

Driven-Dissipative Quantum Dot Circuit-QED systems

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Collaboration

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R. Hartle (Göttingen)

Phys. Rev. B, **94**, 035434 (2016)
Phys. Rev. B, **94**, 121305 (**R**) (2016)

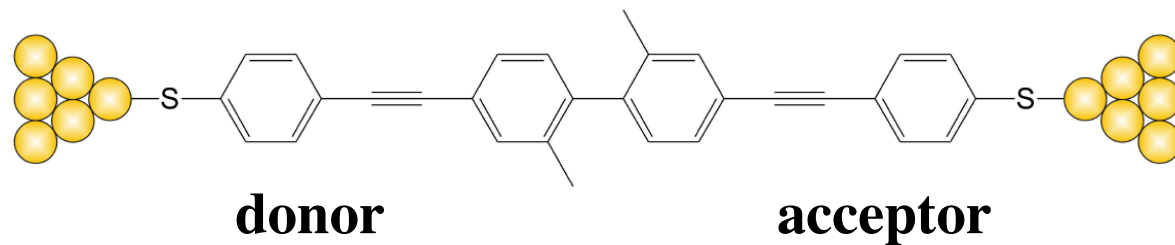
Also,

Phys. Rev. B **92**, 045309 (2015)
Phys. Rev. B **91**, 245429 (2015)
Phys. Rev. B, **90**, 125402 (2014)

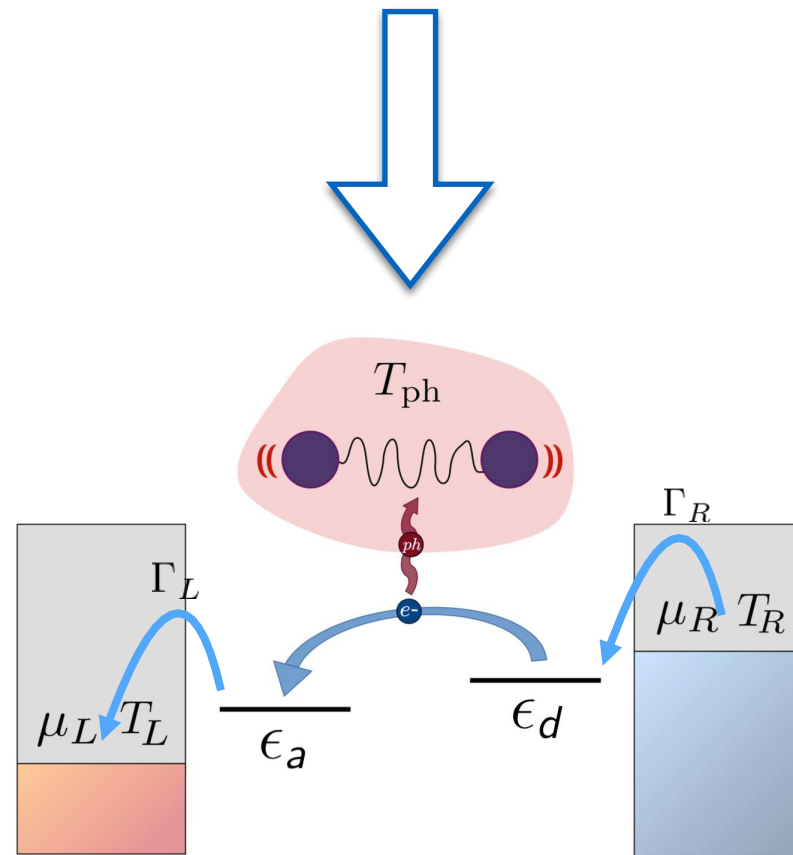


Engineered Hybrid Quantum Systems:

Electron-vibration interaction: (Nano-Electromechanical system)



Ballman et al., Phys. Rev. Lett. 109, 056801 (2012)

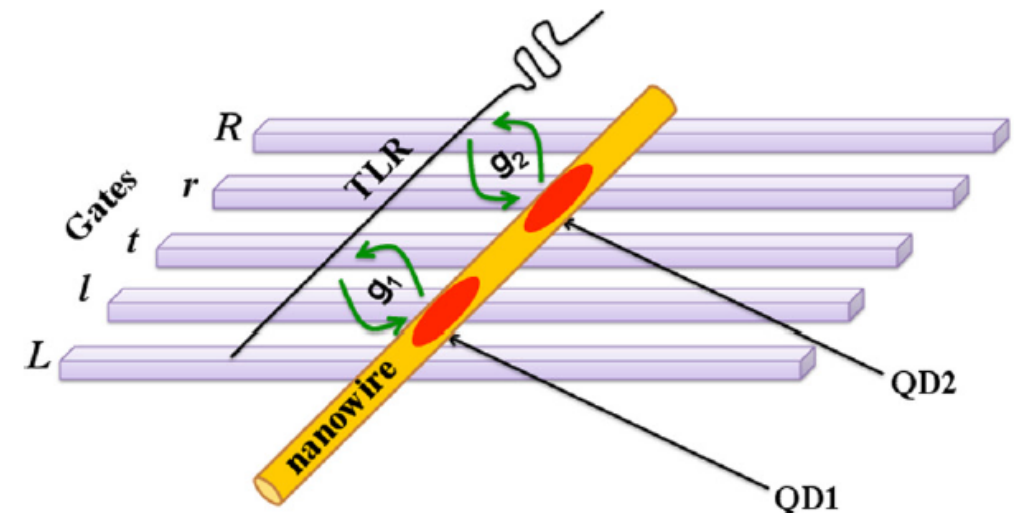


Donor-Acceptor model

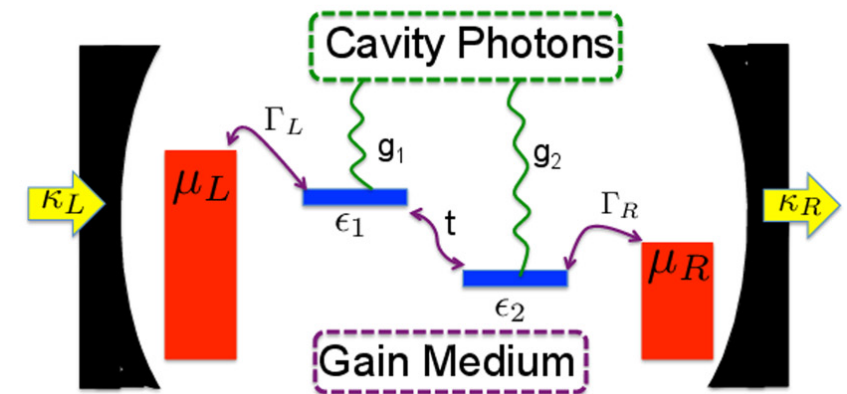
Hartle, Kulkarni, Phys. Rev. B 91, 245429 (2015)

