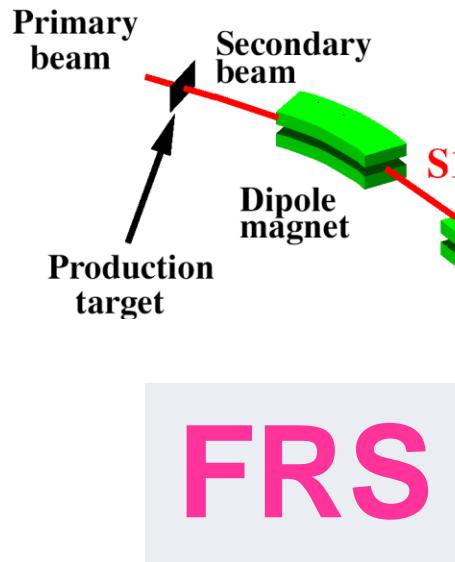


# *Nuclear structure studies through in-flight measurements*

Today

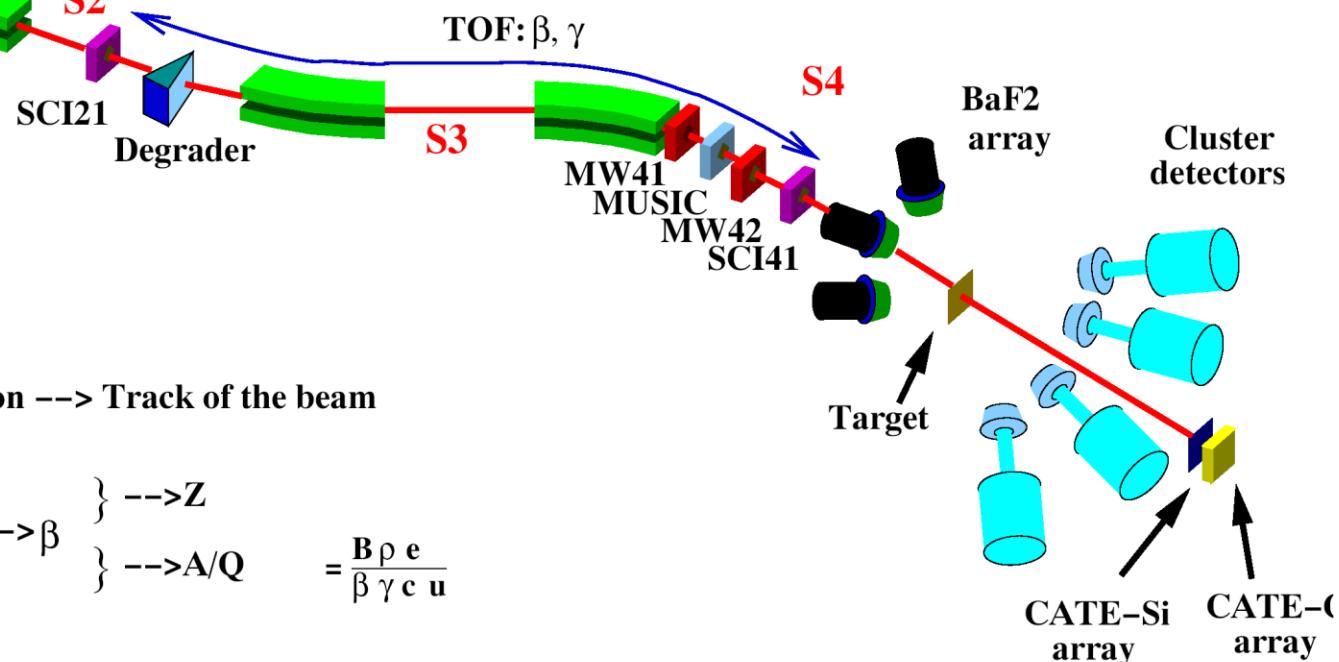
- 3. Physics case: ,Shell model and isospin symmetry'
- 4. Physics case: ,Neutron deficient Sn nuclei and the seniority scheme'
- $\gamma$ -ray tracking Part I

# High resolution $\gamma$ -spectroscopy at the FRS



FRS provides secondary radioactive ion beams:

- fragmentation and fission of primary beams
- high secondary beam energies: 100 – 500 MeV/u
- fully stripped ions



MW41, 42 x y --> Position --> Track of the beam

MUSIC --> dE

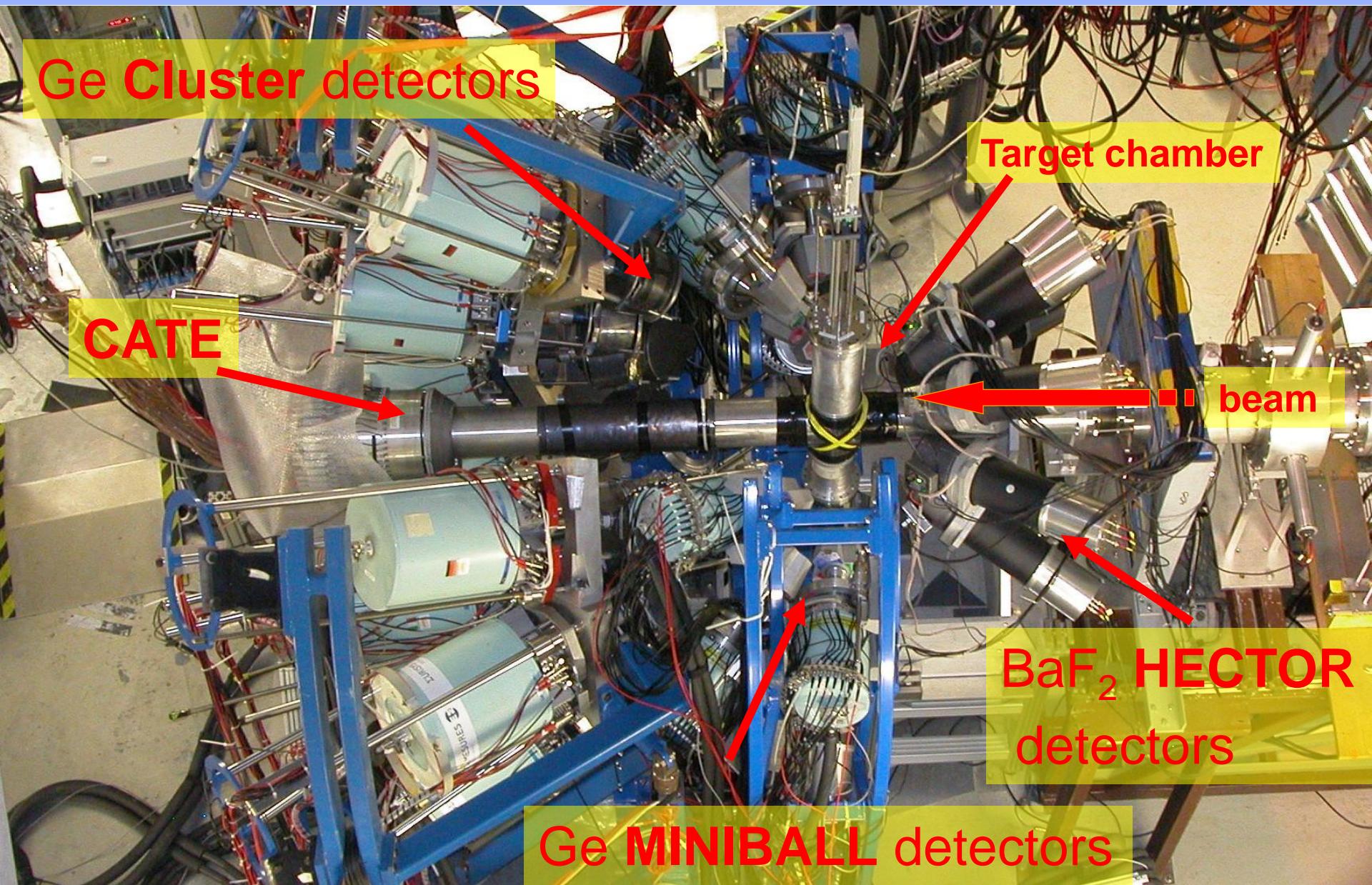
SCI 21, 41 --> TOF -->  $\beta$       } --> Z

D. Magnet --> B  $\rho$

$$= \frac{B \rho e}{\beta \gamma c u}$$

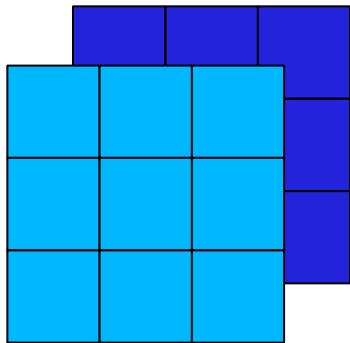
## RISING

# RISING experimental setup



# CALorimeter TElescope CATE Particle Identification and Tracking after Target

R. Lozeva et al, NIM B, 204 (2003) 678

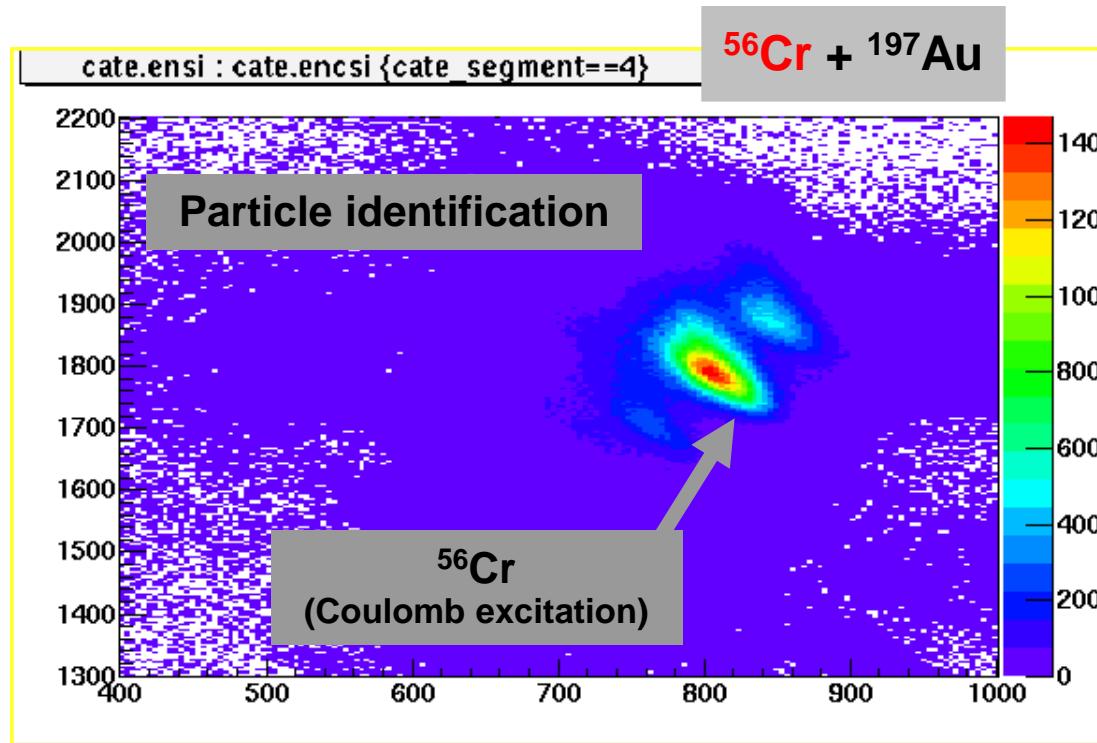


$\Delta E$

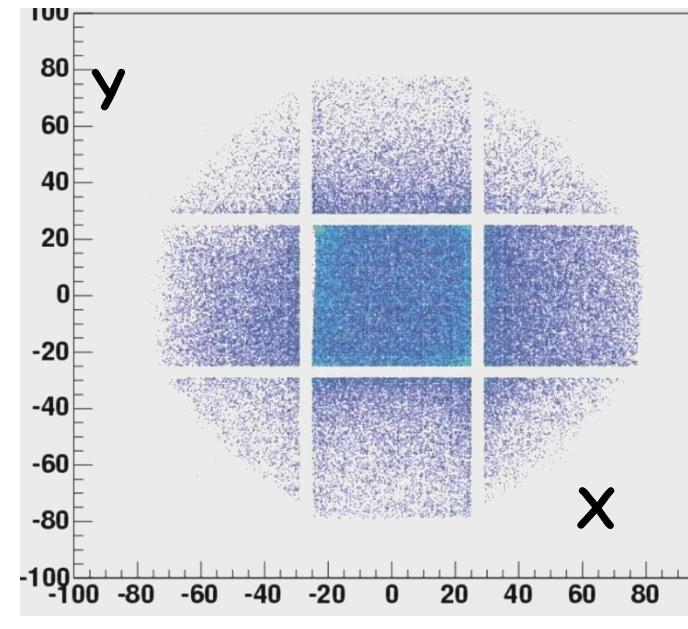
- 0.3 mm thick Si detectors
- Z identification
- Position sensitive

