



TATA INSTITUTE OF FUNDAMENTAL RESEARCH

Living matter April 16 to April 26

Chance and determinism in cell differentiation. Random walk across the epigenetic landscape

András Páldi

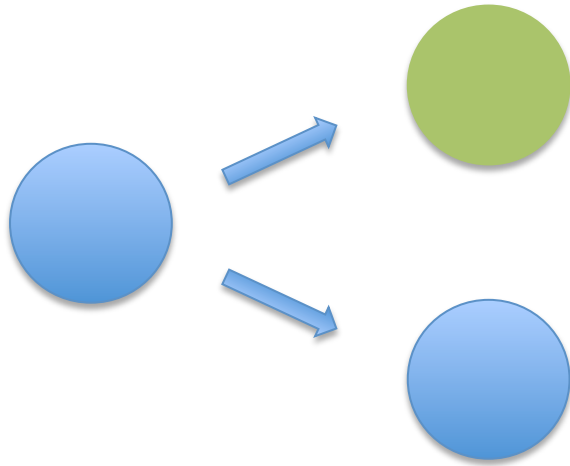
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École Pratique
des Hautes Études

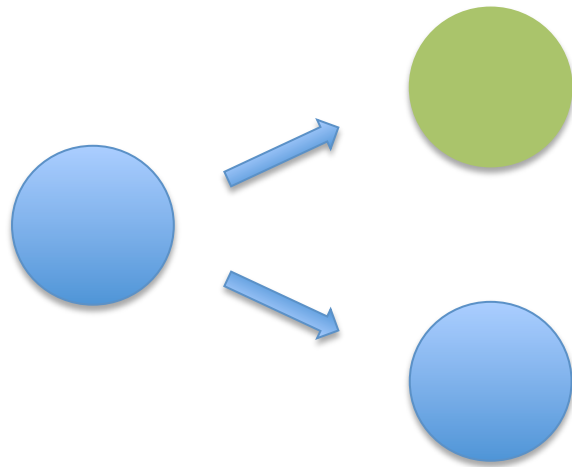


Cell differentiation



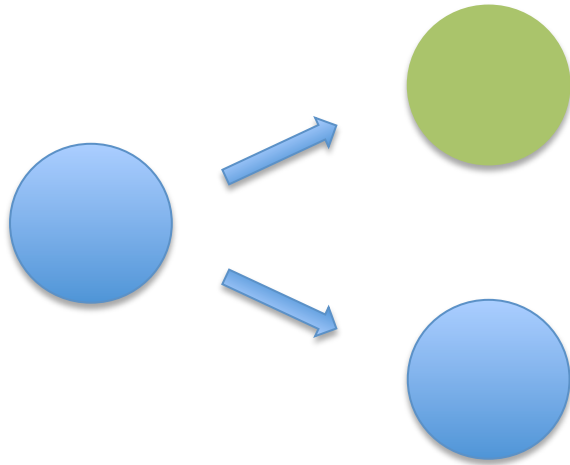
Occurs in multicellular, but also in unicellular and ambiguous organisms.

Cell differentiation



Implicitly: change in
morphology and in gene
expression pattern

Cell differentiation



Implicitly: change in the gene expression pattern

But: how many genes?

Cell differentiation

Stability/change

Ordered, deterministic/disordered (random, stochastic ...)

Inherited/acquired

Genotype/phenotype

1 Order and stability in living systems: a short (and superficial) historical background.

2 Disorder and stochasticity in living cells: noise or variation?

3 How cells function reliably with such an inherent variability in gene expression?

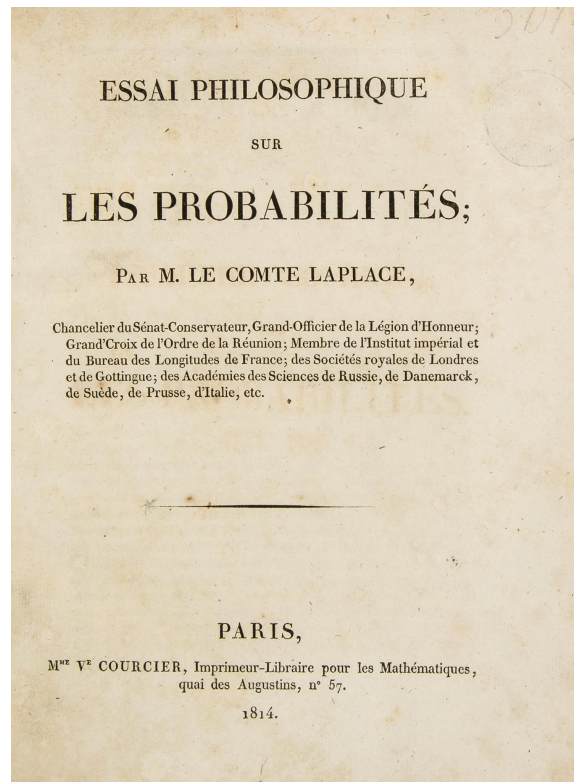
1 Order in living systems: a short (and superficial) historical background.

2 Stochasticity in living cells: noise or variation?

3 How cells function reliably with such an inherent variability in gene expression?



Pierre-Simon de Laplace
1749-1827



We may regard the present state of the universe as the effect of its past and the cause of its future. An intellect which at a certain moment would know all forces that set nature in motion, and all positions of all items of which nature is composed, if this intellect were also vast enough to submit these data to analysis, it would embrace in a single formula the movements of the greatest bodies of the universe and those of the tiniest atom; for such an intellect nothing would be uncertain and the future just like the past would be present before its eyes.

— Pierre Simon Laplace, *A Philosophical Essay on Probabilities*



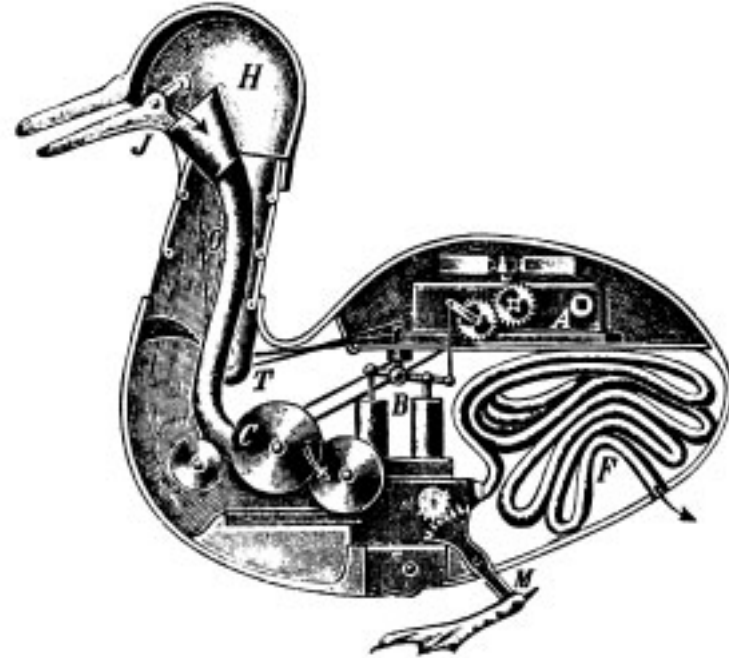
Now, a living organism is nothing but a wonderful machine endowed with the most marvellous properties and set going by means of the most complex and delicate mechanism.

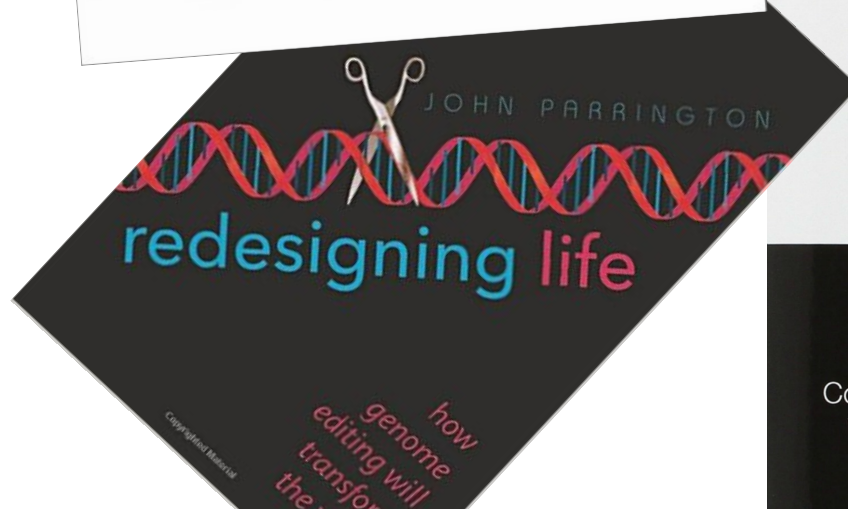
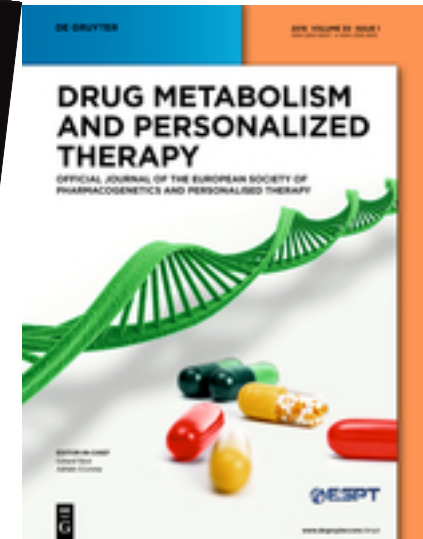
Claude Bernard

1813-1878



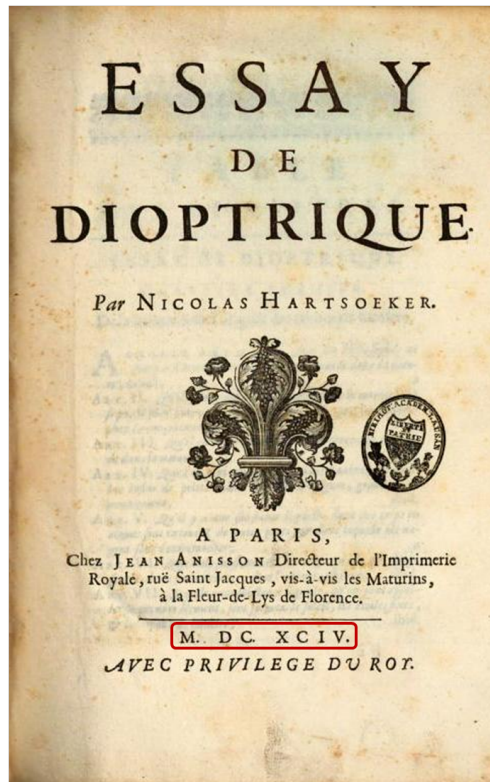
Jacques Vaucanson
1709-1782



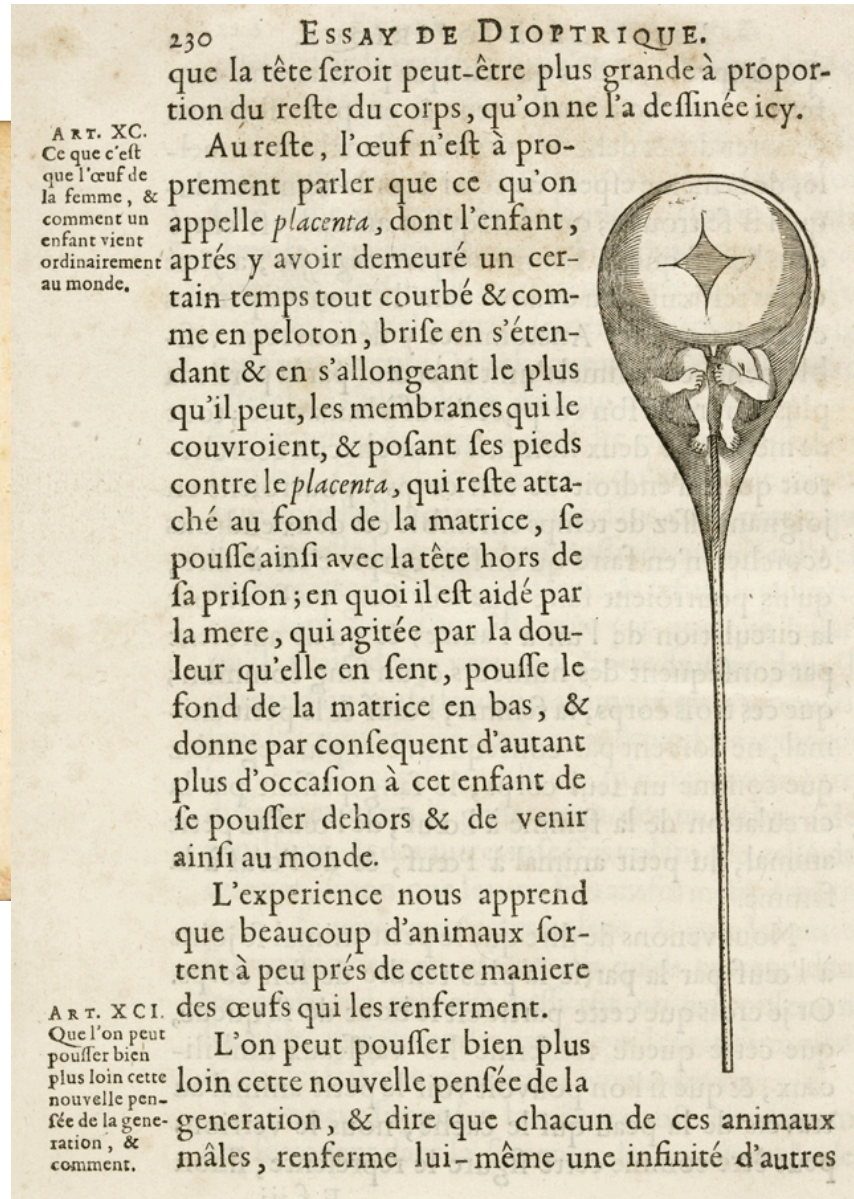


Heredity is one of the clearest manifestations of the order in nature

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Hartsoeker, N.
(1694).





Epigénèse



from Jacob Rueff, *De conceptu et generatione hominis ...*
1554

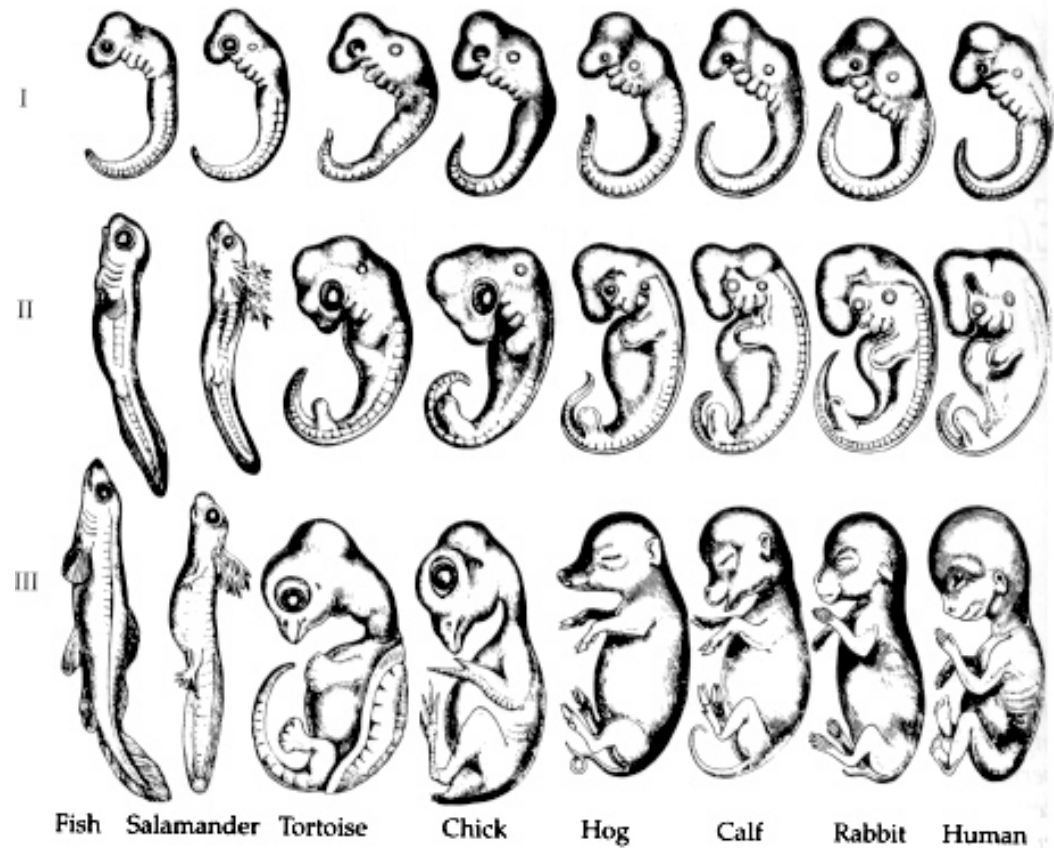
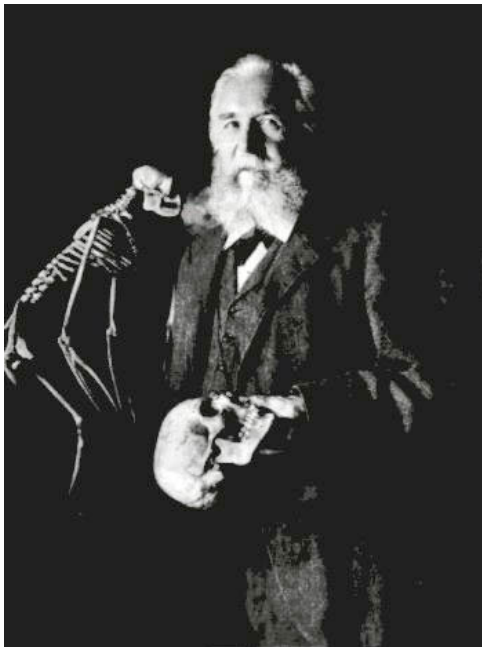


Caspar Friedrich Wolff
1734-94

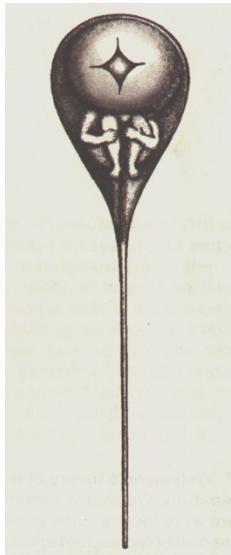


William Harvey
1578-1657

Ernest Haeckel,
1834-1919



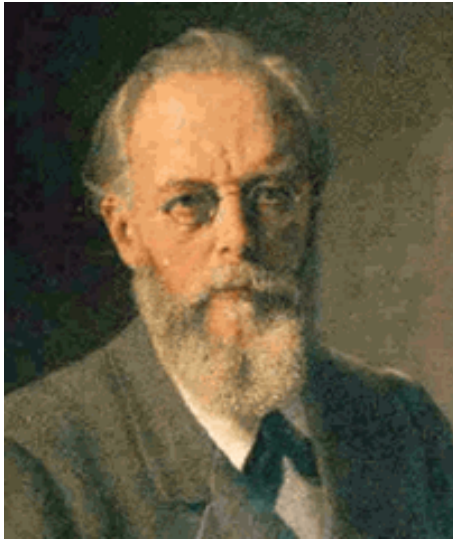
Modern genetics: dissociation of the two concepts



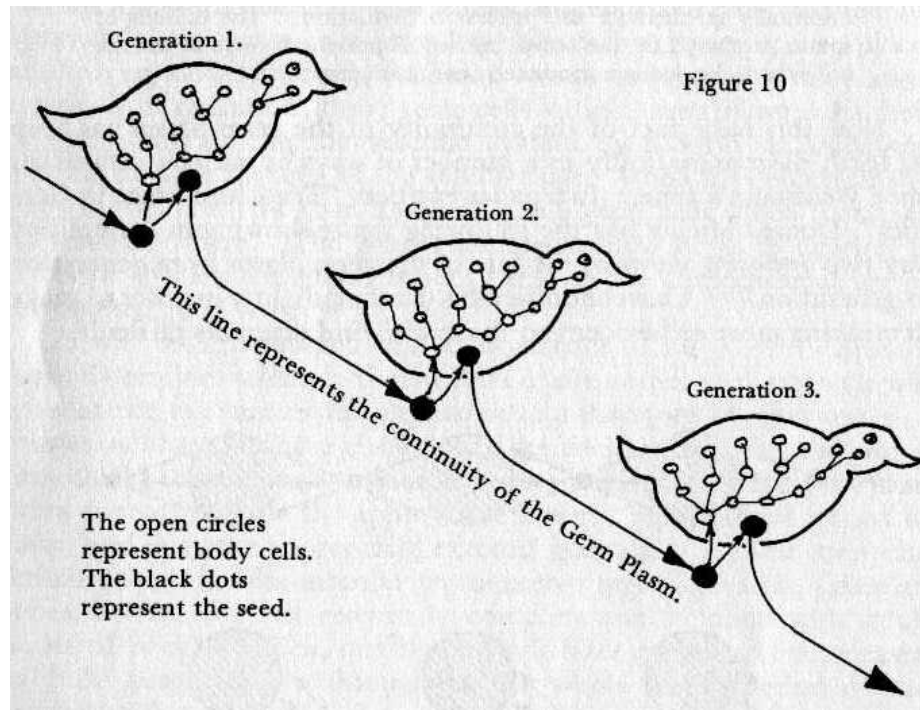
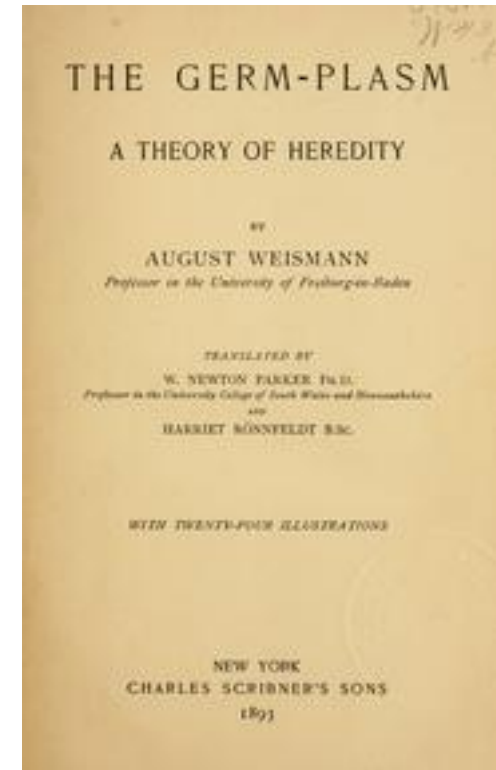
Genotype: stable over generations



Phenotype: variable

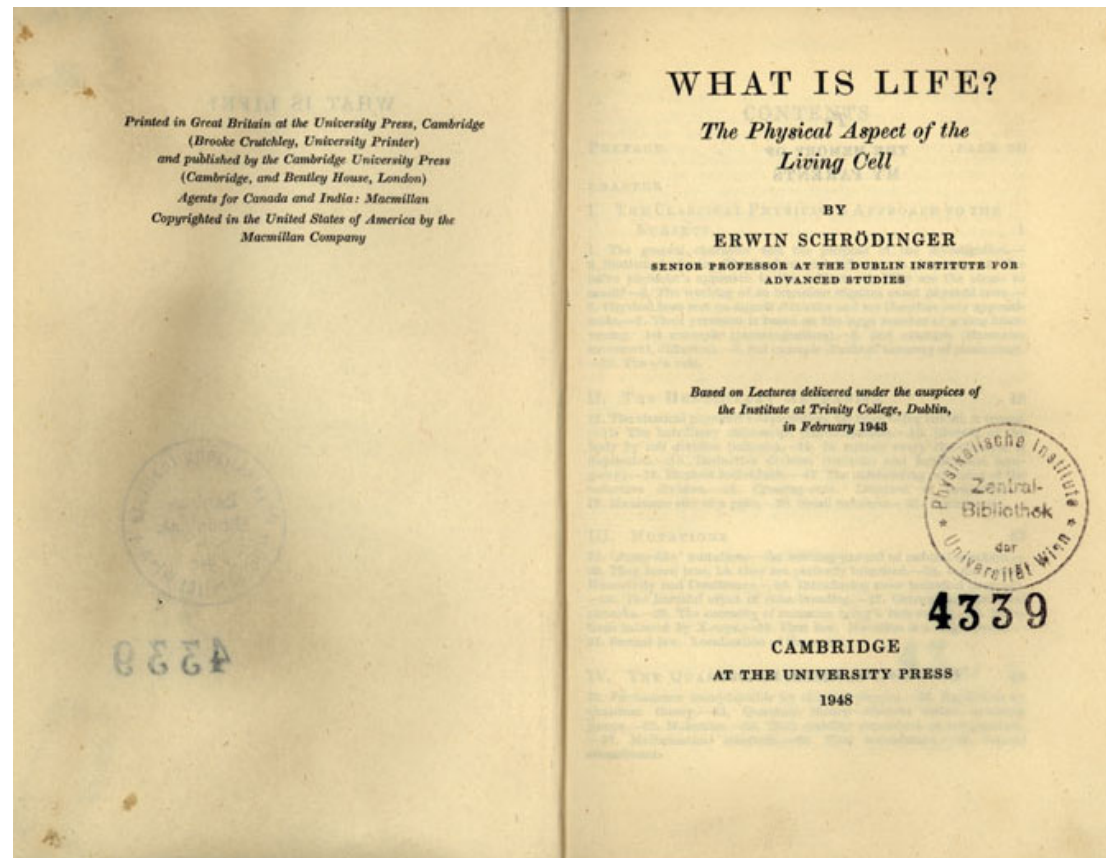


August Weismann
1834-1914



Hardy, Sir Alister, *This Living Stream*, London, Collins, 1965, p.76.

Order from disorder  Order from order



Erwin Schrödinger 1944

Order from disorder Order from order

“It appears that there are two different ‘mechanisms’ by which orderly events can be produced: the ‘statistical mechanism’ which produces ‘order from disorder’ and the new one, producing ‘order from order’.”

“From all we have learnt about the structure of living matter, we must be prepared to find it working in a manner that cannot be reduced to the ordinary laws of physics. And that not on the ground that there is any “new force” or what not, directing the behavior of the single atoms within a living organism, but because the construction is different from anything we have yet tested in the physical laboratory. ”

“...living matter, while not eluding the "laws of physics" as established up to date, is likely to involve "other laws of physics" hitherto unknown, which however, once they have been revealed, will form just as integral a part of science as the former. ”

“We must also be prepared to find a new type of physical law prevailing in it. Or are we to term it a non-physical, not to say a super-physical, law? ”

“It is these chromosomes ... that contain in some kind of code-script the entire pattern of the individual's future development and of its functioning in the mature state. Every complete set of chromosomes contains the full code...”

« Chaque œuf contient donc, dans les chromosomes reçus de ses parents, tout son propre avenir, les étapes de son développement, la forme et les propriétés de l'être qui en émergera. L'organisme devient ainsi la réalisation d'un programme prescrit par l'hérédité. »

François Jacob 1970

"Life, we now know, is nothing but a vast array of coordinated chemical reactions. The 'secret' to that coordination is the breathtakingly complex set of instructions inscribed, again chemically, in our DNA. »

James Watson

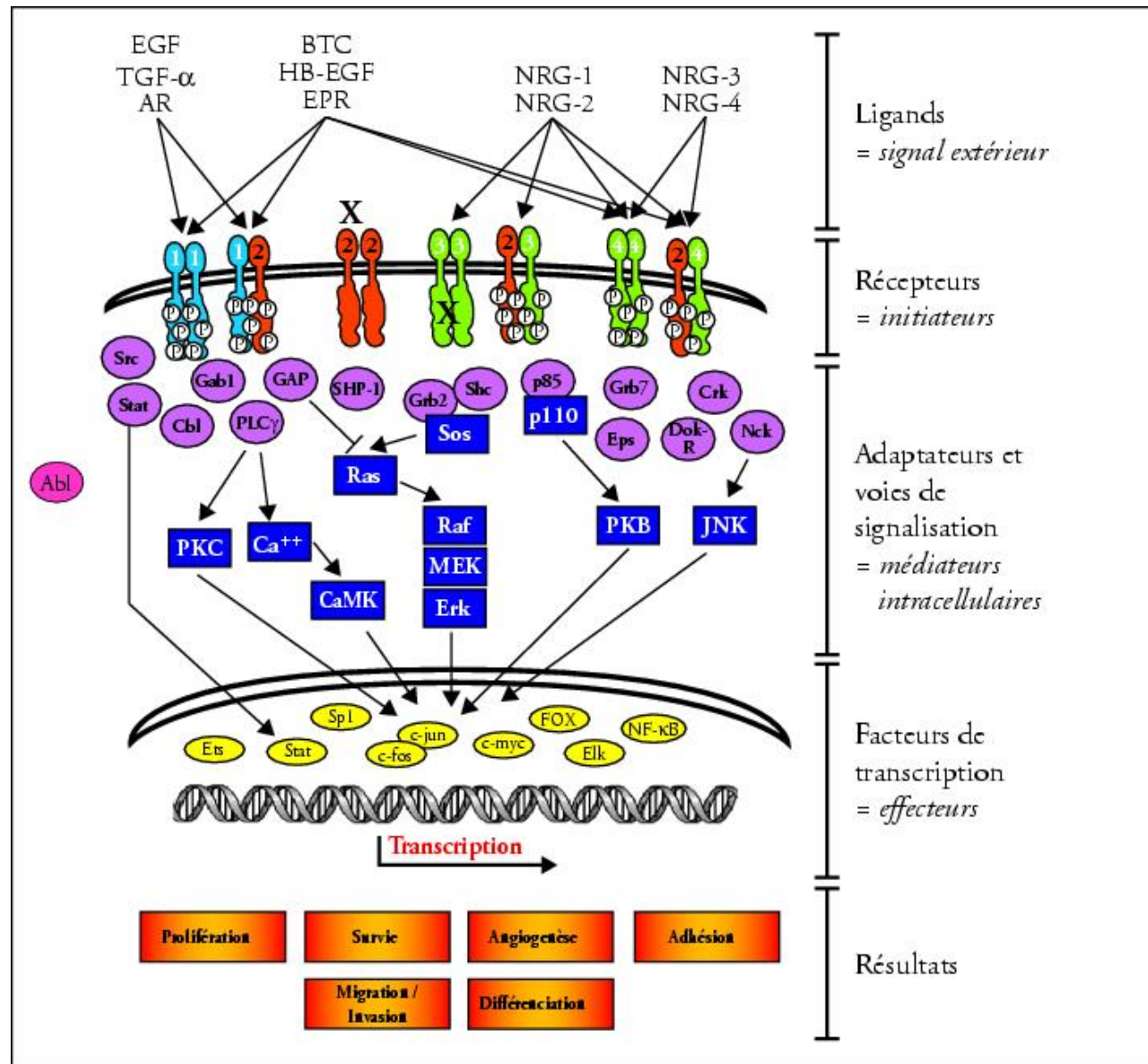
Order from order

Phenotype from genotype

Genotype  phenotype



René Magritte 1898-1968

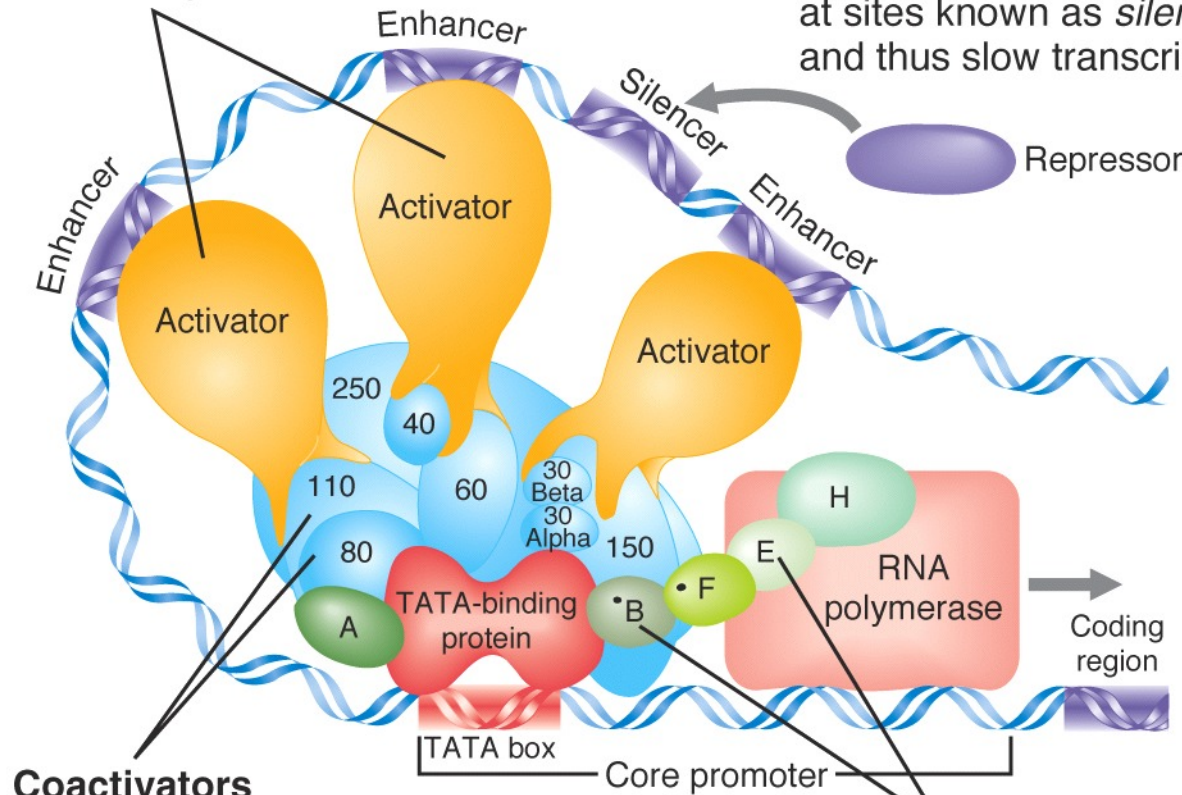


Activators

These proteins bind to genes at sites known as *enhancers* and speed the rate of transcription.

Repressors

These proteins bind to selected sets of genes at sites known as *silencers* and thus slow transcription.



Coactivators

These “adapter” molecules integrate signals from activators and perhaps repressors.

Basal transcription factors

In response to injunctions from activators, these factors position RNA polymerase at the start of

Stability  Change

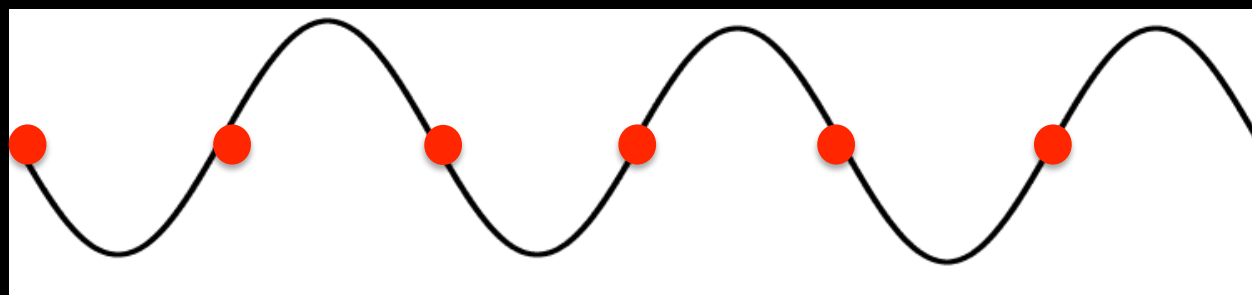
But how to detect change?

