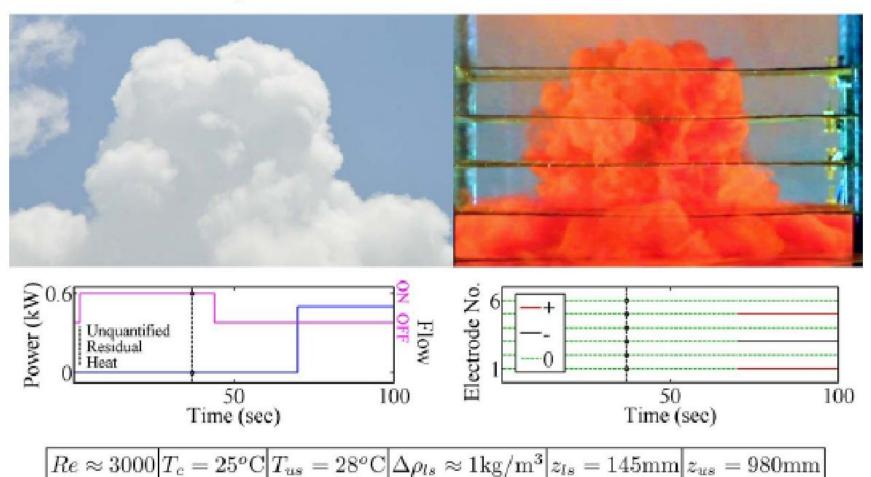
Fluffy, sharp edges, flower-like



Comparison

Cumulus Congestus

Different Shapes

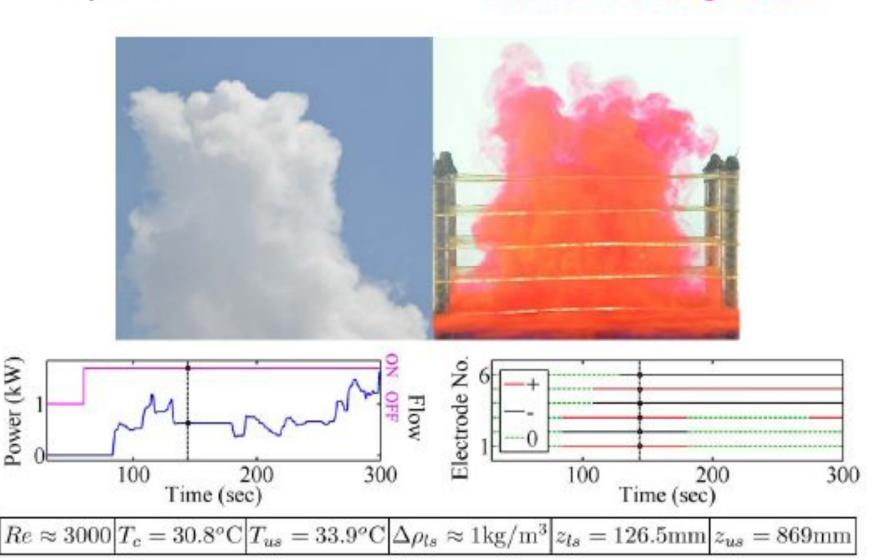


$$Re \approx 3000 T_c = 25^{\circ} C T_{us} = 28^{\circ} C \Delta \rho_{ls} \approx 1 \text{kg/m}^3 z_{ls} = 145 \text{mm} z_{us} = 980 \text{mm}$$



Comparison

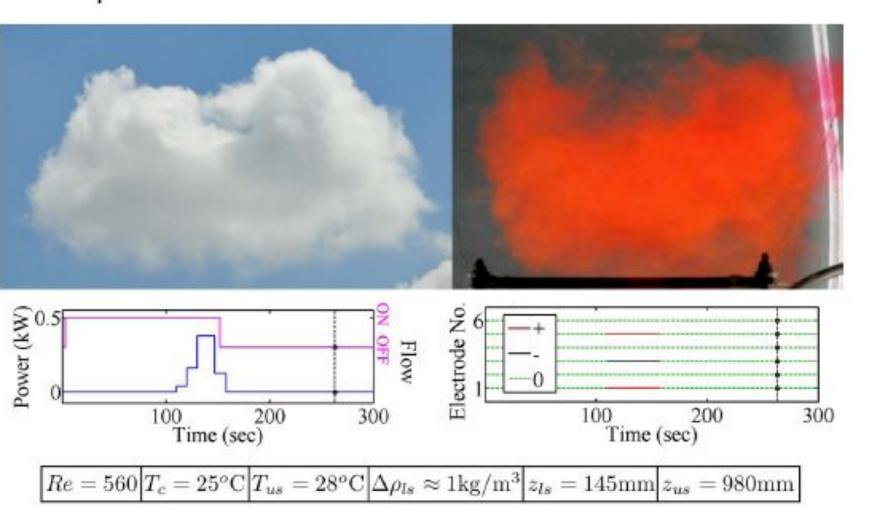
Cumulus Congestus





Comparison

Cumulus Mediocris

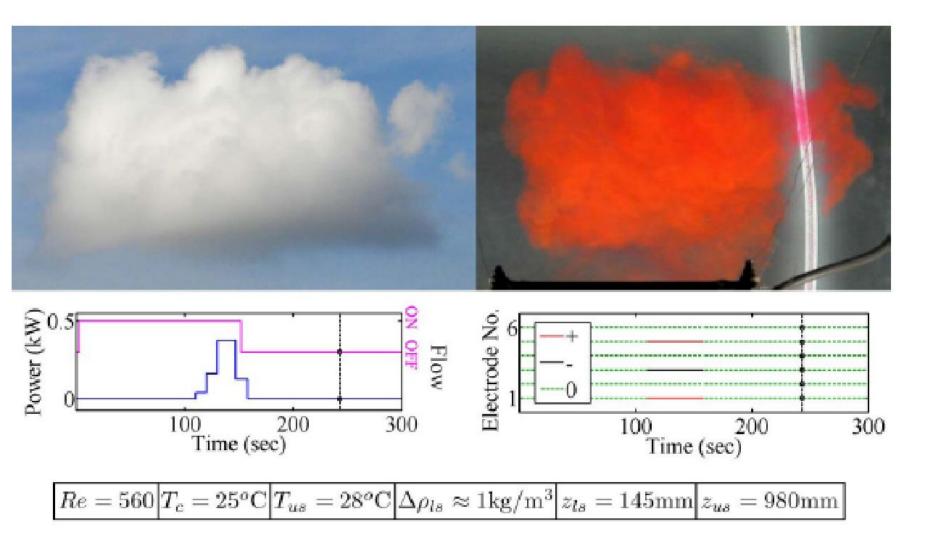


Hovering (slowly sinking), Evaporating



Comparison

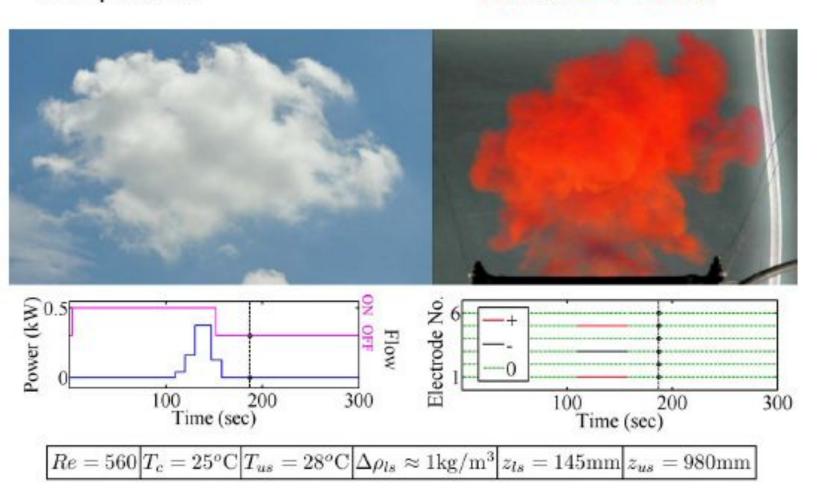
Cumulus Mediocris





Comparison

Cumulus Fractus

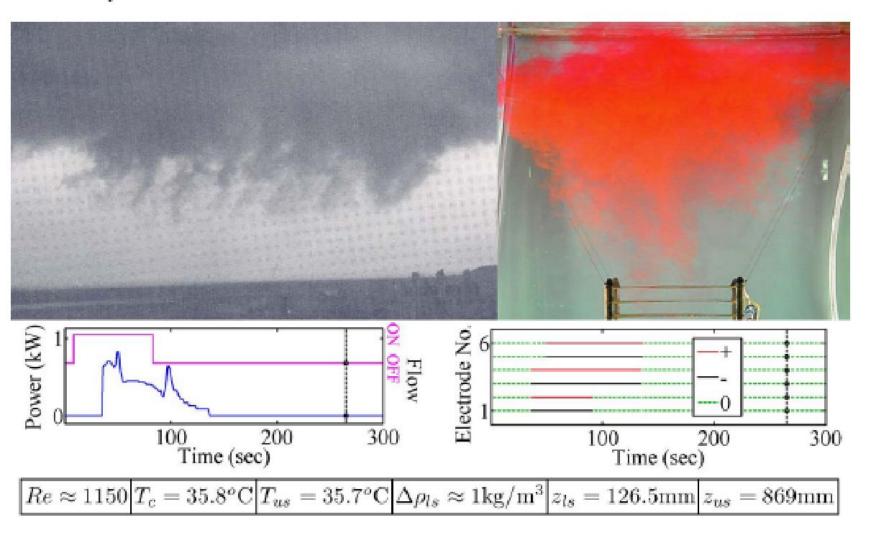


Jagged edges, dissolving stage



Comparison

Cumulus Fractus





- The important parameters identified
 - 1. Flow history
 - Heating profile history
 - Lower and upper stratification (heights and magnitudes)
 - 4. Source momentum / buoyancy flux
- Different combinations can give wide variety of cumulus shapes, types, flows