E

- Čsl detectors
- Z identification



Tracking after target

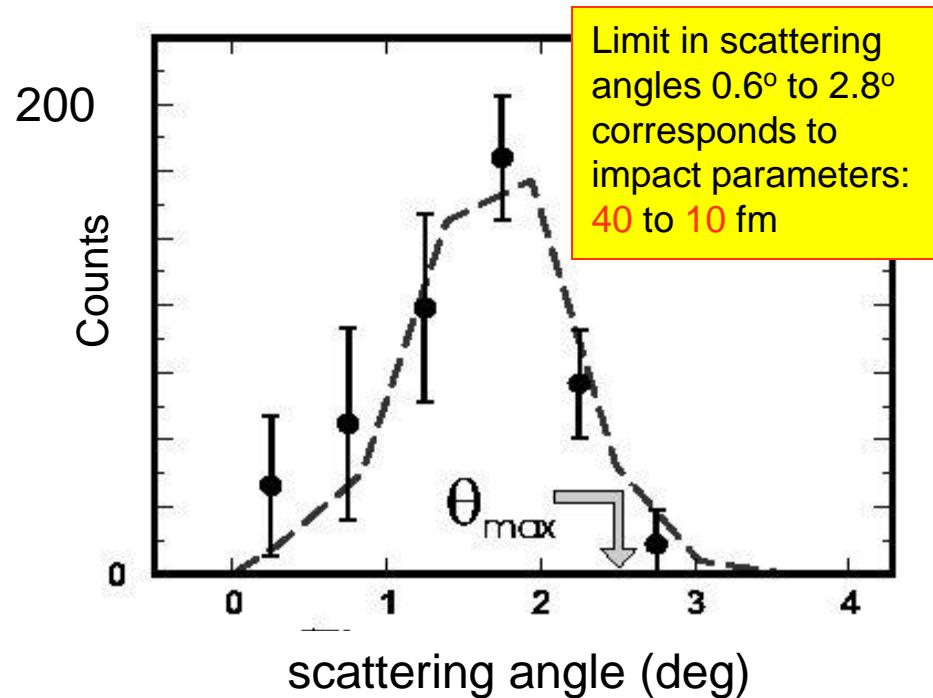
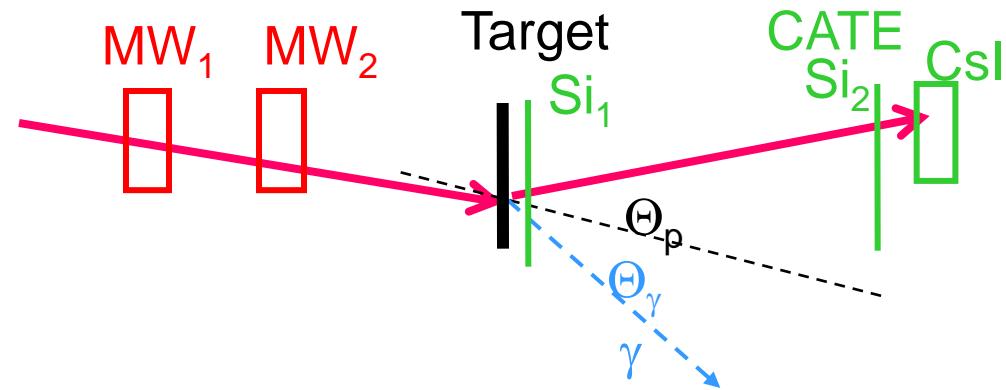
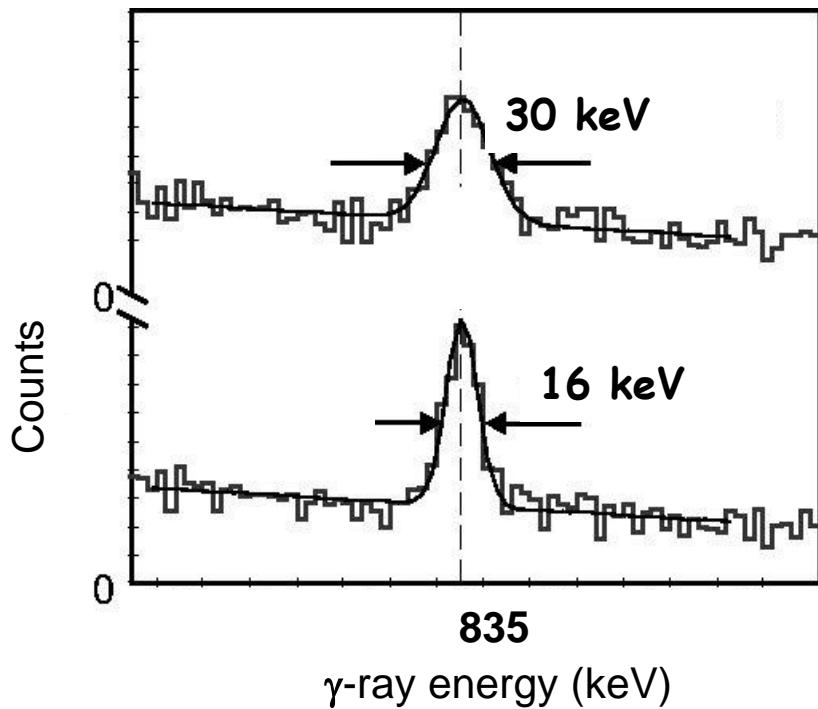


# Tracking:

- Doppler correction
- scattering angle

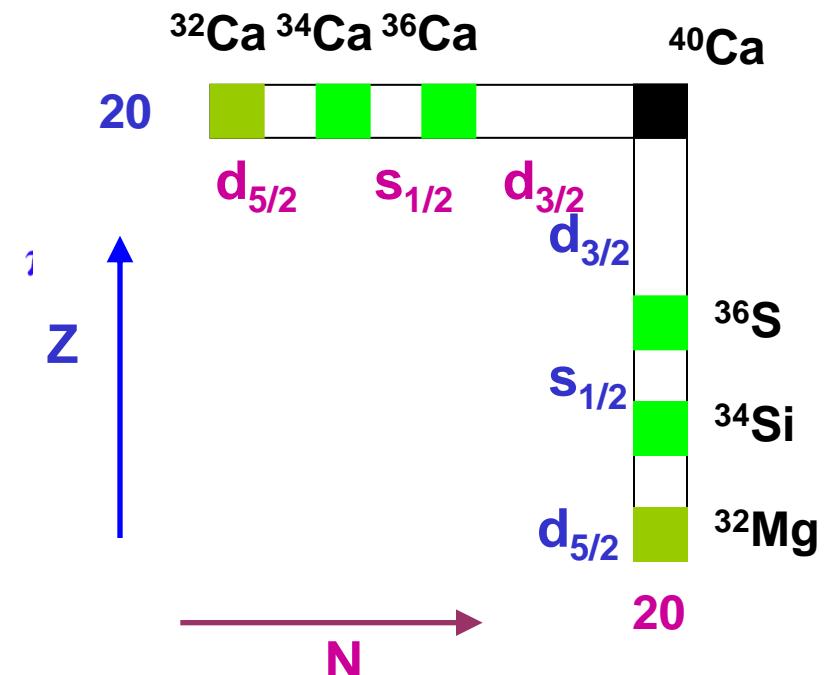
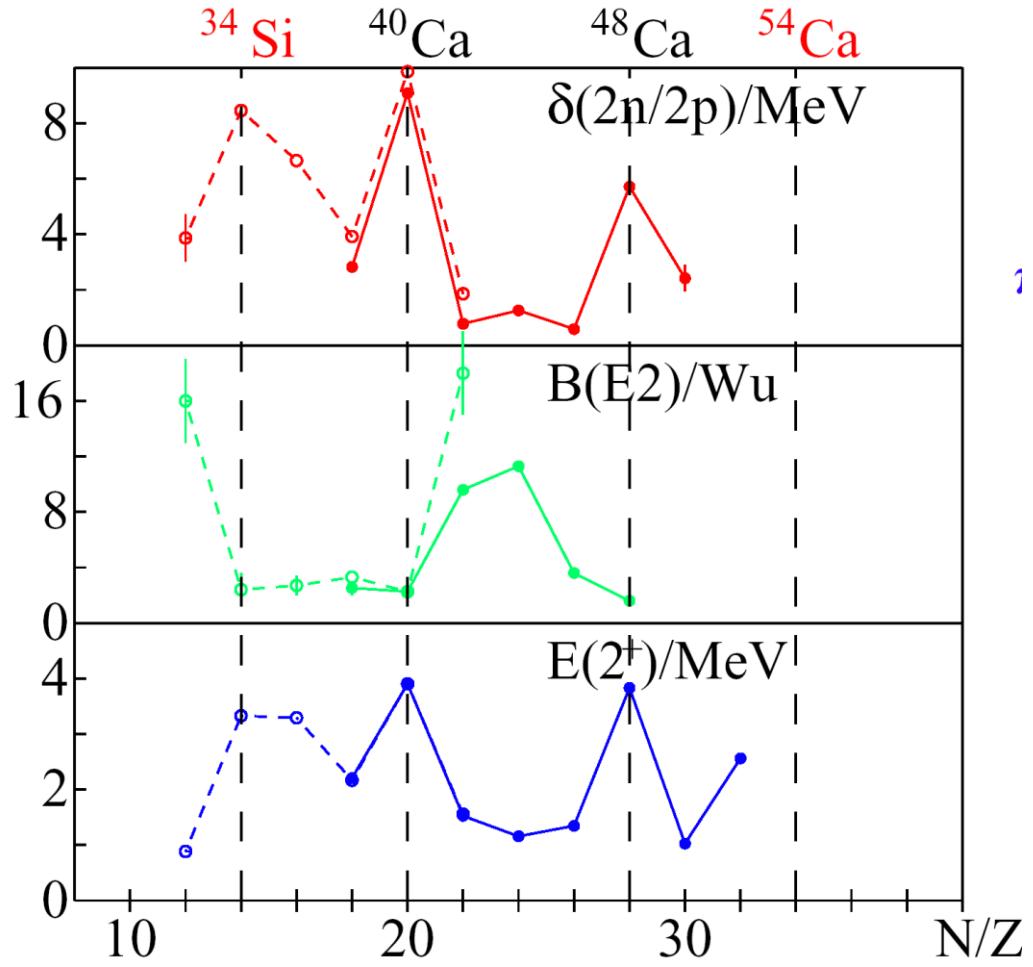
- velocity v/c from TOF (event-by-event)
- tracking of ions:  $\gamma$ -ray emission angle

$\Rightarrow \gamma$ -ray energy resolution  
 $\Rightarrow$  scattering angle



# New Shell Structure at $N \gg Z$

- the mirror point of view -

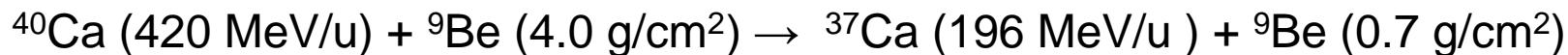


Is  $N, Z=14(16)$  shell stabilisation and  $N=20$  shell quenching symmetric in isospin projection  $T_z$ ?

