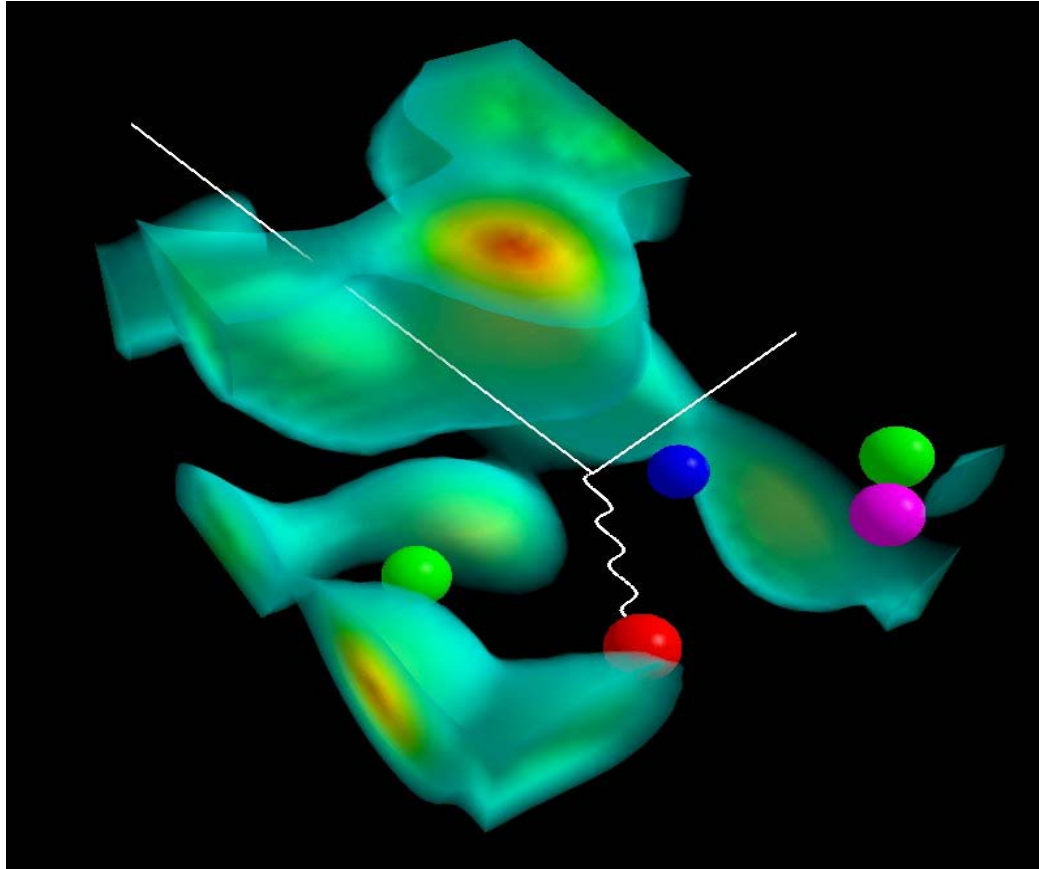


# The Effective Hadron-Hadron Interaction in-Medium



Australian Government  
Australian Research Council

Anthony W. Thomas

NN Interaction & the Nuclear Many-Body Problem  
ICTS - TIFR : November 25<sup>th</sup> 2010



# A Personal View of the Problems

- Traditional non-relativistic potential models or EFT with expansion in powers of  $Q/m_\rho$  inapplicable at high density – even at  $2\rho_0$
- Even at or below  $\rho_0$  chiral EFT suffers from not knowing the relevant degrees of freedom – typically start with N only; then discover the  $\Delta$ ; but are these the correct degrees of freedom?
- Phenomenological (“realistic” or “ab initio”) NN forces have many ( $>20$ ) parameters and often serious cancellations – e.g. Jülich  $\Lambda$ N force



# Problems (cont.)

- **Traditional fit to NN force also needs lots of data (OK for NN but hopeless for HN) to determine parameters (within assumed form) and 3-body force fit to nuclear energy levels**
- **Finally, many fundamental problems such as EMC effect cannot be addressed**

