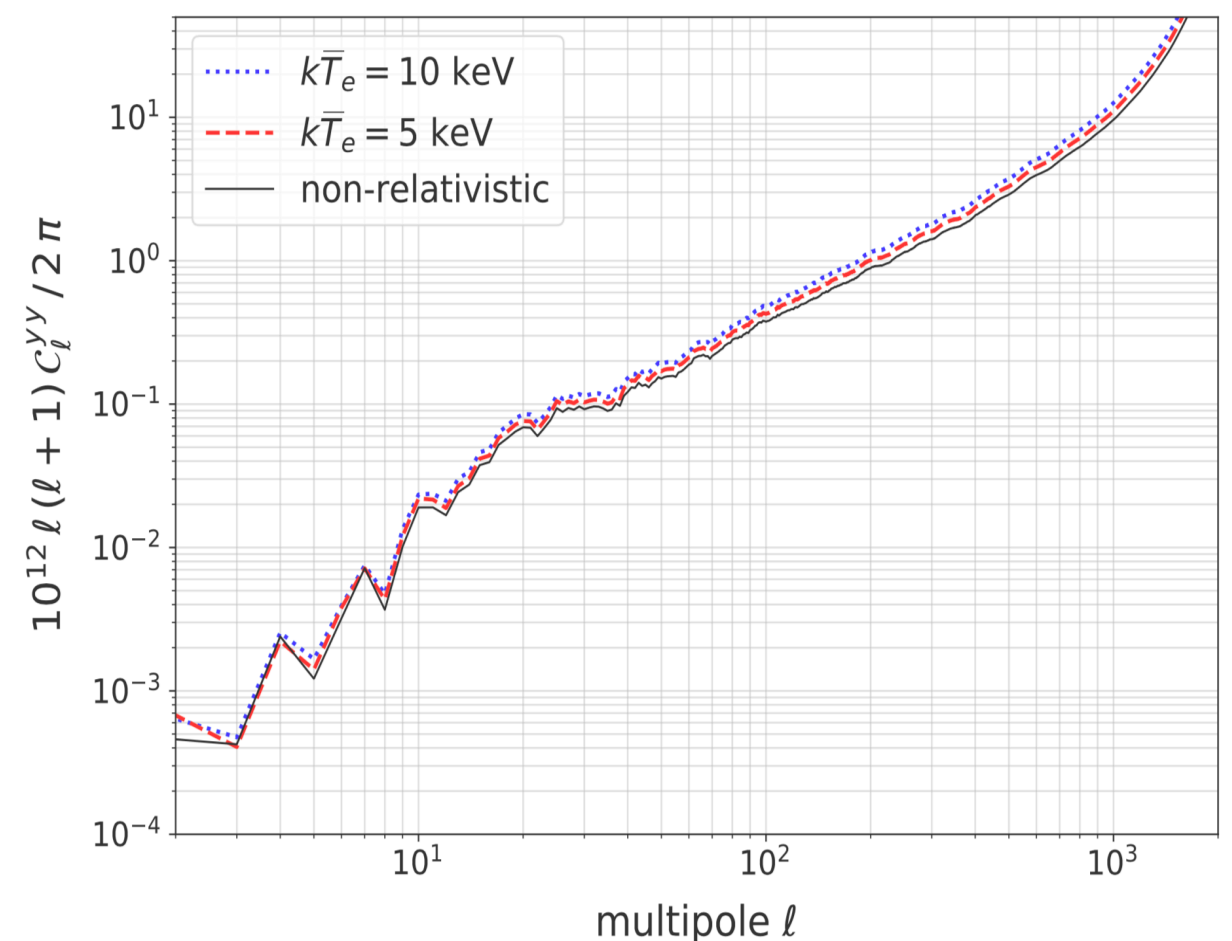
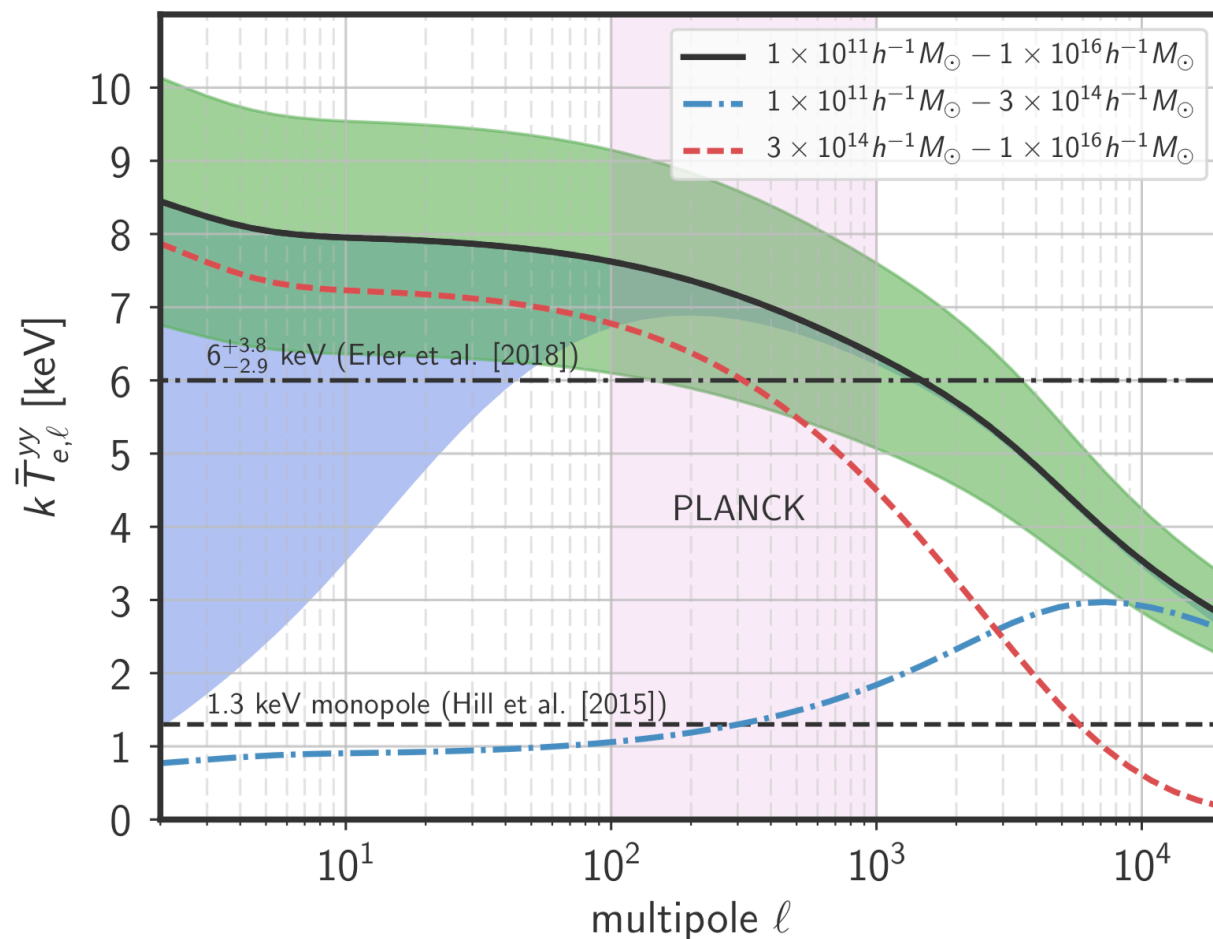
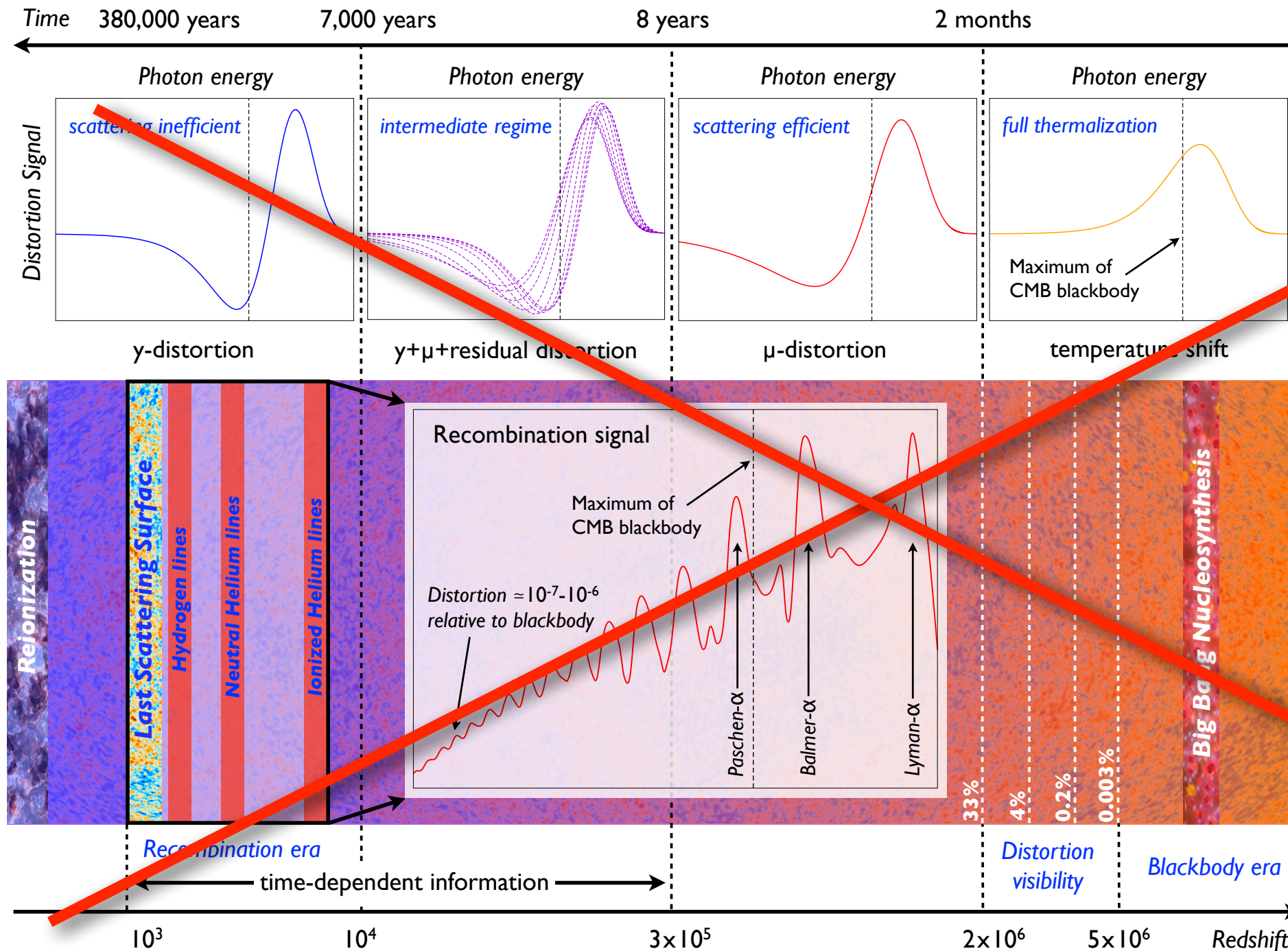


Can we neglect relativistic temperature corrections in the Planck SZ analysis?



Remazeilles, Bolliet, Rotti & JC, MNRAS, 483, 3459, 2019
Rotti, Bolliet, Remazeilles & JC, in preparation

Uniqueness of CMB Spectral Distortion Science



Guaranteed distortion signals in Λ CDM

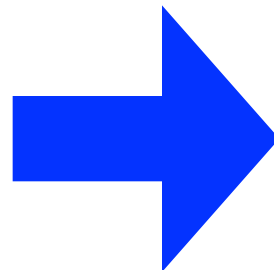
New tests of inflation and particle/dark matter physics

