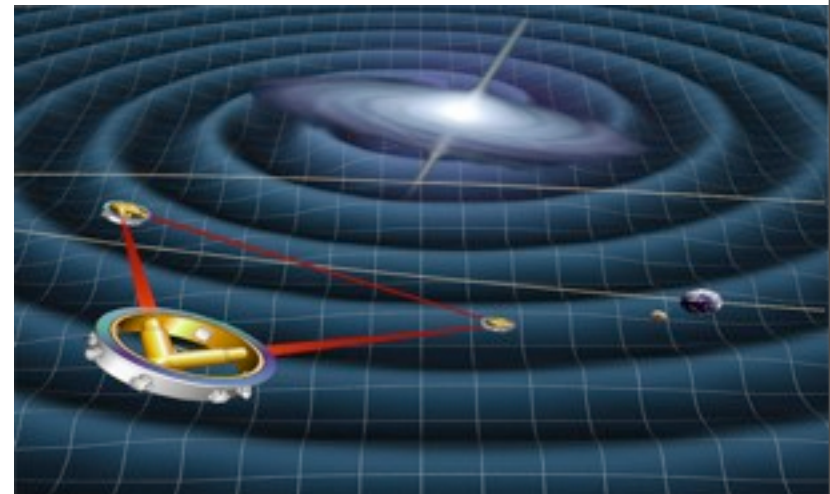


Black Hole Research: A New Golden Age

Kip Thorne



7th International Conference on Gravitation and Cosmology
Goa, India, 15 December 2011

First Golden Age of Black-Hole Research 1963 - 1977

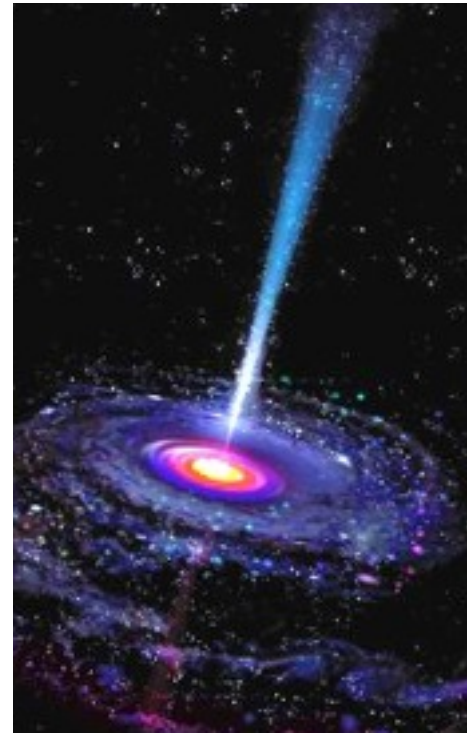
First Golden Age of Black-Hole Research 1963 - 1977

- Driven by Observational Discoveries:
 - » Quasars



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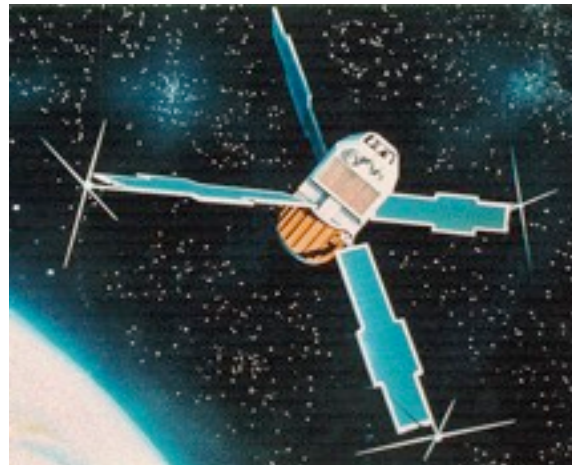
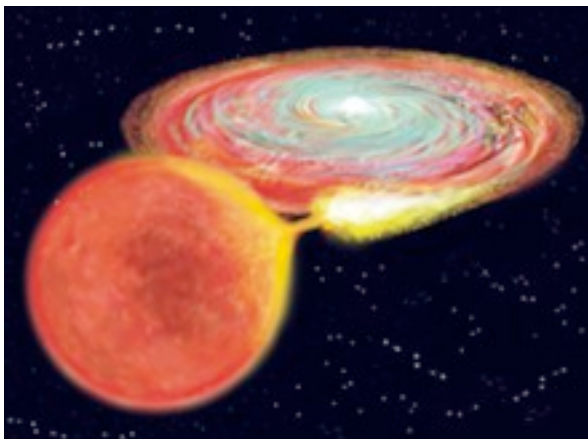
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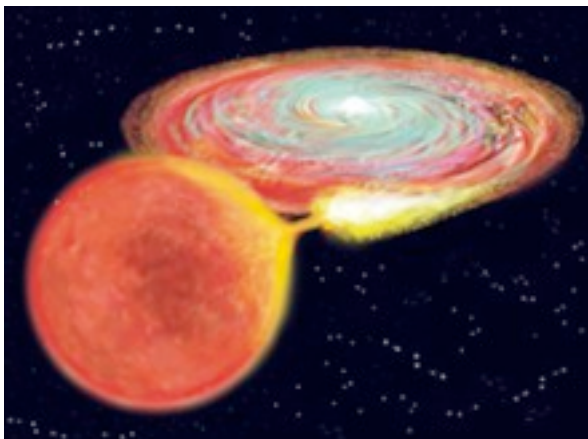
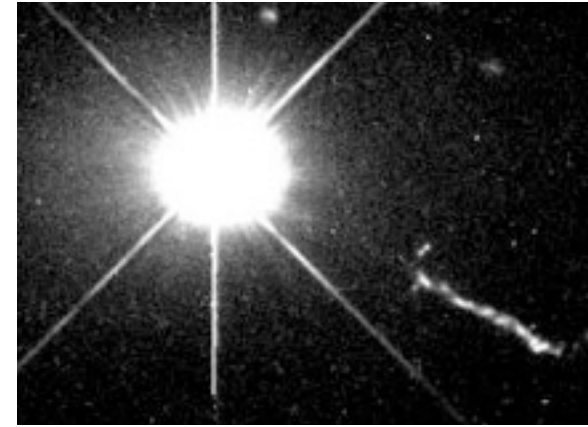
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- There is a big black hole at center of most large galaxies

- » Compact X-ray Sources

- A hundred million small black holes in every galaxy like our own



Theoretical Discoveries in 1st Golden Age

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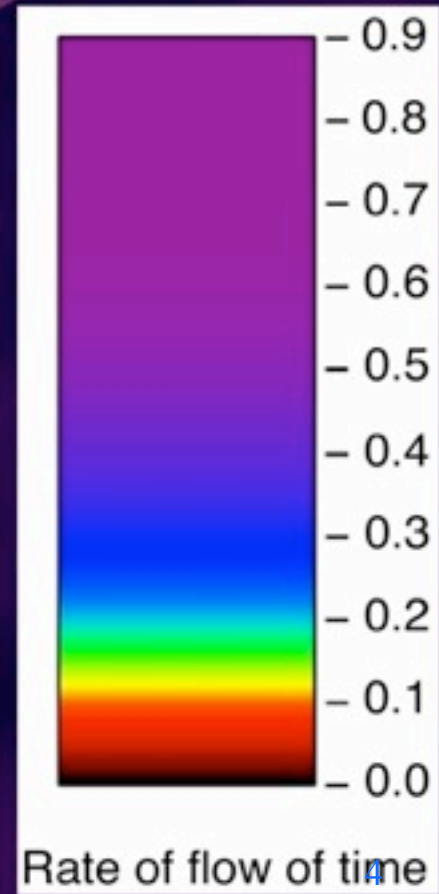
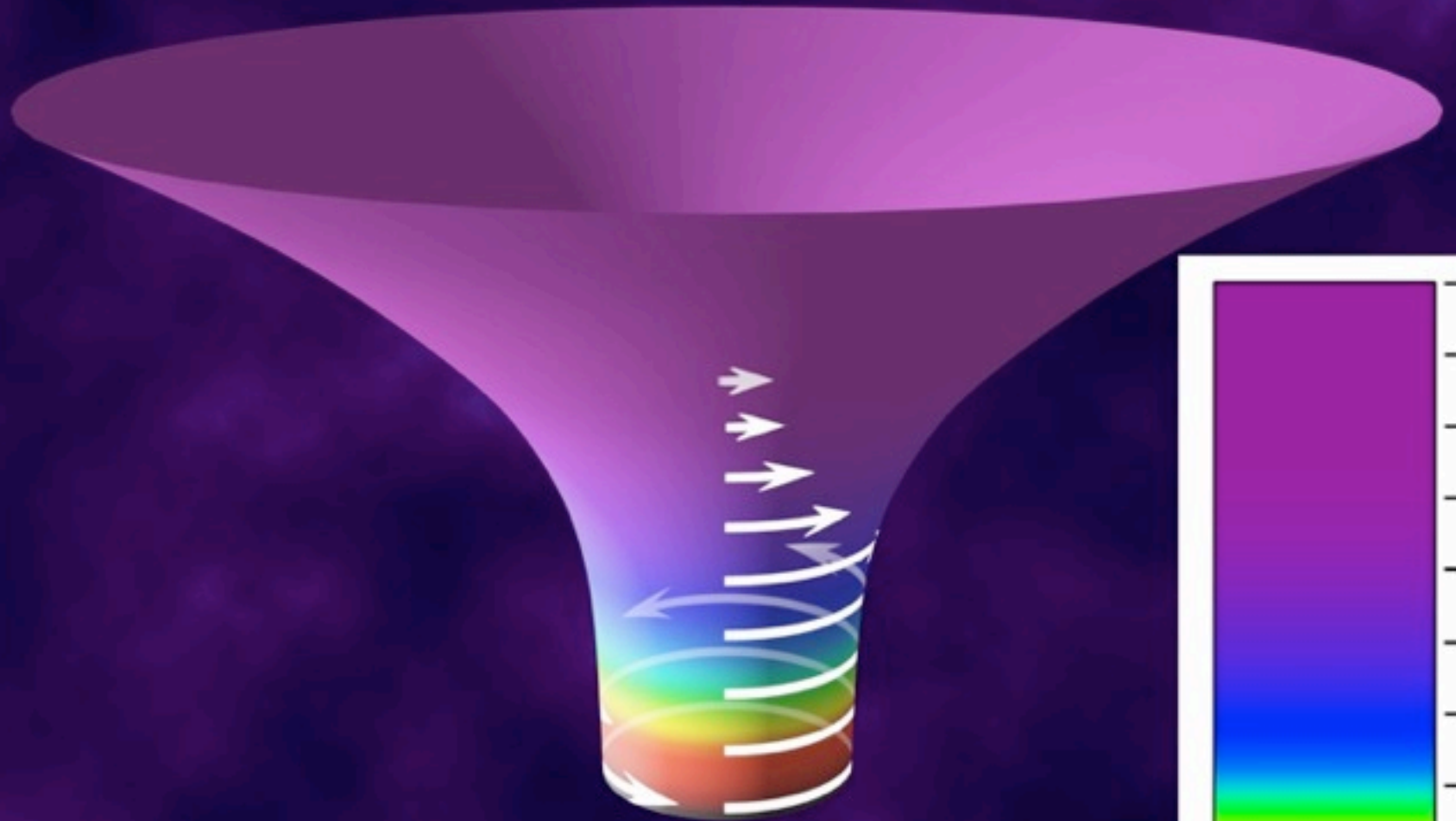
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- Black hole thermodynamics (Hawking, Bekenstein)
 - Hawking radiation; temperature $T \sim \kappa$, entropy $S \sim A$

Quiescent Black Hole: Embedding Diagram



Roy Kerr

Black Hole Status in 2009

Object

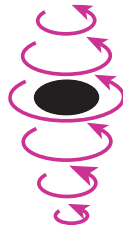
Understood? Observed?

Black Hole Status in 2009

Object

Understood? Observed?

Quiescent Black Hole



Yes

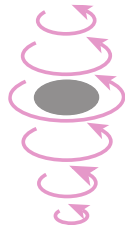
No

Black Hole Status in 2009

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Understood? Observed?

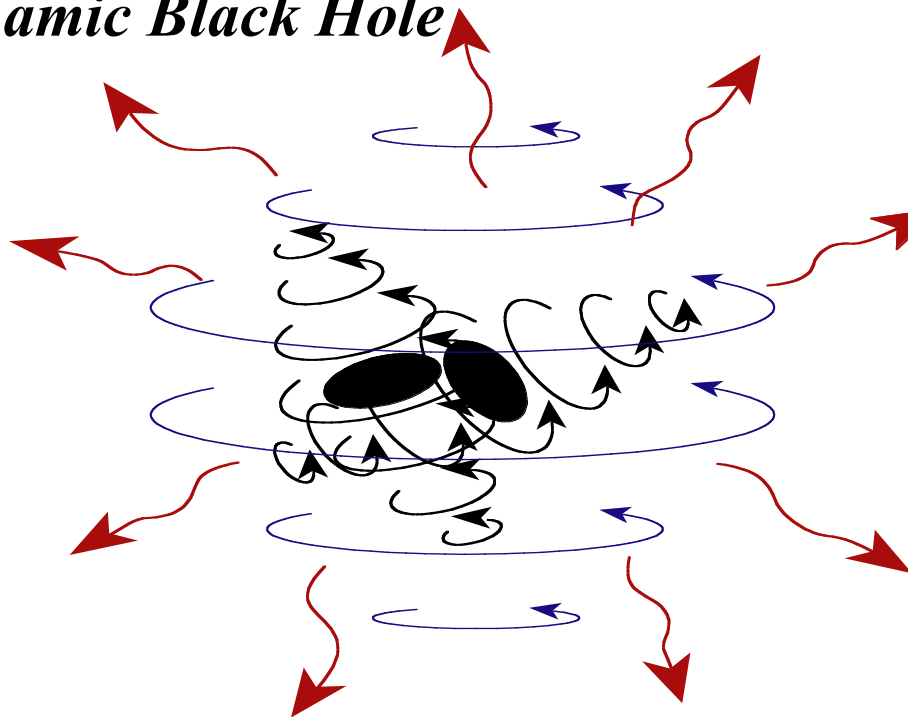
Quiescent Black Hole



Yes

No

Wildly dynamic Black Hole



*No **

No

- * except for some very important theorems:
- * Penrose: singularity at center
- * Hawking: Area Increase

Black Hole Status in 2009



Understood? Observed?

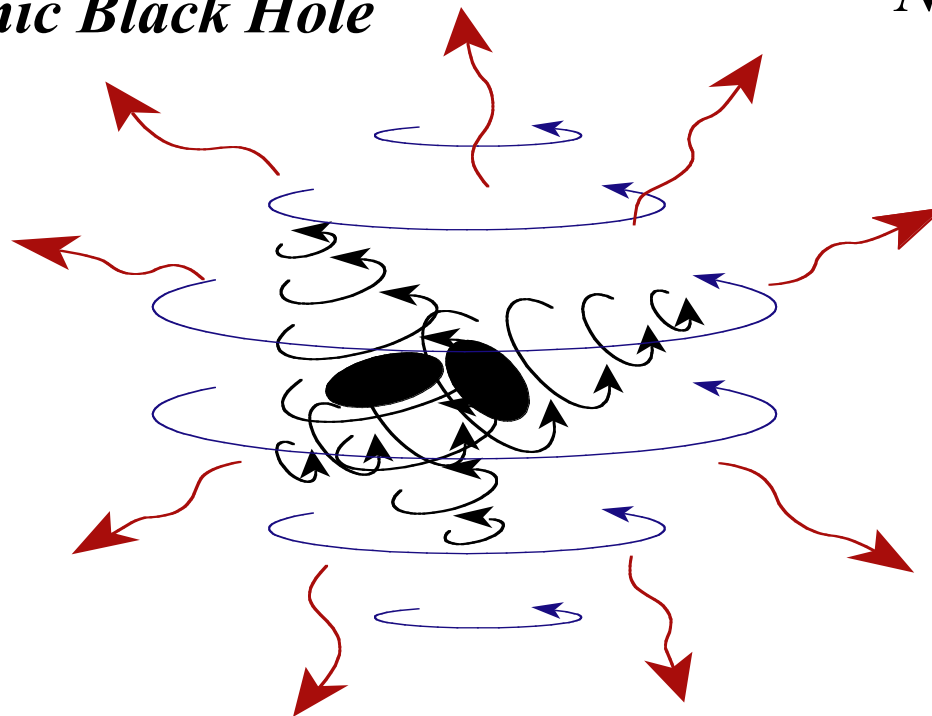
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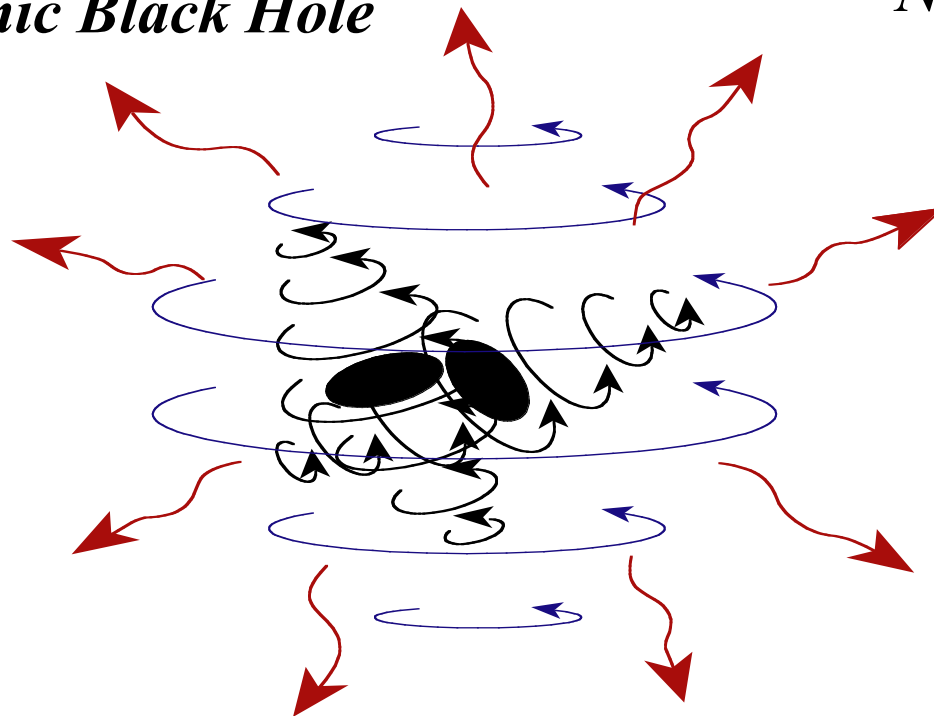
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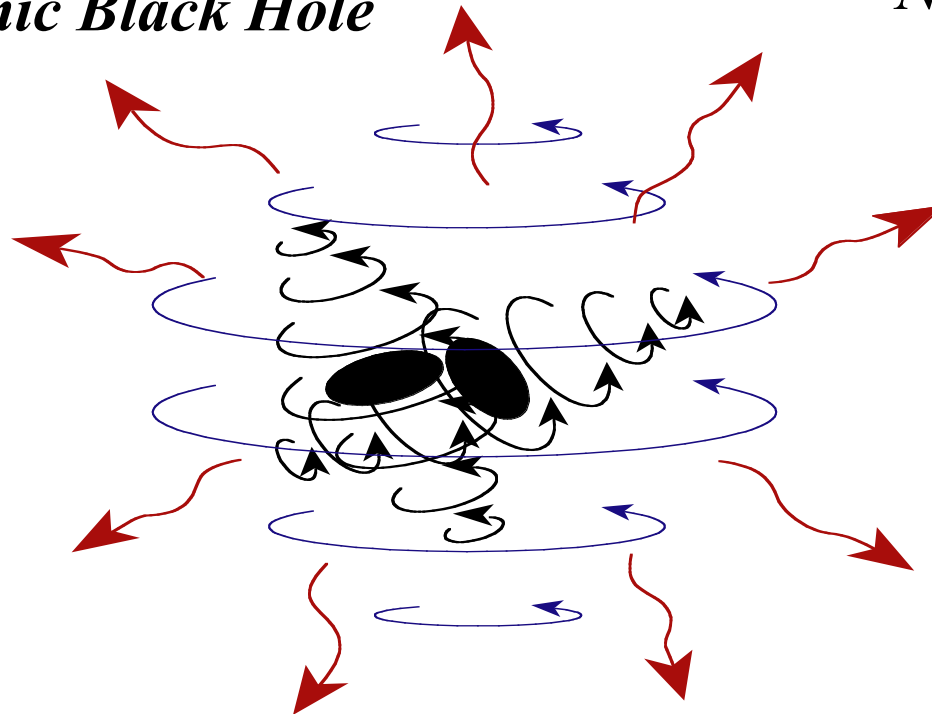
Yes

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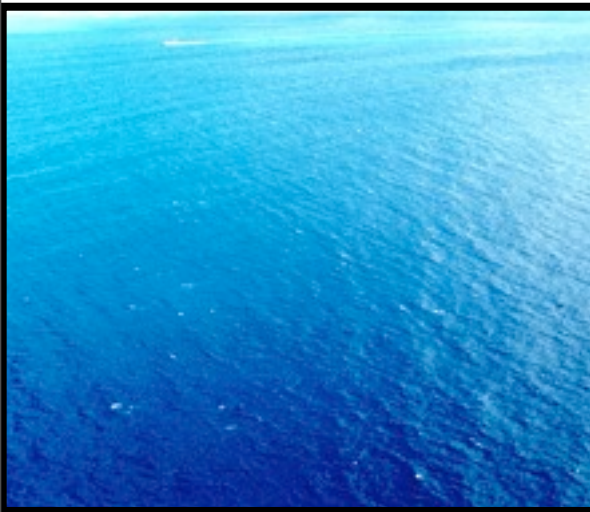
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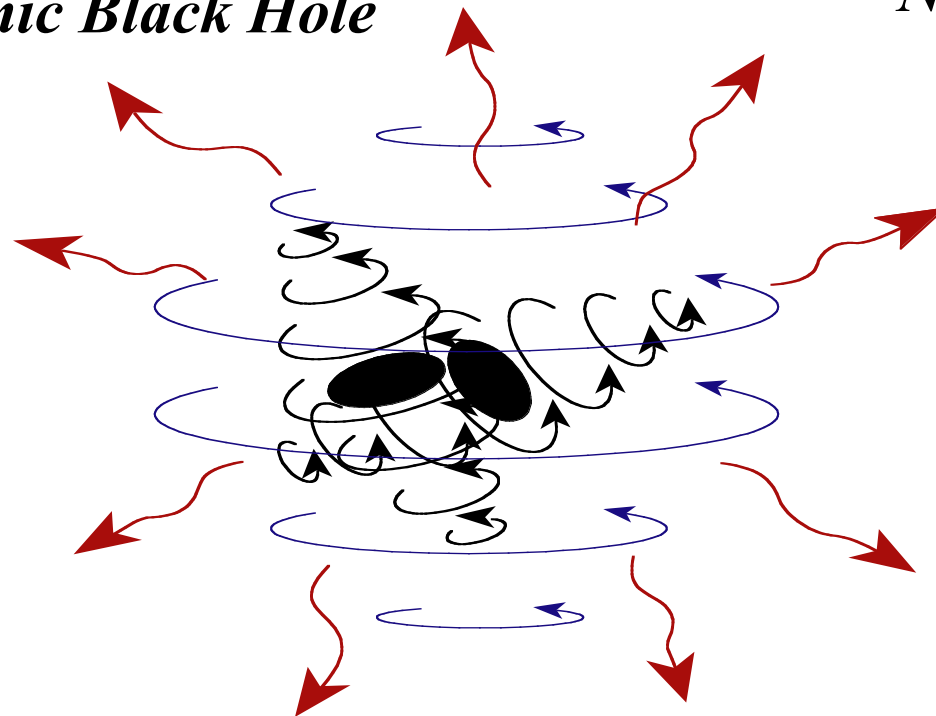
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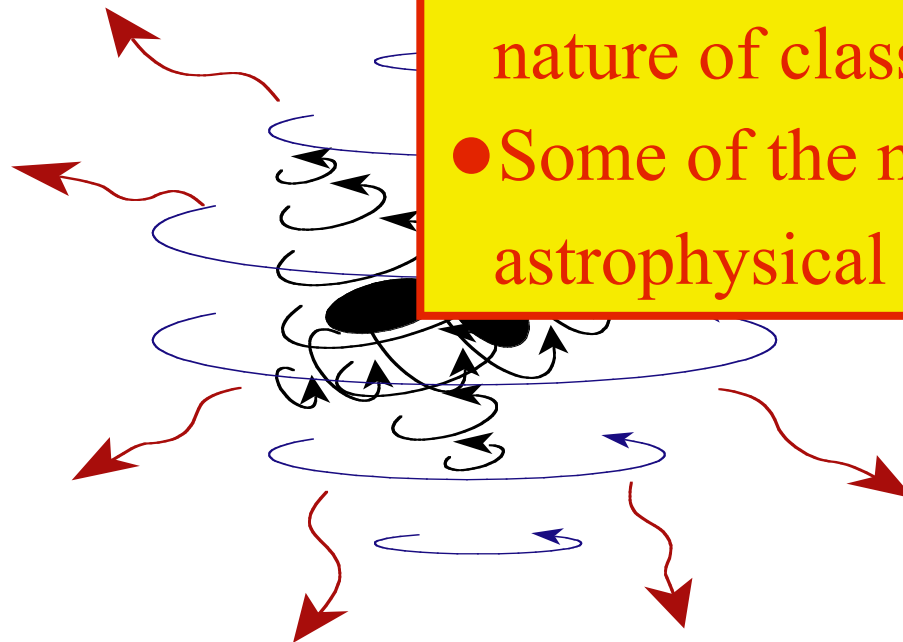
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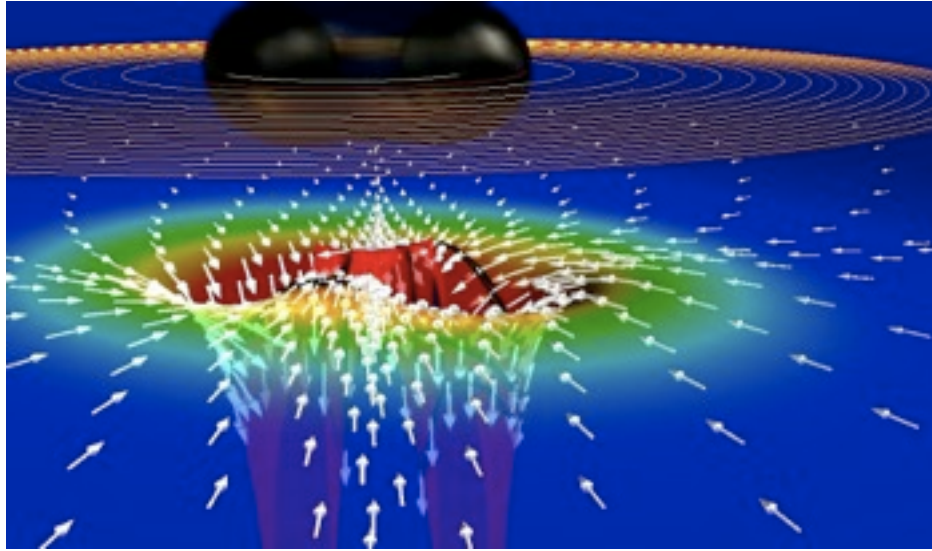
- Some of the deepest issues in nature of classical spacetime
- Some of the most interesting astrophysical phenomena



A New Golden Age: 2010 - ??

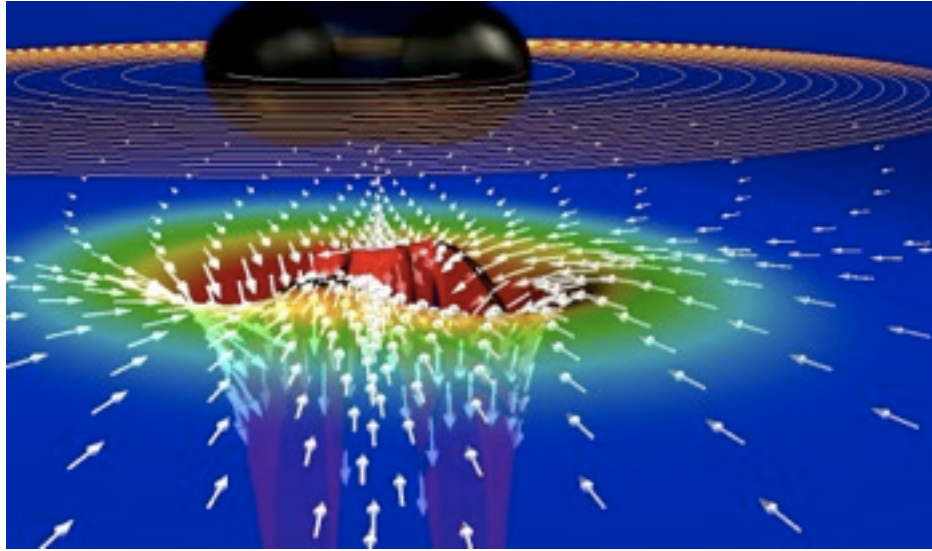
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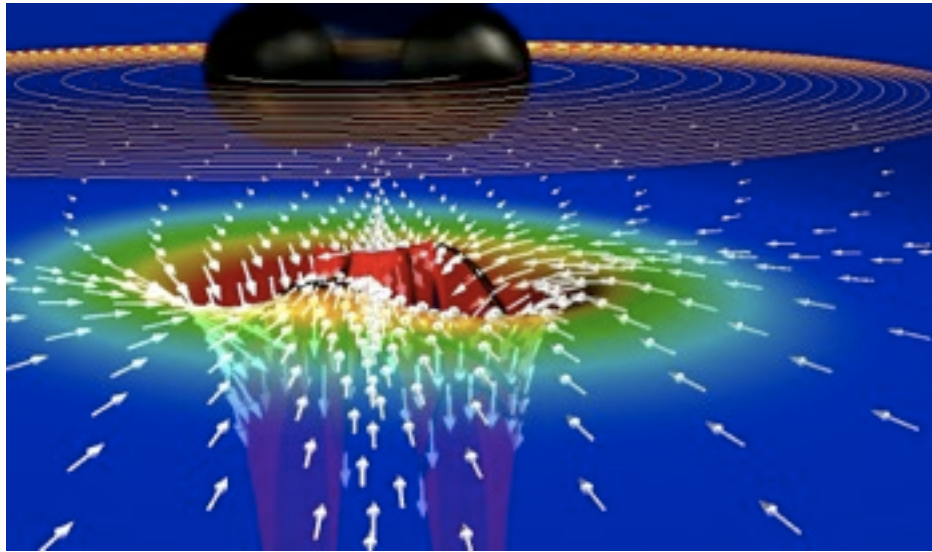


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A New Golden Age: 2010 - ??

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Also:

Research into quantum black holes
- connections to string theory, LHC physics, ...

I will not discuss



Numerical Simulations (numerical relativity)

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 - Big success in past several years
 - » *beginning to teach us about the “nonlinear dynamics” of curved spacetime*
- John Wheeler's GEOMETRODYNAMICS



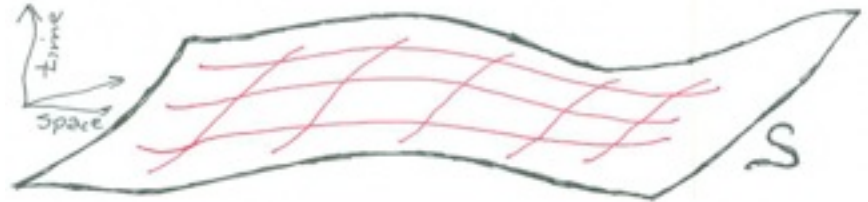
Numerical Relativity: How is it Done?

