



How the Nucleus of Human Cells is Structured by Entropy

Dieter W. Heermann

Heidelberg University

Key Problem



Derive a **chromosome model** that works across species, across phases, hence that is able to capture the underlying principles of chromosome folding.

Can explain data from various sources simultaneously.

Can predict biological as well as mechanical properties.

Key Problem



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386

Human chromosomes (interphase
and metaphase)

Escherichia coli

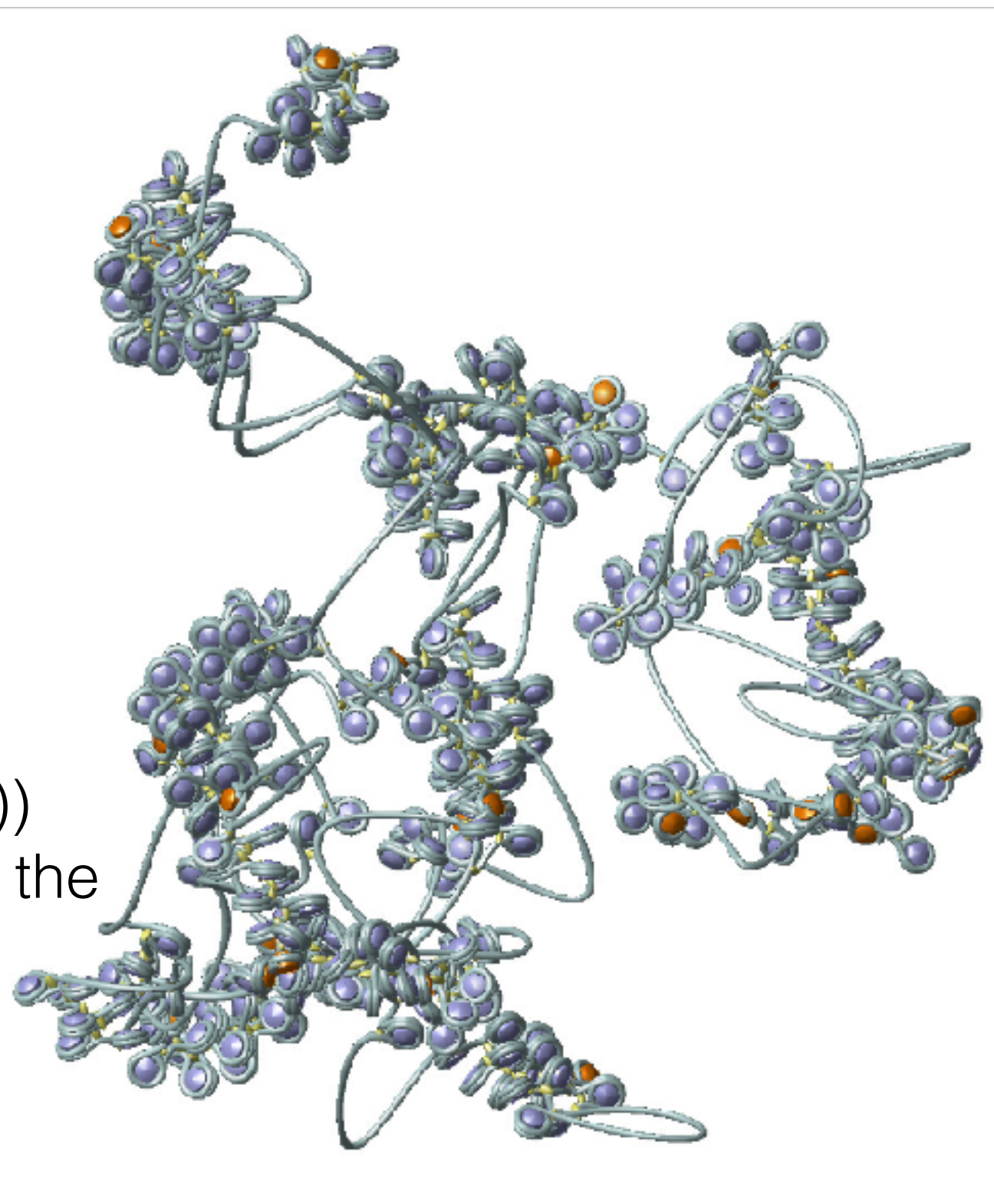
Yeast

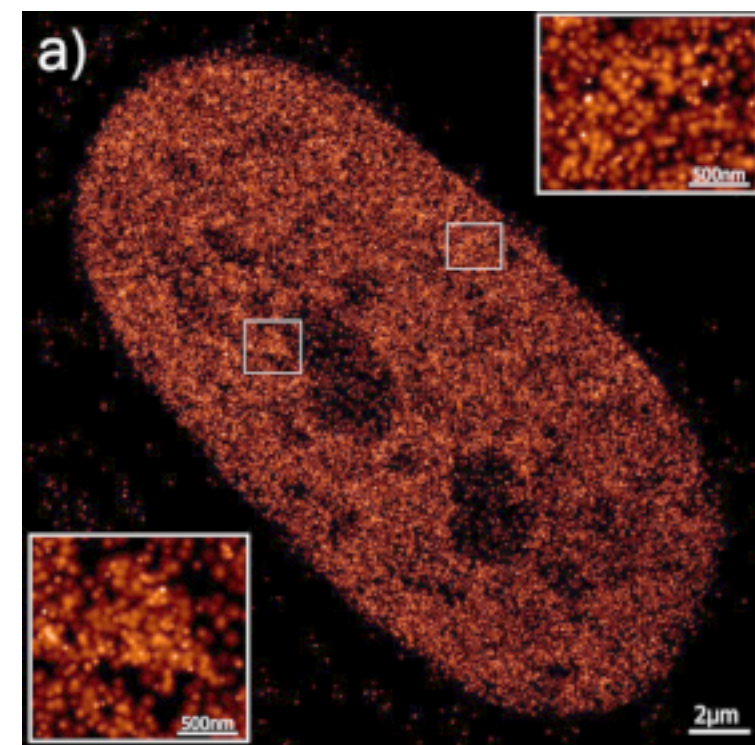
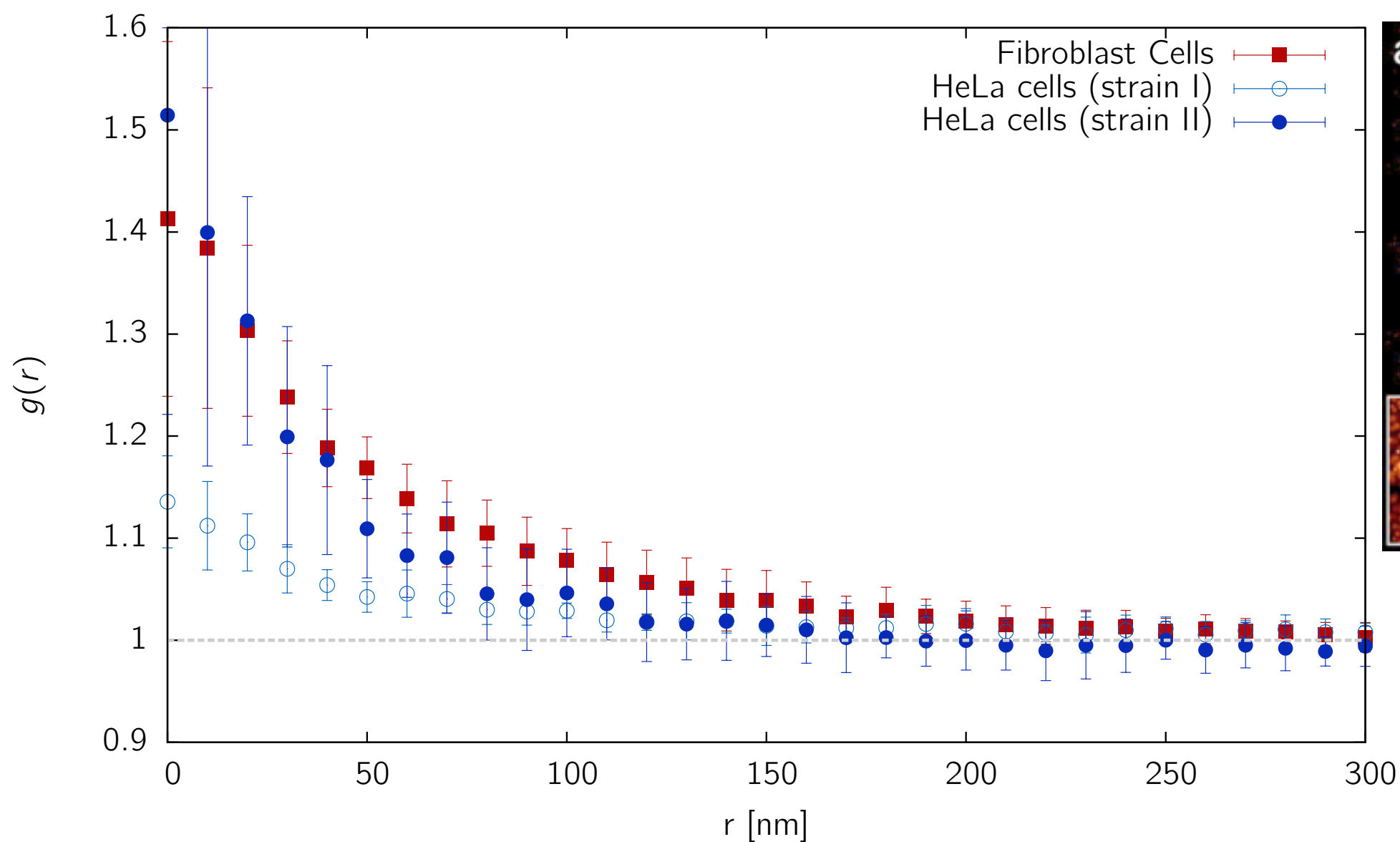


How can we obtain information on
the structure?



Label (for example
fluorescence in situ
hybridization (FISH))
specific sites along the
chromosome.



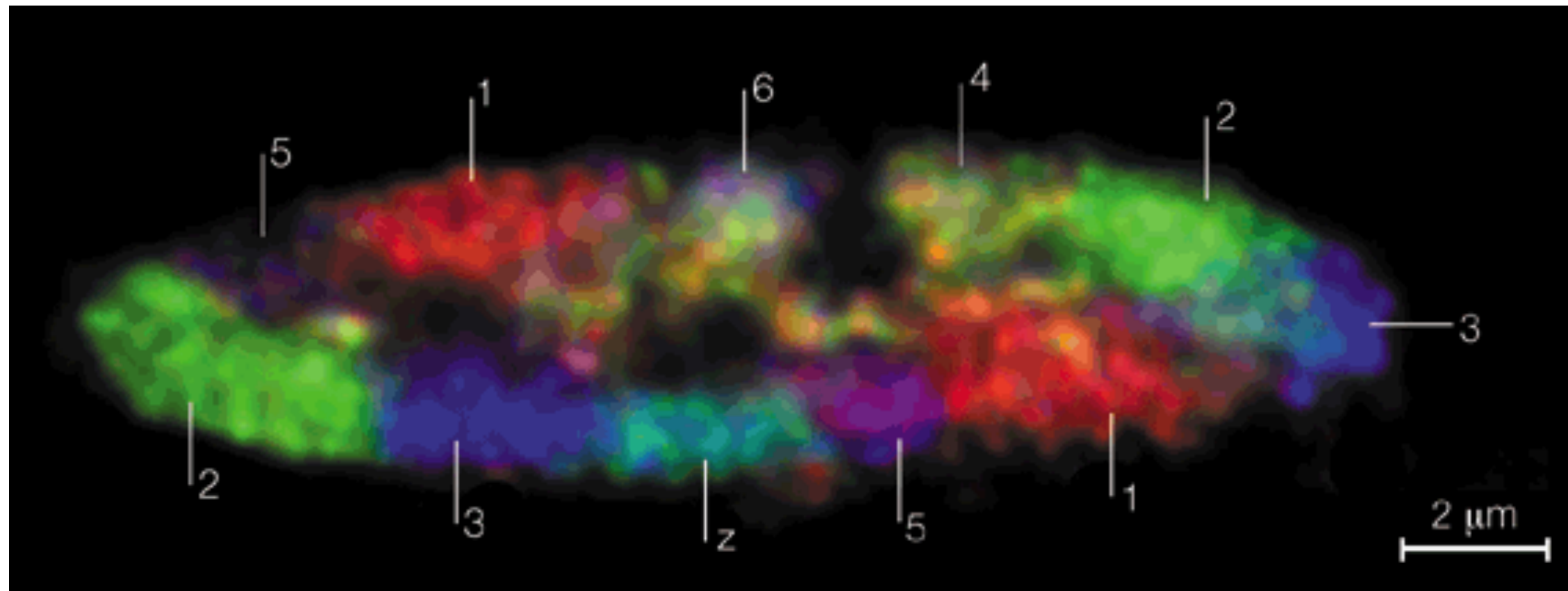


Localization microscopy reveals expression-dependent parameters of chromatin nanostructures

Manfred Bohn, Philipp Diesinger, Rainer Kaufmann, Yanina Weiland, Patrick Müller, Manuel Gunkel, Alexa von Ketteler, Paul Lemmer, Michael Hausmann, Dieter W. Heermann and Christoph Cremer

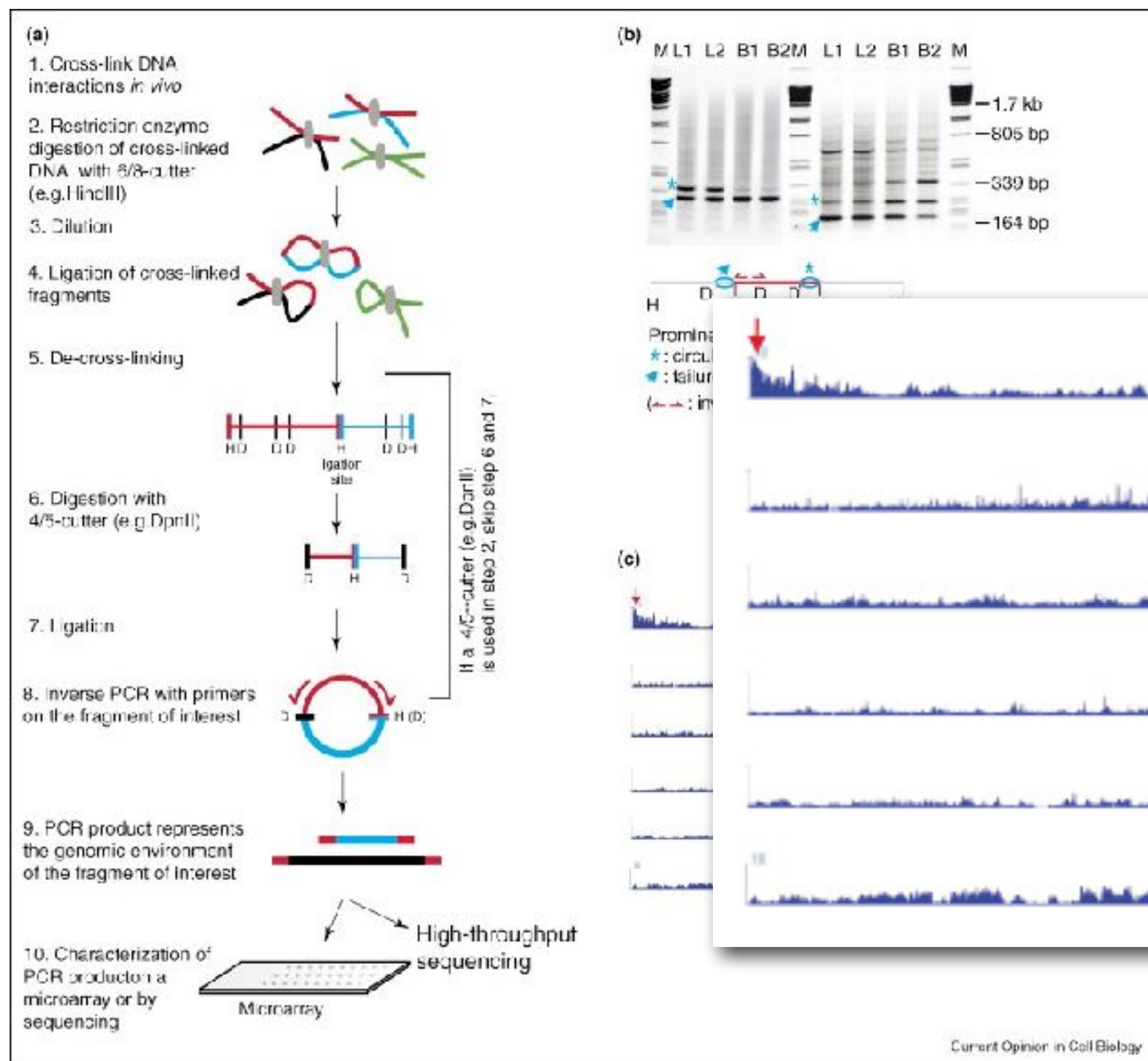
Biophysical Journal, Volume 99, Issue 5, 1358-1367, 8 September 2010

Staining of the entire chromosome

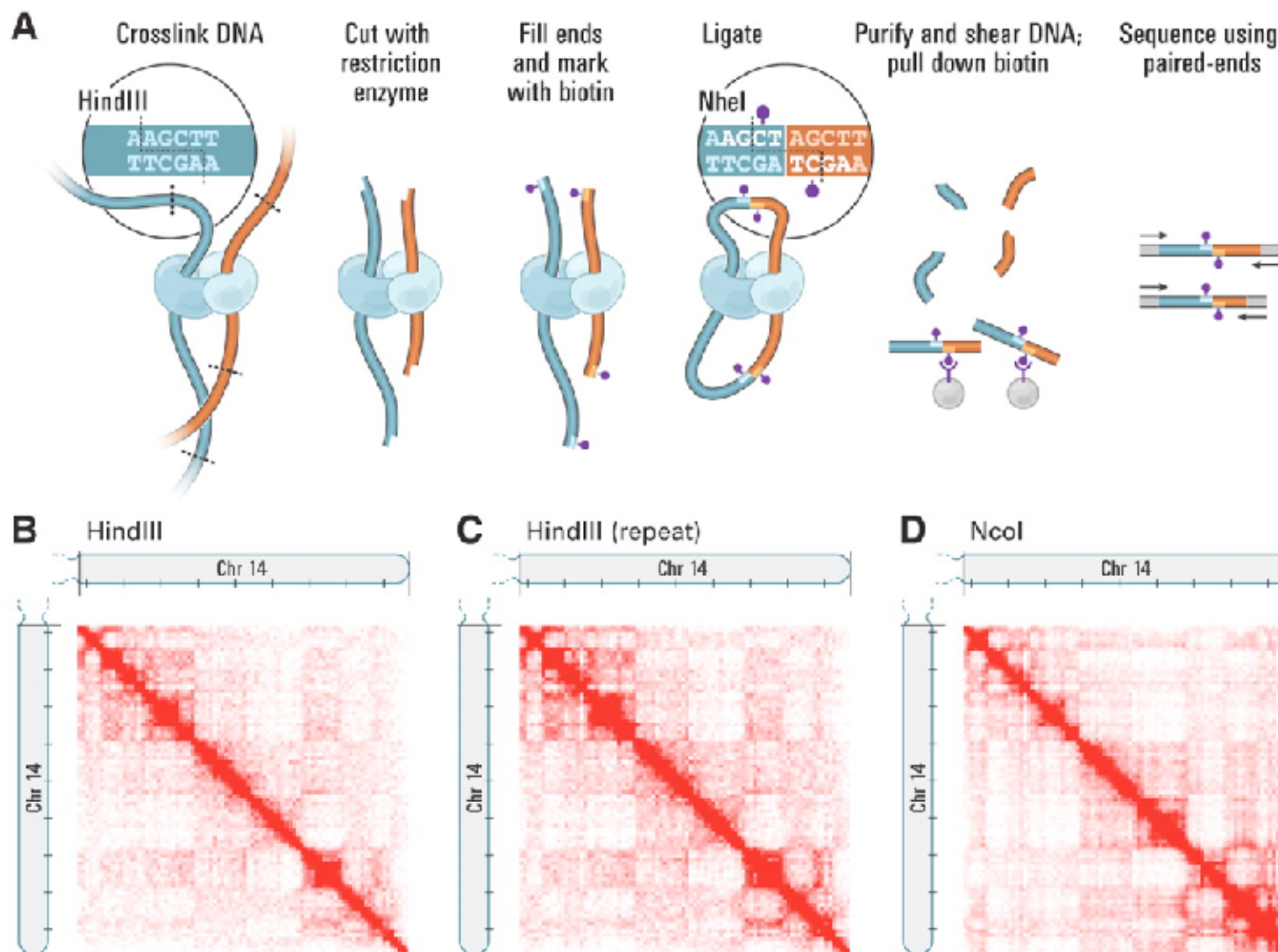


Chromosome Territories

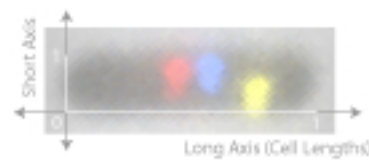
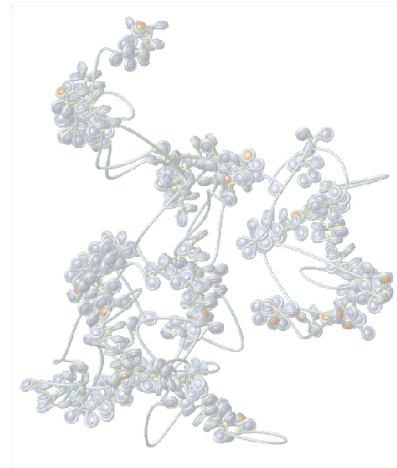
T.Cremer and C. Cremer, Nature Reviews Genetics vol. 2, no. 4, pp. 292-301 (April, 2001)



W. de Laat, Current Opinion in Cell Biology 2007, 19:317–320

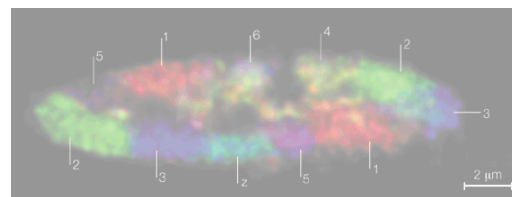
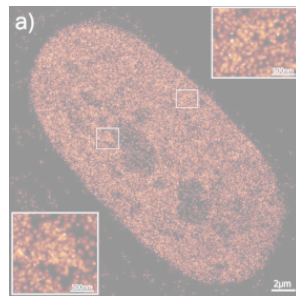


Comprehensive Mapping of Long-Range Interactions Reveals Folding Principles of the Human Genome
E. Lieberman-Aiden et. al., Science 2010



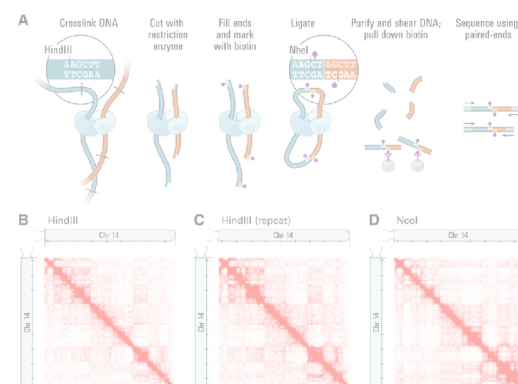
Spatial Information

Measure two, few or many physical positions



Topological Information

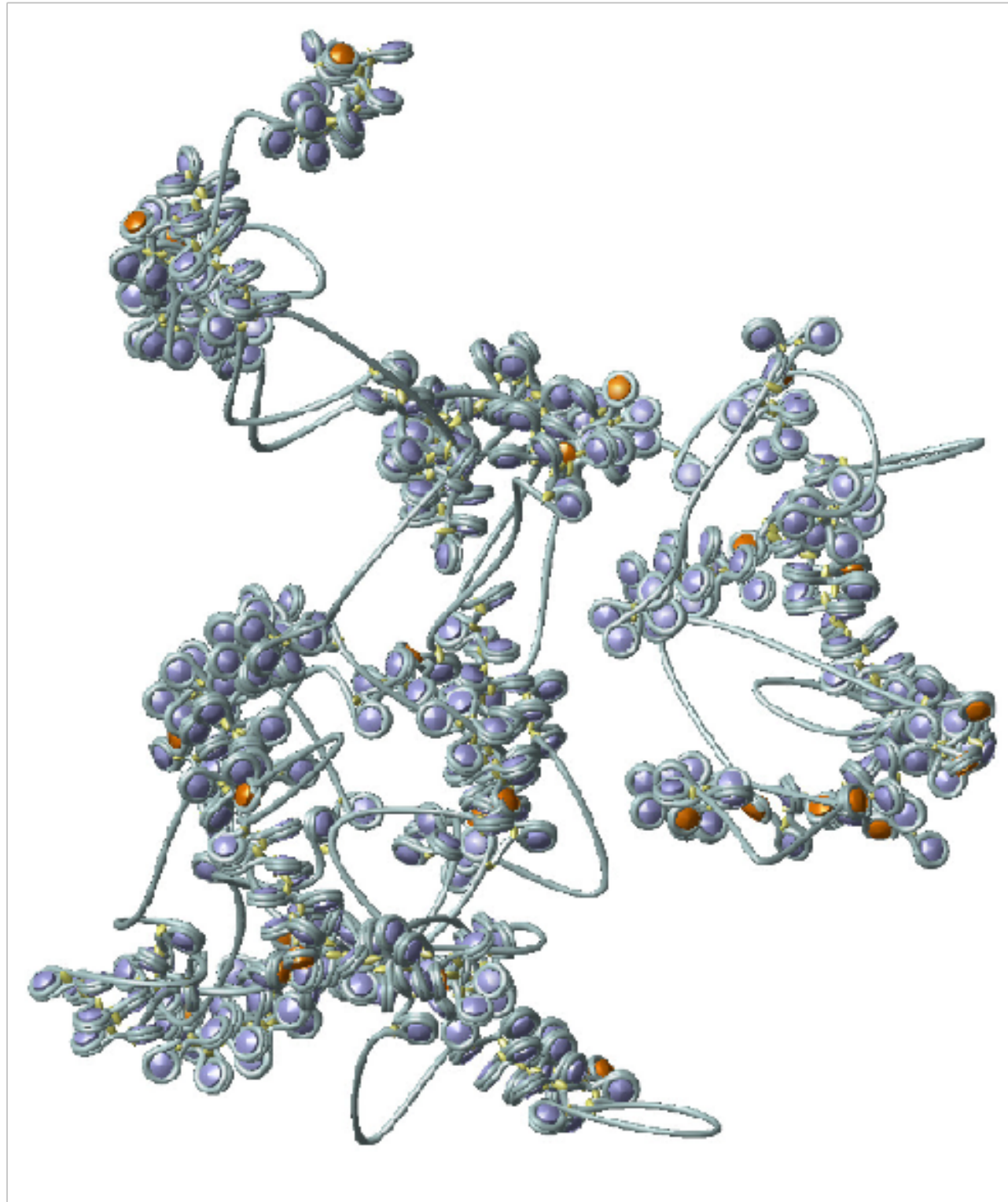
Measure contacts without spatial information



The Model



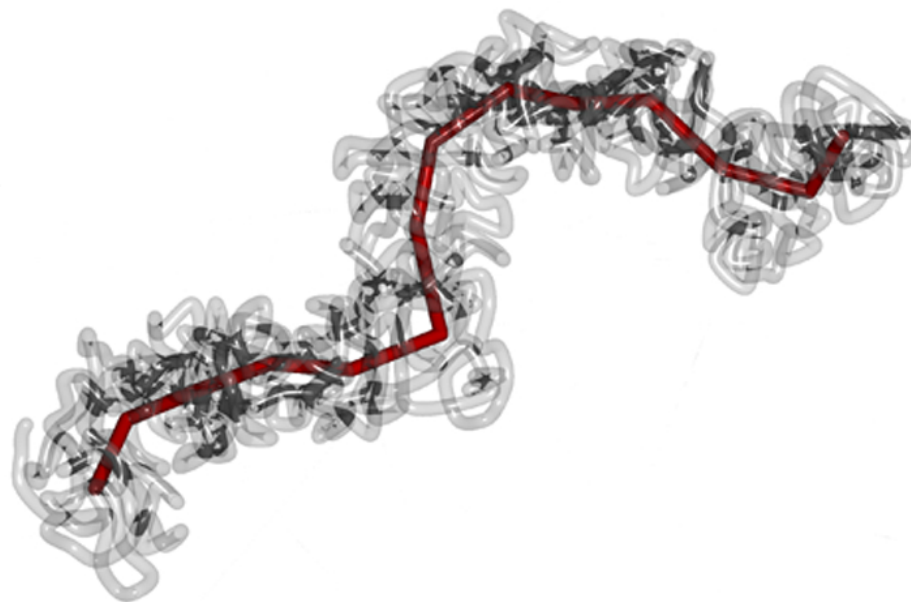
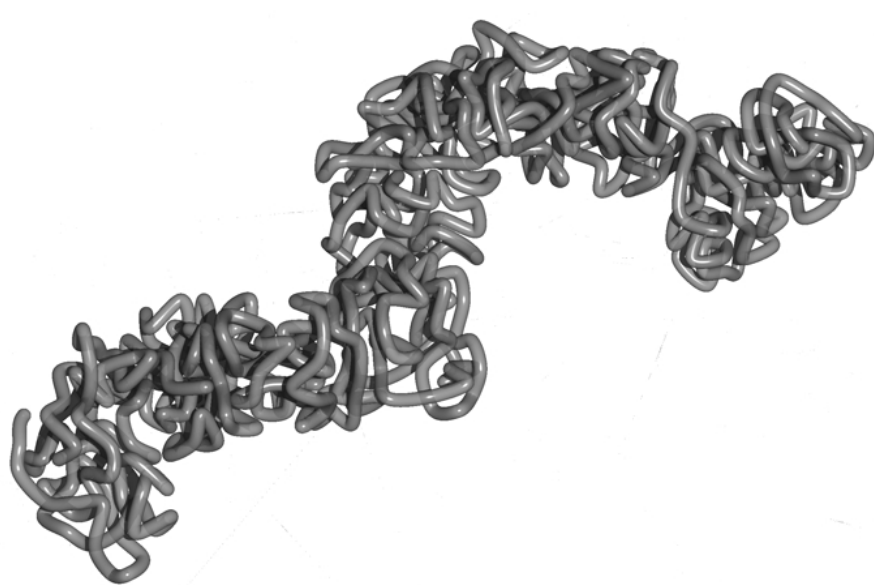
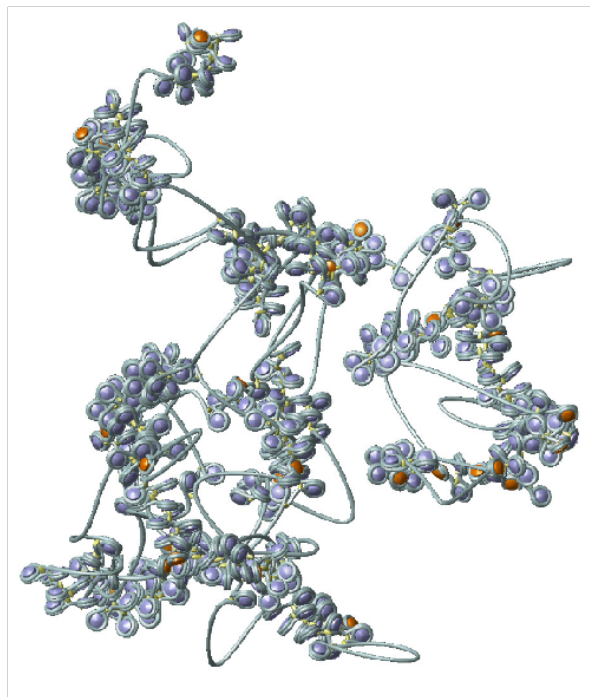
UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



The Model

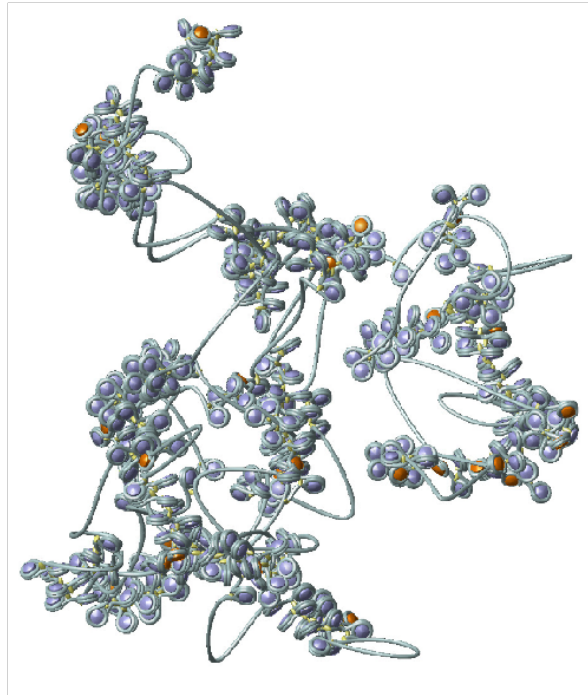


UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



coarse grained description

The Model



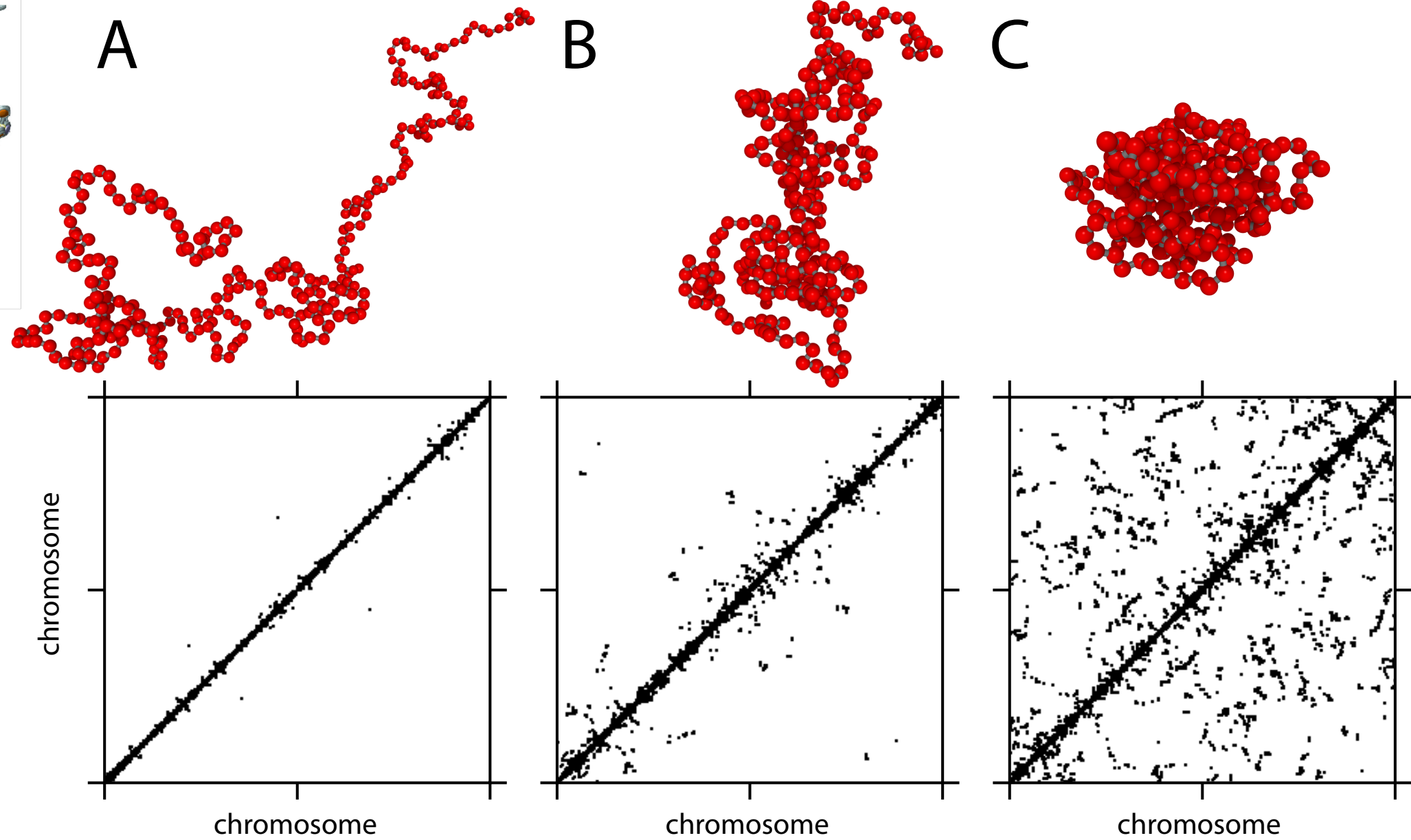
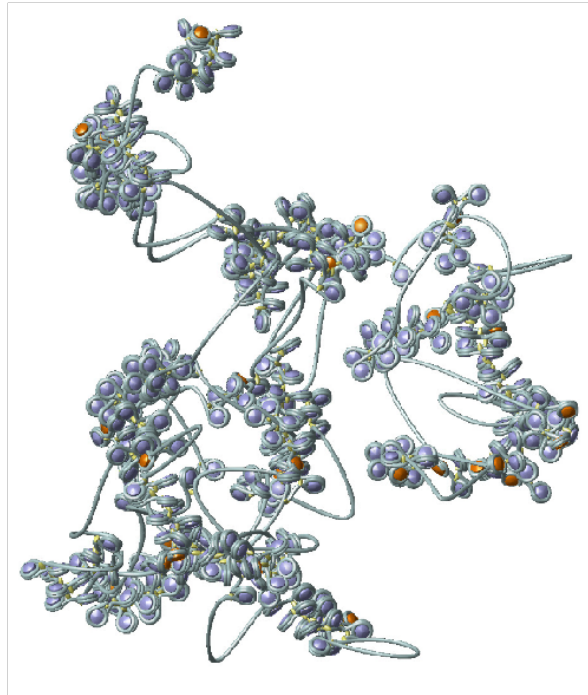
Basic assumptions:

The backbone of the chain is given by a simple self-avoiding walk.