Signals from the reionization and recombination eras

Huge discovery potential

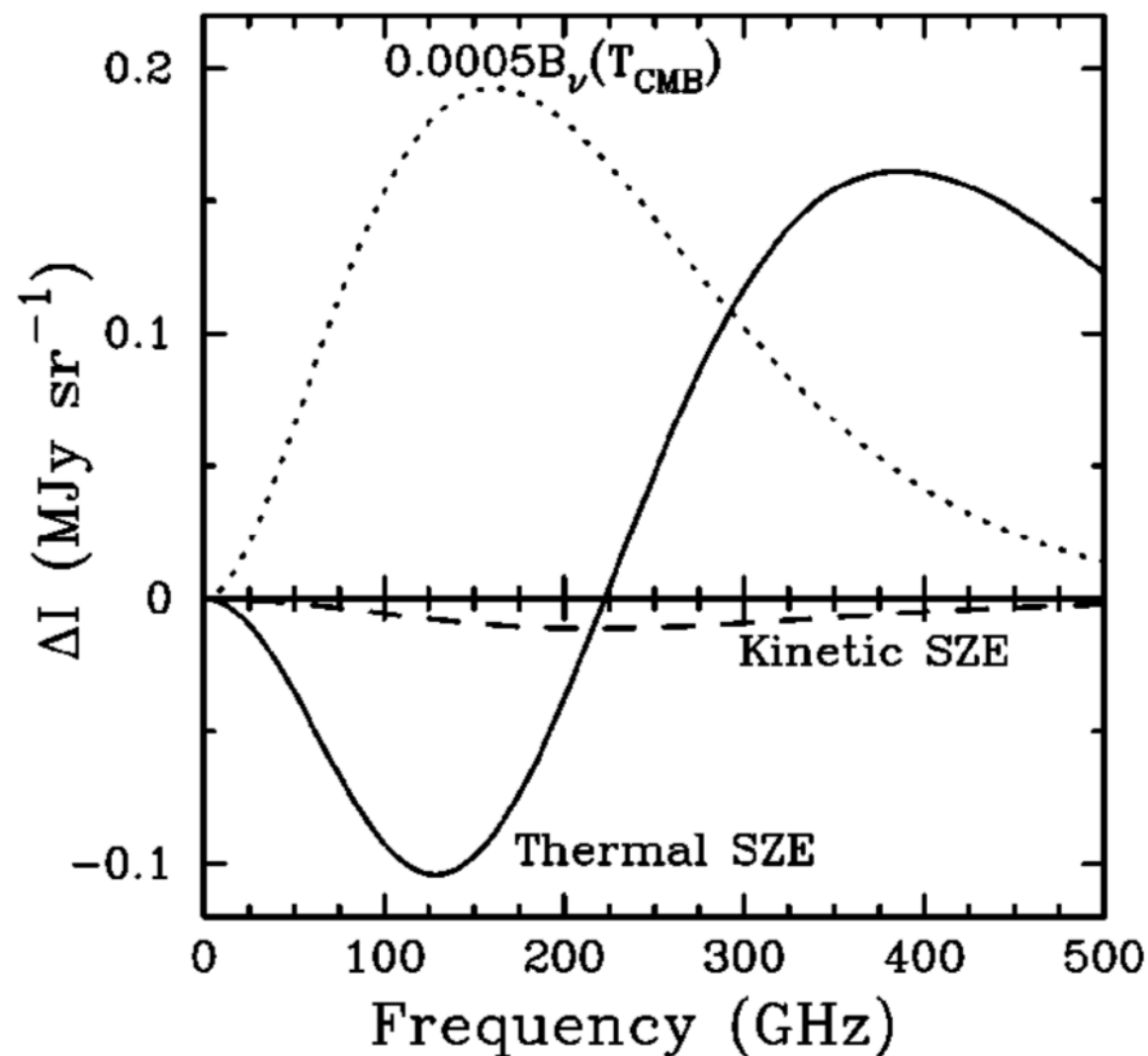
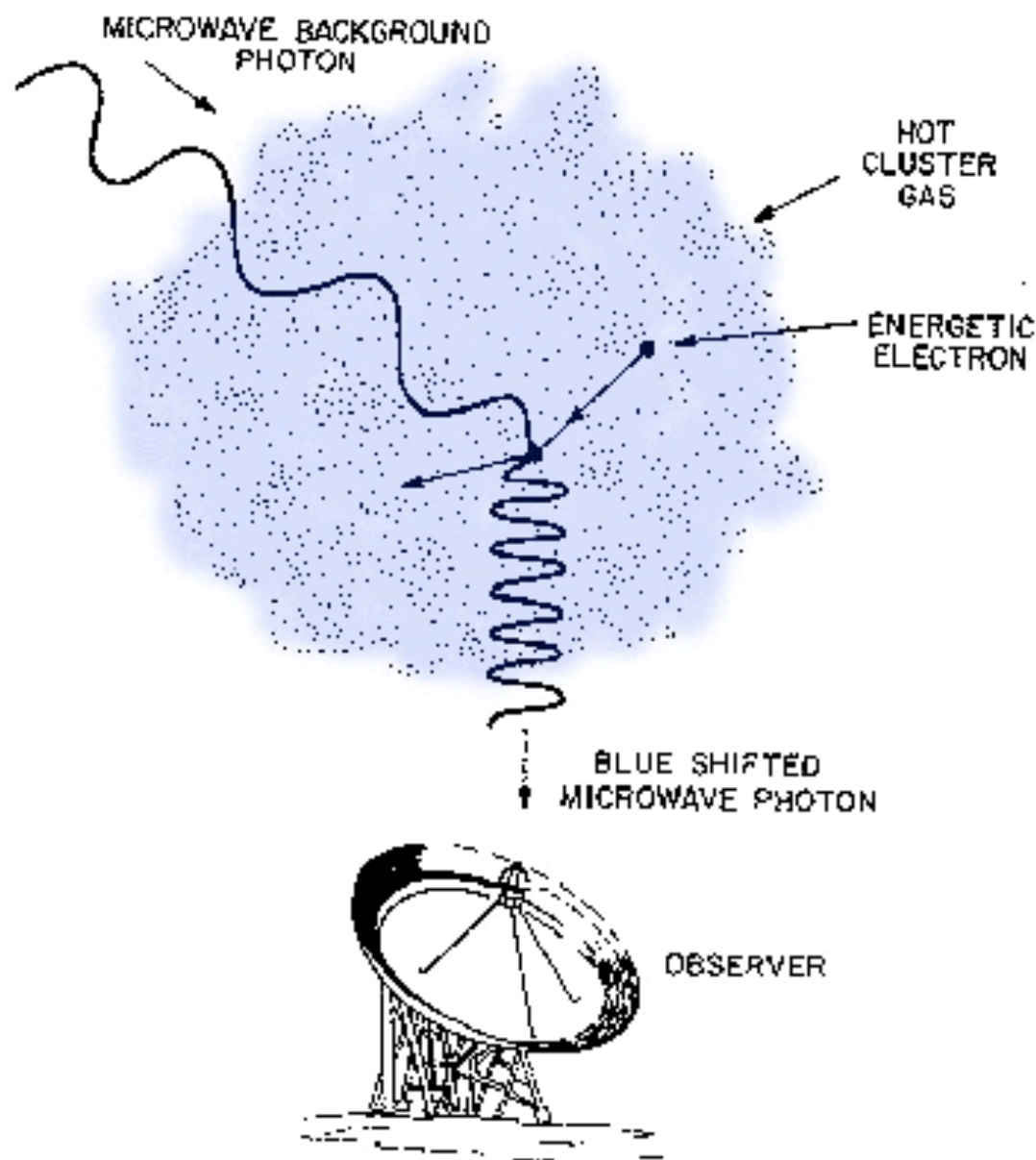
Complementarity and synergy with CMB anisotropy studies

Chluba & Sunyaev, *MNRAS*, 419, 2012
 Chluba et al., *MNRAS*, 425, 2012
 Silk & Chluba, *Science*, 2014
 Chluba, *MNRAS*, 2016



**PRISTINE
 COSMO
 CMB-Bharat**

Classical SZ effects



- SZ clusters are a great cosmological probe
- Many years of developments since its first prediction by Zeldovich & Sunyaev, 1969

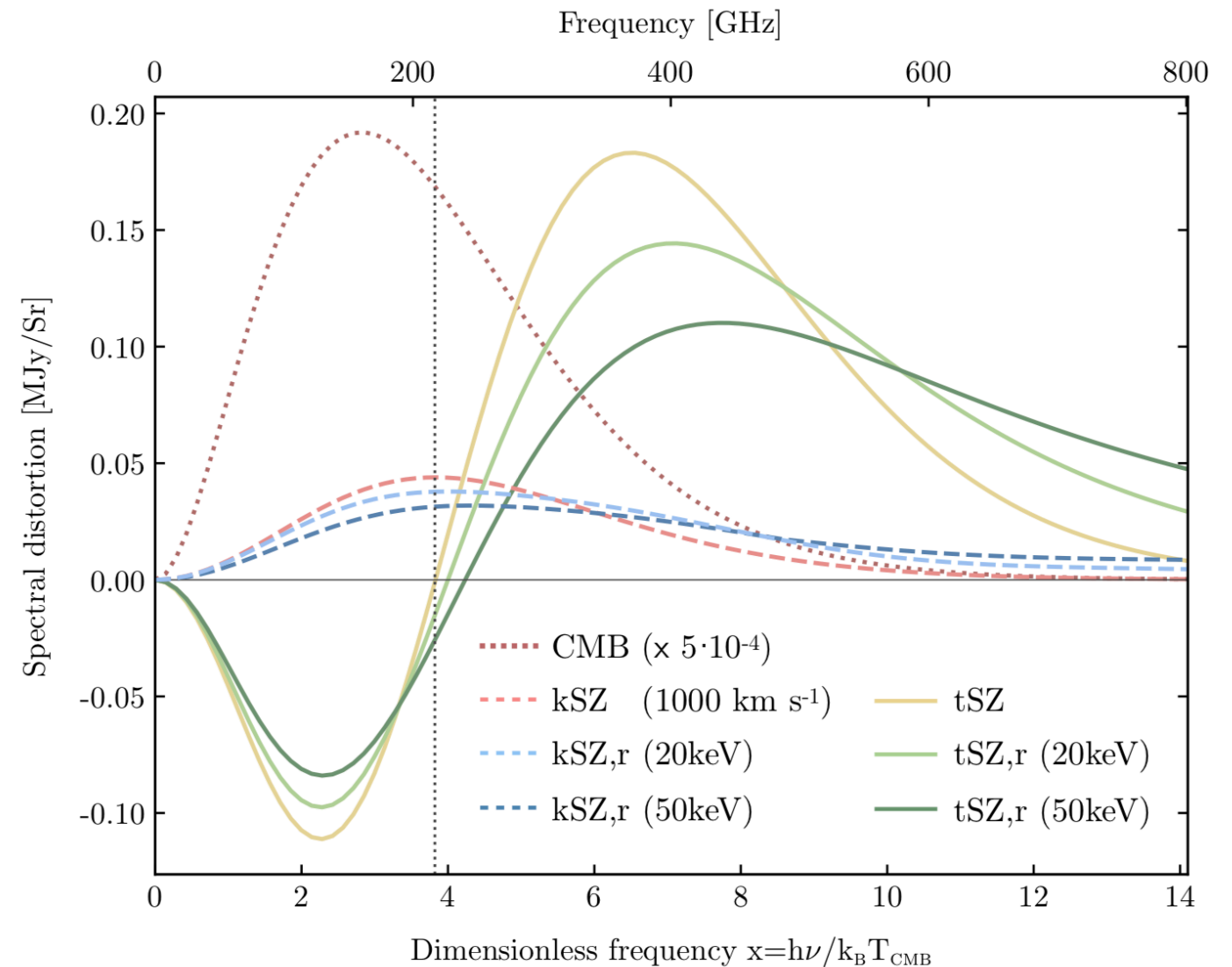
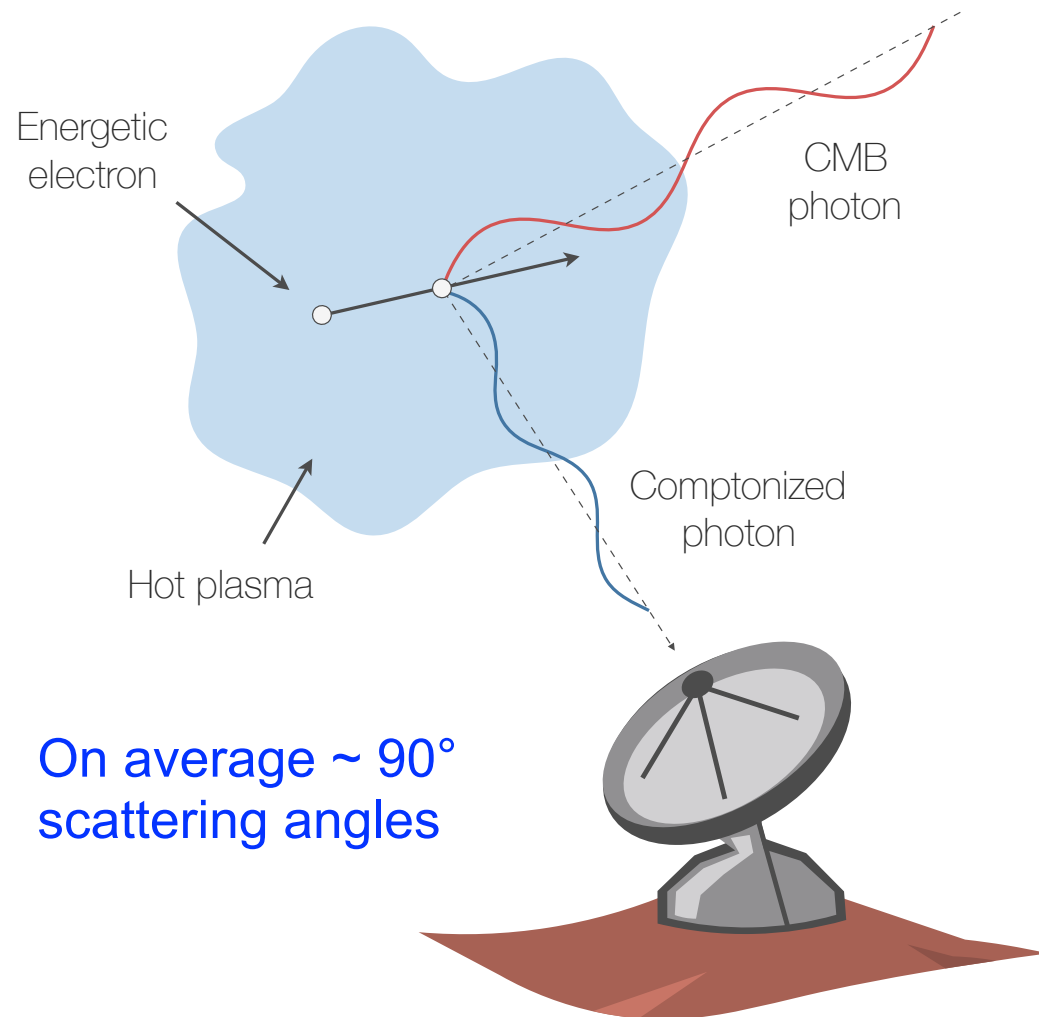
[Sunyaev & Zeldovich, 1980](#)

[Rephaeli, 1995](#)

[Birkinshaw, 1999](#)

[Carlstrom, Holder & Reese, 2002](#)

New Comprehensive Review of SZ effects



Astrophysics with the Spatially and Spectrally Resolved Sunyaev-Zeldovich Effects

