



# The physics of birdsong

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**10 temporada**

# Why birdsong?

- Animal model to study mechanisms of **vocal learning**
- Shared properties with humans:
  - Similar learning stages
  - Similar sound production mechanisms
- Vocal learning is not common in mammals  
(just humans, cetaceans, bats)

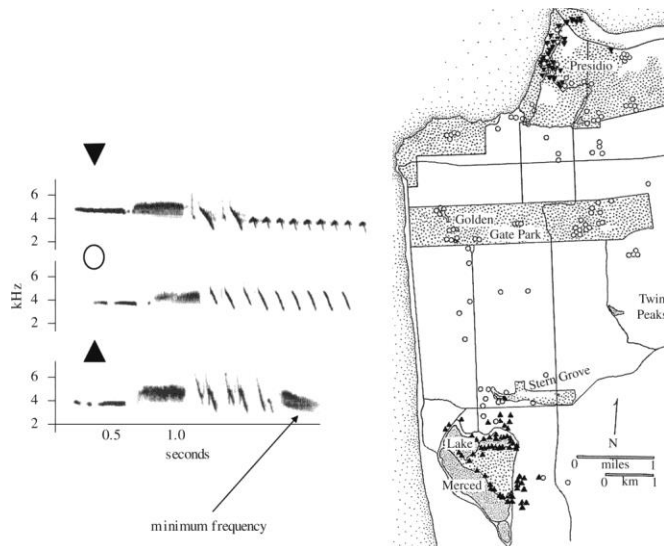
## Why birdsong ... for a dynamicist?

1. How much of the “complex features” observed in behavior is due to the **Nonlinear nature** of the peripheral system?
2. Is it pertinent to reduce dimensionalities in biology?
3. Can we translate from physics the idea of “progressive” modeling?



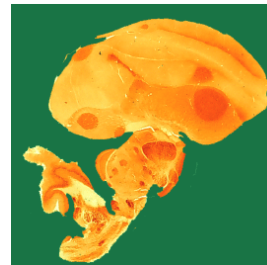
# Landmarks in study of Birdsong

50's



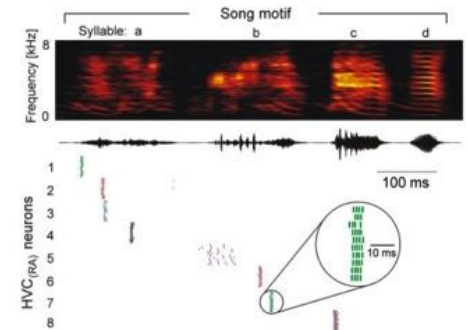
Dialects

70's



Vocalizations reflected  
The operations of a definable  
Collection of neural structures

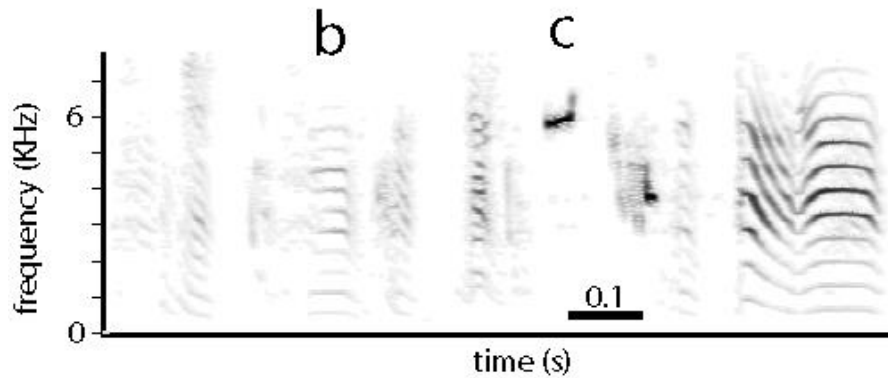
00's



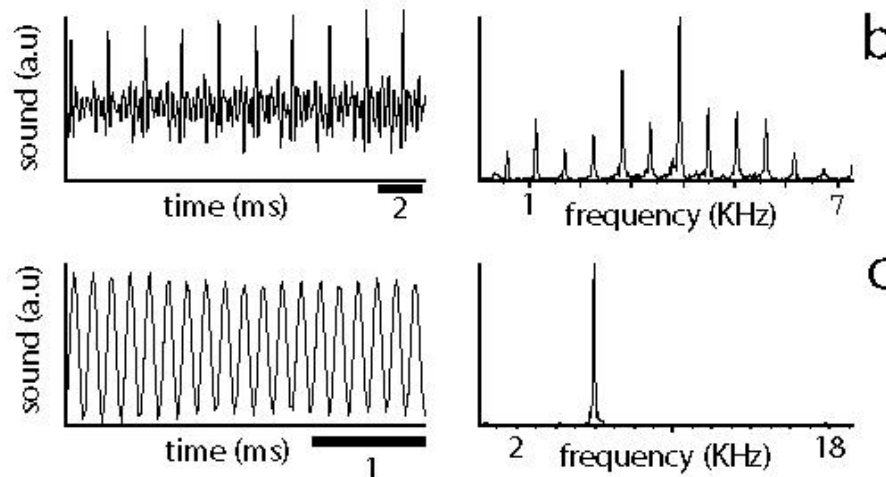
The ability to monitor  
Neural activity in awake  
Singing birds.

“How much of the complex features observed in behavior is due to the **Nonlinear nature** of the peripheral system?”

Example of a “complex feature”



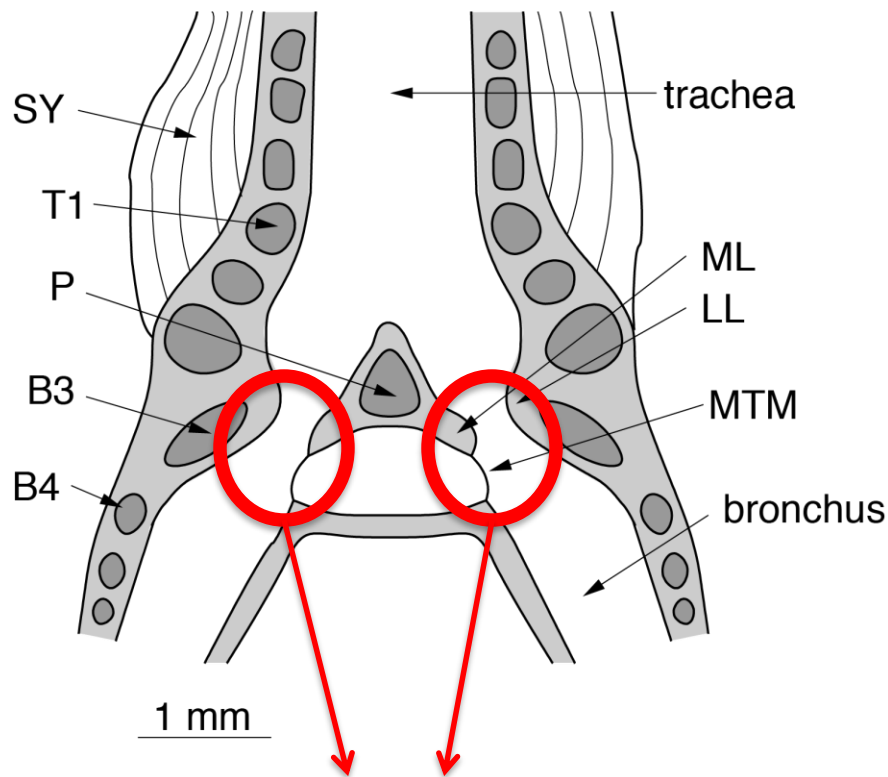
Zebra finch  
song



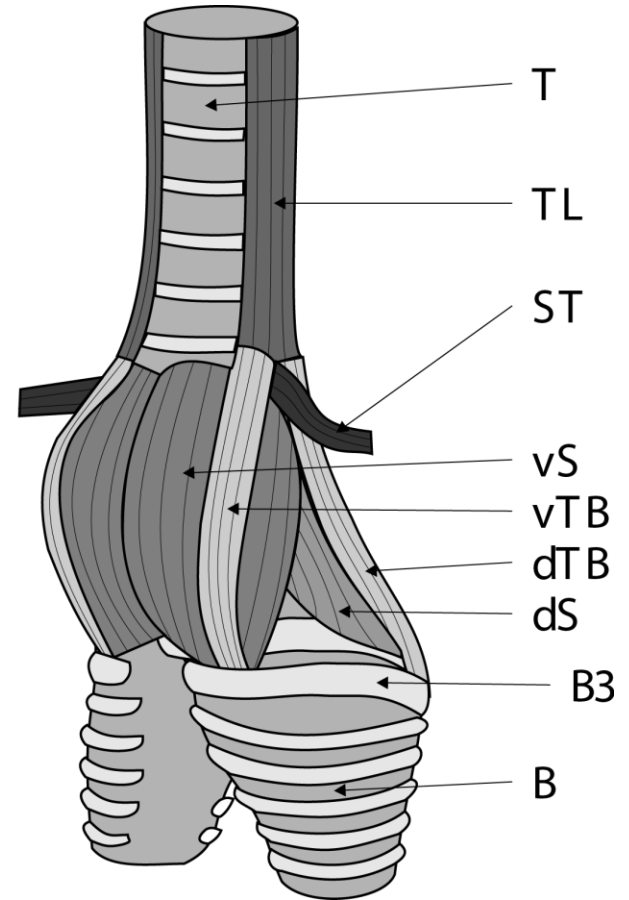
Spectrally rich  
notes

Almost tonal  
notes

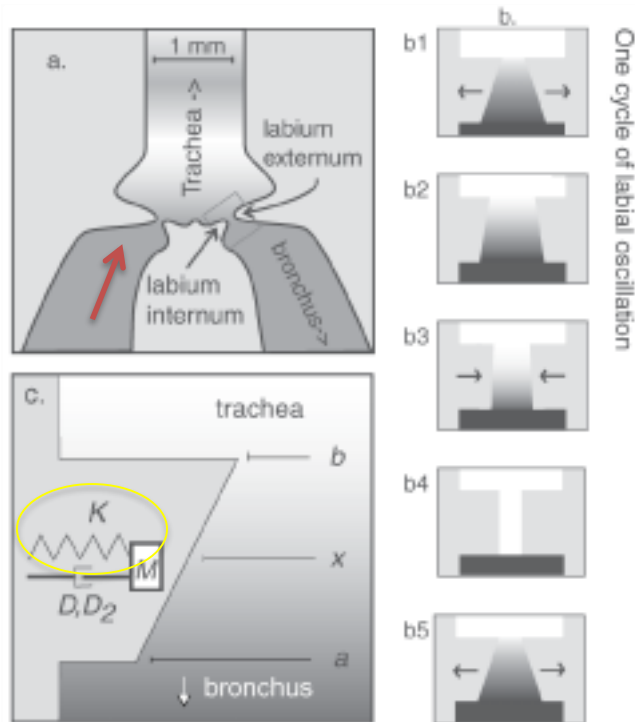
Between the song and the neural architecture,  
the avian vocal organ: the **syrinx**



Two independent sound sources



# Our first steps in the field: the basic mechanics of labial motion



$$\frac{dx}{dt} = y,$$

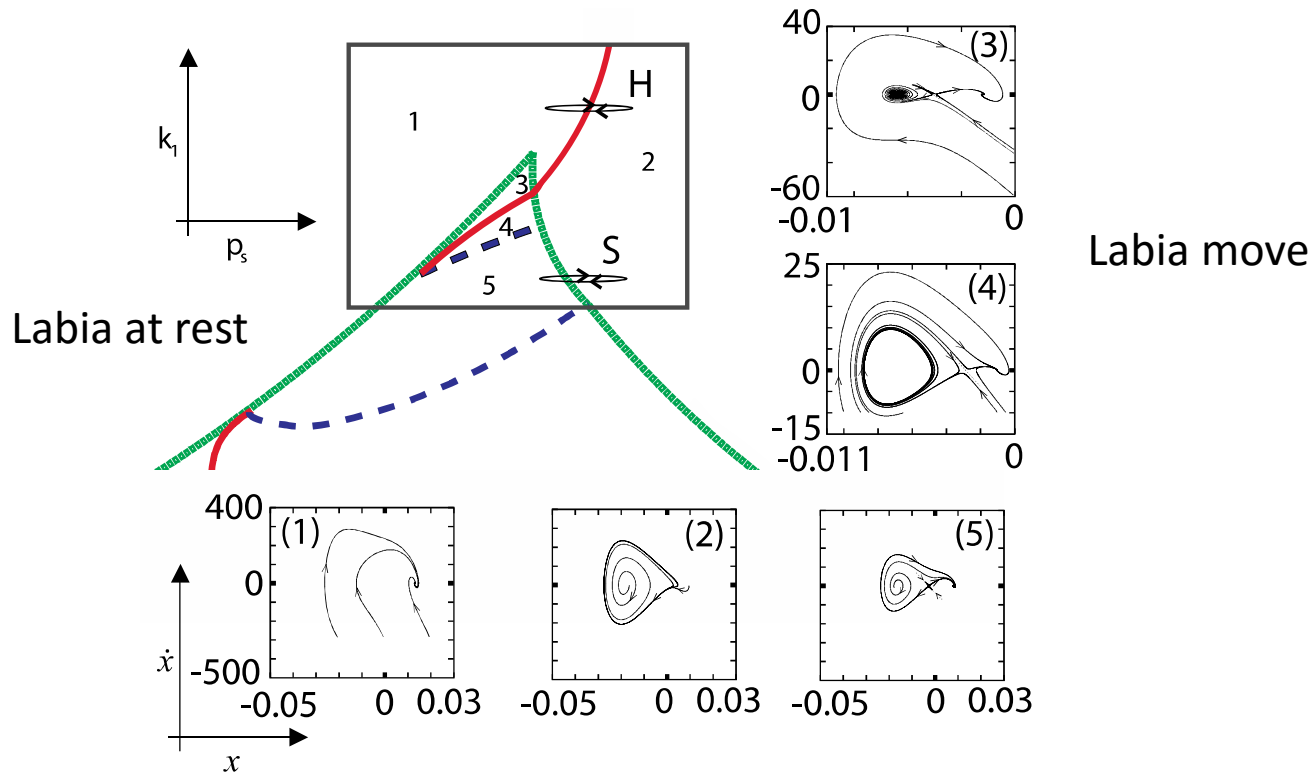
$$\frac{dy}{dt} = (1/m) \left[ -k(x)x - b(y)y - cx^2y + a_{\text{lab}}p_s \left( \frac{\Delta a + 2\tau\tau}{a_{01} + x + \tau y} \right) \right].$$