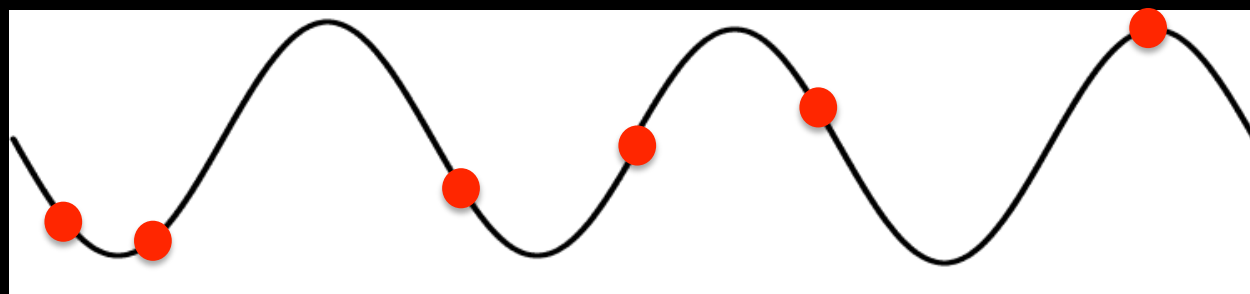
Stability  Change

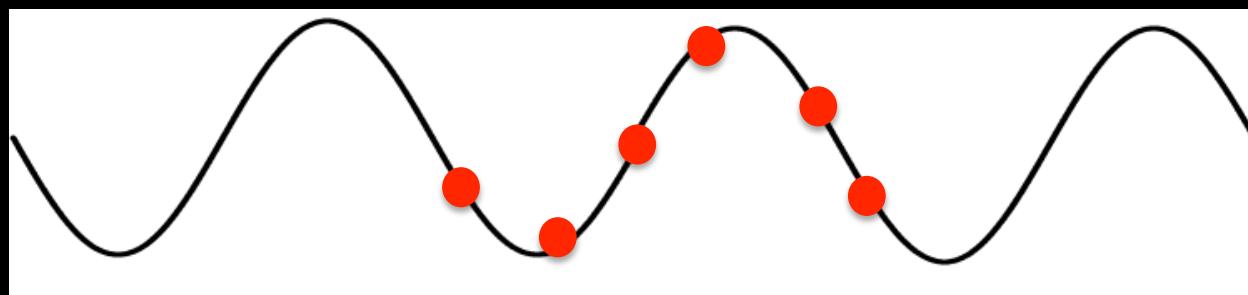
But how to detect change?

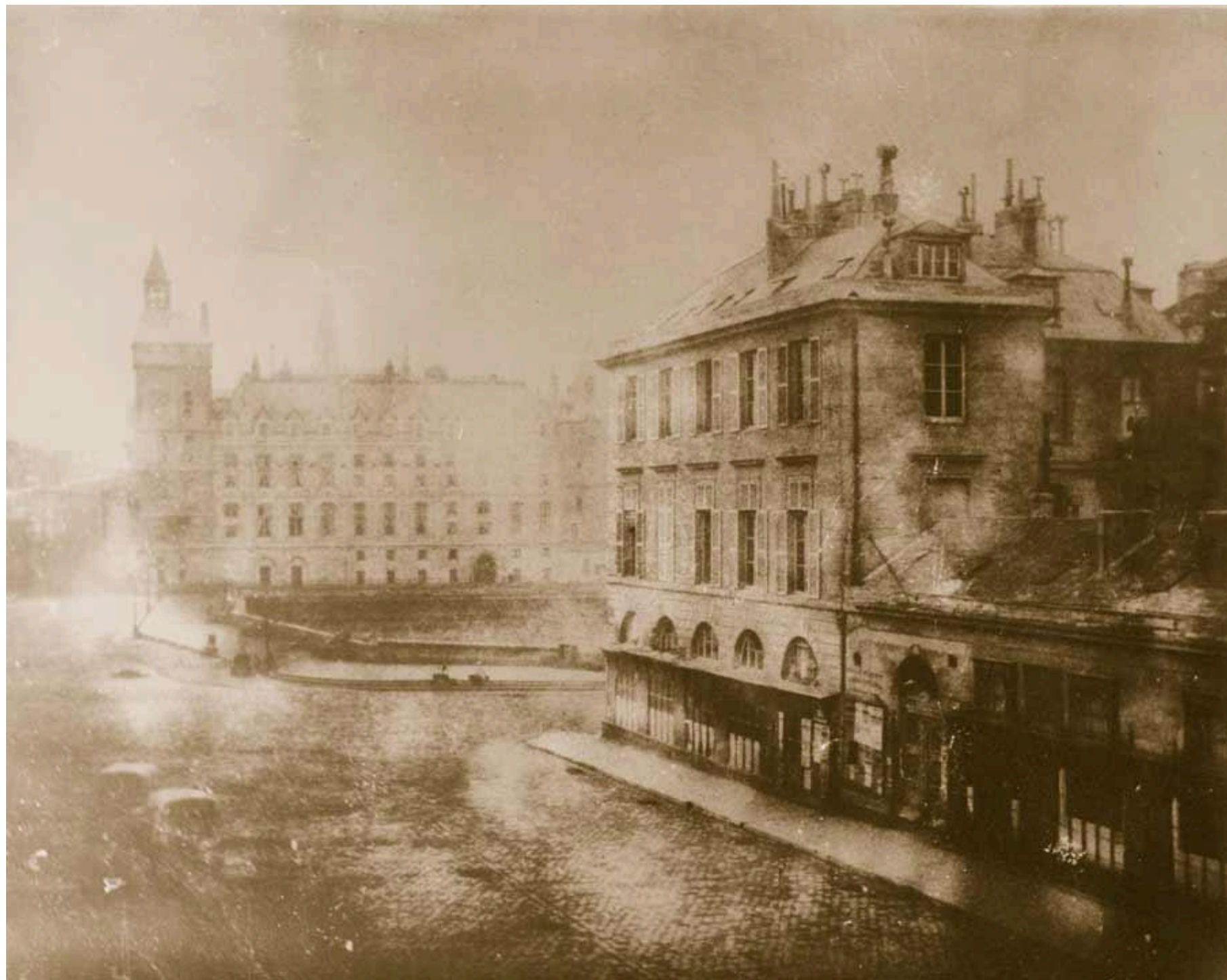
Complementary question: How create
change with stable elements?











Stability  Change

But how to detect change?

Relativity of scales

1 Order and stability in living systems: a short (and superficial) historical background.

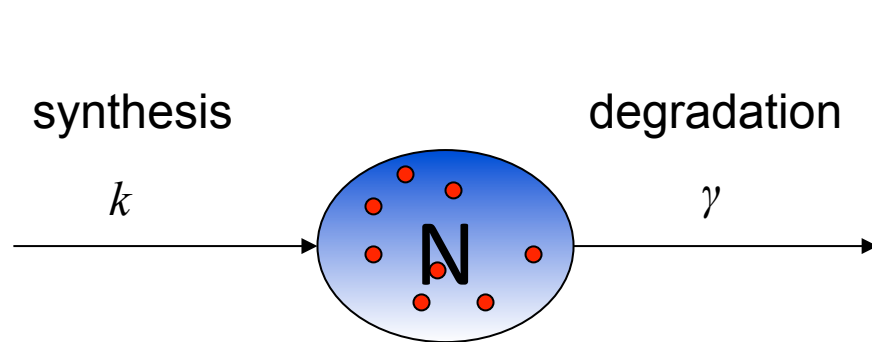
2 Stochasticity in living cells: noise or variation?

3 How cells function reliably with such an inherent variability in gene expression?

“And why could all this not be fulfilled in the case of an organism composed of a moderate number of atoms only and sensitive already to the impact of one or a few atoms only? Because we know all atoms to perform all the time a completely disorderly heat motion, which, so to speak, opposes itself to their orderly behaviour and does not allow the events that happen between a small number of atoms to enrol themselves according to any recognizable laws.”

Erwin Schrödinger, What is life?

Birth-death process: Protein synthesis and degradation



Deterministic solution:

$$\frac{dN}{dt} = k - \gamma N \Rightarrow N(t) = \frac{k}{\gamma} (1 - e^{-\gamma t})$$

Stochastic solution:

$$\frac{dP_N}{dt} = kP_{N-1} + \gamma(N+1)P_{N+1} - (k + \gamma N)P_N; \quad N \neq 0, P_{-1} = 0$$

Master equation

$$\frac{d\langle N \rangle}{dt} = k - \gamma \langle N \rangle \Rightarrow \mu(t) = \frac{k}{\gamma} (1 - e^{-\gamma t})$$

Solution: **mean**

$$\frac{d\langle N^2 \rangle}{dt} = -2\gamma \langle N^2 \rangle + (\gamma + 2k) \langle N \rangle + k \Rightarrow \sigma^2(t) = \frac{k}{\gamma} (1 - e^{-\gamma t})$$

Solution: **variance**

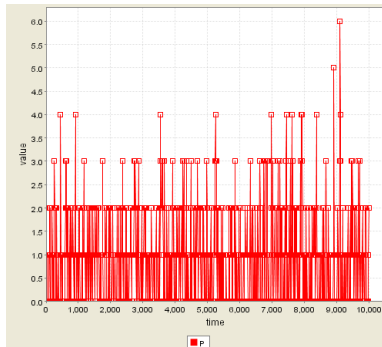
$$CV = \frac{\sigma(t)}{\mu(t)} = \sqrt{\frac{\gamma}{k(1 - e^{-\gamma t})}} = \frac{1}{\sqrt{\mu(t)}} \quad CV = \text{Coefficient of Variation}$$

Solution: **noise**

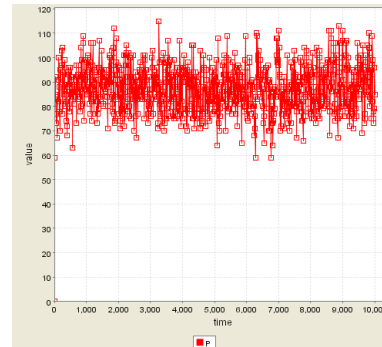
Stochastic simulation: Protein synthesis and degradation

synthesis

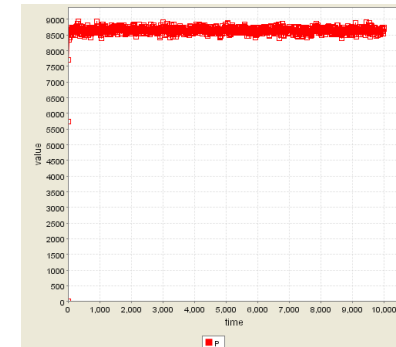
$k=0.1$



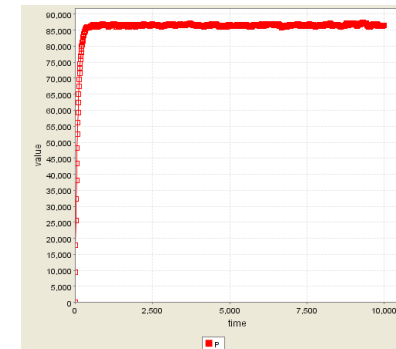
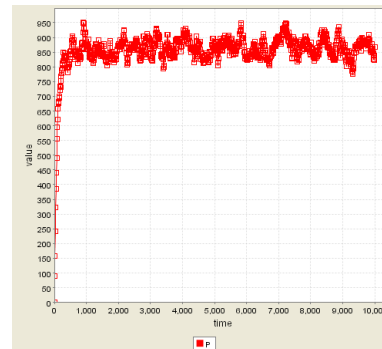
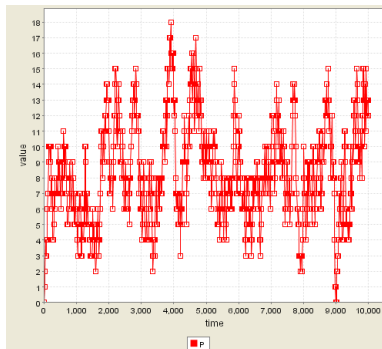
$k=10$



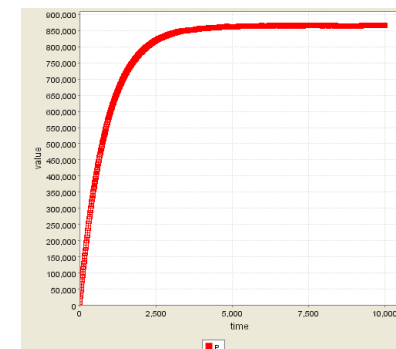
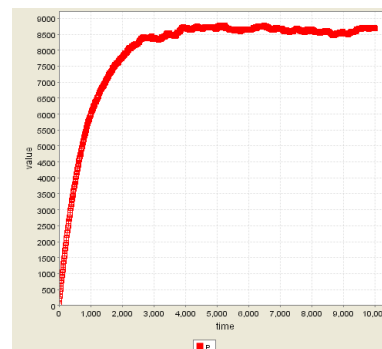
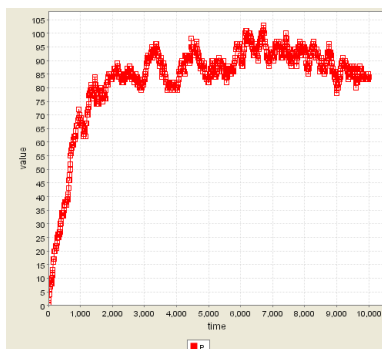
$k=1000$



$\gamma=\ln(2)/6$



$\gamma=\ln(2)/60$



$\gamma=\ln(2)/600$

degradation

SnapShot: Key Numbers in Biology

Cell

Uri Moran,¹ Rob Phillips,² and Ron Milo¹

¹Weizmann Institute of Science, Rehovot, Israel; ²California Institute of Technology, Pasadena, CA, USA

Cell size	Concentration	Diffusion and catalysis rate
<p>Bacteria (<i>E. coli</i>): $\approx 0.7\text{--}1.4\ \mu\text{m}$ diameter, $\approx 2\text{--}4\ \mu\text{m}$ length, $\approx 0.5\text{--}5\ \mu\text{m}^3$ in volume; $10^8\text{--}10^9$ cell/ml for culture with $\text{OD}_{600} \approx 1$</p> <p>Yeast (<i>S. cerevisiae</i>): $\approx 3\text{--}6\ \mu\text{m}$ diameter $\approx 20\text{--}160\ \mu\text{m}^3$ in volume</p> <p>Mammalian cell volume: $100\text{--}10,000\ \mu\text{m}^3$; HeLa cell: $500\text{--}5000\ \mu\text{m}^3$ (adhering to slide $\approx 15\text{--}30\ \mu\text{m}$ diameter)</p>	<p>Concentration of 1 nM: in <i>E. coli</i> ≈ 1 molecule/cell; in HeLa cells ≈ 1000 molecules/cell</p> <p>Characteristic concentration for a signaling protein: $\approx 10\ \text{nM}\text{--}1\ \mu\text{M}$</p> <p>Water content: $\approx 70\%$ by mass; general elemental composition (dry weight) of <i>E. coli</i>: $\approx \text{C}_4\text{H}_7\text{O}_2\text{N}_1$; Yeast: $\approx \text{C}_6\text{H}_{10}\text{O}_3\text{N}_1$</p> <p>Composition of <i>E. coli</i> (dry weight): $\approx 55\%$ protein, 20% RNA, 10% lipids, 15% others</p> <p>Protein concentration: $\approx 100\ \text{mg/ml} = 3\ \text{mM}$. $10^6\text{--}10^7$ per <i>E. coli</i> (depending on growth rate); Total metabolites (MW < 1 kDa) $\approx 300\ \text{mM}$</p>	<p>Diffusion coefficient for an “average” protein: in cytoplasm $D \approx 5\text{--}15\ \mu\text{m}^2/\text{s} \rightarrow \approx 10\ \text{ms}$ to traverse an <i>E. coli</i> $\rightarrow \approx 10\ \text{s}$ to traverse a mammalian HeLa cell; small metabolite in water $D \approx 500\ \mu\text{m}^2/\text{s}$</p> <p>Diffusion-limited on-rate for a protein: $\approx 10^8\text{--}10^9\ \text{s}^{-1}\text{M}^{-1} \rightarrow$ for a protein substrate of concentration $\approx 1\ \mu\text{M}$ the diffusion-limited on-rate is $\approx 100\text{--}1000\ \text{s}^{-1}$ thus limiting the catalytic rate k_{cat}</p>
Length scales inside cells	Division, replication, transcription, translation, and degradation rates	Genome sizes and error rates
<p>Nucleus volume: $\approx 10\%$ of cell volume</p> <p>Cell membrane thickness: $\approx 4\text{--}10\ \text{nm}$</p> <p>“Average” protein diameter: $\approx 3\text{--}6\ \text{nm}$</p> <p>Base pair: $2\ \text{nm}$ (D) $\times 0.34\ \text{nm}$ (H)</p> <p>Water molecule diameter: $\approx 0.3\ \text{nm}$</p>	<p>Cell cycle time (exponential growth in rich media): <i>E. coli</i> $\approx 20\text{--}40\ \text{min}$; budding yeast $70\text{--}140\ \text{min}$; HeLa human cell line: $15\text{--}30\ \text{hr}$</p> <p>Rate of replication by DNA polymerase: <i>E. coli</i> $\approx 200\text{--}1000$ bases/s; human ≈ 40 bases/s. Transcription by RNA polymerase $10\text{--}100$ bases/s</p> <p>Translation rate by ribosome: $10\text{--}20\ \text{aa/s}$</p> <p>Degradation rates (proliferating cells): mRNA half life < cell cycle time; protein half life \approx cell cycle time</p>	<p>Genome size: <i>E. coli</i> $\approx 5\ \text{Mbp}$ <i>S. cerevisiae</i> (yeast) $\approx 12\ \text{Mbp}$ <i>C. elegans</i> (nematode) $\approx 100\ \text{Mbp}$ <i>D. melanogaster</i> (fruit fly) $\approx 120\ \text{Mbp}$ <i>A. thaliana</i> (plant) $\approx 120\ \text{Mbp}$ <i>M. musculus</i> (mouse) $\approx 2.6\ \text{Gbp}$ <i>H. sapiens</i> (human) $\approx 3.2\ \text{Gbp}$ <i>T. aestivum</i> (wheat) $\approx 16\ \text{Gbp}$</p> <p>Number of protein-coding genes: <i>E. coli</i> = 4000; <i>S. cerevisiae</i> = 6000; <i>C. elegans</i>, <i>A. thaliana</i>, <i>M. musculus</i>, <i>H. sapiens</i> = 20,000</p> <p>Mutation rate in DNA replication: $\approx 10^{-8}\text{--}10^{-10}$ per bp</p> <p>Misincorporation rate: transcription $\approx 10^{-4}\text{--}10^{-5}$ per nucleotide translation $\approx 10^{-3}\text{--}10^{-4}$ per amino acid</p>
Energetics		
<p>Membrane potential $\approx 70\text{--}200\ \text{mV} \rightarrow 2\text{--}6\ k_{\text{B}}T$ per electron ($k_{\text{B}}T \equiv$ thermal energy)</p> <p>Free energy (ΔG) of ATP hydrolysis under physiological conditions $\approx 40\text{--}60\ \text{kJ/mol} \rightarrow \approx 20\ k_{\text{B}}T$/molecule ATP; ATP molecules required during an <i>E. coli</i> cell cycle $\approx 10\text{--}50 \times 10^9$</p> <p>$\Delta G^\circ$ resulting in order of magnitude ratio between product and reactant concentrations: $\approx 6\ \text{kJ/mol} \approx 60\ \text{meV} \approx 2\ k_{\text{B}}T$</p>		

Organism	Transcription factor	Copies per cell order of magnitude	BNID
<i>E. coli</i>	LacI (carbon utilization)	10^1 - 10^2	100734
<i>E. coli</i>	AraC (carbon utilization)	10^2	105139
<i>E. coli</i>	ArcA (general aerobic respiration control)	10^4	102632
<i>S. cerevisiae</i>	Gal4 (carbon utilization)	10^2	109208
<i>S. cerevisiae</i>	Tfb3 (general transcription initiation factor)	10^3	109208
<i>S. cerevisiae</i>	Pho2 (phosphate metabolism)	10^4	109208
<i>D. melanogaster</i> , anterior blastoderm nuclei	Bicoid (development)	10^4	106843
<i>D. melanogaster</i> , Schneider cell line	GAGA zinc finger	10^6	106846
Mouse/Rat murine macrophage	Glucocorticoid, Thyroid and Androgen receptors associated zinc fingers	10^4	106899
Mouse/Rat murine macrophage	NF-kappaB p65	10^5	106901
<i>H. sapiens</i> cell lines	P53 (growth and apoptosis)	10^4 - 10^5	100420
<i>H. sapiens</i> cell lines	Glucocorticoid, Estrogen, Steroid receptors associated zinc fingers	10^4 - 10^5	106904, 106906, 106911
<i>H. sapiens</i> cell lines	STAT6	10^4 - 10^5	106914
<i>H. sapiens</i> cell lines	NF-kappaB p65	10^5	106909
<i>H. sapiens</i> cell lines	Myc (global chromatin structure regulation)	10^5	106907

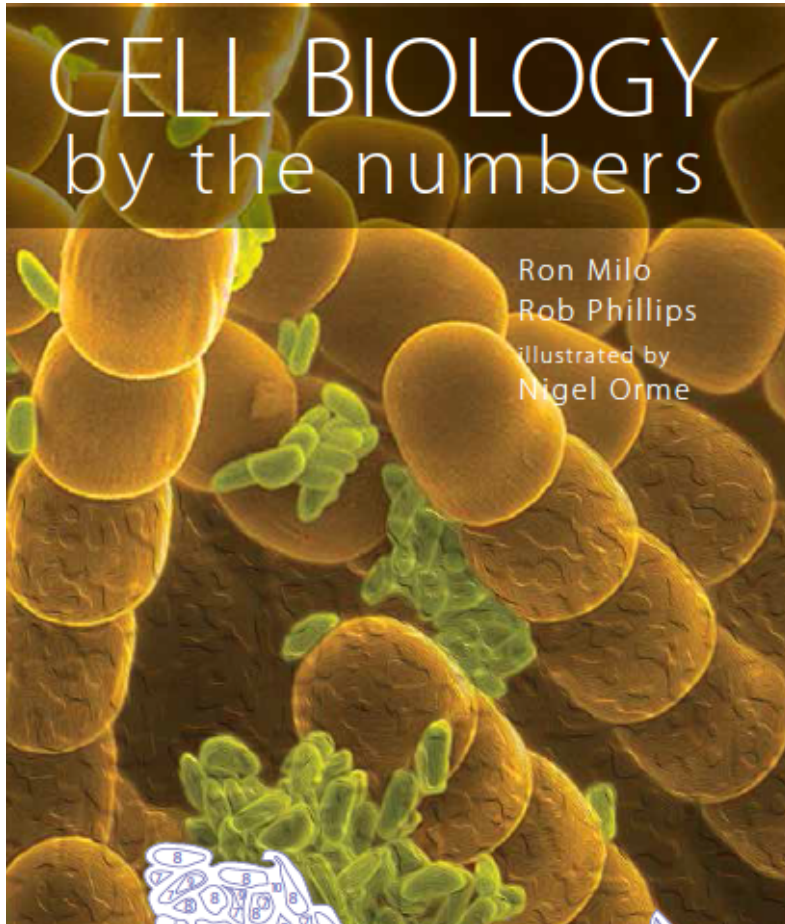
Protein	Name	Molecules/cell	Standard Error	Concentration (nM)
G protein-coupled receptor	Ste2	7,000	400	400
G- α	Gpa1	2,000	300	130
G- β	Ste4	2,000	100	110
PAK kinase	Ste20	4,000	500	200
Scaffold	Ste5	500	60	30
MAPKKK binding partner	Ste50	1,000	100	70
MAPKKK	Ste11	4,000	90	200
MAPKK	Ste7	900	70	50
MAPK	Fus3	20,000	3,000	1,100
MAPK	Kss1	20,000	2,000	1,200
MAPK	Hog1	6,000	400	300
Scaffold/MAPKK	Pbs2	2,000	200	140
MAPK phosphatase	Msg5	40	3	2
Cell cycle inhibitor	Far1	200	20	14
Transcriptional activator	Stw12	1,400	40	80
Transcriptional repressor	Dig1	5,000	500	300
Transcriptional repressor	Dig2	1,000	80	70

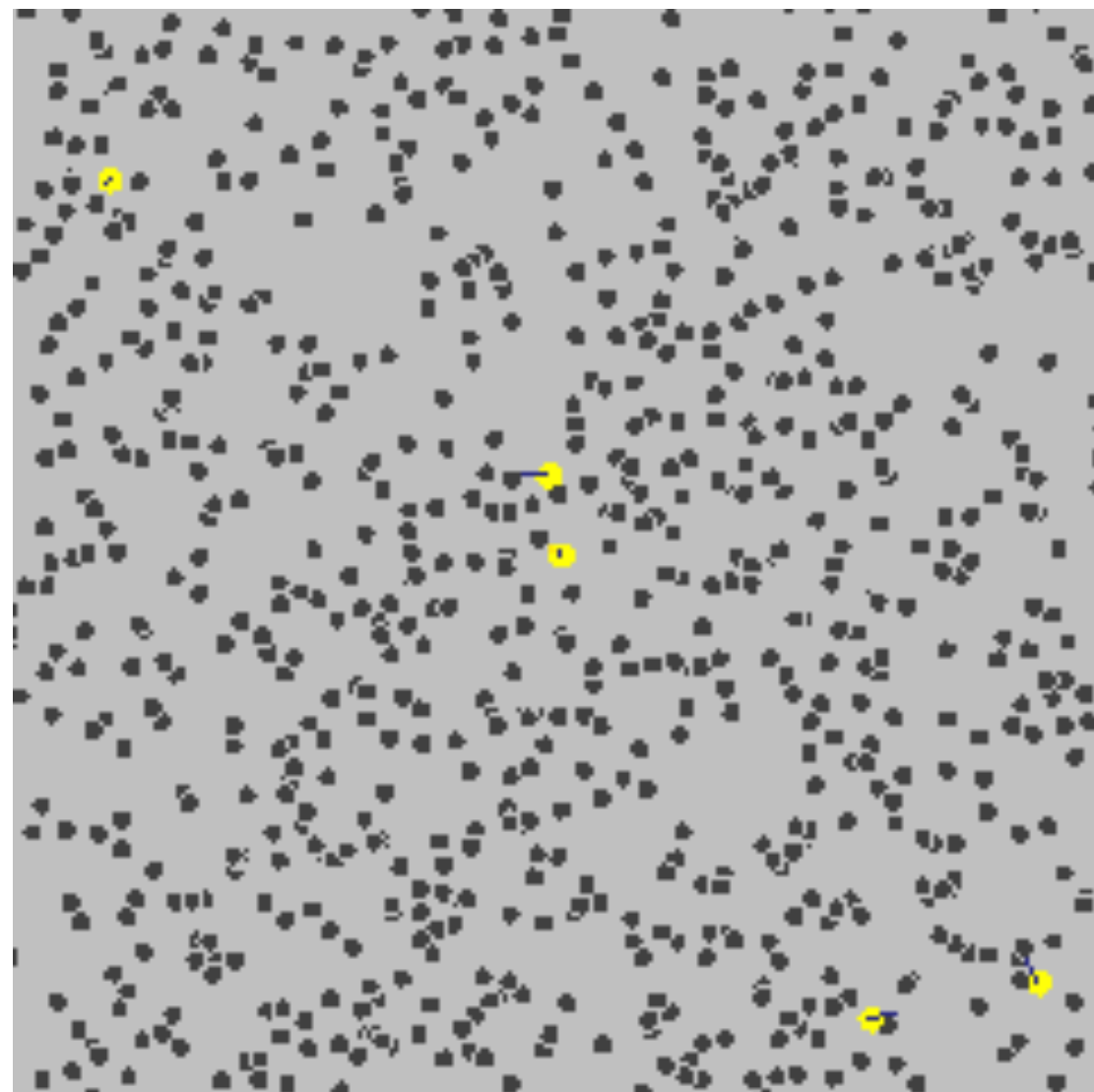
Table 1: Abundances of signaling molecules associated with the MAPK cascade in budding yeast before pheromone addition. Abundances are based on quantitative immunoblotting. Concentration was calculated assuming a cell volume of 29 fL. The standard error indicates the uncertainty on the number of molecules per cell as estimated in this specific experiment. Values were rounded to one significant digit. Adapted from Thomson et al, PNAS 2012 (BNID 107680).

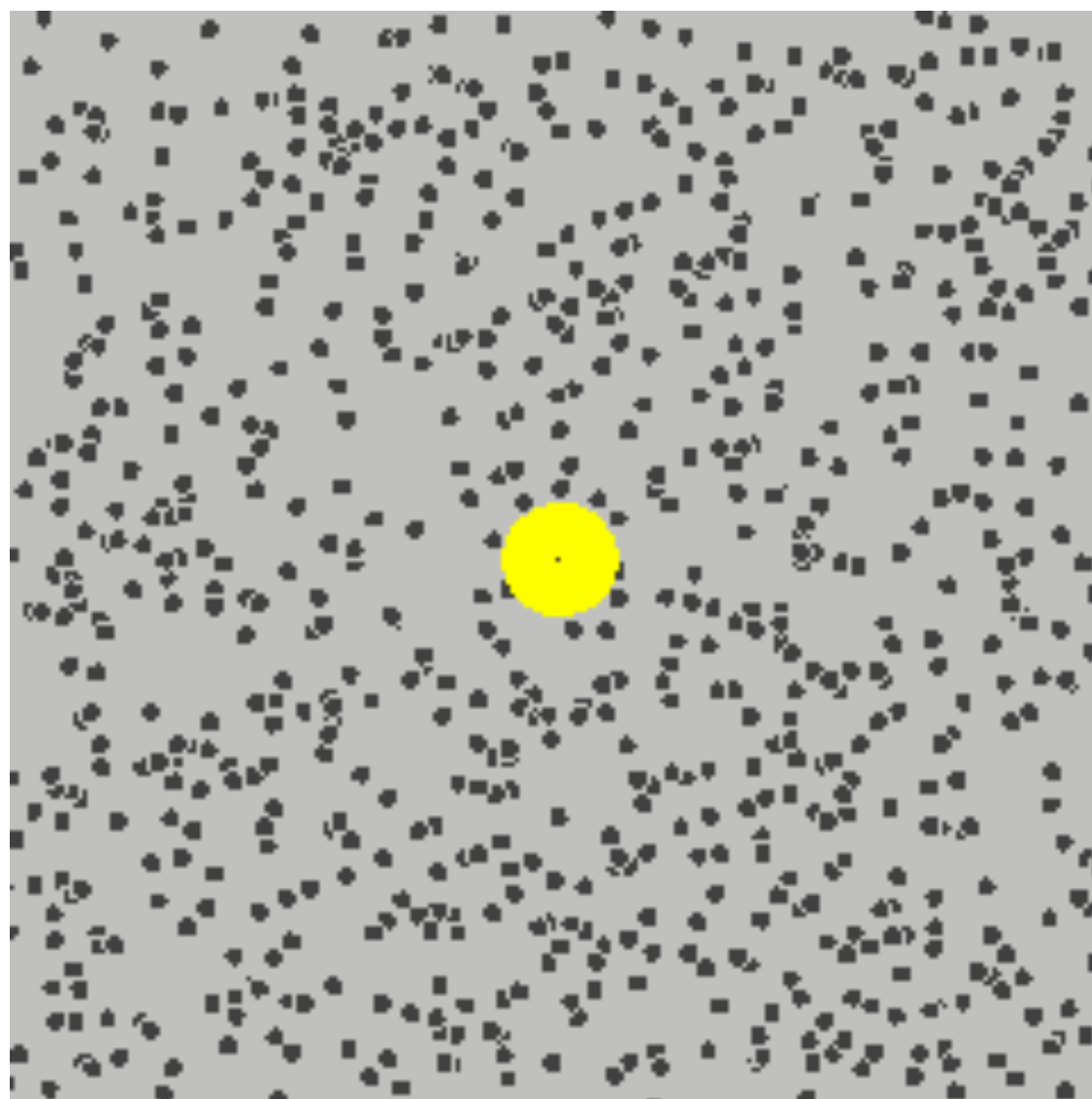
CELL BIOLOGY

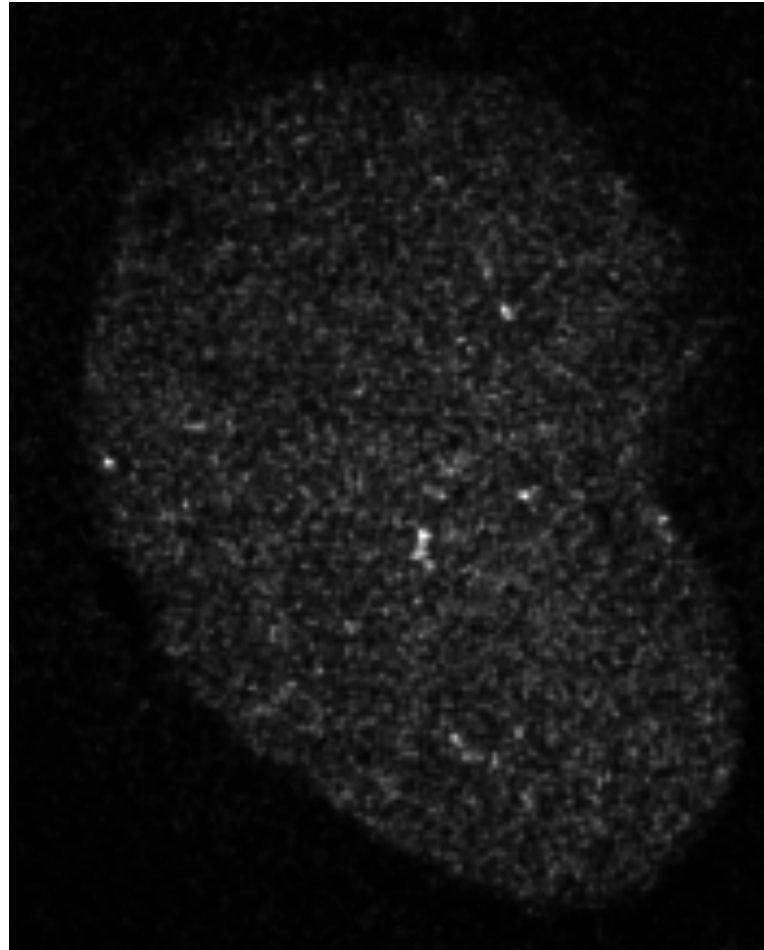
by the numbers

Ron Milo
Rob Phillips
illustrated by
Nigel Orme

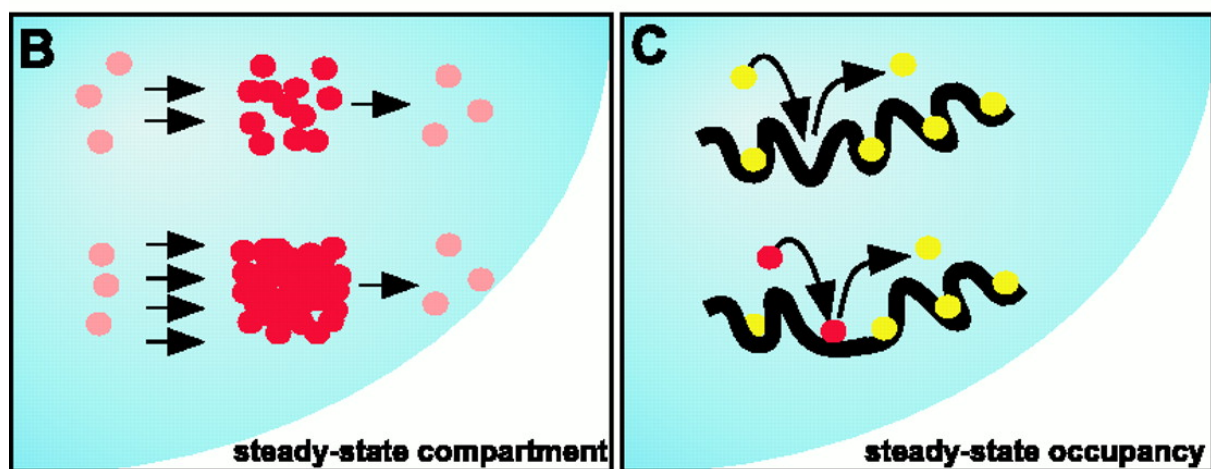
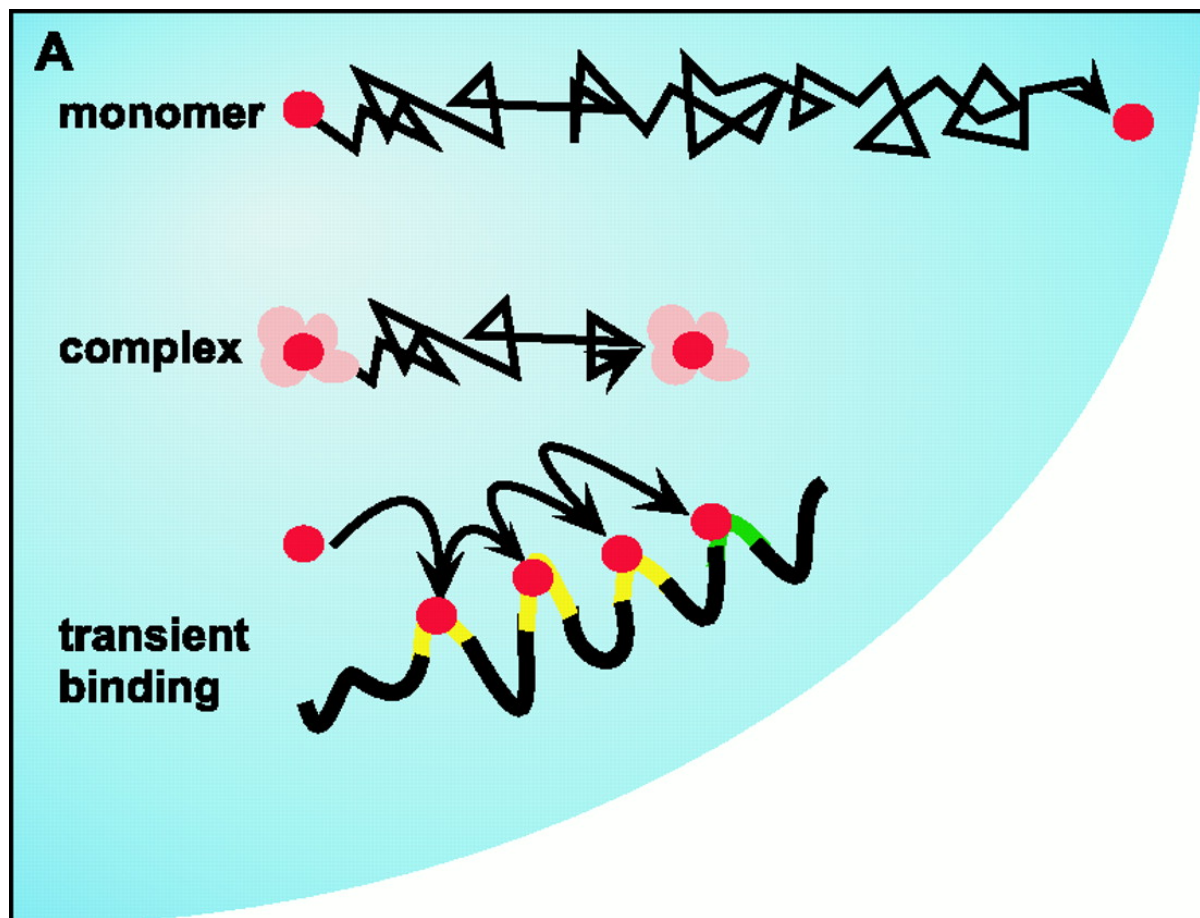