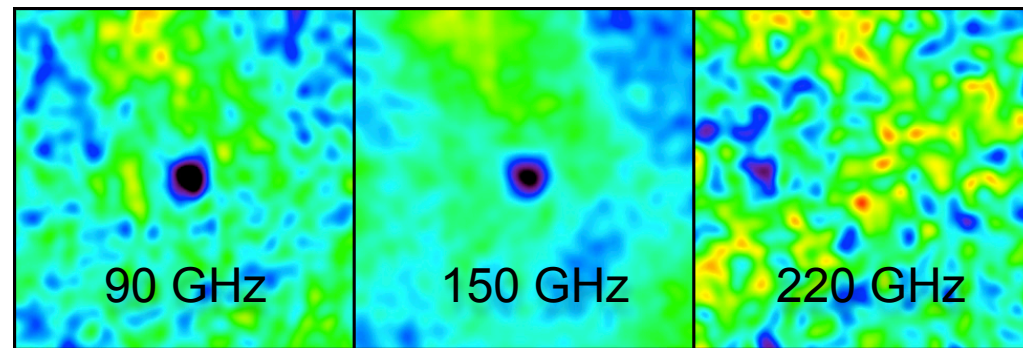
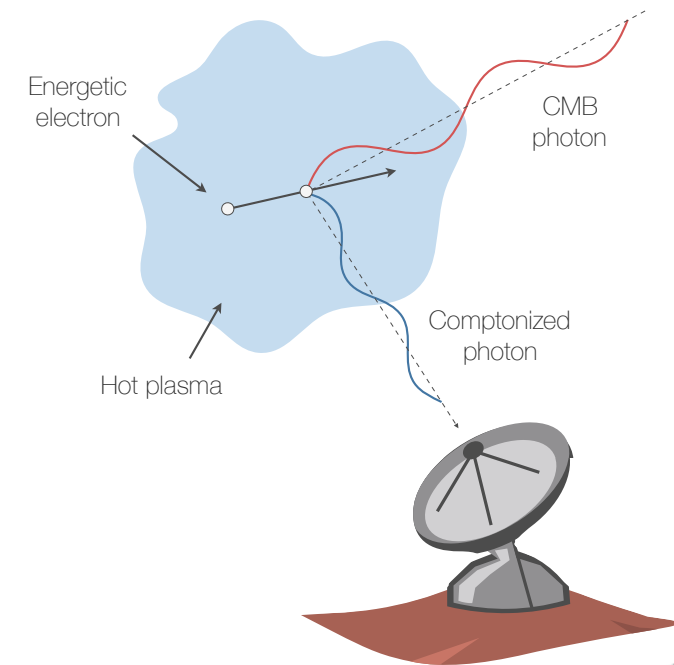
A Millimetre/Submillimetre Probe of the Warm and Hot Universe

Tony Mroczkowski • Daisuke Nagai • Kaustuv Basu • Jens Chluba • Jack Sayers • Rémi Adam • Eugene Churazov • Abigail Crites • Luca Di Mascolo • Dominique Eckert • Juan Macias-Perez • Frédéric Mayet • Laurence Perotto • Etienne Pointecouteau • Charles Romero • Florian Ruppin • Evan Scannapieco • John ZuHone

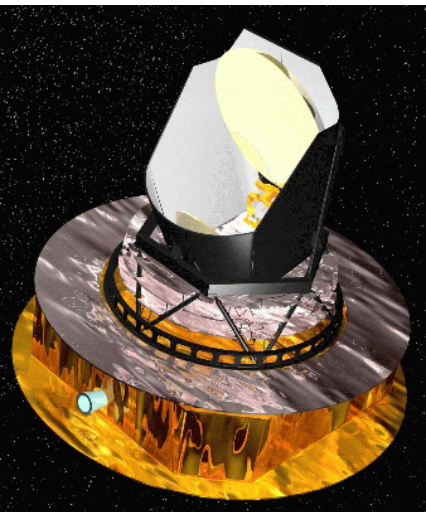
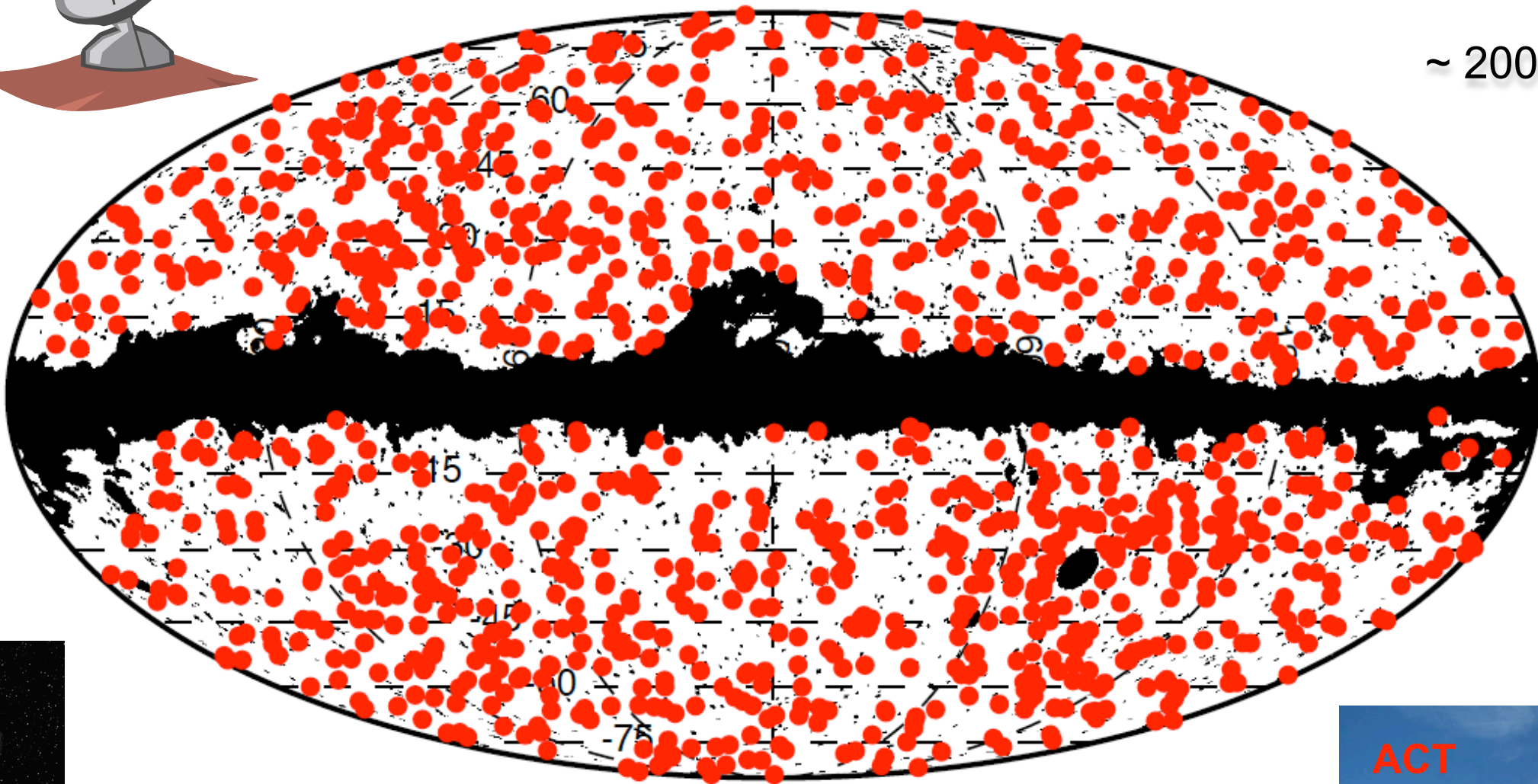
- Highlights high-resolution and high-sensitivity SZ
- Illuminates new directions
- Connection to simulations

See [arXiv:1811.02310](https://arxiv.org/abs/1811.02310) → To appear as *Space Science Reviews*

Thermal SZ effect is now routinely observed!



~ 2000 objects

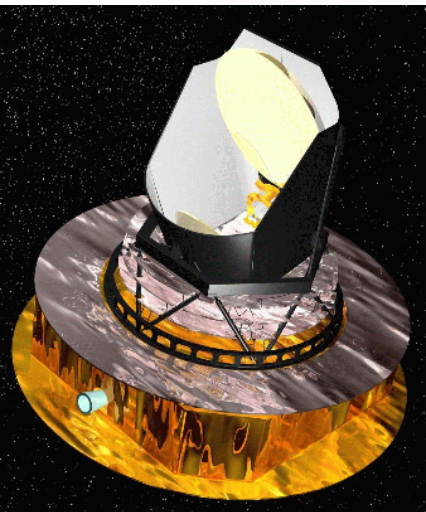
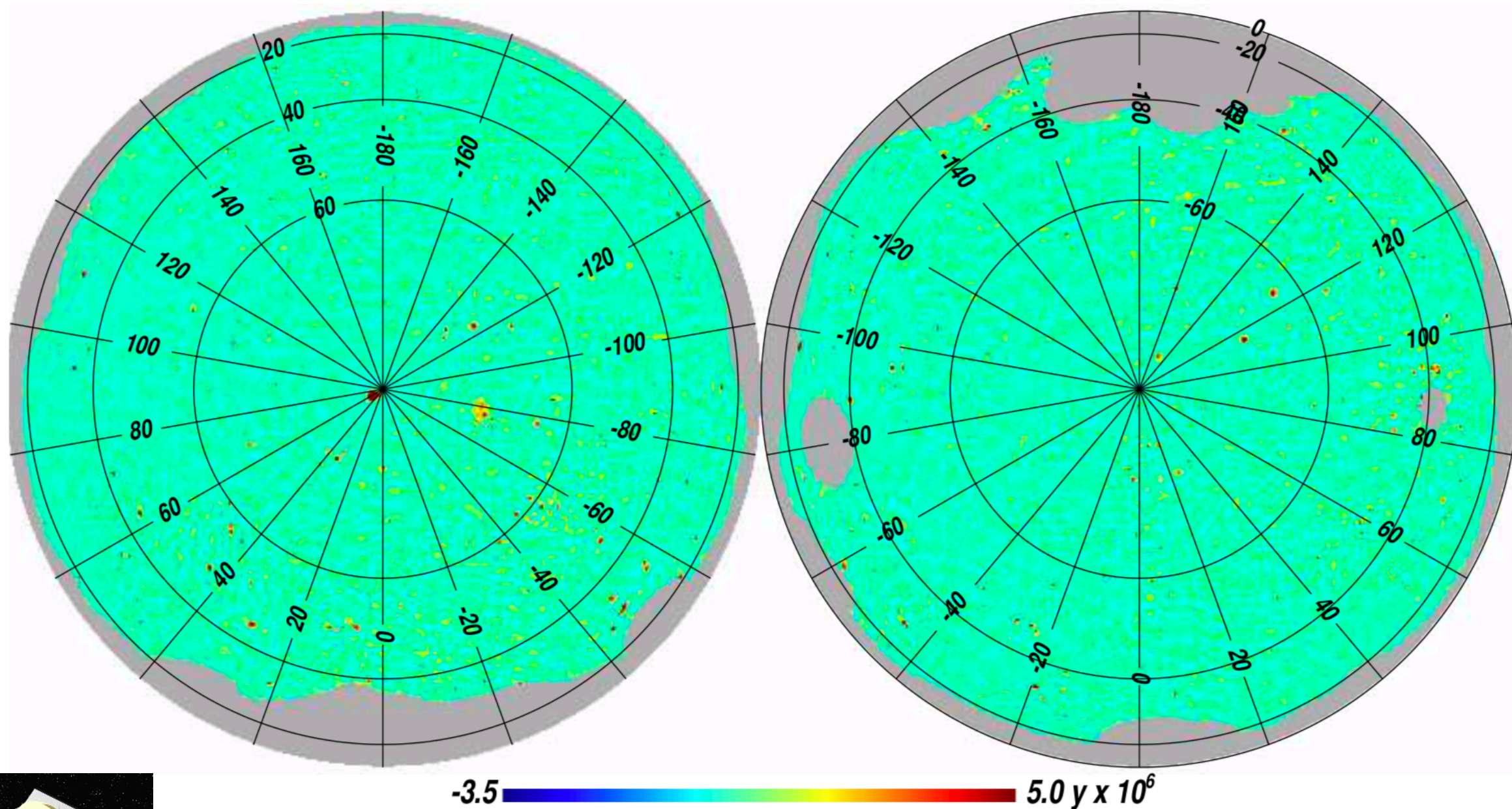


