

Engineering Topological Phases *:A Materials Perspective*

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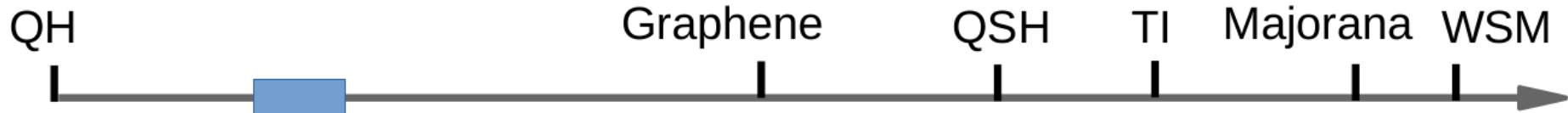


: Department of Science & Technology, India

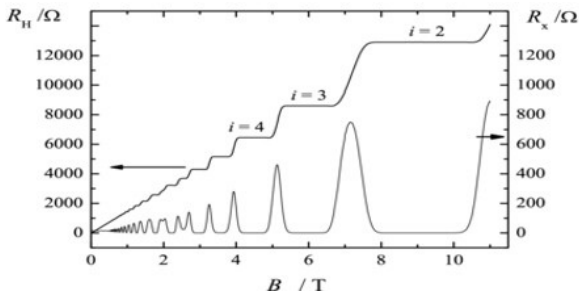


POCO
SHOT ON POCO F1

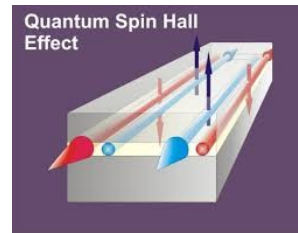
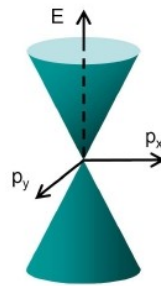
Topology "ZOO"



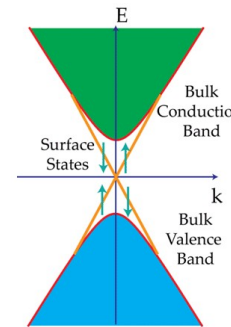
1975-80



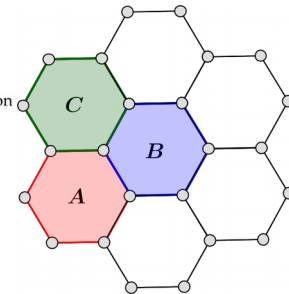
2004



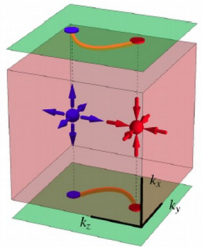
2007



2009

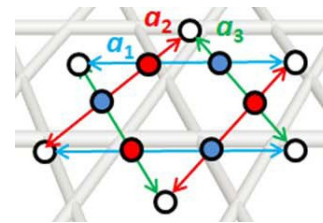
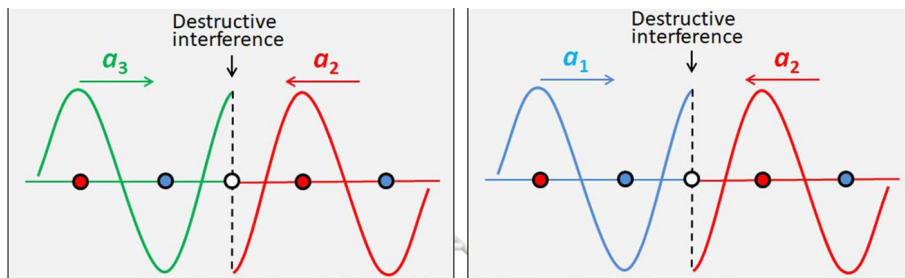


2012 2013

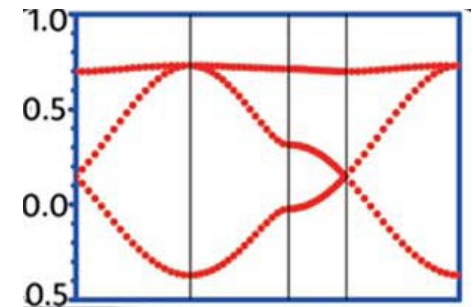


Topological phases from gapped matter (insulator) to gap-less systems (metals)

Topologically non-trivial Flat bands : Fractional QHE (site of "instability")

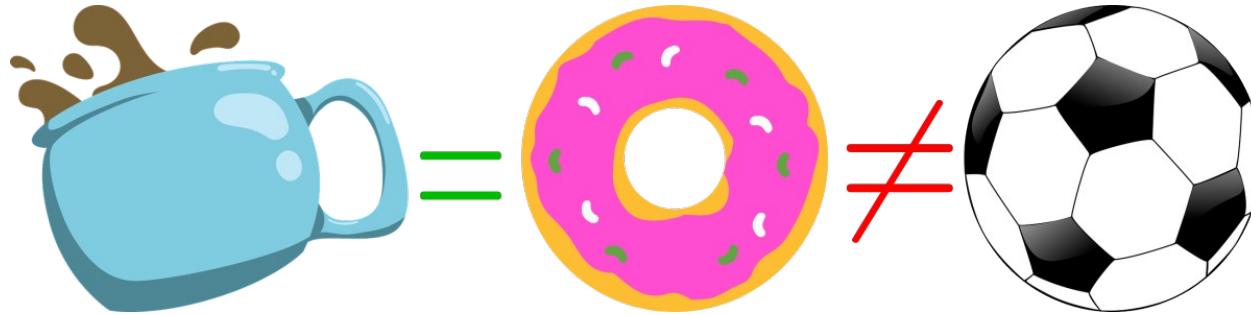


Li et al Sci Adv 2018



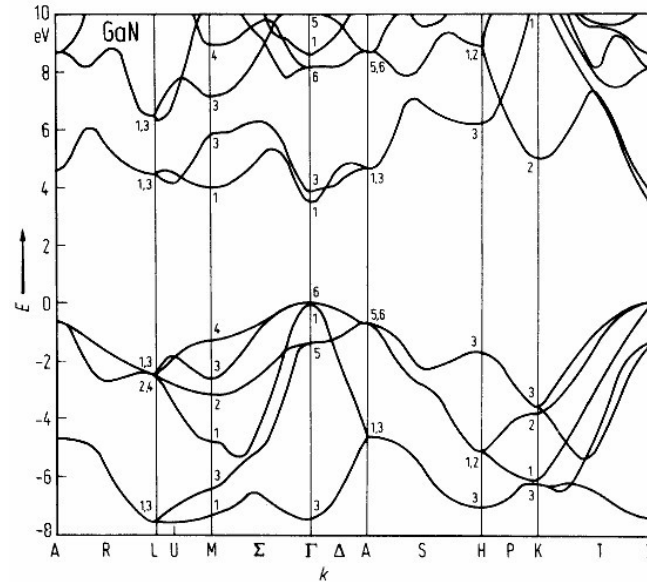
Topology (2016 Nobel prize)

Geometrical Topology:



“Same” if can be deformed without singularity. The value of an orientable surface's genus is equal to the number of holes! **Topological Invariant:** Quantity that does not change under continuous deformation

Band Structure Topology:



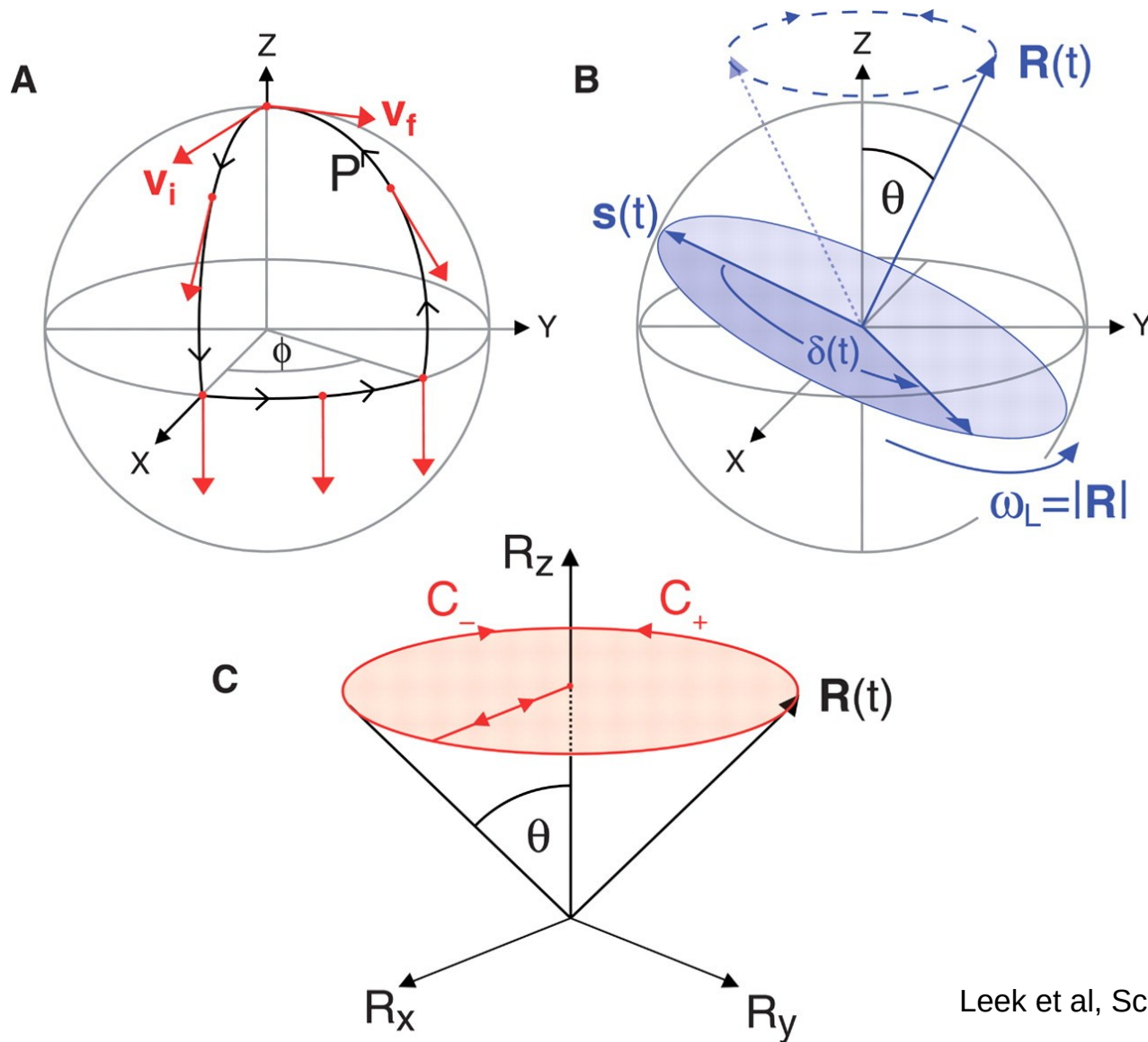
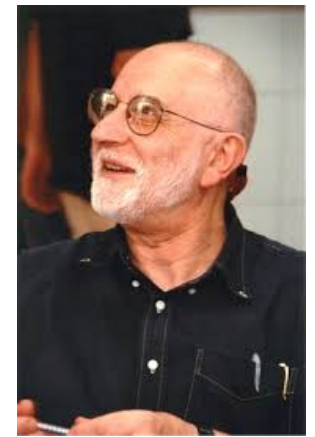
“Same” if can be adiabatically perturbed without gap closure.

Topological Invariant: Cannot change unless the energy gap between bands closes and reopens

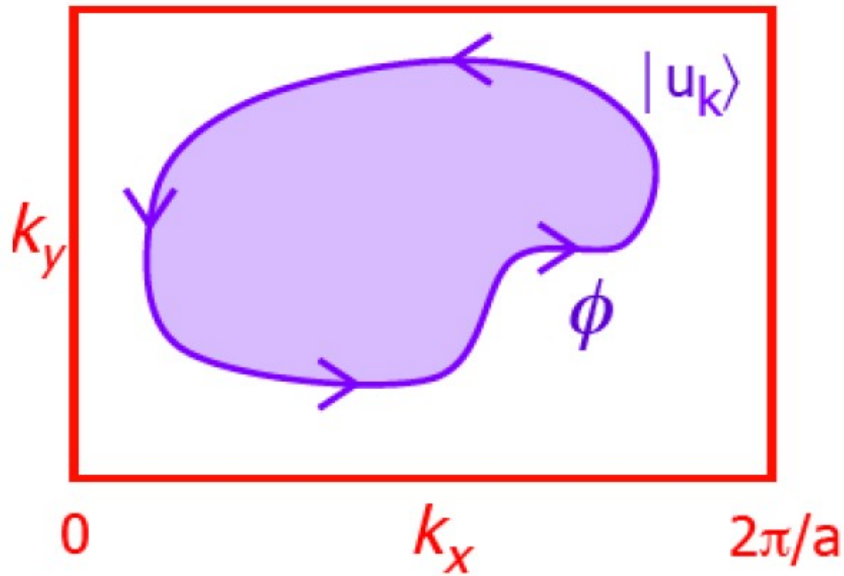


Pancharatnam Berry Phase

Geometrical Phase



Berry Phase and Curvature in the BZ



$$u_{\mathbf{k}}(\mathbf{r}) = e^{-i\mathbf{k}\cdot\mathbf{r}} \underbrace{\psi_{\mathbf{k}}(\mathbf{r})}_{\text{Bloch function}}$$

$$A_n^a(\mathbf{k}) = -i \langle \Psi_n(\mathbf{k}) | \frac{\partial}{\partial k_a} \Psi_n(\mathbf{k}) \rangle$$

“Berry connection”: k-space analog of the magnetic vector potential.

$$F_n^{ab}(\mathbf{k}) = \frac{\partial}{\partial k_a} A_n^b(\mathbf{k}) - \frac{\partial}{\partial k_b} A_n^a(\mathbf{k})$$

“Berry curvature”: k-space analog of magnetic flux density (gauge invariant)

the integer quantum Hall effect in a 2D crystal

$$n = \sum_{\text{bands}} \frac{i}{2\pi} \int d^2k \left(\left\langle \frac{\partial u}{\partial k_1} \middle| \frac{\partial u}{\partial k_2} \right\rangle - \left\langle \frac{\partial u}{\partial k_2} \middle| \frac{\partial u}{\partial k_1} \right\rangle \right) \quad \mathcal{F} = \nabla \times \mathcal{A}$$

$$\sigma_{xy} = n \frac{e^2}{h} \quad \text{TKNN, 1982} \quad \text{“first Chern number”}$$

“Chern number” classifies Bloch bands with broken time-reversal symmetry

Chern I ←

Gapless chiral edge states → potential use in dissipationless electronic circuits

T-invariant systems

“spin Chern number”

Each pair of spin-orbit-coupled bands in 2D has a Z_2 invariant, essentially integral over half the BZ

$$Z_2 = \sum_n^{\text{occ.}} \frac{1}{2\pi} \left(\oint_{\text{Half BZ}} \mathbf{A}_n \cdot d\mathbf{k} - \int_{\text{Half BZ}} dk_x dk_y F_n \right) = 0 \text{ or } 1 \pmod{2} \quad \Rightarrow \quad \mathbb{Z}_2$$

Topological Flat Bands, Landau Levels

- Lattice models with complex hopping parameters (SOC)

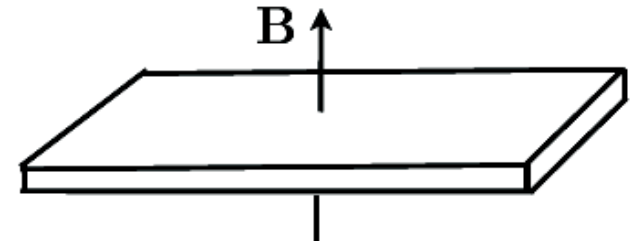
 - ➔ Analogues of Landau Levels

- Almost flat, topological bands with any Chern number, $C = N$, possible

- Time-reversal broken spontaneously - No need for strong magnetic field

- Partial filling may give rise to Fractional QH state.

