

Study Of Nuclei at High Angular Momentum - Day 3

Some Current Topics In High-Spin Studies

- 1) Re-emergence of Collectivity at High Spin
- 2) A New “Spin” on Octopole Collectivity
- 3) High Spinners can study Neutron Rich Nuclei too!

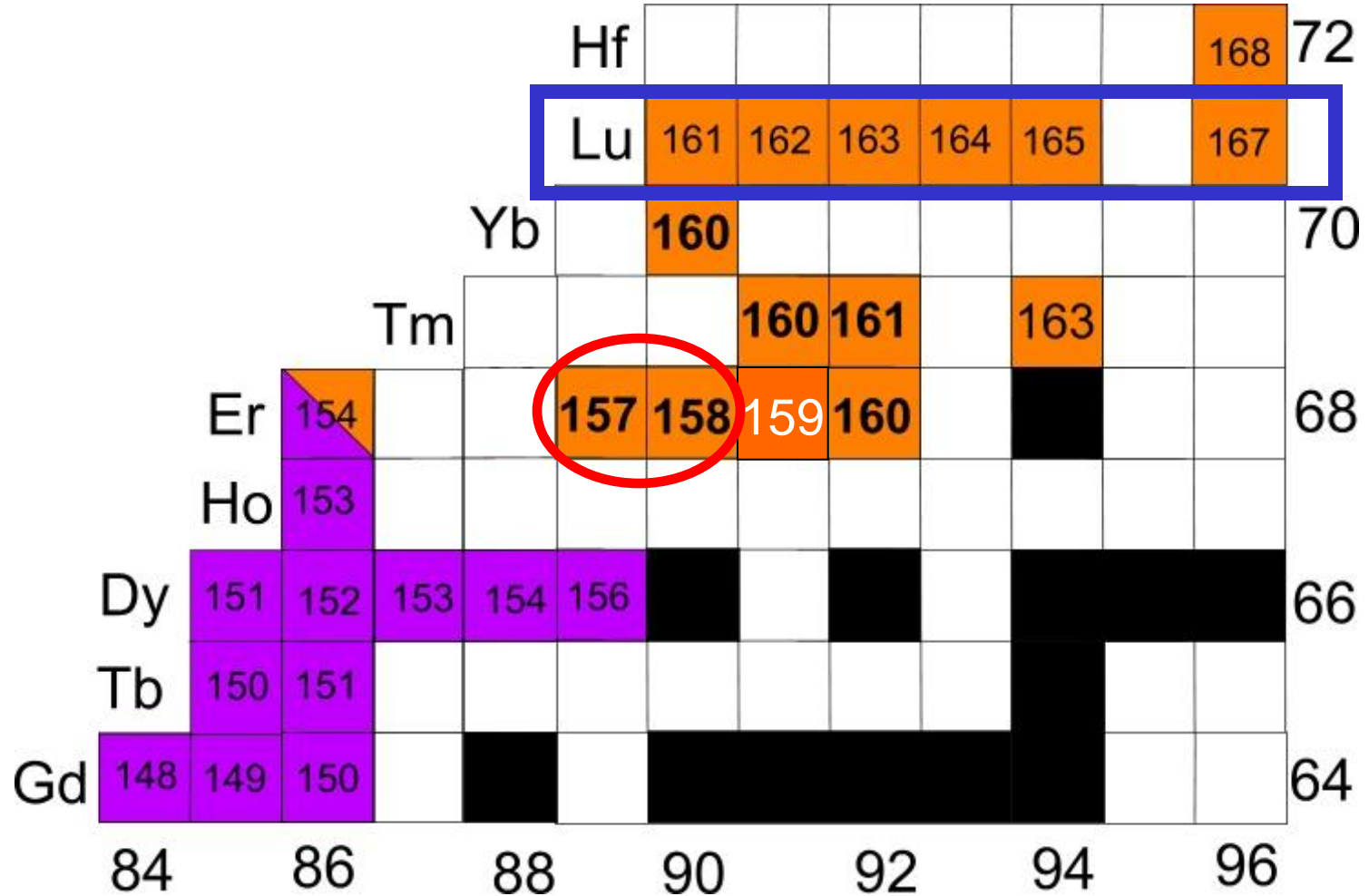
*Michael P. Carpenter
Nuclear Physics School, Goa, India
Nov. 9-17, 2011*

Re-Emergence of Collectivity at High Spin



Nuclei at the highest spins: Beyond band termination

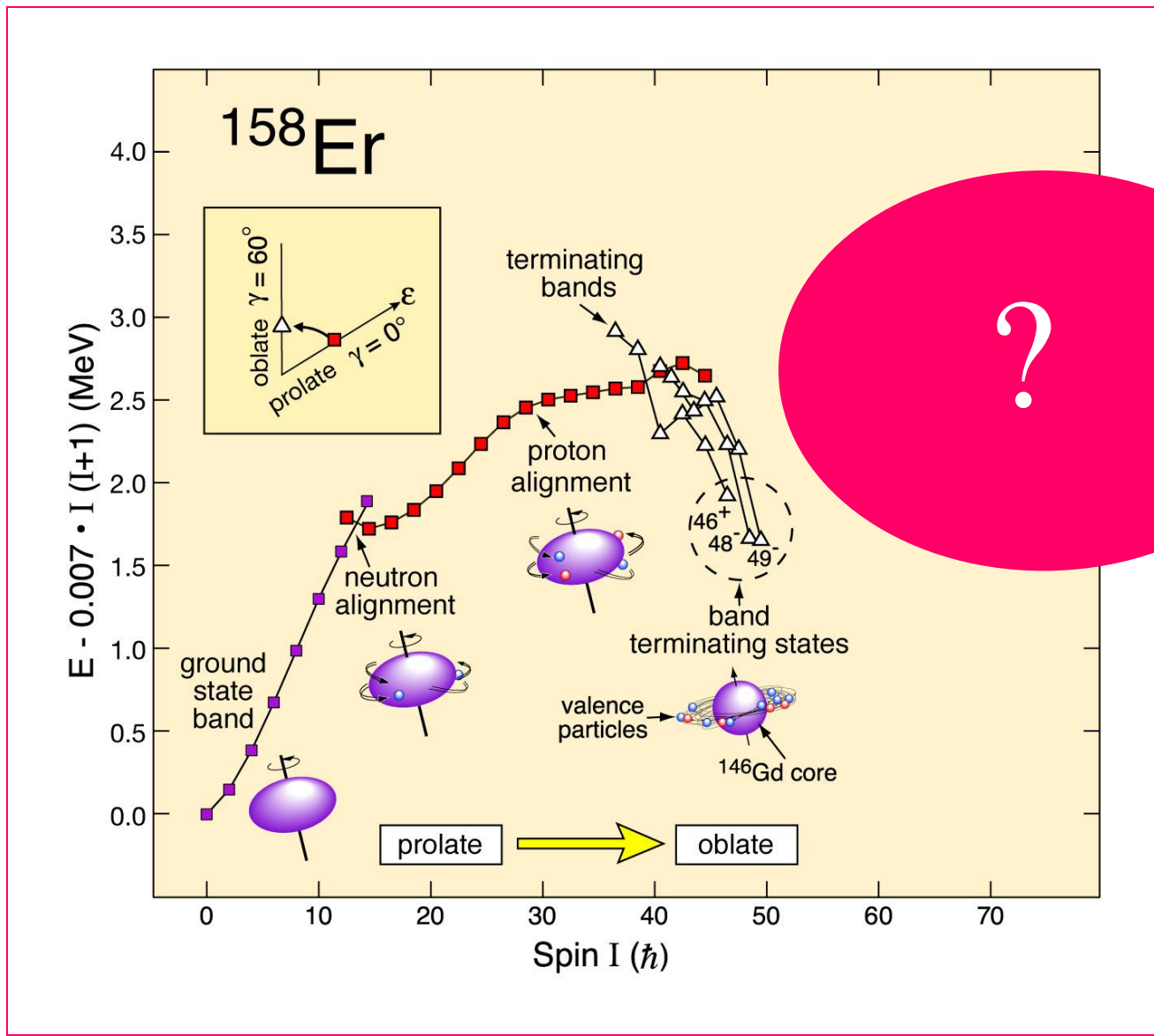
Triaxial strongly
Deformed (TSD)



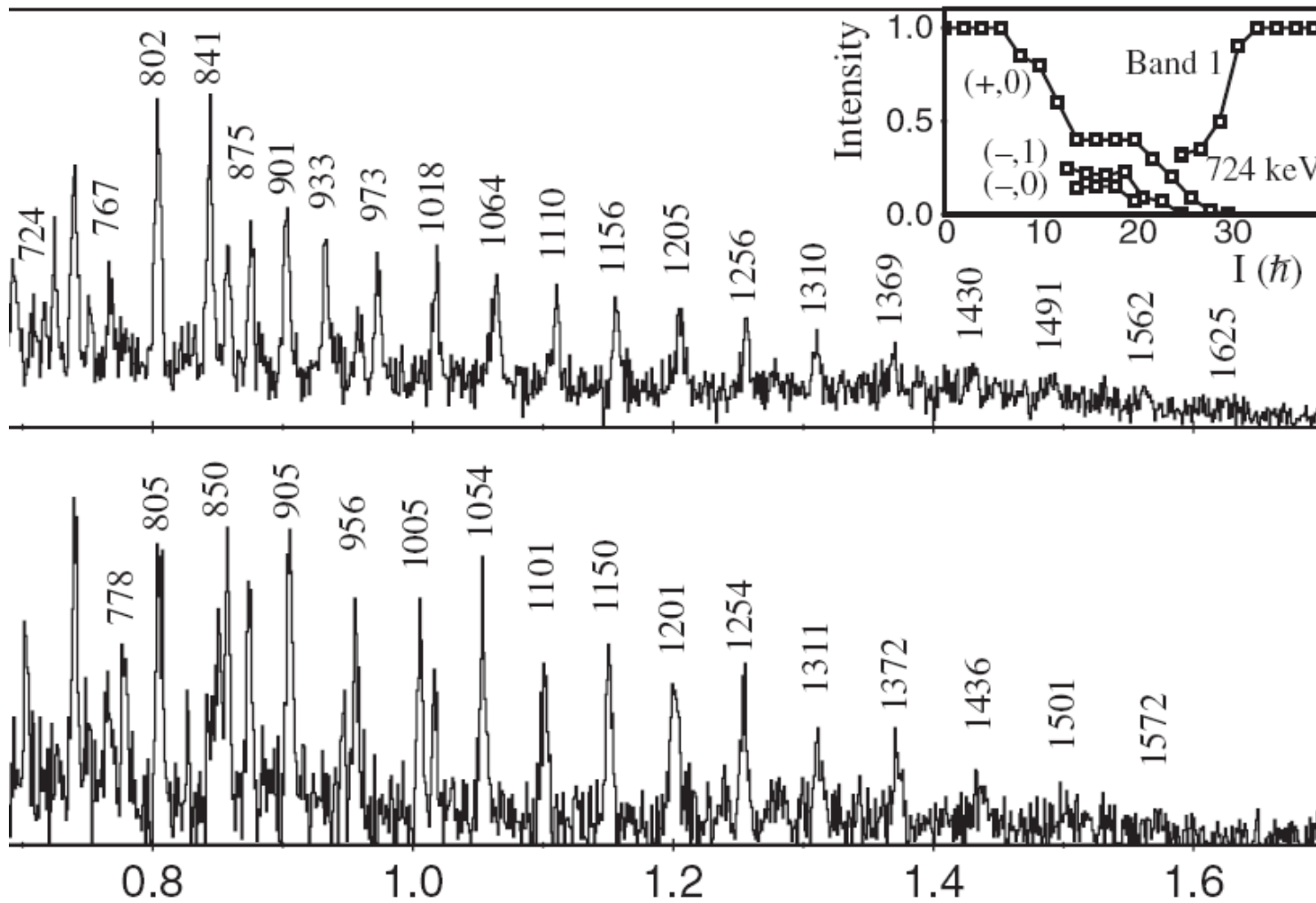
Superdeformed (SD)



Mid-90's: From collective rotation to band termination



2007: Evidence for return to collectivity



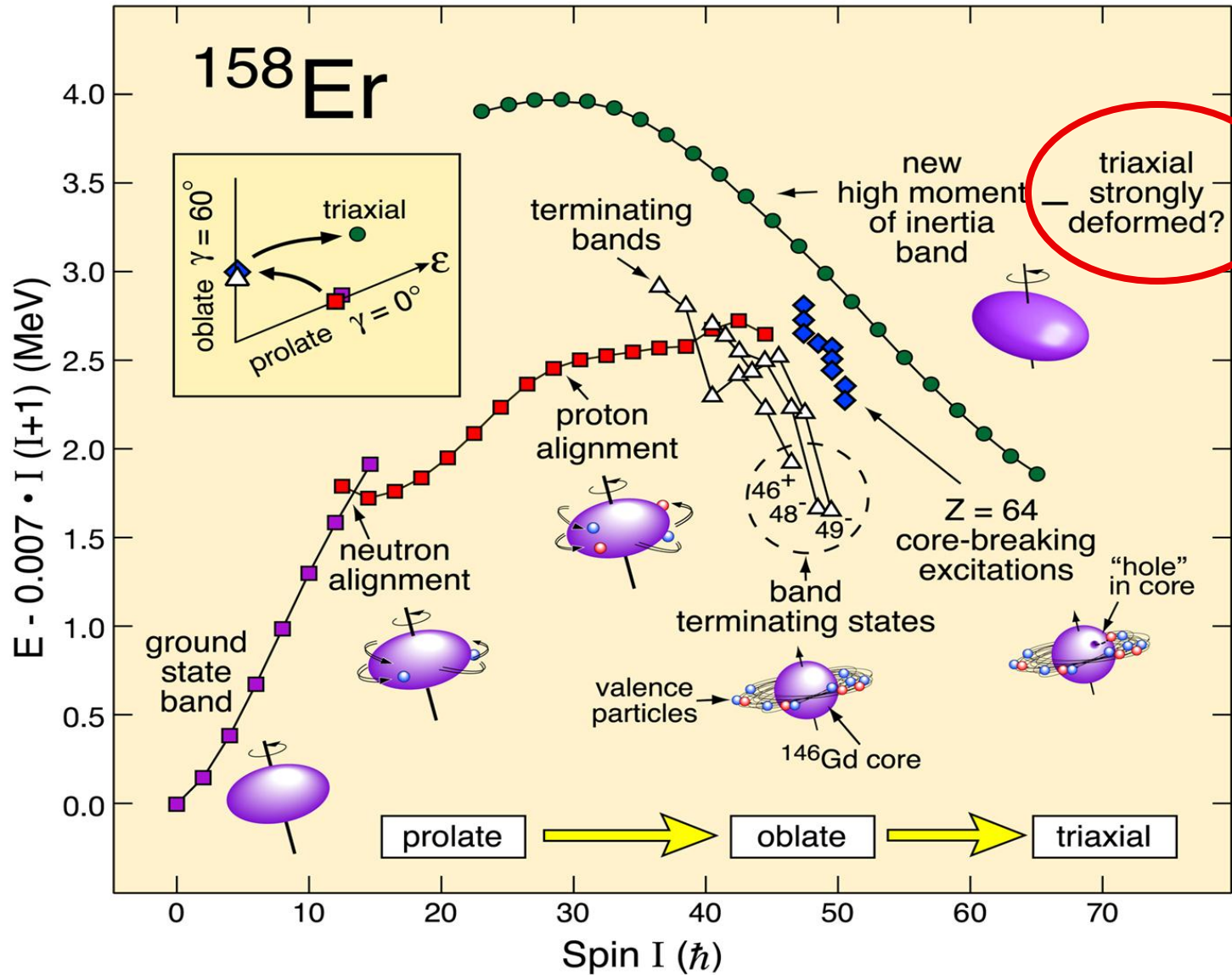
^{158}Er

^{157}Er

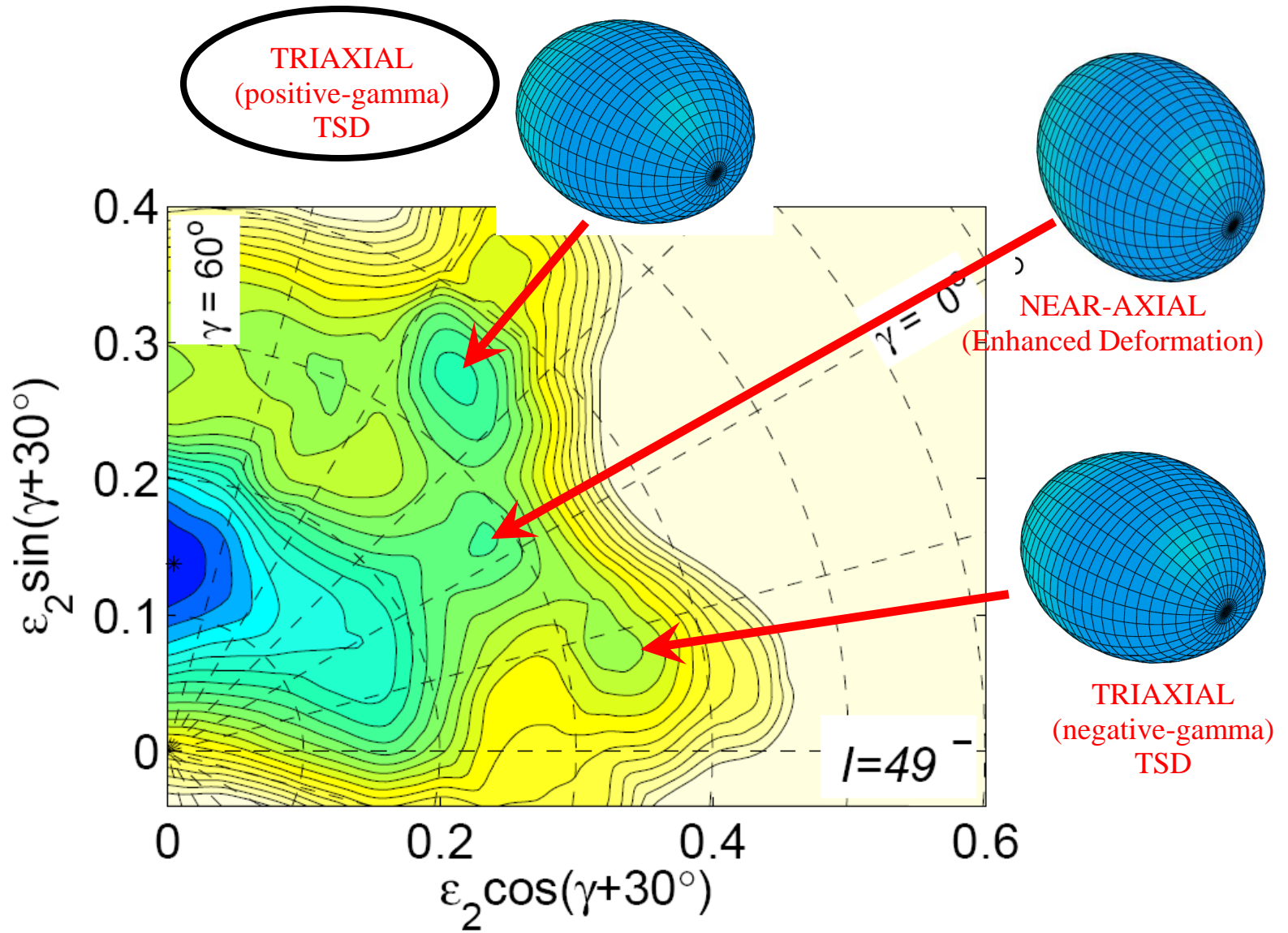
E.S. Paul et al., PRL 98, 012501(2007)



