

Mechanical properties of filamentous biopolymers

Networks of filamentous biopolymers have unusual elastic properties:

Low elastic modulus at very low volume fraction ($<0.1\%$)

Stiffness increases at (very low) increasing strain

Effects of substrate mechanics on cell function.

Cell type specific

How do cells measure stiffness?

Length and time scales?

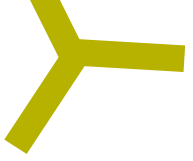
Linear vs non-linear elastic substrate

Qi Wen, Fitzroy Byfield, Ilya Levental, Shang Tee

Fred MacKintosh, Kees Storm, Tom Lubensky

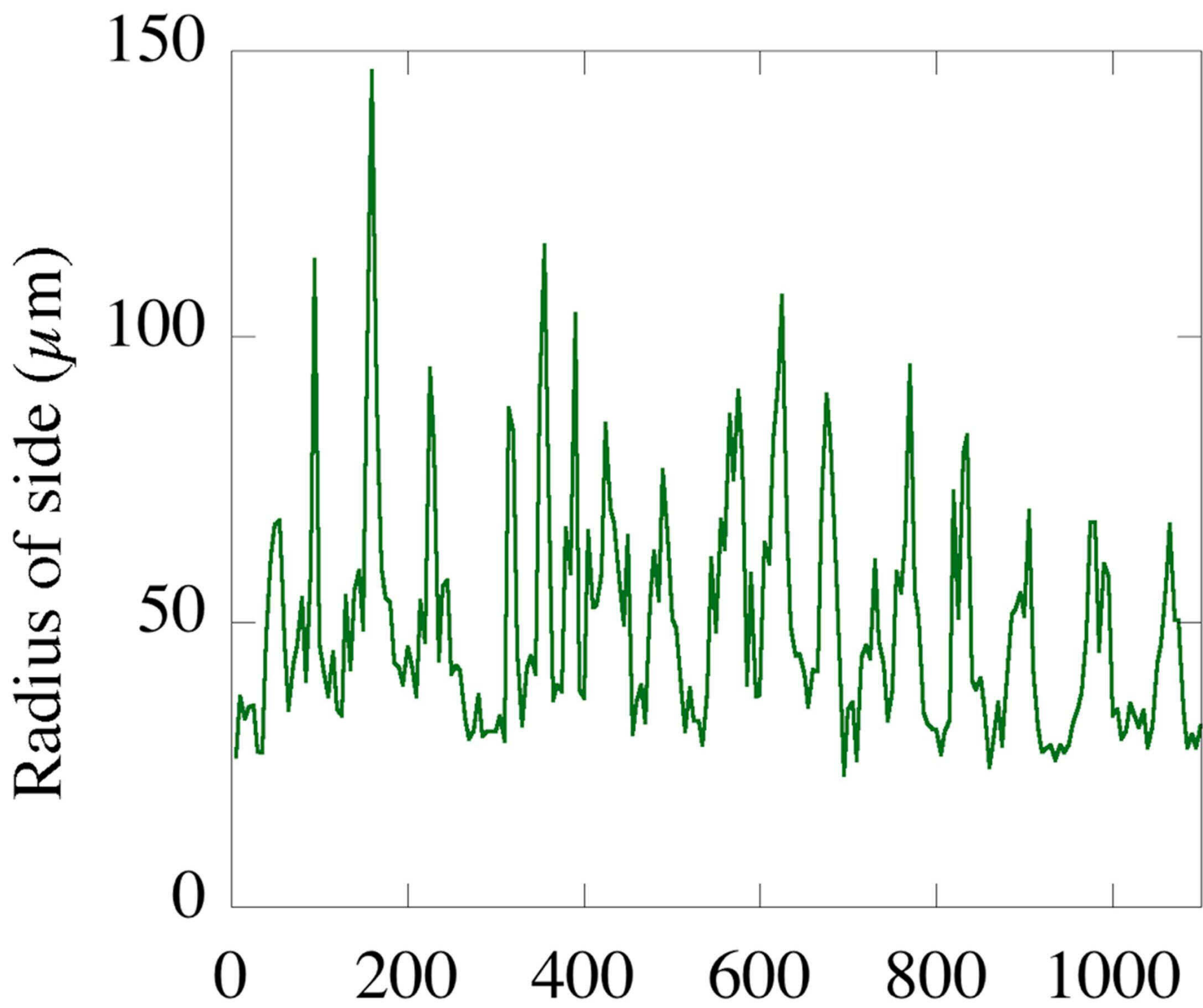
generating force

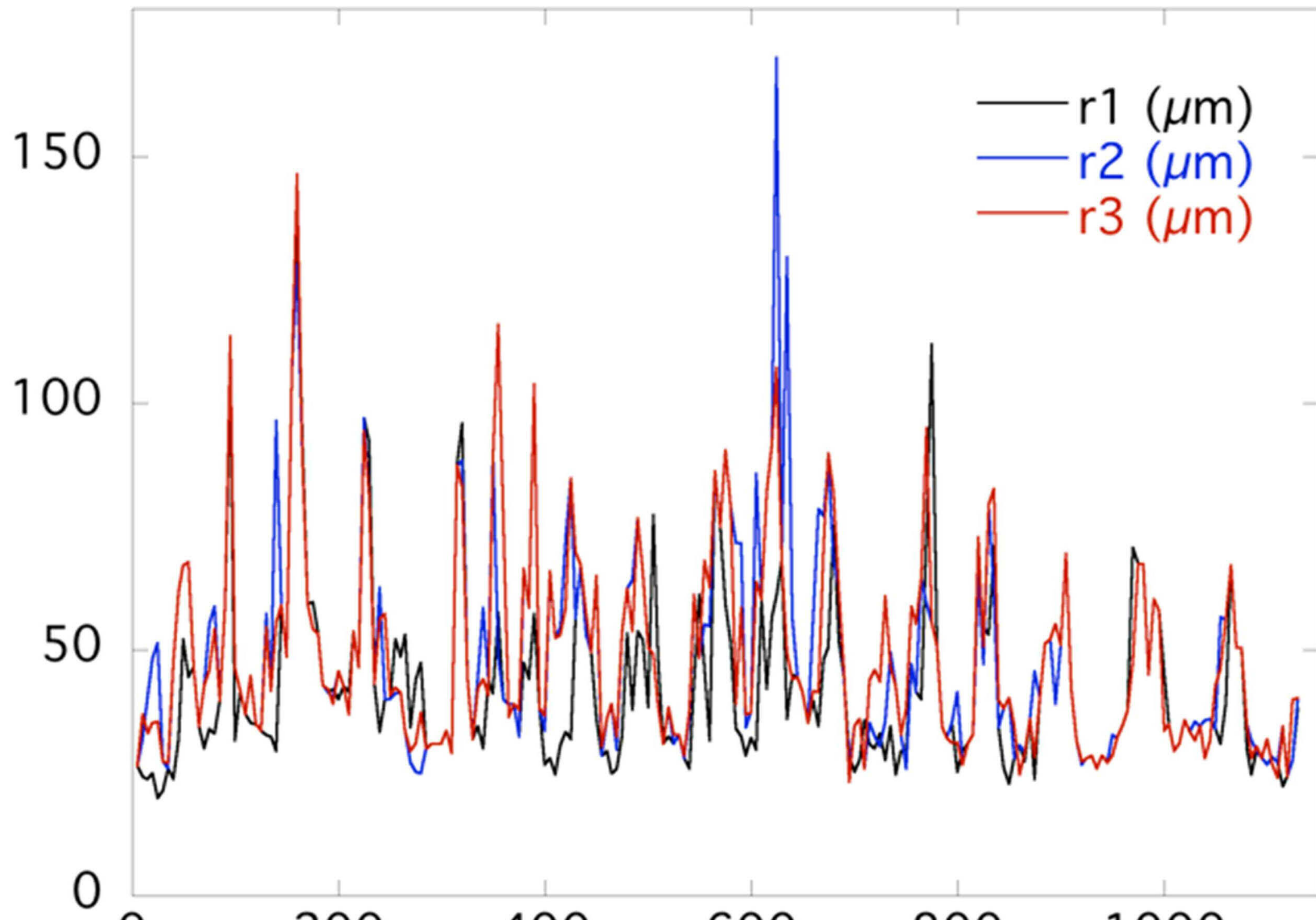
adhesive
island



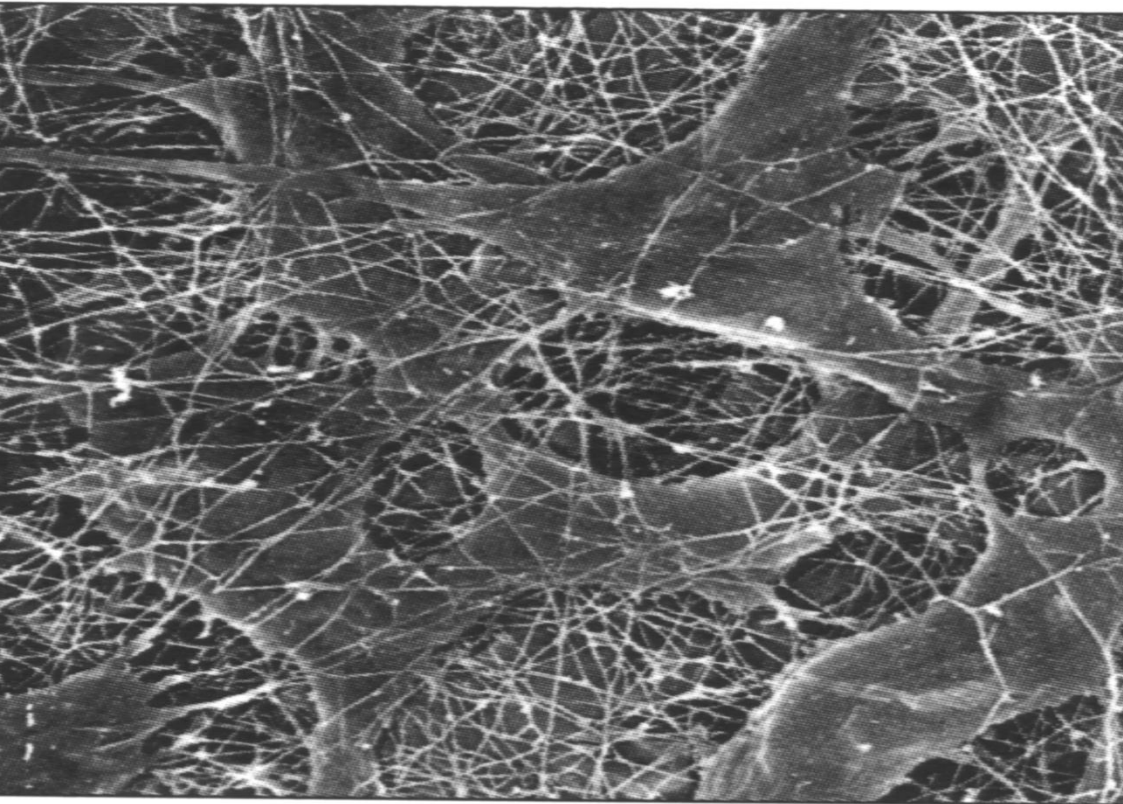
QuickTime and a
decompressor
are needed to see this picture.

Cells can measure stiffness, because they are always pulling

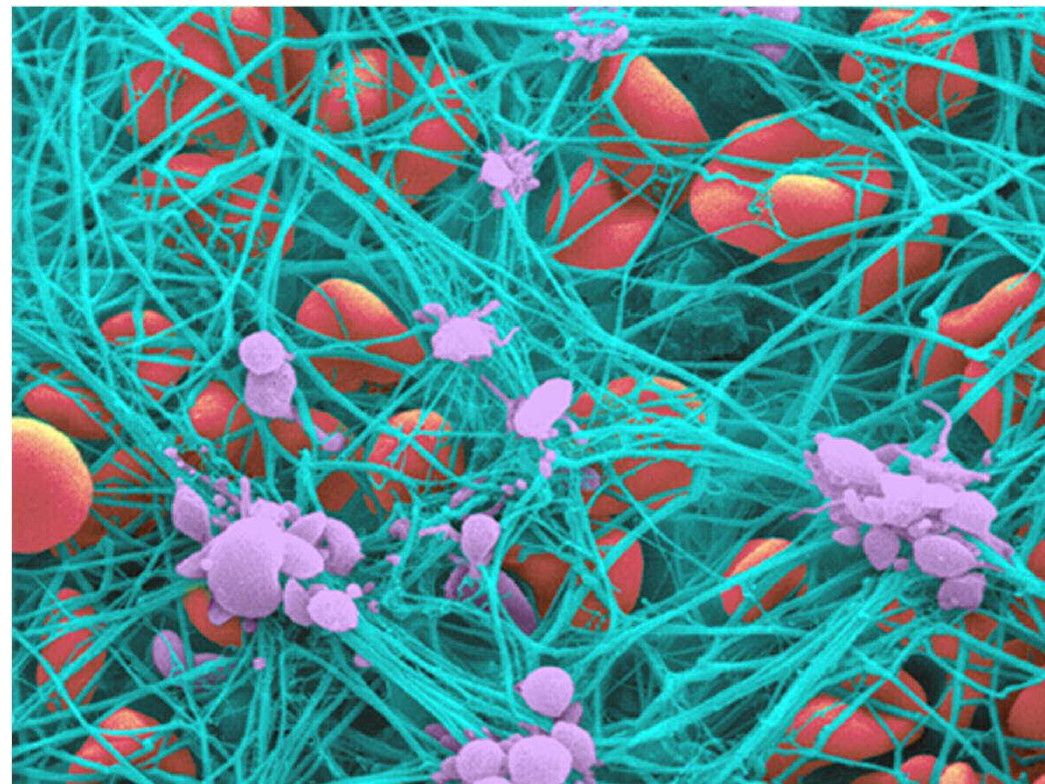




$E = 10$ to $100,000$ Pa) compared to plastic or glass ($E > \text{GPa}$)

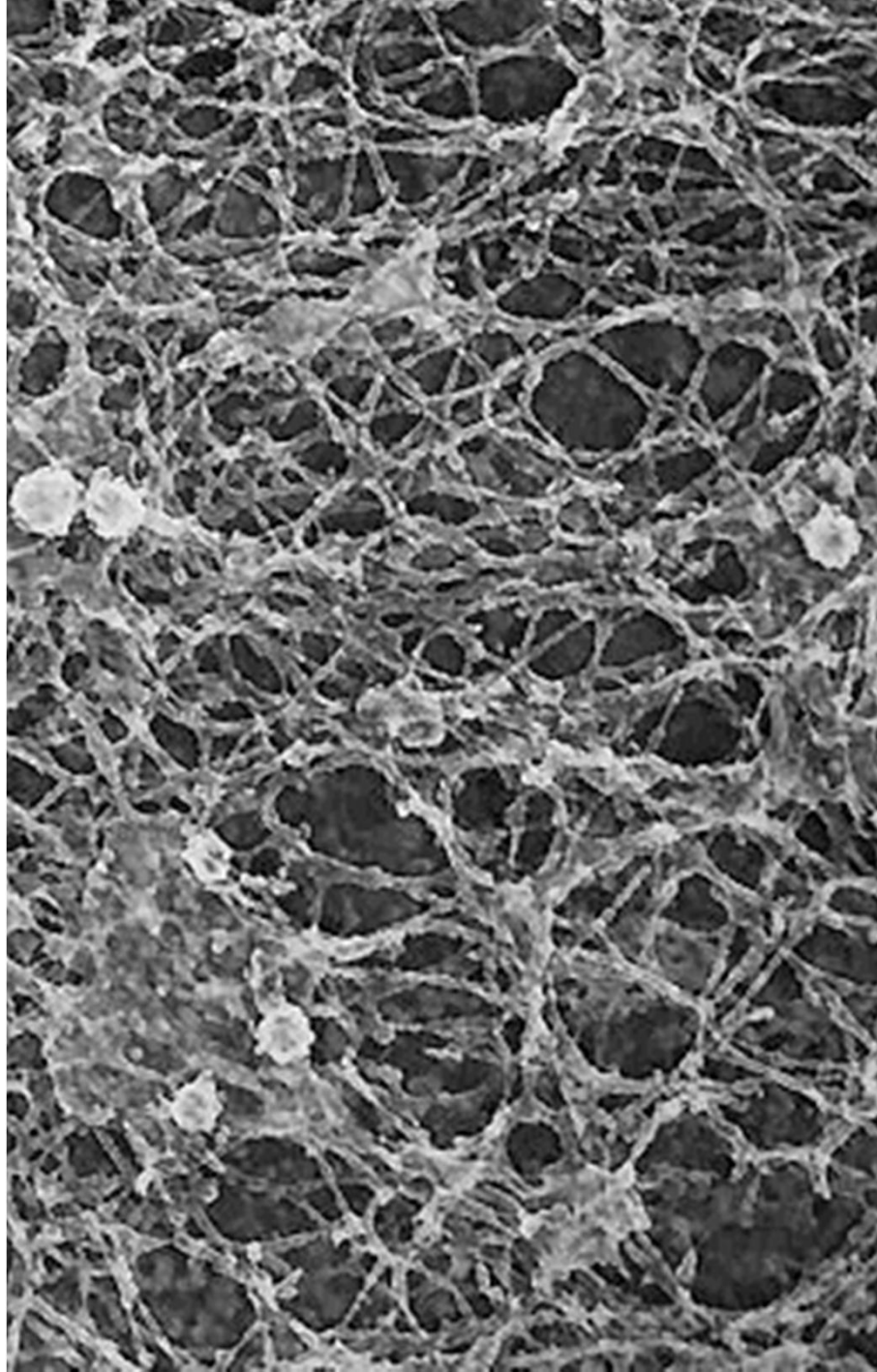


Fibroblasts in collagen ECM
(T. Nishida et al. Invest. Ophthalmol. Vis.)