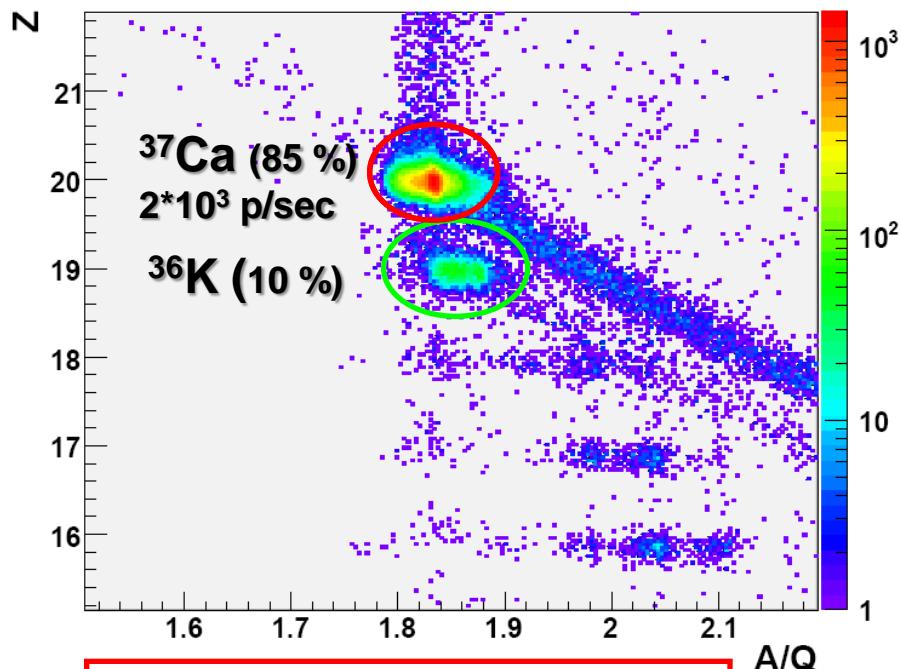
Isospin symmetry in  $Z=20$  isotopes  
- excited states in  $^{36}\text{Ca}$  vs  $^{36}\text{S}$

# Particle identification before and after the secondary target

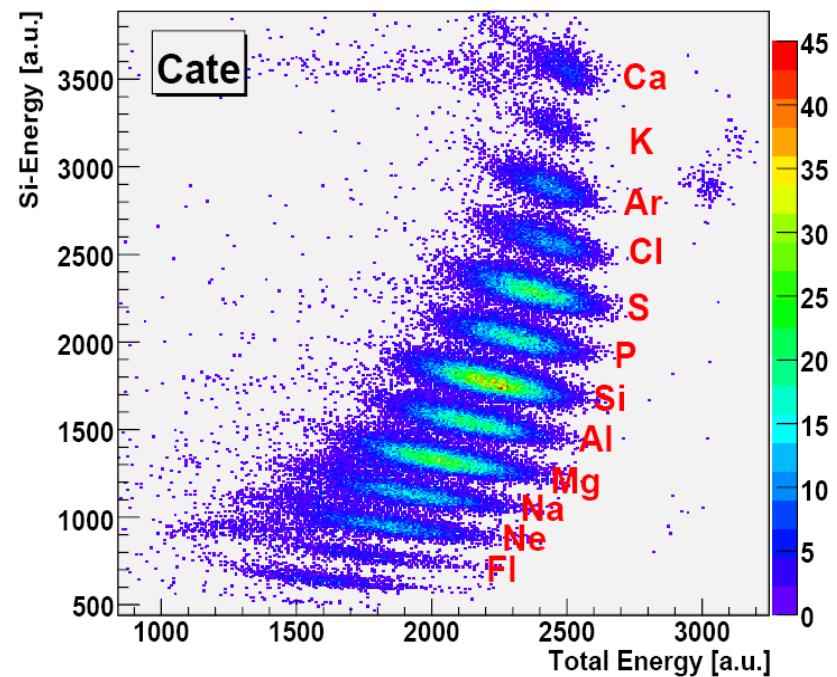
Double fragmentation reaction:



**Selection by FRS**



**Selection by CATE**

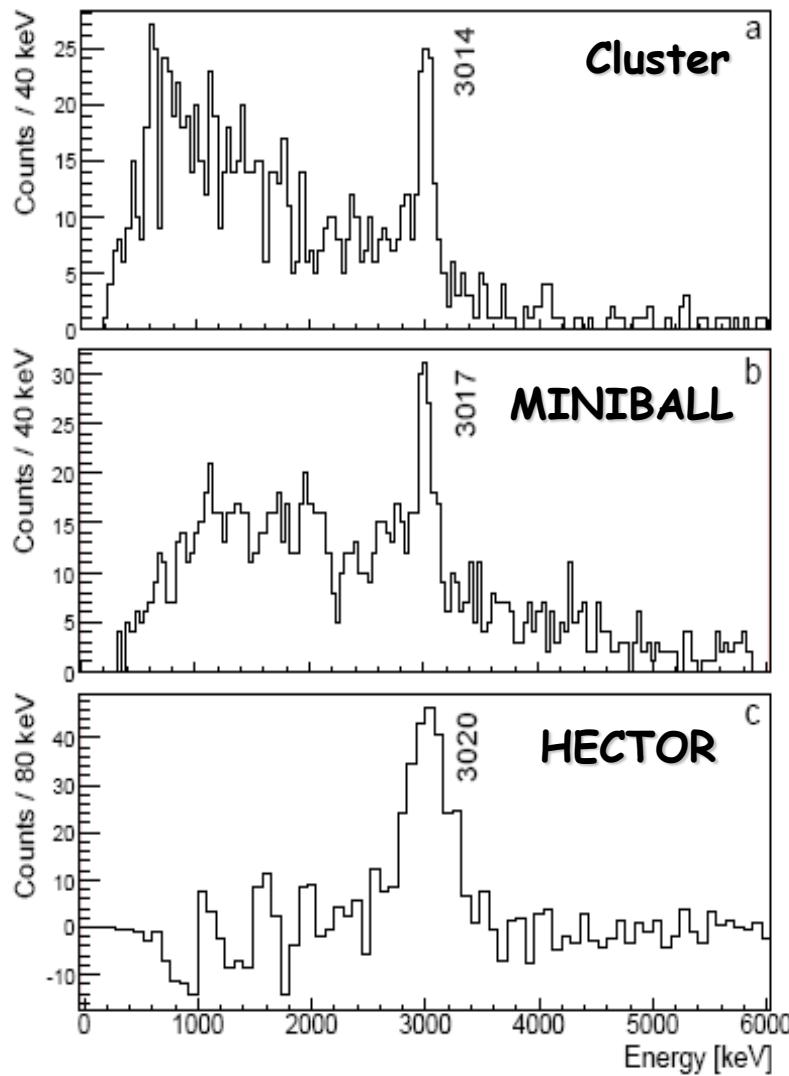


$$\Delta E \sim Z^2; \frac{A}{Q} = \frac{e}{uc} \frac{B\rho}{\beta\gamma}$$

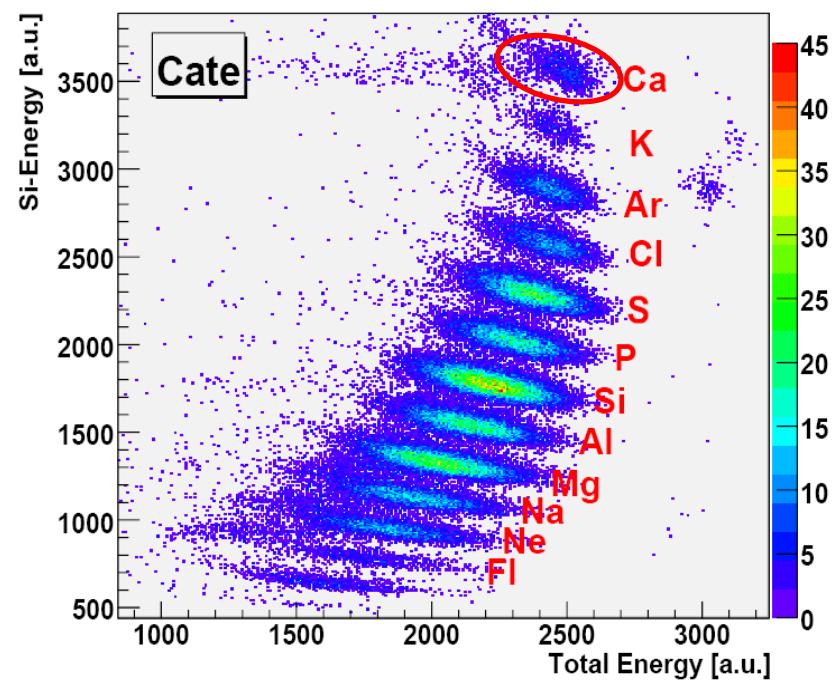
$$\Delta E \sim Z^2; E_{tot} \sim A$$

# $E(2^+)$ -transition in $^{36}\text{Ca}$

$\beta = 0.545$



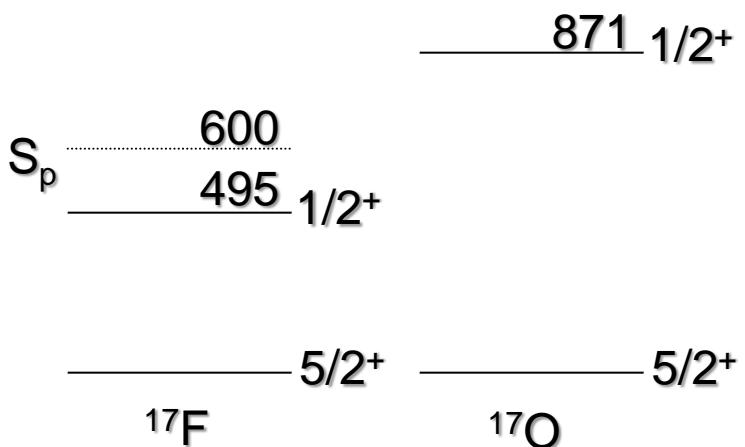
$^{36}\text{Ca } E(2^+) = 3015(16) \text{ keV}$



