

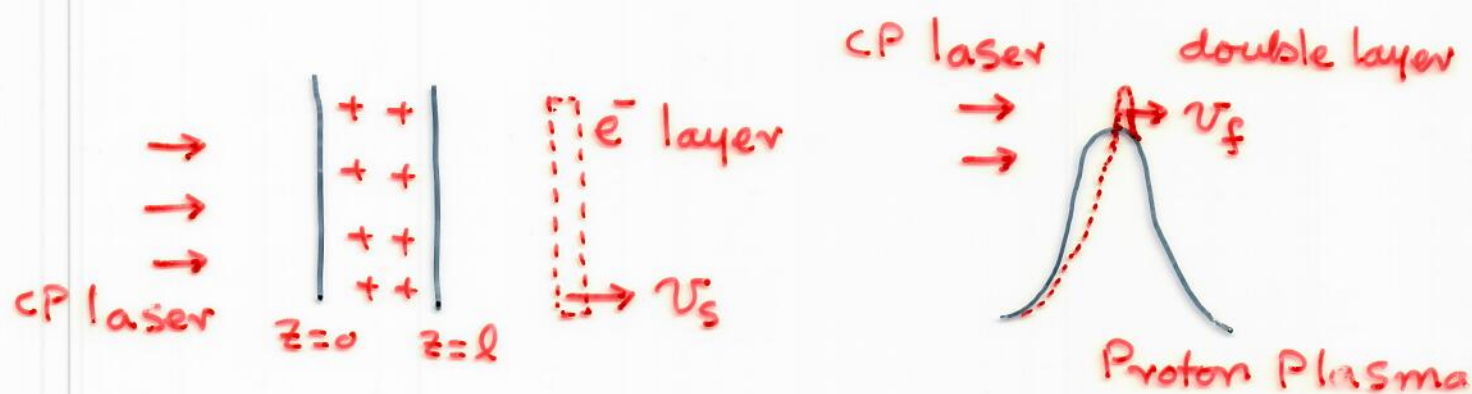
1 Radiation Pressure Proton Accel. from Sub-critical Foils & Gaseous Targets

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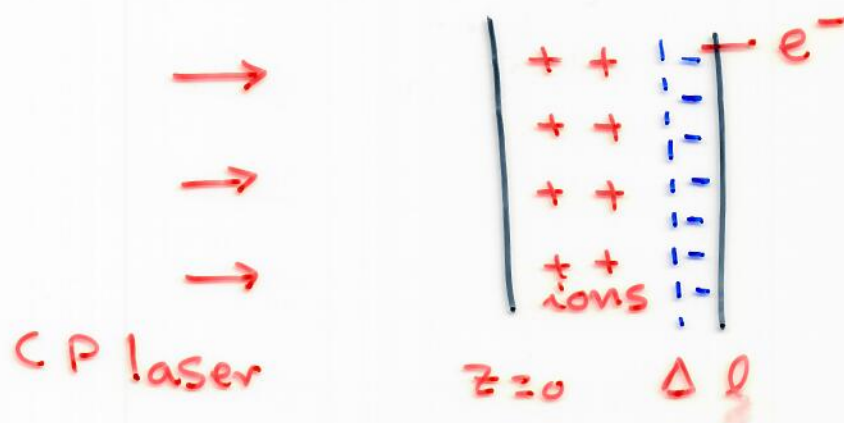
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- Basic Physics of RPA
- Critical Foil Thickness
- Proton Accel : Subcritical Foils
- Double Layer Formation in Gas Targets
- Snow Plow Accel. of Upstream Protons
- Conclusions