The Model

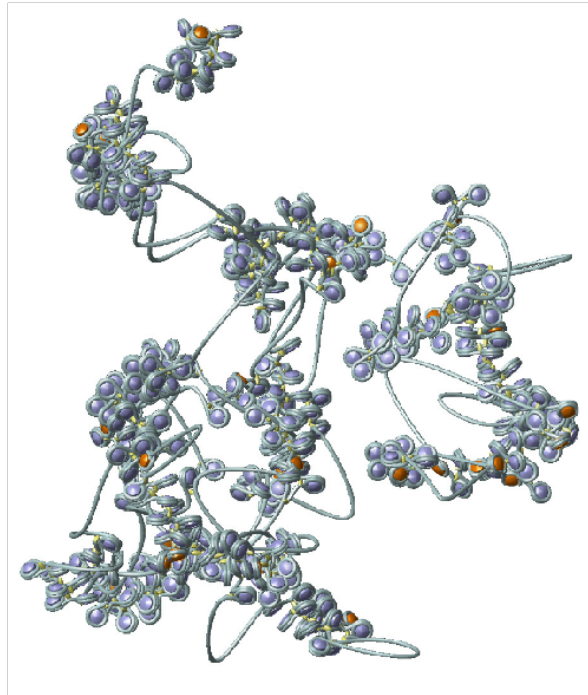


UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



The effect of loops on the conformation

The Model

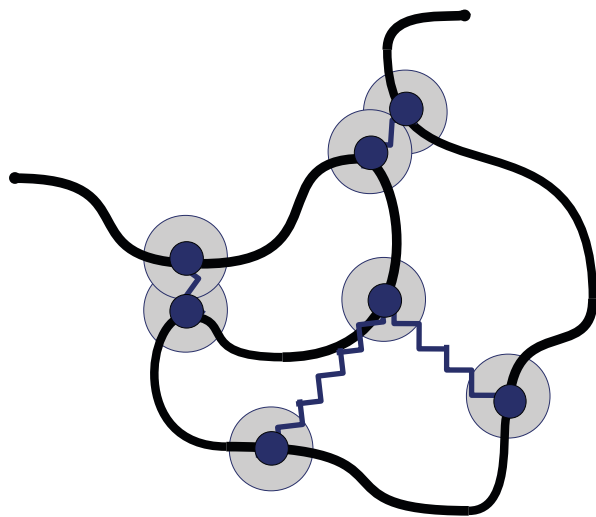


Basic assumptions:

The backbone of the chain is given by a simple self-avoiding walk.

Two parts of the polymer form loops with a certain probability.

Loops are not static but can change in the course of time; their size and position are chosen from a broad range.

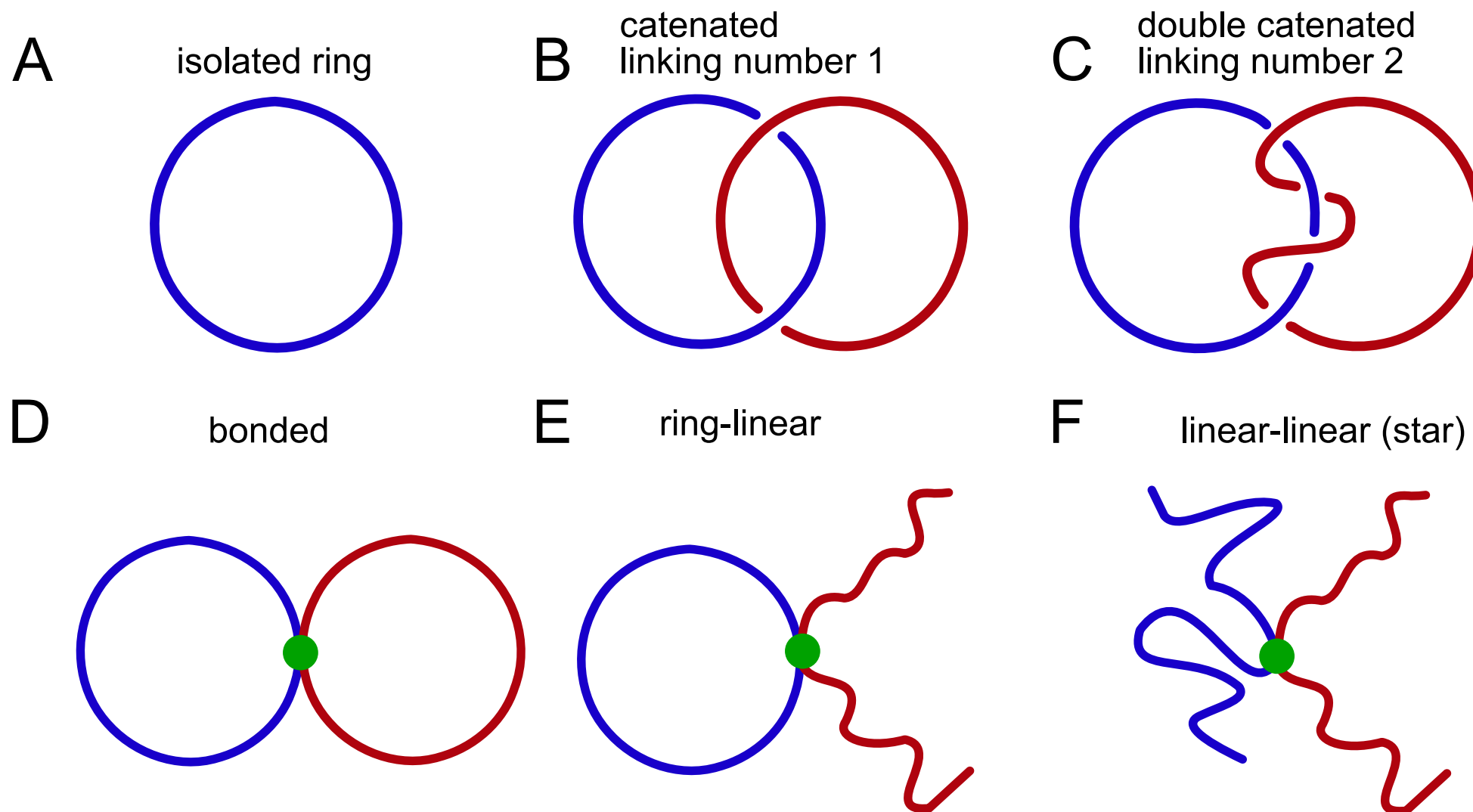


Diffusion-Driven Looping Provides a Consistent Framework for Chromatin Organization Manfred Bohn and Dieter W. Heermann
PLoS ONE 5(8): e12218. doi:10.1371/journal.pone.0012218 (2010)

Loops



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



Influence of the catenation constraint on elongation and segregation of ring polymers

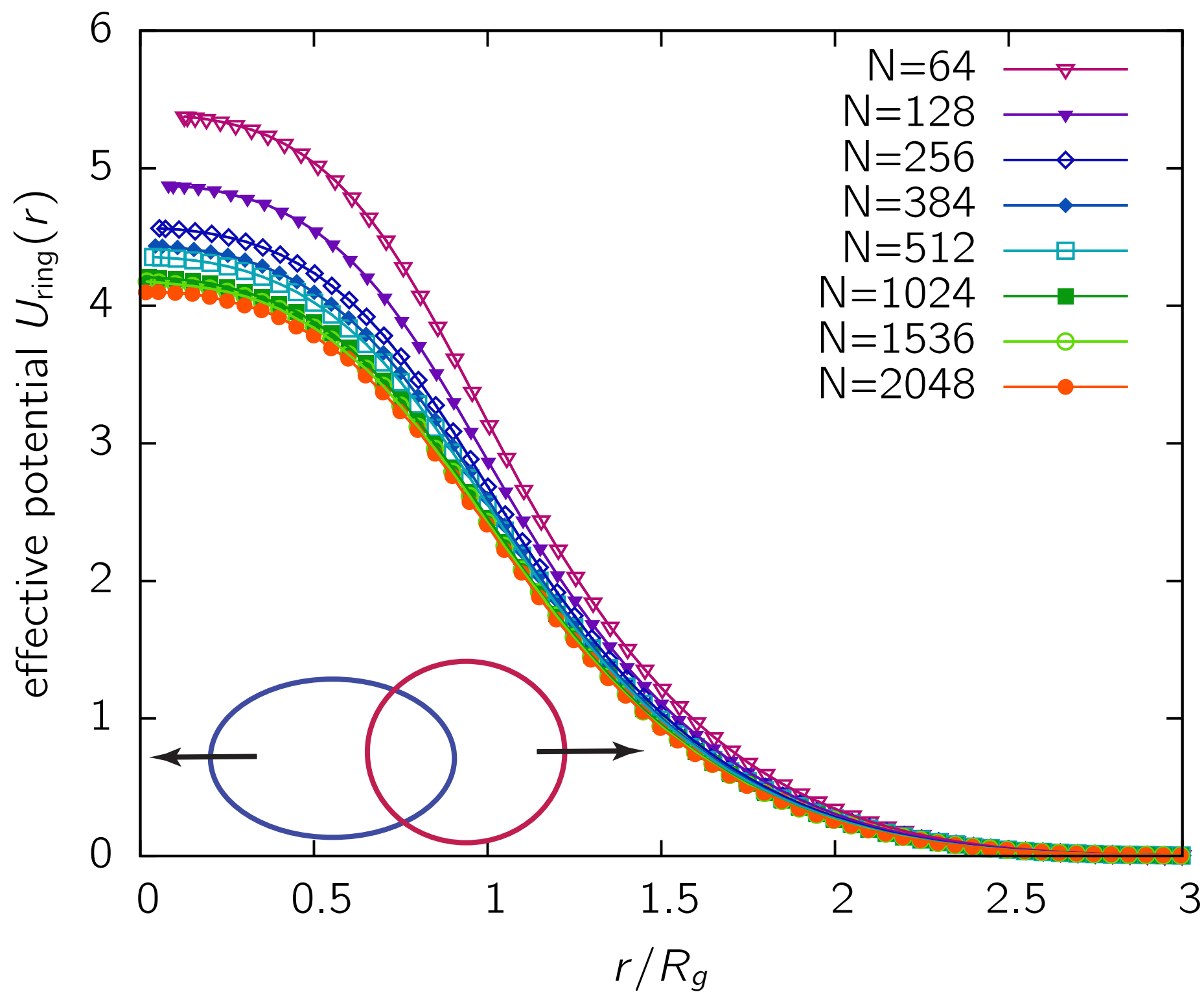
Manfred Bohn, Dieter W. Heermann, Odilon Lourenço, Claudette Cordeiro

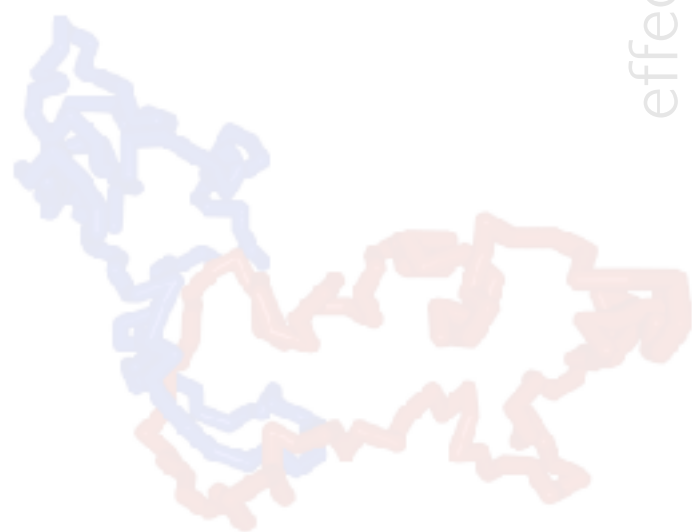
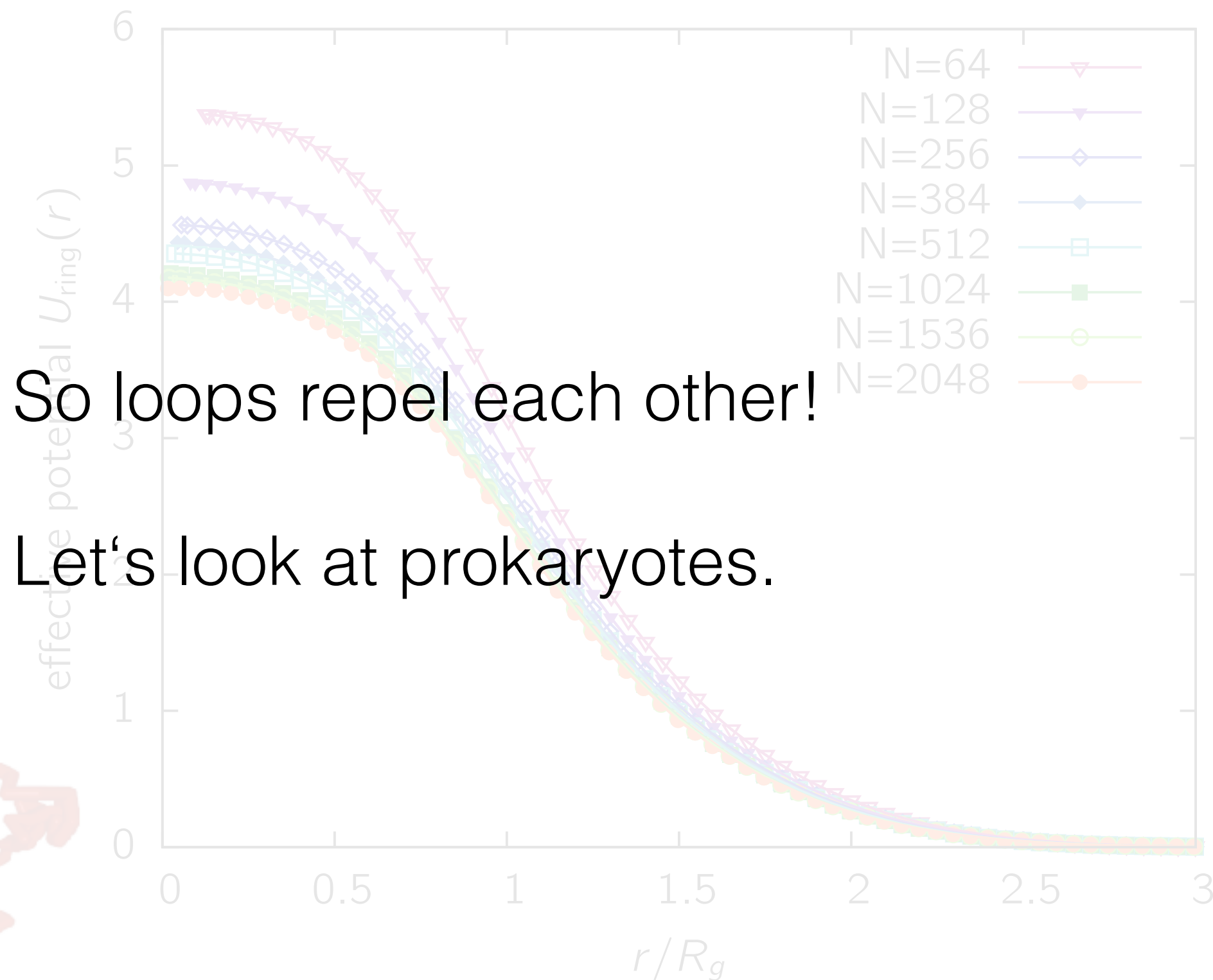
Macromolecules, 43 (5), 2564–2573 (2010)

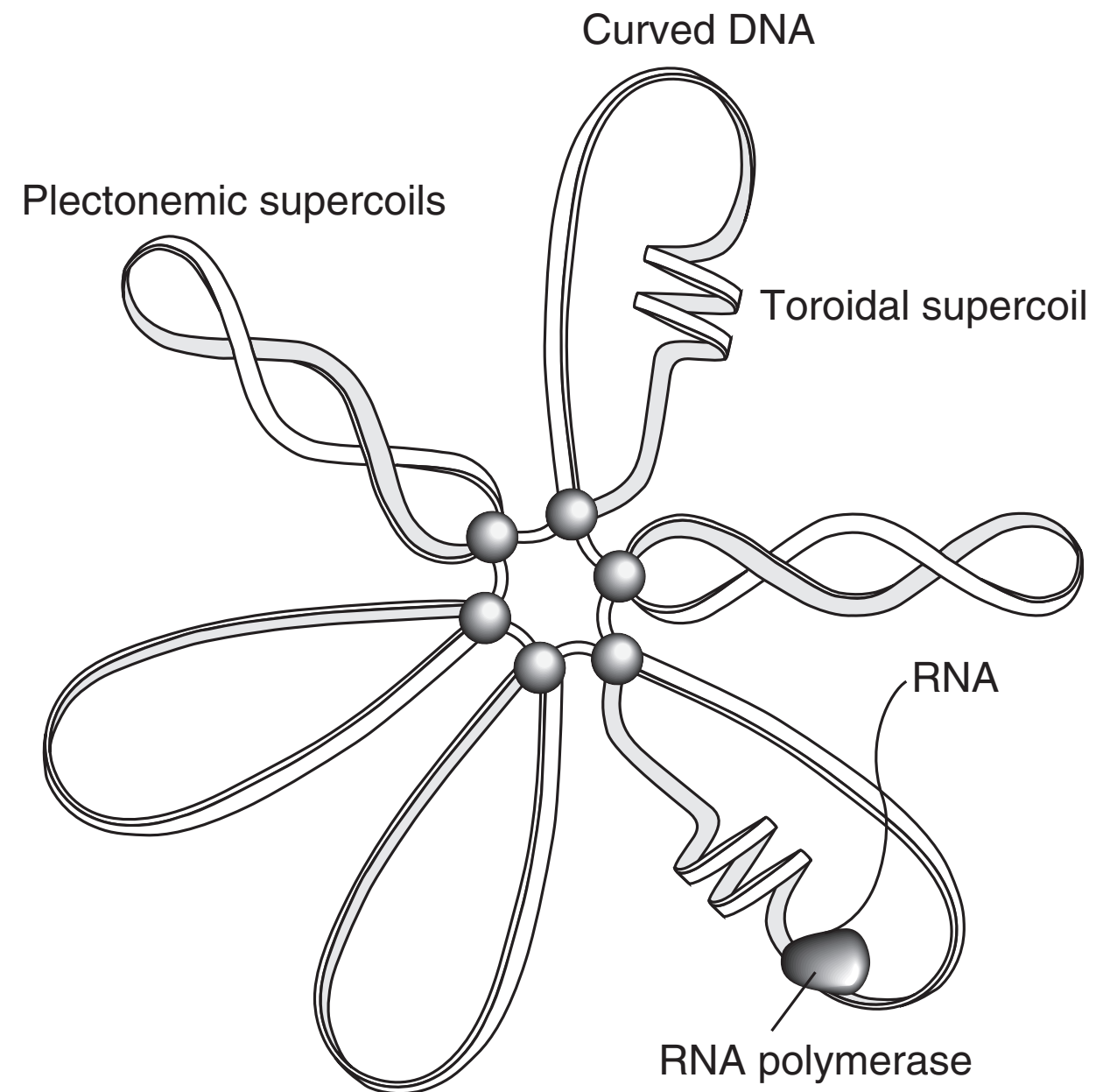
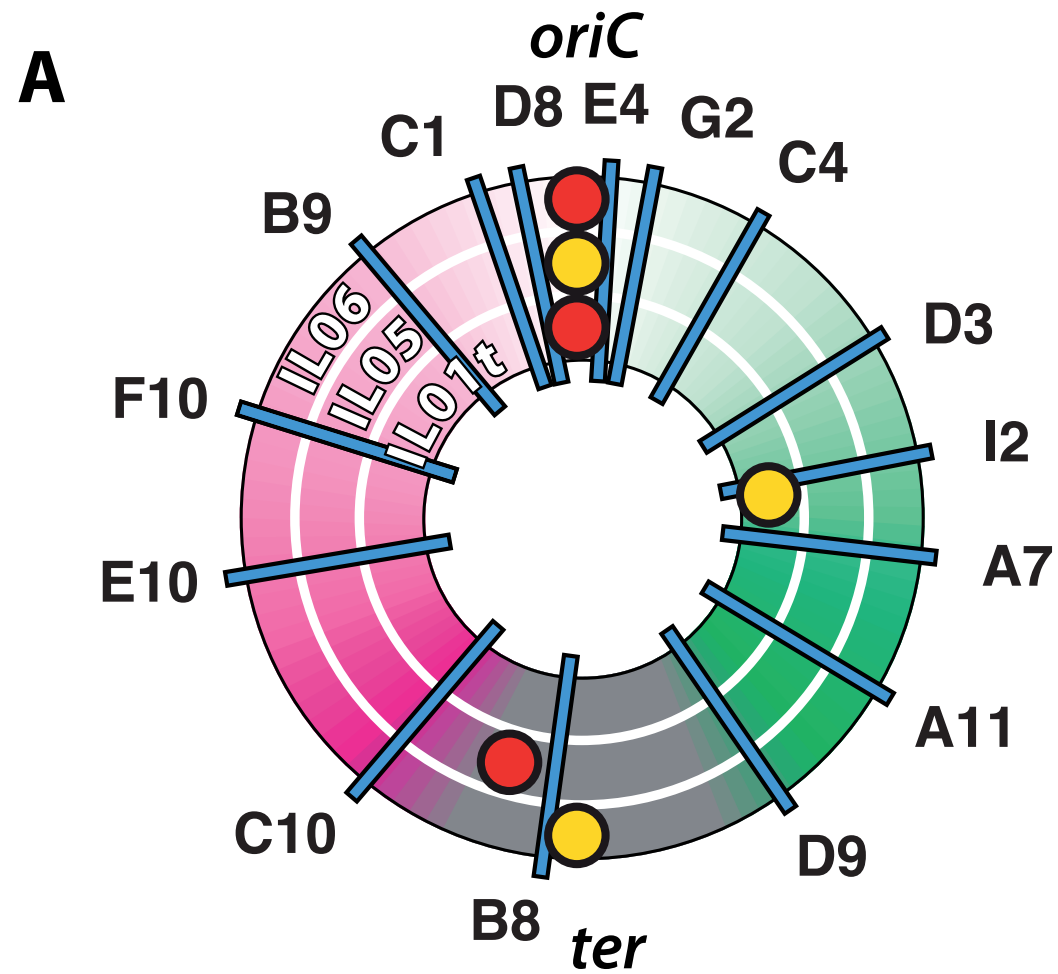
Topological interactions between ring polymers: Implications for chromatin loops

Manfred Bohn and Dieter W. Heermann

J. Chem. Phys. 132, 044904 (2010)





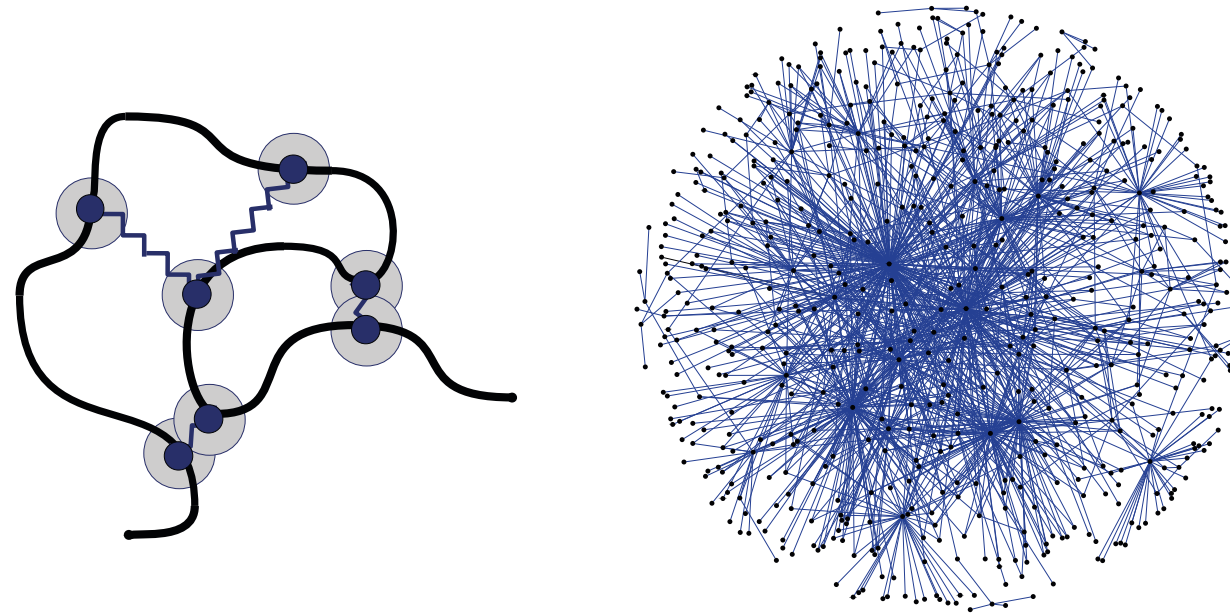


Source: Willenbrock and Ussery *Genome Biology* 2004 **5**:252 doi:10.1186/gb-2004-5-12-252

Loops: Biology and Physics



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



Ansatz: Dynamic Loop Model + genes that are co-regulated by a set of same or similar transcription factors, might stay in physical proximity in order to guarantee the efficiency of gene regulation and expression.

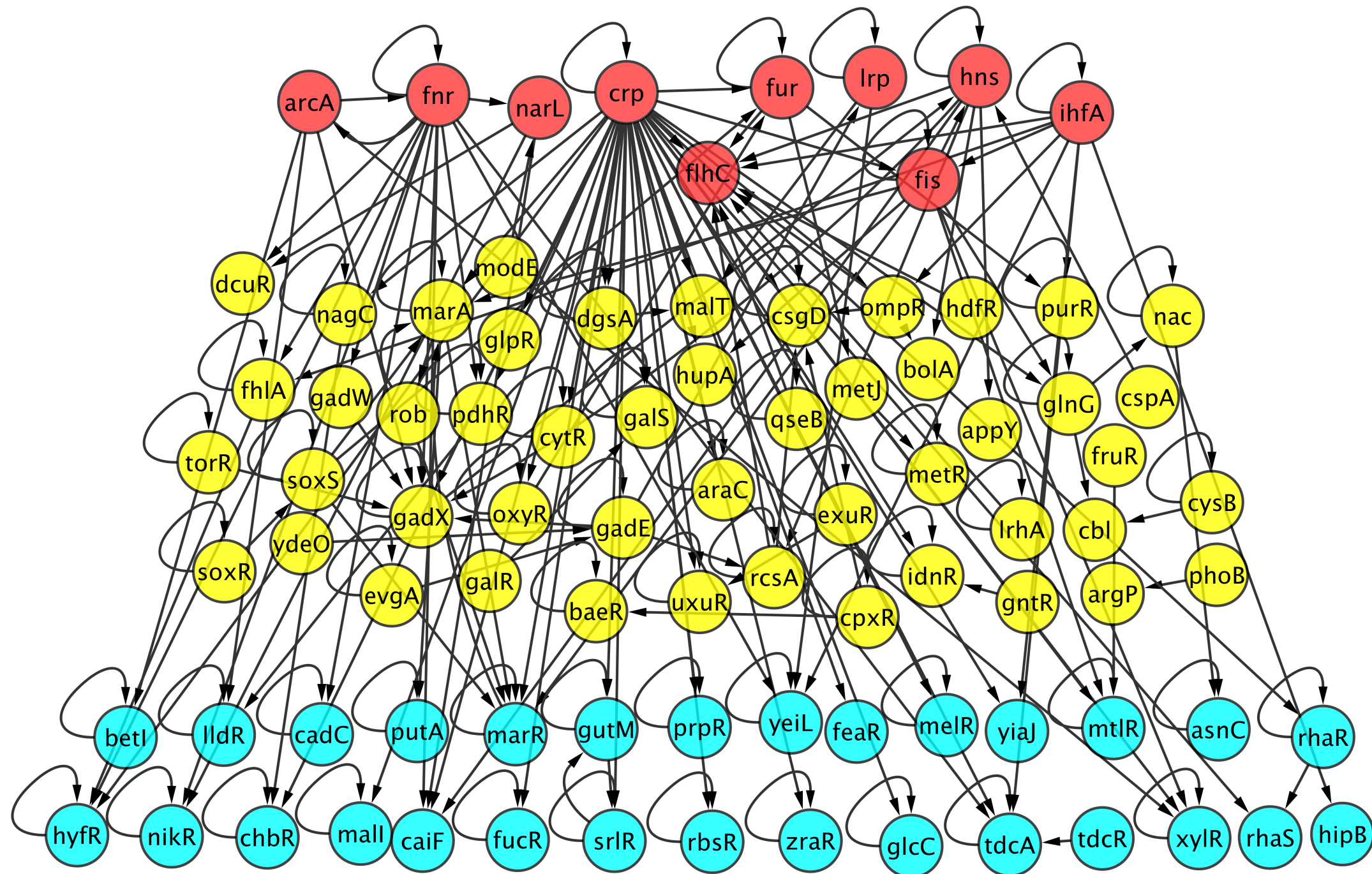
Transcription Factor Induced DNA Domain Formation Structures the E. coli Chromosome

M. Fritsche, S. Li, P. Wiggins and D.W. Heermann, Nucleic Acids Res. 2012 Feb;40(3):972-80.

Loops: One More Thing

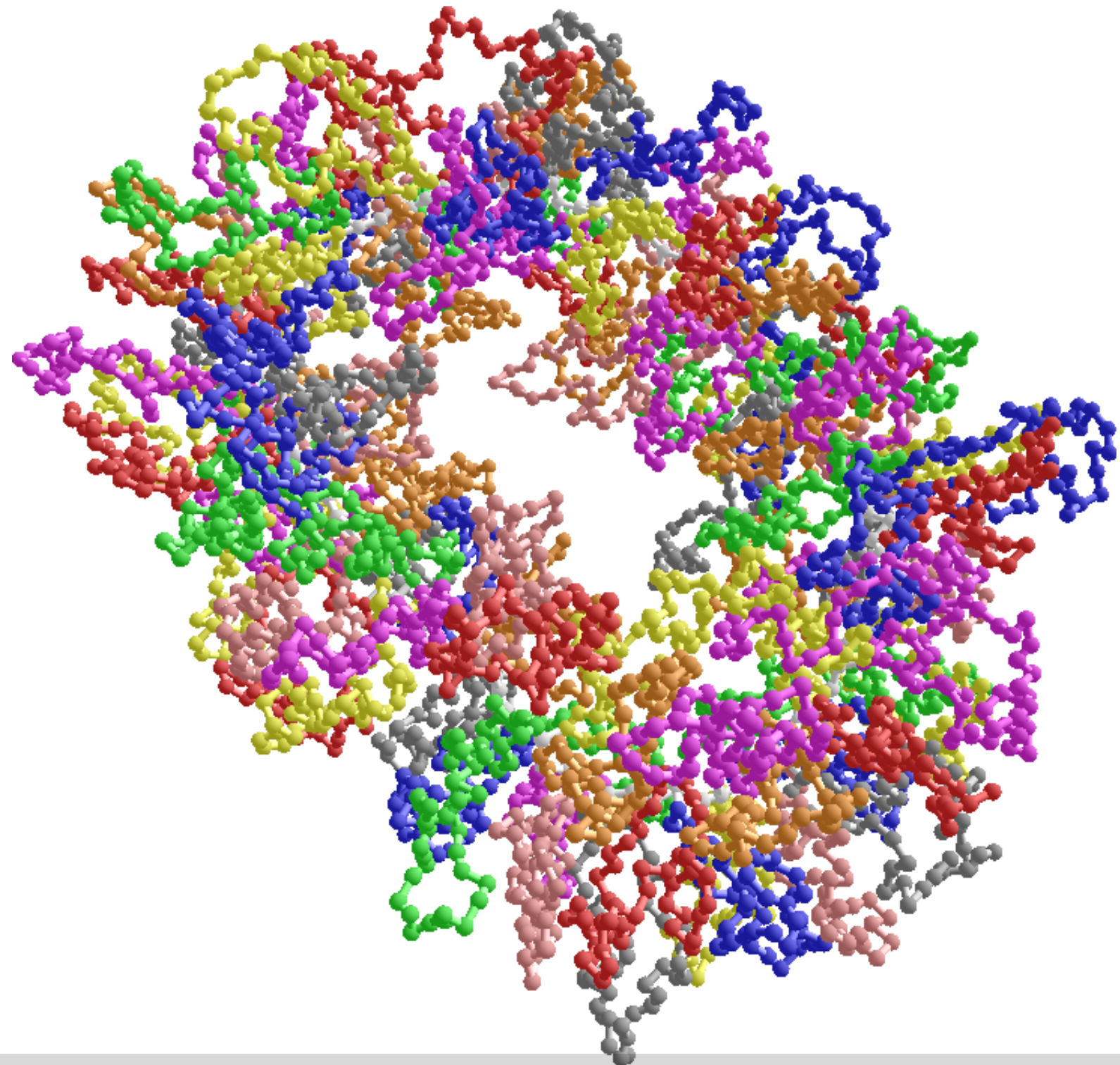
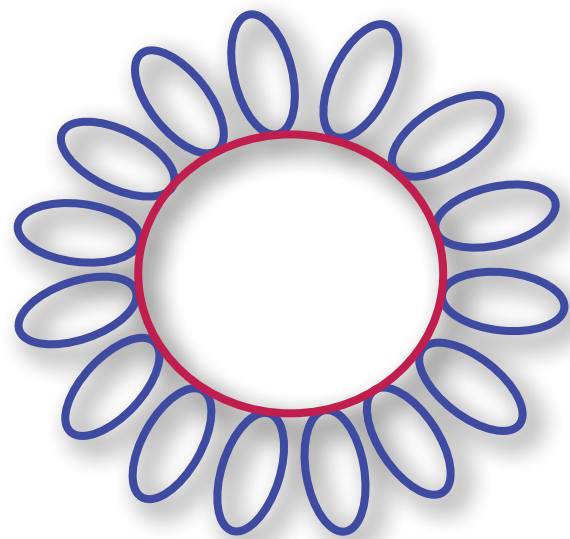
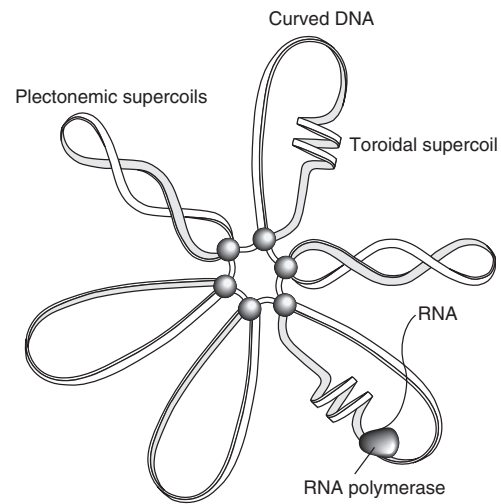


UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386

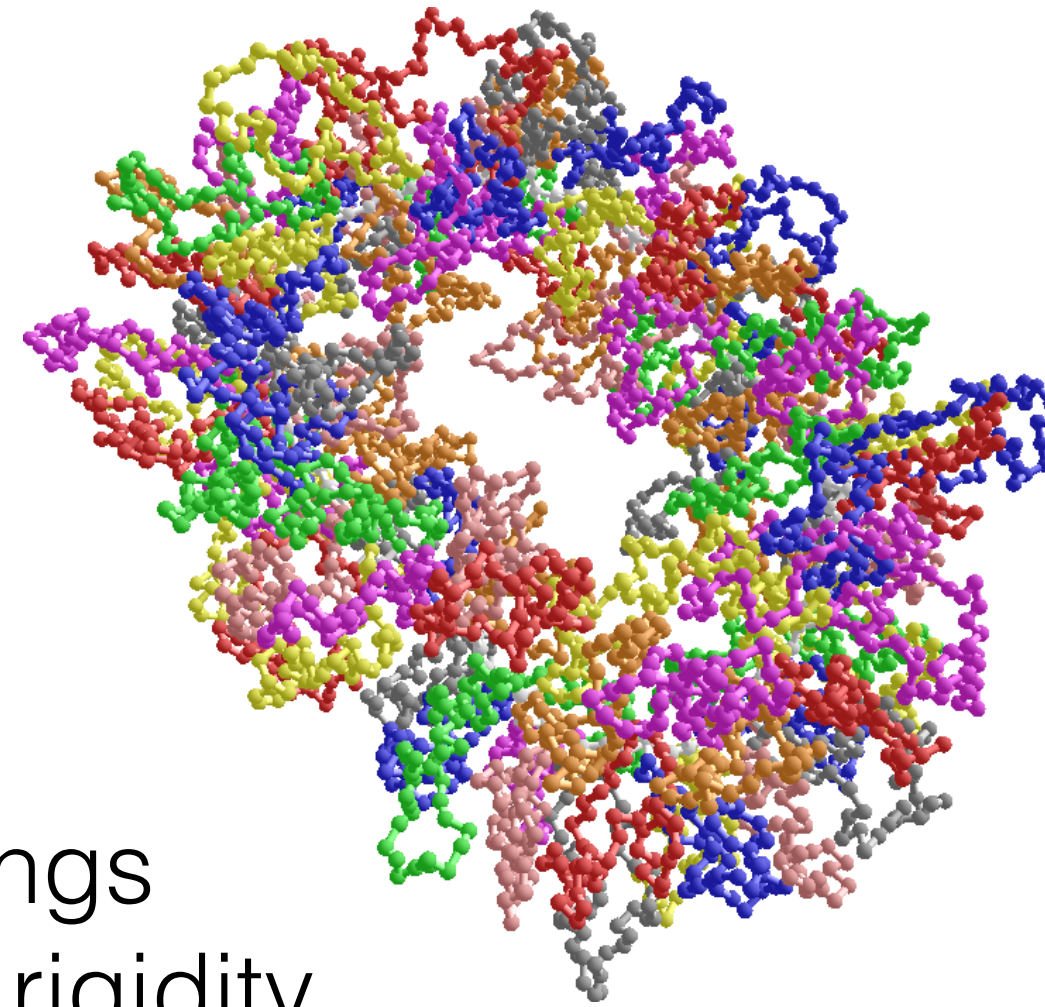
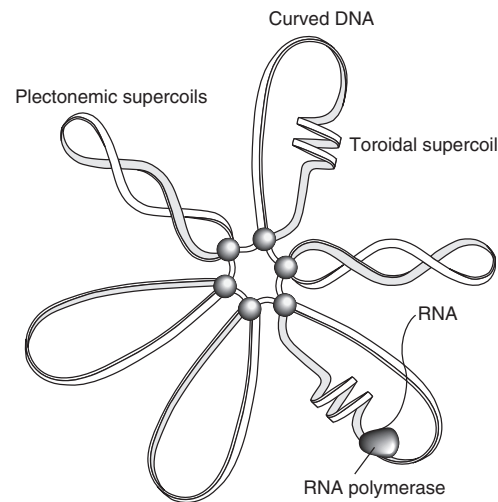


Transcription Factor Induced DNA Domain Formation Structures the E. coli Chromosome

M. Fritsche, S. Li, P. Wiggins and D.W. Heermann, Nucleic Acids Res. 2012 Feb;40(3):972-80.



Looped Star Polymers Show Conformational Transition from Spherical to Flat Toroidal Shapes
Pascal Reiß, Miriam Fritsche, and Dieter W. Heermann, Phys. Rev. E 84, 051910 (2011)



Entropic repulsion between rings
leads to an effective bending rigidity.

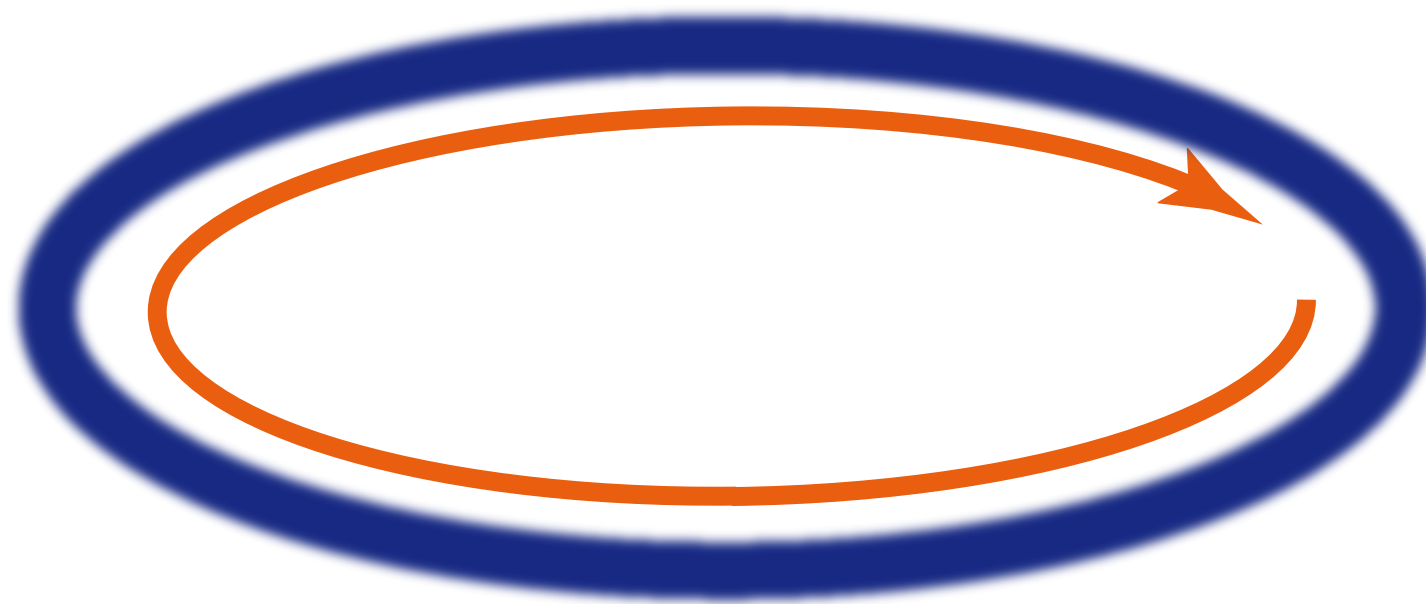
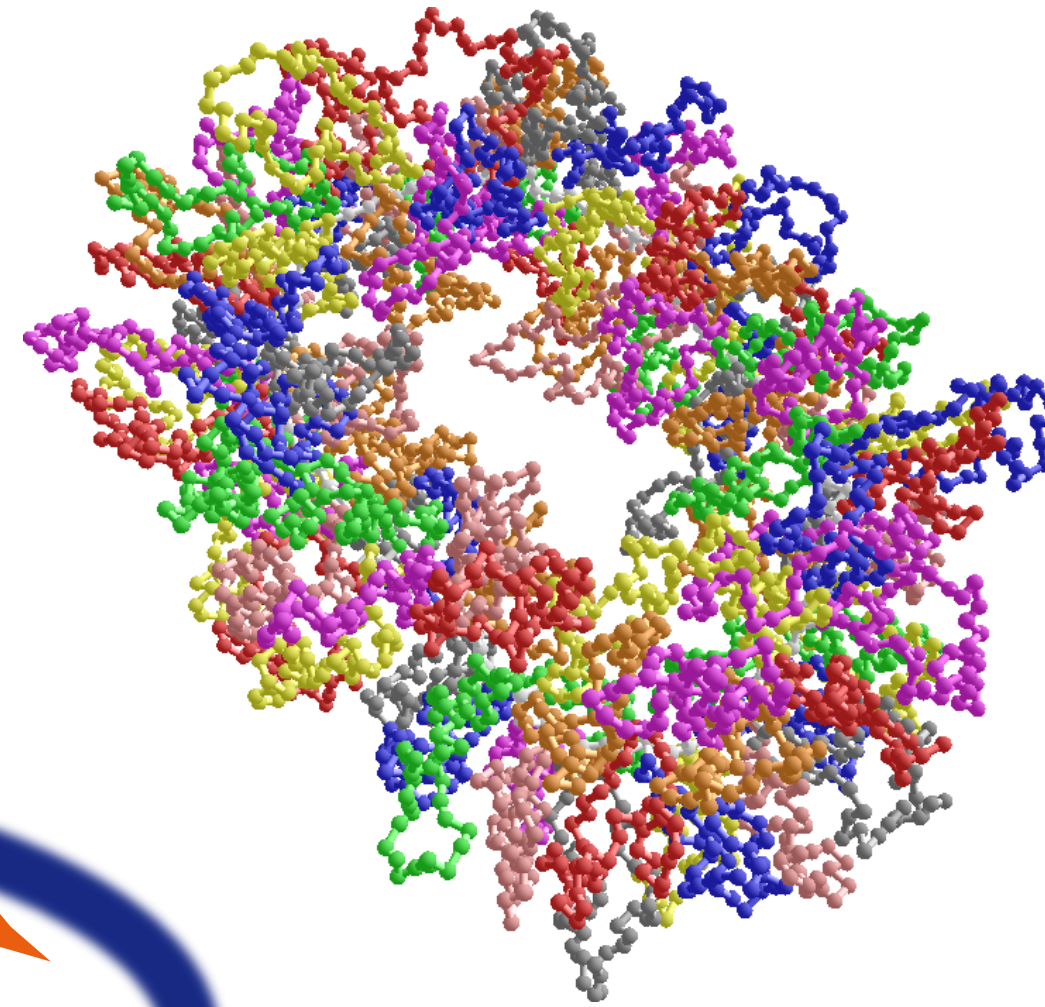
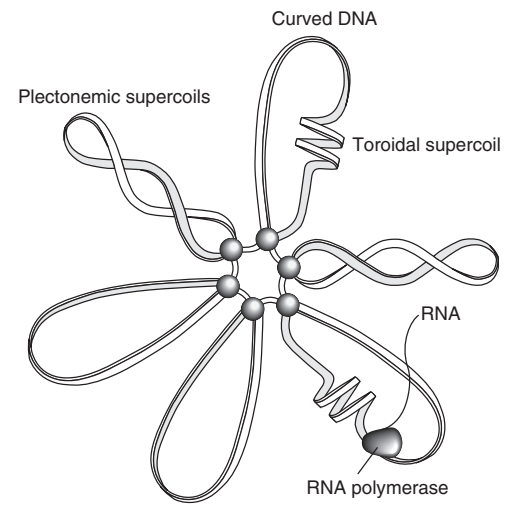
Looped Star Polymers Show Conformational Transition from Spherical to Flat Toroidal Shapes

Pascal Reiß, Miriam Fritsche, and Dieter W. Heermann, Phys. Rev. E 84, 051910 (2011)

e.coli



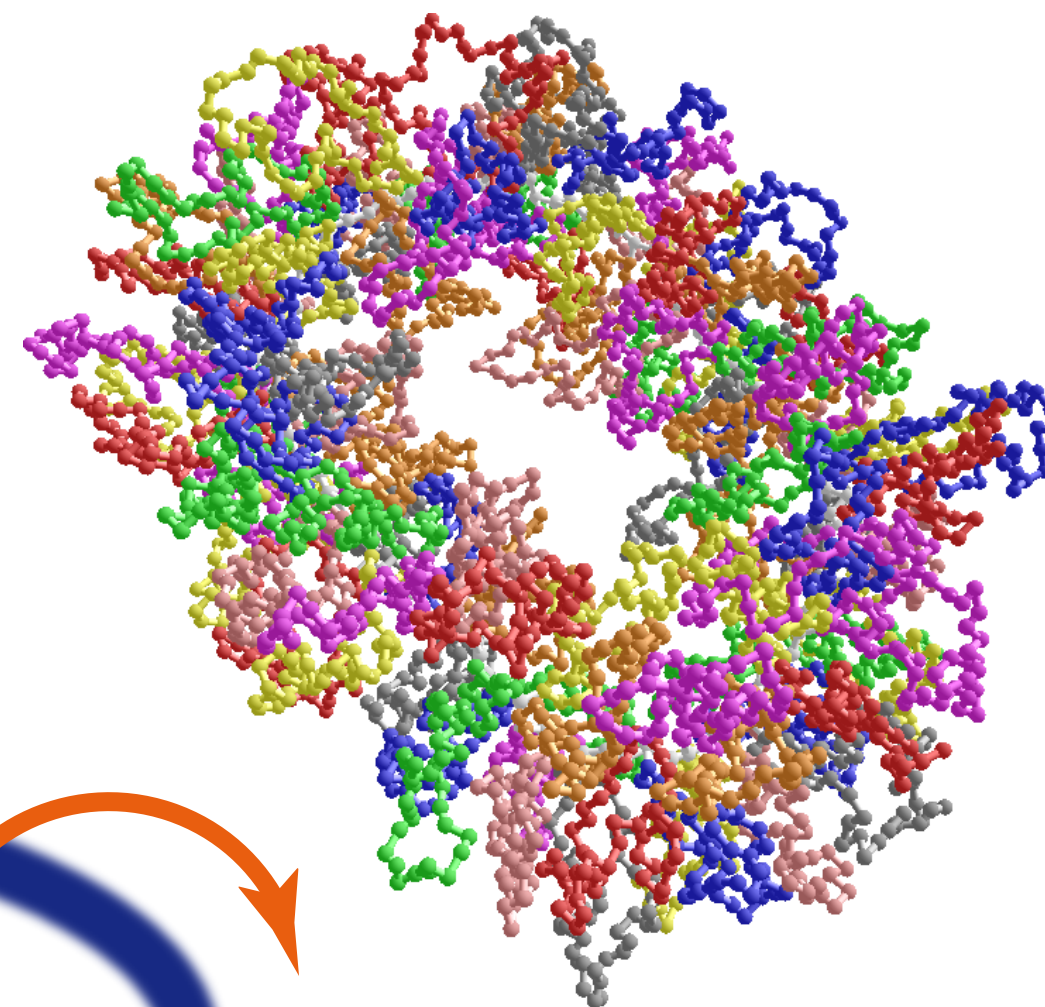
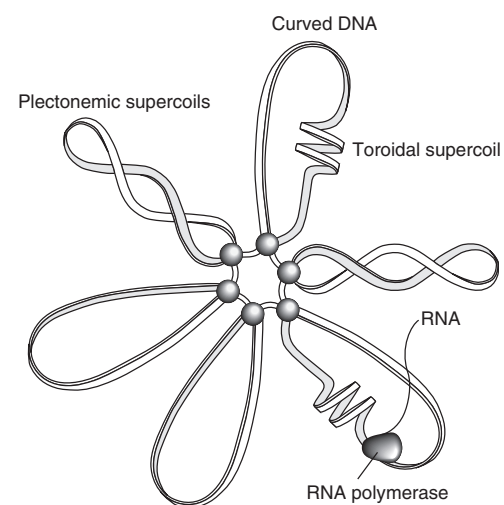
UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



e.coli



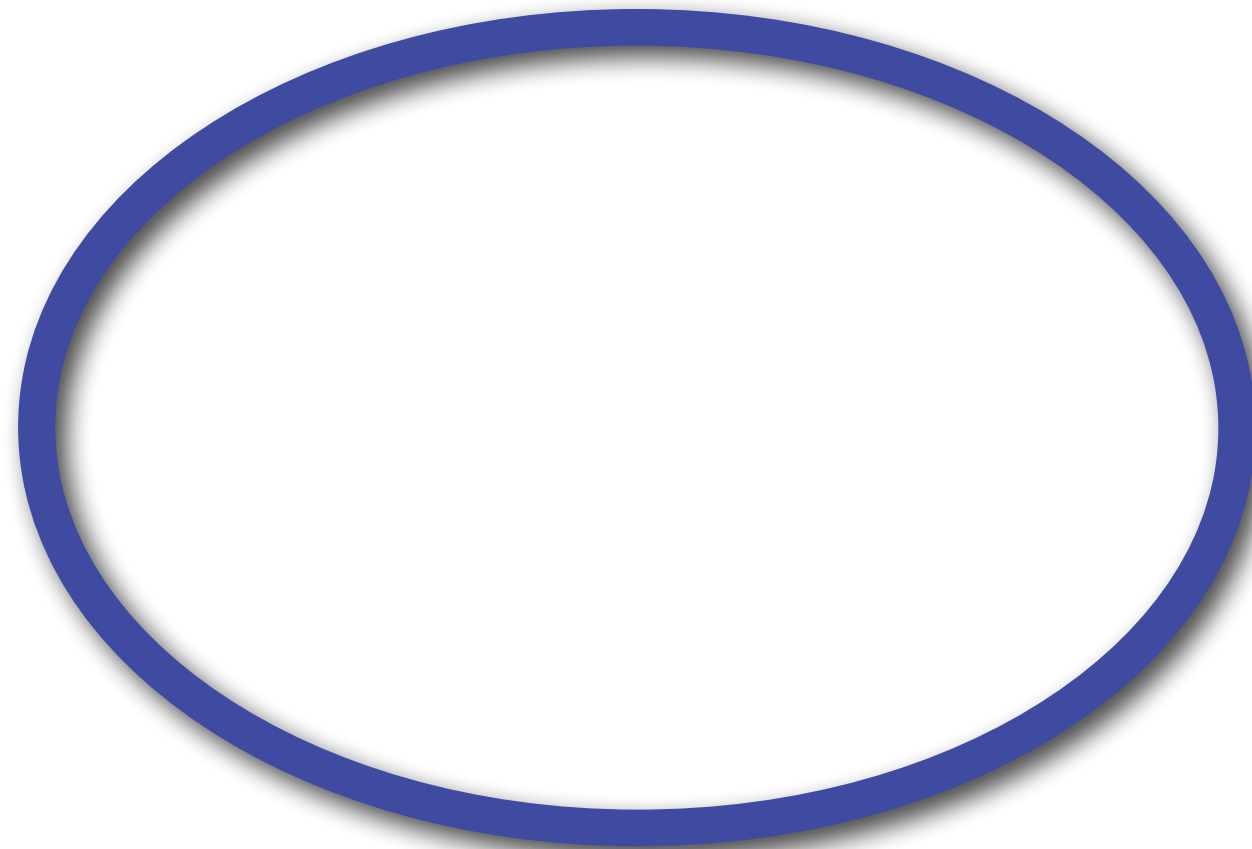
UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



e.coli



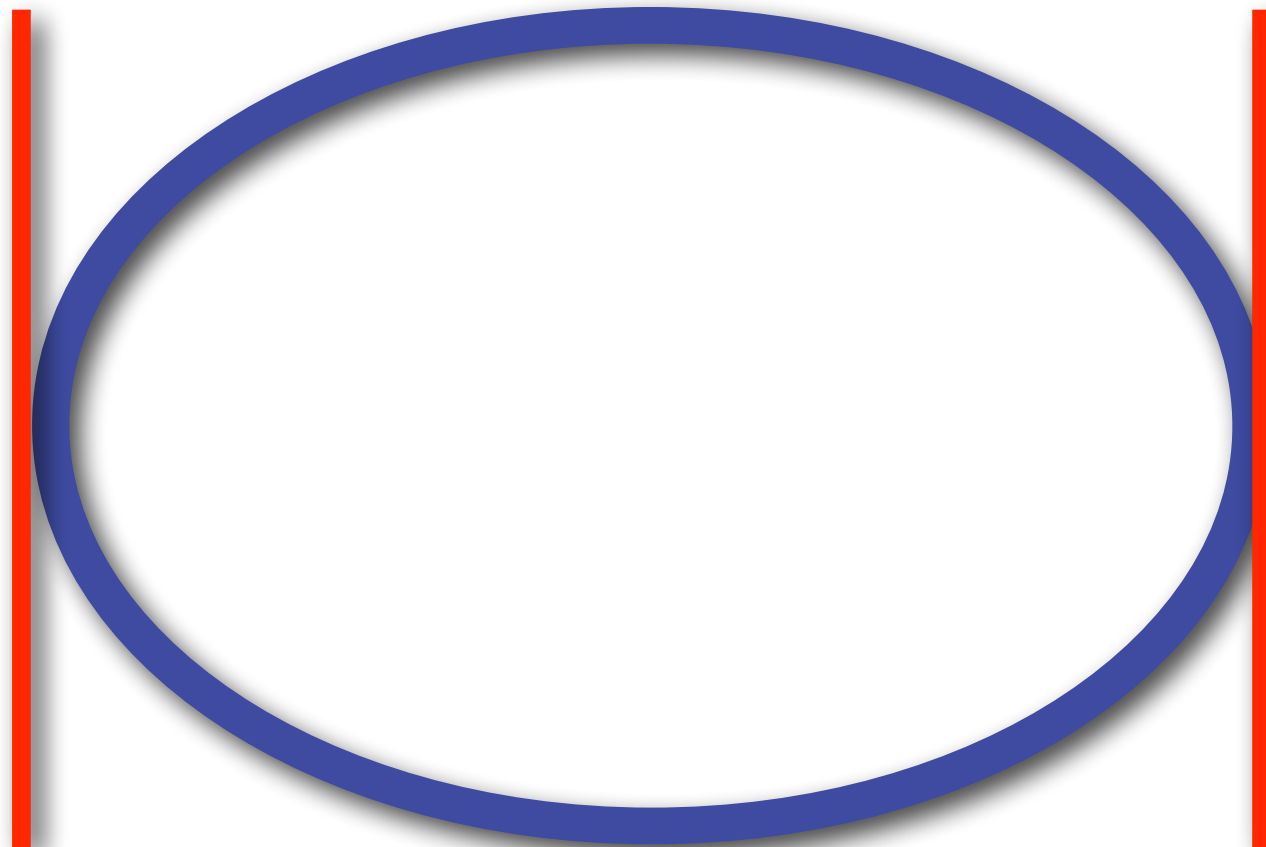
UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



e.coli



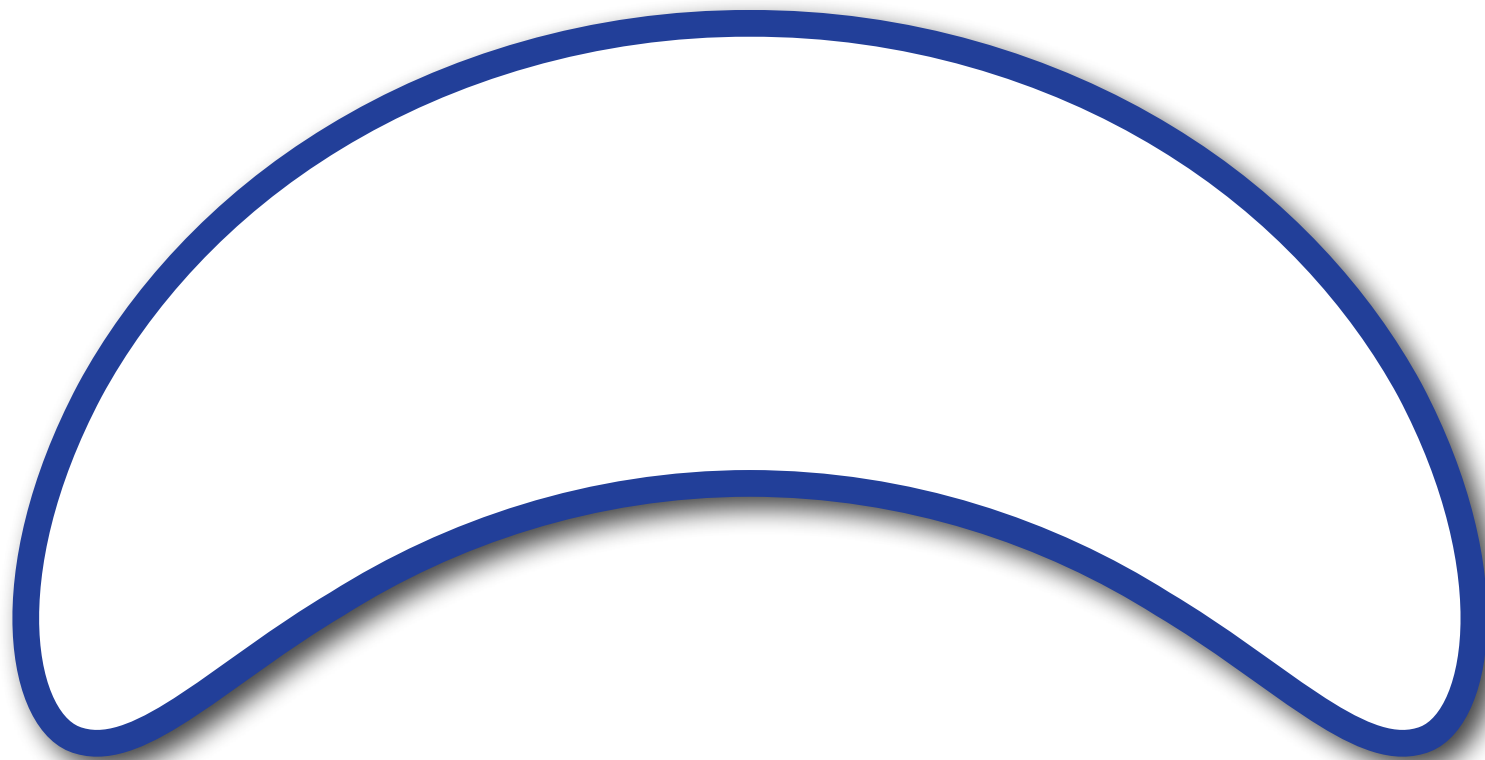
UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



e.coli



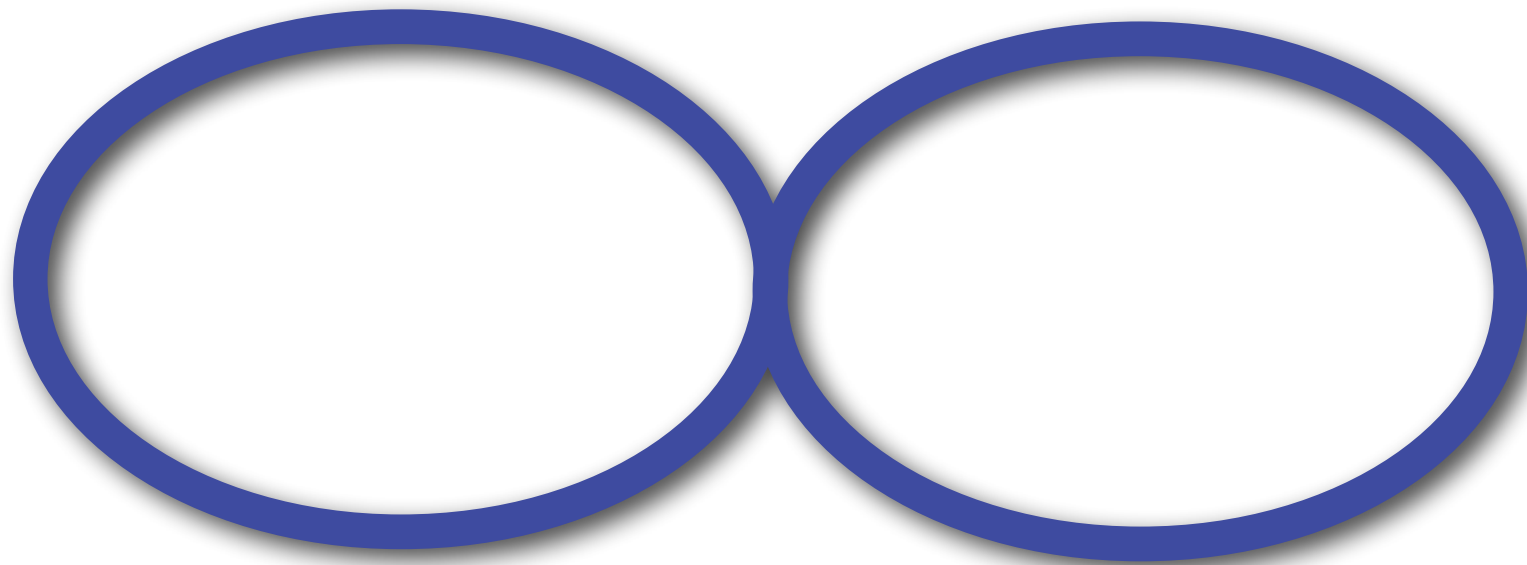
UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



e.coli



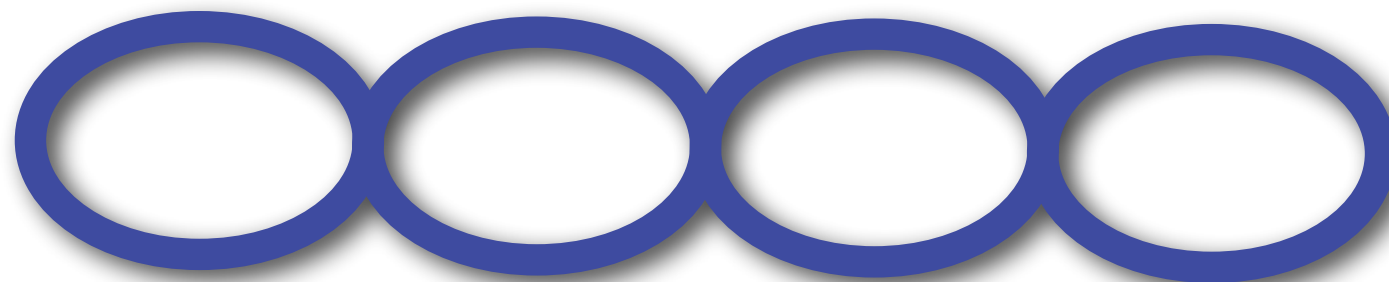
UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



e.coli



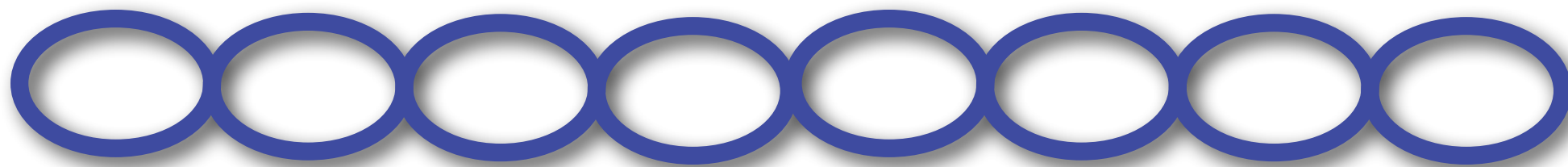
UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



e.coli



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



e.coli



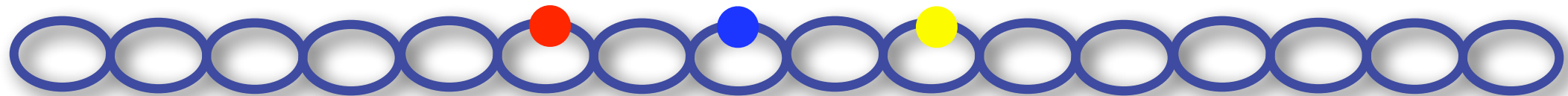
UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



e.coli



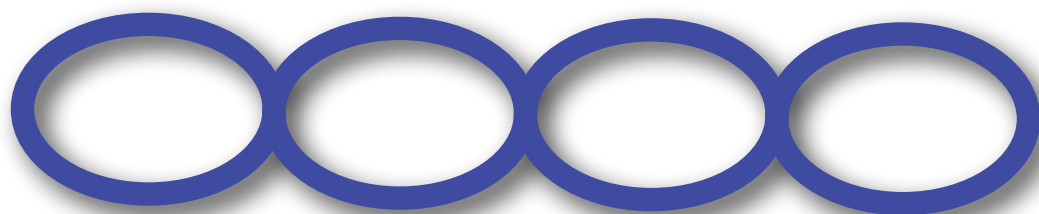
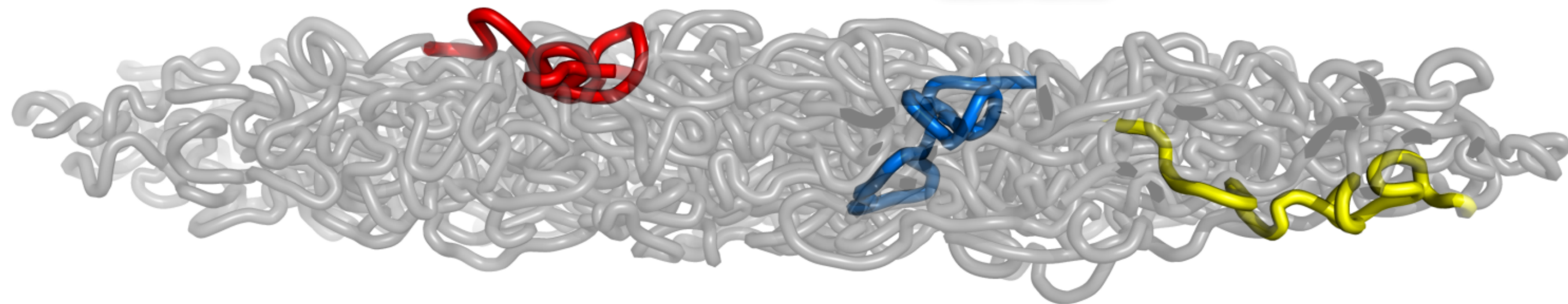
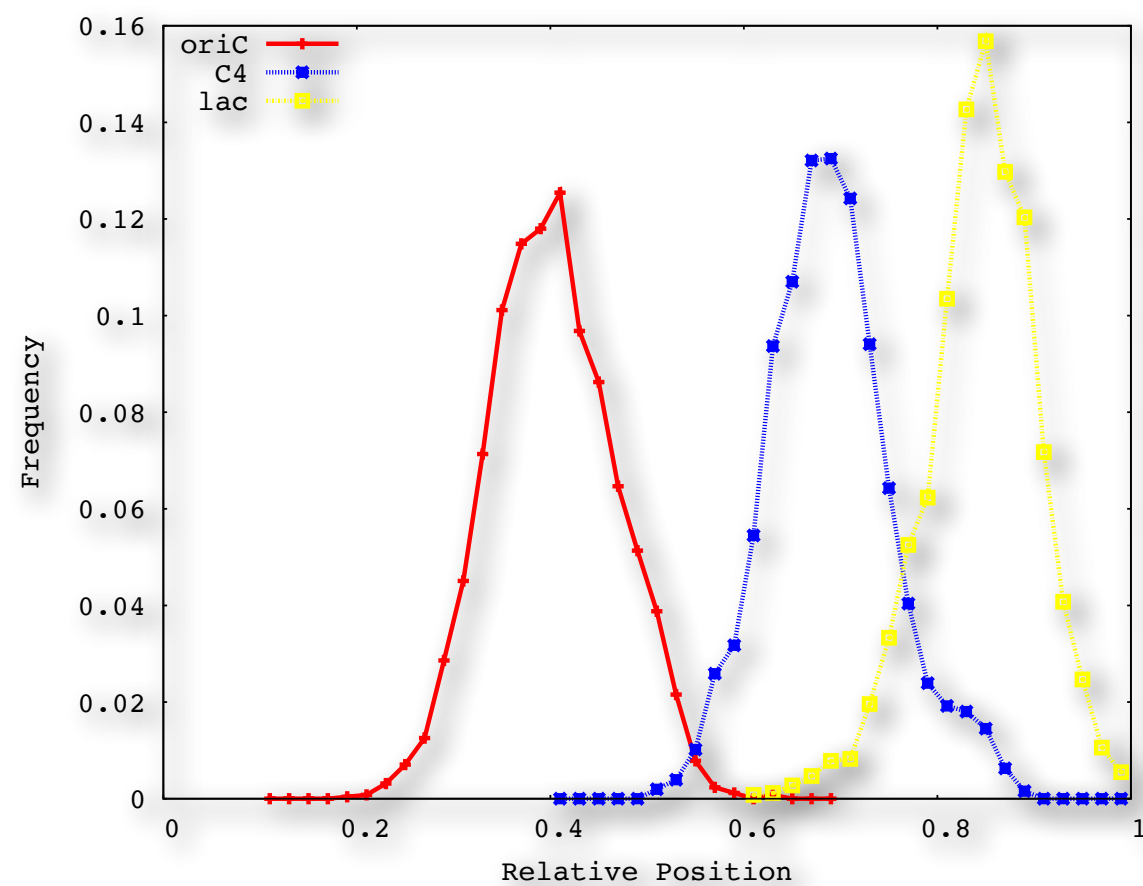
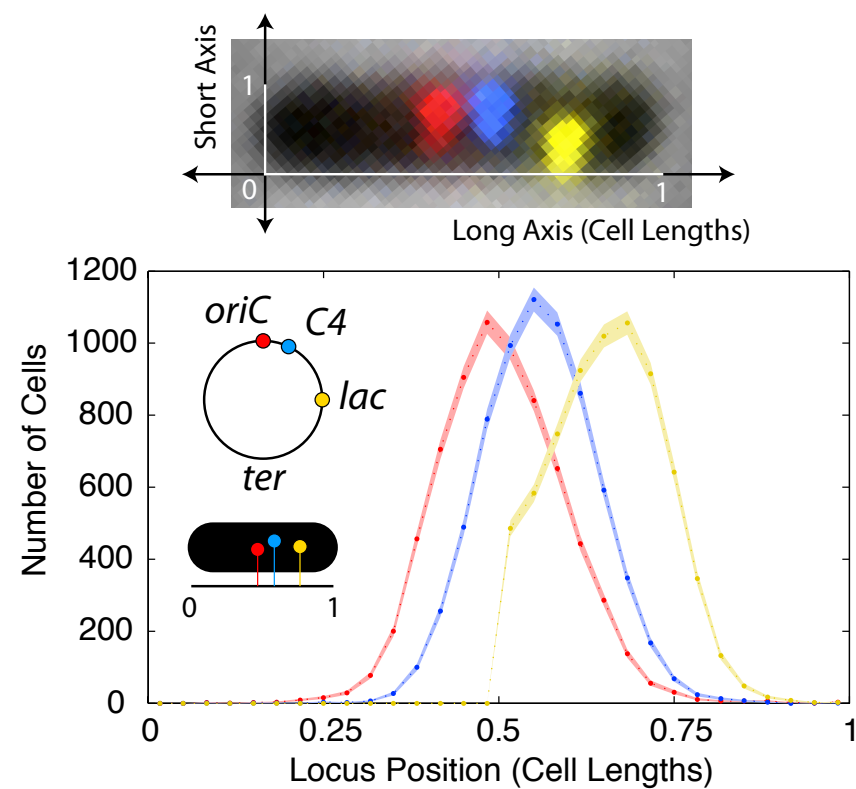
UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386