Analogy between molecular junctions and QD-cQED systems

Electron-Photon interaction: Circuit-Quantum Electrodynamics



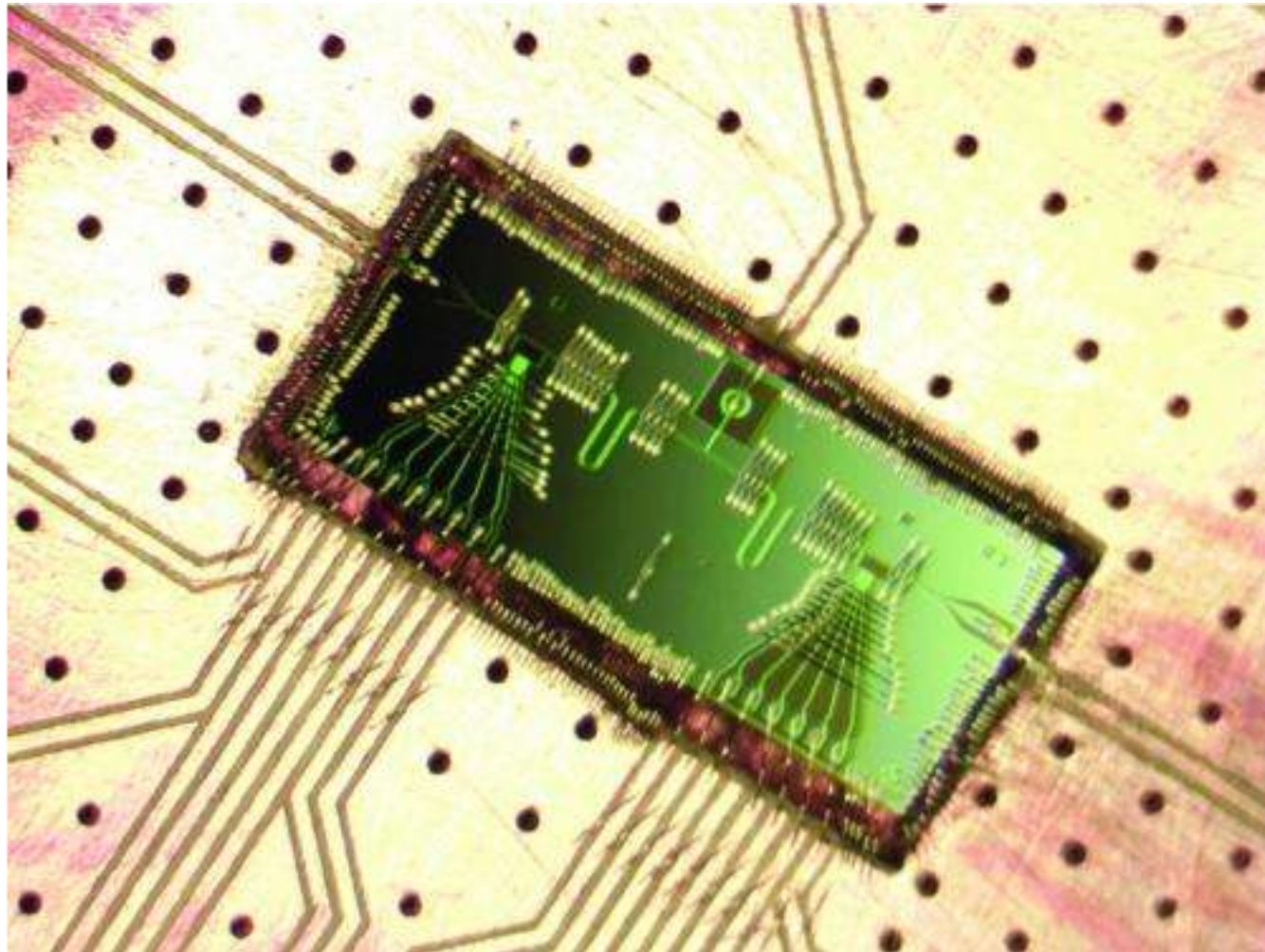
... , J Petta et al,
Nature 490, 380
(2012)



dc transport of electrons lead to photon
emission: micromasers

Rice-sized laser, powered one electron at a time, bodes well for quantum computing

January 15, 2015



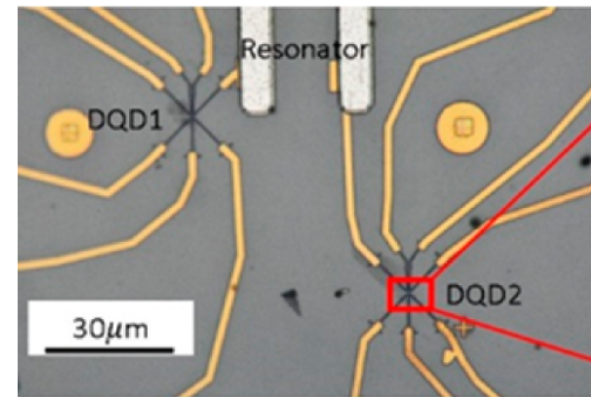
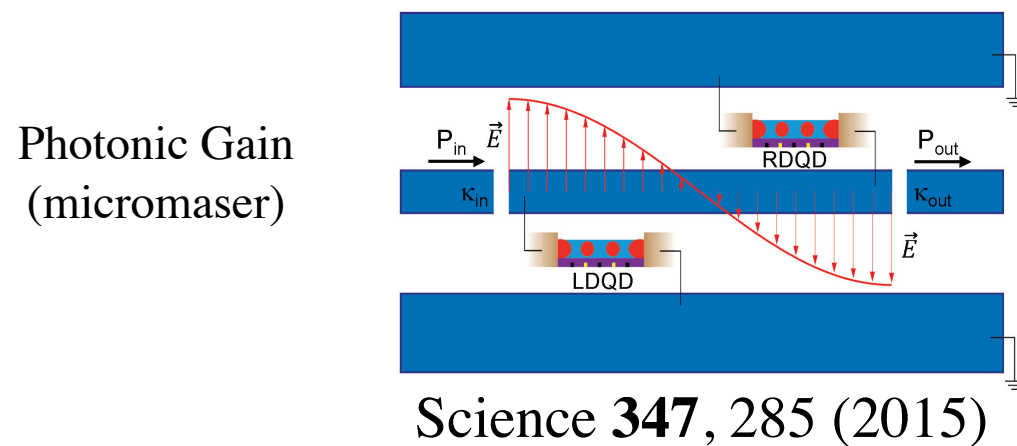
Science **347**, 285 (2015)
Petta Lab Princeton