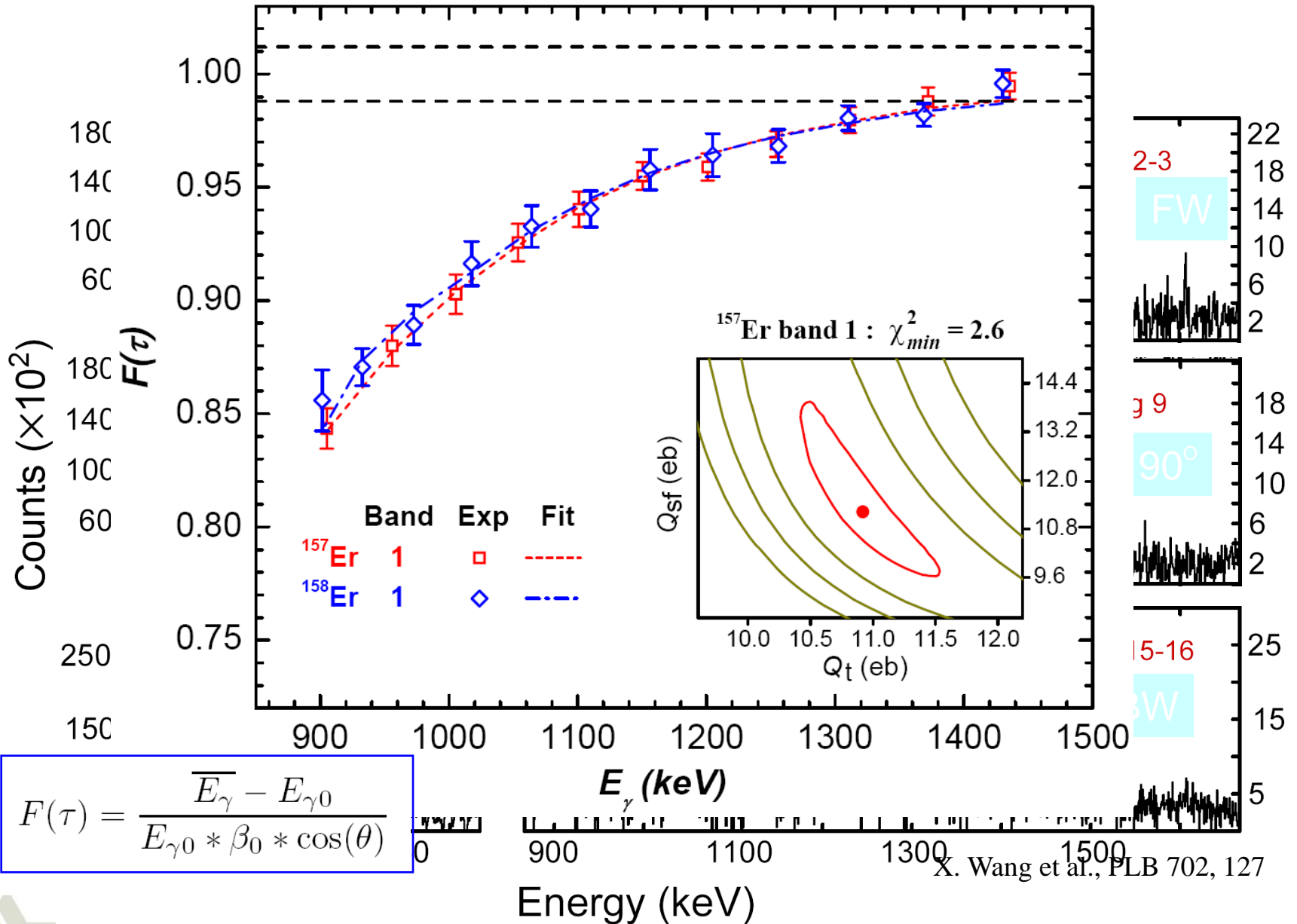
2007: Return to collectivity



2011: What deformation?



2011: Doppler Shift (DSAM) Measurement



Theory vs Experiment

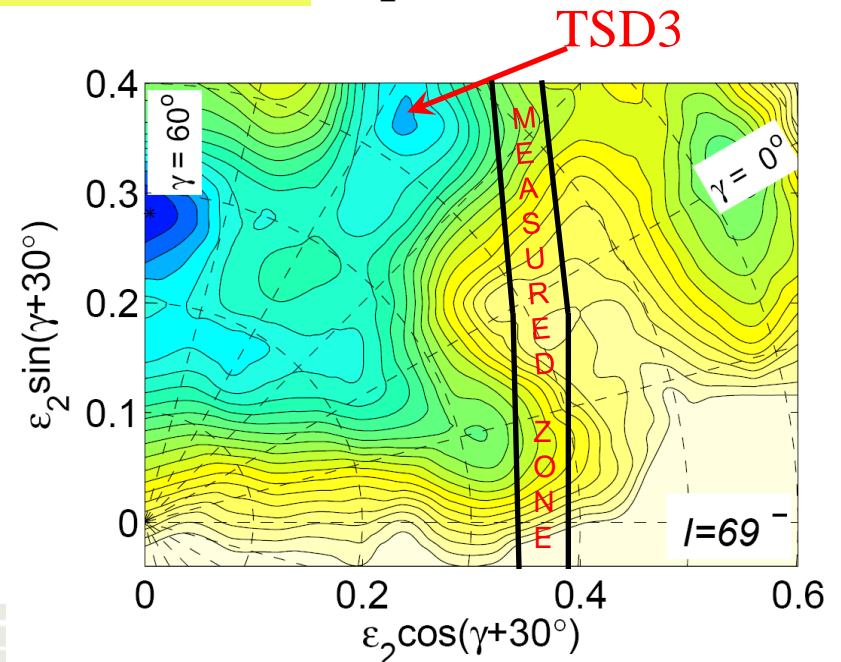
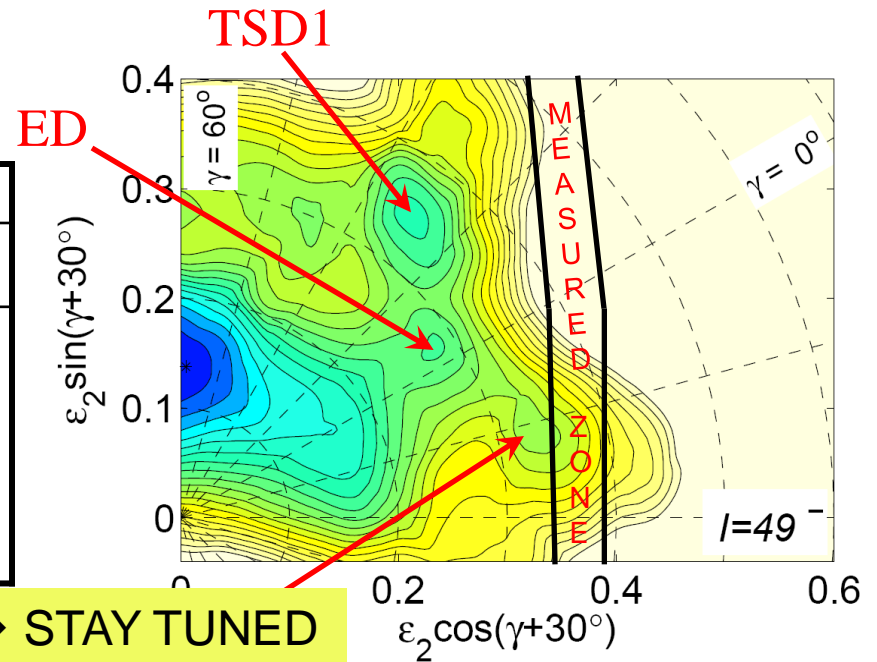
	MEASURED (band 1s)	CALCULATED			
		TSD1	TSD2	TSD3	ED
Q_t (<i>eb</i>)	^{158}Er : 11.7 (+0.7, -0.6)	6.0 – 7.2	10 – 11.2	8 – 9.2	6.7 – 7.9
	^{157}Er : 10.9 (+0.6, -0.5)				

THEORY NEEDS WORK → STAY TUNED

$$Q_t = Q_0 * \cos(\gamma+30^\circ)/\cos(30^\circ);$$

$$Q_0 = [\varepsilon_2 * (1 + \varepsilon_2/2) + 25/33 * \varepsilon_4^2 - \varepsilon_2 * \varepsilon_4] * [4/5 * (1.2)^2 * Z * A^{(2/3)}] / 100;$$

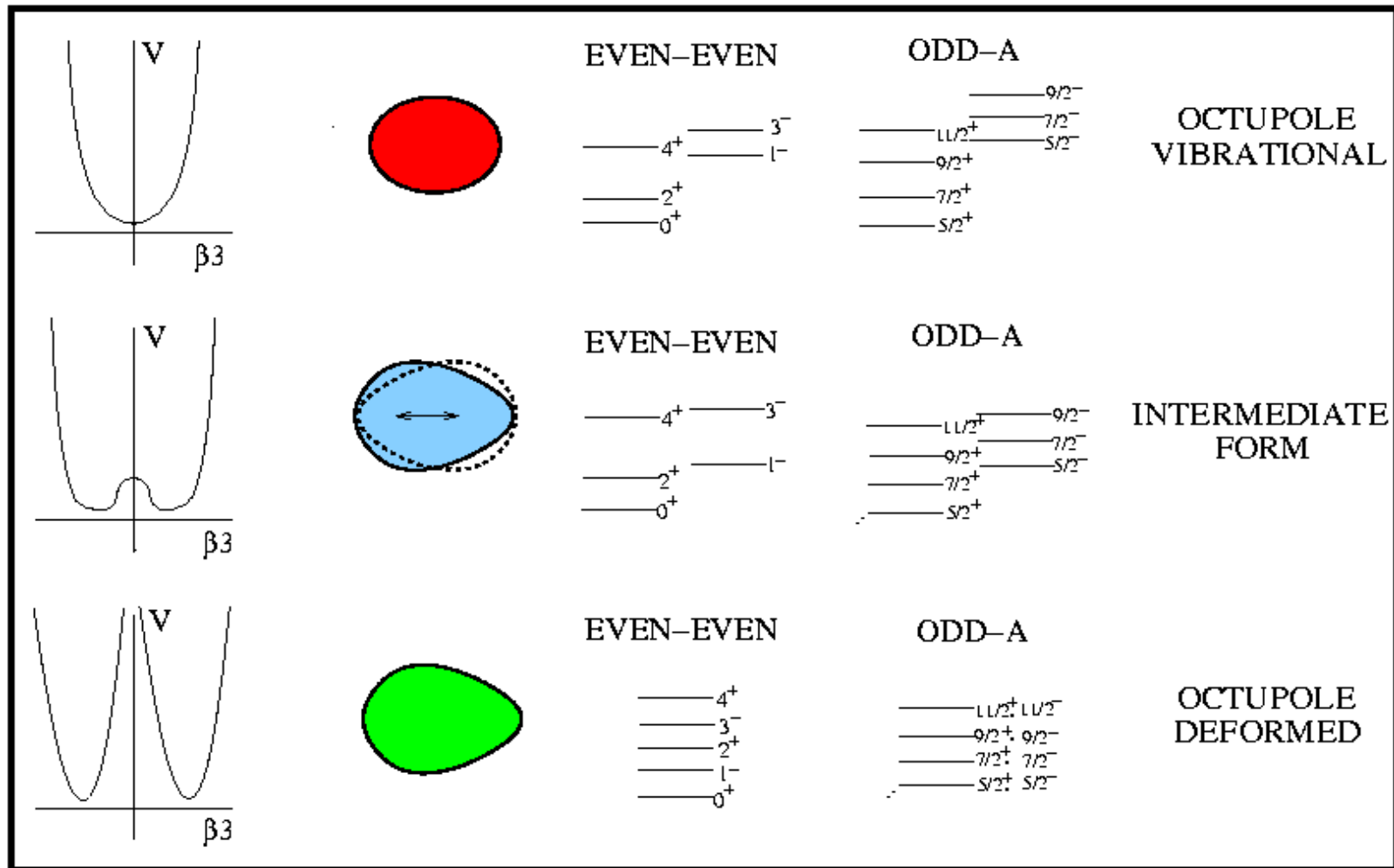
Q_t is transitional quadrupole moment; Q_0 is intrinsic quadrupole moment; ε_4 is set to be 0 here; Z is proton number; A is mass number.



A New “Spin” On Octupole Collectivity



Octupole Collectivity



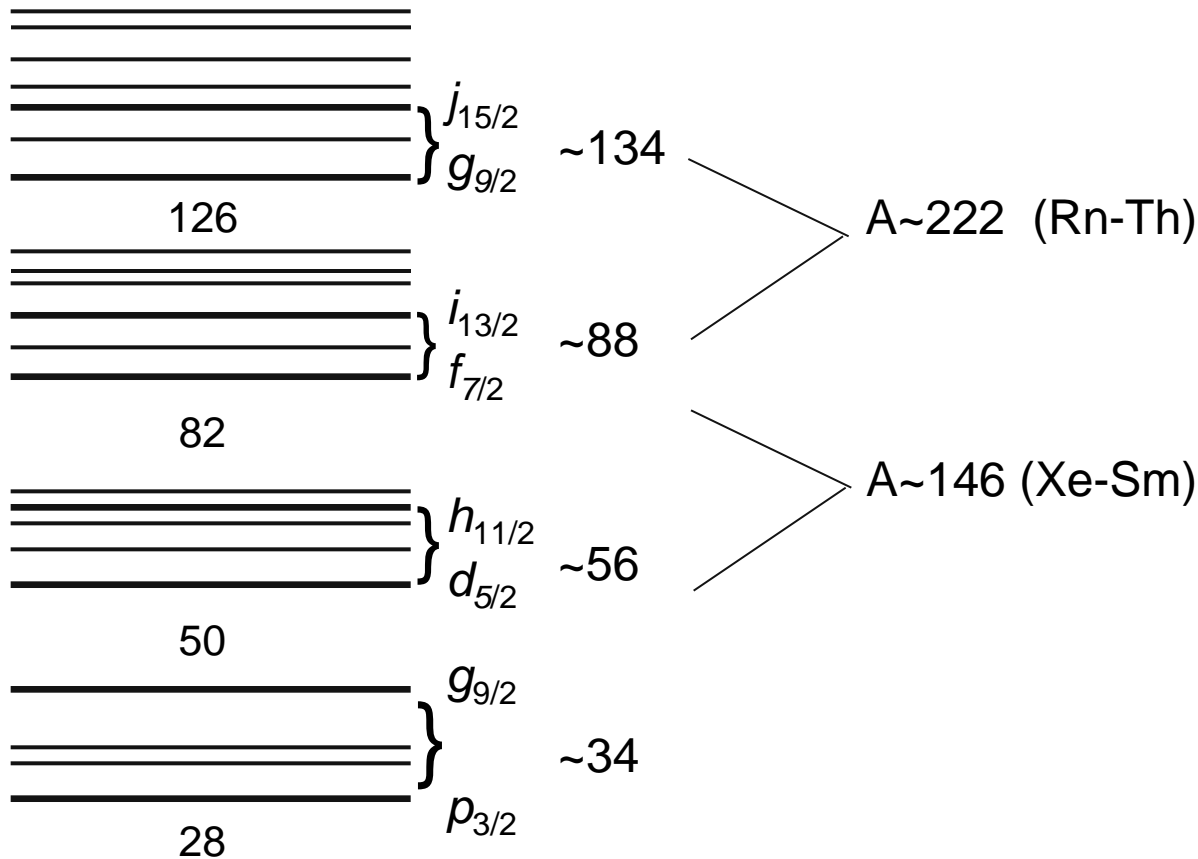
I. Ahmad & P. A. Butler, Annu. Rev. Nucl. Part. Sci. **43**, 71 (1993).