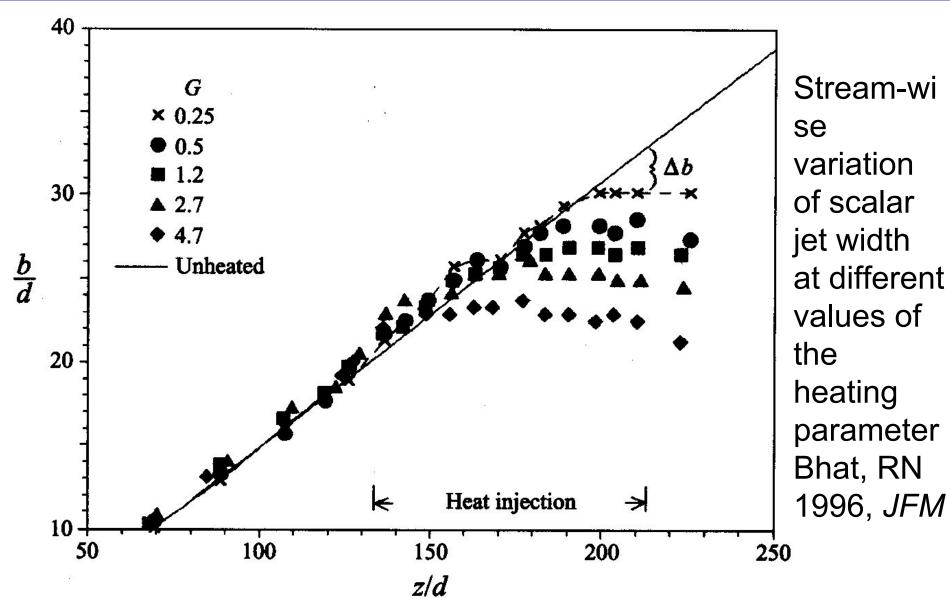


Measurements on a

Steady Diabatic Jet

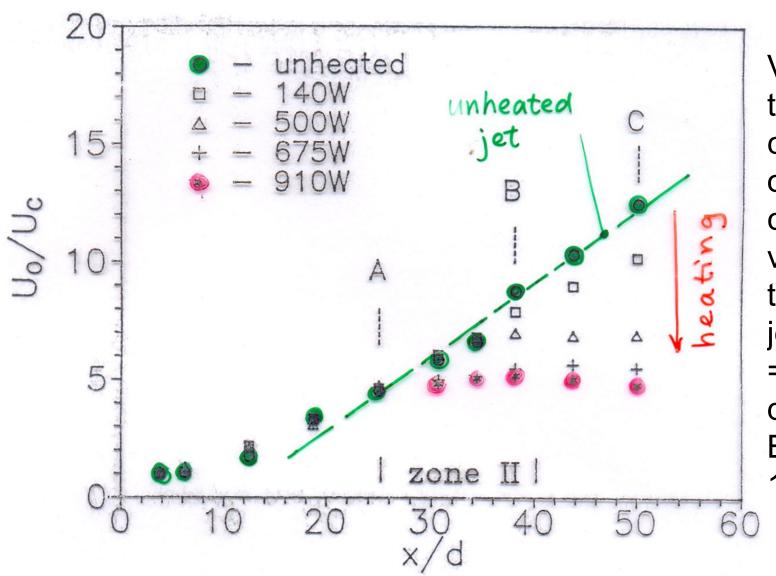


JET WIDTH





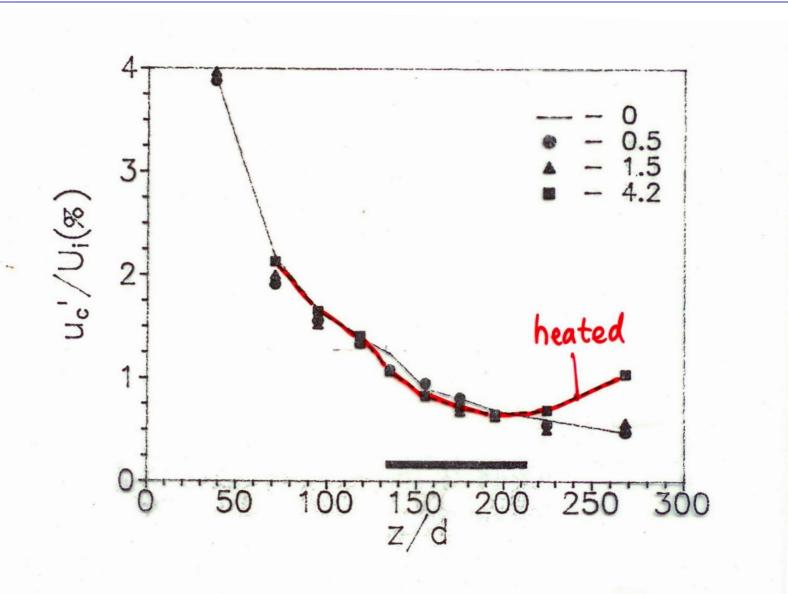
HEATING ACCELERATES FLOW



Variation of the axial component of the centreline velocity in the heated jet. Re =1480 and d = 8 mmBhat, RN 1996, *JFM*

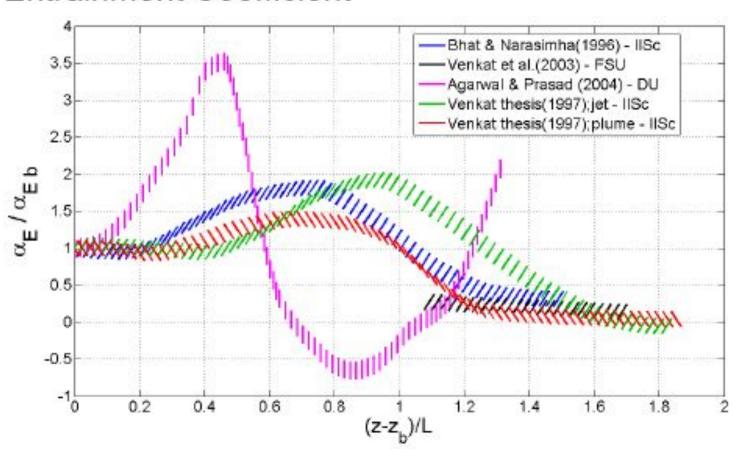


TURBULENCE IN CLOUD-FLOW





Entrainment Coefficient



$$\alpha_E = \frac{dm}{dz} / (2\pi b_u U_c)$$

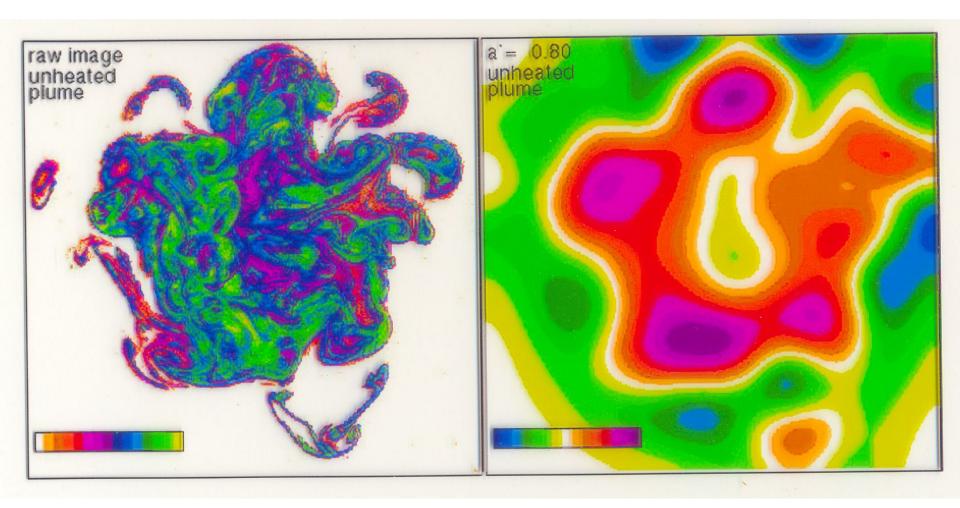
m: integrated mass flux, b_u : velocity width of the flow

Uc: mean centerline velocity

L: height of HIZ, Z_b: beginning of HIZ



WAVELETS REVEAL HIDDEN ORDER, ORDINARY PLUME

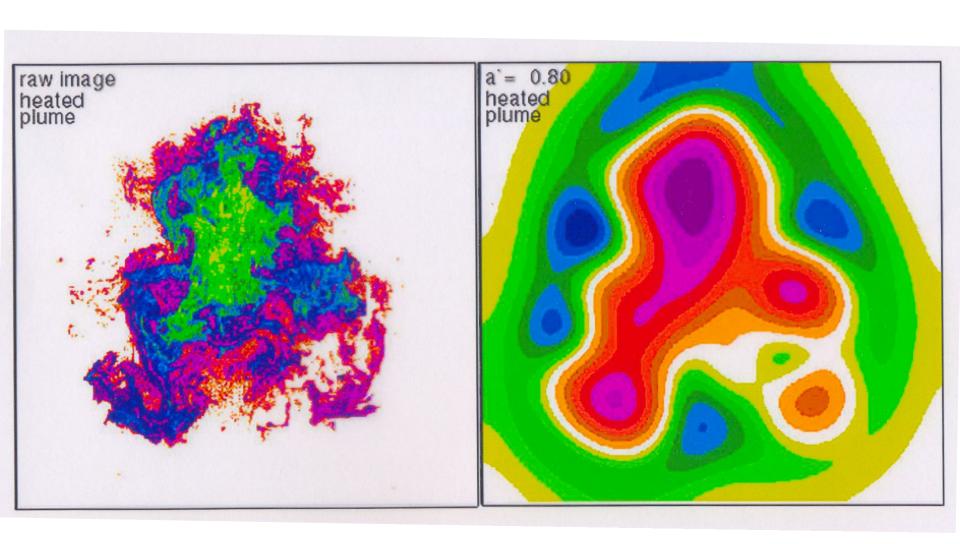


Turbulent chaos conceals lobed vortex ring?