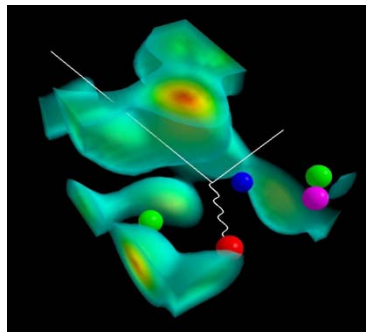


# A Really Attractive Alternative

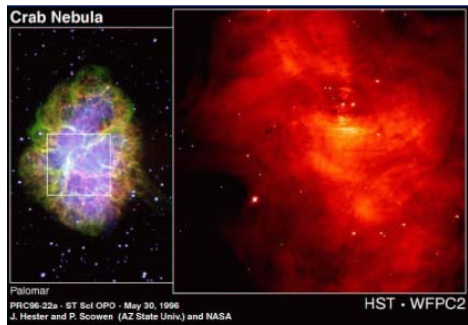
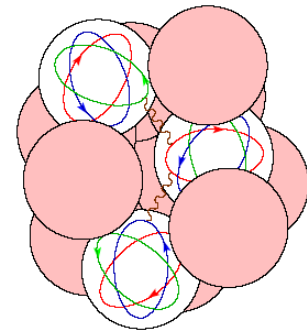
- Start with a quark and gluon based model of hadron structure
- Imbed the hadron in-medium and solve (respecting special relativity) for its structure self-consistently at mean-field level (using Born-Oppenheimer approximation)
- Determine the small number of parameters (3 quark-meson coupling constants) from saturation of nuclear matter
- This yields the effective in-medium forces felt by every hadron that exists in the quark model chosen
  - with no new parameters



**N,  $\Lambda$ ,  $\Xi$ ,  $\omega$ , D, J/ $\Psi$  ..... in nuclear matter**



**QCD & hadron structure**



**n star**

**$\infty$  nuclear matter**

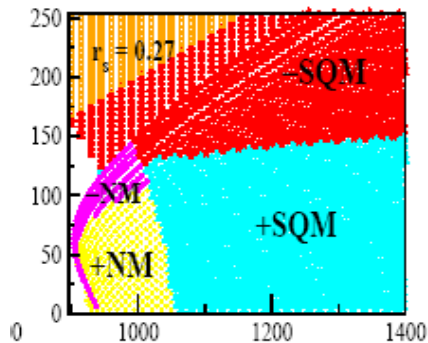
**Effective NN (and N  $\Lambda$ , N  $\Xi$  ...) forces**



**quark matter**



**Finite nuclei  
Hypernuclei**



# Where to find more information

- **Two major, recent papers:**
  - I. Guichon, Matevosyan, Sandulescu, Thomas, Nucl. Phys. A772 (2006) 1.
  - II. Guichon and Thomas, Phys. Rev. Lett. 93 (2004) 132502
- **Built on earlier work on QMC: e.g.**
  - III. Guichon, Phys. Lett. B200 (1988) 235
  - IV. Guichon, Saito, Rodionov, Thomas, Nucl. Phys. A601 (1996) 349
- **Major review of applications of QMC to many nuclear systems:**
  - V. Saito, Tsushima, Thomas, Prog. Part. Nucl. Phys. 58 (2007) 1-167 (hep-ph/0506314)

# Model Independent Features of NN Force

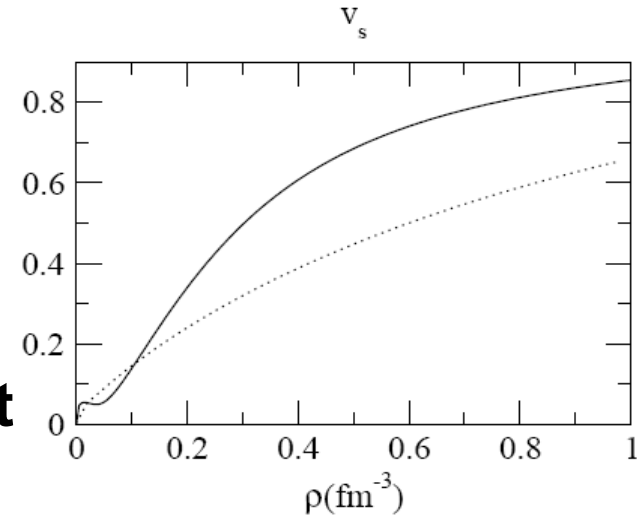
- Intermediate Range attraction is **Lorentz scalar-isoscalar** (since 70's, dispersion relations, Paris potential...)
- **Lorentz scalar force is strong (too strong in QHD)!**
- Short distance repulsion is **Lorentz vector** (not so model independent BUT lots of support)
- At high density MFA gets to be accurate
- Classical implementation is Walecka model  
    ➔  $m_N^* / m_N \sim 0.5$  at  $\rho_0$



# Relativity Matters in Dense Matter

- Non-relativistic expansion in powers of  $k_F$  unlikely to be successful.....

e.g.  $v_{\text{sound}} > c / 2$  at  $\rho = 2 \rho_0$   
and exceeds  $c$  at higher density;  
- whereas  $v_{\text{sound}} = 0.3 c$  and never exceeds  $c$  in relativistic treatment



- BUT what is missing in Walecka model (QHD)?

- Effect of  $m_N^* = m_N / 2$  on internal structure of nucleon; this is a huge external field!