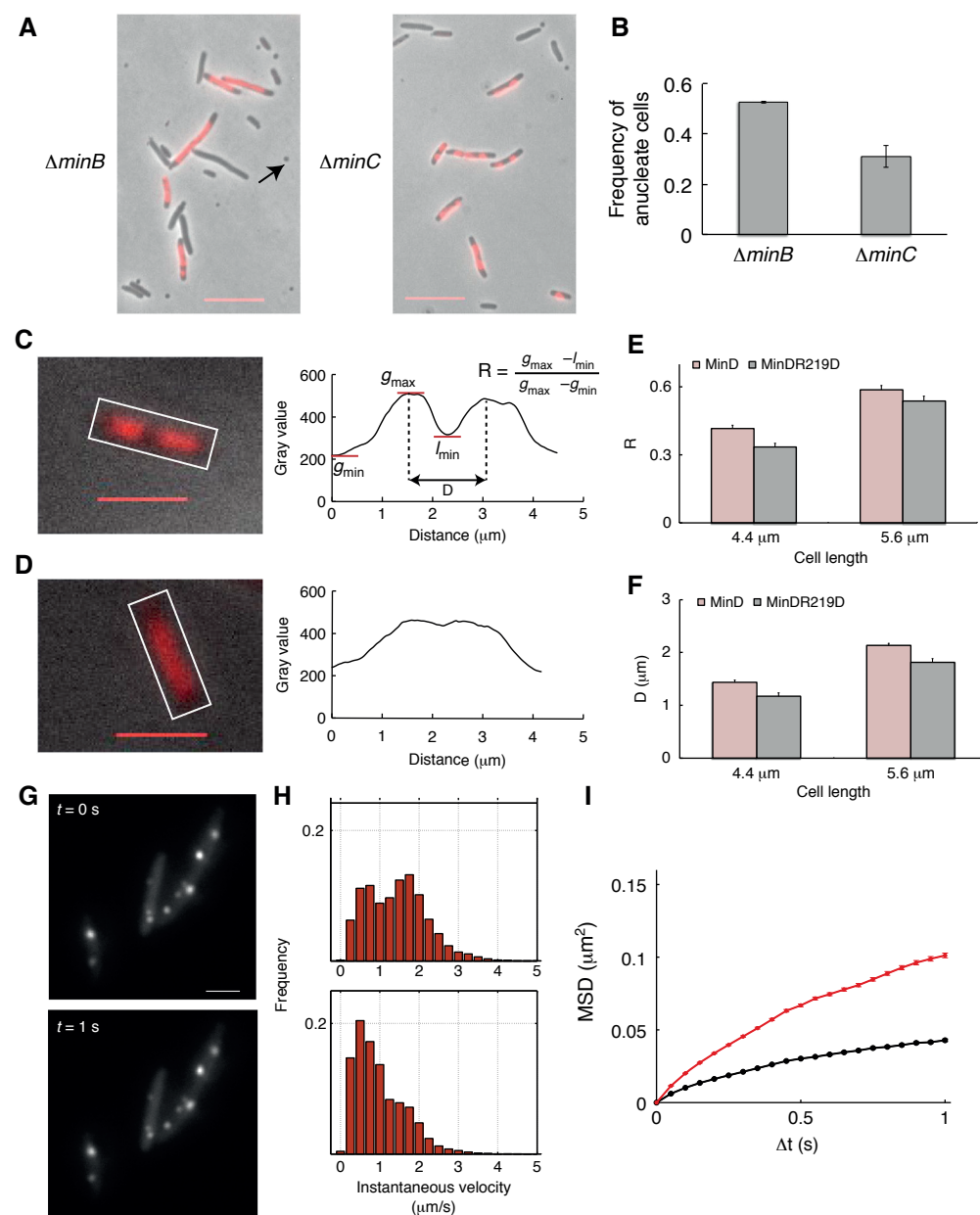


e.coli

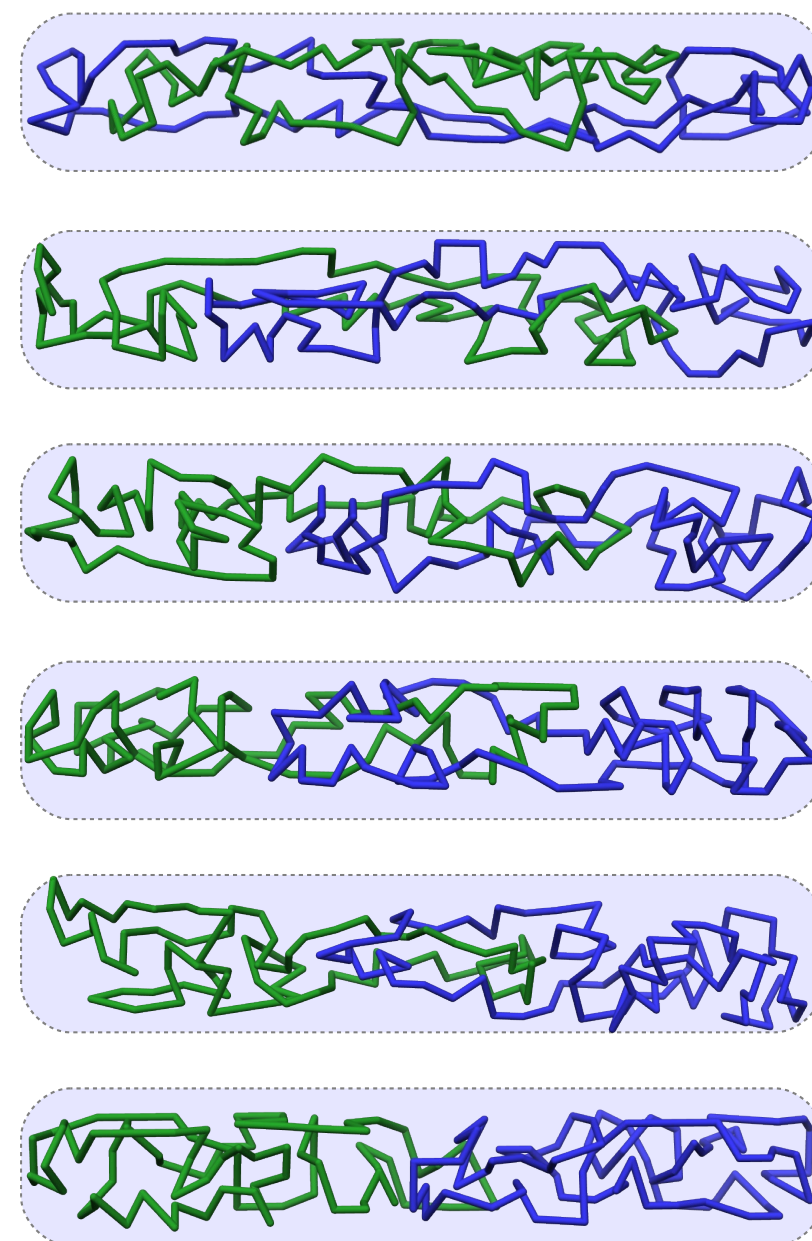


UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386





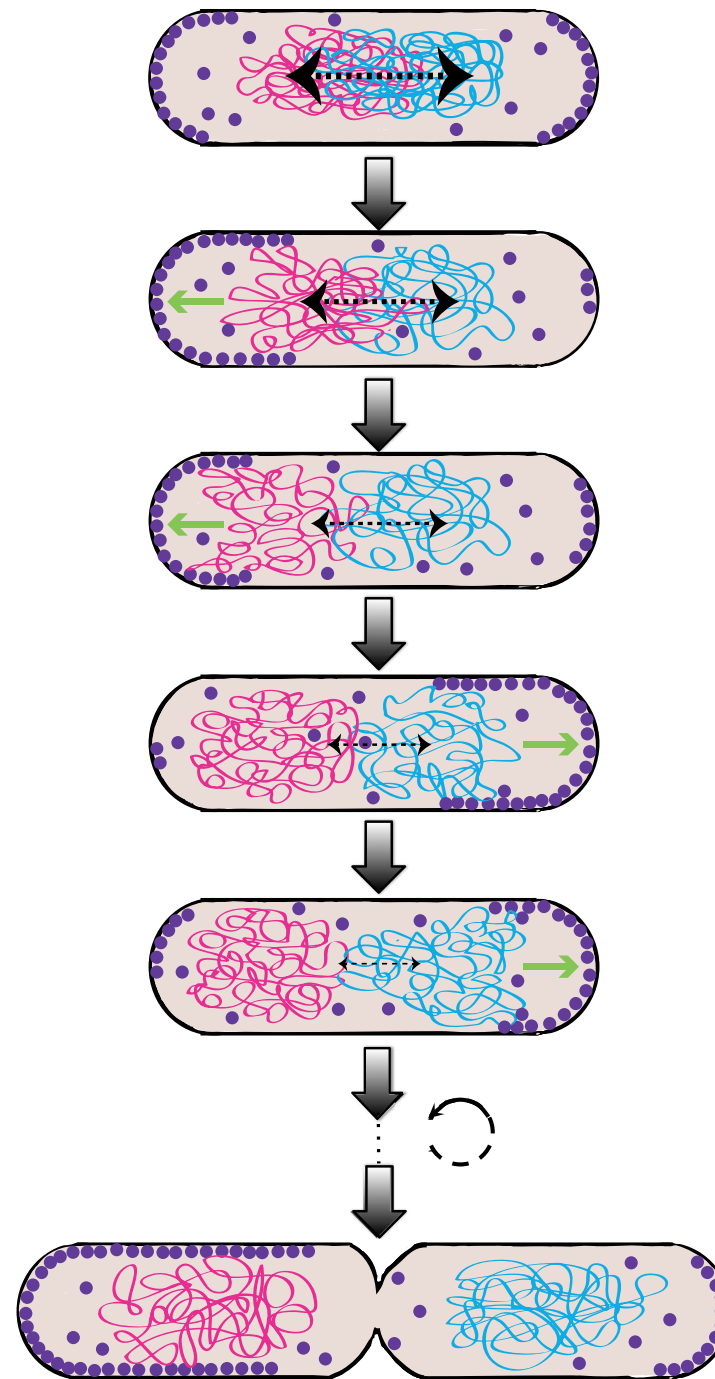
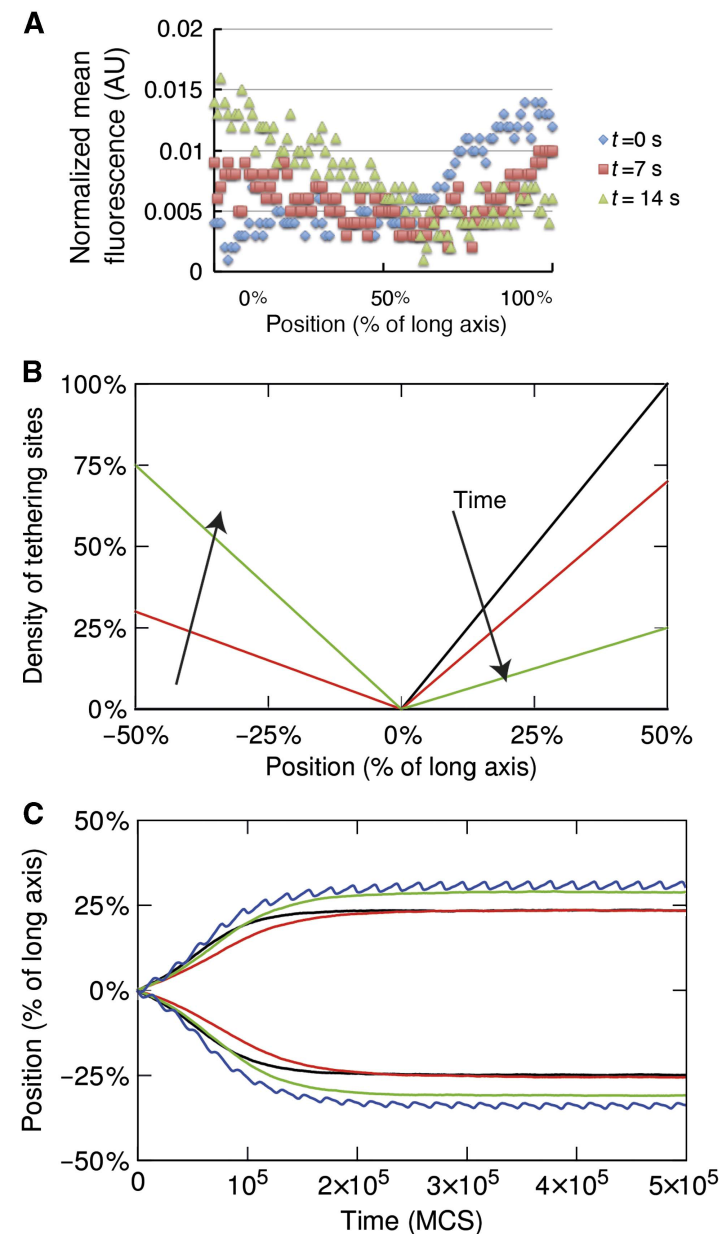
Monte Carlo steps



Chromosome segregation by the Escherichia coli Min system

Barbara Di Ventura, Benoit Knecht, Helena Andreas, William J. Godinez, Miriam Fritsche, Karl Rohr, Walter Nickel, Dieter W Heermann, Victor Sourjik

Molecular Systems Biology 9 Article number: 686 doi:10.1038/msb.2013.44, 2014

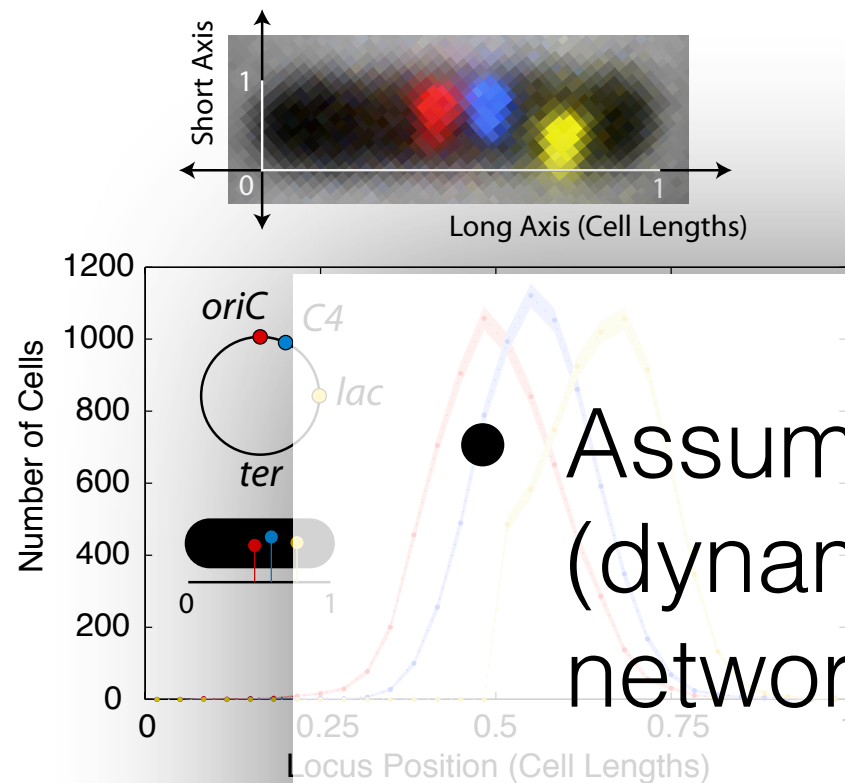


entropic forces alone are not sufficient to achieve and maintain full separation of chromosomes

Chromosome segregation by the Escherichia coli Min system

Barbara Di Ventura, Benoit Knecht, Helena Andreas, William J. Godinez, Miriam Fritsche, Karl Rohr, Walter Nickel, Dieter W Heermann, Victor Sourjik

Molecular Systems Biology 9 Article number: 686 doi:10.1038/msb.2013.44, 2014

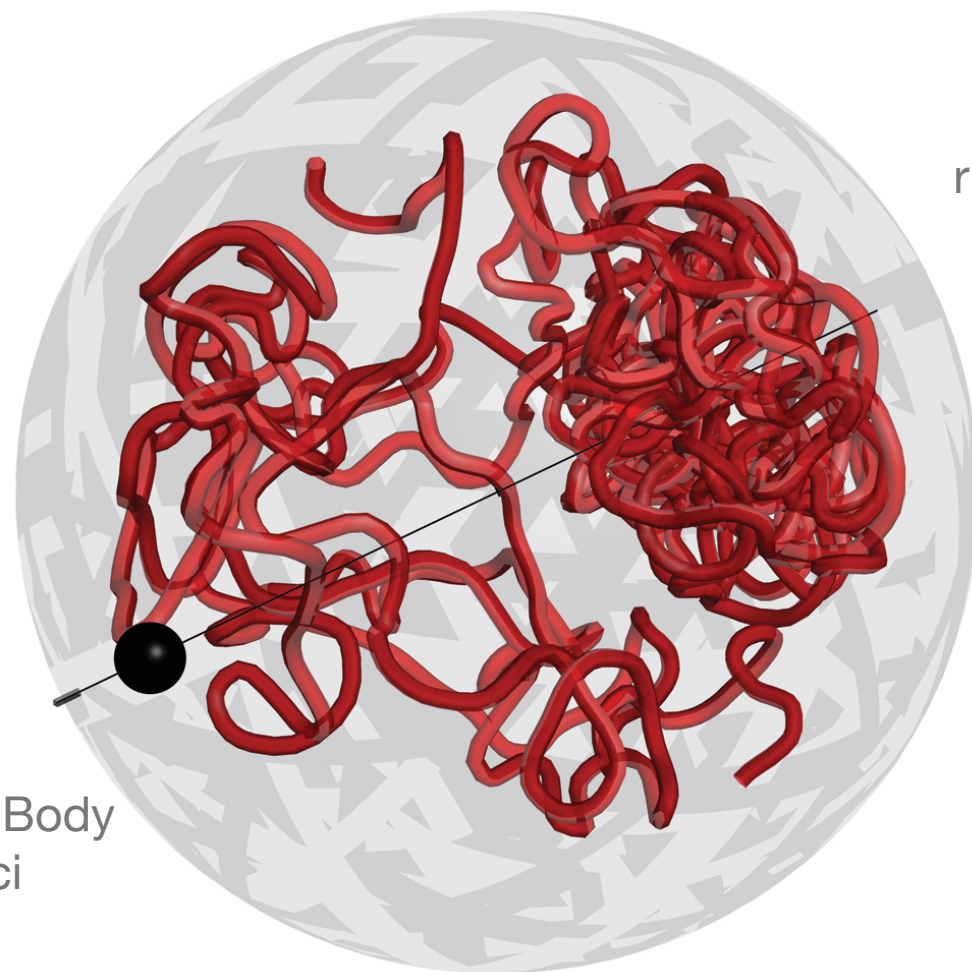


- Assumption of spatial proximity (dynamic loop model + transcriptional network) leads to a „looped-star“.
- Loop structure
+ entropic repulsion
+ confinement
induces ordering.
- Can explain recent experiments.

Yeast

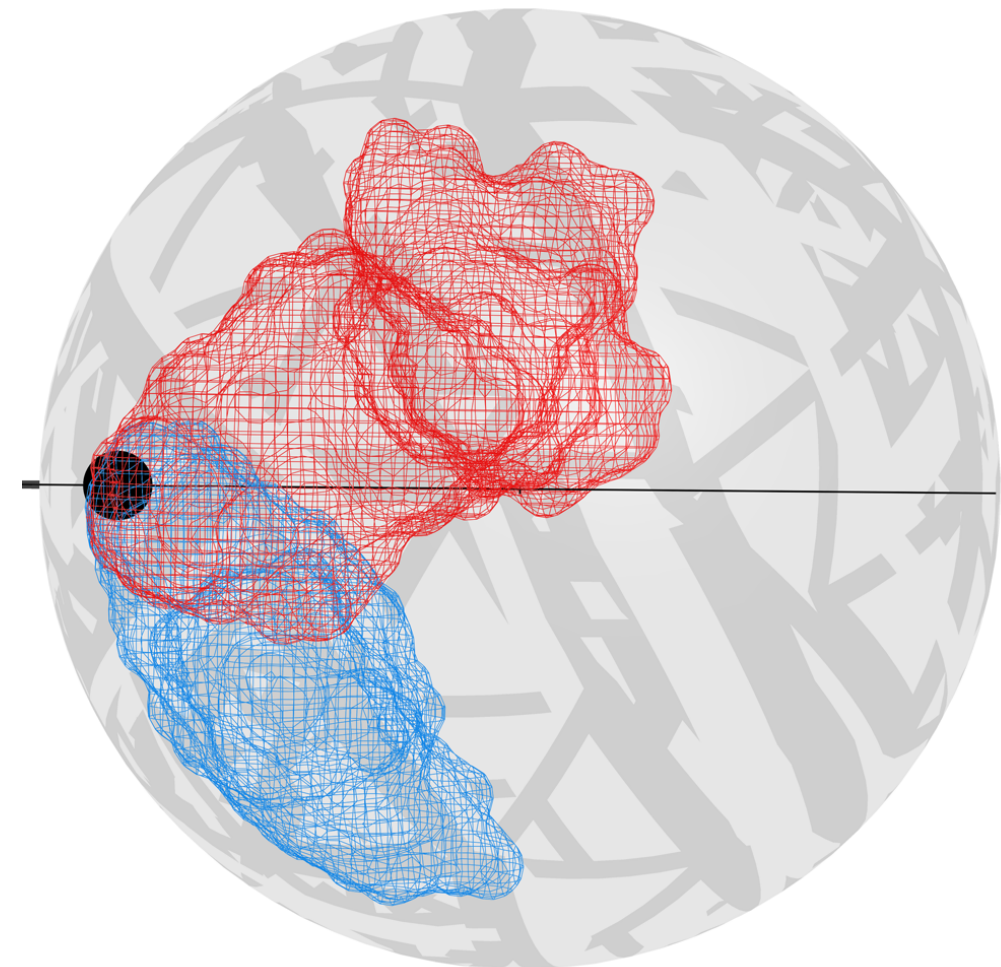


UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



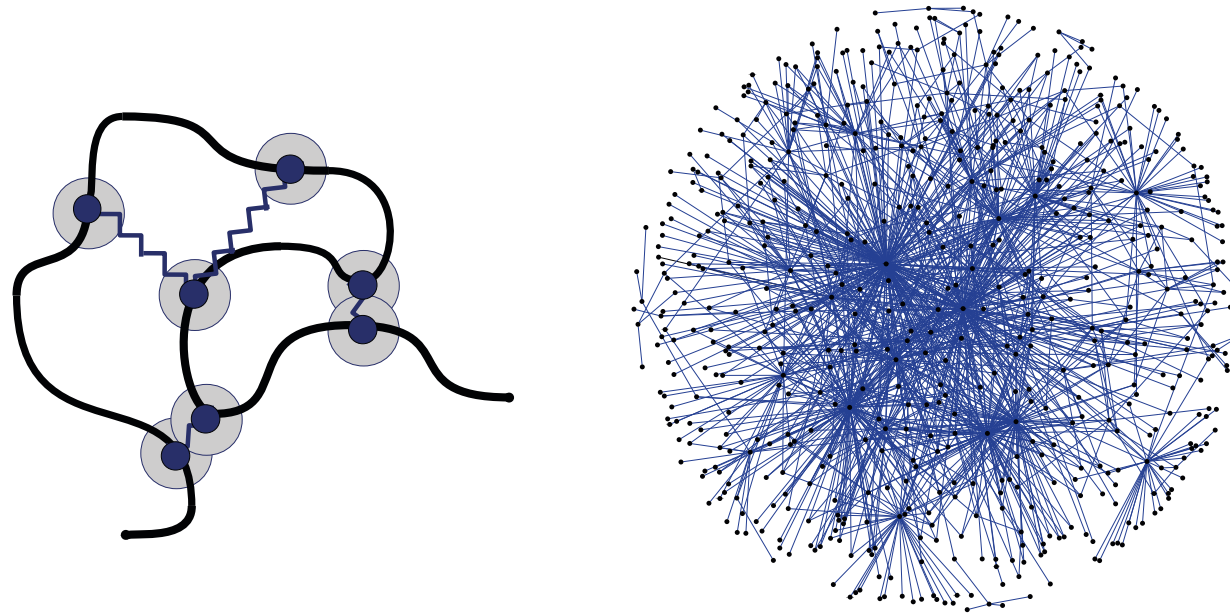
Spindle Pole Body
(SPB) loci

rDNA gene cluster



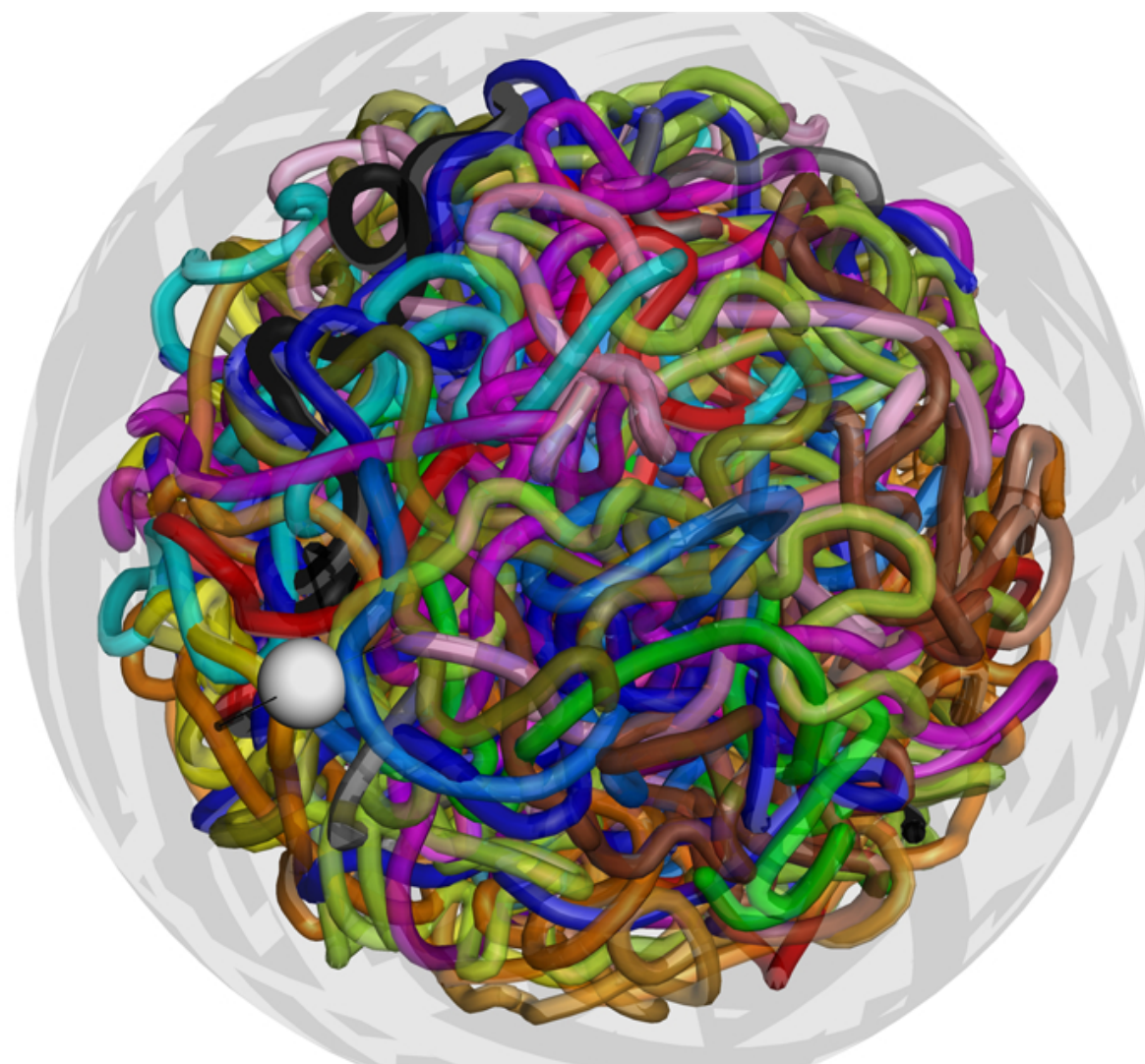
Transcriptional Regulatory Network Shapes the Genome Structure of *Saccharomyces cerevisiae*

Songling Li and Dieter W. Heermann, *Nucleus*. 2013 May-Jun;4(3):216-28



Ansatz: Dynamic Loop Model + genes that are co-regulated by a set of same or similar transcription factors, might stay in physical proximity in order to guarantee the efficiency of gene regulation and expression.

Transcriptional Regulatory Network Shapes the Genome Structure of *Saccharomyces cerevisiae*
Songling Li and Dieter W. Heermann,
Nucleus. 2013 May-Jun;4(3):216-28.

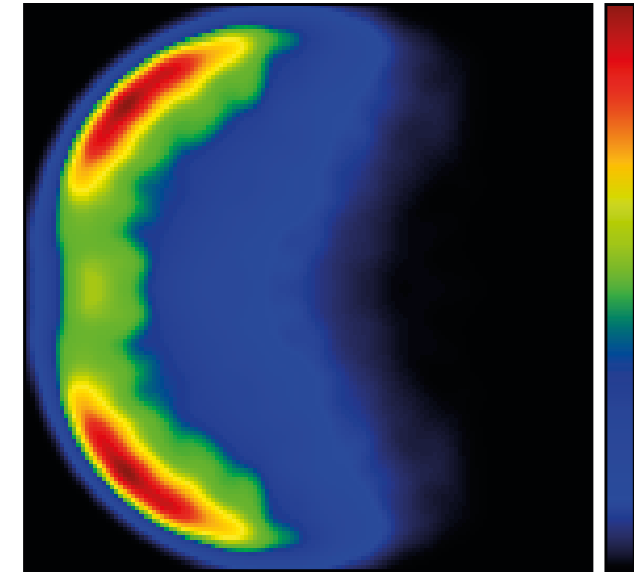
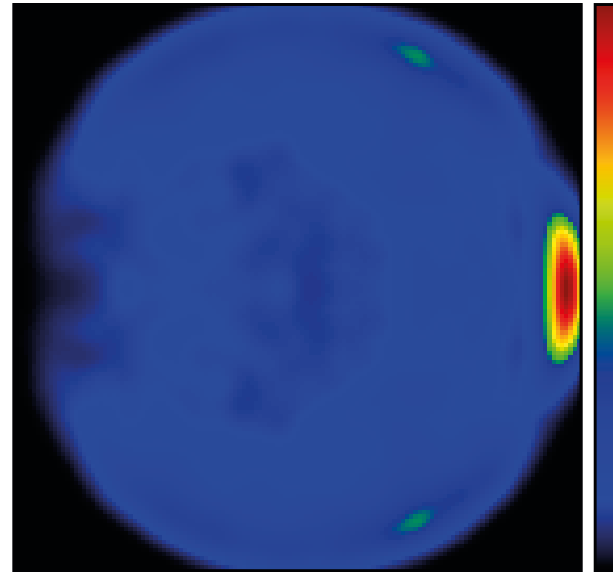
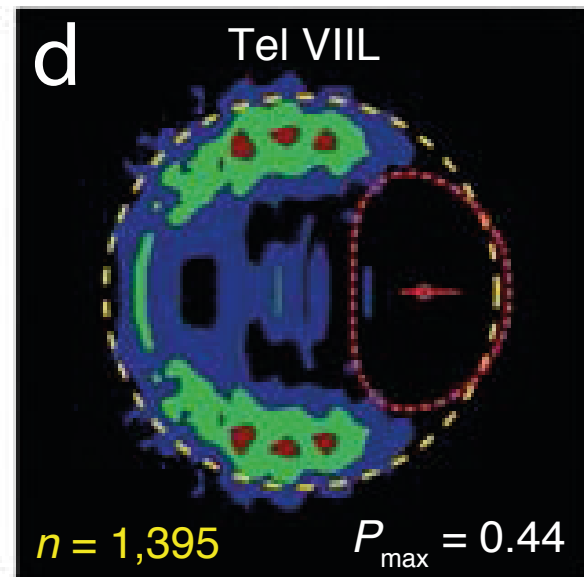


Transcriptional Regulatory Network Shapes the Genome Structure of *Saccharomyces cerevisiae*
Songling Li and Dieter W. Heermann,
Nucleus. 2013 May-Jun;4(3):216-28.