Princeton University researchers have built a rice grain-sized microwave laser. Credit: Jason Petta, Princeton University

Circuit Quantum Electrodynamics Experiments

Experiments:

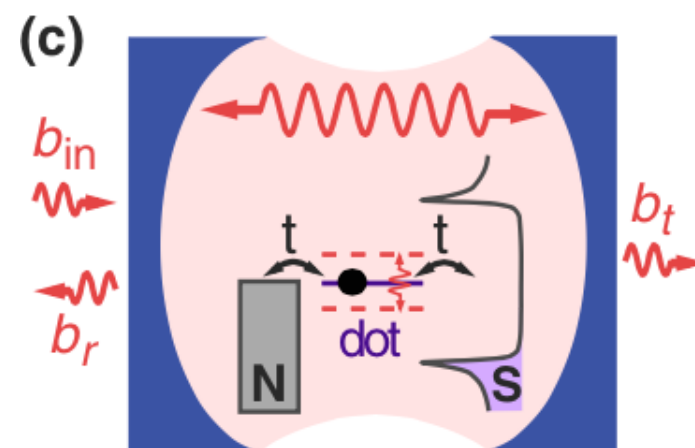
- Experiments are widely tunable: Access to new parameter regimes
- Many circuit geometries can be achieved : Thanks to versatile nano fabrication techniques



photon mediated
coupling between
two distant quantum
dots

Nano Lett. 15, 6620 (2015),

- Various types of Fermionic contacts: *Normal, Superconducting, Ferromagnetic*



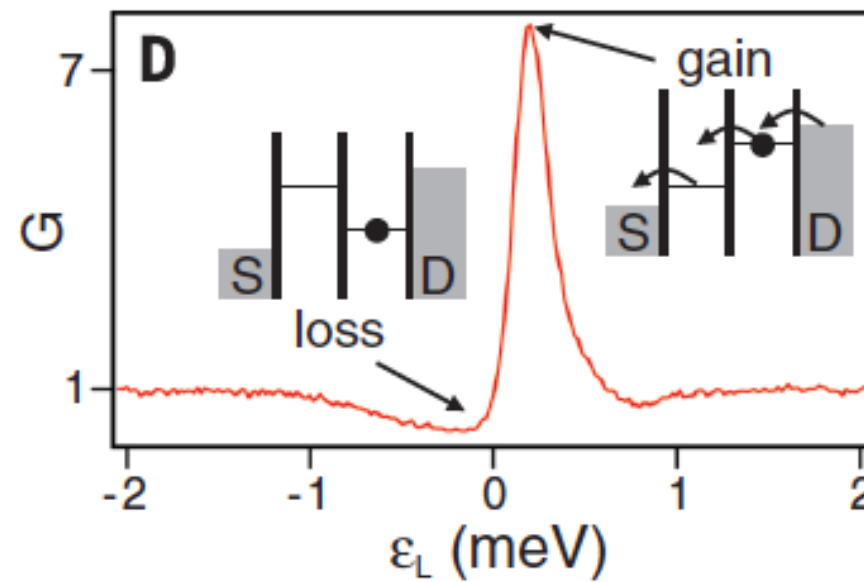
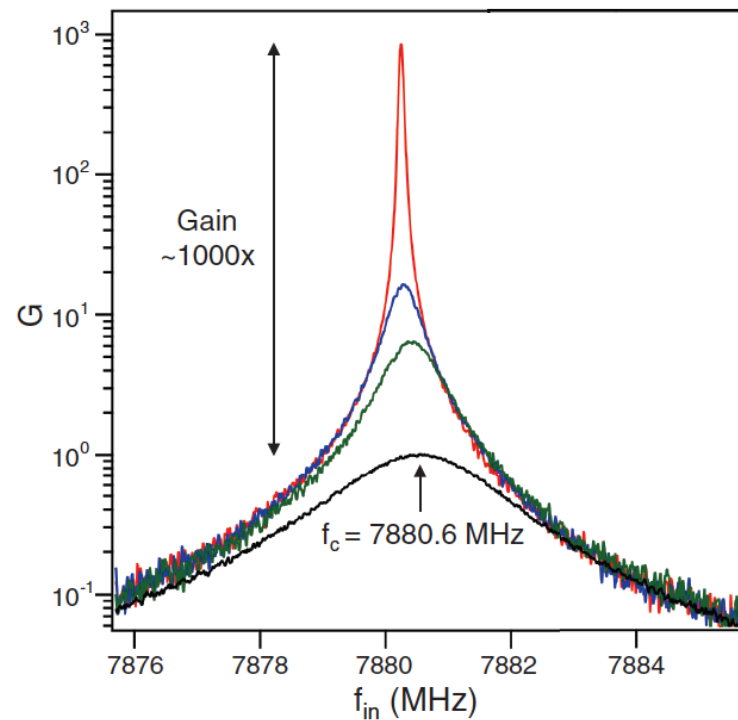
PHYS. REV. X **6**, 021014 (2016)

Excellent test bed to
answer fundamental
questions in quantum
optics and quantum
impurity systems