2 RPA



Laser

$$\vec{E} = A_0 (\hat{x} + i\hat{y}) e^{-i(\omega t - \frac{\omega}{c} z)}$$

$$I_0 = \frac{A_0^2}{\mu_0 c}$$

Ponderomotive Force on e^-

$$F_p = -mc^2 \frac{\partial}{\partial z} \gamma_e, \quad \gamma_e = (1 + a_T^2)^{1/2}$$

$$a_T = \frac{e A_T}{m \omega c}$$

Radiation Pressure

$$\int F_p n_e dz = \frac{2 I_0}{c}$$

Pushes e^- to the rear $\Delta \sim l$

Space charge Field

$$E_s = \frac{n_0 e z}{\epsilon_0}$$

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Choose foil thickness l such that

$$\frac{2I_0}{c} = n_0 e l E_s, E_s = \frac{n_0 e l}{\epsilon_0}$$

↑

Space charge force on e^- layer
per unit area

Critical Foil Thickness

$$l_{cr} = \sqrt{2} a_0 \frac{n_{cr}}{n_0} \frac{\lambda_L}{2\pi}$$

$$a_0 = \frac{e A_0}{m \omega c}, \lambda_L: \text{laser wavelength}$$

Double Layer Acceleration

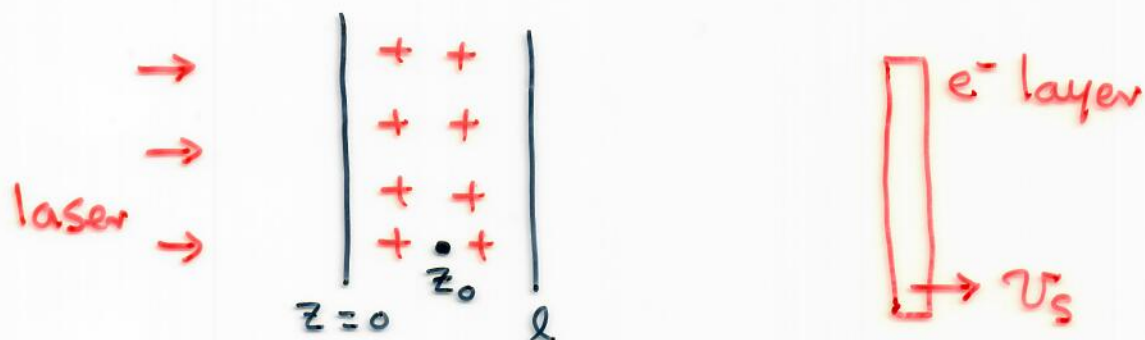
$$g = \frac{2 I_0 / c}{m_p n_0 l_{cr}}$$

$$g' = g \frac{1 - v_f / c}{1 + v_f / c}$$

v_f : foil velocity

$$\text{Proton energy } E_p \sim t^{1/3}$$

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RPA of Subcritical Foil, $l < l_{cr}$ 

- Electron layer is detached from the foil when

$$\frac{2 I_0}{c} > n_0 e l E_s$$

- As e^- layer moves radiation pressure on it decreases. It acquires steady state velocity v_s ,

$$\frac{2 I_0}{c} \frac{1 - v_s/c}{1 + v_s/c} = n_0 e l E_s, \quad E_s = \frac{n_0 e l}{\epsilon_0}$$

$$\frac{v_s}{c} = \frac{1 - l^2/l_{cr}^2}{1 + l^2/l_{cr}^2}$$

- Ion located at z_0 experiences a constant force $= \frac{n_0 e^2}{\epsilon_0} z_0$

No sheet crossing

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- Proton Energy at $z = z_p$

$$m_p c^2 (\gamma_p - 1) = \frac{n_0 e^2}{\epsilon_0} z_0 z_p$$

- Proton catches up with e^- layer at

$$z_p = \frac{2 V_S / c}{\alpha_p (1 - V_S^2 / c^2)}$$

$$\alpha_p = 2 \sqrt{2} \pi a_0 \frac{m}{m_p} \frac{z_0}{l_{cr}}$$

$$\epsilon_p = \frac{1}{2} m_p c^2 \left(\frac{l_{cr}^2}{l^2} - \frac{l^2}{l_{cr}^2} \right)$$

$$\sim 1.2 \text{ GeV for } l / l_{cr} \approx 0.6$$

- ϵ_p is independent of z_0 . All protons acquire same energy if V_S is maintained constant.
- Limit on Foil Thickness