Narasimha et al. 2002 Expts. Fl., Srinivas+ 2007 JoT



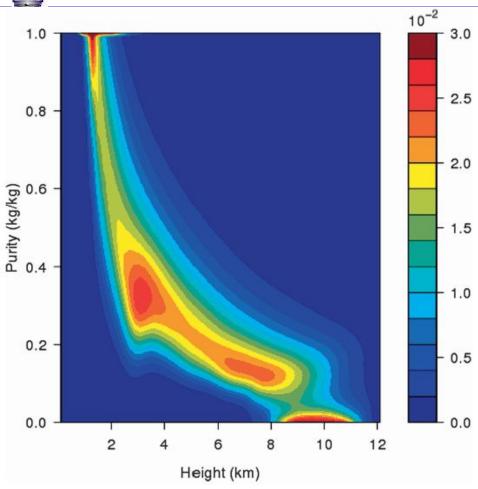
CLOUD PLUME: UNMIXED CORE

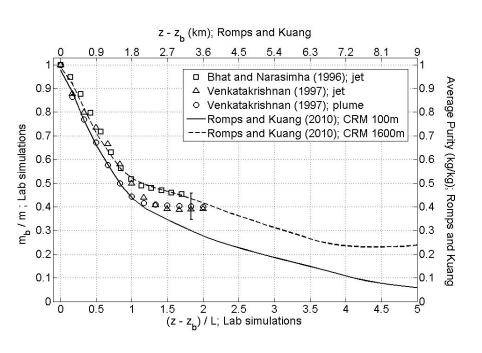


RN+ 2002 *Expts. Fl.*



DILUTION AND PURITY





Romps & Kuang 2010 JAS

Comparison with Lab results (RN+2011PNAS)



A MODEST PROPOSAL

A Cumulus Cloud Flow is a Special Example of a

TRANSIENT DIABATIC PLUME



CYBER CLOUDS 1 SPECTRAL METHODS

MEGHA 1

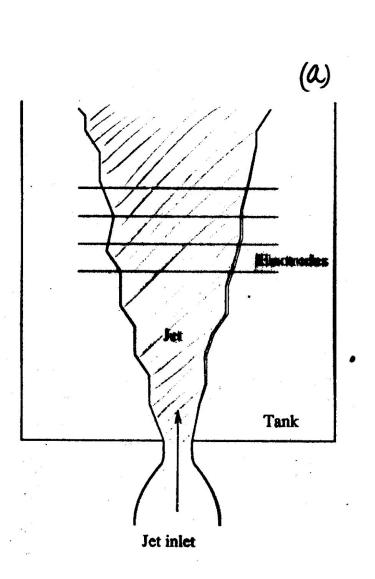
TRANSIENT DIABATIC JET

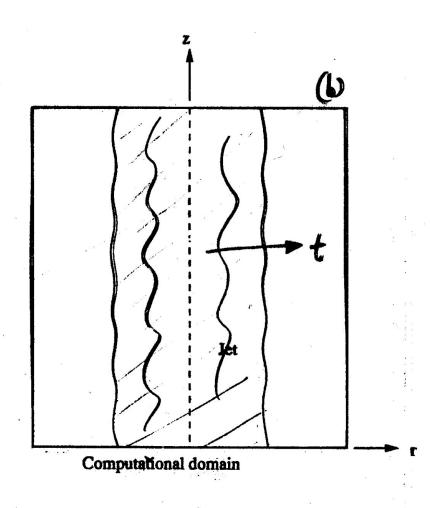


LABORATORY SETUP

VERSUS

TEMPORAL SIMULATION





Basu, Narasimha 1999, JFM



INITIAL AND BOUNDARY CONDITIONS

$$w = 1, \qquad \forall r \leq r_0 - \delta/2$$

$$= 0, \qquad \forall r \geq r_0 + \delta/2$$

$$= \frac{1}{2} \left(1 - \tanh \frac{r - r_0}{2\theta_0} \right), \quad \forall r_0 - \delta/2 < r < r_0 + \delta/2, \qquad (2.9)$$

where δ is the characteristic width of the shear layer. Here r_0 is the initial mean radius of the shear layer, θ_0 is the initial momentum thickness, and u_θ and u_r are assumed to be zero everywhere. We impose a small perturbation on this shear layer corresponding to an increment in u_r given by

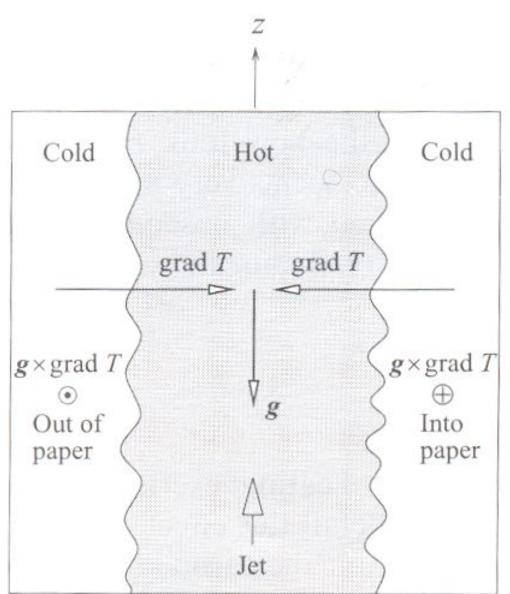
$$\Delta u_r = f(r) \left[\sum_i a_j \sin \left(\frac{2\pi z}{\lambda_j} + \varphi_j \right) + a_\theta \sum_i \sin (l\theta + s_l) \right], \tag{2.10}$$

with prescribed amplitudes a_j and a_{θ} , streamwise wavelength λ_j and phases ψ_j and s_l ; f(r) is the filtering function

$$f(r) = \exp\left[-2\left(\frac{r - r_0}{\delta}\right)^2\right],\tag{2.11}$$



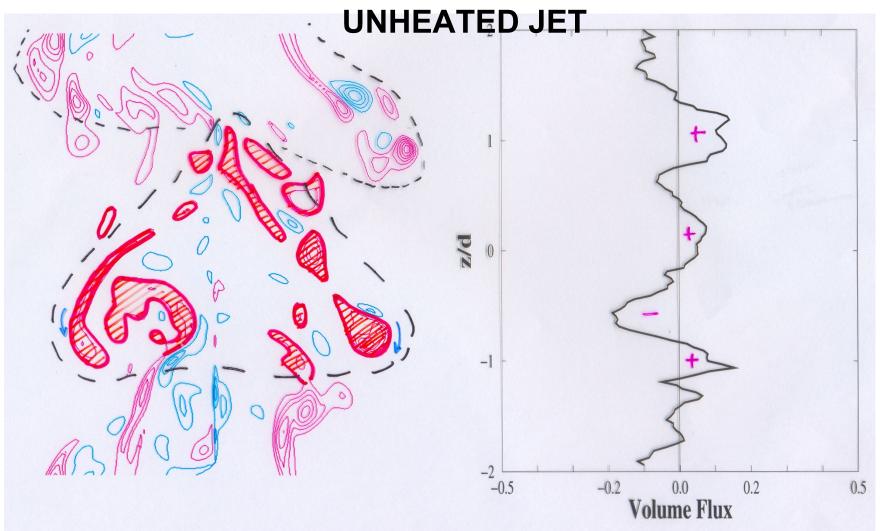
CREATING VORTICITY BY BAROCLINIC TORQUE



Basu, RN 1999 J. Fluid Mech.