P. A. Butler and W. Nazarewicz, Rev. Mod. Phys. **68**, 349 (1996).



Where to find enhanced octupole collectivity

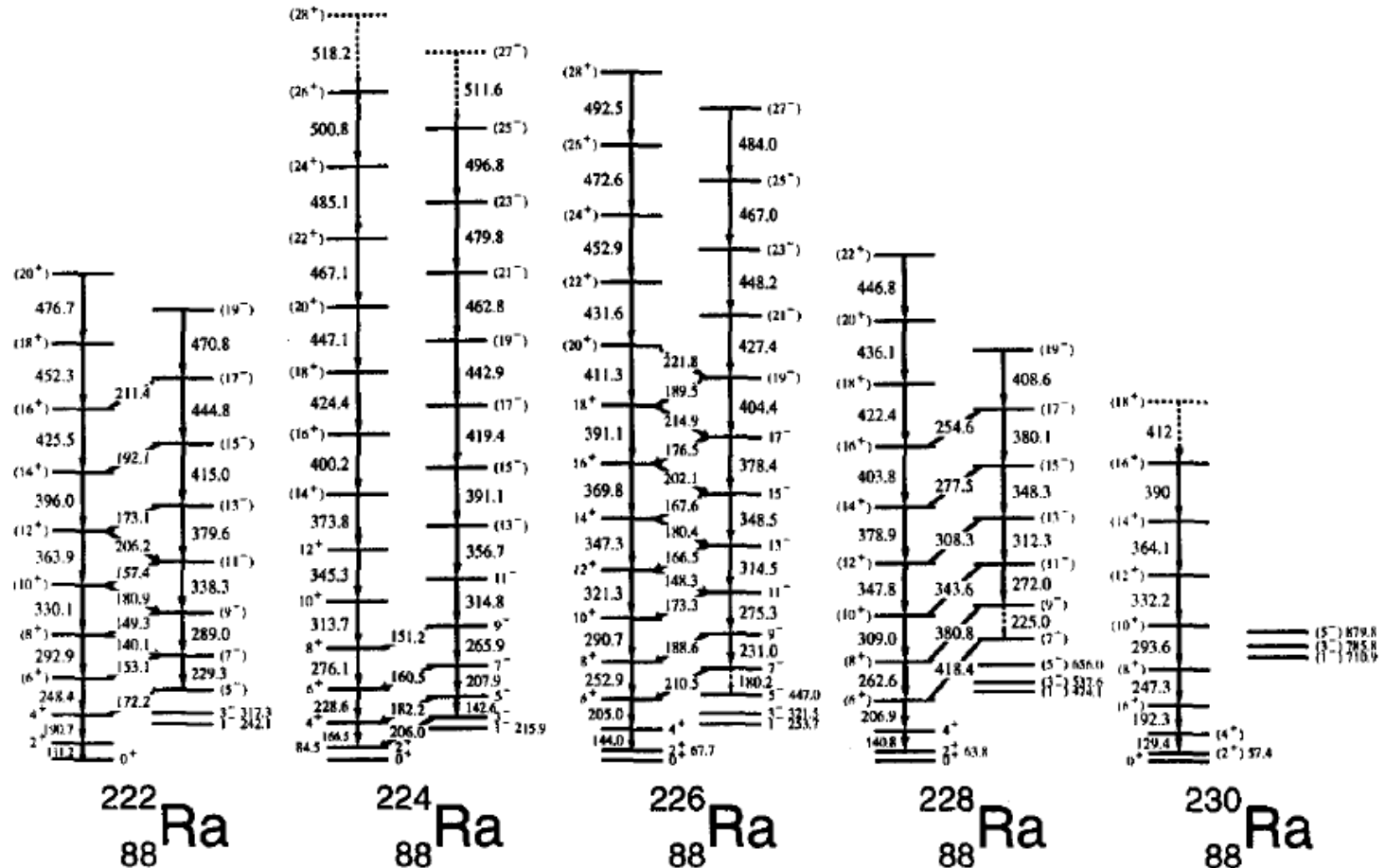
Long-range interactions between single particle states with $\Delta j = \Delta l = 3$;



Difficult regions to study experimentally



Multi-Nucleon Transfer: $^{136}\text{Xe} + ^{232}\text{Th}$ (Gammasphere)



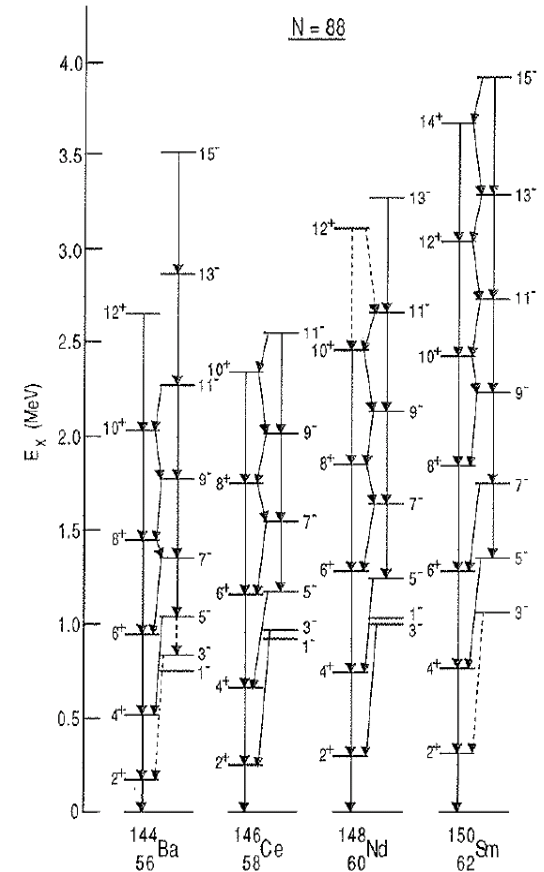
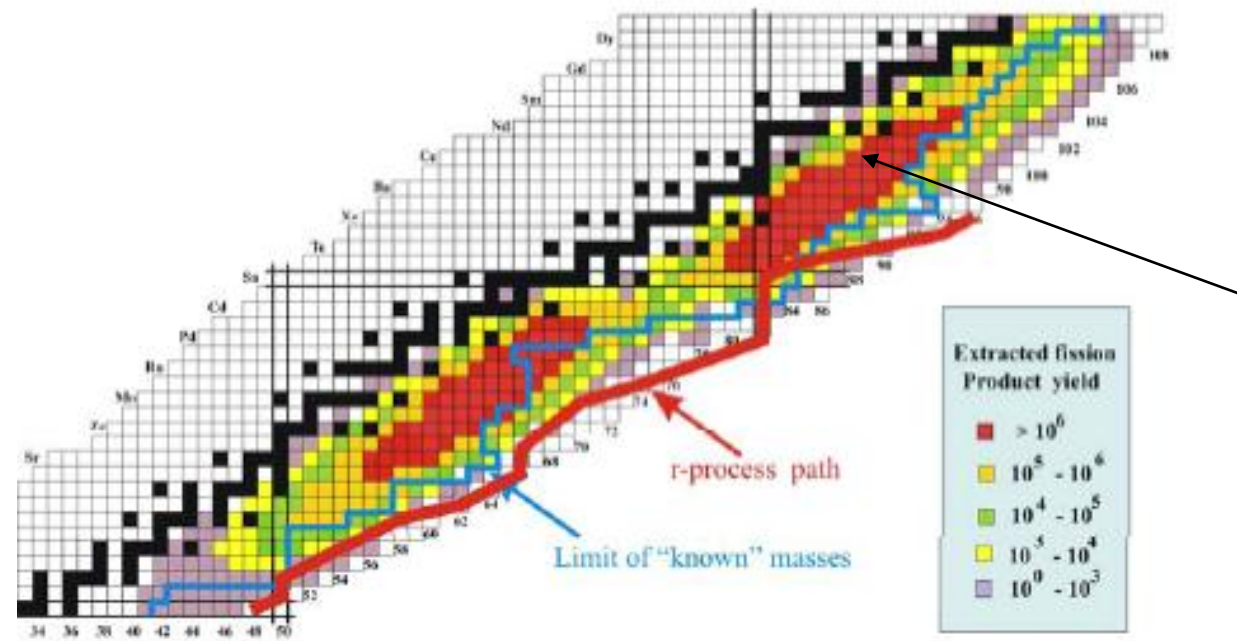
In addition, $^{226,228,230,232,234}\text{Th}$

J.F.C. Cocks et al., Nuc. Phys. A 645 (1999) 61



A~146 Region (Ba, Ce, Nd, Sm)

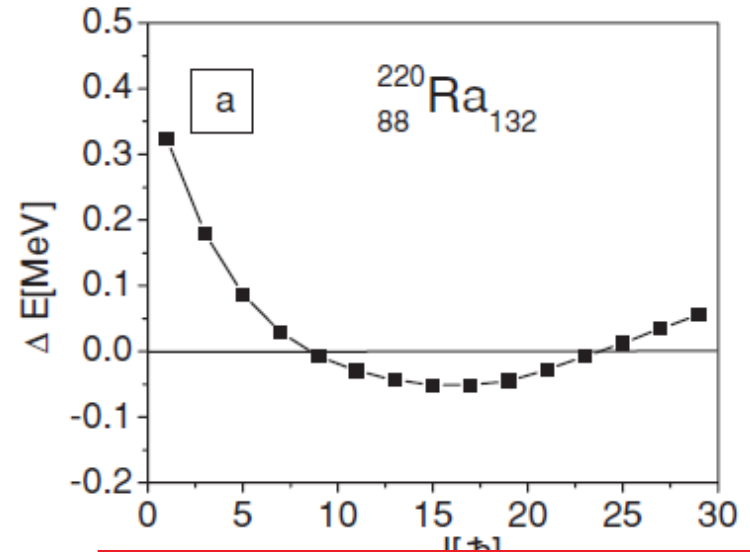
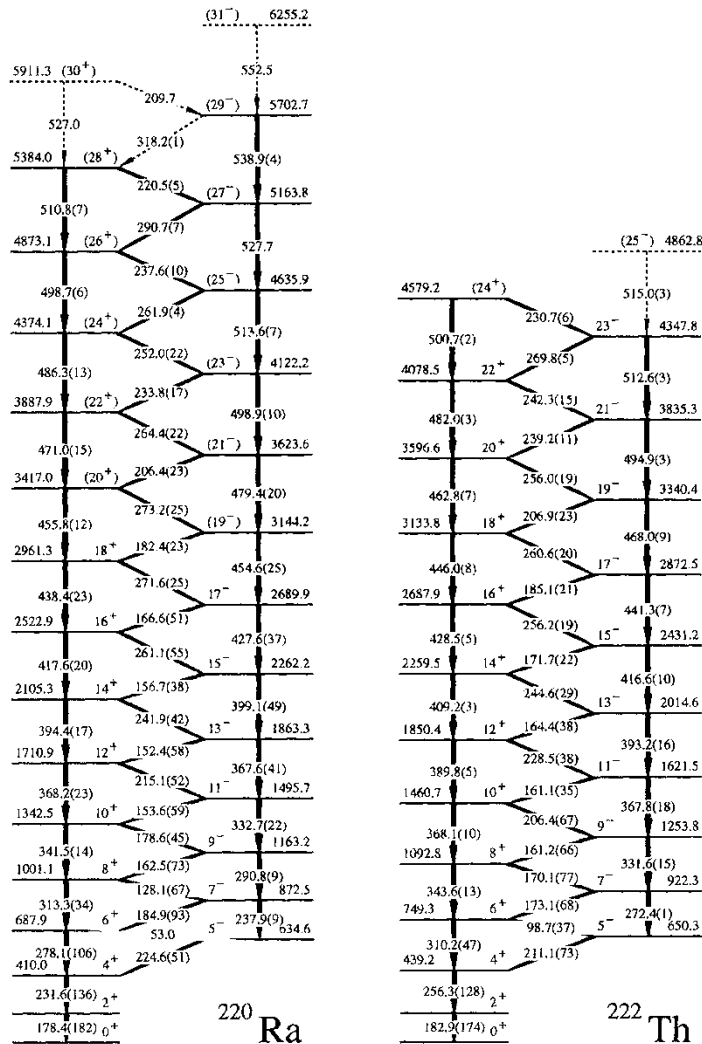
^{252}Cf spontaneous fission yield
 $T_{1/2}=2.6 \text{ a}$ 3+% fission branch



- Neutron rich region, excited states populated by spontaneous fission.
- CARIBU at ANL will provide reaccelerated beams of neutron-rich Ba isotopes for Coulomb excitation studies.



Rotation appears to stabilize static octupole shape



$$S(I) \equiv E_I - \frac{(I+1) \cdot E_{I-1} + I \cdot E_{I+1}}{2I+1}$$

Large Dipole Moments

$$D_0 \sim [B(E1)/\langle I_i 010 | I_f 0 \rangle]^{1/2}$$

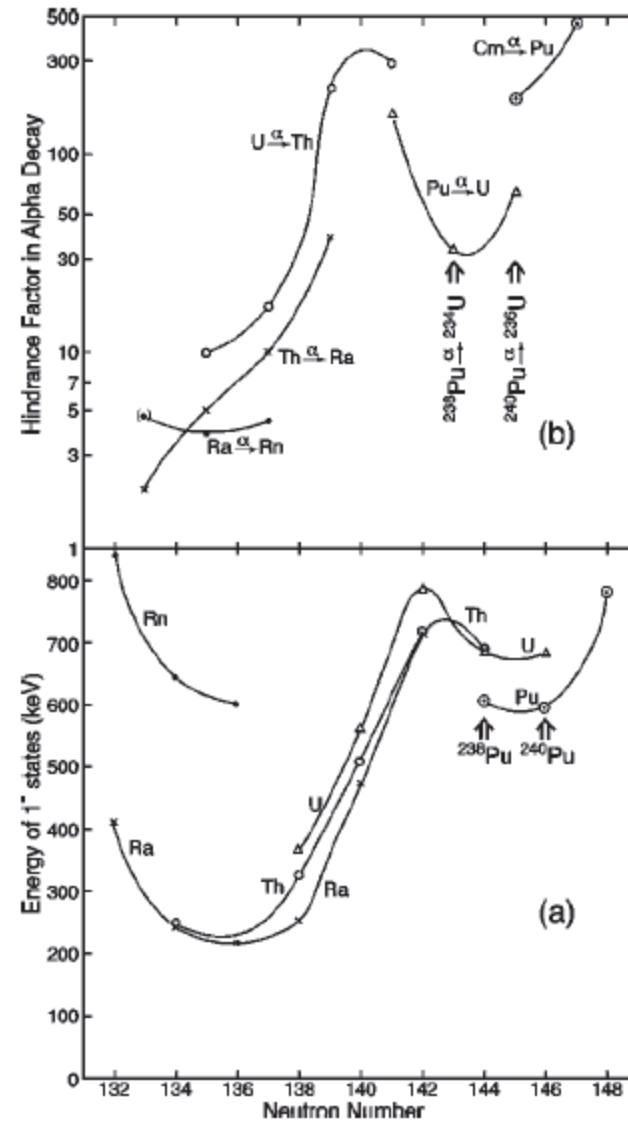
where

$$D_0 > 0.2 \text{ eb-fm}$$

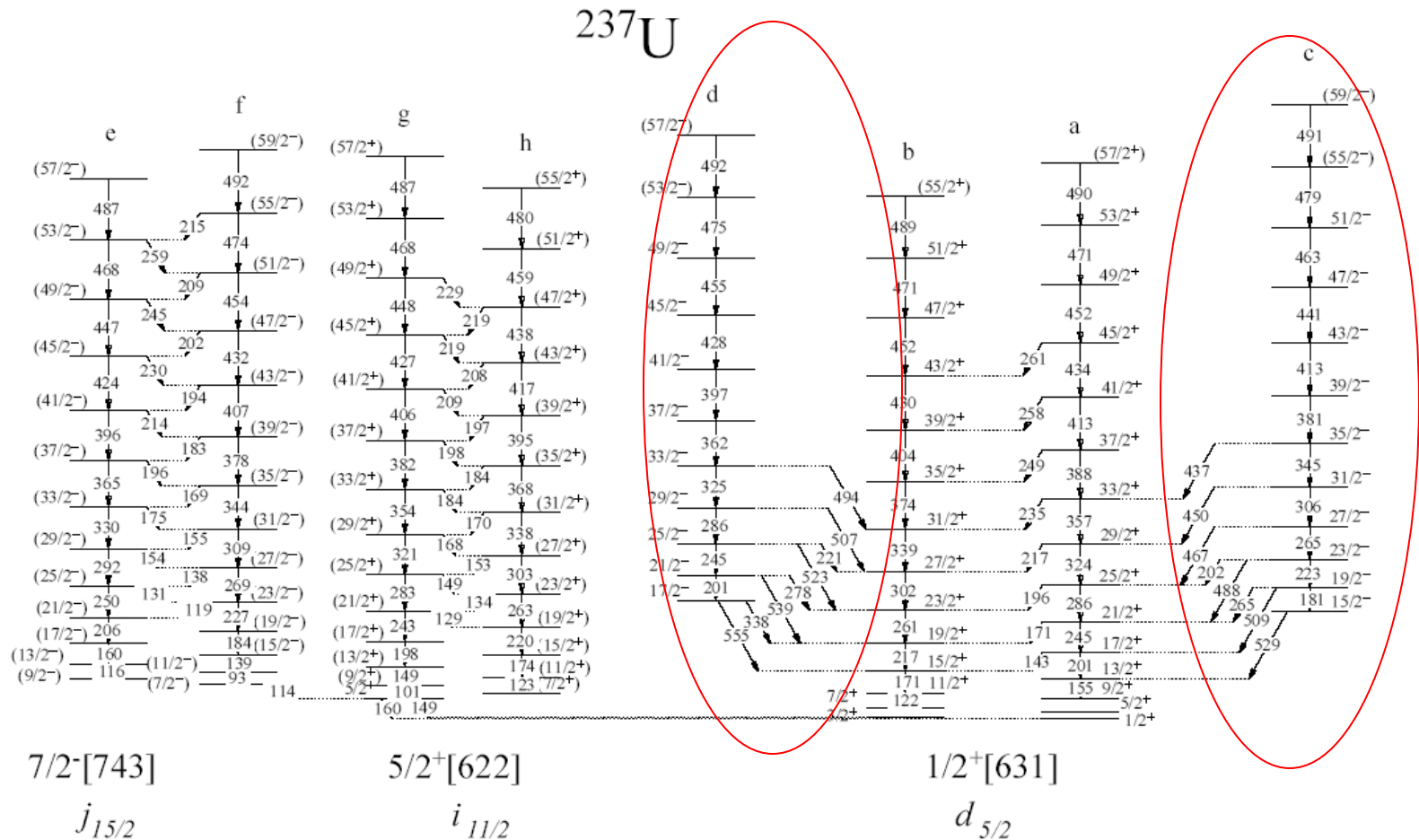
J. Smith *et al.*, Phys. Rev. Lett. 75 (1995) 1050.