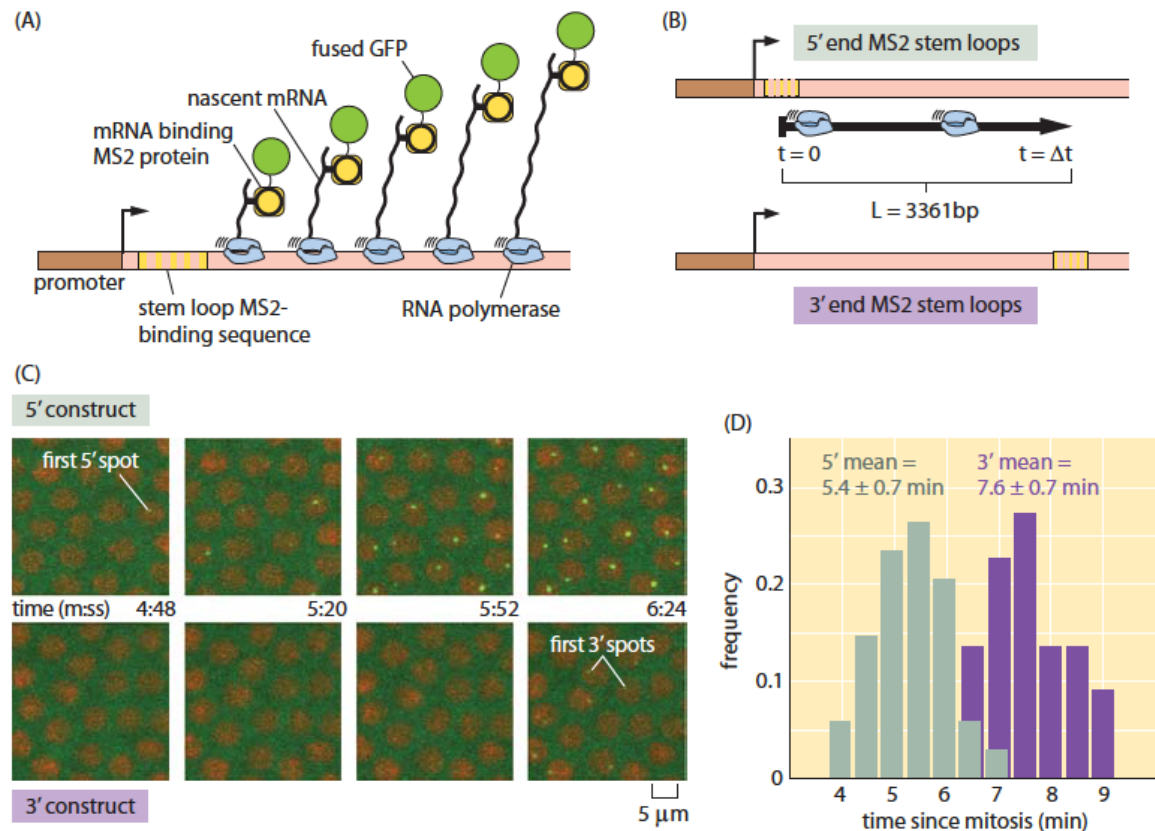






Biochemical reactions in the cells are limited by the diffusion of the molecules.





$$\Rightarrow \text{transcription rate} = \frac{\text{length}}{\text{time difference}} = \frac{L}{\Delta t} = \frac{3361 \text{ bp}}{2.2 \text{ min}} \approx 1500 \text{ nt/min} \approx 25 \text{ nt/s}$$

Figure 4: Dynamics of transcription in the fly embryo. (A) Schematic of the

Global quantification of mammalian gene expression control

Björn Schwanhäusser¹, Dorothea Busse¹, Na Li¹, Gunnar Dittmar¹, Johannes Schuchhardt², Jana Wolf¹, Wei Chen¹
& Matthias Selbach¹

Absolute mRNA and protein copy numbers

We calculated absolute cellular mRNA copy numbers based on the number of sequencing reads in the unfractionated sample in conjunction

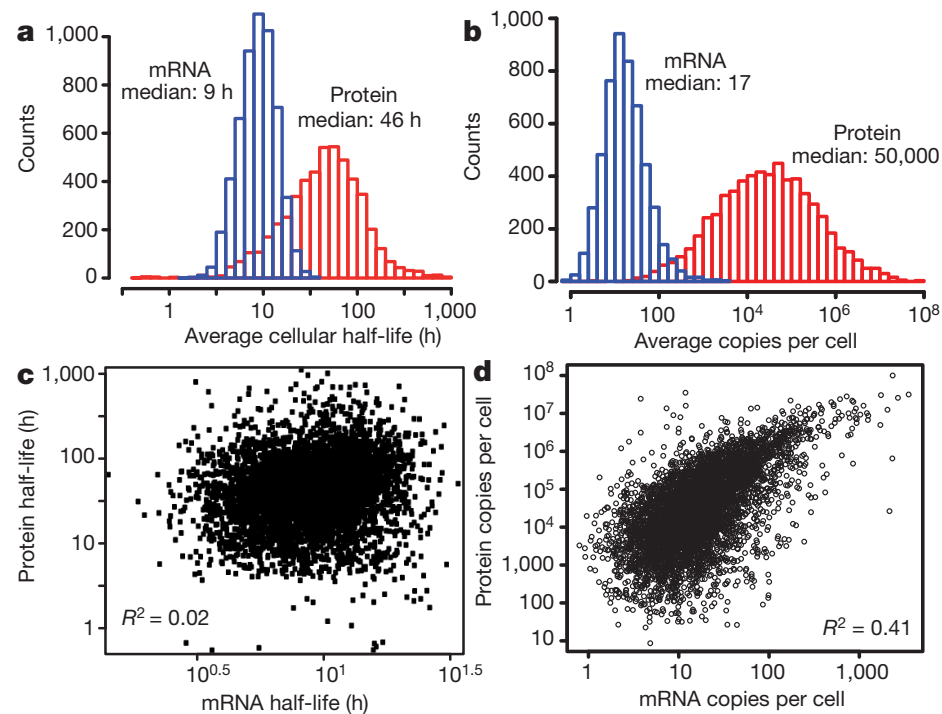
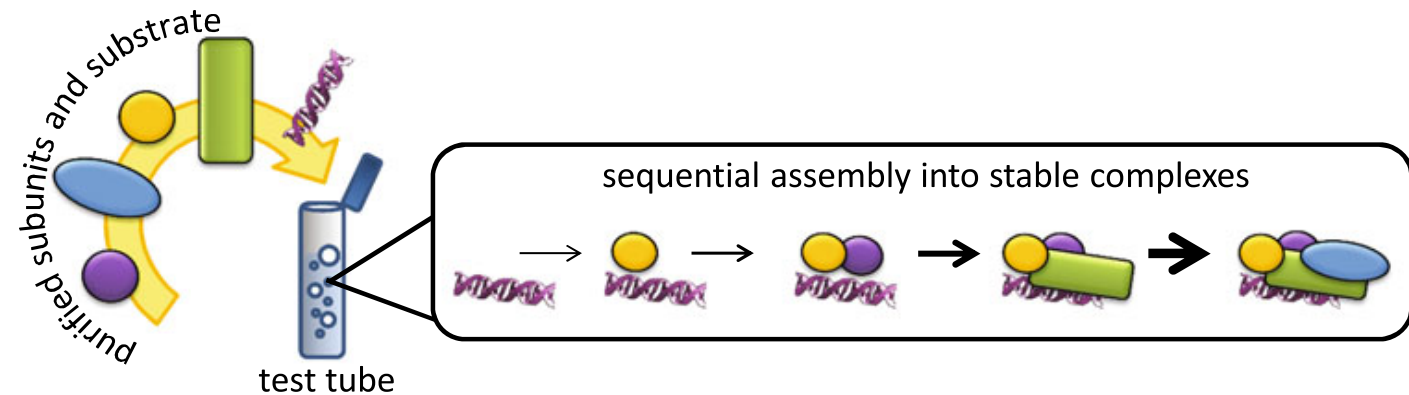


Figure 2 | mRNA and protein levels and half-lives. **a, b**, Histograms of mRNA (blue) and protein (red) half-lives (**a**) and levels (**b**). Proteins were on average 5 times more stable and 2,800 times more abundant than mRNAs and spanned a higher dynamic range. **c, d**, Although mRNA and protein levels correlated significantly, correlation of half-lives was virtually absent.

Assembly of the transcription machinery: ordered and stable, random and dynamic, or both?

Timothy J. Stasevich • James G. McNally

a. Assembly according to biochemistry:



b. Assembly according to fluorescence microscopy:

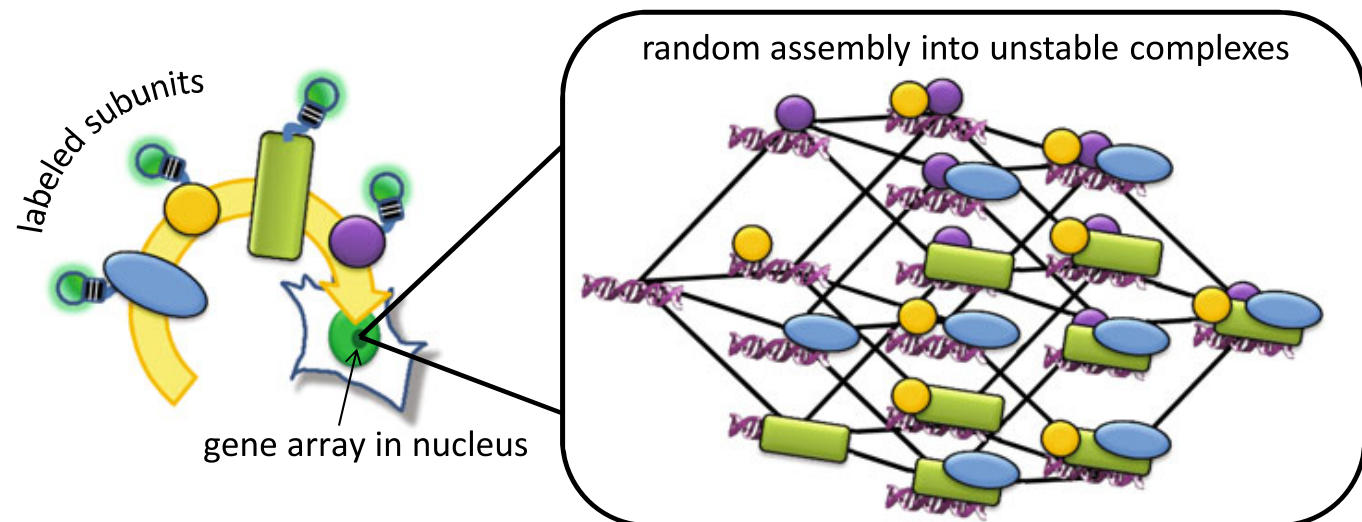


Table 1 Comparing biochemical measurements of transcription machinery binding times with live-cell microscopy measurements

Complex	Estimated binding times (min)			
	Biochemistry		Live cell microscopy	
TFIIA:DNA	1-21	[<i>t_{off}</i> , TIRFM-array, yeast] (Bonham et al, 2009)		
TFIIB:DNA	4-260	[<i>t_{off}</i> , TIRFM-array, yeast] (Bonham et al, 2009)	< 0.02	[<i>t_{1/2}</i> , FRAP, yeast] (Sprouse et al, 2008)
TBP:DNA	65-100	[<i>t_{1/2}</i> , TATA box, band shift, yeast] (Hoopes et al, 1992)	< 0.02	[<i>t_{1/2}</i> , FRAP, yeast] (Sprouse et al, 2008)
	7-327	[<i>t_{off}</i> , TIRFM-array, yeast] (Bonham et al, 2009)	~1	[<i>t_{1/2}</i> , FRAP, human] (Chen et al, 2002)
	~37 / ~63 / ~80	[<i>t_{on+off}</i> , Pol II / III / I DNA, ChIP, yeast] (van Werven et al, 2009)	1.7 - 2.8	[<i>t_{off}</i> , FRAP, human] (de Graaf et al, 2010)
NF-KB:DNA	3-7	[<i>t_{off}</i> , SPM, human] (Linnell et al, 2004)	0.02-0.03	[<i>t_{1/2}</i> , FRAP, mouse] (Sung et al, 2009)
			< 0.3	[<i>t_{off}</i> , p65, FLIP, human] (Bosisio et al, 2006)
GR:DNA	~1.5 / ~77	[<i>t_{off}</i> , monomer / dimer, band shift, rat] (Lieberman & Nordeen, 1997)	0.01 – 0.03	[<i>t_{off}</i> , FRAP/FCS, mouse] (Stasevich et al, 2010)
	~ 151	[<i>t_{off}</i> , DNase footprint, rat] (Perlmann et al, 1990)	0.05	[<i>t_{off}</i> , FRAP, mouse] (Mueller et al, 2008)
SWI/SNF : chromatin	> 30	[<i>t_{off}</i> , comp. exp., yeast] (Hassan et al, 2002)	0.17	[<i>t_{1/2}</i> , FRAP, mouse] (Johnson et al, 2008)
Gal4:DNA	~ 250	[<i>t_{off}</i> , SPM, yeast] (Shumaker-Parry et al, 2004)		
	~ 15	[<i>t_{on+off}</i> , ChIP, yeast] (Nalley et al, 2009)		
TFIIE:Pol II	~ 4.8	[<i>t_{off}</i> , SPM, yeast] (Bushnell et al, 1996)		
TFIIB:Pol II	~ 44	[<i>t_{off}</i> , SPM, yeast] (Bushnell et al, 1996)		
TFIIF:Pol II	~ 3.7	[<i>t_{off}</i> , SPM, yeast] (Bushnell et al, 1996)		

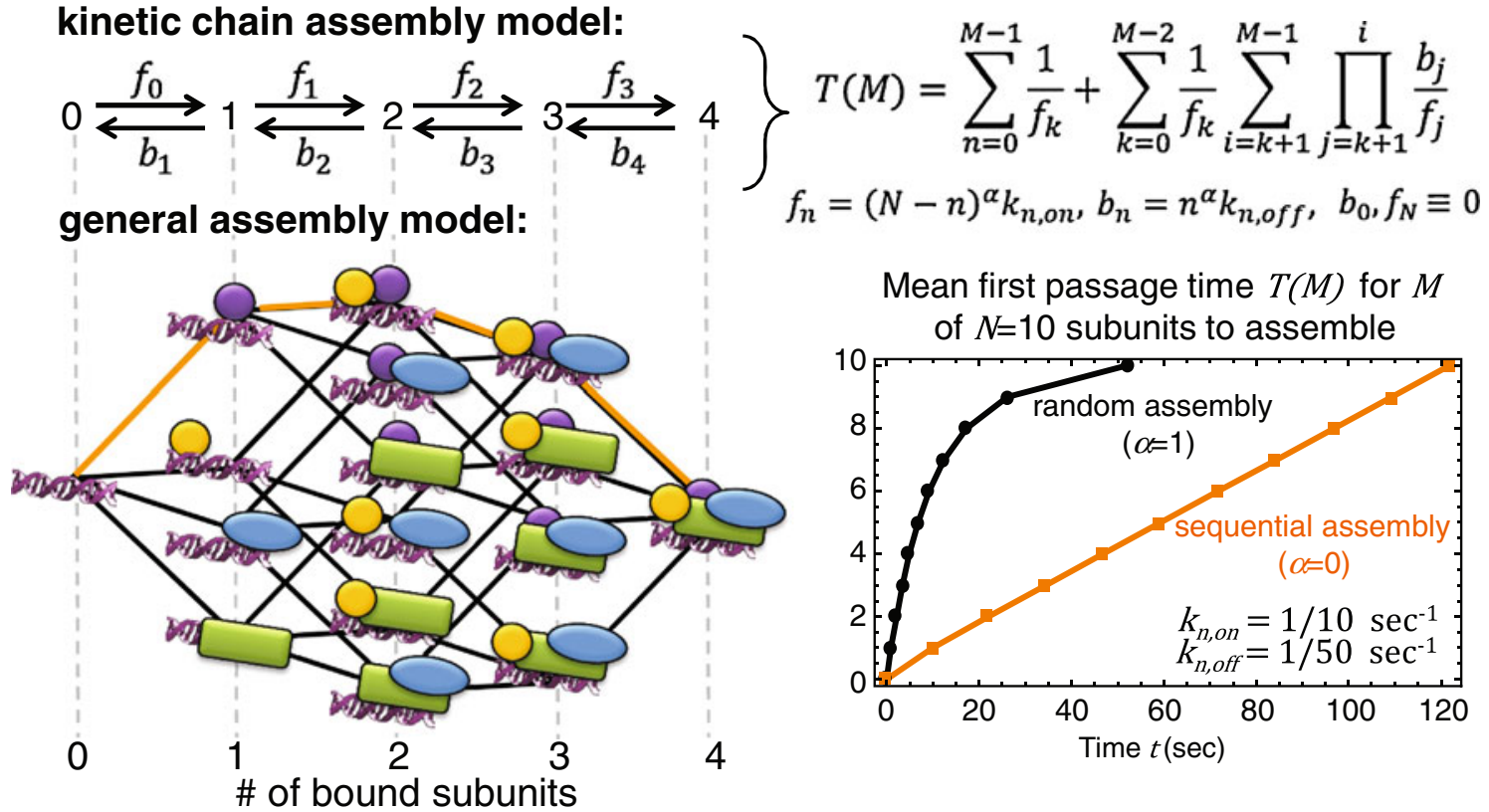


Fig. 3 Kinetic chain model for assembly. In the most general assembly model involving N components (either individual subunits or preformed subcomplexes), there are 2^N assembly states and $N2^{N-1}$ association constants. In the kinetic chain model of assembly, this is reduced to just $2N$ parameters representing forward (f_n) and backward (b_n) transitions between complexes with n bound subunits. In this simplified model, the mean time $T(M)$ to first form a complex with M of N subunits assembled, referred to as the MFPT, can be explicitly written in terms of f_n and b_n , which themselves depend on the subunit

binding on and off rates, $k_{n,on}$ and $k_{n,off}$, respectively, with n ranging from 0 to N . In this model, when $\alpha=1$ assembly is random and when $\alpha=0$ assembly is sequential. The figure on the *left* illustrates the simplified kinetic chain model (*top of panel*) for the general assembly model (*bottom of panel*) for $N=4$ subunits. All paths are used in a random assembly strategy, but only one path (*thick orange*) is used in a sequential assembly strategy. The graph on the *right* compares the random ($\alpha=1$) and sequential ($\alpha=0$) MFPTs for a complex with $N=10$ subunits with $k_{n,on}=1/10 \text{ s}^{-1}$ and $k_{n,off}=1/50 \text{ s}$



Protein Dynamics: Implications for Nuclear Architecture and Gene Expression

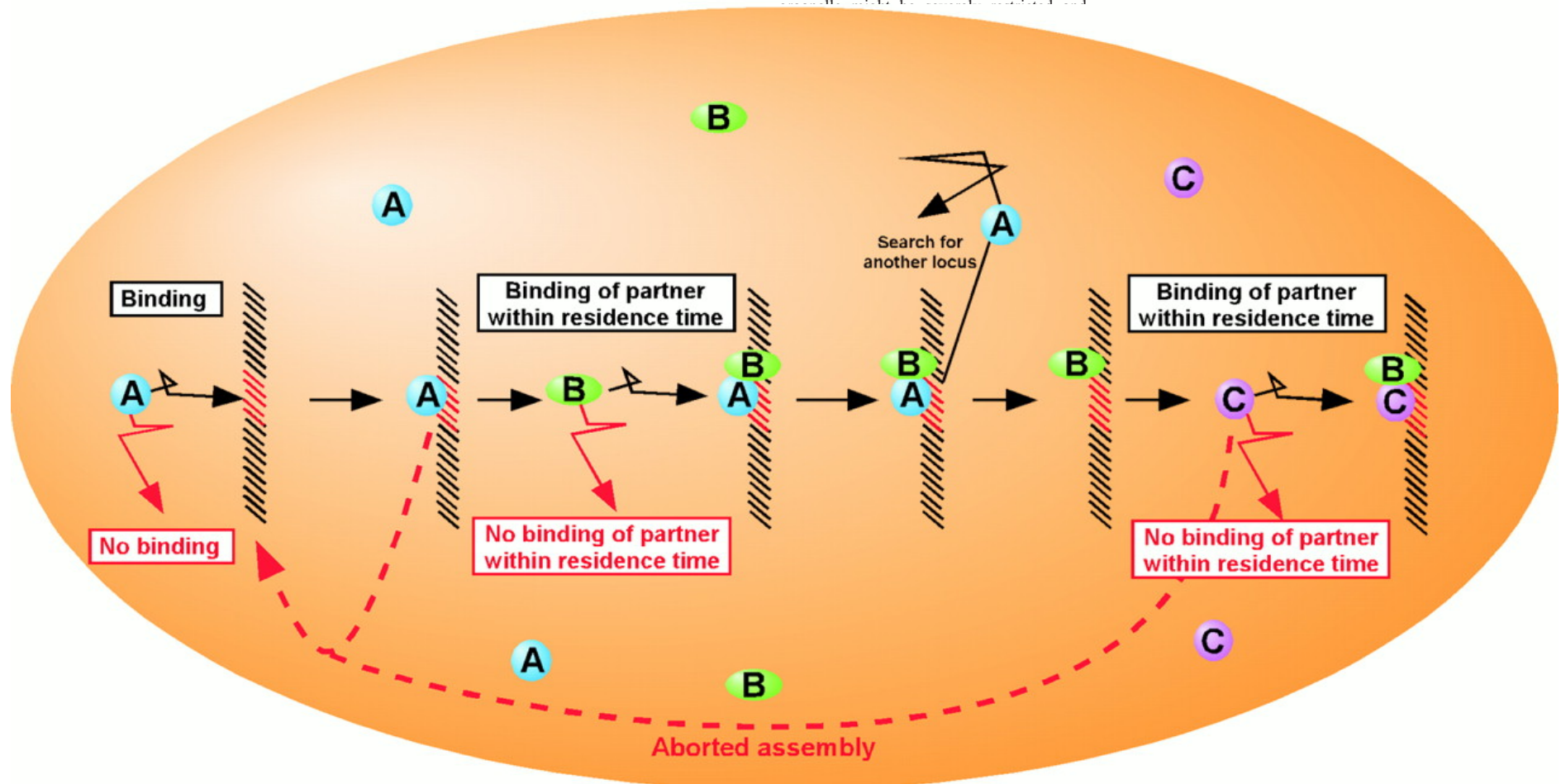
Tom Misteli

Studies of nuclear architecture reveal that the dynamic properties of proteins in the nucleus are critical for their function. The high mobility of proteins ensures their availability throughout the nucleus; their dynamic interplay generates an ever-changing, but overall stable, architectural framework, within which nuclear processes take place. As a consequence, overall nuclear morphology is determined by the functional interactions of nuclear components. The observed dynamic properties of nuclear proteins are consistent with a central role for stochastic mechanisms in gene expression and nuclear architecture.

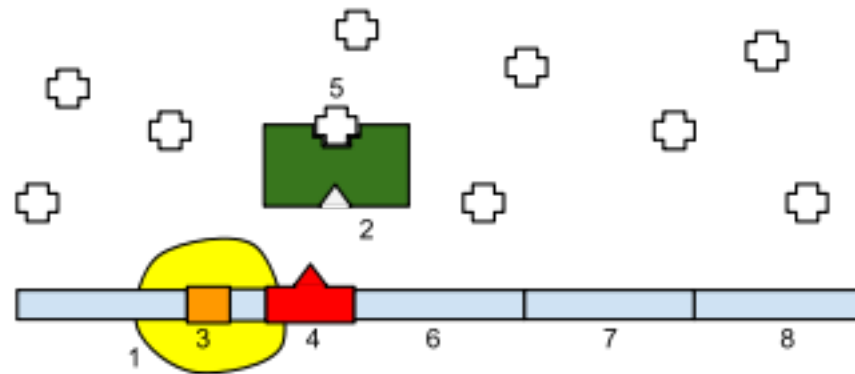
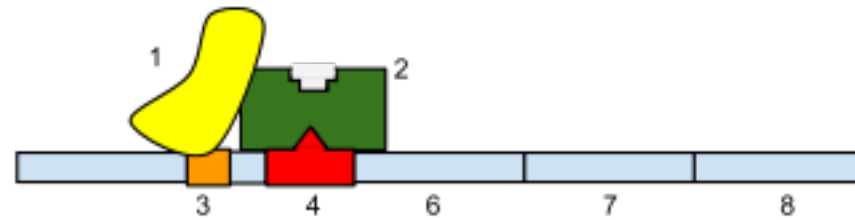
(Fig. 2). These experiments have given important new insights into nuclear architecture and function.

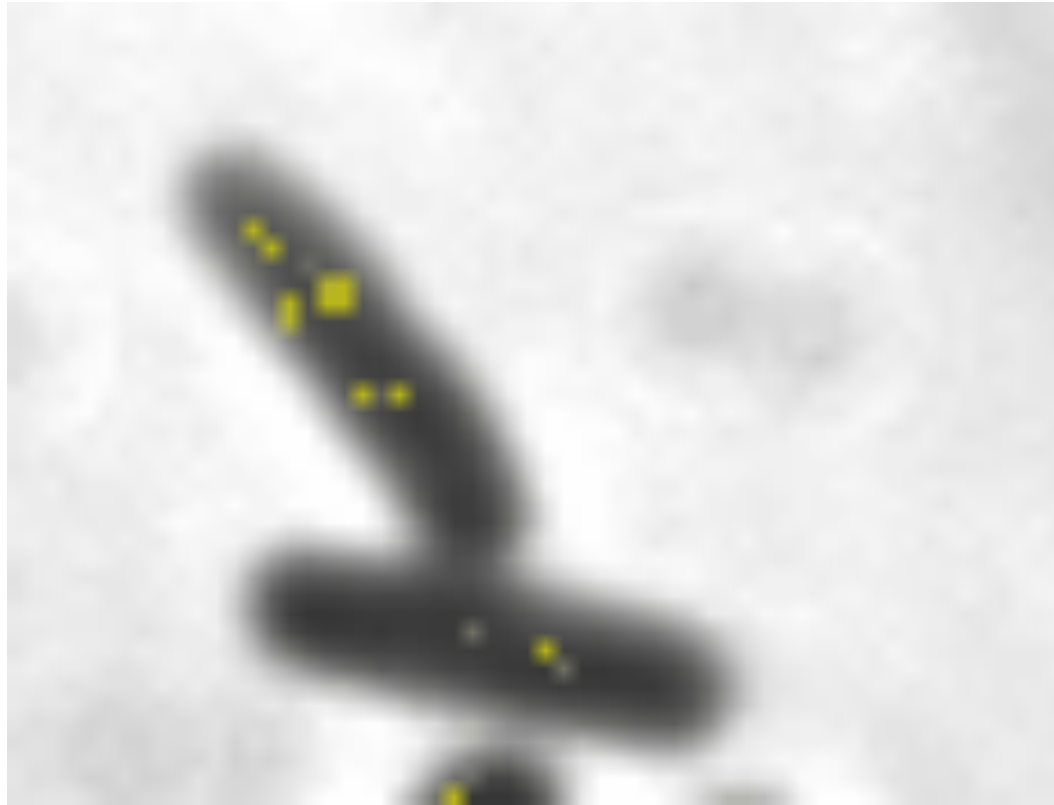
Proteins Roam the Cell Nucleus

Considering the high DNA content and the large amounts of RNAs and proteins, one might intuitively think of the nucleus as a viscous, gel-like environment. If this were true, the movement of proteins within the nucleus would be severely restricted, and



Lac operon





This time-lapse movie shows fluorescence overlay (yellow) on phase contrast images of a cell dividing into two genetically identical daughter cells. One daughter cell changes into a phenotype with very high fluorescence, while the other daughter cell does not. This change in phenotype is the result of the stochastic, full dissociation of the tetrameric repressor from all of its binding sites.

Choi Paul, Cai Long, Frieda Kirsten, Xie Xiaoliang Sunney(2008). A stochastic single-molecule event triggers phenotype switching of a bacterial cell. *Science* . **322** : 442-446.

Probing Transcription Factor Dynamics at the Single-Molecule Level in a Living Cell

Johan Elf,^{1*} Gene-Wei Li,^{2*} X. Sunney Xie^{1†}

Transcription factors regulate gene expression through their binding to DNA. In a living *Escherichia coli* cell, we directly observed specific binding of a *lac* repressor, labeled with a fluorescent protein, to a chromosomal *lac* operator. Using single-molecule detection techniques, we measured the kinetics of binding and dissociation of the repressor in response to metabolic signals. Furthermore, we characterized the nonspecific binding to DNA, one-dimensional (1D) diffusion along DNA segments, and 3D translocation among segments through cytoplasm at the single-molecule level. In searching for the operator, a *lac* repressor spends ~90% of time nonspecifically bound to and diffusing along DNA with a residence time of <5 milliseconds. The methods and findings can be generalized to other nucleic acid binding proteins.

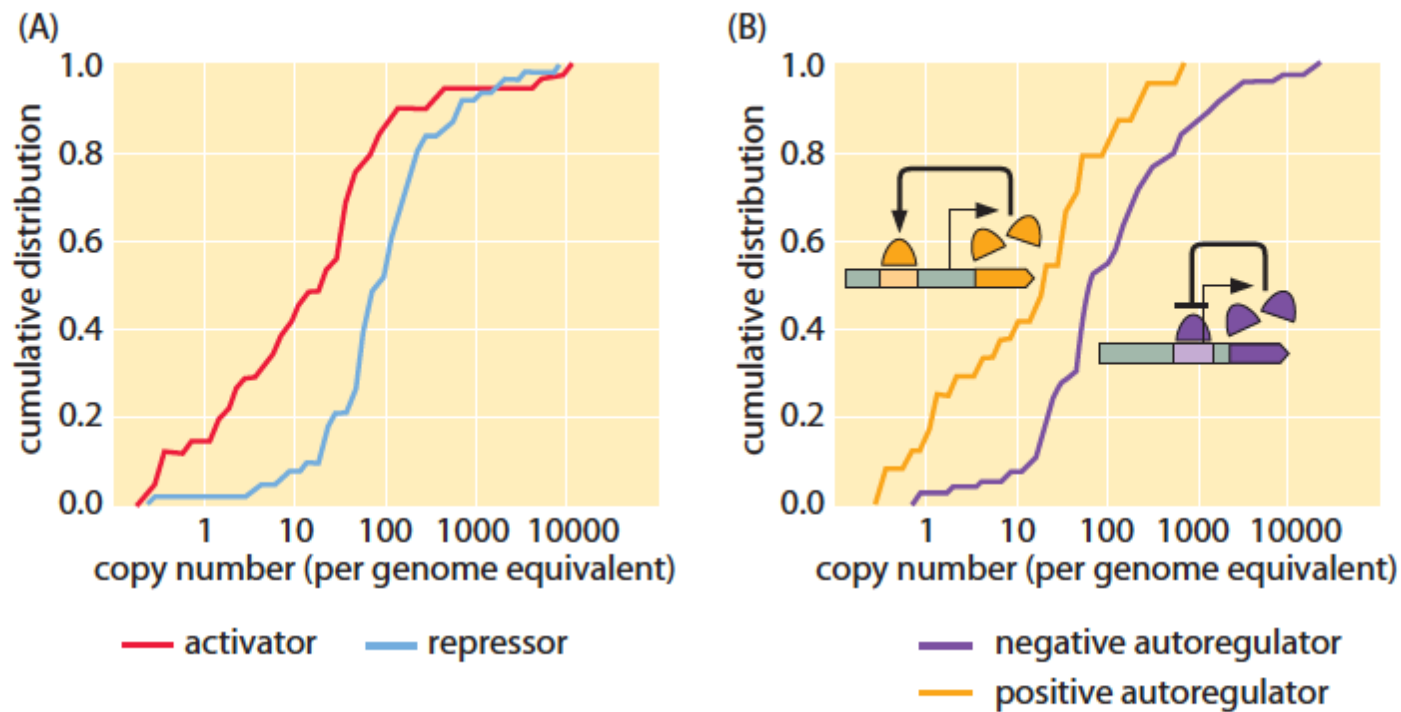
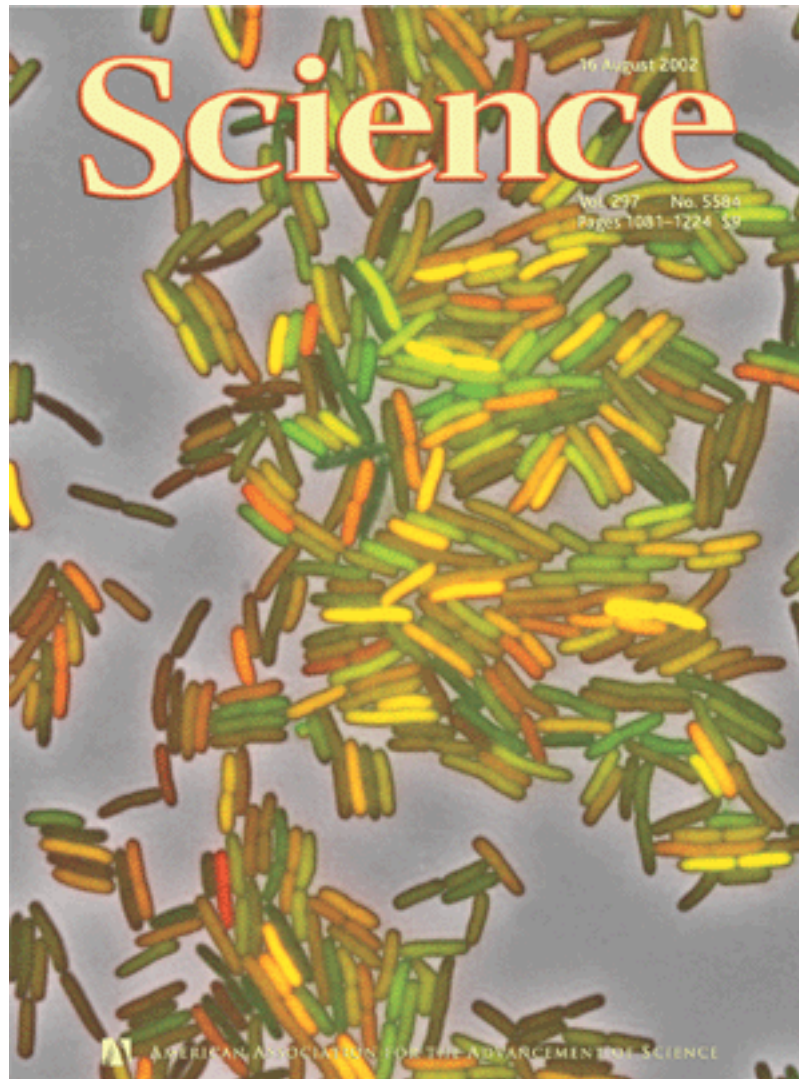


Figure 1: Measured copy numbers of transcription factors in *E. coli*. (A) Cumulative distributions for both activators and repressors showing that activators typically occur between 1 and 100 copies per cell whereas repressors generally occur between 10-1000 copies per cell. (B) Cumulative distributions for autoregulators. (adapted from G.-W. Li et al, Cell 157, 624–635, 2014)



Science 16 August 2002:

Vol. 297 no. 5584 pp. 1183-1186

DOI: 10.1126/science.1070919

REPORT

Stochastic Gene Expression in a Single Cell

Michael B. Elowitz, Arnold J. Levine, Eric D. Siggia, Peter S. Swain



Research paper

Highly multiplexed quantitation of gene expression on single cells

Maria H. Dominguez ^{a,1}, Pratip K. Chattopadhyay ^{a,*,1}, Steven Ma ^b, Laurie Lamoreaux ^b, Andrew McDavid ^c, Greg Finak ^c, Raphael Gottardo ^c, Richard A. Koup ^b, Mario Roederer ^a

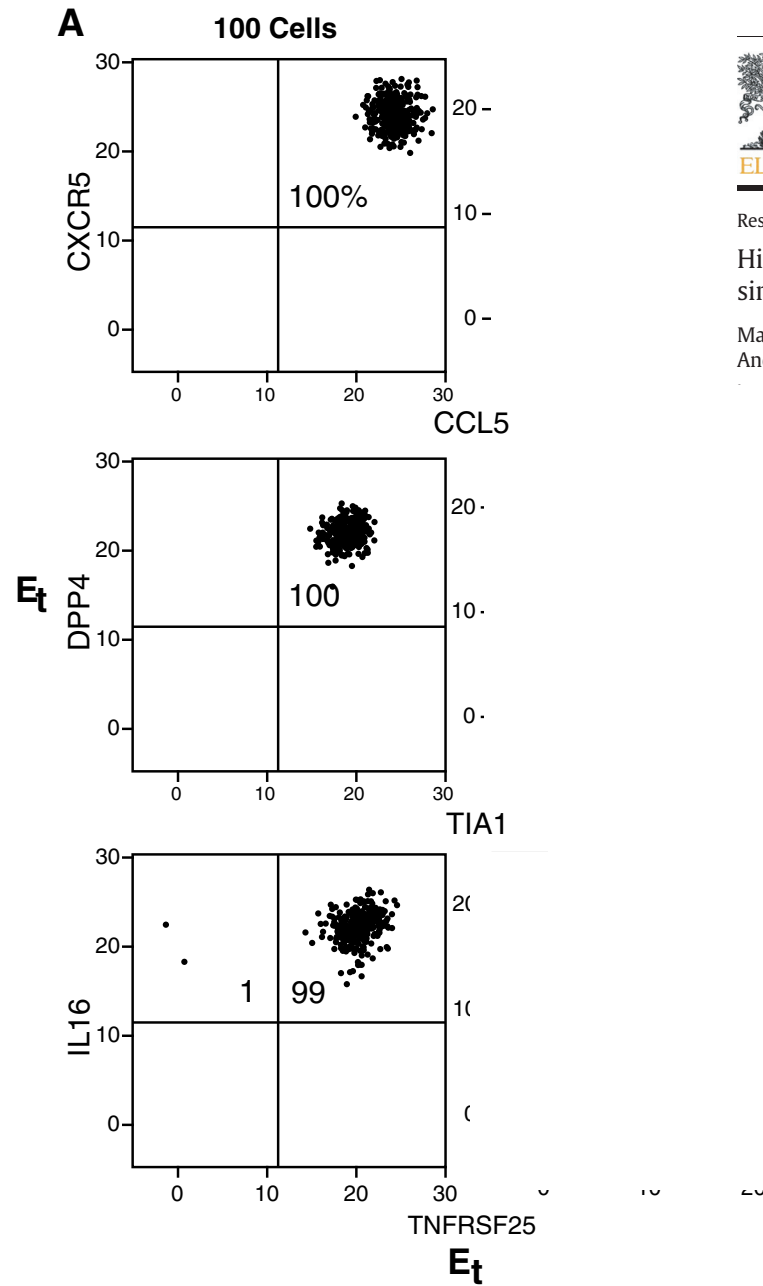


Fig. 9. Gene expression compared between single-cell and 100-cell samples. A) 100-cell data suggests that genes are co-expressed; however, at the single-cell level the true, independent expression of these genes can be recognized (percent of cells expressing given marker combinations are shown at each quadrant). B) There is a strong correlation between single-cell and 100-cell gene expression data (normalized to single cells).