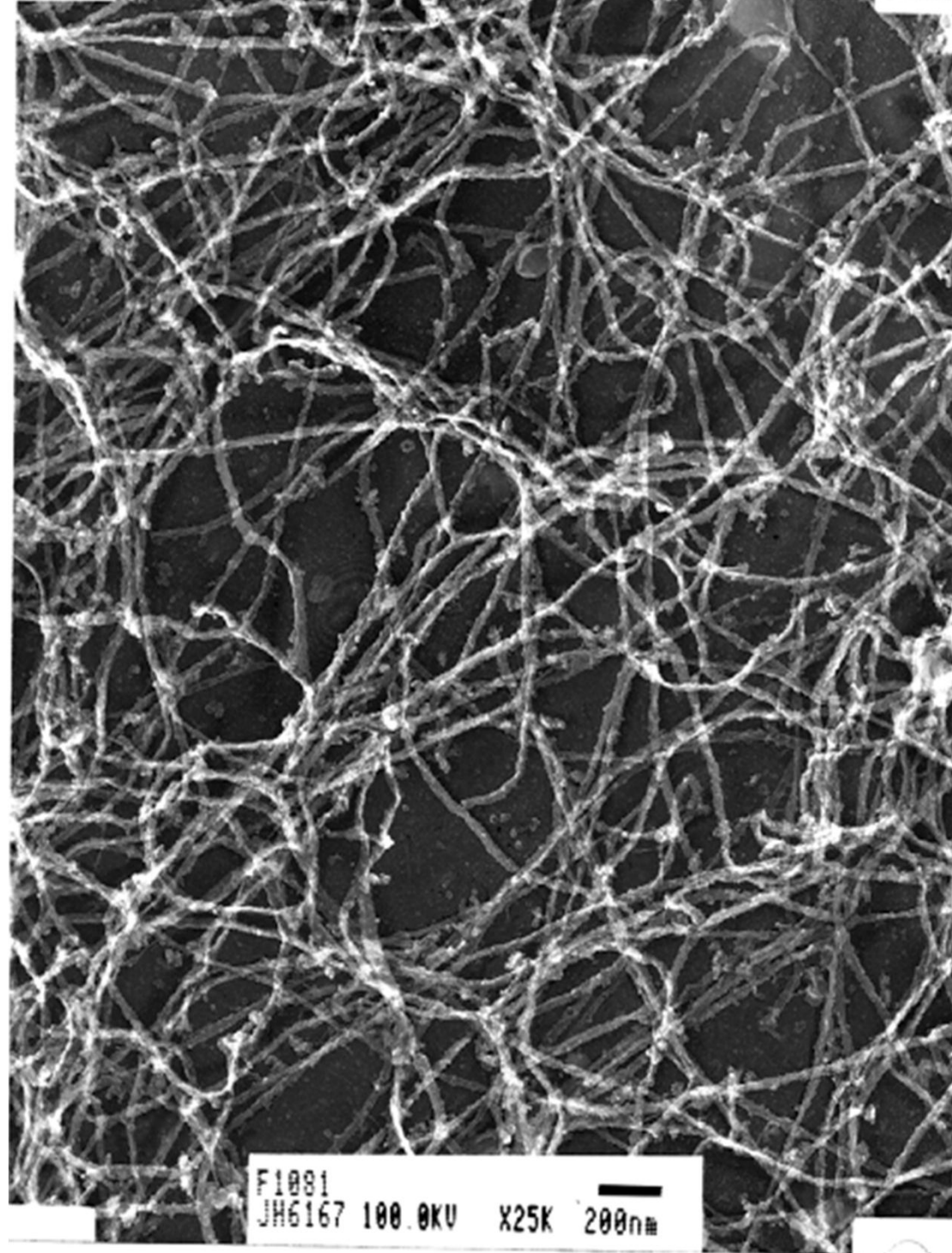


Red cells and **platelets** in
blood clot. John Weisel- Penn

Can rheology (stiffness) direct cell function and differentiation?
What magnitude of stiffness do cells probe (what's hard or soft)?



Cortical actin gel
JH Hartwig



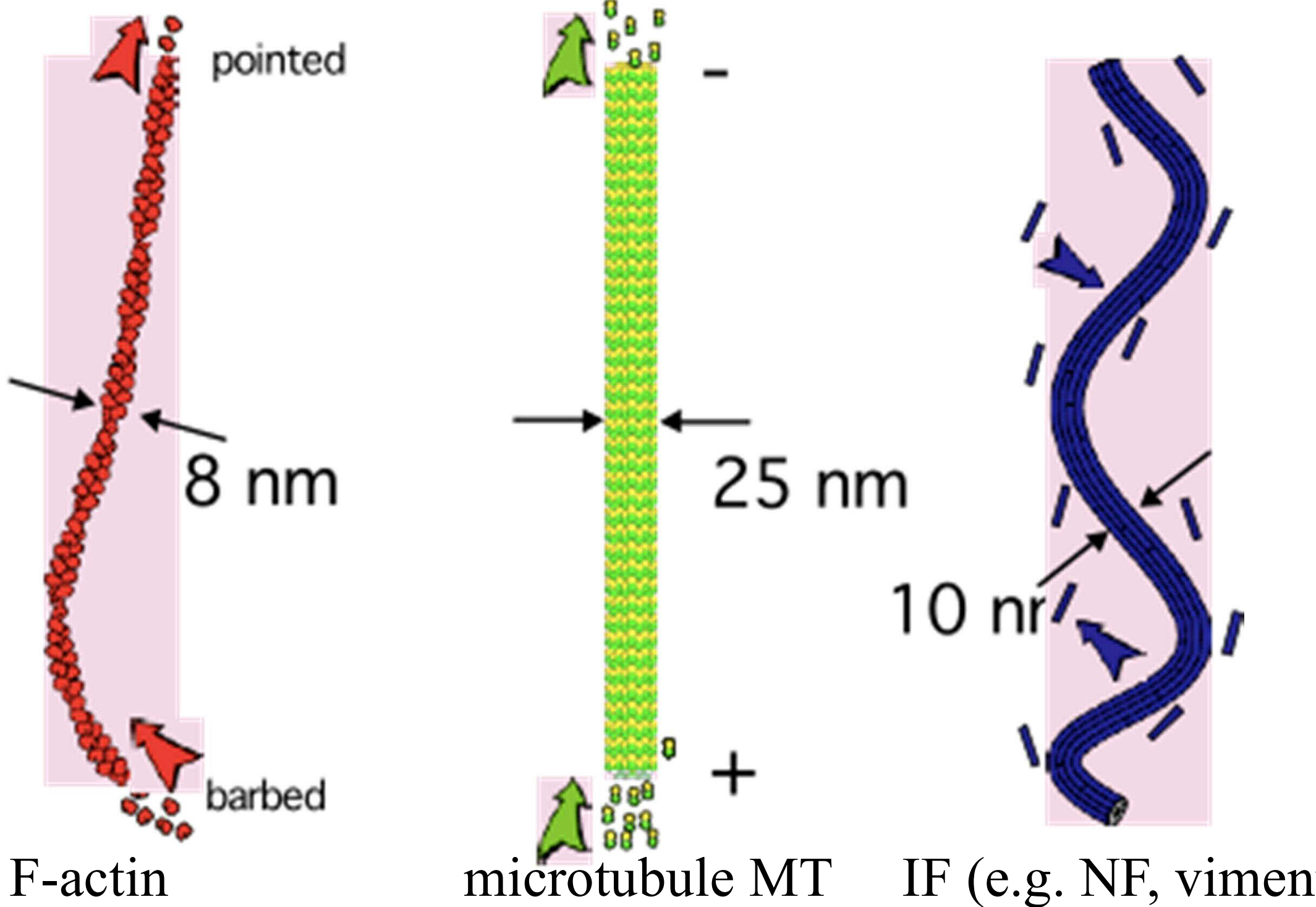
neurofilament network

filaments are all approximately
semiflexible polymers

Filament contour is slightly curved:

contour length $>$ but not \gg end-to end
distance, or distance between crosslinks

Thermal motions are sufficient to bend the
filament at least a little.



F-actin

microtubule MT

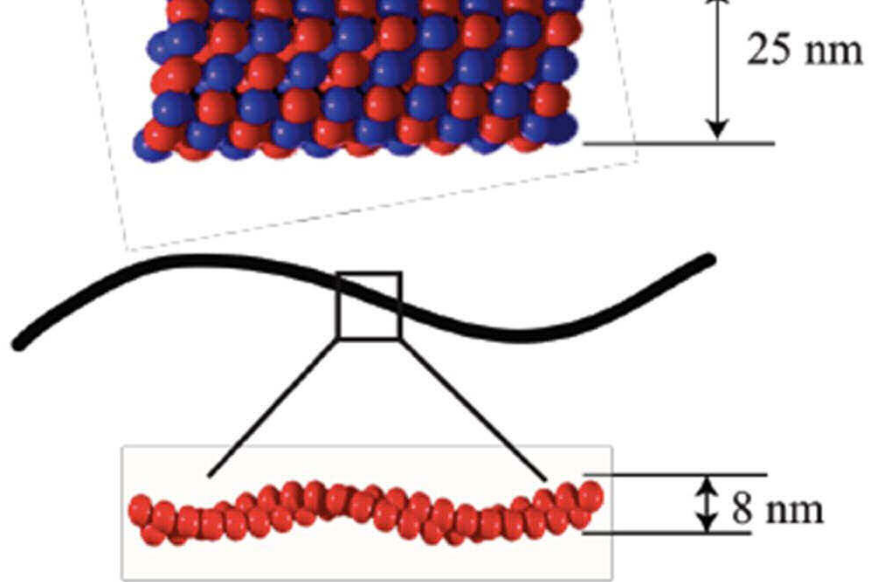
IF (e.g. NF, vimentin)

2-16

> 1

200-500

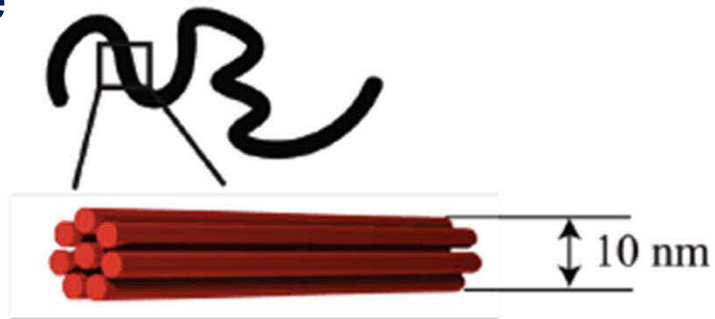
tin



$l_p \sim 10 \text{ } \mu\text{m}$

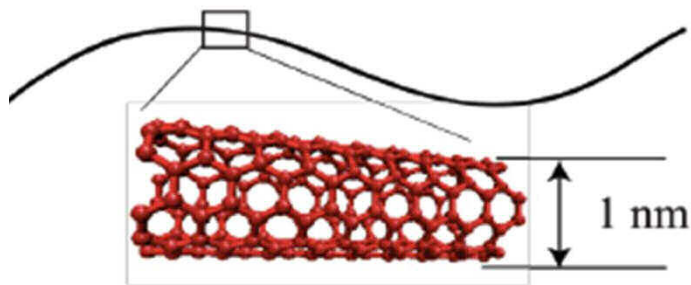
Uniquely extended
conformation of
biopolymers determi
their rheologic propere

diate
nts



$l_p < 1 \text{ } \mu\text{m}$

bon
oes



$l_p \sim 30 \text{ } \mu\text{m}$

Wen et al, Curr. Opin. Coll. 2

NA
e.g.