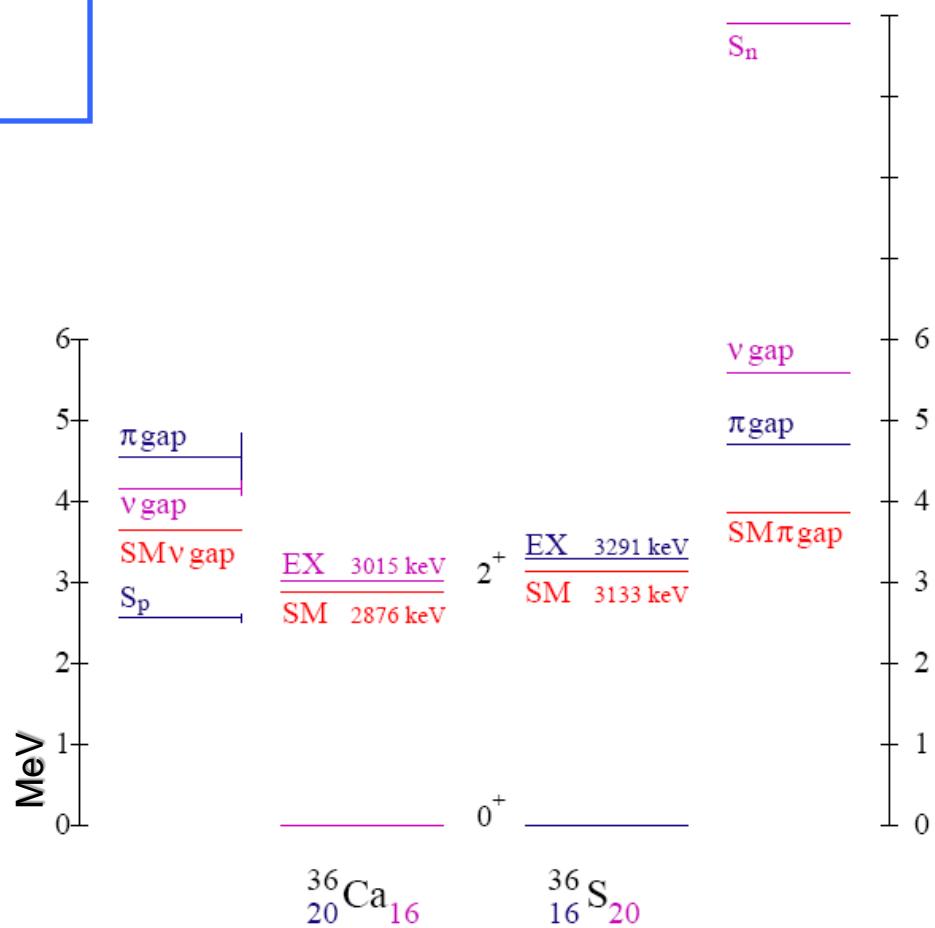
$^{36}\text{Ca } E(2^+) - ^{36}\text{S } E(2^+) = -276(16) \text{ keV}$

# Shell model calculation for $^{36}\text{Ca}$ and $^{36}\text{S}$

- sd shell model with (USD)<sup>\*</sup> interaction and experimental single particle energies (SPE) from  $^{17}\text{O}$  and  $^{17}\text{F}$  reproduce the energy shift qualitatively



→ MED = -257 keV



# Shell model calculation for $^{36}\text{Ca}$ and $^{36}\text{S}$

Monopol modification ( $\text{USD}^m_1$ ),  
deduced from Utsuno *et al.*\*:

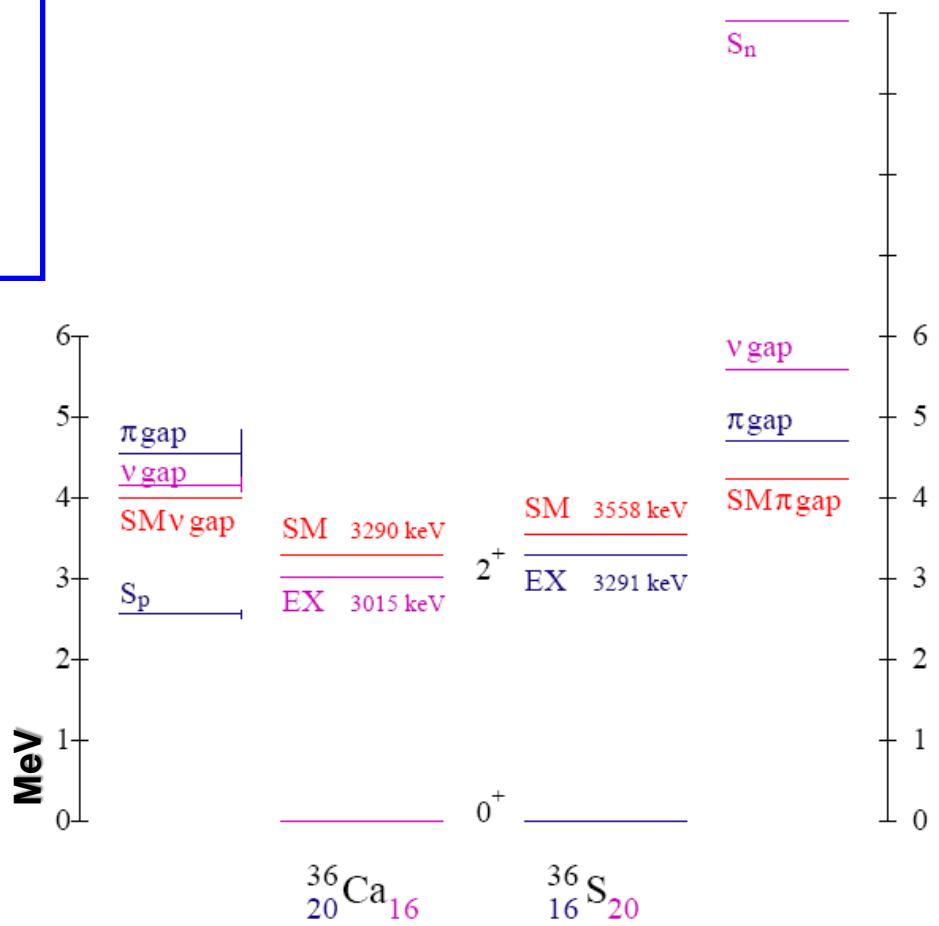
$$\delta V_{d_{5/2}, d_{3/2}}^{T=1,0} = +0.20, -0.6 \text{ MeV}$$

$$\delta V_{d_{5/2}, s_{1/2}}^{T=1,0} = +0.10, +0.1 \text{ MeV}$$

→ MED = -268 keV

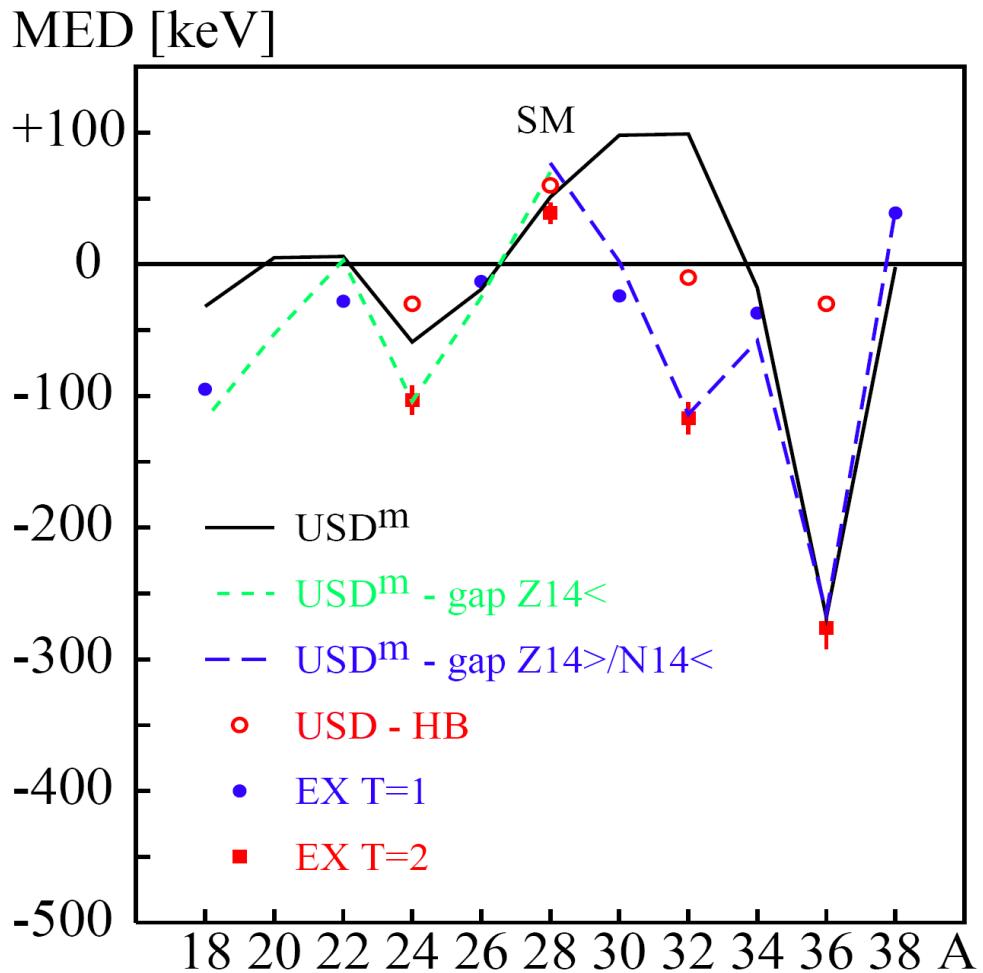
→  $\nu, \pi$  gaps better reproduced!

→ how does it fit for other cases  
in sd-shell?



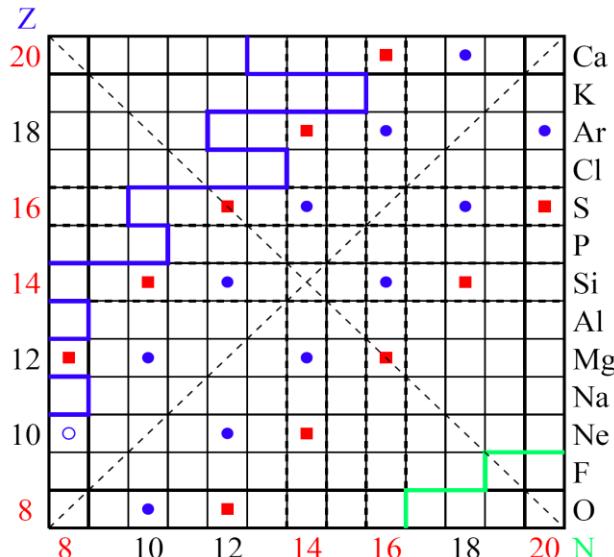
\*Y. Utsuno *et al.*, Phys. Rev. C 60 (1999) 054315

# Shell model calculation for T=1,2 nuclei in *sd*-shell



## Ad hoc modifikation introduced H. Grawe

- For  $A = 16 - 28$  increased  
 $\pi 0d_{5/2}$  SPE by 200 keV
  - For  $A = 28 - 40$  reduced  
 $\pi 0d_{5/2}$  SPE by 300 keV  
 $\nu 0d_{5/2}$  SPE by 900 keV