Octupole Rotation: signatures



Odd-A Nuclei Exhibit Evidence of Octupole Collectivity

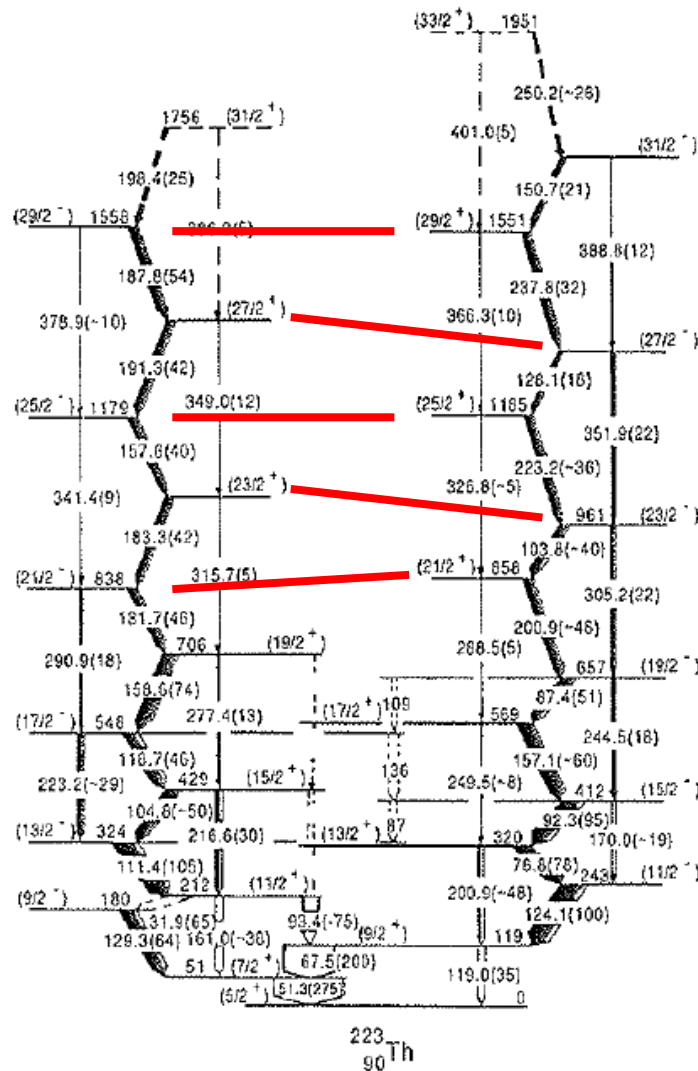


Octupole phonon coupled to quasiparticle

S. Zhu *et al.*, Phys. Lett. B618, 51 (2005)



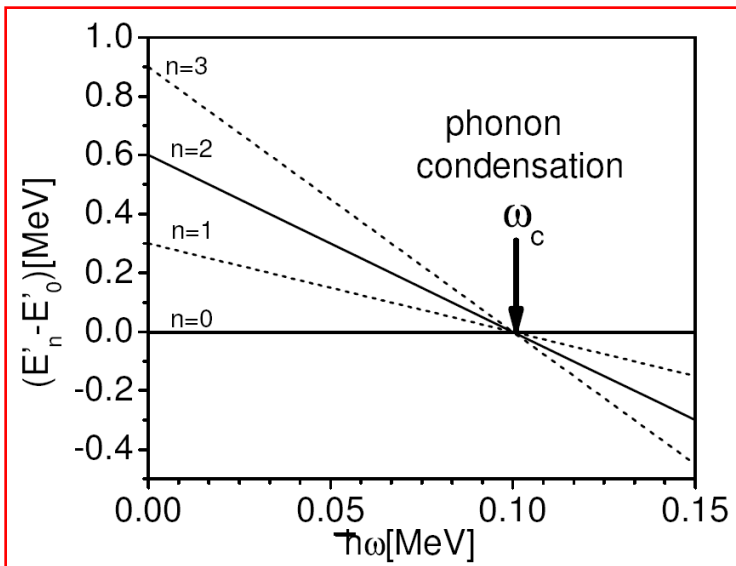
Signature of Octupole Collectivity in Odd-A Systems



Parity Doublets (Octupole deformed)



Alternative Explanation of static Octupole Deformation



Energy = Vibrational + Rotational

$$E_n = \hbar\Omega_3 \left(n + \frac{1}{2}\right) + \frac{1}{2} \mathfrak{I}\omega^2$$

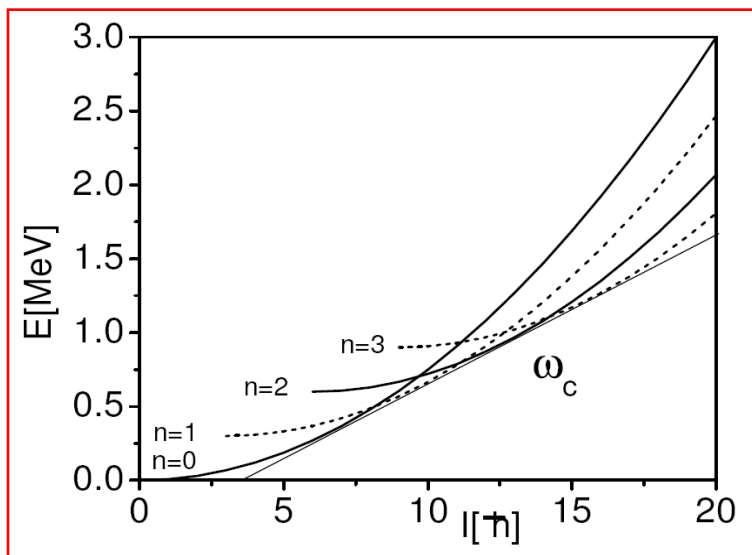
Lowest excitation when phonon's align with rotational axis.

$$E'_n(\omega) = \hbar\Omega_3 \left(n + \frac{1}{2}\right) - n i \omega - \frac{1}{2} \mathfrak{I}\omega^2$$

At critical frequency, ω_c , all phonon Routhians converge resulting in phonon condensation.

$$\omega_c = \Omega_3 / i$$

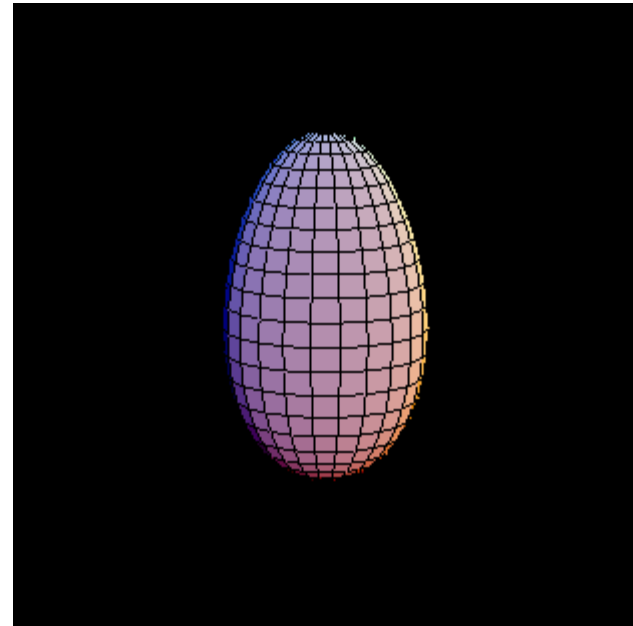
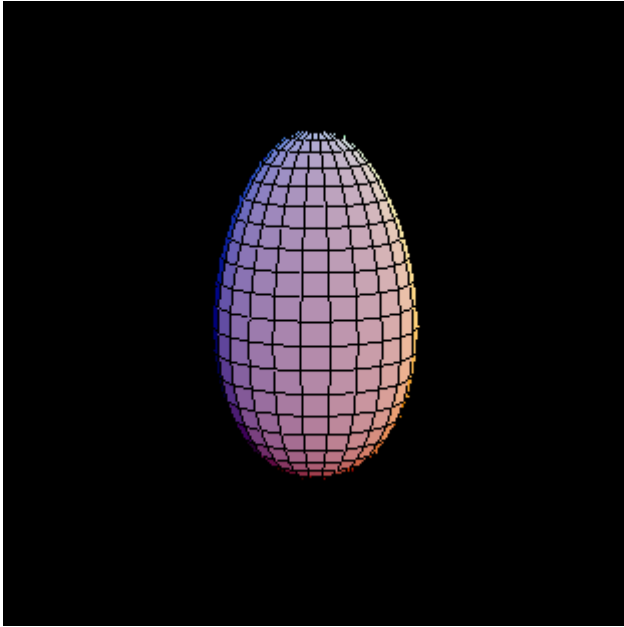
$$\omega_c : E_n(\omega) = E_{n+1}(\omega)$$



S. Frauendorf, Phys Rev. C 77 (2008) 021304(R).



What is the Resultant Shape at Condensations



$$\omega_c = \Omega_3 / 3$$

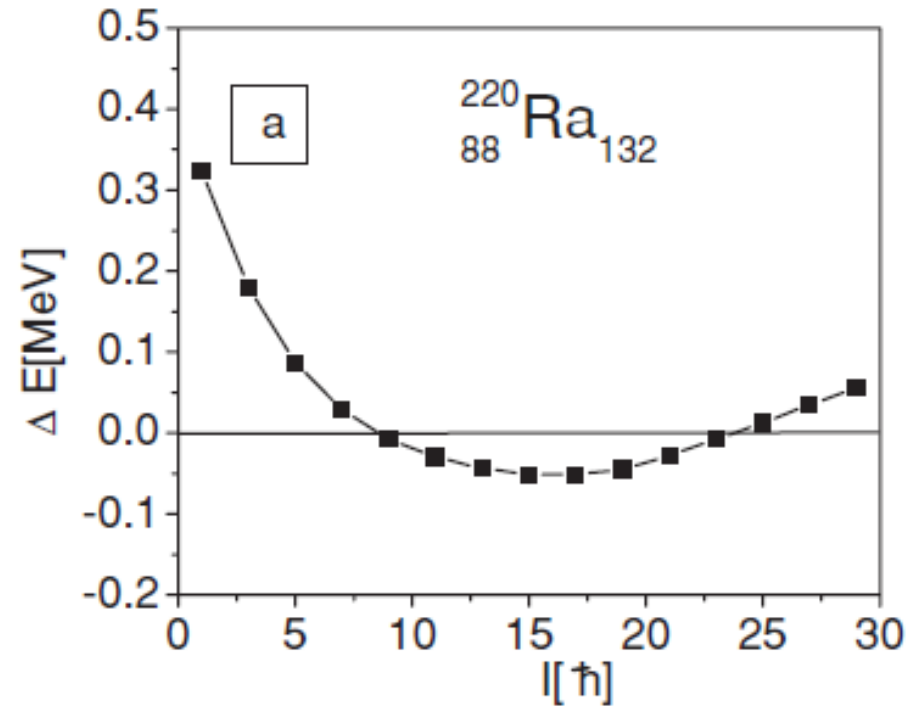


Consequence of Anharmonicities.

$$\mathcal{R}_z(\pi) = \mathcal{P}$$



1		π
8	—	+
7	—	-
6	—	+
5	—	-
4	—	+
3	—	-

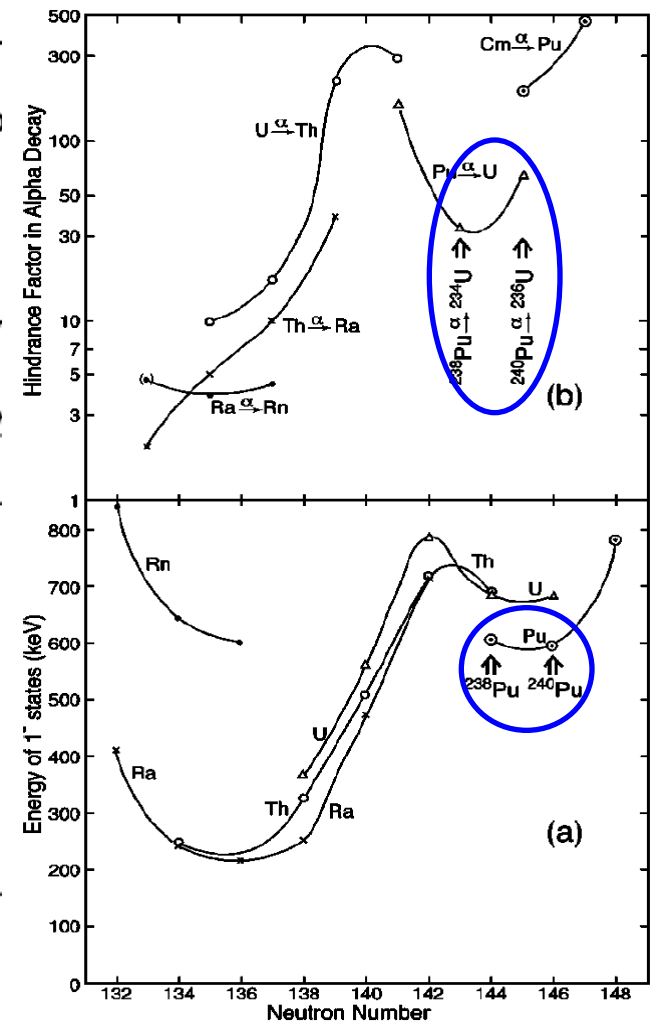
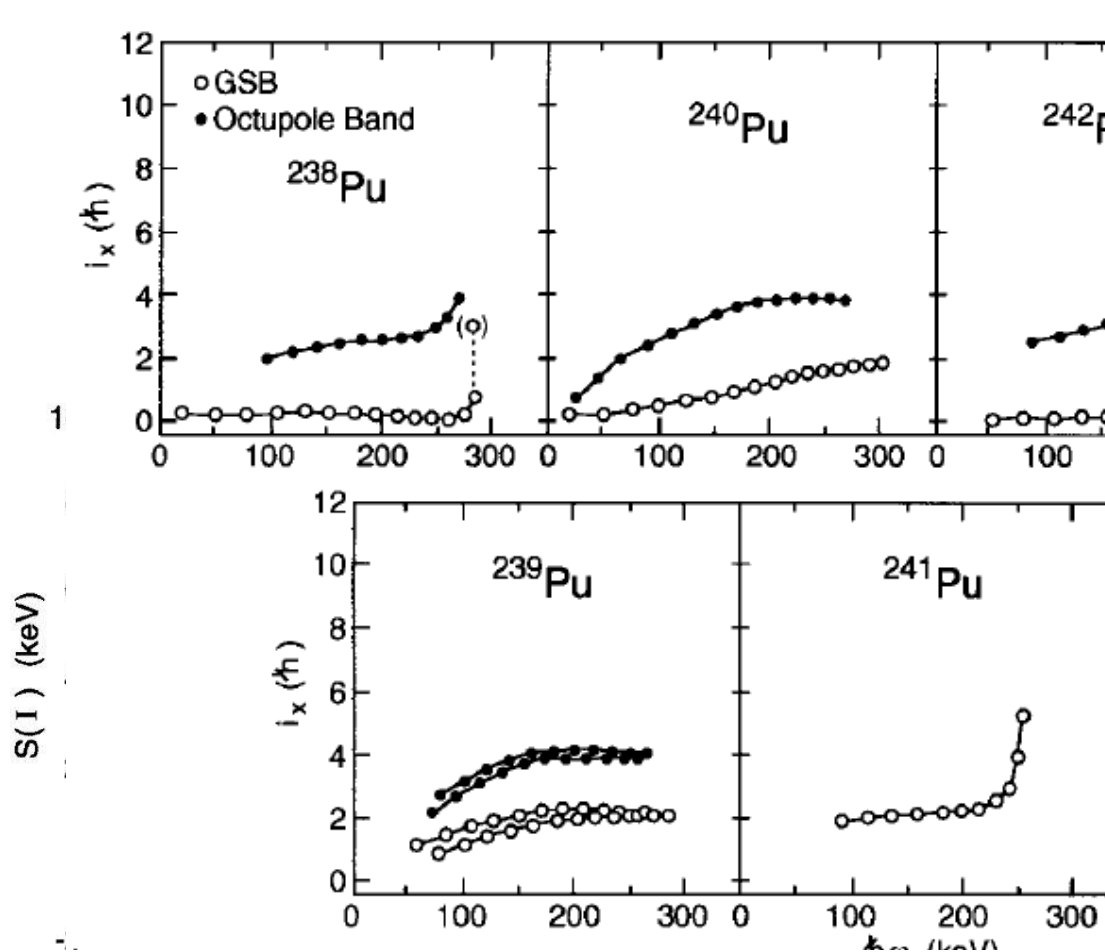


- Due to anharmonicities, phonons bands will cross at different frequencies
- Phonon's of same parity will interact.
- Resulting yrast line will have states on average which appear to be interweaved as expected for static octupole shape.