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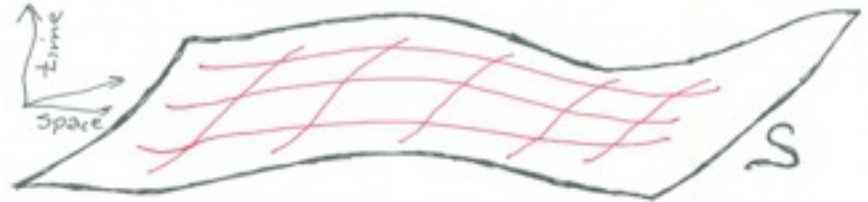
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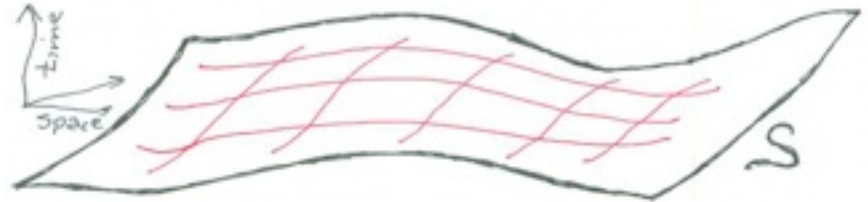
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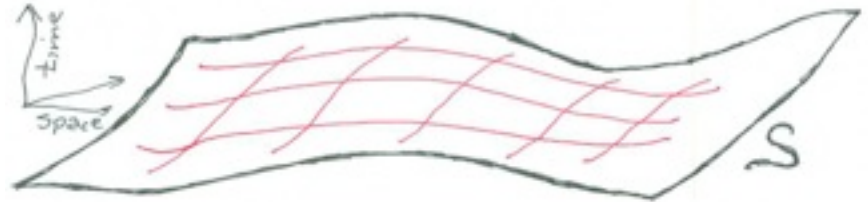
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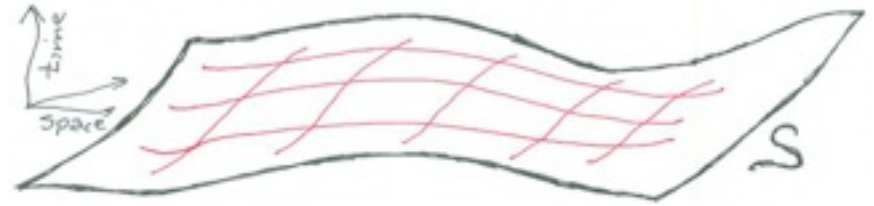
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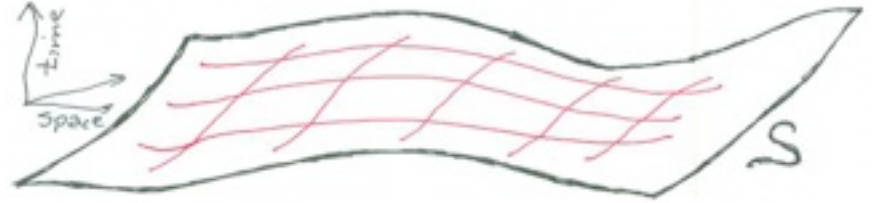


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$$ds^2 = -\alpha^2 dt^2 + g_{ij} (dx^i - \beta^i dt) (dx^j - \beta^j dt)$$

Two Mature Approaches

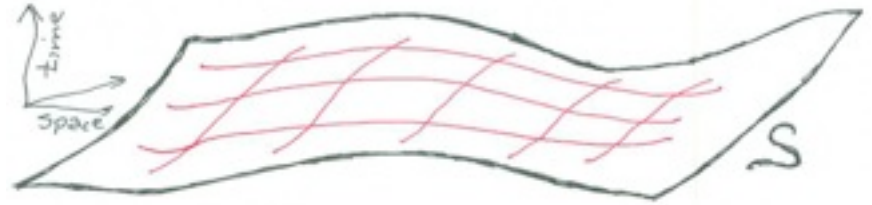


Two Mature Approaches



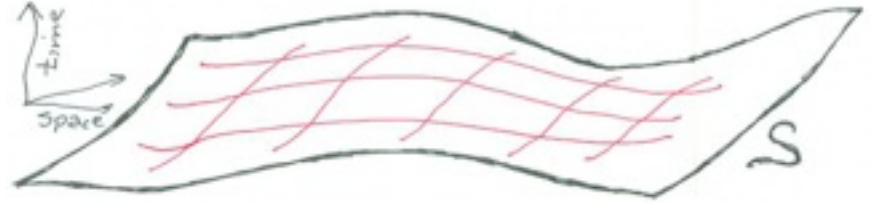
- Finite-difference description of spatial geometry

Two Mature Approaches



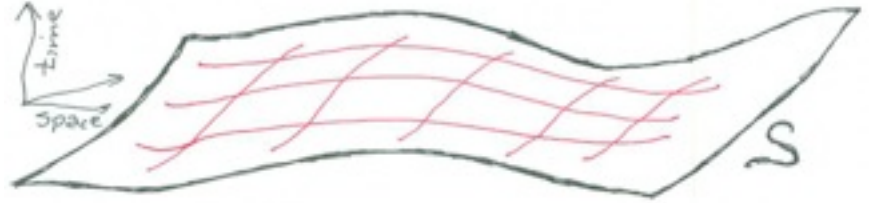
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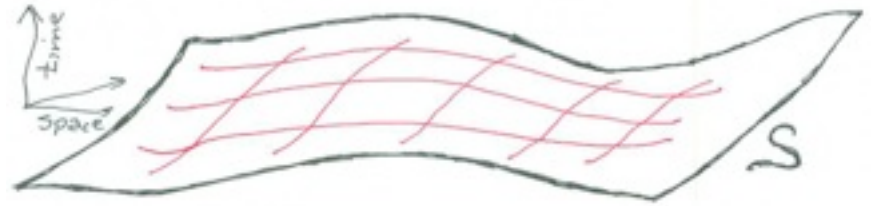
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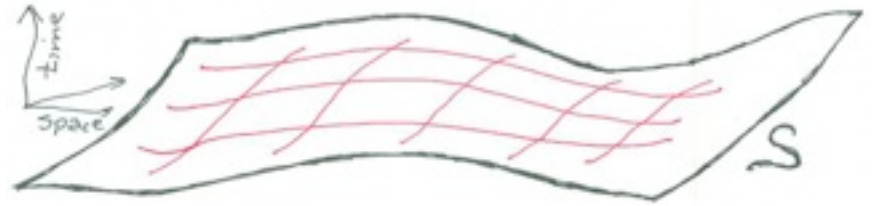
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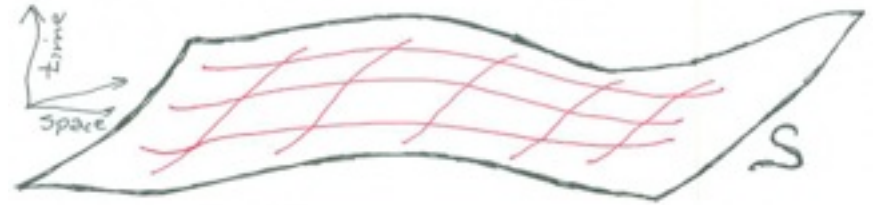
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Two Mature Approaches

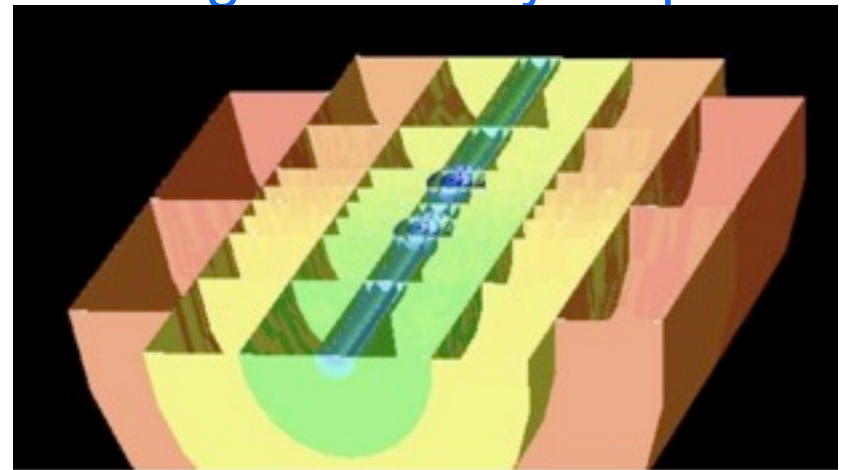


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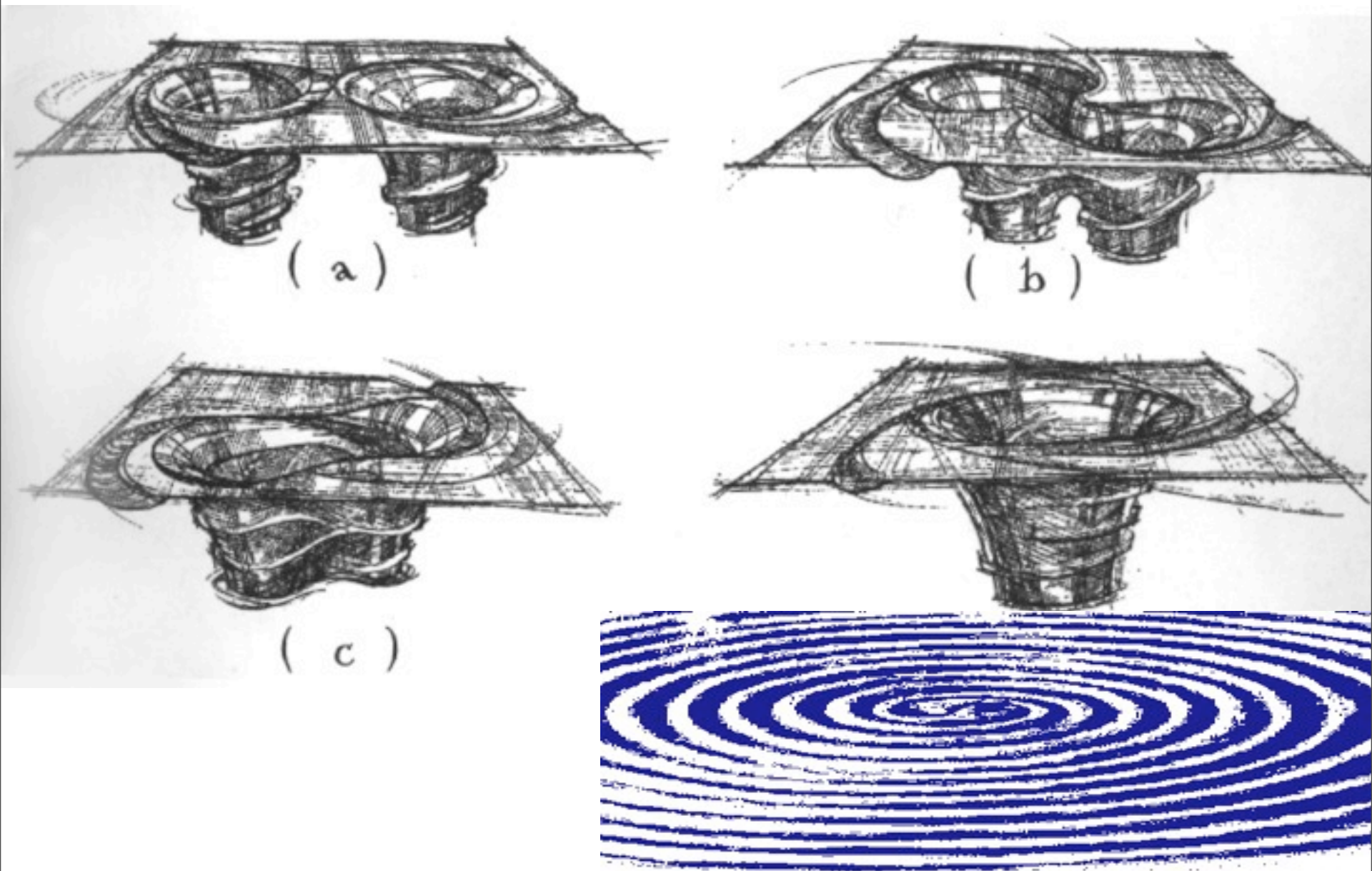
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 - » Explore geometrodynamics
 - » Gravitational waveforms - very high accuracy; huge numbers.



Numerical Relativity Research Groups

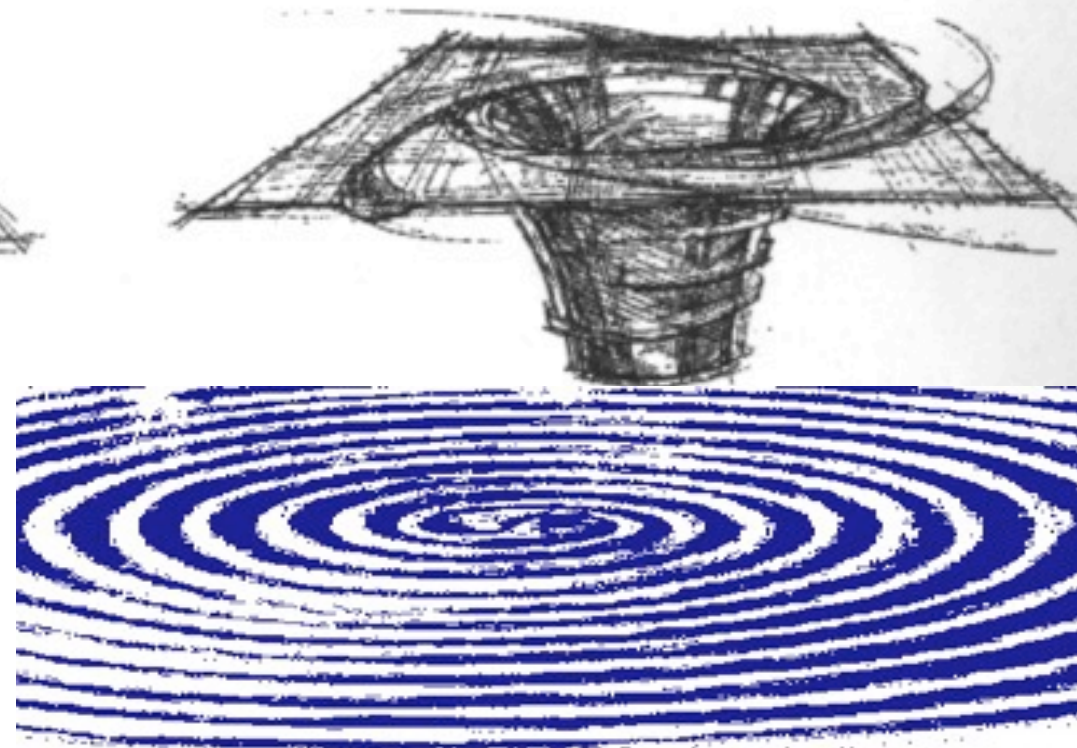
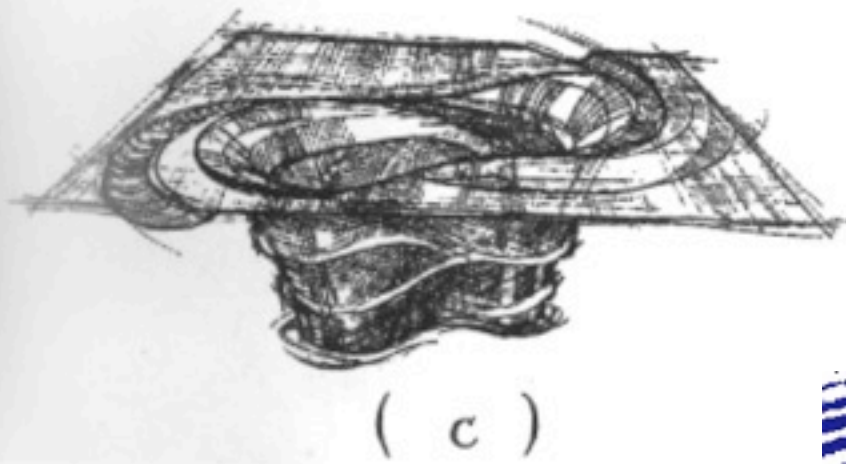
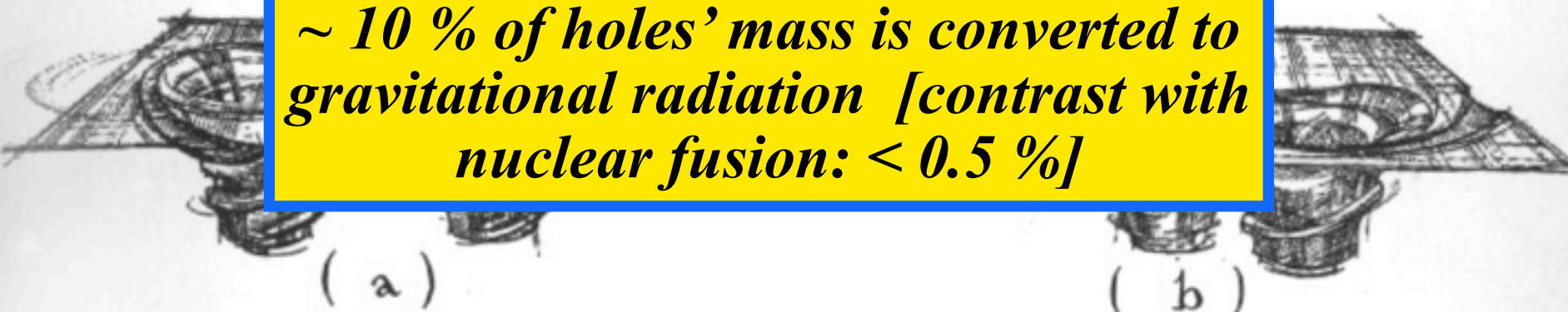
- ***Simulating Generic Black-Hole Binaries:***
 - » Princeton (Pretorius),
 - » Rochester Institute of Technology (Campanelli, ...),
 - » Goddard Spaceflight Center (Centrella, ...),
 - » U. Illinois (Shapiro, ...),
 - » Albert Einstein Institute & LSU (Rezolla, Pollney, ...),
 - » U. Jena (Bruegmann, ...),
 - » Georgia Tech (Laguna, ...),
 - » U. Texas (Matzner, ...),
 - » Perimeter/Guelph (Lehner, ...)
 - » U. Maryland (Tiglio, ...),
 - » Florida Atlantic U. (Tichy, ...),
 - » Barcelona (Sperhake, ...),
 - » Cornell/Caltech/CITA (Teukolsky, Kidder, Scheel, Pfeiffer, Szilagyi), ...

Black Hole / Black Hole Collisions: The most violent events in the Universe



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*~ 10 % of holes' mass is converted to
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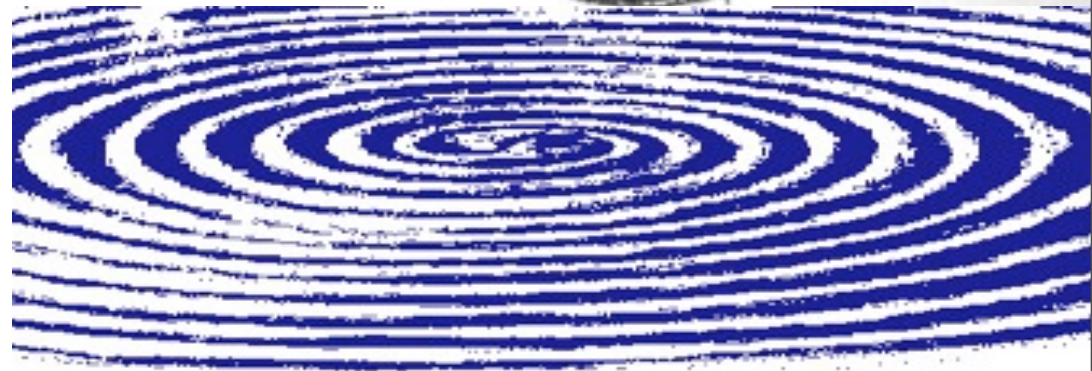


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*GW Luminosity $\sim 0.1 Mc^2 / (100 GM/c^3)$
 $= 0.001 c^5/G \sim 10^{24} L_{\text{sun}} \sim 10^4 L_{\text{EM universe}}$*

(c)



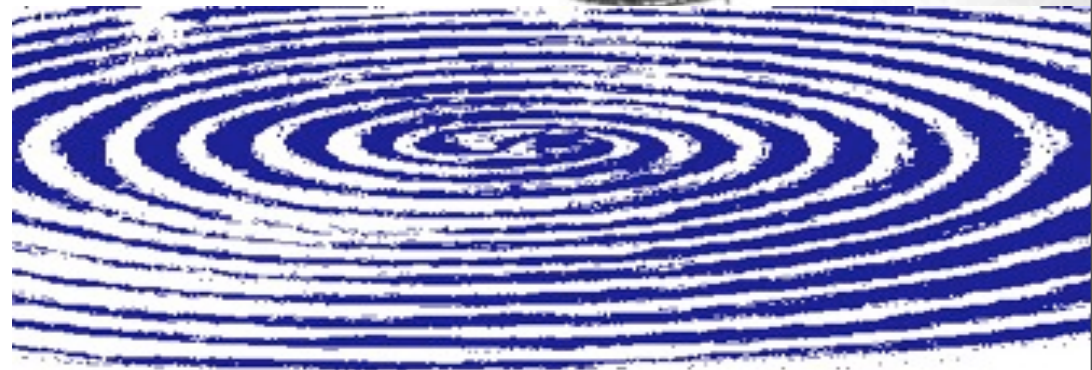
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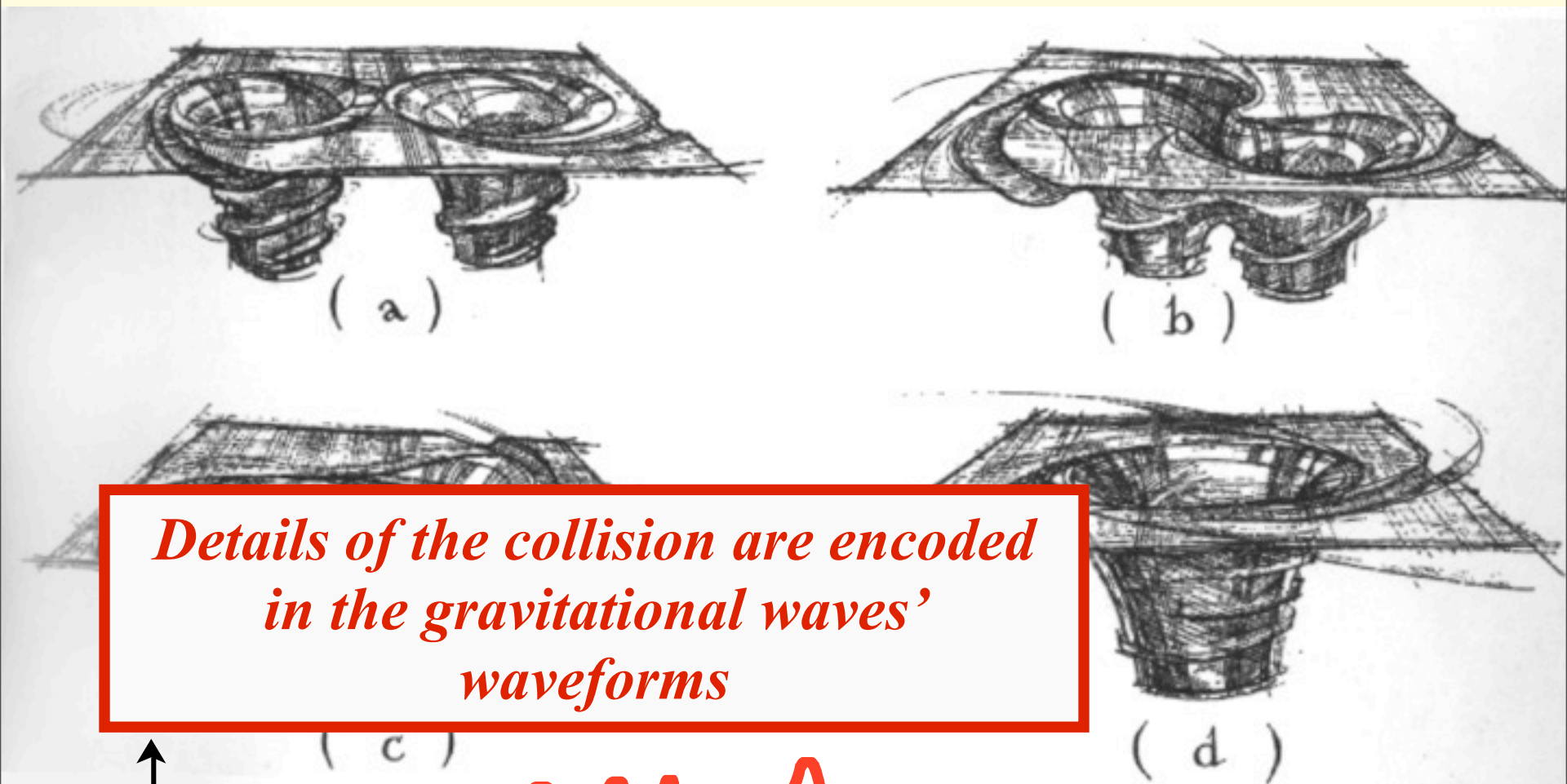
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*No Electromagnetic Waves emitted whatsoever -
except from, e.g., disturbed accretion discs*

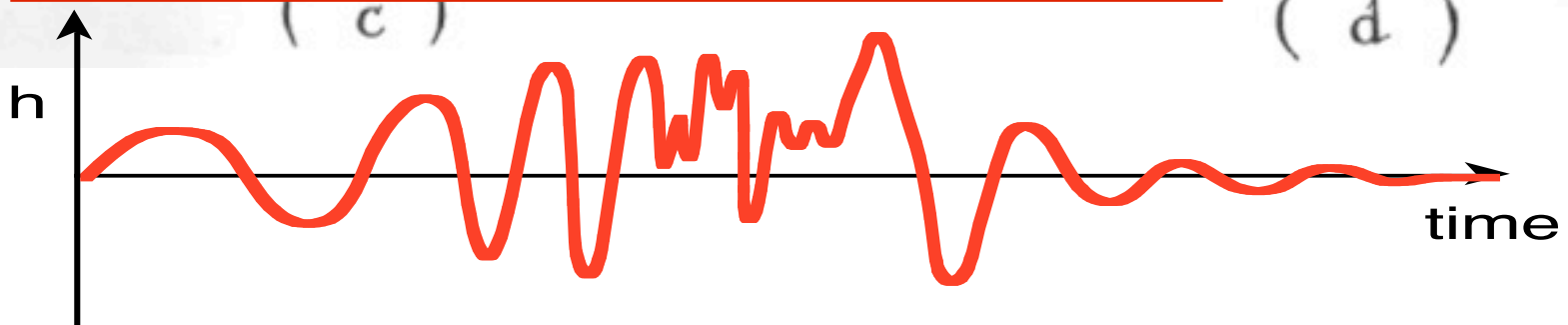
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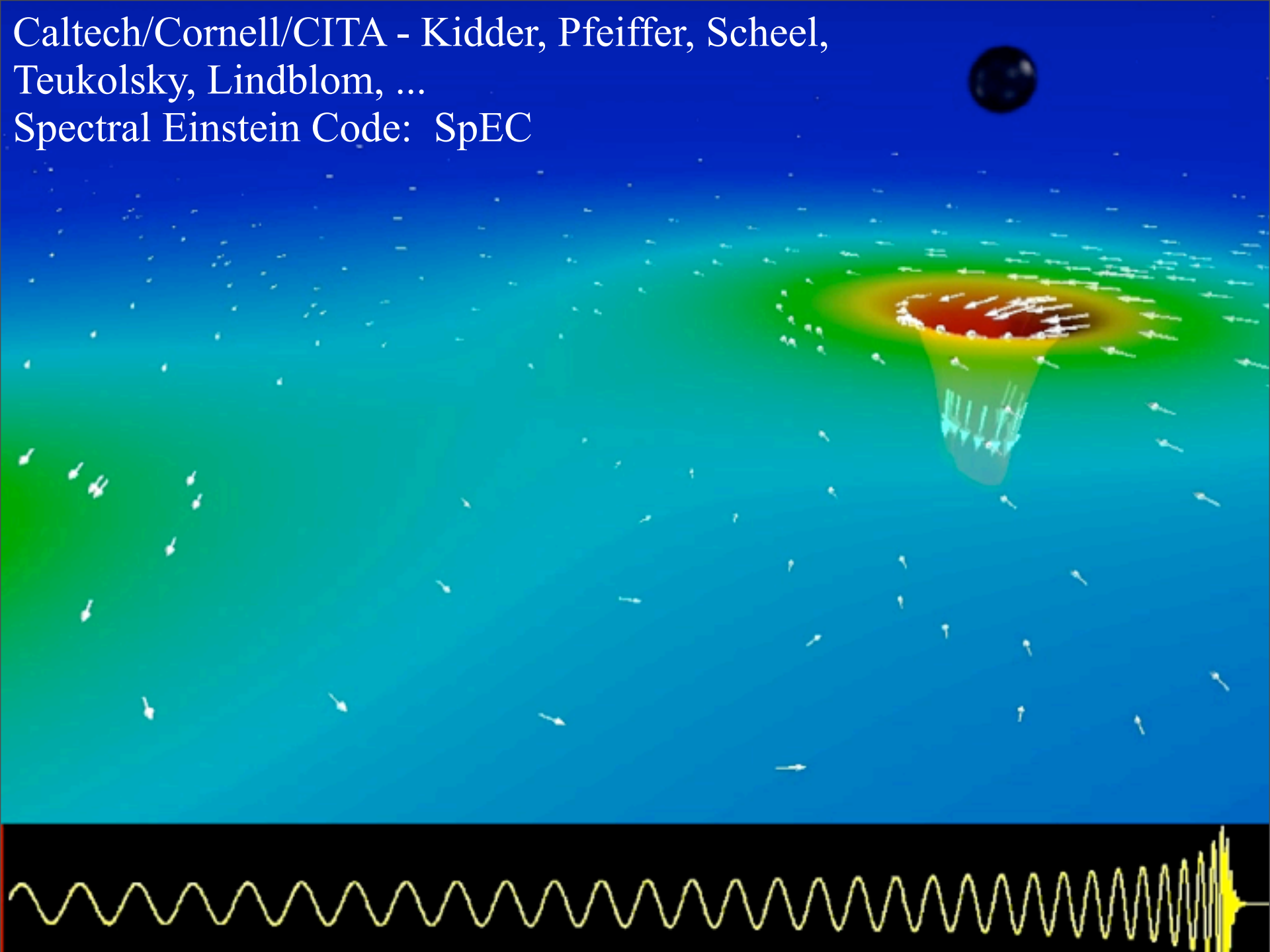
Collisions of Black Holes: The most violent events in the Universe



*Details of the collision are encoded
in the gravitational waves'
waveforms*



Caltech/Cornell/CITA - Kidder, Pfeiffer, Scheel,
Teukolsky, Lindblom, ...
Spectral Einstein Code: SpEC



Monday 2 January 12

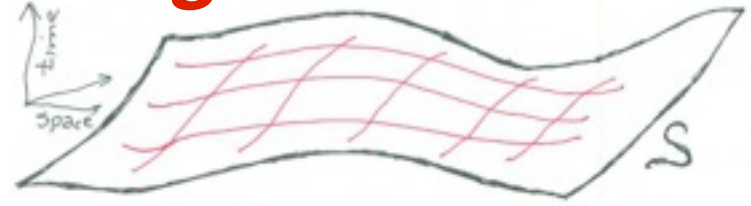
A New Way to Visualize the Curvature of Spacetime

**Rob Owen, Jeandrew Brink, Yanbei Chen,
Jeff Kaplan, Geoffrey Lovelace, Keith Matthews,
David Nichols, Mark Scheel, Fan Zhang,
Aaron Zimmerman, and Kip Thorne**

Caltech, Cornell, and NiTheP (South Africa)

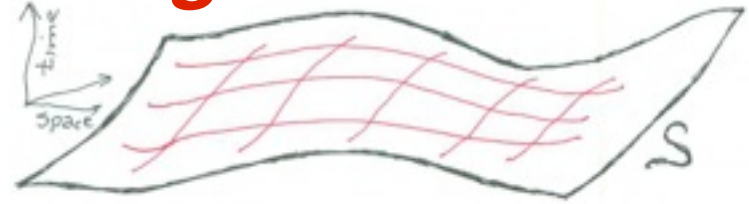
Physical Review Letters , **106**, 151101 (2011)