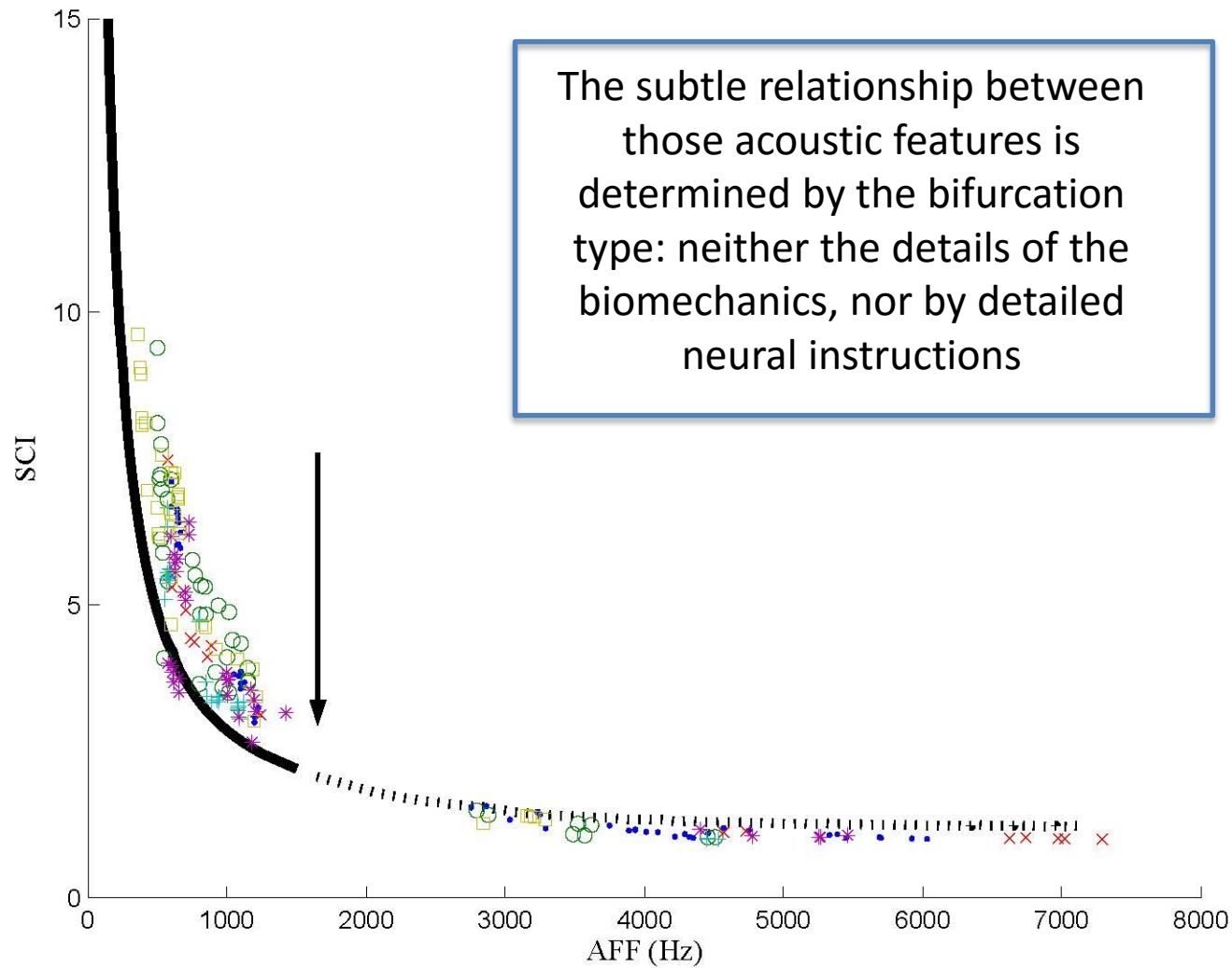
A yellow arrow points from the term  $-k(x)x$  in the equation to the text "Two time dependent parameters". A red arrow points from the term  $a_{\text{lab}}p_s$  in the equation to the text "Control many features of the vocalizations: air sac pressure and s.v. tension".

**Two** time dependent parameters  
Control many features of the vocalizations:  
air sac pressure and s.v. tension

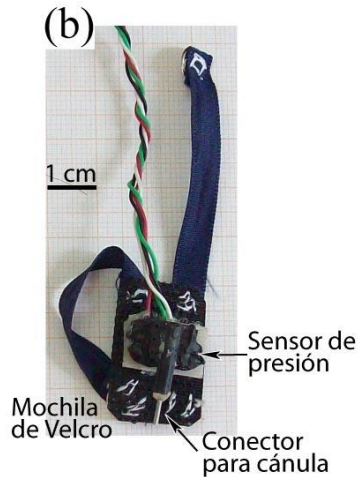
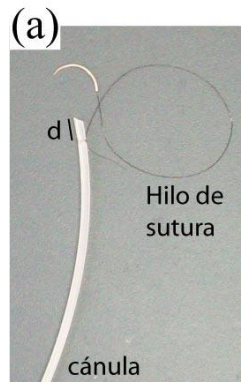


# Dynamics of the model





# Direct measurement of pressure and muscle activity

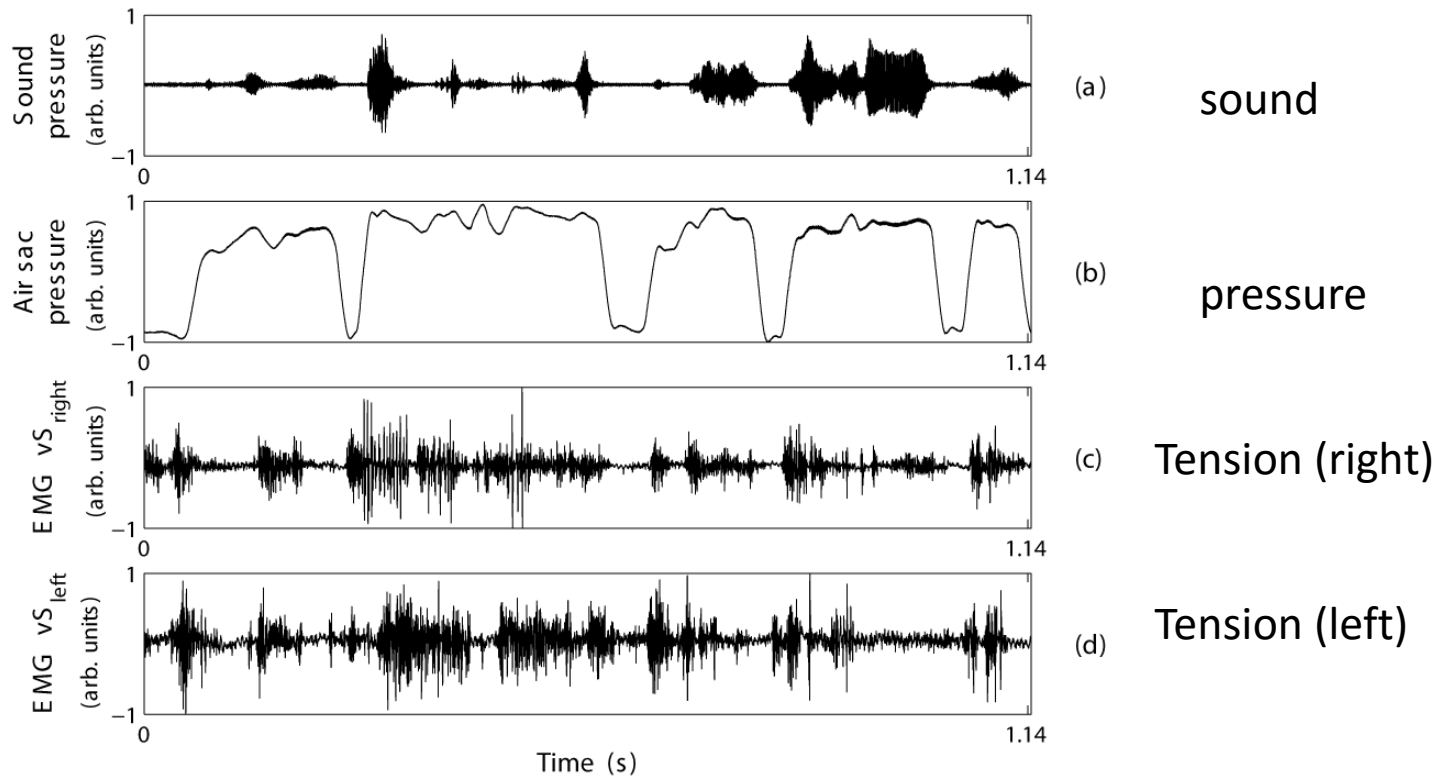
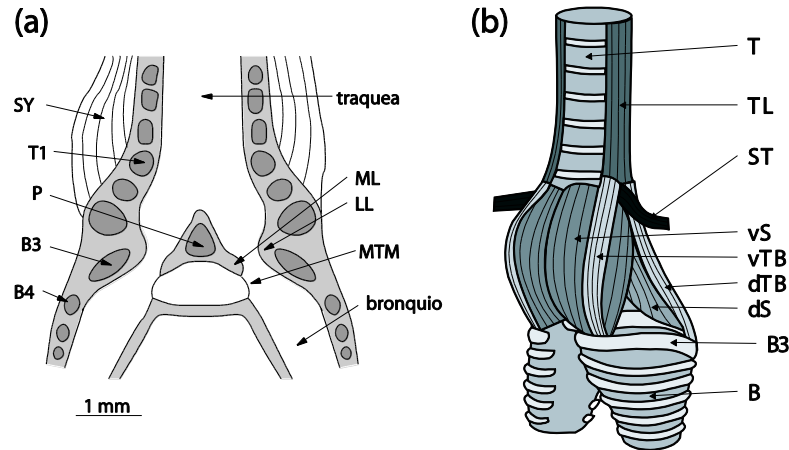


Air sac Pressure

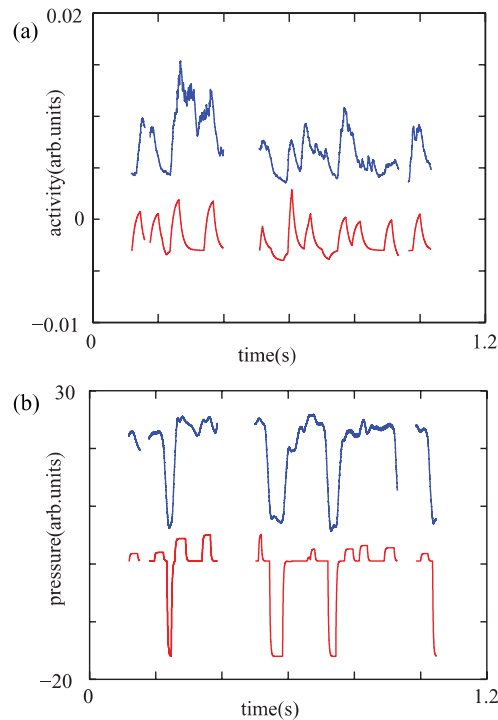


Tension  
(activity of vS muscle)