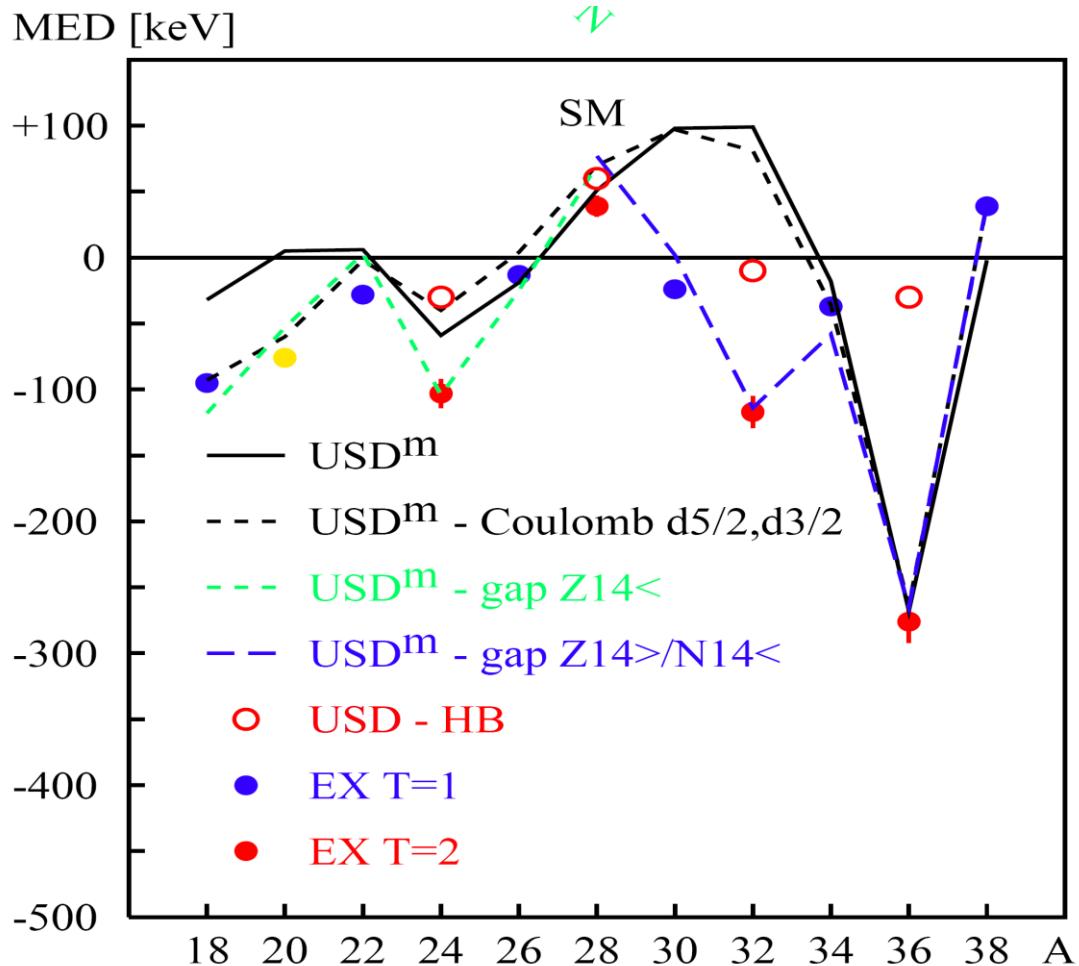


=> reduced neutronen gap in  $^{34}\text{Ca}$   
 $(\Delta_v = 5.498 \text{ MeV})$  with respect to  
 protonen gap in  $^{34}\text{Si} (\Delta_\pi = 6.241 \text{ MeV})$

*\*H. Herndl et al., Phys. Rev. C 52 (1995) 1078  
P. Doornenbal et al., Phys. Lett. B647, 237 (2007).*

\*Y. Utsuno et al., Phys. Rev. C 60 (1999) 054315

# Shell model calculation for T=1,2 nuclei in sd-shell



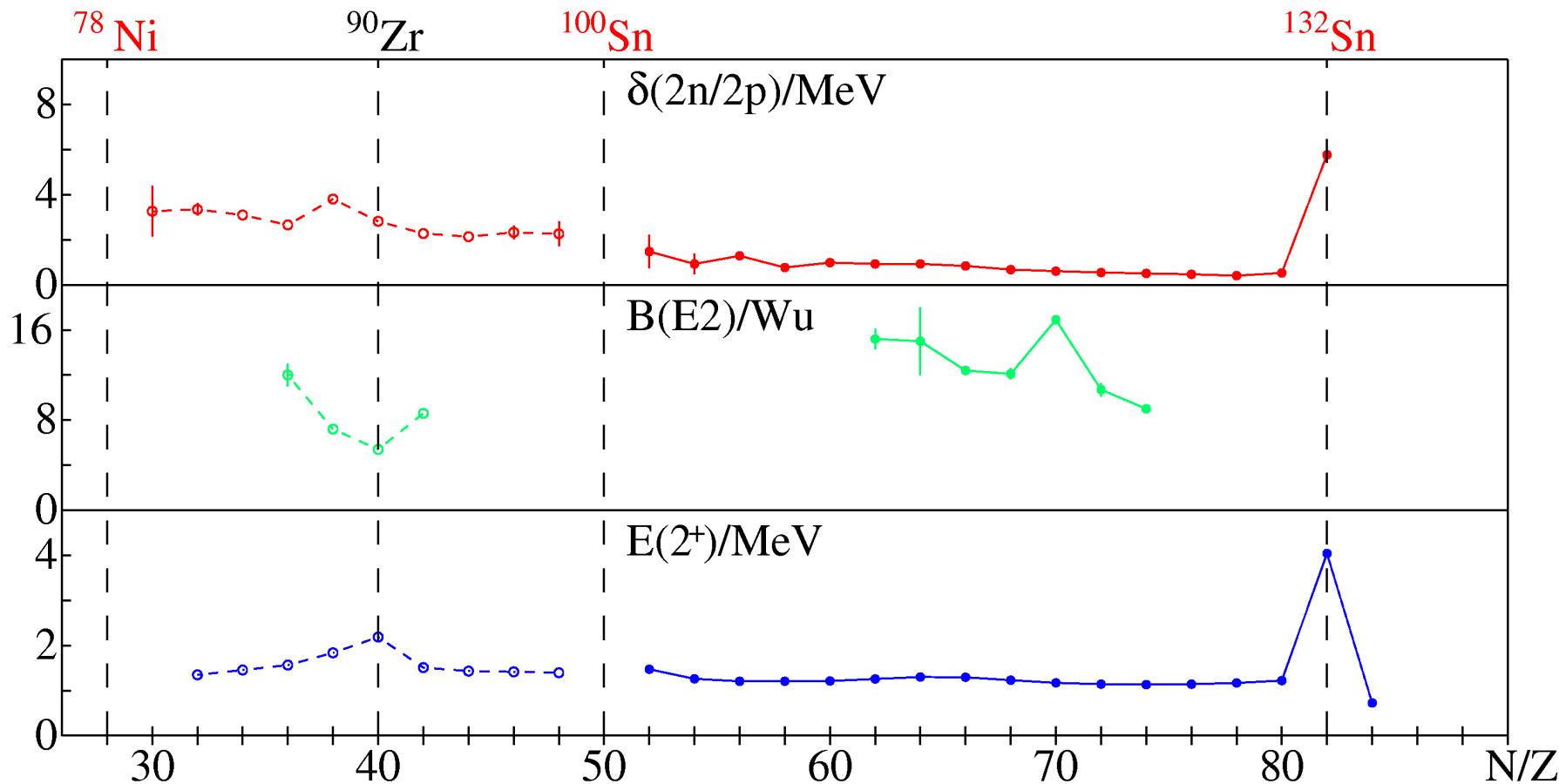
- Confirmation of modifications by MSU result on last and missing 2<sup>+</sup> MED in sd-shell for <sup>20</sup>Mg and <sup>20</sup>O pair.
- Motivation for future work:

\*H. Herndl et al., Phys. Rev. C 52 (1995) 1078

P. Doornenbal et al., Phys. Lett. B647, 237 (2007).

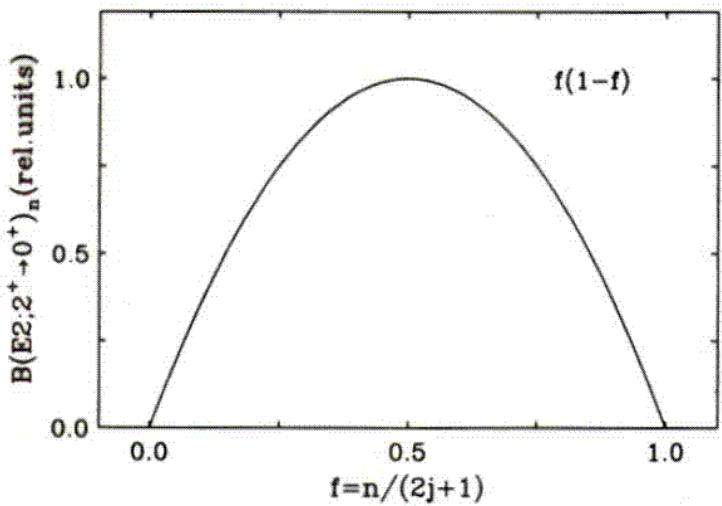
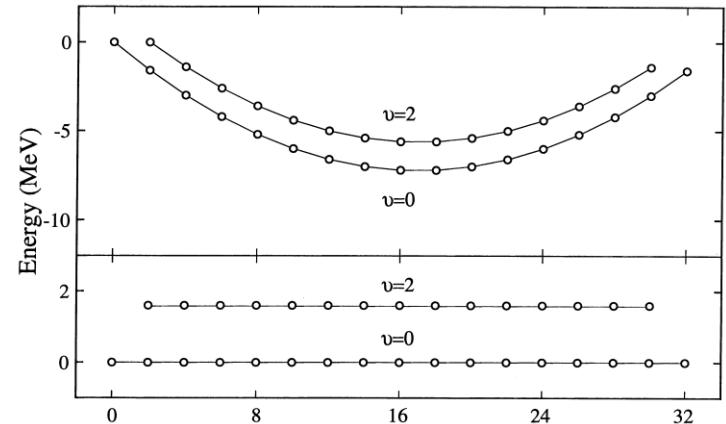
● A. Gade et al. Phys. Rev. C 76, 024317 (2007)

# Relativistic Coulomb Excitation of Nuclei Near $^{100}\text{Sn}$

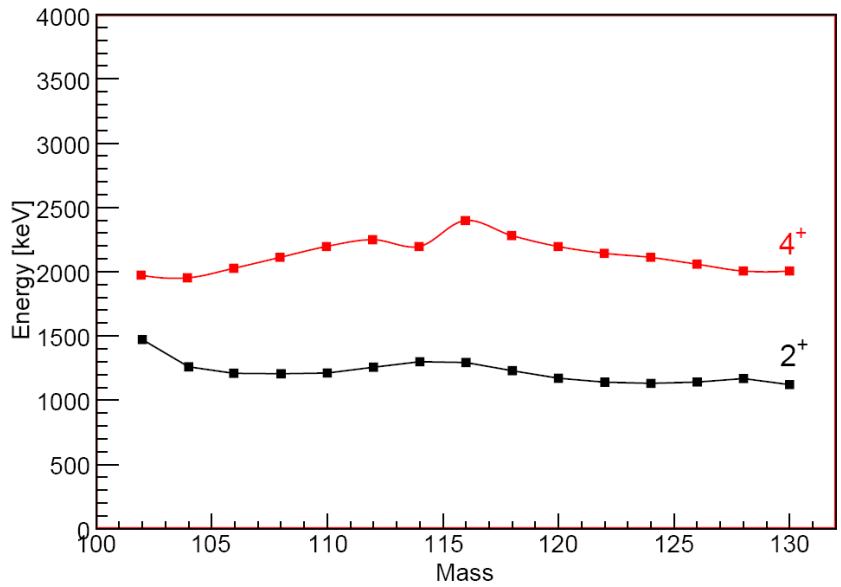


- $B(E2, 2^+ \rightarrow 0^+)$  values provide E2 correlations related to core polarization.
- Lifetime measurements hampered by isomeric  $6^+$  states in even Sn isotopes
- $2^+ \rightarrow 0^+$  decay too fast for electronic timing methods.
- Coulomb excitation of unstable Sn isotopes