Tidal Field & Frame-Drag Field



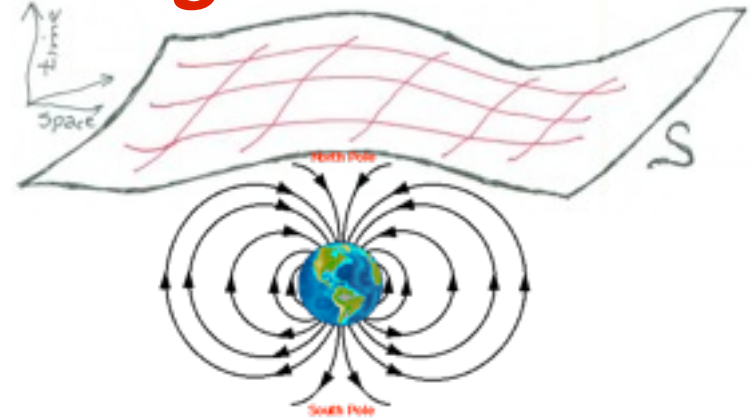
Tidal Field & Frame-Drag Field

- Slice spacetime into space plus time



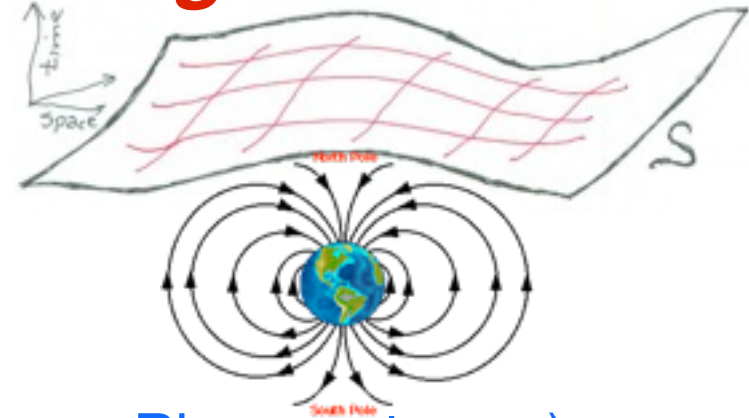
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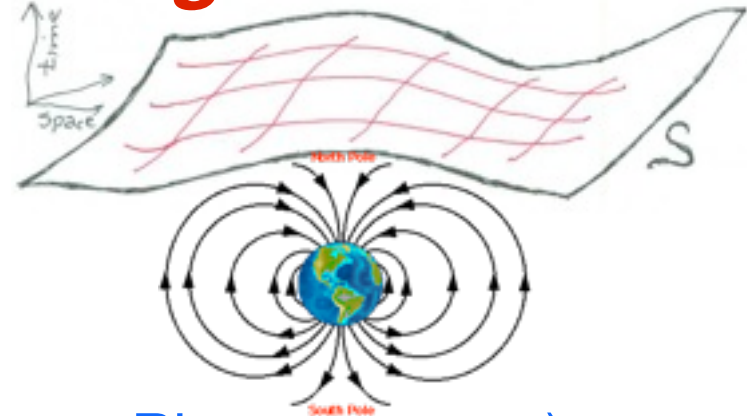


- Weyl curvature tensor (in vacuum, same as Riemann tensor) \rightarrow “electric” part \mathcal{E}_{jk} and “magnetic” part \mathcal{B}_{jk}

$$\mathcal{E}_{jk} = C_{0j0k} \quad \mathcal{B}_{jk} = \frac{1}{2} \epsilon_{jpk} C^{pq}_{k0} \quad \text{Symmetric, Trace-Free (STF) tensors}$$

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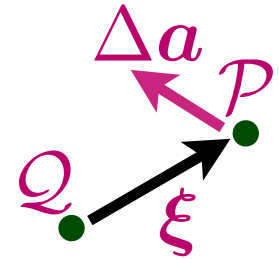
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- \mathcal{E}_{jk} describes tidal accelerations

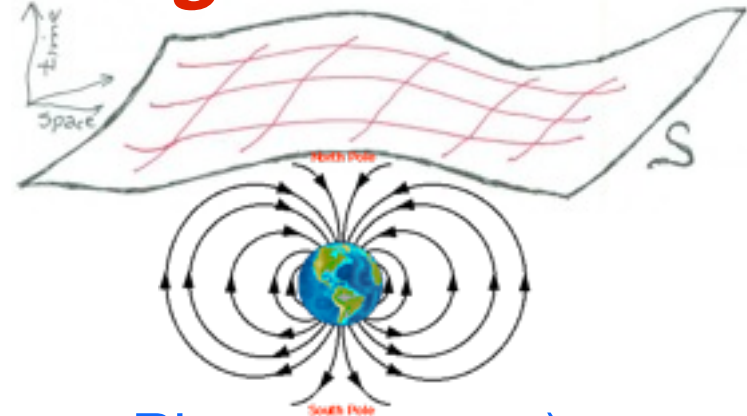
$$\Delta a_j = -\mathcal{E}_{jk} \xi^k$$

We call \mathcal{E}_{jk} the **tidal field**



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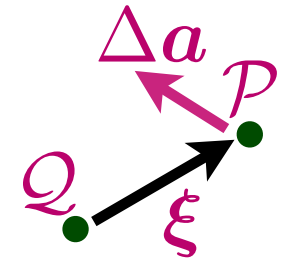


- Weyl curvature tensor (in vacuum, same as Riemann tensor) \rightarrow “electric” part \mathcal{E}_{jk} and “magnetic” part \mathcal{B}_{jk}

$$\mathcal{E}_{jk} = C_{0j0k} \quad \mathcal{B}_{jk} = \frac{1}{2} \epsilon_{jpk} C^{pq}_{k0} \quad \text{Symmetric, Trace-Free (STF) tensors}$$

- \mathcal{E}_{jk} describes **tidal accelerations**

$$\Delta a_j = -\mathcal{E}_{jk} \xi^k$$



We call \mathcal{E}_{jk} the **tidal field**

- \mathcal{B}_{jk} describes **differential frame dragging**: Gyroscope at P precesses relative to inertial frames at Q with angular velocity

$$\Delta \Omega_j = \mathcal{B}_{jk} \xi^k$$

We call \mathcal{B}_{jk} the **frame-drag field**

Tendex Lines and their Tendicities

- Any **STF tensor** is completely characterized by **three orthogonal eigenvectors**, and their **eigenvalues**.
- For the tidal field \mathcal{E}_{ab} , the **integral curve of an eigenvector n** is called its *Tendex Line*; its **eigenvalue** is its *Tendicity*

Tendex Lines and their Tendicities

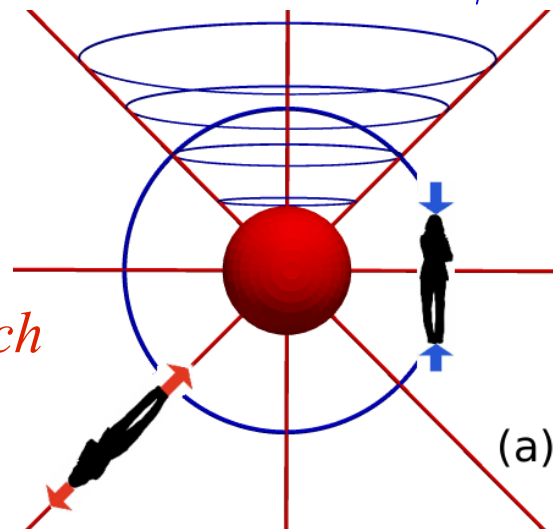
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Tendex Lines and their Tendicities

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- For the tidal field \mathcal{E}_{jk} , the **integral curve of an eigenvector n** is called its **Tendex Line**; its **eigenvalue \mathcal{E}_{nn}** is its **Tendicity**
- Example: Tidal field above the Earth or outside a Nonrotating BH

» *eigenvector fields* $e_{\hat{r}}, e_{\hat{\theta}}, e_{\hat{\phi}}$

Three sets of tendex lines, each with its own tendicity

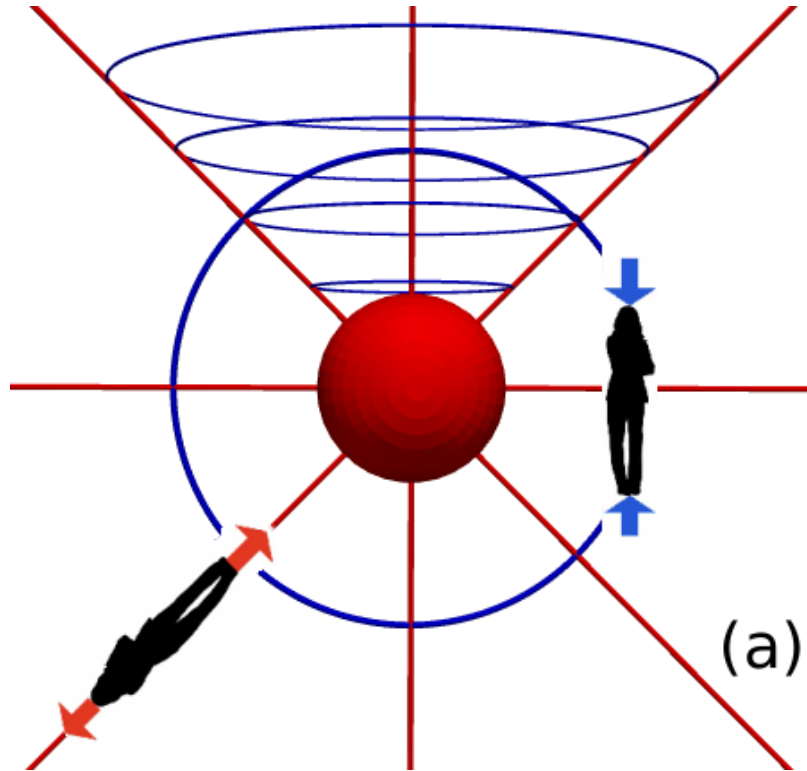


$\mathcal{E}_{\hat{r}\hat{r}} < 0$ *tidal stretch*
negative tendicity

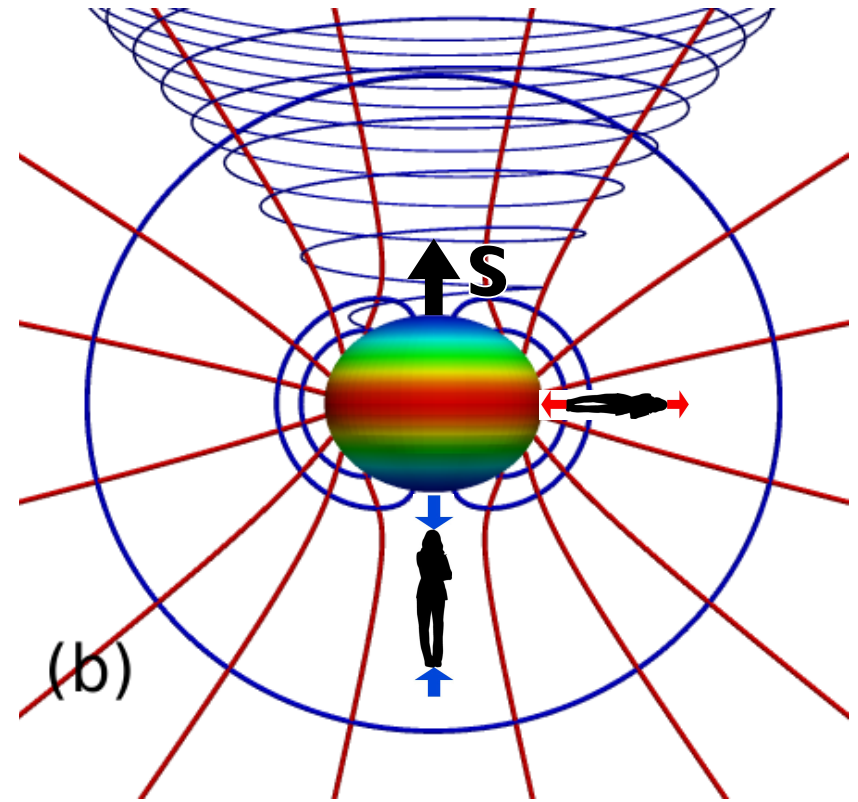
$\mathcal{E}_{\hat{\theta}\hat{\theta}} > 0$ *tidal squeeze*
positive tendicity

Tendexes around Black Holes

Non-Spinning Black Hole

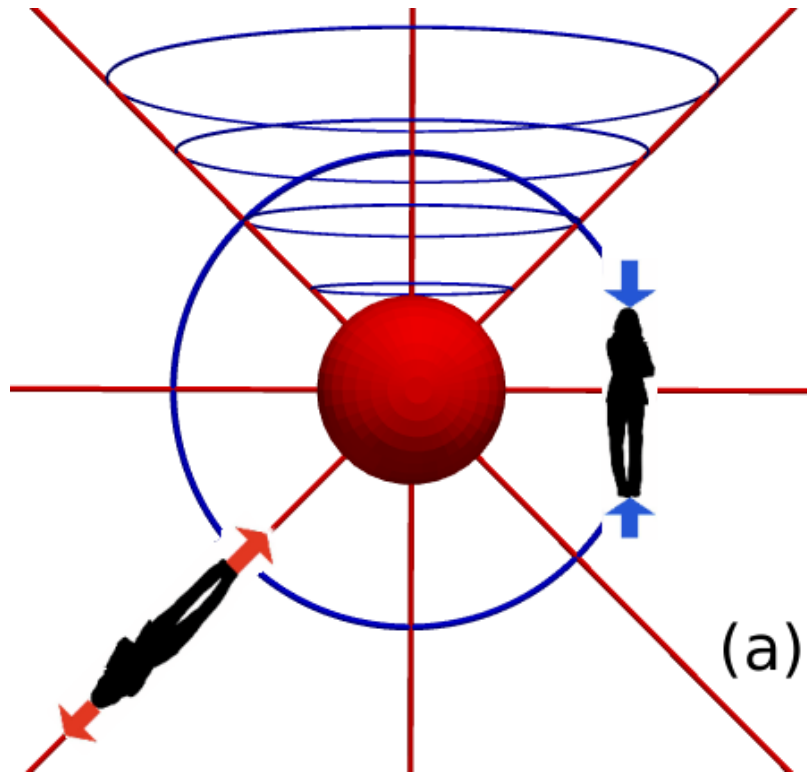


Fast Spinning Black Hole, $a=0.95$



Tendexes around Black Holes

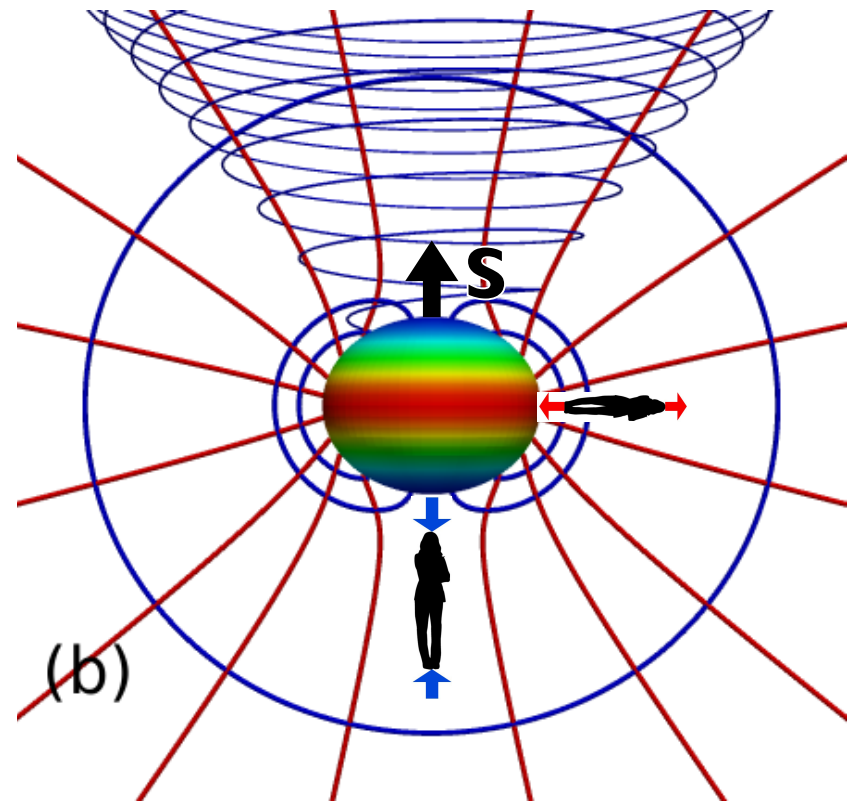
Non-Spinning Black Hole



(a)

Horizon Tendex:
region of large tendicity

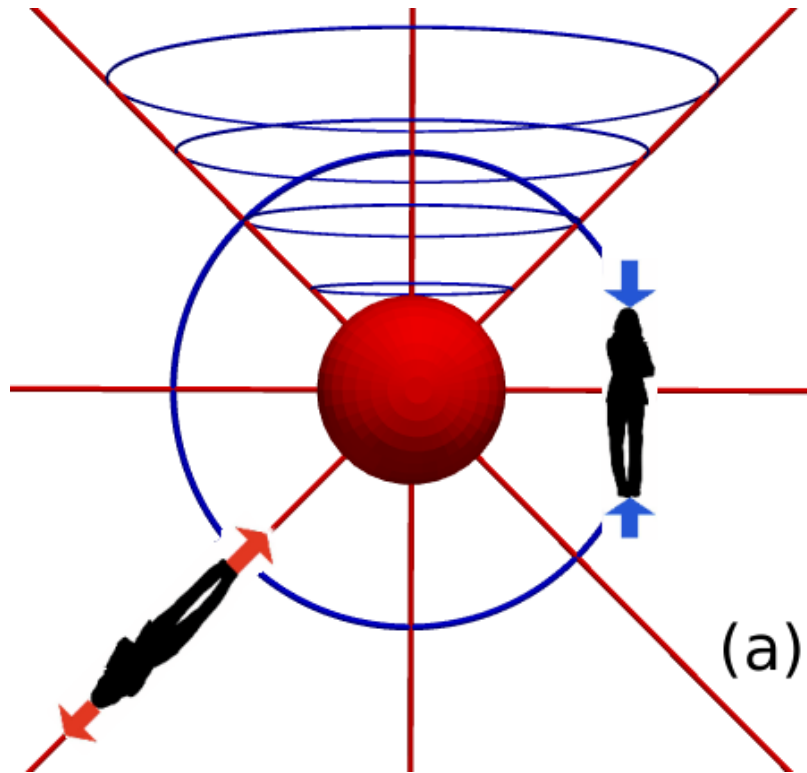
Fast Spinning Black Hole, $a=0.95$



(b)

Tendexes around Black Holes

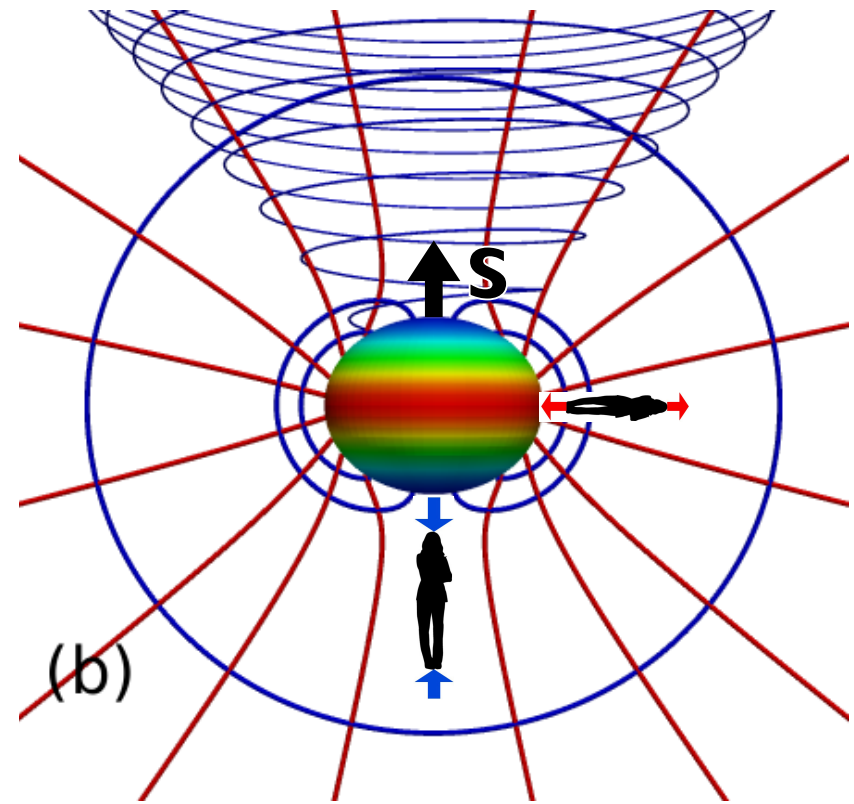
Non-Spinning Black Hole



(a)

Horizon Tendex:
region of large tendicity

Fast Spinning Black Hole, $a=0.95$



(b)

Horizon Tendicity: \mathcal{E}_{NN}

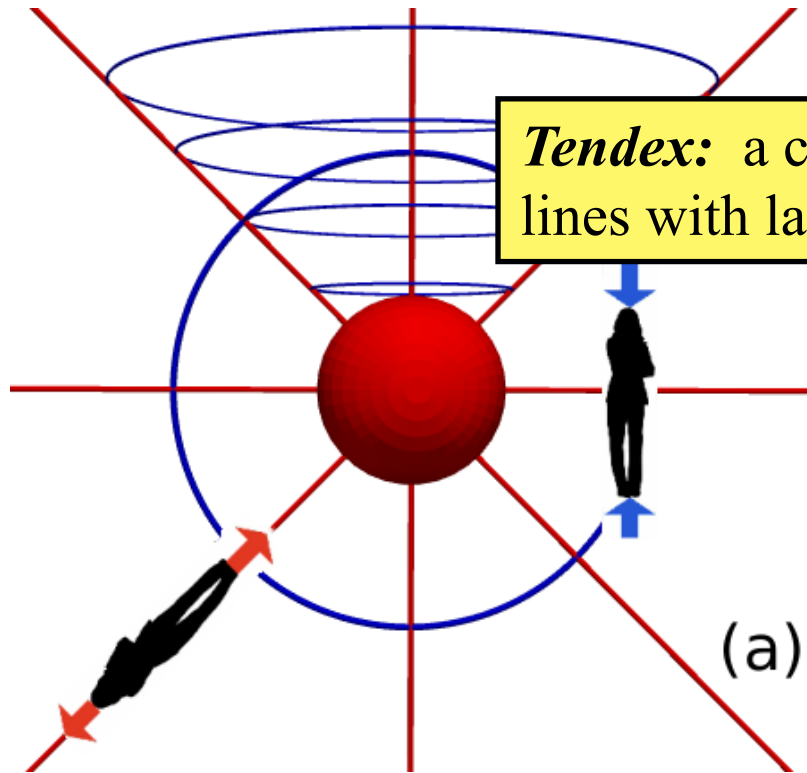
Blue: positive tendicity

Green: near zero

Red: negative tendicity

Tendexes around Black Holes

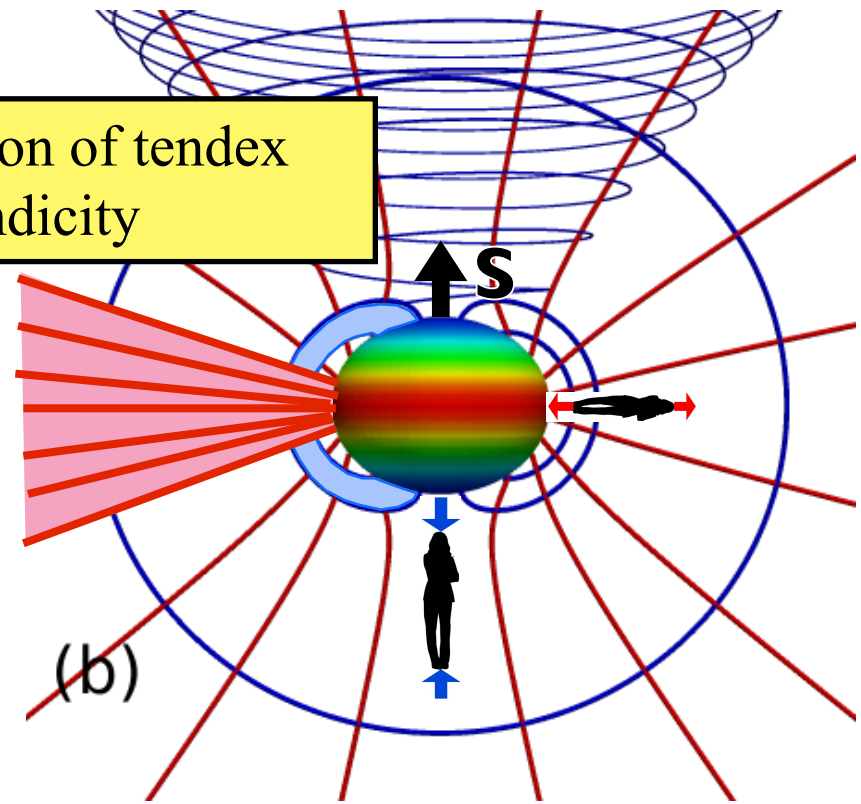
Non-Spinning Black Hole



Tendex: a collection of tendex lines with large tendicity

Horizon Tendex:
region of large tendicity

Fast Spinning Black Hole, $a=0.95$



Horizon Tendicity: \mathcal{E}_{NN}

Blue: positive tendicity

Green: near zero

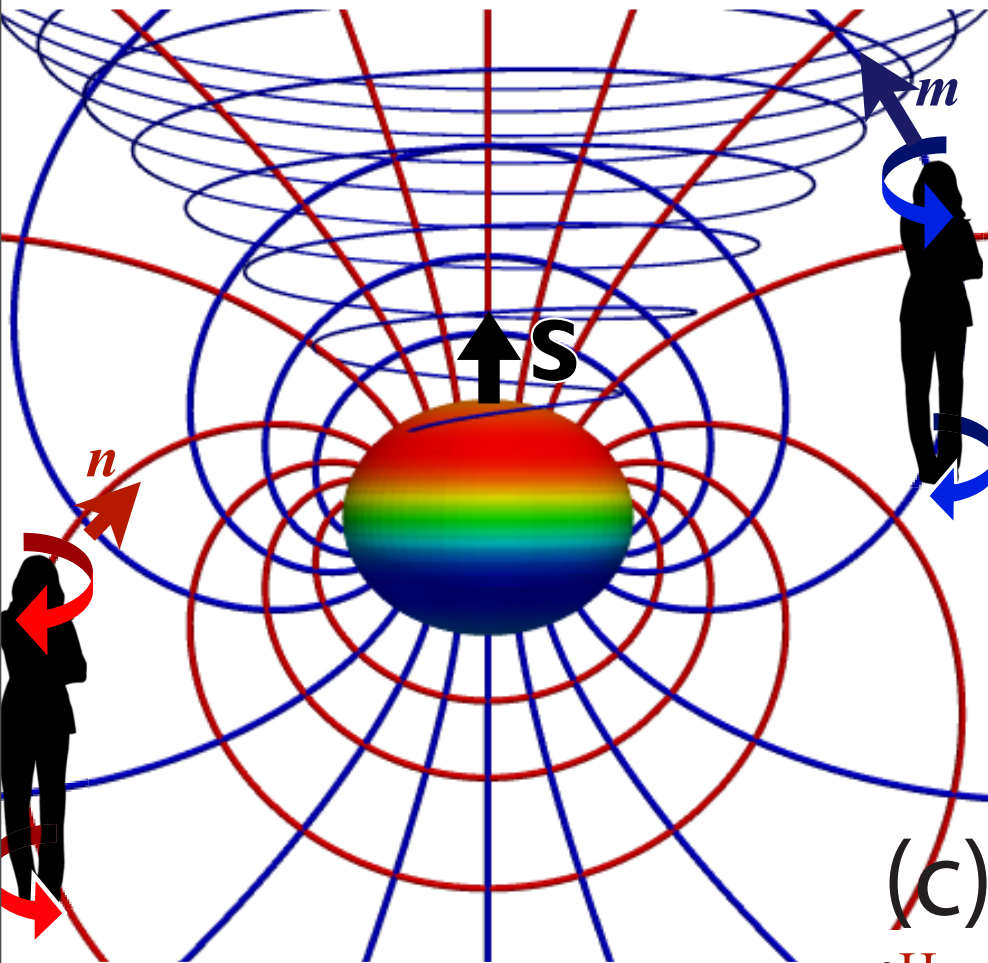
Red: negative tendicity

Vortex Lines and Their Vorticities

- For the frame-drag field \mathcal{B}_{jk} , integral curve of eigenvector field \mathbf{n} is called its *Vortex Line*; its eigenvalue \mathcal{B}_{nn} is *Vorticity*

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Fast-spinning hole, $a=0.95$

positive-vorticity

vortex lines $\mathcal{B}_{mm} > 0$

- Head sees feet dragged clockwise
- Feet see head dragged clockwise

negative-vorticity

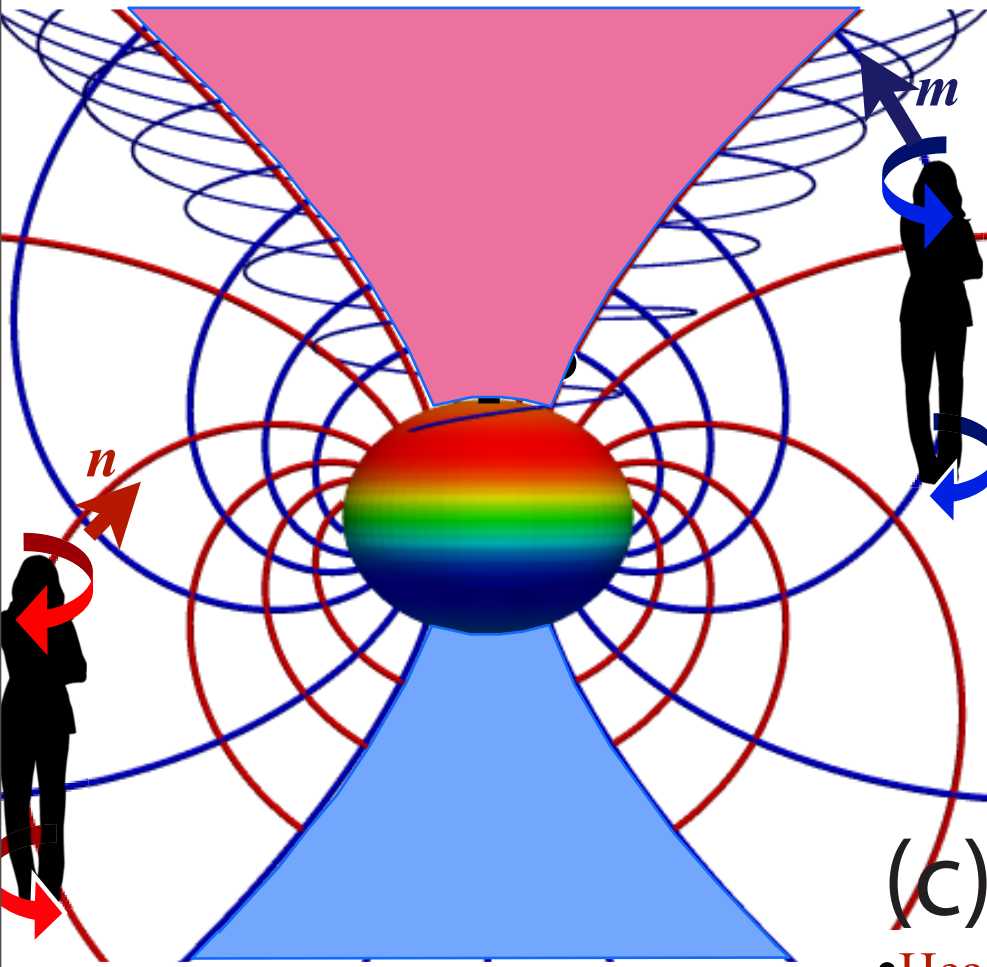
vortex lines $\mathcal{B}_{nn} < 0$

- Head sees feet dragged counter-clockwise
- Feet see head dragged counter-clockwise

(C)