COHRERENT STRUCTURE IN AZIMUTHAL VORTICITY



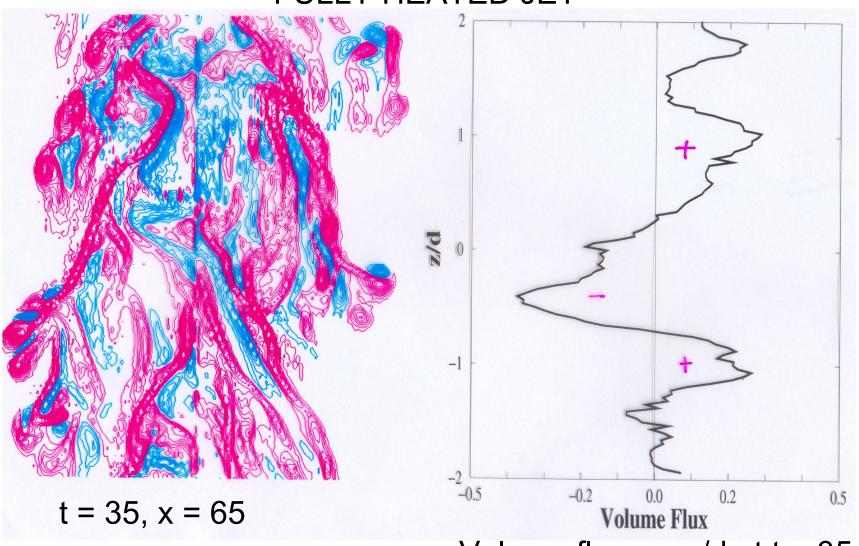
t = 35, x = 65

Volume flux vs. z/d at t = 35 RN, Shivakumar 1999 IUTAM Goettingen



AZIMUTHAL VORTICITY

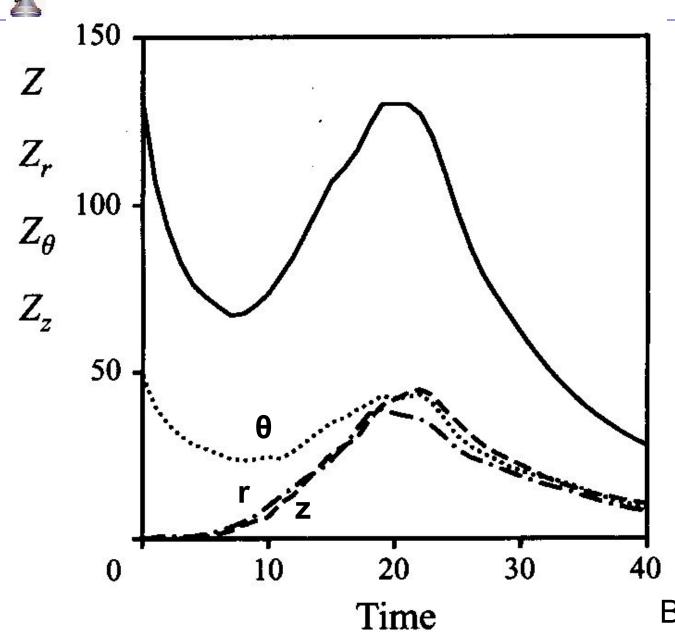
FULLY HEATED JET



Volume flux vs. z/d at t = 35



ENSTROPHY IN ORDINARY JET

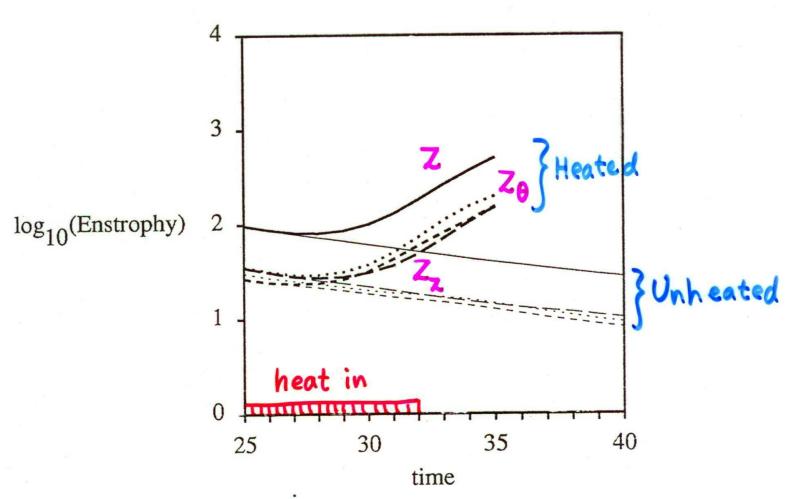


Enstrophy = mean squared fluctuating vorticity

Basu, RN 1999 *JFM*



ENSTROPHY INCREASE WITH HEATING



Basu, RN 99, JFM



TRANSIENT DIABATIC PLUME MEGHA 3



AN EXPLORATORY NUMERICAL EXPERIMENT

Direct Navier-Stokes-Boussinesq

- Reynolds number: 2000.
- Fractional-step method is used to solve the governing equations.
- ♦ Non-uniform grid, size 129 x 10⁶.
- Poisson solver: Preconditioned (multi-grid based) GMRes.



SIMULATION STATISTICS - I

Grid size:129 M

Time step: 0.0025

Number of time steps: 26,000

Total hard disk, including post-processing at 4PI cluster: 5 TB

Size of code: A few hundred KB / 5000 lines

Simulation run on: 216 CPUs

Compute time: 0.12 M core hours (~6 days wall time)

Prasanth 2013 MS thesis, JNC



SIMULATION STATISTICS - II

Final simulation (November 2013):

Grid size: 2.5 B

Time step: 0.00125

No. of time steps: 52,000

Total hard disk storage, including post-processing at 4 PI new

cluster: 100 to 200 TB

Compute time: 8 M core hours (~ 15 to 20 days wall time) with

5320 CPUs



BASIC SCALES, NON-DIMENSIONAL NUMBERS

$$\operatorname{Re} = \frac{U_o d_o}{\nu} \qquad \qquad \operatorname{Reynolds}$$

$$\operatorname{Number}$$

$$\operatorname{Pr} = \frac{\nu}{k} \qquad \qquad \operatorname{Prandtl}$$

$$\operatorname{Number}$$

$$\operatorname{G} = \frac{J}{\rho c_p} \, \frac{d_o}{U_o T_o} \qquad \qquad \operatorname{Heat} \, \operatorname{Release}$$

$$\operatorname{Number}$$

$$U_0 = \sqrt{g\alpha d_o T_o}$$
, $d_0 = \text{diameter of hot patch}$

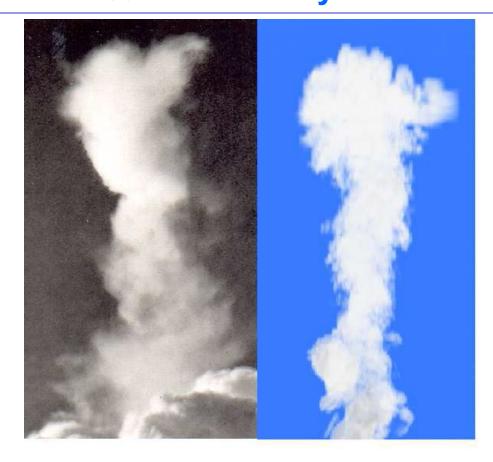
 T_0 = temperature differential of hot patch over ambient



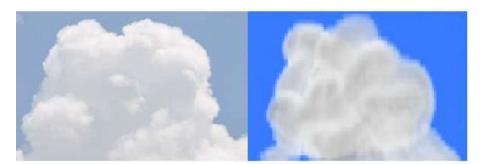
Results and Discussion



COMPARISON OF CLOUD SHAPES Real Cyber

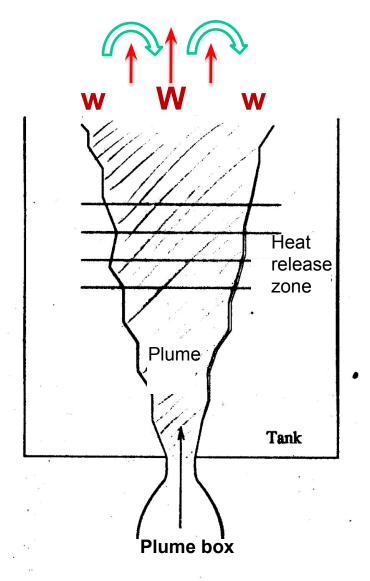


- Re = 2000
- Pr = 1.0
- $\Delta t = 0.005$
- Grid: 128 x 128 x 256
- HIZ: $Z_b = 10d$, $Z_t = 15d$
- Volumetric visualisation using PARAVIEW.





HOW THE BAROCLINIC TORQUE WORKS



The Baroclinic Torque
The varying buoyancy force
Temperature gradient

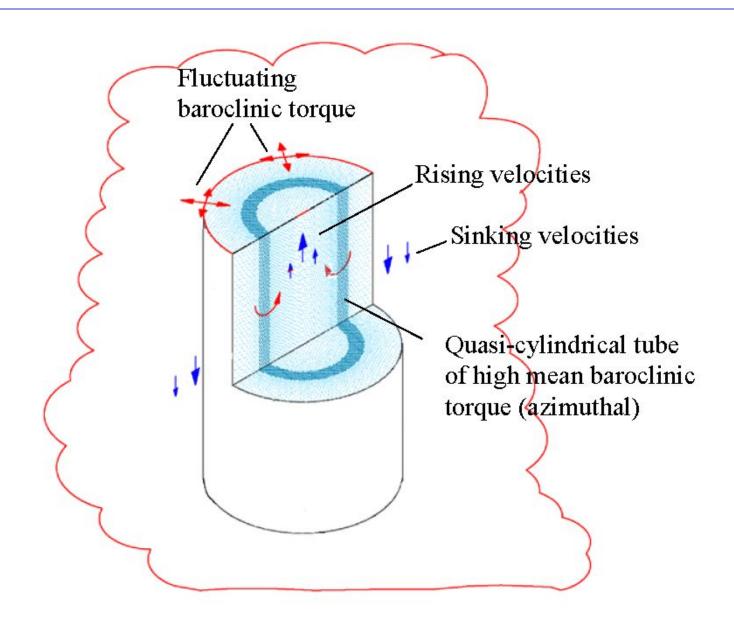
The baroclinic torque is proportional to the temperature gradient, so is a maximum mid-way between cloud centre and edge

There is a quasi-cylindrical tube of maximum baroclinic torque embedded within the cloud flow

The fluctuating baroclinic torque is a huge source of small-scale vorticity. Could that be what makes some cumulus clouds so crinkly at the edges?



HOW THE BAROCLINIC TORQUE WORKS





VORTICITY BUDGET

- For simplicity, consider a temporal diabatic jet/plume (Basu, RN 1999)
- Notation:

	Mean	Fluctuatio	Rms
		ns	
Velocity	U	u'	
Vorticity	Ω	ω'	
Temperatur		T'	
е			
Strain rate	Sij	S'ij	





Vorticity budget continued.....

Navier-Stokes + Mean Vorticity

$$\begin{split} \frac{\partial\Omega_{i}}{\partial t} &= -\overline{u'_{j}}\frac{\partial\omega'_{i}}{\partial x_{j}} \; \{ \text{turbulent transport of turbulent vorticity} \} \\ &+ \Omega_{j}S_{ij} \quad \{ \text{mean flow stretching mean vorticity} \} \\ &+ \overline{\omega'_{j}S'_{ij}} \; \{ \text{turbulent flow stretching turbulent vorticity} \} \\ &+ v \frac{\partial}{\partial x_{i}}\frac{\partial\Omega_{i}}{\partial x_{j}} \; \{ \text{viscous diffusion} \} \; -----> (1) \end{split}$$



Vorticity budget continued.....

• Turbulent enstrophy:

$$\frac{\partial}{\partial t} \left(\frac{\widehat{\omega}^2}{2} \right) = -\overline{u'_j \omega'_i} \frac{\partial \Omega_i}{\partial x_j} \qquad \{\text{generation by mean vorticity gradient}\}$$

$$+ \frac{\partial}{\partial x_j} \left(\frac{\overline{\omega'^2 u'_j}}{2} \right) \qquad \{\text{turbulent transport}\}$$

$$+ \overline{\omega'_i \omega'_j S_{ij}} \qquad \{\text{stretching by mean strain}\}$$

$$+ \overline{\omega'_i \omega'_j S_{ij}} \qquad \{\text{stretching by turbulent strain}\}$$

$$+ v \frac{\partial}{\partial x_j} \frac{\partial}{\partial x_j} \left(\frac{\widehat{\omega}^2}{2} \right) \qquad \{\text{viscous diffusion}\}$$

$$- v \left(\frac{\partial \omega_i}{\partial x_j} \frac{\partial \omega_i}{\partial x_j} \right) \qquad \{\text{viscous dissipation}\} \qquad (2)$$



Vorticity budget continued.....