# Seniority Scheme



$$B(E2) \sim N_{\text{particles}} * N_{\text{holes}}$$

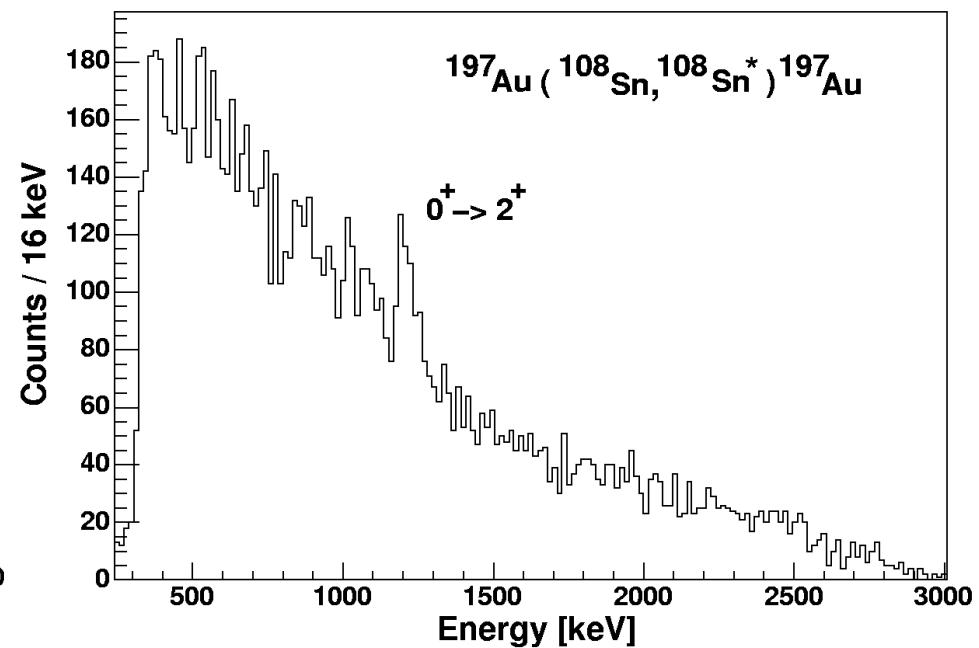
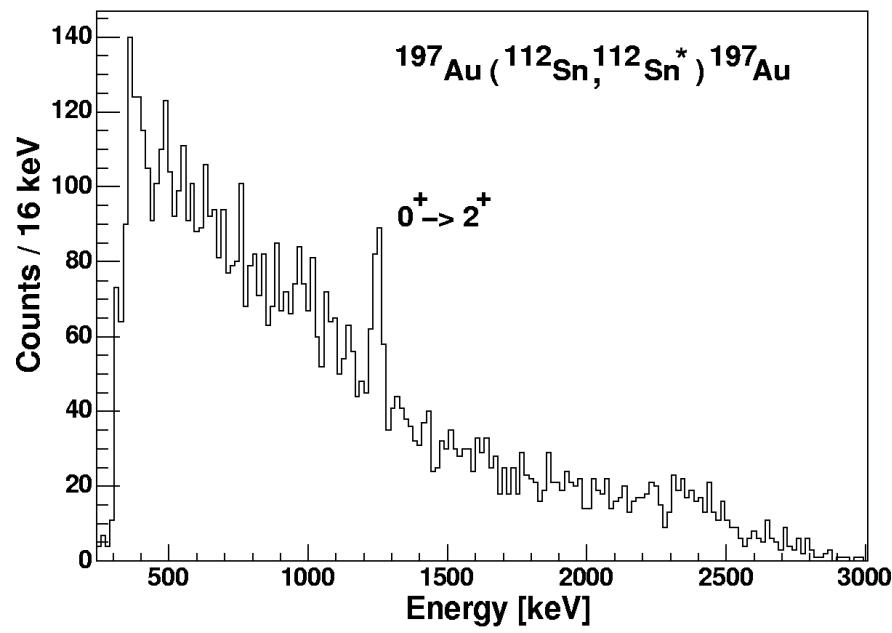


**Experimental  $2^+$  and  $4^+$  Levels  
of Sn isotopes are text book  
examples.**

**How about the  $B(E2)$  values?**

# Relativistic Coulomb excitation of nuclei towards $^{100}\text{Sn}$

- $^{108,112}\text{Sn}$  secondary beam with 150MeV/u
- Au – Coulex target



$^{108}\text{Sn}$   $B(E2:2^+ \rightarrow 0^+)$  value:

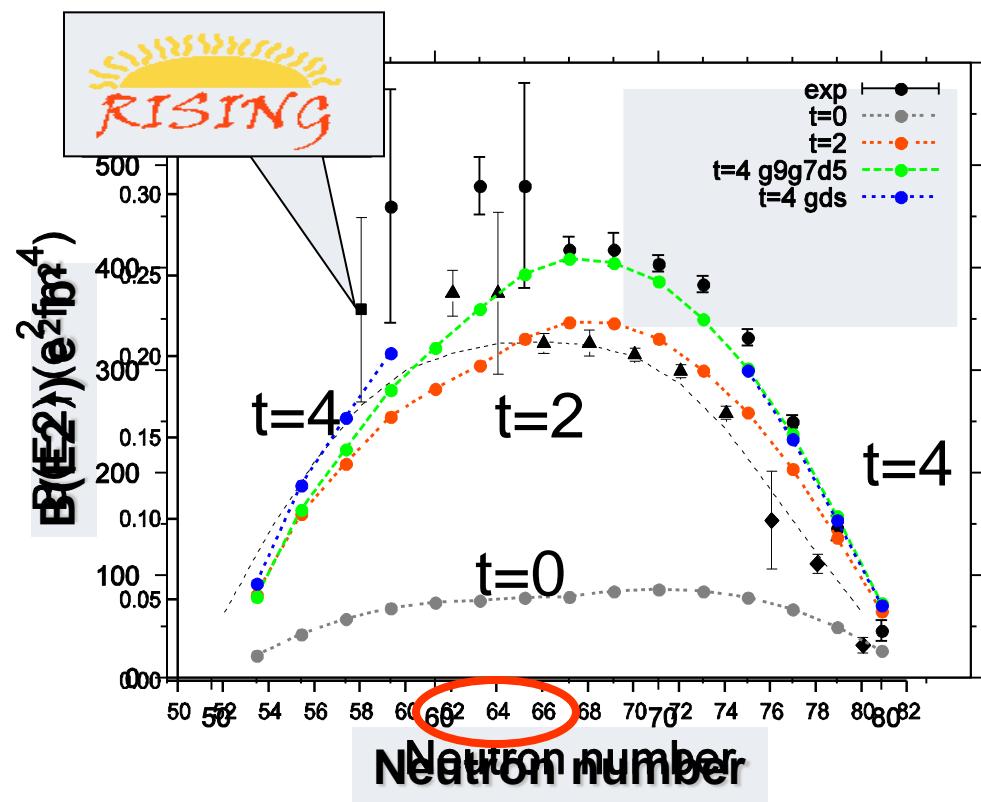
EXP: 15.1 (3.3) W.u.

TH1: 11.2 W.u. Morten Hjorth-Jensen

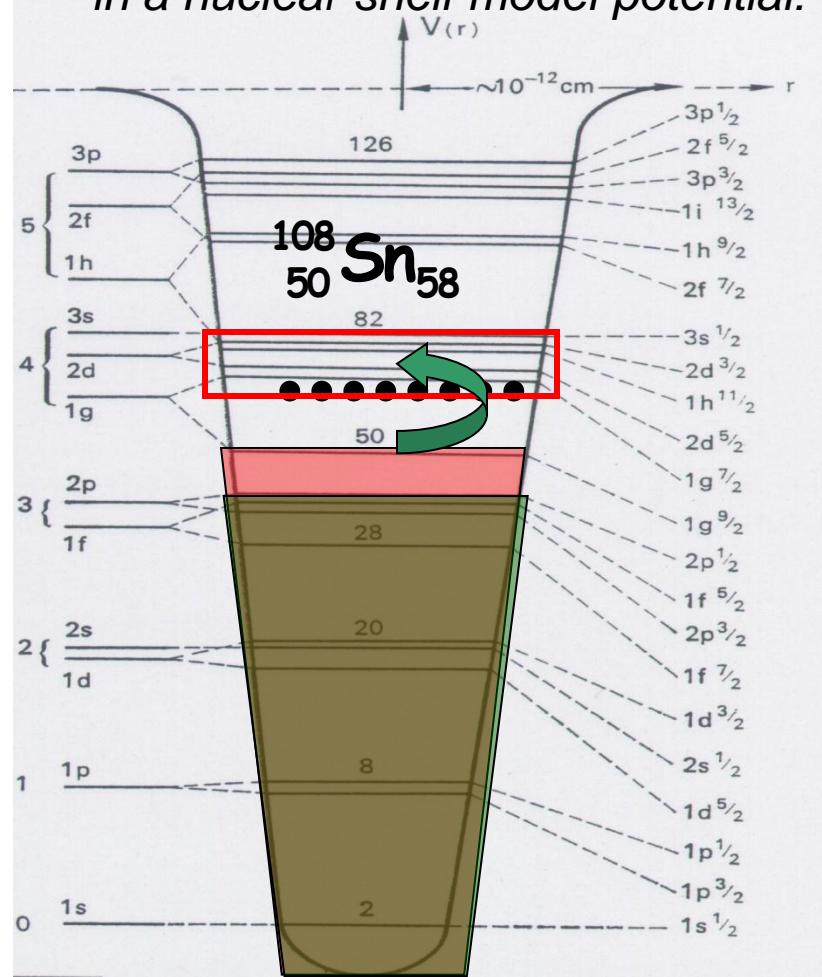
TH2: 11.5 W.u. Frederic Nowacki

# Comparison with Shell Model calculations

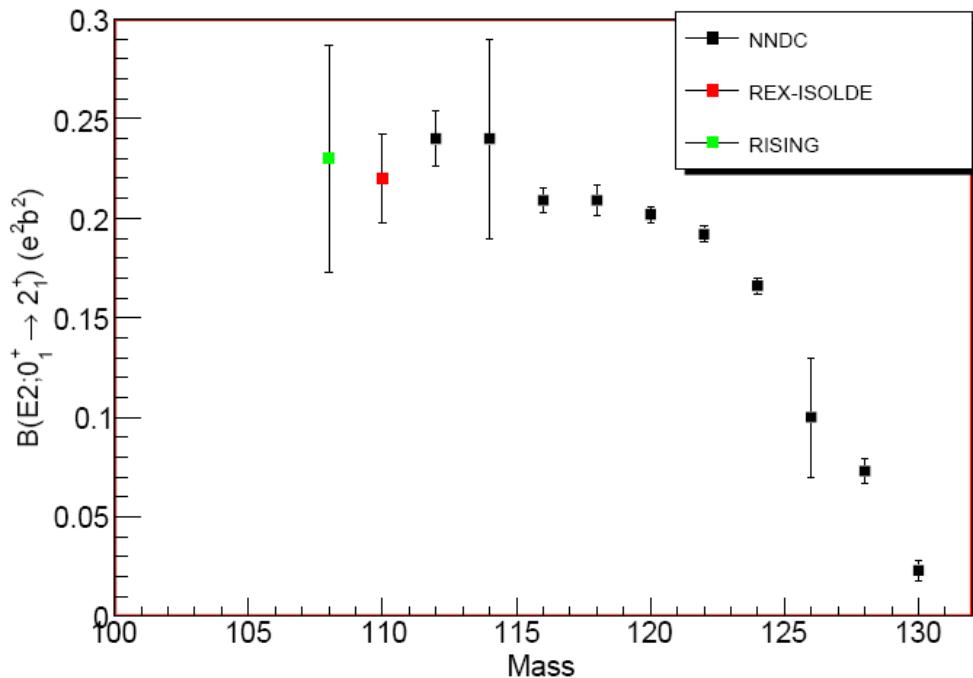
..... theory ((**neutron valence and proton core excitations and**)  
 **$^{108}_{50}\text{Sn}$** )  
 **$^{90}_{40}\text{Zr}$  as closed-shell core)**



Neutron/proton single-particle states  
in a nuclear shell-model potential:



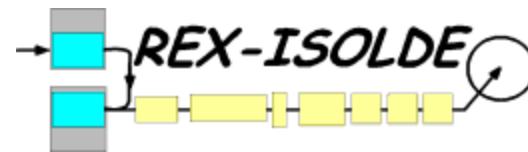
# Experimental B(E2) values of Sn Isotopes



An new measurement of  $^{114}\text{Sn}$   
would enlighten the picture!