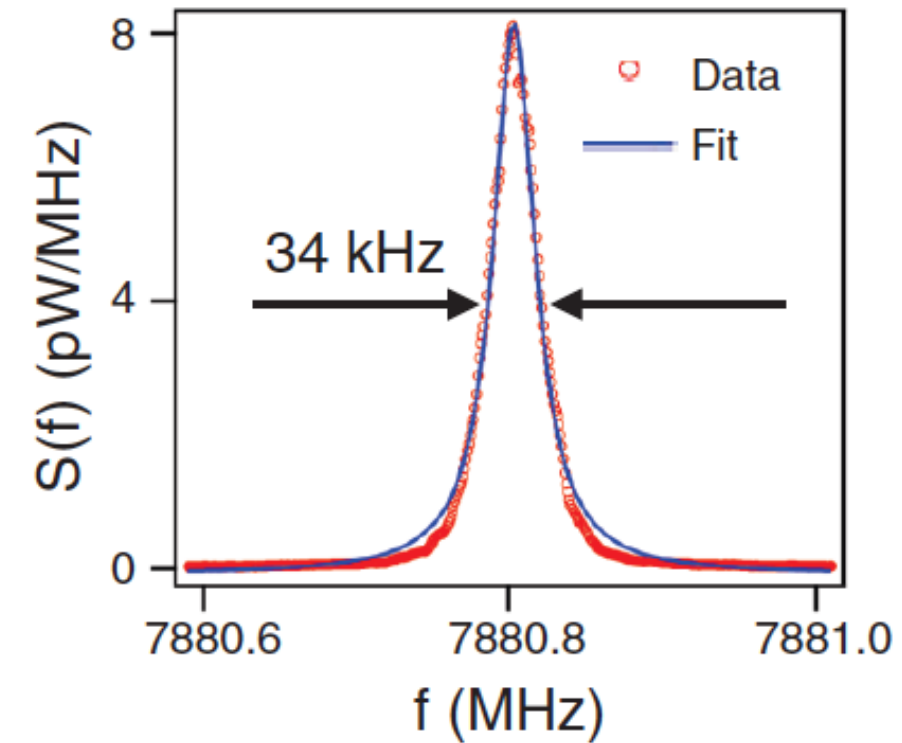
Experimental observables

Photonic Measurements:

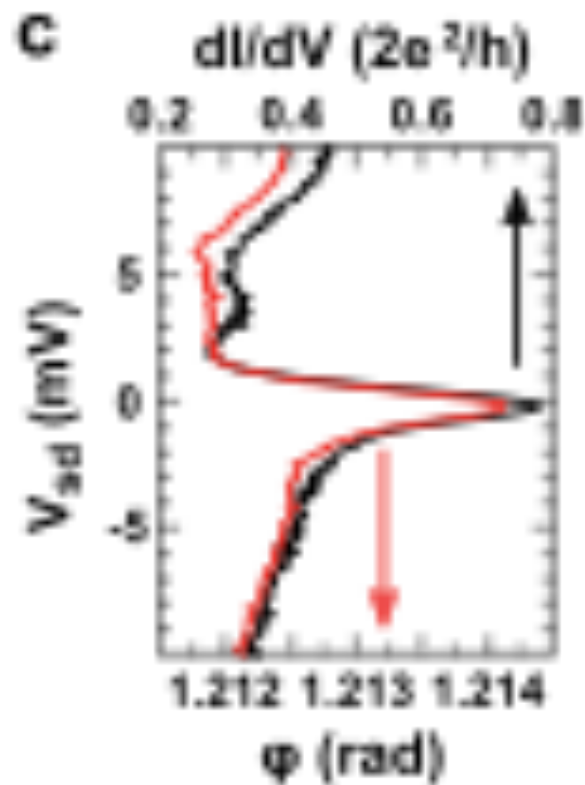
Photon Transmission (Gain)



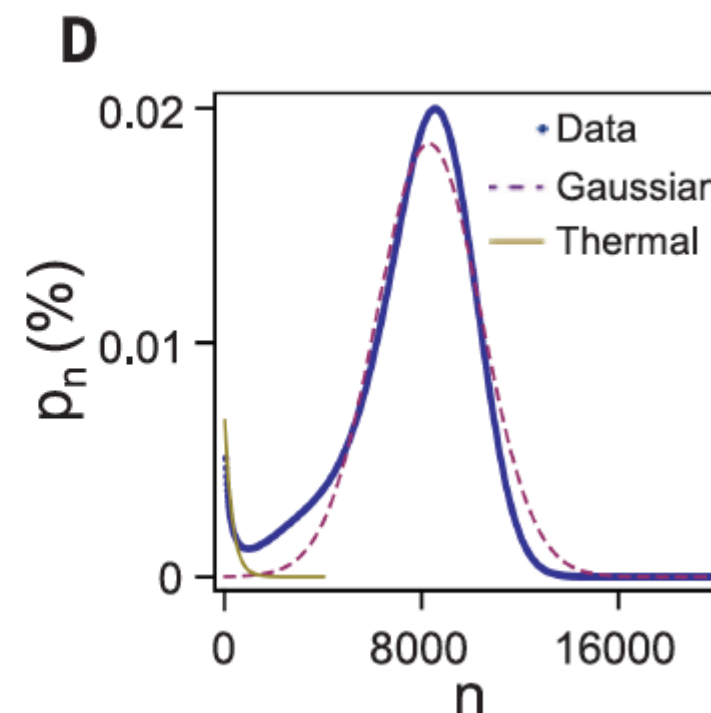
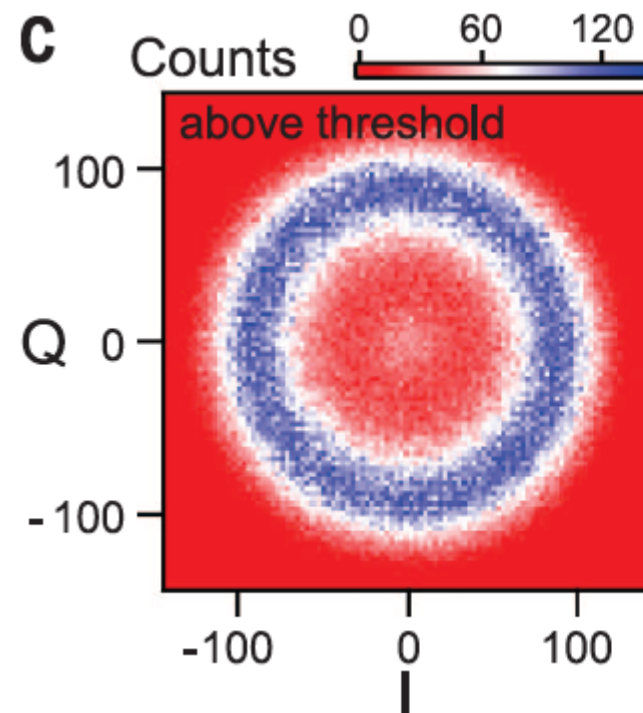
Emission Spectrum