Noting:
$$\Omega \sim S \sim \frac{U_c}{b}$$
, $\widehat{\omega} \sim S \sim \frac{\widehat{u}}{\lambda} \sim \Omega Re^{\frac{1}{2}}$, $\widehat{u} \sim U_c$, Re = $\frac{U_c b}{V}$,

introducing Kolmogorov: $l_k=(\frac{{
m V}^3}{\epsilon})^{\frac{1}{4}}$, $u_k \sim \frac{\nu}{k}$ and taking

$$\frac{\partial \omega_i}{\partial x_j} \sim \frac{\widehat{u}'}{\lambda} \cdot \frac{1}{l_k},$$

we have enstrophy dissipation $\sim v \frac{\hat{u}^3}{\lambda^3}$.

Only the starred terms survive! So, with heating

$$\frac{\partial}{\partial t} \left(\frac{\widehat{\omega}^2}{2} \right) = \overline{\omega'_i \omega'_j s_{ij}} - \overline{v \left(\frac{\partial \omega_i}{\partial x_j} \frac{\partial \omega_i}{\partial x_j} \right)} + (\beta \boldsymbol{g}. (\overline{\boldsymbol{\omega}' \mathbf{x} (\nabla \mathbf{T}')}) -----> (3)$$





THE VORTICITY SOURCE

The source for enstrophy is

$$\overline{\beta \omega'.(\mathbf{g} \times \nabla T')} \equiv \beta \mathbf{g}.(\overline{\omega' \times \nabla T'}). \tag{10}$$

Noting that $\beta \nabla T' = -(\nabla \rho')/\rho_o$, and taking $\nabla \rho'$ as of order $\hat{\rho}_c/\lambda_\rho$, where $\hat{\rho}_c$ is (say) the centreline rms of value ρ' , and introducing λ_ρ as the Taylor microscale for the density field (although no measurements of λ_ρ are known to the author), the enstrophy source is of order

$$\frac{\mathbf{g}}{\rho_o} \frac{U_c}{\lambda} \frac{\hat{\rho}_c}{\lambda_\rho},\tag{11}$$

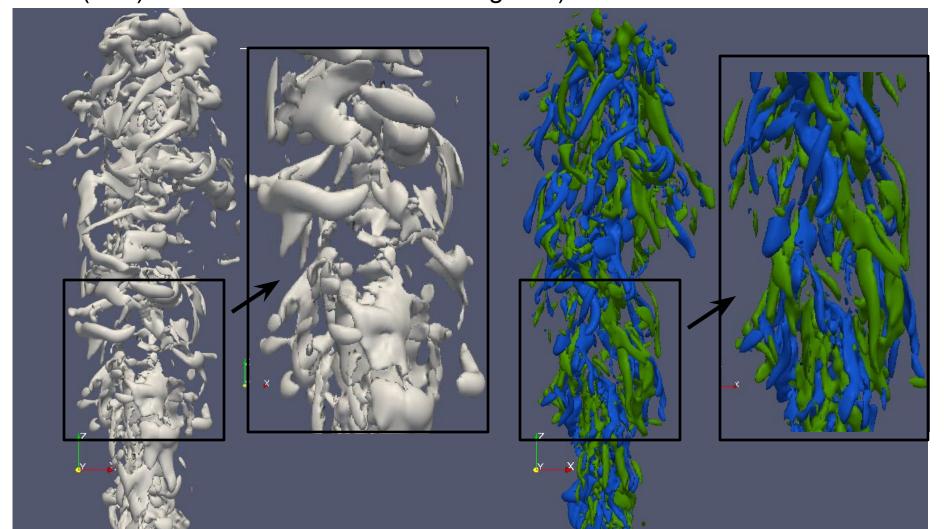
where $\hat{\rho}$ will be determined by the heat release. This term seems to be responsible for the explosive increase in enstrophy found in the BaN simulations, particularly in the spectrum at high wave numbers (see Figure 5f).



Vorticity iso surface for plumes

Azimuthal component (-1.0)

Axial component (-1.0 blue, green)

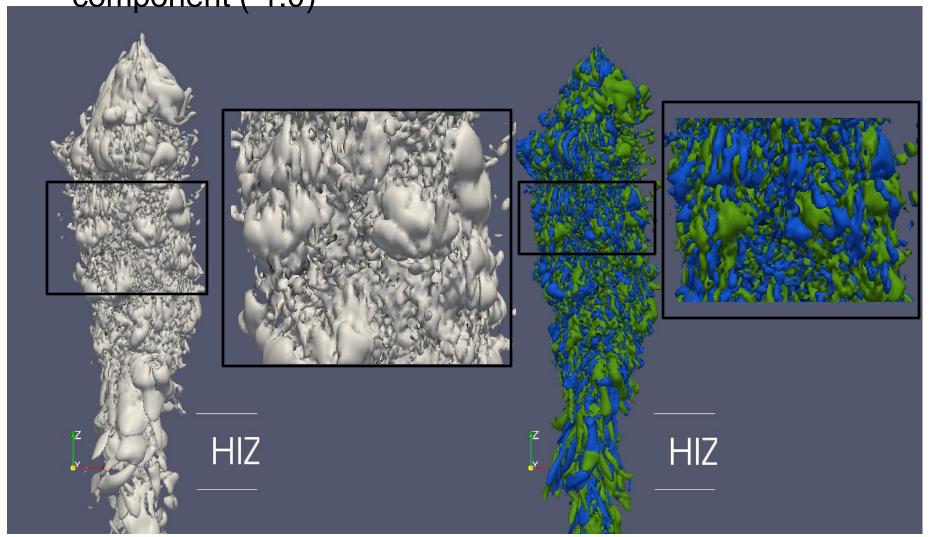




Vorticity iso surface for cloud flow

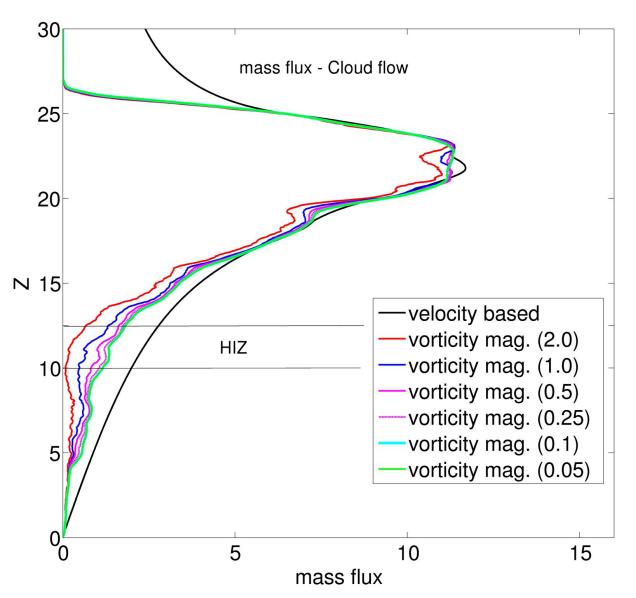
Azimuthal component (-1.0)

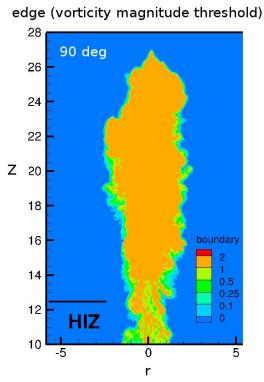
Axial component (-1.0 blue, 1.0 green)





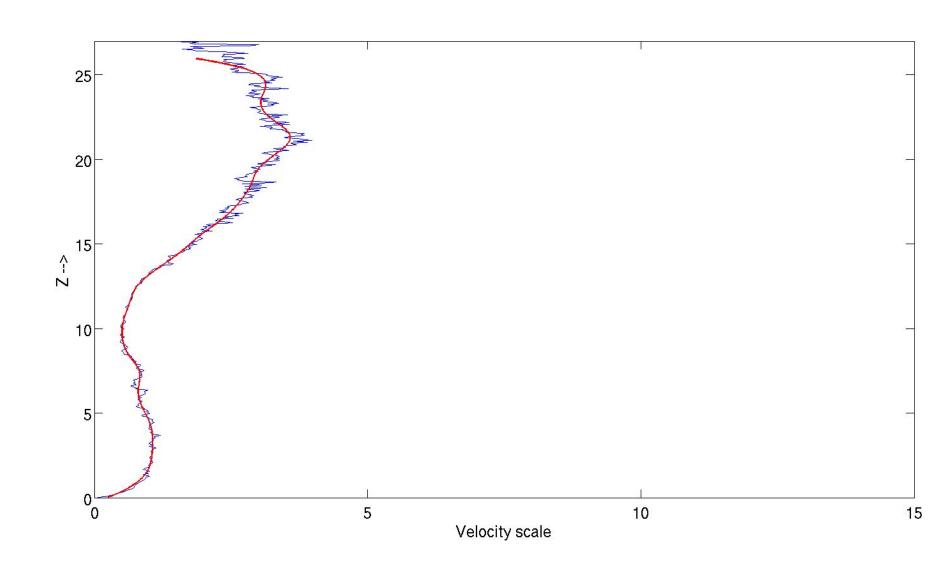
WHAT IN-CLOUD MASS FLUX?