2 Methods applicable for neutron deficient Sn isotopes:

- Sub-barrier Coulex



$$^{110}\text{Sn} B(E2) = 0.220(22) e^2 b^2$$

J. Cederkäll et al., PRL98, 172501(2007)

- Intermediate Energy Coulex



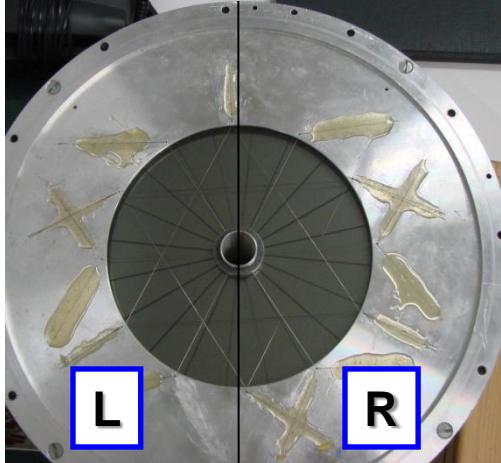
$$^{108}\text{Sn} B(E2) = 0.230(57) e^2 b^2$$

A. Banu et al, PRC 72 061305(R) (2005)

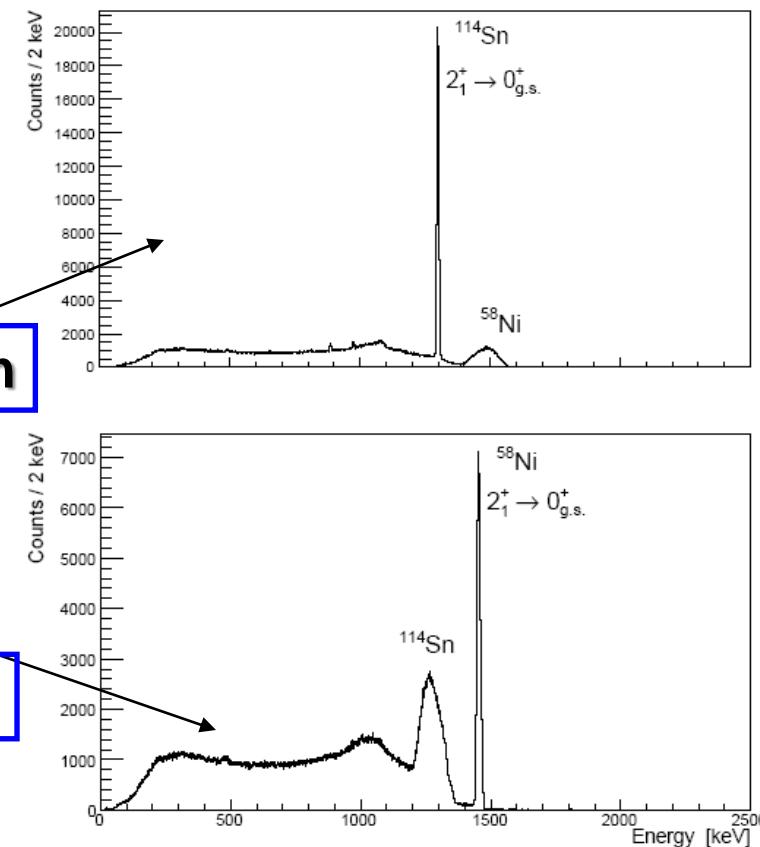
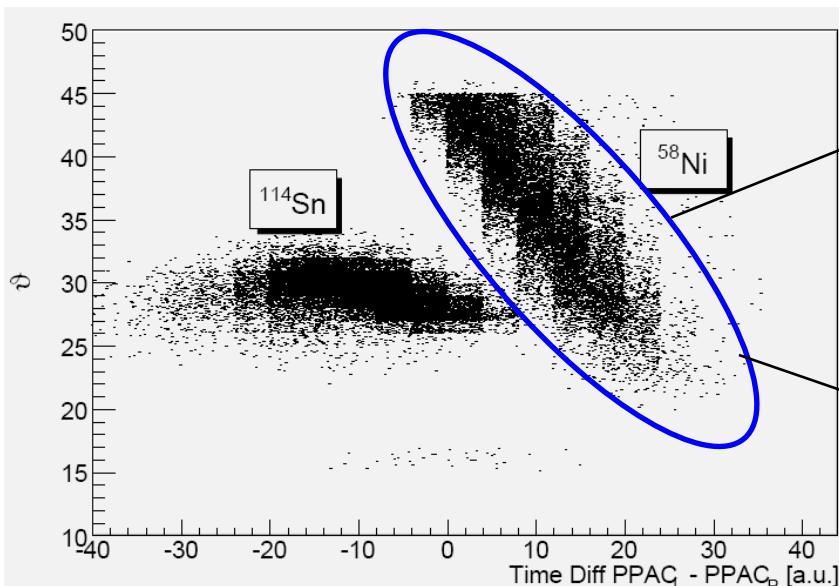
# Coulex Experiment with stable beams

- Previous Coulex measurements were performed using  $^{114}\text{Sn}$  as target material
  - Natural abundance is only 0.65%
  - Enriched materials have contaminations of other Sn isotopes, which cannot be separated, as the  $2^+$  levels have the same energy
- **$^{114}\text{Sn}$  used as beam and studied via inverse kinematics**
- $^{116}\text{Sn}$  measured in addition to minimize systematic errors
- Sub-barrier beam energies of  $3.4 \text{ A MeV}$  provided by UNILAC at GSI

# Particle Identification

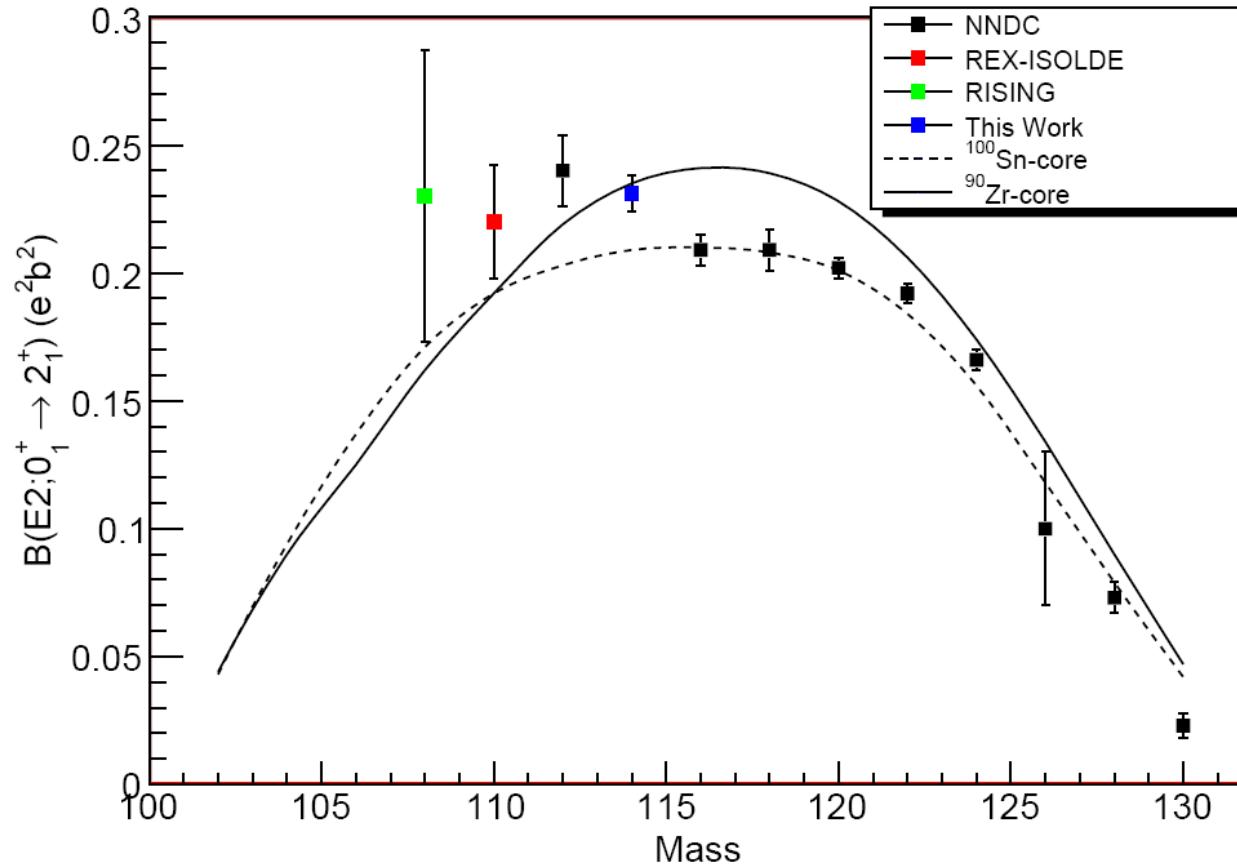


Scattered particle identification with PPAC  
 $\varphi$  and  $\theta$  determination