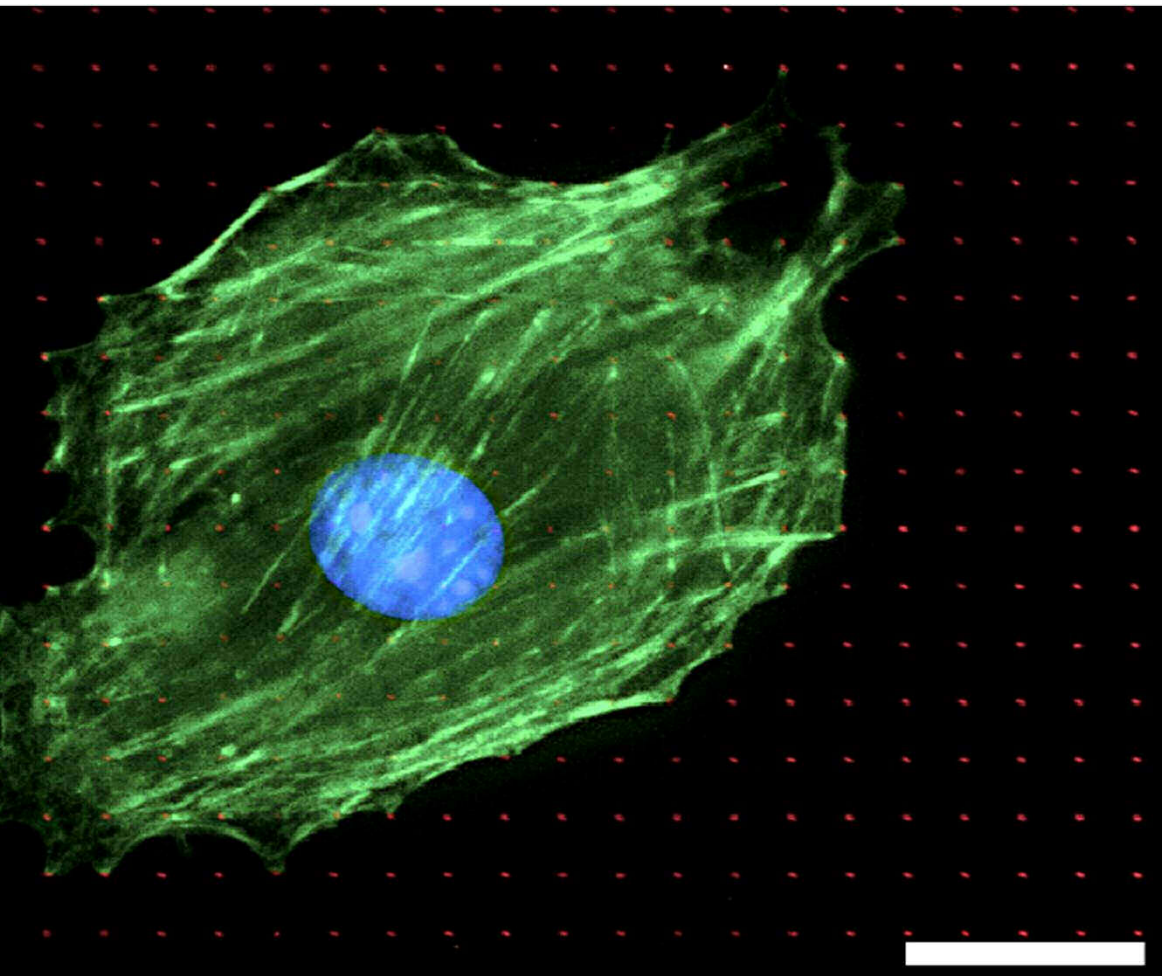


$l_p \sim 45 \text{ nm}$

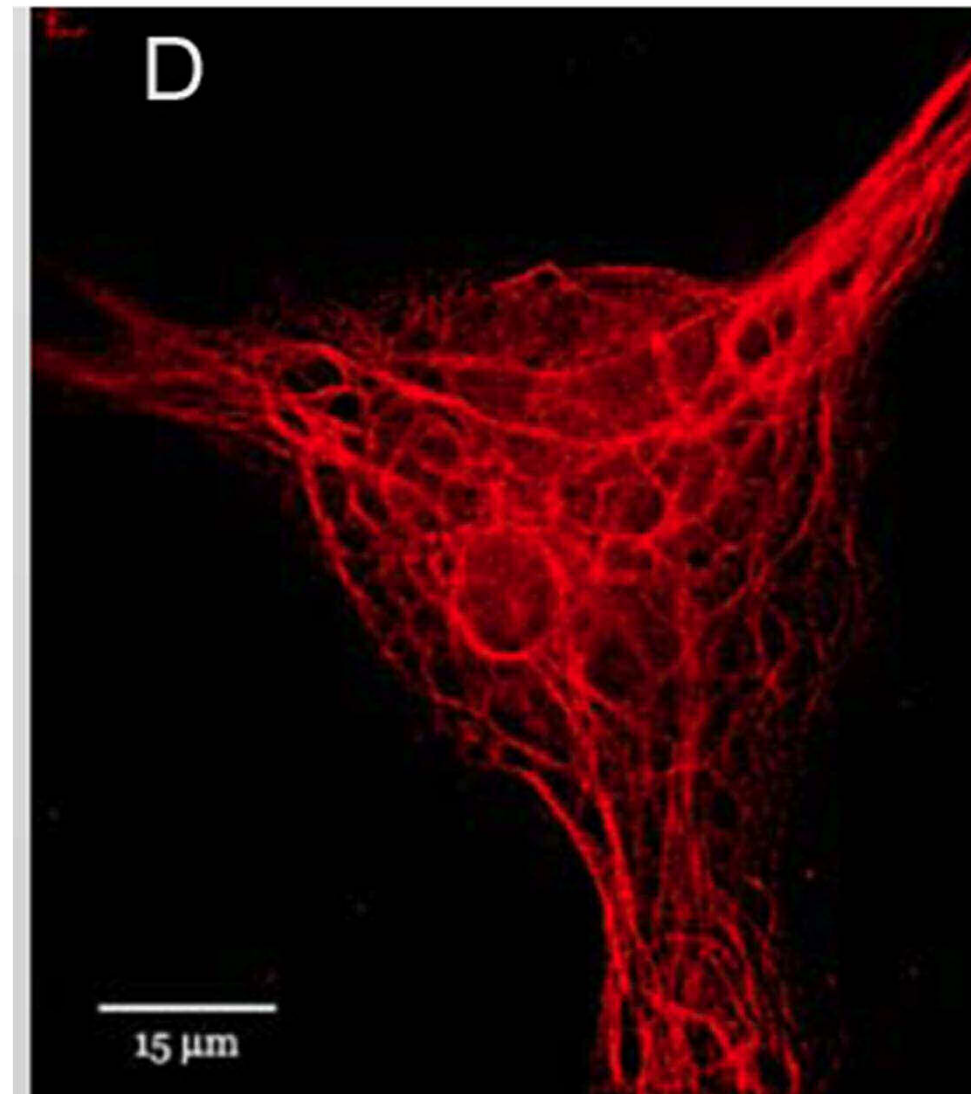
Polyethylene

$l_p \sim 0.3 \text{ nm}$

polyethylene

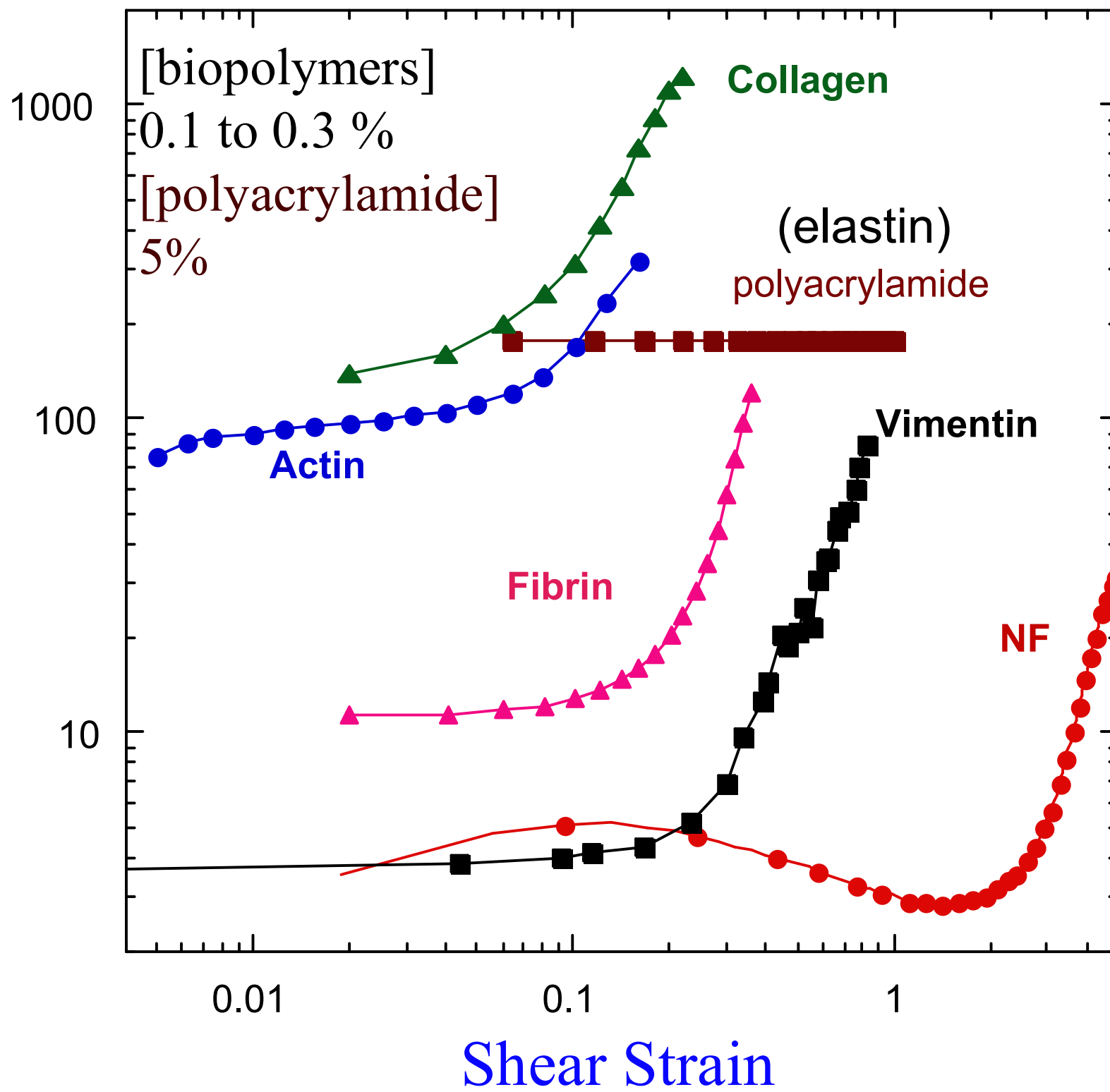


in filaments in a fibroblast

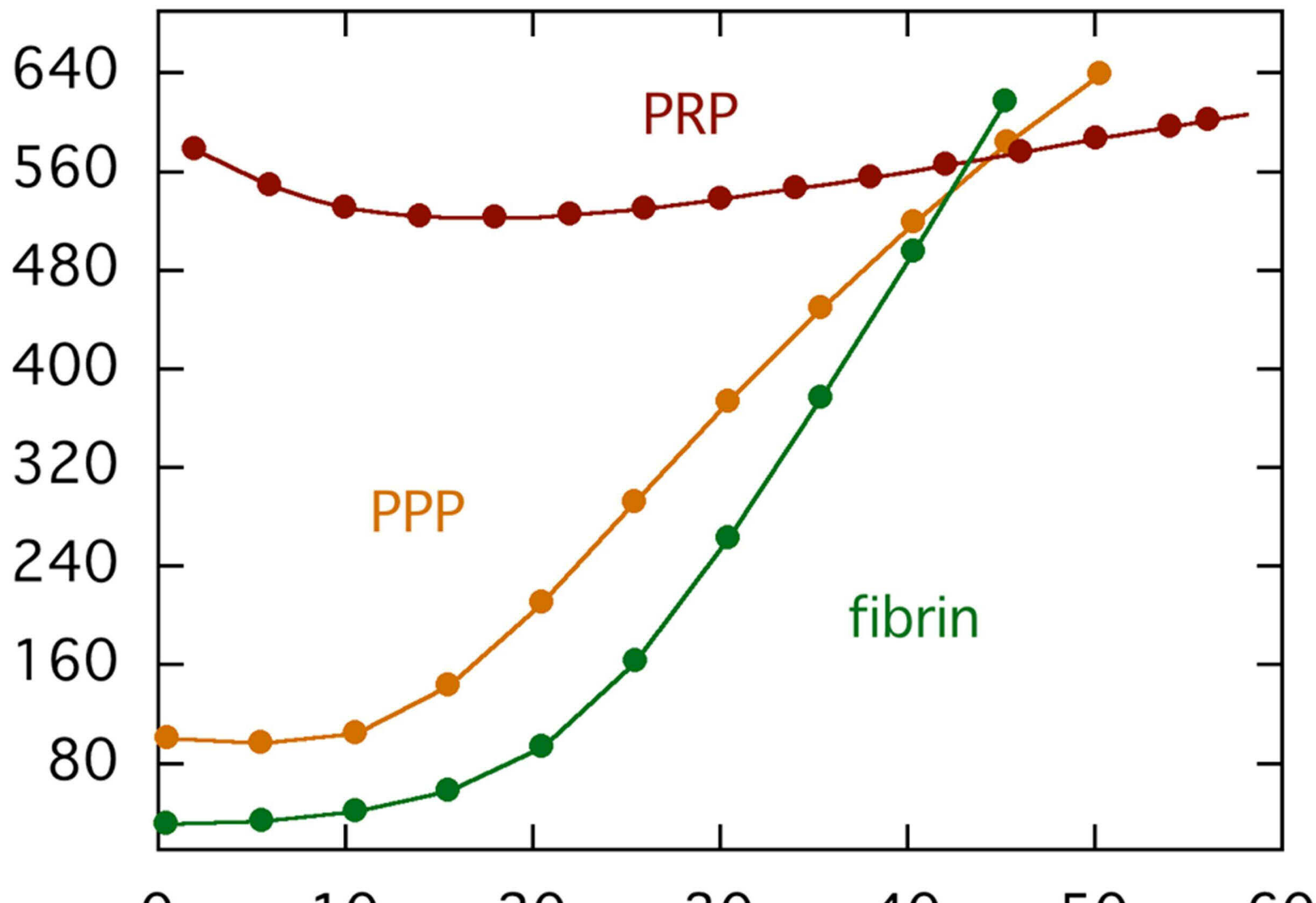


Intermediate filaments in an astrocyte

Shear modulus, G (Pa)

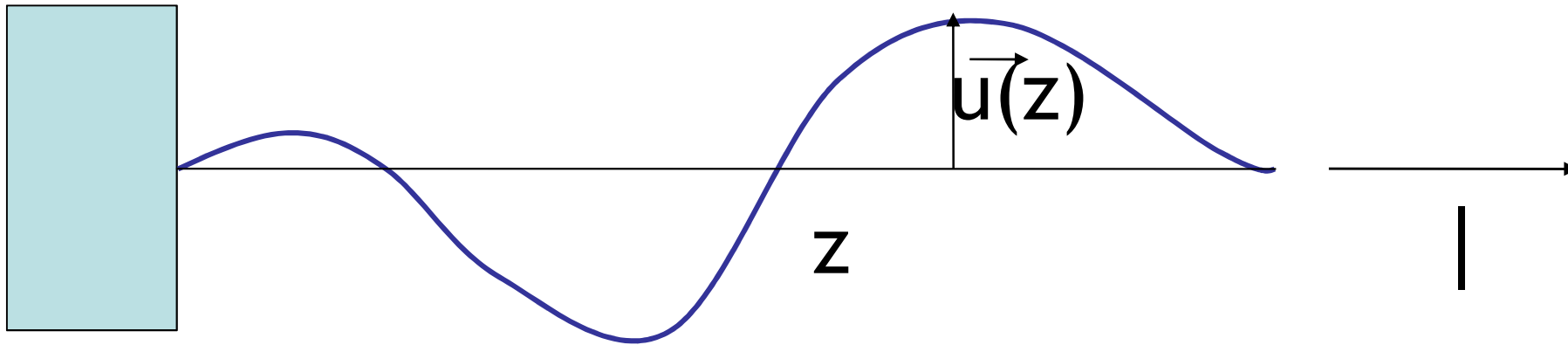


Storm et al
Nat. 2005
Gardel et al
Sci 2005



Why are networks of biopolymers strain-stiffening?

1. Intrinsic non-linear force-extension relation of thermally fluctuating semi-flexible polymer
entropic, affine
2. Orientation of stiff fibers in network under shear
shift from bending to stretching
enthalpic, non-affine,
fiber need not have non-linear elasticity

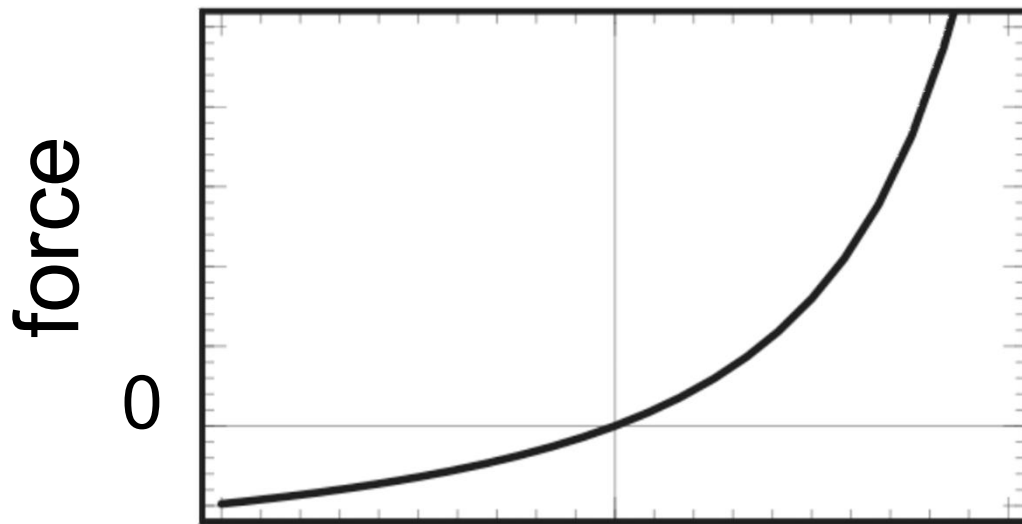


energy :

$$E = \int_0^L dz \left\{ \frac{\kappa}{2} |\vec{u}''|^2 + \frac{\tau}{2} |\vec{u}'|^2 \right\}$$

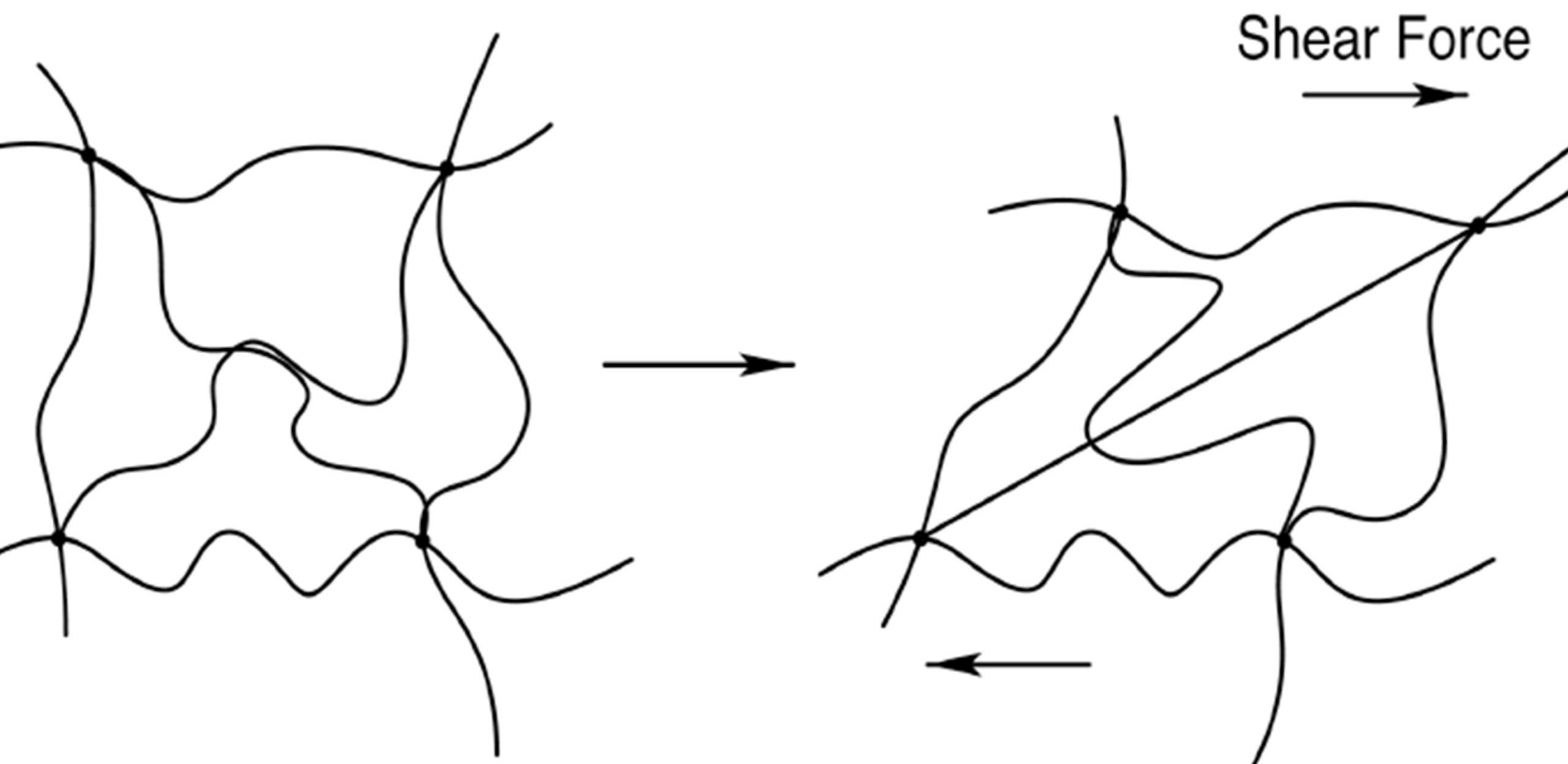
force-extension :

$$\langle \Delta L \rangle = L_c - r = \frac{L_c^2}{l_p \pi^2} \sum_n \frac{1}{(n^2 + \phi)}$$



) = normalized force = $\frac{r}{L_c}$

... predicts increasing stiffness with increasing str...