# Not that simple, these instructions...



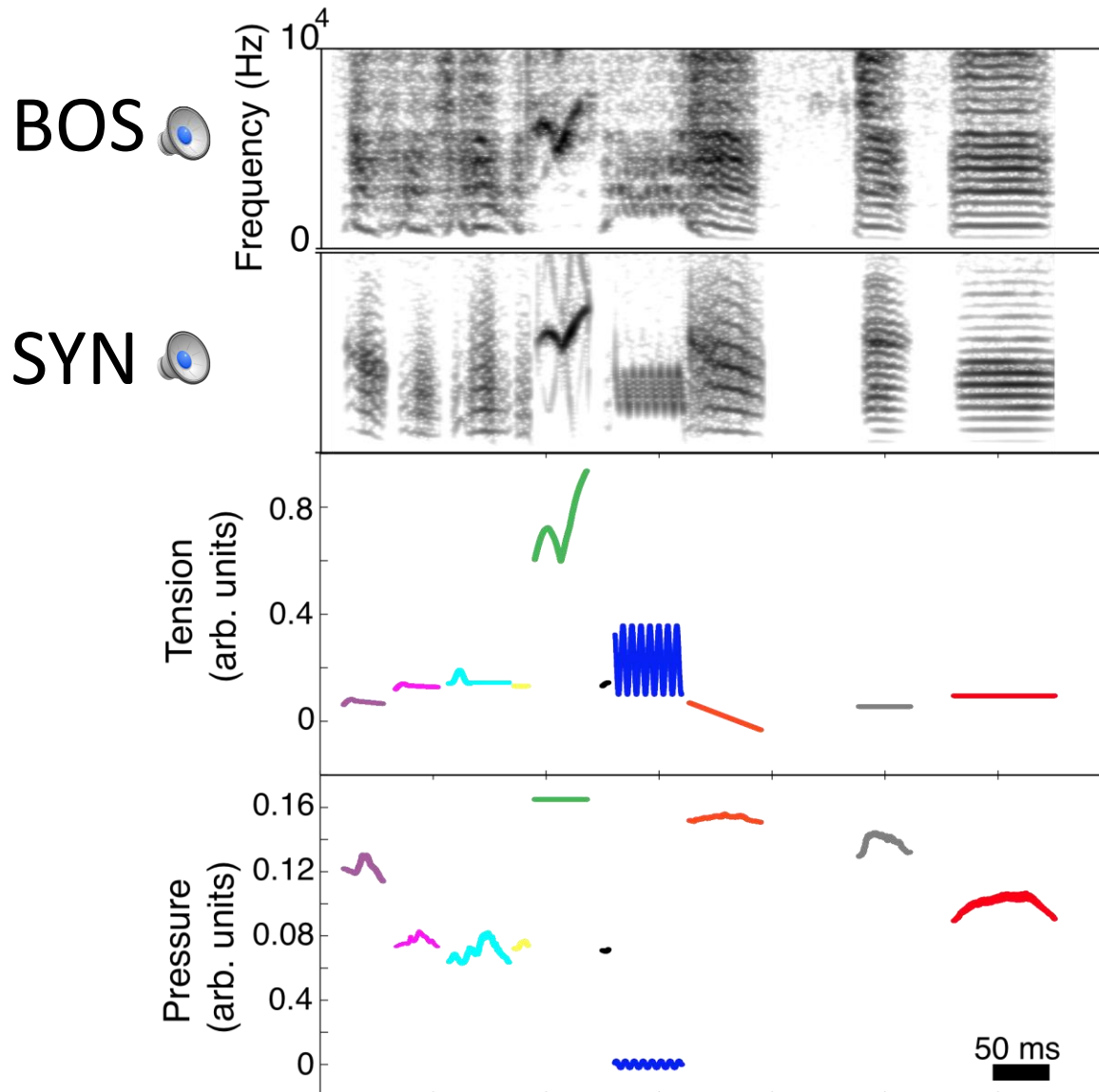
# 1. Reconstructed Instructions, Compared with the measured ones



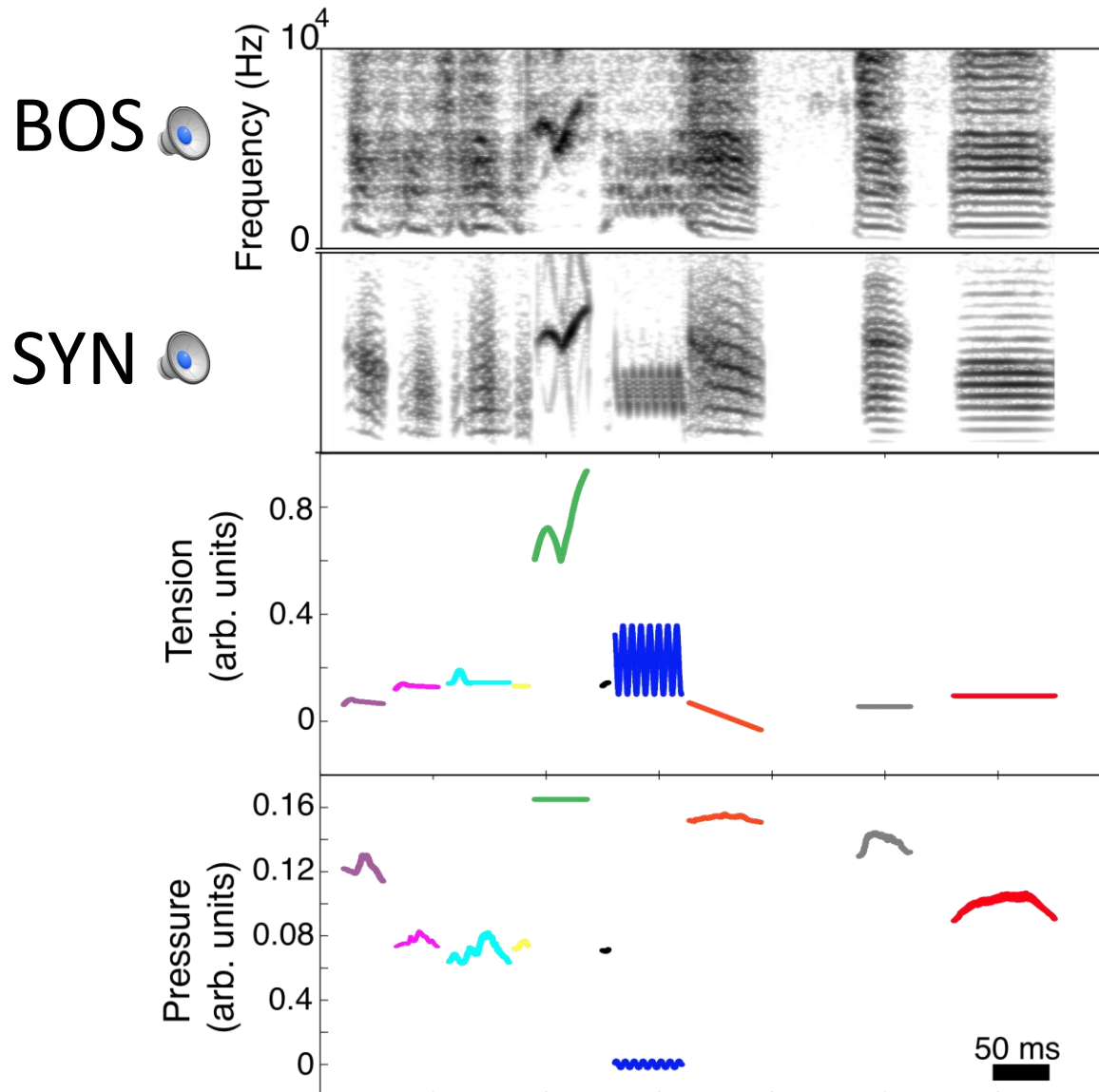
we fit  $\alpha$  (pressure) and  $\beta$  (tension) in the normal form model so that BOS and SYN share spectral features (Fundamental, Spectral content)



## 2. Synthesize song with the model



## 2. Synthesize song with the model



But... can we ask  
the bird?



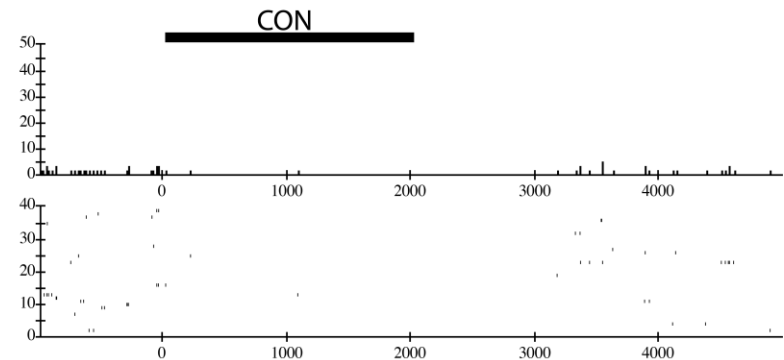
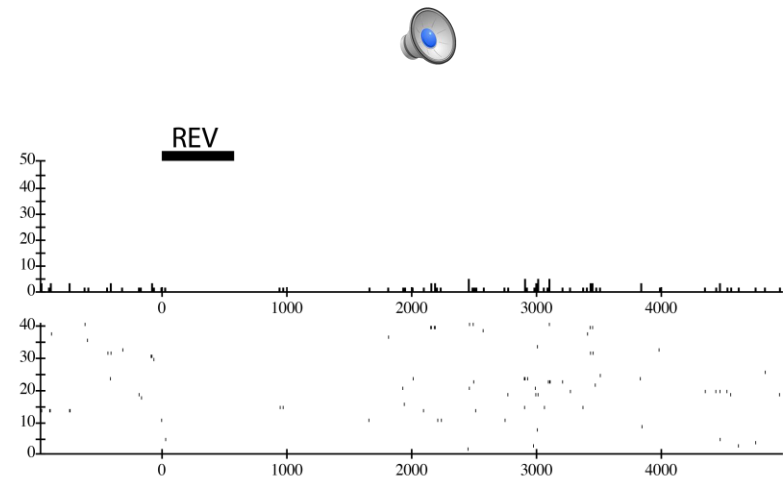
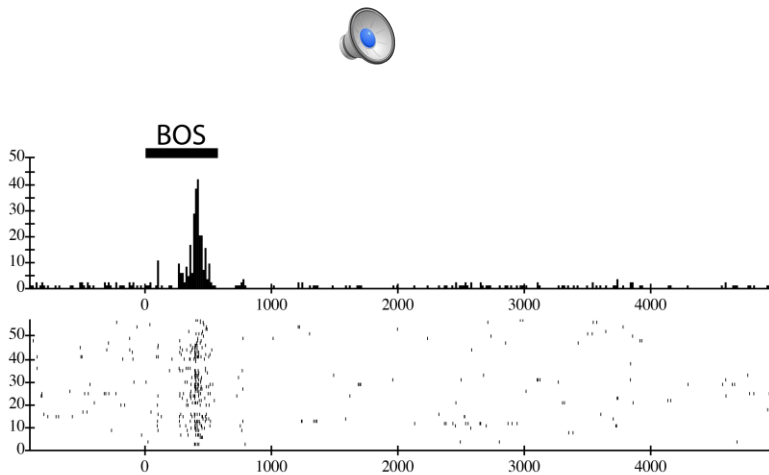
From Dan's Lab



From Dan's Lab

# Testing the model

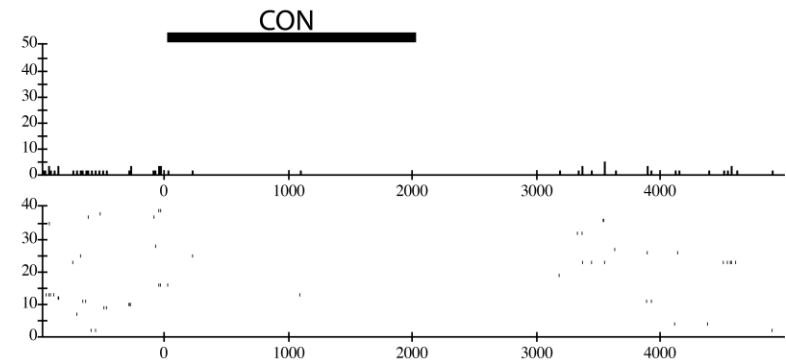
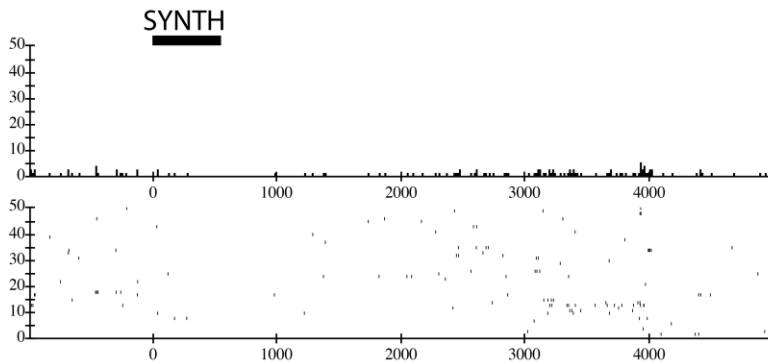
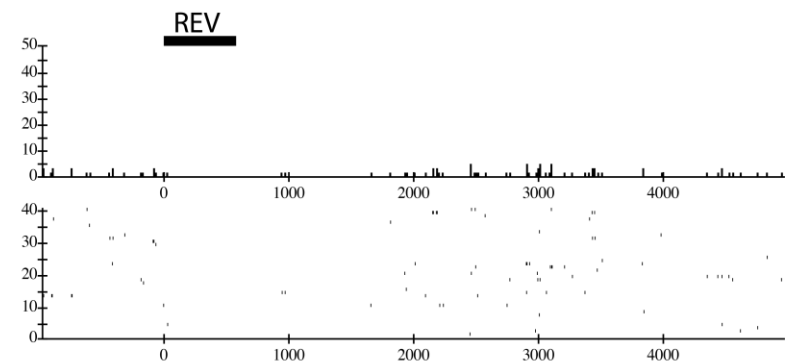
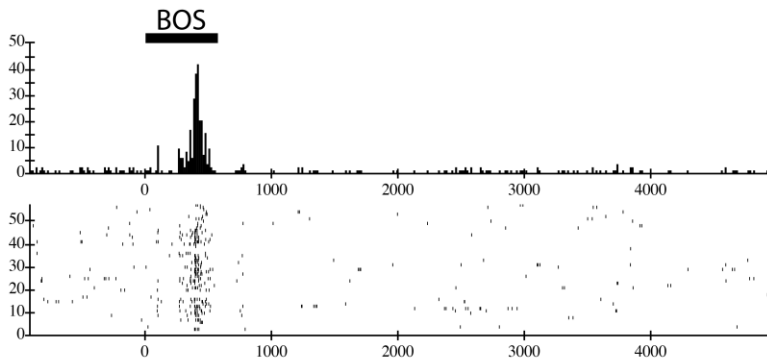
Neurons in HVC respond selectively to the bird's own song (BOS)