S. Frauendorf, Phys. Rev. C 77 021304(R).



Octupole Correlations around $^{239,240}\text{Pu}$: Rotation, Vibration or something else?



Evidence for strong correlations at high spin: 1^+ & 1^- form 1 band at high spin, parity doublets in ^{239}Pu alignments, $E(1^-)$, hindrance factors

. Wiedenhoever et al., Phys. Rev. Lett. 83, 2143 (1999).
 S. Zhu et al., Phys. Lett. B618, 51 (2005).
 R. K. Sheline & M. A. Riley, Phys. Rev. C 61, 057301 (2000).

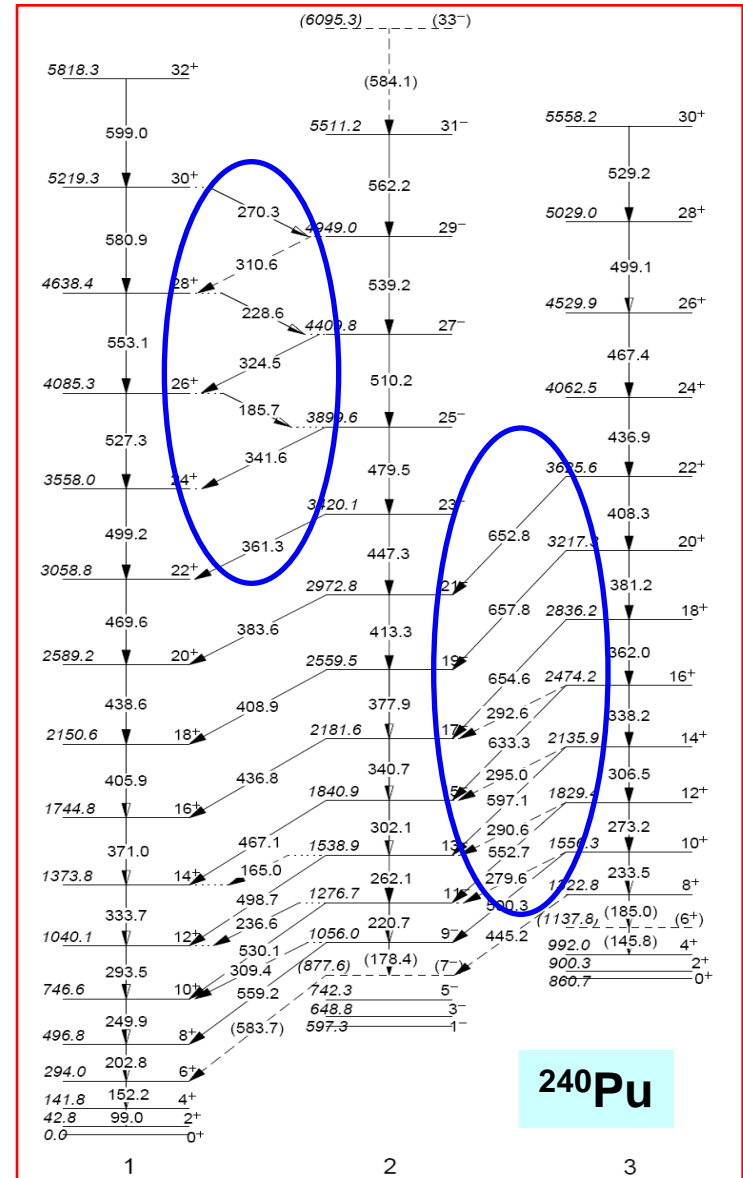


Can One Distinguish Between the Two Pictures?

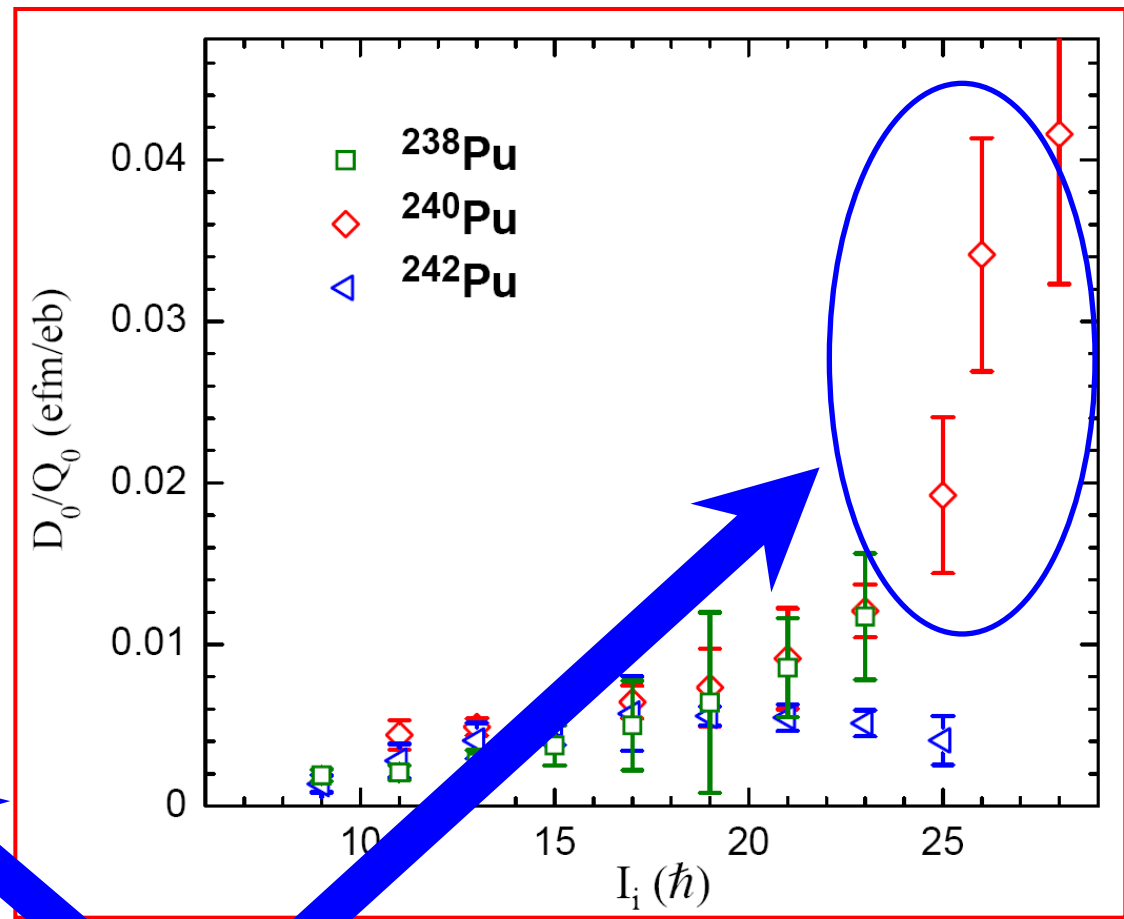
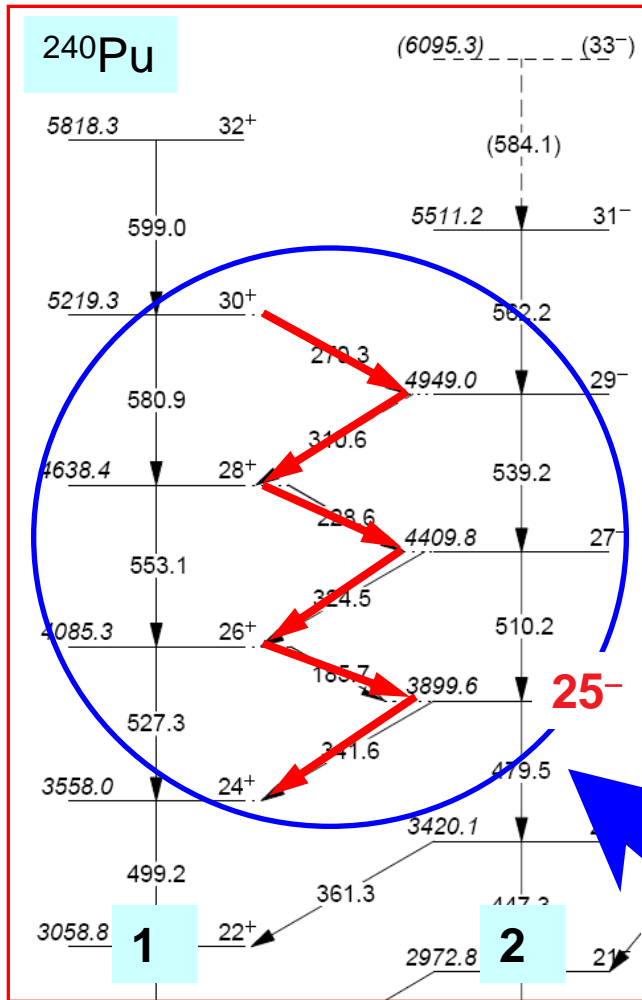
New Results on ^{240}Pu

- Interleaving E1 transitions now observed between yrast (1) and octupole (2) bands.
- Positive parity band built on 0^+ state at 861 keV is observed to high-spin.
 - Competes in excitation energy with yrast band.
 - Decays exclusively to octupole band
 - Large $B(E1)/B(E2)$ ratios: $\sim 1 \times 10^{-8} \text{ fm}^{-2}$
 - Band with these characteristics not seen before

X. Wang *et al.*, Phys. Rev. Lett. 102, 122501 (2009)



Dipole Moment at High-Spin is Large

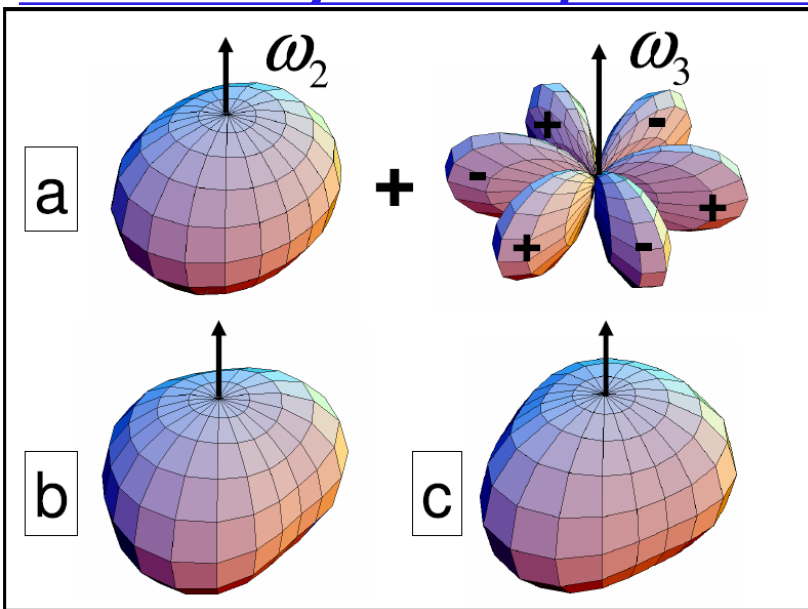


$D_0 > 0.2$ e fm (assuming $Q_0 \sim 11$ eb)

X. Wang *et al.*, Phys. Rev. Lett. 102 122501 (2009)



Evidence for Octupole Condensation?

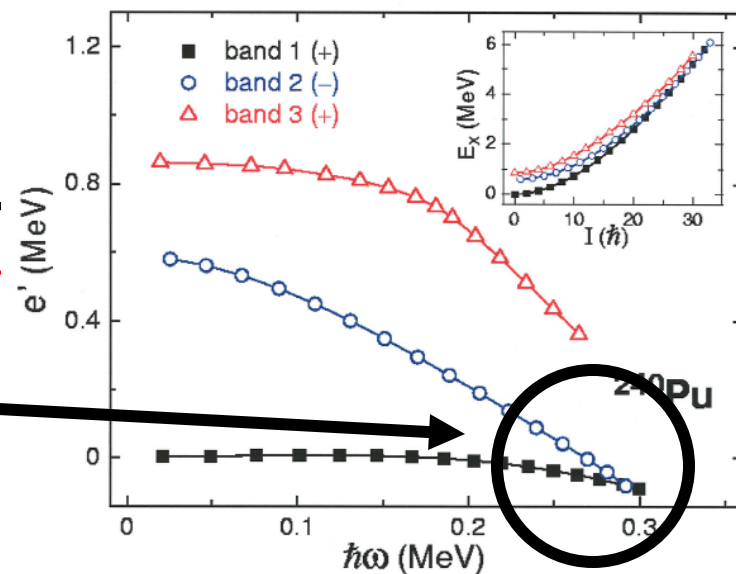
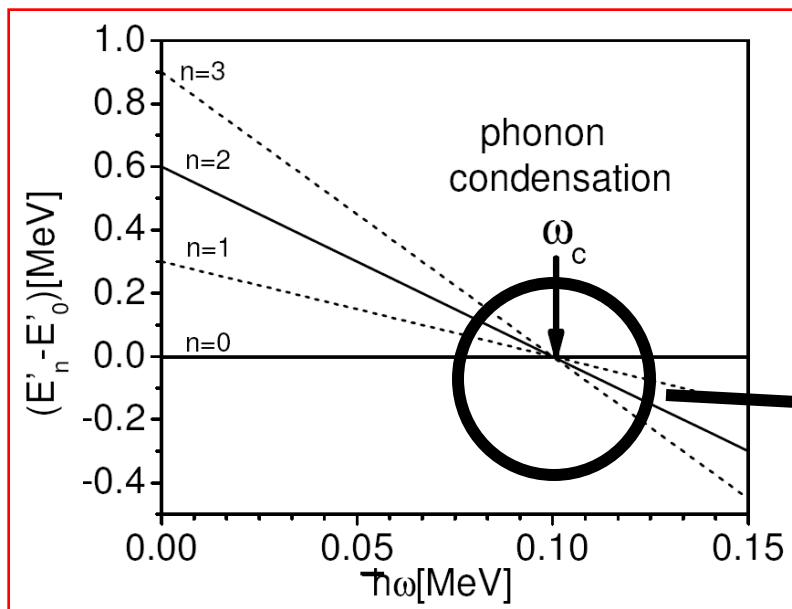


Octupole Condensation concept:

Rotation of a prolate deformed nucleus with a super-imposed octupole vibration with phonon spin aligned with rotational axis

Band 1 \rightarrow 0 phonon, Band 2 \rightarrow 1 phonon, Band 3 \rightarrow 2 phonons

Accounts for observations, i.e., bands, energies, alignments, branching ratios etc.



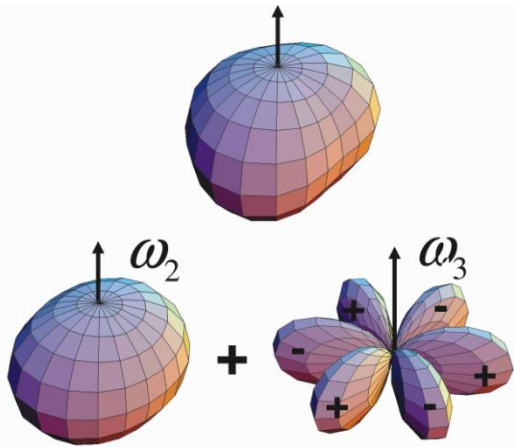
X. Wang et al., PRL 102, 122501 (2009)



Octupole Correlations: Generalization of Picture \rightarrow Tidal Waves

$N=130$ vs. $N=132$

Less “rotational-like”
(weakly deformed), but
Octupole features
persist.

