

# CT 5: Car Parrinello Molecular Dynamics

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## Motivation

- Propagation of wavefunction without minimizing at each step
- Long time step set by nuclear motion (not electronic)

## Basic Idea

- Classical–mechanical energy–scale separation: time separation between fast electrons & slow nuclei
- Two component quantum/classical system  $\rightarrow$  two purely classical problem
- Classical evolution of  $\Psi$  destroys their true time dependence

# Equations of Motion

## Lagrangian

$$\begin{aligned}\mathcal{L}_{\text{CP}} = & \sum_I \frac{1}{2} M_I \dot{\mathbf{R}}_I^2 + \sum_i \frac{1}{2} \mu_i \langle \dot{\psi}_i | \dot{\psi}_i \rangle \\ & - \langle \Psi_0 | \hat{H}_e | \Psi_0 \rangle \\ & + \sum_i \sum_j \Lambda_{ij} (\langle \psi_i | \psi_j \rangle - \delta_{ij})\end{aligned}$$

## Euler Lagrange Equations

$$\begin{aligned}\frac{d}{dt} \frac{\partial \mathcal{L}}{\partial \dot{\mathbf{R}}_I} &= \frac{\partial \mathcal{L}}{\partial \mathbf{R}_I} \\ \frac{d}{dt} \frac{\partial \mathcal{L}}{\partial \dot{\psi}_i^*} &= \frac{\partial \mathcal{L}}{\partial \psi_i^*}, \quad \dot{\psi}_i^* = \langle \dot{\psi}_i | \end{aligned}$$

# Equations of Motion (· · · cont)

$$\begin{aligned} M_I \ddot{\mathbf{R}}_I(t) &= -\nabla_I \langle \Psi_0 | \hat{H}_e | \Psi_0 \rangle + \nabla_I \left[ \sum_i \sum_j \Lambda_{ij} (\langle \psi_i | \psi_j \rangle - \delta_{ij}) \right] \\ \mu_i \ddot{\psi}_i(t) &= -\frac{\partial}{\partial \psi_i^*} \langle \Psi_0 | \hat{H}_e | \Psi_0 \rangle + \frac{\delta}{\delta \psi_i^*} \left[ \sum_i \sum_j \Lambda_{ij} (\langle \psi_i | \psi_j \rangle - \delta_{ij}) \right] \end{aligned}$$

- Starting from B.O. surface
- Cold wavefunction (thermostats)
- $\mu_i$  and  $\Delta t$  has to be appropriately

- Degenerate electronic states
- Zero band-gap
- Orthogonalization needed