

Multi-phonon giant resonances

Observation of multi-phonon states

direct proof of vibrational character

 $E_n = n \cdot \hbar \omega$

- Existence
- Harmonicity of nuclear response
- Damping/Coupling of multi-phonon states
- 'Applications' (RHIC, LHC, RIB production)

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Quantized Harmonic Oszillator



FIG. 9.2. Multiphonon states of a one-dimensional linear harmonic vibrator of $J^{\pi} = 1^{-}$ phonons (IVGDR). After (EML94).



Two-phonon giant resonances were observed in:

• Double-charge exchange reactions: **DIAS**, **DGDR** ($\Delta T_z = \pm 2$) [Los Alamos]

S. Mordechai, H. Fortune, J. O'Donell, G.Lui, M. Burlein, A. Waosmaa, S. Greene, C. Morris, N. Auerbach, S. Yoo, and C. Moore, Phys. Rev. C41, 202 (1990).

Inelastic heavy-ion scattering : isoscalar DGQR [Orsay]

P. Chomaz and N. Frascaria, Phys. Rep. 252, 275 (1995)

[GSI]

• Relativistic Coulomb breakup: isovector **DGDR** ($\Delta T_z = 0$)

T. Aumann, P. F. Bortignon, and H. Emling, Ann. Rev. Nucl. Part. Sci. 48, 351 (1998).

[early review articles]



Double charge-exchange reaction $({}^{+}\pi, {}^{-}\pi)$

<u>Features of $((\pi, \pi, \pi)$ reaction:</u>

 $\Delta S = 0$ in forward scattering (pion is spinless) $\Delta T = 2$; $\Delta T_z = -2$; $T = T_z$ favored

IAS and GDR strongly populated in pion reactions (pion strongly absorbed at nucl. surface + surface-peaked IAS,GDR transition density)

Experiments performed at LAMPF / Los Alamos, pion energies 200 – 300 MeV + EPICS spectrometer



Double charge-exchange reactions $({}^{+}\pi, {}^{-}\pi)$





LAMF data [MOR96]

Double charge-exchange reactions $({}^{+}\pi, {}^{-}\pi)$

short SUMMARY:

DGDR systematically observed in $A = 12 \dots A = 197$ nuclei

excitation energy and width within expectation for a sequential excitation

angular distributions show $\Delta L = 2$ pattern

But: cross sections difficult to analyze $\Delta L = 0$ component seemingly missing

Double isoscalar GQR

Evidence for

two-phonon giant quadrupole resonance

from direct-proton decay

(missing mass spectra, ⁴⁰Ca + ⁴⁰Ca)

J.A.Scarpaci et al., Phys.Rev.Lett., 1994









Double-Phonon Giant Dipole Resonance (DGDR)



Relativistic heavy-ion collisions

LARGE cross sections :

- ~ barns for GDR
- ~ 100 mb for DGDR



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PHYSICAL REVIEW LETTERS

1 FEBRUARY 1993

First Observation of the Coulomb-Excited Double Giant Dipole Resonance in 208 Pb via Double- γ Decay

J. Ritman, F.-D. Berg, W. Kühn, V. Metag, R. Novotny, M. Notheisen, P. Paul,^(a) M. Pfeiffer, and O. Schwalb II. Physikalisches Institut, Universität Giessen, Giessen, Germany

> H. Löhner and L. Venema KVI Groningen, Groningen, The Netherlands

A. Gobbi, N. Herrmann,^(b) K.D. Hildenbrand, J. Mösner,^(c) R.S. Simon, K. Teh, J. P. Wessels, and T. Wienold^(b) Gesellschaft für Schwerionenforschung Darmstadt, Darmstadt, Germany (Received 4 September 1992)





Double-photon decay:

10⁻⁴ branch

DGDR and TGDR – summary of results LAND collaboration

K. Boretzky et al., Phys.Rev.C 68, 024317 (2003)

S. Ilievski et al., Phys. Rev. Lett. (2004)



LAND experimental setup&method

The invariant mass measurement



The experiment

- ▶ e.g., ²⁰⁸Pb ~ 500 MeV/A
 ▶
- select projectile breakup
 - (neutron emission)
- background measured with empty target
- nuclear contribution measured with C target