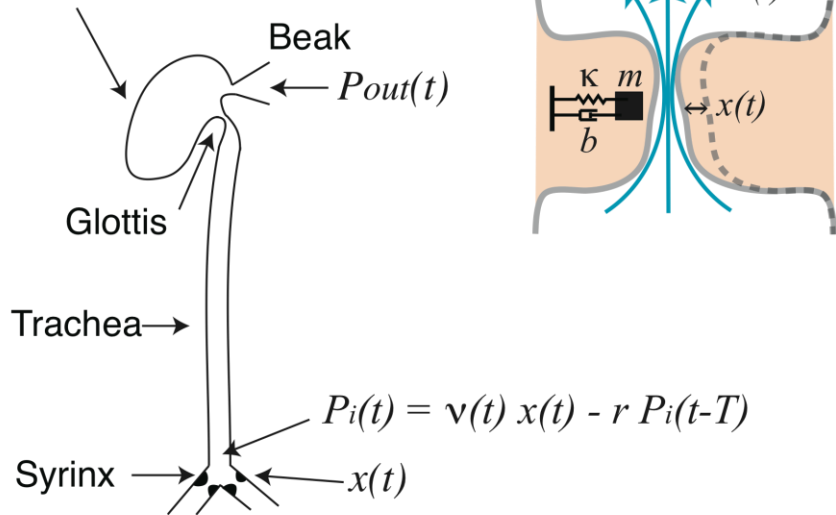
# Testing the model

Neurons in HVC respond selectively to the bird's own song (BOS)



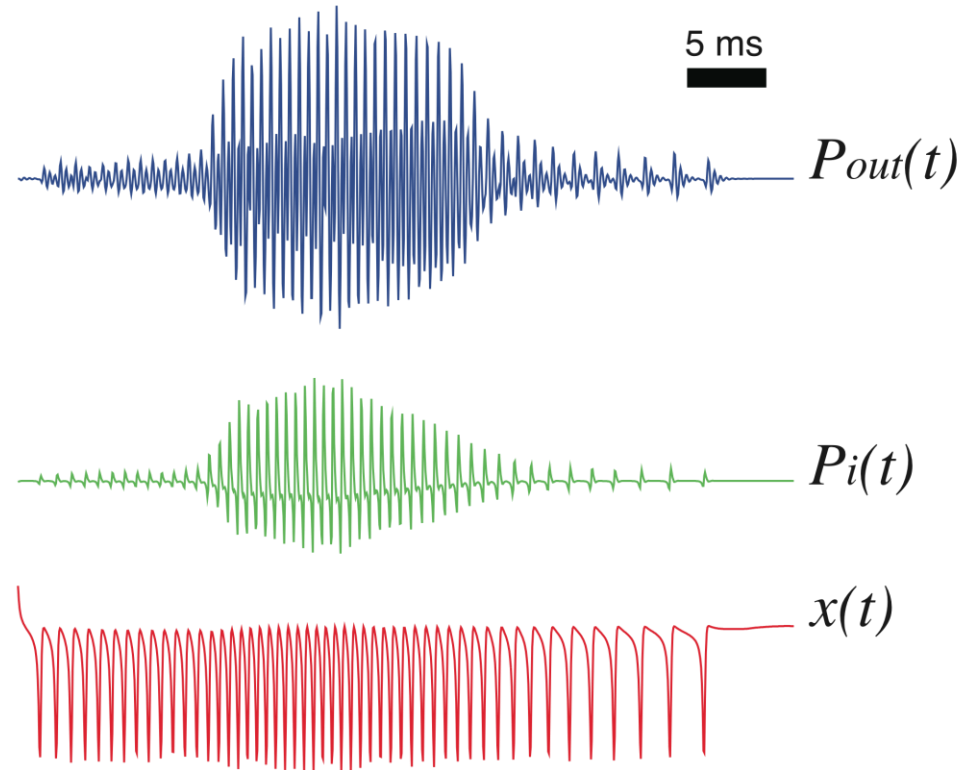
# A more detailed modeling

OEC: modelled as a  
Helmholtz oscillator



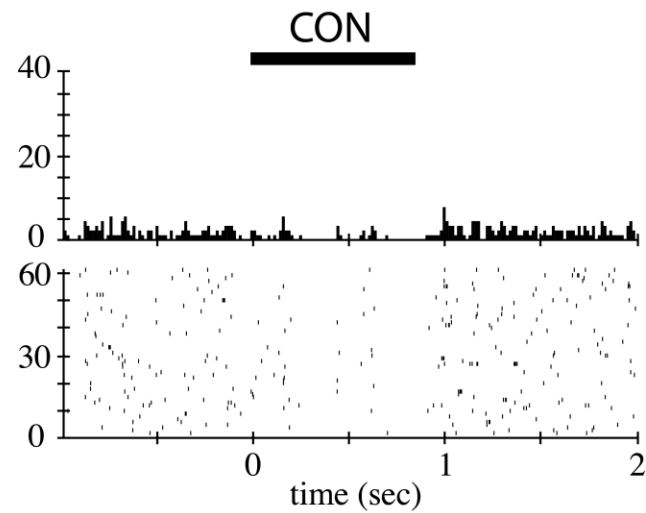
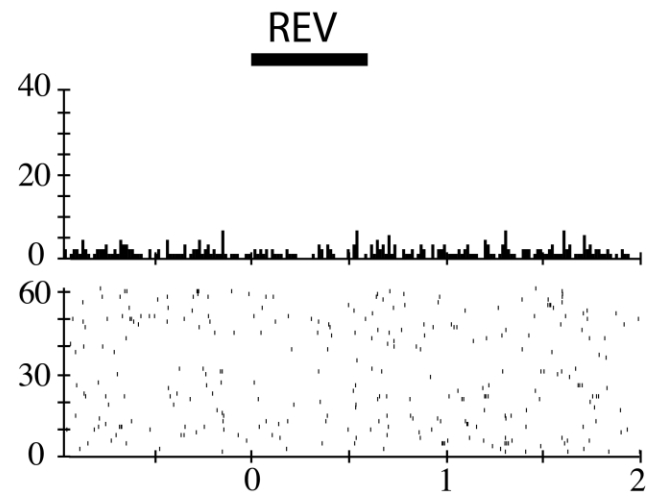
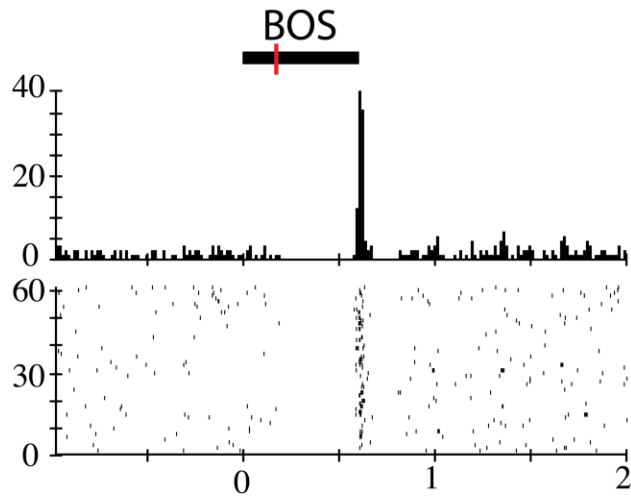
$$\frac{dx}{dt} = y$$

$$\frac{dy}{dt} = -\alpha(t)\gamma^2 - \beta(t)\gamma^2 x - \gamma^2 x^3 - \gamma x^2 y + \gamma^2 x^2 - \gamma x y$$

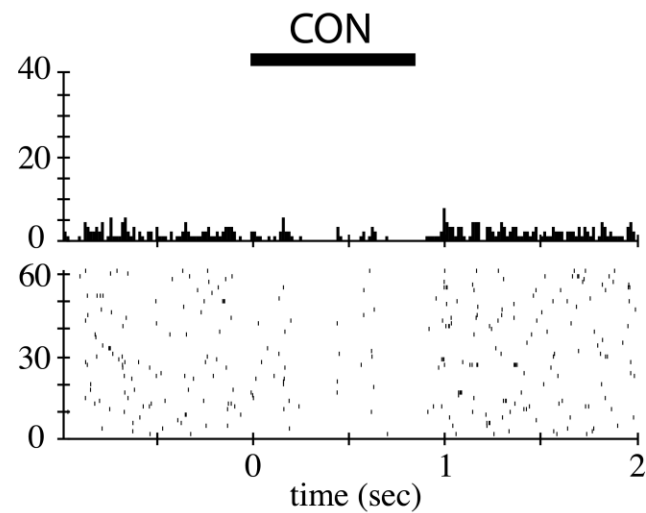
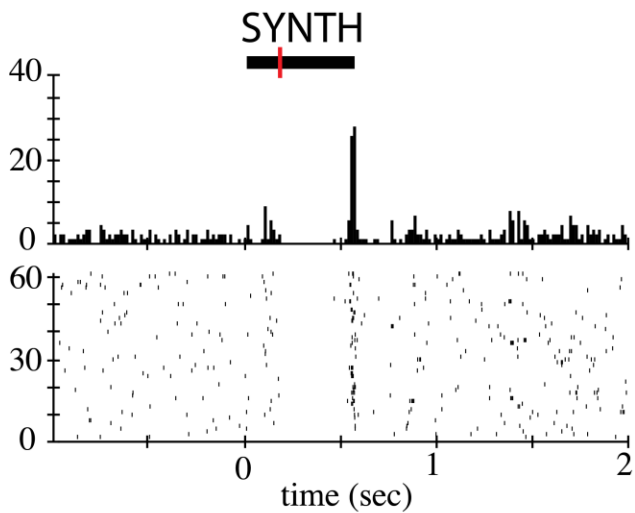
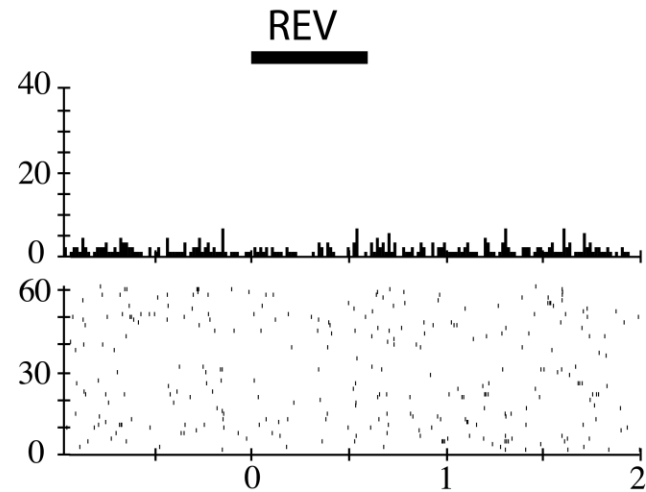
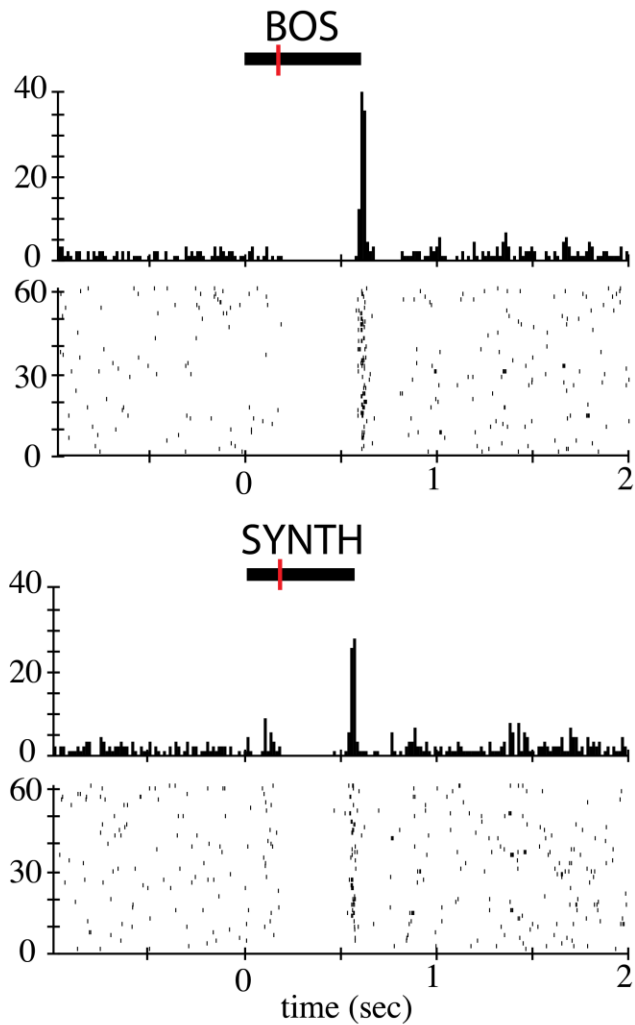


- ✓ More detailed modeling of the vocal tract (not just 3 tubes).  
Oropharyngeal cavity as a resonator
- ✓ Intrinsic noise in the activity of the syringeal muscles