Model needs as input: mesh size, bending stiffness
Assumes that network is isotropic and the persistence length
similar to mesh size

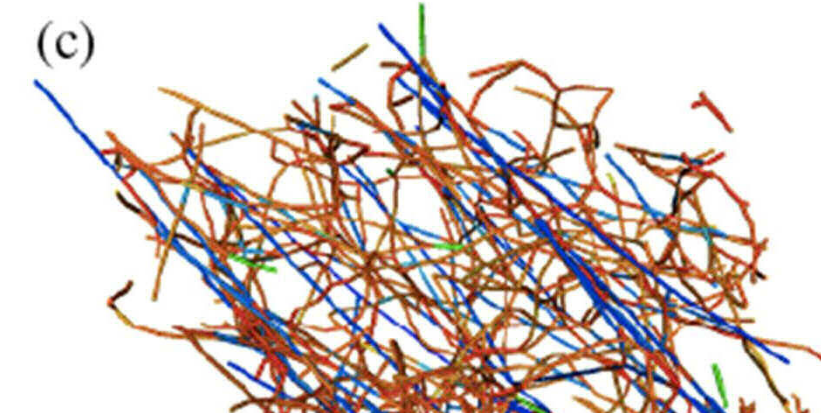
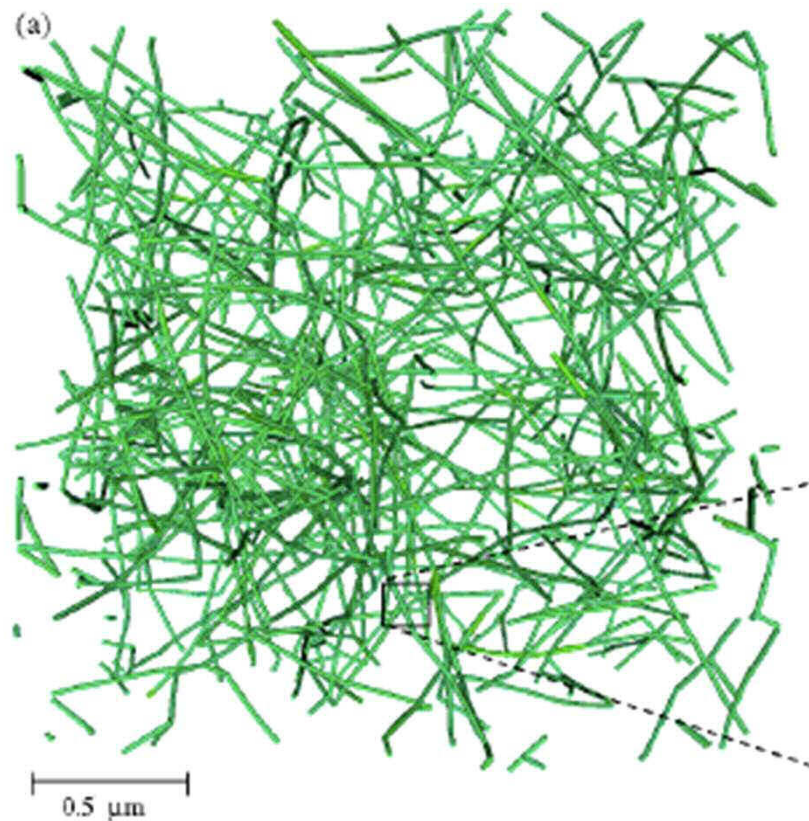
ent alignment, something contractile cells do very w

P. R. Onck, et al. PRL 95,
178102 (2005).

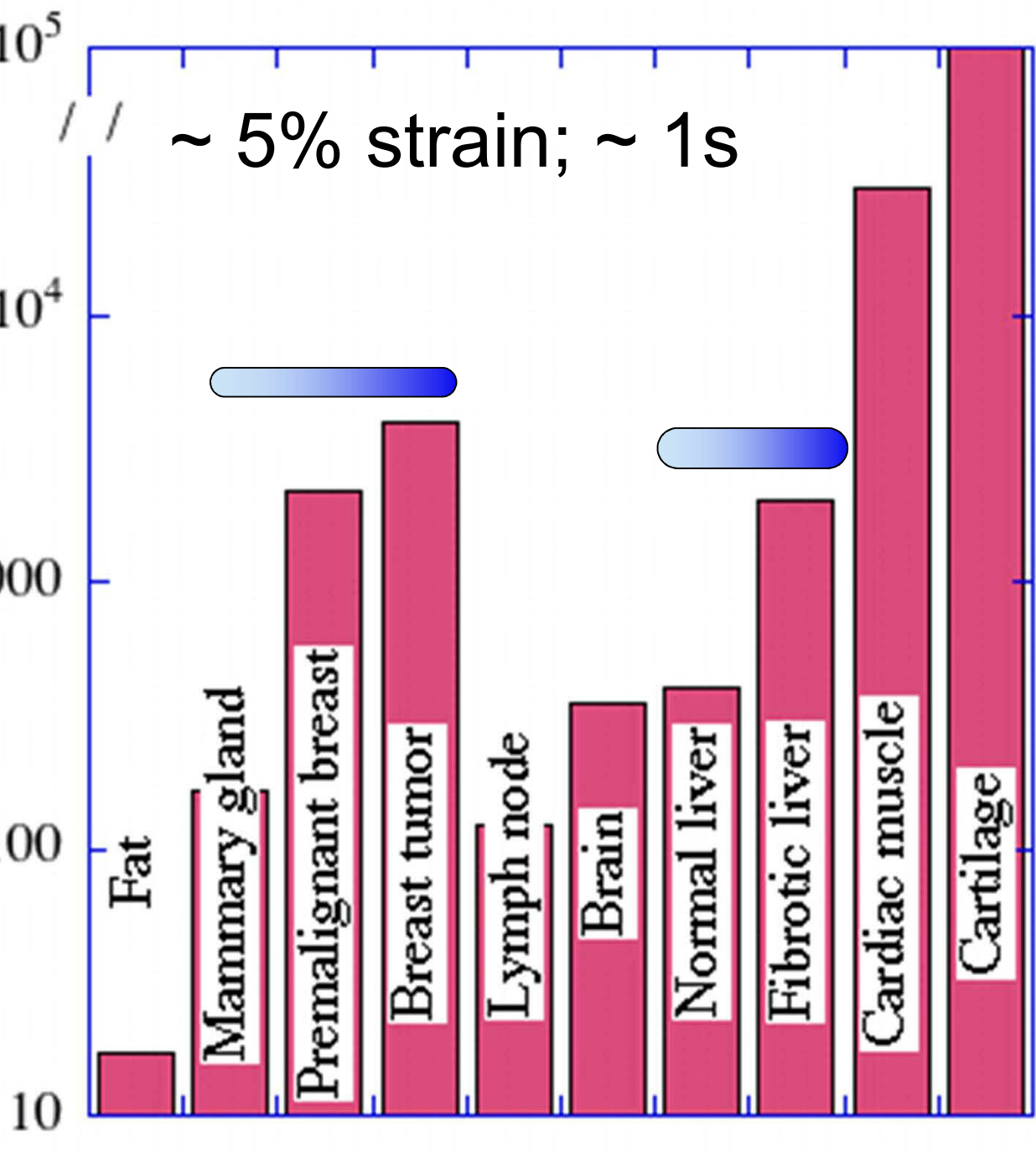
QuickTime and a
BMP decompressor
are needed to see this picture.

Three-Dimensional Cross-Linked F-Actin Networks: Relation between Network Architecture and Mechanical Behavior

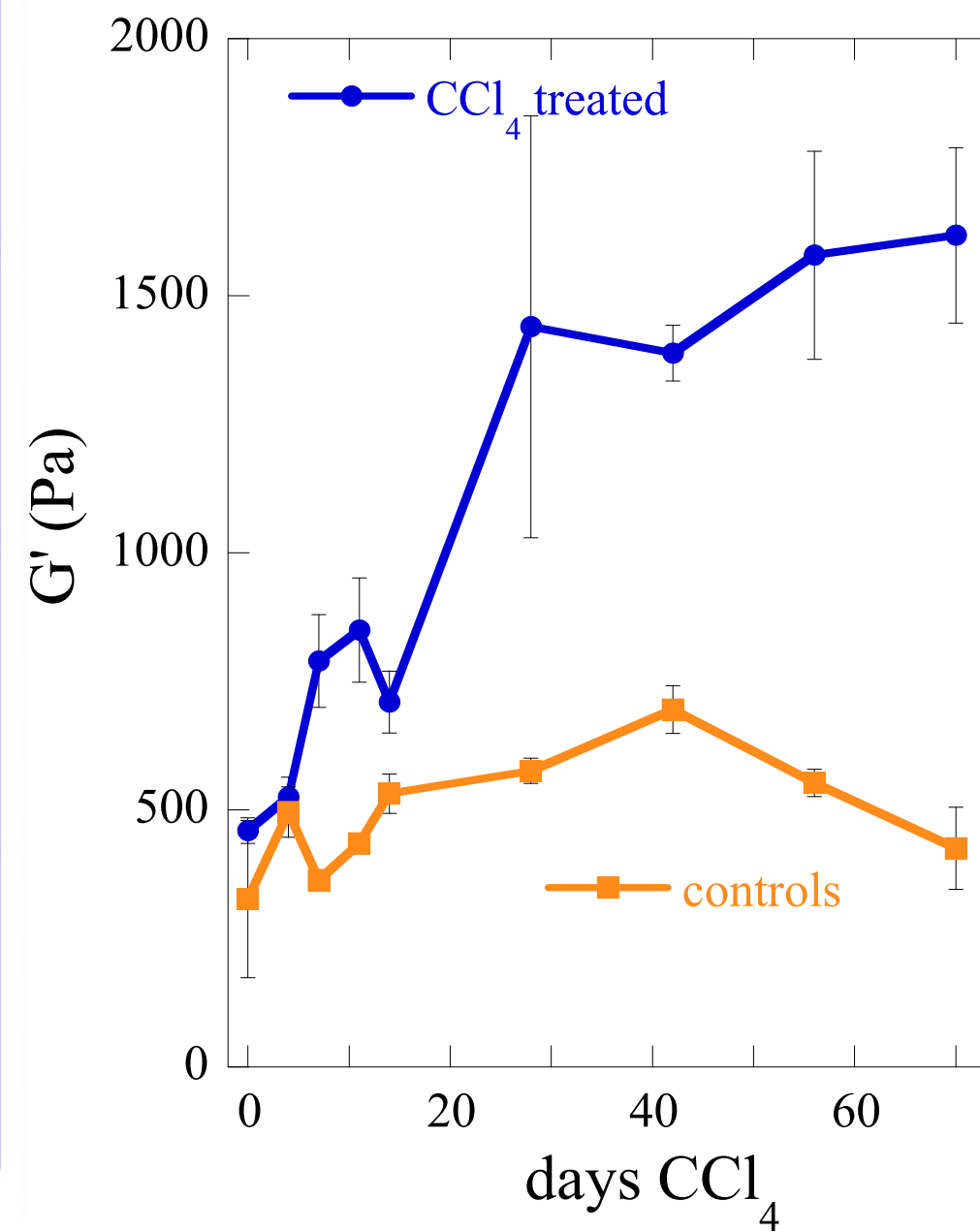
E. M. Huisman, T. van Dillen, P. R. Onck, and E. Van der Giessen



characterized by an elastic modulus

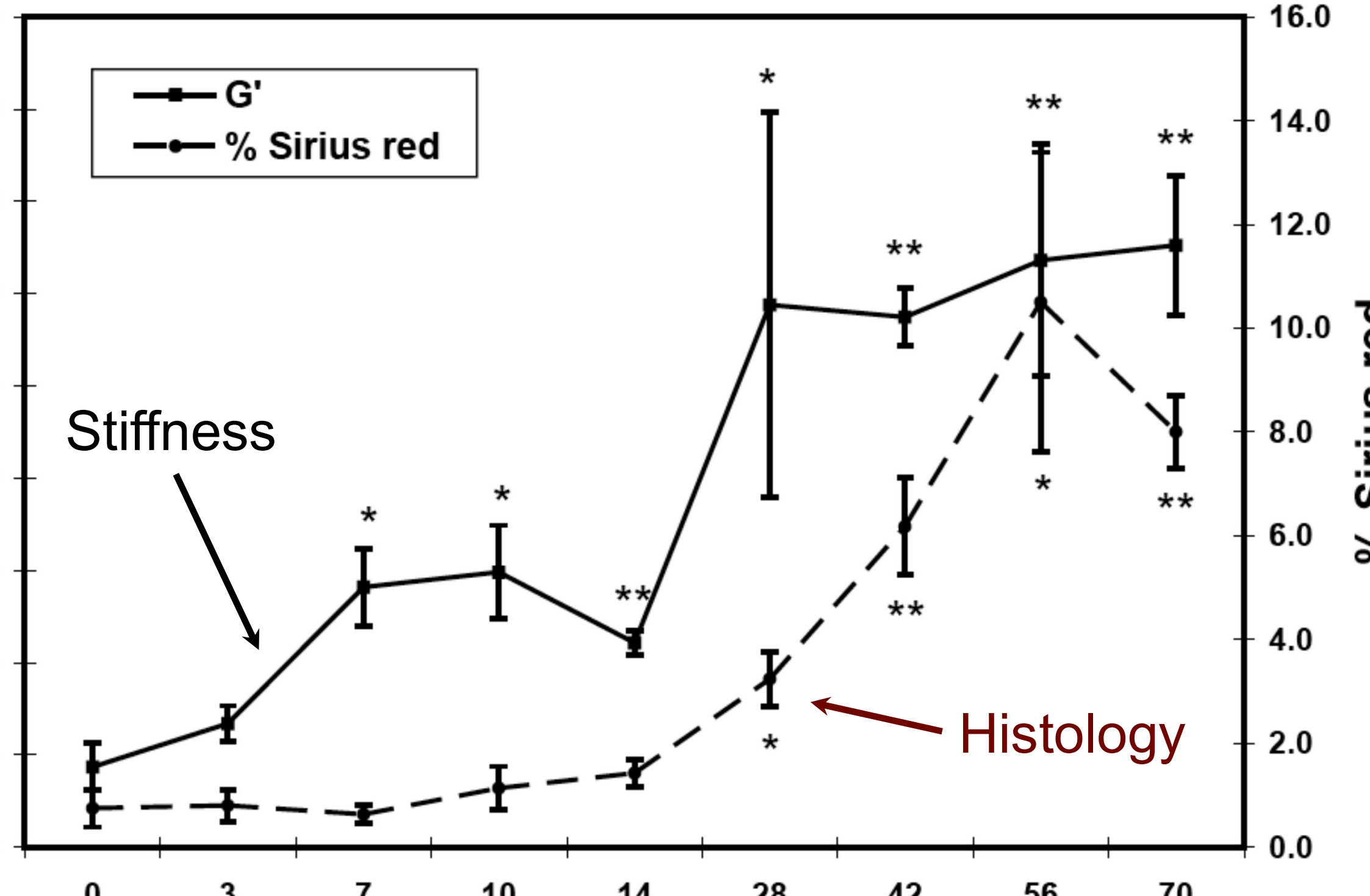


Change in liver stiffness after inducing



Changes in organ stiffness often accompany diseases

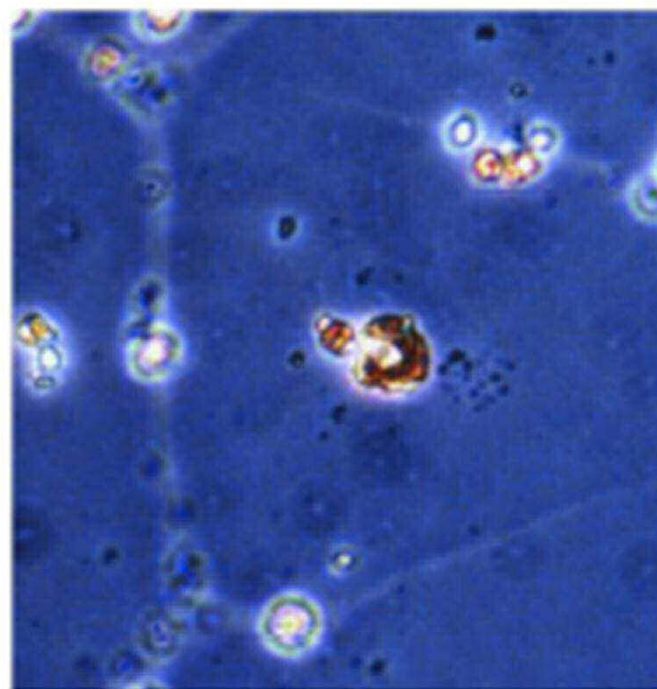
Biological evidence of fibrosis occurs *after* liver stiffening