Excitation energy – from kinematically complete measurement of momenta of all outgoing particles:

$$\left(m_{proj} + E^{*}\right)^{2} = \left(\sum_{j} P_{j}\right)^{2}$$



cross section dg/dE [mb/MeV]

10²

10²

10

1

10²

0

10

20

30

Pb (thin)

Ō

10

20

Ho

please notice perfect fit of one-phonon part



Pb (thick)

╧┿┯┯ጚ

30

— K. Boretzky et al., Phys.Rev.C 68, 024317 (2003)

excitation energy E* [MeV]







quick look into the decay of DGDR



→ Maxwell distribution (here, linearized)

Harmonic response?

Deviations from harmonic response:

- Splitting of $I^{\scriptscriptstyle\rm T}=0^{\scriptscriptstyle+}$ and $I^{\scriptscriptstyle\rm T}=2^{\scriptscriptstyle+}$ states
- Shifts in centroid energy





FIG. 9.2. Multiphonon states of a one-dimensional linear harmonic vibrator of $J^{\pi} = 1^{-}$ phonons (IVGDR). After (EML94).

Harmonic response?

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MULTIPHONONS



FIG. 9.2. Multiphonon states of a one-dimensional linear harmonic vibrator of $J^{\pi} = 1^{-}$ phonons (IVGDR). After (EML94).

The Double-Phonon Giant Dipole Resonance in ¹³⁶Xe, ²⁰⁸Pb, and ²³⁸U K. Boretzky et al.



' Cross section enhancement ' evoked many discussions

Anharmonicities ?

but also many attemptsto find explanationby means of other effects

'Mixed' – Phonon Contributions



II. Dynamical Effects

See papers: B. Carlsson et al., Gu and Weidenmueller





mass number



P.F. Bortignon and C.H. Dasso, Phys. Rev. C 56, 574 (1997).

PHYSICAL REVIEW C

VOLUME 56, NUMBER 1

JULY 1997

Anharmonic effects in the excitation of double-giant dipole modes in relativistic heavy-ion collisions

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We investigate the consequences of anharmonic terms in the vibrational spectrum of giant dipole resonances for the double Coulomb excitation of such modes in relativistic heavy-ion collisions. It is found that apparent discrepancies between the results of two separate experiments <u>can be put in harmony assuming minor depar-</u> tures from the harmonic limit because of the special features of the reaction mechanism.





FIG. 1. Calculations for the reaction 208 Pb + 208 Pb at a bombarding energy of 640.4 MeV. Top: Probability for the excitation of the second $\lambda = 1$ state in lead as a function of the anharmonicity parameter *B*. The values are normalized to the harmonic case (*B* = 0). Bottom: Ratio between the energy of the "two-phonon" state and twice the energy of the "one-phonon" state in lead as a function of the anharmonicity parameter *B*. The full-drawn and dashed curves correspond, respectively, to the components with angular momentum *L*=2 and 0. Unperturbed values for the mode are $\hbar \omega_0 = 13.4$ MeV and mass parameter d = 1.2 MeV \hbar^2 . The calculations are for an impact parameter b = 30 fm. The shaded area indicates the range of values of *B* that leads to enhancements of about 30%.



FIG. 2. Analogous to Fig. 1 but for the reaction ${}^{136}Xe + {}^{208}Pb$ at a bombarding energy of 700.4 MeV. Unperturbed values for the mode in xenon are $\hbar \omega_0 = 15.2$ MeV and mass parameter d = 0.8 MeV \hbar^2 . The shaded area in this case has been obtained from that in Fig. 1 exploiting the mass-scaling law discussed in the text.