Vortex Lines and Their Vorticities

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positive-vorticity

vortex lines $\mathcal{B}_{mm} > 0$

- Head sees feet dragged clockwise
- Feet see head dragged clockwise

Vortex: a collection of vortex lines with large vorticity

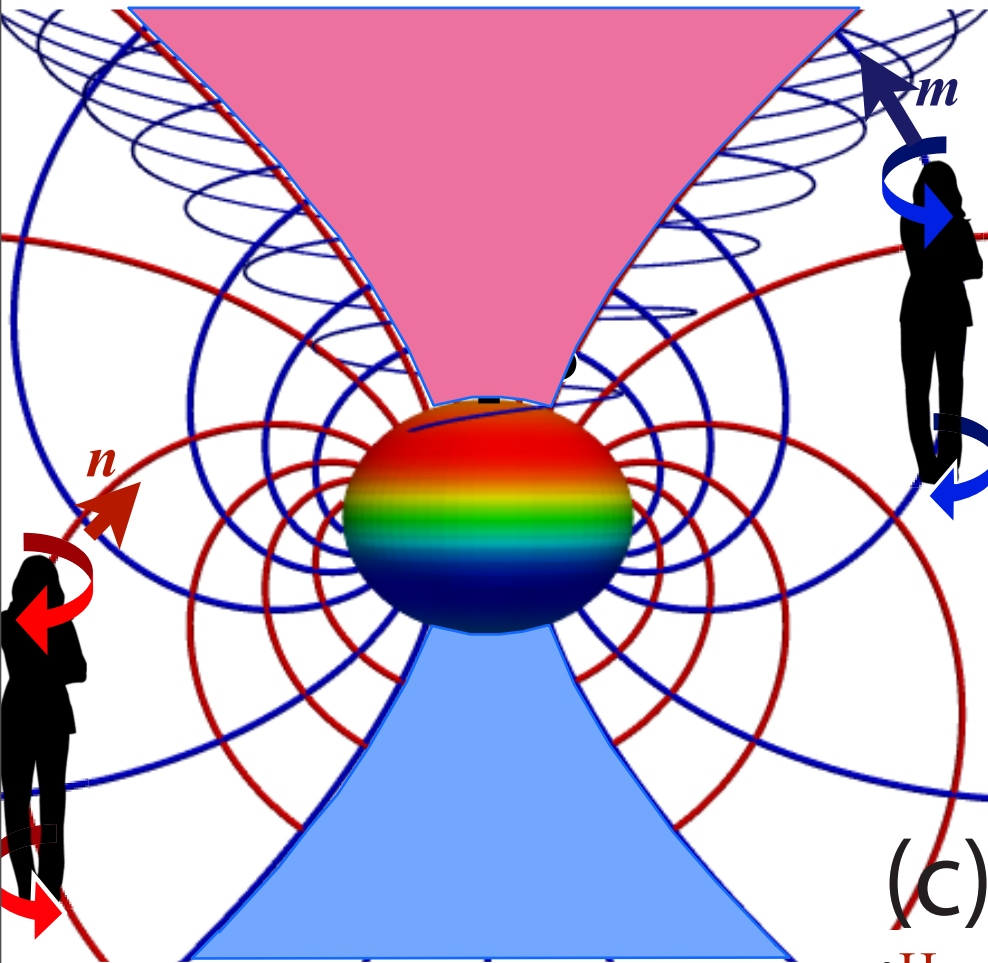
negative-vorticity

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Vortex Lines and Their Vorticities

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Horizon vorticity: \mathcal{B}_{NN}

Horizon Vortex: region of large vorticity

negative-vorticity

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- Feet see head dragged counter-clockwise

(C)

Head-On Collision with Transverse Spin

Keith Matthews, Geoffrey Lovelace, Mark Scheel

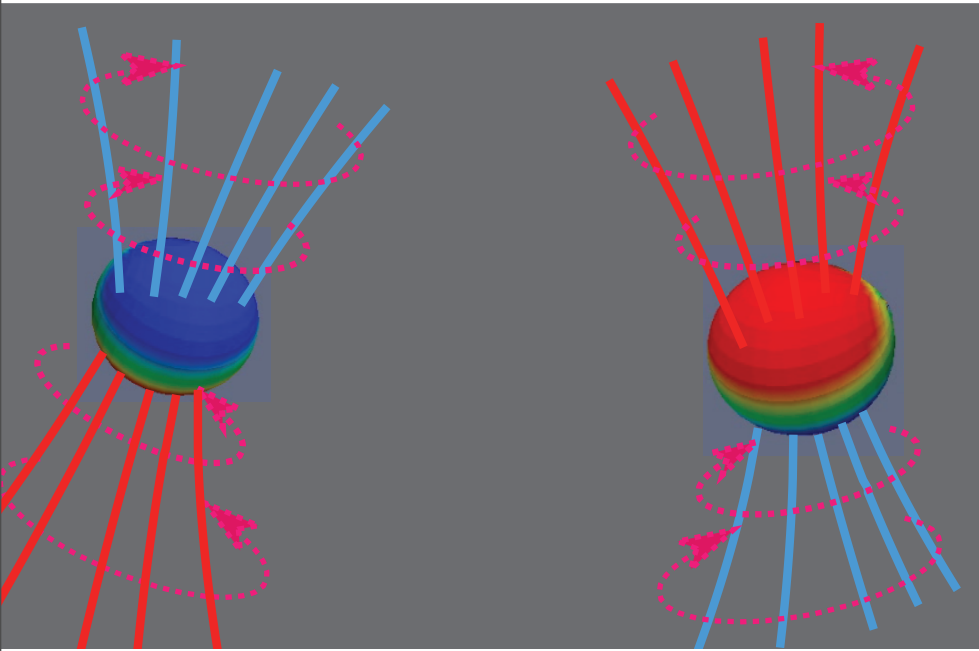
Head-On Collision with Transverse Spin

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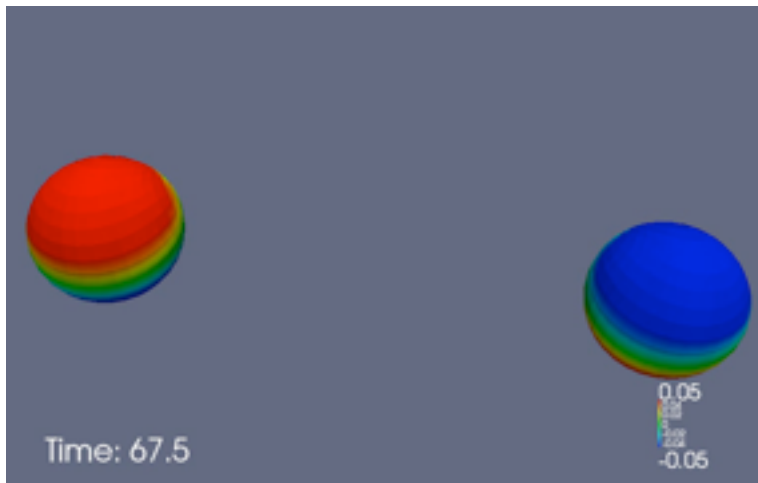
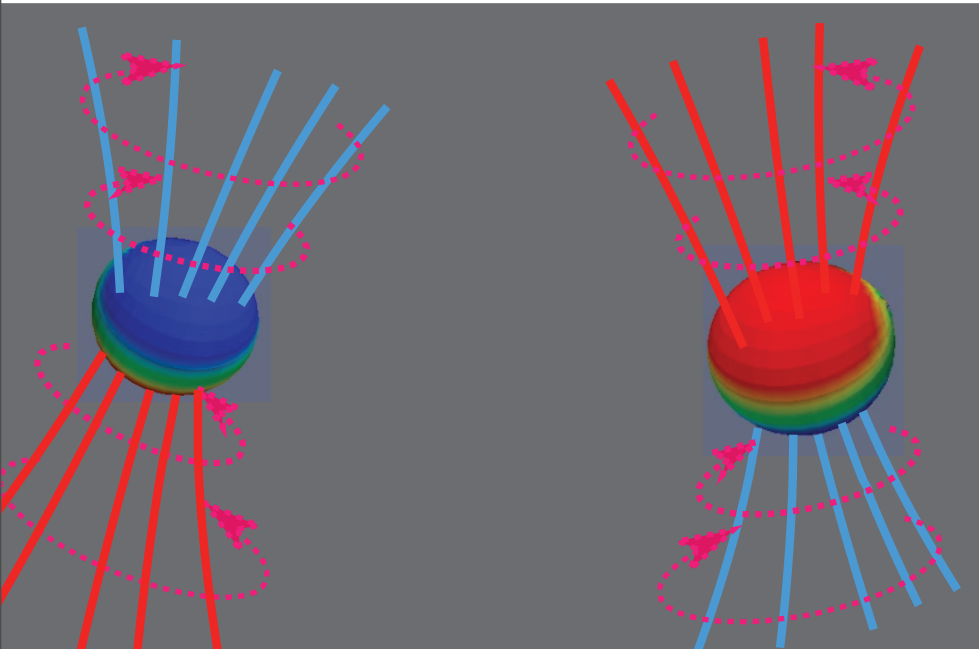
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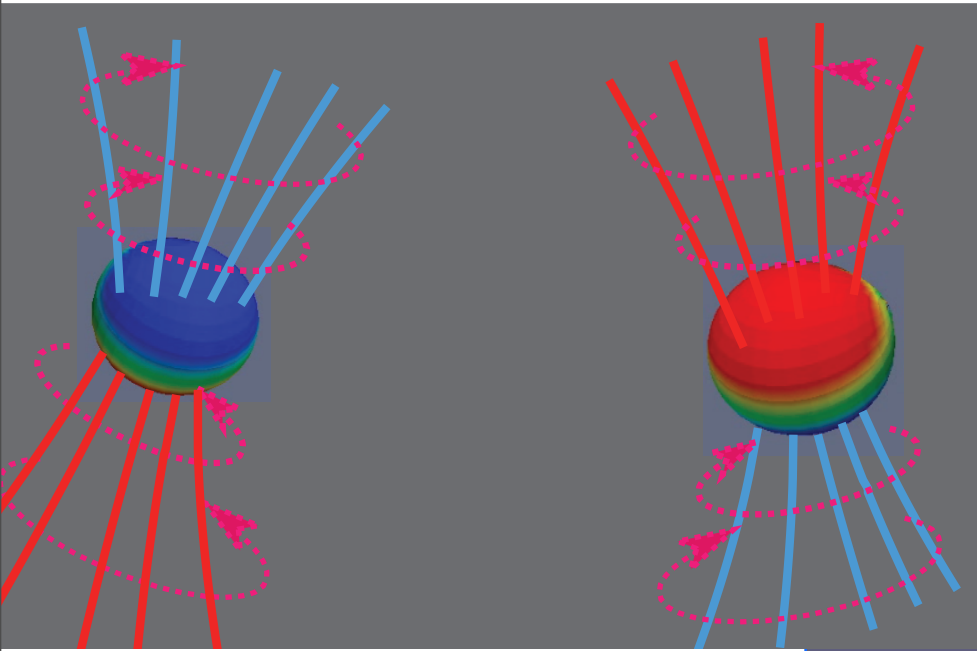
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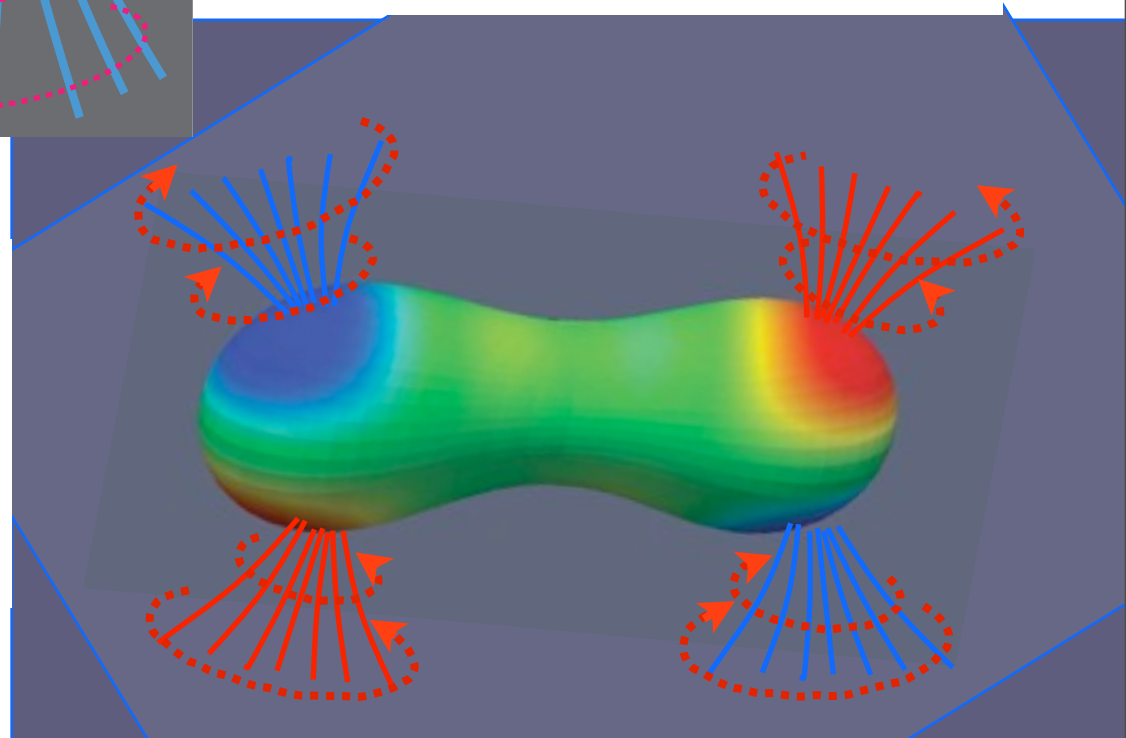
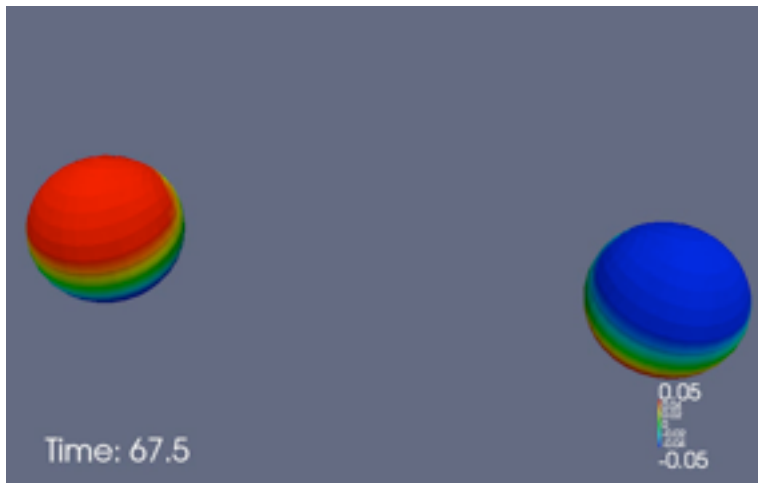


Head-On Collision with Transverse Spin

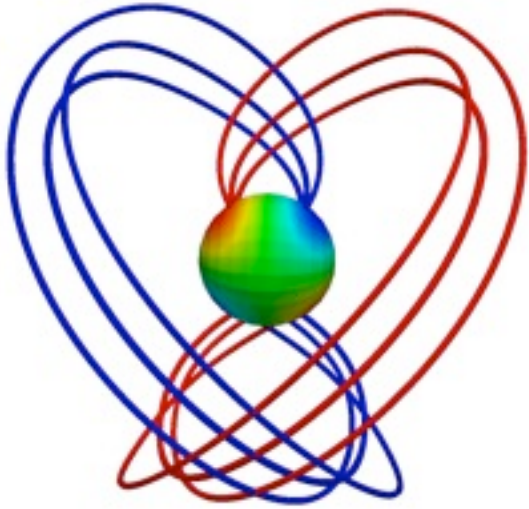
Keith Matthews, Geoffrey Lovelace, Mark Scheel



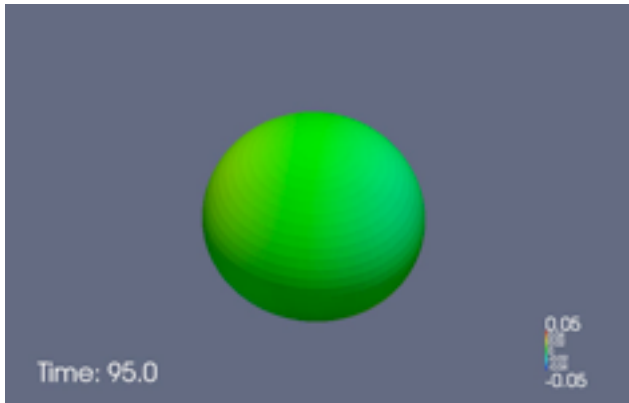
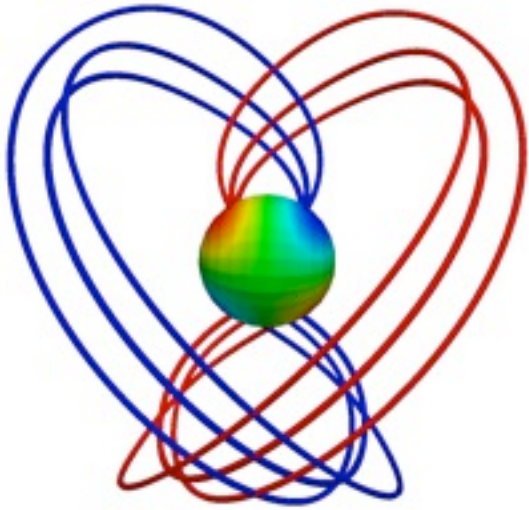
Vortexes robustly retain their individuality



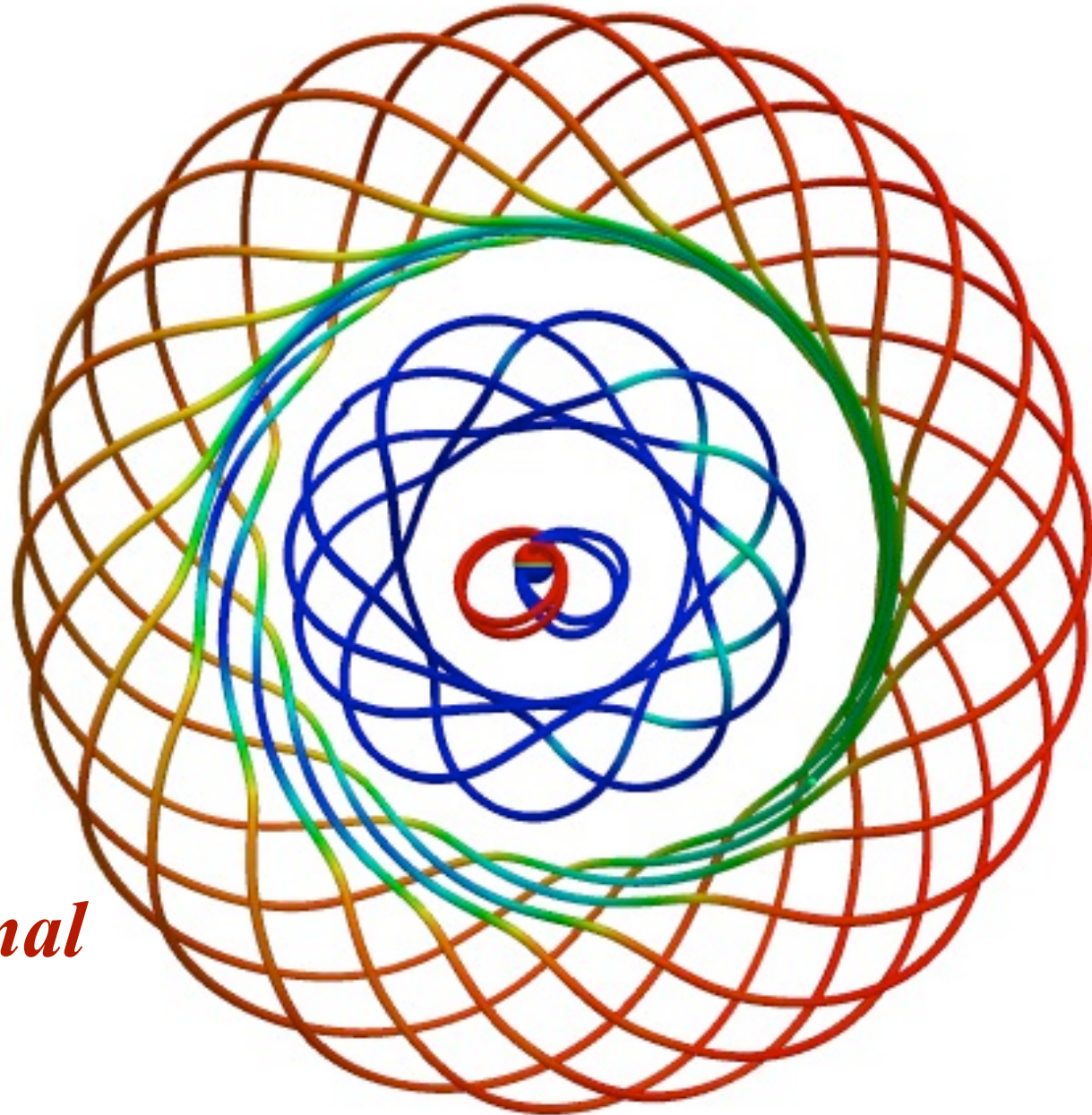
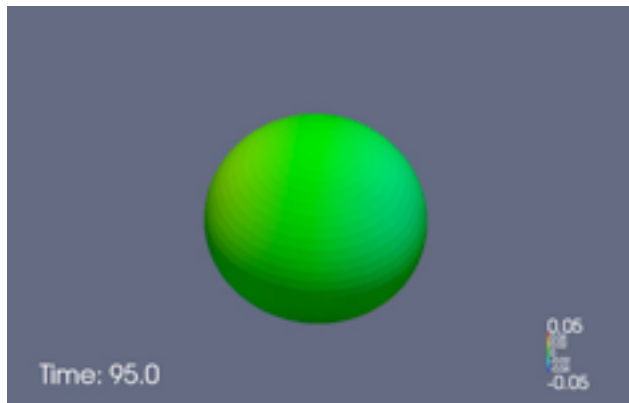
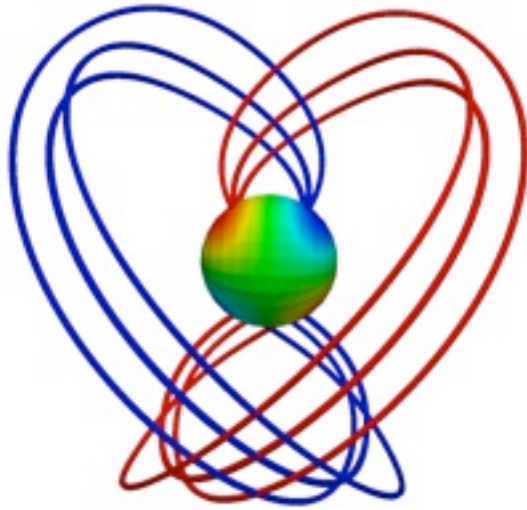
Sloshing Ejects Vortexes



Sloshing Ejects Vortexes

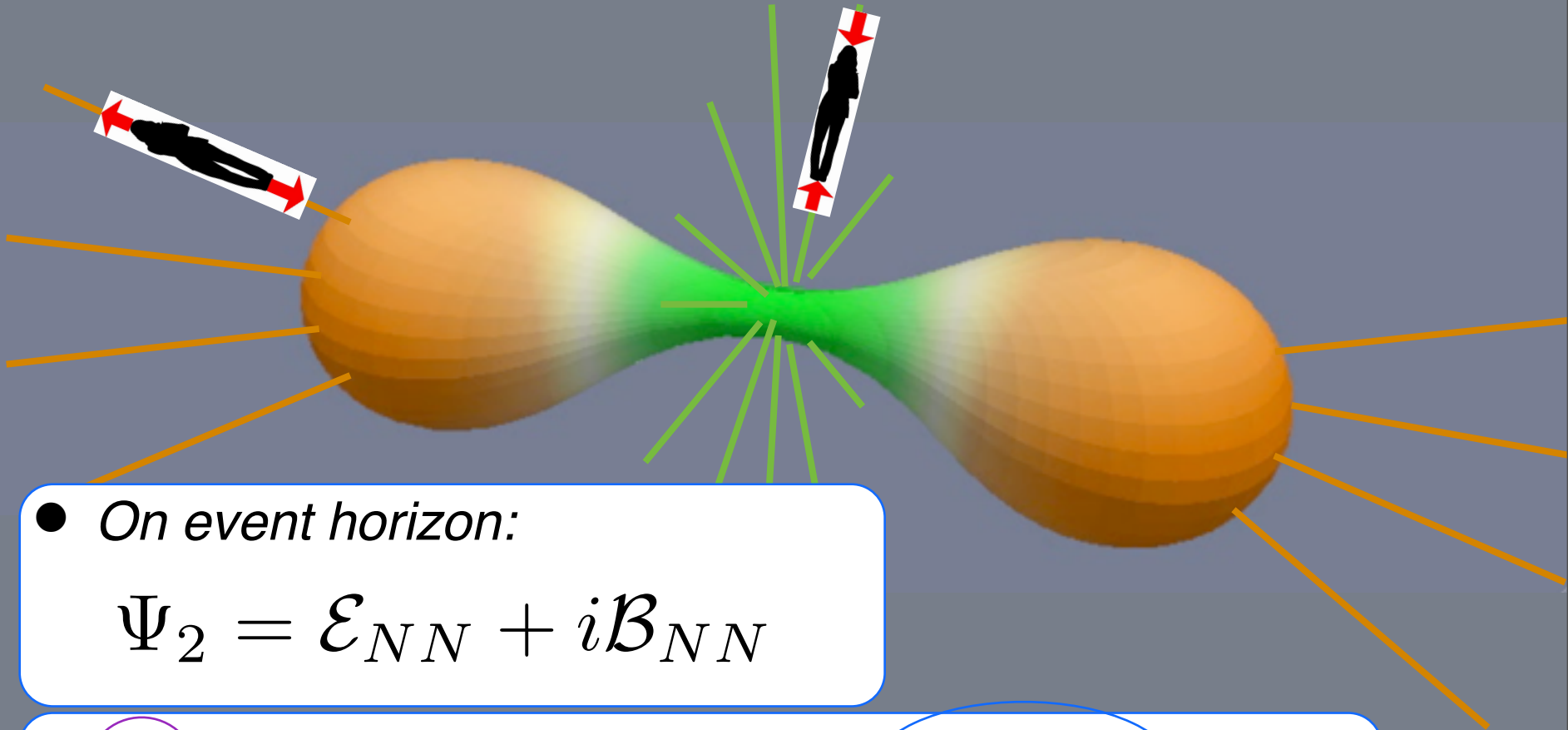


Sloshing Ejects Vortexes



*gravitational
waves*

Horizon Tendicity and Vorticity



- *On event horizon:*

$$\Psi_2 = \mathcal{E}_{NN} + i\mathcal{B}_{NN}$$

$$\mathcal{K} = \mathcal{R} + i\chi = -\Psi_2 + \mu\rho - \lambda\sigma$$

Complex
curvature

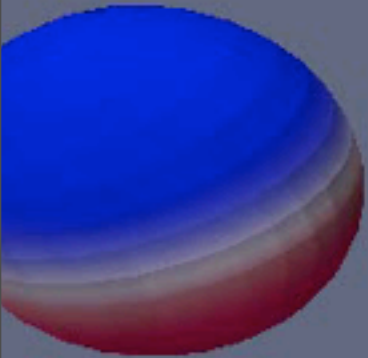
numerically small

Head-On Collision with Transverse Spin

Keith Matthews, Geoffrey Lovelace, Mark Scheel

Head-On Collision with Transverse Spin

Keith Matthews, Geoffrey Lovelace, Mark Scheel



Vortexes



Tendexes



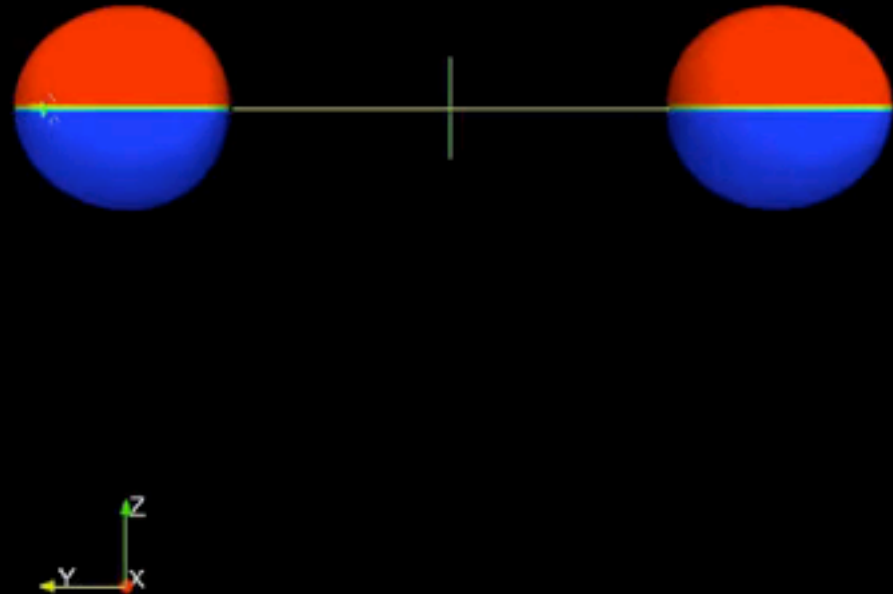
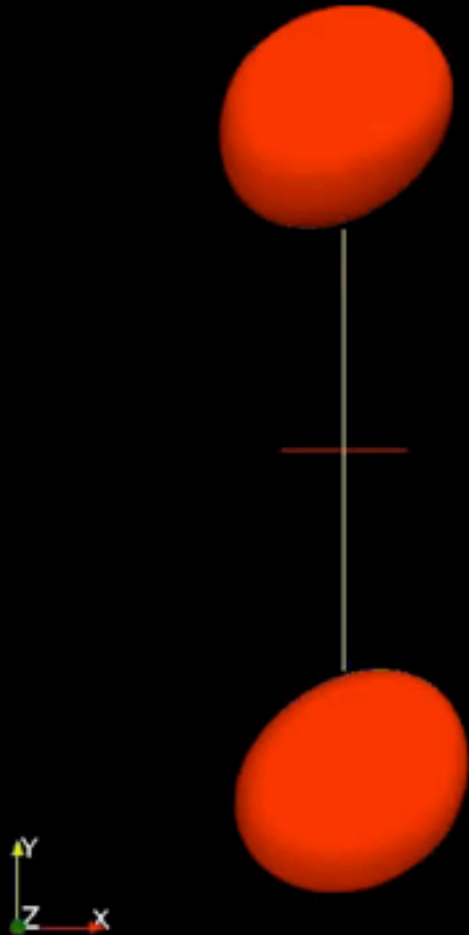
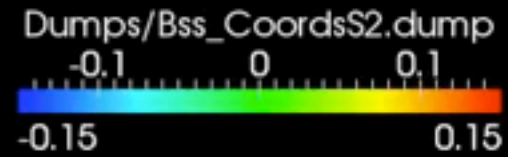
Time: 50.0

Anti-Aligned Binary : $a=0.95$

SXS: Geoffrey Lovelace, Mike Boyle,
Mark Scheel, Bela Szilagyi

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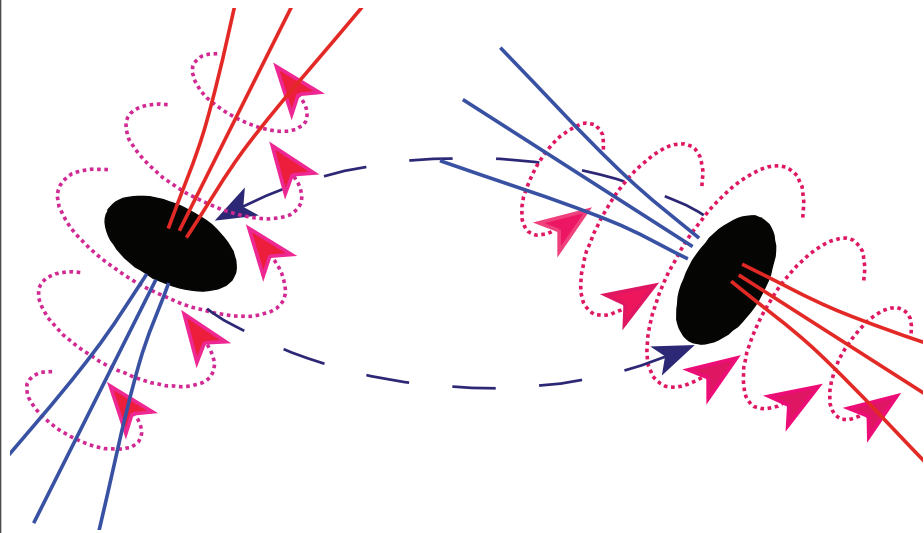