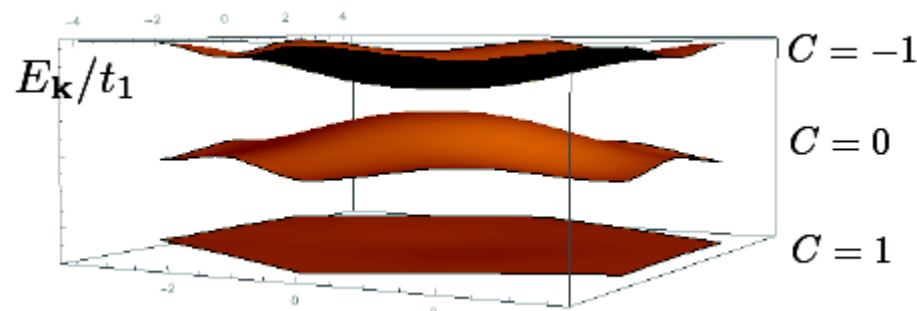
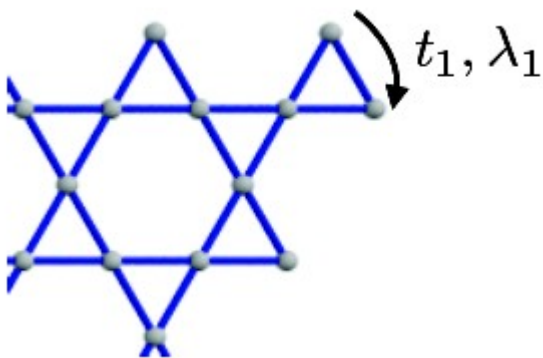
- High temperature scale may be achievable



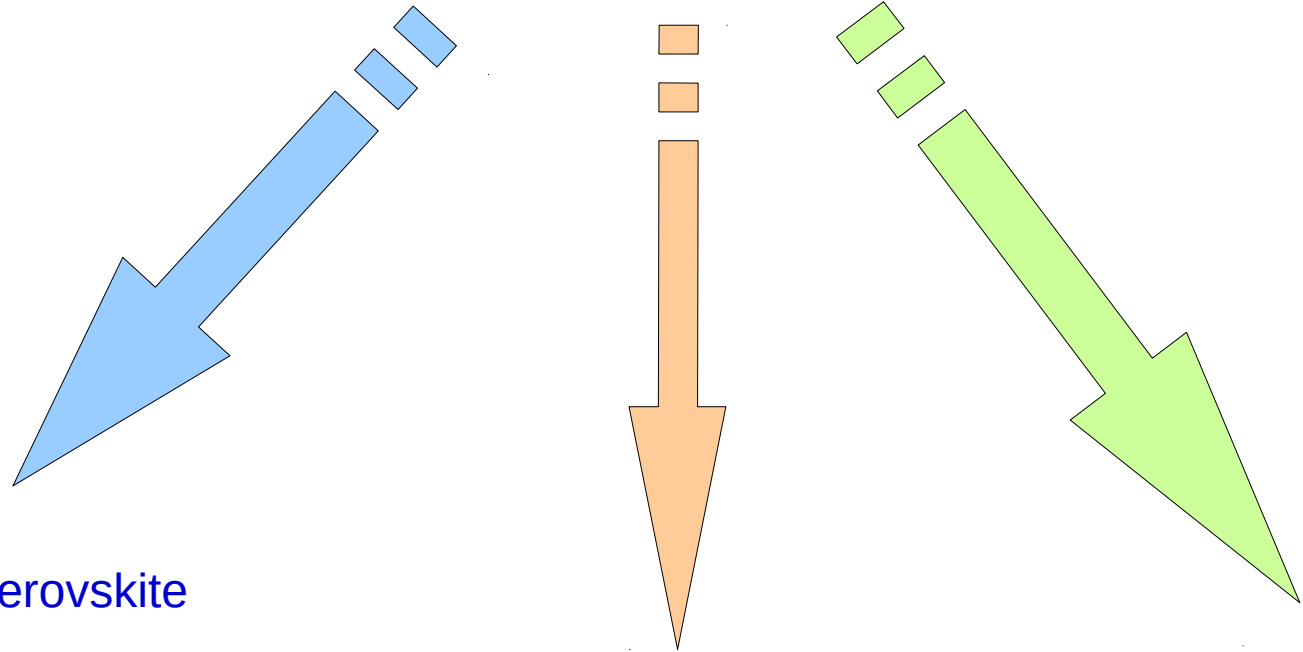
- Cold 2D electrons in a strong magnetic field

- Flat Landau bands with $C=1$

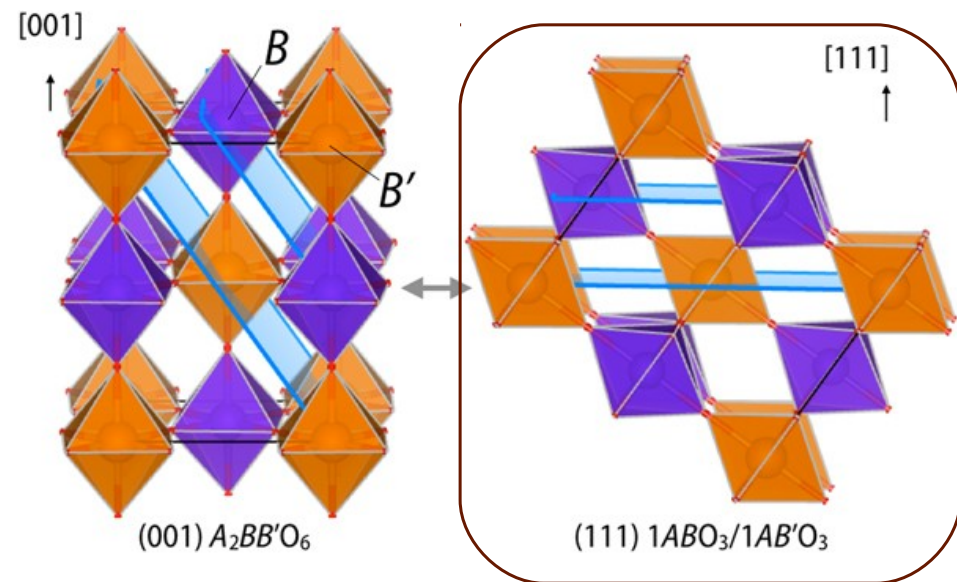
- Interaction scale set by magnetic length ~ 1 K



Search for Materials Candidates

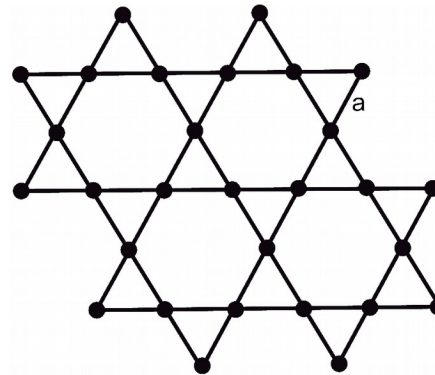


Bilayer Double Perovskite



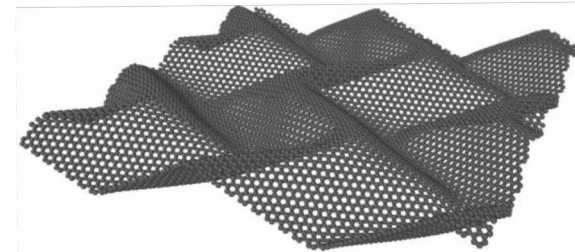
Candidate for RT QAH ?!

Binary Intermetallics in kagome lattice



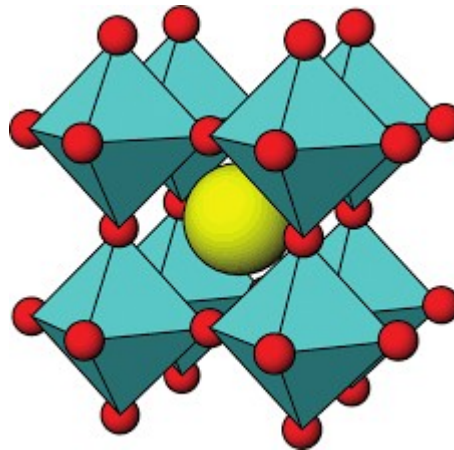
Possible Host for Chern metal, Topological SC ?!

Graphene under Deformation - "Ripplocation"



Topological Flat band ?!

OXIDE MATERIALS



Santu Baidya
(SNBCBS-> Duisburg-Essen
-> SNU-> Rutgers)



Arun Paramakanti
(U. Toronto)



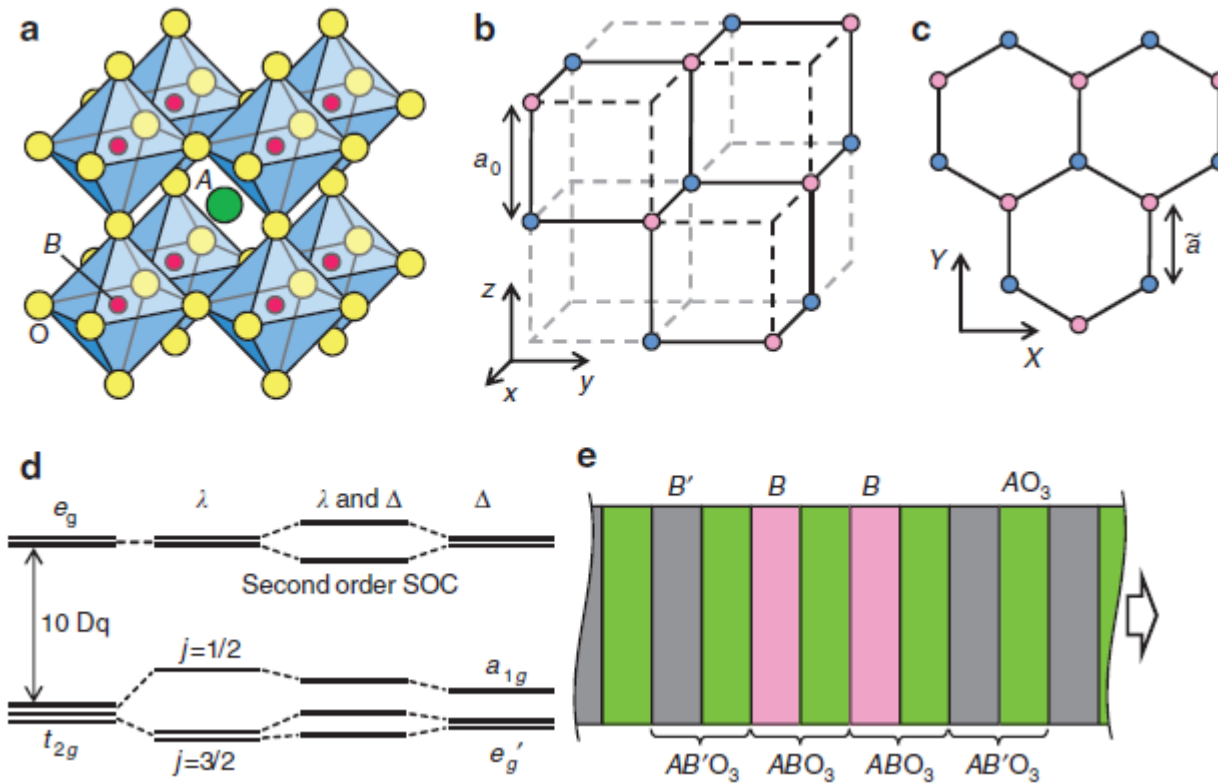
Umesh Waghmare
(JNCASR, Bangalore)

Interface Engineering of QAH effects ?

Bilayers of Perovskites grown along [111]

Theoretical Prediction:

Combination of buckled honeycomb structure together with SOC can give rise to 2D time reversal Invariant TI.



QAH: MOTIVATION

For practical usage one would like to:

● **Boost the temperature scale for QAH effect**

[Use d-electron systems rather s or p electron based systems.]

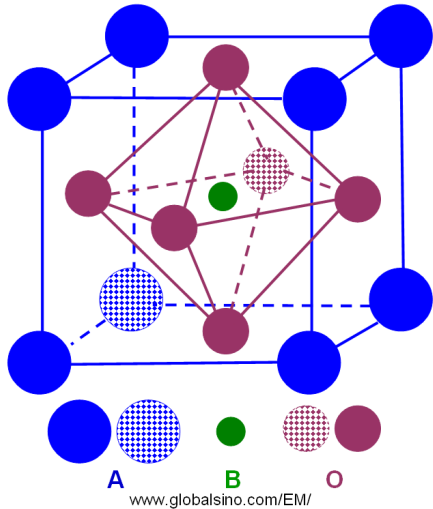
● **Engineer a large topological band gap**

● **Avoid possible dopant or adatom-induced inhomogeneities by considering stoichiometric composition**

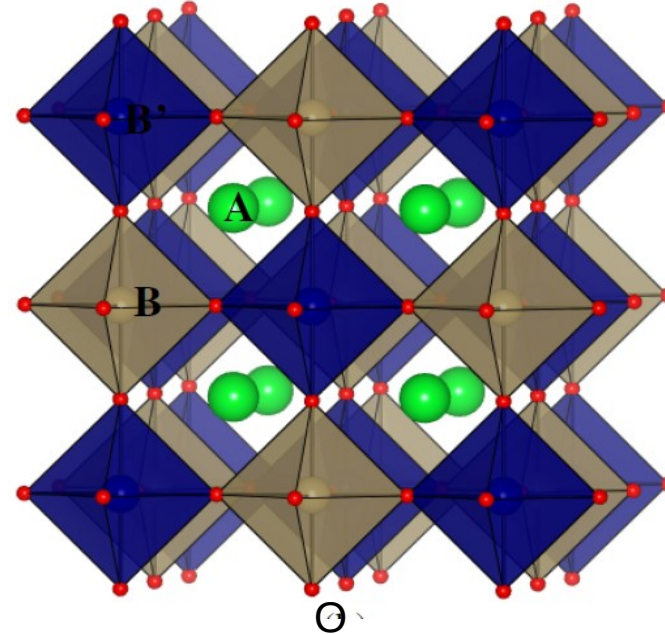
*[Doping TR-invariant TIs with magnetic atoms (Chang et al, Science 2013),
Magnetic atoms on graphene (Qiao et al, PRB 2010), heavy atoms with large
SOC on magnetic substrates (Garrity, PRL 2013)]*

Double Perovskites : $A_2BB'O_6$

Perovskite: ABO_3



Doubling of unit cell
($A_2B_2O_6$)
Replacing one of B by B'
Ordering of B/B'



Diversity of Applications:

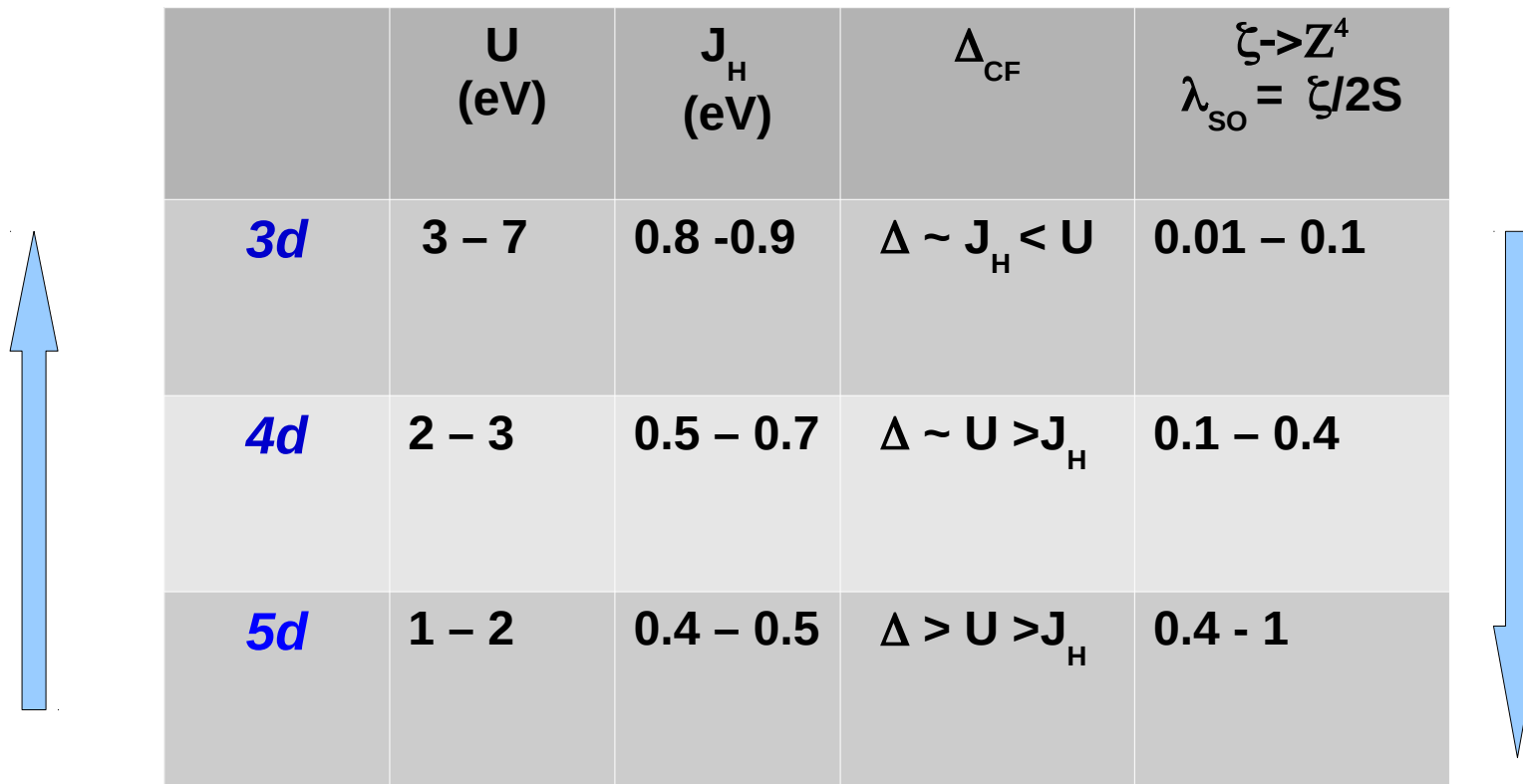
Spintronics: Sr_2FeMoO_6 (Nature, 1998; PRL 2000)

Multiferroicity: Bi_2NiMnO_6 (JACS, 2005)

Magnetodielectric: La_2NiMnO_6 , La_2CoMnO_6 (Adv Mater 2005;
PRL 2008; PRB 2008)

Magneto-optic Devices:
 Sr_2CrWO_6 , Sr_2CrReO_6 , Sr_2CrOsO_6 (APL, 2008)

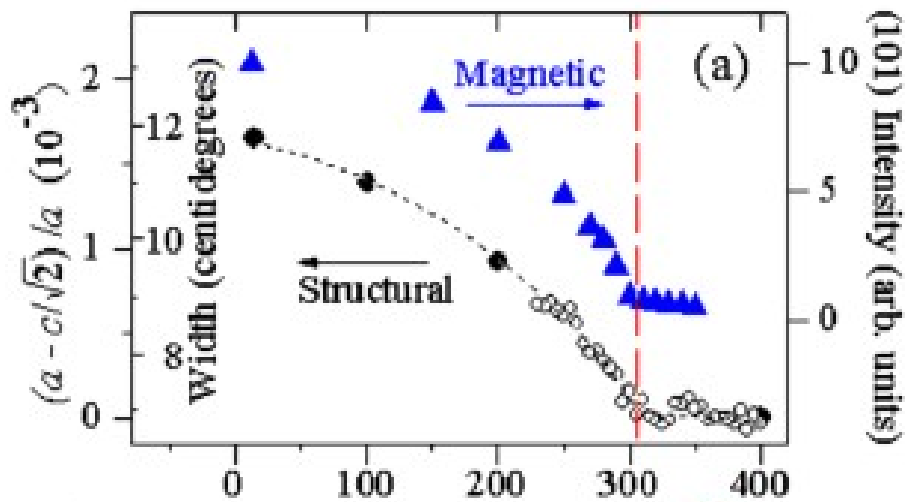
3d-4d/5d DPs:



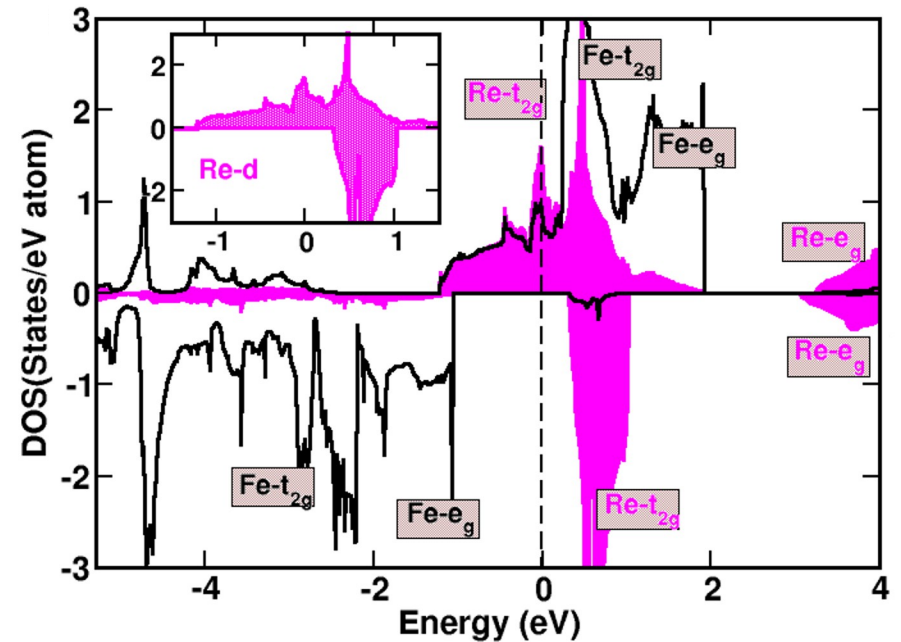
	U (eV)	J _H (eV)	Δ _{CF}	$\zeta \rightarrow Z^4$ $\lambda_{SO} = \zeta/2S$
3d	3 – 7	0.8 -0.9	$\Delta \sim J_H < U$	0.01 – 0.1
4d	2 – 3	0.5 – 0.7	$\Delta \sim U > J_H$	0.1 – 0.4
5d	1 – 2	0.4 – 0.5	$\Delta > U > J_H$	0.4 - 1

- **3d TM (B)** can allow for a high energy scale for magnetism, while the **4d/5d TM (B')** can feature strong SOC.
- Physical separation of ions hosting magnetism from those hosting strong SOC, avoids the issue related to interplay of correlation effect and SOC at the same site.
- Low energy physics is described by t_{2g} bands \longrightarrow suppresses JT (trivial Ins)
[Doennig et al, PRB 2016, (LaXO₃)₂/(LaAlO₃)₄ X = Ti-Cu]

$\text{Ba}_2\text{FeReO}_6$ (BFRO) : Half-metallic (HM) ferromagnet with transition temperature of 304 K

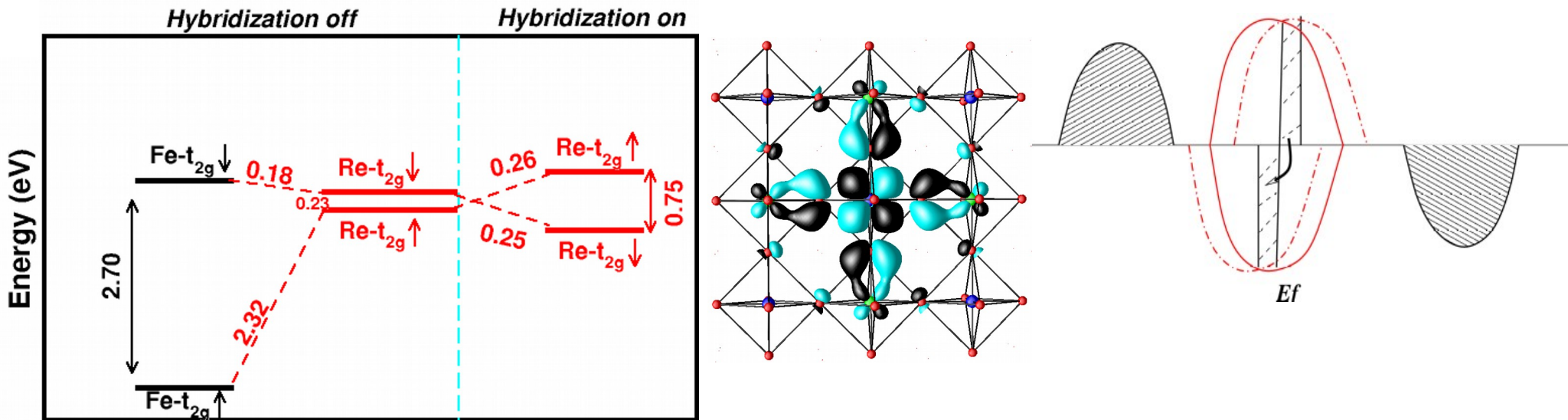


Phys. Rev. Lett. 98, 017204 (2007).



Ferromagnetism is driven by hybridization driven mechanism as found in $\text{Sr}_2\text{FeMoO}_6$

Sarma, Mahadevan, TSD, et al, Phys. Rev. Lett. 85, 2549 (2000)



Effective double exchange type model Hamiltonian

Fe^{3+} : $3d^5$: Hund's rule: Large (classical) spin $S=5/2$: Site-localized.

Re^{5+} : $4d^2$: Mobile electron: gives rise to metallic behavior.

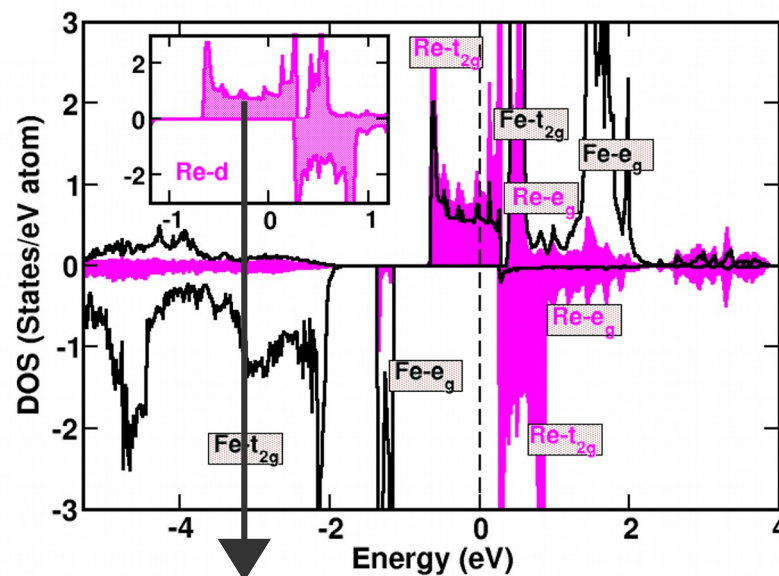
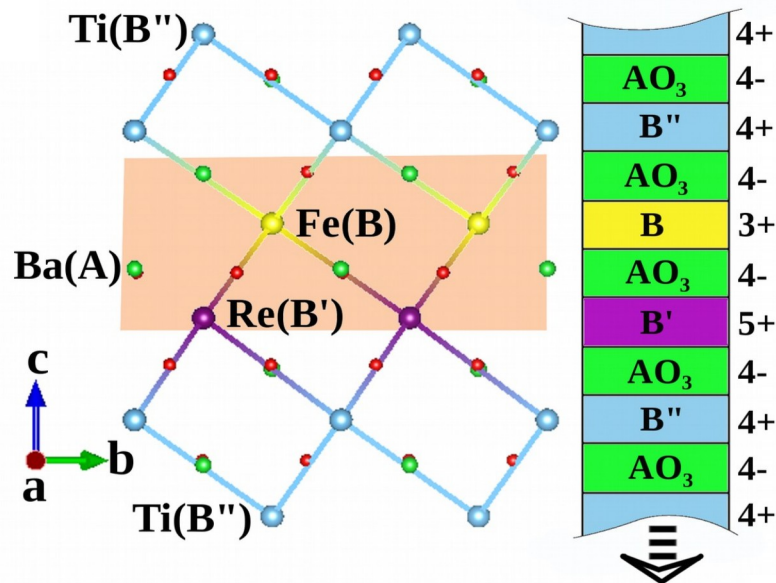
Ferromagnet: $S_{\text{total}} = 3/2$

2-sublattice Kondo lattice Hamiltonian : Energy scales: t_{FeRe} , $\Delta = \epsilon_{\text{Re}} - \epsilon_{\text{Fe}}$, J

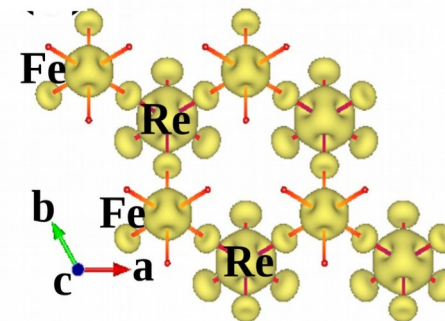
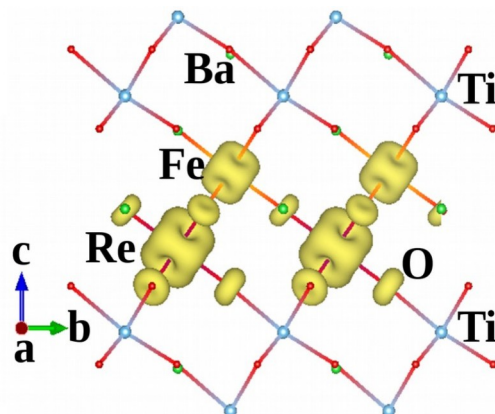
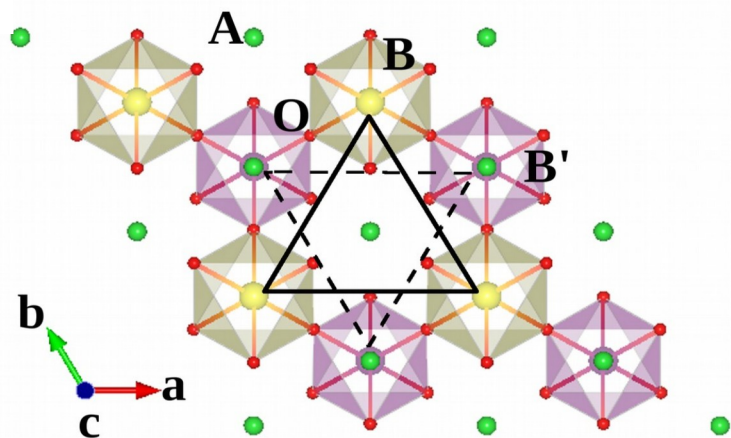
$$H = \epsilon_{\text{Fe}} \sum_{i \in \text{A}} f_{i\sigma, \alpha}^{\dagger} f_{i\sigma, \alpha} + \epsilon_{\text{Re}} \sum_{i \in \text{B}'} m_{i\sigma, \alpha}^{\dagger} m_{i\sigma, \alpha} + t_{\text{FM}} \sum_{\langle ij \rangle \sigma, \alpha} (f_{i\sigma, \alpha}^{\dagger} m_{j\sigma, \alpha} + h.c.) + J \sum_{i \in \text{B}} S_i \cdot f_{i\alpha}^{\dagger} \sigma_{\alpha\beta} f_{i\beta}$$