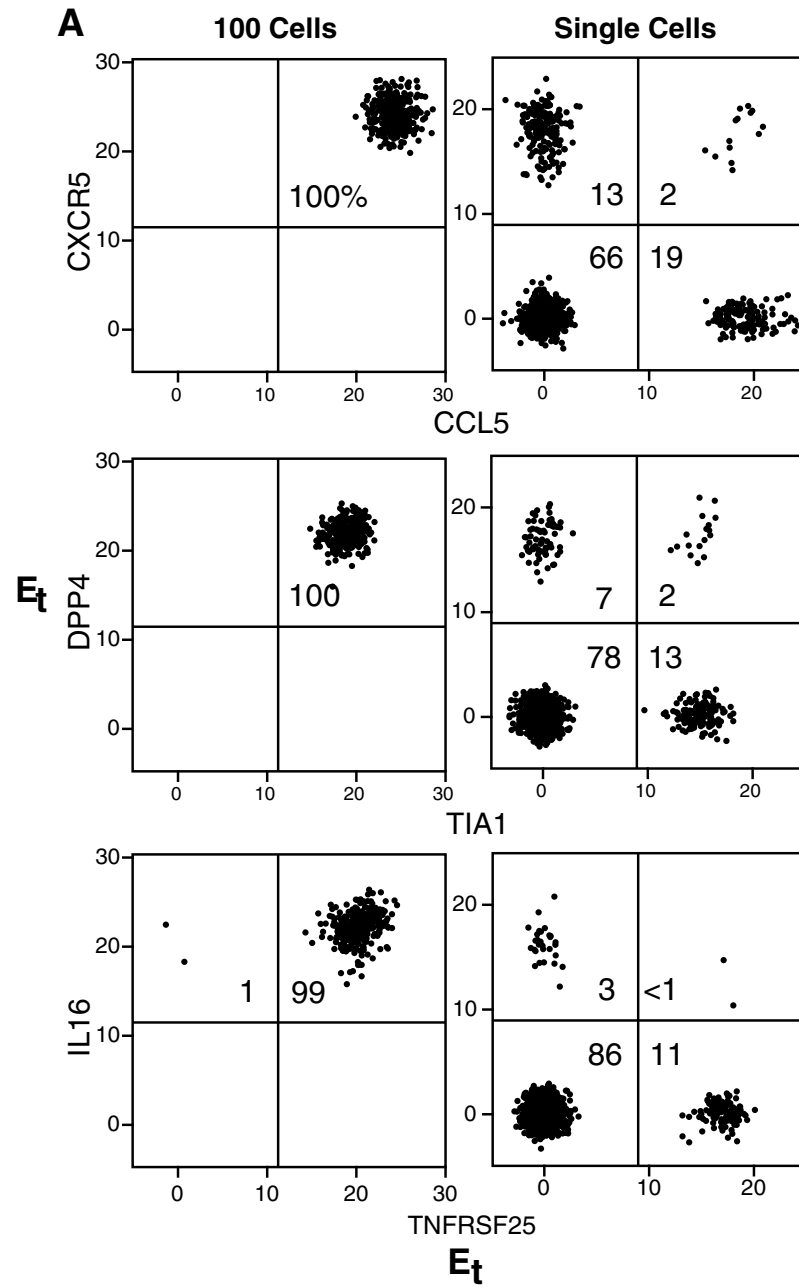


Fig. 9. Gene expression compared between single-cell and 100-cell samples. A) 100-cell data suggests that the true, independent expression of these genes can be recognized (percent of cells expressing given is a strong correlation between single-cell and 100-cell gene expression data (normalized to single

Transcriptome *in vivo* analysis (TIVA) of spatially defined single cells in live tissue

Ditte Lovatt^{1,6}, Brittani K Ruble^{2,6}, Jaehee Lee¹, Hannah Dueck³, Tae Kyung Kim¹, Stephen Fisher³, Chantal Francis³, Jennifer M Spaethling¹, John A Wolf⁴, M Sean Grady⁴, Alexandra V Ulyanova⁴, Sean B Yeldell², Julianne C Griepenburg², Peter T Buckley¹, Junhyong Kim^{3,5}, Jai-Yoon Sul¹, Ivan J Dmochowski^{2,7} & James Eberwine^{1,5,7}

| VOL.11 NO.2 | FEBRUARY 2014 | **NATURE METHODS**

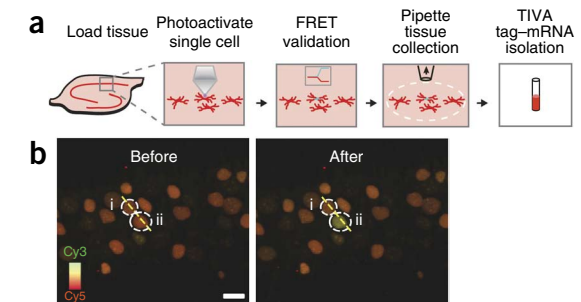


Figure 5 | TIVA tag capture of mRNA from cells in human live brain tissue specimen obtained from biopsy of the right frontal cortex from a subject undergoing surgery for communicating hydrocephalus. **(a)** Micrographs of TIVA tag-loaded cells identified by FRET signal, before and after uncaging, which was performed using the same parameters as in mouse. Scale bar, 10 μm. **(b)** FRET signal upon TIVA-tag activation (lightning bolt). **(c)** Heatmap comparing expression of common cell type-specific markers in an average pool of 13 TIVA tag captured cells and in two TIVA tag captured individual cells.

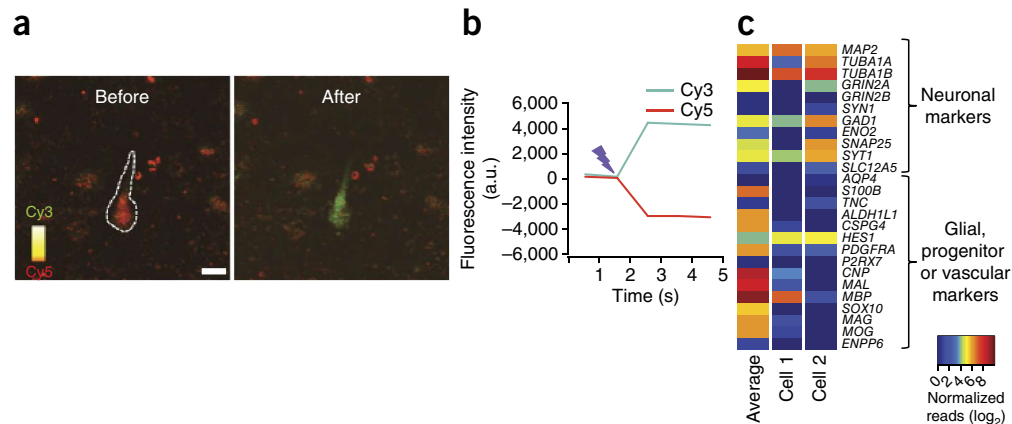
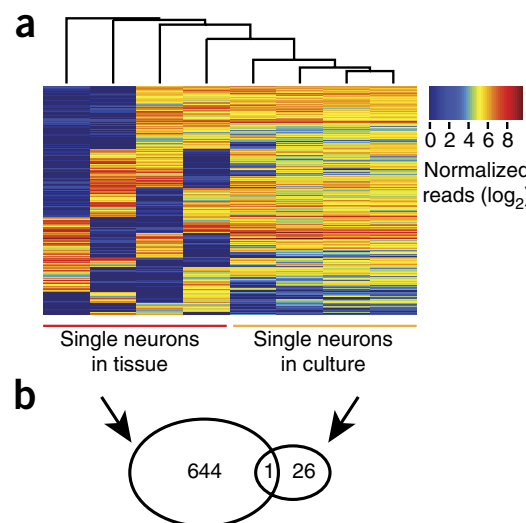
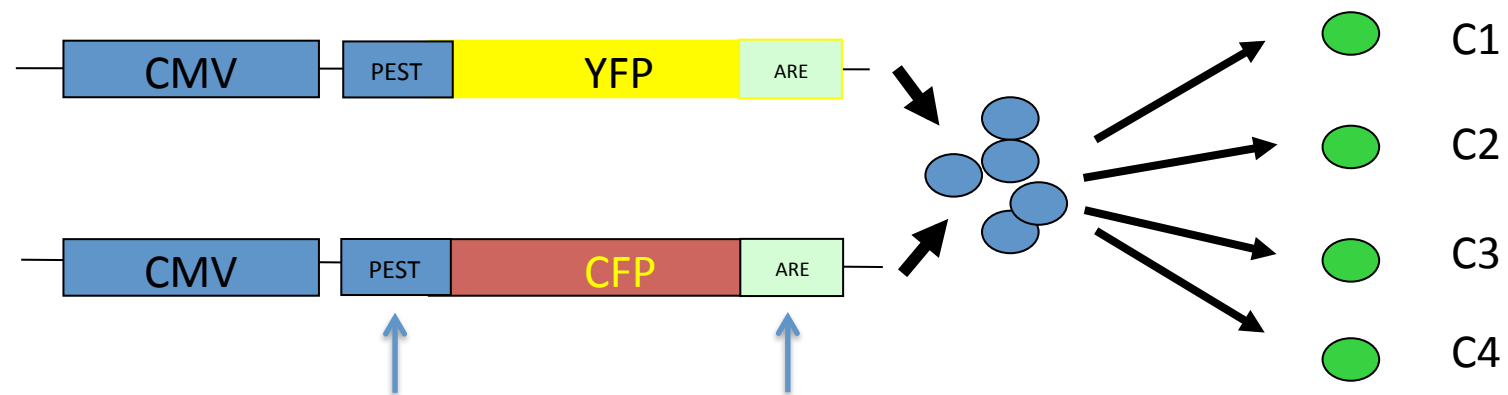


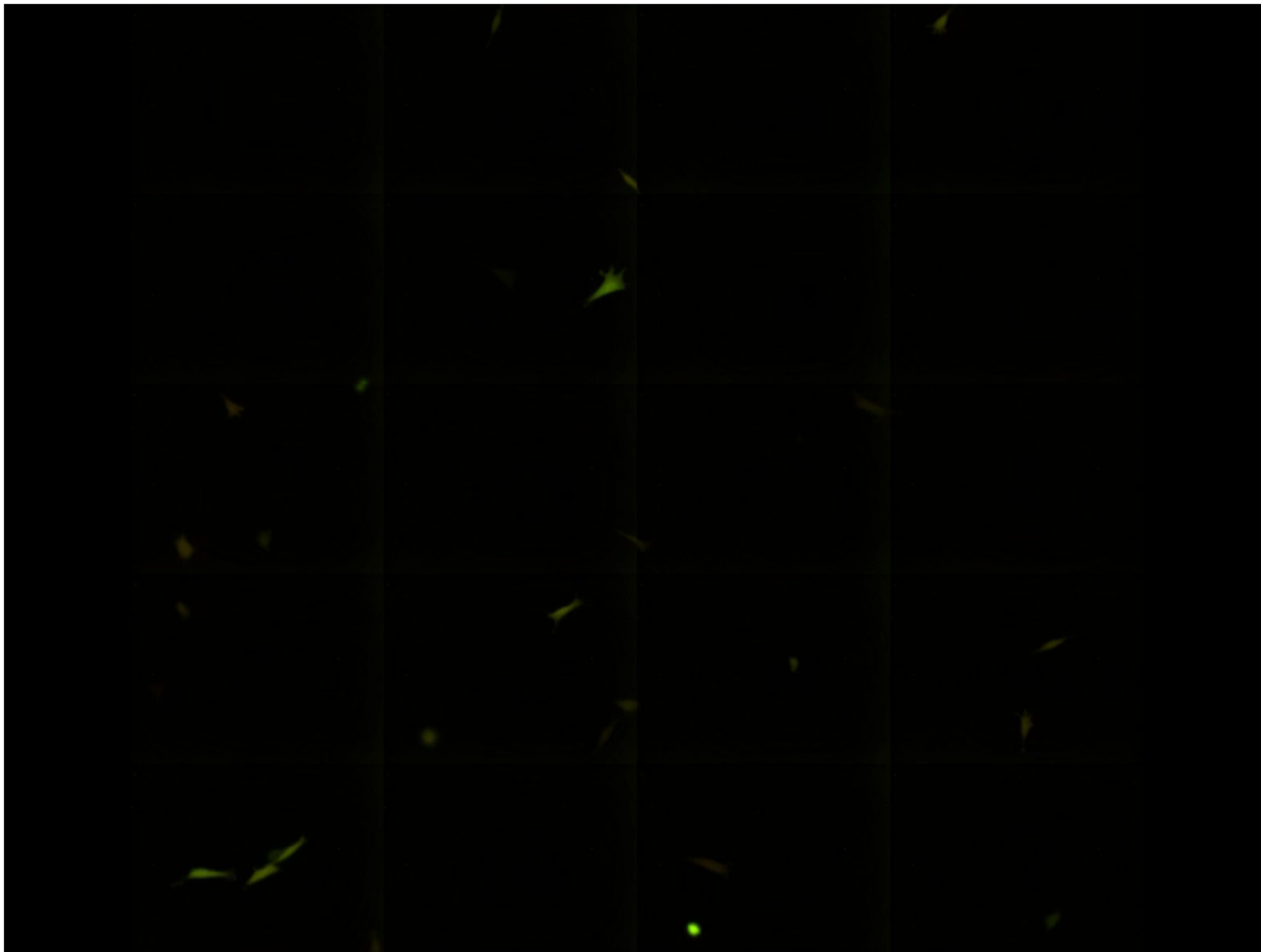
Figure 6 | Bimodal transcripts in single hippocampal neurons in tissue and in culture. **(a)** Heatmaps shows clustering of 645 bimodally expressed genes (horizontal lines) in four single cells from hippocampal tissue compared to four single hippocampal neurons in culture. Bimodally expressed genes were defined as having a gap in expression of at least four log units in two samples. To be especially stringent in this analysis, two samples were required to have expression values on either side of this gap. The cells with low expression were required to have fewer than ten normalized counts for the bimodally expressed transcript. **(b)** Overlap between bimodal genes in single neurons from tissue and from culture (4 cells in each group).

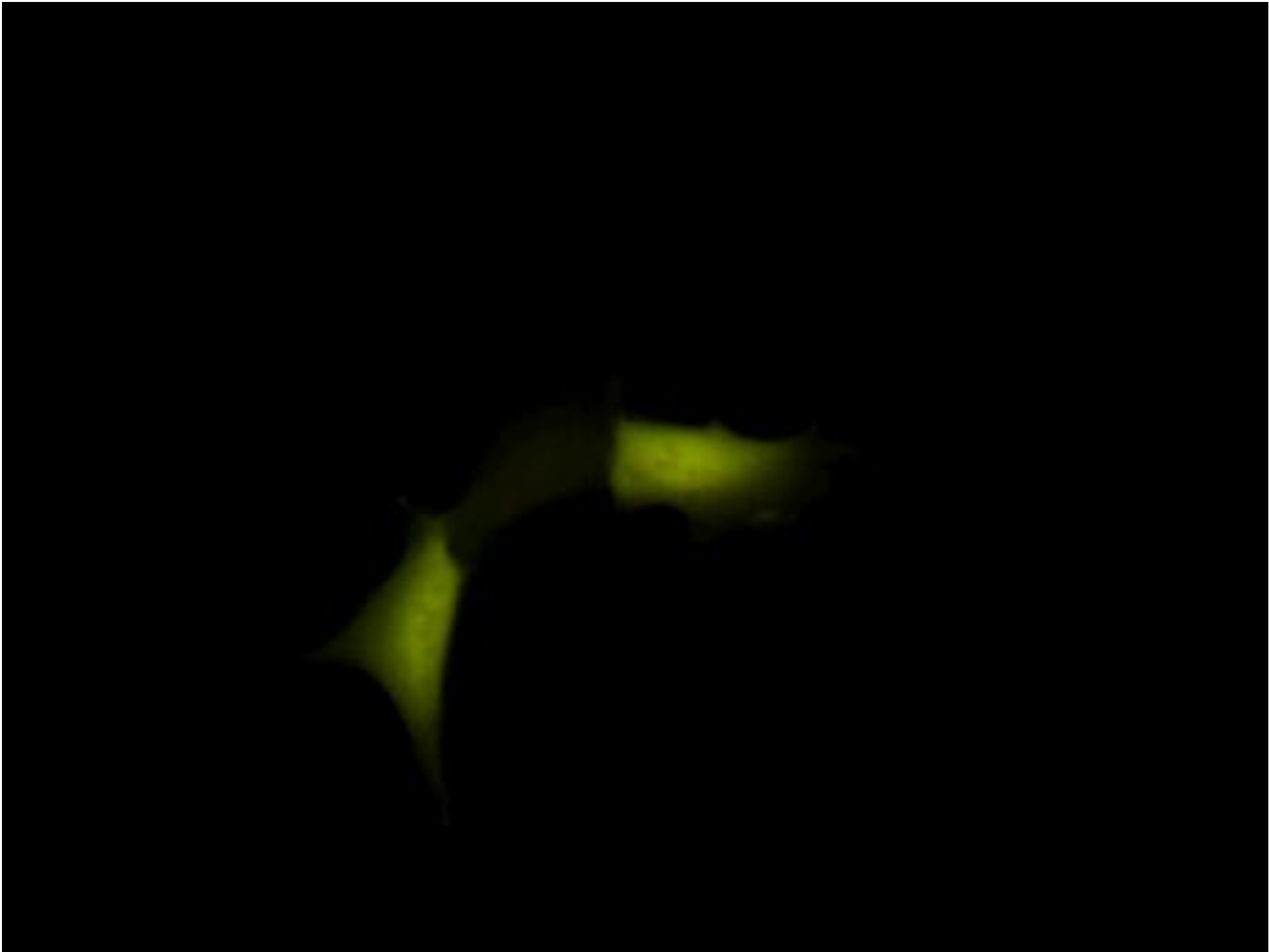


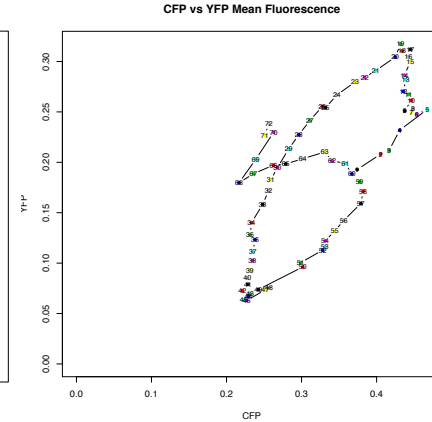
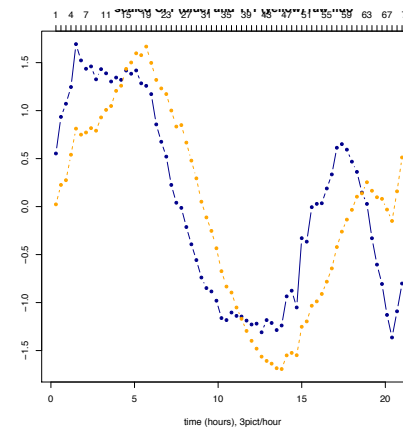
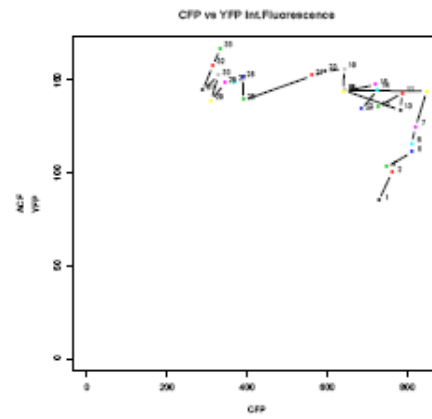
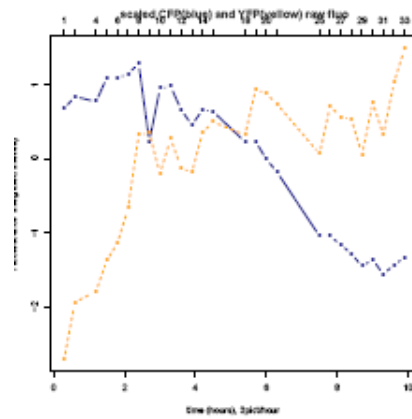
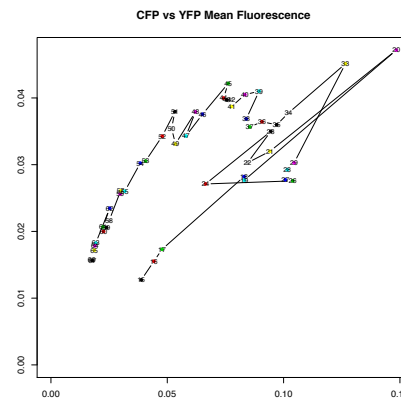
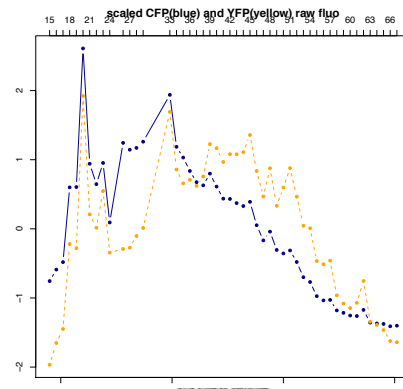
Single-cell heterogeneity is a well-accepted phenomenon but has remained understudied in complex tissues owing to technical limitations of mRNA isolation. We showed using the TIVA tag that CA1 hippocampal neurons in live hippocampal tissue expressed fewer genes overall but had more bimodally expressed genes than hippocampal neurons in culture (Fig. 6), suggesting an important role for the microenvironment in modulating gene expression in cells. Recently, there have been suggestions that variation in expression is in part stochastic, arising from both intrinsic noise (stochastic nature of biochemical reactions) and extrinsic noise (changes in cellular regulatory proteins)⁴. Our data suggest that the ~30% difference in number of genes expressed may be attributable to extrinsic noise. When a neuron is removed



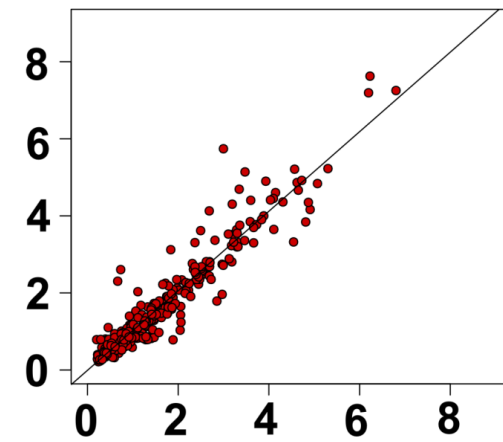
reduced mRNA and protein stability







Correlation of the half-life of the YFP and CFP fluorescent proteins.



hours

Fundamental limits on the suppression of molecular fluctuations

Ioannis Lestas¹, Glenn Vinnicombe¹ & Johan Paulsson²

Life in the cell is a complex battle between randomizing and correcting statistical forces: births and deaths of individual molecules create spontaneous fluctuations in abundances¹⁻⁴—noise—and many control circuits have evolved to eliminate, tolerate or exploit the noise⁵⁻⁸. The net outcome is difficult to predict because each control circuit in turn consists of probabilistic chemical reaction:

In such systems, the minimal error decreases with the quartic root of the integer number of signalling events, making a decent job 16 times harder than a half-decent job. This perhaps explains why there is so much biochemical noise—correcting it would be too costly—but also constrains other aspects of life in the cell. For example, the noise levels may increase or decrease along signalling cascades, depending on the kinetic details at each step, but information about upstream states is always progressively and irreversibly lost. Although it is tempting to believe that large reaction networks are capable of almost anything if the rates are suitably nonlinear, the opposite perspective may thus be more appropriate: having more steps where one component affects the rates of another creates more opportunities for information to be lost and fundamentally prevents more types of behaviour.

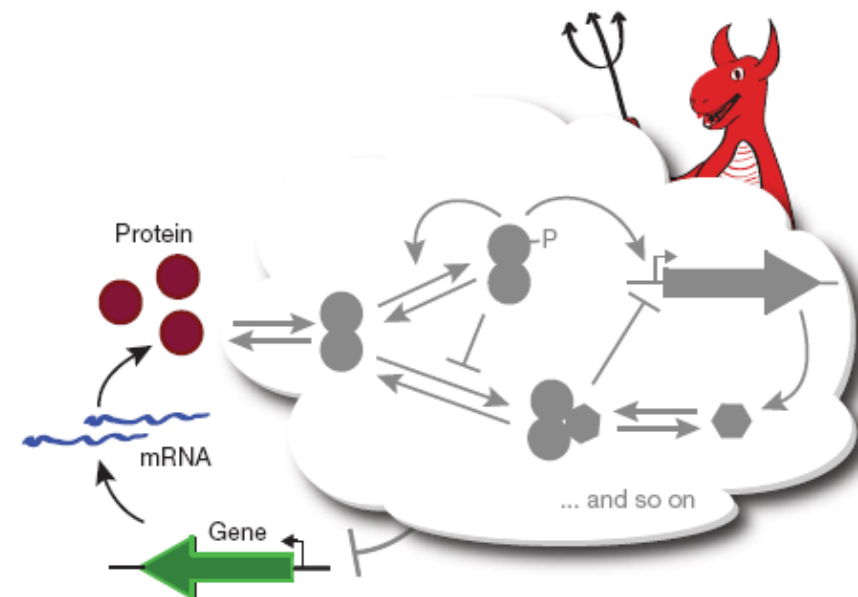
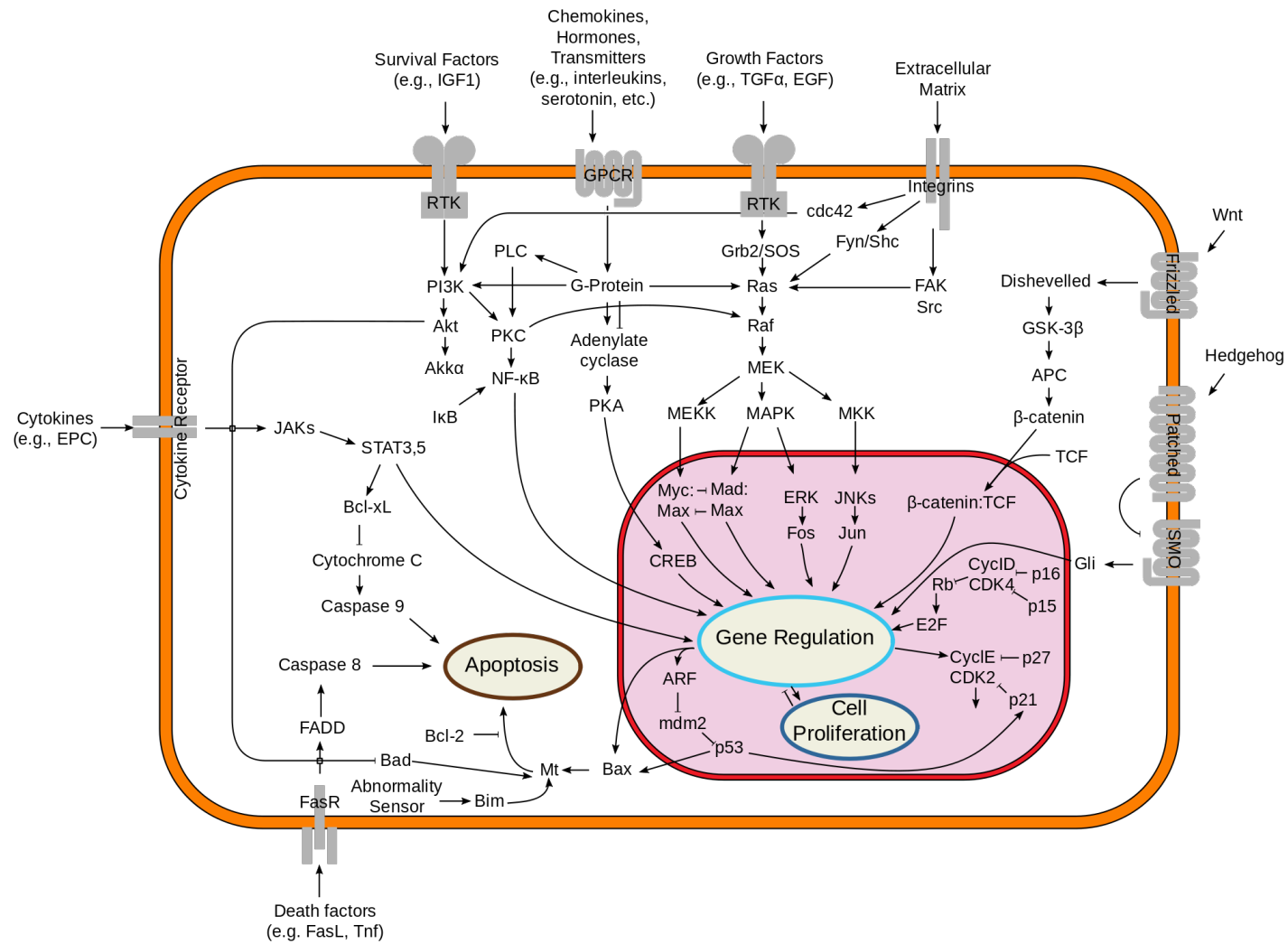


Figure 1 | Schematic of optimal control networks and information loss. Biological networks can be overwhelmingly complex, with numerous feedback loops and signalling steps. Predictions about noise then rely on quantitative estimates for how every probabilistic reaction rate responds to every type of perturbation. To investigate bounds on behaviour, most of the network is here replaced by a ‘control demon’ representing a controller that is optimized over all possible network topologies, rates and mechanisms. The bounds are then calculated in terms of the few specified features.





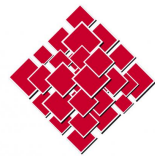
TATA INSTITUTE OF FUNDAMENTAL RESEARCH

Living matter April 16 to April 26

Random walk across the epigenetic landscape Part 2

András Páldi

andras.paldi@ephe.sorbonne.fr



École Pratique
des Hautes Études



1 Order and stability in living systems: a short (and superficial) historical background.

2 Stochasticity in living cells: noise or variation?

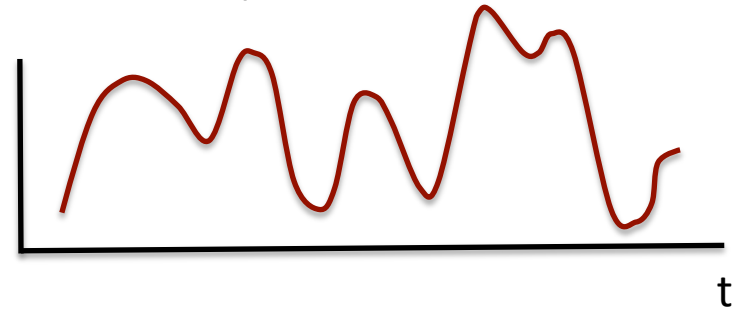
3 How cells function reliably with such an inherent variability in gene expression?

STABILITY/VARIATION

Postulate of stability



Observed phenomenon: variation



Stochasticity and Cell Fate

Richard Losick¹ and Claude Desplan²

Fundamental to living cells is the capacity to differentiate into subtypes with specialized attributes. Understanding the way cells acquire their fates is a major challenge in developmental biology. How cells adopt a particular fate is usually thought of as being deterministic, and in the large majority of cases it is. That is, cells acquire their fate by virtue of their lineage or their proximity to an inductive signal from another cell. In some cases, however, and in organisms ranging from bacteria to humans, cells choose one or another pathway of differentiation stochastically, without apparent regard to environment or history. Stochasticity has important mechanistic requirements. We speculate on why stochasticity is advantageous—and even critical in some circumstances—to the individual, the colony, or the species.

“I, at any rate, am convinced that He does not play dice.”