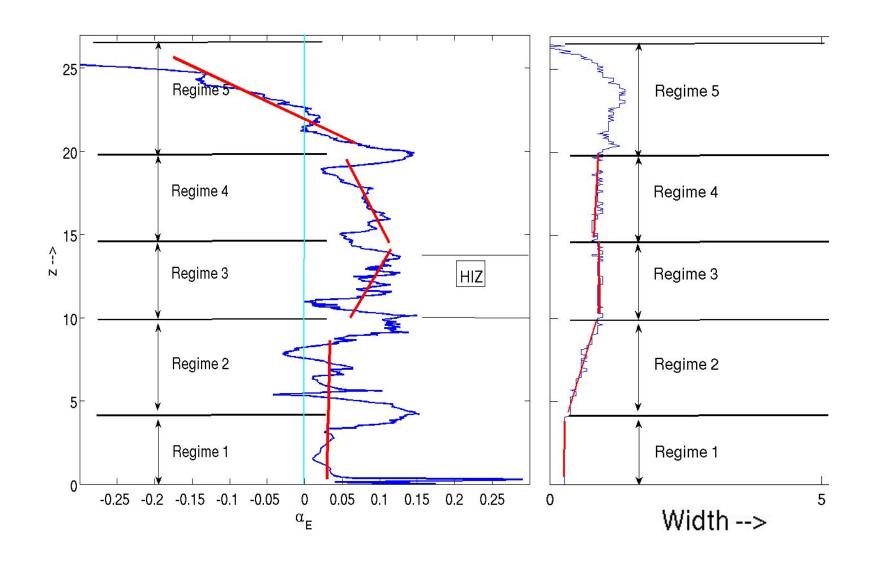


Velocity scale





Entrainment coefficient and width





HEATED PLUME

Re = 2000

Totally 90 FU

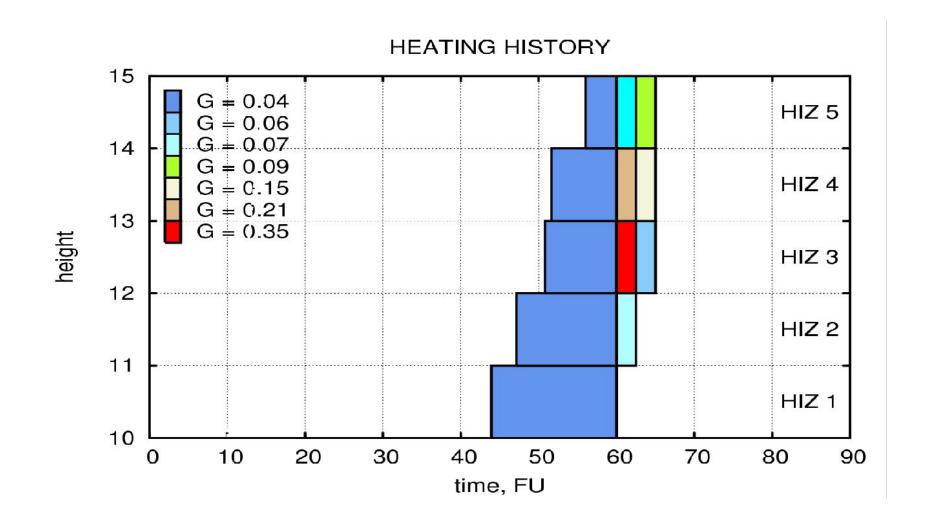
HIZ: 10 - 15 diameters

Heating stops at 65 FU

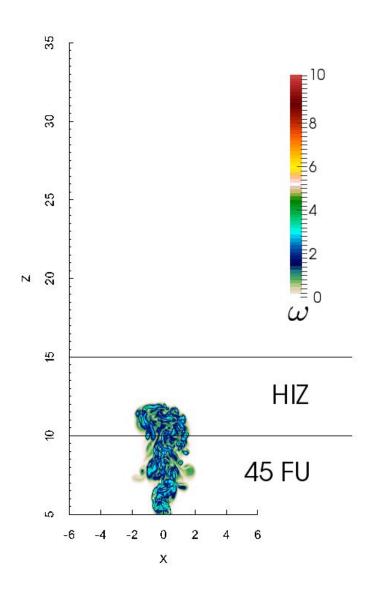


Axial sections at y = 0

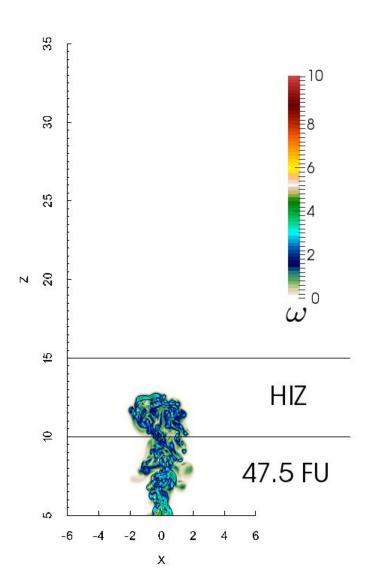




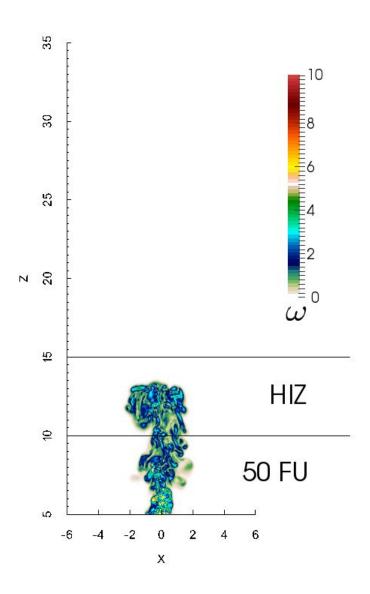




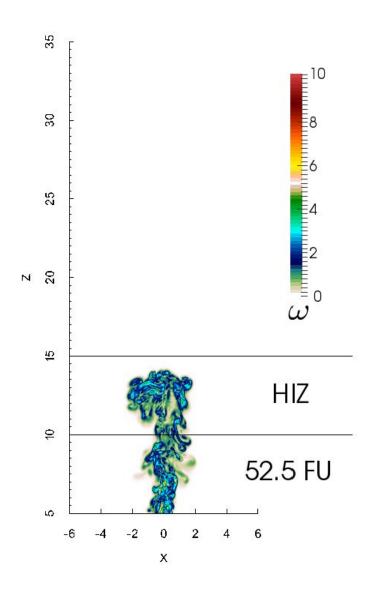




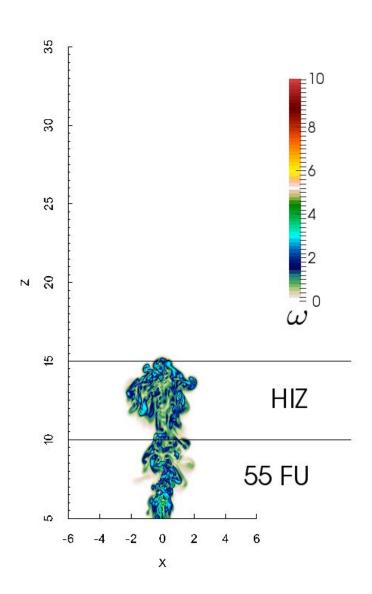




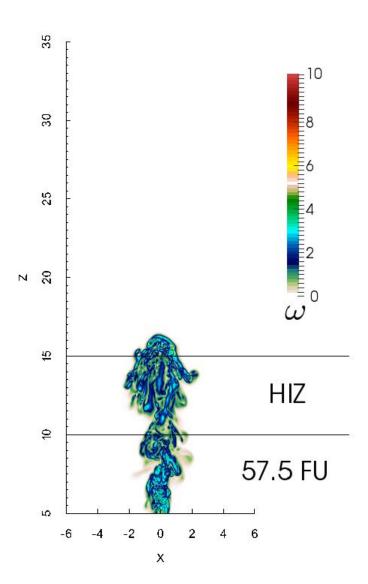




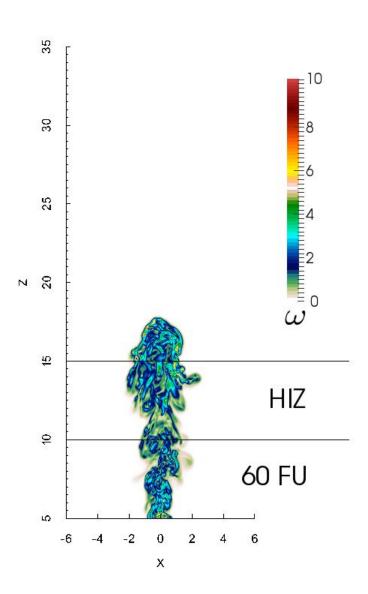




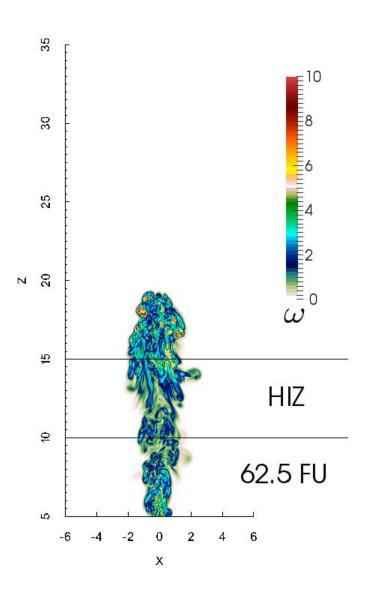




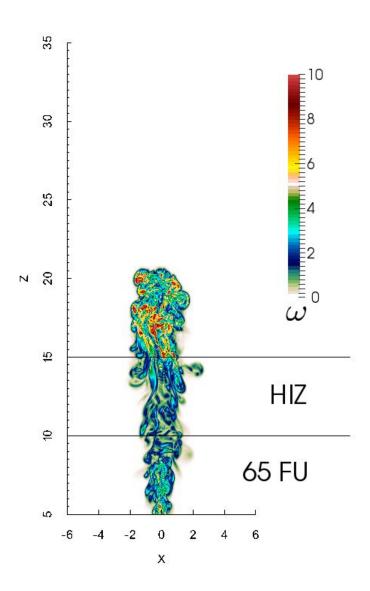




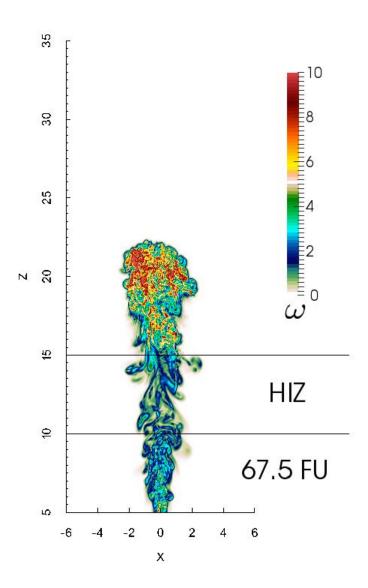




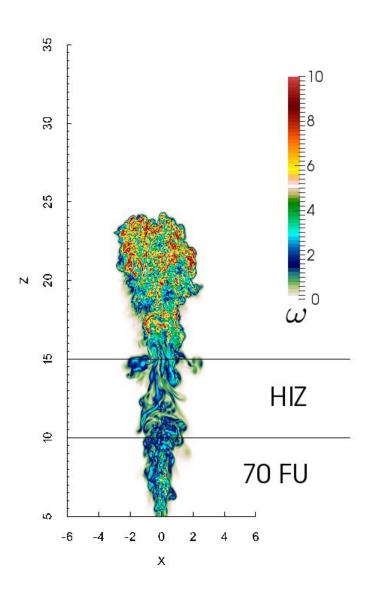




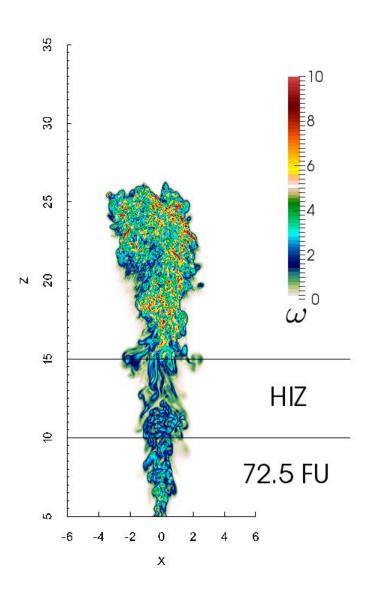




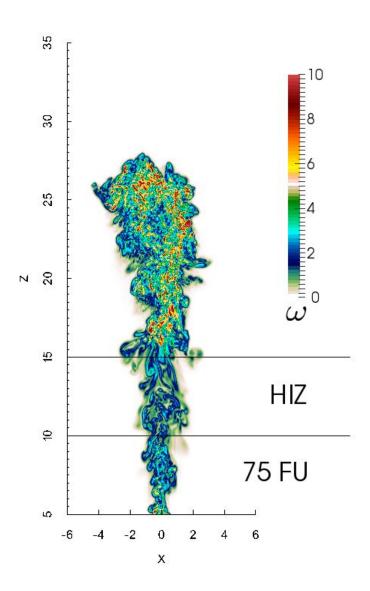




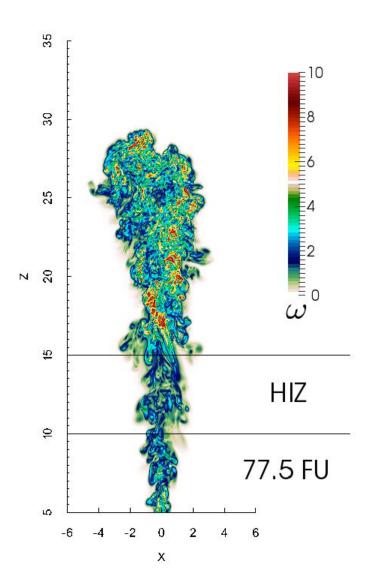




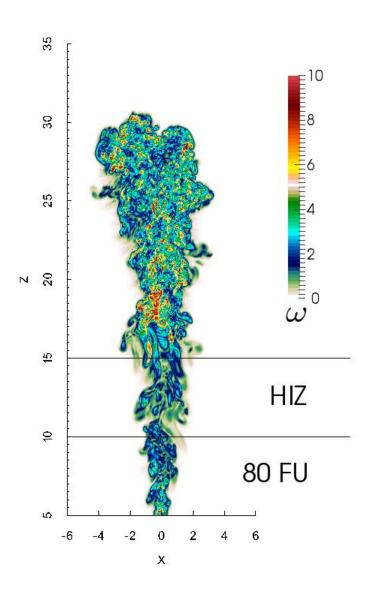




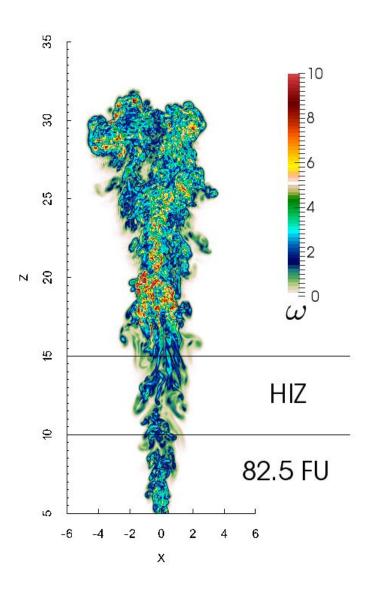




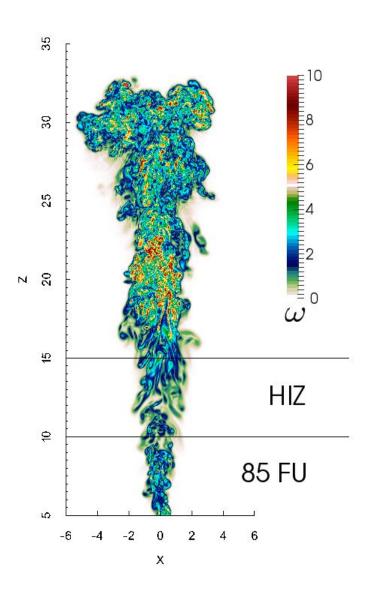




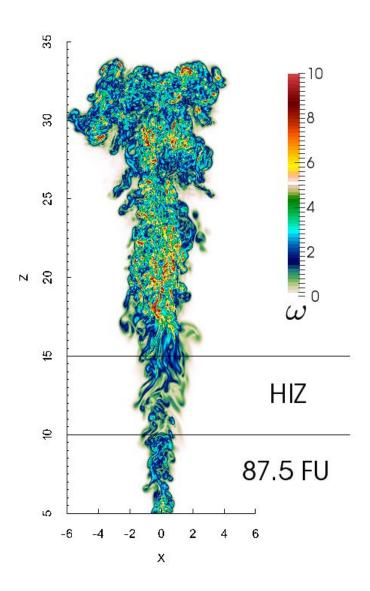




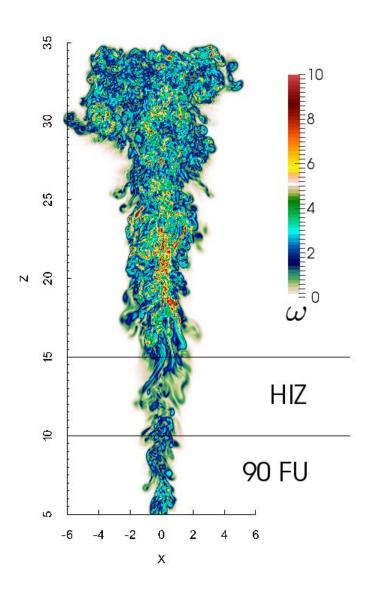