PHYSICAL REVIEW C, VOLUME 64, 064605

Anharmonicities of giant dipole excitations

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(Received 26 July 2001; published 16 November 2001)

$$H = H_0 + F(x, y, z; t),$$
 (1)

where H_0 is the anharmonic oscillator describing the intrinsic motion of the projectile,

$$H_{0} = \frac{1}{2D} (p_{x}^{2} + p_{y}^{2} + p_{z}^{2}) + \frac{C}{2} (x^{2} + y^{2} + z^{2}) + \frac{B}{4} (x^{2} + y^{2} + z^{2})^{2}, \qquad (2)$$

$$H_0 = \hbar \omega \left[\frac{1}{2} (\pi^2 + \rho^2) + \beta \rho^4 \right].$$
 (4)

In the above, the commonly used variable transformations

$$\rho_i = \sqrt{\frac{D\omega}{\hbar}} r_i; \quad \pi_i = \frac{p_i}{\sqrt{D\hbar\omega}},$$
(5)

have been made, where r_i and p_i stand for the components of the position and momentum operators, respectively. The oscillator frequency is given by

$$\hbar \omega = \hbar \sqrt{\frac{C}{D}}$$
, (6)



ANHARMONICITIES OF GLANT DIPOLE EXCITATIONS



FIG. 2. The enhancement in the excitation of the DGDR in the collision of 208 Pb+ 208 Pb at 640.4 MeV for the impact parameter b = 30 fm. The solid line represents the results of the present calculation while the dashed line corresponds to a constant oscillator frequency.



FIG. 3. Enhancement factor of the (a) DGDR and (b) GDR cross sections in the collision of ²⁰⁸Pb+²⁰⁸Pb at 640.4 MeV. The dashed lines correspond to the results obtained with fixed oscillator frequency, while the full lines correspond to a fixed E_{GDR} .



FIG. 1. The ratio $E_{DGDR}^{l}/(2 E_{GDR})$ vs the anharmonicity para eter *B*, for ²⁰⁸Pb. The solid line is for l=2 and the dashed line l=0. The reduced mass for the oscillation of protons against n trons is used for the mass parameter *D*.

and the dimensionless strength β is related to B as

$$B = \left[\frac{4(\hbar\omega)^3 D^2}{\hbar^4}\right]\beta.$$

$$\begin{split} E_{DGDR}^{l=0}(\beta) &= 2\hbar\omega(1+7.5\beta), \\ E_{DGDR}^{l=2}(\beta) &= 2\hbar\omega(1+6\beta), \\ \langle GDR \| E1 \| GS \rangle &= e \left(\frac{S_1}{\hbar\omega} \right)^{1/2} (1-2.5\beta), \\ \langle DGDR, l &= 0 \| E1 \| GDR \rangle &= e \left(\frac{S_1}{\hbar\omega} \right)^{1/2} \sqrt{\frac{2}{3}} (1-5\beta), \\ \langle DGDR, l &= 2 \| E1 \| GDR \rangle &= e \left(\frac{S_1}{\hbar\omega} \right)^{1/2} \sqrt{\frac{10}{3}} (1-3.5\beta), \\ S_1 &= \frac{9}{4\pi} \frac{\hbar^2}{2m_0} \frac{NZ}{A}. \end{split}$$

 $E_{GDR}(\beta) = \hbar \omega (1+5\beta).$

In order to maintain $E_{GDR}(\beta)$ at the experimental value, namely, $E_{GDR}(\beta) = E_{GDR}^{exp}$ (13.4 MeV, in the present case), the oscillator frequency must be renormalized as β is changed. The resulting renormalized frequency, from Eq. (8), is

$$\hbar\,\omega(\beta) = \frac{E_{GDR}^{\exp}}{(1+5\,\beta)}.\tag{11}$$



Triple – Phonon GDR ?

relativistic Coulomb-Fission of ²³⁸U





simple-minded argument:

Multi-phonon states are located at increasing excitation energy + Fission probability increases steeply with excitation energy

Higher-phonon states appear enriched in fission channel (relative to neutron evaporation channel)