Consider quantum wells of a double perovskite ($\text{Ba}_2\text{FeReO}_6$) embedded in a wide band gap insulating oxide (BaTiO_3)

[111] growth direction



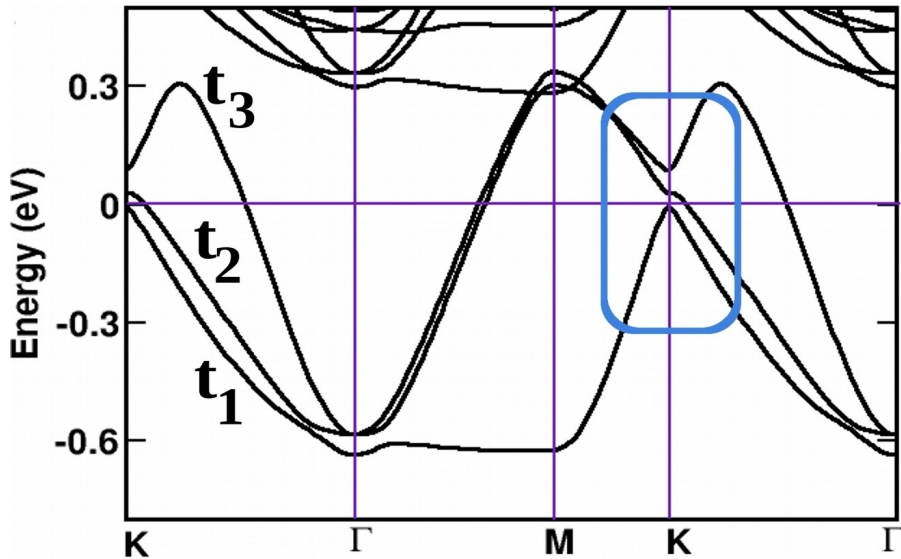
Signature of 1-D features \rightarrow Reduced dimensionality



★ Highly confined 2D electron gas

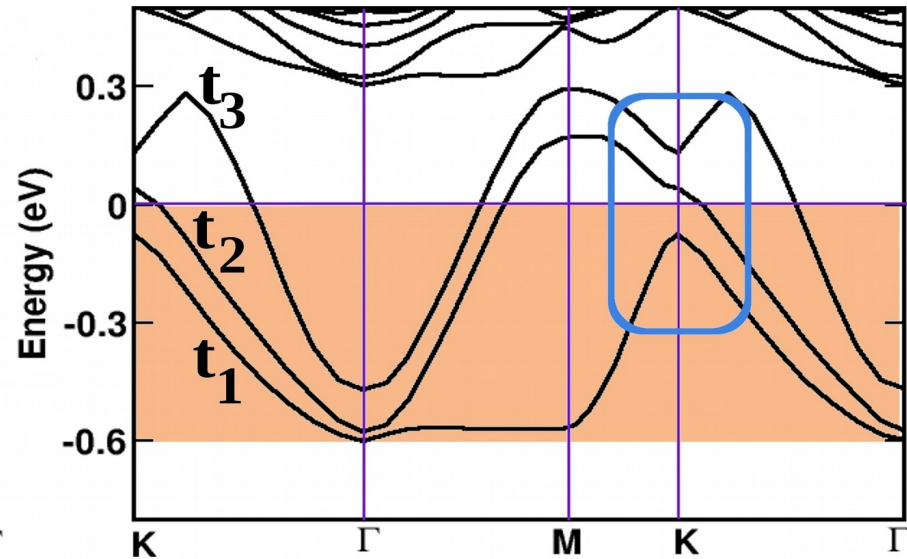
Band structure of [111] heterostructure

GGA



GGA+SO

[Topological HM band structure]



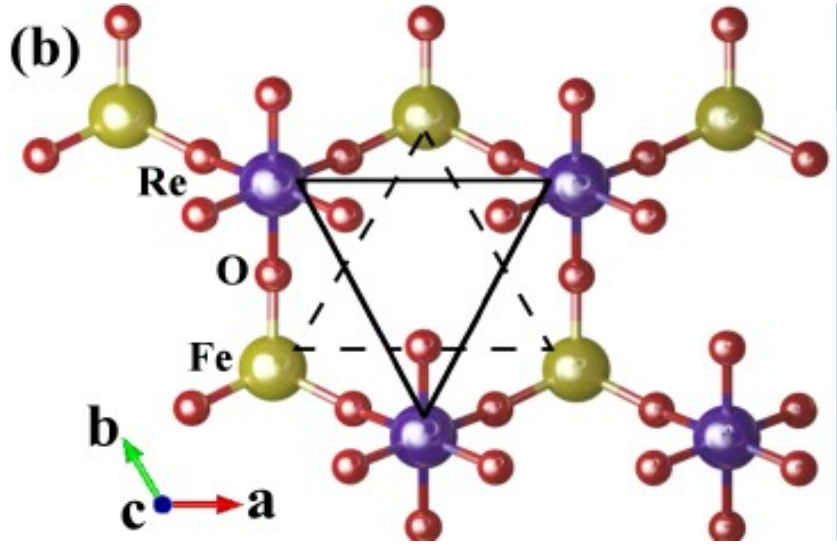
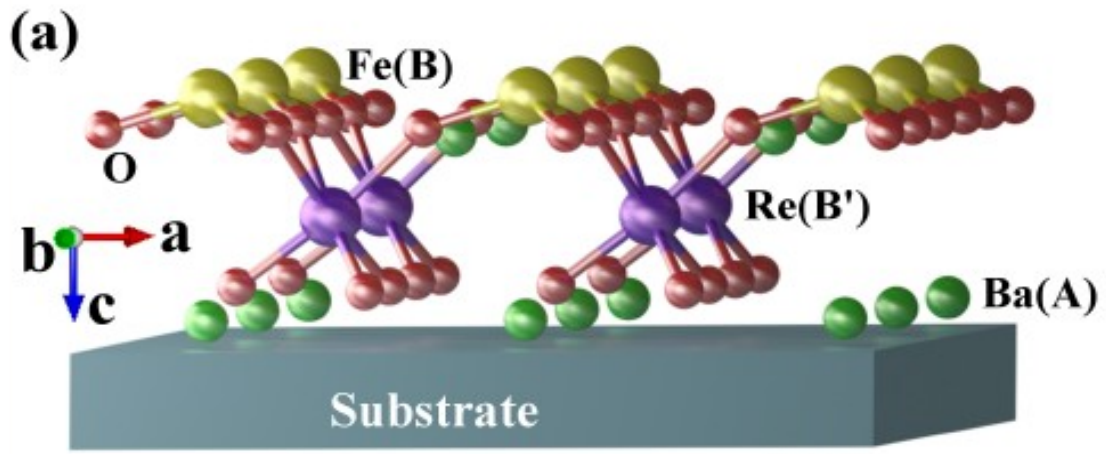
Nontrivial Chern numbers for t_1 and t_2 bands: -2, 2

$$C_n = \sum_{n' \neq n} \int \frac{d^2 \mathbf{k}}{2\pi} \text{Im} \frac{\langle n\mathbf{k} | v_x(\mathbf{k}) | n'\mathbf{k} \rangle \langle n'\mathbf{k} | v_y(\mathbf{k}) | n\mathbf{k} \rangle}{(E_n(\mathbf{k}) - E_{n'}(\mathbf{k}))^2}$$

The (111) bilayer thus can be a quantum anomalous Hall insulator, if t_1 and t_2 bands can be prevented from spanning a common energy window.

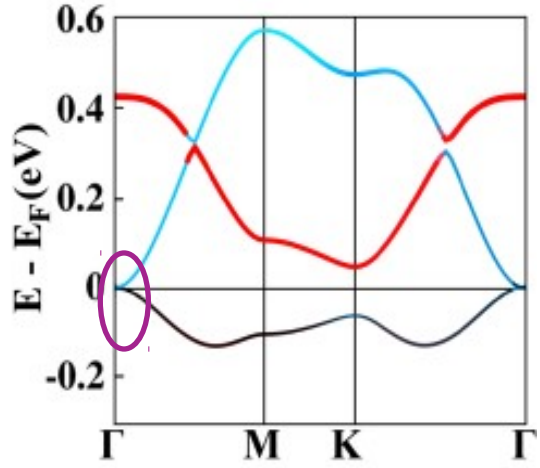
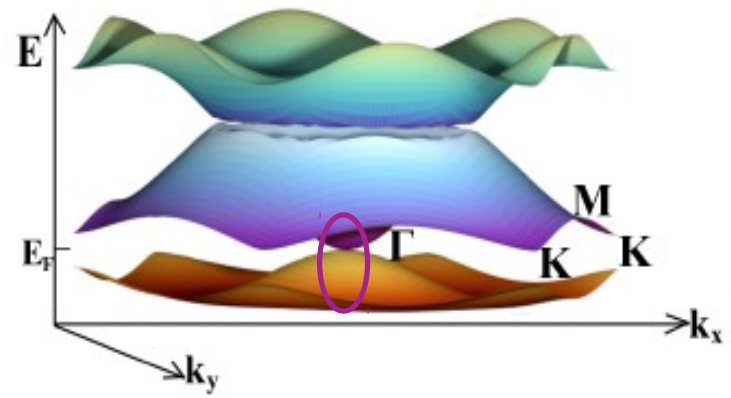
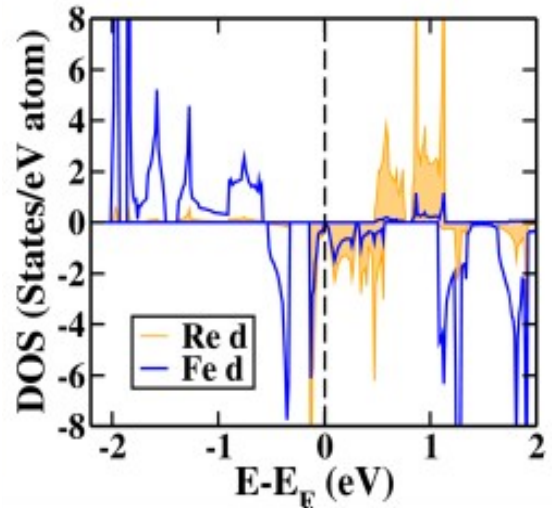


TRY OVERLAYER-SUBSTRATE GEOMETRY



GGA electronic structure:

Band structure in minority spin spin

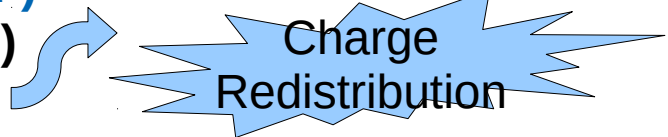


Half-metallic!

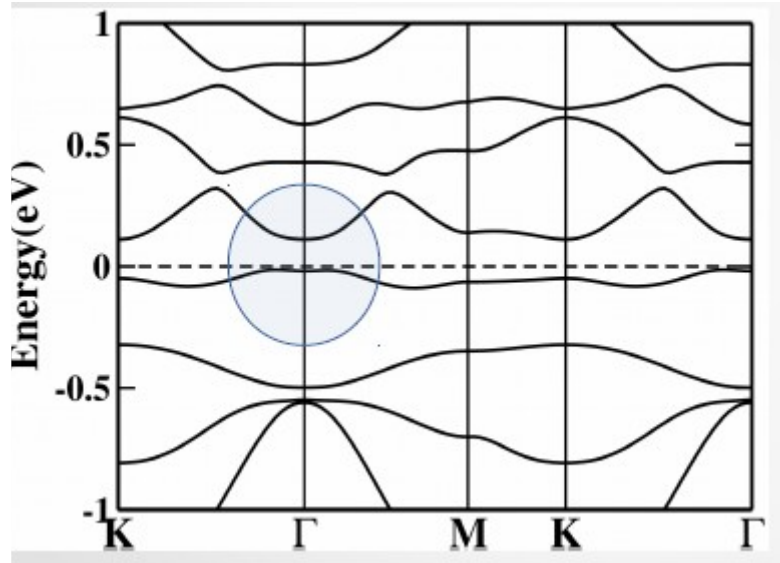
Gapped at every point except Γ (*half semi-metal*)

Quadratic band touching at Γ

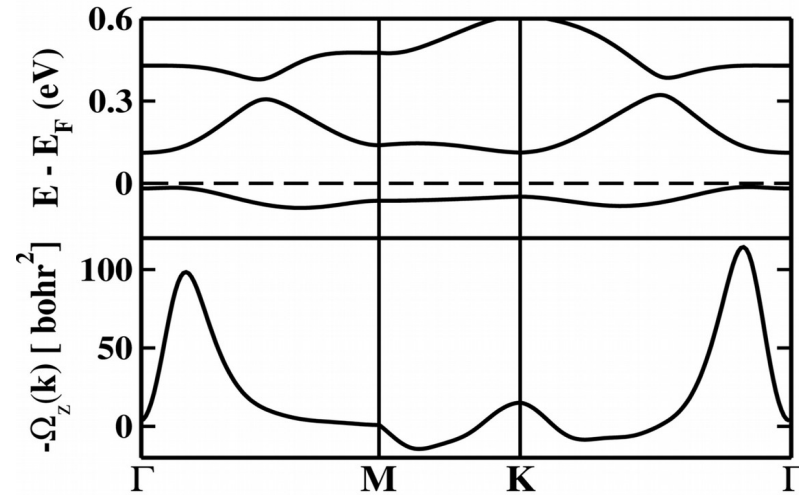
Overlayer: $\text{Fe}^{2+}(\text{d}^6)\text{-Re}^{6+}(\text{d}^1)$
 Bulk/QW: $\text{Fe}^{3+}(\text{d}^5)\text{-Re}^{5+}(\text{d}^2)$