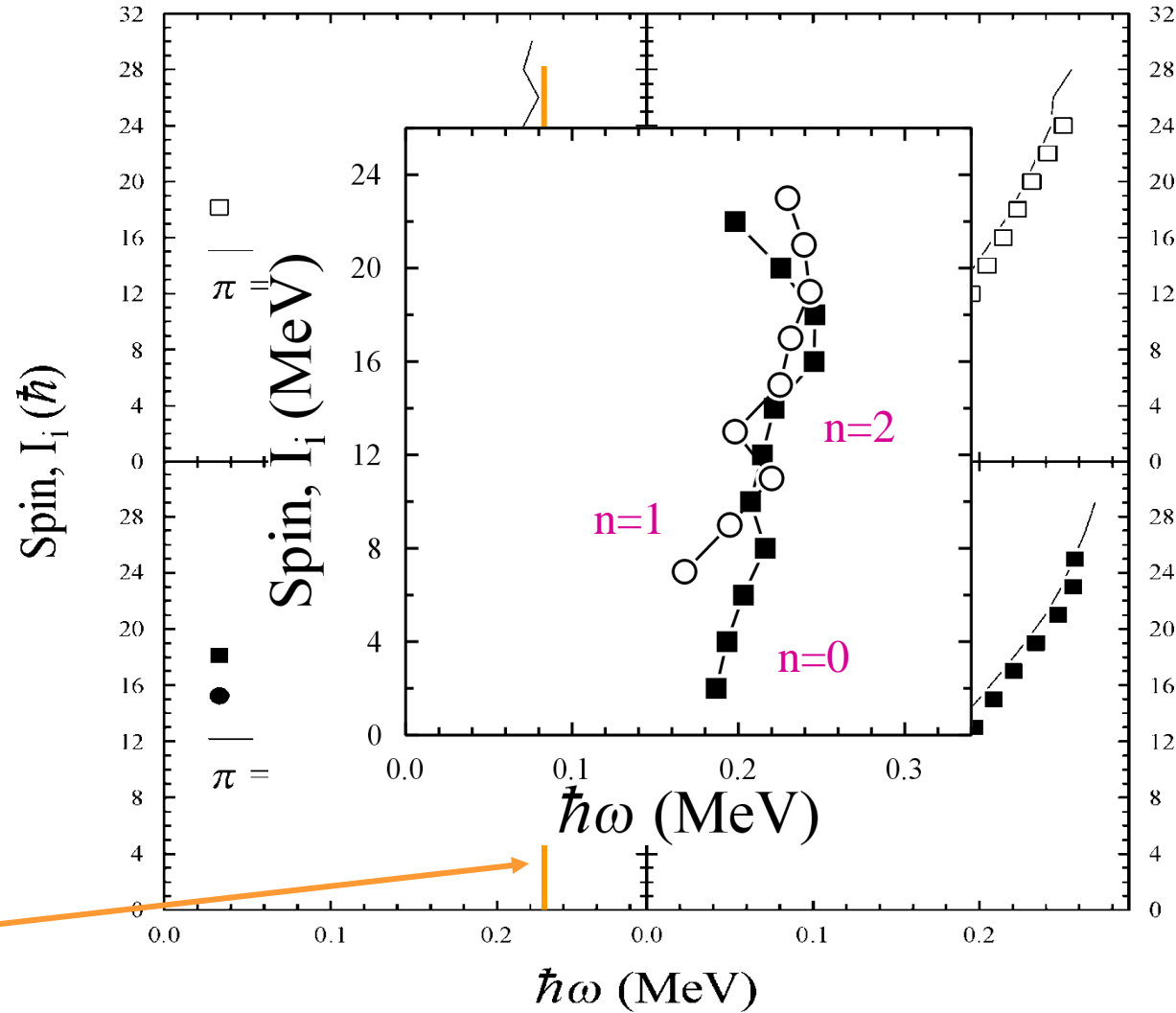


Superposition of two surface waves with
 $\omega_2 = 1/2 E_\gamma$ and $\omega_3 = 1/3 \Delta E_{\Delta I=3}$

$\hbar\omega_c = 0.21$ MeV
(constant ω)

$N=130$

$N=132$

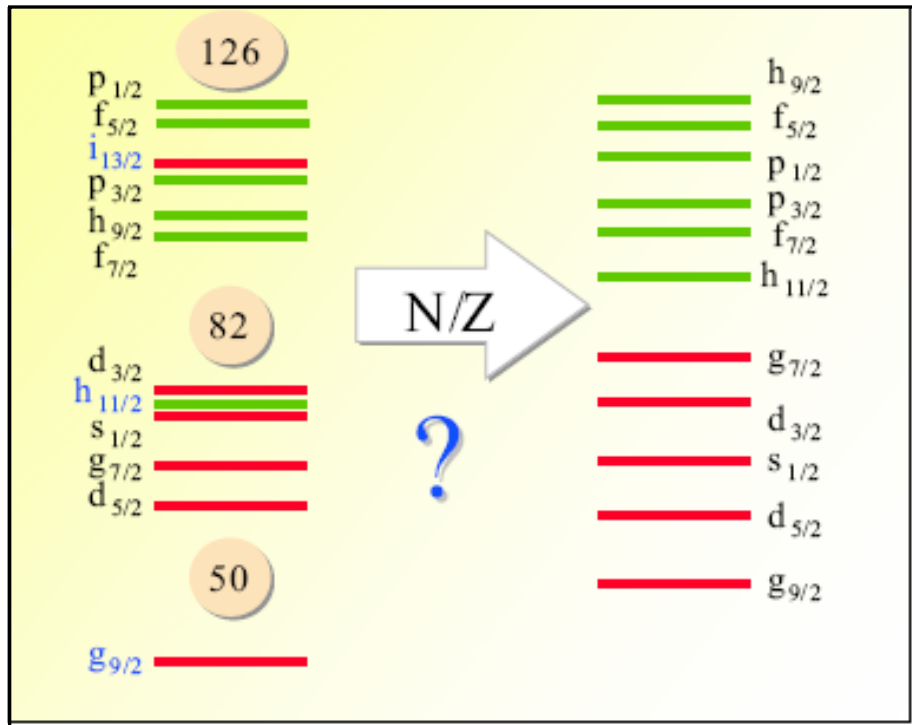


High Spinners Can Study Neutron Rich Nuclei Too!



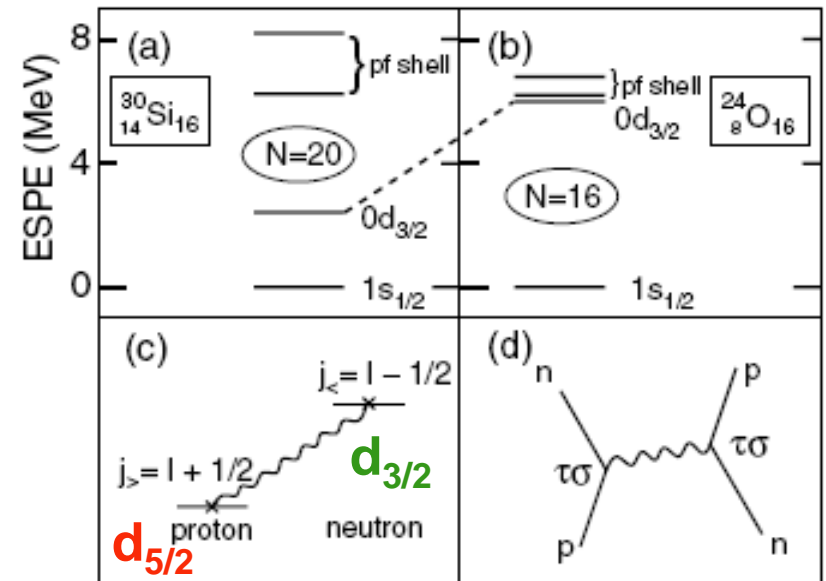
Modification or Disappearance of Shell Gaps

T. Otsuka et al., Phys. Rev. Lett. 87
(2001), 082502.



known

predicted

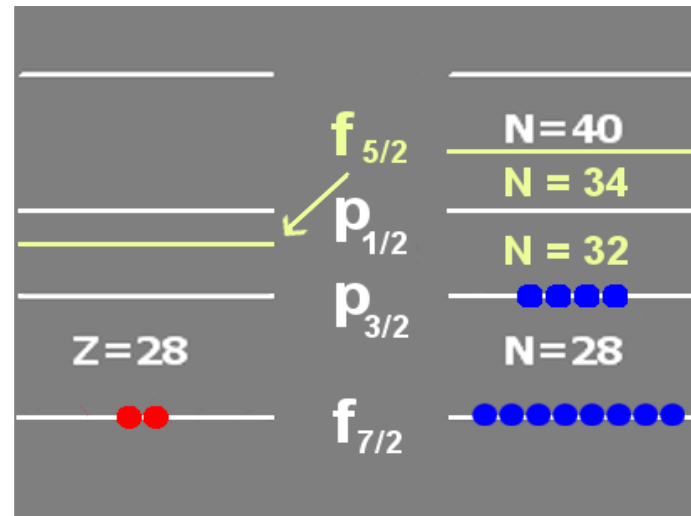


$$V_{\tau\sigma} = \tau \cdot \tau\sigma \cdot \sigma f_{\tau\sigma}(r).$$

Explains why $^{24}\text{O}_{16}$ is heaviest bound oxygen isotope and not $^{28}\text{O}_{20}$

Explains why $^{32}\text{Mg}_{20}$ is deformed and not spherical.

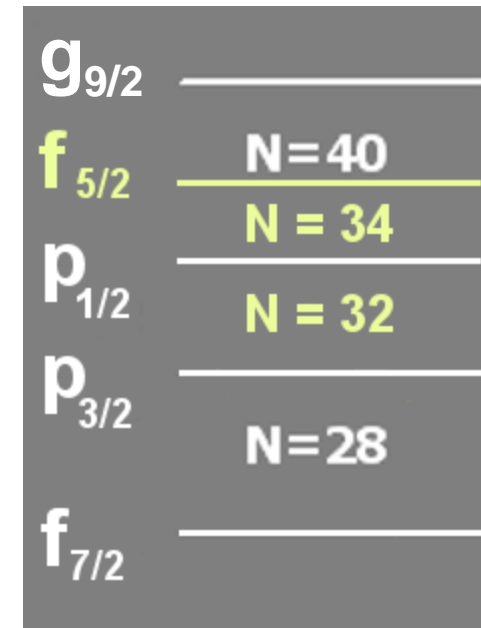
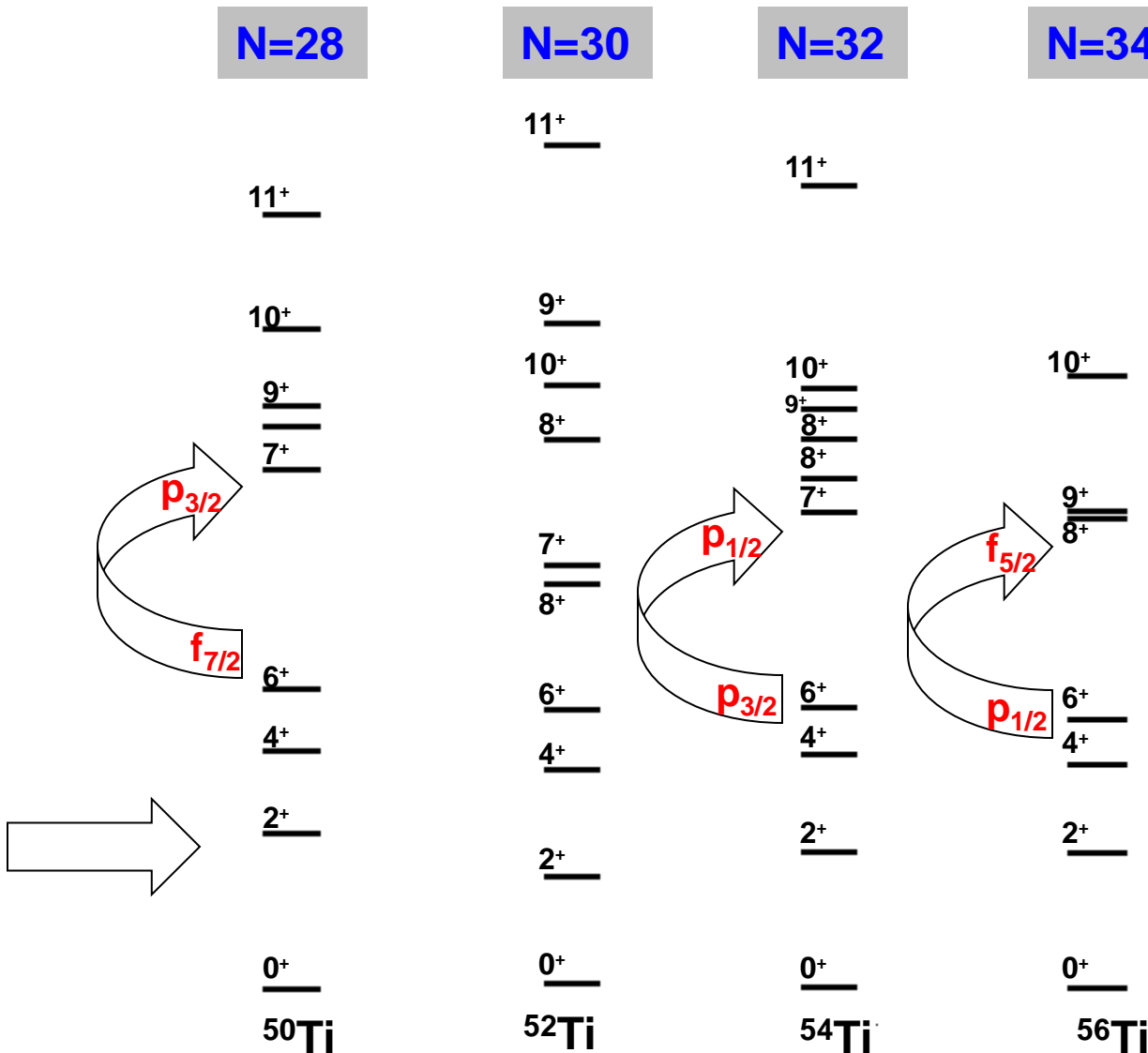
Do New Shell Gaps Develop in the f-p Shell?



Removal of protons from $f_{7/2}$ shell weakens the $\pi f_{7/2}-\nu f_{5/2}$ monopole interaction strength, resulting in the $\nu f_{5/2}$ orbital pushing up in energy.

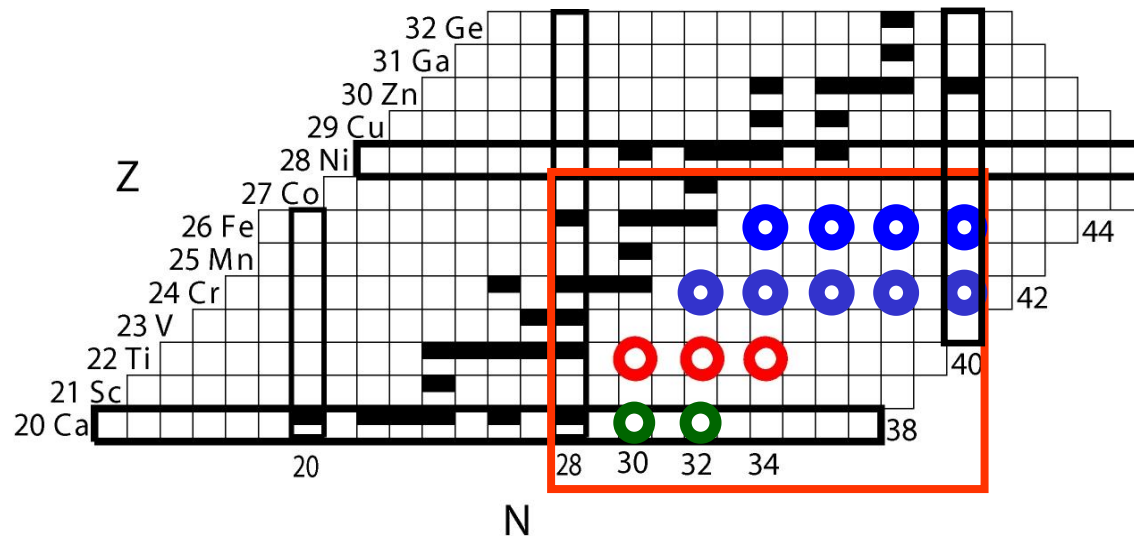
Opens possibility for shell gaps at $N = 32, 34$.

Shell Model Predictions using GXPF1 Interaction



Studies of Ca-Ni Neutron Rich Isotopes:

- Collaboration began 2001 between ANL, NSCL, Krakow, Manchester, Maryland
- Data obtained at several different facilities (NSCL and ATLAS) utilizing different techniques to excite the nucleus and measure the γ decay:

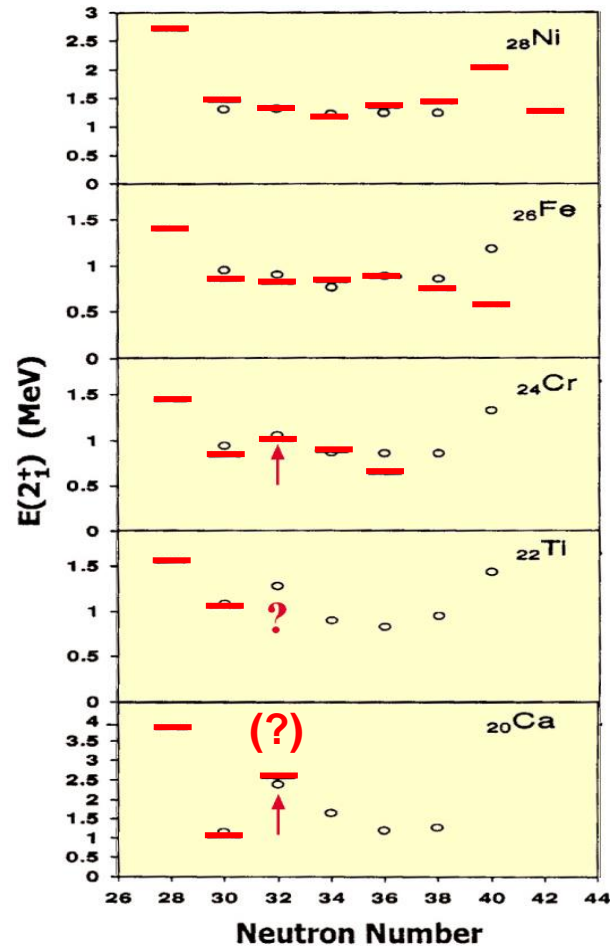


What is the evidence of new shell gaps at $N=32$ and 34 for $Z<28$.

How robust is the $N=40$ gap for $Z<28$?

Experiment Evidence for N=32 Gap (circa 2001)

J.I. Prisciandaro *et al.*, PLB **501**, 17 (2001)



First Results on neutron rich ^{54}Ti (N=32):

R.V.F. Janssens *et al.*, PLB 546, 22 (2002)

Before this investigation, very little known about ^{54}Ti .