Albert Einstein, 1926

SCIENCE VOL 320 4 APRIL 2008

Stochastic switching as a survival strategy in fluctuating environments

Murat Acar^{1,2}, Jerome T Mettetal^{1,2} & Alexander van Oudenaarden¹

A classic problem in population and evolutionary biology is to understand how a population optimizes its fitness in fluctuating environments^{1–4}. A population might enhance its fitness by allowing individual cells to stochastically transition among multiple phenotypes, thus ensuring that some cells are always prepared for an unforeseen environmental fluctuation. Here we experimentally explore how switching affects population growth by using the galactose utilization network of *Saccharomyces cerevisiae*. We engineered a strain that

and concentrations of nutrients and toxins. Early theoretical work on this topic often focused on understanding the connection between environmental fluctuations and genetic diversity^{1–4}. However, recent studies demonstrating the importance of phenotypic heterogeneity in genetically identical cells have renewed an interest in studying this problem from the perspective of an isogenic population that is able to express multiple distinct phenotypes^{10–17}. Without the need to sense the environment, cells could ‘blindly’ anticipate and survive environ-

NATURE GENETICS VOLUME 40 | NUMBER 4 | APRIL 2008

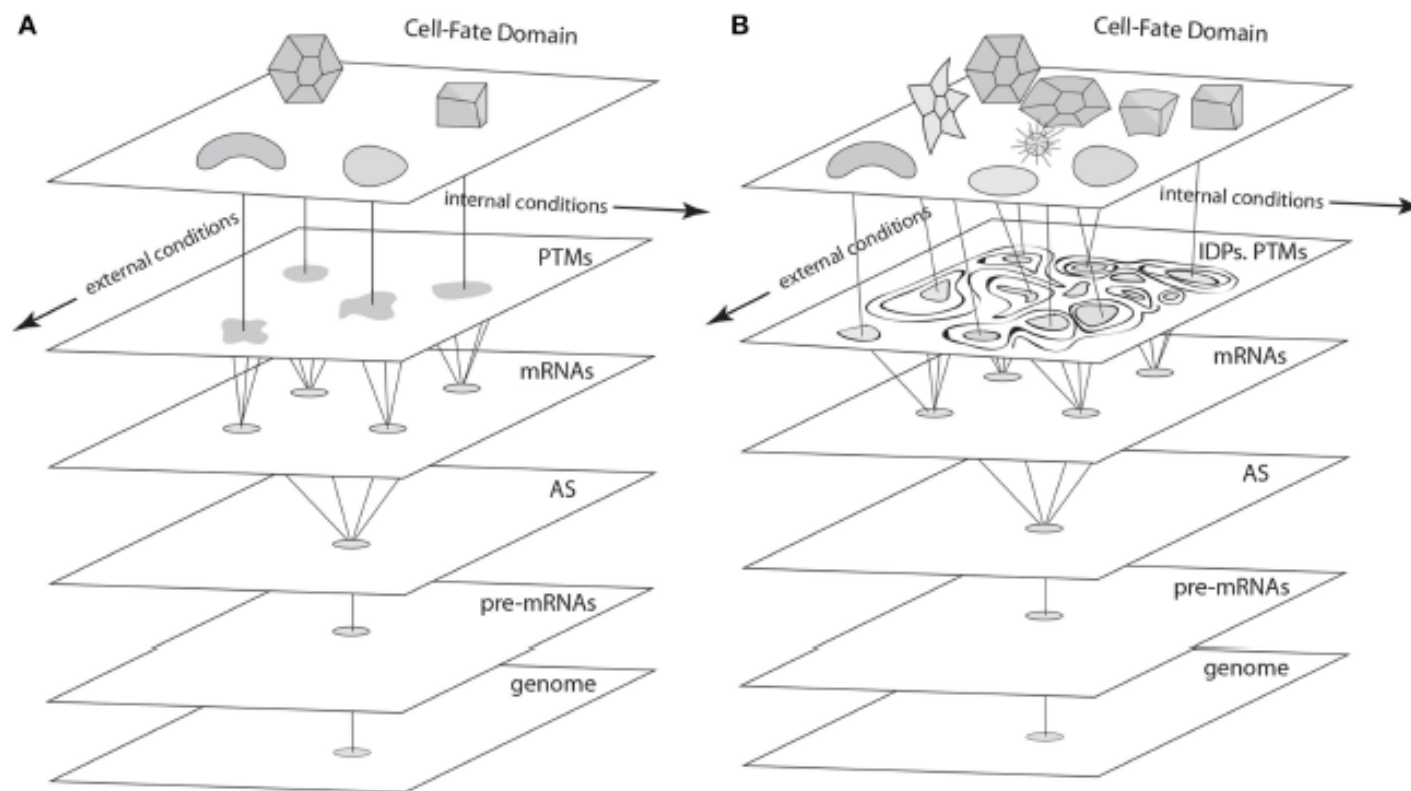


FIGURE 4 | Schematics of cell fate specification viewed from the standard deterministic GRN perspective (A) and the non-deterministic GRN perspective described in the text (B). (A) In the standard view, pre-mRNAs undergo alternative splicing (AS), and transcription factors specified by the variant mRNAs undergo post-translational modifications (PTMs) to form a cadre of proteins involved in cell-fate specification networks (GRNs, represented as irregular shapes) via their cis-acting targets. Discrete cell types result from the deterministic properties of

these GRNs. **(B)** In the proposed non-deterministic view, transcription factors are generated by AS and PTM operating in the context of intrinsically disordered protein (IDP) domains. Cell-fate determination in this case (represented by interactions among components of variable, context-dependent identity and specificity), is a consequence of the time- and spatial-context dependency of each of the levels shown in this schematic, which depend on internal and external cellular conditions in a fashion that eludes deterministic description at the level of GRNs.



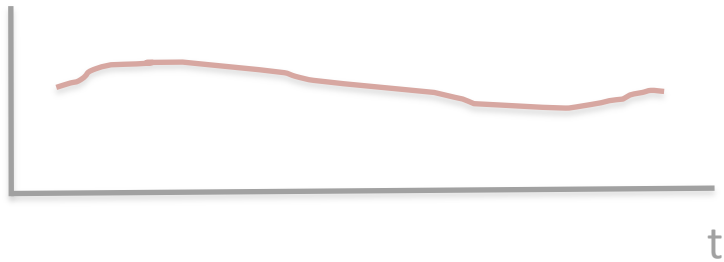
Rethinking gene regulatory networks in light of alternative splicing, intrinsically disordered protein domains, and post-translational modifications

Karl J. Niklas^{1*}, Sarah E. Bondos², A. Keith Dunker³ and Stuart A. Newman⁴

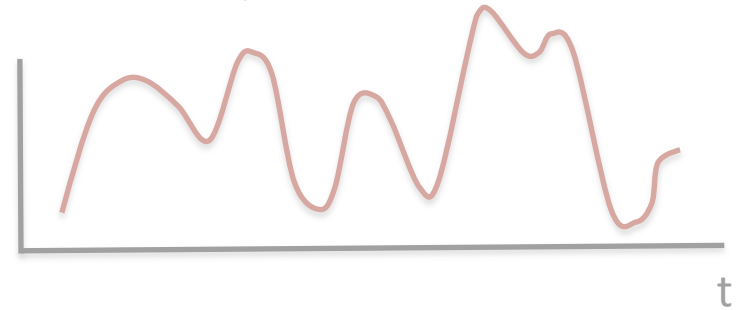
These are particular examples that explain only a small subset of observed cases!

STABILITY/VARIATION

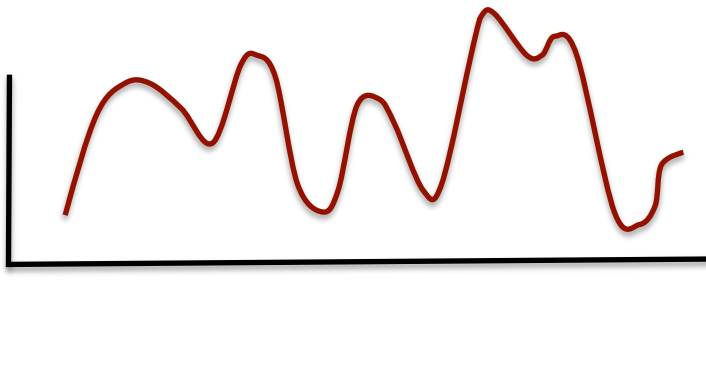
Postulate of stability



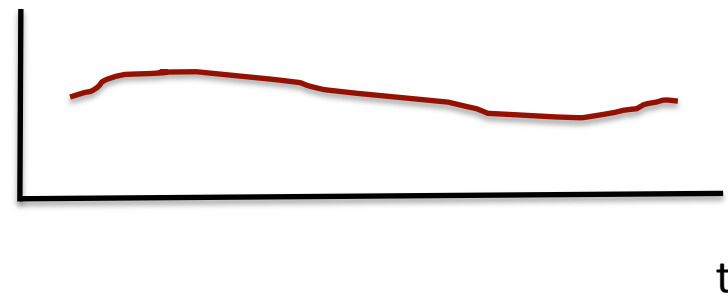
Observed phenomenon: variation



Postulate of variation



Observed phenomenon: stability



How cells function reliably with such an inherent variability of biochemical reactions (i.e. gene expression)?

How cells function reliably with such an inherent variability of biochemical reactions (i.e. gene expression)?

Spatio-temporal averaging

How cells function reliably with such an inherent variability of biochemical reactions (i.e. gene expression)?

‘ ‘All [the] epistemological value of the theory of probability is based on this:
large scale random phenomena in their collective action create strict, non random regularity’ ’ .

(From: B.V. Gnedenko and A.N. Kolmogorov,
Limit Distributions for Sums of Independent Random Variables,
Reading, Ma: Addison-Wesley, 1954).

How cells function reliably with such an inherent variability of biochemical reactions (i.e. gene expression)?

“The non-physicist finds it hard to believe that really the ordinary laws of physics, which he regards as the prototype of inviolable precision, should be based on the statistical tendency of matter to go over into disorder.”

Erwin Schrödinger, What is life?

Quantitative Imaging of Transcription in Living *Drosophila* Embryos Links Polymerase Activity to Patterning

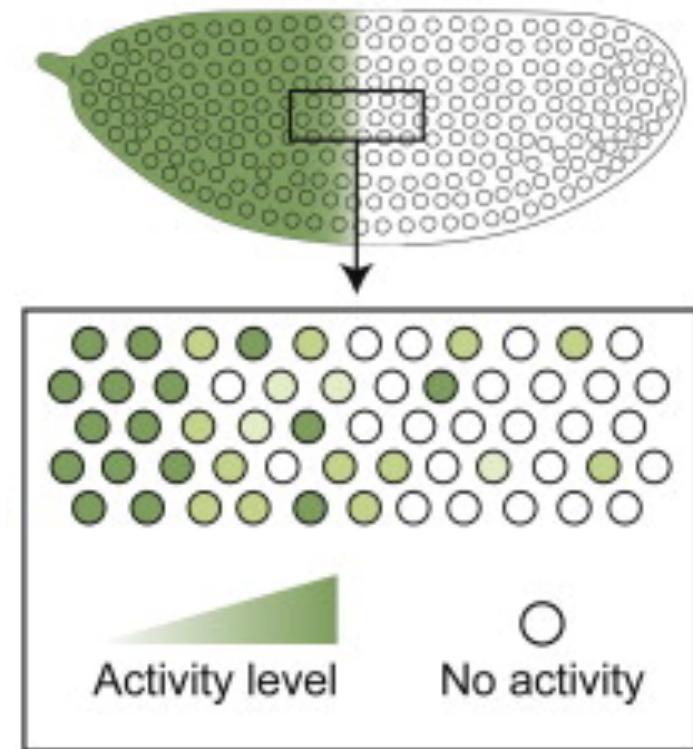
Hernan G. Garcia,¹ Mikhail Tikhonov,^{1,2} Albert Lin,¹
and Thomas Gregor^{1,2,*}

¹Joseph Henry Laboratories of Physics, Princeton University,
Princeton, NJ 08544, USA

²Lewis-Sigler Institute for Integrative Genomics,
Princeton University, Princeton, NJ 08544, USA

Current Biology 23, 2140–2145, November 4, 2013

of the dynamic range of the expression boundary. This amplification is accomplished by nuclei randomly adopting active or inactive states of transcription, leading to a collective effect where the fraction of active nuclei is modulated in space. Thus, developmental patterns are not just the consequence of reproducible transcriptional dynamics in individual nuclei, but are the result of averaging expression over space and time.



Precise Developmental Gene Expression Arises from Globally Stochastic Transcriptional Activity

Shawn C. Little,^{1,4} Mikhail Tikhonov,^{2,3,4} and Thomas Gregor^{2,3,*}

¹Department of Molecular Biology, Howard Hughes Medical Institute

These regions thereby reveal the greatest degree of precision achievable by the system. We show that in these regions, the earliest expressed genes share common expression characteristics: despite their expression in spatially distinct territories, their rates of production are identical, and all display intrinsically stochastic transcriptional activity. These similarities suggest that expression rate and variability result from fundamental, global features of transcriptional regulation that limit the attainable degree of precision. Nevertheless, the stochastic expression results in precise and nearly uniform transcript accumulation, achieved by straightforward spatiotemporal averaging.

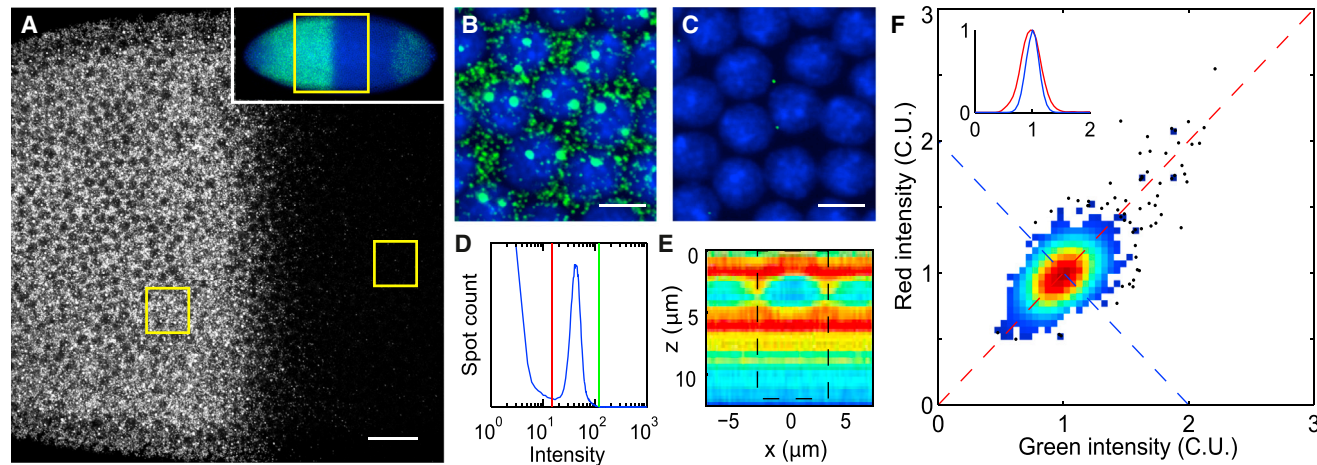


Figure 1. Counting of Absolute Transcript Number in *Drosophila* Embryos

How cells function reliably with such an inherent variability of biochemical reactions (i.e. gene expression)?

Epigenetics: the branch of biology which studies the causal interactions between genes and their products which bring the phenotype into being.

Epigenesys + **Genetics**

Process of change

Stability

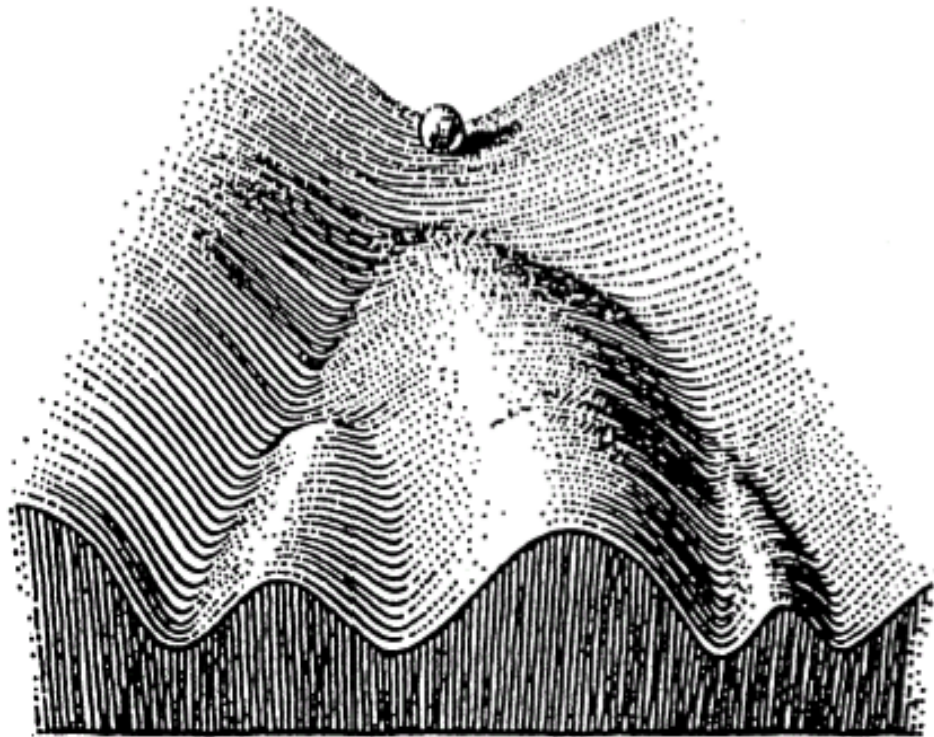
Development

Heredity

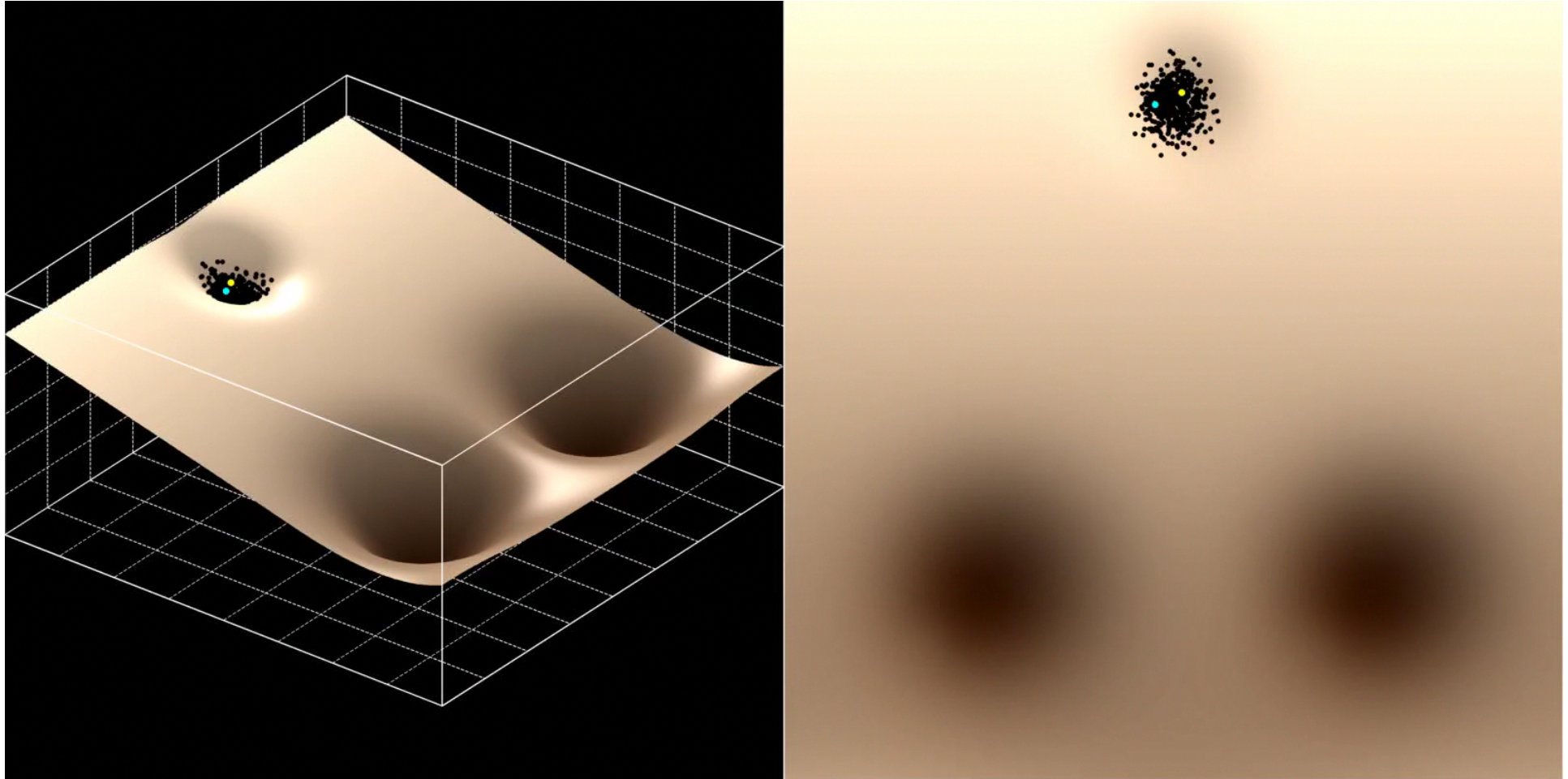


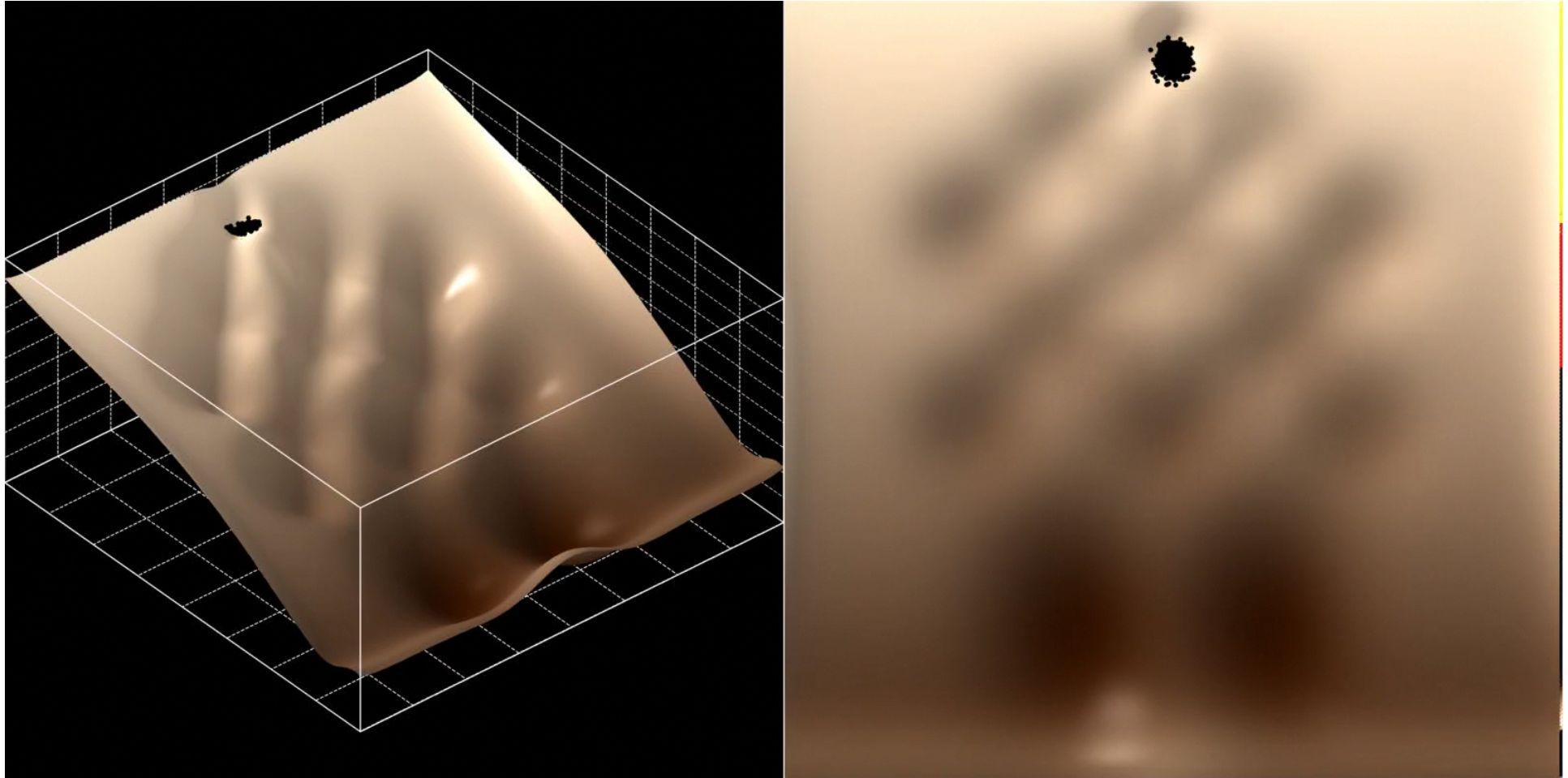
C. Waddington (1942)

Epigenetics: the branch of biology which studies the causal interactions between genes and their products which bring the phenotype into being.



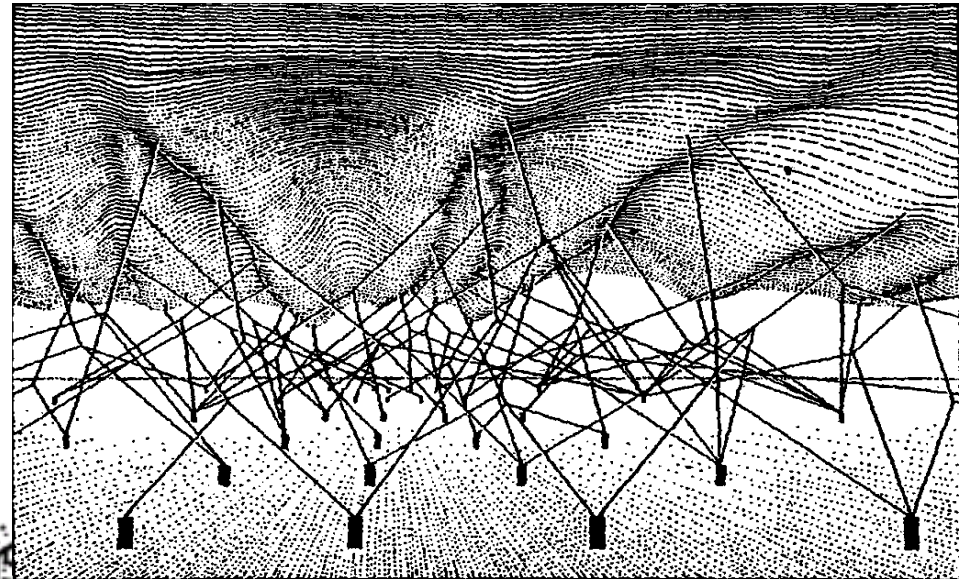
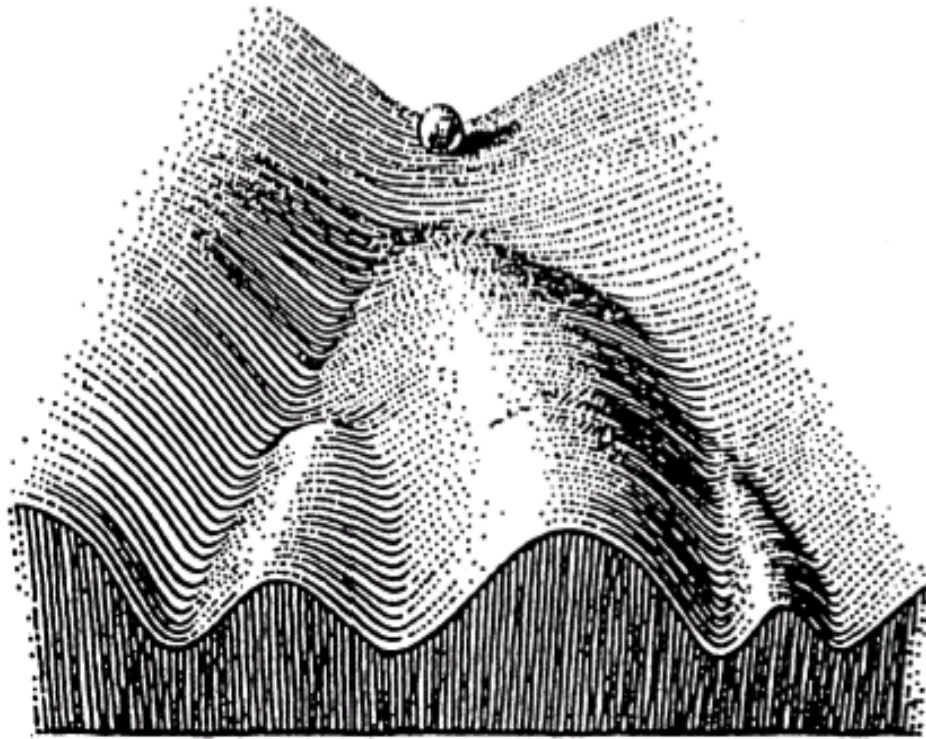
C. Waddington (1942)





Epigenetics

C. Waddington (1942)



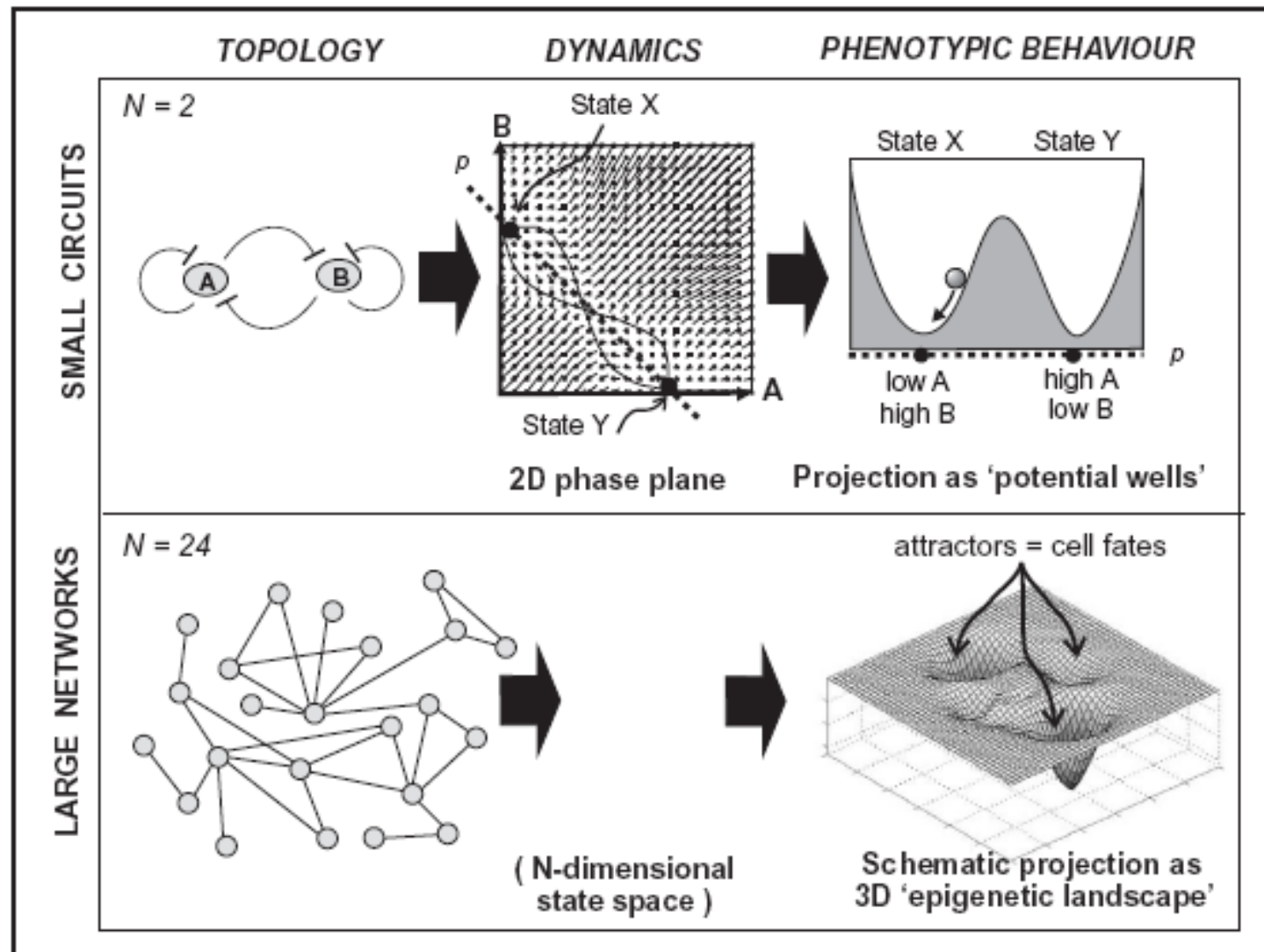
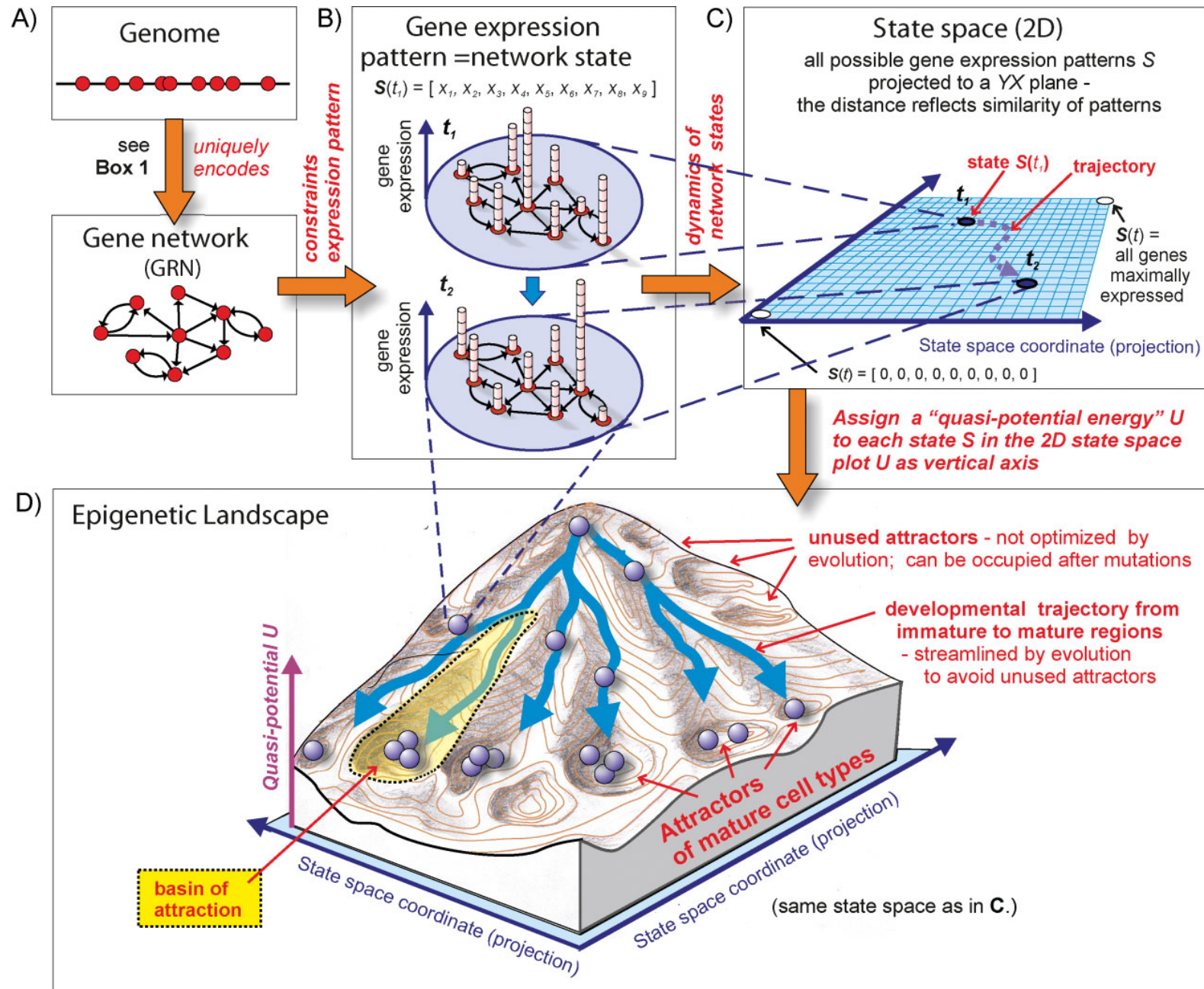
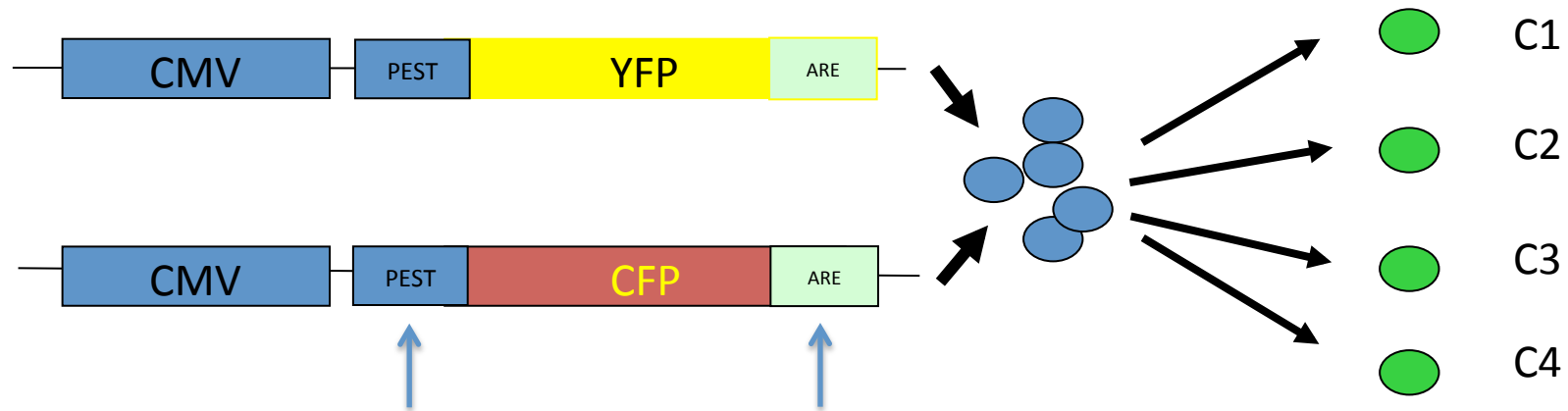