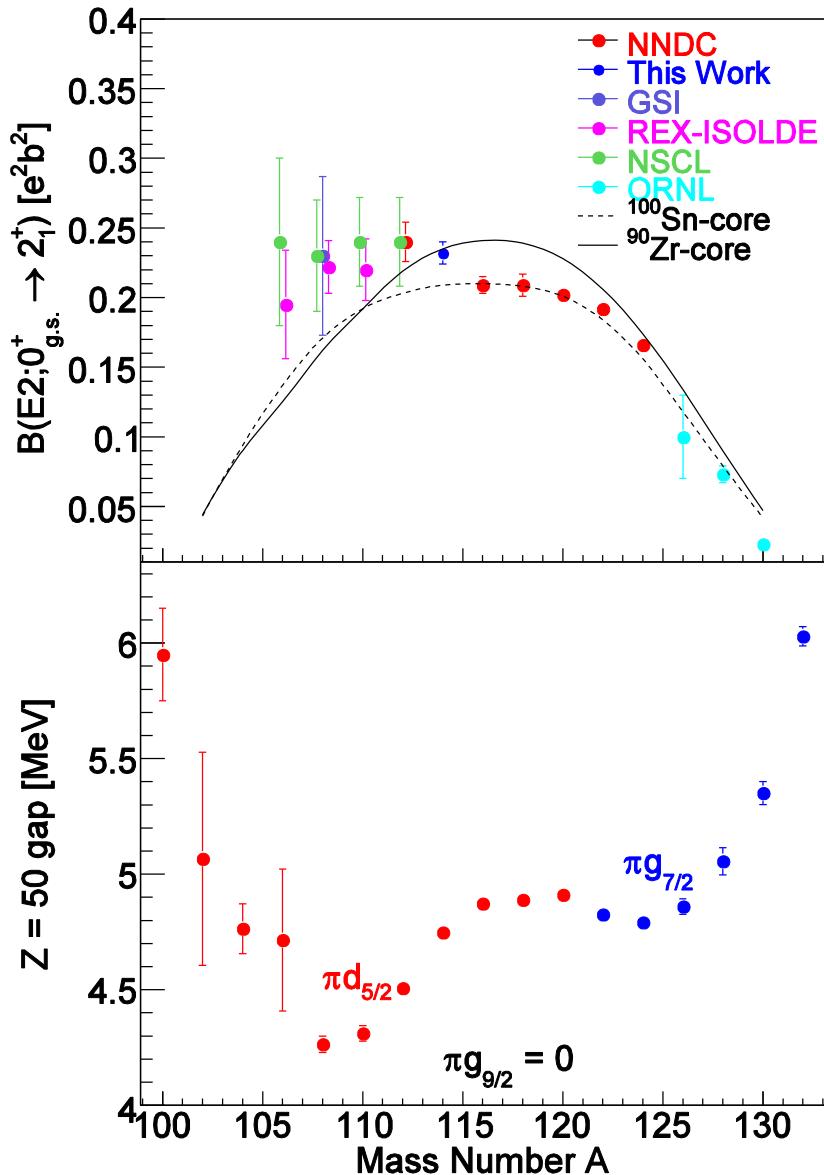
Doppler Correction

# B(E2) Systematics for Sn isotopes



$$^{114}\text{Sn} \text{ B(E2)} = 0.231(7) \text{ } e^2 b^2$$

# Enhanced B(E2) values towards $^{100}\text{Sn}$



$^{100}\text{Sn}$  core

$v(d_{5/2}g_{7/2}s_{1/2}h_{11/2})$ ,  $e_v = 1.0e$

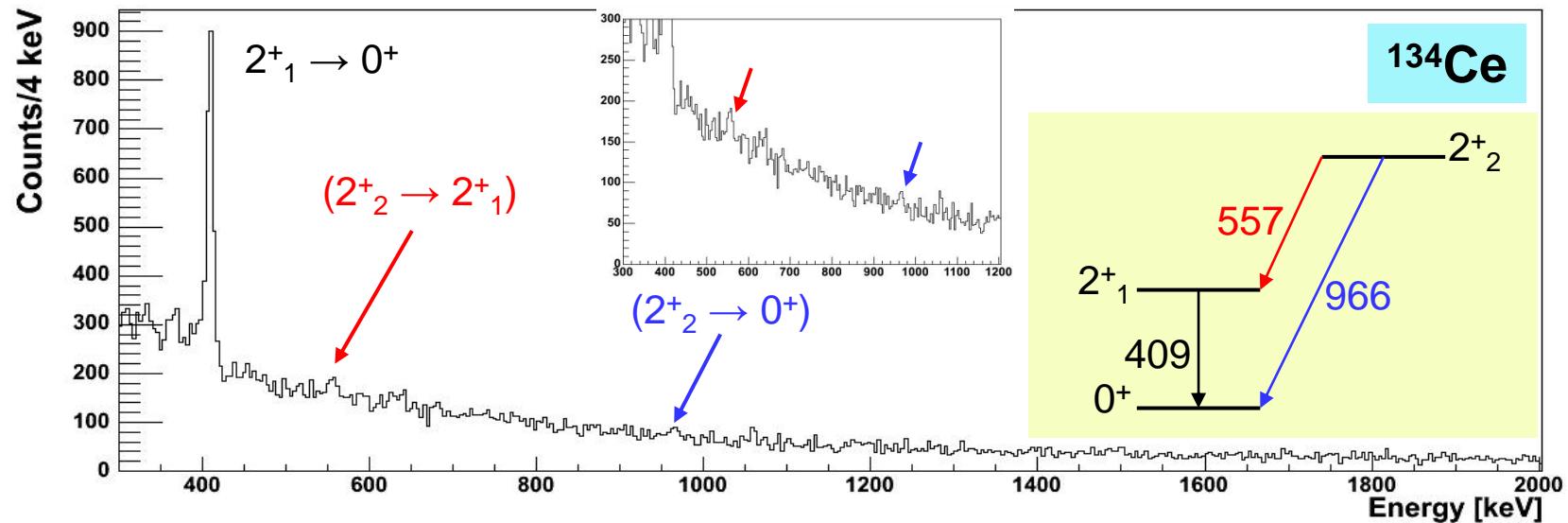
$^{90}\text{Zr}$  core

$v(d_{5/2}g_{7/2}s_{1/2}h_{11/2})$ ,  $e_v = 0.5e$ ,  
 $\pi(g_{9/2}g_{7/2}d_{5/2}d_{3/2}s_{1/2})$ ,  $e_\pi = 1.5e$

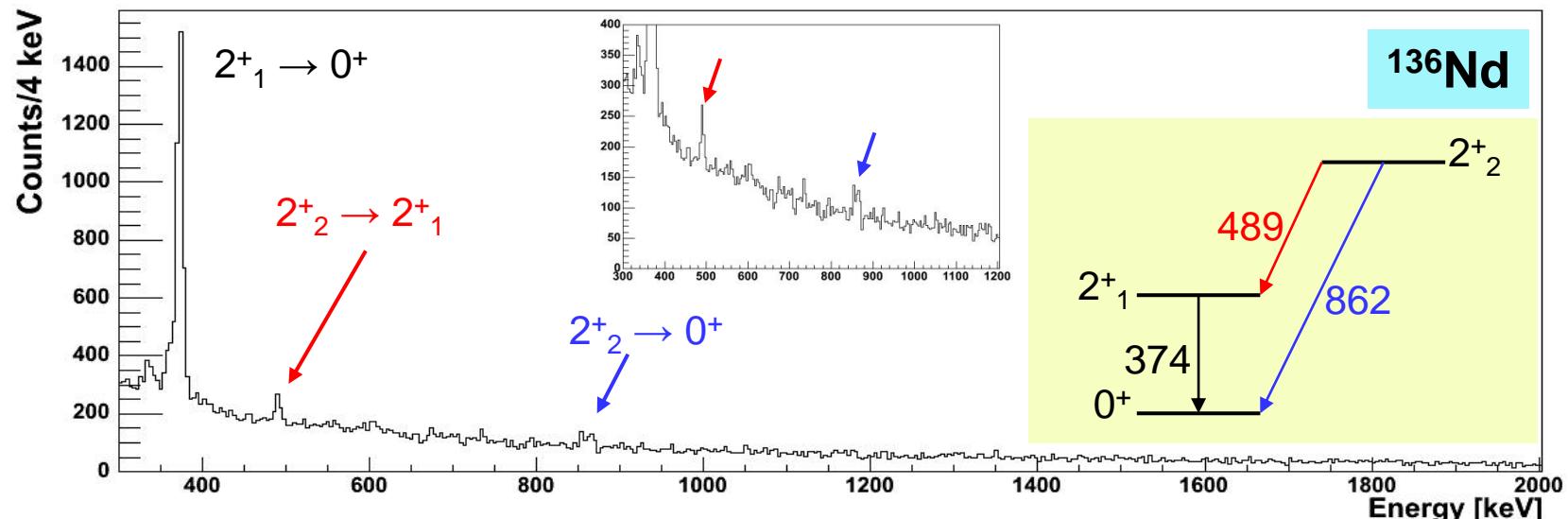
$\pi\nu$  monopoles tuned to  
ESPEs and  $Z = 50$  shell gap

- A. Banu et al, PRC, 72 061305(R) (2005)
- J. Cederkäll et al., PRL98, 172501 (2007)
- A. Ekström et al., PRL 101, 012502 (2008)
- C. Vaman et al., PRL 99, 162501 (2007),
- P. Doornenbal et al., PRC 78, 031303 (R) (2008)

# Triaxiality in even-even core nuclei of N=75 odd-odd isotones



B(E2)  
[W.U.]  
 $53 \pm 5$   
 $< 12^*$   
 $< 206^*$



B(E2)  
[W.U.]  
 $90 \pm 11$   
 $12 \pm 3^*$   
 $251 \pm 95^*$

# RISING collaboration

H.J. Wollersheim<sup>a</sup>, D.E. Appelbe<sup>b</sup>, A. Banu<sup>a</sup>, R. Bassini<sup>c,d</sup>, T. Beck<sup>a</sup>,  
F. Becker<sup>a</sup>, P. Bednarczyk<sup>a,d,e</sup>, K.-H. Behr<sup>a</sup>, M.A. Bentley<sup>f</sup>, G. Benzoni<sup>c,d</sup>,  
C. Boiano<sup>c,d</sup>, U. Bonnes<sup>g</sup>, A. Bracco<sup>c,d</sup>, S. Brambilla<sup>c,d</sup>, A. Brünle<sup>a</sup>,  
A. Bürger<sup>h</sup>, K. Burkard<sup>a</sup>, P.A. Butler<sup>i</sup>, F. Camera<sup>c,d</sup>, D. Curien<sup>j</sup>, J. Devin<sup>j</sup>,  
P. Doornenbal<sup>a</sup>, C. Fahlander<sup>k</sup>, K. Fayz<sup>b</sup>, H. Geissel<sup>a</sup>, J. Gerl<sup>a</sup>, M. Górska<sup>a,\*</sup>,  
H. Grawe<sup>a</sup>, J. Grębosz<sup>a,e</sup>, R. Griffiths<sup>b</sup>, G. Hammond<sup>f</sup>, M. Hellström<sup>a</sup>,  
J. Hoffmann<sup>a</sup>, H. Hübel<sup>h</sup>, J. Jolie<sup>l</sup>, J.V. Kalben<sup>g</sup>, M. Kmiecik<sup>e</sup>, I. Kojouharov<sup>a</sup>,  
R. Kulessa<sup>m</sup>, N. Kurz<sup>a</sup>, I. Lazarus<sup>b</sup>, J. Li<sup>a,n</sup>, J. Leske<sup>h</sup>, R. Lozeva<sup>a,o</sup>, A. Maj<sup>e</sup>,  
S. Mandal<sup>a</sup>, W. Męczyński<sup>e</sup>, B. Million<sup>c,d</sup>, G. Münzenberg<sup>a</sup>, S. Muralithar<sup>p</sup>,  
M. Mutterer<sup>g</sup>, P.J. Nolan<sup>i</sup>, G. Neyens<sup>q</sup>, J. Nyberg<sup>r</sup>, W. Prokopowicz<sup>a</sup>,  
V.F.E. Pucknell<sup>b</sup>, P. Reiter<sup>l</sup>, D. Rudolph<sup>k</sup>, N. Saito<sup>a</sup>, T.R. Saito<sup>a</sup>, D. Seddon<sup>i</sup>,  
H. Schaffner<sup>a</sup>, J. Simpson<sup>b</sup>, K.-H. Speidel<sup>h</sup>, J. Styczeń<sup>e</sup>, K. Sümmerer<sup>a</sup>,  
N. Warr<sup>l</sup>, H. Weick<sup>a</sup>, C. Wheldon<sup>a</sup>, O. Wieland<sup>c,d</sup>,  
M. Winkler<sup>a</sup>, M. Ziębliński<sup>e</sup>

Local FRS & RISING group:

A. Banu, T. Beck, F. Becker, P. Bednarczyk, K.-H. Behr, P. Doornenbal,  
H. Geissel, J. Gerl, M. Gorska, J. Grębosz, M. Hellström, M. Kavatsyuk,  
O. Kavatsyuk, I. Kojouharov, N. Kurz, R. Lozeva, S. Mandal, S. Muralithar, N. Saito,  
T. Saito, H. Schaffner, H. Weick, M. Winkler, H.J. Wollersheim

GSI Darmstadt, Germany

# Summary

## Coulomb excitation results from fast beam RISING

- Coulomb excitation at 130-150 MeV established
- Coulomb excitation of  $2^+_1$  in  $^{108,112}\text{Sn}$   
*A. Banu et al., Phys. Rev. C 72, 061305(R) (2005)*
- Coulomb excitation of  $2^+_1$  in  $^{54,56,58}\text{Cr}$   
*A. Bürger et al., Phys. Lett. B 622, 29 (2005)*
- RDDS results confirms B(E2) of  $^{56}\text{Cr}$   
*M. Seidlitz et al., Phys. Rev. C 84, 034318 (2011)*
- Collective modes and E1 strength distribution:  $^{68}\text{Ni}$   
*O. Wieland et al., Phys. Rev.Lett. 102, 092502 (2009)*
- Coulomb excitation of  $2^+_1$  and  $2^+_2$  in  $^{134}\text{Ce}$ ,  $^{136}\text{Nd}$   
*T. Saito et al., Phys. Lett. B 669 (2008) 19*
- Mirror symmetry in  $^{36}\text{Ca}$   
*P. Doornenbal et al., Phys. Lett. B647, 237 (2007).*

## Future

fast beam experiments PRESPEC employing  $\gamma$ -ray tracking