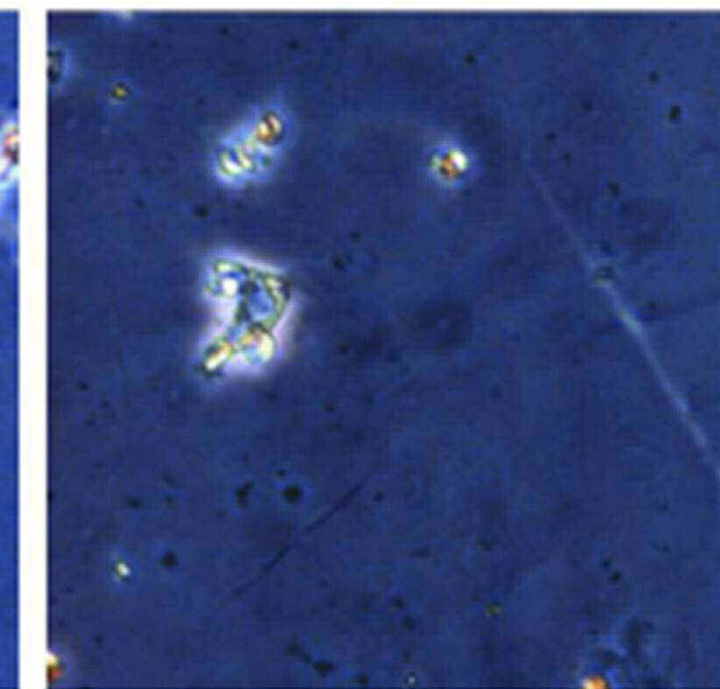
Mechanobiologically stiff substrates

ecca
s

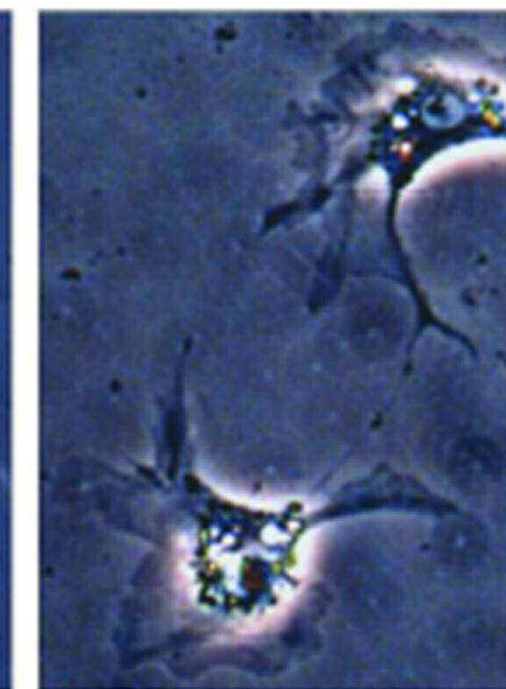
0.4 kPa



1.0 kPa

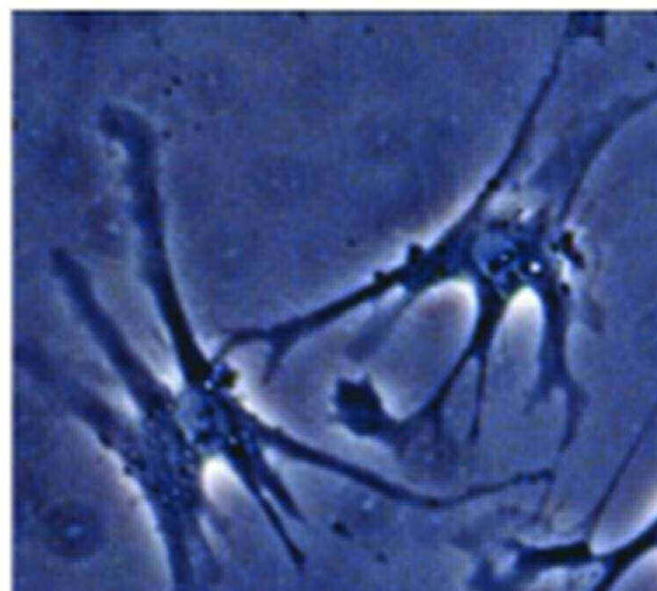


1.75 kPa

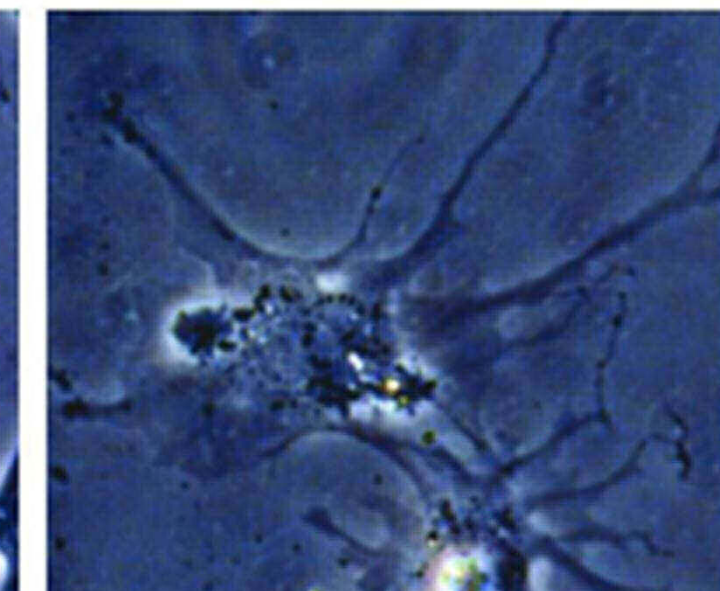


et al,
Physiol.

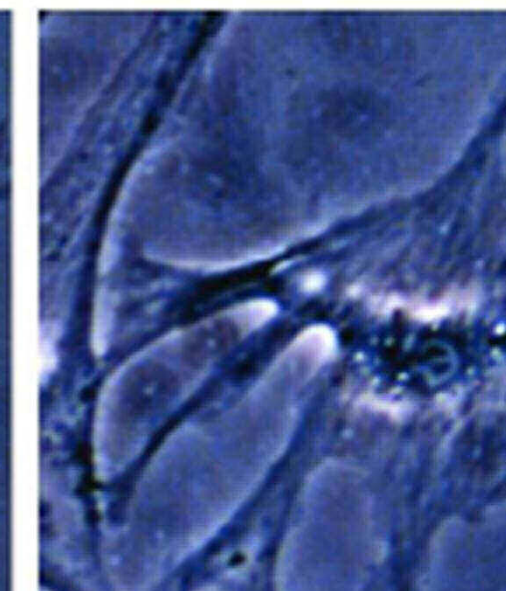
2.5 kPa



8.0 kPa



12 kPa



What determines tissue stiffness?

Extracellular matrix
Cytoskeleton

Passive viscoelasticity or poroelasticity

Active (motor driven) tension and non-thermal motions

Extracellular and intra-tissue pressures / water flow

Wells and pillar arrays

nm

um

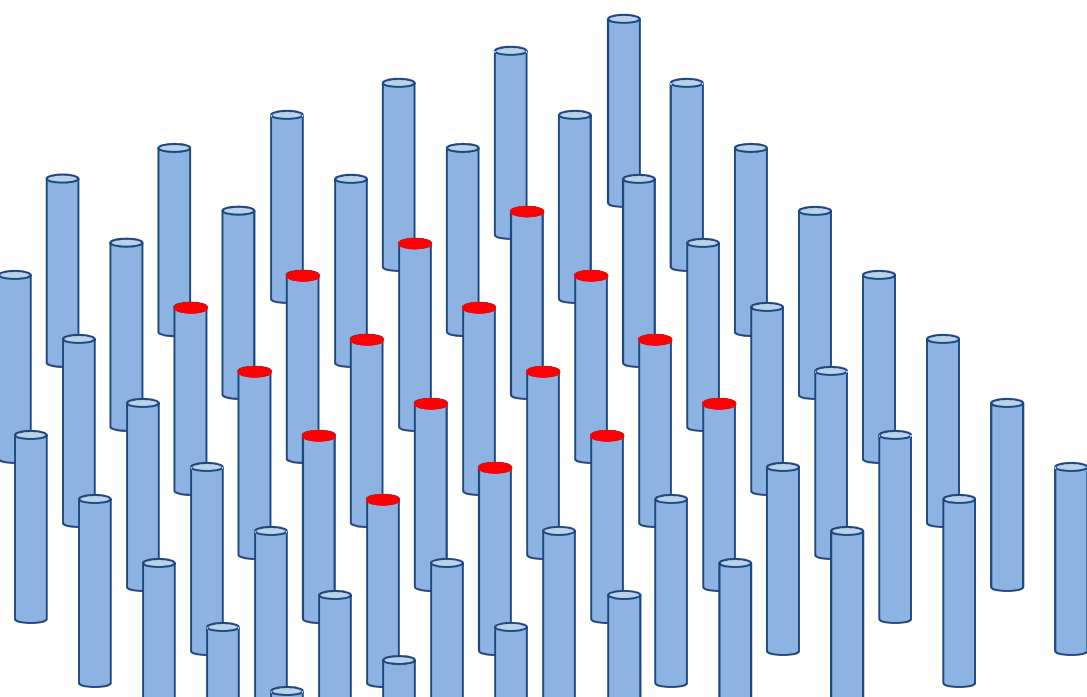


ECM protein

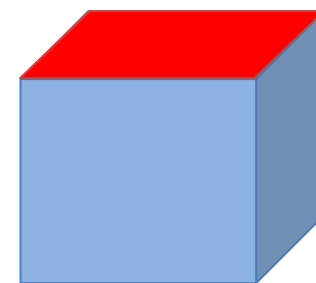
cadherin

PA gel

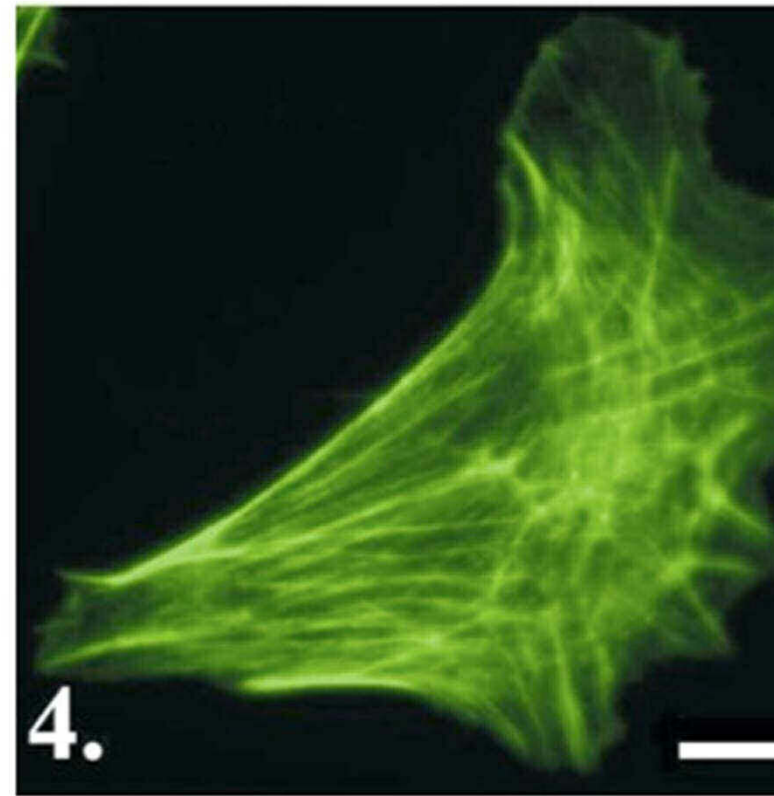
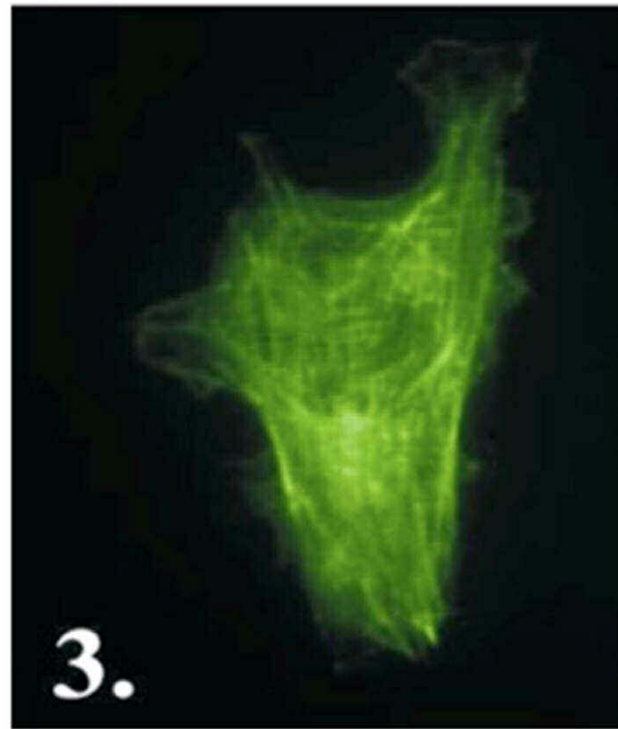
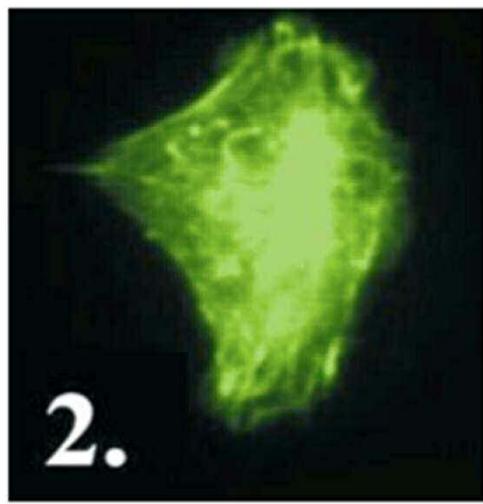
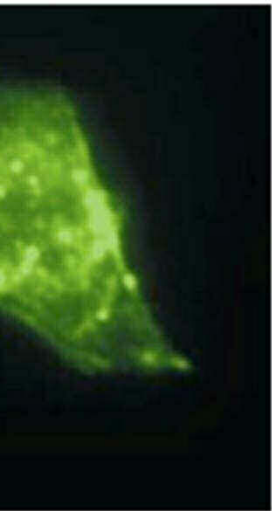
Glass