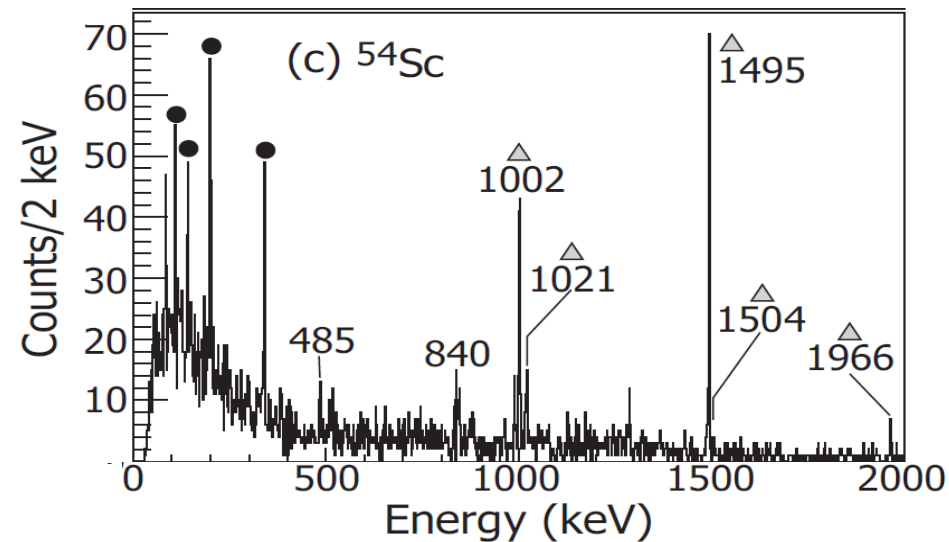
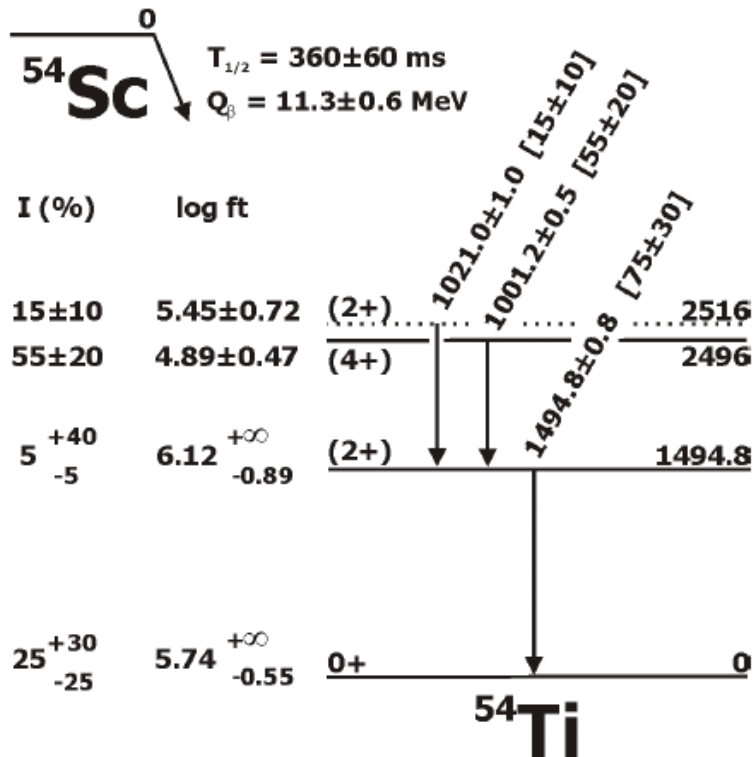
Two experiments undertaken to study properties of ^{54}Ti .

Beta decay of ^{54}Sc at NSCL *production of ^{54}Sc from fragmentation of a ^{86}Kr beam*

In-beam spectroscopy with Gammasphere utilizing the reaction $^{48}\text{Ca} + ^{208}\text{Pb}$ *production of ^{54}Ti via a deep inelastic reaction instead of fusion-evaporation*

^{54}Sc b-Decay Results (NSCL)

Production rate: $0.5 \text{ }^{54}\text{Sc/s}$



H.L. Crawford *et al.*,

Phys. Rev. C 82 (2010) 014311



Deep-inelastic data: Quest for ^{54}Ti

^{48}Ca (305 MeV) + ^{208}Pb (thick)
ATLAS + GAMMASPHERE
 at Argonne

	At 204 9.2 m	At 205 26.2 m	At 206 29.4 m	At 207 1.8 h	At 208 1.63 h	At 209 5.4 h	At 210 8.3 h	At 211 7.22 h	At 212 119 ms	At 213 0.11 μs	At 214 121 μs	At 215 0.1 ms
Po	Po 203 46 s	Po 204 3.53 h	Po 205 1.66 h	Po 206 8.6 d	Po 207 2.8 s	Po 208 2.998 a	Po 209 102 a	Po 210 138.38 d	Po 211 32.5 s	Po 212 0.3 μs	Po 213 4.2 μs	Po 214 164 μs
Pb	Bi 202 1.72 h	Bi 203 11.76 h	Bi 204 11.22 h	Bi 205 15.31 d	Bi 206 6.24 d	Bi 207 31.55 a	Bi 208 3.68 $\cdot 10^5$ a	Bi 209 $> 10^9$ a	Bi 210 5.019 a	Bi 211 2.17 m	Bi 212 60.55 m	Bi 213 45.59 m
Hg	Pb 201 26.1 h	Pb 202 73.1 h	Pb 203 12.23 d	Pb 204 29.524 a	Pb 205 1.5 $\cdot 10^7$ a	Pb 206 24.1 a	Pb 207 22.1 a	Pb 208 52.4 a	Pb 209 3.253 h	Pb 210 22.3 a	Pb 211 36.1 m	Pb 212 10.64 h
Pt	Tl 200 2.61 h	Tl 201 73.1 h	Tl 202 12.23 d	Tl 203 29.524 a	Tl 204 3.78 a	Tl 205 70.476 a	Tl 206 4.37 m	Tl 207 3.05 m	Tl 208 3.05 m	Tl 209 2.16 m	Tl 210 1.30 m	Tl 211 1.30 m
	Hg 199 42.8 m	Hg 200 23.10	Hg 201 7.2	Hg 202 29.86	Hg 203 46.59 d	Hg 204 6.87	Hg 205 5.2 m	Hg 206 8.15 m	Hg 207 2.9 m	Hg 208 42 m	Hg 209 35 s	Hg 210
	Au 198 2.30 d	Au 199 3.139 d	Au 200 18.7 h	Au 201 26.4 m	Au 202 28 s	Au 203 60 s	Au 204 39.8 s	Au 205 31 s				
	Pt 197 94.4 m	Pt 198 7.2	Pt 199 13.6 s	Pt 200 12.5 h	Pt 201 2.5 m	Pt 202 ~ 43.6 h						



Cr	Cr 48 21.6 h	Cr 49 42 m	Cr 50 4.345	Cr 51 27.70 d	Cr 52 83.789	Cr 53 9.501	Cr 54 2.365	Cr 55 3.50 m	Cr 56 5.9 m	Cr 57 21.1 s	Cr 58 7.0 s	Cr 59 0.46 s
Ti	Ti 46 8.0	Ti 47 7.3	Ti 48 73.8	Ti 49 5.5	Ti 50 5.4	Ti 51 5.8 m	Ti 52 1.7 m	Ti 53 32.7	Ti 54 1.5 s	Ti 55 0.60 s	Ti 56 0.15 s	Ti 57 56 ms
Ca	Ca 44 2.096	Ca 45 163 d	Ca 46 0.004	Ca 47 4.54 d	Ca 48 0.187	Ca 49 8.72 m	Ca 50 13.9 s	Ca 51 10.0 s	Ca 52 4.6 s	Ca 53 90 ms		
Ar	K 43 22.2 h	K 44 17.8 m	K 45 17.8 m	K 46 17.5 s	K 47 17.5 s	K 48 17.5 s	K 49 1.26 s	K 50 472 ms	K 51 365 ms	K 52 105 ms	K 53 30 ms	K 54 10 ms
	Ar 42 33 a	Ar 43 11.87 m	Ar 44 21.5 s	Ar 45 7.8 s	Ar 46 7.8 s	Ar 47 700 ms	Ar 48 700 ms	Ar 49 700 ms	Ar 50 ?	Ar 51 ?		

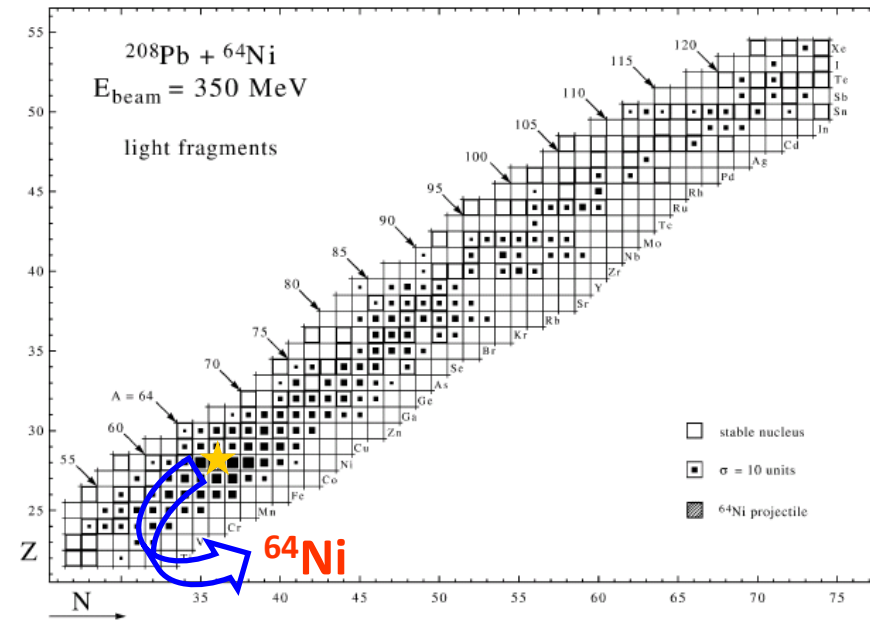
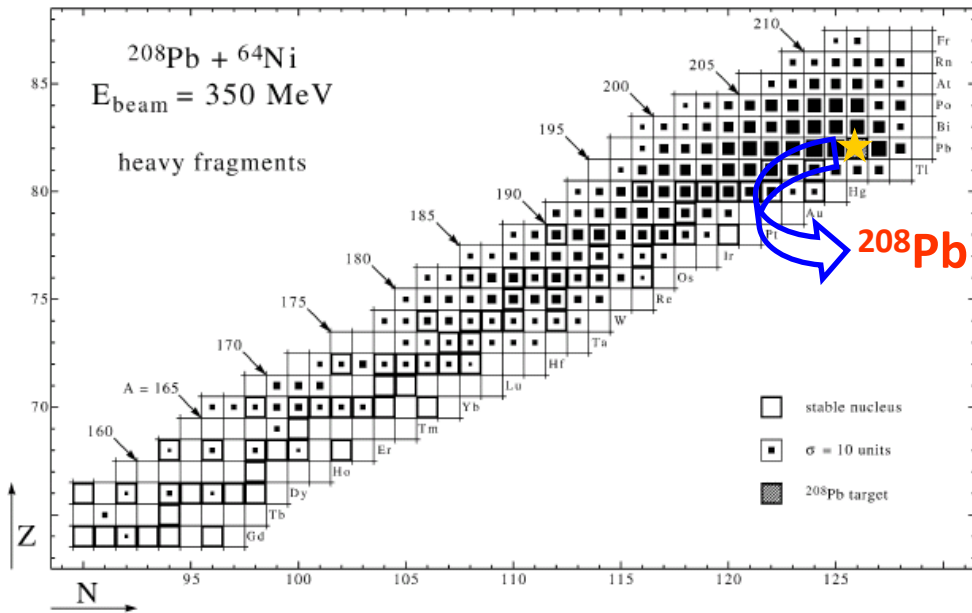


N/Z equilibration line

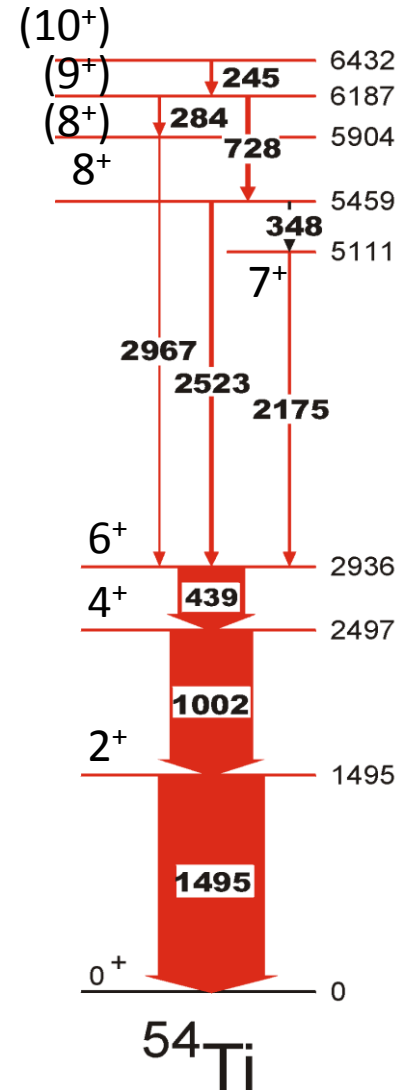
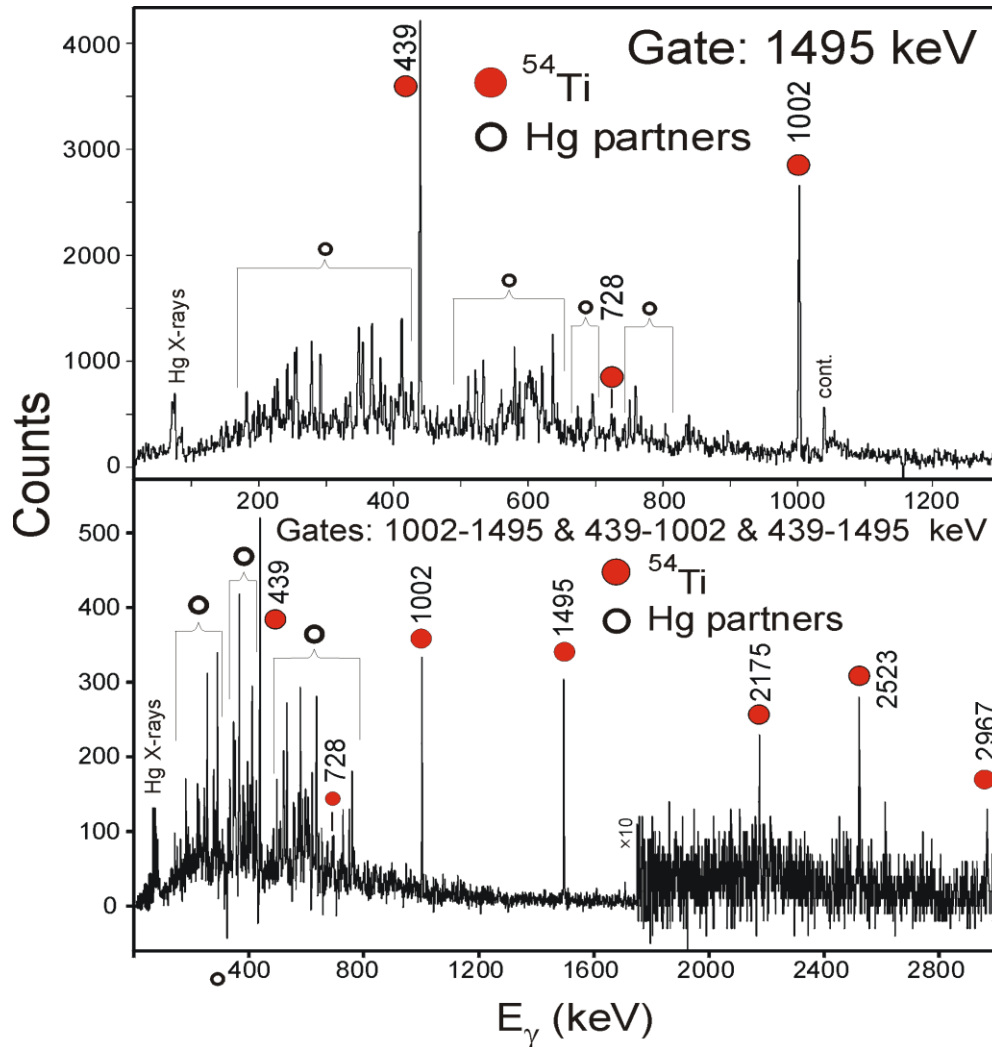


Identified Products from $^{208}\text{Pb} + ^{64}\text{Ni}$ @ 350 MeV

W. Królas, R. Broda, B. Fornal, T. Pawlat, H. Grawe, K.H. Maier M. Schramm, R. Schubart, Nucl. Phys. **A724** (2003) 289.