Yeast



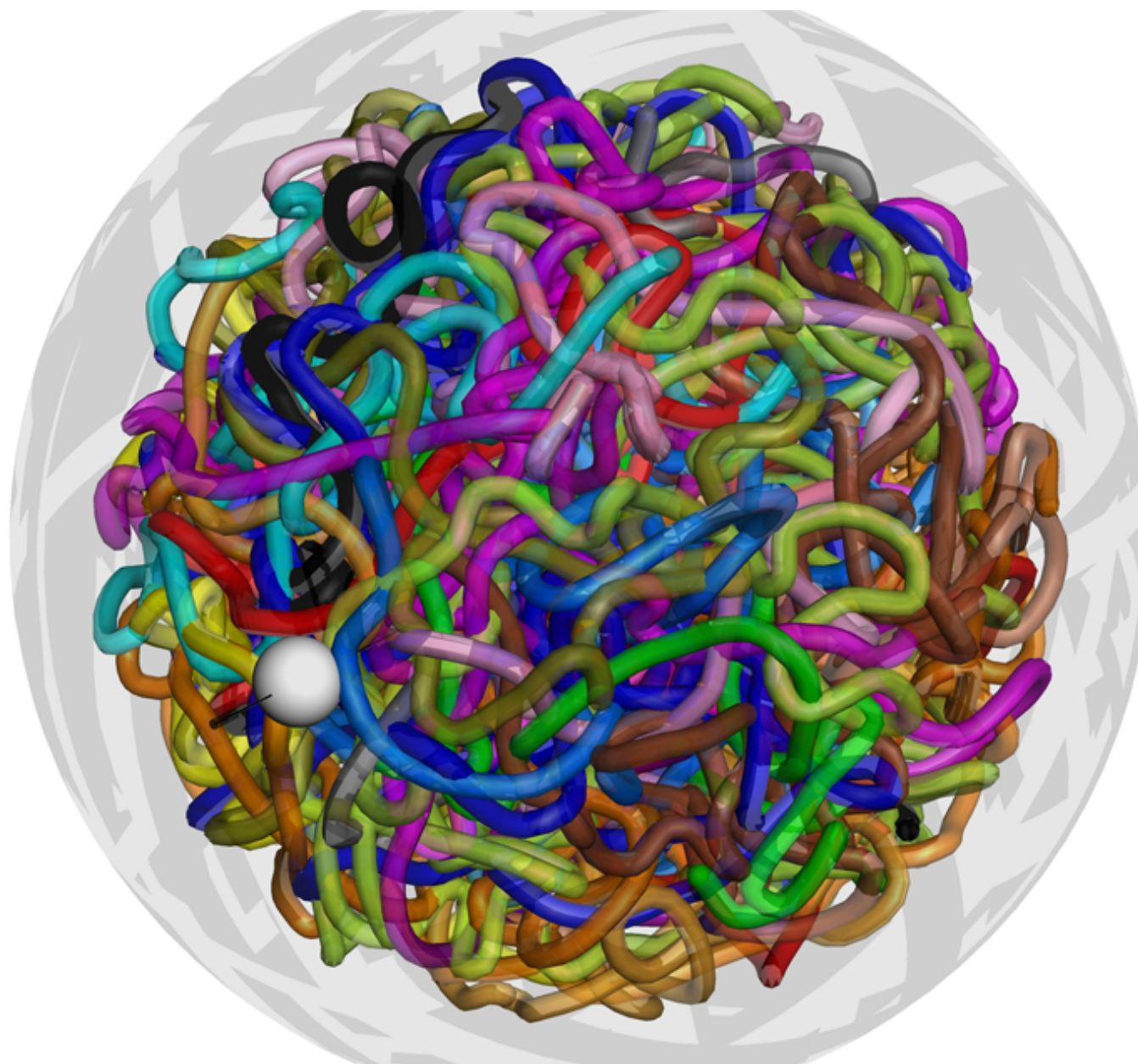
UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



Gene Territories

Data taken from
A. B. Berger, G. G. Cabal, E. Fabre, T. Duong, H. Buc, U. Nehrbass, et al. High-resolution statistical mapping reveals gene territories in live yeast. Nat Methods, 5(12):1031–7, 2008

Transcriptional Regulatory Network Shapes the Genome Structure of *Saccharomyces cerevisiae*
Songling Li and Dieter W. Heermann,
Nucleus. 2013 May-Jun;4(3):216-28.

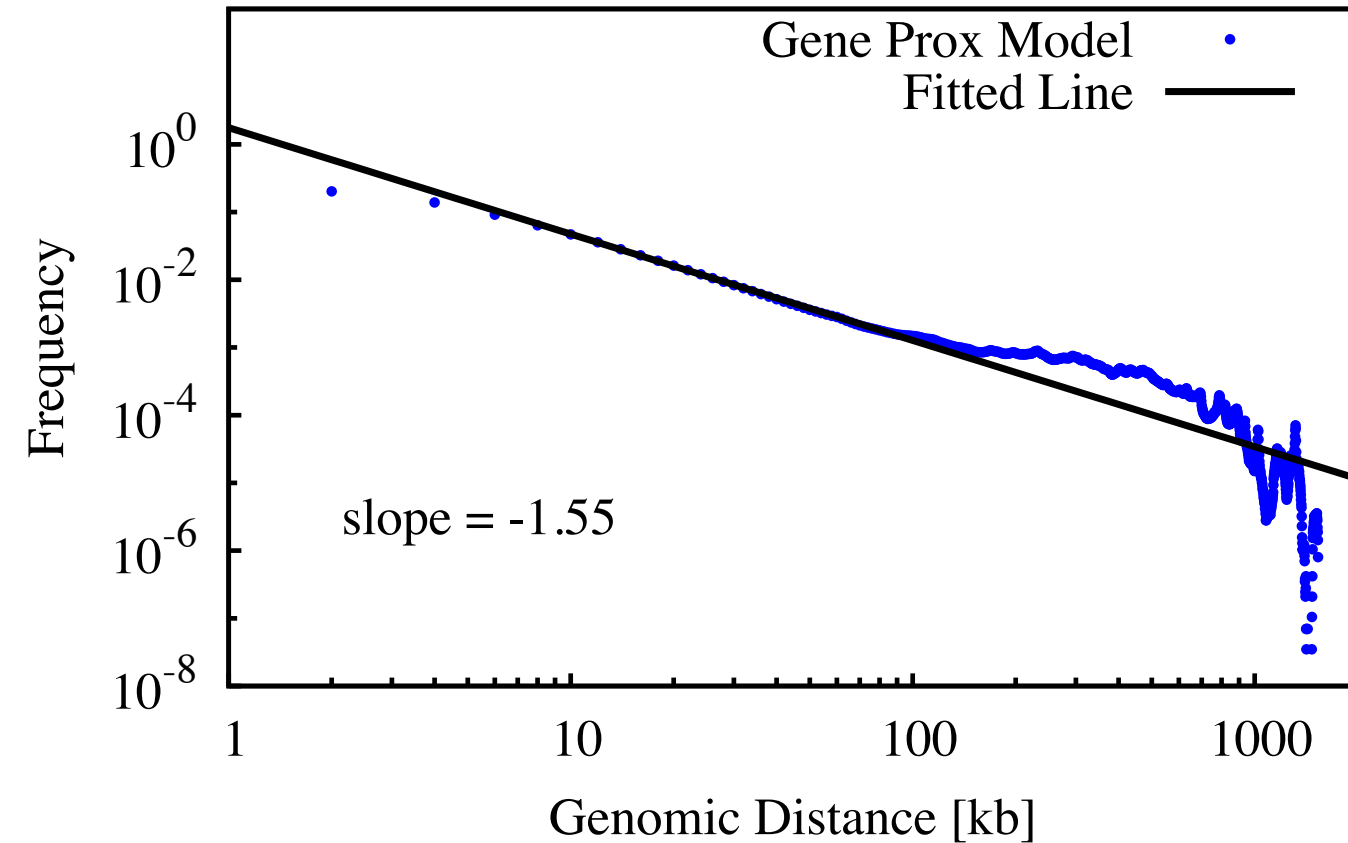
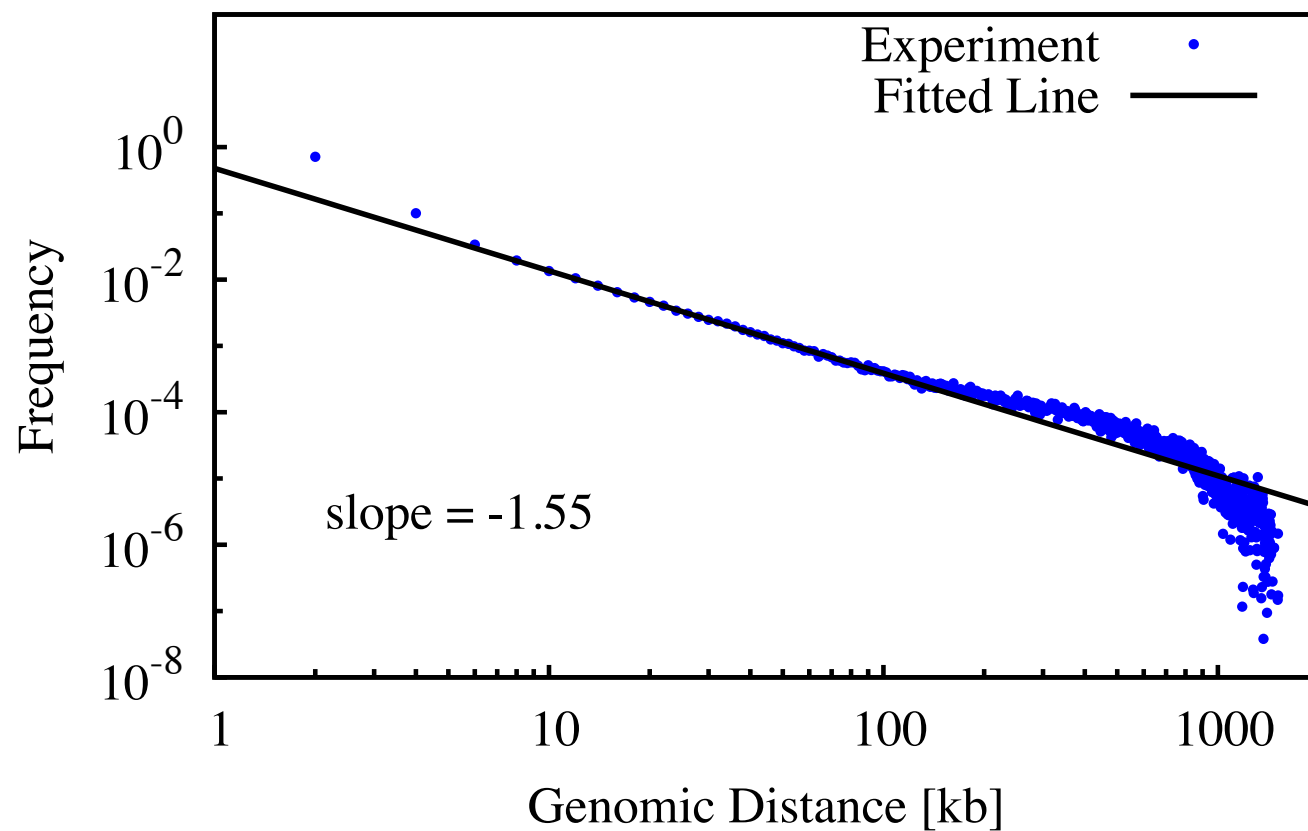


Transcriptional Regulatory Network Shapes the Genome Structure of *Saccharomyces cerevisiae*
Songling Li and Dieter W. Heermann,
Nucleus. 2013 May-Jun;4(3):216-28.

Yeast

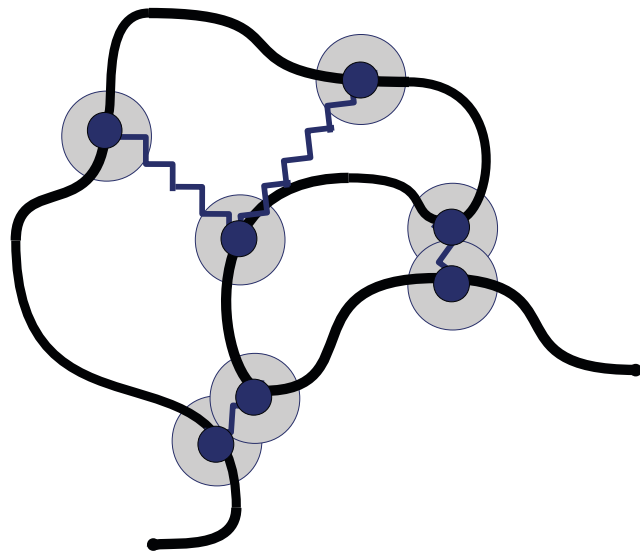


UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386

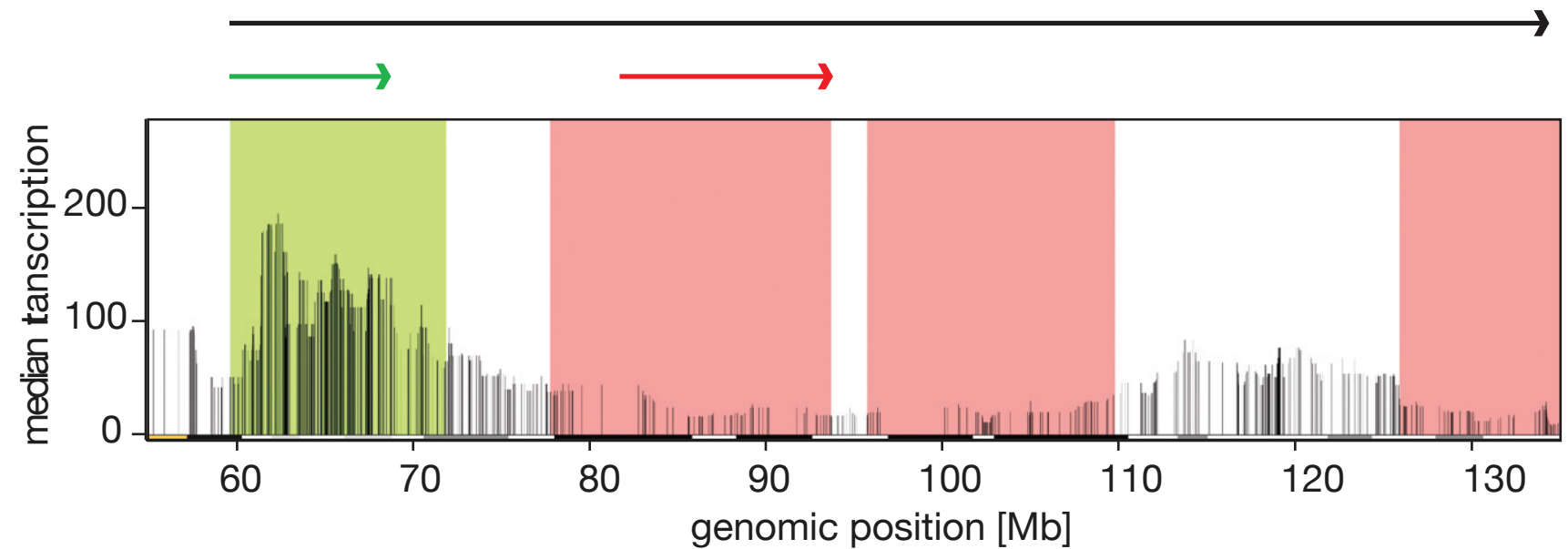


Data: Justin O'Sullivan

Transcriptional Regulatory Network Shapes the Genome Structure of *Saccharomyces cerevisiae*
Songling Li and Dieter W. Heermann,
Nucleus. 2013 May-Jun;4(3):216-28.



Chromosome 11

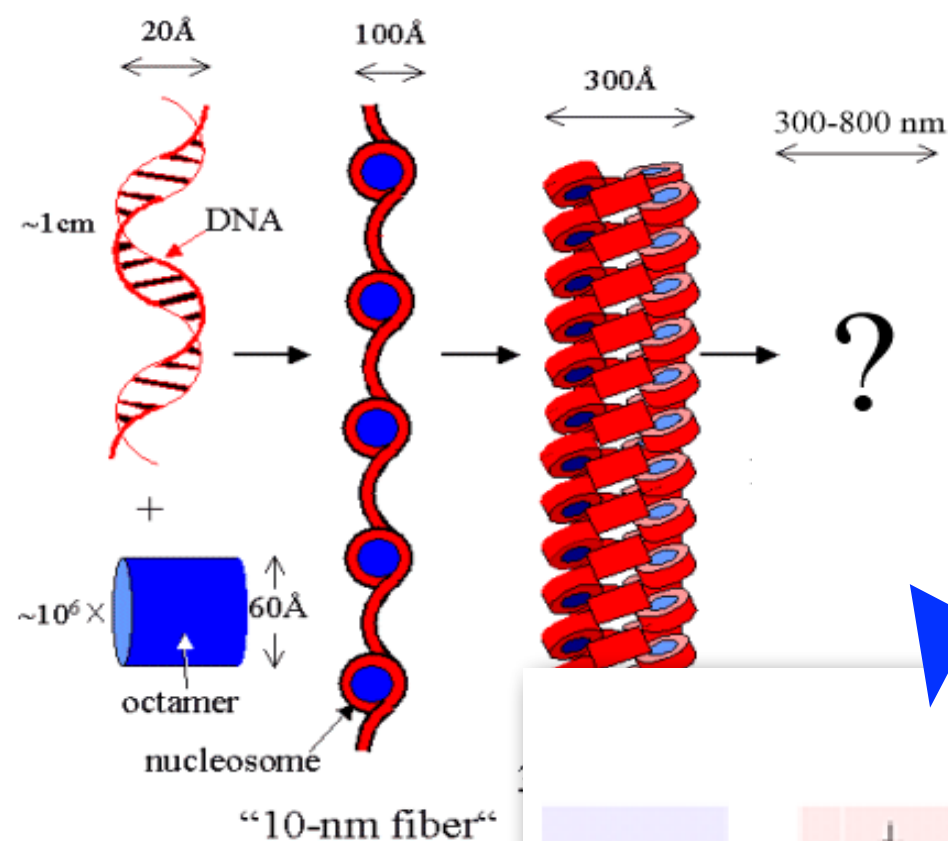


Ansatz: Dynamic Loop Model + gene expression.

Diffusion-Driven Looping Provides a Consistent Framework for Chromatin Organization

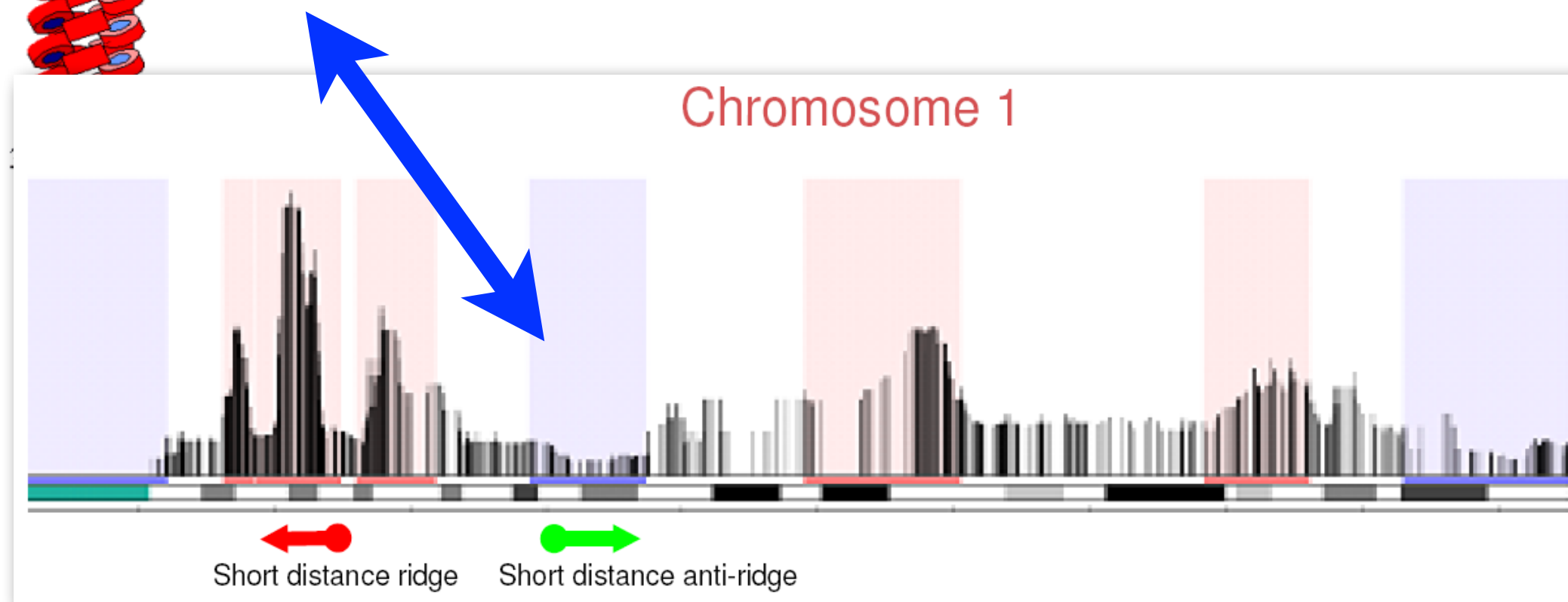
Manfred Bohn and Dieter W. Heermann

PLoS ONE 5(8): e12218. doi:10.1371/journal.pone.0012218 (2010)



M. Bohn, D.W. Heermann and R. van Driel, **Phys. Rev. E** **76**, 051805 (2007)

Julio Mateos-Langerak, Manfred Bohn, Dieter W. Heermann, Roel van Driel and Sandra Goetze, **PNAS** 2009

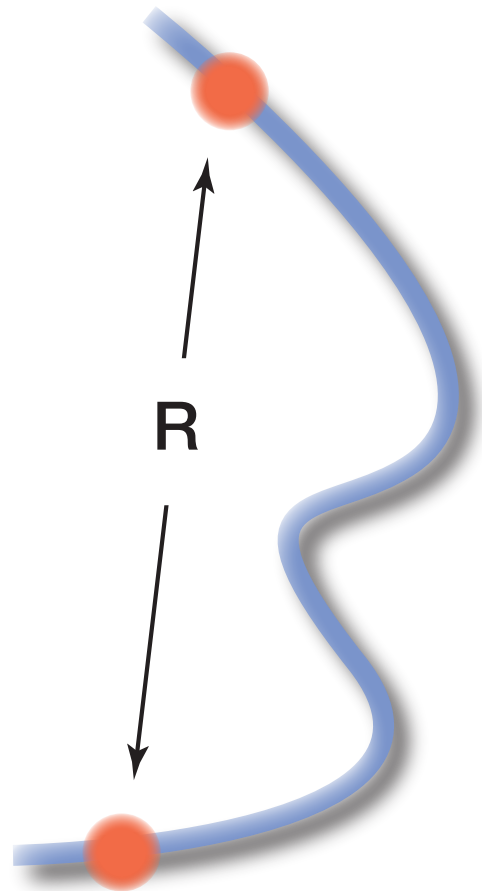


RIDGE: region of increased gene expression

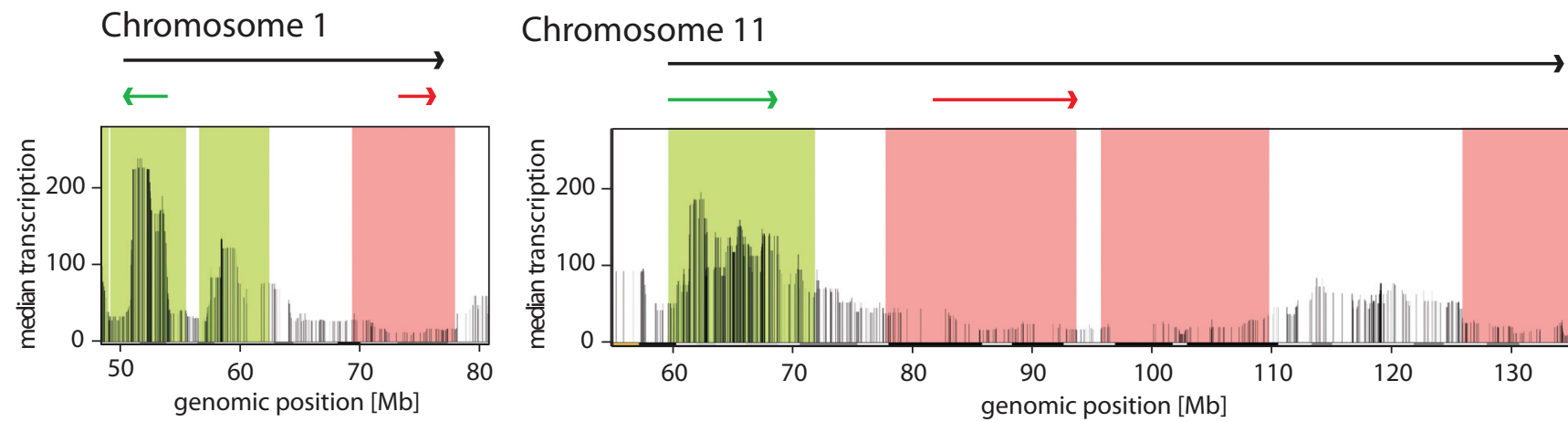
Human Chromosomes



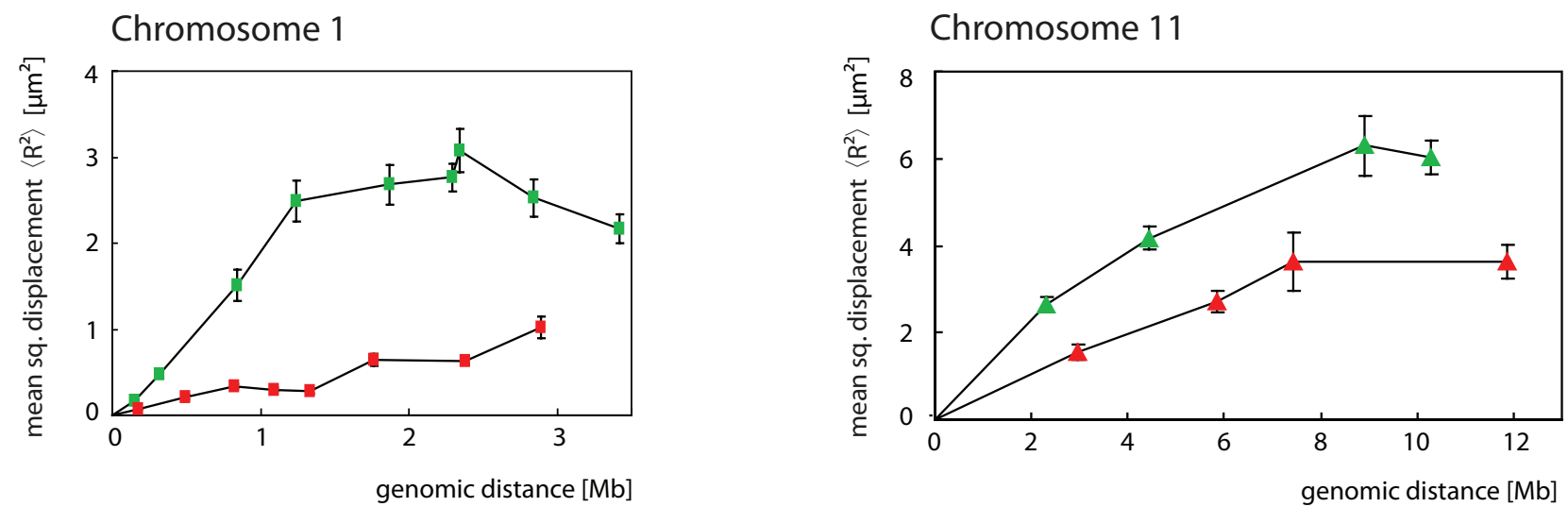
UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



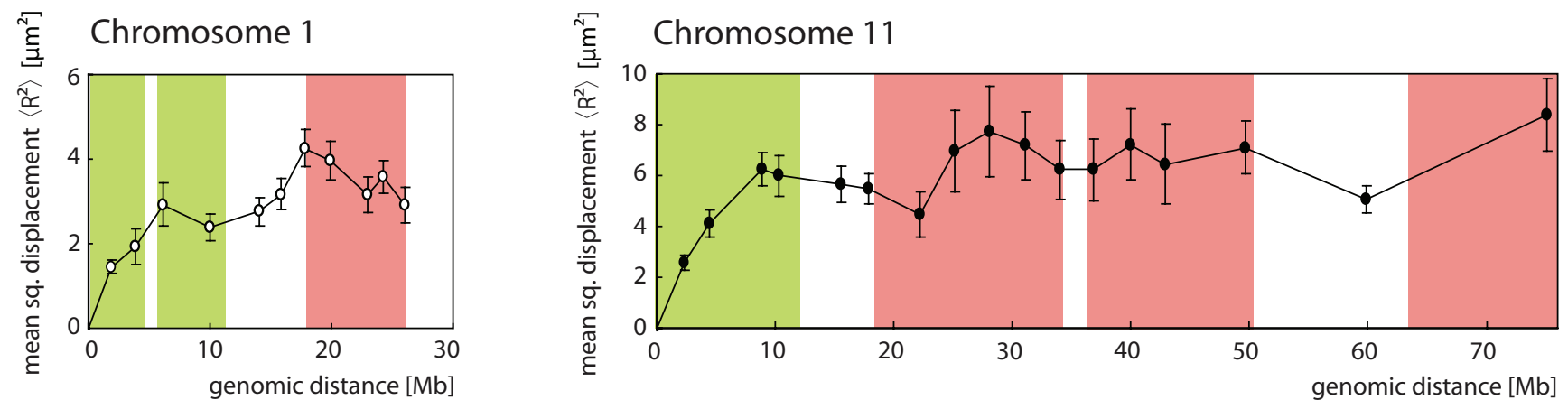
A



B



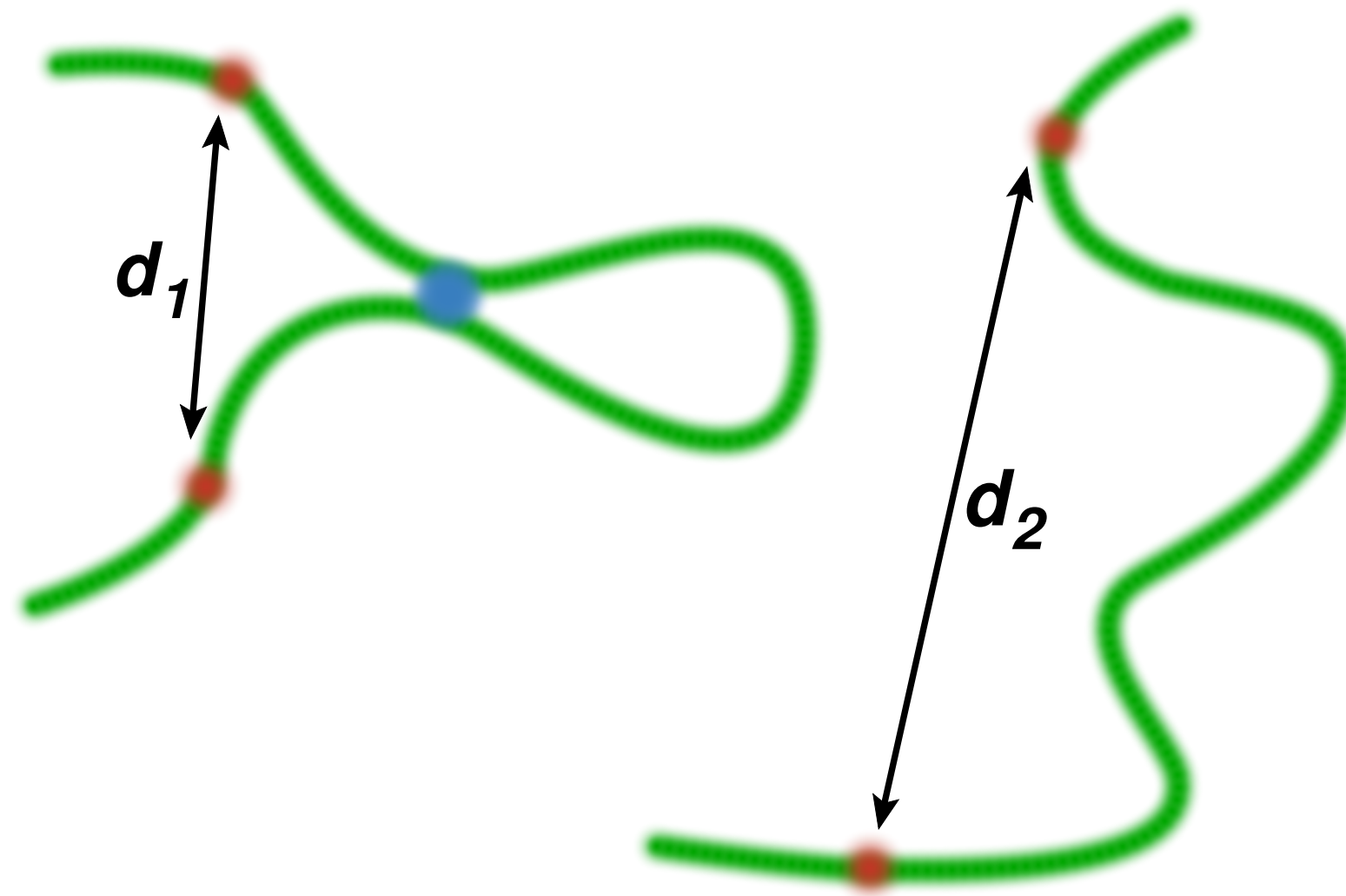
C



Human Chromosomes



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



Diffusion-Driven Looping Provides a Consistent Framework for Chromatin Organization