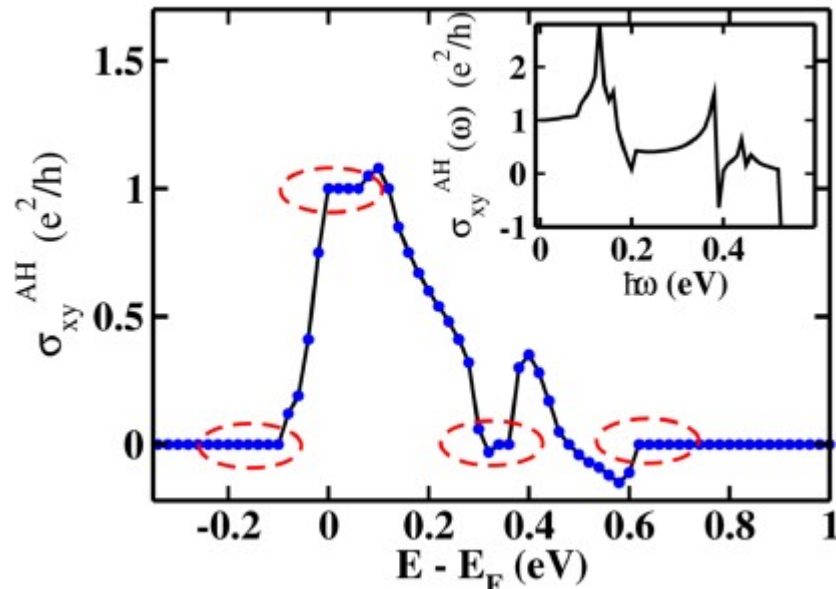
Effect of SOC: GGA +SOC electronic structure



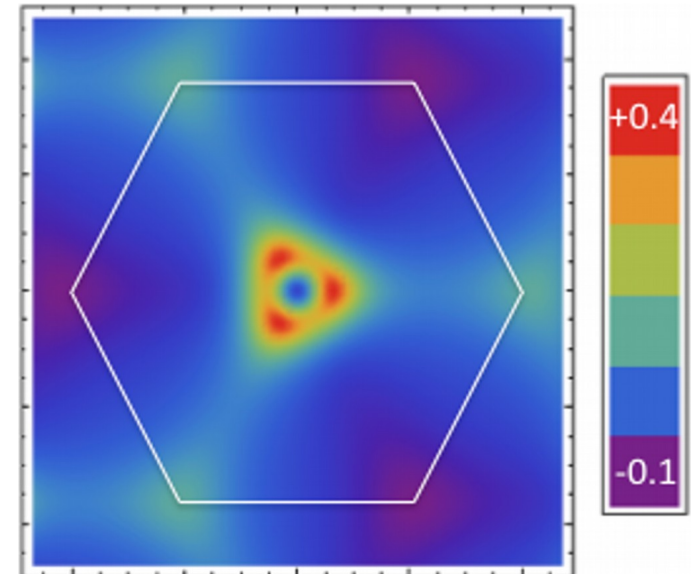
Large gap ~ 110 meV



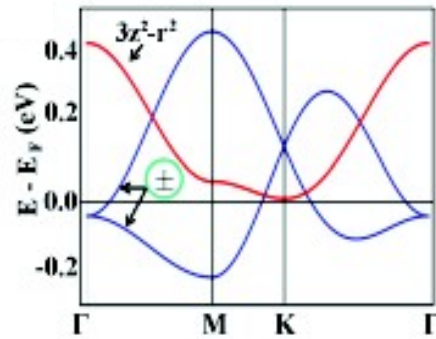
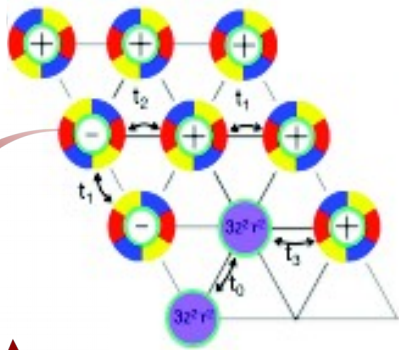
Inclusion of SOC gaps out the QBT



$C = 1$

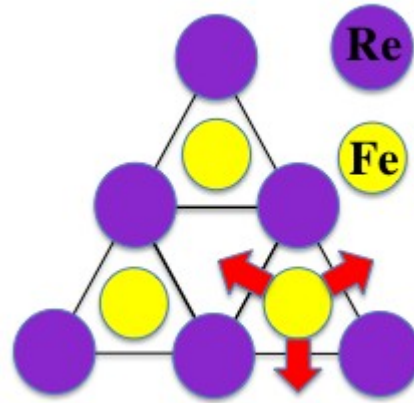
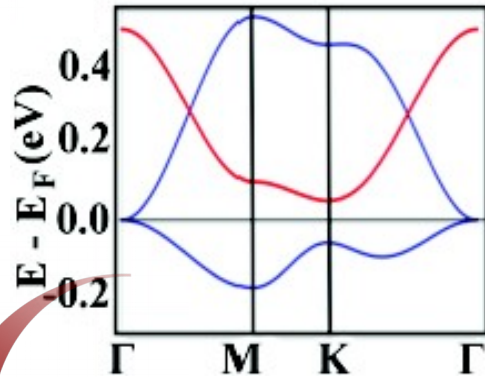


Analysis of band structure: 3 band TB model



3 band model derived from 5d Re t_{2g} bands in reduced C_3 symmetry

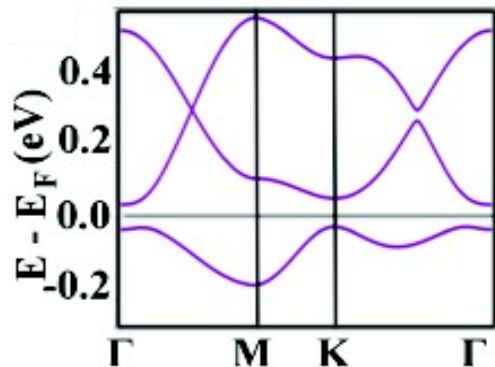
Dirac BT at hexagonal BZ corners and QBT at Γ



In-plane inversion symmetry breaking by localized 3d Fe generates in-plane electric field that couples with electric dipoles formed by $\pm e_g^\pi$ doublets

Gaps out the Dirac points at BZ corners.

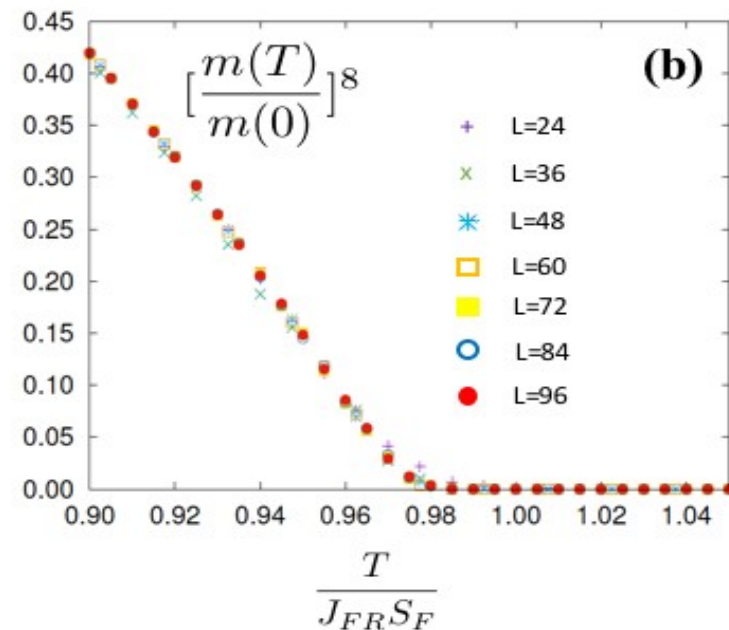
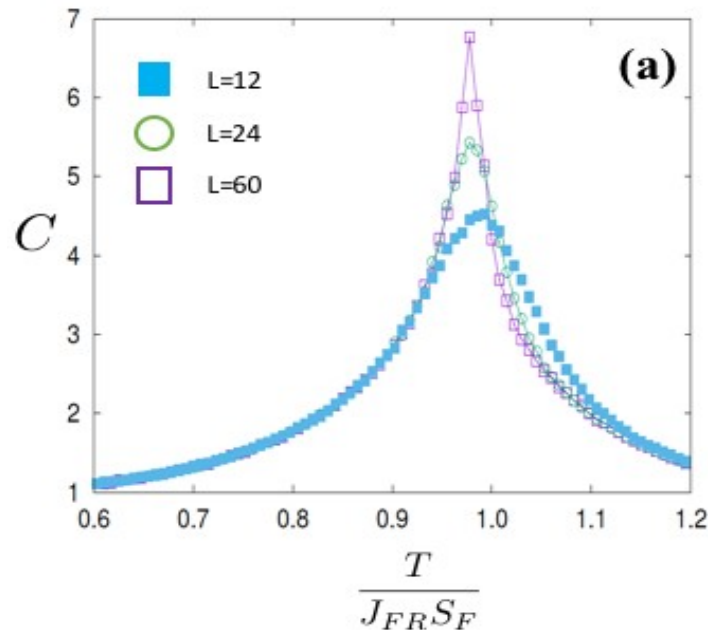
► *Orbital Rashba-type effect (PRL 2011)*



Introduction of SOC term gaps out the QBT.

► For **right filling** (d^1 of Re), this leads to QAHI

Strong SOC and trigonal distortion conspire to pin the Re moments to be perpendicular to the plane, leading to high FM T_c



DFT: $J_{\text{Fe-Fe}}$ (bulk) ~ 1 meV [agrees well INS Phys. Rev. B 87, 184412 (2013)],
 $J_{\text{Fe-Fe}}$ (bilayer) ~ 3.5 meV

$$H_{\text{Fe-Re}} = J_{\text{F-R}} \sum_{i \in \text{Fe}, \delta} S_i^z \sigma_{i+\delta}$$

Monte Carlo

(mixed Heisenberg-Ising):

$T_c \sim 315\text{K}$

(even slightly higher than bulk!)



Three Key Ingredients

1. [111] Bilayers of half-metallic 3d-4d/5d DPs show a strong **trigonal** distortion, favoring a non-Kramers doublet from t_{2g} states of 4d/5d TM in reduced C_3 symmetry \rightarrow bands in conducting spin channel features **Dirac band touching at +/- K, and a QBT at Γ .**

2. Breaking of in-plane inversion symmetry by 3d TM ions gaps out Dirac points BZ corners (**orbital Rashba effect**) \rightarrow for appropriate filling of 4d/5d this leads **half semi-metal.**

3. Strong SOC of 4d/5d TM ions gaps out QBT. *Strong SOC and trigonal distortion also conspire to pin 4d/5d moments perpendicular to the plane, maintaining high FM T_c even for bilayer.*

Should be general [DPs like Sr_2FeMoO_6 (T_c - 420 K), Sr_2CrWO_6 (T_c - 458 K)]

Santu Baidya, Umesh Waghmare, Arun Paramakanti, TSD Phys. Rev. B 94, 155405 (2016)

KAGOME INTERMETALLICS



Santu Baidya
(SNBNCBS-> Duisburg-Essen
-> SNU-> Rutgers)

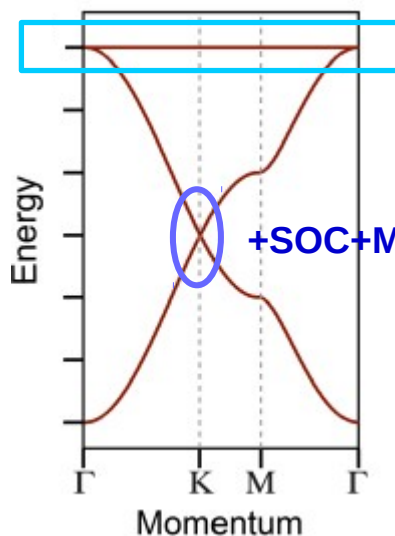
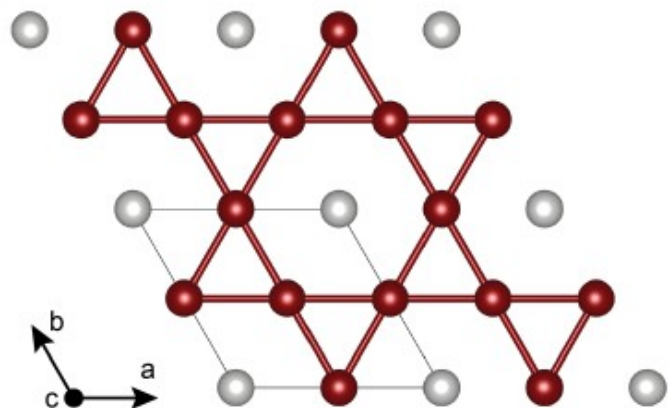


Aabhaas Mallik
(ICTS, Bangalore)



Subhro Bhattacharya
(ICTS, Bangalore)

Isolated Kagome' Layer

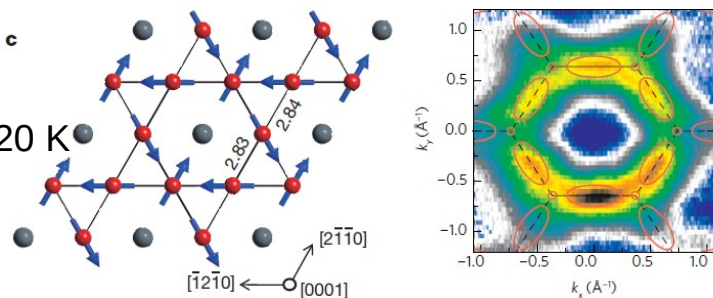


Phenomenology of Landau levels without external magn field

2D Chern Insulator (QAH)

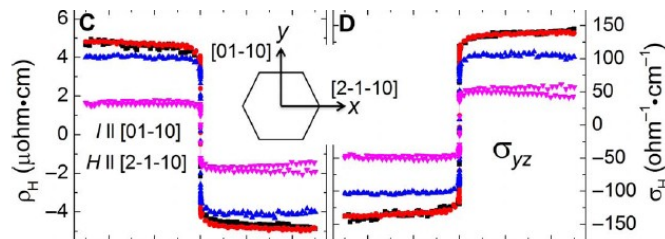
Binary intermetallic $T_m X_n$ Kagome' series ($T = \text{Mn/Fe/Co}$, $X = \text{Sn/Ge}$, $m:n = 3:1, 3:2, 1:1$)

Mn_3Sn
AFM, $T_N \sim 420 \text{ K}$



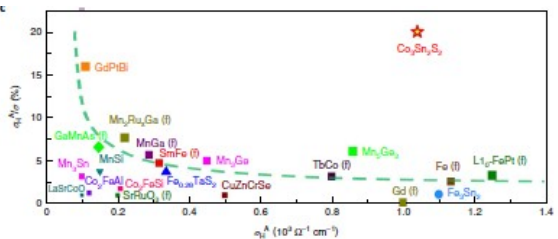
Large Anomalous Hall at RT (Nature, 2015)
Magnetic Weyl points (Nature Mater, 2017)

Mn_3Ge
AFM, $T_N \sim 365 \text{ K}$



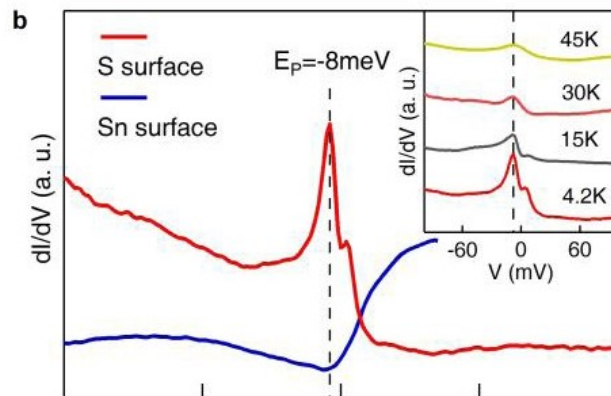
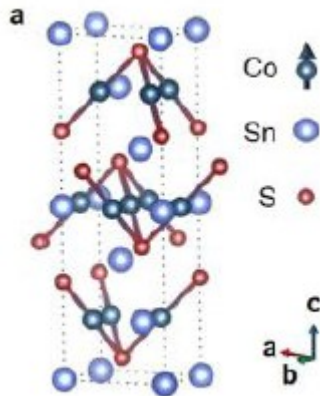
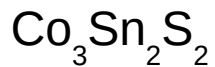
Large Anomalous Hall (Sci Adv, 2016)