Time: 3472.889800

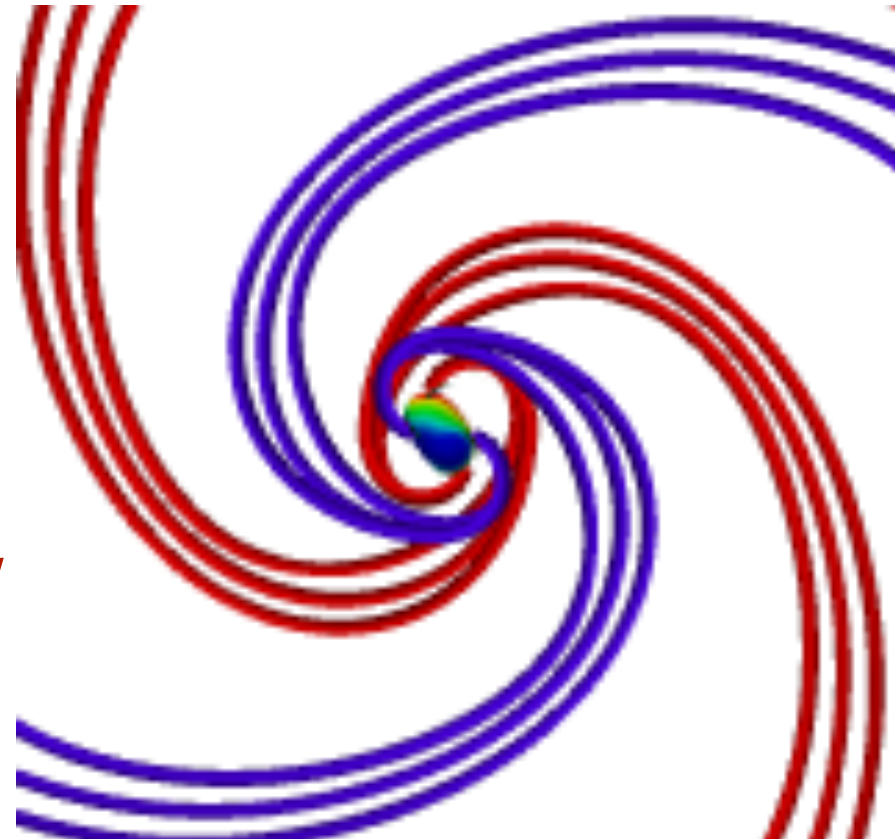
Anti-Aligned Binary : $a=0.95$

SXS: Geoffrey Lovelace, Mike Boyle,
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Generic Orbiting Collision



Spiraling Vortexes



*gravitational
waves*

Pulsations of a Nonrotating Hole [$l=m=2$ “odd-parity normal modes”]

First Golden Age:

Regge & Wheeler

Chandrasekhar & Detweiler

$$\omega = (0.747 - i 0.178) / 2M$$

Pulsations of a Nonrotating Hole [$l=m=2$ “odd-parity normal modes”]

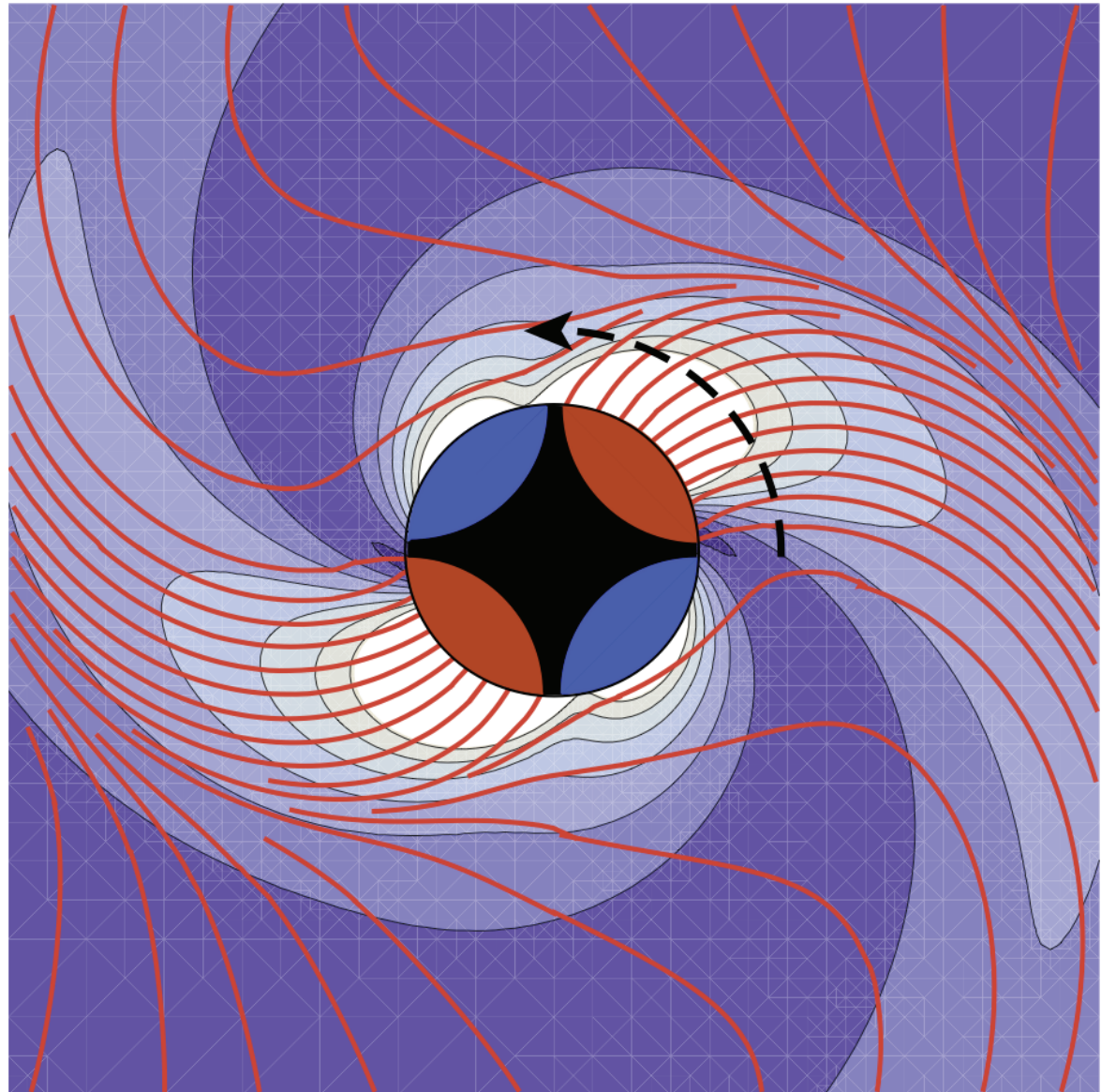
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- Spiraling vortexes traveling around hole



Pulsations of a Nonrotating Hole [$l=m=2$ “odd-parity normal modes”]

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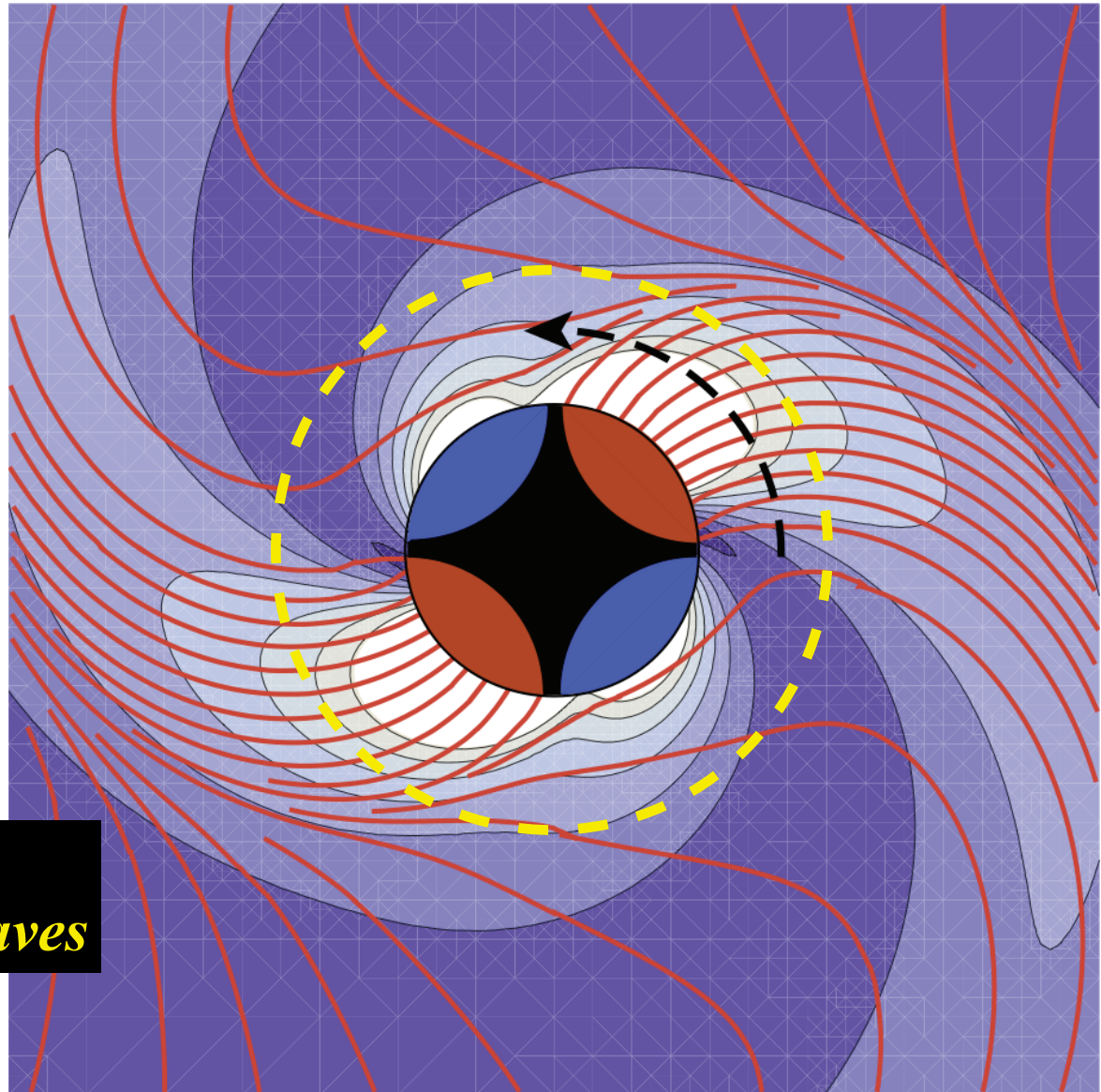
Regge & Wheeler

Chandrasekhar & Detweiler

$$\omega = (0.747 - i 0.178) / 2M$$

- Spiraling vortexes traveling around hole

*Near-hole vortexes
generate gravitational waves*



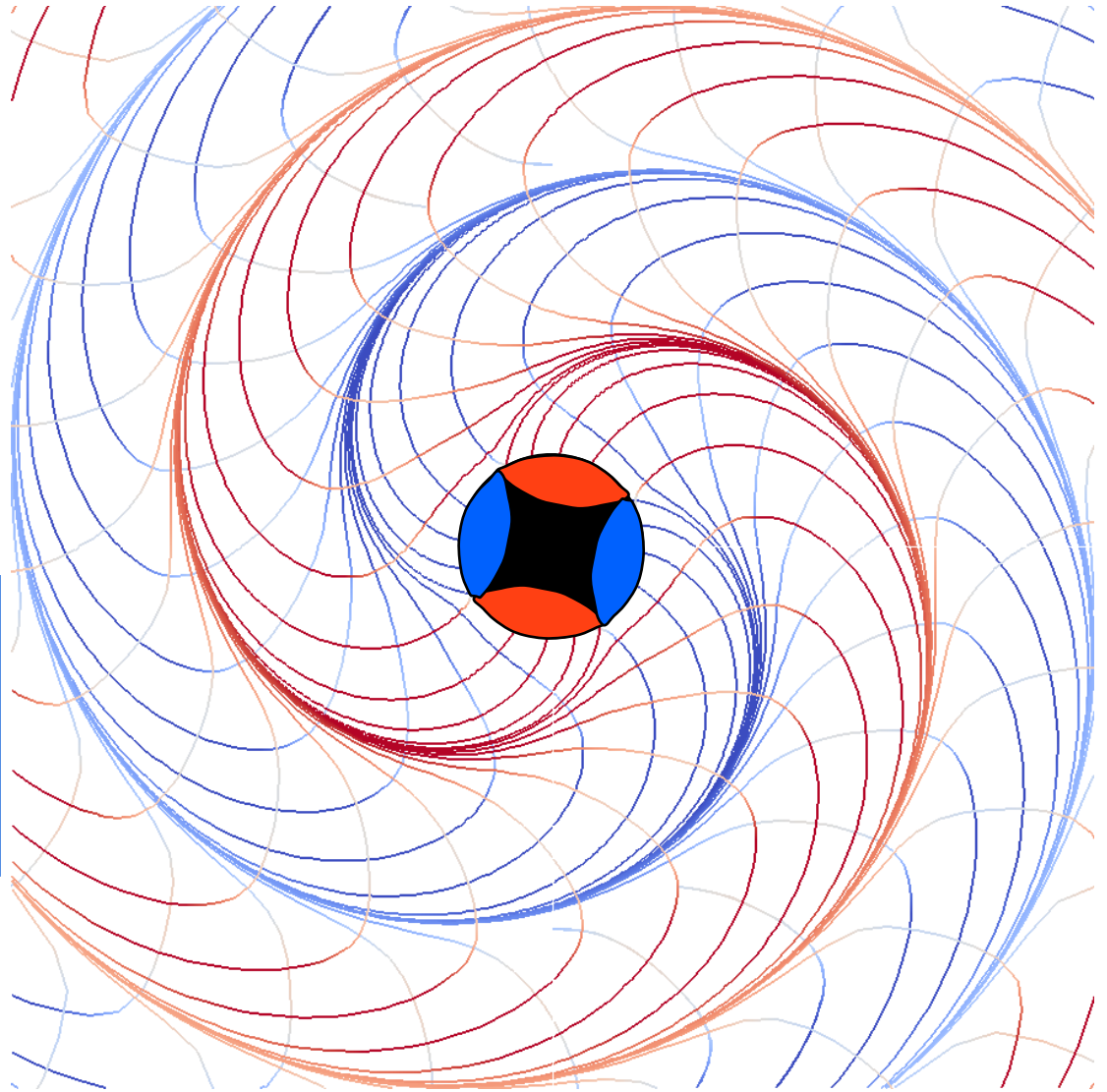
Pulsations of a Nonrotating Hole [$l=m=2$ “odd-parity normal modes”]

Old Golden Age:

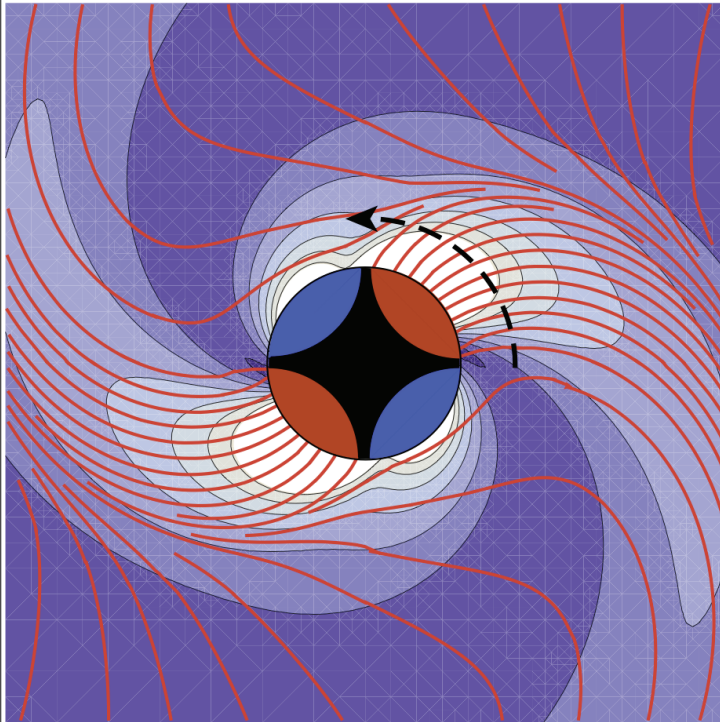
Regge & Wheeler,
Chandrasekhar & Detweiler

$$\omega = (0.747 - i 0.178) / 2M$$

$l=m=2$ “even-parity” normal modes: same, but vortex lines \rightarrow tendex lines for perturbation of Weyl tensor



Gravitational Wave Generation

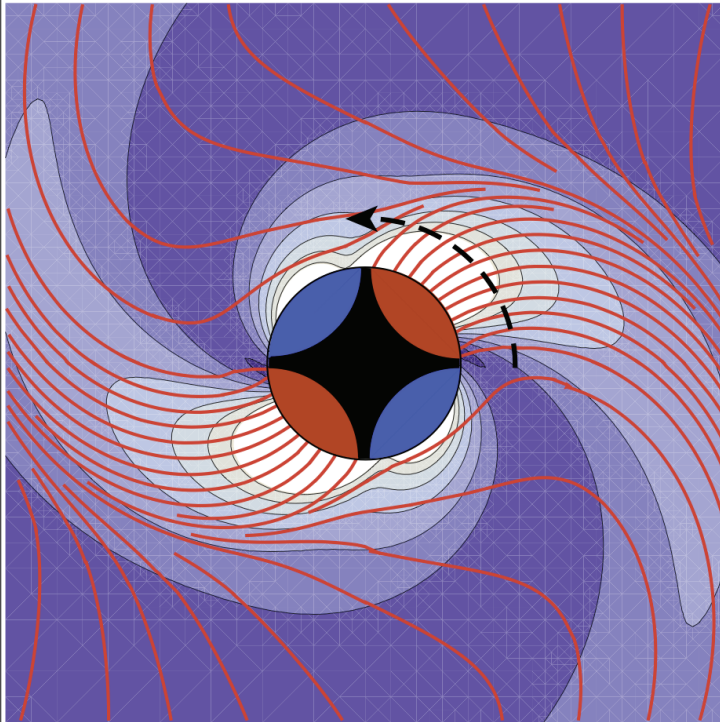


$$\frac{\partial \mathcal{E}}{\partial t} = (\nabla \times \mathcal{B})^S$$

$$\frac{\partial \mathcal{B}}{\partial t} = -(\nabla \times \mathcal{E})^S$$

In local Lorentz frame

Gravitational Wave Generation



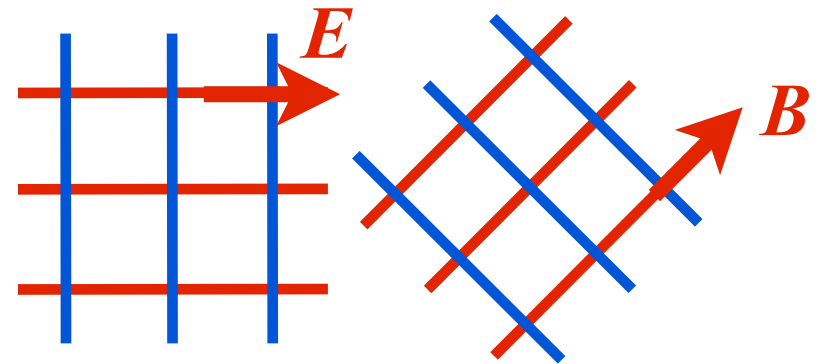
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In local Lorentz frame

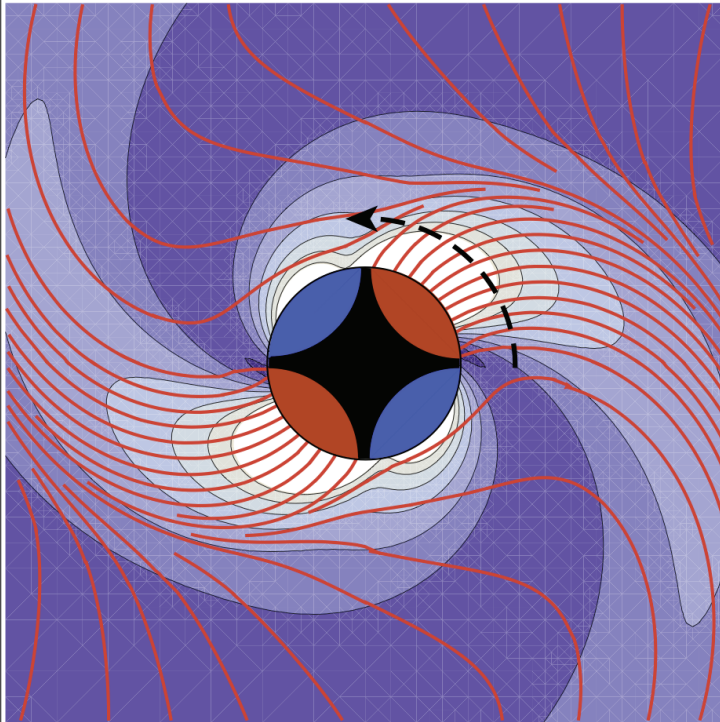
Plane Gravitational Wave

tendex lines *vortex lines*



$E \times B$ is direction of wave propagation

Gravitational Wave Generation



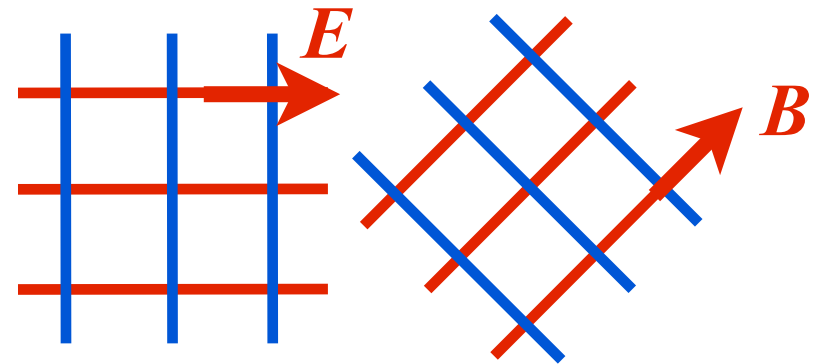
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In local Lorentz frame

Plane Gravitational Wave

tendex lines *vortex lines*



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Vortex/Tendex Research

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- Thus far: primarily phenomenology, from simulations

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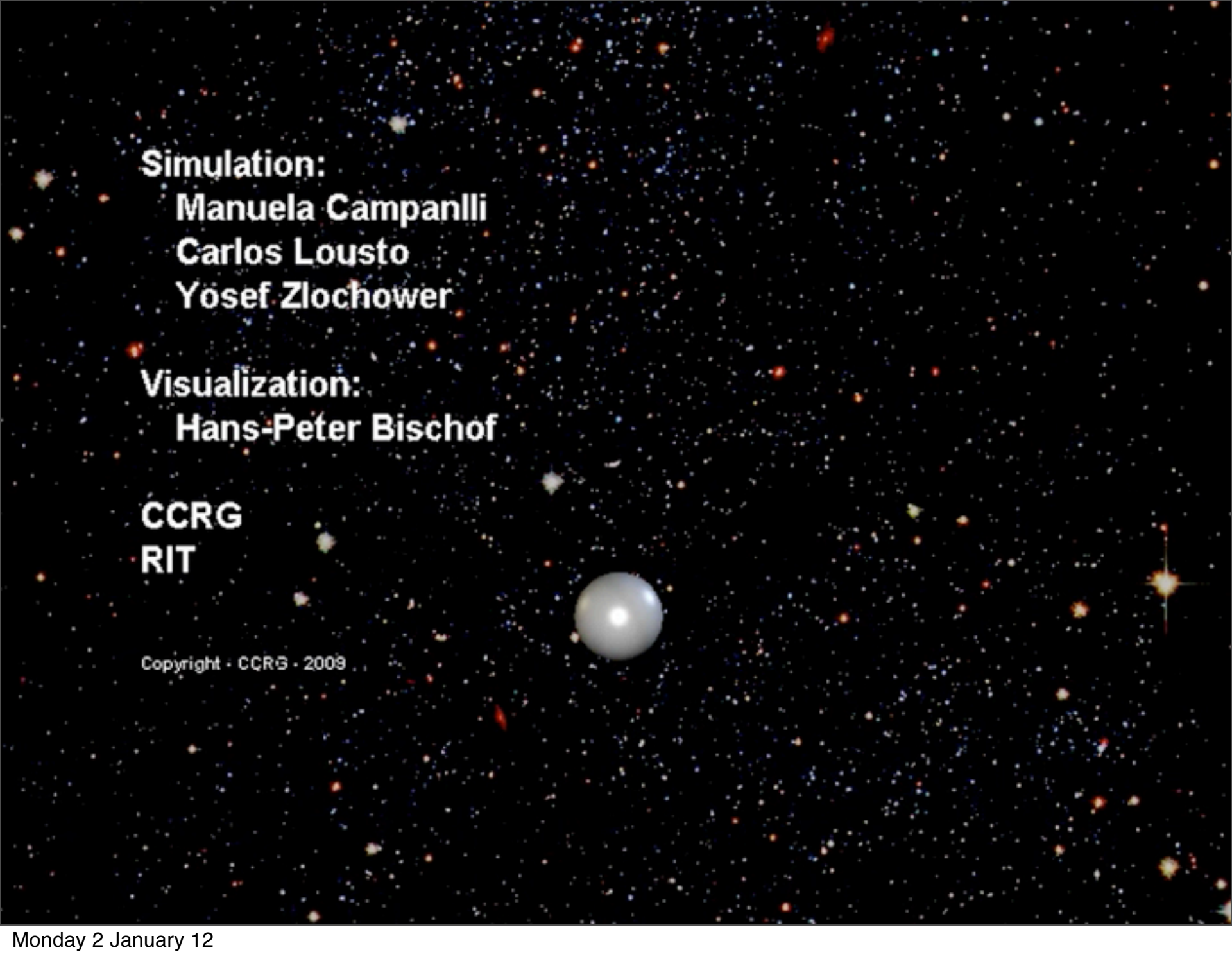
Vortex/Tendex Research

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 - » duality between tendexes (tidal field) and vortexes (frame-drag field) - need to understand it more deeply
 - » **Why** do vortexes and tendexes usually retain identity instead of diffusing and annihilating
 - » What is mechanism for exchange of vorticity in head-on, transverse-spin collisions?

“Extreme-Kick” Collision of Black Holes

Rochester Institute of Technology:
Campanelli, Lousto, Zlochower





Simulation:

Manuela Campanlli

Carlos Lousto

Yosef Zlochower

Visualization:

Hans-Peter Bischof

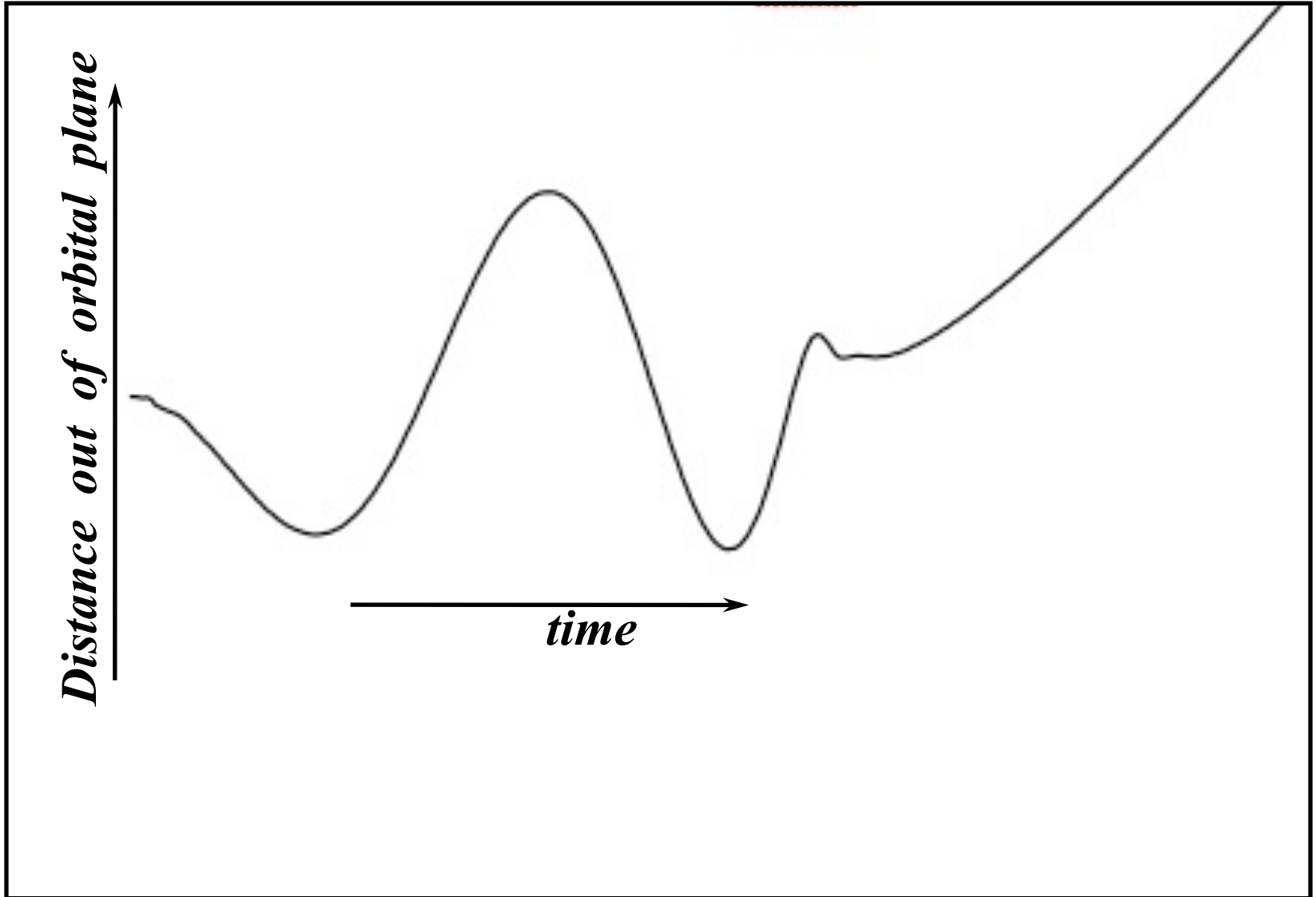
CCRG

RIT

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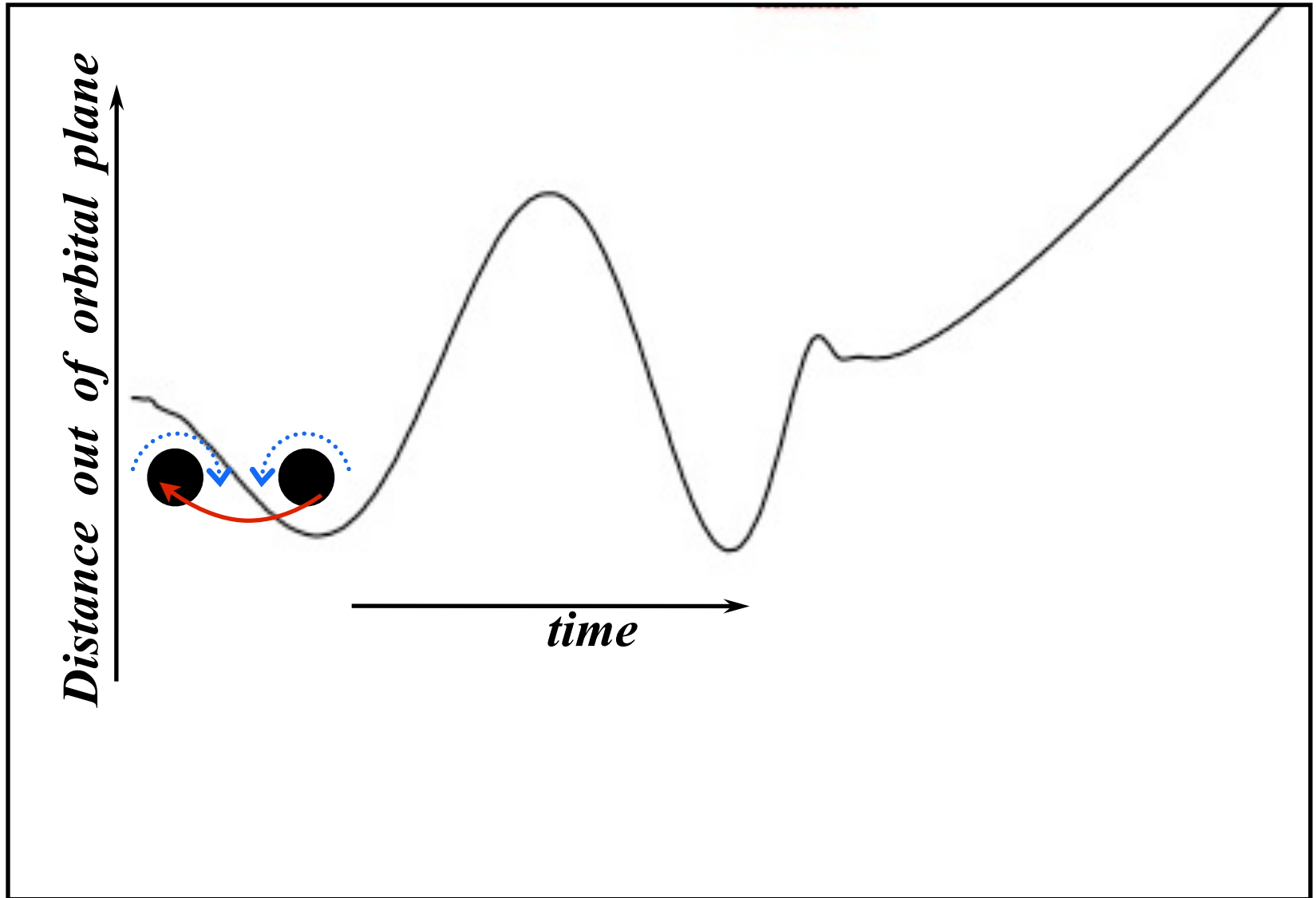
Explanation of Bobbing