Planck Collaboration, 2013, paper XXIV
Planck Collaboration, 2015, paper XXIV



All-sky Compton y -map from Planck

NILC tSZ map

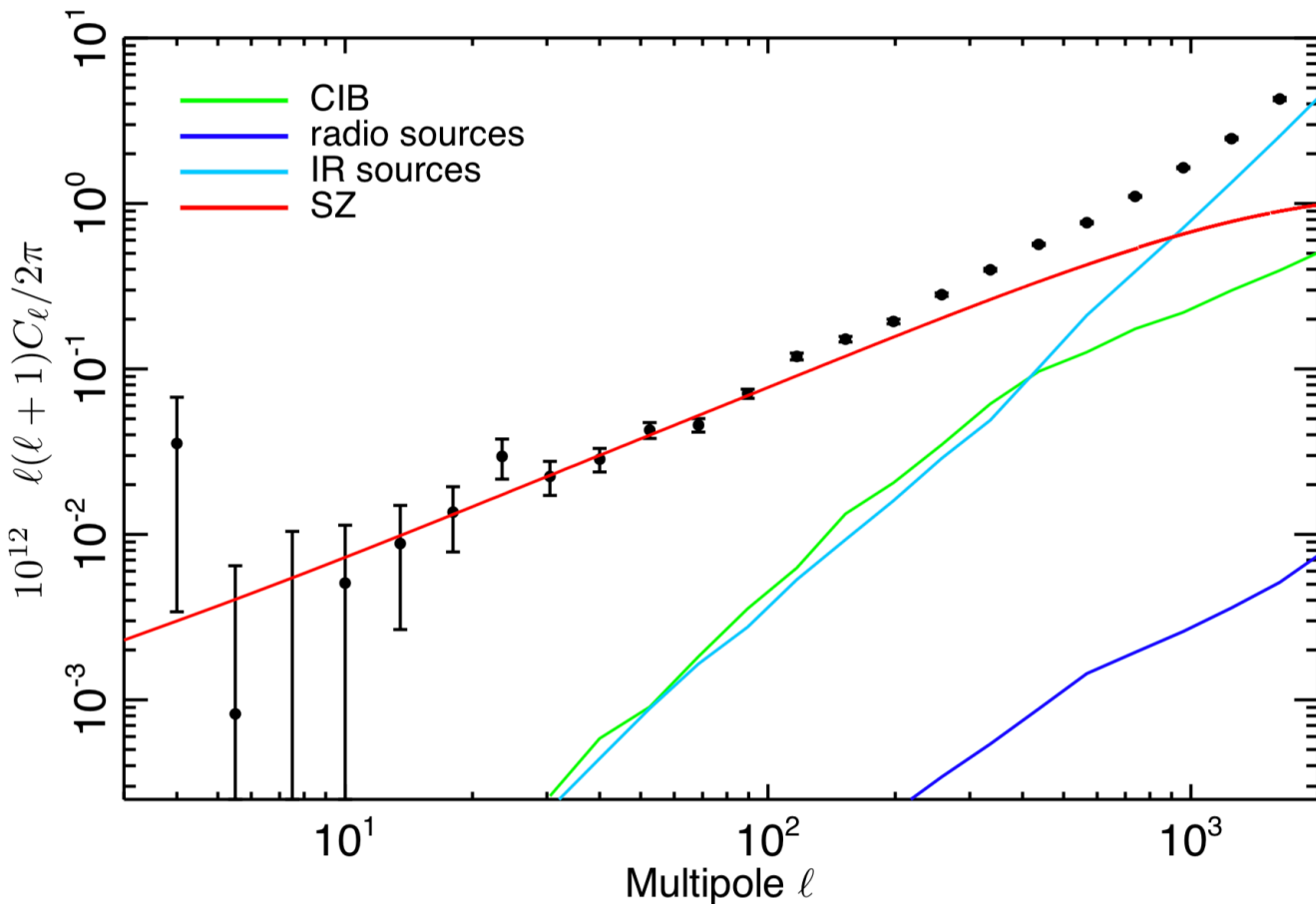


Planck Collaboration, 2013, paper XXI
Planck Collaboration, 2015, paper XXII

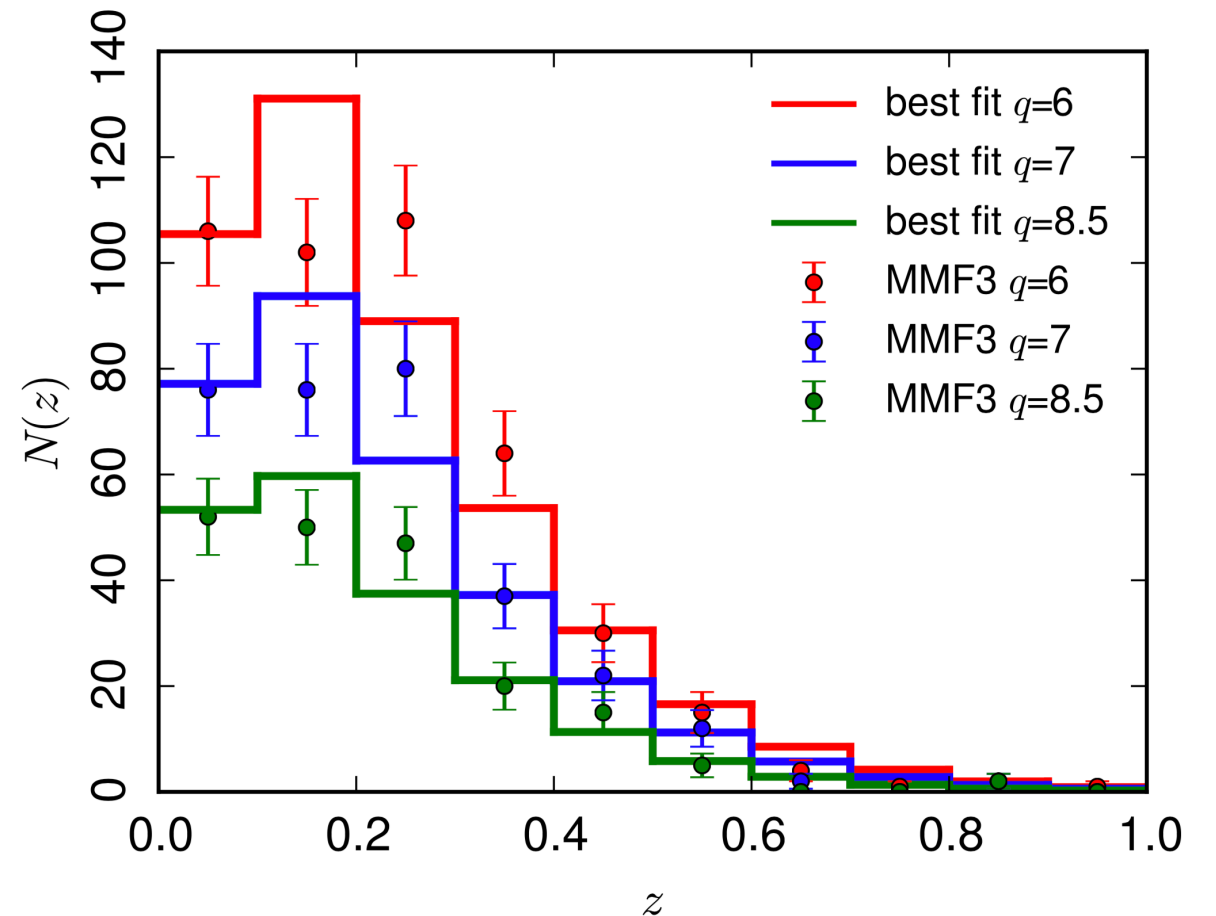
Map was produced by
Mathieu Remazeilles

Planck SZ analysis

Power spectrum

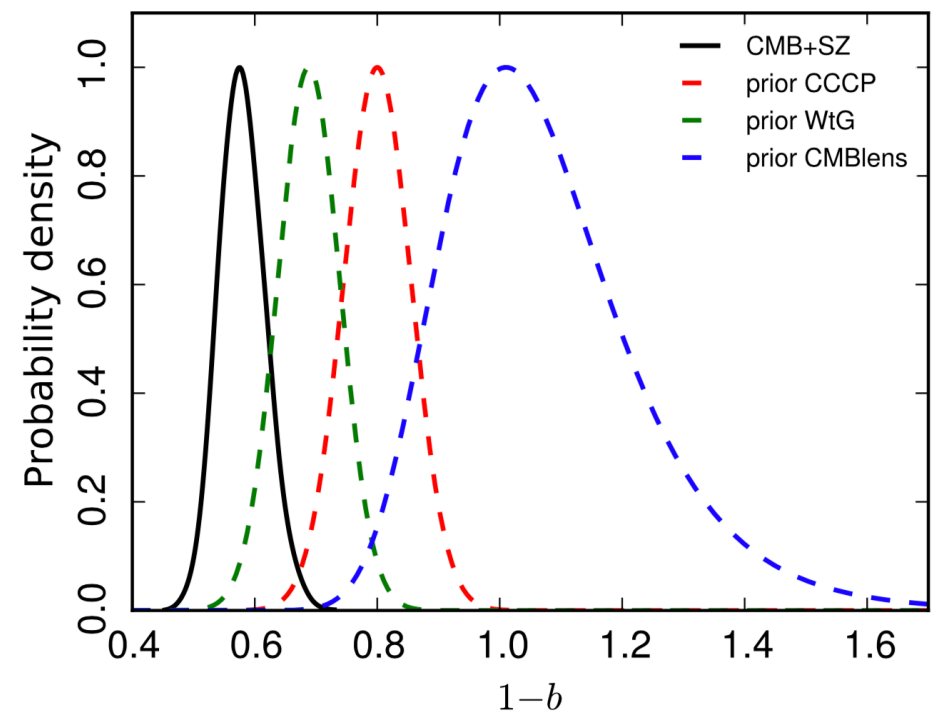
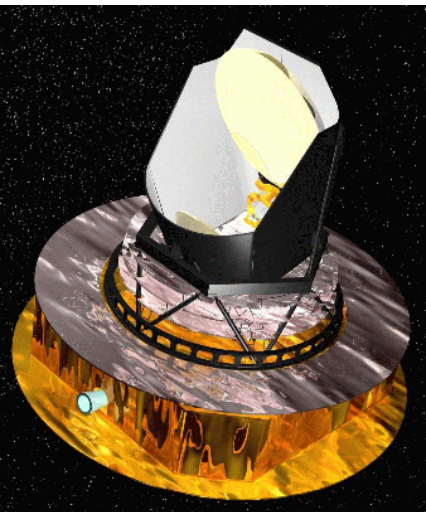


Number counts



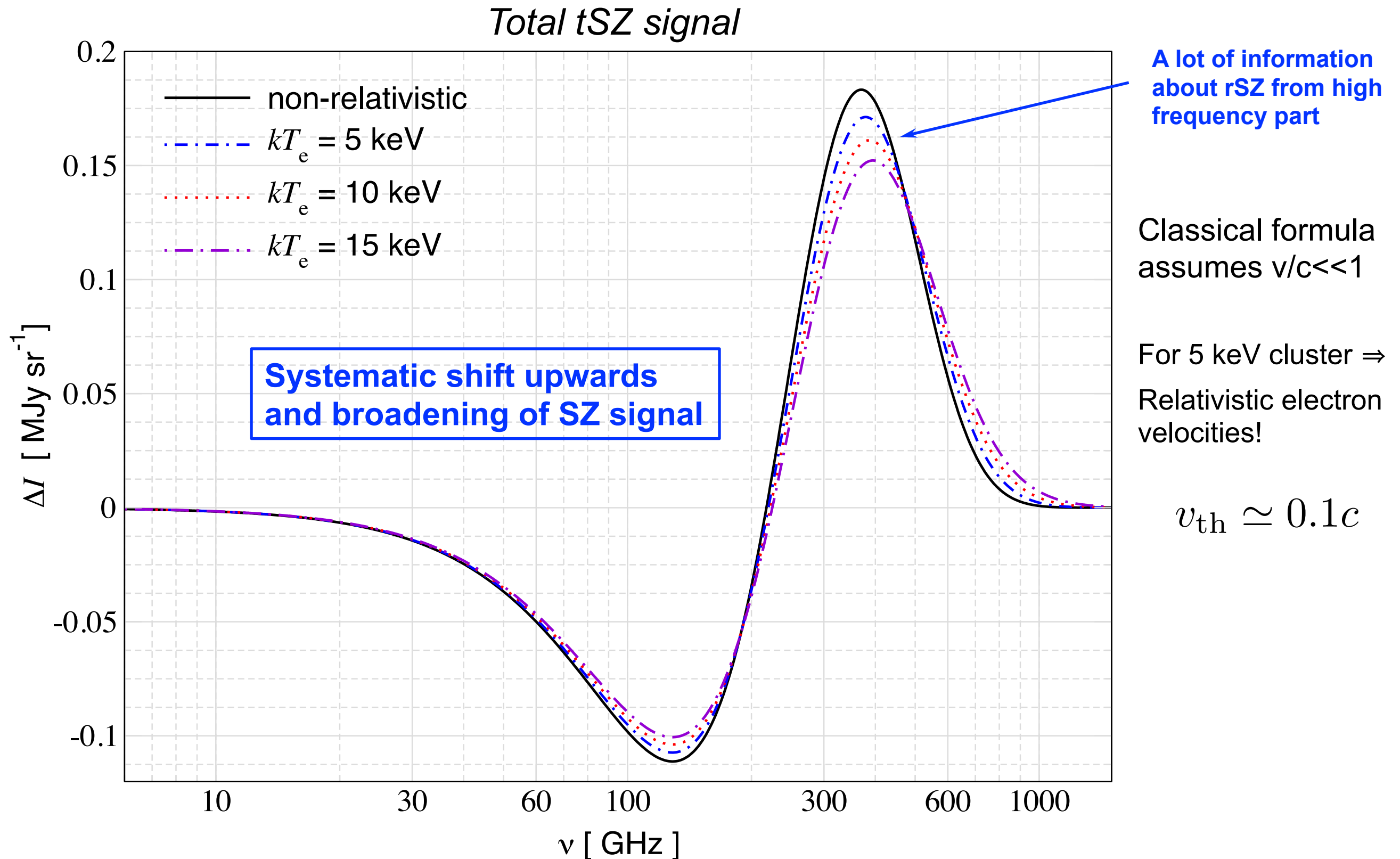
- SZ results on σ_8 in tension with CMB only result
- Hydrostatic mass bias
- Dependence on combination of data and modeling details

Planck Collaboration, 2015, paper XXIV
Planck Collaboration, 2015, paper XXII



What is the role of relativistic SZ (rSZ) in this?