$\text{Co}_3\text{Sn}_2\text{S}_2$
FM, $T_C \sim 170 \text{ K}$

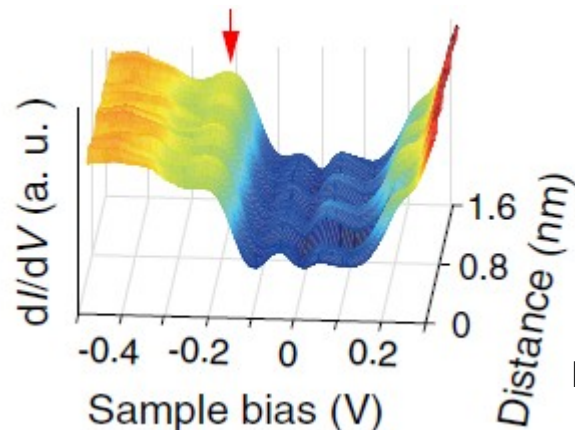
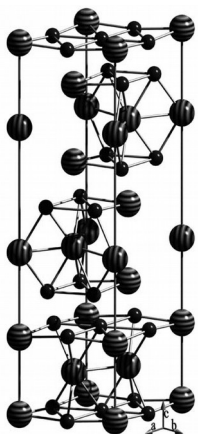
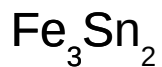


Giant Anomalous Hall (Nat Phys, 2018)

Search for Flat Bands

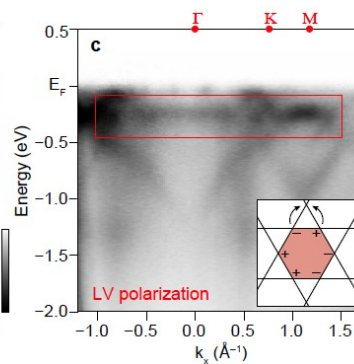
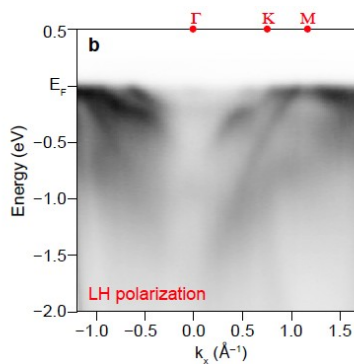
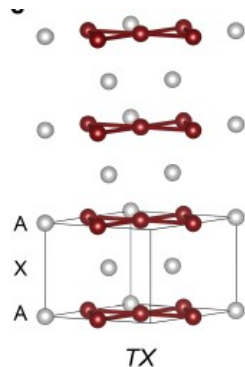


Nat Phy 15, 443 (2019)



PRL 121, 96401 (2018)

FeSn
(A-type AFM
FM Kagome layers
coupled AF)



$E_{\text{flat}} = -0.23$ eV

Kang et al, arXiv:1906.02167

Direct Signatures
remain elusive



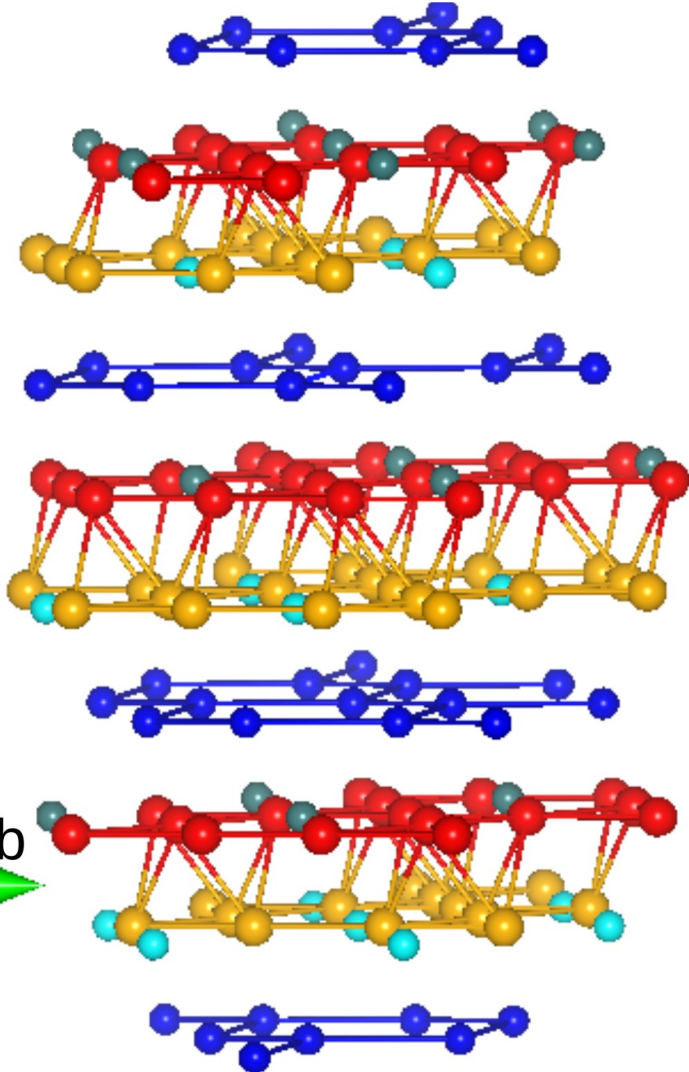
Can it be made better ?



How about creating 2D (quasi-2D) compounds ?

(a)

Bulk Fe_3Sn_2



Sn''

$\text{M}_3\text{Sn}'$

$\text{M}_3\text{Sn}'$

Sn''

$\text{M}_3\text{Sn}'$

$\text{M}_3\text{Sn}'$

Sn''

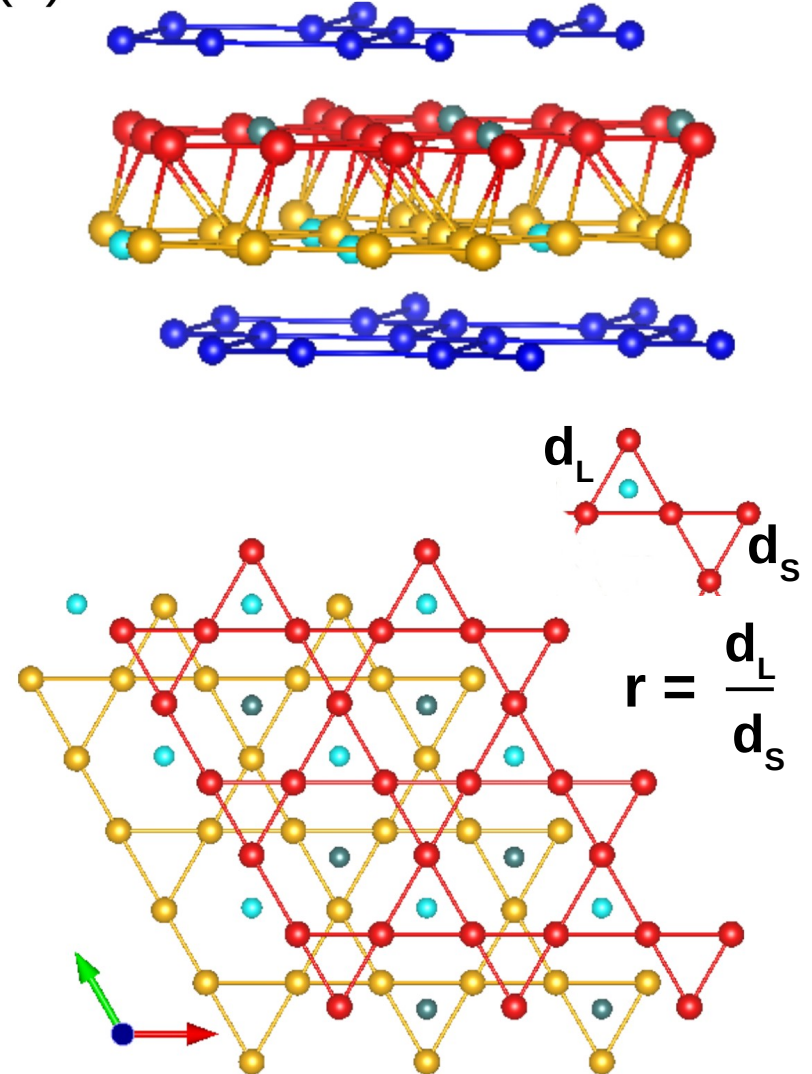
$\text{M}_3\text{Sn}'$

$\text{M}_3\text{Sn}'$

Sn''

(b)

BL Fe_6Sn_6

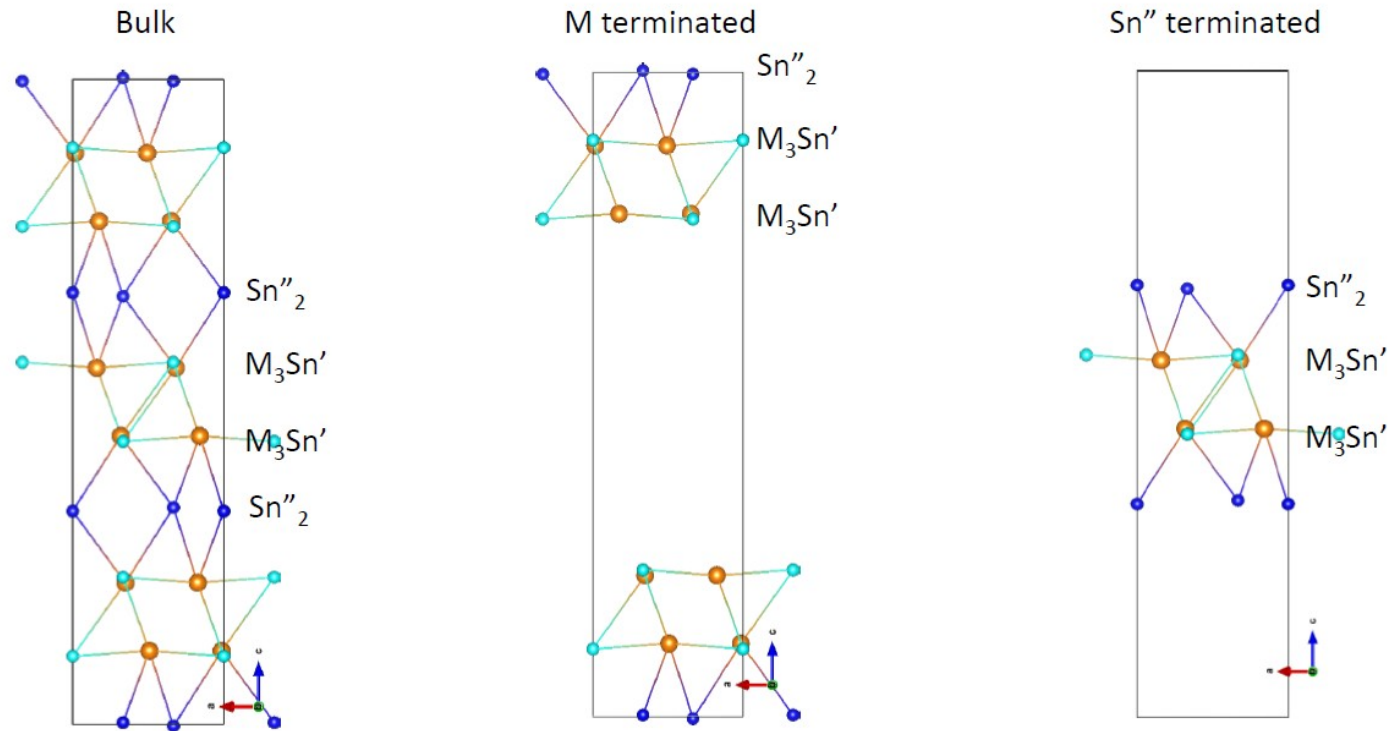


d_L

d_S

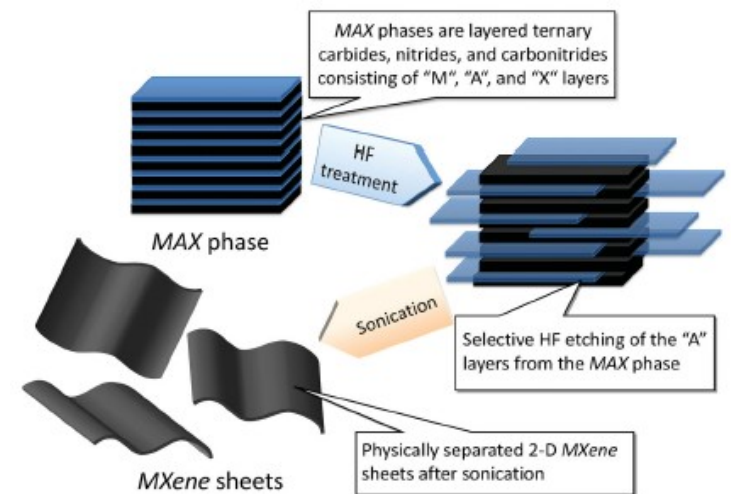
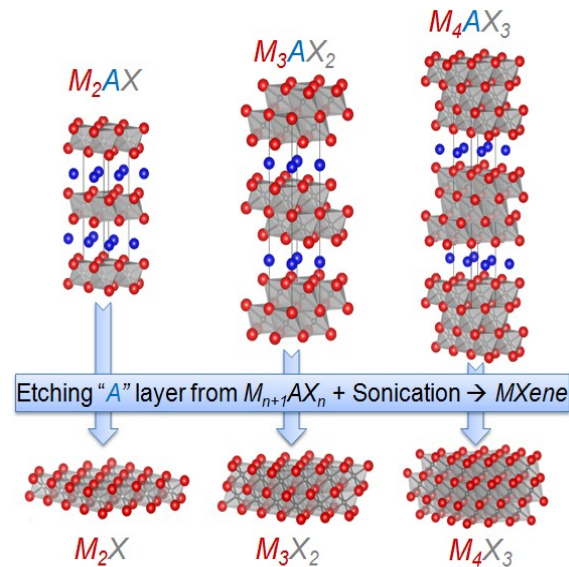
$r = \frac{d_L}{d_S}$