PDMS



20um ; green = GFP-actin

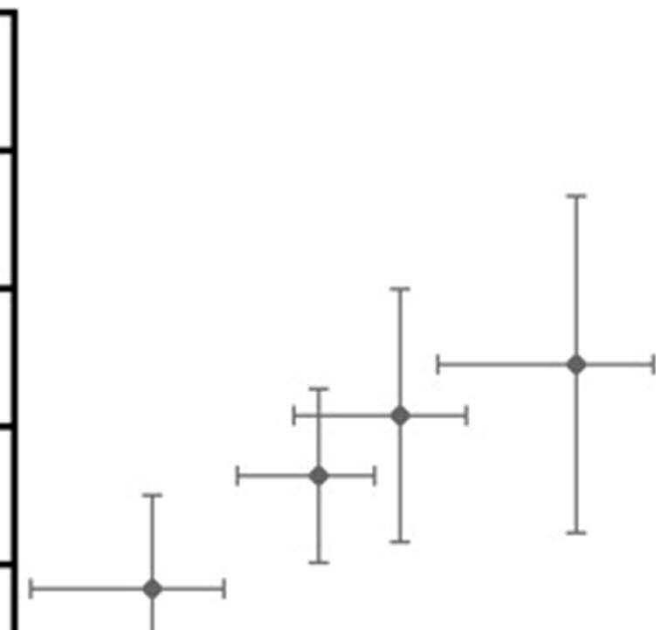


kPa

5kPa

10kPa

Glass ~ GPa

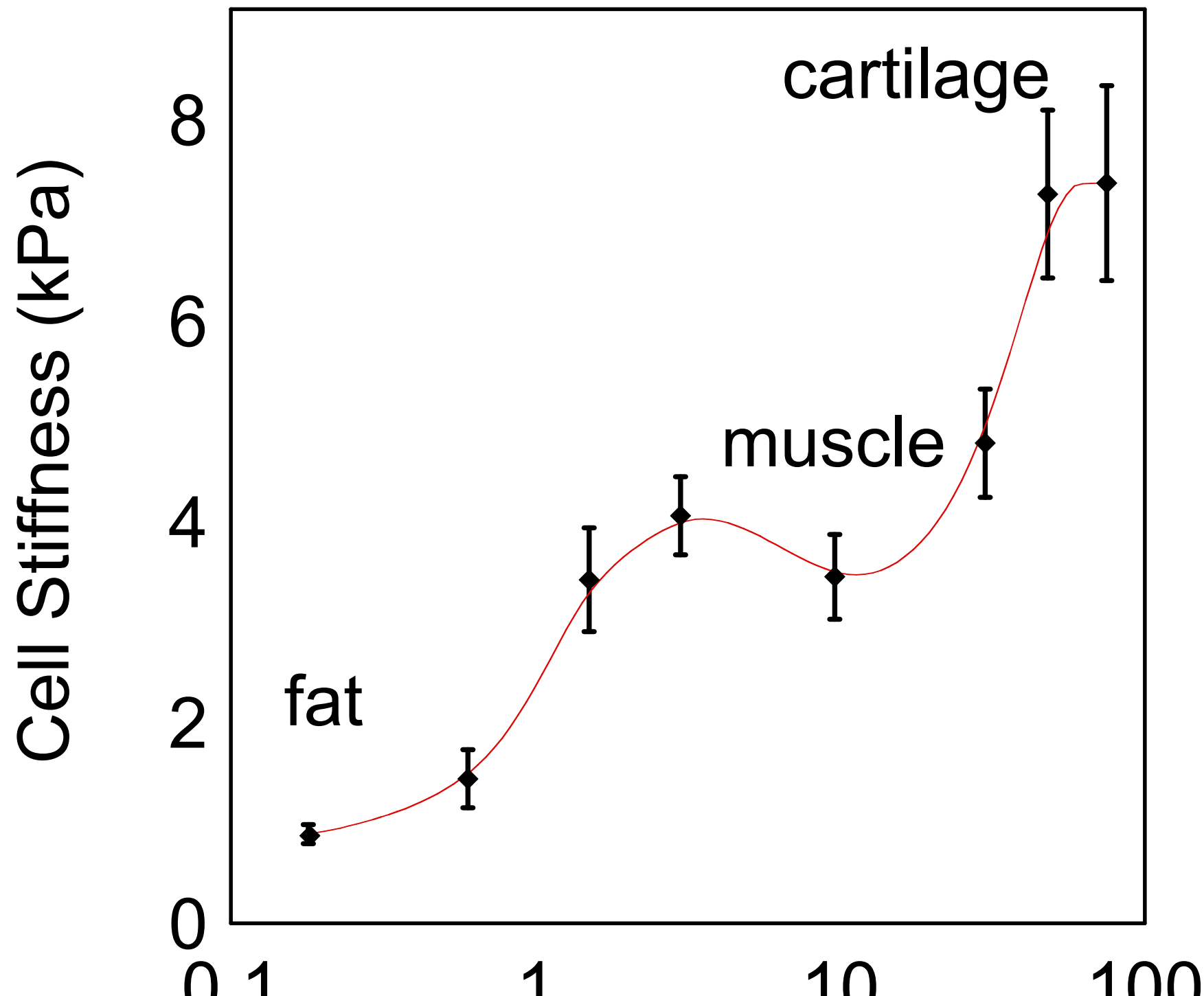


Pelham and Wang PNAS 1

Fibroblasts stiffen and increase adherent area on stiff substrates

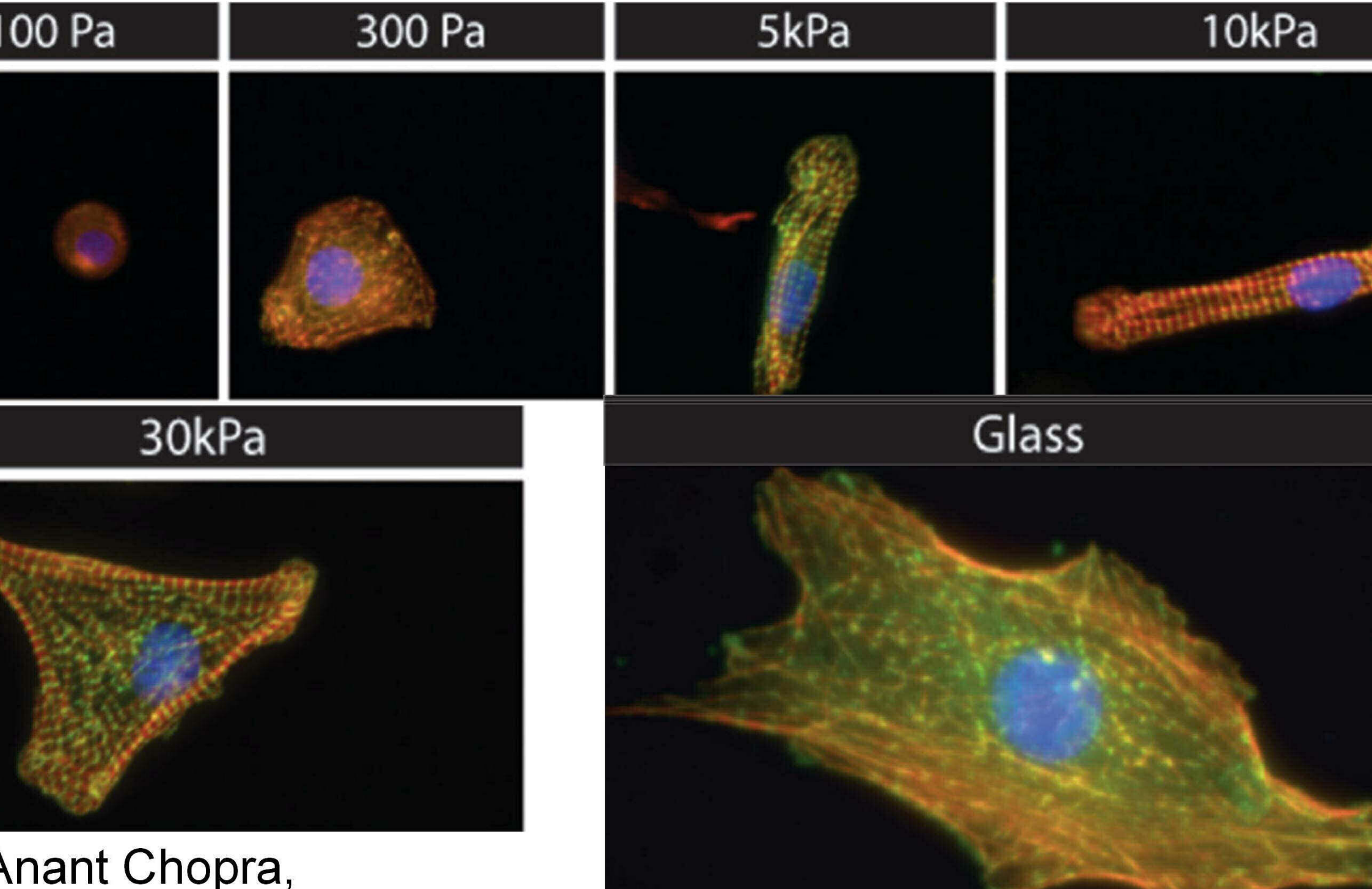
Selen et al. Biophys J 2007

Biphasic change in hMSC stiffness

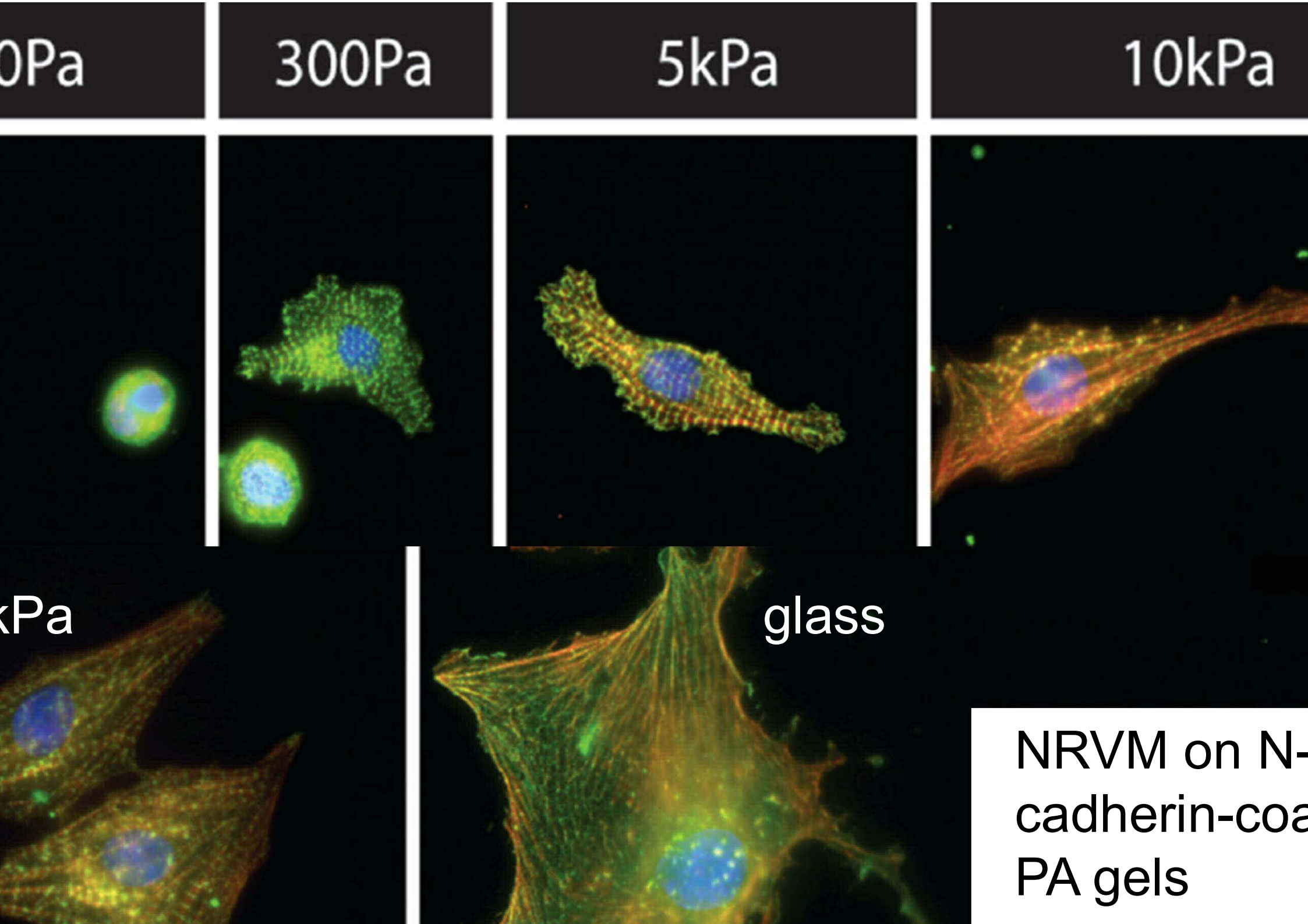


F-actin

α -actinin



Anant Chopra,



How do cells sense or respond to stiffness?

What is the range of stiffness that can be probed?

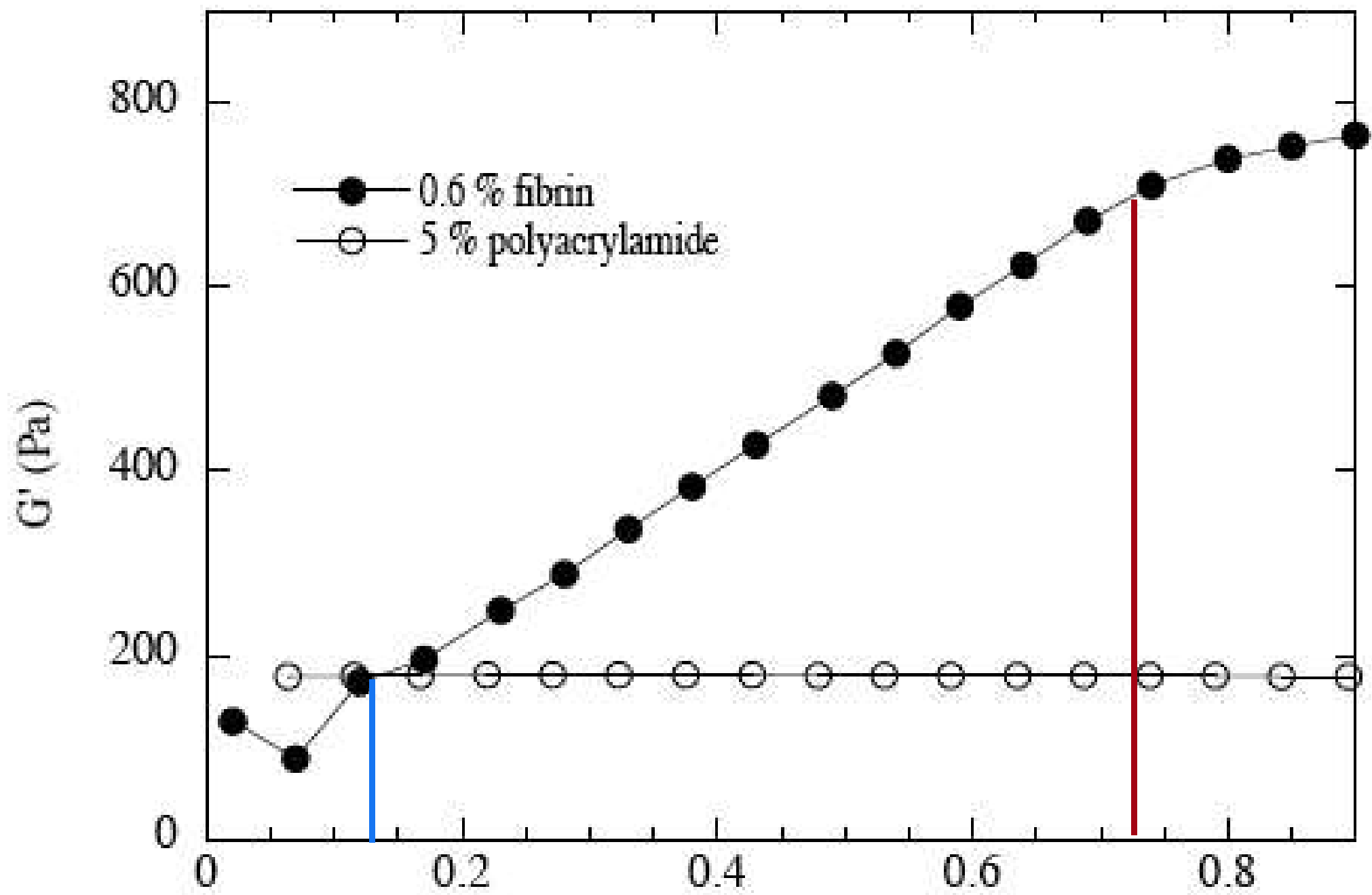
- 100,000 Pa

How much do they strain their substrate?

How large an area do they probe?

How long do they integrate signal?