Figure 3: From topology to dynamics; illustrated for a small circuit and a large network. *Top panel:* Small circuit (signalling module) consisting of two proteins A and B, which are mutually inhibitory, and promote their own decay. For a wide range of kinetic parameters, this topology gives rise to bistability. The middle diagram shows a phase plane (two-dimensional state space)

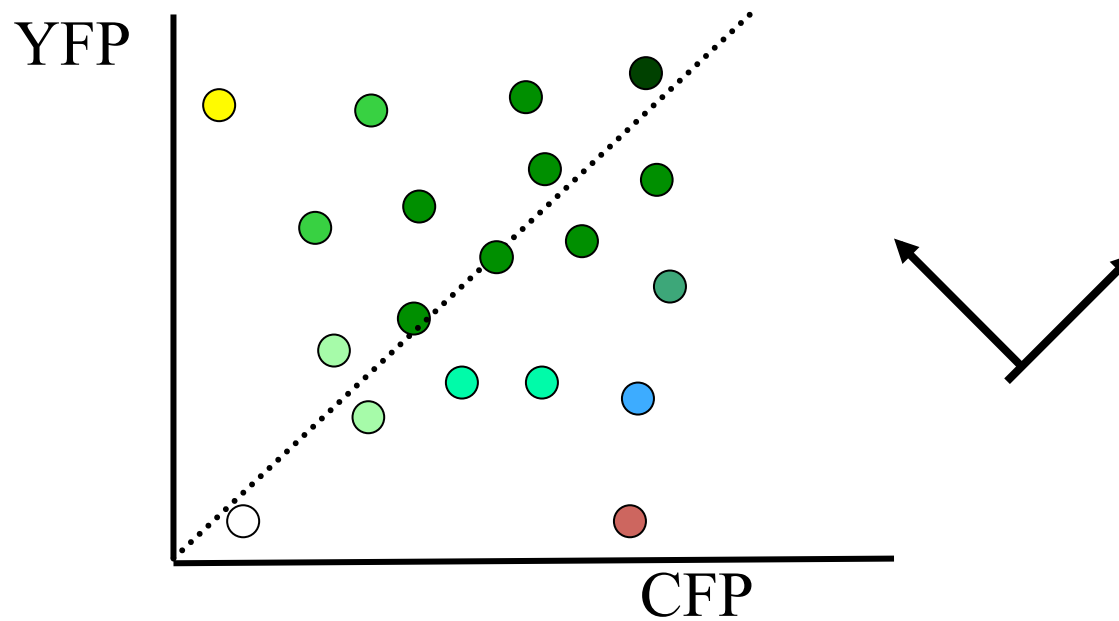


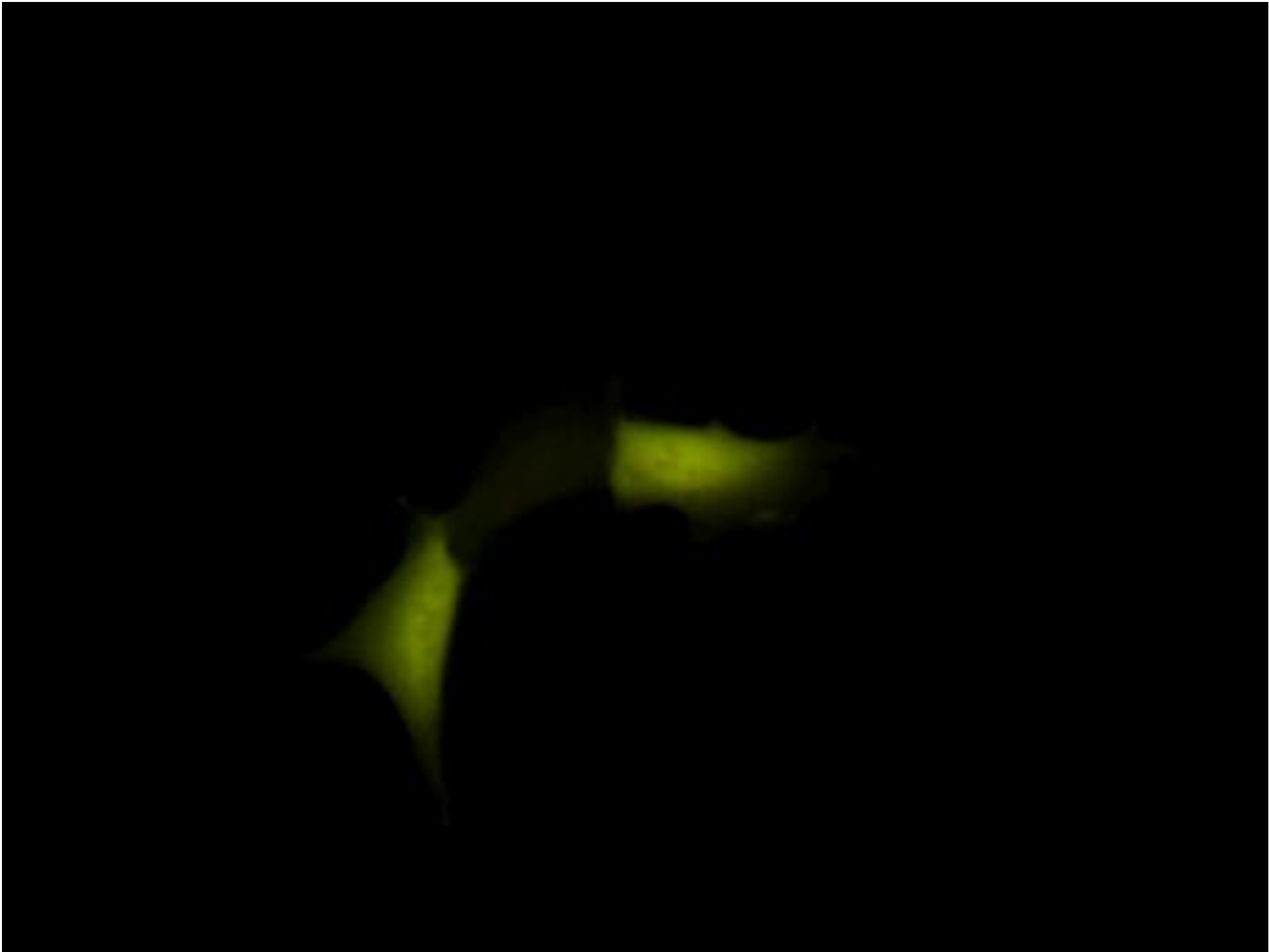
How interactions in the network state can stabilize the fluctuations?

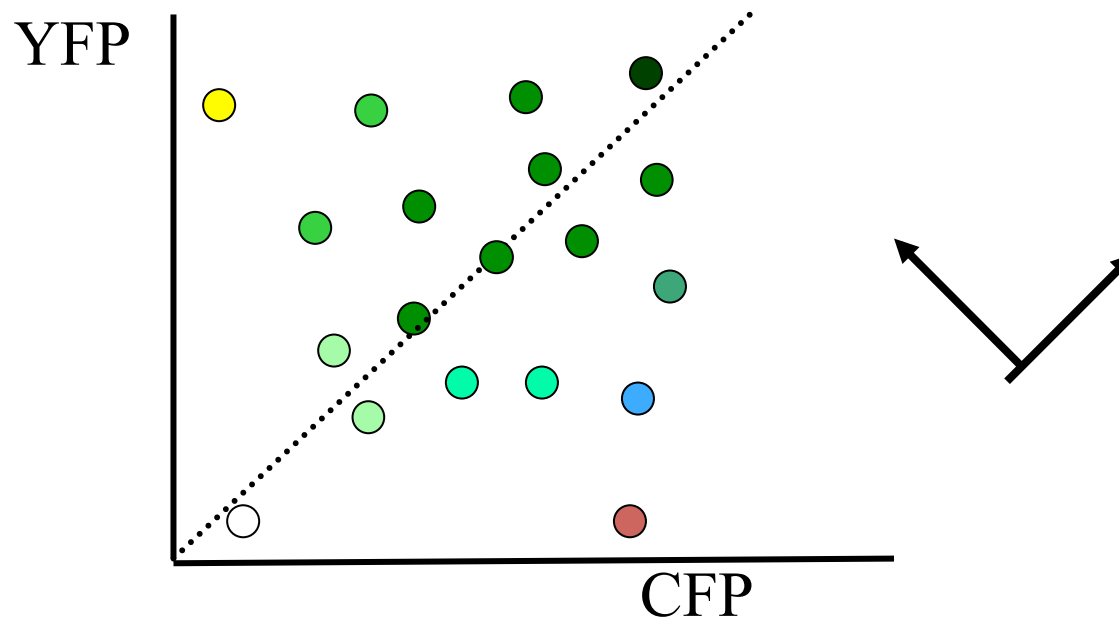
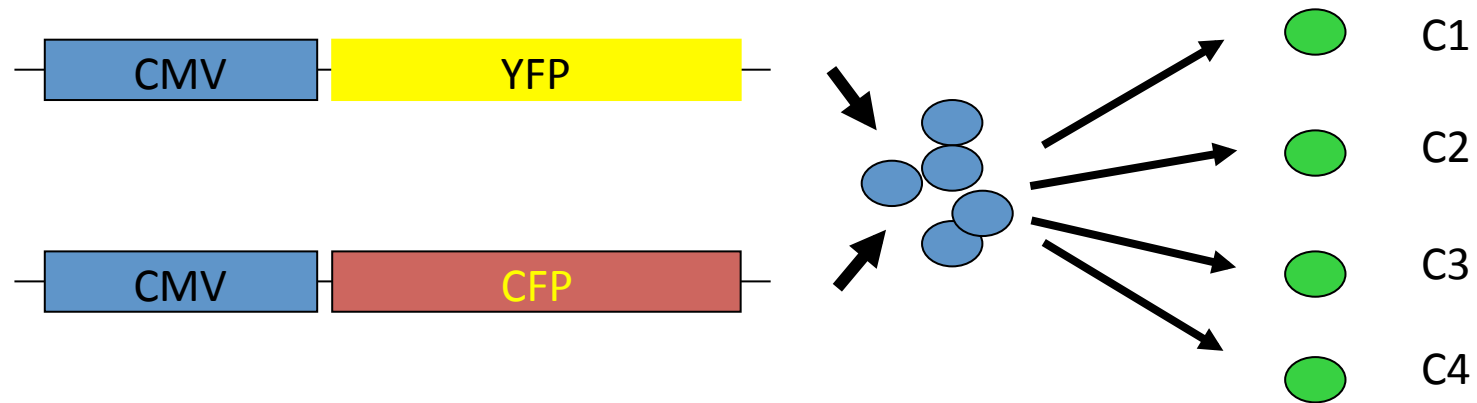
Example:

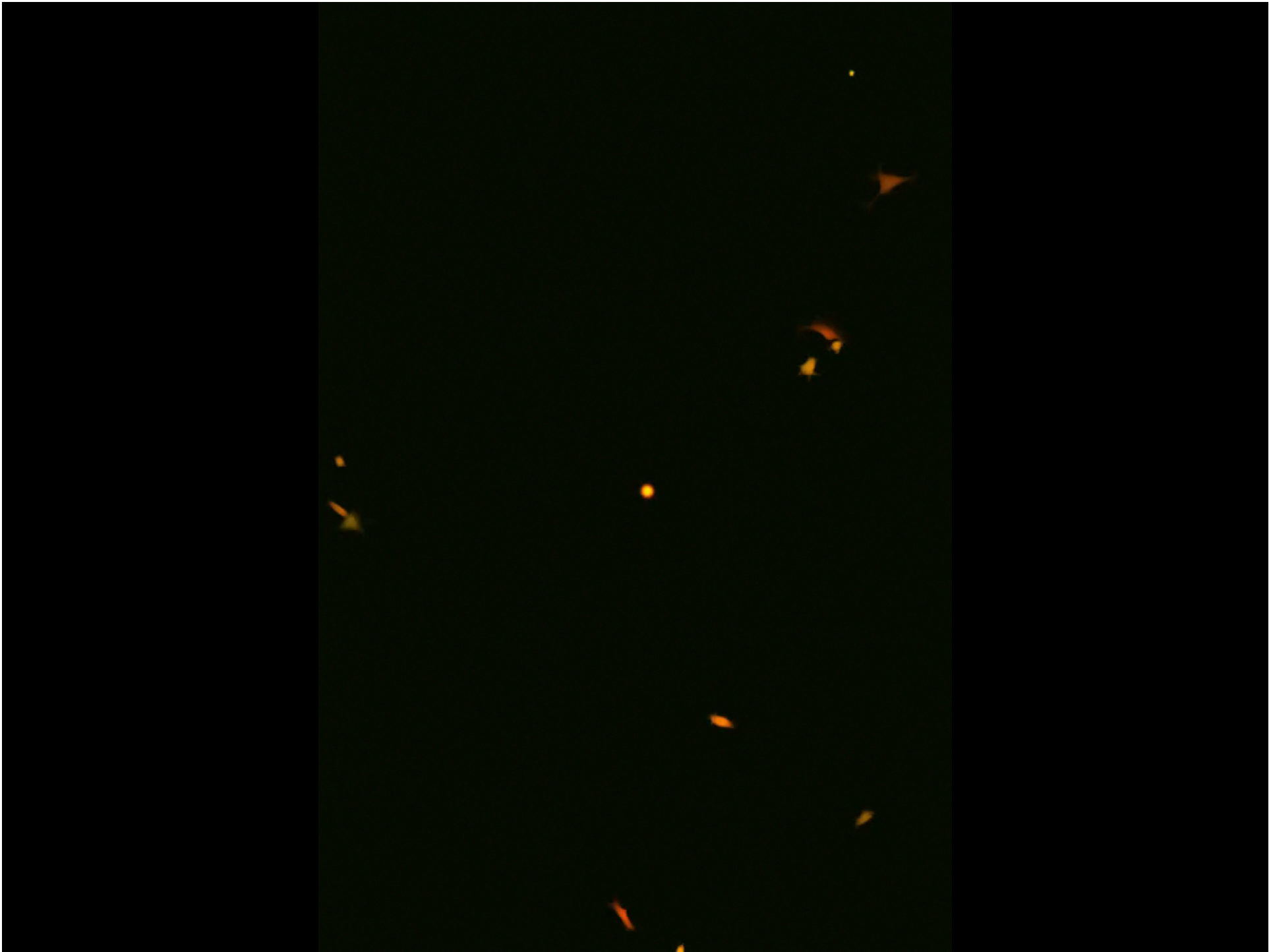


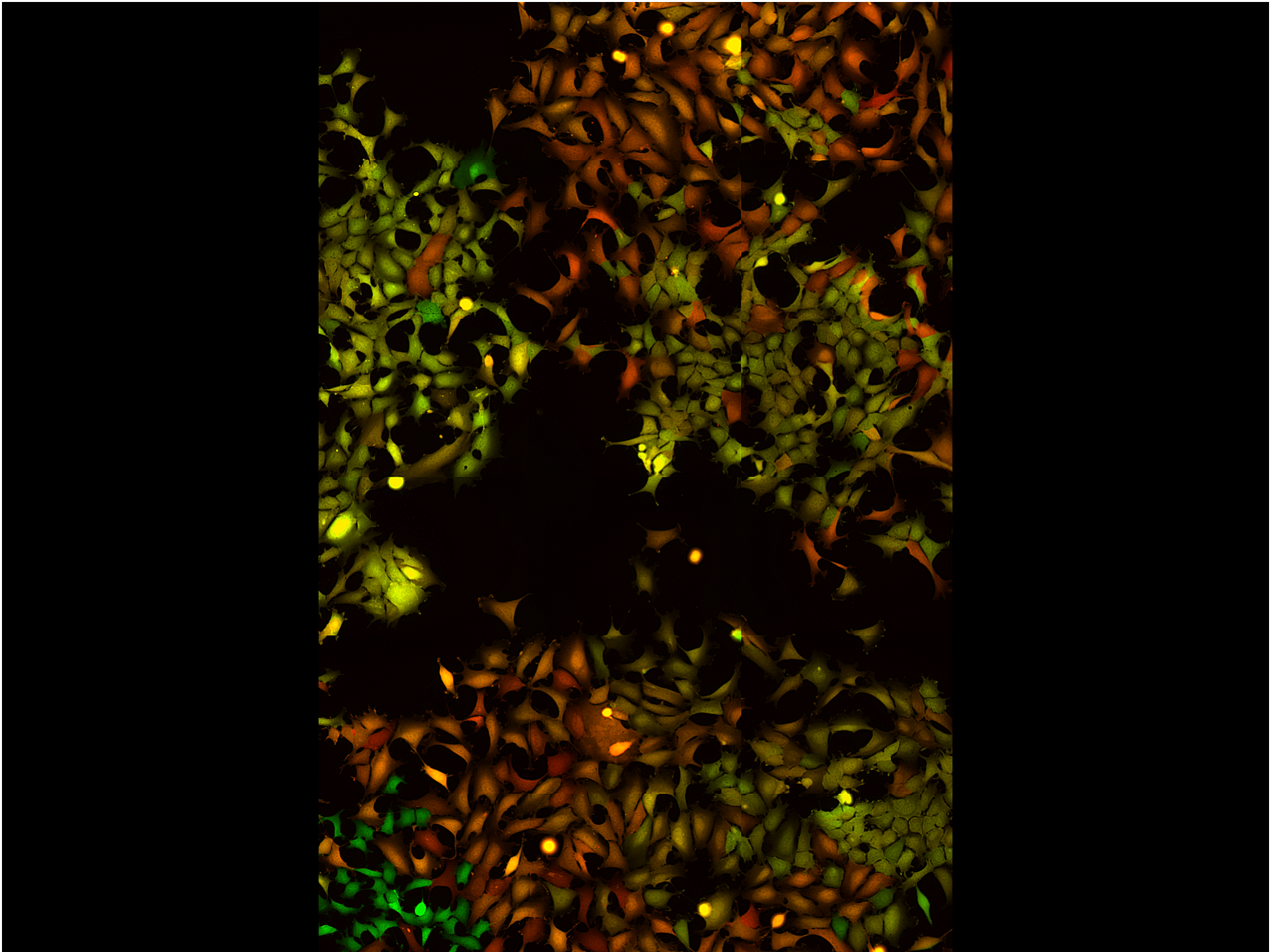
reduced mRNA and protein stability







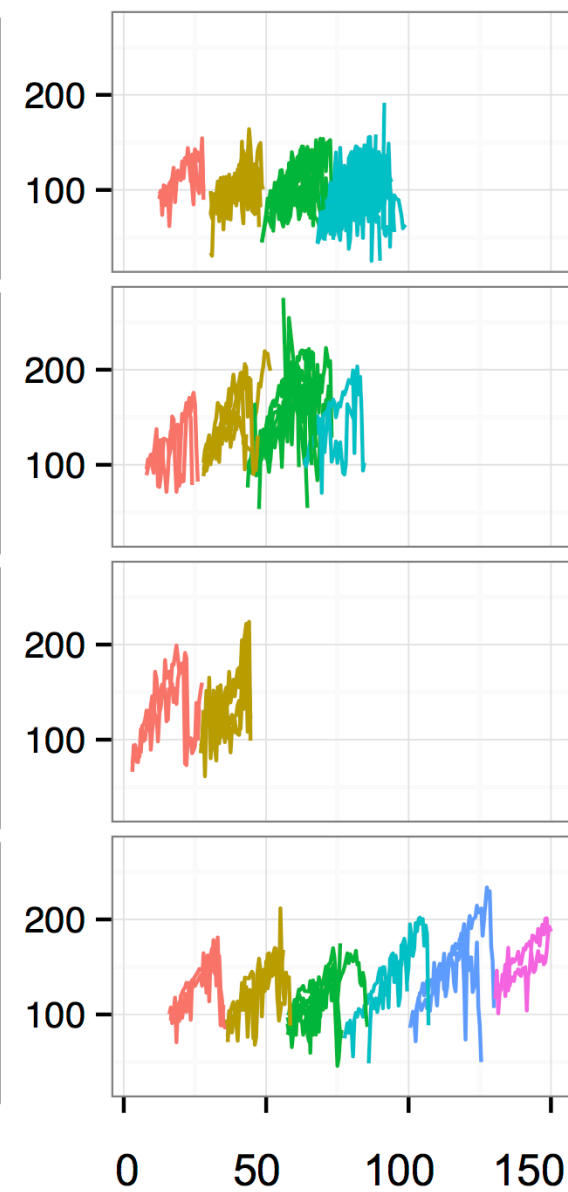
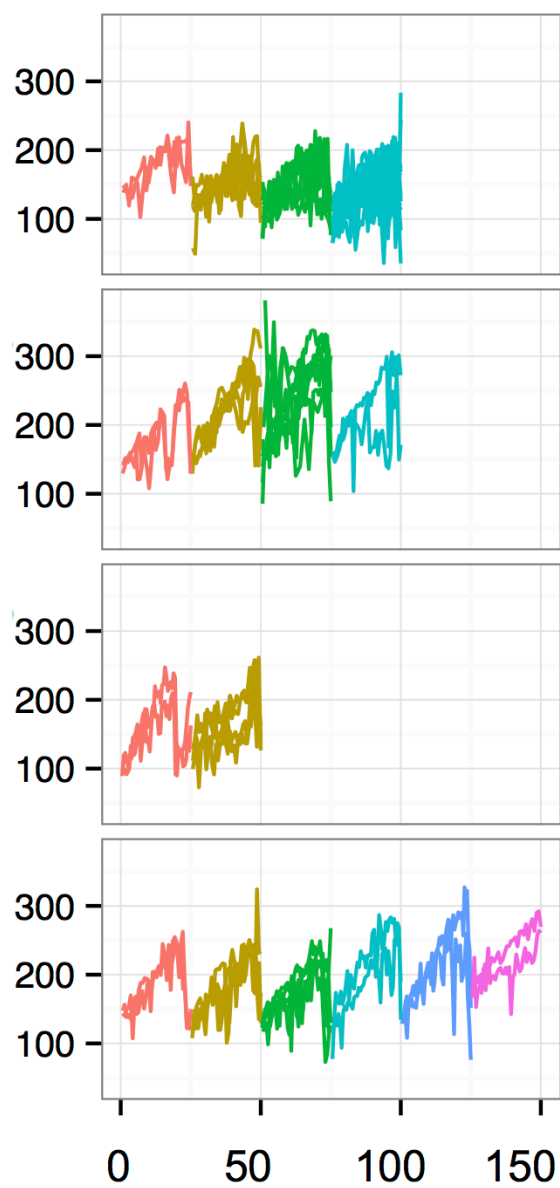




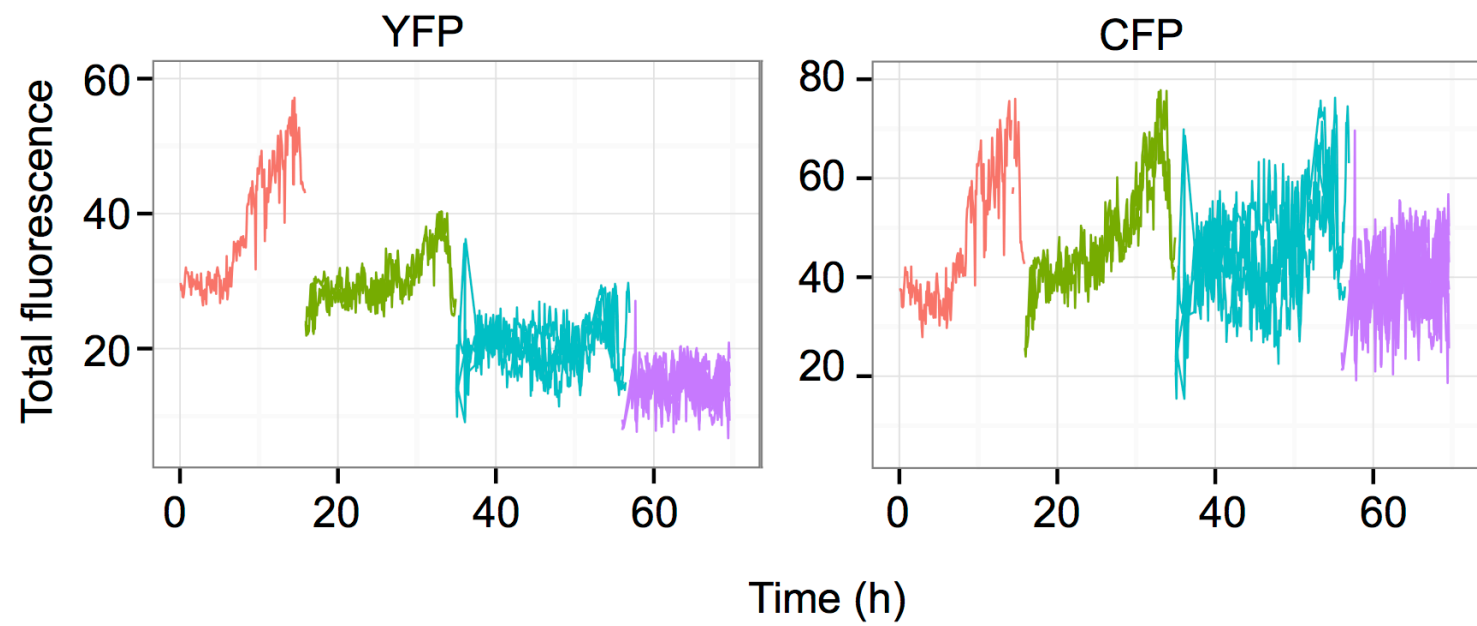
Fluorescence Intensity

CFP

YFP

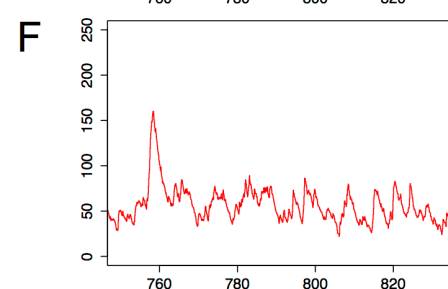
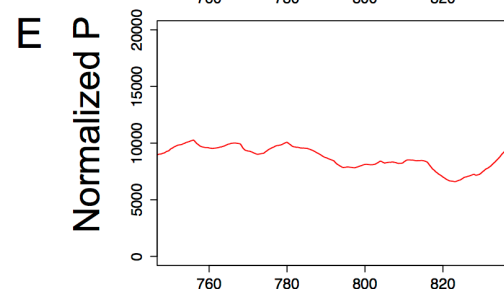
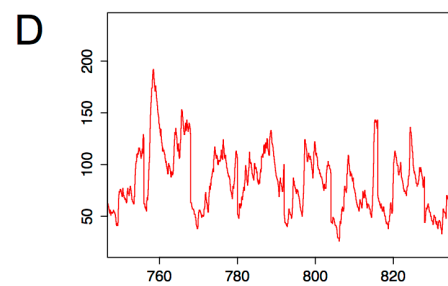
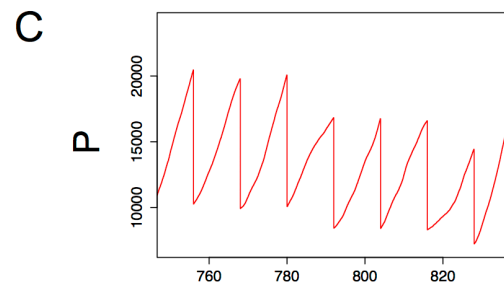
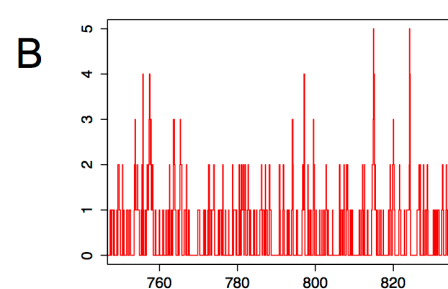
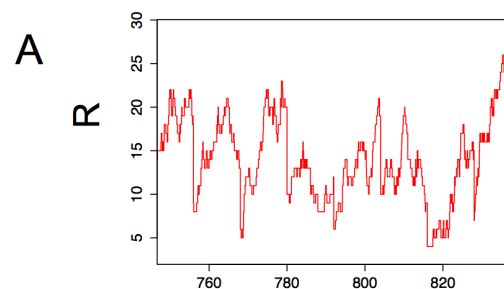


Time (h)



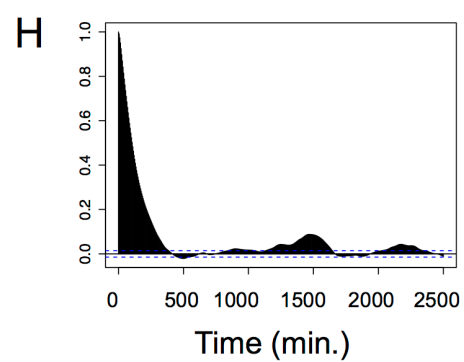
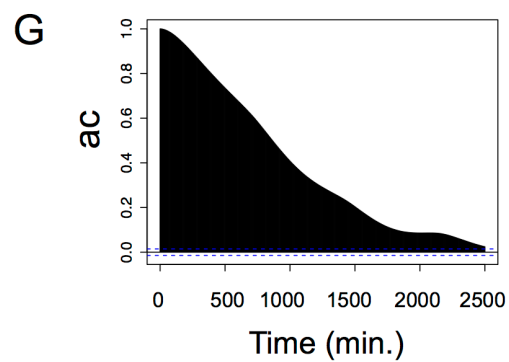
Stable

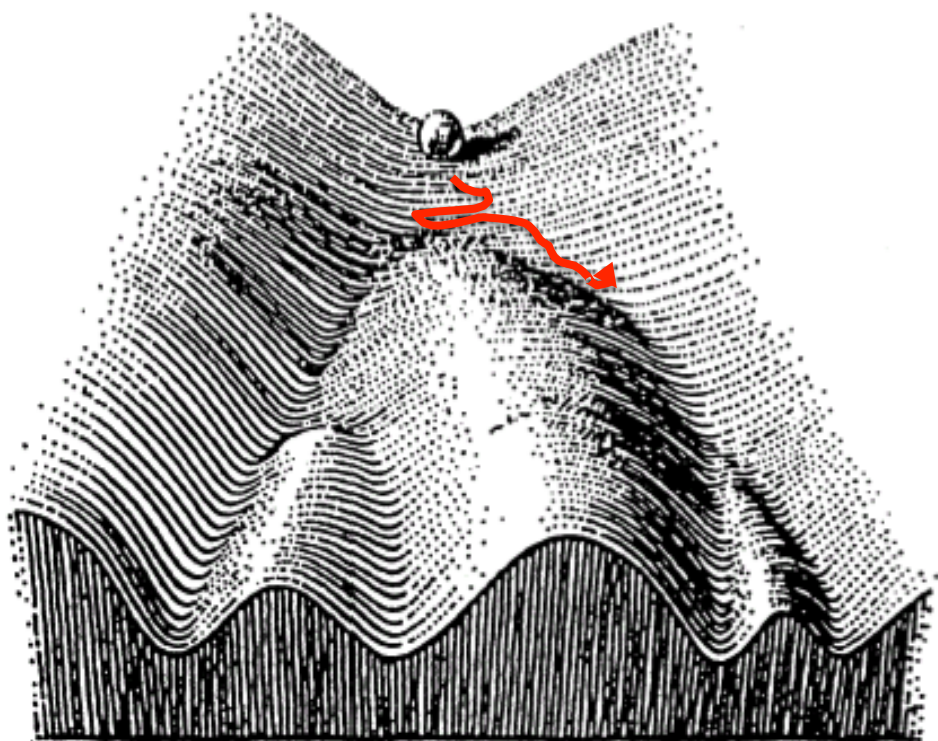
Unstable

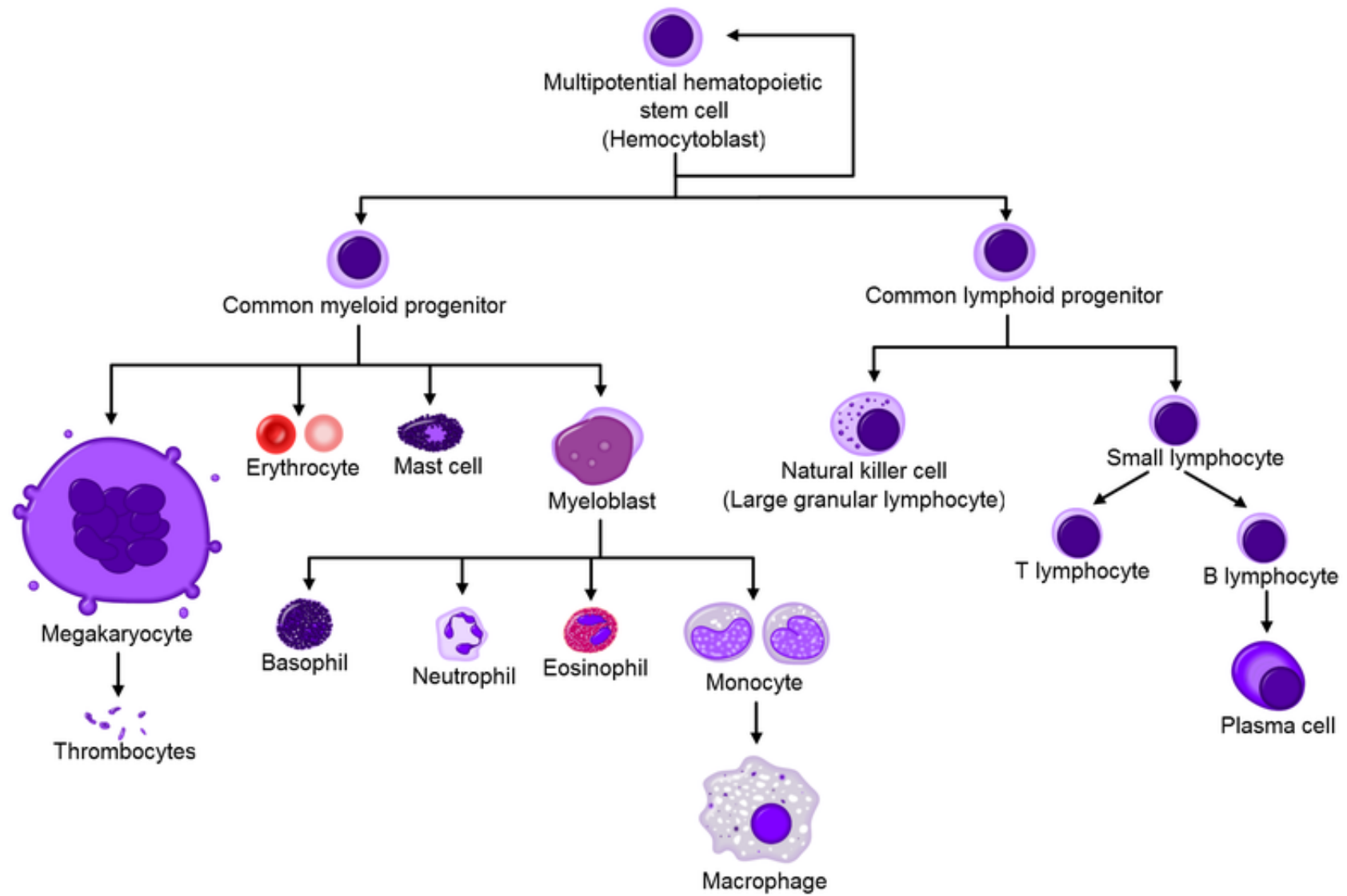


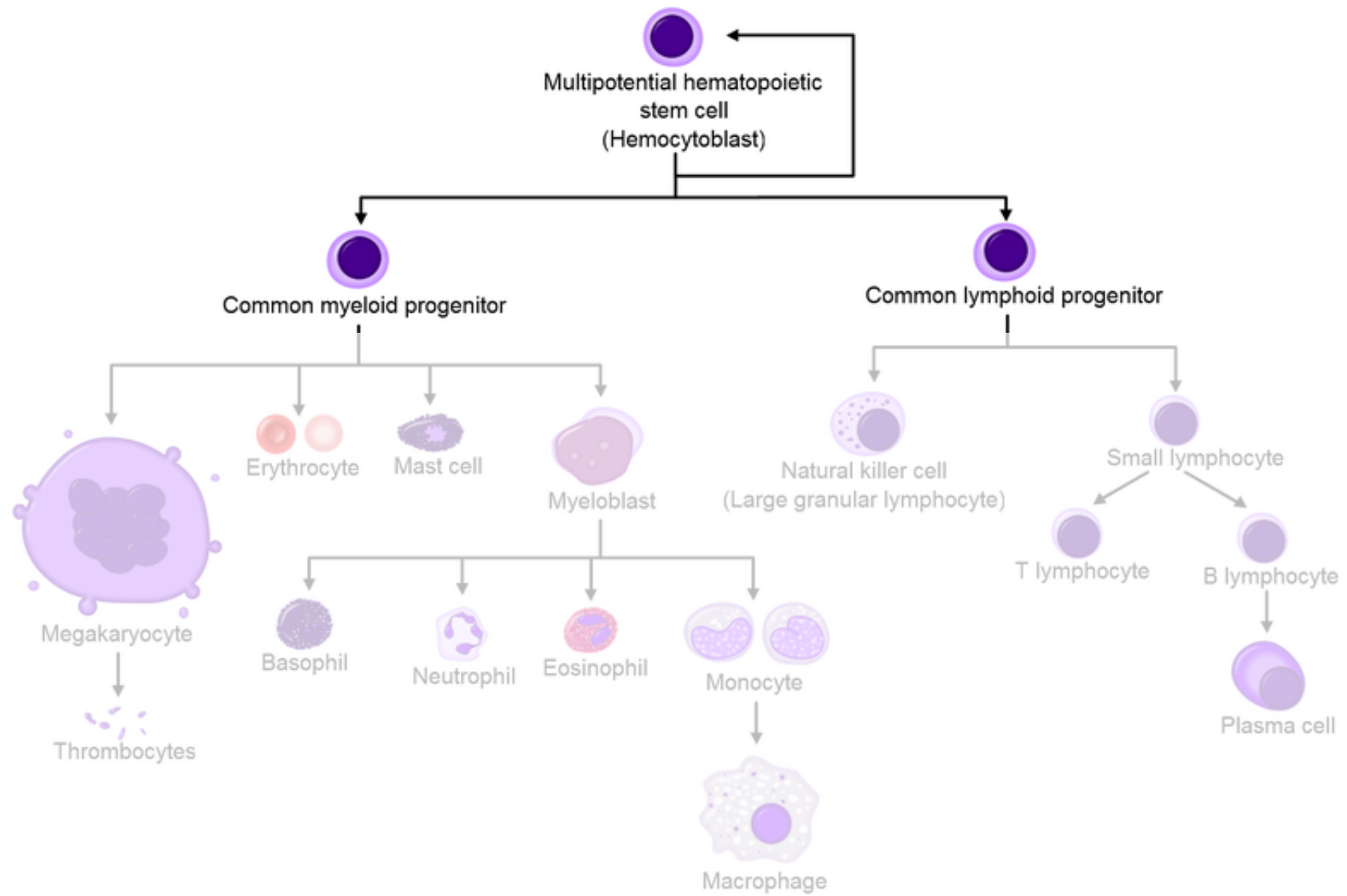
Time (h)