CLEAVAGE ENERGY



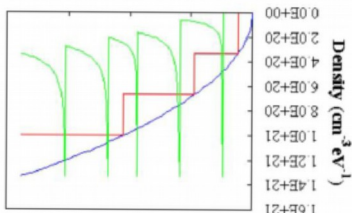
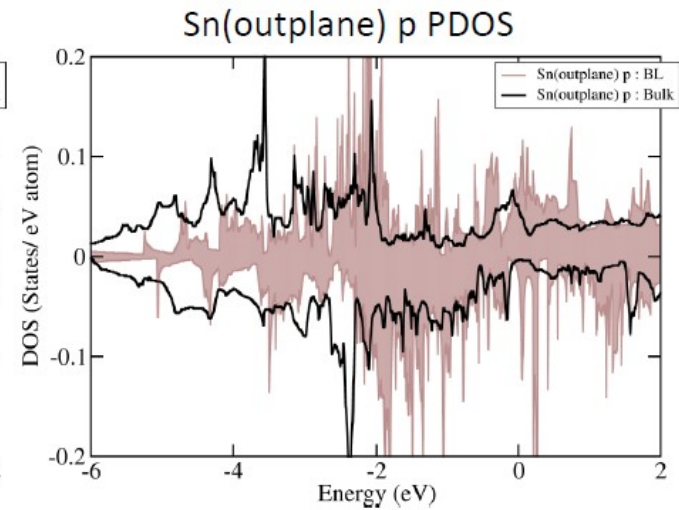
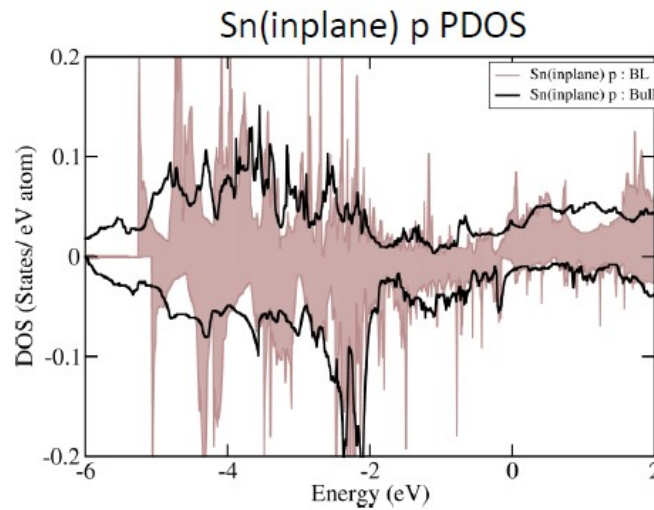
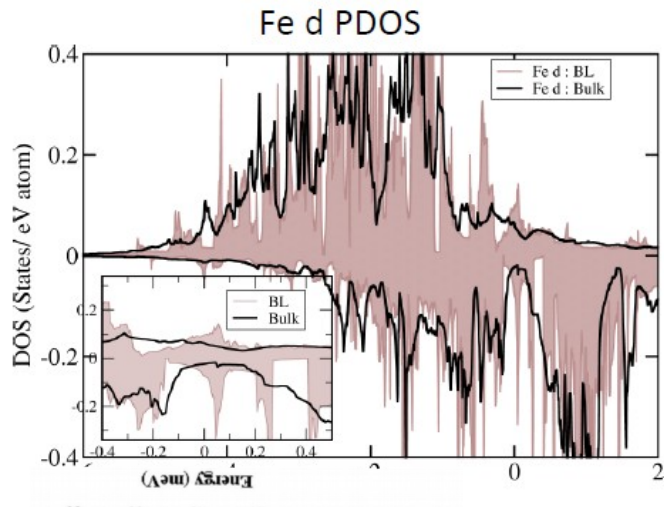
$$\text{Cleave Energy} = (\text{Energy}^{\text{M-term}} + \text{Energy}^{\text{Sn''term}} - \text{Energy}^{\text{Bulk}}) / (2 * \text{Area of surface of the slab})$$

Employ *chemical etching* route



Adv.Mater.2014,26,992-1005

Electronic Structure – Bulk vs BL



band	$m_{[100]}$	$m_{[010]}$	$m_{[001]}$
1	-3.50	-0.46	2041
2	-2.50	11.3	-2176
3	-5.43	0.33	16297

	Spin moment in μ_B	
	Bulk(Rhomb)	Bilayer
Fe :	2.2	2.0
Sn' :	-0.2	-0.2
Sn'' :	-0.13	-0.1

Total moment:		
	12.3217	11.5432

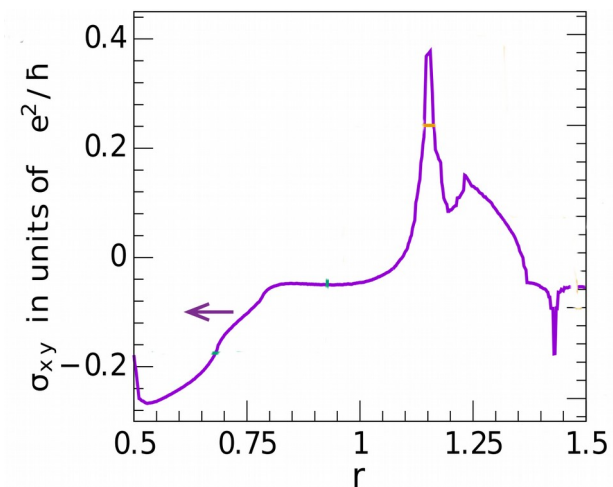
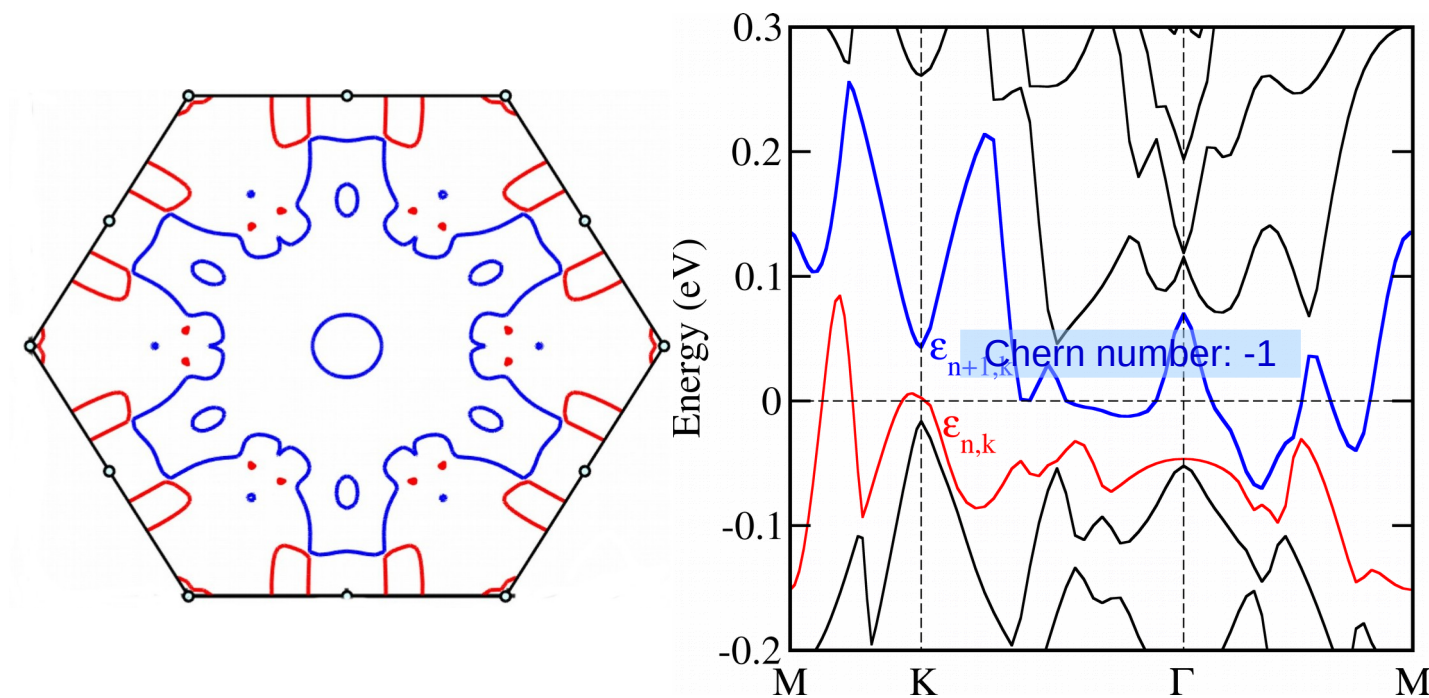
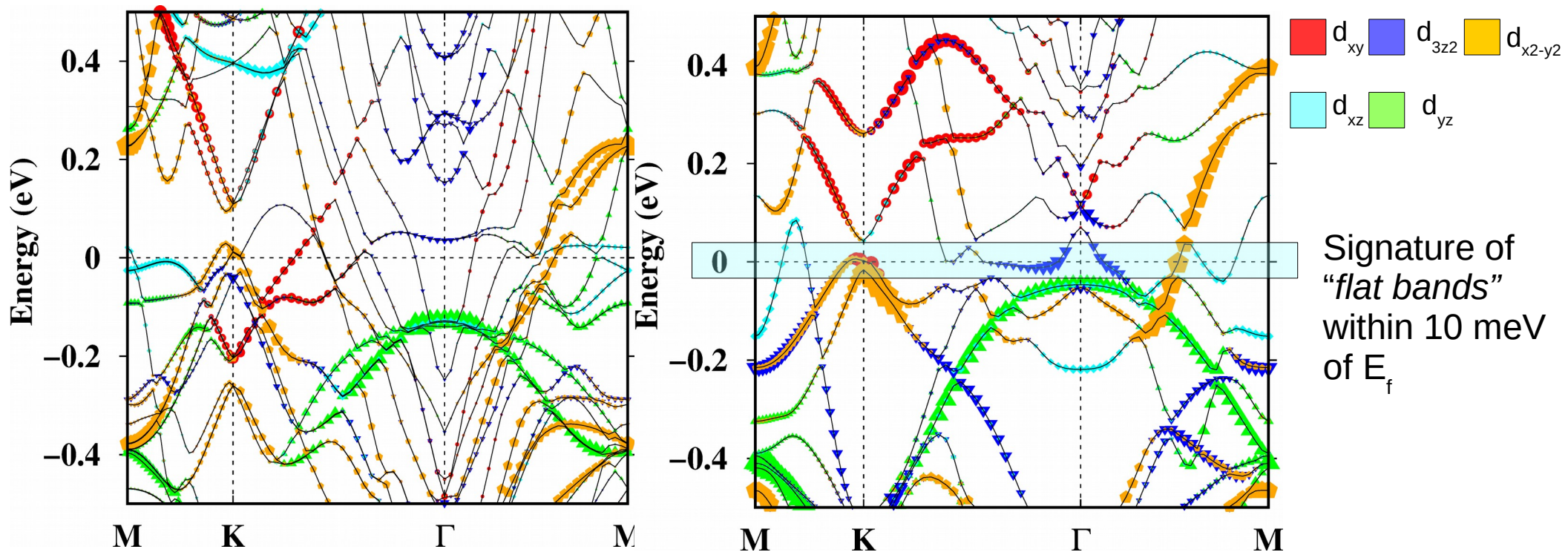
Magnetic exchanges:

$$J_{||} \sim 10 \text{ meV}$$

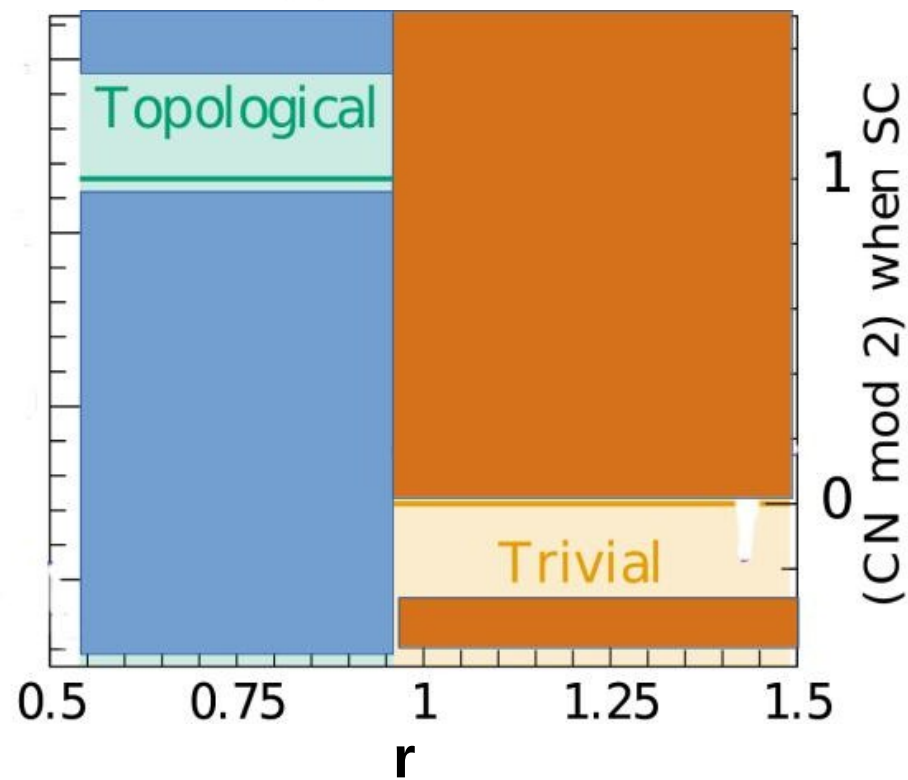
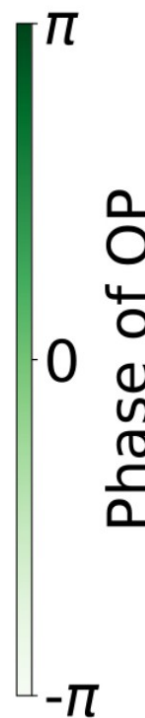
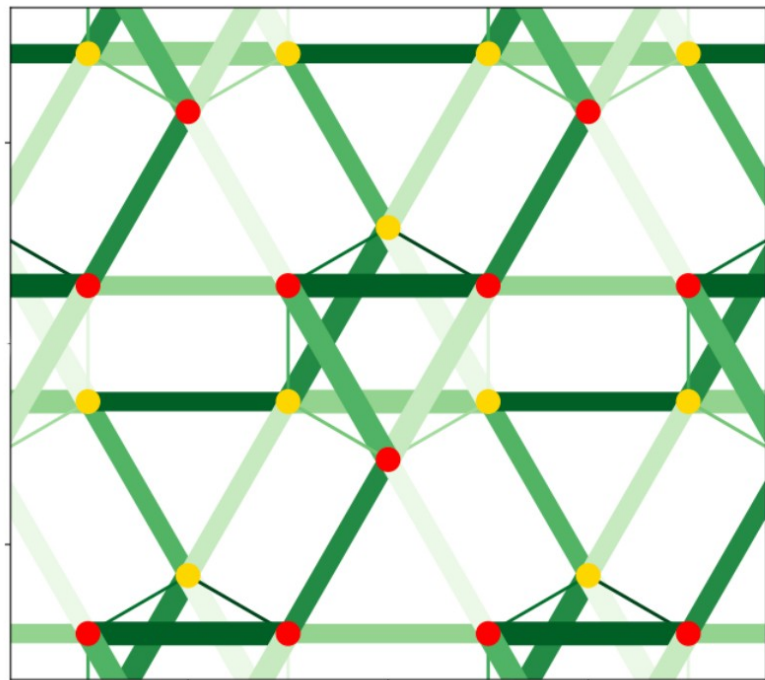
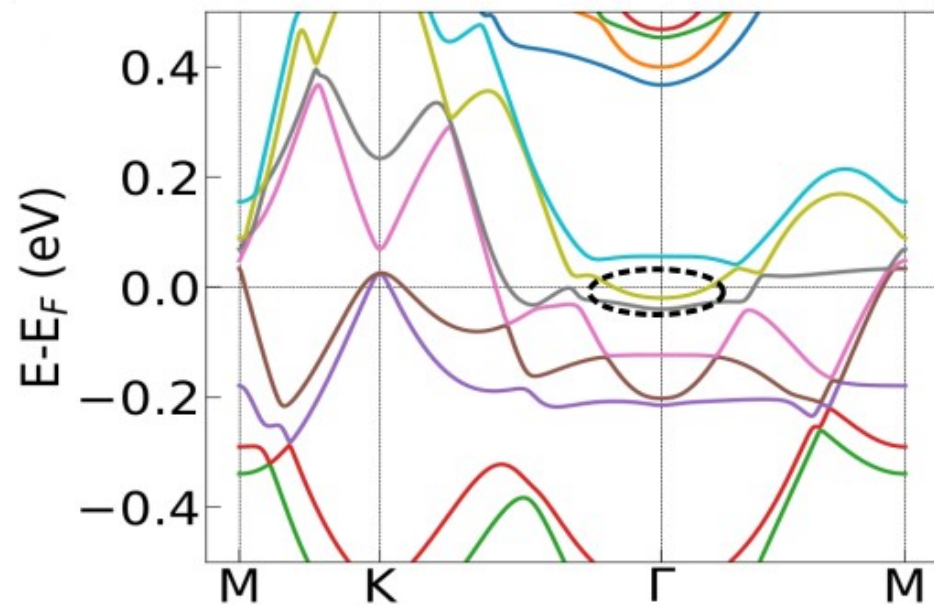
$$J_{\perp} \sim 0.3 \text{ meV}$$

FM correlation survives down to BL

Electronic Structure – Bulk vs BL




Unconventional Superconductivity





Conclusions

1. Geometric confinement to bilayer, results in (a) **quasi-2D or 2D** electronic structure, (b) survival of **ferromagnetic correlation**, and (c) realization of low-energy bands with suppressed band width – almost **flat bands**.
2. Finite AHC response for a wide range of asymmetry parameter, r .  Robust feature of a possible **Chern metal** phase in bilayer FeSn and allied materials.
3. Destruction of magnetic long-range order due to enhanced quantum fluctuations in low dimension can lead to **exotic superconductivity** (or fractional Chern insulating phase).