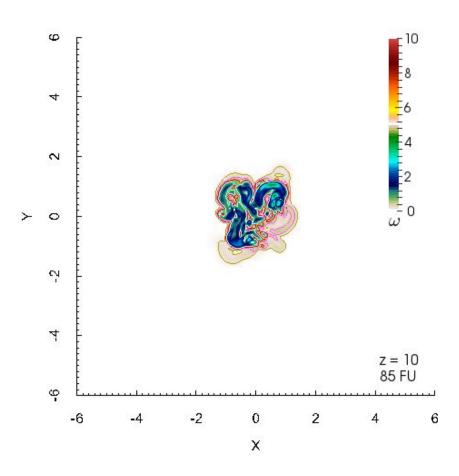




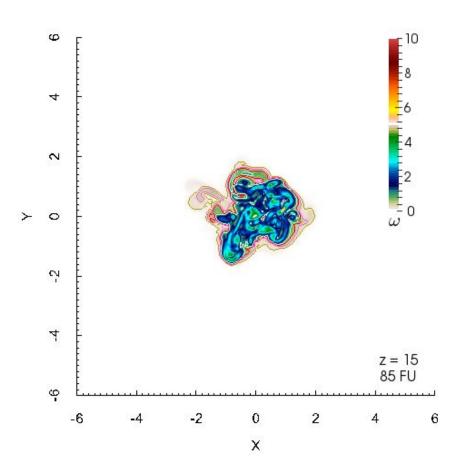
Diametral cross-sections

at 85 FU, with z

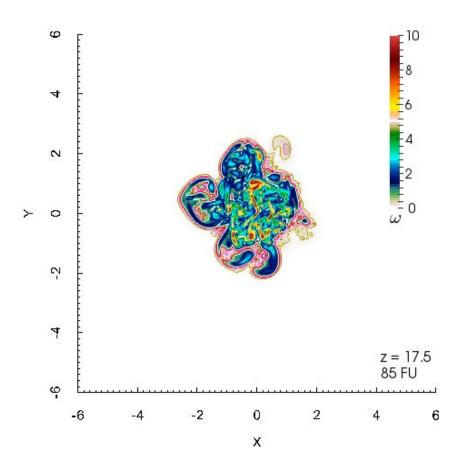




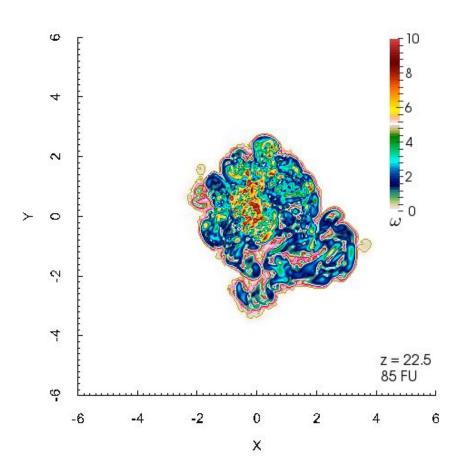




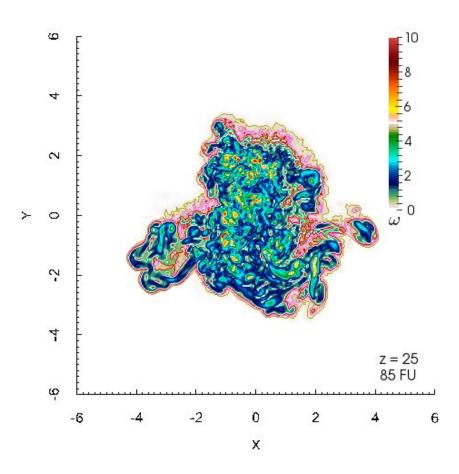




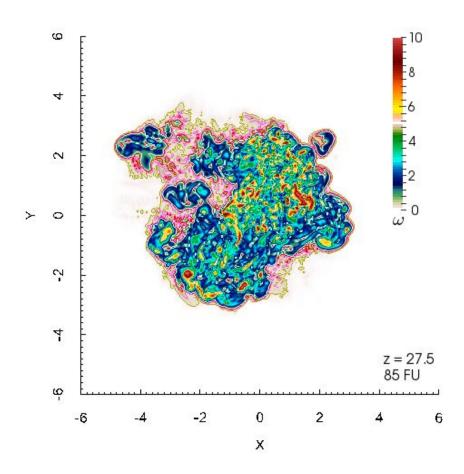




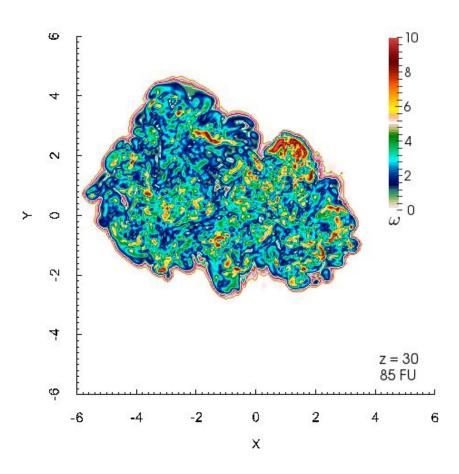








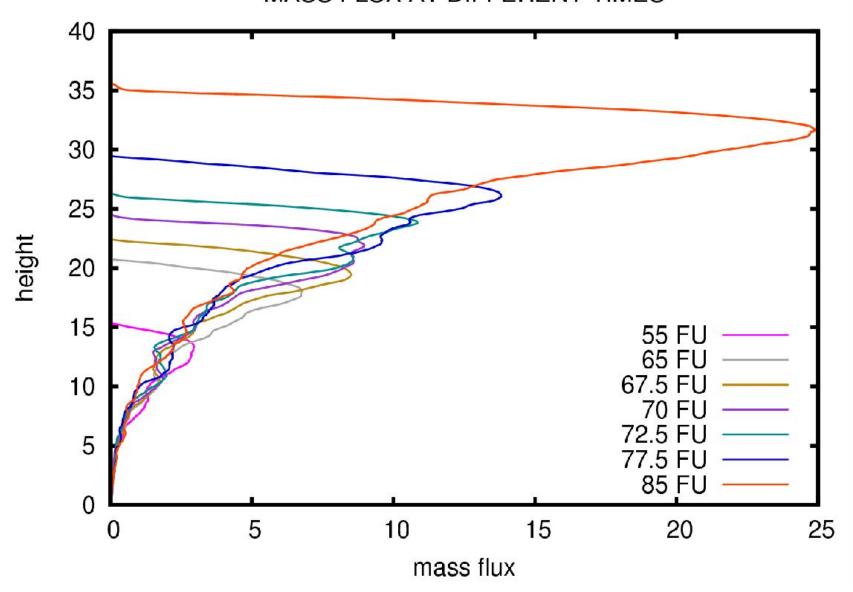






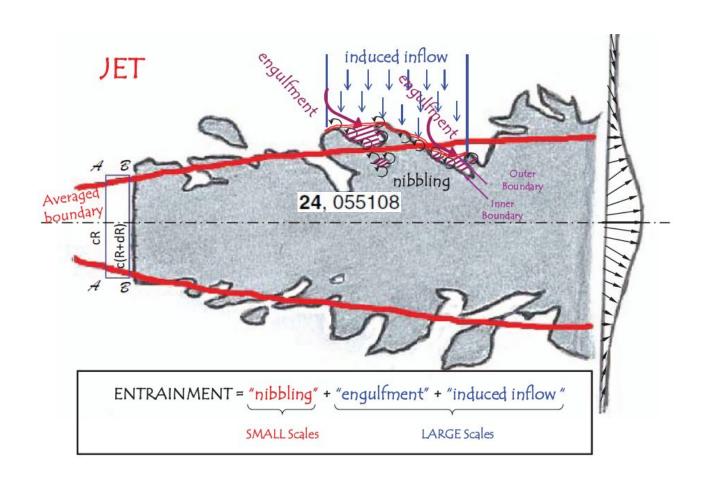
ENTRAINMENT DYNAMICS

MASS FLUX AT DIFFERENT TIMES



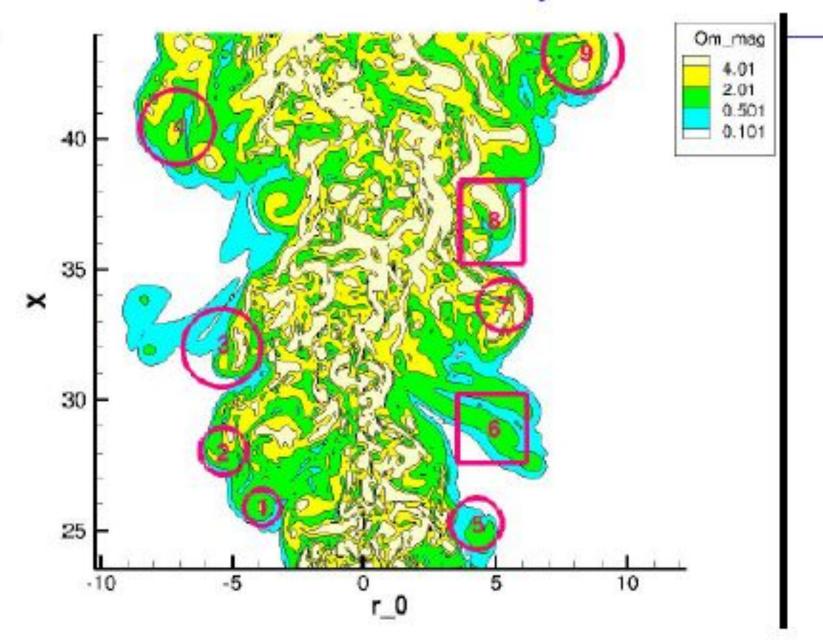


ONE VIEW OF ENTRAINMENT



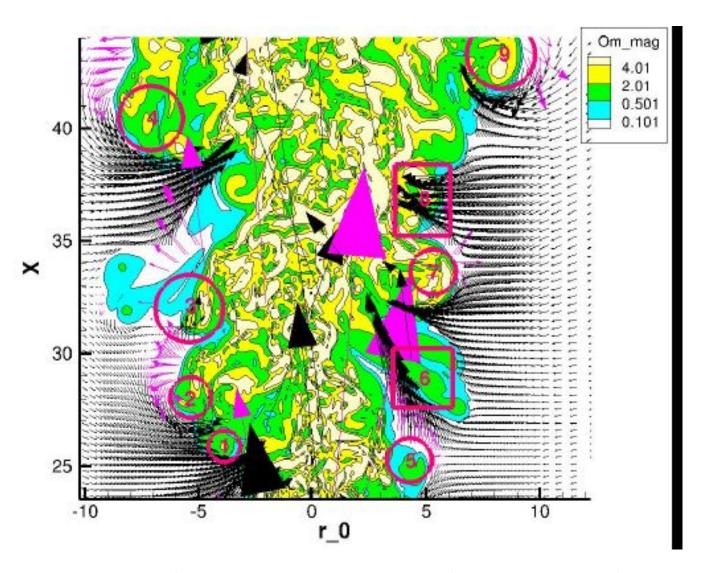


AXIAL Section : Vorticity field





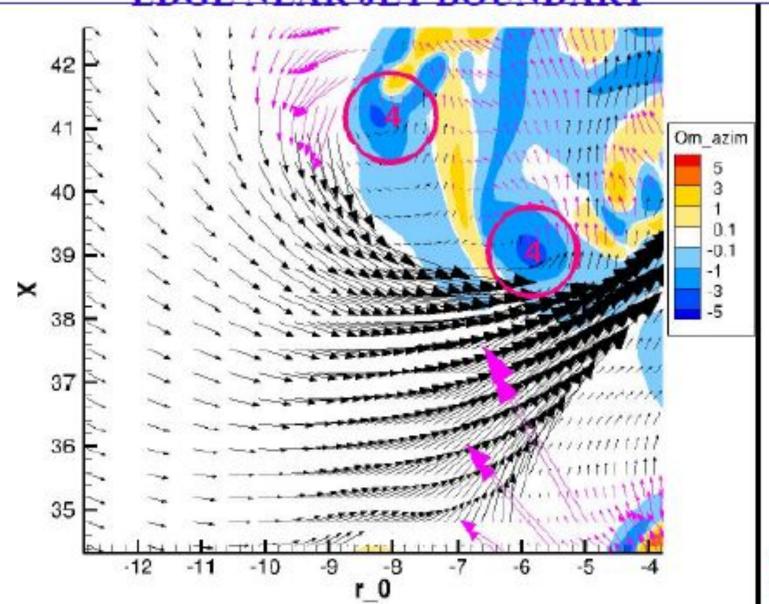
ANOTHER VIEW OF ENTRAINMENT



AXIAL Section : Velocity & Vorticity fields



AZIMUTHAL OMEGA AND INFLOW ACROSS EDGE NEAR JET BOUNDARY





Conclusions



CONCLUSION

- Cumulus clouds are generally transient flows
- Latent heat release on condensation of water vapour changes an ordinary plume into a cloud-like flow
- So a transient diabatic plume seems like a good fluid-dynamical model for cumulus flow
- Measurements in transient diabatic plumes show systematic but wide variations in entrainment coefficient with cloud height. Reason for great variety of proposals made over decades have all 'seemed' based on 'fact'?
- Computer simulations suggest that the baroclinic torque drives the cumulus flow engine



Conclusions

- 3D Navier-Stokes solver capable of simulating cloud flow was developed and validated.
- The significant role played by the heat distribution in determining the shape of any cumulus flow.
- Effect of off-source buoyancy addition and baroclinic torque on the structure of the flow was studied.
- Five distinct regimes:
 - 1. A nearly laminar constant width regime
 - 2. A nearly linearly growing turbulent plume regime
 - 3. HIZ where the width is nearly constant
 - 4. A regime of slow growth in width culminating at the maximum
 - 5. A short dome like cloud top
- Preliminary estimates on the entrainment coefficient.
- Key role of vorticity, baroclinic torque demonstrated
- Cumulus congestus is a special class of Transient Diabatic Plumes



Acknowledgements

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Thank you for listening!