Time (h)

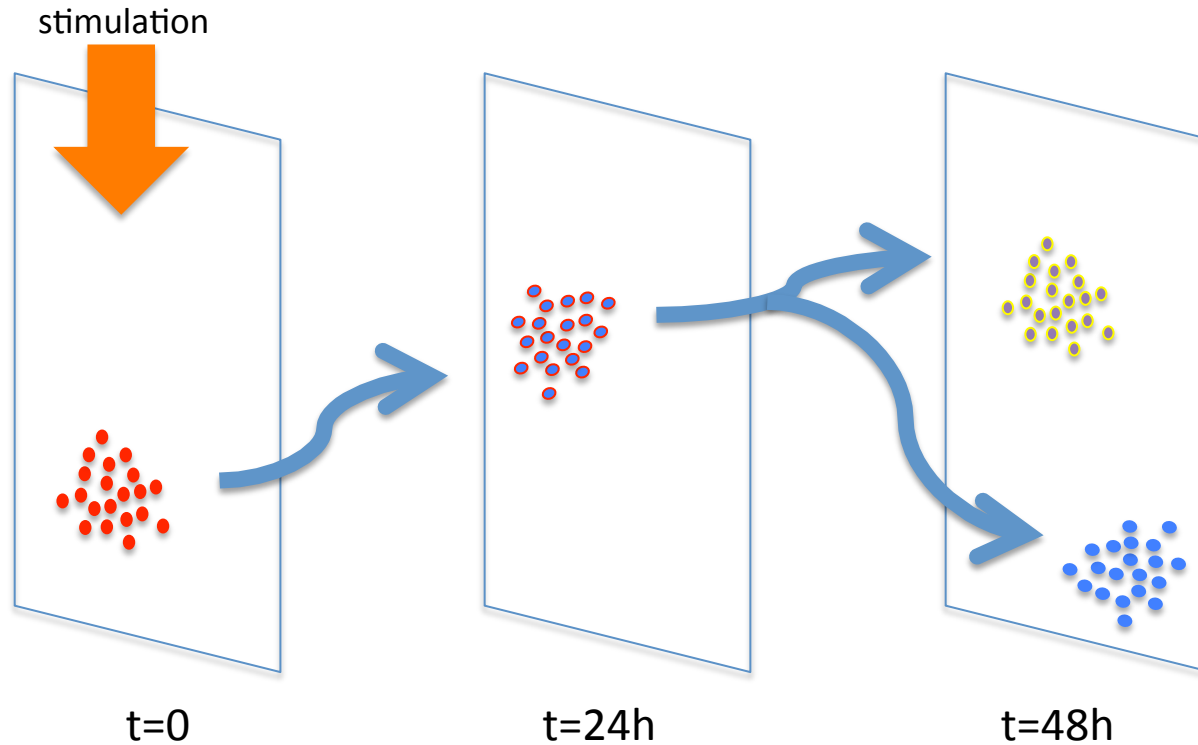






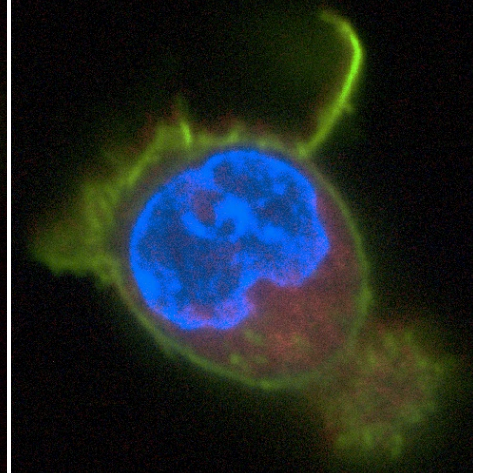
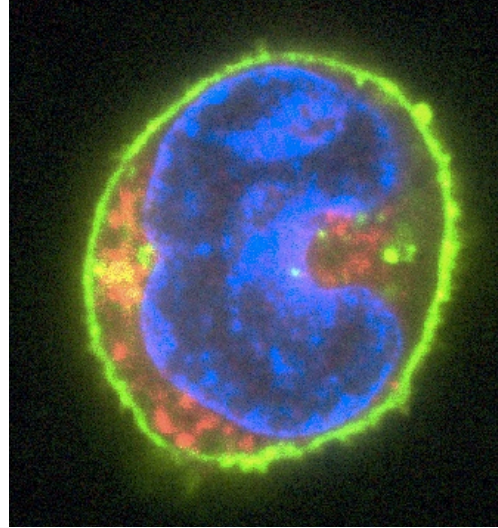
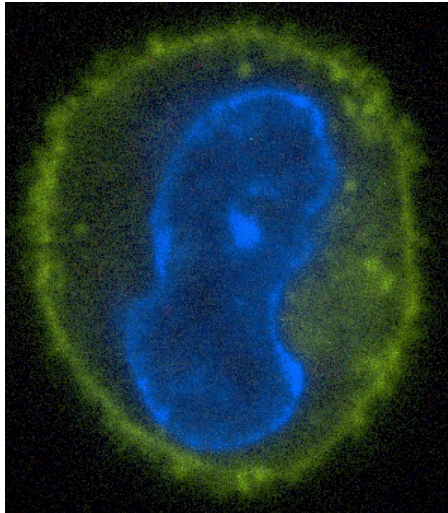
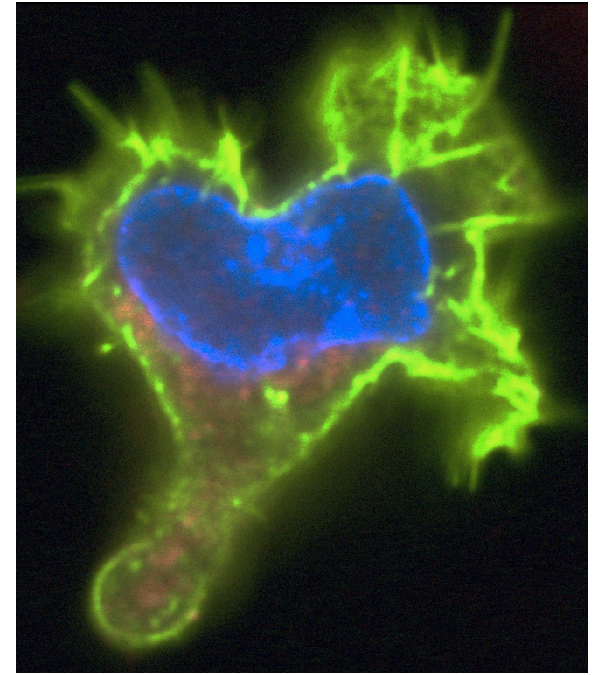
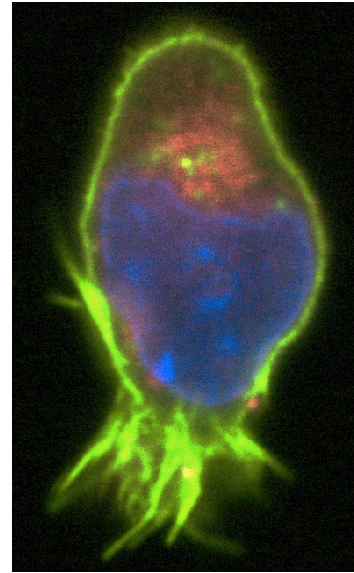
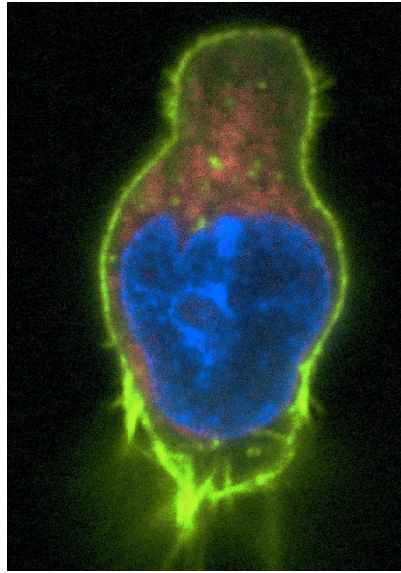
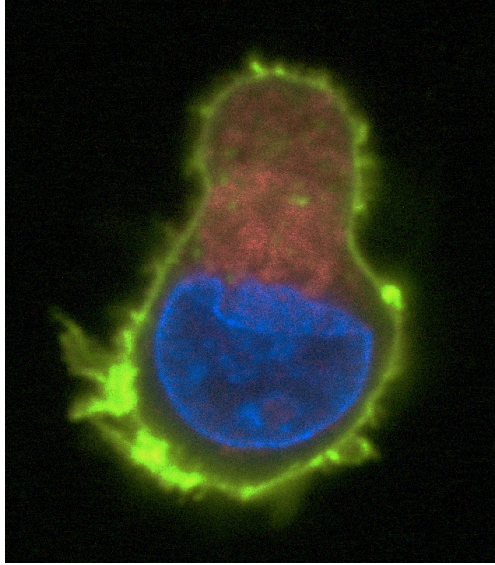


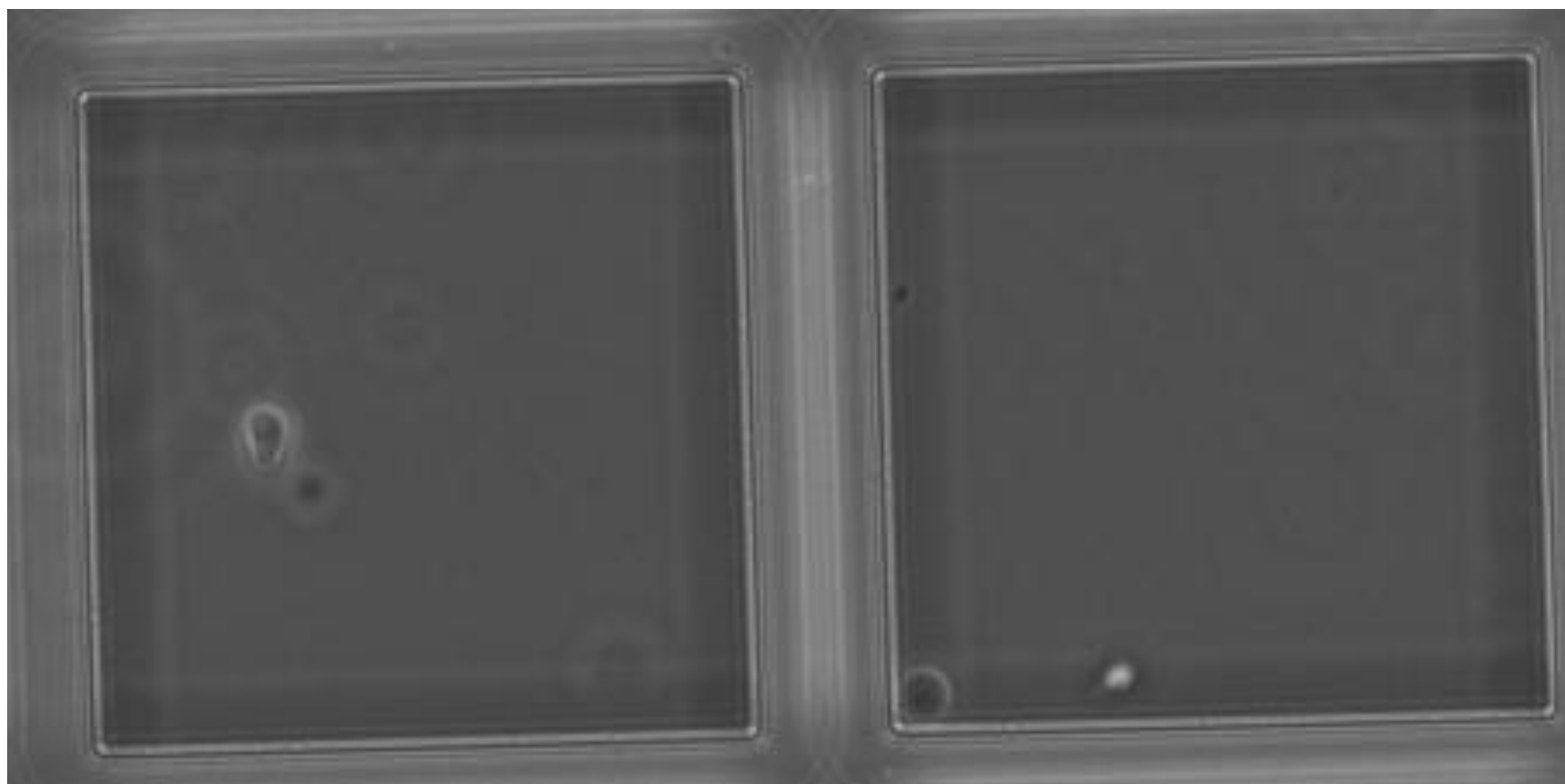
Evolution of single cell gene expression patterns

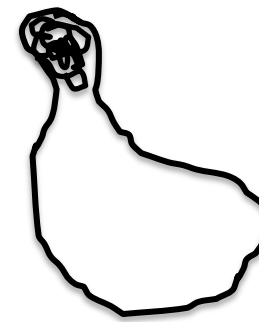
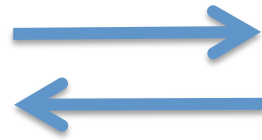
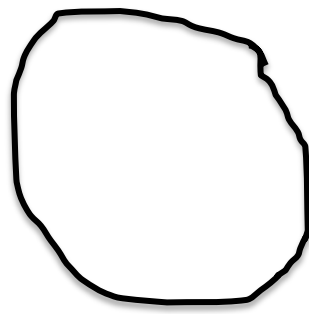


Multiprimed
stage:
simultaneous
expression of
lineage-
associated genes

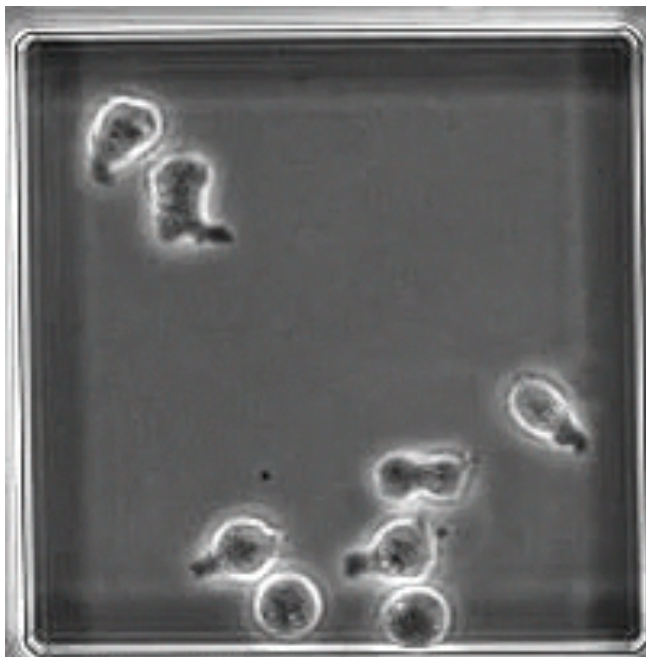
Exit from multiprimed and transition to two
distinct profiles



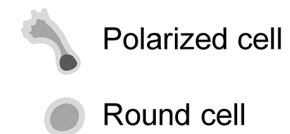
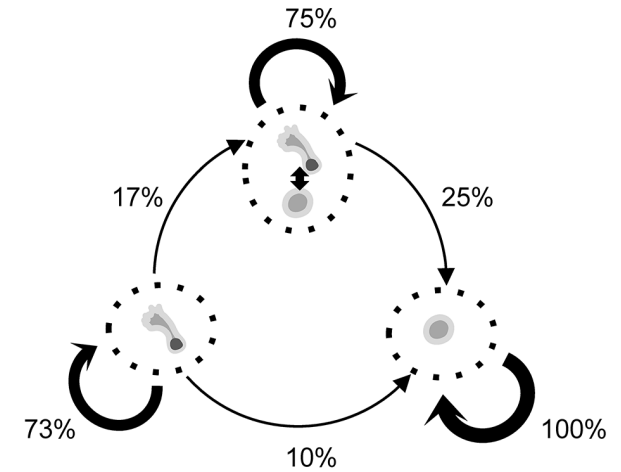




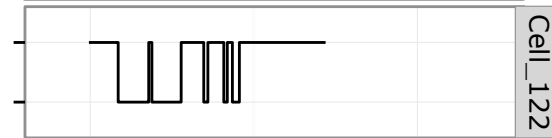
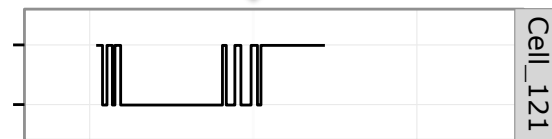
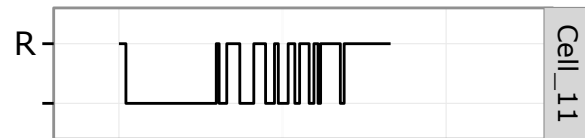
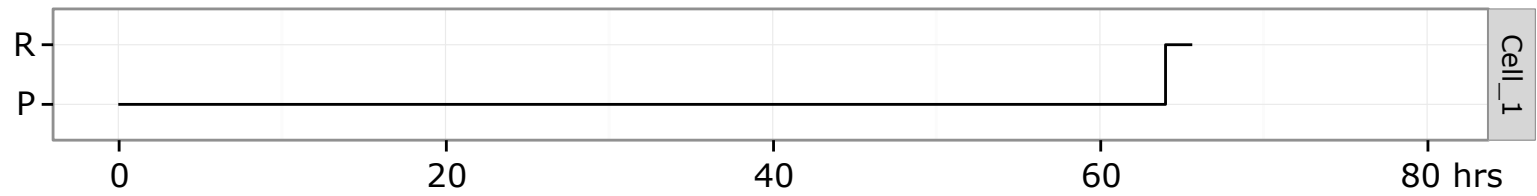
CD133



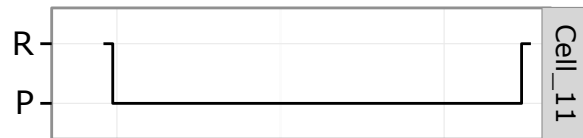
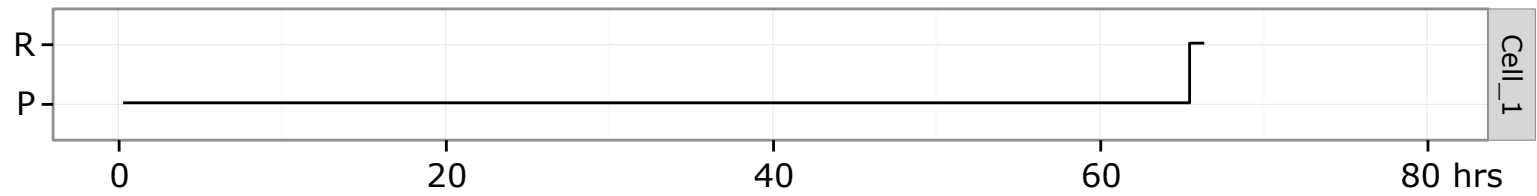
Upon cell division:



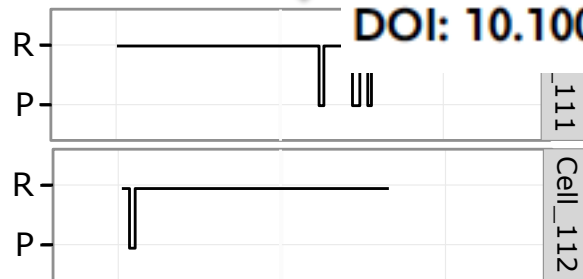
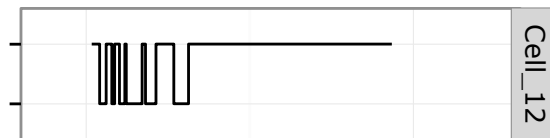
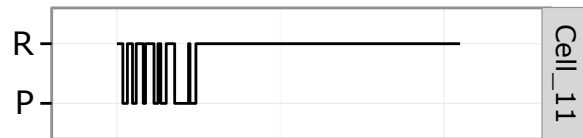
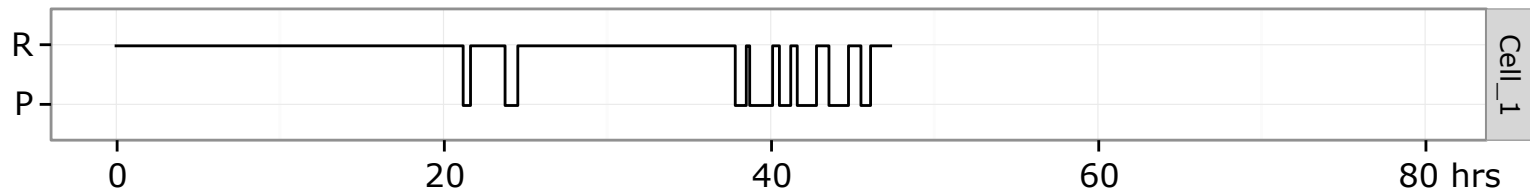
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15_02_17_05_12



15_07_15_12_22



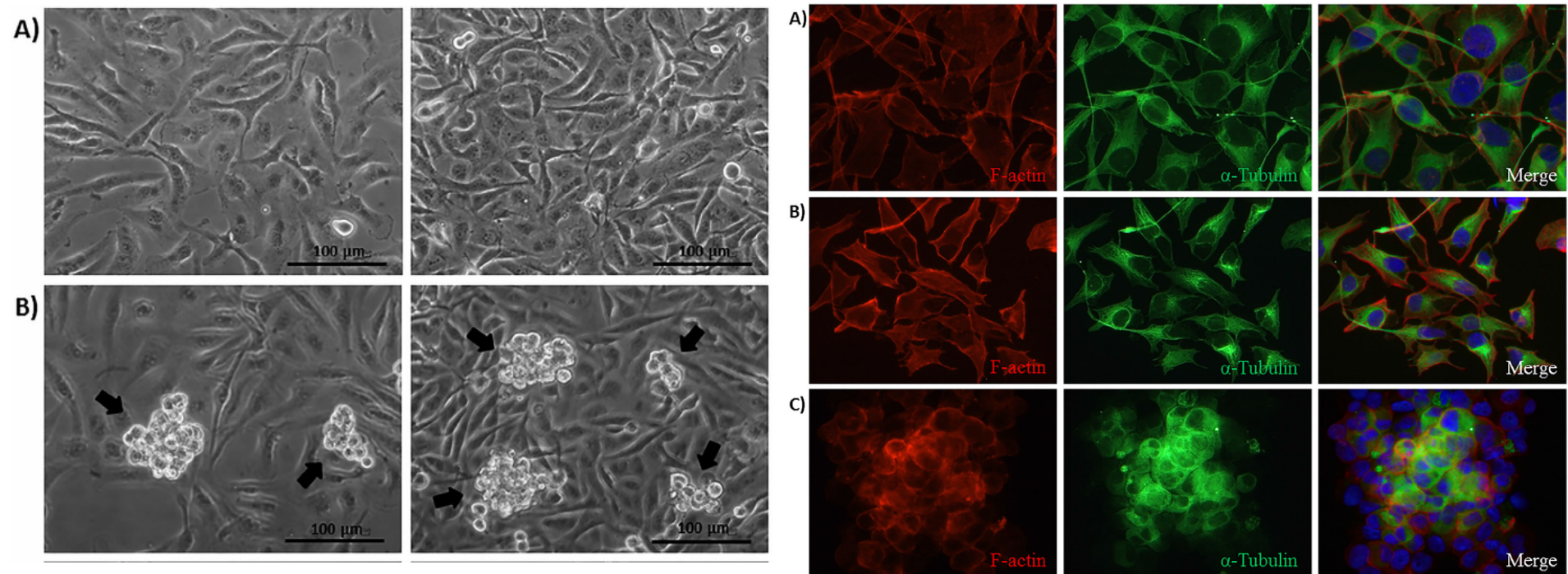
DOI: 10.1002/bies.201700138

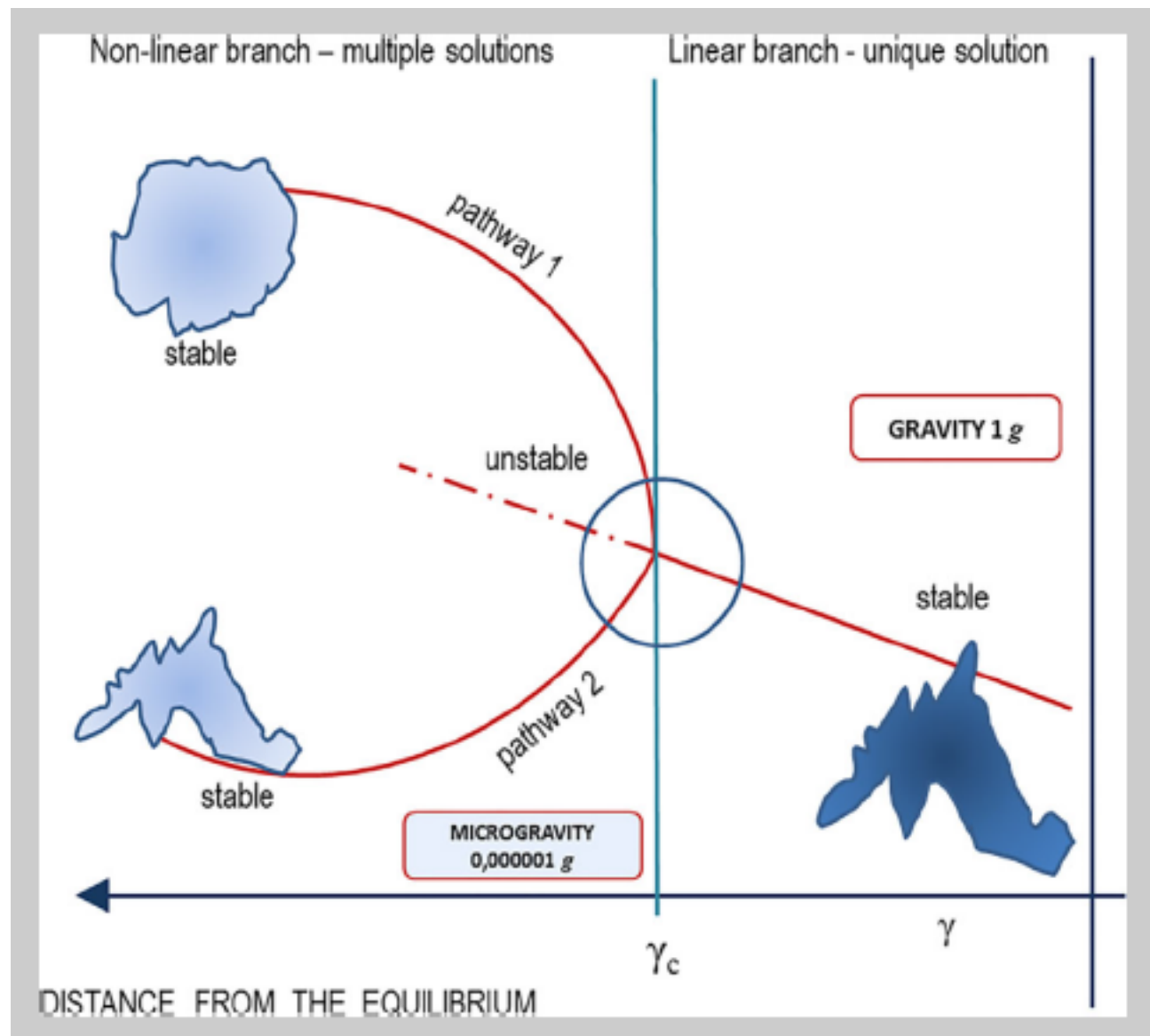
Gravity Constraints Drive Biological Systems Toward Specific Organization Patterns

Commitment of cell specification is constrained by physical cues

Mariano Bizzarri, Maria Grazia Masiello, Alessandro Giuliani, and Alessandra Cucina*

BioEssays 2017, DOI: 10.1002/bies.201700138





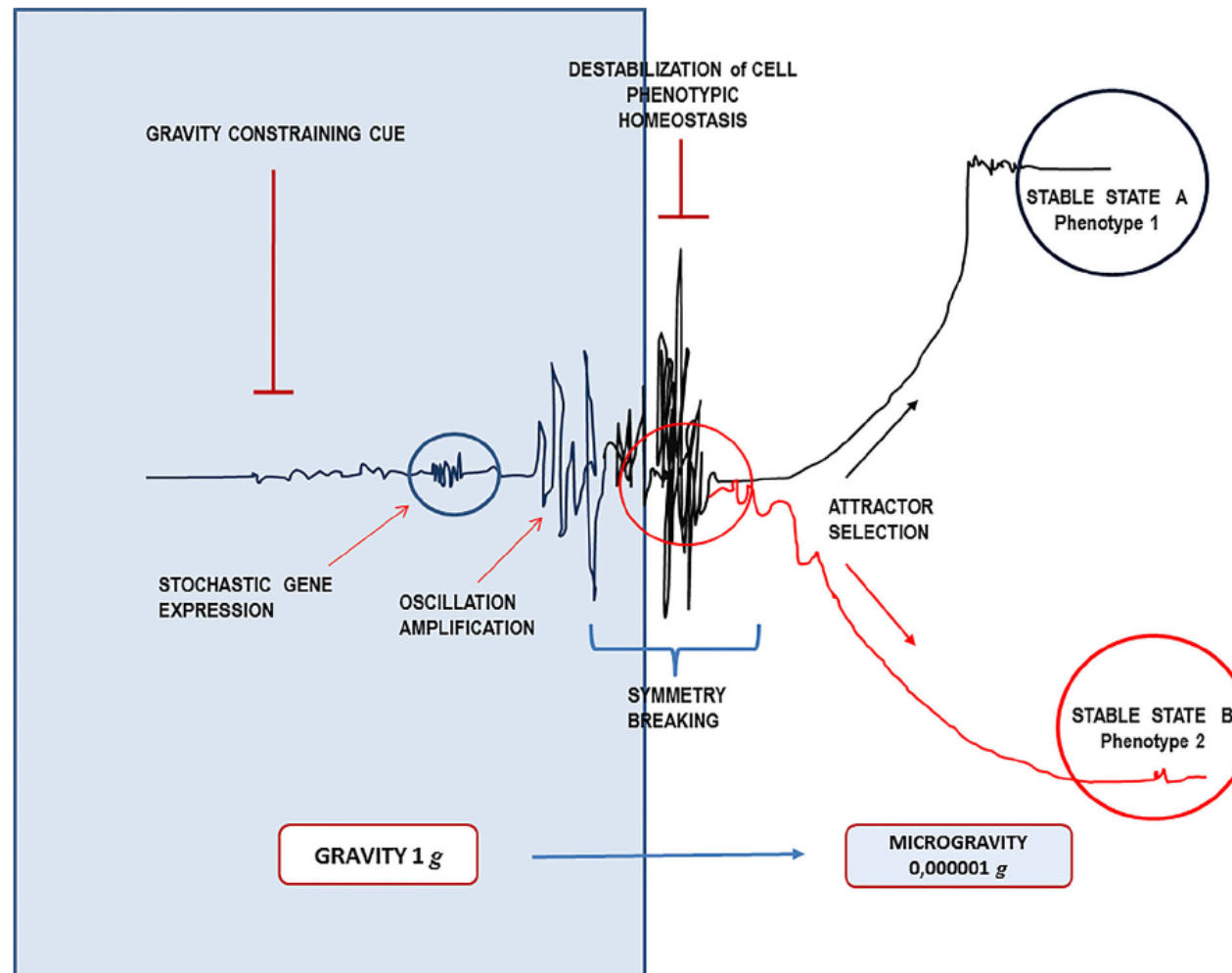
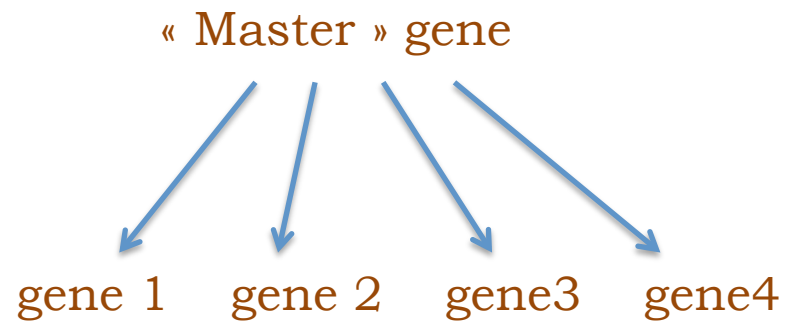
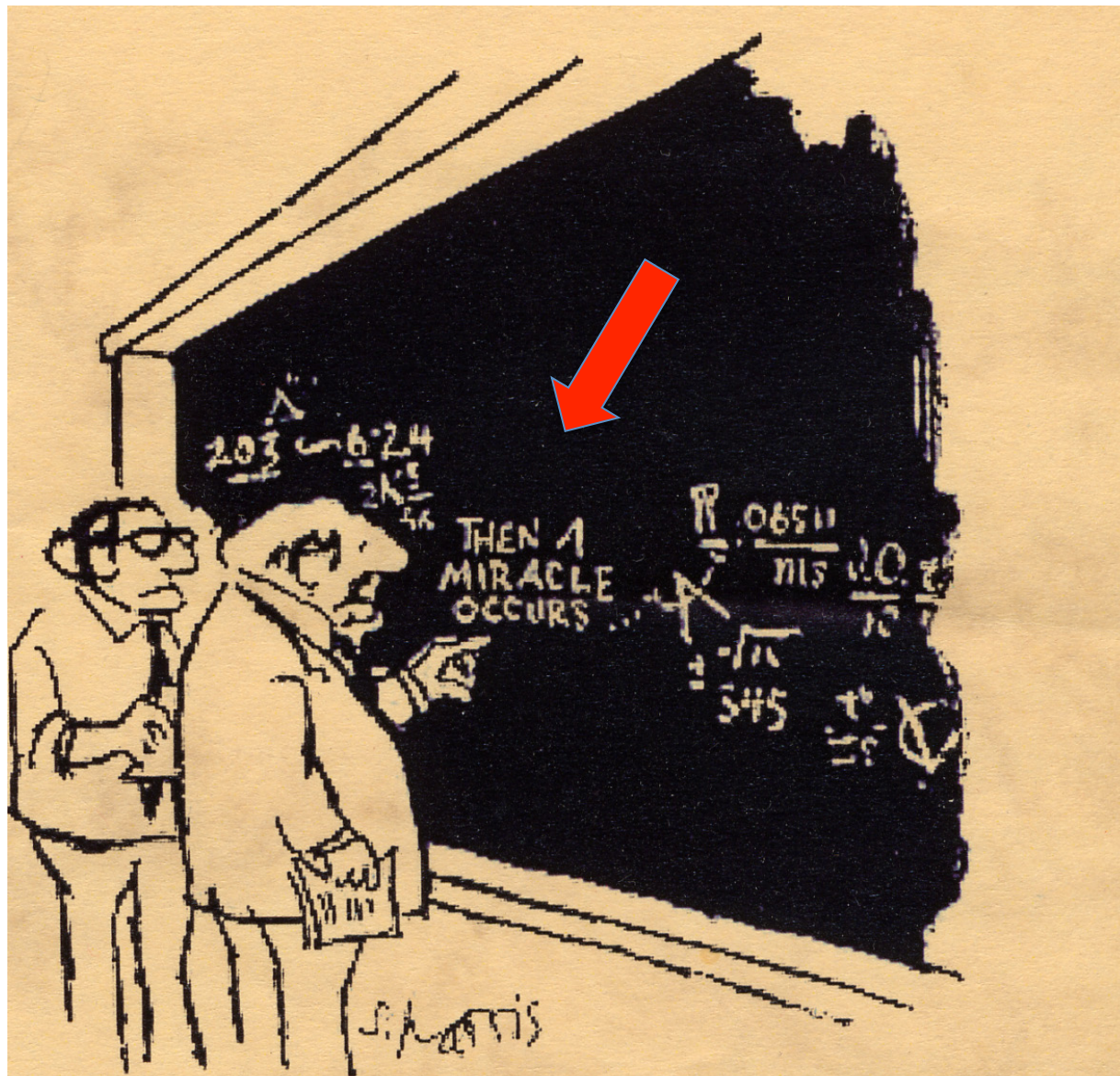


Figure 3. Phase transition toward cell fate commitment in complex systems in a non-equilibrium thermodynamics model. In dissipative systems, there are conditions far from the equilibrium in which even small external influences can produce dramatic effects, namely when the system approaches phase transitions, as those occurring during mitosis or cell differentiating processes. In the presence of normal gravity, despite the presence of oscillations in gene activity and/or availability of transcription factors, cooperativity among system's elements leads the external energy field to overcome the intrinsic fluctuation. In this condition, gene-regulatory networks and transcription signaling behave like "instructional factors," driving the system – seemingly in a "deterministic" way – toward a single, specific fate. However, when gravity disappears, fluctuation in many order parameters (gene expression patterns, transcription factors, enzymatic pathways, and cytoskeleton dynamics) steadily increases, leading to a symmetry breaking at the bifurcation point. Removal of gravity constraints leads thus to a widely destabilizing effect. As a result, the systems can freely explore new gene-regulatory networks, likely enacting a wide remodeling of the architecture of the transcription network. This will lead the systems to explore new phenotypic configurations, ultimately driving the systems into two new, stable attractors, in which fluctuation of order parameters can be more efficiently damped. Indeed, the new phenotypic configurations demonstrated themselves stable and reproducible, even for longer periods of observation (>7 days). Conversely, when the two population are seeded again on ground conditions, the superposition of the gravity field may break the system's symmetry, giving the system a directional preference, which will make it evolve into a specific state. In other words, the "weak" gravity force dramatically influences the system to favor one among different, potential configurations.