phase spectroscopy



Photon counting statistics



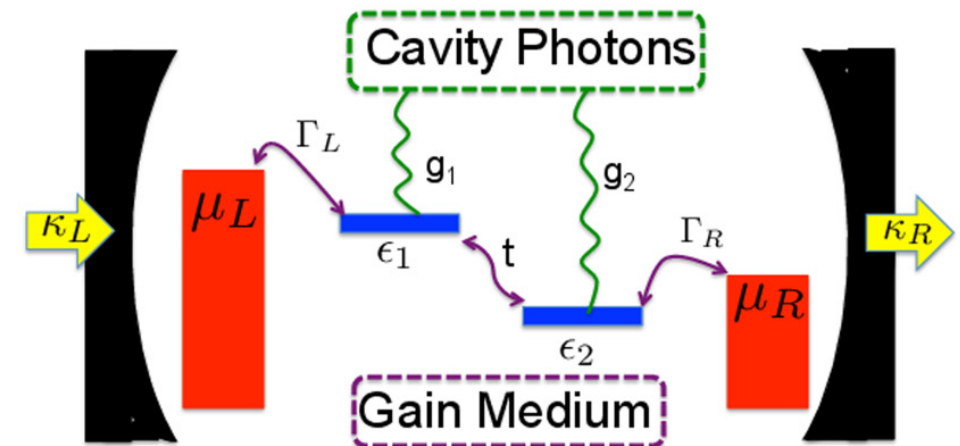
Model and Hamiltonian

$$\hat{H}_T = \hat{H}_{el} + \hat{H}_{ph} + \hat{H}_{el-ph}$$

$$\begin{aligned} \hat{H}_{el} = & \epsilon_1 \hat{c}_1^\dagger \hat{c}_1 + \epsilon_2 \hat{c}_2^\dagger \hat{c}_2 + t(\hat{c}_1^\dagger \hat{c}_2 + \hat{c}_2^\dagger \hat{c}_1) + \sum_{l \in L} \epsilon_l \hat{c}_l^\dagger \hat{c}_l \\ & + \sum_{r \in R} \epsilon_r \hat{c}_r^\dagger \hat{c}_r + \sum_{l \in L} v_l (\hat{c}_l^\dagger \hat{c}_1 + \hat{c}_1^\dagger \hat{c}_l) + \sum_{r \in R} v_r (\hat{c}_r^\dagger \hat{c}_2 + \hat{c}_2^\dagger \hat{c}_r) \end{aligned}$$

$$\hat{H}_{ph} = \omega_0 \hat{a}^\dagger \hat{a} + \sum_{j \in K} \omega_{jK} \hat{a}_{jK}^\dagger \hat{a}_{jK} + \sum_{j \in K} v_j \hat{a}_{jK}^\dagger \hat{a} + \text{H.c.}$$

$$\hat{H}_{el-ph} = [g_1 \hat{n}_1 + g_2 \hat{n}_2](\hat{a}^\dagger + \hat{a})$$



Keldysh diagrammatic nonequilibrium Green's function

$$D(\tau, \tau') \equiv -i \langle T_c \hat{a}(\tau) \hat{a}^\dagger(\tau') \rangle \quad \text{Photon}$$

$$D(\tau, \tau') = D_0(\tau, \tau') + \text{Diagram}$$

$$F_{el}(\tau_1, \tau_2) = -i \left[g_1^2 \text{Diagram}_1 + g_2^2 \text{Diagram}_2 + g_1 g_2 \text{Diagram}_3 + g_1 g_2 \text{Diagram}_4 \right]$$

Quantities of Interest

$$D(\tau, \tau') \equiv -i \langle T_c \hat{a}(\tau) \hat{a}^\dagger(\tau') \rangle$$



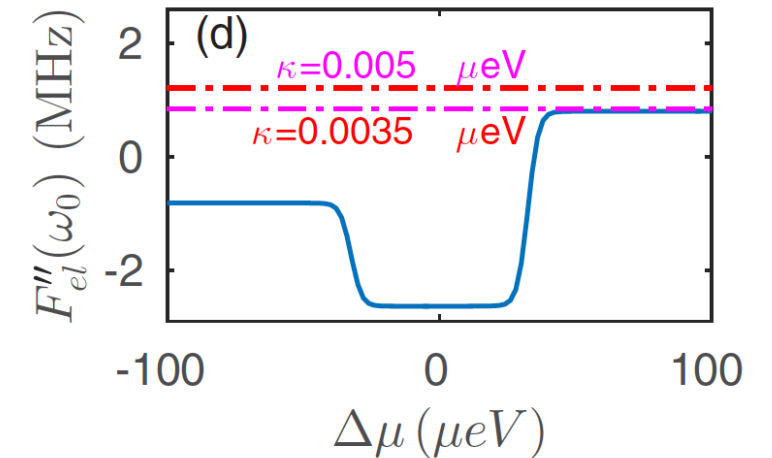
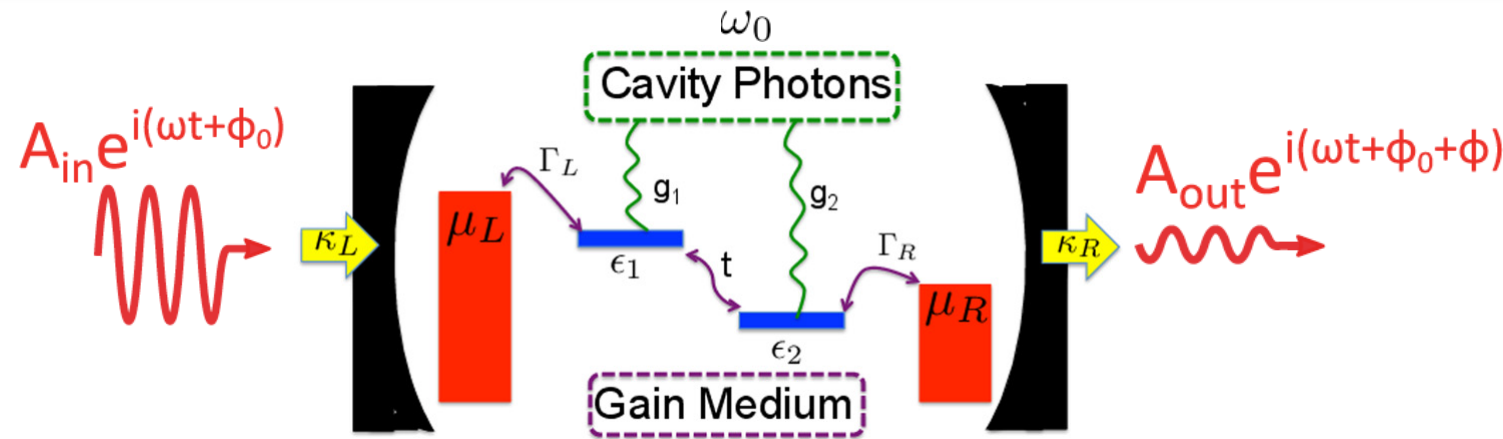
$$\langle \hat{n}_c \rangle \equiv i \int_{-\infty}^{\infty} \frac{d\omega}{2\pi} D^<(\omega) \quad \text{Photon number}$$

