

Abstract:

Let k be any field.

In this talk we shall consider rings of the form $A = k[X, Y, Z, T]/(X^m Y - F(X, Z, T))$, $m > 1$, and present several equivalent criteria for such a ring A to satisfy:

(i) $A[W] \cong k[X_1, X_2, X_3, X_4]$.

(ii) $A \cong k[X_1, X_2, X_3]$.

For instance, a necessary and sufficient condition for the above ring A to be a polynomial ring is that $F(0, Z, T)$ is a variable in $k[Z, T]$. Another equivalent condition is that A is a UFD, $K_1(A) = k^*$ and a certain invariant called 'Derksen invariant' is trivial.

It follows from these criteria that when $\text{char } k > 0$, there exists an infinite family of non-isomorphic rings which satisfy (i) but violates (ii); in particular, $\text{char } k = 3$ is not cancellative when $\text{char } k > 0$.

Note that the rings of the above type A include Asanuma's candidates for a counter-example to the Linearisation/Cancellation Conjecture in positive characteristic as well as the Russell-Koras' threefold.