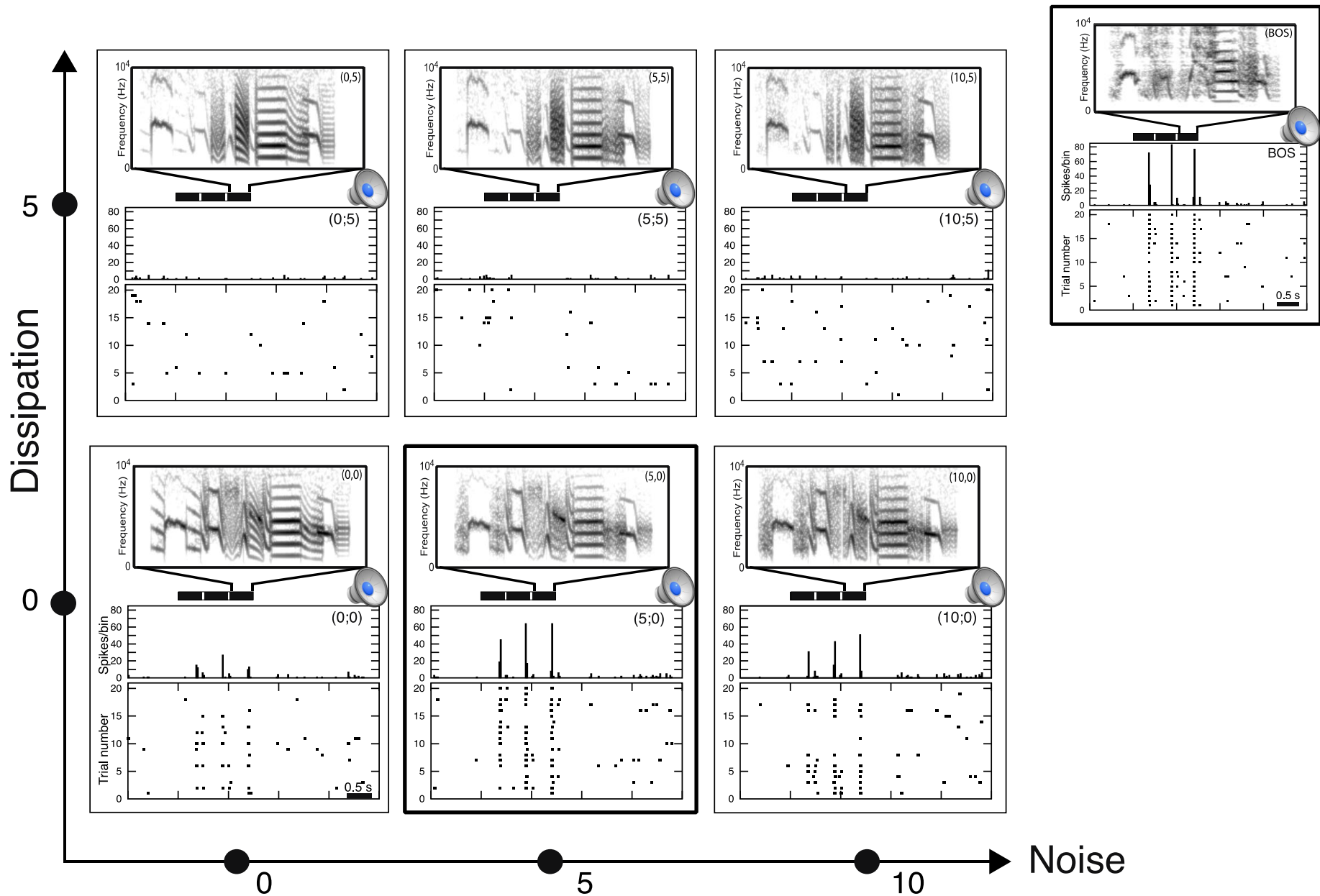
# A more detailed modeling



# A more detailed modeling



# A strategy for studying a hierarchy of importance for the elements in the model

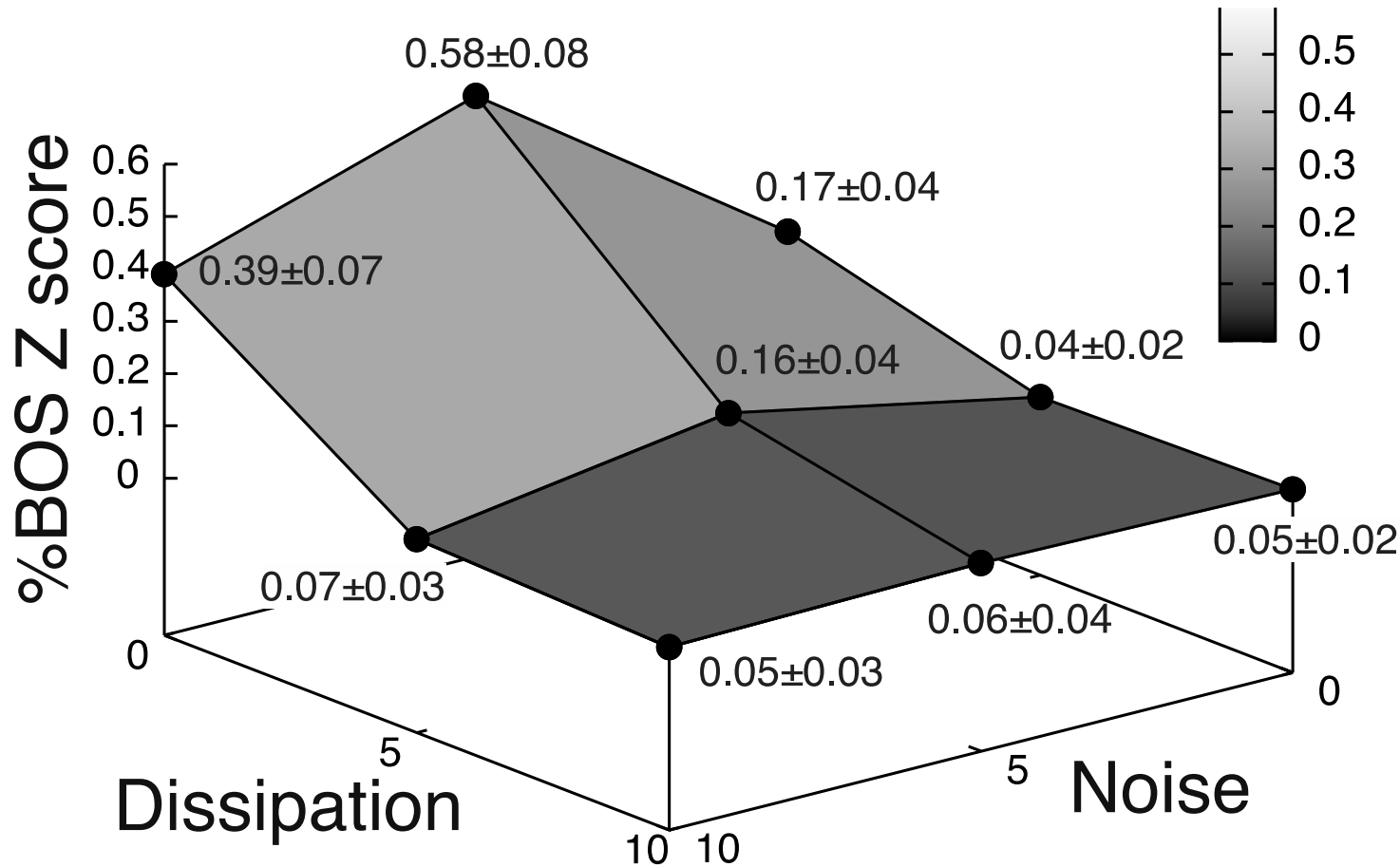




# Tuning surface

The resonant cavity is very relevant (can be controlled by the birds while singing)

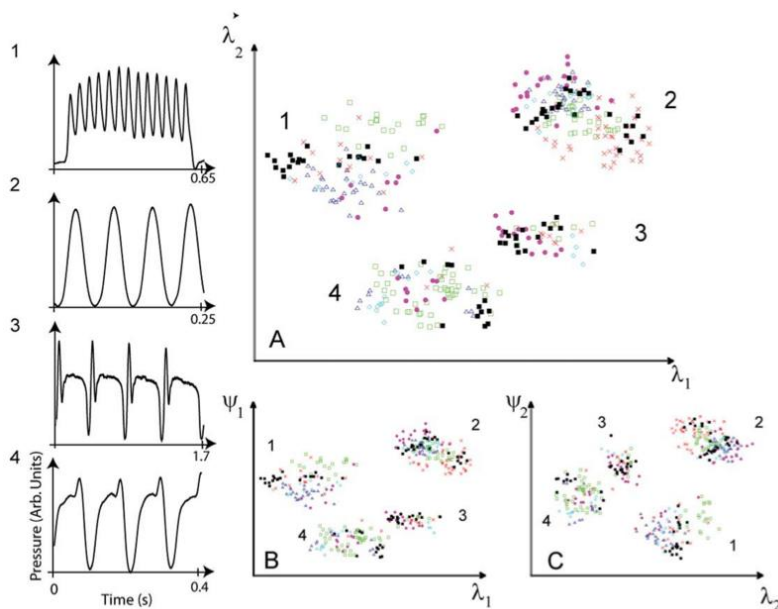
The noise has a particular value that maximize the responses



How complex, those instructions? The canary,  
candidate for simpler gestures...

a

Air sac pressure  
(arb. units)

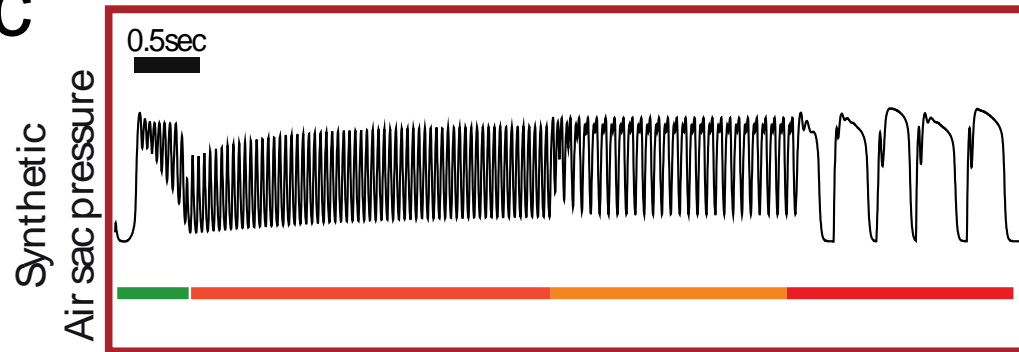


And they are the solutions of a  
low dimensional dynamical system

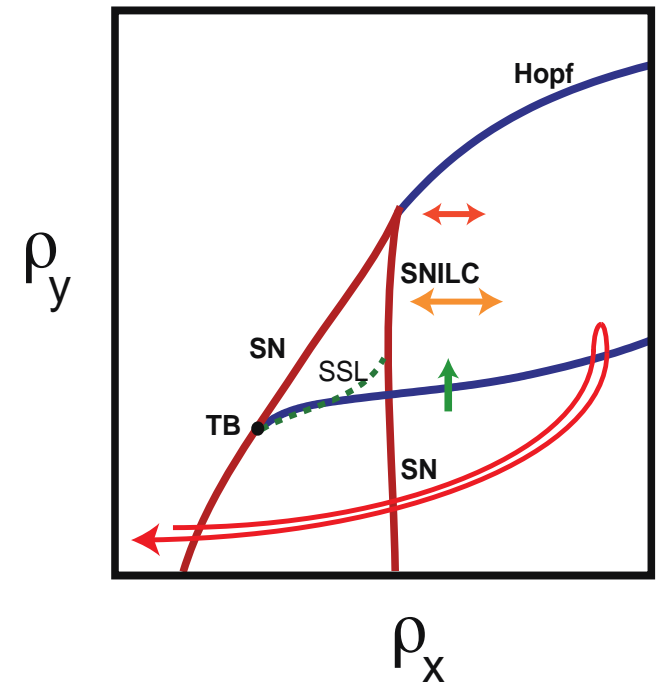
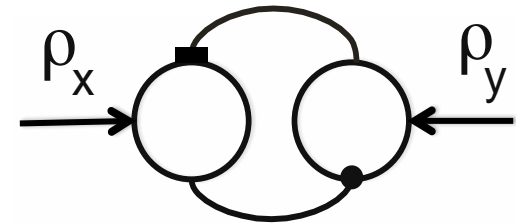
a



c



b

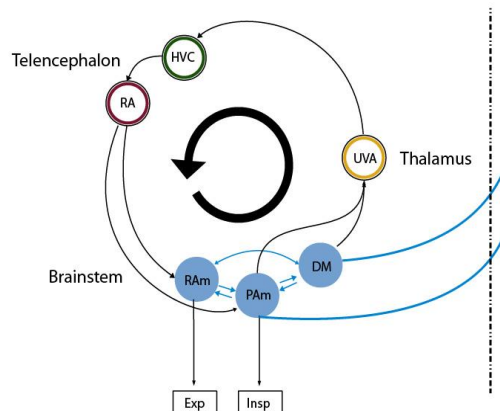


Can we design such a dynamical system compatible with the known anatomy?