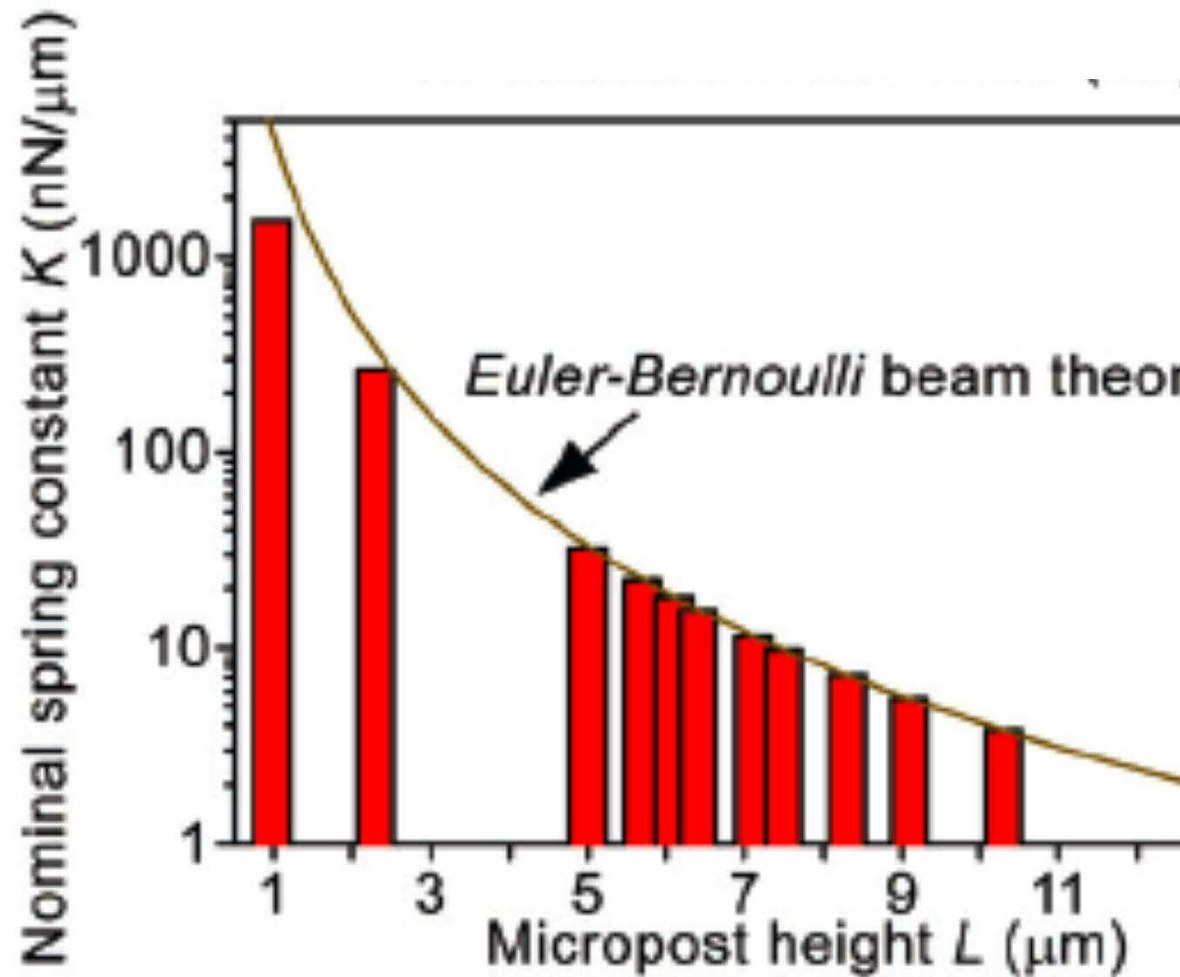
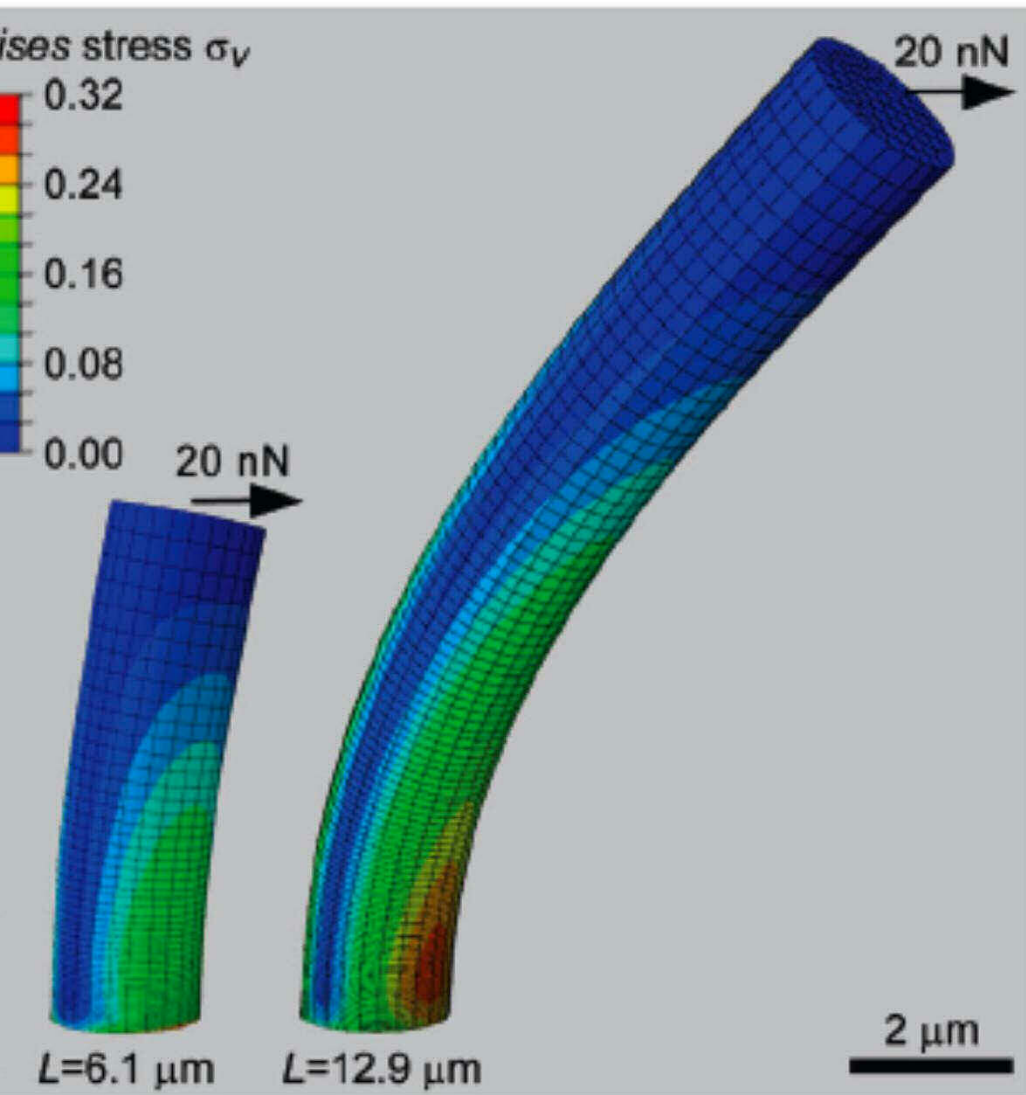
How much do you deform its substrate



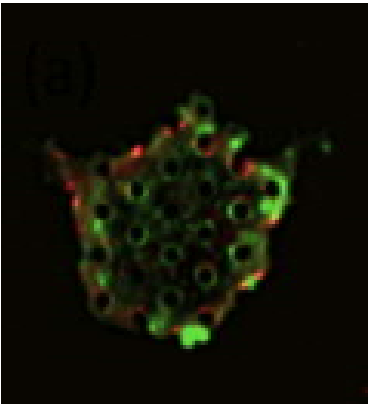
Small strain
Same stiffness

Large strain
Fibrin is stiffer

v large a contact area is needed for mechanosensing

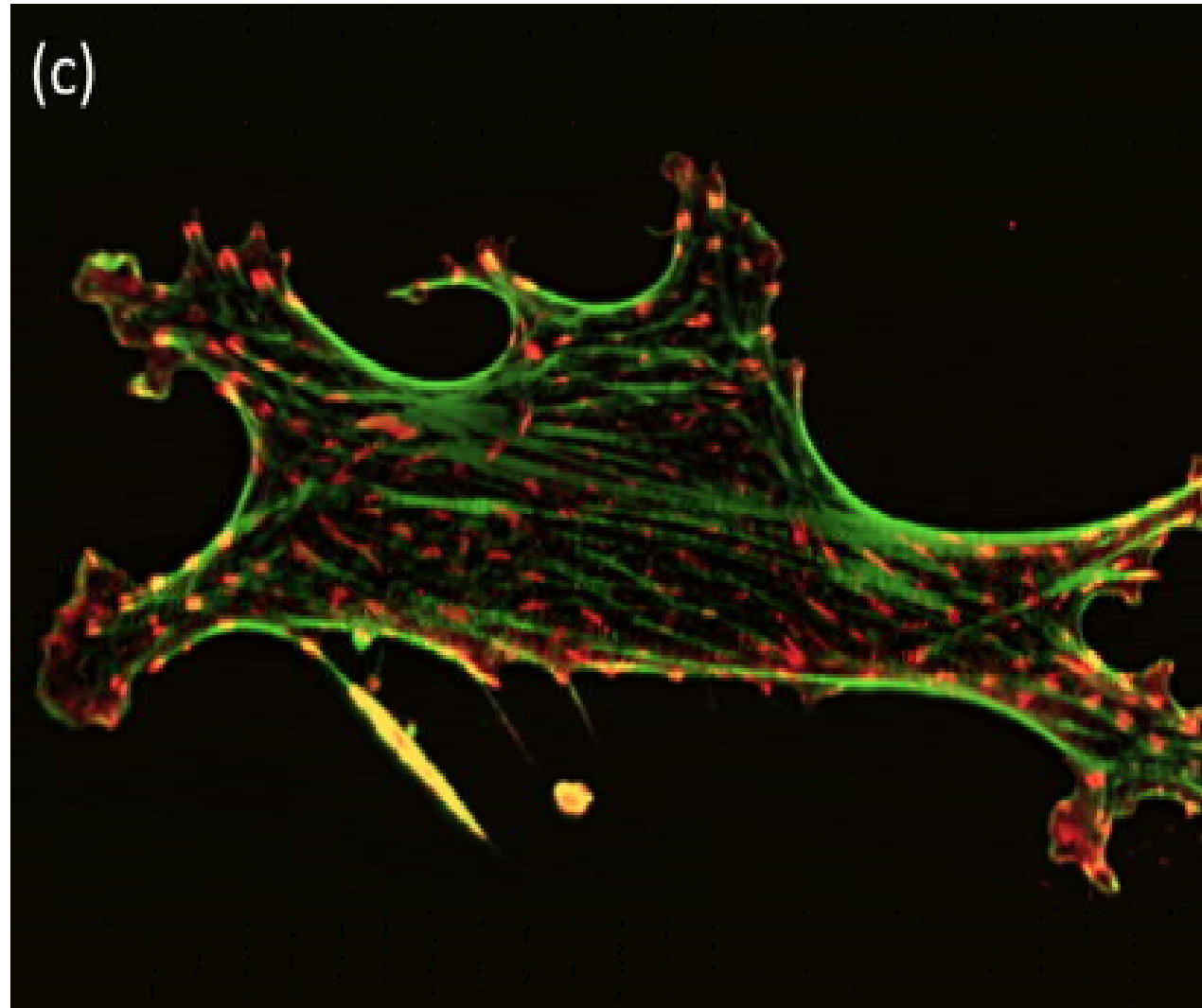
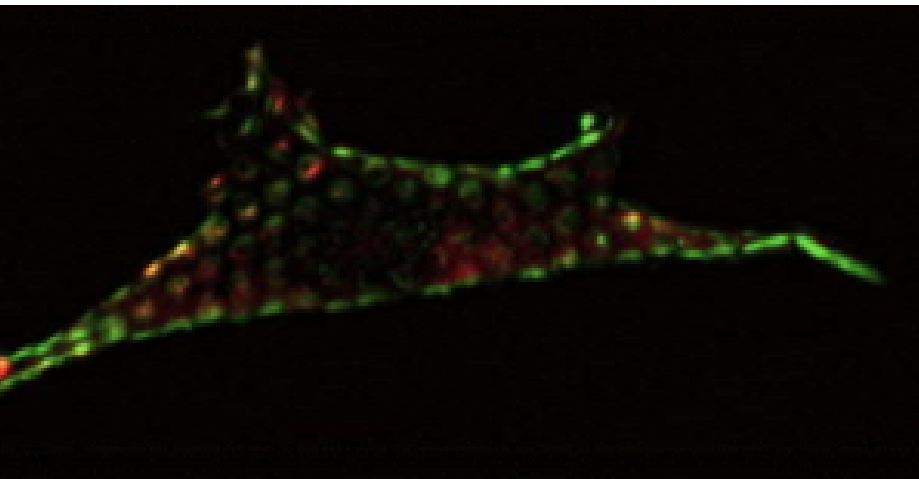


DMS posts of identical composition ($>100 \text{ kPa}$) and diameter ($0.8 \mu\text{m}$), but different length.