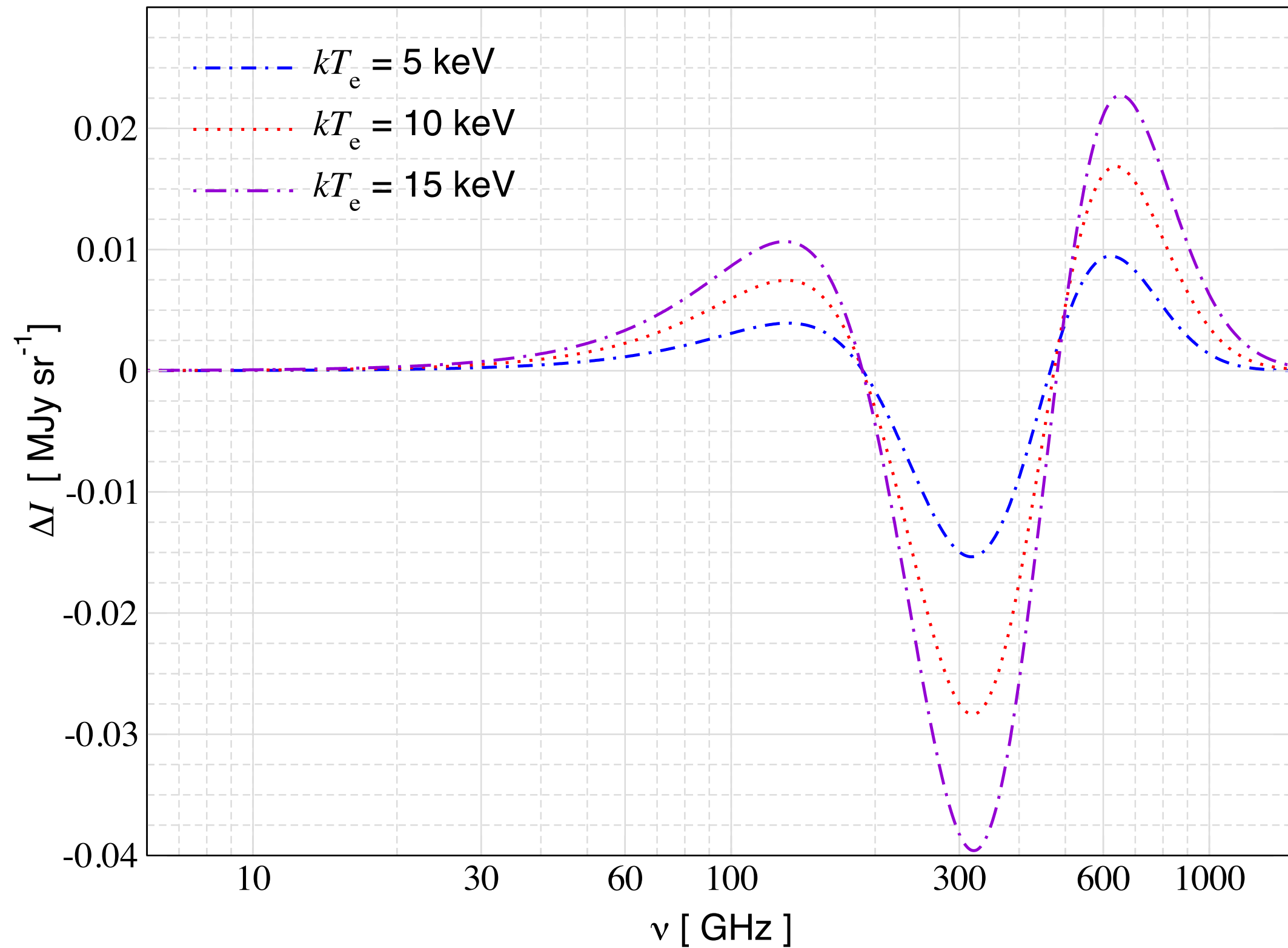
Effect of relativistic temperature corrections



$$y = 10^{-4}$$

High frequencies are crucial for rSZ!

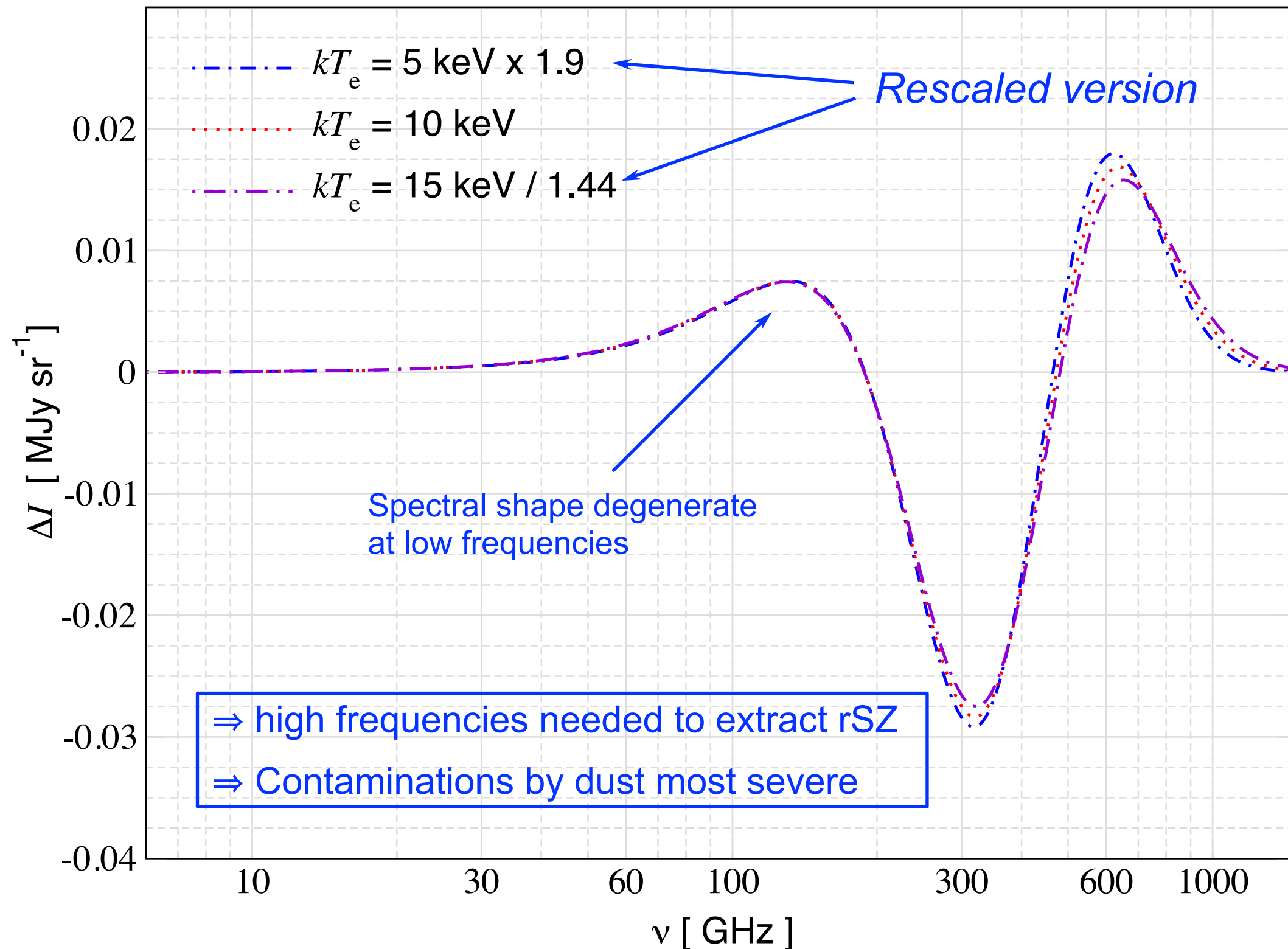
Relativistic correction signal only



$y = 10^{-4}$

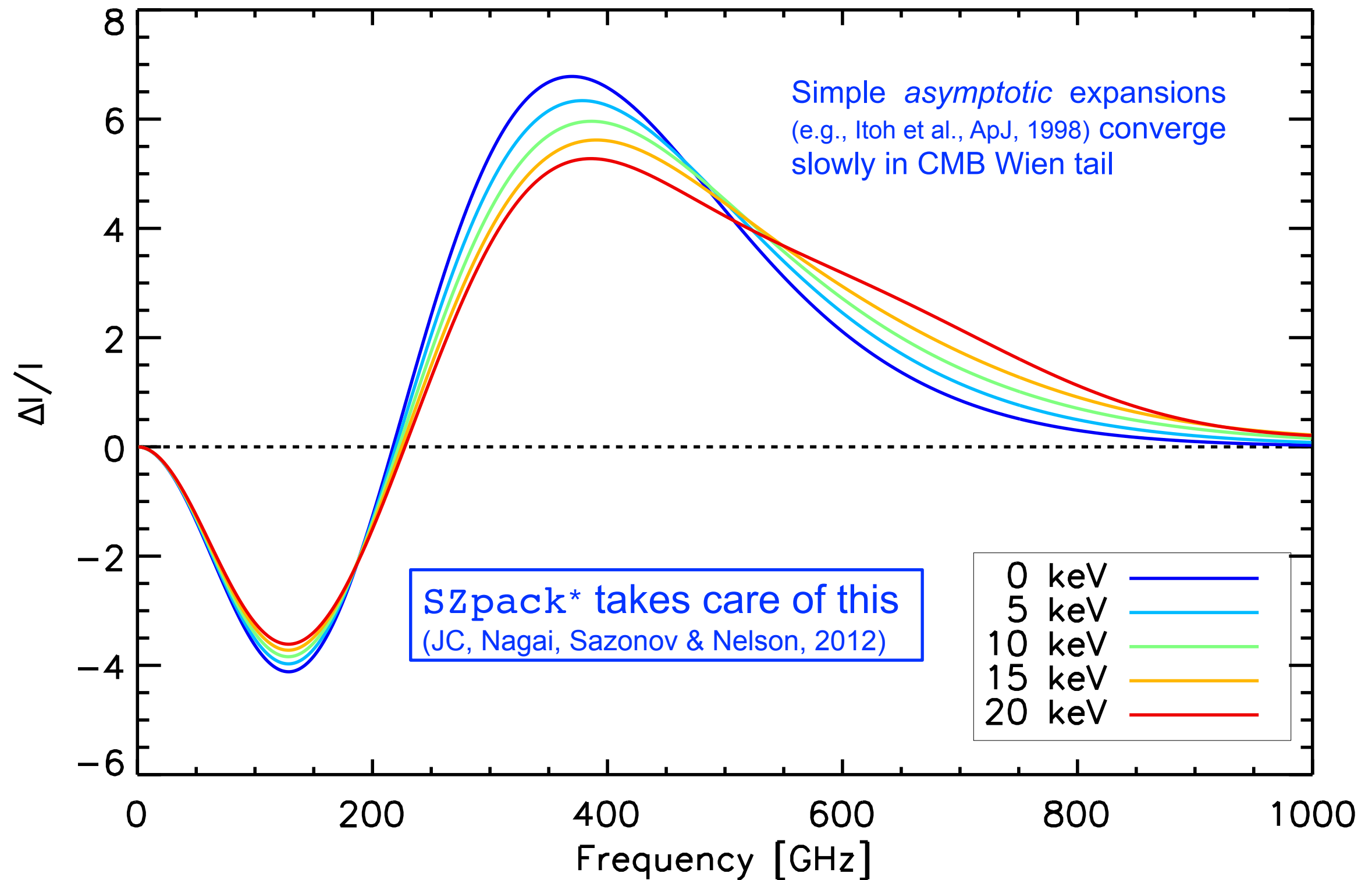
High frequencies are crucial for rSZ!

Relativistic correction signal only

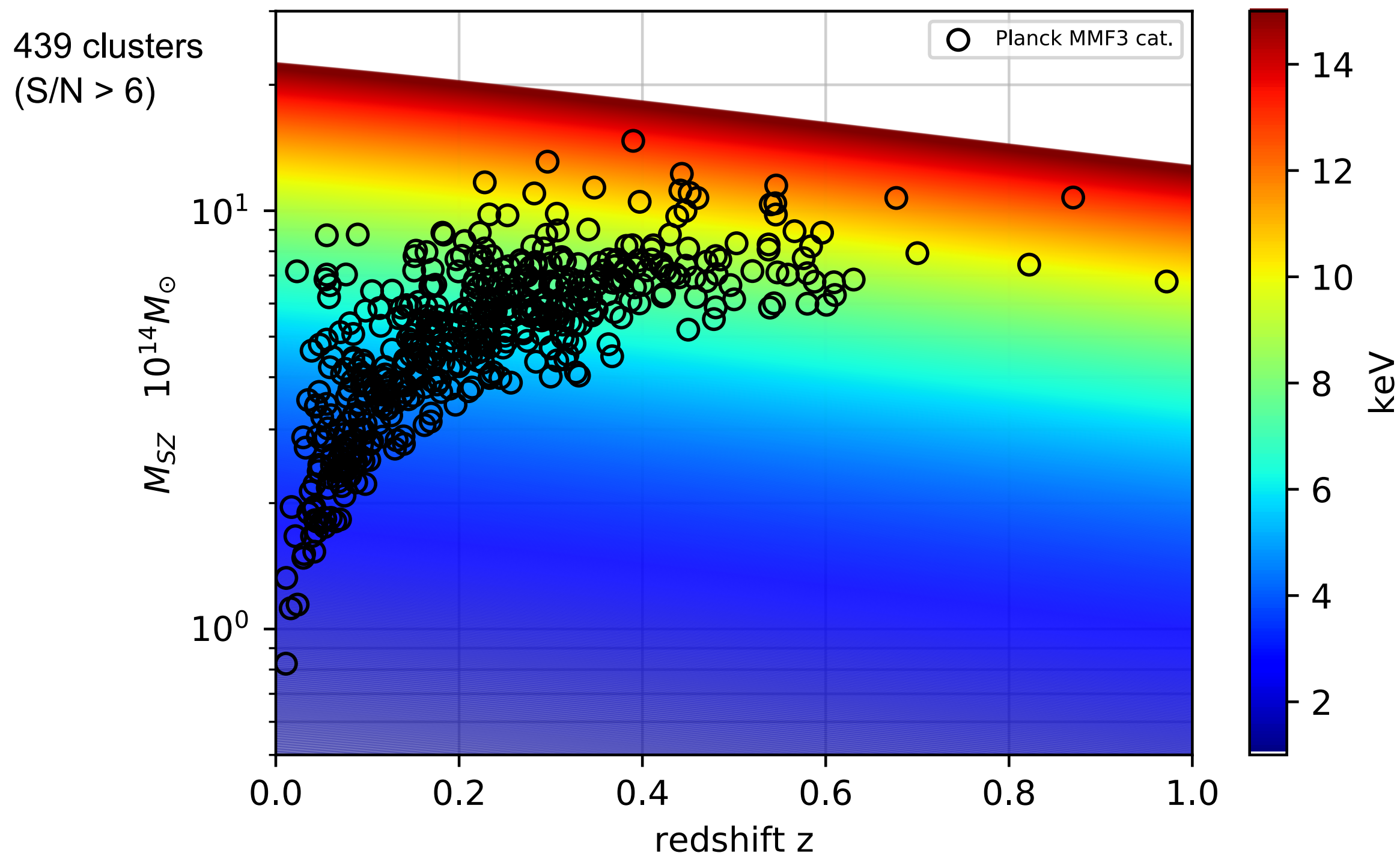


$y = 10^{-4}$

High-frequency spectrum has to be computed carefully...