# Is it possible to build a **model**?

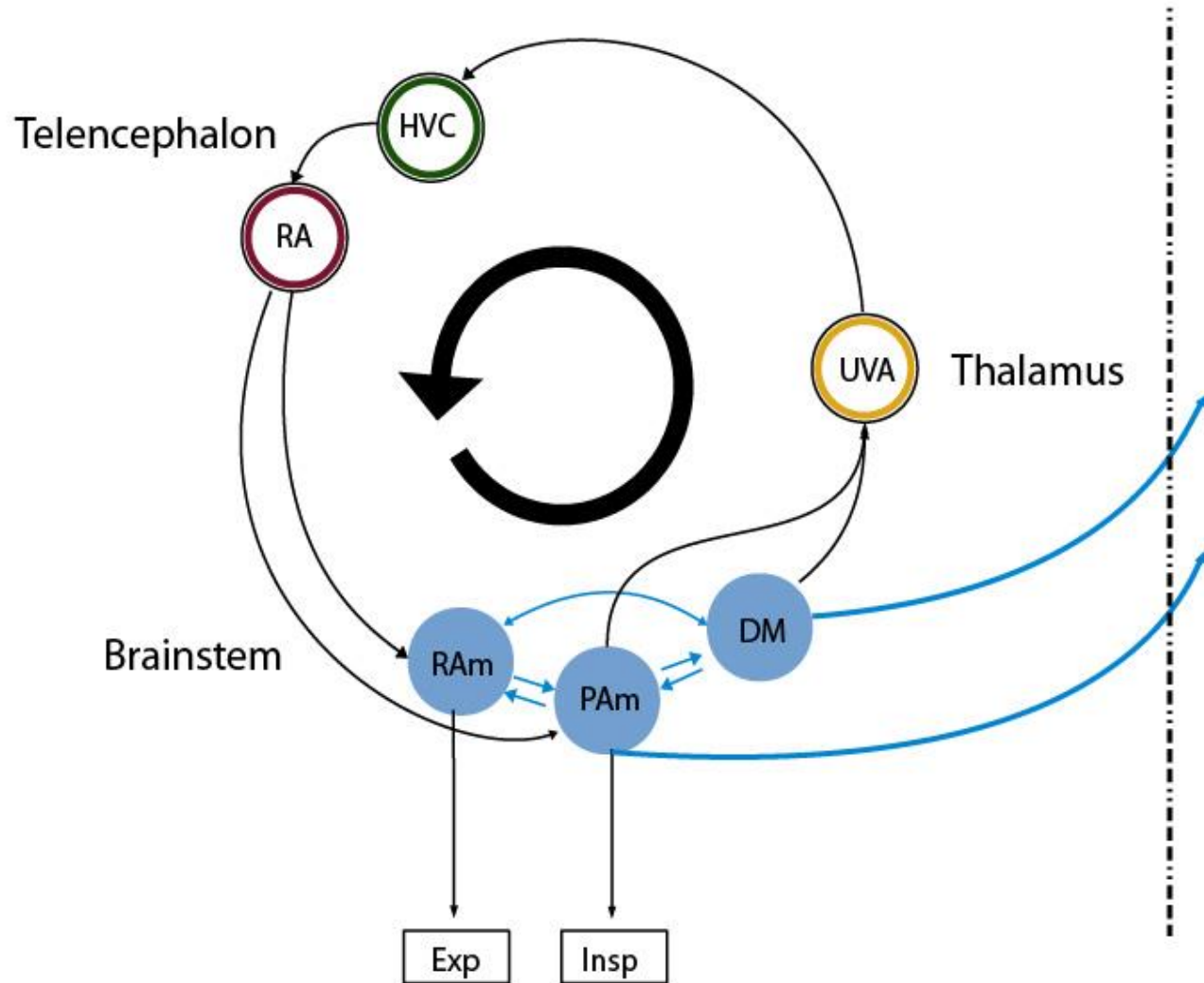
1. whose variables are **the activities** of different areas of the song system,
2. With an **expiratory related** area whose activity fits the **recorded pressure** patterns,

## Conceptual model



## Mathematical model

$$\frac{dx_i}{dt} = -x_i + S \left( \rho_i + \sum_j a_{ij} x_j \right),$$
$$S(x) = \frac{1}{1 + e^{-x}}$$

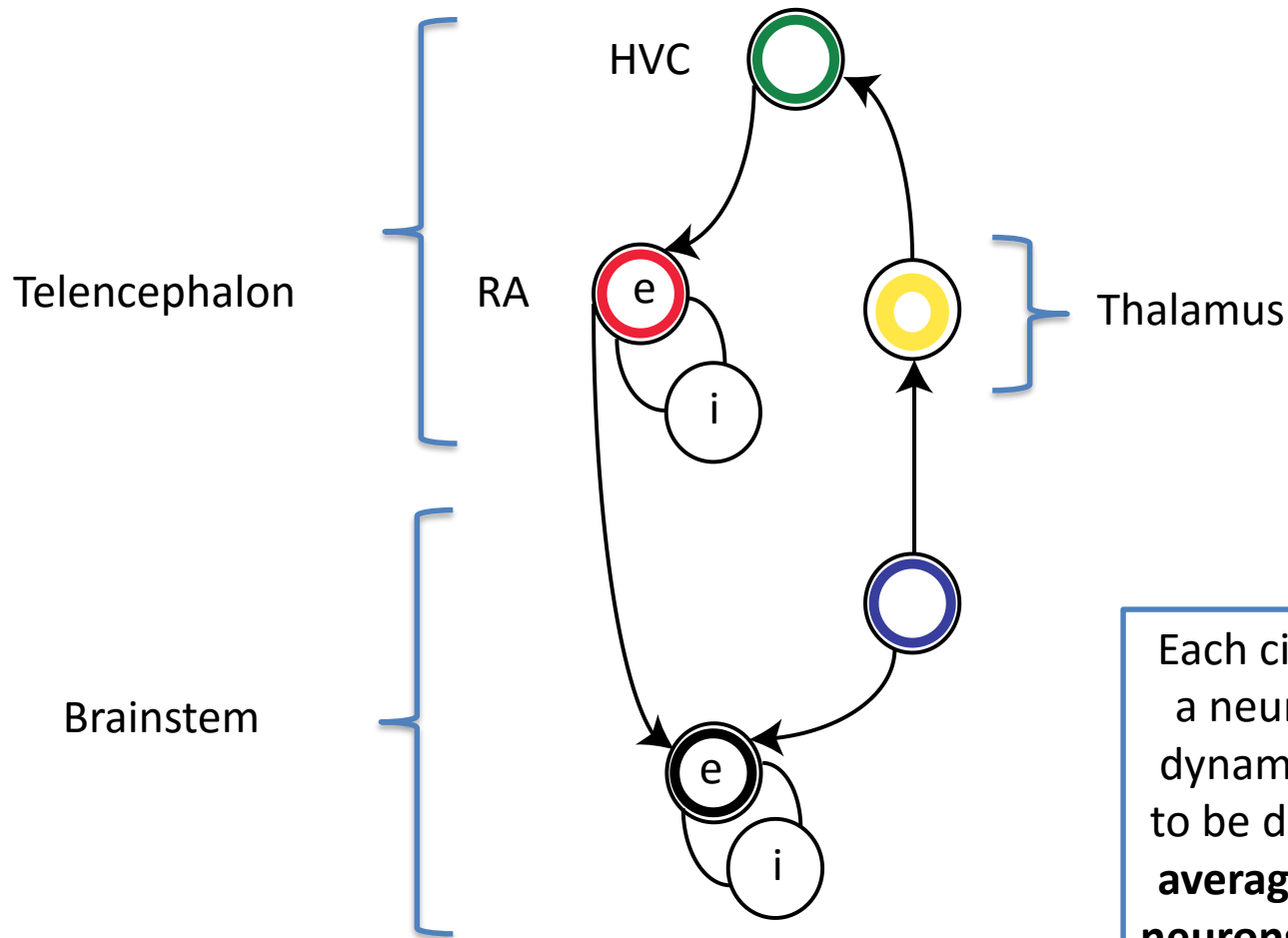


To achieve these goals we'll need  
an integrative or circular architecture

Adapted from Marc Schmidt's



This architecture is capable of generating the observables, with the known neural nuclei



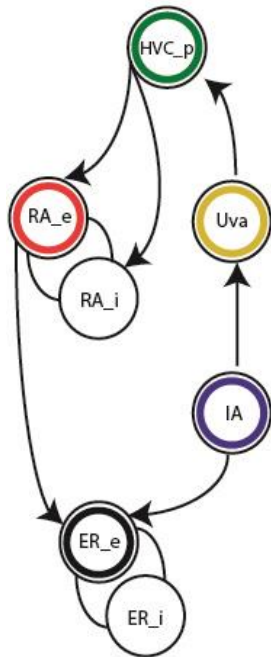
Each circle represents a neural nucleus, its dynamics is assumed to be described by **the average activity of its neurons**, and for those, we propose a simple **additive model**