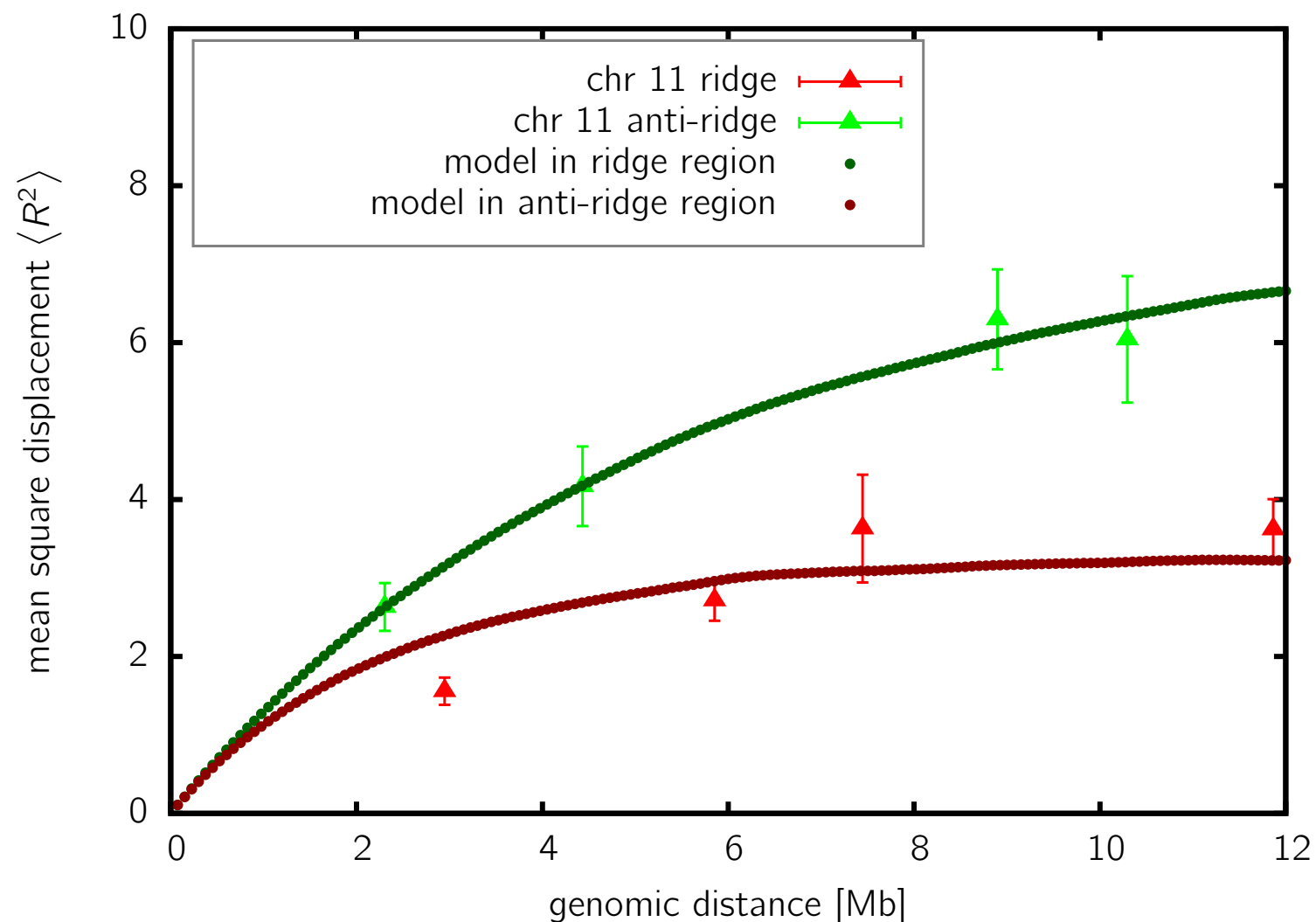
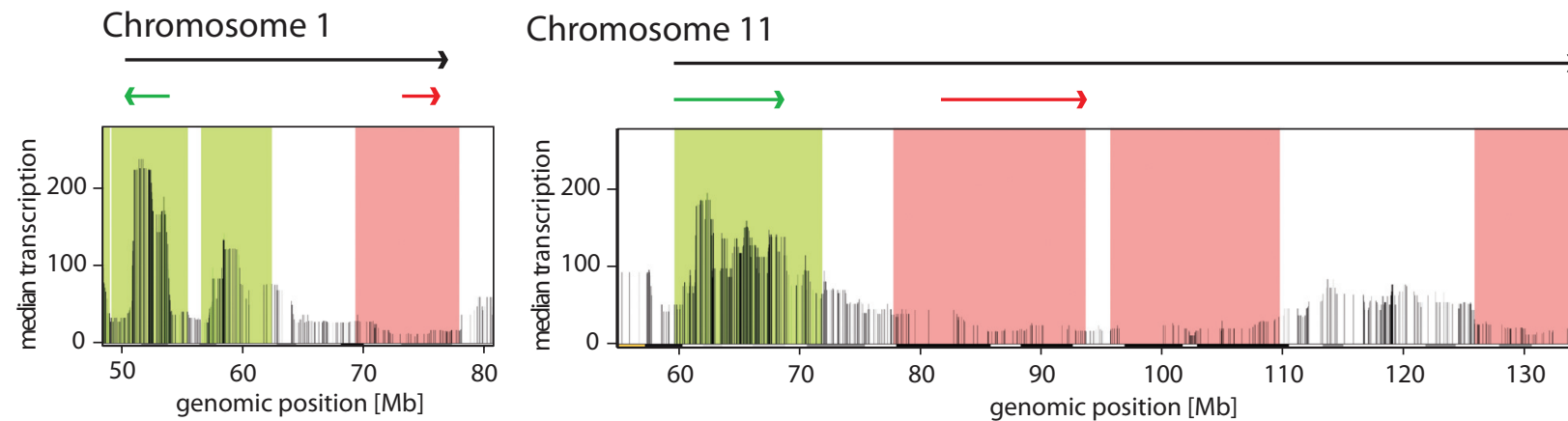
Manfred Bohn and Dieter W. Heermann

PLoS ONE 5(8): e12218. doi:10.1371/journal.pone.0012218 (2010)

Human Chromosomes



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386

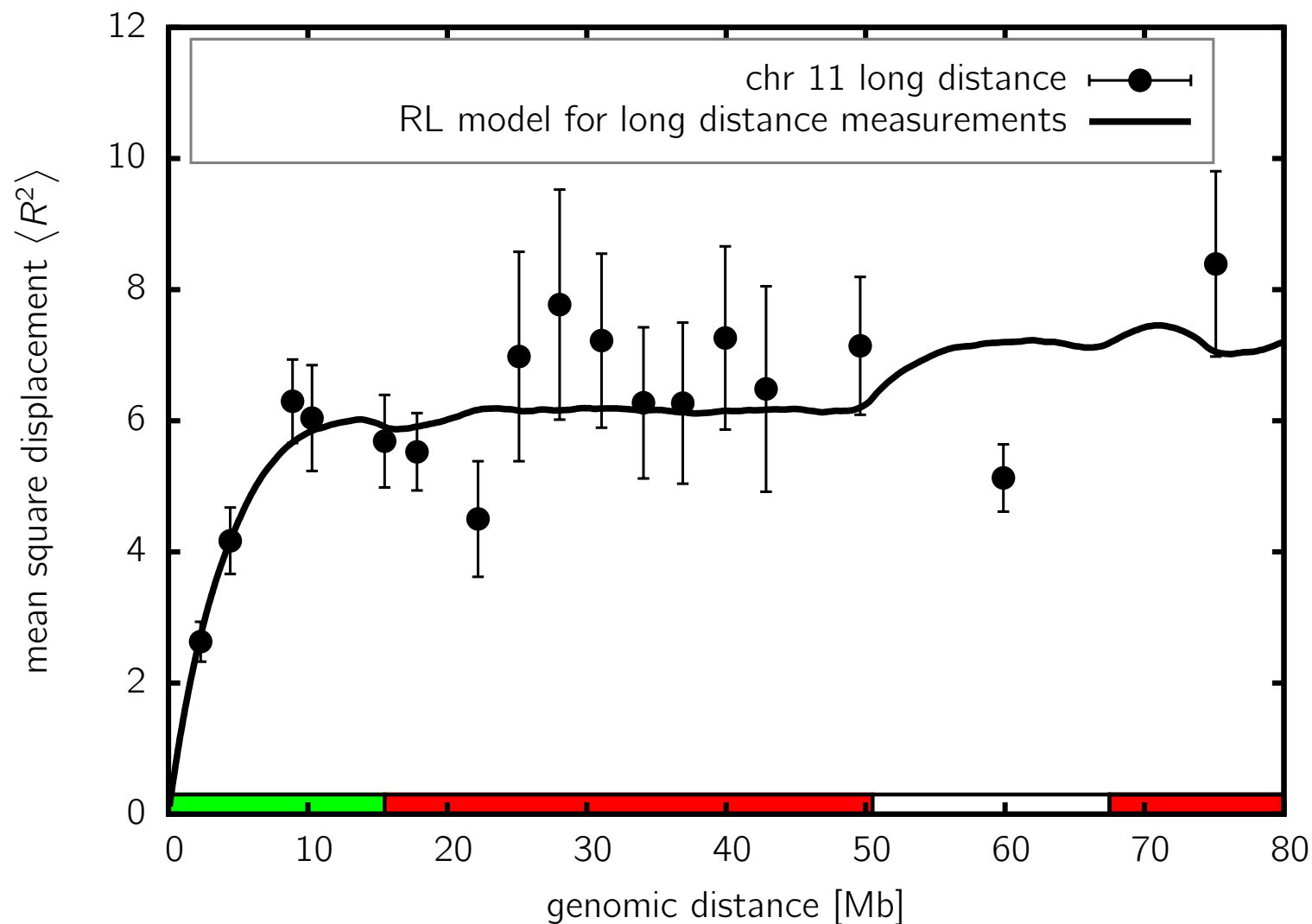
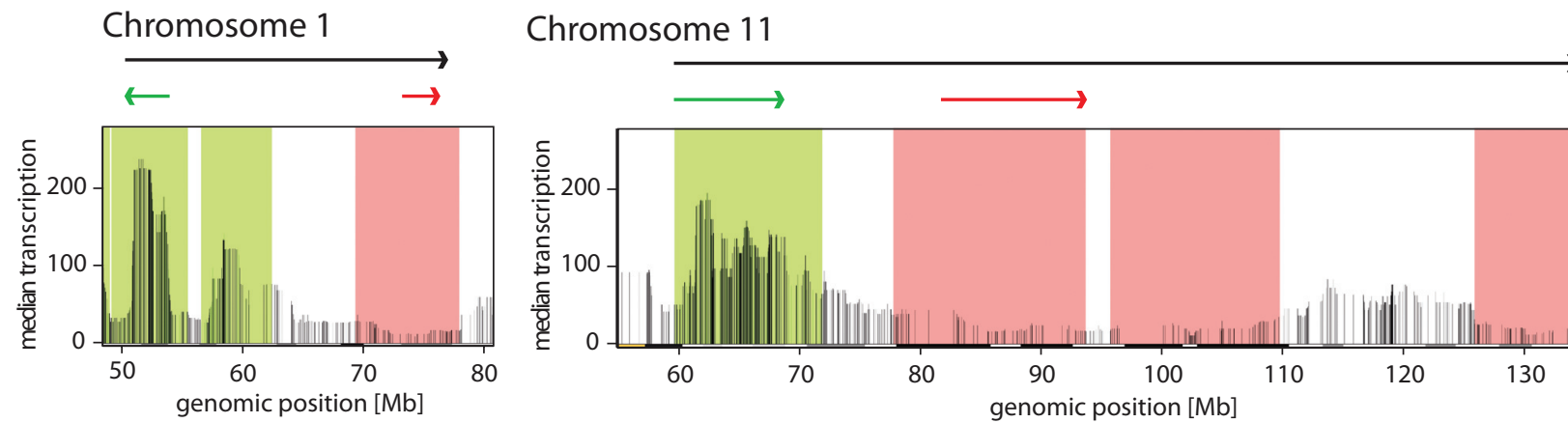


The dynamic loop model very well explains differences between ridges and anti-ridges by different local looping probabilities.

Human Chromosomes



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386

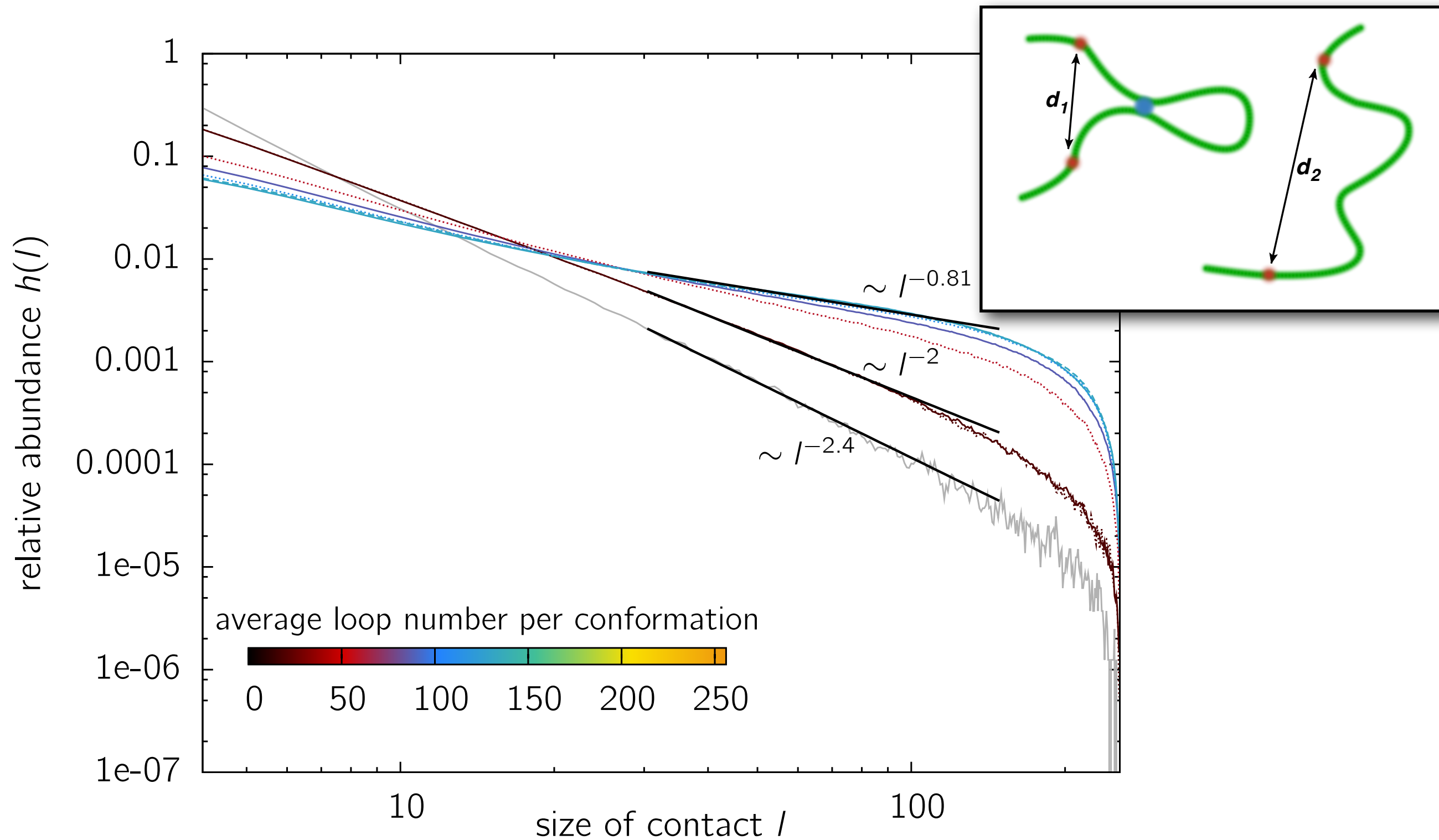


The dynamic loop model also reproduces the experimental findings on the scale of a complete chromosome arm.

Human Chromosomes



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386

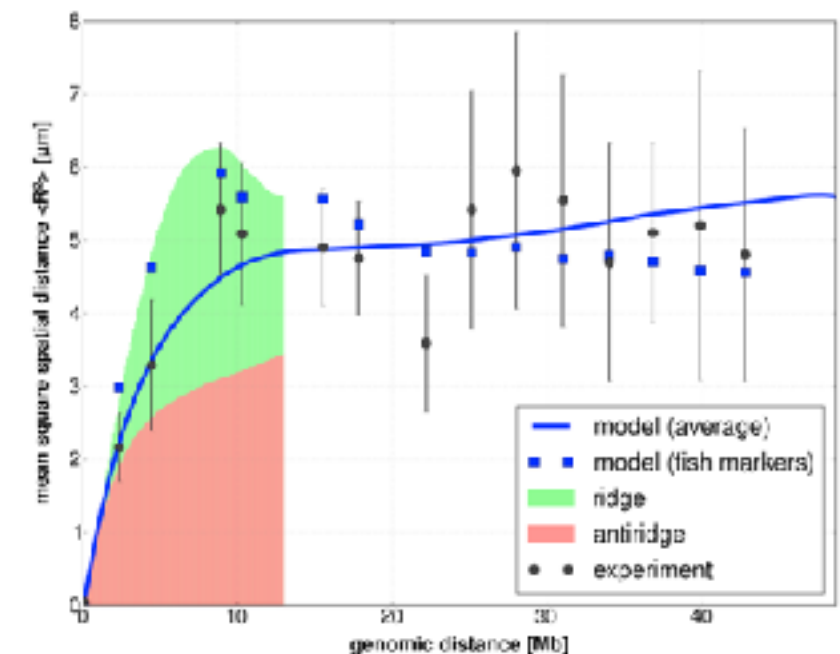
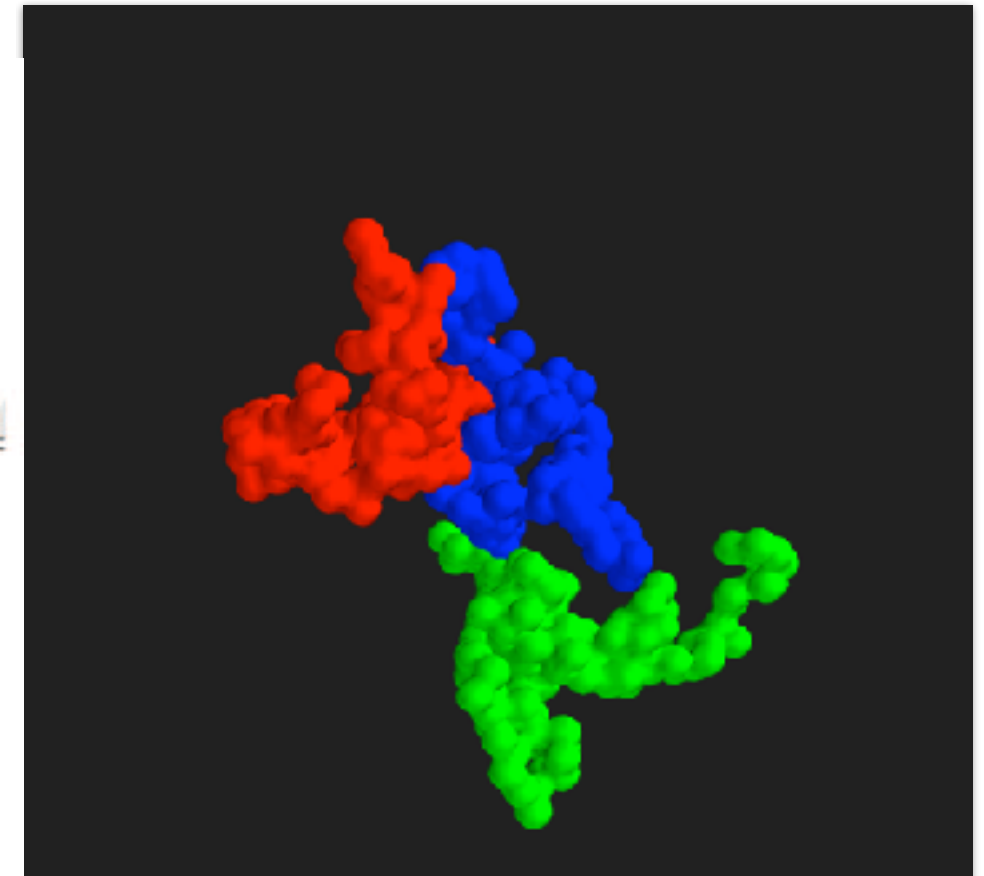
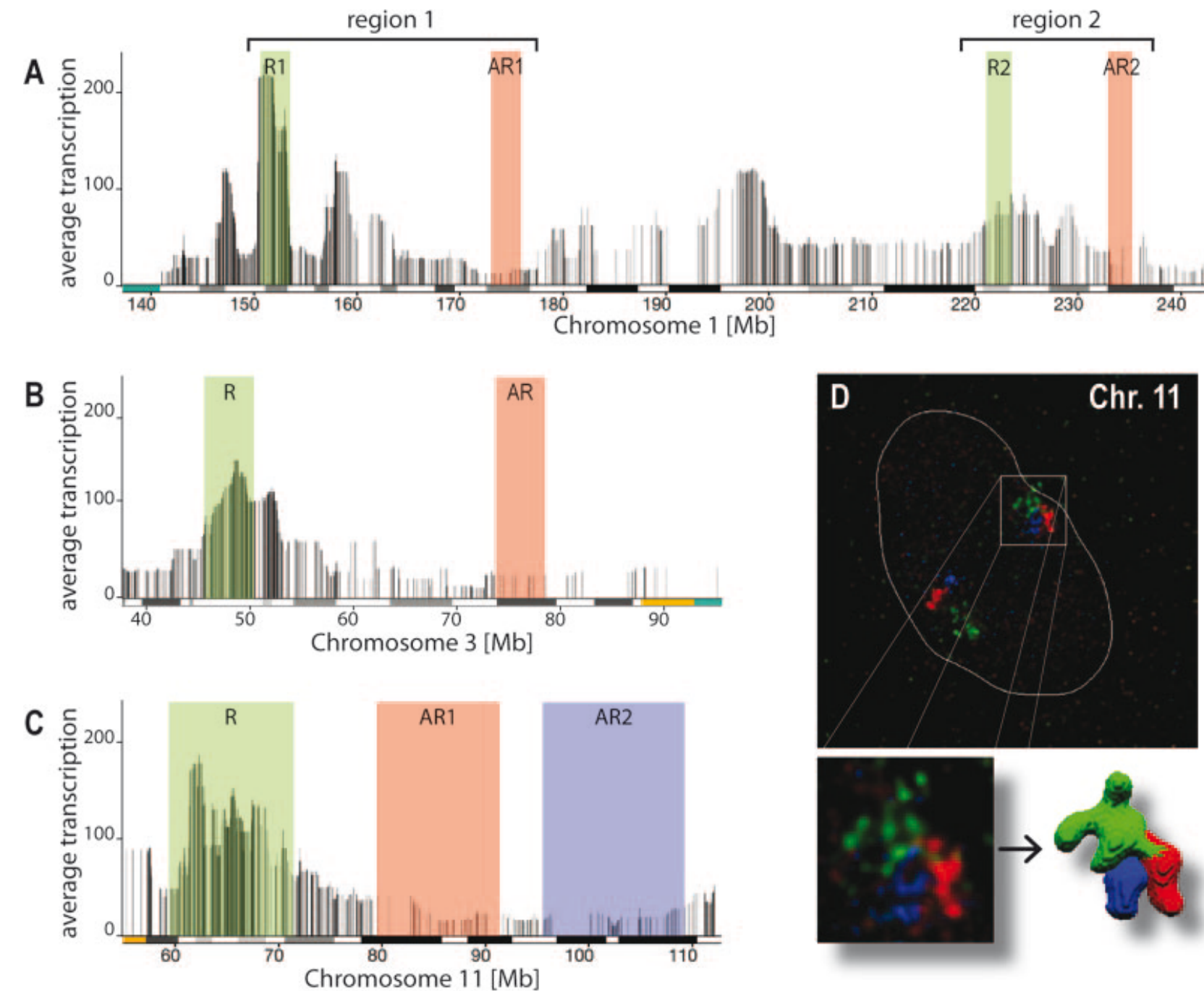


Human Chromosomes



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386

Agrees with Sandra Goetze et. al. MOLECULAR AND CELLULAR BIOLOGY, June 2007, p. 4475–4487





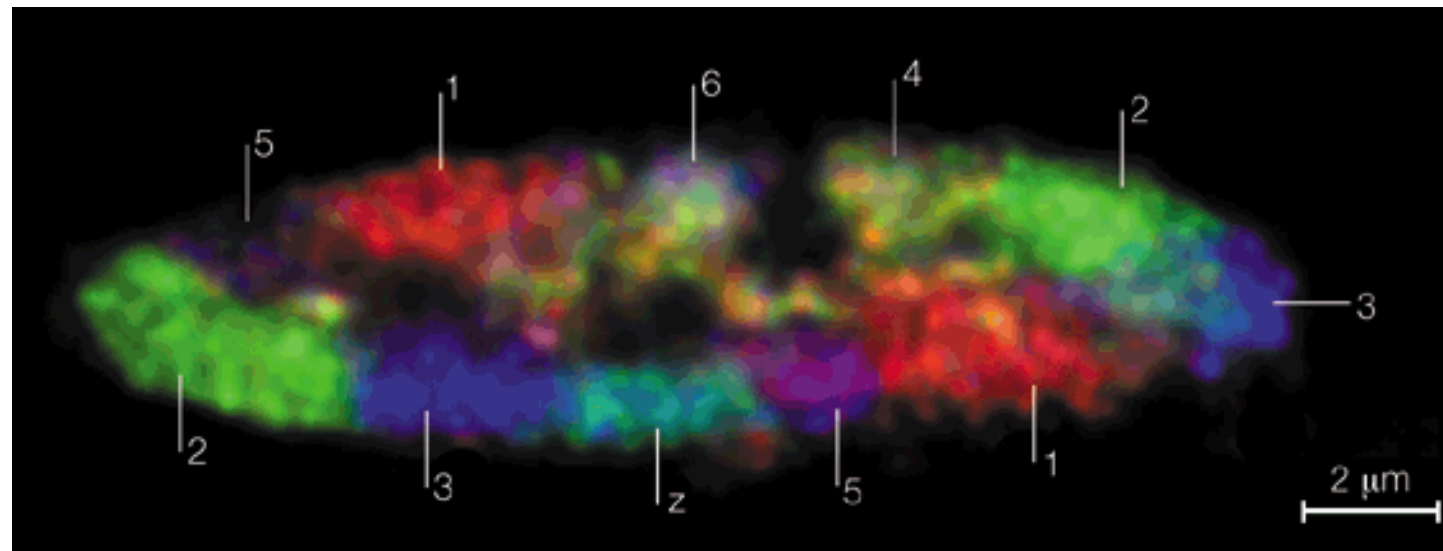
We understand the folding pattern of chromosomes in interphase:

Folding is governed by loops on all scales mediated by proteins (transcriptional hubs, ...)

Human Chromosomes



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



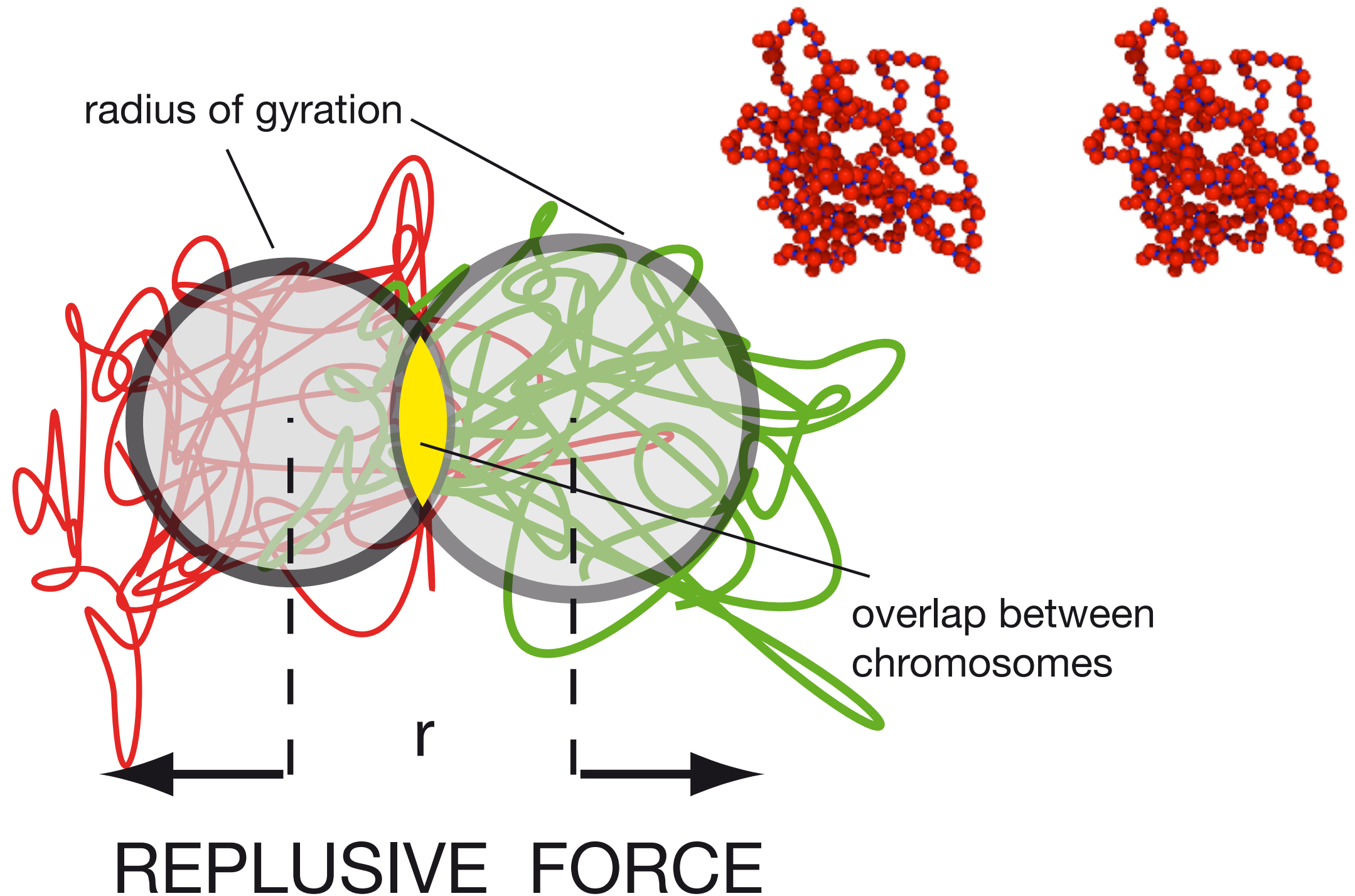
T.Cremer and C. Cremer, Nature Reviews
Genetics vol. 2, no. 4, pp. 292-301 (April,
2001)

Why do chromosomes not mix?

Human Chromosomes



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386

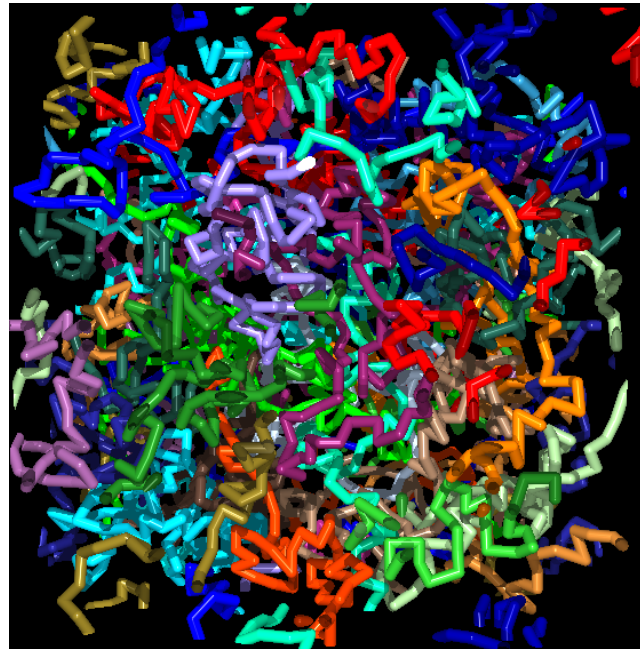


Human Chromosomes

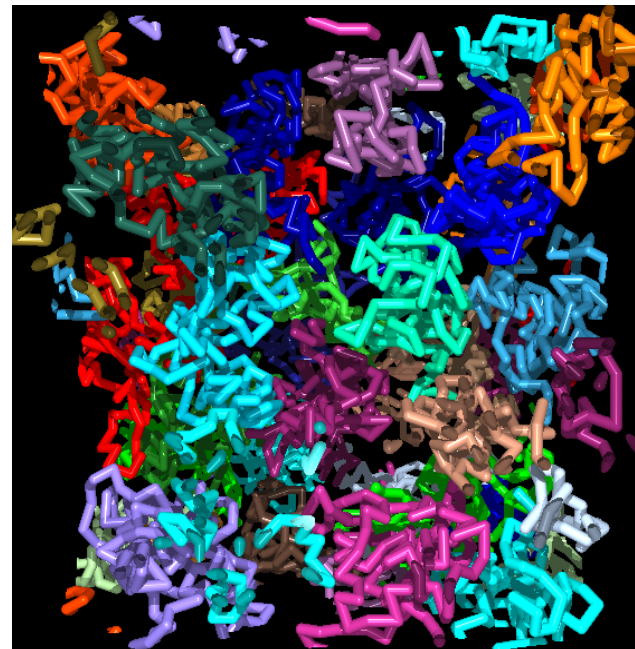


UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386

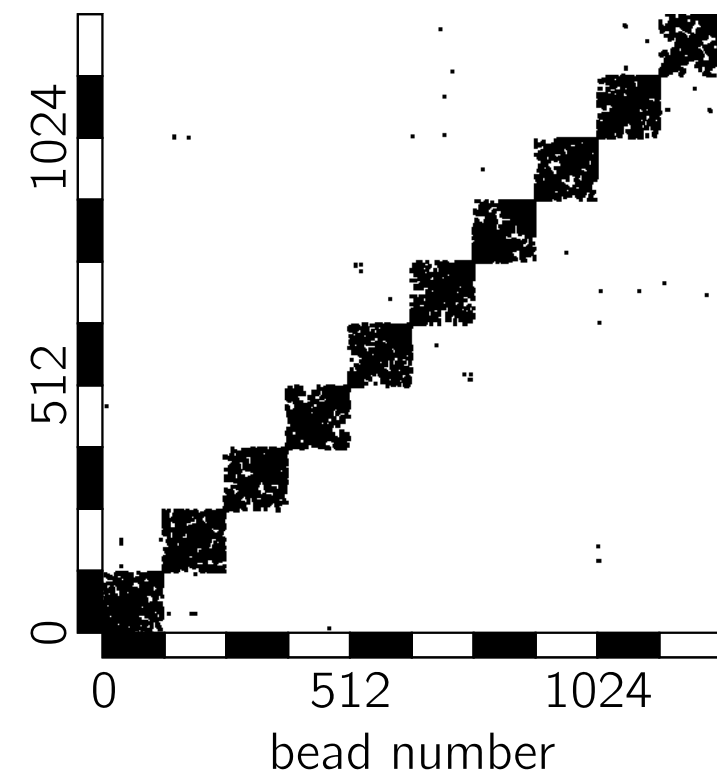
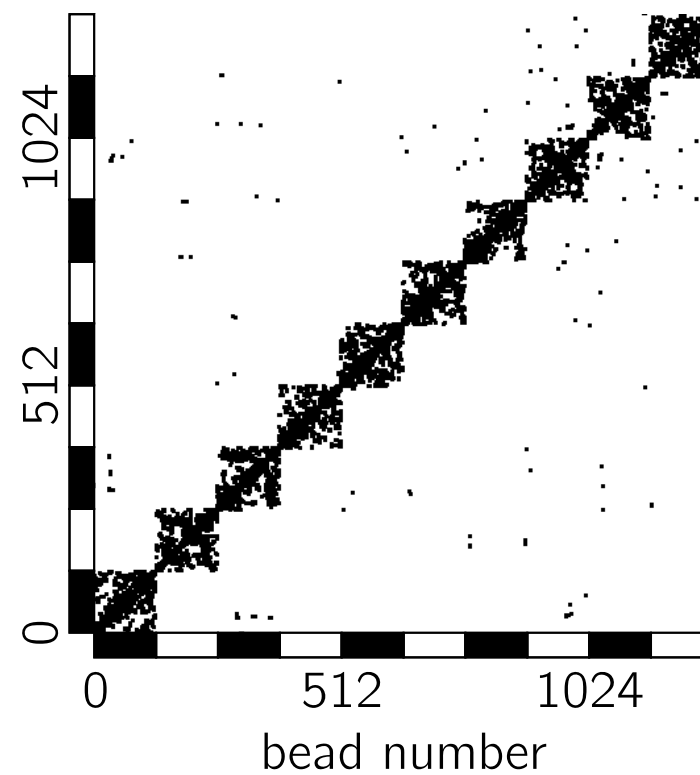
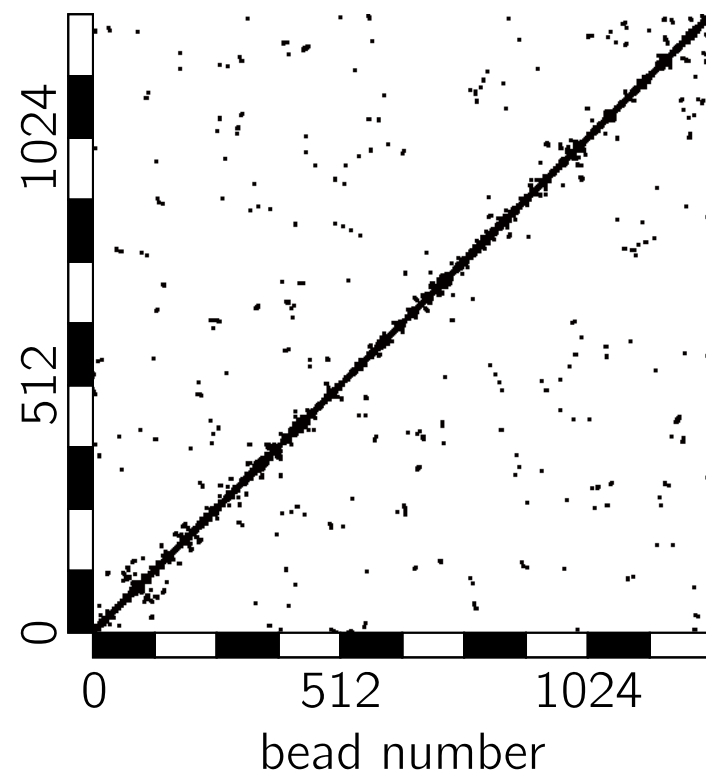
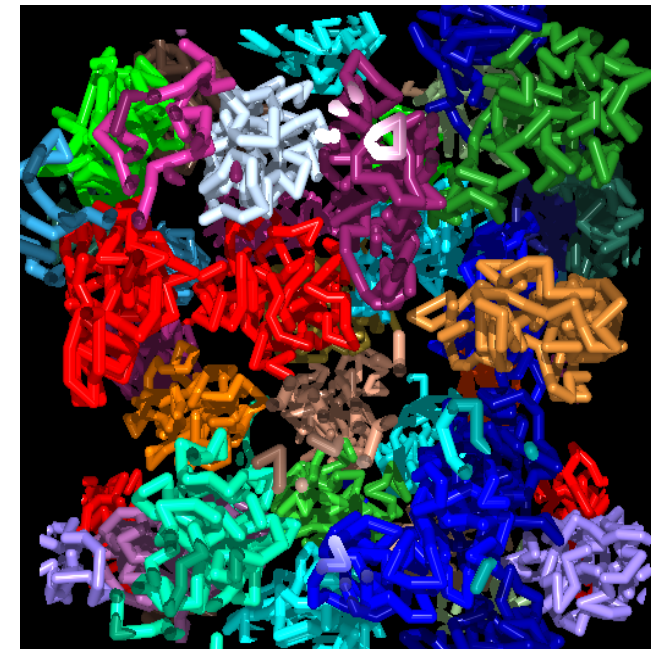
A. Linear chains



B. 45 loops per chain



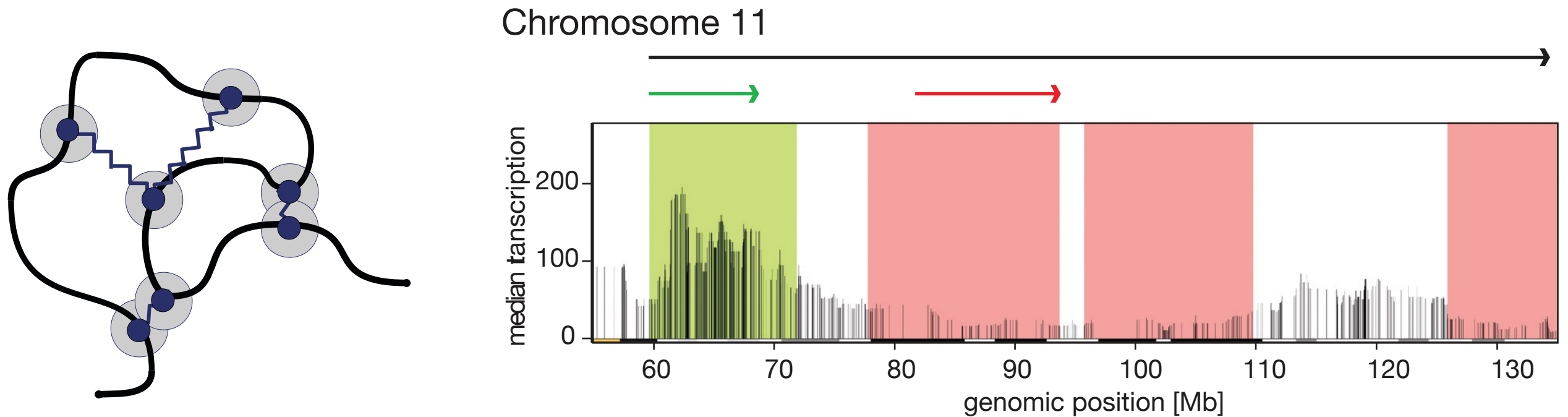
C. 92 loops per chain



Chromosomes in Metaphase



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



Ansatz: Dynamic Loop Model + gene expression.