$$l > l_{skin} = a_0^{1/2} c / \omega_p$$

$$a_0 \geq \frac{n_0}{2 n_{cr}} \frac{l_{cr}^2}{l^2}$$

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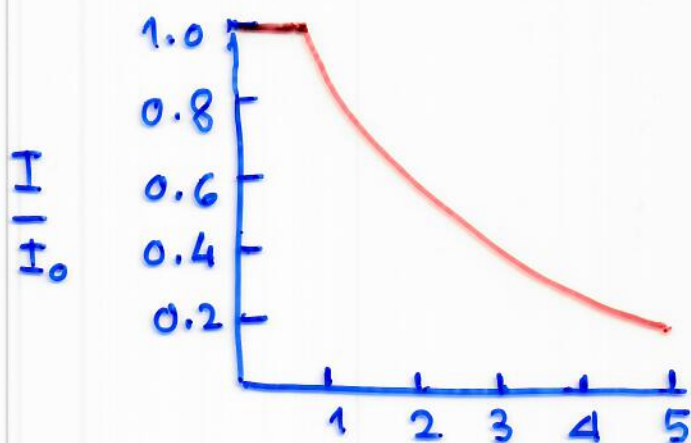
- Pulse Shape for minimum Proton Energy Spread

As the ions cross the e^- layer the ion space charge pull on e^- layer decreases, so must the laser intensity to keep v_s constant

$$I = I_0 \frac{t_s}{t} \left(1 - \frac{v_s}{c}\right) \quad \text{for } t > t_s \left(1 - \frac{v_s}{c}\right)$$

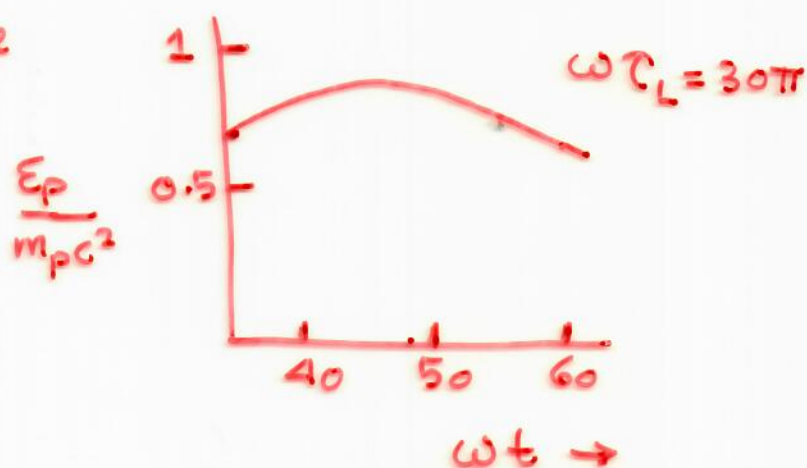
$$= 1 \quad \text{for } t < t_s \left(1 - \frac{v_s}{c}\right)$$

$$t_s = \frac{1}{8\sqrt{2}\pi a_0} \frac{m_p}{m} \frac{l_{cw}}{l} \left(\frac{l^2}{l_{cw}^2} + \frac{l_{cw}^2}{l^2} \right)^{\frac{1}{2}} \frac{2\pi}{\omega}$$



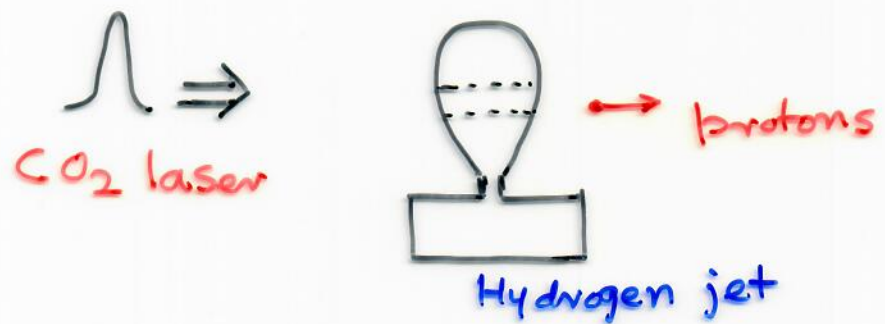
- Gaussian Pulse

$$I = I_0 e^{-(t - z/c)^2 / \tau_L^2}$$



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RPA of Gaseous Target : CO_2 laser



- Palmer et al. PRL 106, 14801 (2011)

CP laser : $I \leq 10^{16} \text{ W/cm}^2$ ($a_0 \lesssim 0.5$)

$L_n \sim 825 \mu\text{m}$, $n_{\text{max}} = 10 n_{\text{cr}}$

$E_p \sim 1 \text{ MeV}$

hole boring accel.