GRAPHENE UNDER DEFORMATION



Santu Baidya
(SNBNCBS-> Duisburg-Essen
-> SNU-> Rutgers)



Surajit Sengupta
(TIFR, Hyderabad)

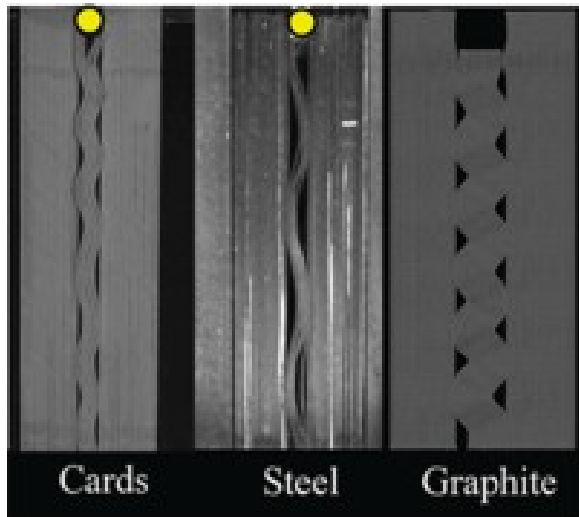


Debankur Das
(TIFR, Hyderabad)

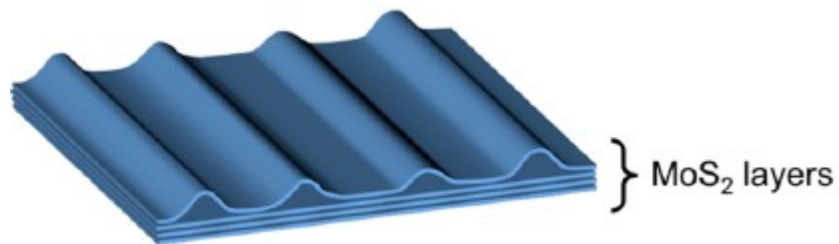


C. Sandhya
(TIFR, Hyderabad)

Deformation Mechanism in Layered Solids

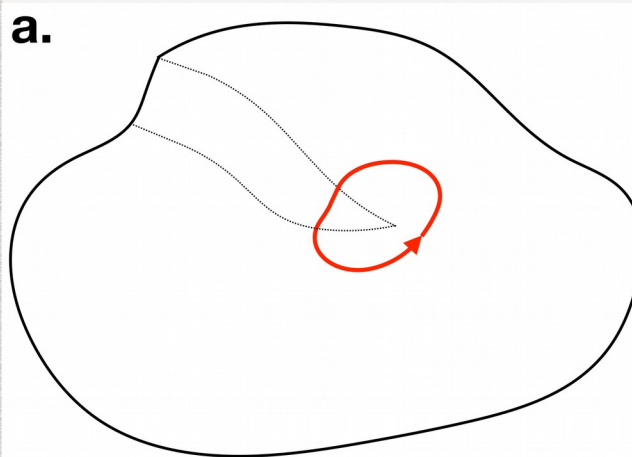


Phys. Rev. Materials 3, 013602 (2019)

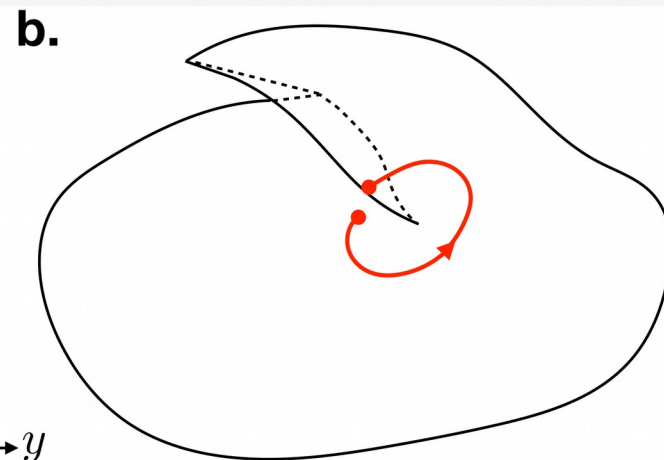


Nano Lett. 2015, 15, 1302–1308

TWO KINDS OF FLUCTUATIONS ARE POSSIBLE

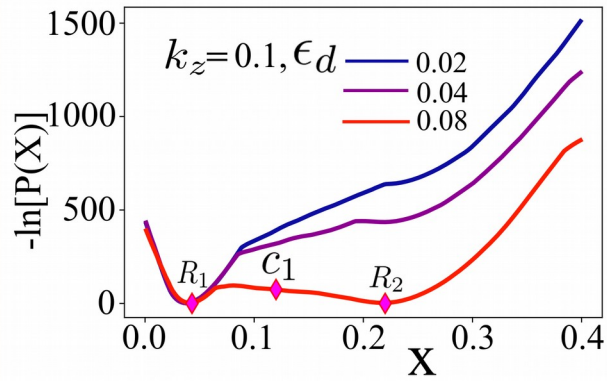


Ripples

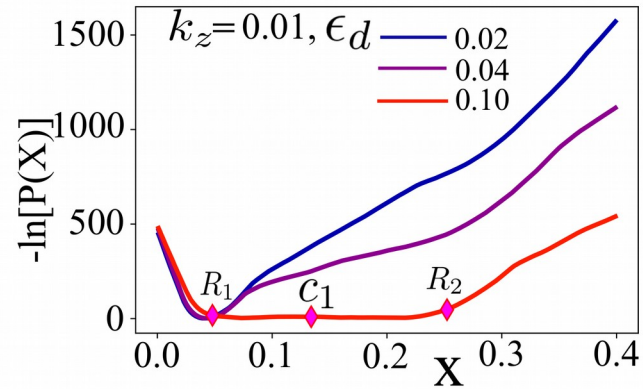


Ripplocations

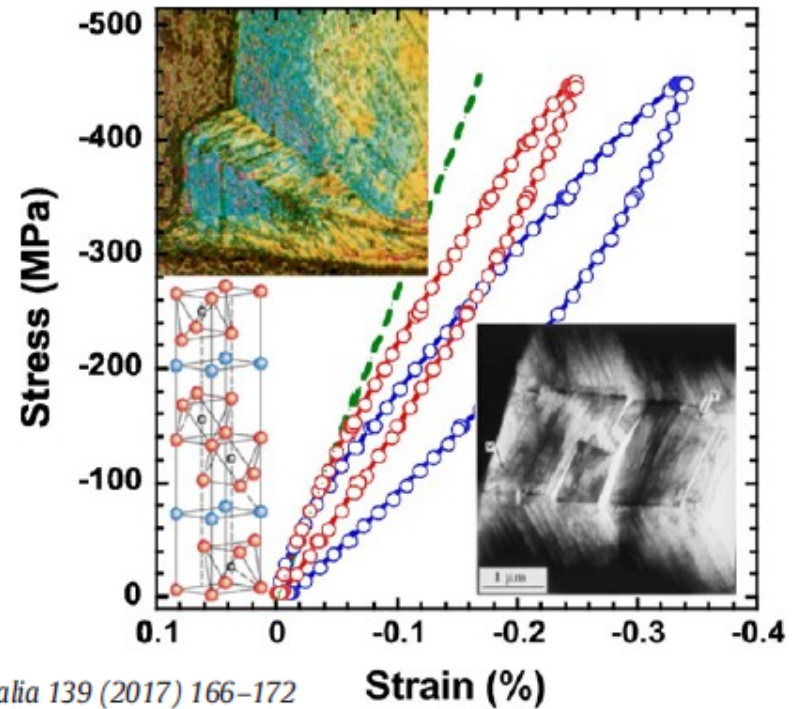
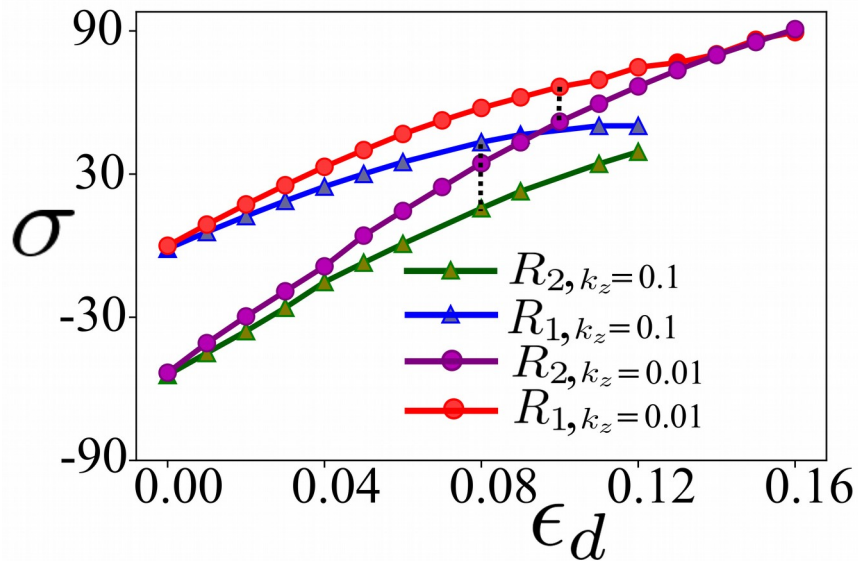
STRONG CONFINEMENT FAVOURS RIPPLES



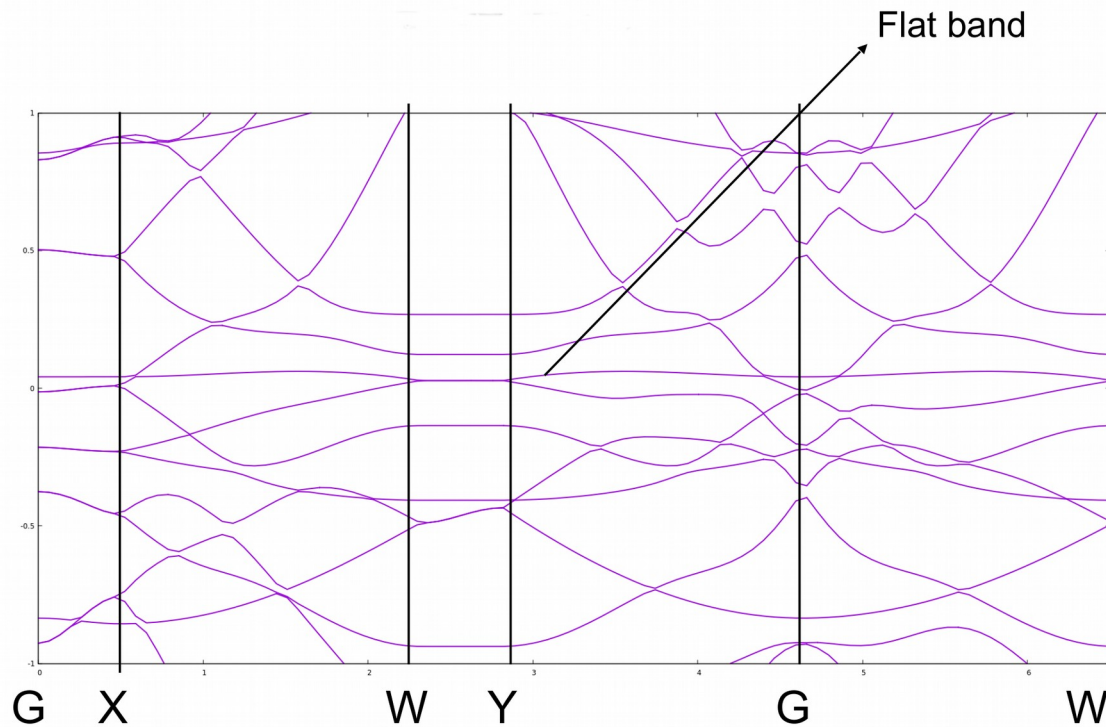
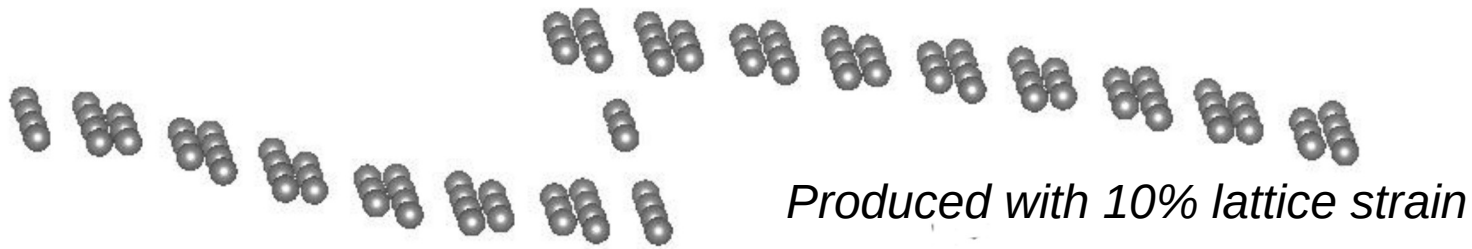
Ripplings



Ripples

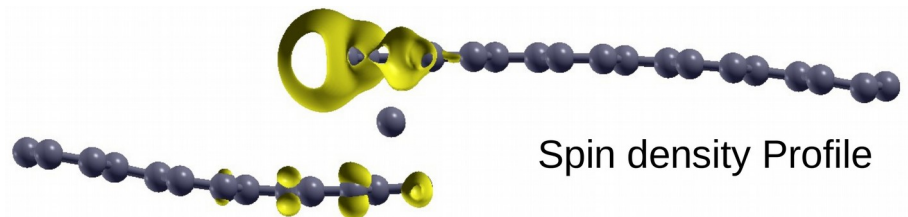


ELECTRONIC STRUCTURE OF PLEATED GRAPHENE



Calculated Chern Number turned out to be non trivial (-2)

Deformed graphene under strain may be source of **magnetic flat** Bands with **non trivial topological characters.**



Thank You