$$\frac{dx_i}{dt} = -x_i + S \left( \rho_i + \sum_j a_{ij} x_j \right),$$

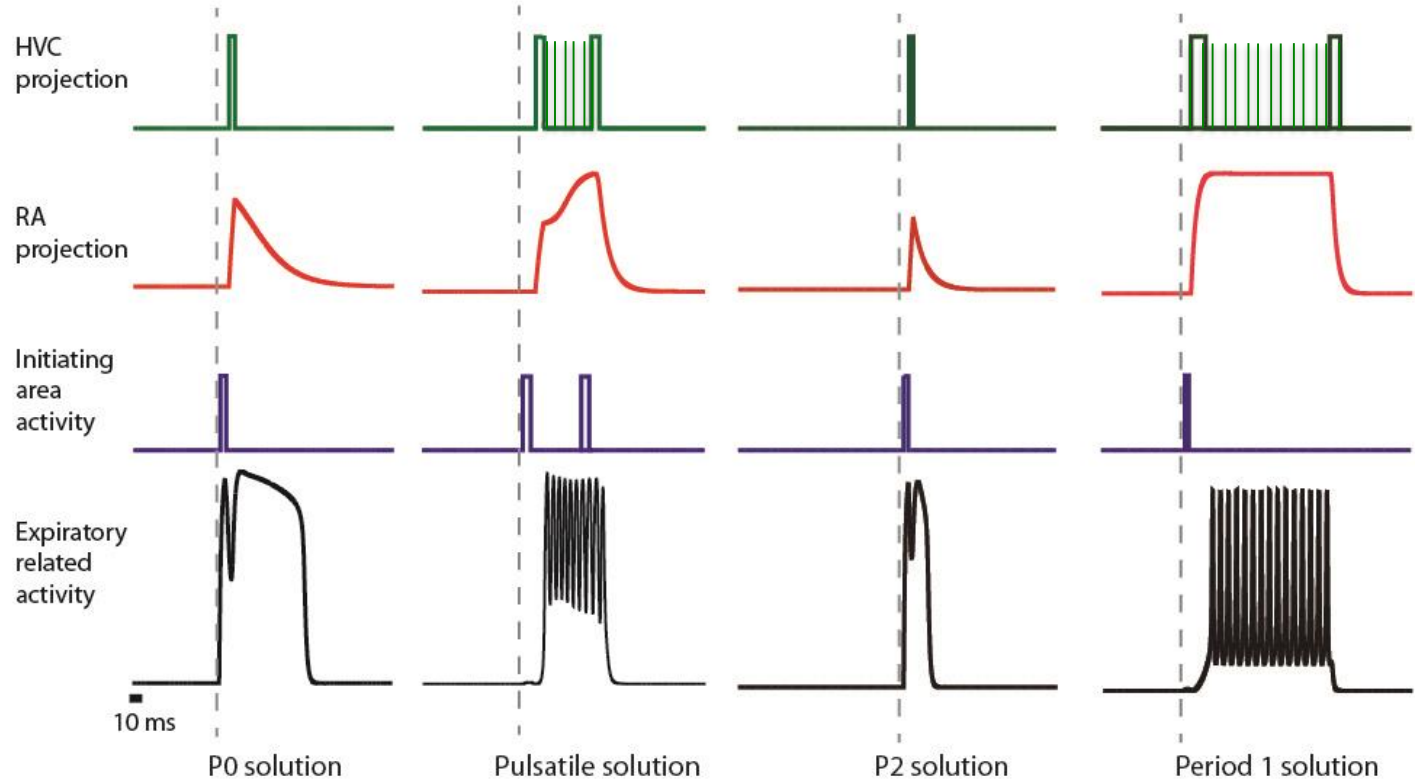
$$S(x) = \frac{1}{1 + e^{-x}}$$

# The circular model

A



B

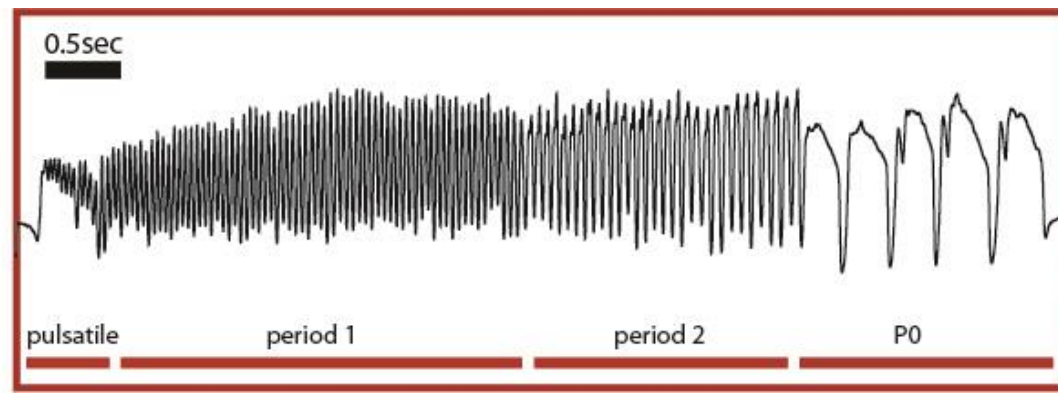


C

D

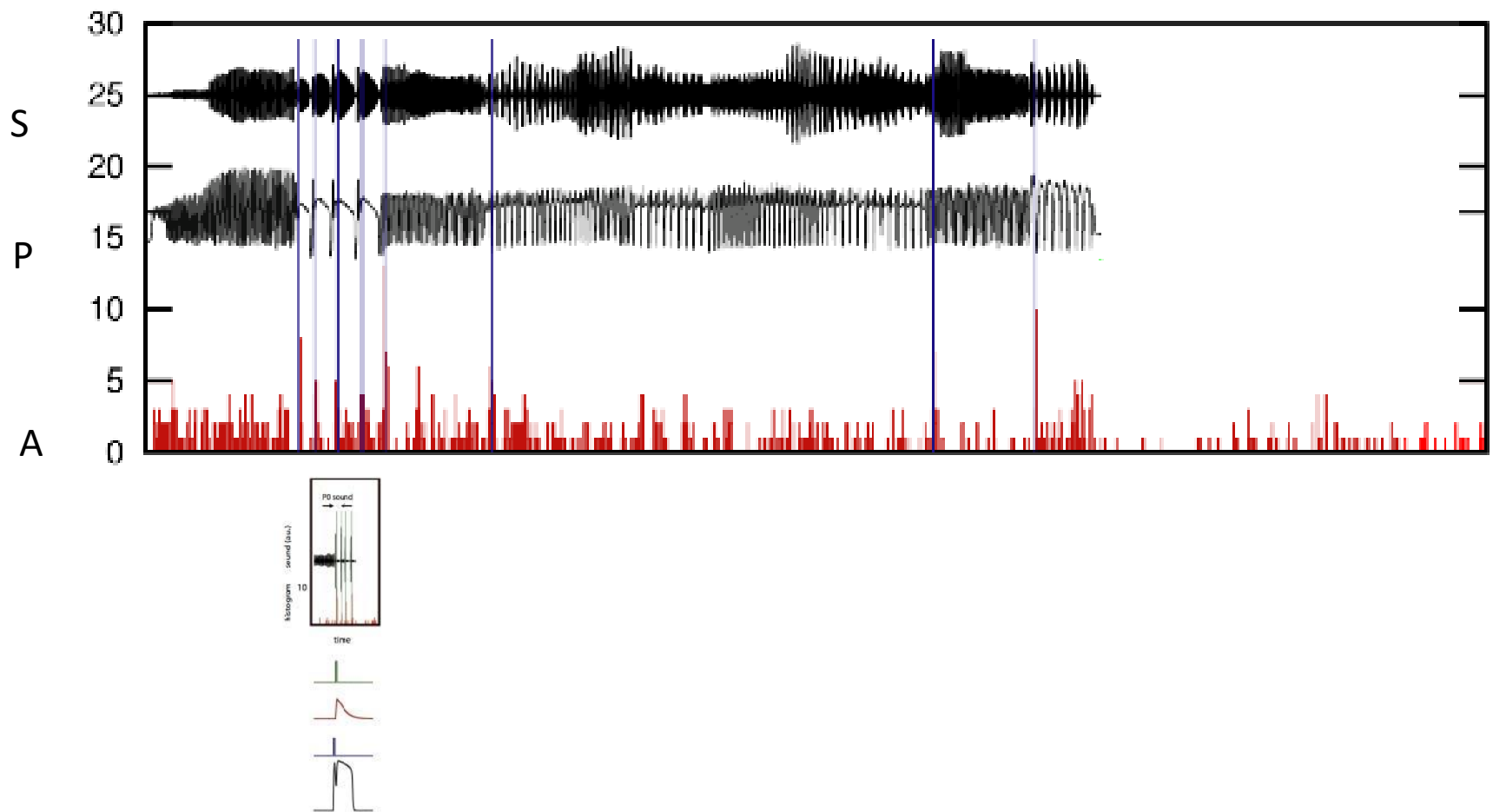
E

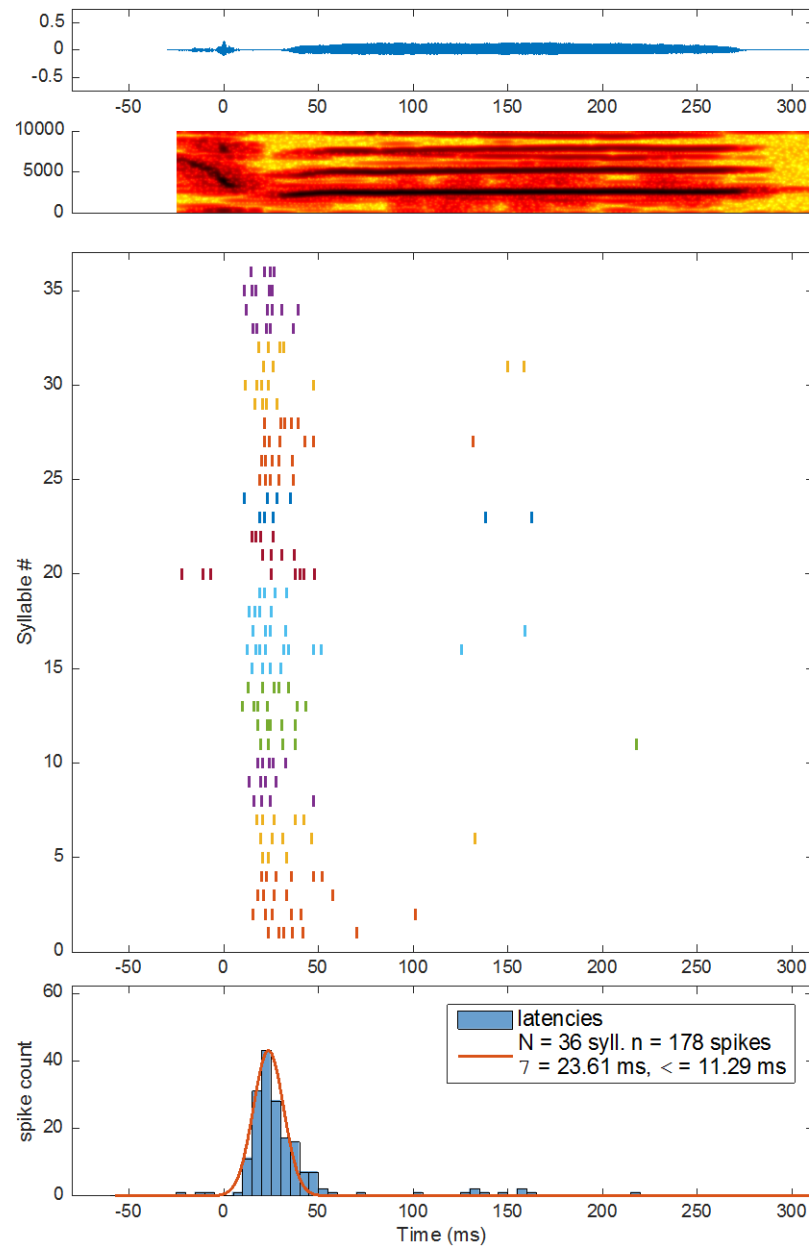
Air sac pressure  
(arb. units)



## Preliminary data

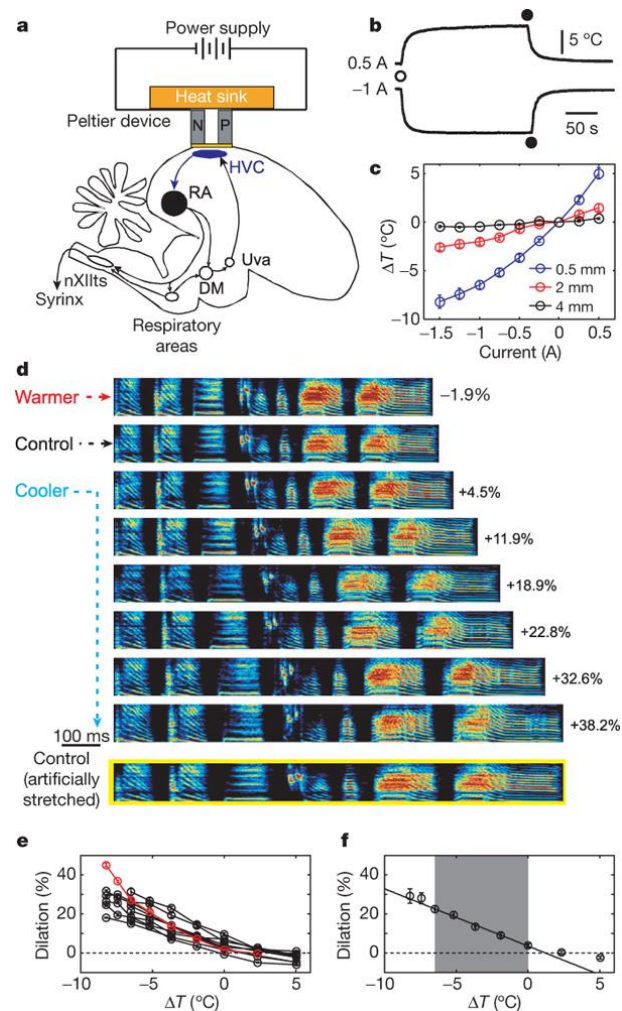
1. For P0 solutions, after the first pressure peak
2. At transitions





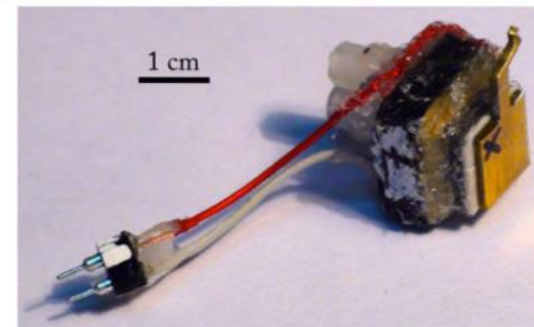
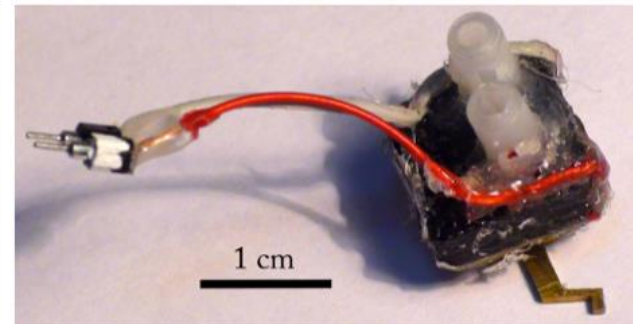
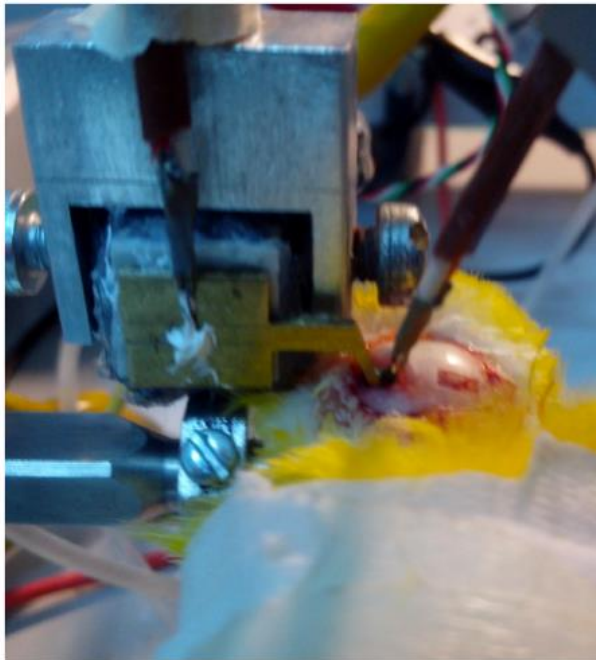
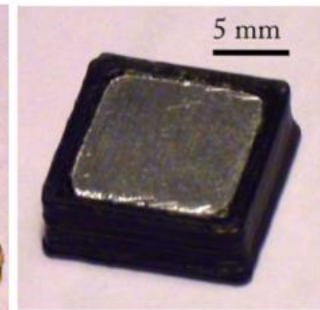
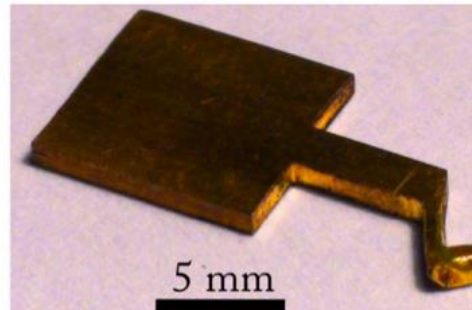
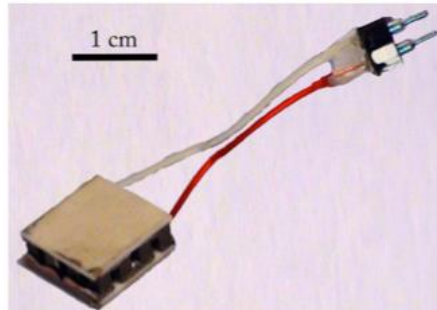
Ana Amador,  
Santiago Boari  
Cecilia Herbert