- Haberberger et al. , Nat. Phys. 8, 95 (2012)

LP laser , $I \lesssim 6.6 \times 10^{16} \text{ W/cm}^2$ ($a_0 = 1.5 - 2.5$)

$n \sim 3 - 5 n_{\text{cr}}$

steepened density profile

$E_p \approx 22 \text{ MeV}$, 1% energy spread

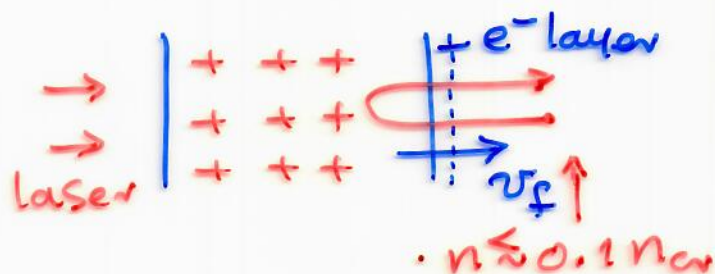
Shock reflected upstream protons

- Luanliang Ji , A. Pukhov, B. Shen, New J. Phys 16, 063047 (2014).

Dragging Field Proton
Accel.

$a_0 \sim 200$, $n_0 \gg n_{\text{cr}}$

$E_p \gtrsim 100 \text{ GeV}$



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Model Problem : Reflection from Density Hill

$$\omega_p^2 = \omega_{p2}^2, |z| < l$$

$$= \omega_{p1}^2, |z| > l$$

$\omega \rightarrow$
 \rightarrow
 laser
 $z = -l \quad l$

$$\frac{\omega_{p2}^2}{\omega^2} - 1 = 1 - \frac{\omega_{p1}^2}{\omega^2}$$

Intensity Transmission Coeff.

$$T = \frac{1}{\cosh^2(\omega \alpha l/c)}, \quad \alpha = \left(\frac{\omega_{p2}^2}{\omega^2} - 1 \right)^{1/2}$$

$$\approx 0.06 \quad \text{for } \omega_{p2}^2/\omega^2 = 1.1,$$

$$l = \lambda_L = 2\pi c/\omega$$

Radiation Pressure

$$F = \frac{2I}{c}(1-T) \approx \frac{2I}{c}$$

pushes the e^- , creating a double layer

Hill Creation from Parabolic Profile

$$\omega_p^2 = \omega_{p0}^2 \left(1 - \frac{z^2}{L_n^2} \right), \quad |z| < L_n$$

$$= 0 \quad \text{otherwise}$$

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- Gaussian Pulse (CP)

$$\vec{E} = A (\hat{x} + i\hat{y}) e^{-i(\omega t - \omega z/c)}$$

$$A^2 = A_0^2 e^{-(t - z/c)^2 / \tau_L^2}$$

- Low amp. portion reflects from

$$z = -z_0 = -L \ln \sqrt{1 - \omega^2 / \omega_{p0}^2}$$

- High amp. portion (peak) reflects from

$$z = -z_m = -L \ln \sqrt{1 - \omega^2 \gamma_0 / \omega_{p0}^2}$$

- Critical layer propagates with velocity

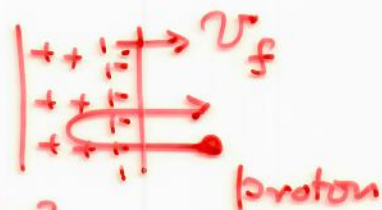
$$v_c \sim L / \tau_L$$

- For $a_0 > 2.5$, this is ~~the~~ close to the speed of ions accel. by radiation pressure. Profile is steepened by a succession of pulses.