[Pretorius]



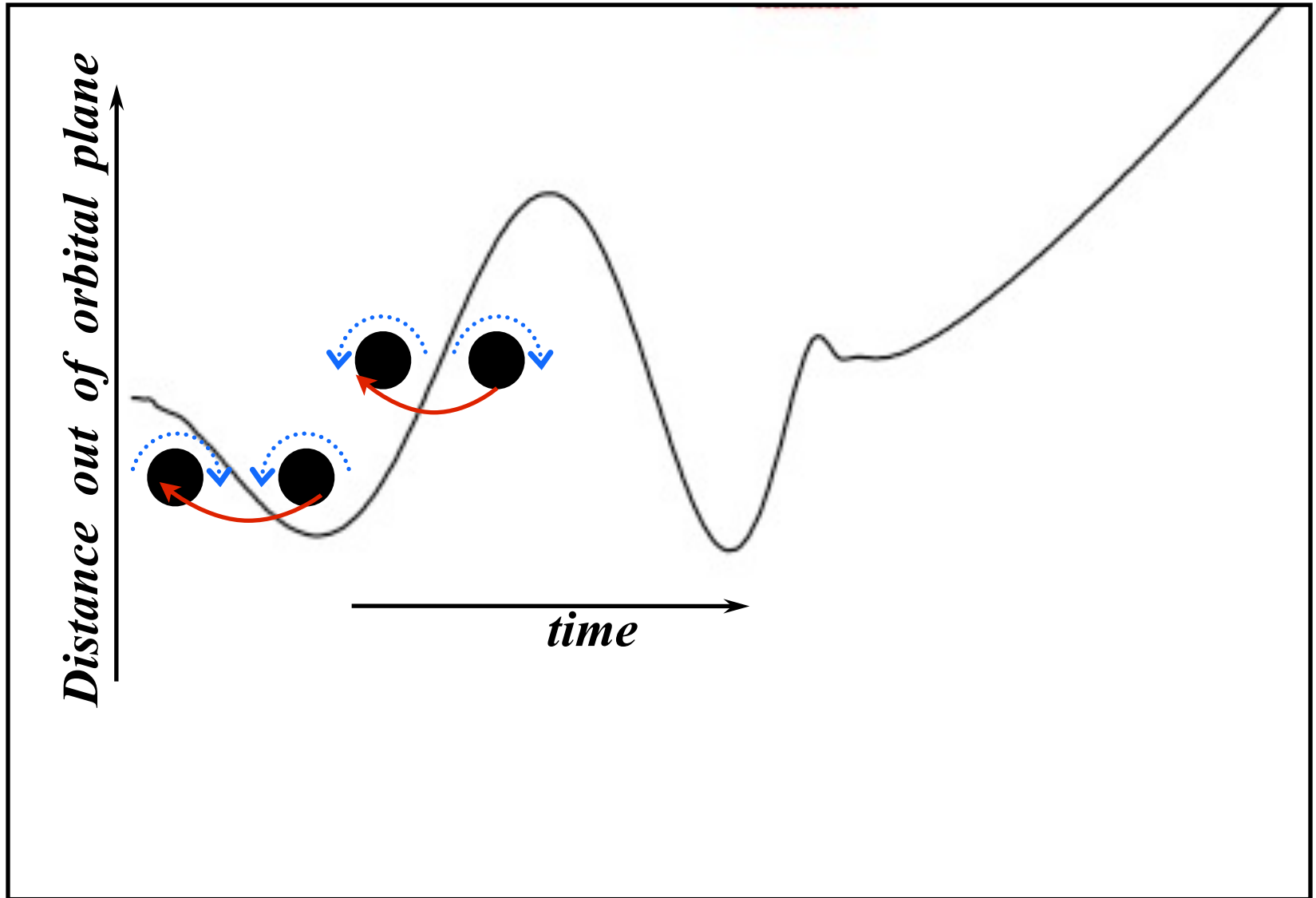
Explanation of Bobbing

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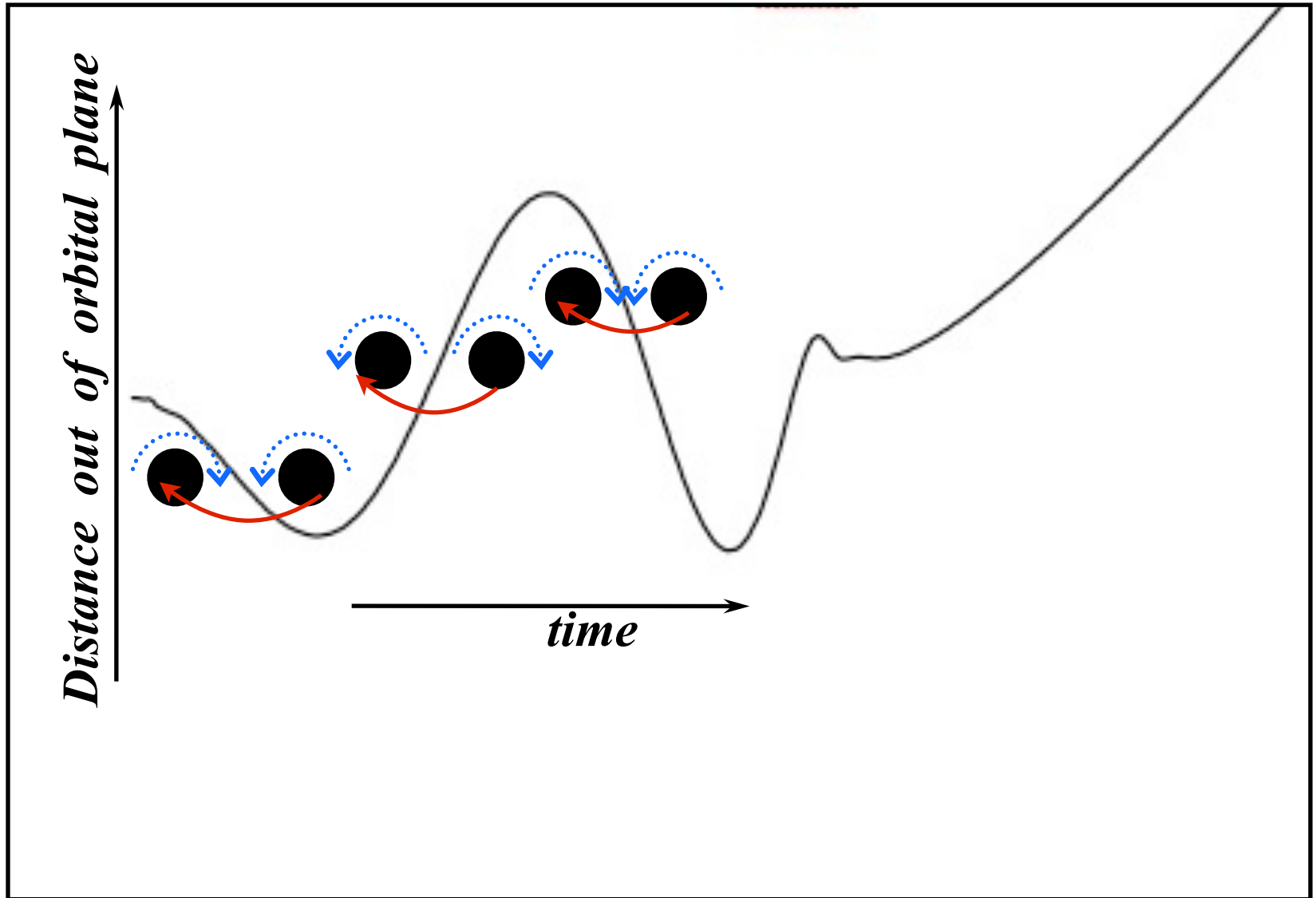
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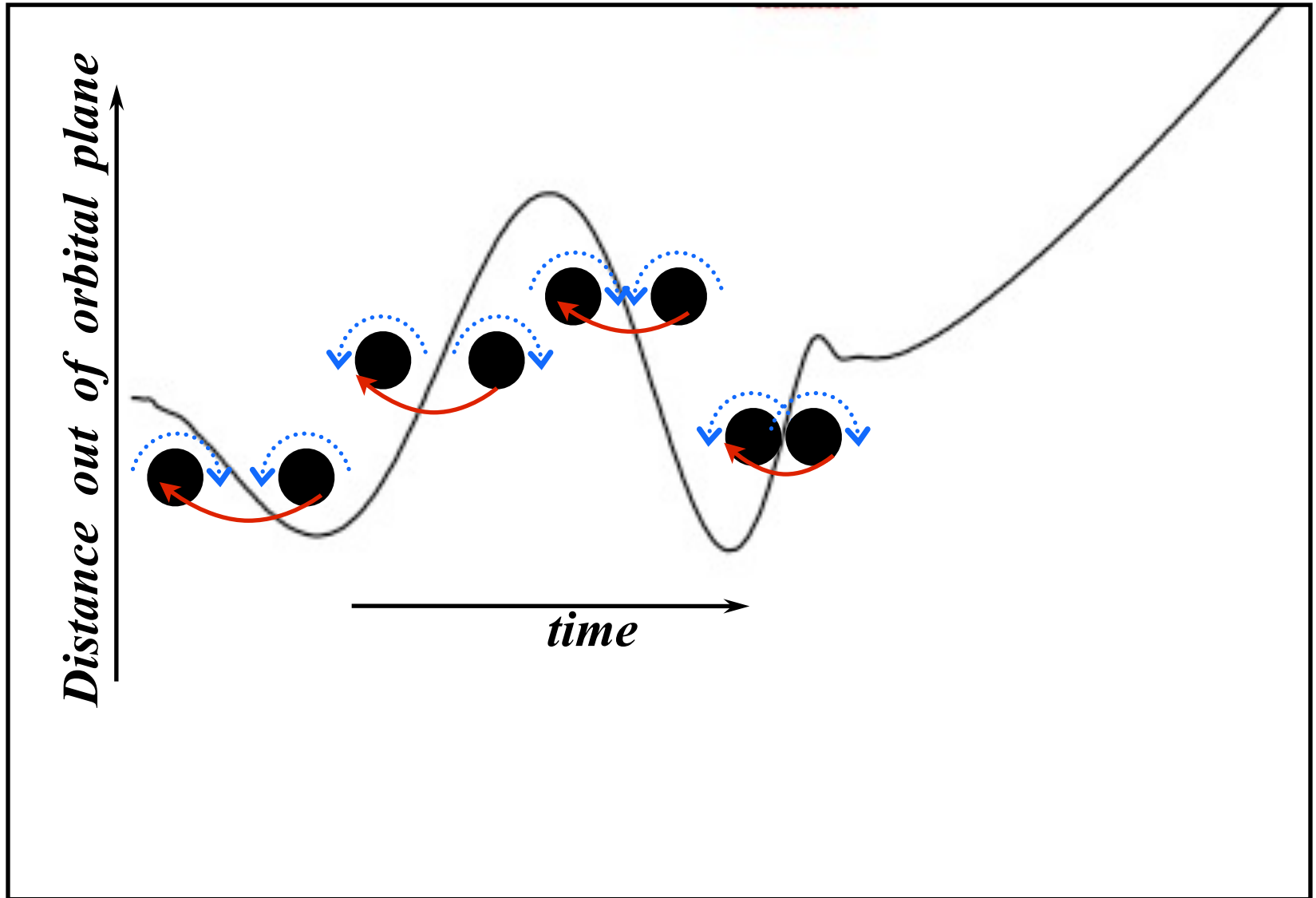
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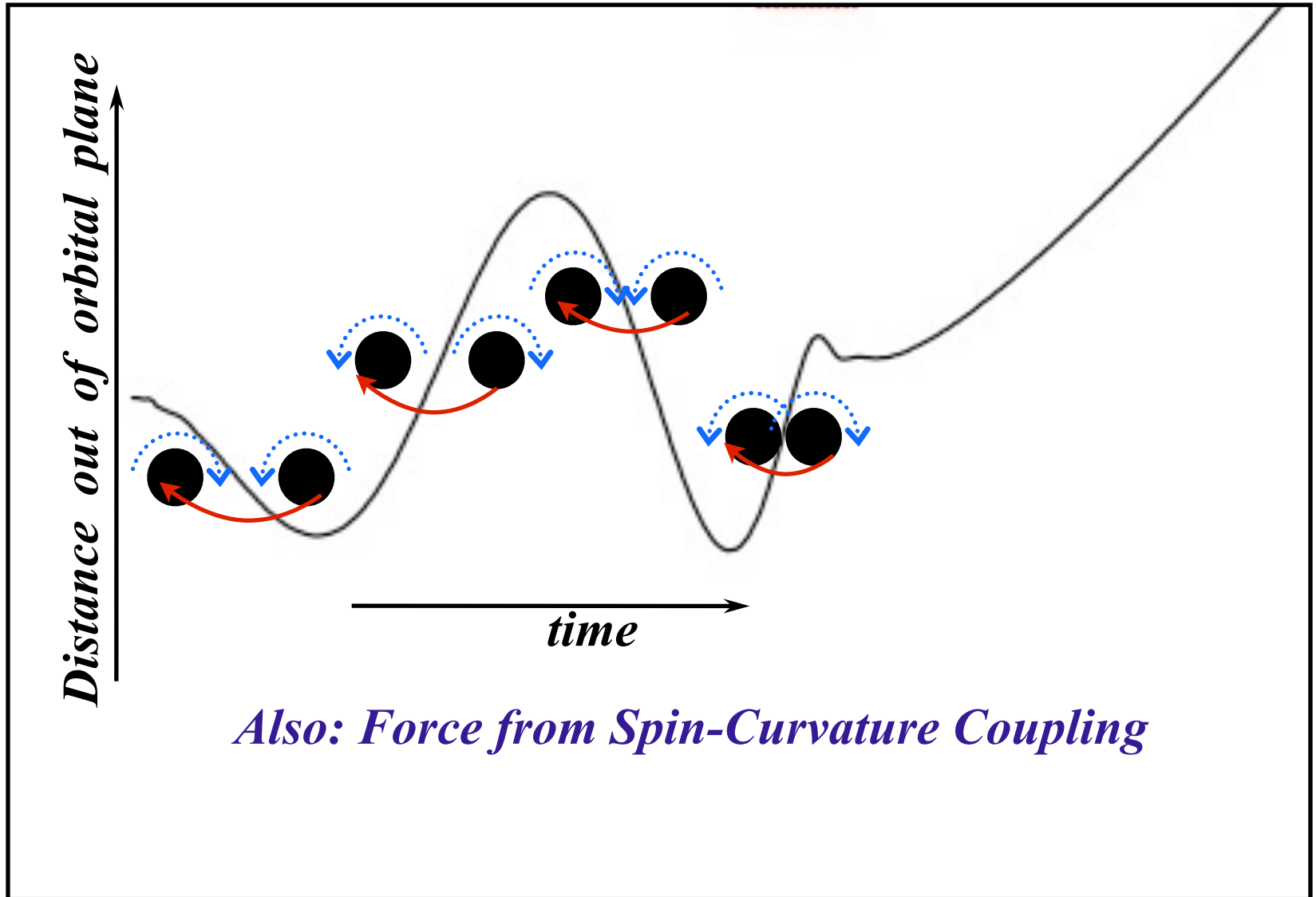
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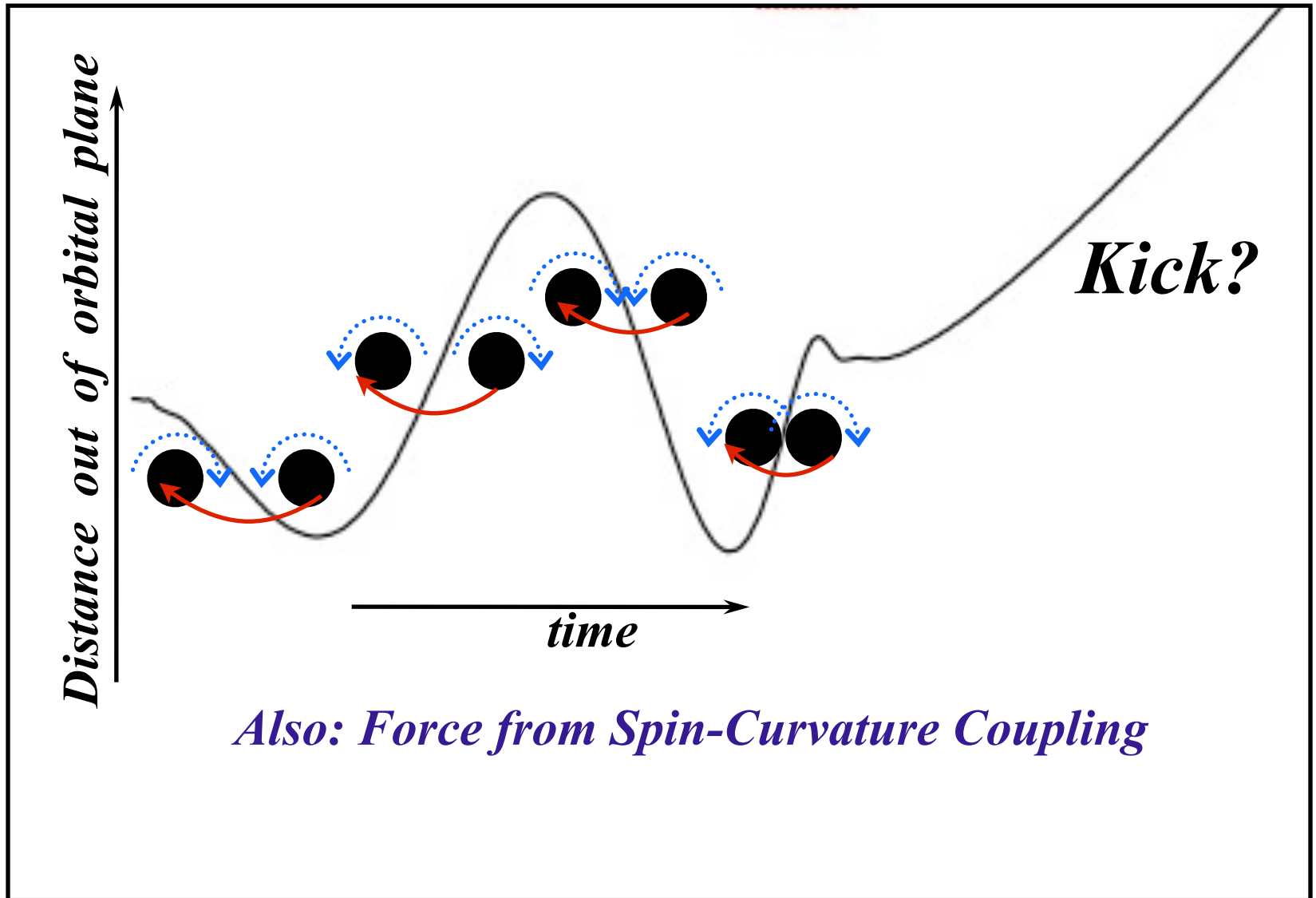
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Explanation of Bobbing

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Analogous to 2 Vortexes in a Fluid

From film *Vorticity* by **Ascher H. Shapiro** (Educational Services Inc, 1961)

Analogous to 2 Vortexes in a Fluid

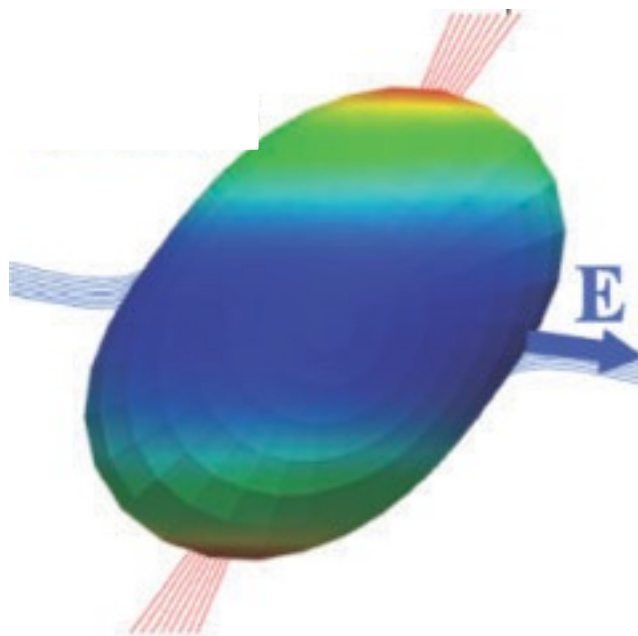
From film *Vorticity* by Ascher H. Shapiro (Educational Services Inc, 1961)



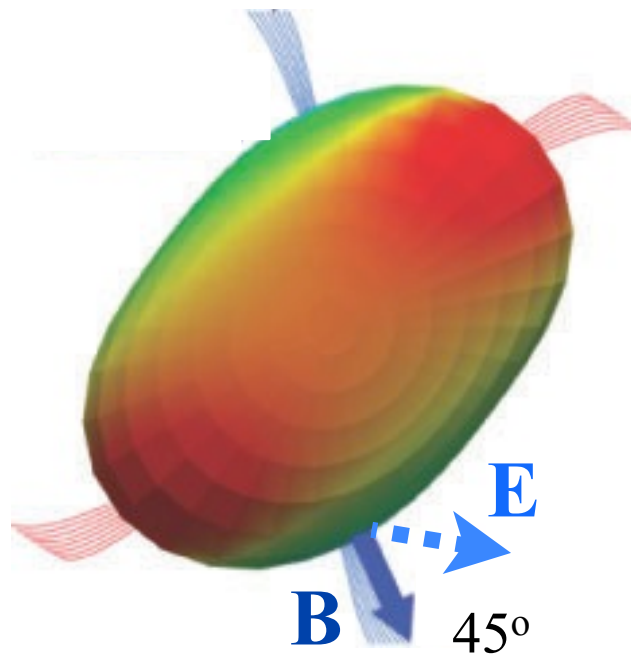
What causes the Kick?

Immediately After Merger

Near-Hole Tendexes



Near-Hole Vortexes



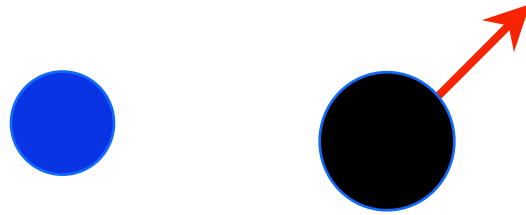
For waves going into screen: Waves from vortices ADD to those from tendexes

For waves going out of screen: Waves CANCEL

Merged hole is kicked out of screen

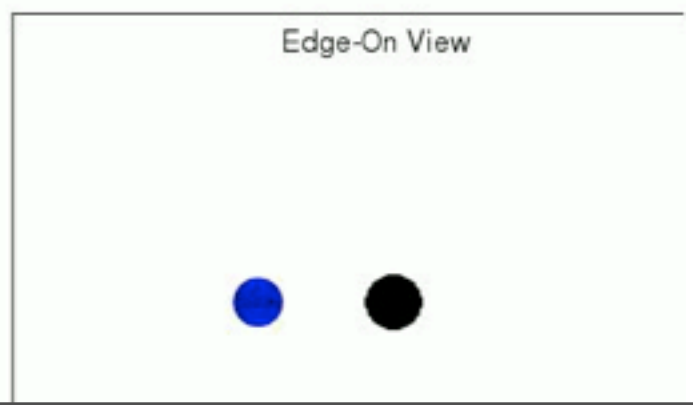
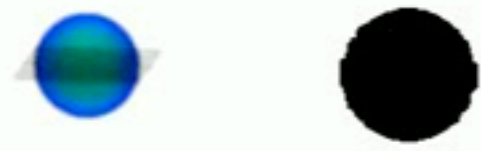
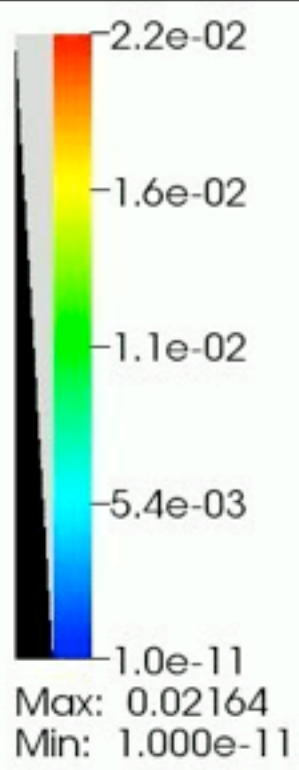
Black Hole Rips a Neutron Star Apart

- Francois Foucart, Mathew Duez, Larry Kidder, Saul Teukolsky (Cornell)



Black hole 3 times heavier than neutron star

Black hole spins at 0.5 maximum rate

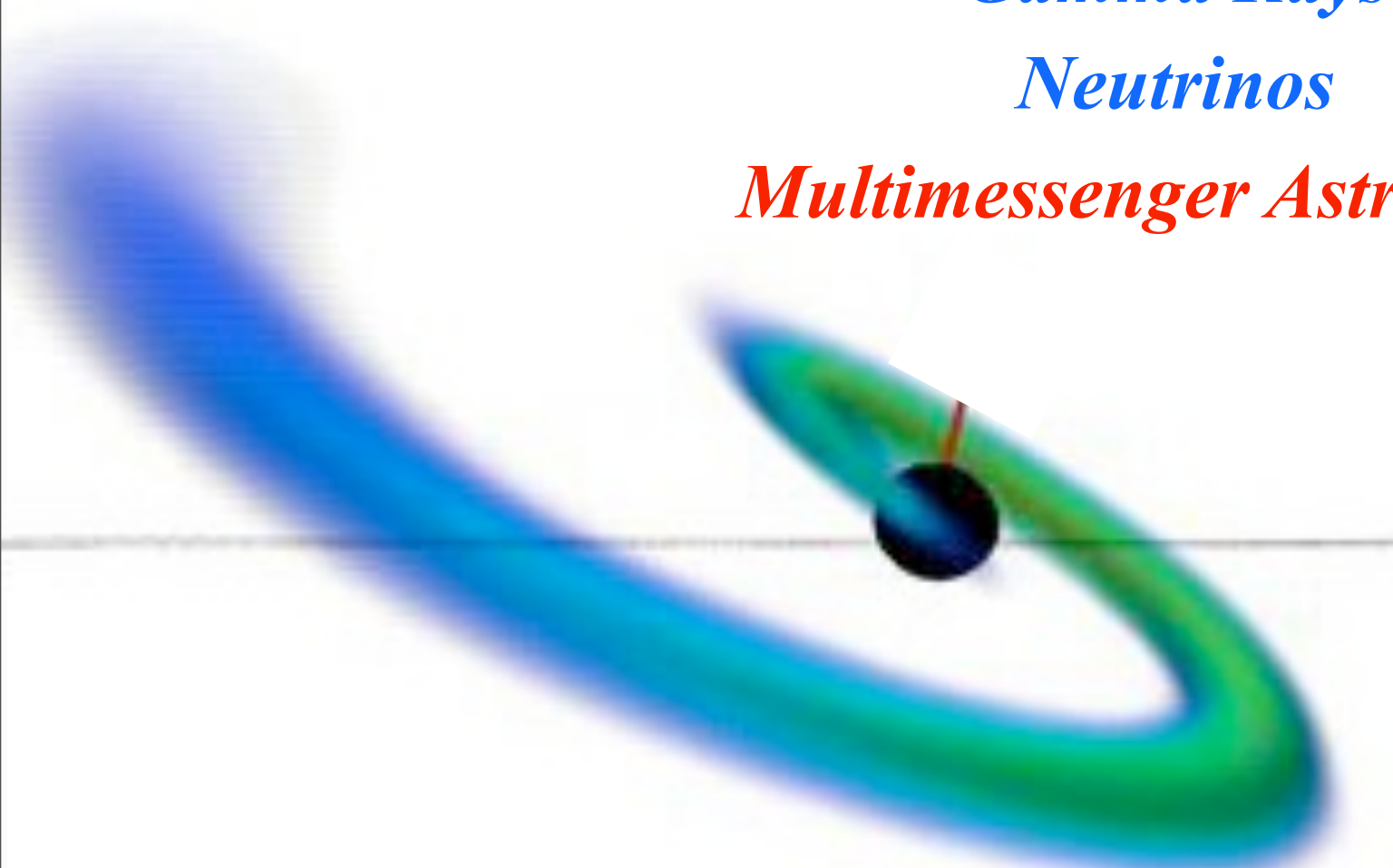


Gravitational Waves

Gamma Rays

Neutrinos

Multimessenger Astronomy

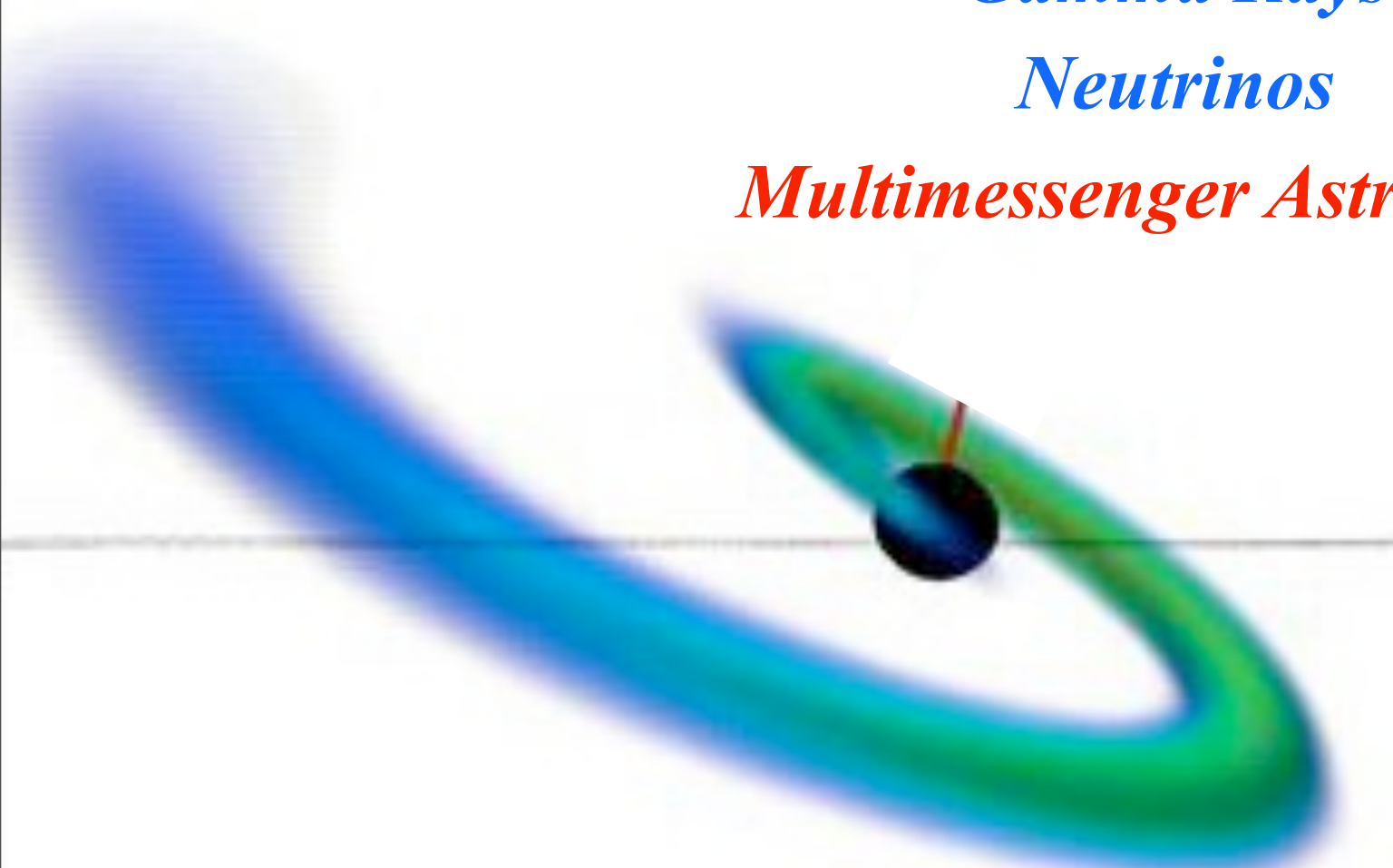


Gravitational Waves

Gamma Rays

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Multimessenger Astronomy



Masaru Shibata - Sunday: BH/NS Binaries

Black String in 4+1 Dimensions: Gregory/LaFlamme Instability

- Luis Lehner & Frans Pretorius,
Phys Rev Lett **105**, 101102 (2010)
 - » self-similar cascade: smaller holes connected by thinner strings
 - » spacetime singularity in finite proper time
 - » violation of cosmic censorship