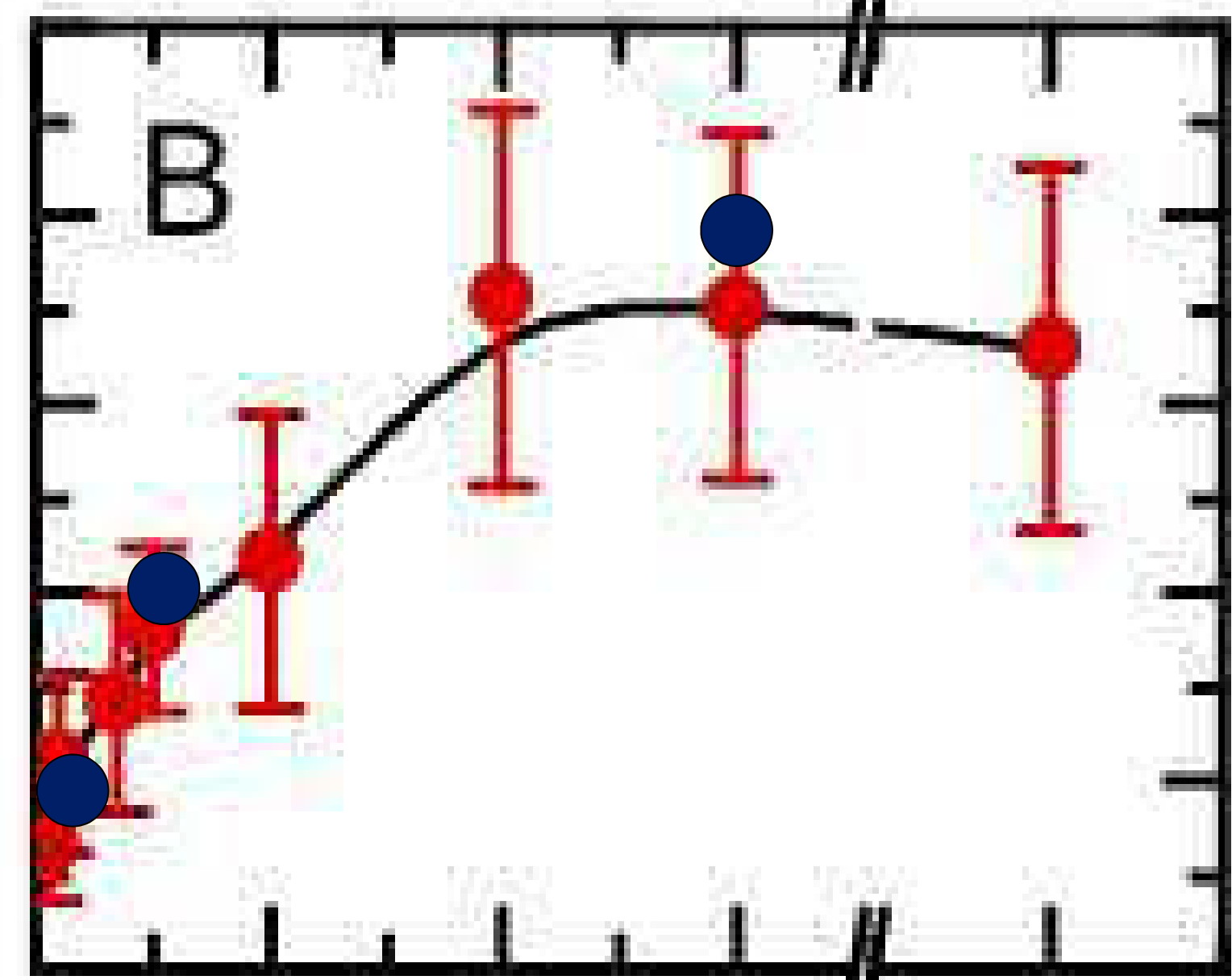
hMSC
on Fn

paxillin
F-actin

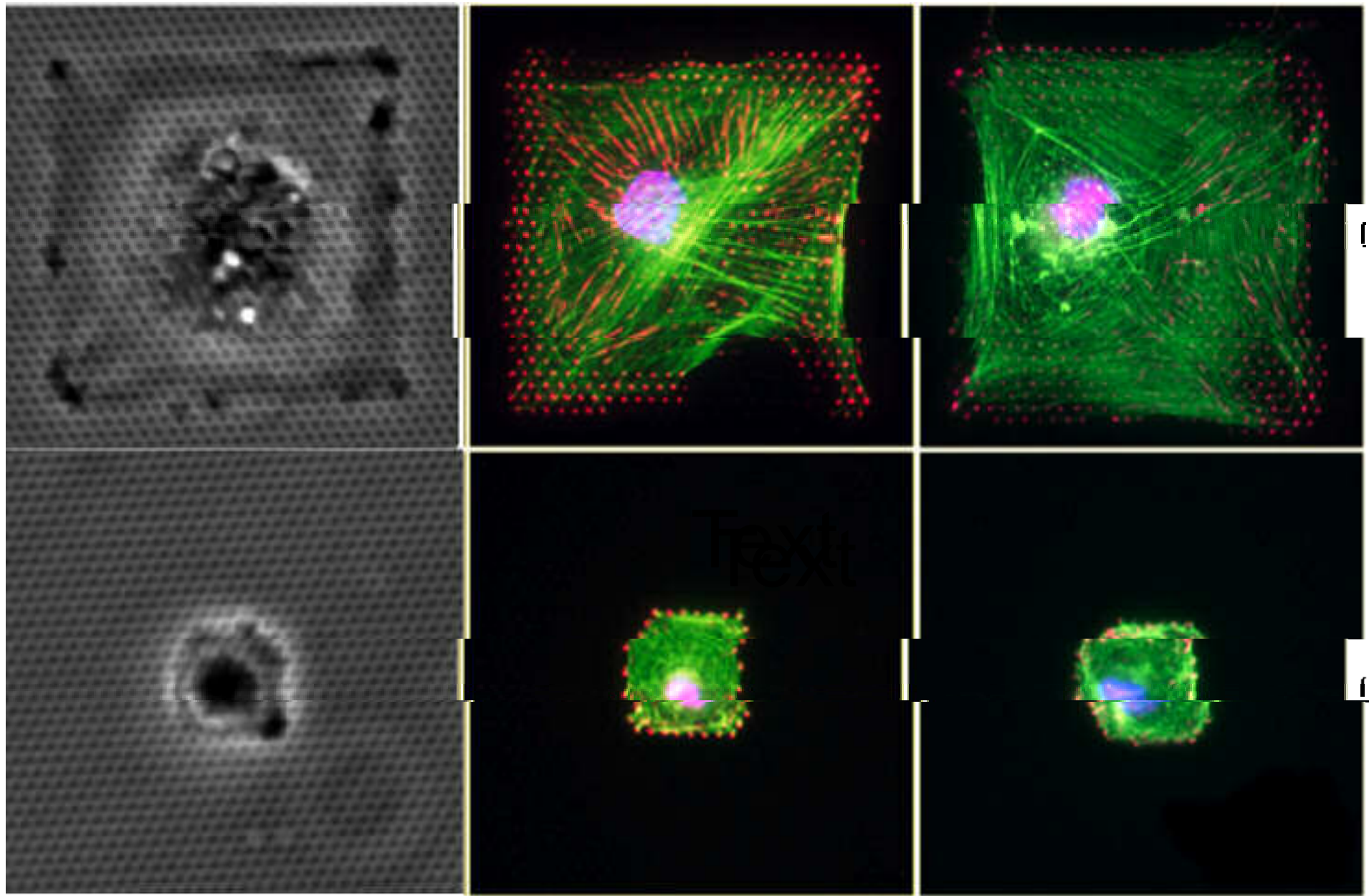


$6\ \mu\text{m}$ PDMS posts ($>100\ \text{kPa}$) of different length spaced $6\ \mu\text{m}$ apart
long posts look soft, short posts look stiff

Cell Stiffness (Pa)



0 10k 20k 30k 70G



Phase Contrast

Stiff Posts

Soft Posts

0.500x100

F-actin

vinculin

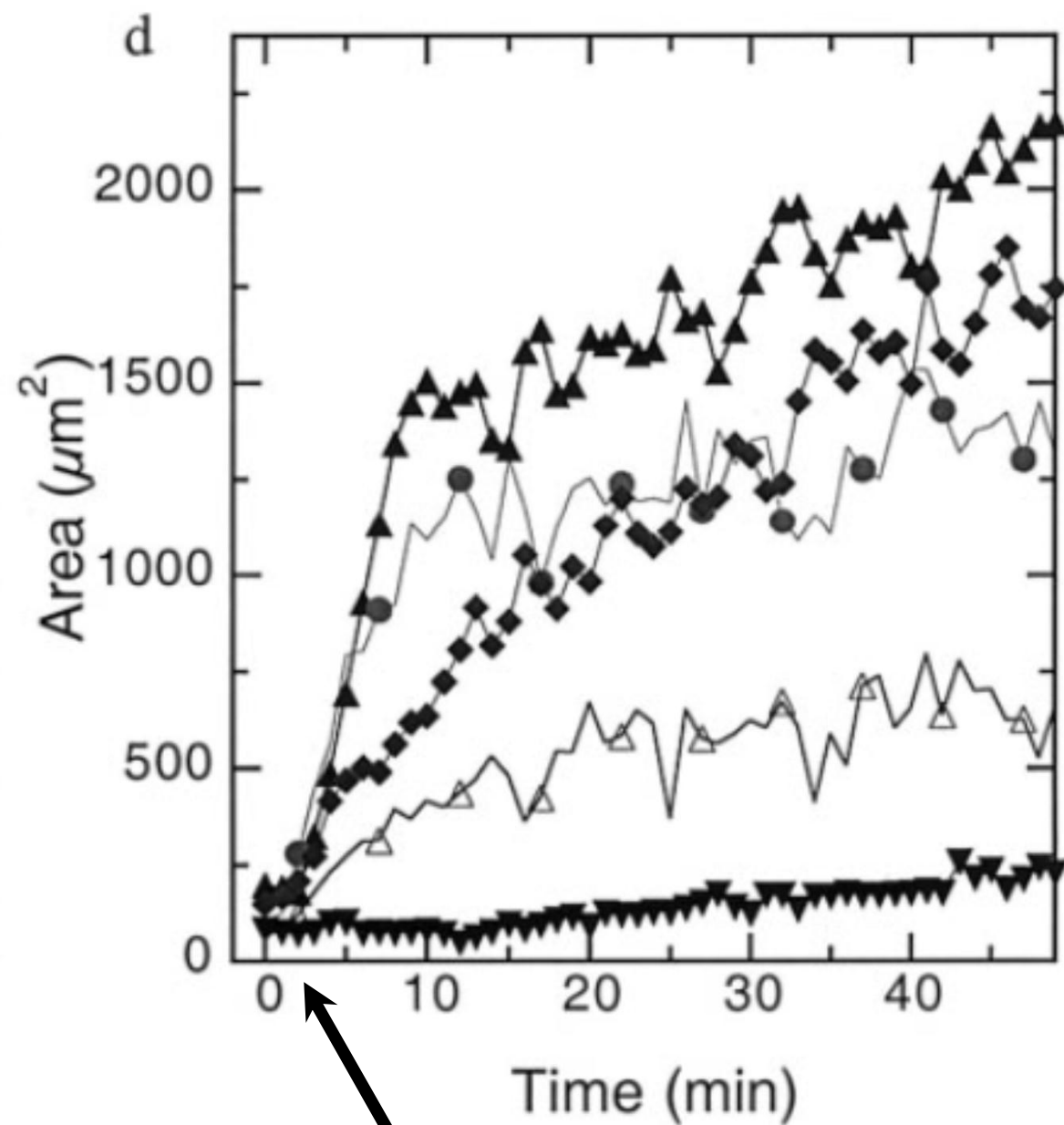
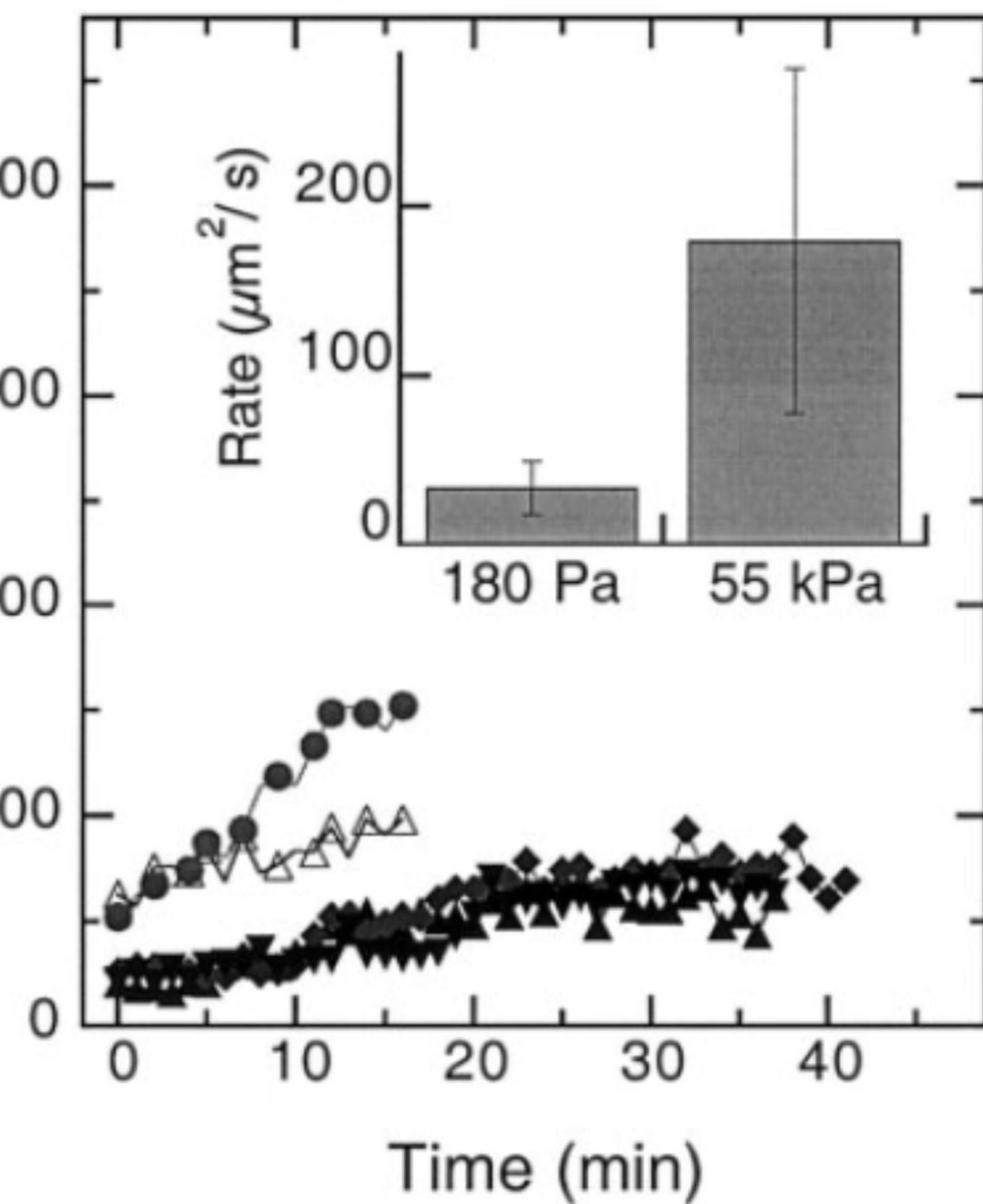
0.500x100

Human bone marrow stem cells (hMSC) constrained on square shapes on PMDS microposts.

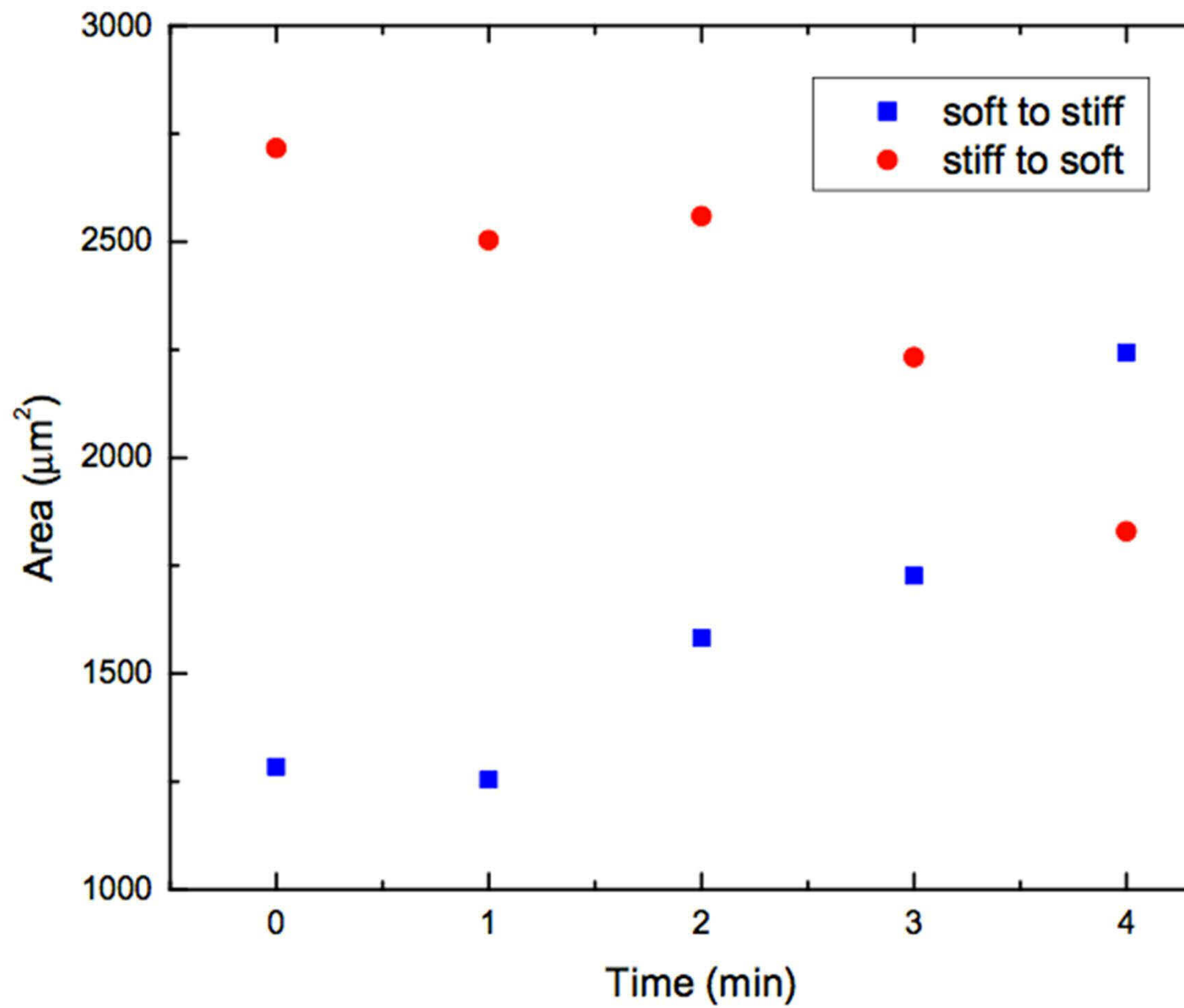
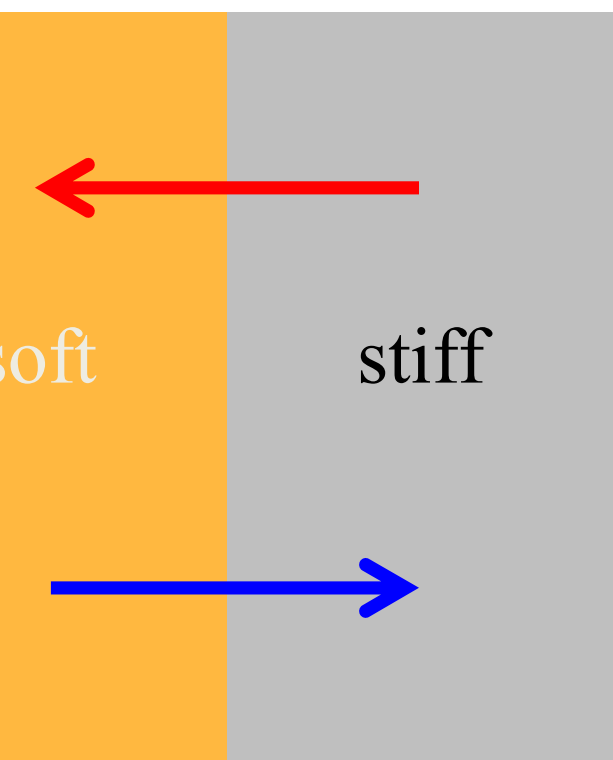
What is the time needed for mechanosensing?

Experimentally what is measured is a cell's response, which is an upper limit

the adhesion ligand density but different stiffness



Two minutes is enough to



Most tissues have well-defined and controlled elastic moduli

Cells in vitro do not: their stiffness depends on environment

The strain-stiffening properties of biopolymer gels contribute to tissue stiffness and provides effective means to reversibly stiffen a cell or tissue.

Substrate stiffness affects each cell type differently, and manipulating matrix stiffness can influence cell fate.

Stiffness sensing appears to operate on a length scale $>1 \mu\text{m}$ and a time $>1 \text{ s}$.