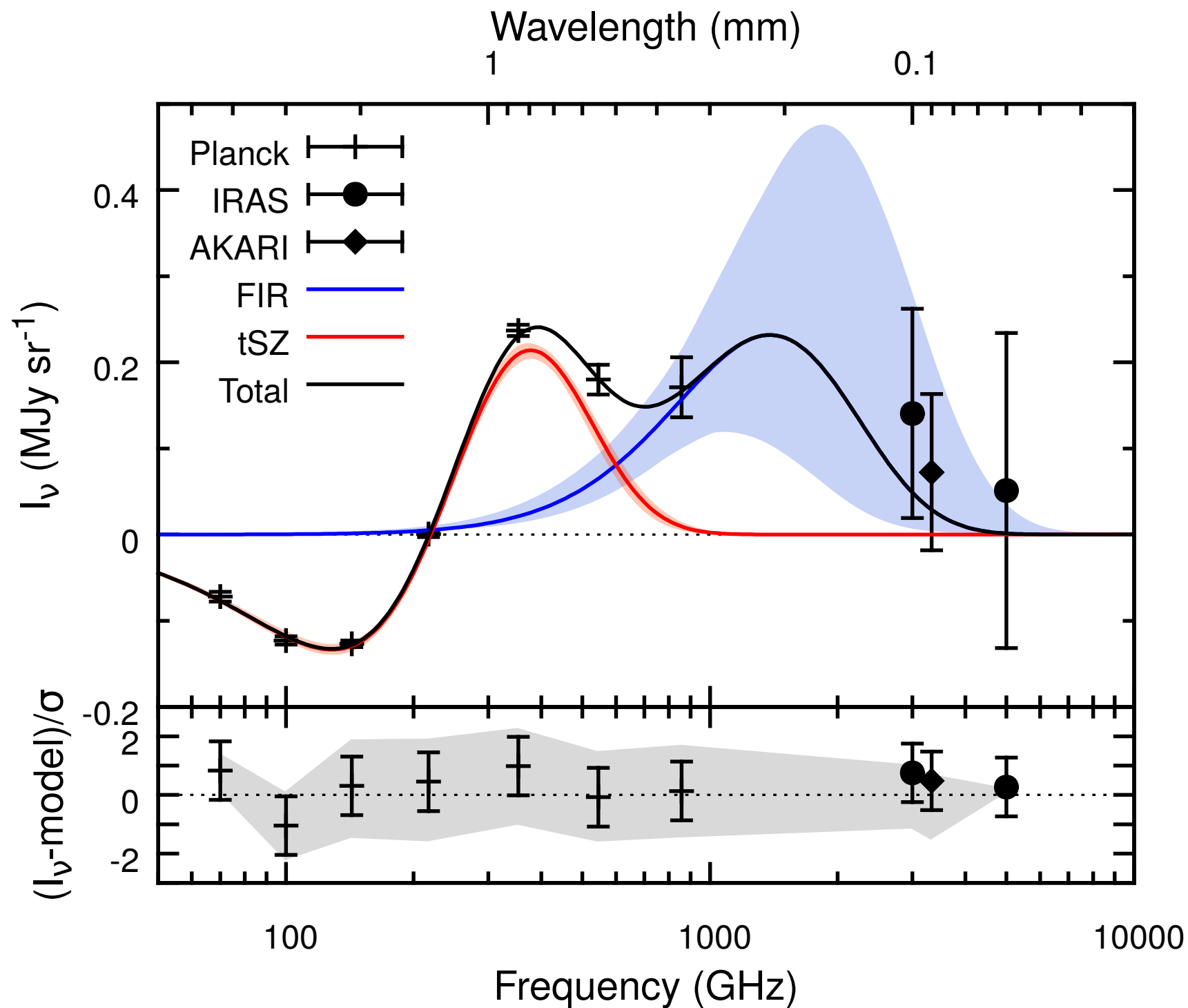
Clusters seen by Planck are pretty hot!



Standard (X-ray)
temperature mass-relation
(e.g., Arnaud et al., 2005, Erler et al. 2018)

$$kT_e \simeq 5 \text{ keV} \left[\frac{E(z) M_{500}}{3 \times 10^{14} h^{-1} M_{\odot}} \right]^{2/3}$$

Stacked Planck tSZ signal + foregrounds



- Matched filter approach
- Combination of data
- 772 clusters (PSZ2)

$$y_0 = 1.24^{+0.04}_{-0.04} \times 10^{-4}$$

$$k_B T_{\text{SZ}} = 4.36^{+2.13}_{-1.95} \text{ keV}$$

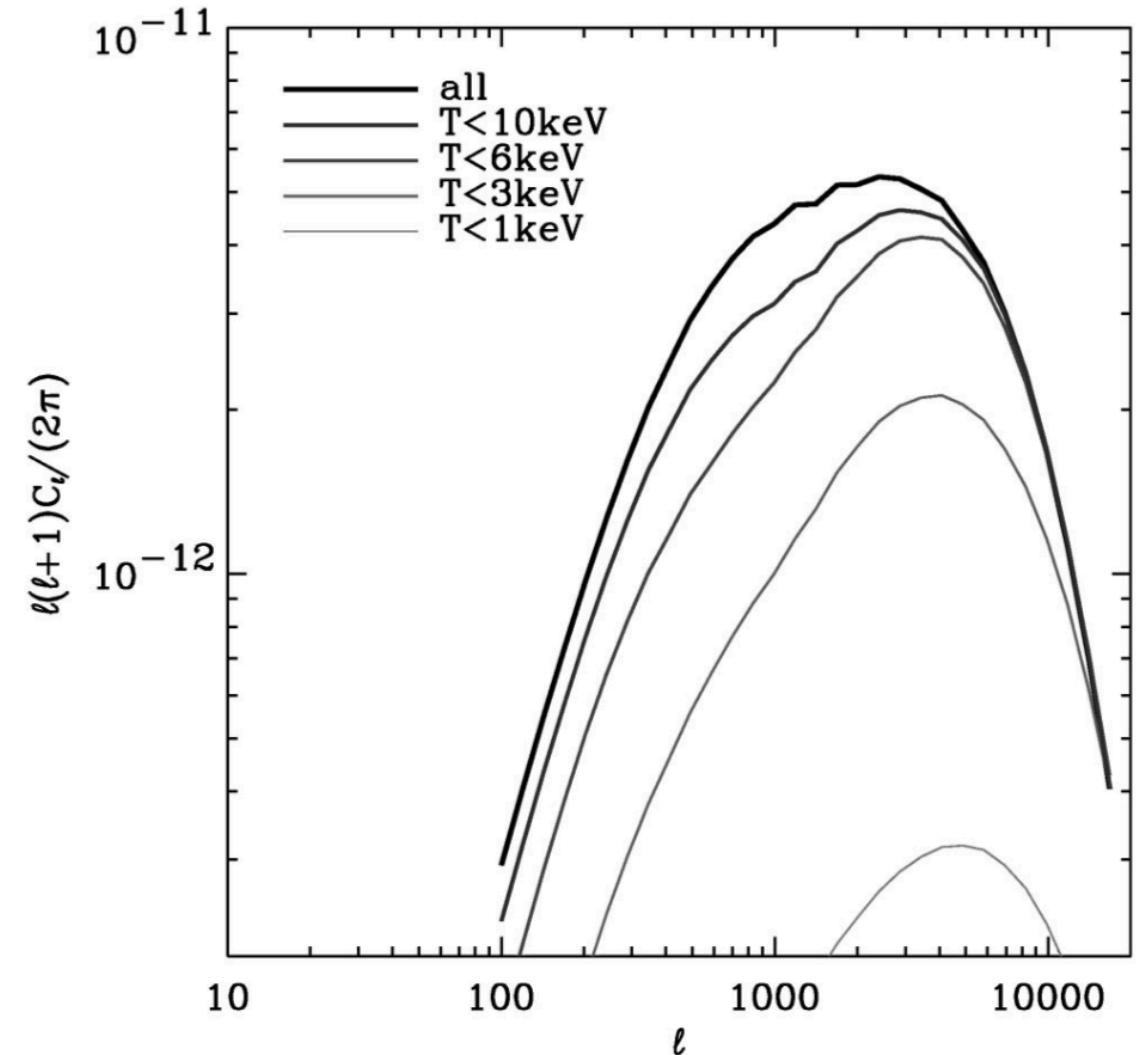
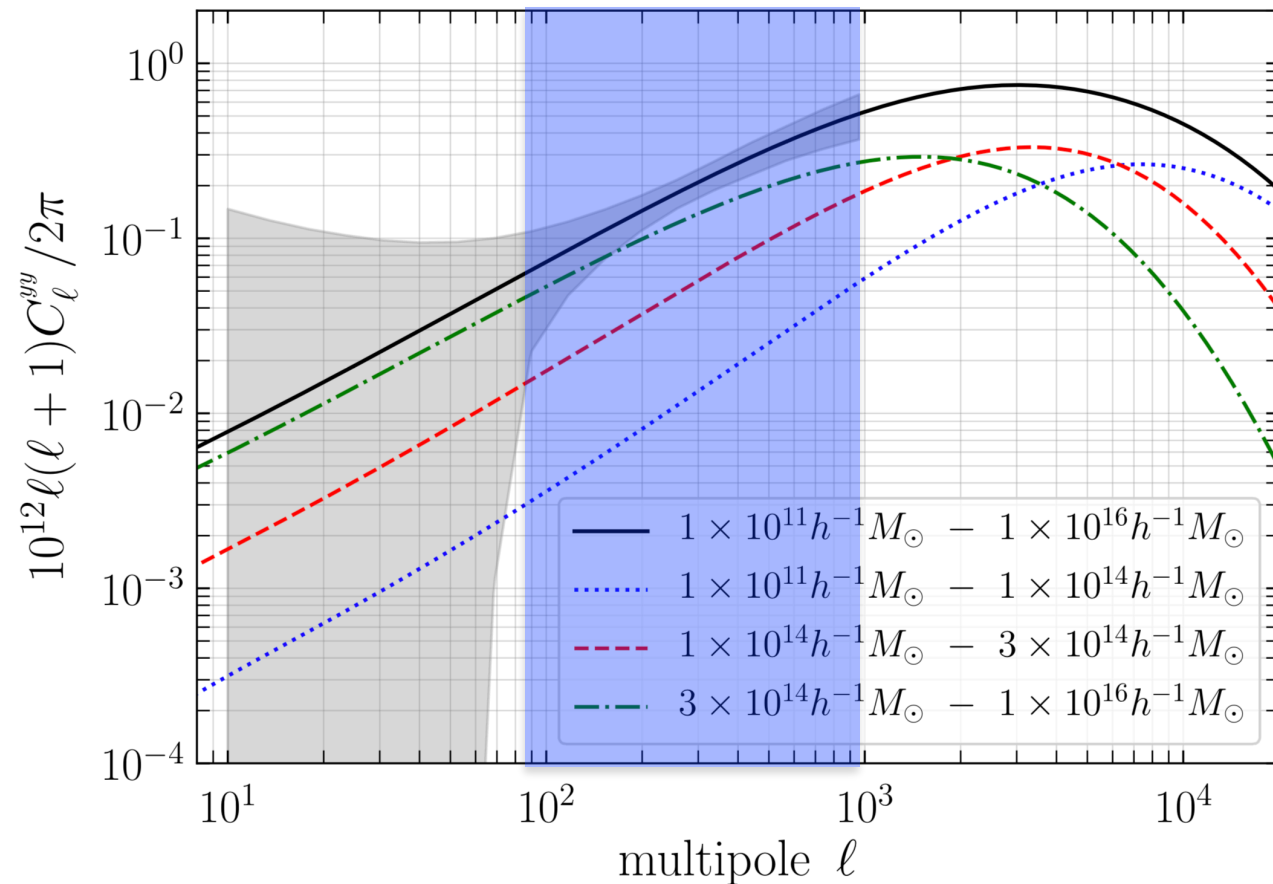
- rSZ at $\sim 2.2 \sigma$ level
- In tension with Hurier, A&A, 2016 (claimed $\sim 5 \sigma$ detection)
- 100 hottest clusters:

$$k_B T_{\text{SZ}} = 5.96^{+3.78}_{-2.93} \text{ keV}$$

\Rightarrow typical y-weighted temperature of ~ 4 -7 keV quite reasonable

Theoretical SZ power spectrum computations

Computation with *CLASS-SZ* (Bolliet et al., 2017)



Refregier et al., 2000

From Komatsu & Seljak, 2002:

$$C_l = \int_0^{z_{\max}} dz \frac{dV}{dz} \int_{M_{\min}}^{M_{\max}} dM \underbrace{\frac{dn(M, z)}{dM}}_{\text{halo mass function}} \underbrace{|\tilde{y}_l(M, z)|^2}_{\text{cluster pressure profile}}$$

→ temperature of systems contributing to the multipole range relevant to *Planck*'s C_l analysis seems > 5 keV

How is the y -map obtained?