Lehner's Lecture - Saturday

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Lehner's Lecture - Saturday

t=0.312

4.09



0.0035

Gravitational Wave Observations of BHs

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Ground-based
Interferometers



Wave Frequencies
10 Hz to 10,000 Hz
“high-frequencies”

Black holes:
2 to one thousand
solar masses

Gravitational Wave Observations of BHs

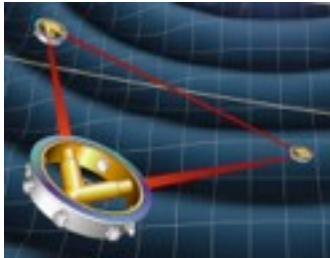
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Space-based Interferometers



Wave Periods
10 sec to 3 hours
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10 thousand to
10 million
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Gravitational Wave Observations of BHs

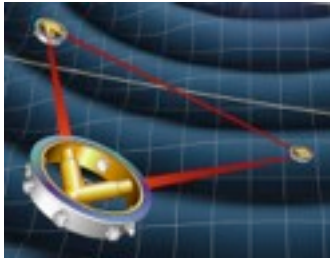
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Pulsar Timing



Wave Periods
A month to 30 years
“very low frequencies”

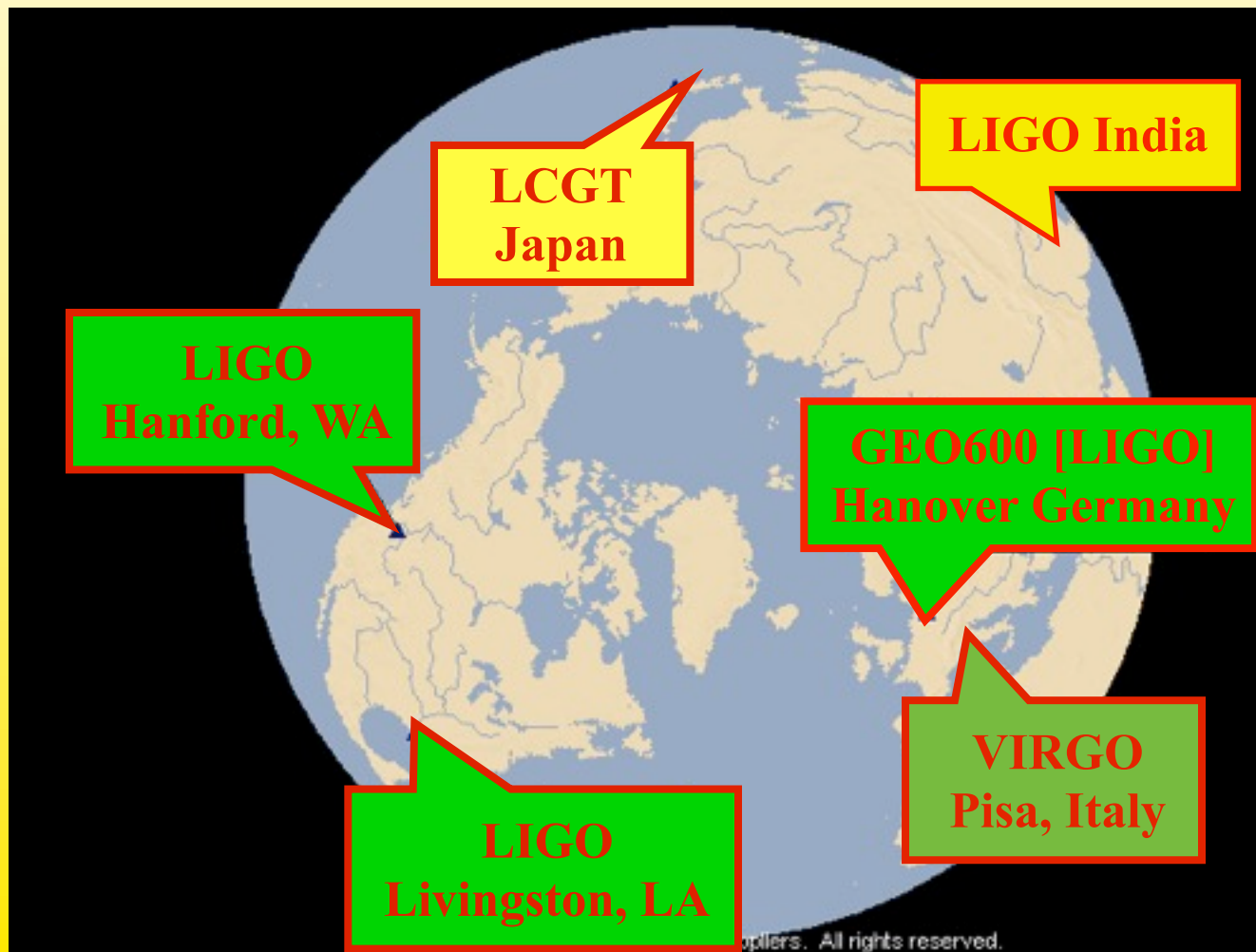
Black holes:
100 million to
10 billion solar
masses

Earth-Based GW Interferometers

Small black holes in distant galaxies:

Masses: ~10 to 1000 Suns . ~ 10 to 1000 km size

Stan Whitcomb's
Lecture
Sunday



Earth-Based GW Interferometers

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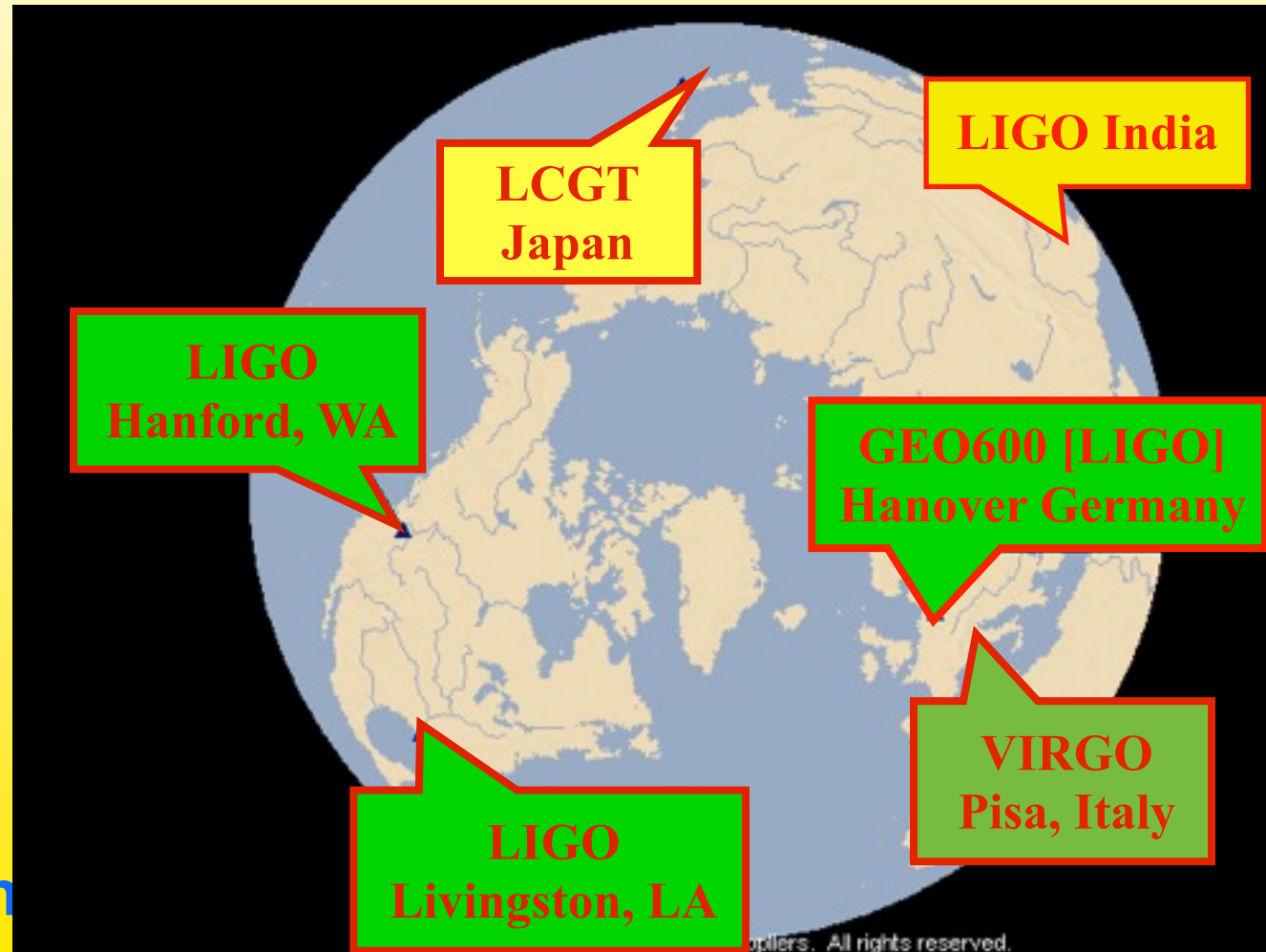
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Stan Whitcomb's
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Sunday

● Network

Required for:

- » Detection Confidence
- » Waveform Extraction
- » Direction by Triangulation



LIGO: Laser Interferometer Gravitational Wave Observatory

Collaboration of 800 scientists at 75 institutions in 13 nations

*USA, UK, Germany, India, Australia, Spain, Canada, China,
Hungary, Japan, Korea, Poland, Russia*

[David Reitze, Director; Gabriella Gonzalez, Spokesperson]

Hanford Washington




**Livingston,
Louisiana**



Sequence of Interferometers in LIGO

100 million
light years



Sequence of Interferometers in LIGO

- 1989 Proposal for LIGO: 2-step strategy:
 - » *Initial interferometers - plausible but not likely to see GWs*
 - » *Advanced interferometers - likely to see GWs from a variety of sources*

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 - » *BH/BH out to 300 million light years*
 - » *none seen yet*
- Advanced interferometers: installation began October 2010. Searches near design sensitivity 2017 - ... LIGO-India 2020- ...
 - » *BH/BH out to 4 billion light years: ~3/yr - 1/day*
 - » *Many other sources.*

100 million
light years

Bernard Schutz, Saturday
GW Astronomy

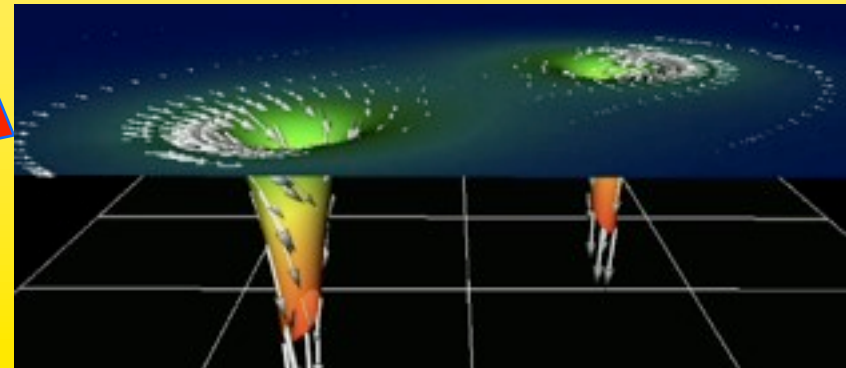
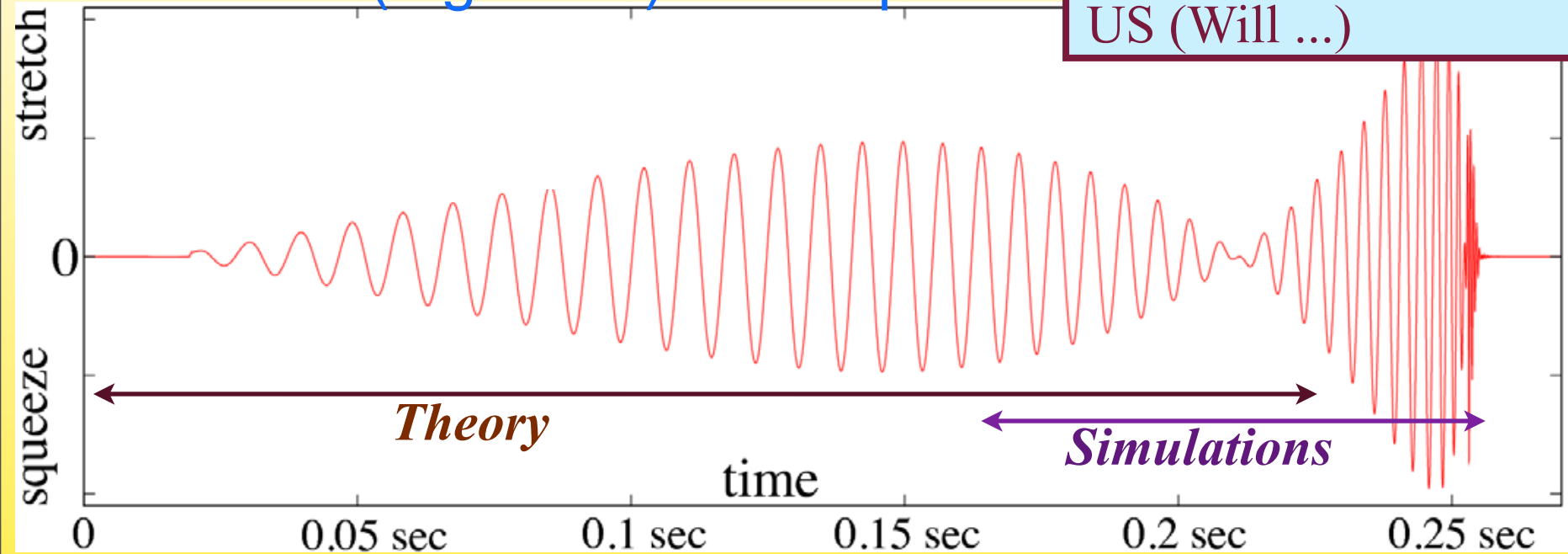
Gravitational Waveforms

Dictionary: Post-Newtonian Theory

Plus Numerical simulations

→ Formula (e.g. EOB) for templates

India (Iyer, ...) +
France (Blanchet, ...) +
US (Will ...)



Gravitational Waveforms

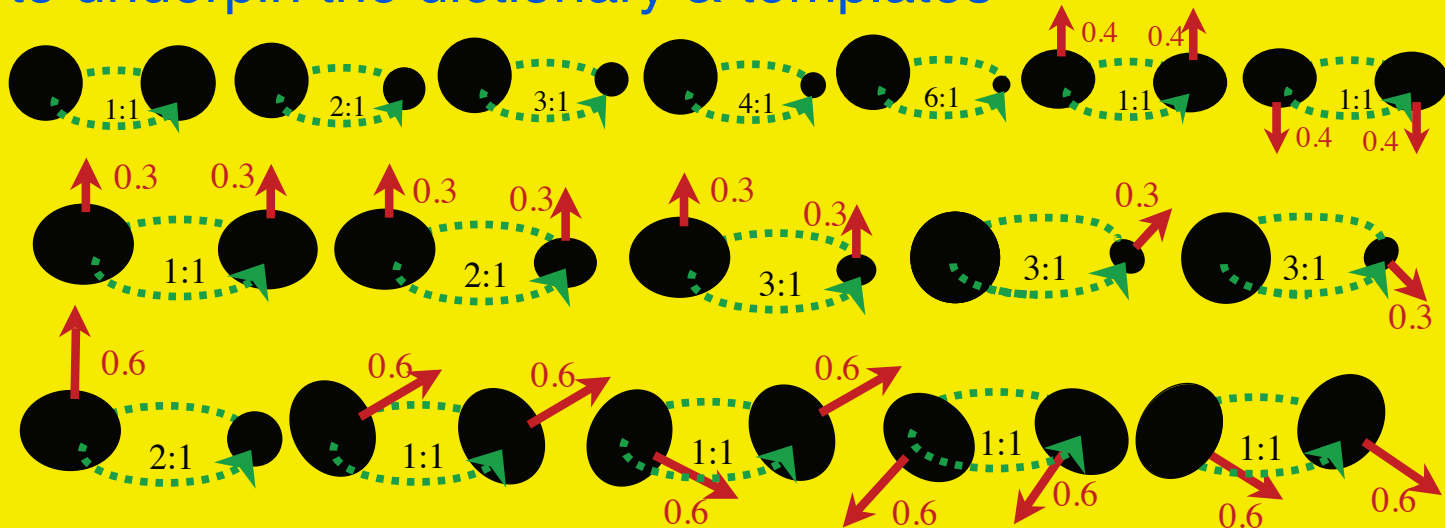
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India (Iyer, ...) +
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US (Will ...)

- NR/AR Collaboration: Now carrying out ~1000 simulations to underpin the dictionary & templates

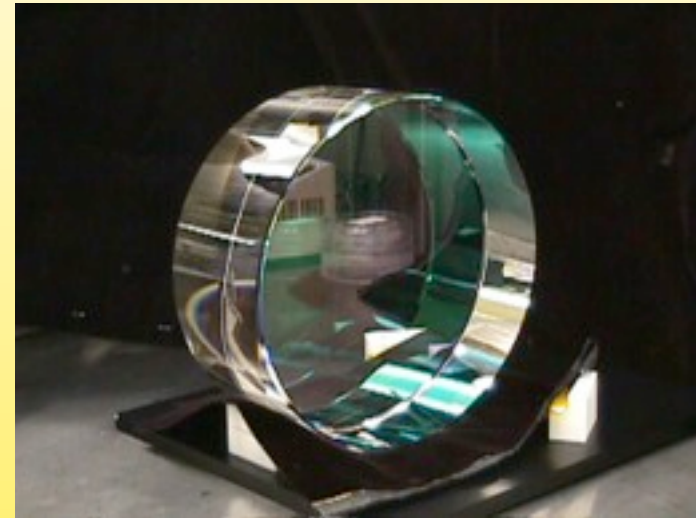


Advanced LIGO Interferometers

The Experimental Challenge

$$\Delta L / L = h$$

- Monitor motions of 40 kg mirrors to:
 - » $\Delta L \sim 10^{-17}$ cm
 - » ~ size where mirror behaves quantum mechanically

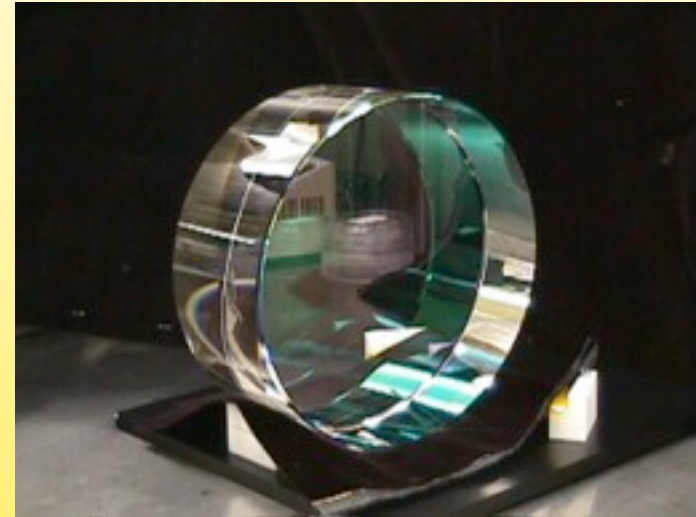


Advanced LIGO Interferometers

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**For the first time humans will see human-sized objects
behave quantum mechanically!**

**Quantum Nondemolition (QND) Technology to deal with this
[Branch of Quantum Information Science]**

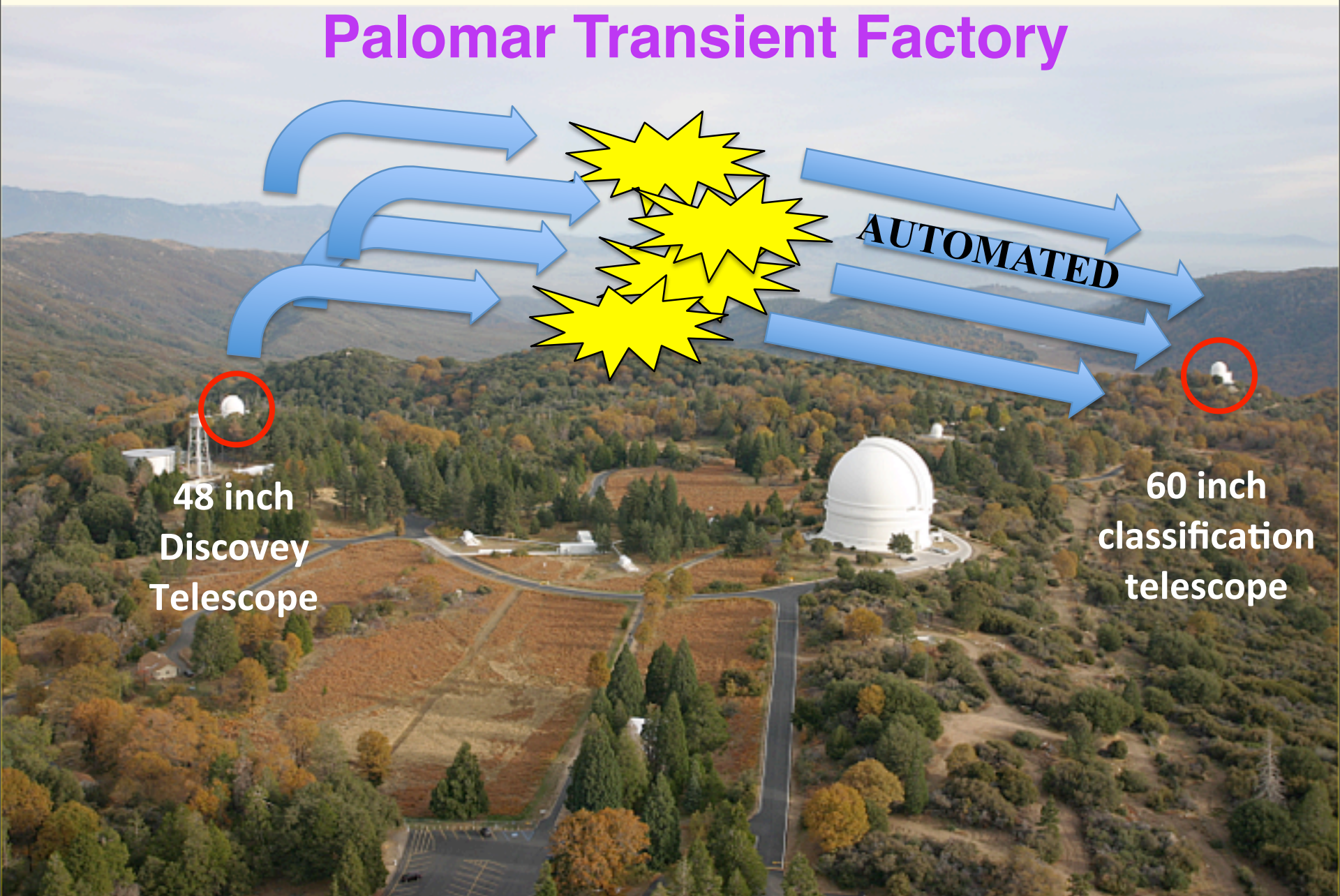
Preparation for Multimessenger Astronomy: Palomar Transient Factory



48 inch
Discovery
Telescope

Preparation for Multimessenger Astronomy:

Palomar Transient Factory



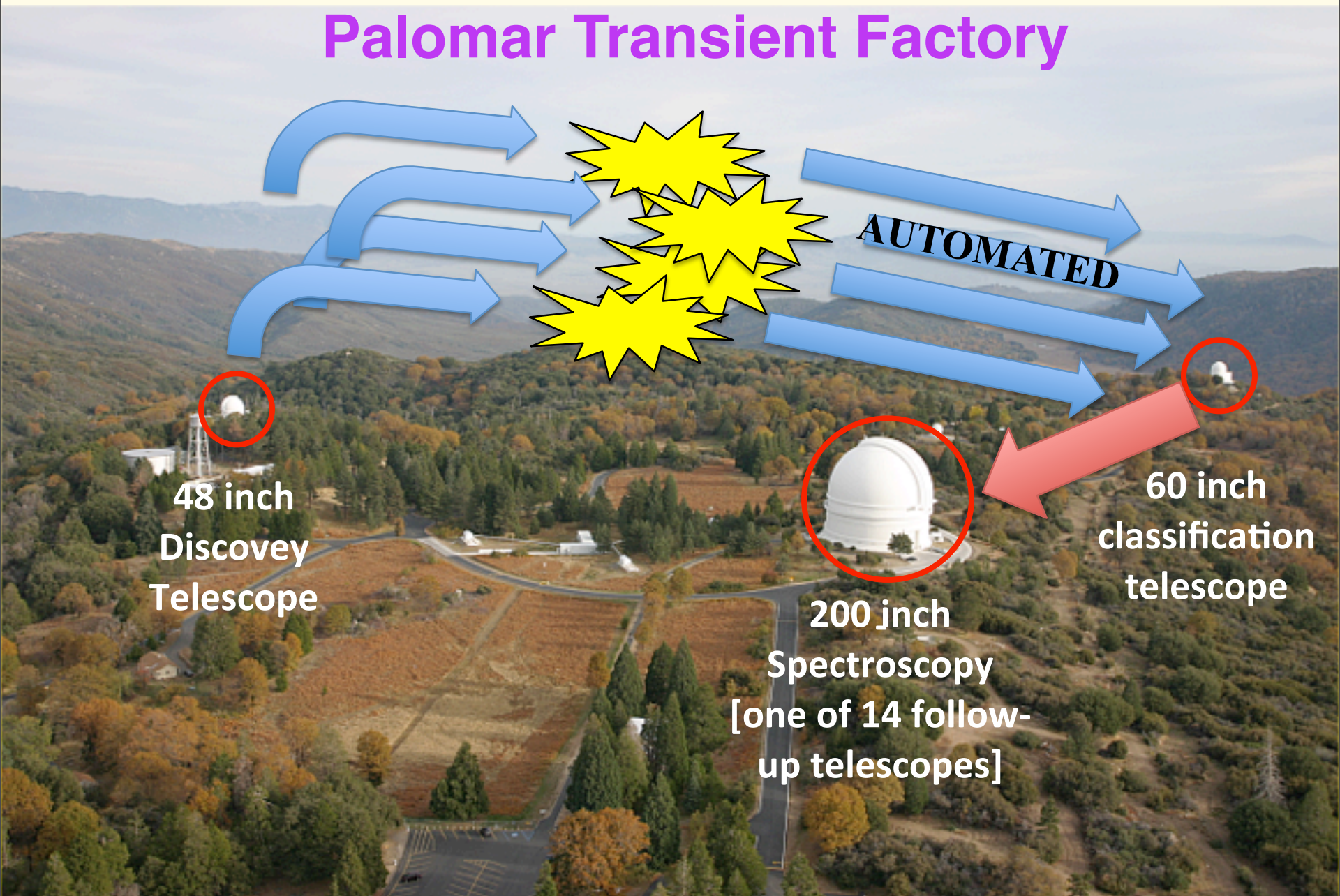
48 inch
Discovery
Telescope

60 inch
classification
telescope

AUTOMATED

Preparation for Multimessenger Astronomy:

Palomar Transient Factory



48 inch
Discovery
Telescope

200 inch
Spectroscopy
[one of 14 follow-
up telescopes]

60 inch
classification
telescope

AUTOMATED

Multimessenger Astronomy

Giant Metrewave Radio Telescope - 80 km north of Pune



**Problem:
Good Enough GW Angular Resolution
for Multi-Messenger Astronomy**

Whitcomb Talk - Sunday

Problem:
**Good Enough GW Angular Resolution
for Multi-Messenger Astronomy**

SOLUTION:
LIGO-INDIA

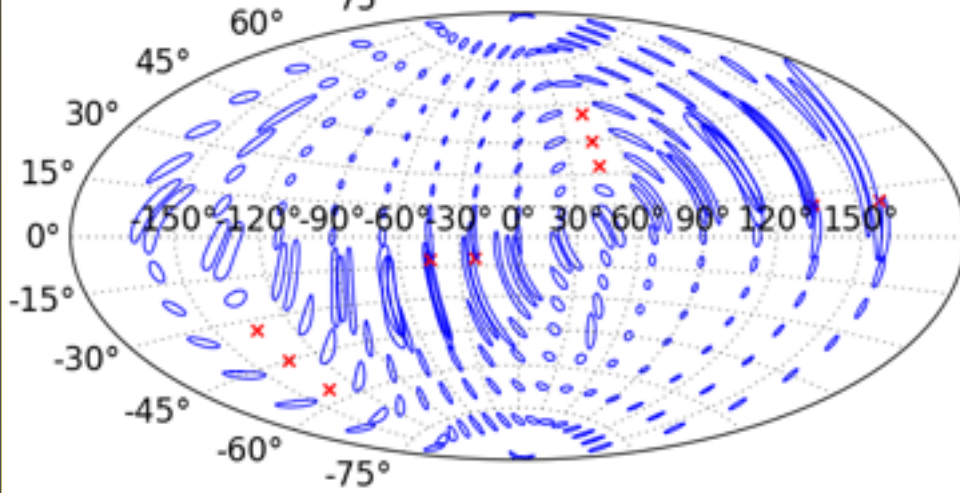
IndIGO - consortium of 10 Indian National Institutions