^{54}Ti results from $^{48}\text{Ca} + ^{208}\text{Pb}$ deep inelastic reaction measured with Gammasphere

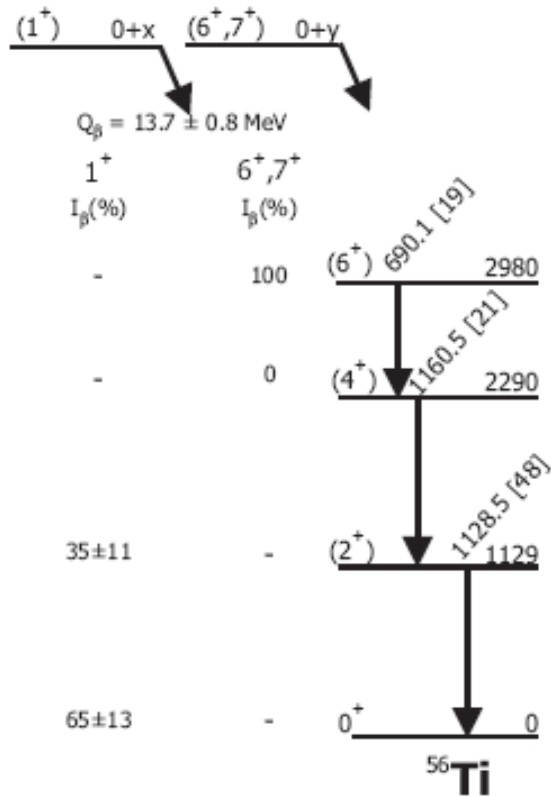


R.V.F. Janssens *et al.*, PLB 546, 22 (2002)

Similar set of experiments on ^{56}Ti

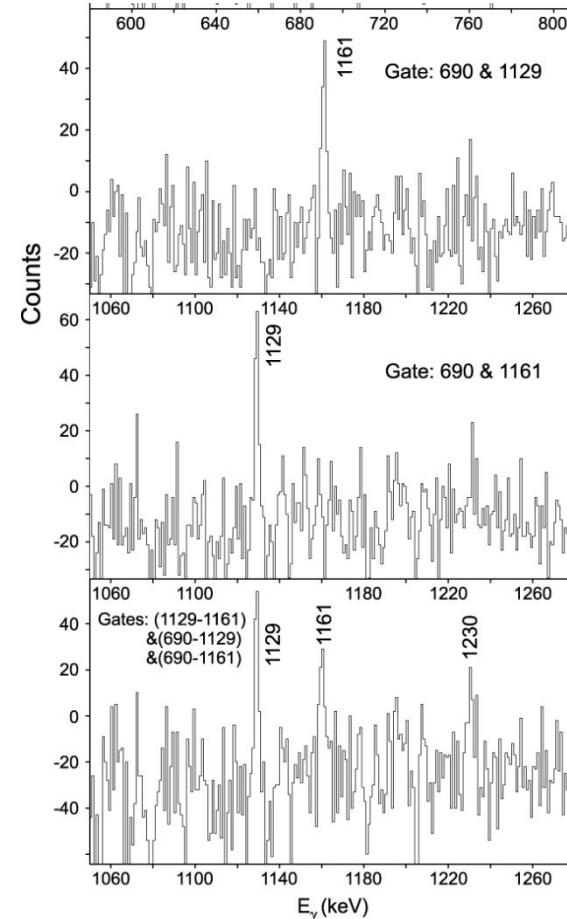
^{56}Sc decay at NSCL with SeGa

$T_{1/2} = 35 \pm 5 \text{ ms}$ $T_{1/2} = 60 \pm 7 \text{ ms}$



S. Liddick *et al.*, PRC 70, 064303 (2004)

$^{48}\text{Ca} + ^{238}\text{U}$ @ ATLAS with Gammasphere



B. Fornal *et al.*, PR.C 70, 064304 (2004)

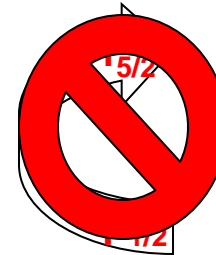
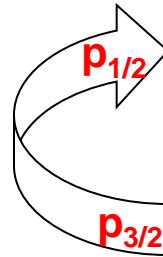
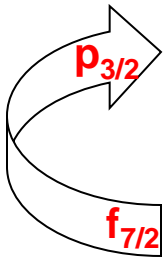


The Ti story: N=32 shell gap, N=34 no gap.

28

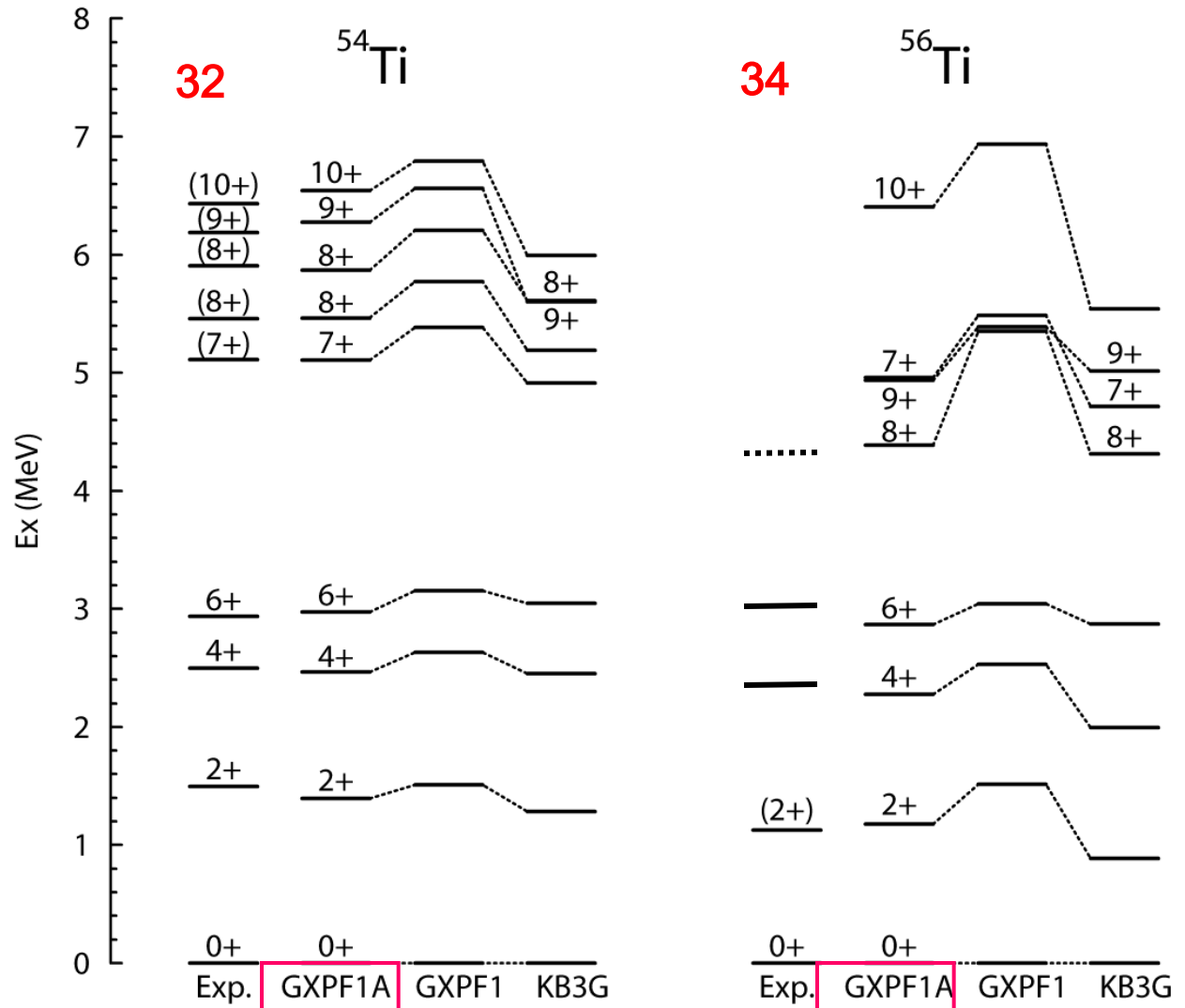
32

34

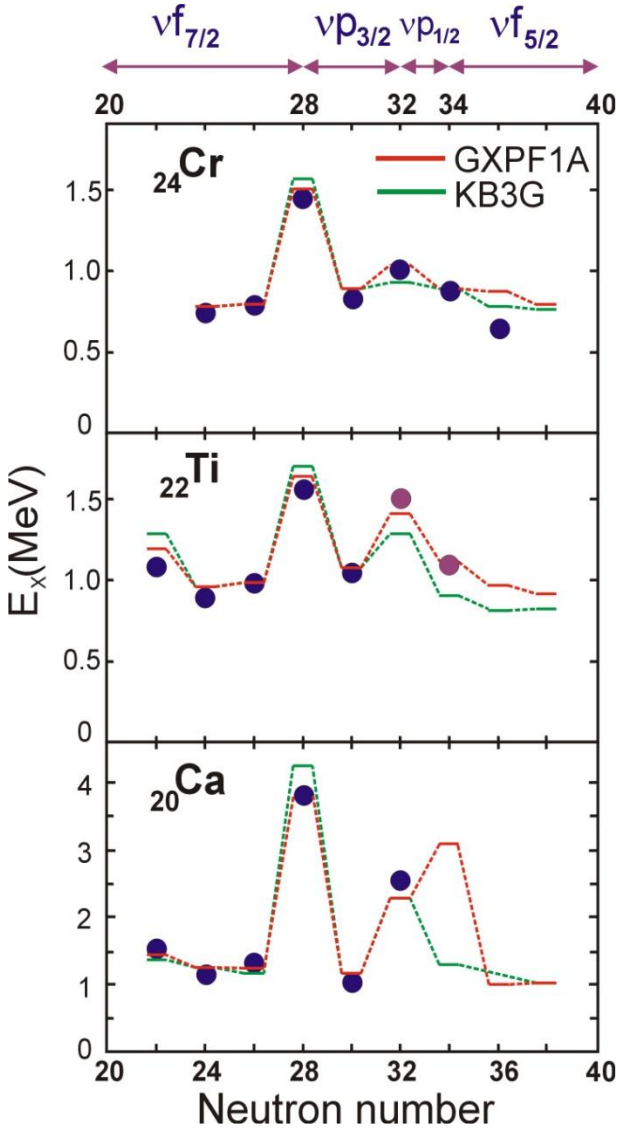


Theory Development: GXPF1A

GXPF1A vs GXPF1:
T=1 matrix elements
involving $\nu p_{1/2}$ and $\nu f_{5/2}$
modified
→
 $(\nu p_{1/2} - \nu f_{5/2})$ gap
reduced by ~ 0.5 MeV



Is there a $N = 34$ gap for ^{54}Ca between $f_{5/2}$ and $p_{3/2}$?

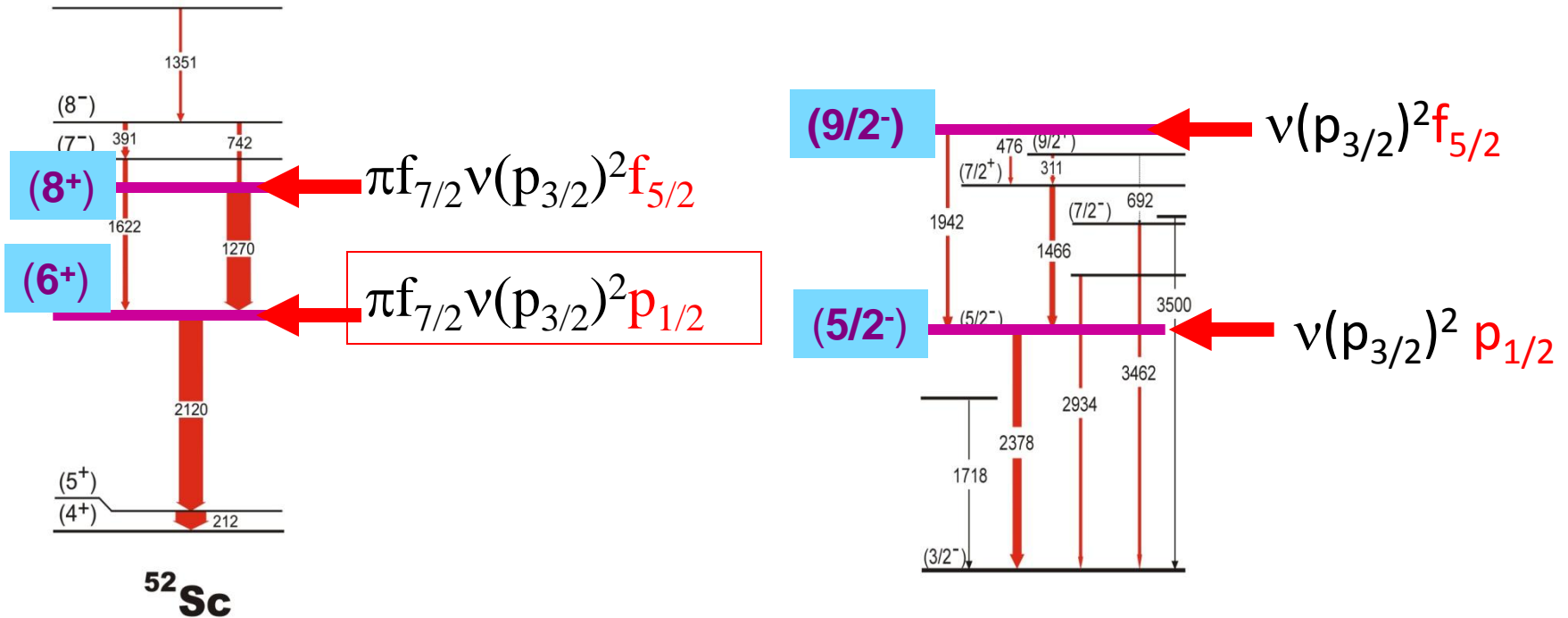


- No evidence of shell gap at $N=34$ for Cr or Ti isotopes.
- Shell model calculations using GXPF1A predict sizeable shell gap for ^{54}Ca ($N=34$).
- Shell model calculations using KB3G interaction predict no neutron shell gap for ^{54}Ca .
- No experimental data available on ^{54}Ca excited states



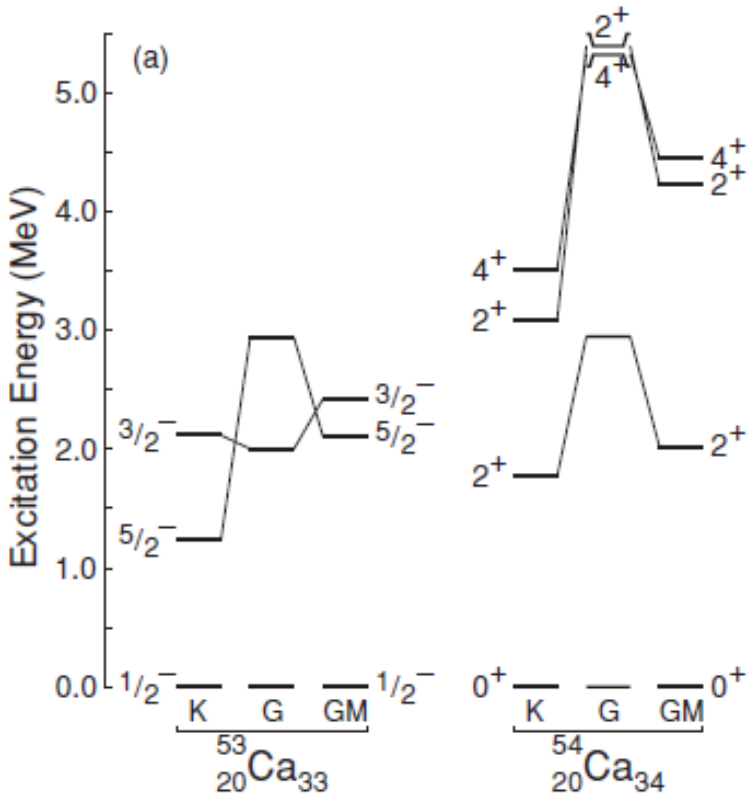
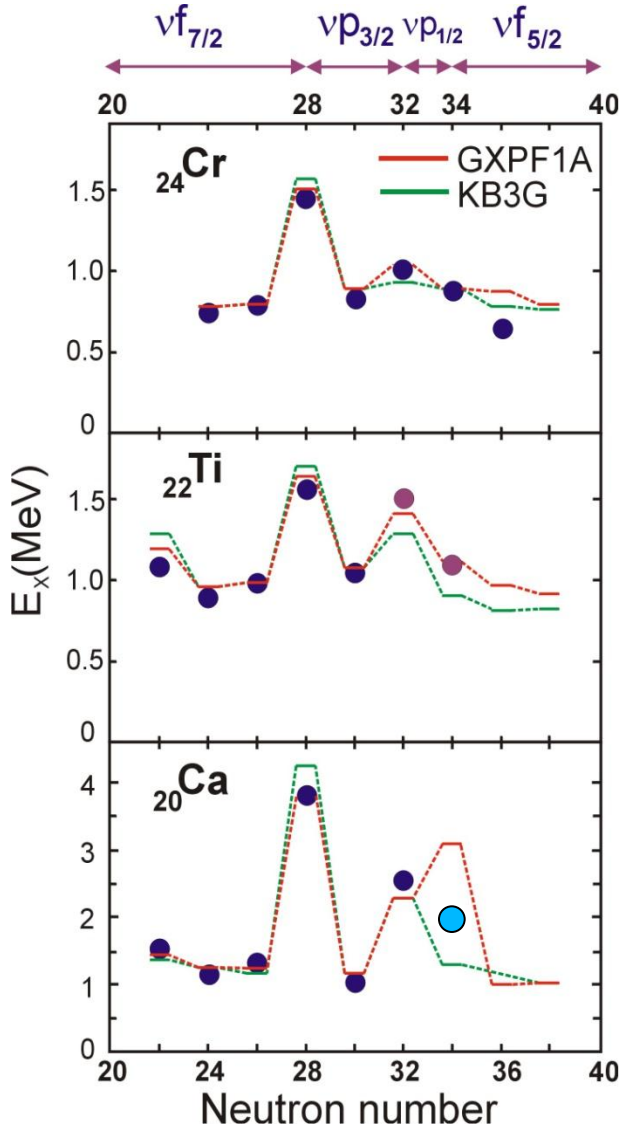
Is there a $N = 34$ gap for ^{54}Ca between $f_{5/2}$ and $p_{3/2}$

B. Fornal *et al.*, Phys. Rev. C 77, 014304 (2008)



See also M. Rejmund *et al.*, Phys. Rev. C **76** (2007) 021304(R)

Is there a $N = 34$ gap for ^{54}Ca between $f_{5/2}$ and $p_{3/2}$?



K = KB3GM G = GXPF1A GM = modified GXPF1A

M. Rejmund *et al.*, Phys. Rev. C **76** (2007) 021304(R)

**Thank You For Your Attention
and
Good Luck With You Thesis Work**