SZ Compton- γ signal reconstruction: ILC

$$\underbrace{d(\nu, \vec{\theta})}_{\text{Planck frequency data}} = \underbrace{Y_0(\nu)}_{\text{signal of interest}} \underbrace{y(\vec{\theta})}_{\text{signal of interest}} + \underbrace{N(\nu, \vec{\theta})}_{\text{foregrounds + noise}}$$

- ILC = weighted linear combination of frequency maps:

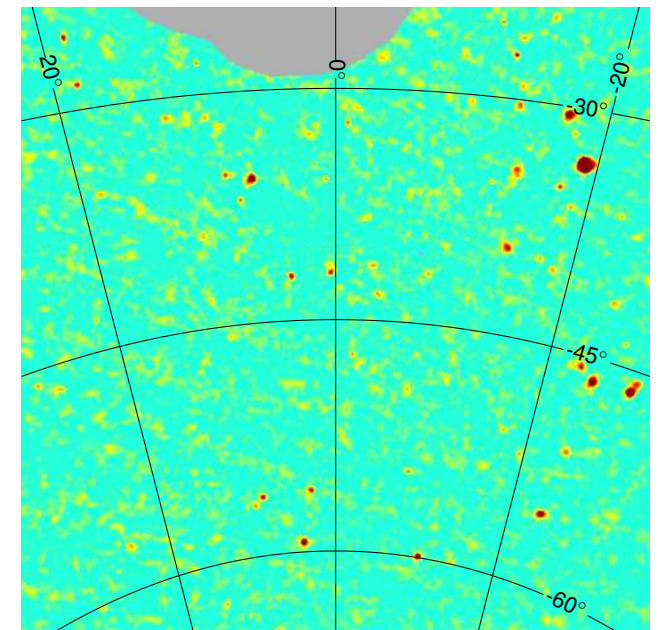
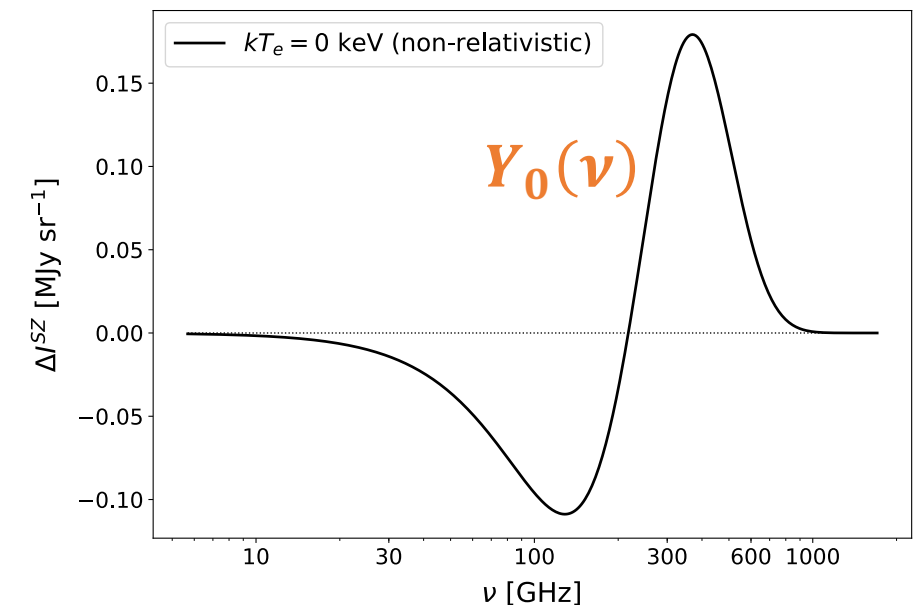
$$\hat{y}(\vec{\theta}) = \sum_{\nu} w(\nu) d(\nu, \vec{\theta})$$

$$\text{such that } \begin{cases} \langle \hat{y}^2 \rangle = \mathbf{w}^t \langle d d^t \rangle \mathbf{w} \text{ minimum} & (1) \\ \sum_{\nu} w(\nu) Y_0(\nu) = 1 & (2) \end{cases}$$

$$\text{ILC weights : } \mathbf{w}^t = \frac{Y_0^t C^{-1}}{Y_0^t C^{-1} Y_0} \quad (C \equiv \langle d d^t \rangle)$$

$$\Rightarrow \hat{y}(\vec{\theta}) = \underbrace{y(\vec{\theta})}_{\substack{\text{recovered} \\ \text{signal}}} + \underbrace{w^t N}_{\substack{\text{minimized} \\ \text{residuals} \\ \text{by (1)}}}$$

(2) by (1)



Planck 2015 results XXII

Miscalibrated Compton- γ signal reconstruction

$$\underbrace{d(\nu, \vec{\theta})}_{\text{Planck frequency data}} = \underbrace{Y(\nu, T_e)}_{\text{signal of interest}} \underbrace{y(\vec{\theta})}_{\text{signal of interest}} + \underbrace{N(\nu, \vec{\theta})}_{\text{foregrounds + noise}}$$

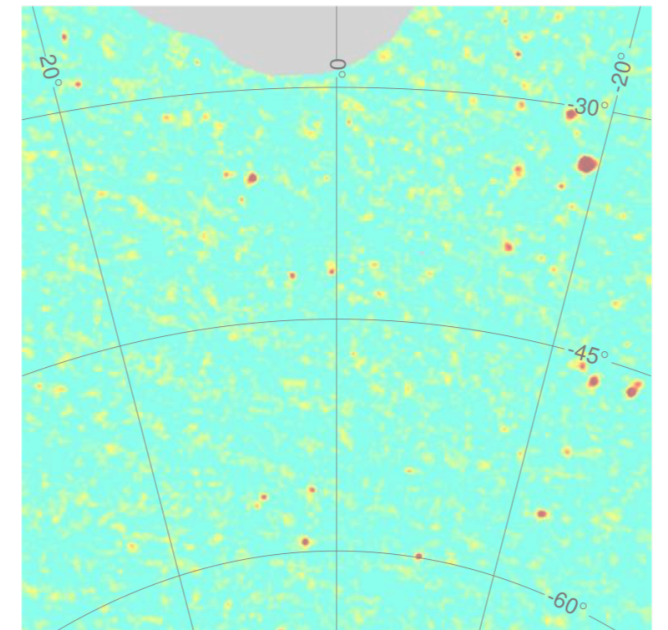
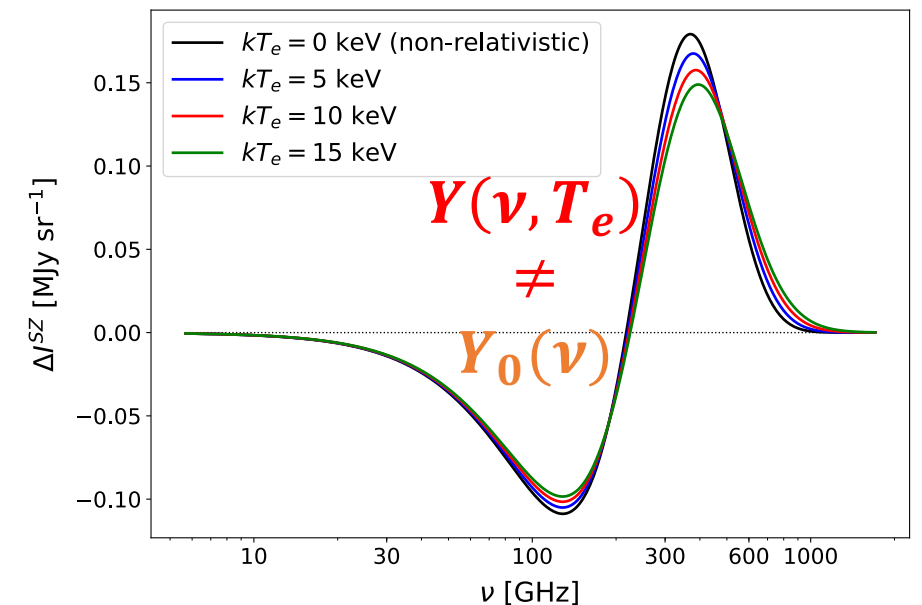
- ILC = weighted linear combination of frequency maps:

$$\hat{y}(\vec{\theta}) = \sum_{\nu} w(\nu) d(\nu, \vec{\theta})$$

$$\text{such that } \begin{cases} \langle \hat{y}^2 \rangle = \mathbf{w}^t \langle d d^t \rangle \mathbf{w} \text{ minimum} & (1) \\ \sum_{\nu} w(\nu) Y_0(\nu) = 1 & (2) \end{cases}$$

$$\text{ILC weights : } \mathbf{w}^t = \frac{Y_0^t C^{-1}}{Y_0^t C^{-1} Y_0} \quad (C \equiv \langle d d^t \rangle)$$

$$\Rightarrow \hat{y}(\vec{\theta}) = \underbrace{\frac{Y_0^t C^{-1} Y(T_e)}{Y_0^t C^{-1} Y_0}}_{\text{Bias} < 1} y(\vec{\theta}) + \mathbf{w}^t N$$

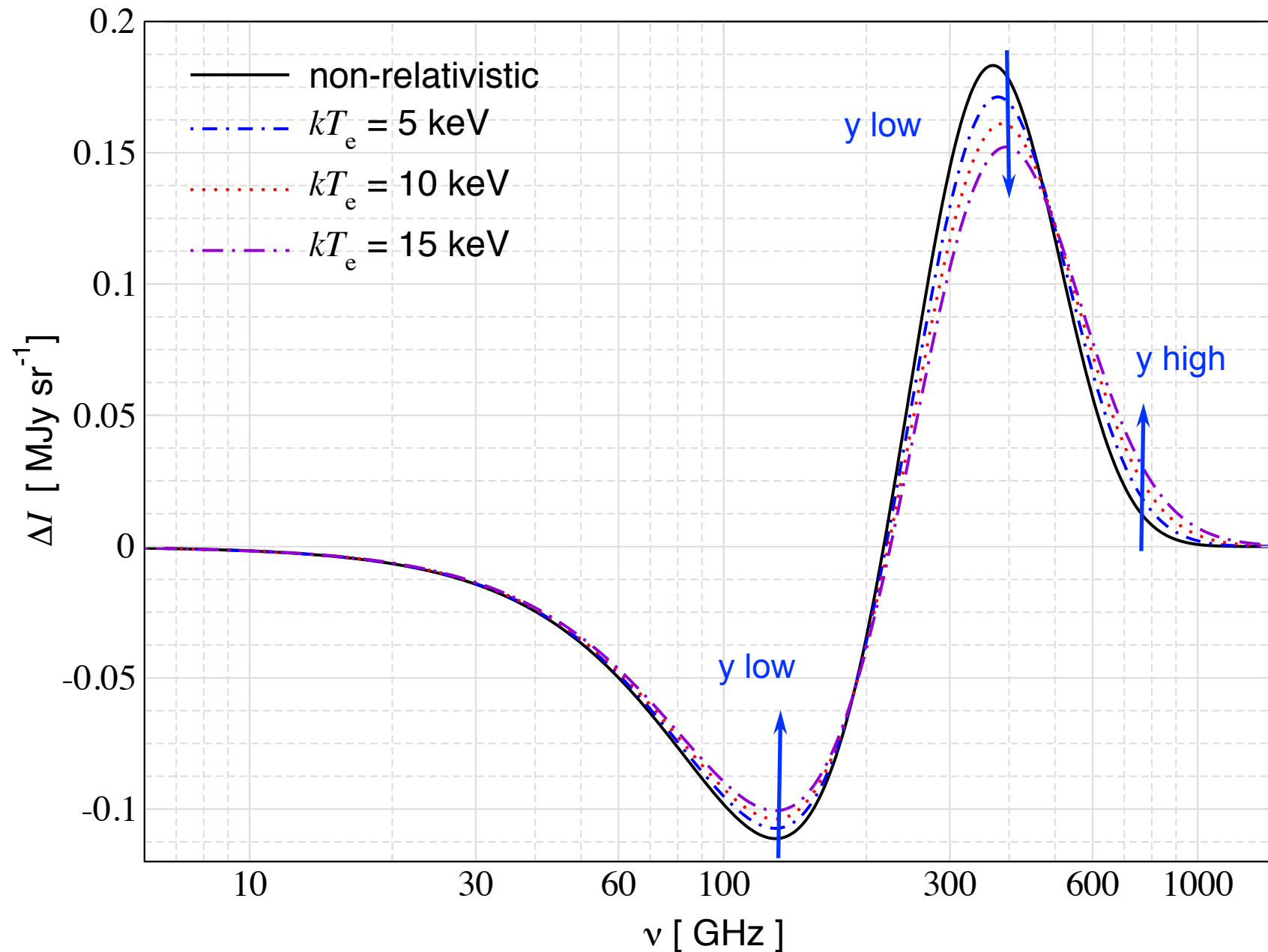


Planck 2015 results XXII

Underestimation of Compton- γ signal !

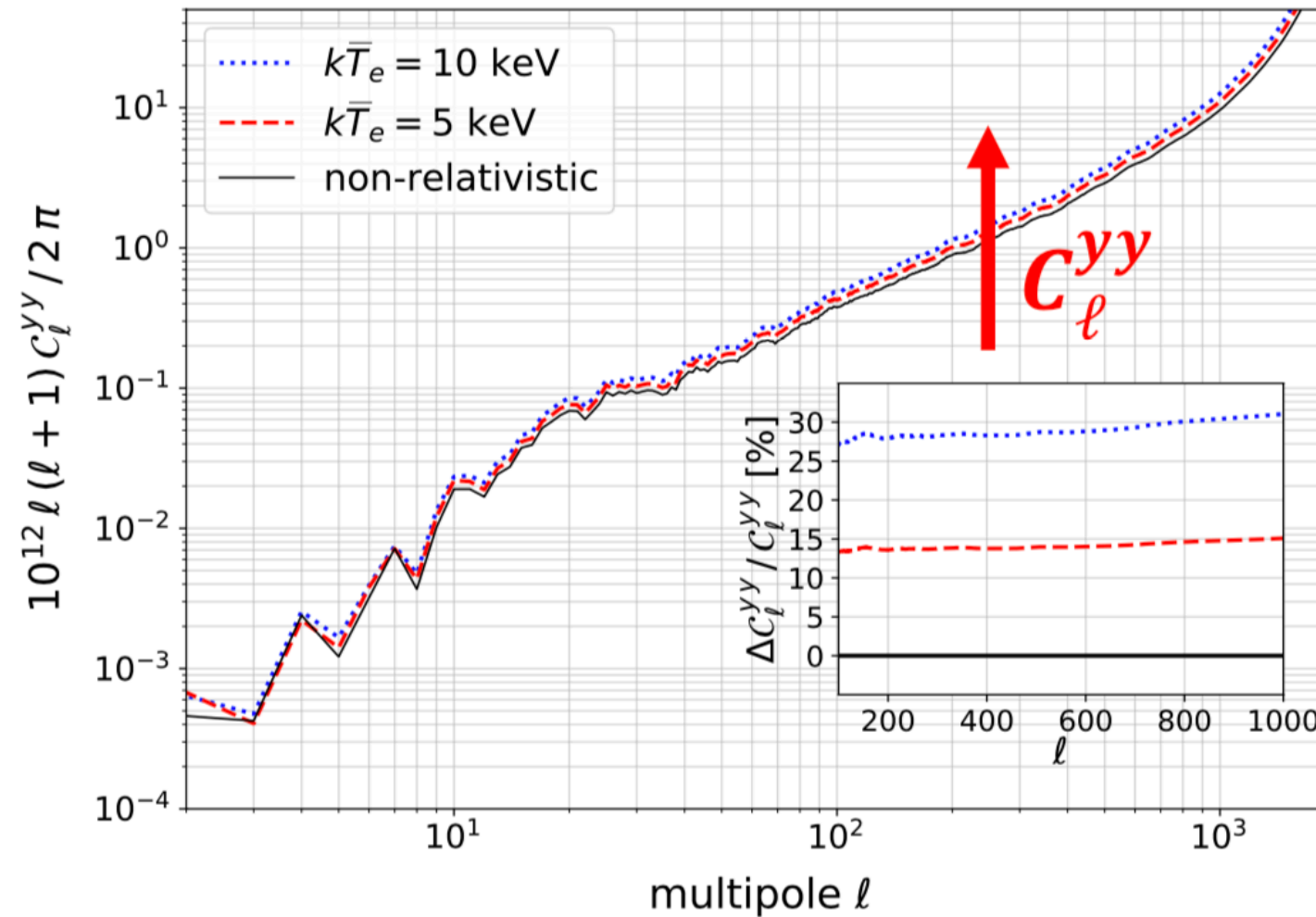
What is the net effect on the y-parameter?