Whitcomb Talk - Sunday

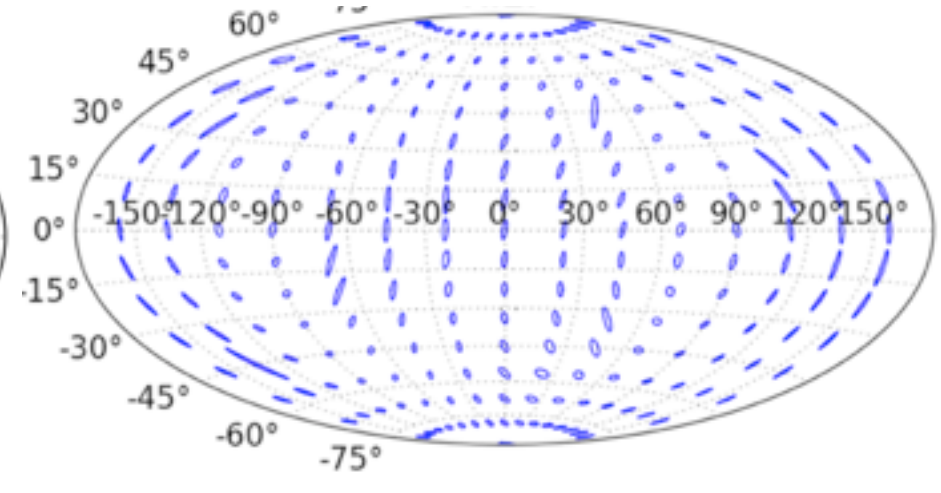
What LIGO-India Brings to Network

Determination of source sky position: NS-NS

LIGO + Virgo



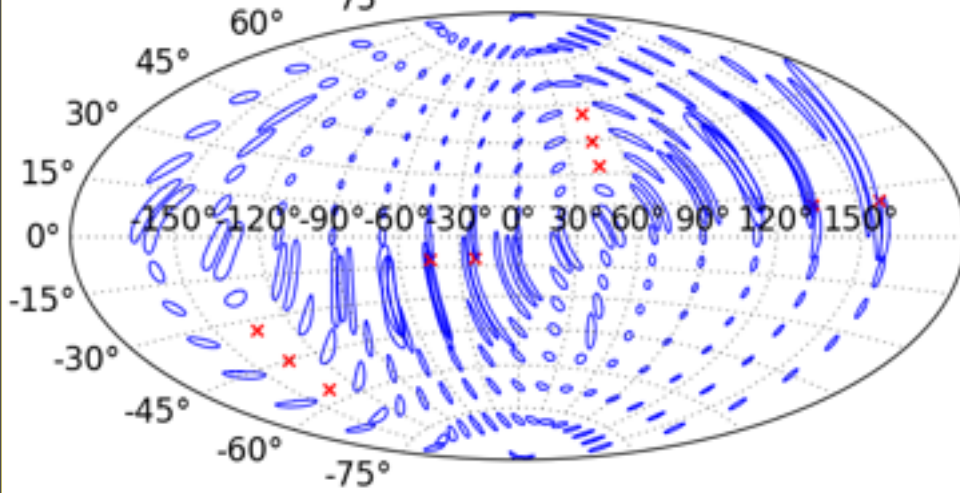
With LIGO-India



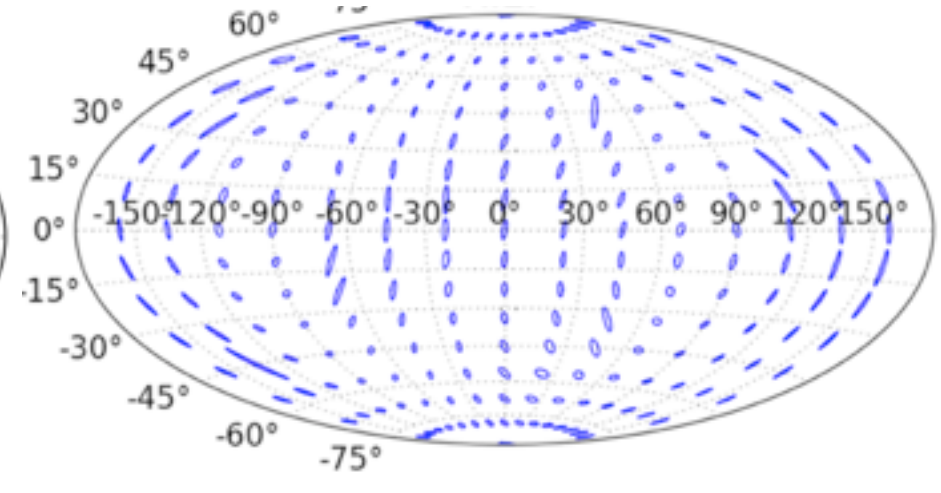
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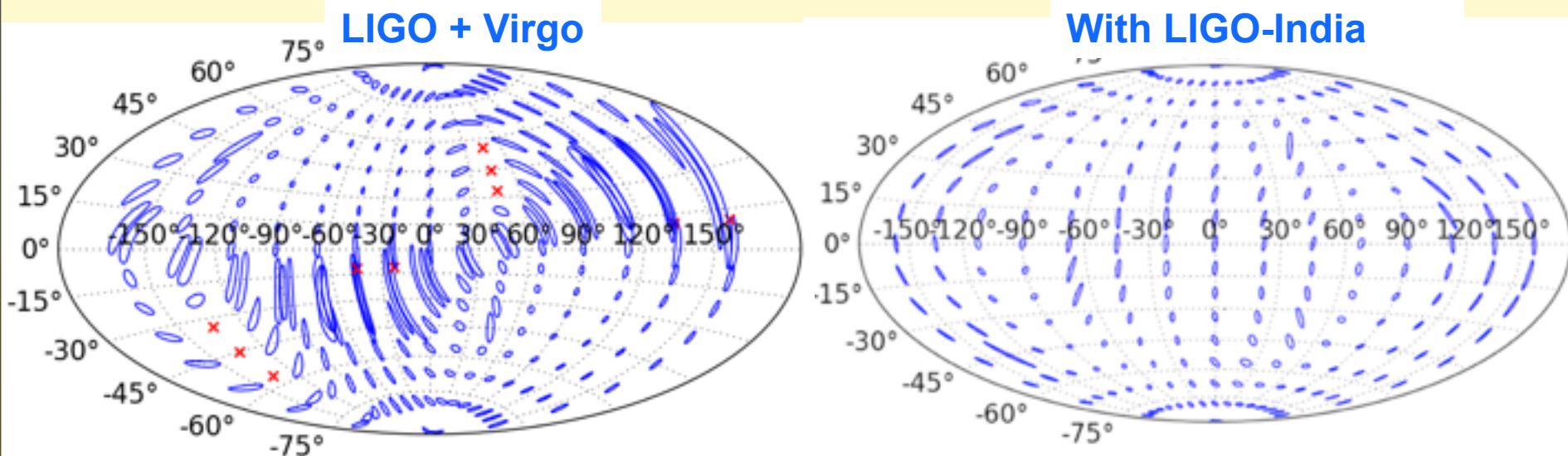
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- North/South uncertainty greatly reduced

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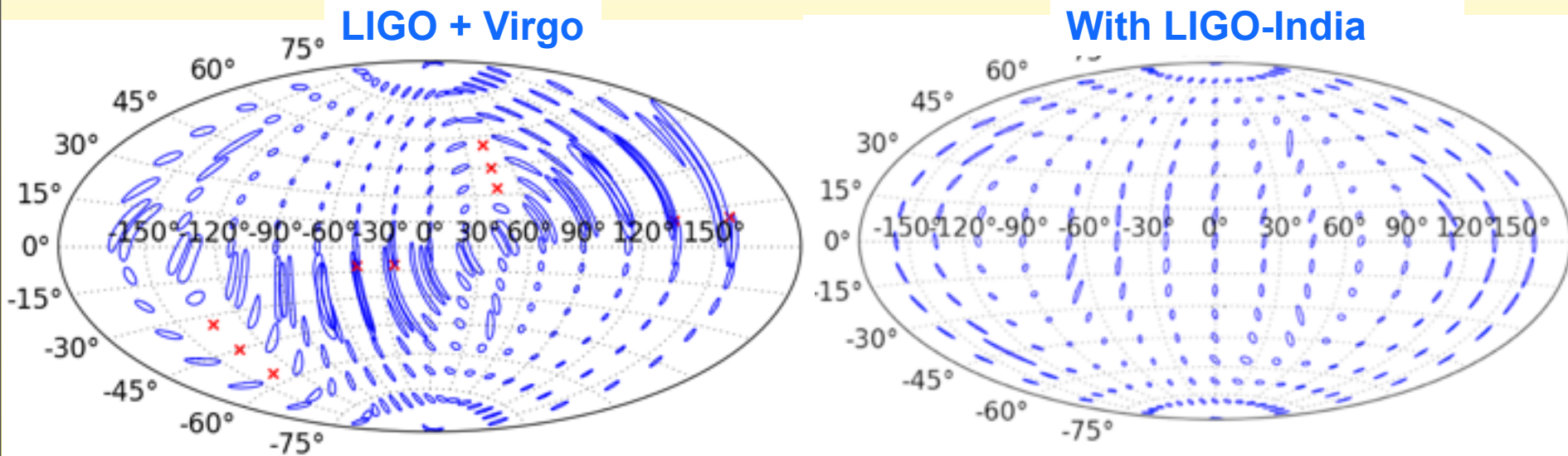
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- Average improvement in angular resolution: a factor 3.5

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Determination of source sky position: NS-NS



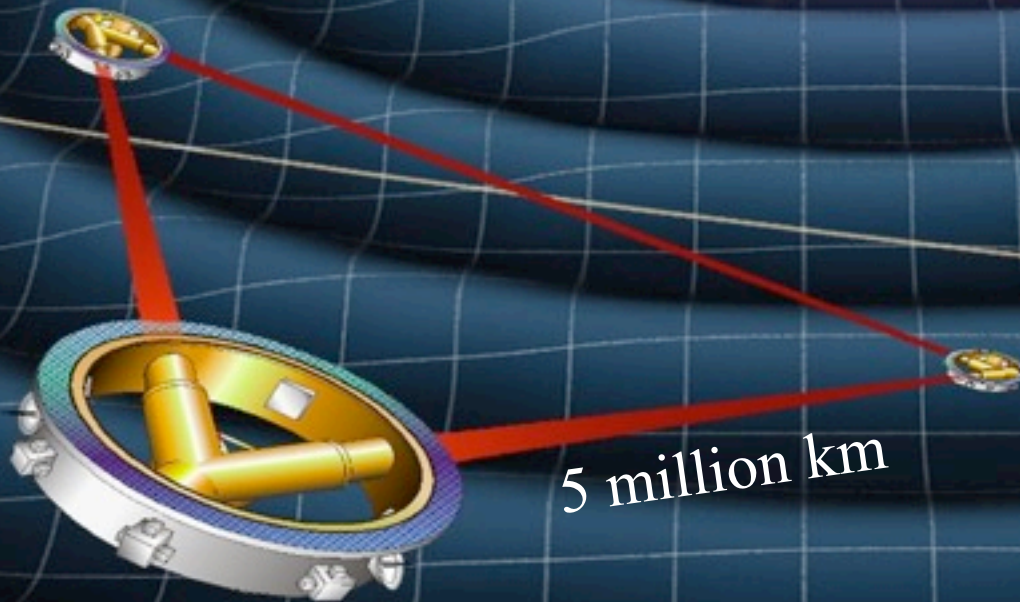
- North/South uncertainty greatly reduced
 - Average improvement in angular resolution: a factor 3.5
- 28 deg² reduced to 8 deg² (for half of sky, 90% confidence)**

LISA



Laser Interferometer Space Antenna

LF; 10^4 to 10^7 Msun BHs



5 million km

LISA

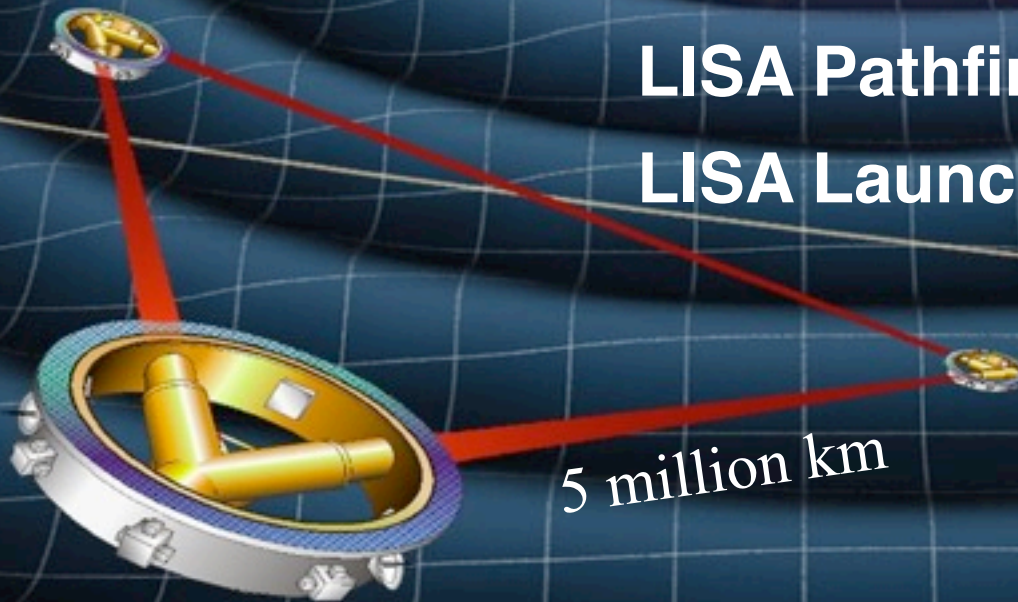


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LISA Pathfinder (test flight): 2013

LISA Launch: ~ 2022 or later



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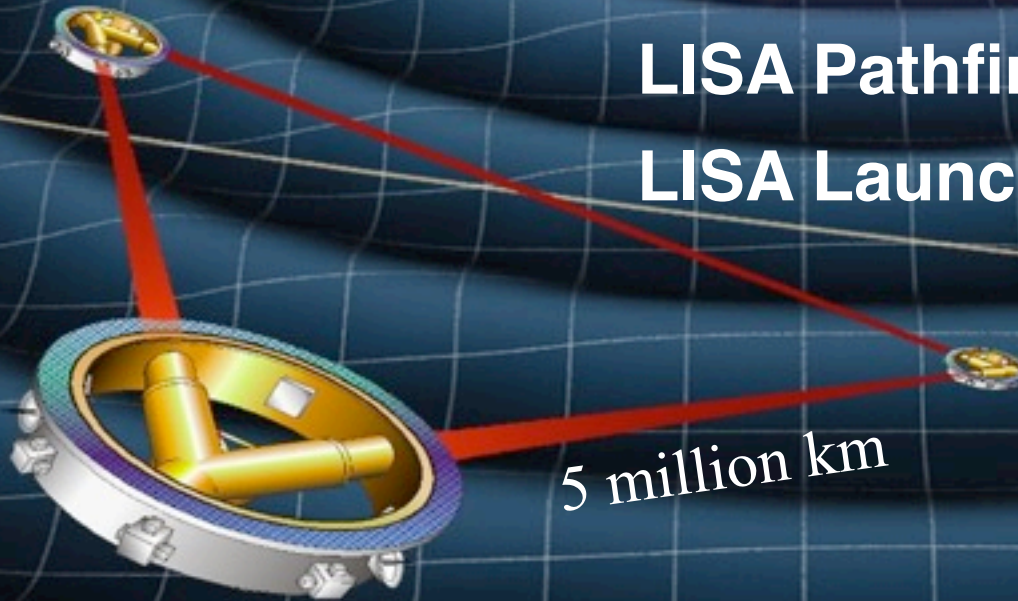


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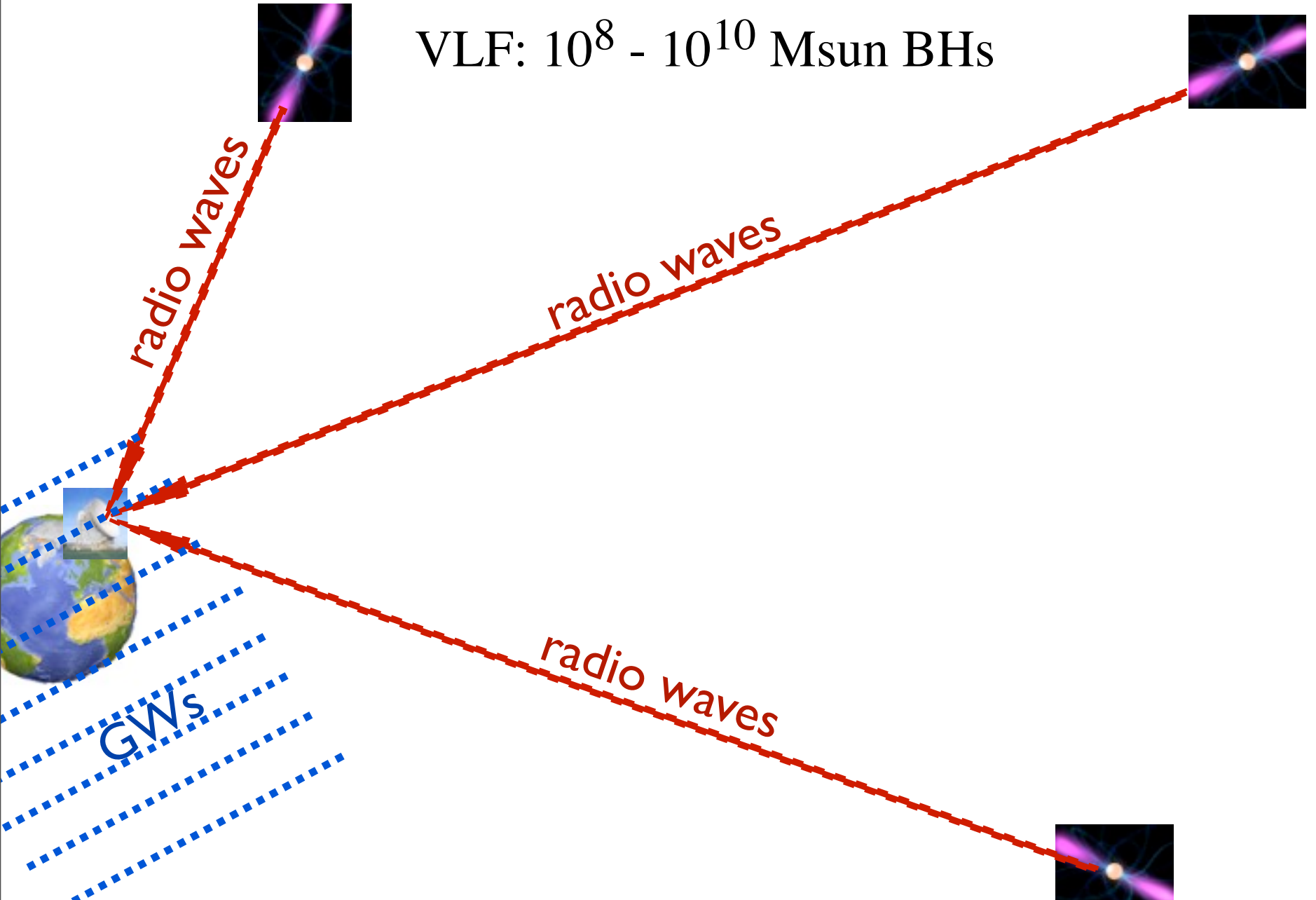
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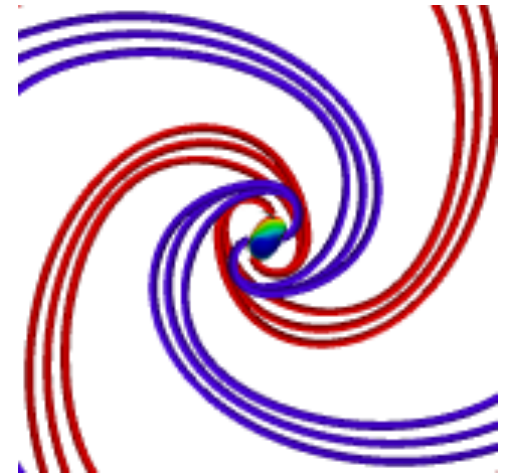
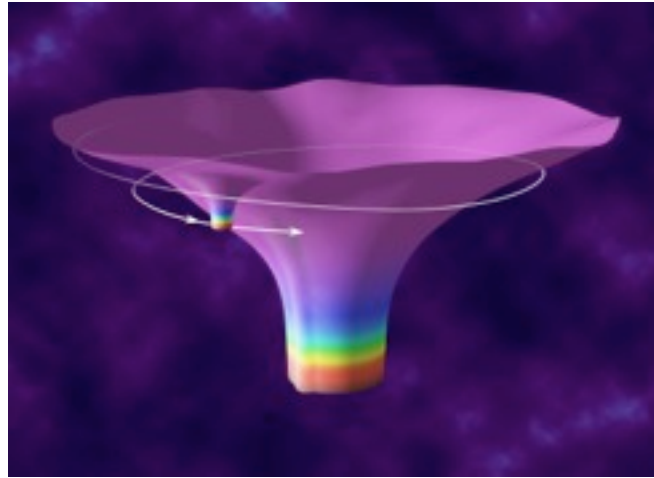
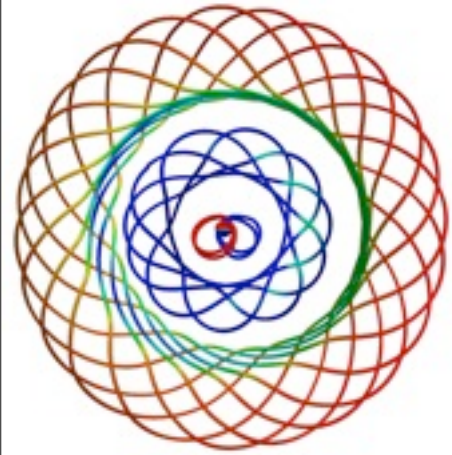
**Being Redesigned as
a ESA-only mission**

Pulsar Timing Array

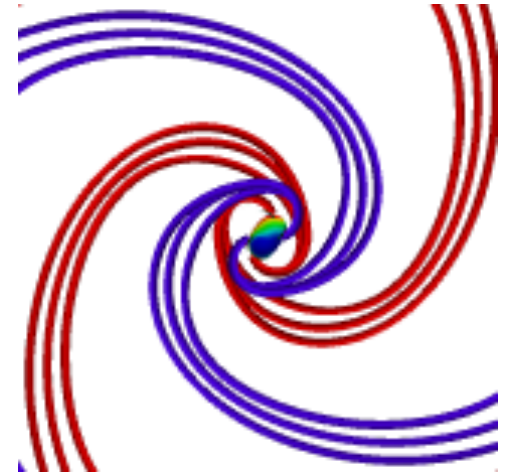
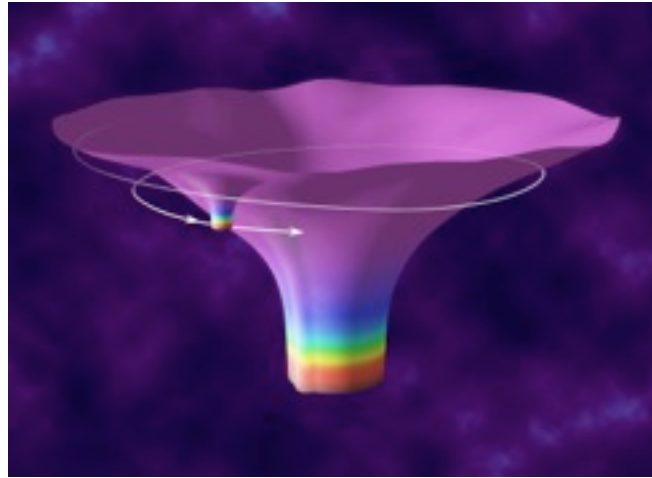
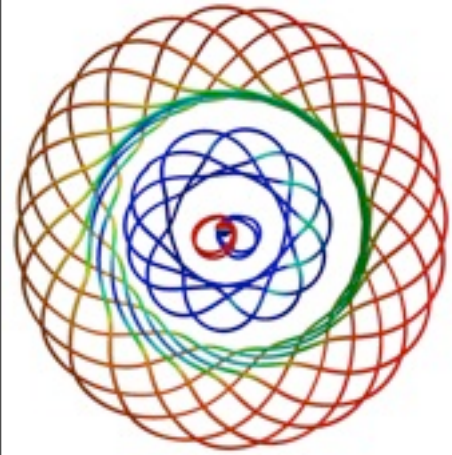
VLF: $10^8 - 10^{10}$ Msun BHs



Conclusion

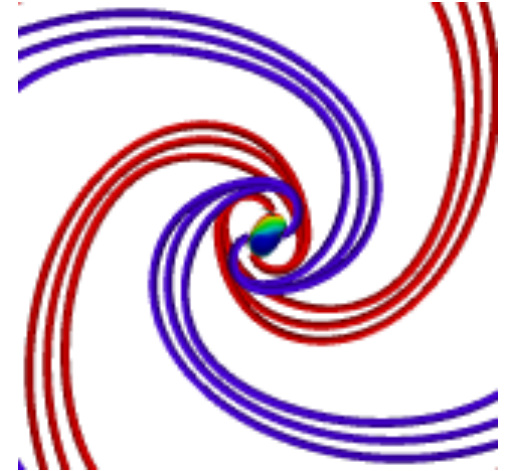
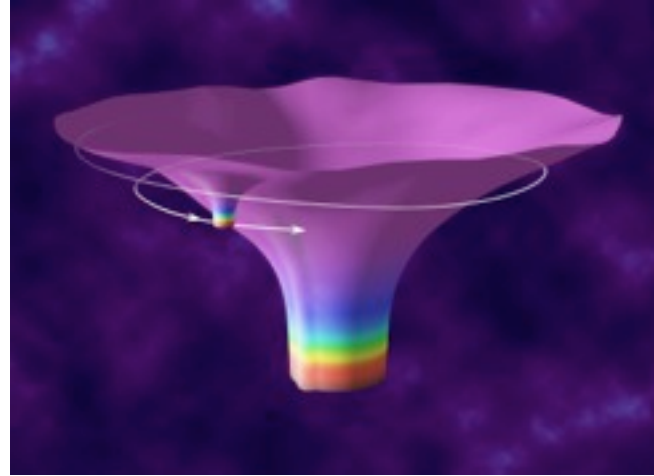
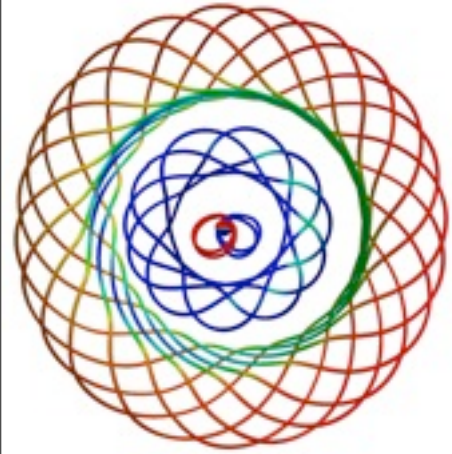


Conclusion



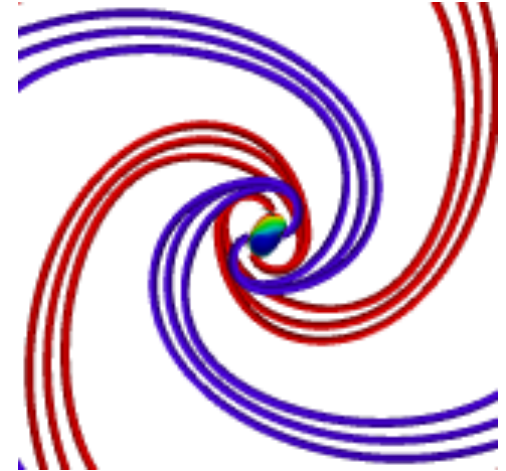
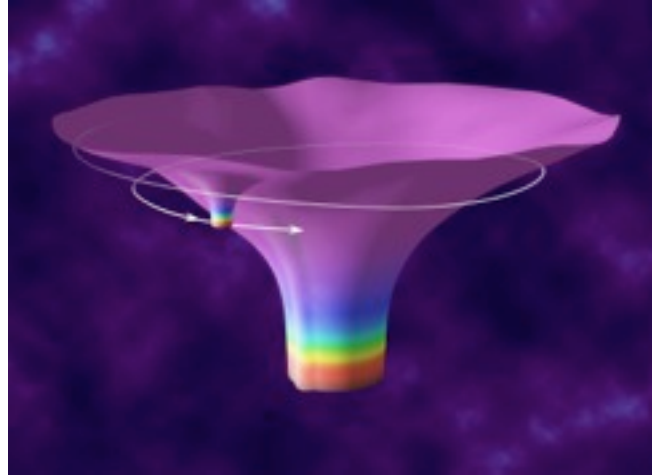
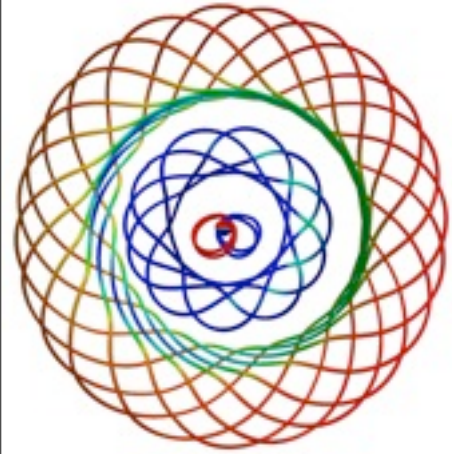
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Conclusion



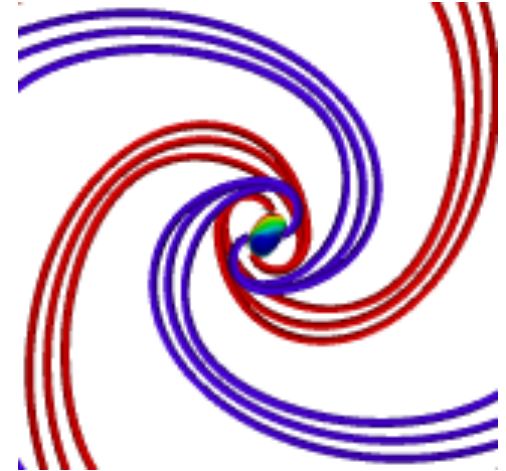
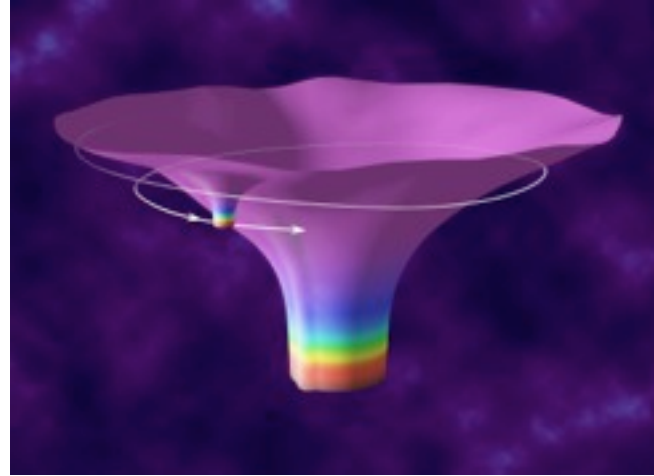
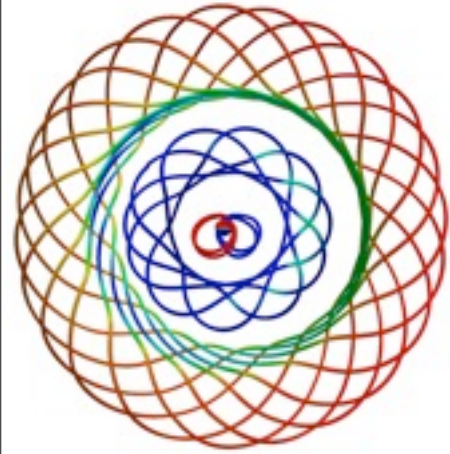
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Conclusion



- Highly dynamical Black Holes show an amazing richness of structure and behaviors
- Numerical Relativity has become a powerful tool for probing this richness
- Gravitational Waves will bring this rich physics into the realm of observations
- A new golden age of black hole research