Loops Determine the Mechanical Properties of Mitotic Chromosomes.

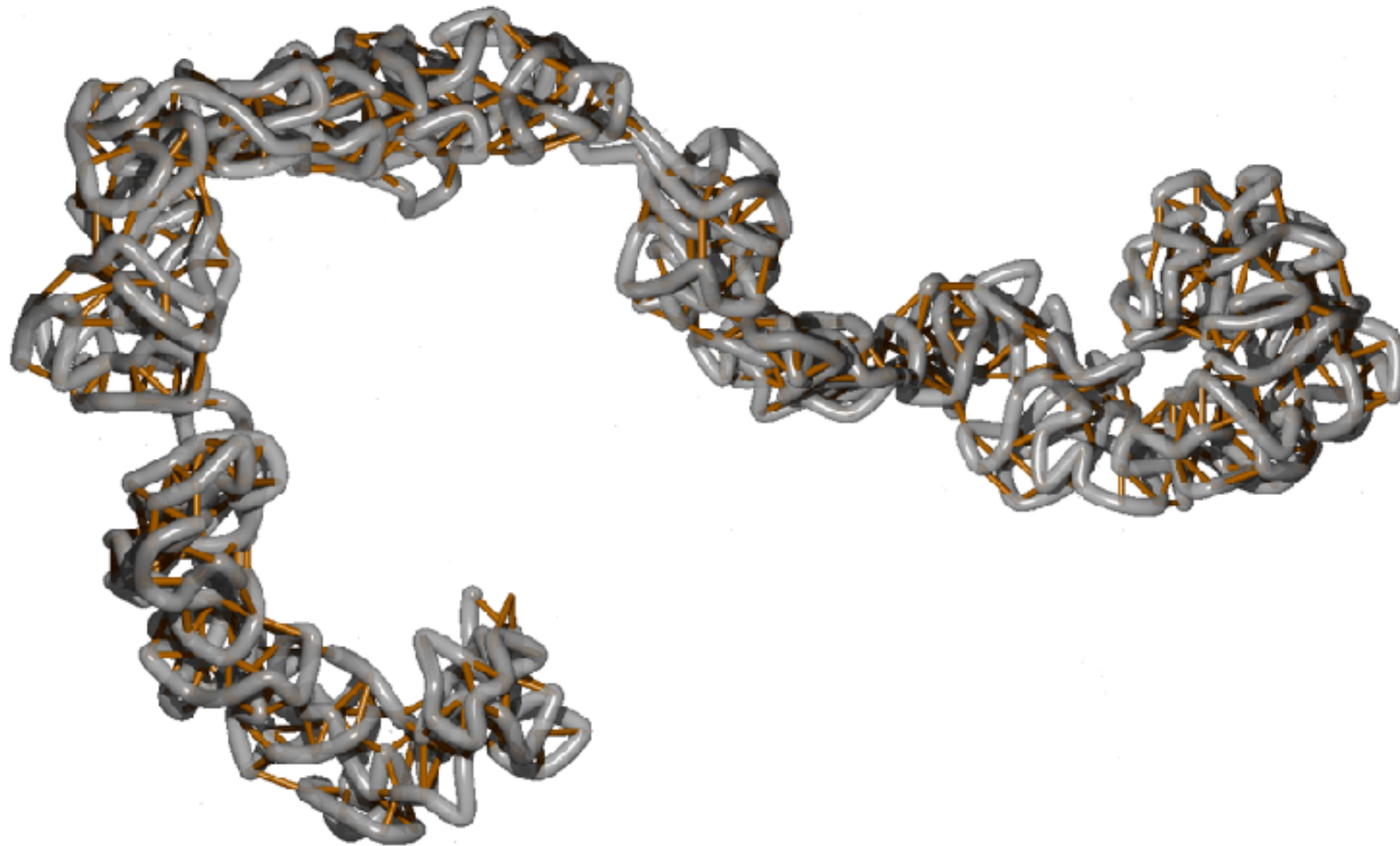
Zhang Y, Heermann DW (2011)

PLoS ONE 6(12): e29225. doi:10.1371/journal.pone.0029225

Chromosomes in Metaphase



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



Loops Determine the Mechanical Properties of Mitotic Chromosomes.

Zhang Y, Heermann DW (2011)

PLoS ONE 6(12): e29225. doi:10.1371/journal.pone.0029225

Chromosomes in Metaphase

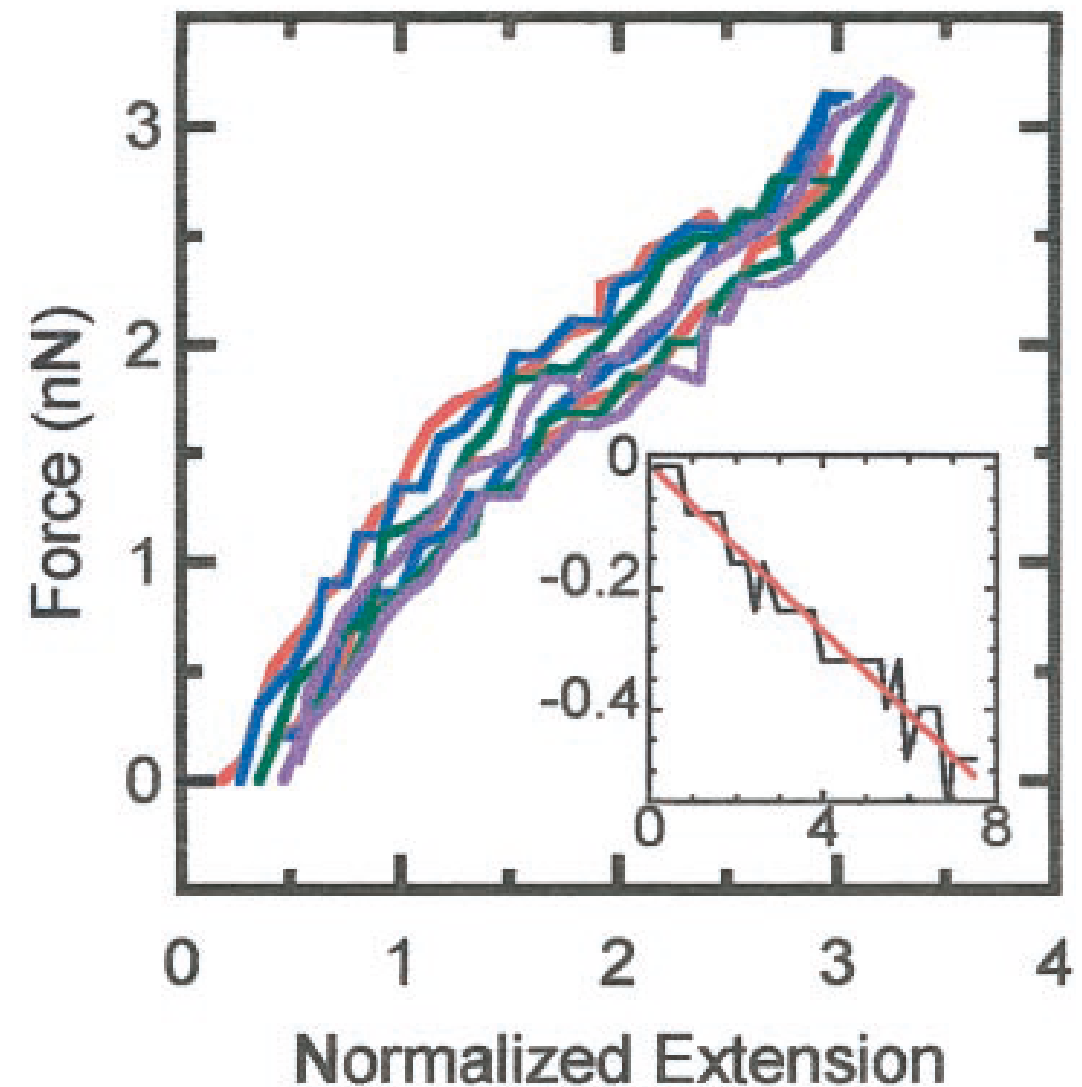
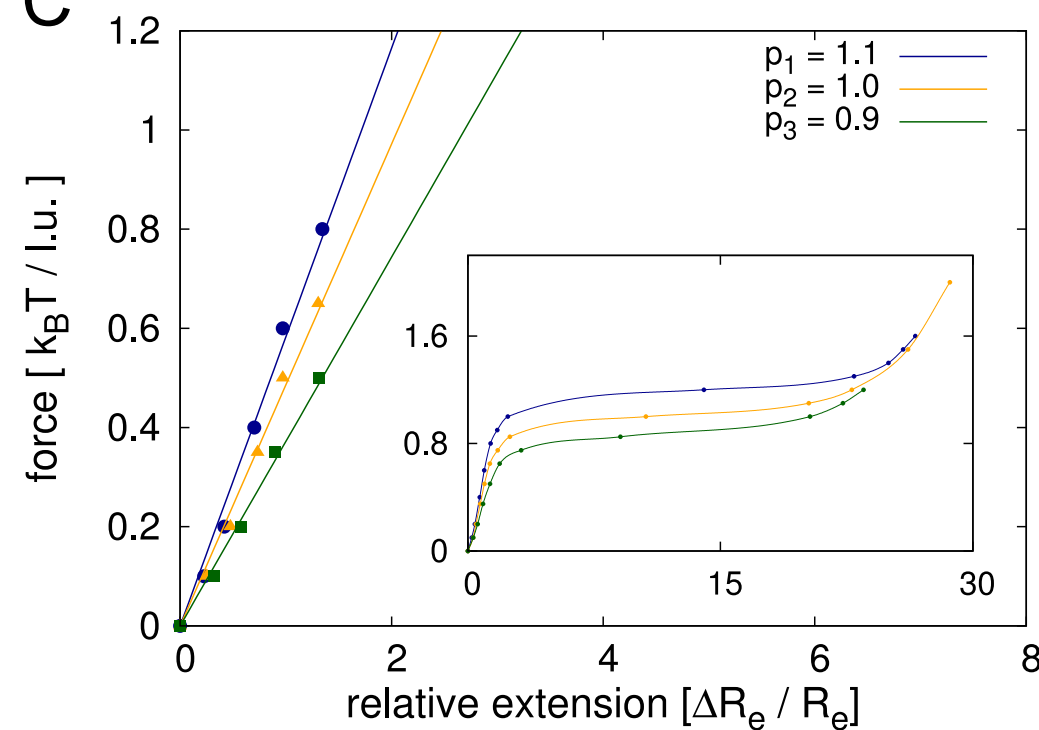


UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386

A



C



Reversible and Irreversible Unfolding of Mitotic Newt Chromosomes by Applied Force

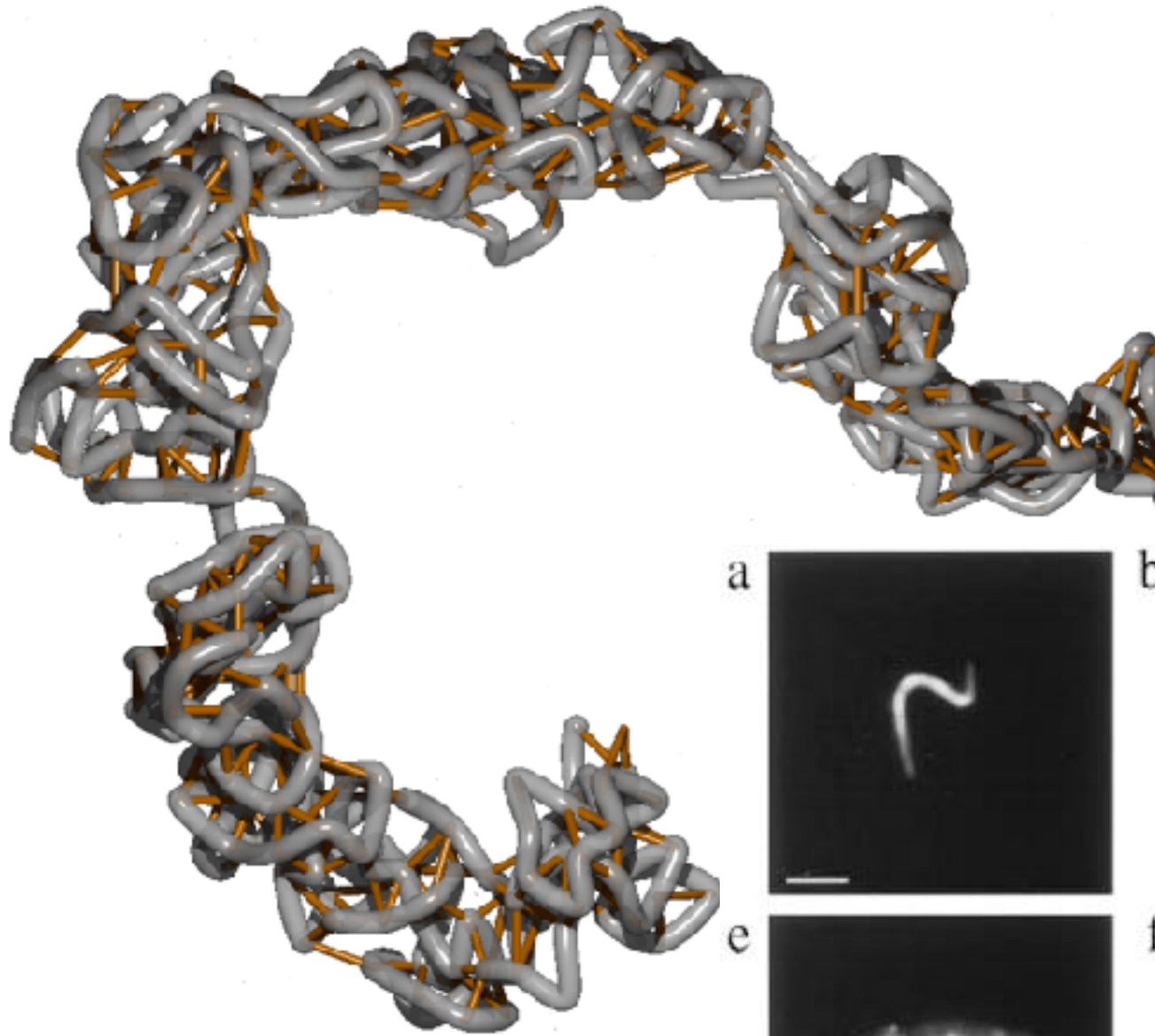
Michael Poirier, Sertac Eroglu Didier Chatenay, and John F. Marko

Mol Biol Cell. 2000 January; 11(1): 269–276.

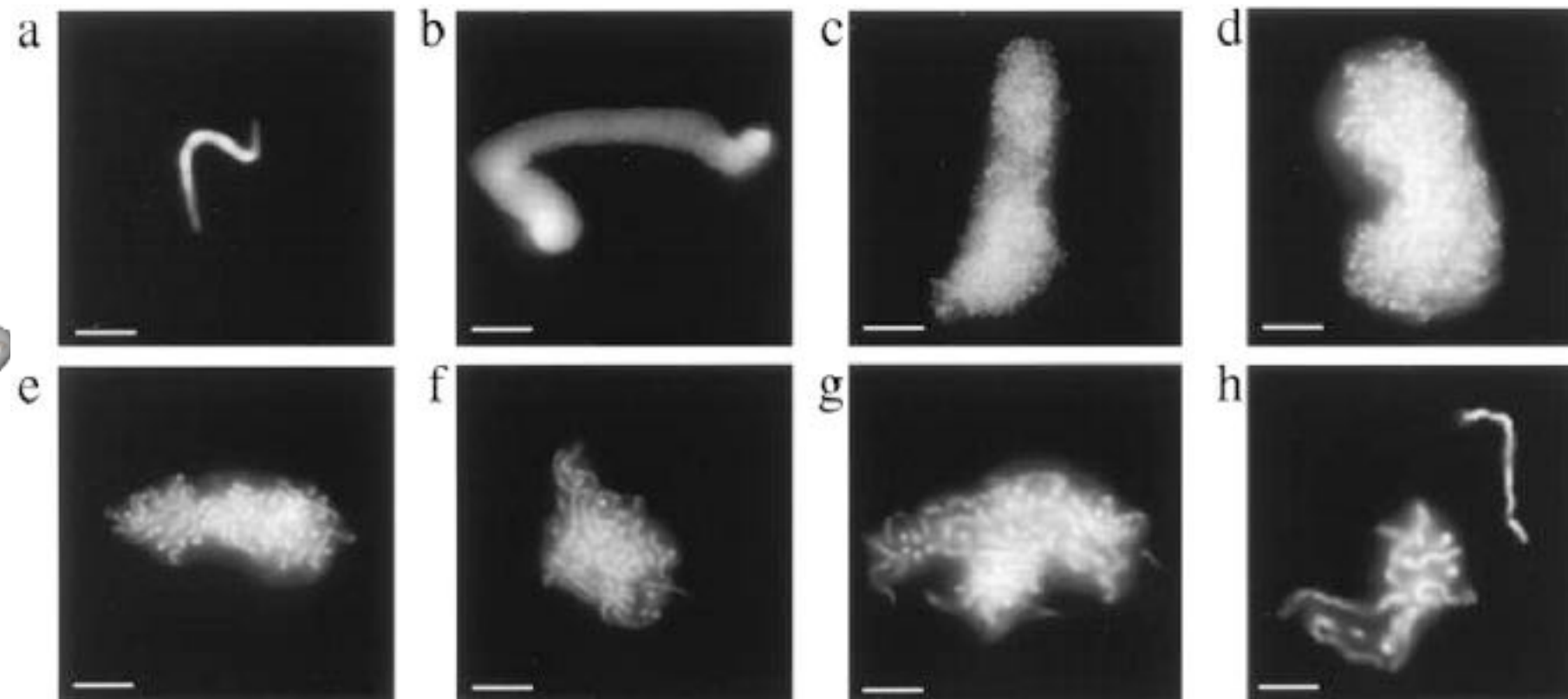
Chromosomes in Metaphase



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386



Structural changes of *Xenopus* sperm nuclei in mitotic egg extract; control sperm nuclei (a), decondensed sperm after 10 min of incubation in the extract (b), chromosomal structures (c–g) found after 30, 60, 90, 120, and 150 min, respectively.



Houchmandzadeh B , Dimitrov S J Cell Biol 1999;145:215-223

Chromosomes in Metaphase

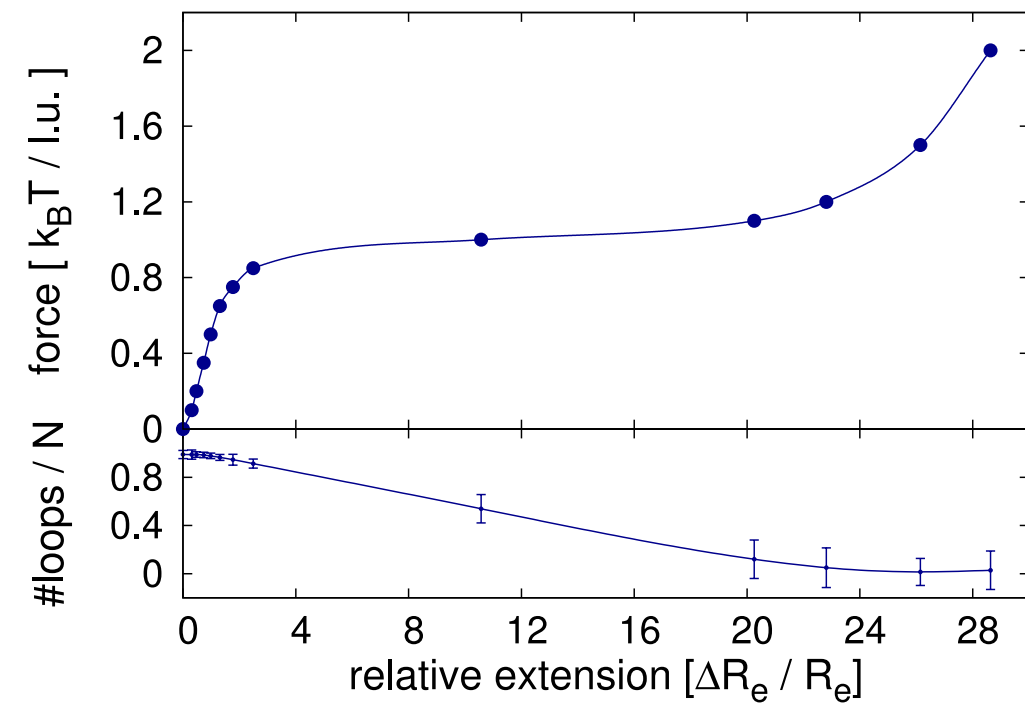


UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386

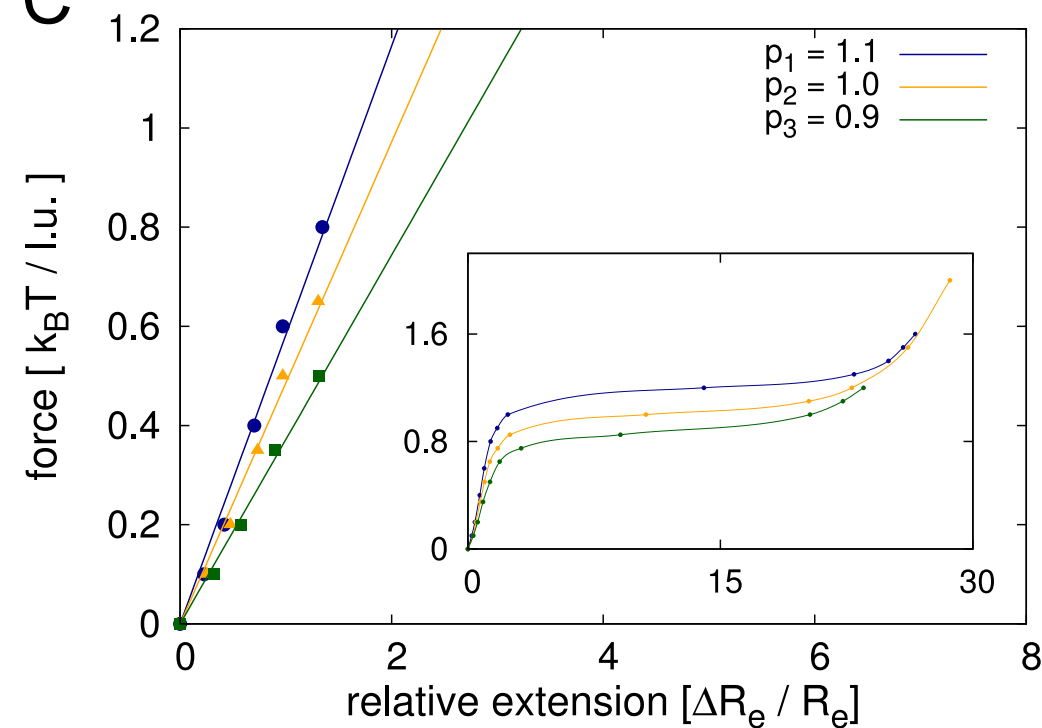
A



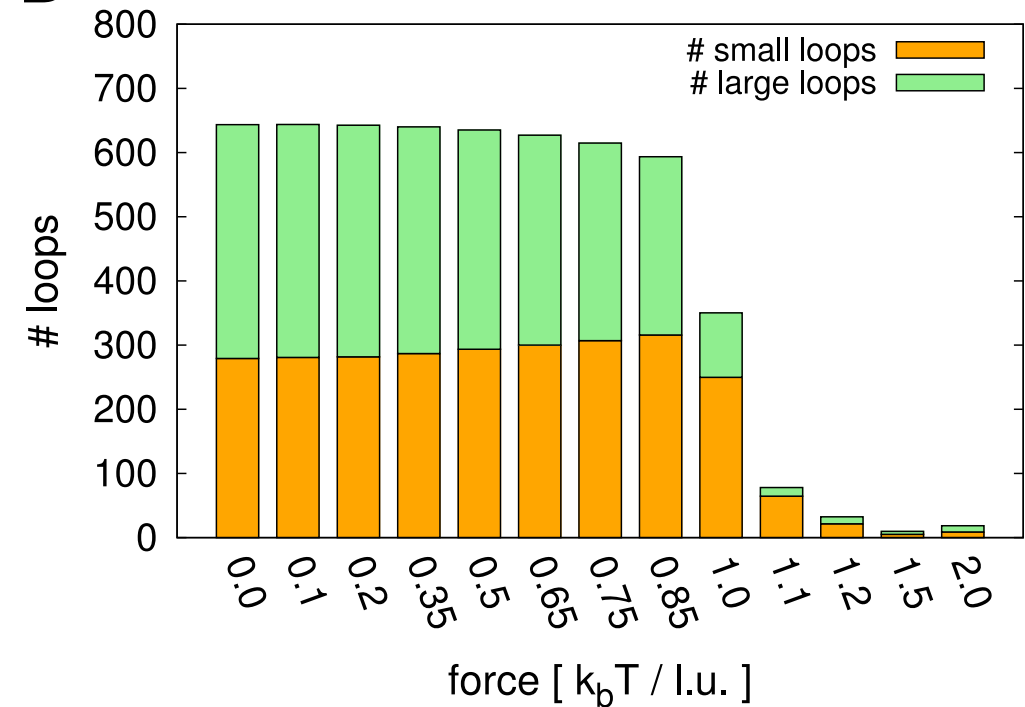
B



C



D



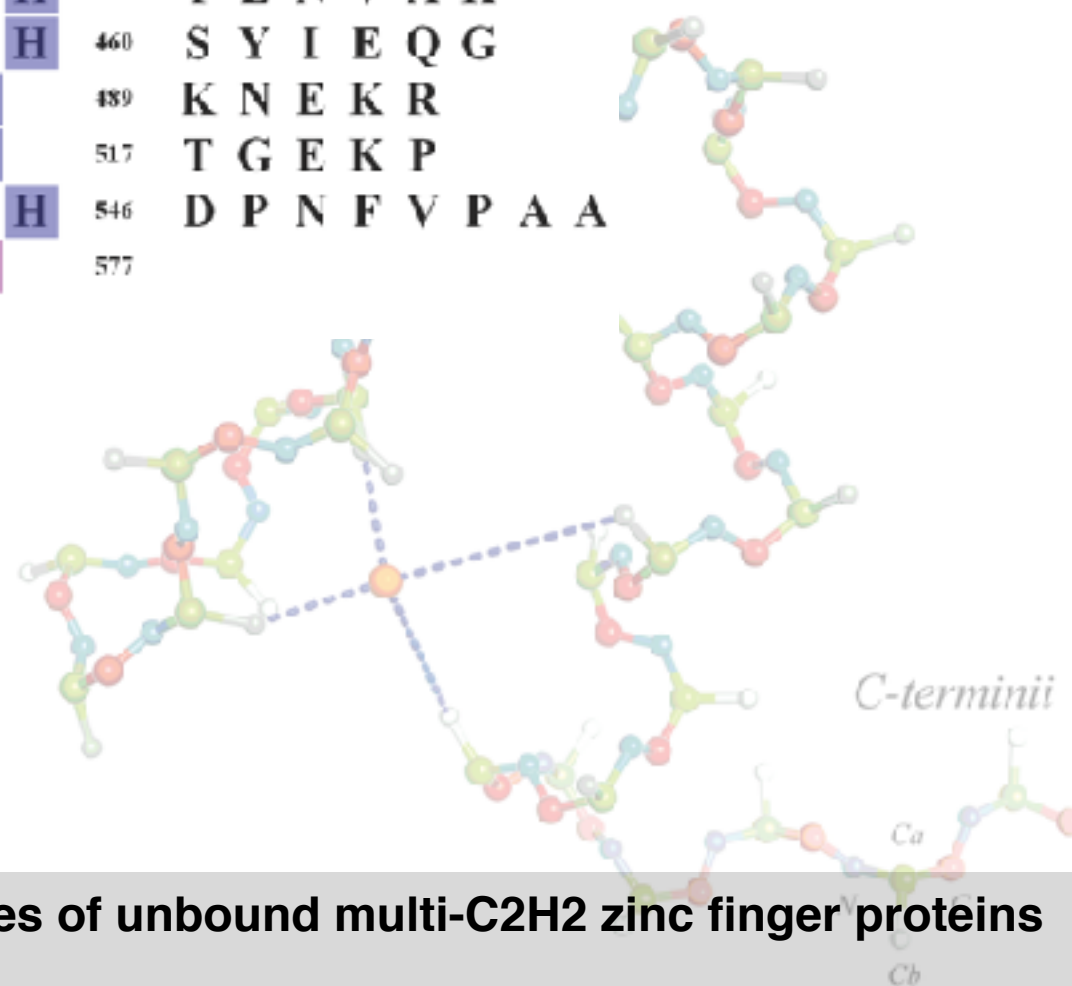
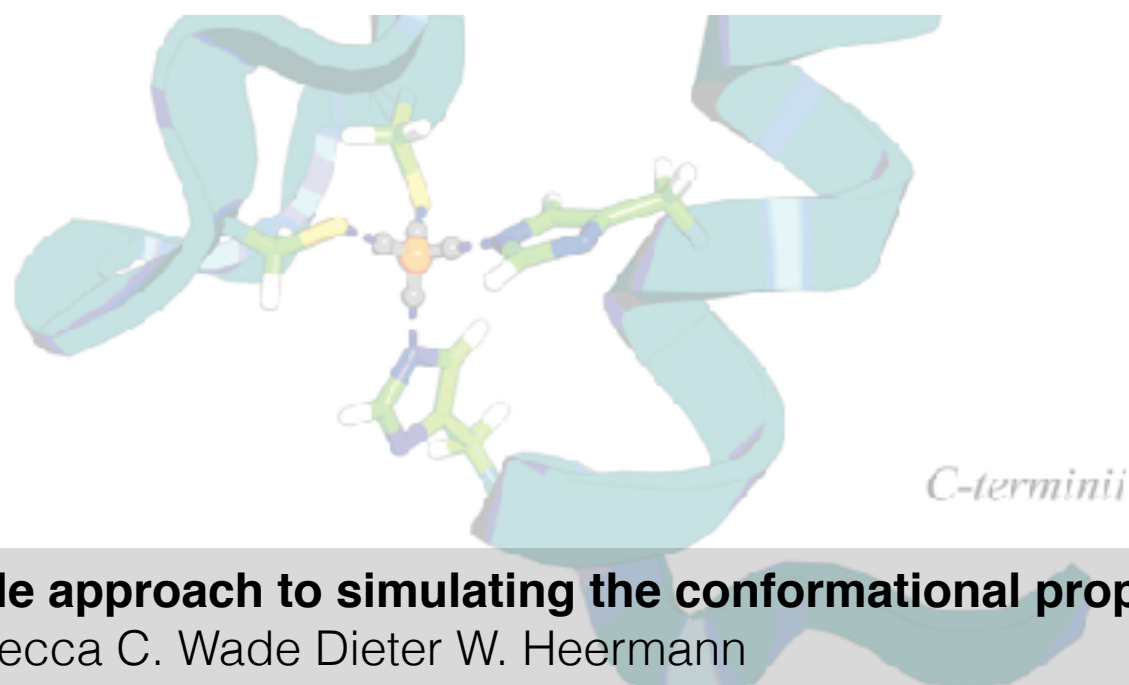