Evidence for multi-phonon giant resonances in electromagnetic fission of ²³⁸U

S. Ilievski,^{1,2} T. Aumann,² K. Boretzky,^{1,3}, Th.W. Elze,¹ H. Emling,² A. Grünschloß,¹ J. Holeczek,⁴

R. Holzmann,² C. Kozhuharov,² J.V. Kratz,³ R. Kulessa,⁴ A. Leistenschneider,¹ E. Lubkiewicz,⁴ T. Ohtsuki,^{3,5} P. Reiter,⁶ H. Simon,⁷ K. Stelzer,¹ J. Stroth,² K. Sümmerer,² E. Wajda,⁴ and W. Waluś⁴ (LAND Collaboration)



FIG. 1: Elemental distribution of fission fragments of 238 U projectiles (500 MeV/nucleon) in a lead target in coincidence with neutrons of a mean multiplicity $\cdot \cdot_n \cdot$ as indicated. The sum of the nuclear charges of the two fission fragments is required to equal 92.

Experiment:

Land setup equipped with fission-fragment detectors

measure neutron multiplicity in coincidence to fission fragments

<u>use neutron multiplicity as a</u> <u>measure for excitation energy</u> *(from literature)*







FIG. 2: Fission cross sections $\cdots d$ for ²³⁸U (500 MeV/nucleon). The axis labels refer to detector multiplicity \cdot_d , associated mean neutron multiplicity $\cdot_n \cdot$, and mean excitation energy $\cdot \cdot \cdot$.

(a) Measured values for Pb and C targets.

(b) Measured electromagnetic fission cross sections for Pb target and calculated values (solid line). Calculated cross sections for the sum of single-phonon (multi-phonon) components is shown as dotted (dashed) curve.

(c) same as (b) but for the Sn target.

TABLE II: Calculated partial electromagnetic fission cross sections $\cdots e^{mf}$ and their peak energies \cdot_p for single and multi-phonon giant resonances in ²³⁸U (500 MeV/nucleon) on Pb and Sn targets.

Resonance	• $_{p}(MeV)$	• • • • ^{emf}	• • • • ^{em f}
		(Pb)	(Sn)
GDR	13.5	.66	.75
GQR_{is}	9.5	.07	.07
GQR_{iv}	21.	.06	.07
GDR⊗GDR	23.	.15	.09
$GDR \otimes GQR_{is}$	21.	.02	.01
$GDR \otimes GQR_{iv}$	32.	.013	.008
$GDR \otimes GDR \otimes GDR$	35.5	.023	.006



Summary

Two-phonon giant resonances were observed

• Double-charge exchange reactions: DIAS , DGDR ($\Delta T_z = \pm 2$) [Los Alamos]

- Inelastic heavy-ion scattering : isoscalar DGQR [Orsay, GANIL]
- Relativistic Coulomb breakup: DGDR ($\Delta T_z = 0$) [LAND, GSI]

T. Aumann, P. F. Bortignon, and H. Emling, Ann. Rev. Nucl. Part. Sci. 48, 351 (1998).

• Evidence for triple-phonon GDR

Harmonic Response (within ~ 10%)



Physics with Rare-Isotope Beams

RIKEN, FRIB, SPIRALII, FAIR, EURISOL

Here: future FAIR facilities emphasis on GR related topics



Preparing for FAIR (Startversion) ~2017/18



RIB -Intensity increase 3-4 orders of magnitude !

H. Simon • The ELISe electron rare isotope scattering exp. ..



External – Target Experiments (R³B) (*T. Aumann*)

Storage and Cooler Rings (EXL) (P. Egelhof)

Electron – Ion collider (ELISe) (H. Simon - coordinator)



Exotic nuclei and light-ion / electron

scattering - shopping list

Experimental method	Light-ion scattering Electron scattering	relevant observables in Exotic nuclei	
elastic scattering (p,p) (e.e)	nuclear matter distribution charge distribution	(neutron) Halo and Skin	
inelastic scattering (p,p'); (⁴ He, ⁴ He') (e.e')	surface collective states electric giant resonances	new collective modes	
charge exchange (p,n); (d, ² He); (³ He,t)	spin-isospin excitations;	(stellar) weak interaction rates;	
transfer reaction (p,d); (d, ³ He); (p,t)	spectroscopic factors	single-particle structure	
quasi-free scattering (p,2p); (p,np); (p, p ⁴ He) (e,e'p)	single-particle spectral function; cluster knockout	(inner-shell) single-particle structure nucleon-nucleon (cluster) correlations	
		EXL collaboration	