How (gene expression) change is initiated?

Deterministic view:



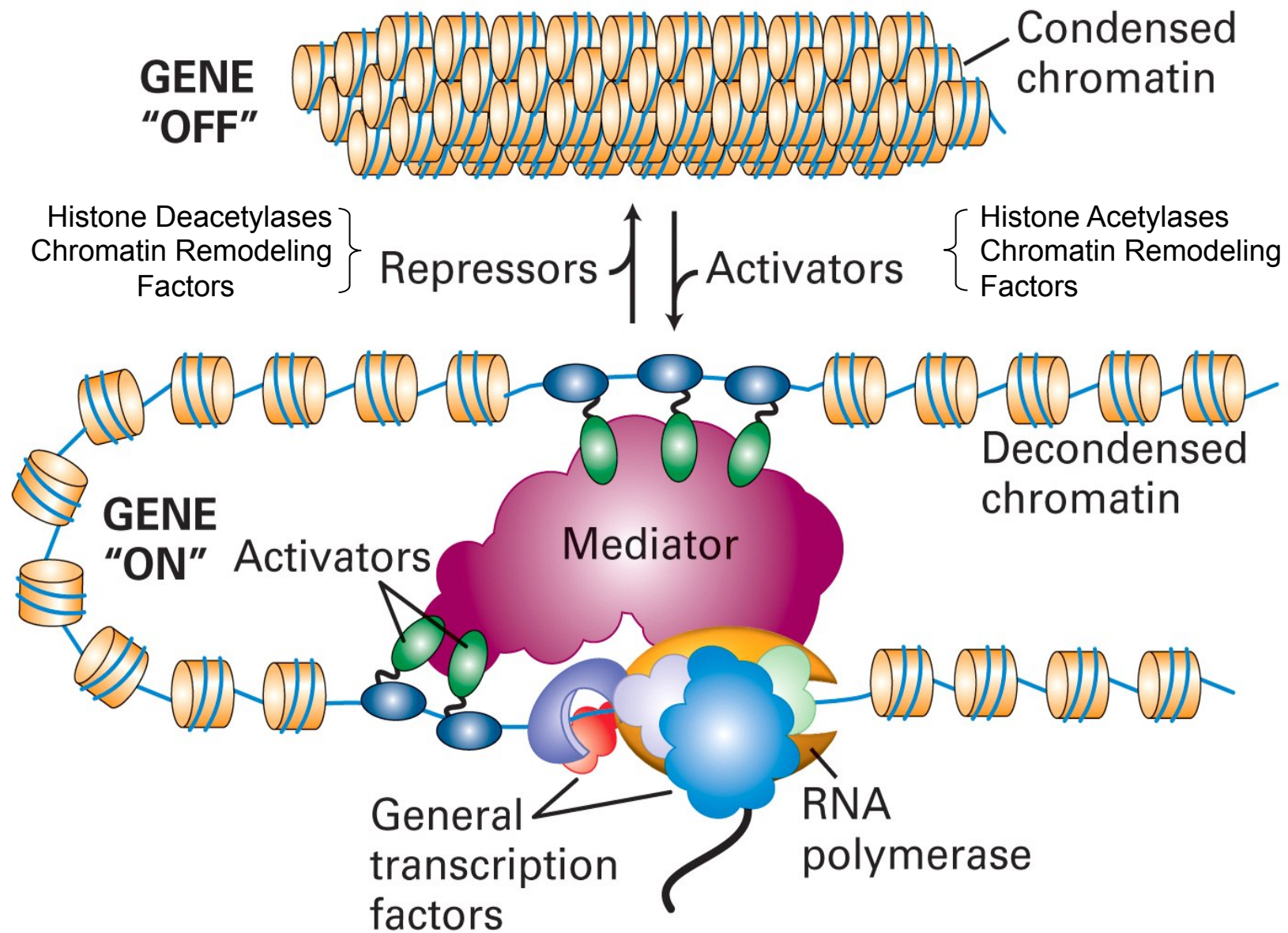


“I think you should be more explicit here in step one”

How gene expression change is initiated?

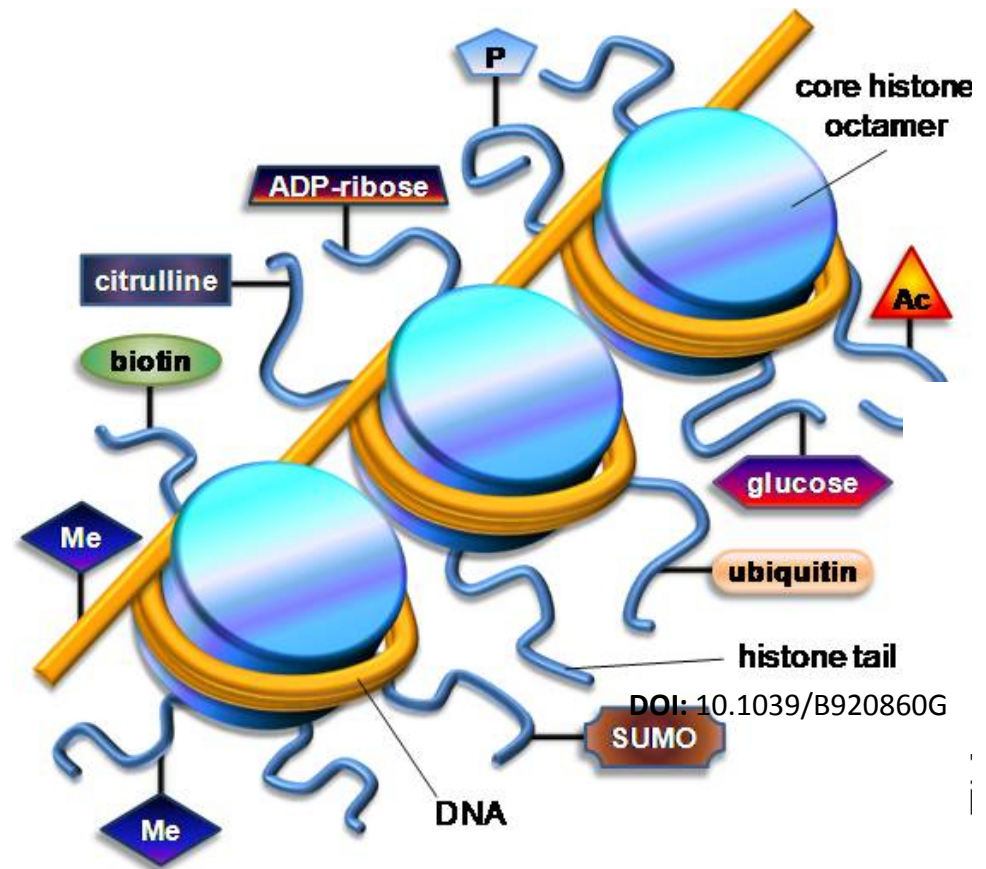
Deterministic view: causality is linear

Stochastic view: no need to explain, because change is the ground state.
What we need to explain is the stability



Genomic DNA is not accessible to regulatory factors. Accessibility depends on chromatin.

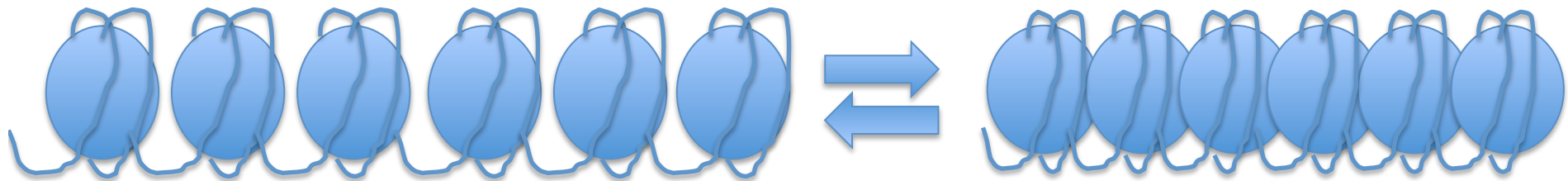
Chromatin is a highly dynamic structure due to reversible post-translational modifications and cycles of association-dissociation.



Chromatin & Epigenetics

« open » « euchromatin »

« closed » « heterochromatin »



Determined by post-translational « epigenetic » changes

DNA is Hypomethylated

Hyperacetylation of Histones H3 and H4

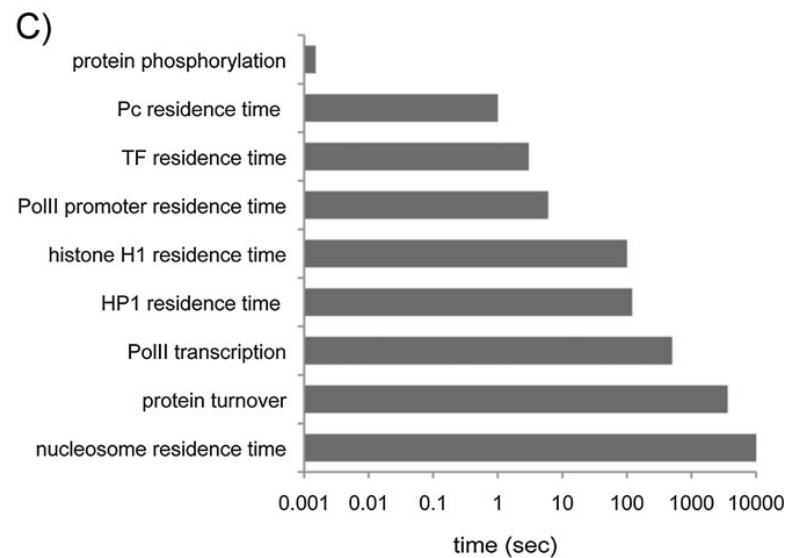
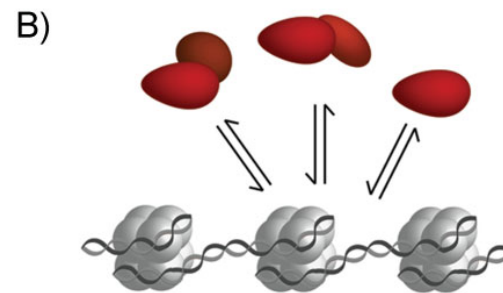
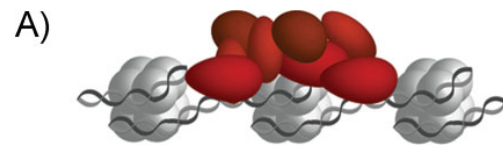
Histone Methylation of H3Kme2, H3K4me3, H3K9me1

DNA that is Hypermethylated

Hypoacetylation of Histones H3 and H4

Histone Methylation of H3K27me2, H3K27me3, H3K9me2, H3K9me3

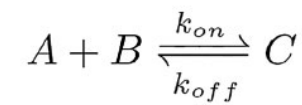
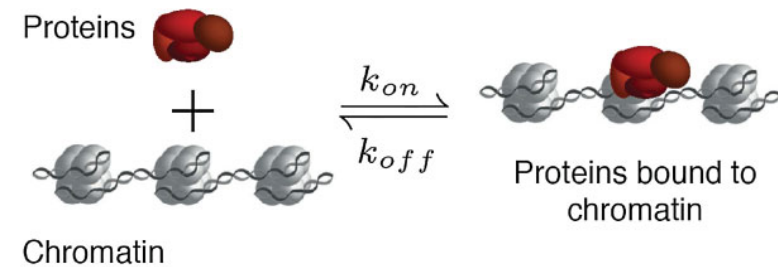
Epigenetic changes can be both reversible and heritable.



Epigenetics meets mathematics: Towards a quantitative understanding of chromatin biology

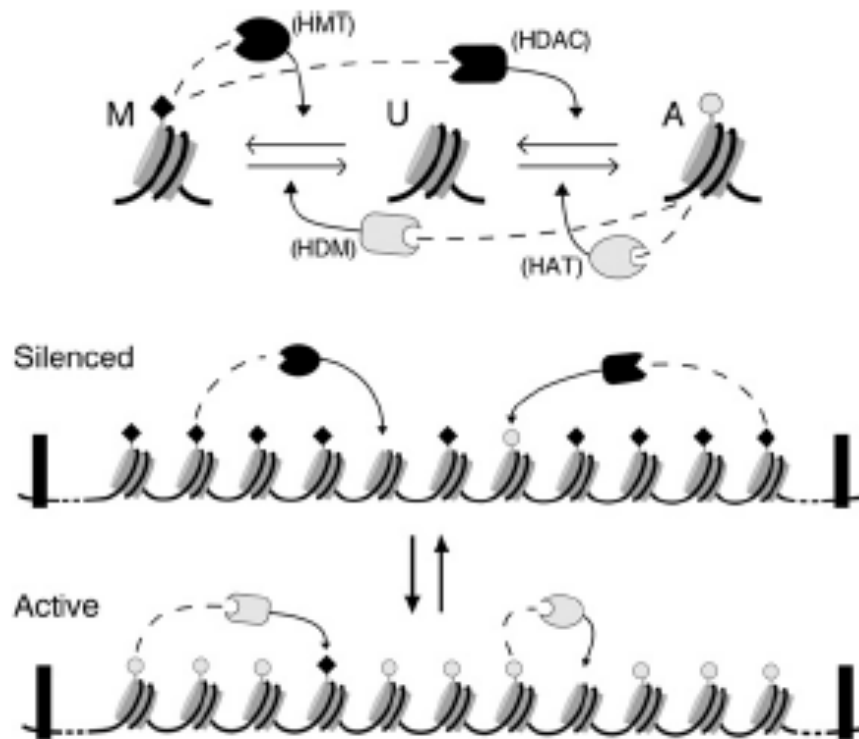
Philipp A. Steffen[†], João P. Fonseca[†] and Leonie Ringrose*

Bioessays 34: 901–913, © 2012



Theoretical Analysis of Epigenetic Cell Memory by Nucleosome Modification

Ian B. Dodd,^{1,2} Mille A. Micheelsen,¹ Kim Sneppen,^{1,*} and Geneviève Thon³



M – repressed chromatin
U – unmodified chromatin
A- Active chromatin
HMT, HDAC, HDM, HAT – enzymes

Cooperativity !!!

Figure 2. Bistability Is a Function of Noise

Theoretical Analysis of Epigenetic Cell Memory by Nucleosome Modification

Ian B. Dodd,^{1,2} Mille A. Micheelsen,¹ Kim Sneppen,^{1,*} and Geneviève Thon³

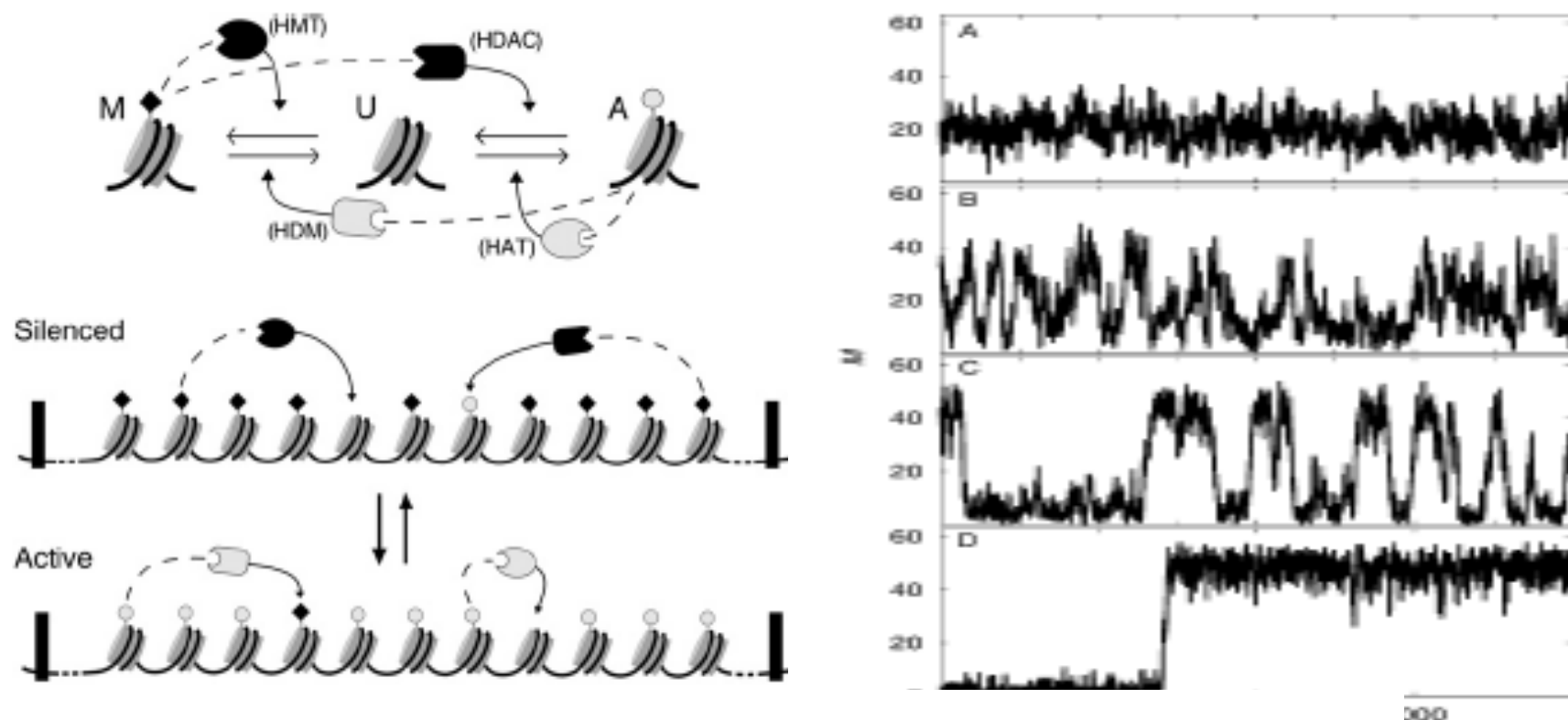
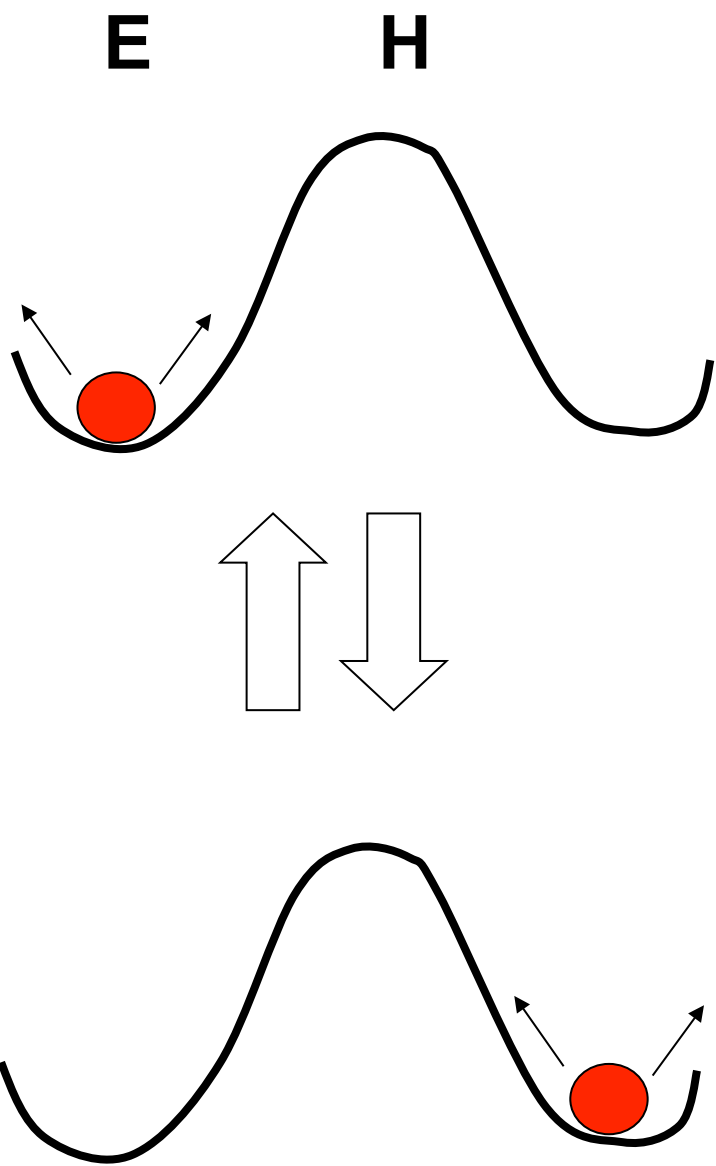


Figure 2. Bistability Is a Function of Noise



Metabolic Regulation of Epigenetics

Chao Lu^{1,2} and Craig B. Thompson^{1,*}

¹Cancer Biology and Genetics Program, Memorial Sloan-Kettering Cancer Center, New York, NY 10065, USA

²Department of Cancer Biology, Perelman School of Medicine, University of Pennsylvania, Philadelphia, PA 19104, USA

*Correspondence: thompsonc@mskcc.org

<http://dx.doi.org/10.1016/j.cmet.2012.06.001>

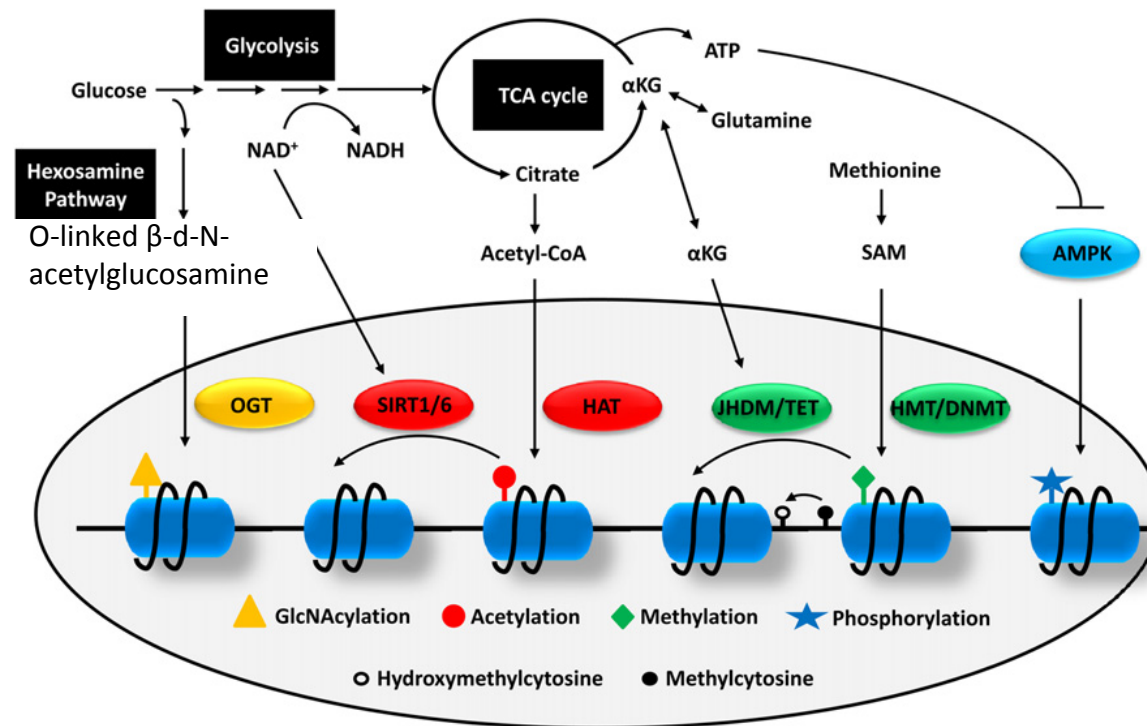


Figure 3. Crosstalk between Metabolism and Epigenetics

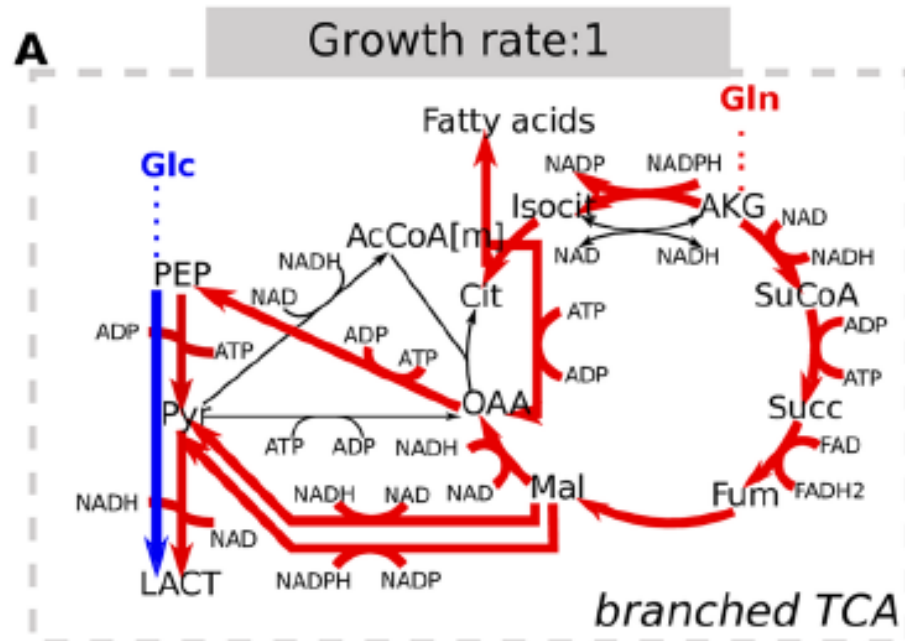
As glucose enters the glycolytic pathway, a minor portion is branched to hexosamine biosynthetic pathway to produce GlcNAc which can be used as substrate for histone GlcNAcylation by OGT. Flux through glycolysis determines the NAD^+/NADH ratio which is important for the activities of sirtuin histone deacetylases. Several TCA cycle intermediates can be exported out of mitochondria including citrate and αKG . Cytosolic citrate is converted to acetyl-CoA which is used as a donor for HAT-mediated histone acetylation. αKG is used as cofactor for histone and DNA demethylation reactions by JHDM and TET, respectively. The substrate for HMT and DNMT is SAM, which is synthesized from essential amino acid methionine. Finally, a low ATP/AMP ratio can activate AMPK, a kinase that phosphorylates histones.

A metabolic core model elucidates how enhanced utilization of glucose and glutamine, with enhanced glutamine-dependent lactate production, promotes cancer cell growth: The WarburQ effect

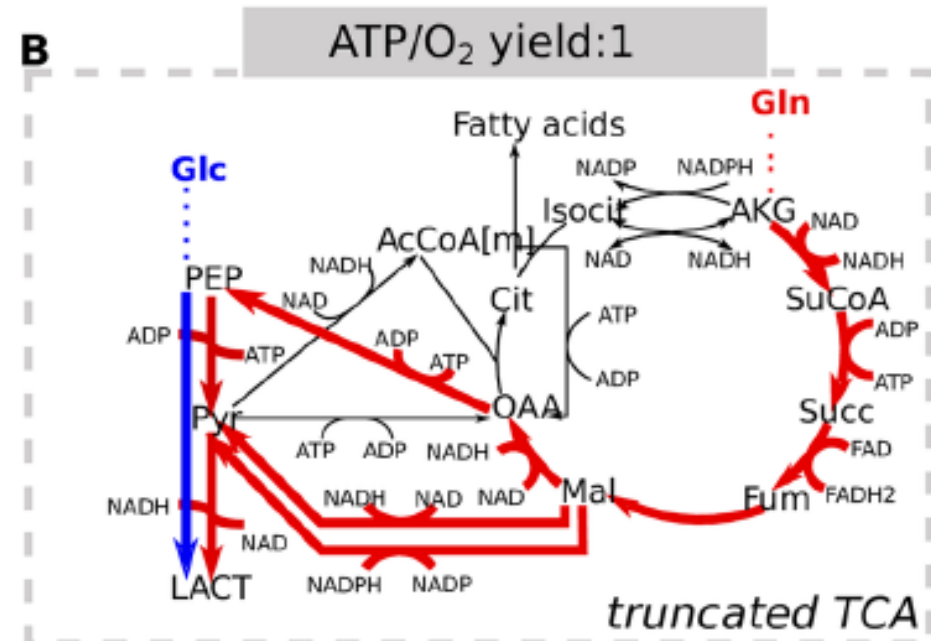
Chiara Damiani^{1,2}, Riccardo Colombo^{1,2}, Daniela Gaglio^{1,3}, Fabrizia Mastroianni^{1,4}, Dario Pescini^{1,5}, Hans Victor Westerhoff^{6,7,8}, Giancarlo Mauri^{1,2}, Marco Vanoni^{1,4*}, Lilia Alberghina^{1,4*}

1 SYSBIO Centre of Systems Biology, Milano, Italy, 2 Dept of Informatics, Systems and Communication,

Growth maximization



ATP maximization



3. Summary

How cells function reliably with such an inherent variability in gene expression?

Intrinsic constraints: generated by the system itself

Extrinsic constraints: environment (what is environment?)







3. Summary

How cells function reliably with such an inherent variability in gene expression?

Intrinsic constraints: generated by the cells themselves

Extrinsic constraints: environment (what is environment?)

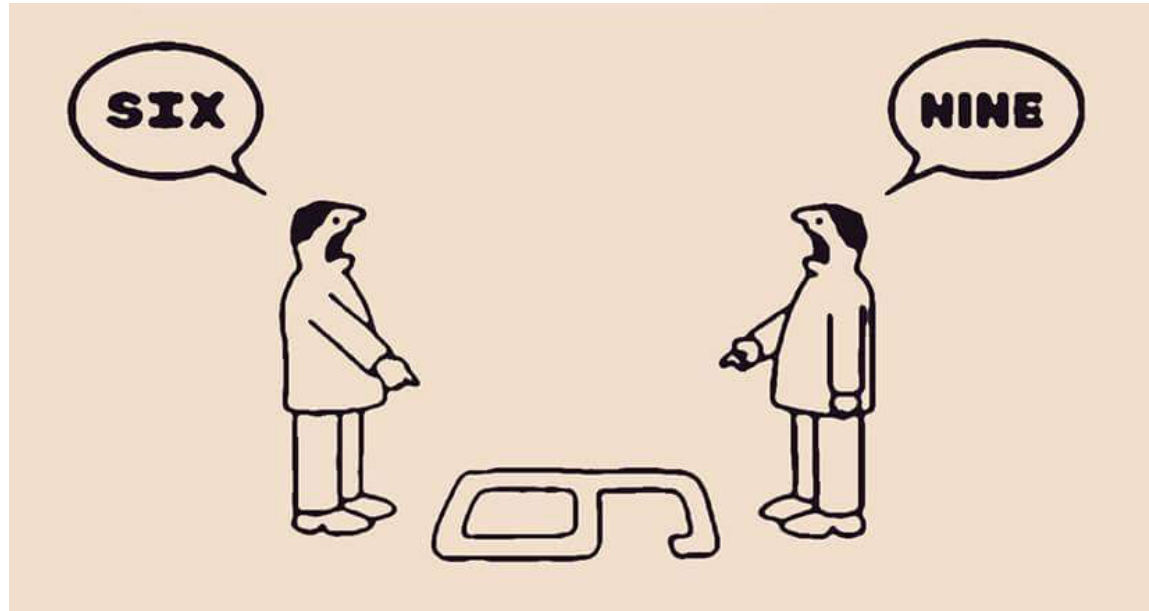
→ define a state space with many different attractors.
But not every attractor is accessible.

spatial (diffusion, steric etc.)

mechanic

thermodynamic (red-ox, “fuel” type)

historical contingency (heredity)



Thank you !

...and wait a moment please