- Moving Double Layer in Upstream Plasma

$$n_e m_p L \frac{dv_f}{dt} =$$

$$\frac{2I}{c} \frac{1 - v_f/c}{1 + v_f/c} - 2n_e m_p v_f^2 \gamma_f^2$$



Moving Double layer

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- At time t moving ion layer extends upto

$$z_f = \frac{n_0 e^2 l t^2}{2 \epsilon_0 m_p} \quad (\text{non-relativistic limit})$$

- Potential Diff. across the layer

$$\phi_s = \frac{n_0 e z_f^2}{2 \epsilon_0 (1 + z_f / l)}$$

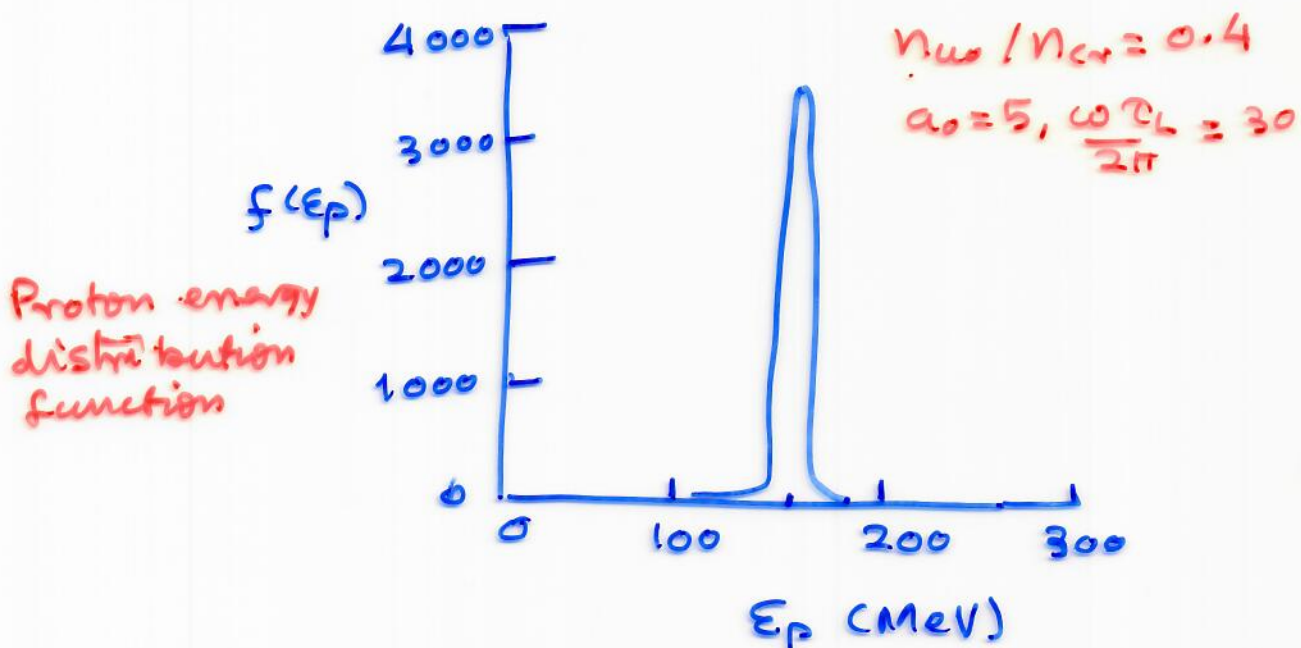
Max. Proton Energy (for which reflection is possible)

$$E_p \approx 2 m_p v_f^2 = 2 m \omega_p^2 \sqrt{z_f l}$$

Relativistic Case: Gaussian Beam / Parabolic Nu

$$\frac{dv_f}{dt} = \frac{2 a_0^2 c^2}{\gamma_f^3 l} \frac{n_{cr}}{n_0} \frac{m}{m_p} \frac{1 - v_f/c}{1 + v_f/c} - \frac{n_{uo} v_f^2}{n_0 l \gamma_f} \left(1 - \frac{z^2}{L_m^2}\right)$$

$$a_0^2 = a_{00}^2 e^{-(t - z/c)^2 / \tau_L^2}$$



Conclusions

- Subcritical thickness foils provide higher acceleration due to extended time for proton accel.
- Suitable tailoring of pulse is needed.
- Gaussian pulse gives finite energy spread.
- R-T instability may be a major concern.
- CP CO₂ laser - gas jet interaction with density peak close to relativistic now appears a promising scheme for upstream proton accel. (via reflection).
- 2 D effects need to be investigated.