$$S(\omega) = \int_{-\infty}^{\infty} dt \langle \hat{a}^\dagger(0) \hat{a}(t) \rangle e^{i\omega t} = i D^<(\omega) \quad \text{Power Spectrum}$$

$$t(\omega) = \frac{i\kappa}{(\omega - \omega_0) + i\kappa - \chi_{el}^r(\omega)} = i\kappa D^r(\omega)$$

Transmission and Phase-Response

Principles for Giant Photon Gain



- Transmission function (GAIN) in microwave photon cavity decay rate

Response function of the cavity mode

$$D^r(t) = -i\theta(t)\langle[a(t), a^\dagger(0)]\rangle$$

$$t(\omega) \equiv i\kappa D^r(\omega) = \frac{i\kappa}{(\omega - \omega_0 - F'_{el}(\omega)) + i(\kappa - F''_{el}(\omega))}$$

Electronic Property: Flip signs for finite current

- Exact Result (NEGF):

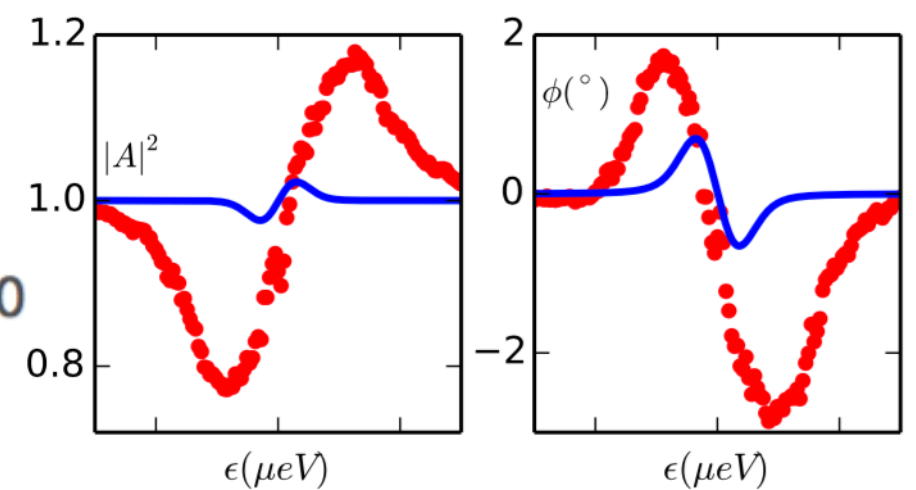
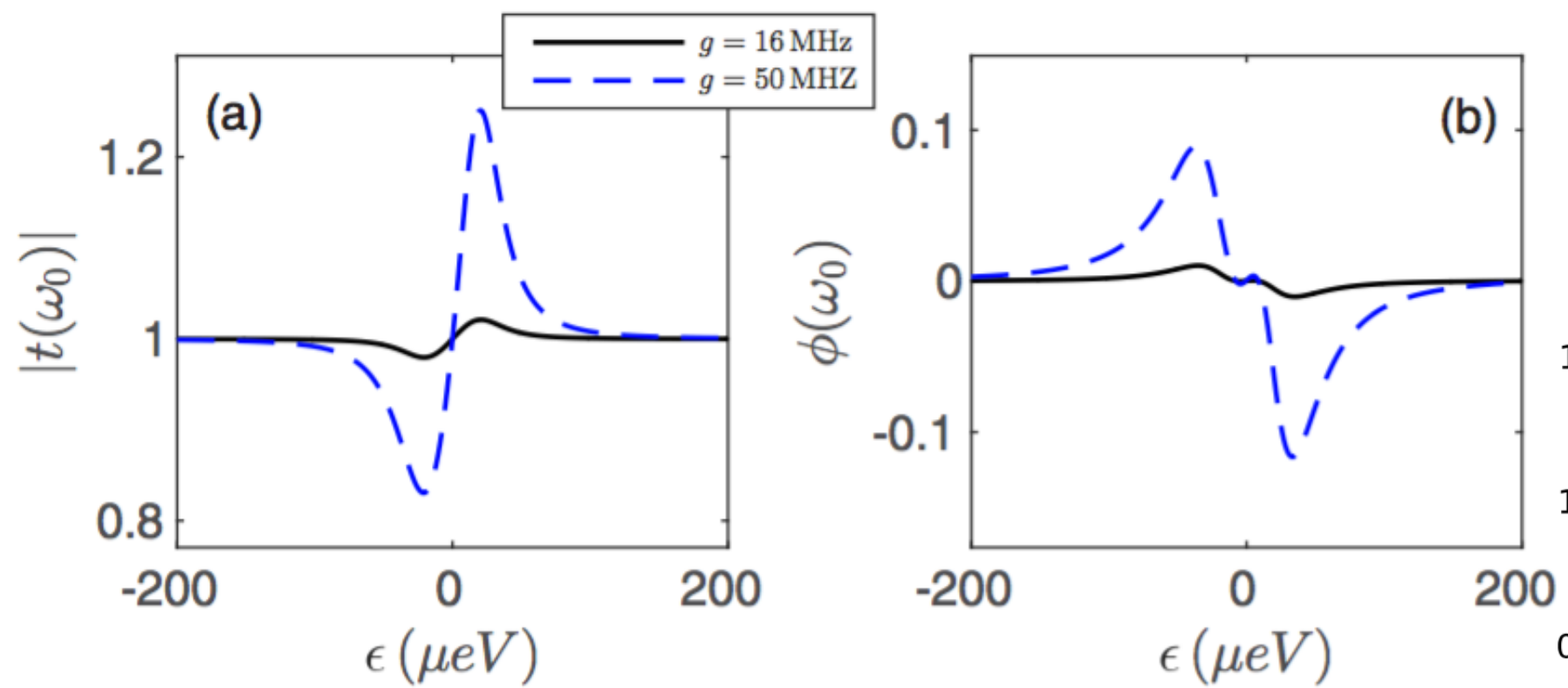
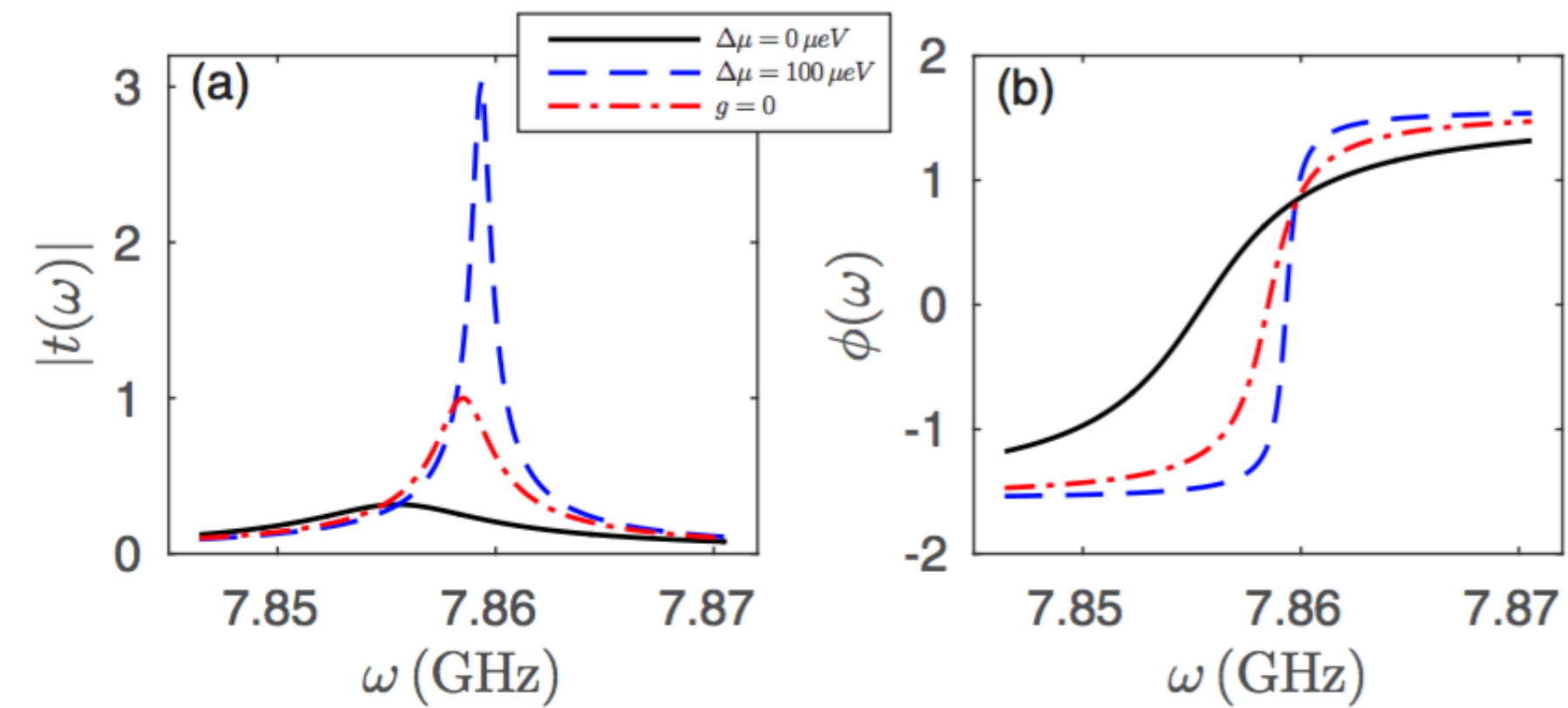
Sum Rule for Transmission

$$\int_{-\infty}^{\infty} \frac{d\omega}{2\pi} t(\omega) = \frac{\kappa}{2}$$

cavity decay rate

B. K. Agarwalla, M. Kulkarni, S. Mukamel, D. Segal, Phys. Rev. B, **94**, 035434 (2016)

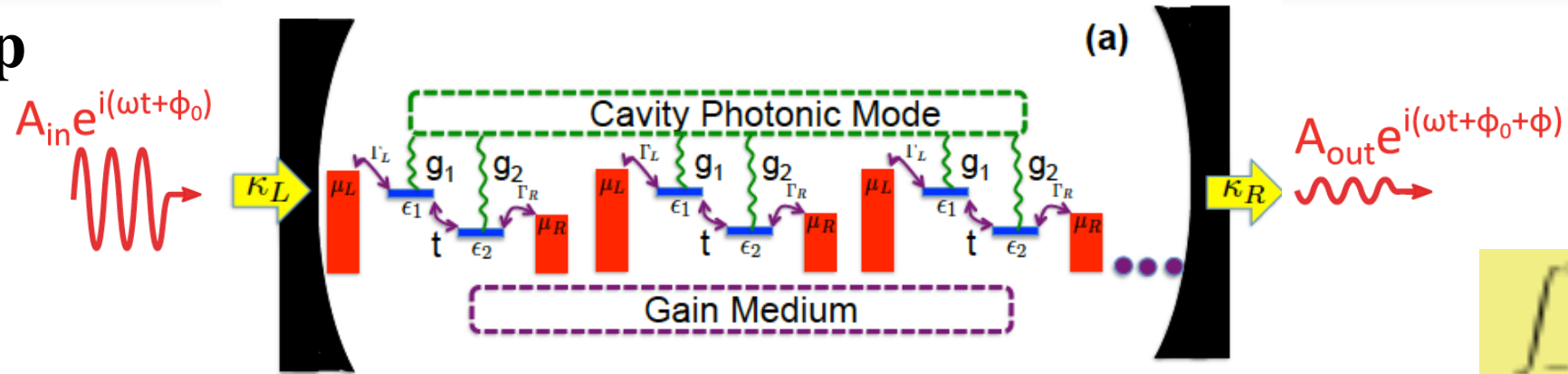
B. K. Agarwalla, M. Kulkarni, S. Mukamel, D. Segal, Phys. Rev. B, **94**, 121305 (R) (2016)