- What is the role of the proteins in the organization of the genome
- Need to understand naturally unfolded proteins or disordered proteins, characterized by lack of stable tertiary structure

Unbound Zinger Proteins

Sequence and Atomic Structure Model of CTCF

zinc finger																			linker														
266	F	Q	C	E	L	C	S	Y	T	P	P	R	R	S	N	L	D	R	H	M	K	S	H	288	T	D	E	R	P				
294	K	K	C	L	L	C	G	R	A	F	R	T	V	T	L	L	R	N	H	L	N	T	H	316	T	G	T	R	P				
322	K	K	C	P	D	C	D	M	A	F	V	T	S	G	E	L	V	R	H	R	R	Y	K	H	345	T	H	E	K	P			
351	F	K	C	S	M	C	D	Y	A	S	V	E	V	S	K	L	K	R	H	I	R	S	H	373	T	G	E	R	P				
379	F	Q	C	S	L	C	S	Y	A	S	R	D	T	Y	K	L	K	R	H	M	R	T	H	401	S	G	E	K	P				
407	Y	E	C	Y	I	C	A	A	R	F	T	Q	S	G	T	M	K	M	H	I	L	Q	K	H	430	T	E	N	V	A	K		
437	F	C	C	P	C	C	D	T	V	I	A	R	K	S	D	L	G	V	H	L	R	K	Q	H	460	S	Y	I	E	Q	G		
467	K	K	C	R	Y	C	D	A	V	F	E	E	R	Y	A	L	I	Q	H	Q	K	S	H	489	K	N	E	K	R				
495	F	K	C	D	Q	C	D	Y	A	R	R	Q	E	R	M	M	I	M	H	K	R	T	H	517	T	G	E	K	P				
523	Y	A	C	S	C	C	D	K	T	F	R	Q	K	Q	L	L	D	M	H	F	K	R	Y	H	546	D	P	N	F	V	P	A	A
555	F	V	C	S	K	C	G	K	T	F	T	R	R	N	T	M	A	R	H	A	D	N	C	577									



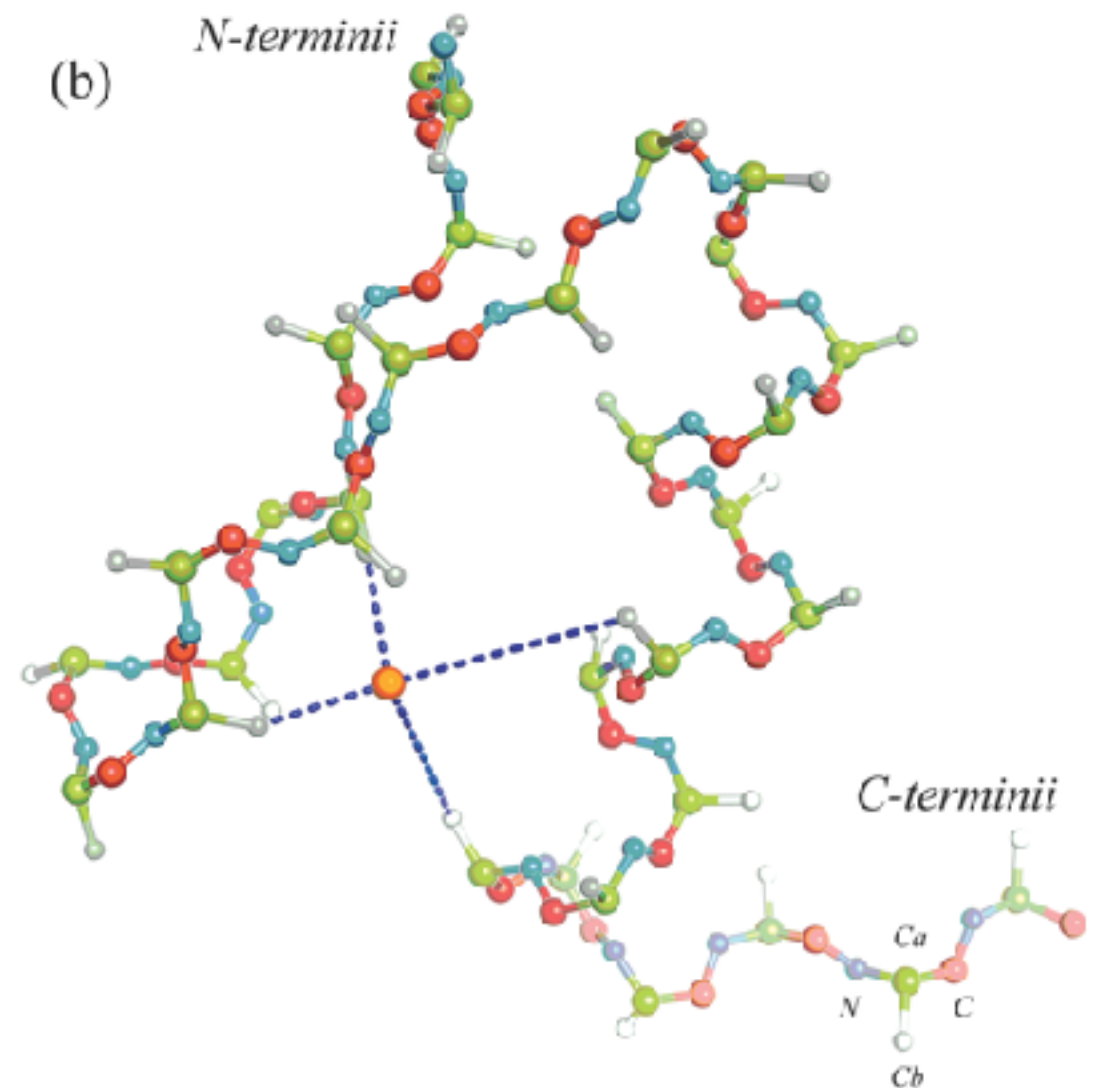
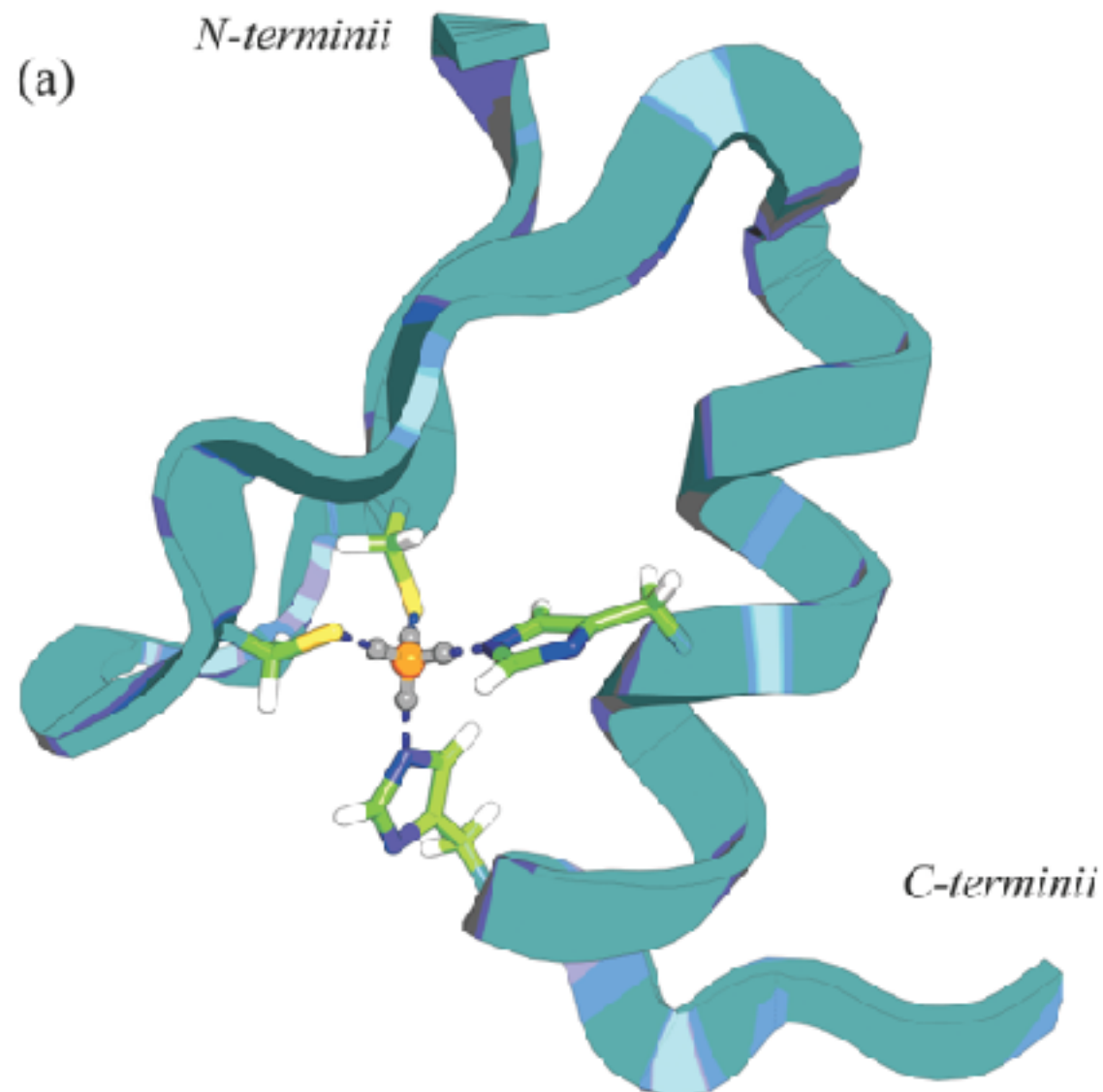
A multiscale approach to simulating the conformational properties of unbound multi-C2H2 zinc finger proteins

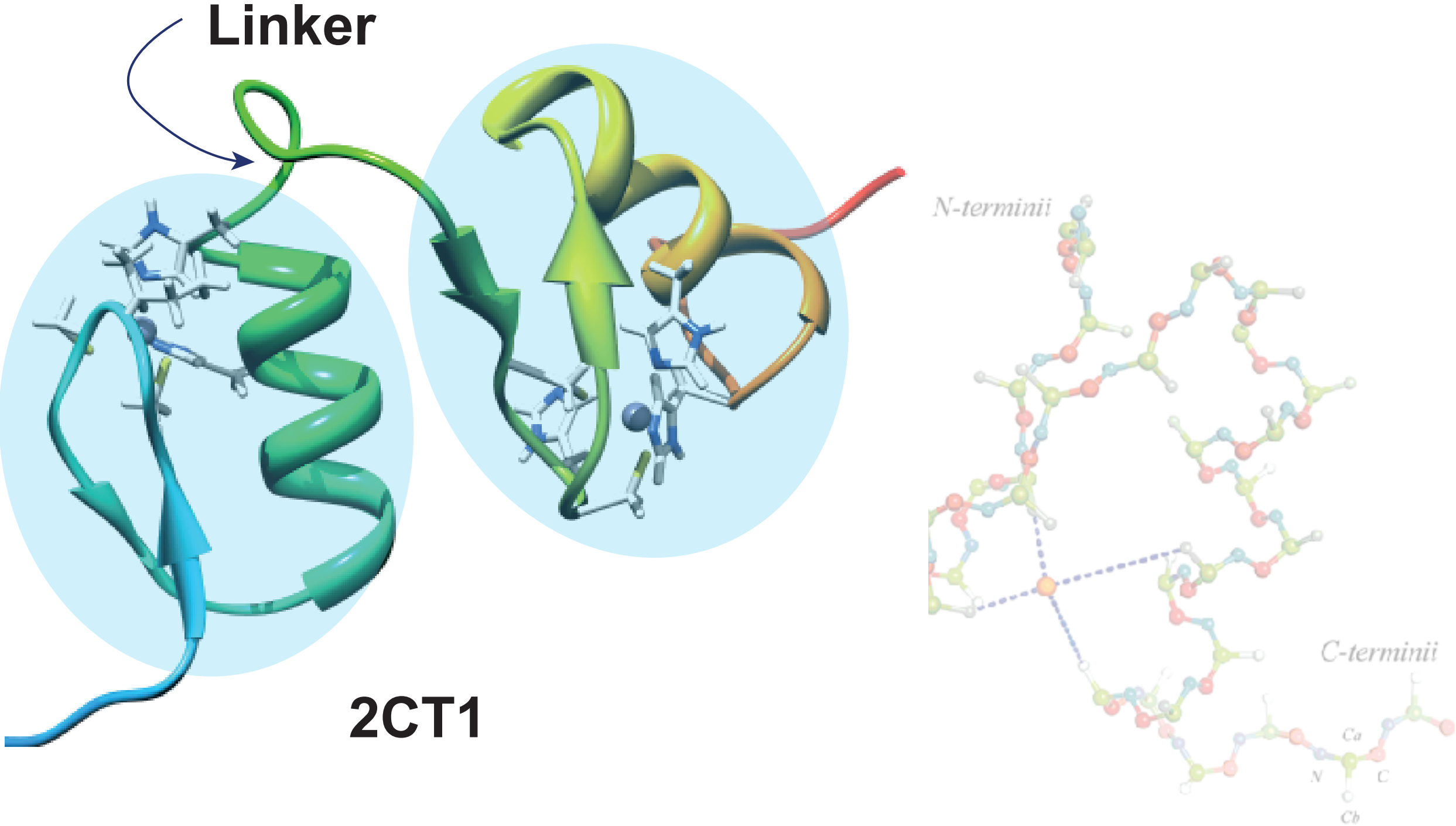
Lei Liu Rebecca C. Wade Dieter W. Heermann

Proteins. 2015 Sep;83(9):1604-15. doi: 10.1002/prot.24845. Epub 2015 Jul 1.

Sequence and Atomic Structure Model of CTCF

Atomic and mesoscale models of 1aay_1. (a) The CaDA representation, where the orange Zn^{2+} ion is surrounded by four gray dummy atoms. (b) Mesoscale model, where each AA is presented by three backbone beads (N , $C\alpha$, C') and one side chain bead ($C\beta$). The Zn^{2+} ion is explicitly modeled as one additional bead, which interacts with $C\beta$ of its coordinating residues.



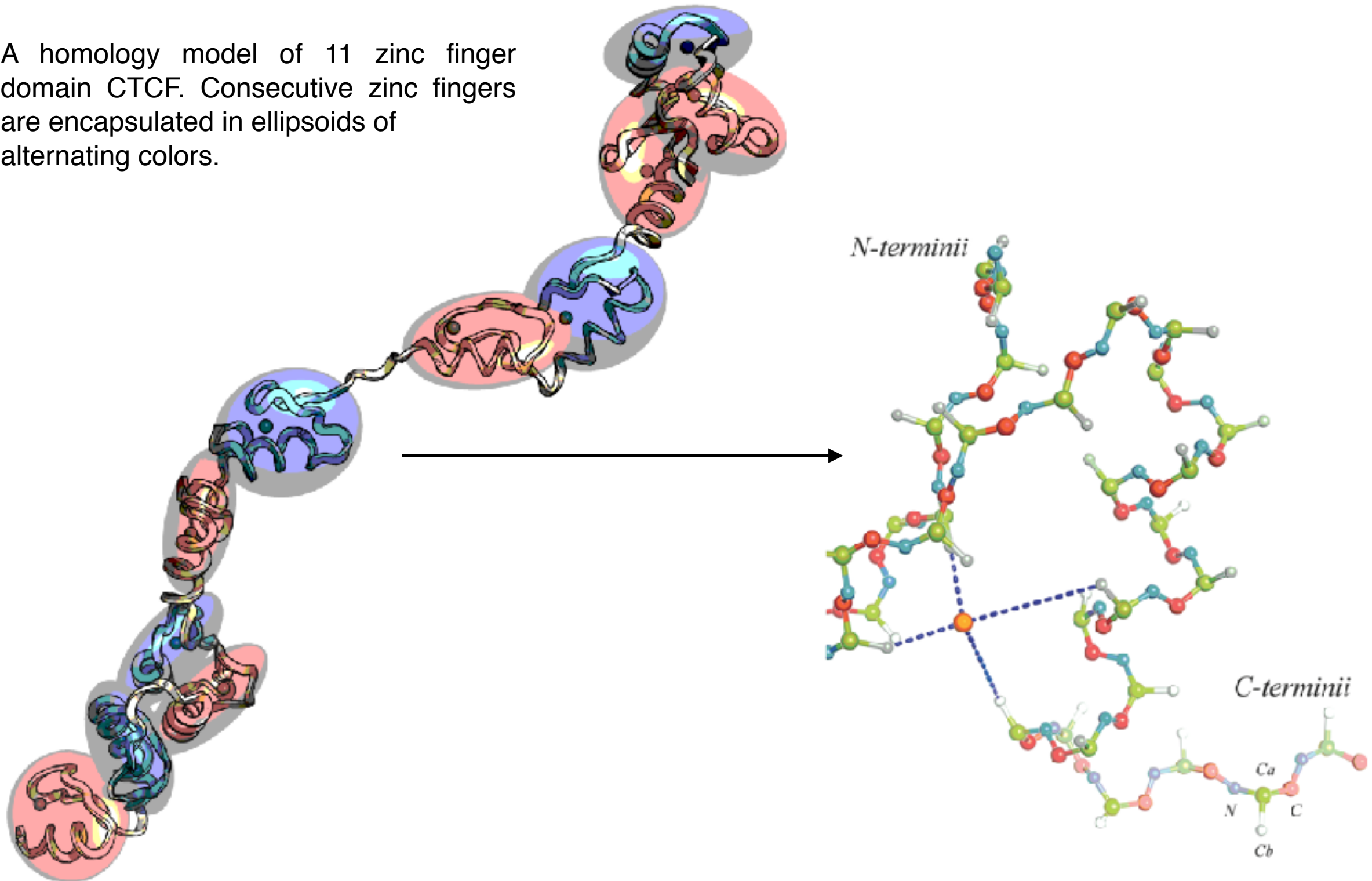


Unbound Zinger Proteins



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386

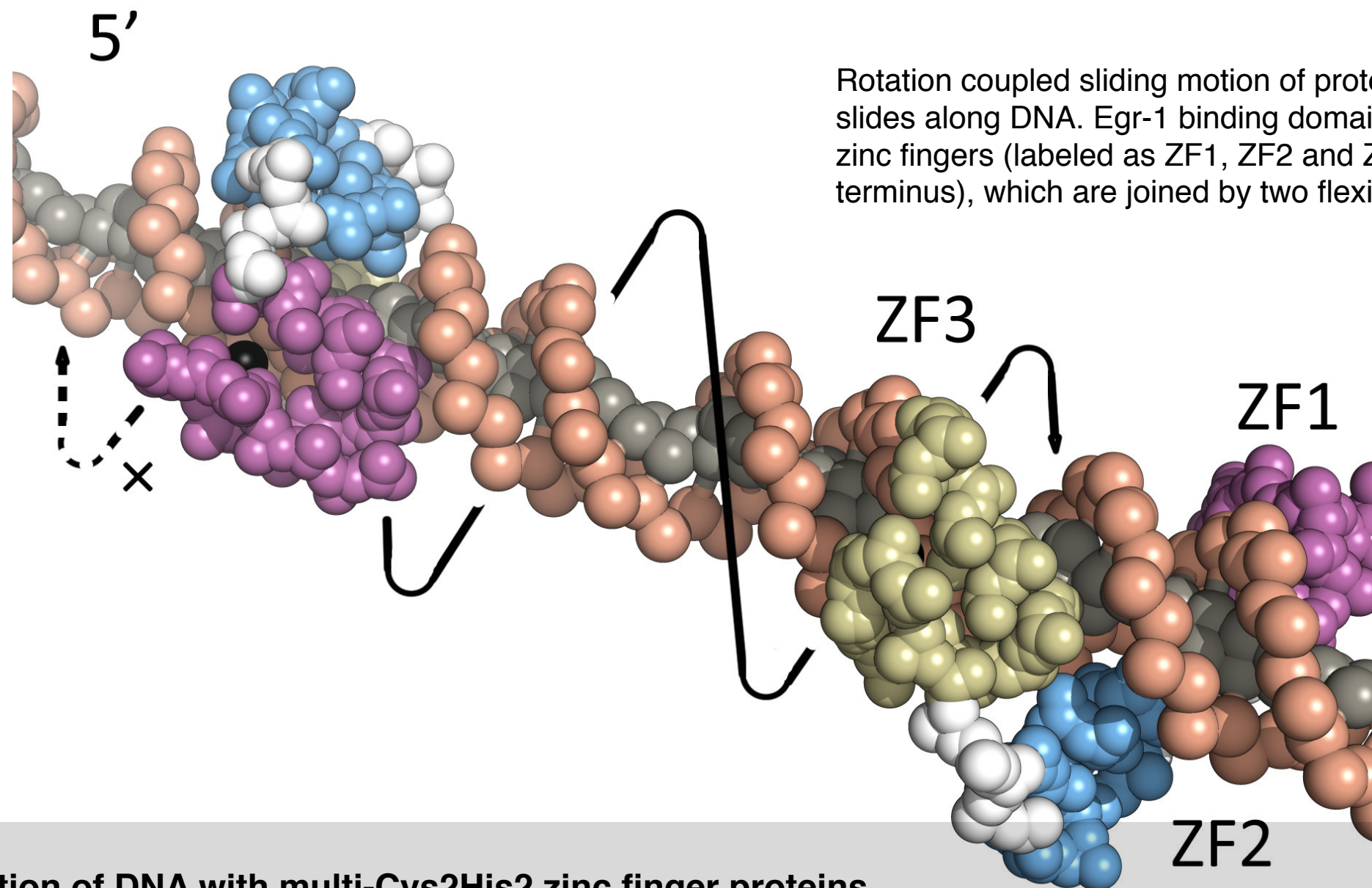
A homology model of 11 zinc finger domain CTCF. Consecutive zinc fingers are encapsulated in ellipsoids of alternating colors.



Interaction of Chromatin with Zinc Finger Proteins

Zinc Finger Proteins in Complexes with DNA

(a)



The interaction of DNA with multi-Cys2His2 zinc finger proteins

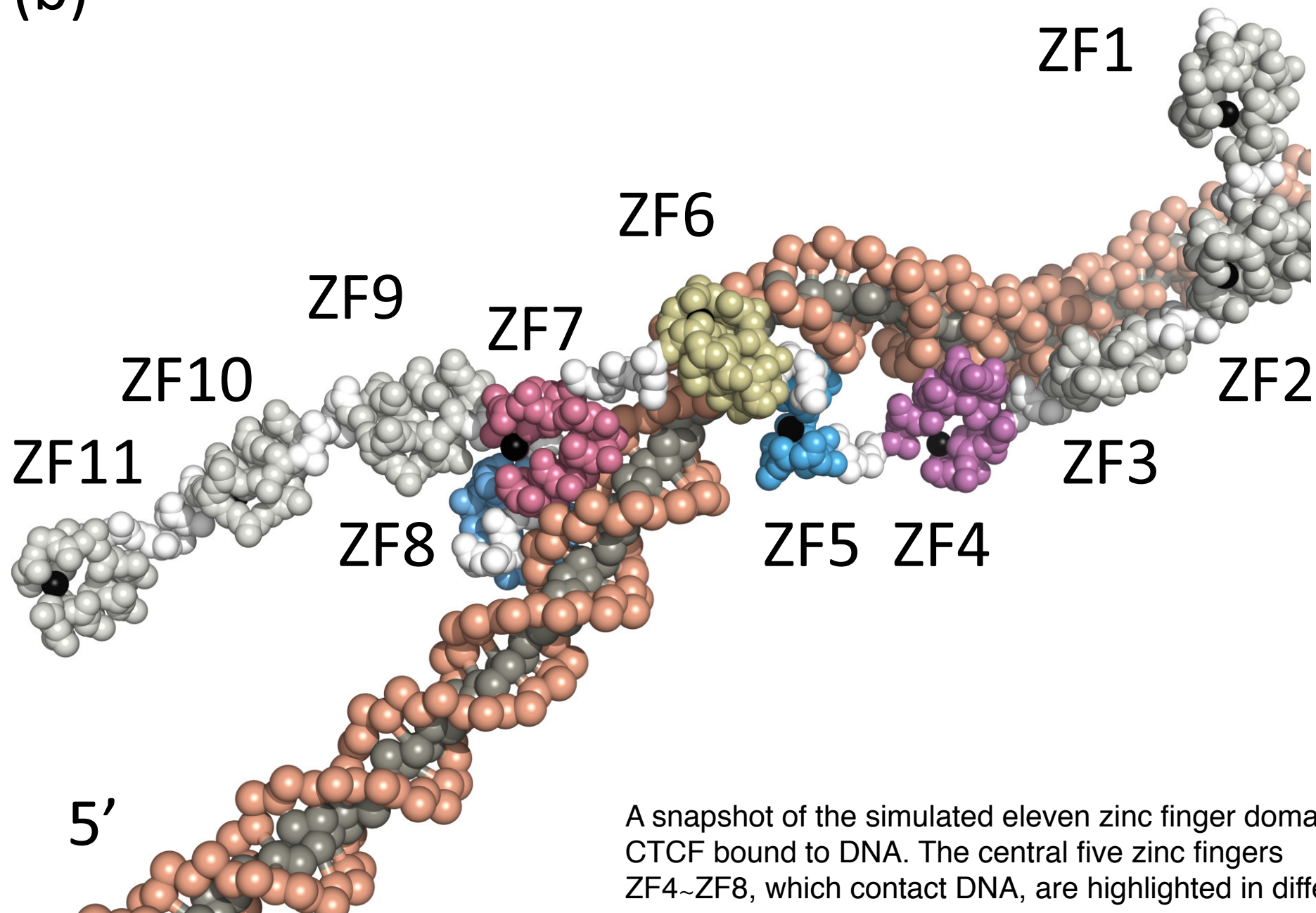
Lei Liu and Dieter W Heermann

J Phys Condens Matter. 2015 Feb 18;27(6):064107. doi: 10.1088/0953-8984/27/6/064107. Epub 2015 Jan 7.

Interaction of Chromatin with Zinc Finger Proteins

Zinc Finger Proteins in Complexes with DNA

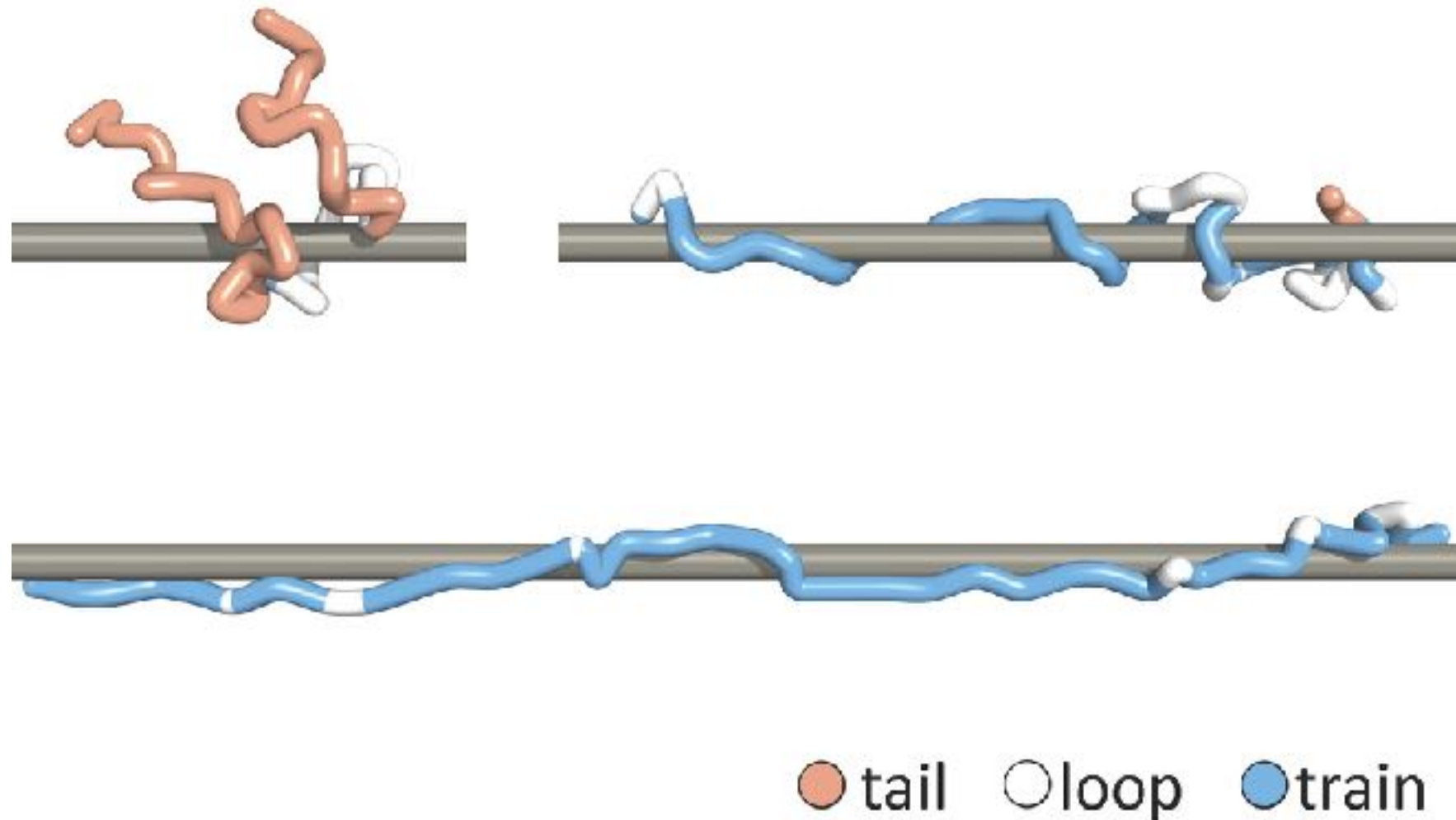
(b)



A snapshot of the simulated eleven zinc finger domains of CTCF bound to DNA. The central five zinc fingers ZF4~ZF8, which contact DNA, are highlighted in different colors.

Winding Of Polymers

The Model

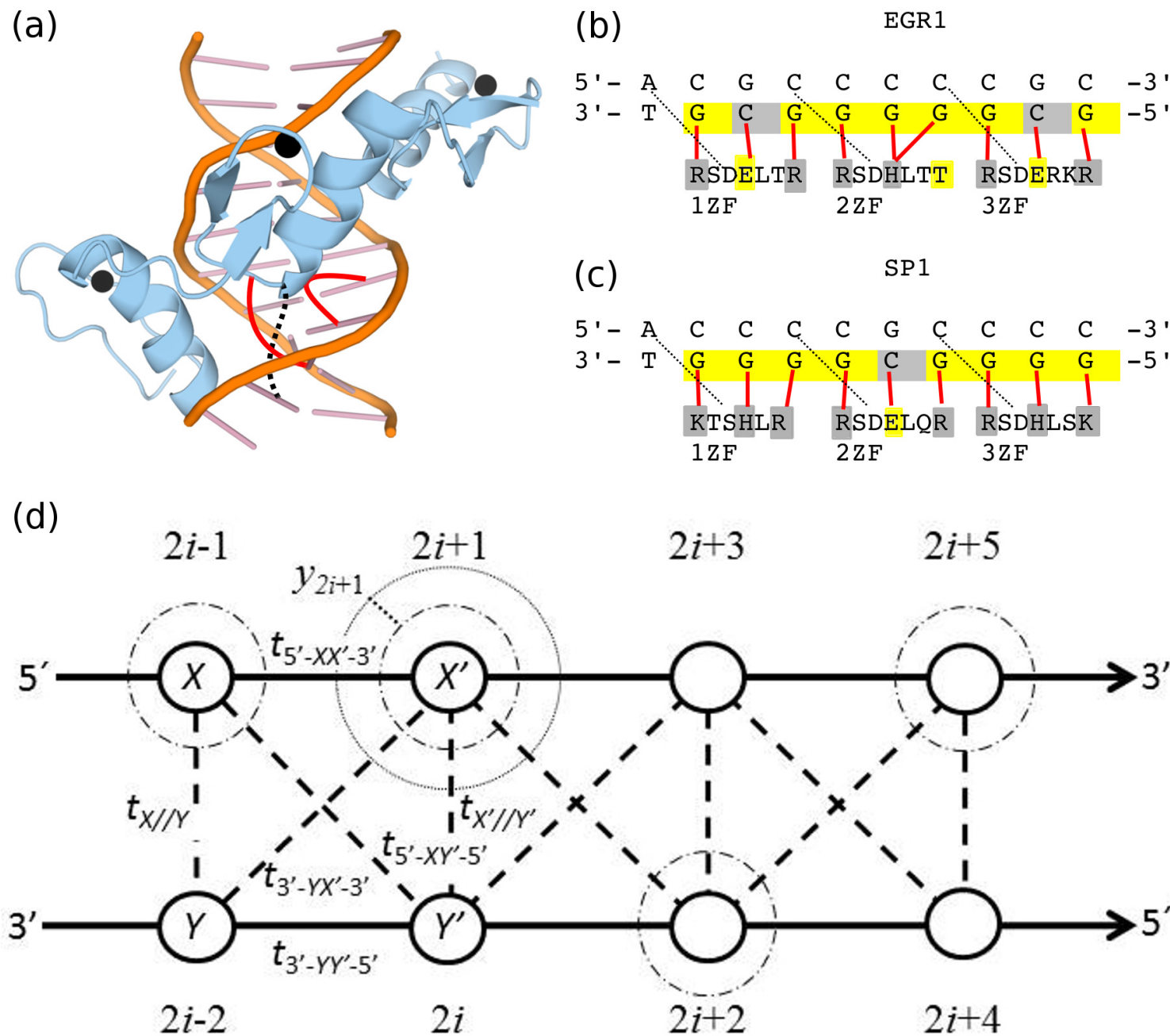


Typical conformations of a flexible polymer of chain length $L = 40$ adsorbed to a rigid polymer, with the adsorption interaction strength $\varepsilon = 0.4, 2.7, 4.7$ (top-left, top-right and bottom panel, respectively). The flexible polymers are divided into three kinds of segments, tail(brown), train(blue) and loop(white).

Phase Transition and Winding properties of a Flexible Polymer adsorbed to a Rigid Periodic Copolymer

Lei Liu, David Schubert, Min Chu, and Dieter W. Heermann

Phys. Rev. E 91, 032601 - Published 11 March 2015



- **ab initio quantum mechanical model** for binding
- correctly identifies the binding sites of zinc fingers
- **de novo prediction** of binding locations

The Electronic Behavior of Zinc-Finger Protein Binding Sites in the Context of the DNA Extended Ladder Model

Nestor Norio Oiwa, Claudette Elisea Cordeiro and Dieter W Heermann

Front. Phys., 11 May 2016 | <https://doi.org/10.3389/fphy.2016.00013>.

Dynamic Loop Model + Biological Input:

Human Chromosomes

- FISH experiments on single chromosomes
- Bio-chemical experiments (4c, Hi-C)
- Partial genome staining experiments
- Whole genome staining experiments
- Mechanical data (metaphase)

Escherichia coli

Yeast



The Physical Architecture of the Genome: Common Principles in Prokaryotes and Eukaryotes

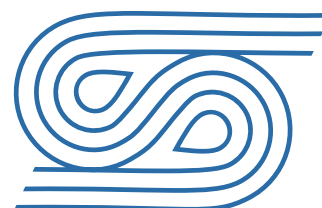
The principles are loops, entropy and confinement

Unified Model



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386

Manfred Bohn
Philipp Diesinger
Roel van Driel
Sandra Götze
Mariliis Tark
Hans-Jörg Jerabek
Songling Li
Miriam Fritsche
Christoph Cremer
Lindsay Shopland
Paul Wiggins
Jörg Bewersdorf



**Heidelberg Graduate School of
Mathematical and Computational
Methods for the Sciences**



Center for Interdisciplinary
Scientific Computing,
Heidelberg



Deutsche
Forschungsgemeinschaft



Spatio/Temporal
Probabilistic Graphical
Models and Applications in
Image Analysis



Leading the search for tomorrow's cures



Thank you for your attention!