# A continuous representation of time at the telencephalon, organizing the system as a top down structure: “Cool” experiments

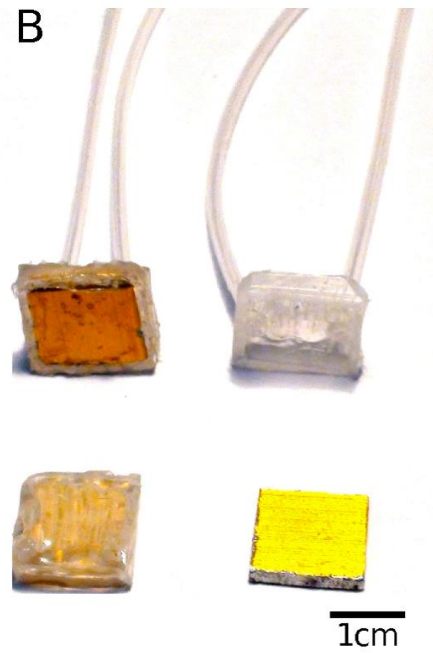


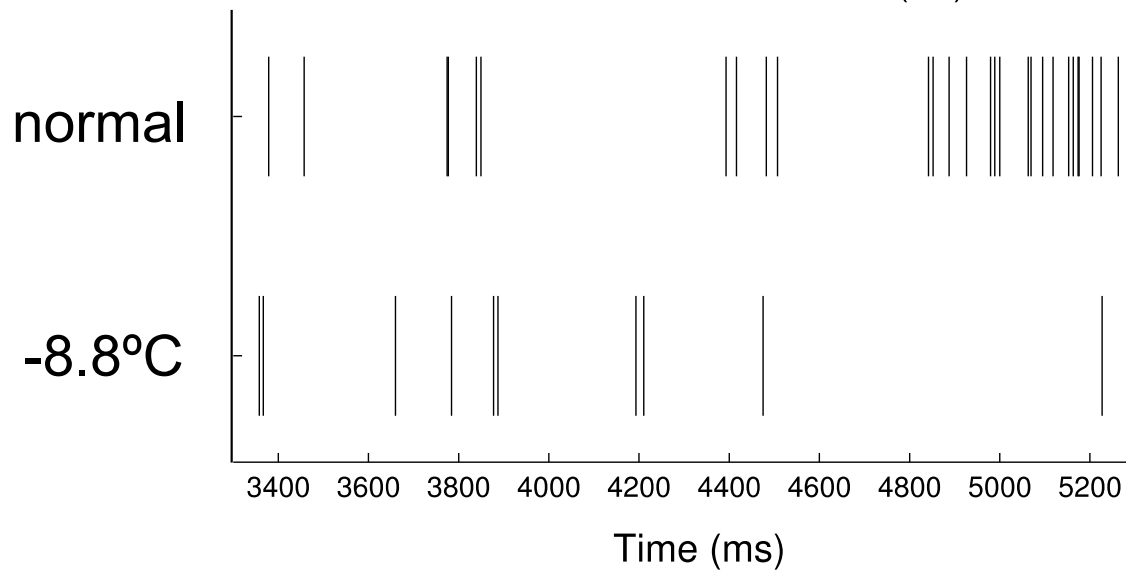
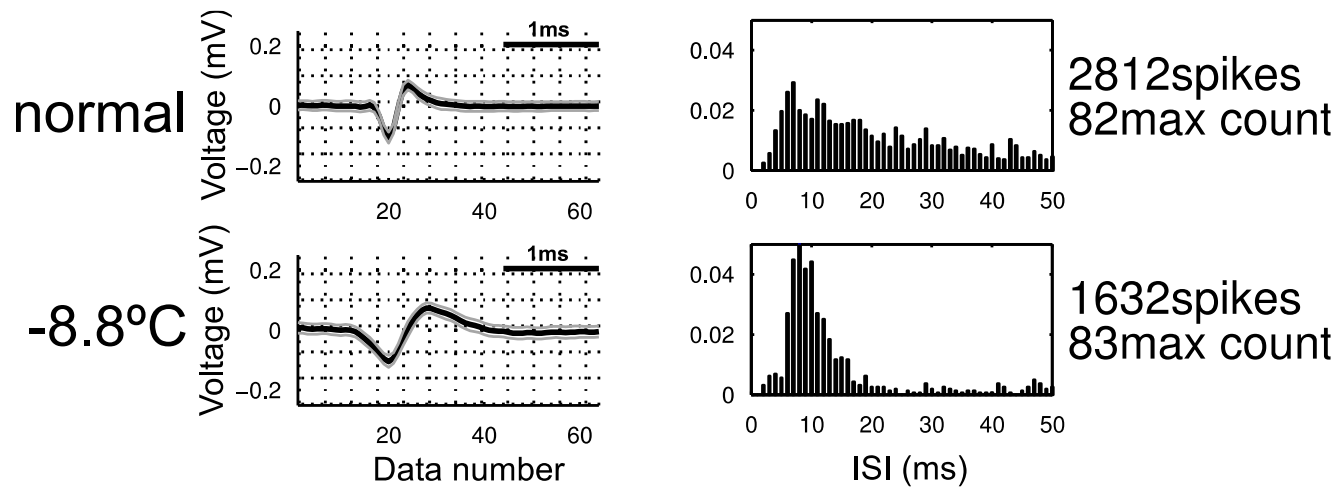
Consistent with one  
Time scale...

How do we introduce the cooling into the model?



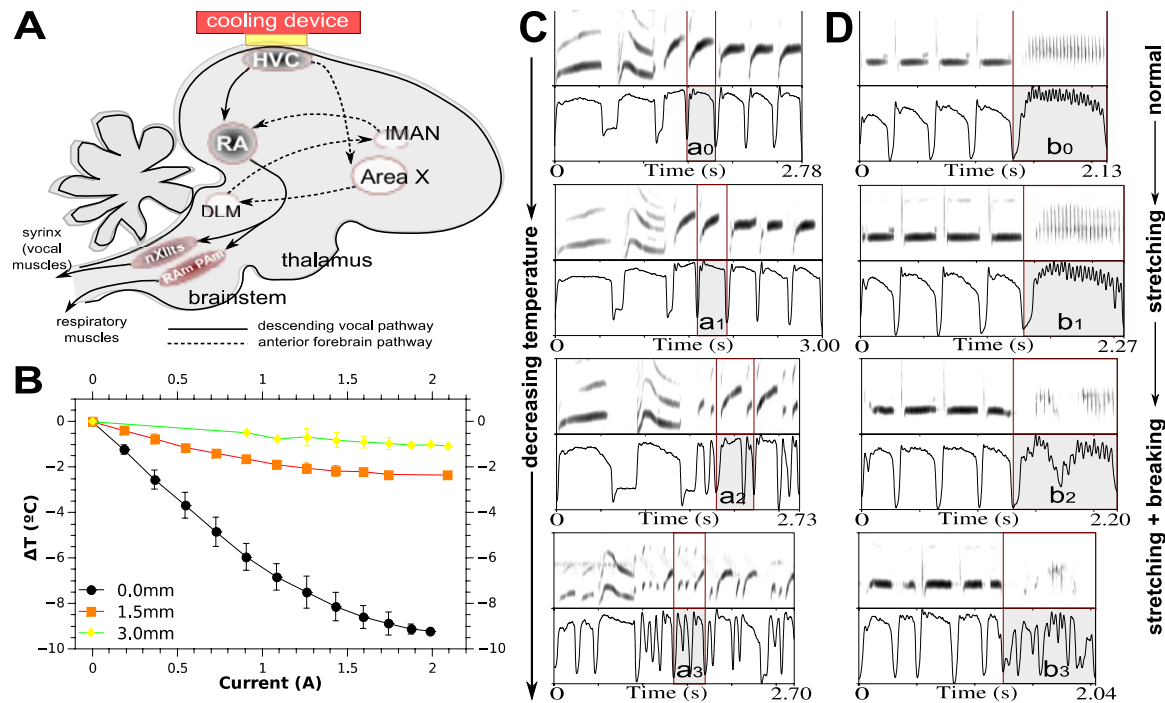








# The experimental data



normal

-1.3°C

-2.6°C

-3.8°C

-4.7°C

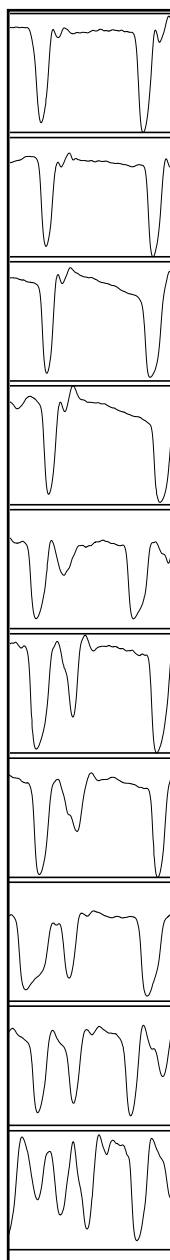
-5.5°C

-6.2°C

-6.6°C

-7.1°C

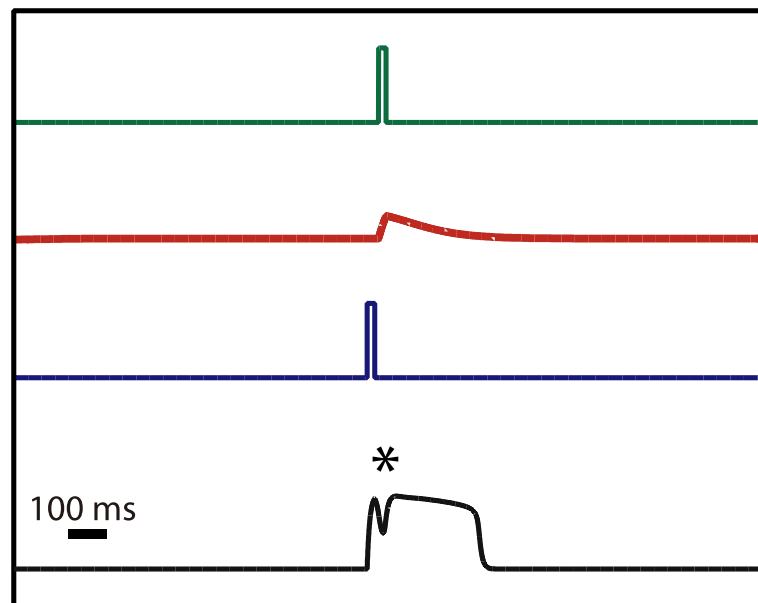
-7.5°C



0.5 sec

**A**

Normal Temperature



HVC  
projection

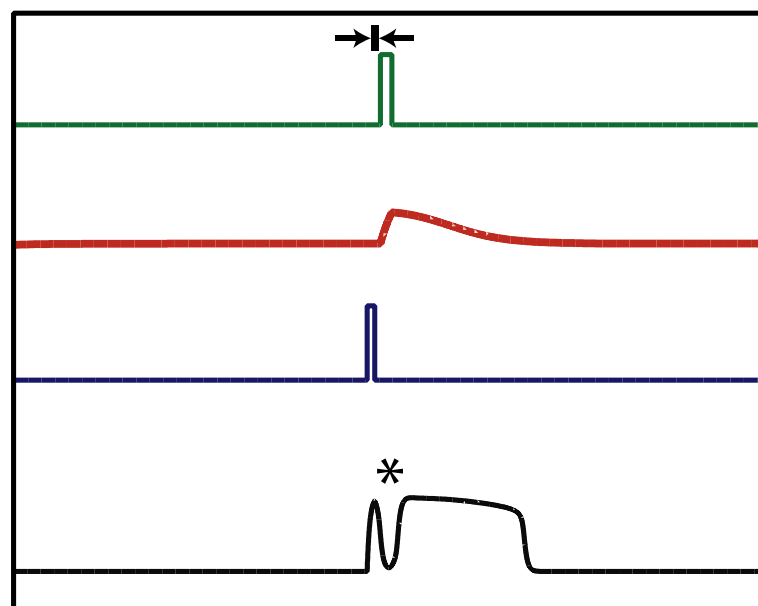
RA  
projection

Initiating  
area  
activity

Expiratory  
related  
activity

**B**

Cold Temperature



HVC  
projection

RA  
projection

Initiating  
area  
activity

Expiratory  
related  
activity

Time

## Conclusions

1. A nonlinear, **low dimensional model** of the syrinx can transduce relatively simple sinstructions into realistic sounds.
2. There seems to be a hierarchy of **progressive simplicity**: those relatively simple instructions are not arbitrary: they are also the solutions of **low dimensional** ODEs.
3. Zebra finches use complex and diverse acoustic units. To build a model for the physiological instructions we chose to work with canaries.
4. Our model requires expiratory related areas receiving a direct input and a processed one, integrated in a circular architecture.
5. Why would bursts occur at GTEs? Auditory-motor integration?

# Conclusions

- **Physics and Biology.** The paradigms are not necessarily incompatible. Hierarchies of importance can be established and progressive modeling is possible.
- Evidence of **low dimensional dynamics** at the level of the periphery
- Evidence of **low dimensional dynamics** at the level of the CNS?