Princeton Experiment (Red)
Kulkarni, Cotlet, Tureci (PRB 2014)

Principles for Giant Photon Gain

○ N-DQD Setup



Sum Rule

$$\int_{-\infty}^{\infty} \frac{d\omega}{2\pi} t(\omega) = \frac{\kappa}{2}$$

Transmission
function

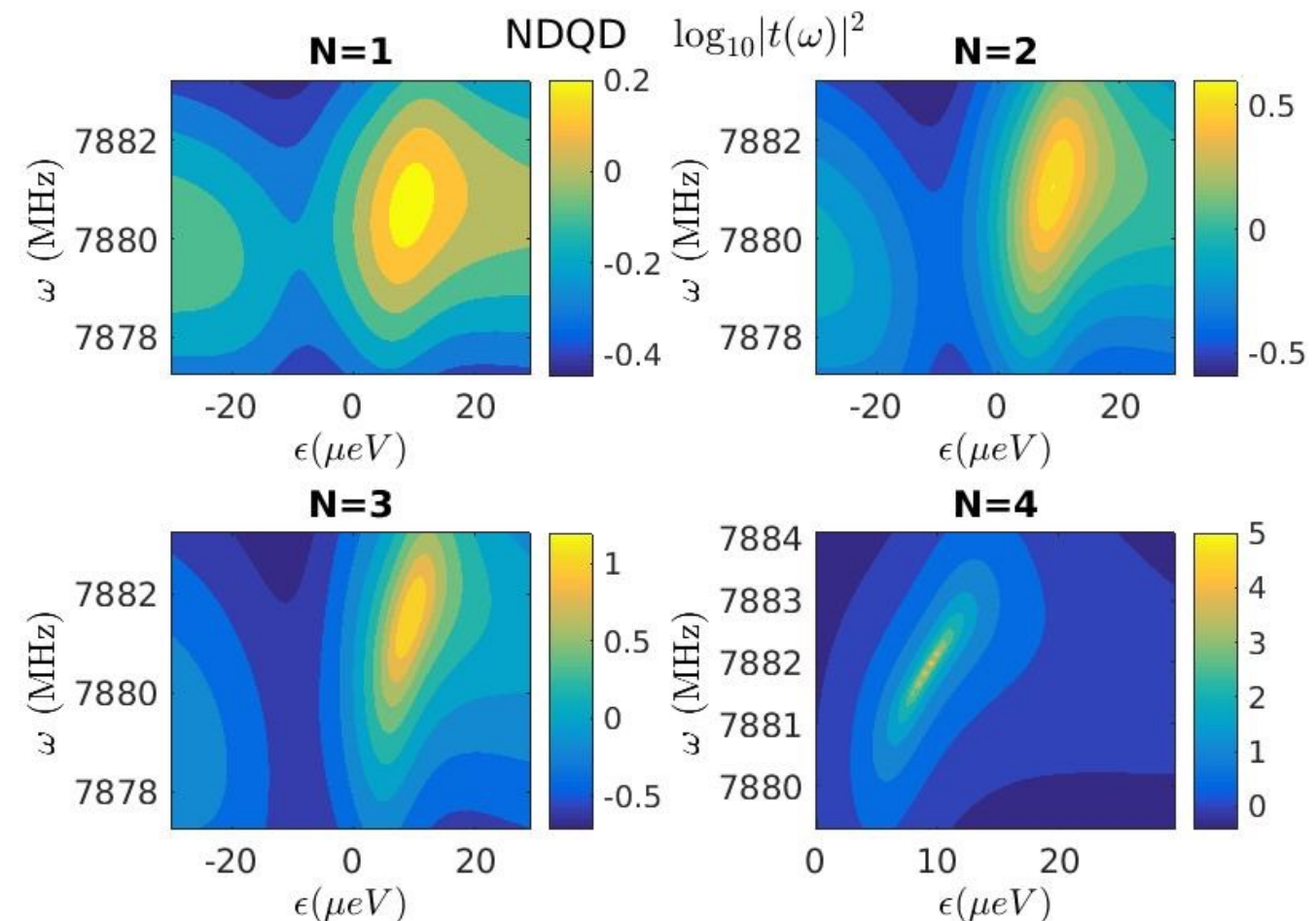
$$t(\omega) = \frac{i\kappa}{(\omega - \omega_0 - N F'_{el}(\omega)) + i(\kappa - N F''_{el}(\omega_0))}$$

○ Power Spectrum

$$S(\omega) = i \frac{N F_{el}^<(\omega)}{[\omega - \omega_c - N F'_{el}(\omega)]^2 + [\kappa - N F''_{el}(\omega)]^2}$$

○ Average photon number

$$\langle \hat{n}_c \rangle = \frac{i N F_{el}^<(\omega_c)}{2 [\kappa - N F''_{el}(\omega_c)]}$$



B. K. Agarwalla, M. Kulkarni, S. Mukamel, D. Segal,
Phys. Rev. B, **94**, 121305 (R) (2016)

Conclusions

- We study the photonic and electronic properties of a non-equilibrium quantum dot coupled to a micro wave resonator
- DQD electronic system can serve as a gain medium for the cavity photons
- Key for realizing photon-source quantum devices,
- Major step forward towards quantum Hamiltonian and bath engineering of hybrid quantum systems (fighting dissipation)
- Identified photon-induced contributions to the current at both positive and negative detuning.

Phys. Rev. B, **94**, 035434 (2016), Phys. Rev. B, **94**, 121305 (**R**) (2016)

Outlook

Non-perturbative method for treating electron-photon interactions in multi-terminal setups
(work in progress -- Lu, Wang, Jiang, **Kulkarni**)

Exploring photon statistics, masing (work in progress -- Agarwalla, **Kulkarni**)

Rectification/Diodes (work in progress --- Lu, Wang, Jiang, **Kulkarni**)

Understanding heavy Fermions / Kondo physics with photons