Total tSZ signal



- Obtained y -parameter is underestimated by $\sim 7\%$ for $kT_e \sim 5$ keV for *Planck*
- This is consistent with 353 GHz channel driving the effect for *Planck* data
- Also consistent with Erler et al. 2018 ILC analysis
- Total effect generally depends on frequency configuration and ability to subtract foregrounds (Rotti et al., in prep.)

Updating the *Planck* y -map power spectrum



Planck C_ℓ^{yy} increases with average cluster temperature \bar{T}_e

$$C_\ell^{yy} \propto \sigma_8^{8.1} \Rightarrow \boxed{\frac{\Delta \sigma_8}{\sigma_8} \simeq 0.019 \left(\frac{k\bar{T}_e}{5 \text{ keV}} \right)} \quad \simeq 1\sigma \text{ increase for } \bar{T}_e \simeq 5 \text{ keV}!$$

Remazeilles, Bolliet, Rotti, Chluba (2018)

Which effective electron temperature should be used?

- Single cluster / stacking \rightarrow y -weighted temperature is relevant

$$kT_e^y = \frac{\langle kT_e y \rangle}{\langle y \rangle} = \frac{\int kT_e^2 N_e dl}{\int T_e N_e dl}$$

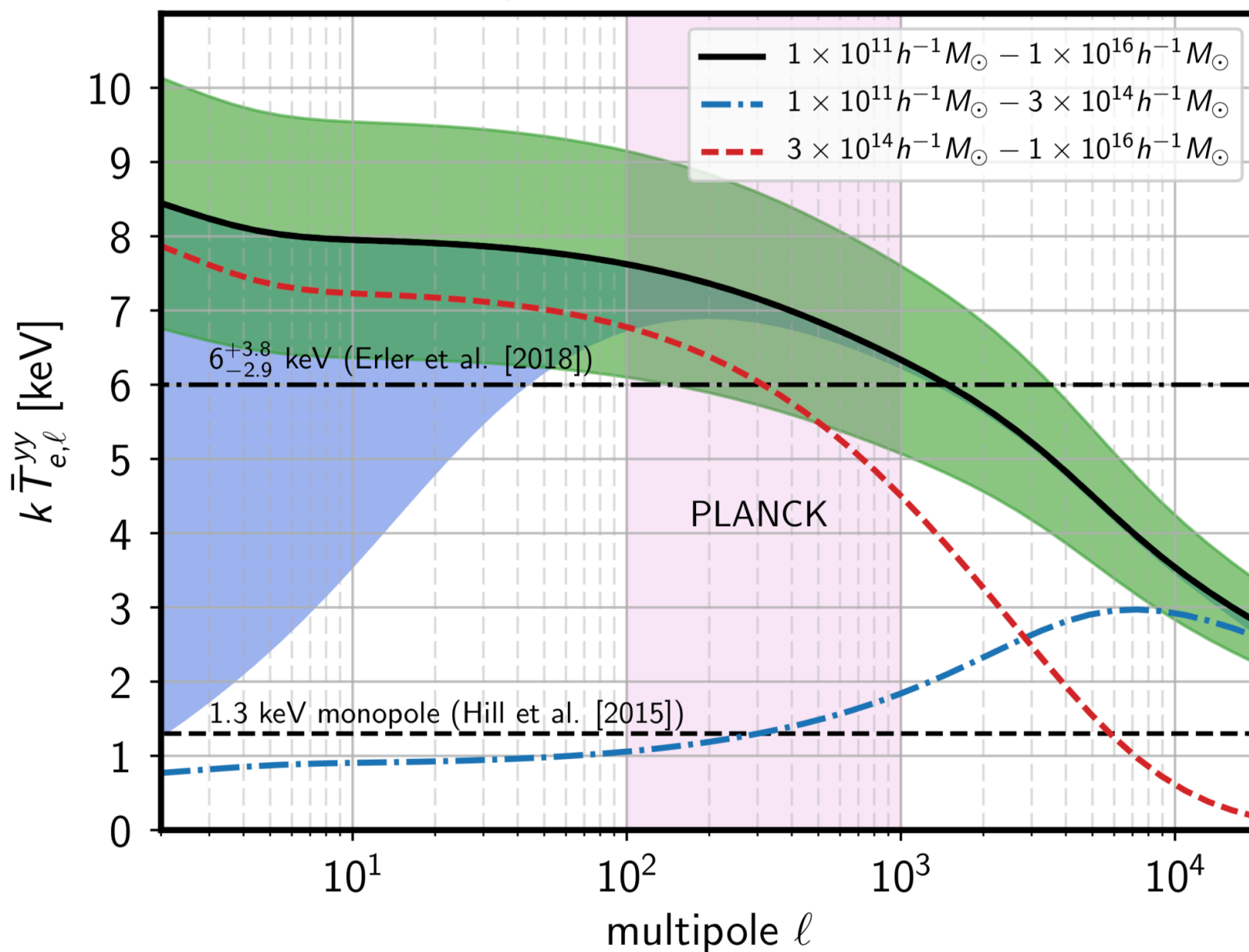
- SZ power spectrum analysis \rightarrow y^2 -weighted temperature is relevant

$$kT_{e,\ell}^{yy} = \frac{\langle kT_e(M, z) |y_\ell|^2 \rangle}{\langle |y_\ell|^2 \rangle} \equiv \frac{C_\ell^{T_e, yy}}{C_\ell^{yy}}$$

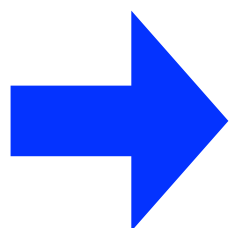
- Can be efficiently computed based on the halo model using CLASS-SZ
- Higher mass systems are up-weighted \rightarrow higher effective temperature expected
- Scale-dependent quantity (but fixed temperature captures leading order effect)!

Theoretical estimate for the y^2 -weighted temperature

CLASS-SZ computation

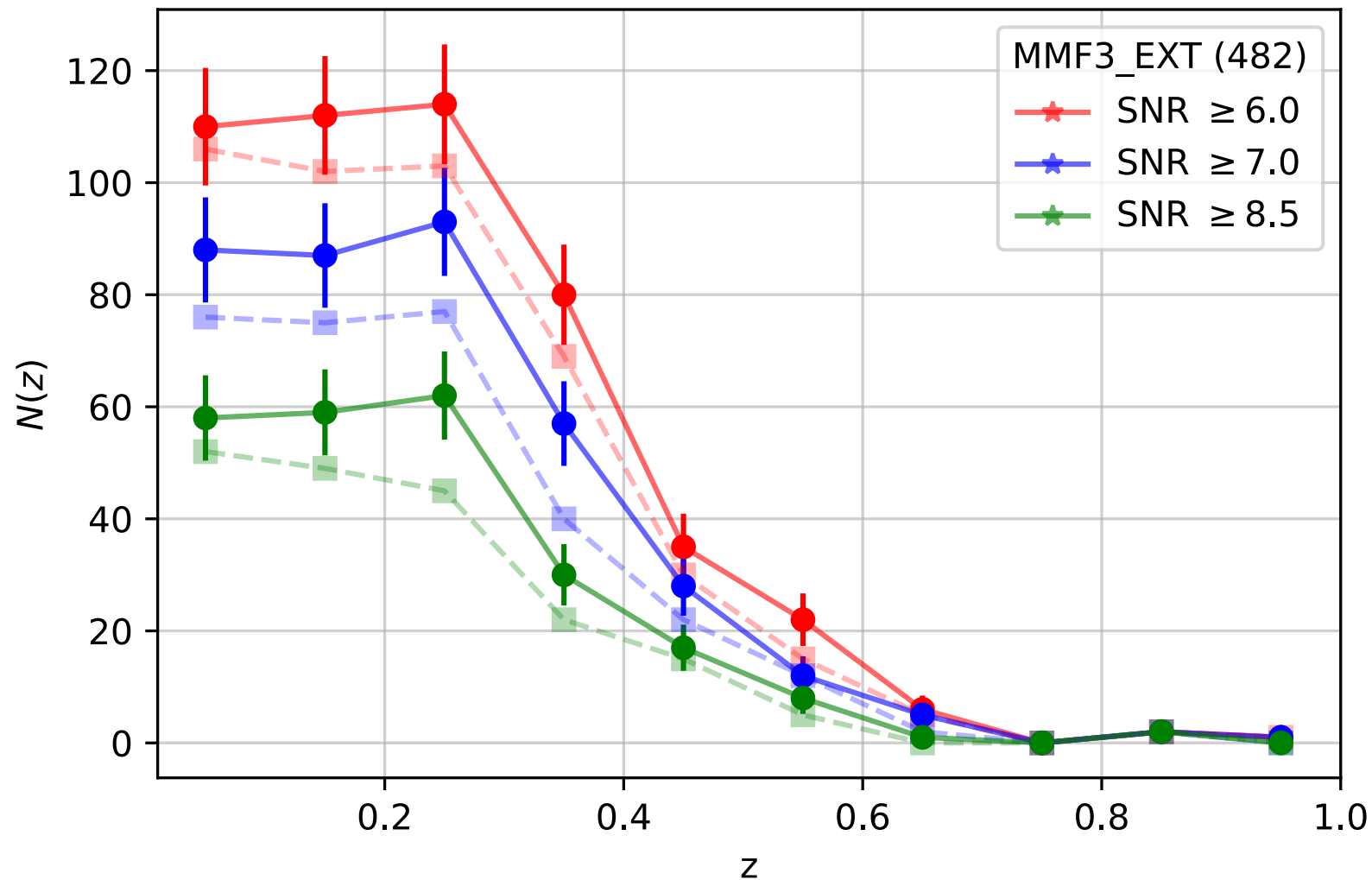


- Significant uncertainties...
- Contributions from diffuse y become important at large angular scales (e.g., Hansen et al., 2005)
- Assuming $kT_e \sim 5$ keV for *Planck* appears conservative
- Effective temperature is roughly constant for scales relevant to *Planck*

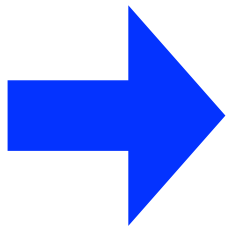


- rSZ plays a part in the σ_8 tension, alleviating it
- rSZ leads to systematic shift + increase of errors

Effect of rSZ on cluster number counts



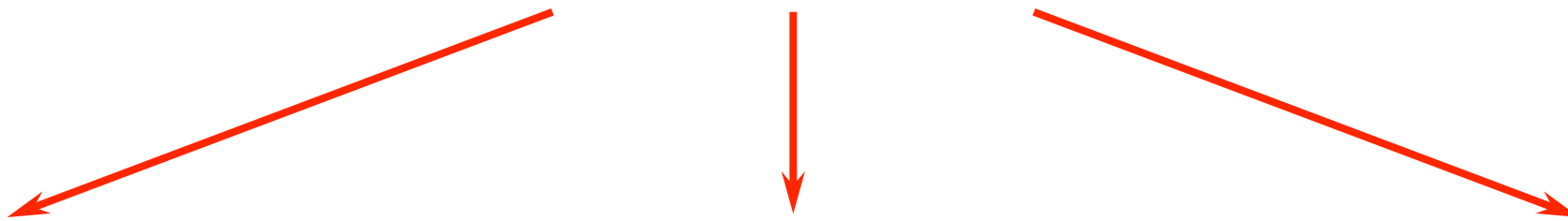
- Rescaled S/N increases
- Effect of rSZ pushes some systems above S/N threshold
→ # of clusters increases
- Caveats regarding noise rescaling
→ filter scale also changed
- shape of $N(z)$ seems better
- Still work in progress....



- rSZ again moves σ_8 into the right direction
- Preliminary effect found at $\sim 1\sigma$ level

Future opportunities for rSZ studies

- Tens of thousands of clusters will be detected through the tSZ effect
- Unprecedented sensitivity, frequency coverage and angular resolution (e.g., SO, CCAT-prime, Millimetron, PICO...)
- Complements X-ray and lensing measurements



Individual systems

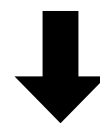
- y -maps, T_e -maps & velocity (?) maps
- Reconstruction of cluster profiles
- Non-thermal SZ (cosmic rays and turbulence)

Stacking analysis

- rSZ in mass bins
- Self-calibration of SZ temperature-mass relation
- Cosmology with new SZ observables (\leftrightarrow moments)

Statistical analysis

- rSZ power spectrum
- Cluster number counts in mass and redshift bins
- Higher order statistics (\leftrightarrow non-Gaussianity)



Highly relevant when using SZ clusters as a cosmological tool
(\leftrightarrow neutrino masses, σ_8 , dark energy)

Conclusions

- rSZ still hard to see for individual clusters or in stacking analysis (e.g., Erler et al., 2017)
- rSZ causes an underestimation of the y -parameter for *Planck*
- rSZ plays a role in the σ_8 tension (shift upwards + increase of error)
- Careful analysis marginalizing over model uncertainties is required
- Net effect on SZ number counts still work in progress...