Light-Ion scattering in STORAGE RING:

Elastic (p,p) ... Inelastic (p,p'), (α, α') ... Charge exchange: (p,n), $({}^{3}He,t)$, $(d,{}^{2}He)$... Quasifree (p,pn), (p,2p), $(p, p\alpha)$... Selective Spin-Isospin probes

 Form factor sensitive to transition multipolarity



Feasibility

Target: 1014 H atoms cm-2; beam loss included740 AMeV100 AMeV

Nucleus	production rate [1/s]	Lifetime including losses in NESR [s]	Luminosity [cm ⁻² s ⁻¹]	Luminosity [cm ⁻² s ⁻¹]
¹¹ Be	2 x 10 ⁹	36	> 10 ²⁸	> 10 ²⁸
⁴⁶ Ar	6 x 10 ⁸	20	> 10 ²⁸	> 10 ²⁸
⁵² Ca	4 x 10 ⁵	12	2 x 10 ²⁶	8 x 10 ²⁵
⁵⁵ Ni	8 x 10 ⁷	0.5	5 x 10 ²⁶	~ 10 ²⁵
⁵⁶ Ni	1 x 10 ⁹	3800	> 10 ²⁸	> 10 ²⁸
⁷² Ni	9 x 10 ⁶	4.1	1 x 10 ²⁷	4 x 10 ²⁶
¹⁰⁴ Sn	1 x 10 ⁶	51	2 x 10 ²⁷	1 x 10 ²⁷
¹³² Sn	1 x 10 ⁸	93	> 10 ²⁸	> 10 ²⁸
¹³⁴ Sn	8 x 10 ⁵	2.7	3 x 10 ²⁵	7 x 10 ²⁴
¹⁸⁷ Pb	1 x 10 ⁷	34	2 x 10 ²⁸	5 x 10 ²⁷

Typical cross sections : 0.1 – 100 mb/sr

Performance

Elastic proton scattering ¹³²Sn

(Matter Distribution)

Inelastic alpha scattering on Sn isotopes

(Giant Monopole Resonance)



EXL: EXotic Nuclei Studied in Light-Ion Induced Reactions at the NESR Storage Ring



ESR at GSI Storage-cooler ring

Start up of part of the EXL physics program with ⁵⁶Ni

Spokesperson: Nasser Kalantar (KVI), Co-spokesperson: Peter Egelhof (GSI), GSI contact: H. Weick (GSI); for the EXL collaboration



<u>(p,p), (α,α'), (³He,t) reactions</u>

⁵⁶Ni: doubly magic

- (p,p) reactions: nuclear matter distr -skin
- (α,α`) reactions: giant resonances
 ISGMR, IVGDR, parameters of the EOS
- (³He,t) reactions: Gamow-Teller matrix elements, important for astrophys.



EXL collaboration see P. Egelhof

Alternative – active target MAYA @ GANIL





C. Monrozeau *et al.*, Phys. Rev. Lett. **100**, 042501 (2008)



The ELISe electron rare isotope scattering experiment



Realization of an RIB electron collider setup The **ELISe** experiment

Haik Simon • GSI / Darmstadt



- 125-500 MeV electrons
- 200-740 MeV/u RIBs

→ up to 1.5 GeV CM energy

 spectrometer setup at the interaction zone & detector system in ring arcs

http://www.gsi.de/fair/reports/btr.html

AIC option:

- 30 MeV antiprotons
- detector system in ring arcs
- schottky probes



H. Simon • The ELISe electron rare isotope scattering exp. ...



Expected Luminosities



Competing project: SCRIT for RARF Test setup @ KSR Kyoto Univ. 100 MeV/100mA

SCRIT (Self-Confining RI Target)

e-beam

Courtesy: Toshimi Suda RIKEN/RARF

Scattered electron



Bright future -_ a lot to do