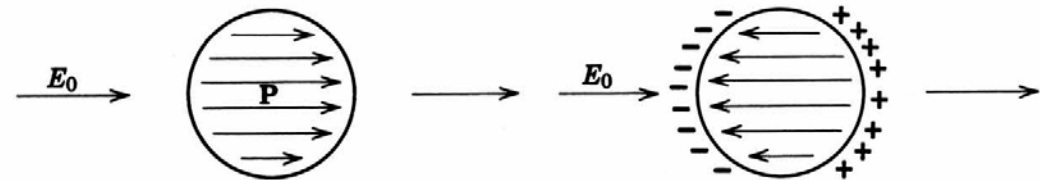




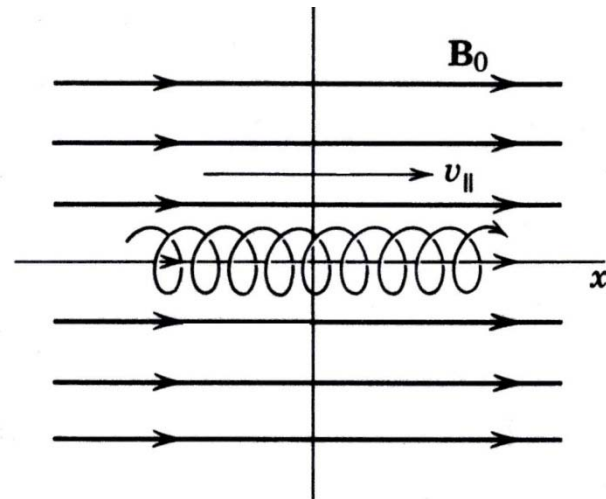
# What happens if we put an atom in a strong electric field?

Jackson :

i.e. atom has a polarizability:  
its internal structure is  
rearranged in response to  
applied field



///'ly in applied magnetic field  
(indeed, in super strong field  
-e.g. n-star surface atoms &  
molecules essentially linear!)



# Electric & Magnetic Polarizabilities of Nucleon are Measured

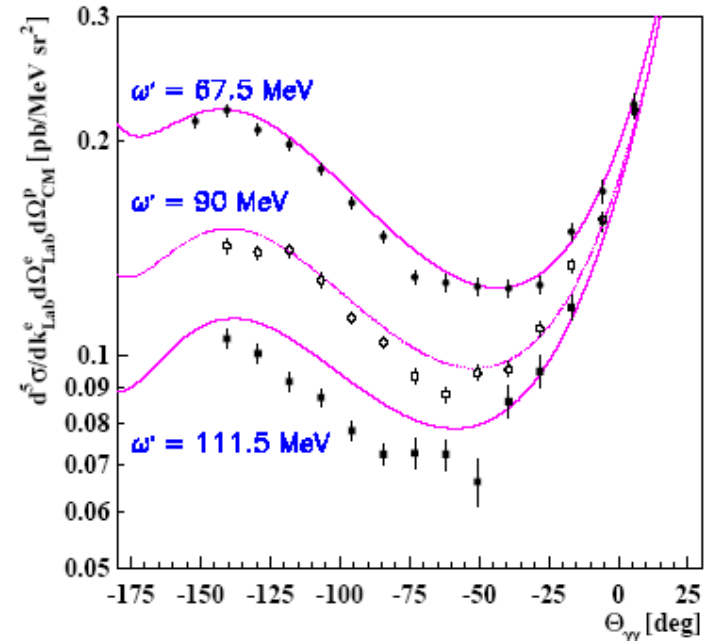
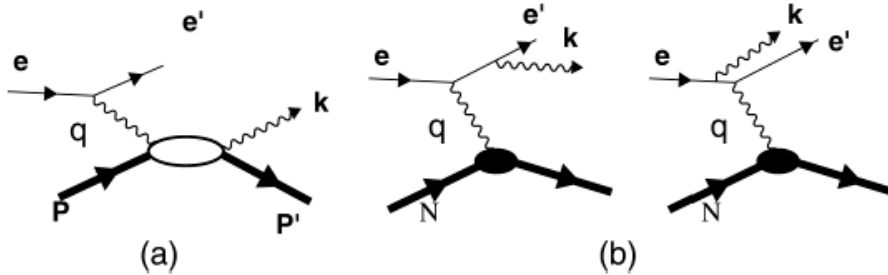
e.g. Compton scattering:

$$4\pi\alpha_E = 2 \sum_{I \neq N} \frac{|\langle I | d_z | N \rangle|^2}{E_I - E_N}$$

$$\alpha_E^p = (12.1 \pm 1.3) \cdot 10^{-4} \text{ fm}^3,$$

$$\beta_M^p = (2.1 \mp 1.3) \cdot 10^{-4} \text{ fm}^3.$$

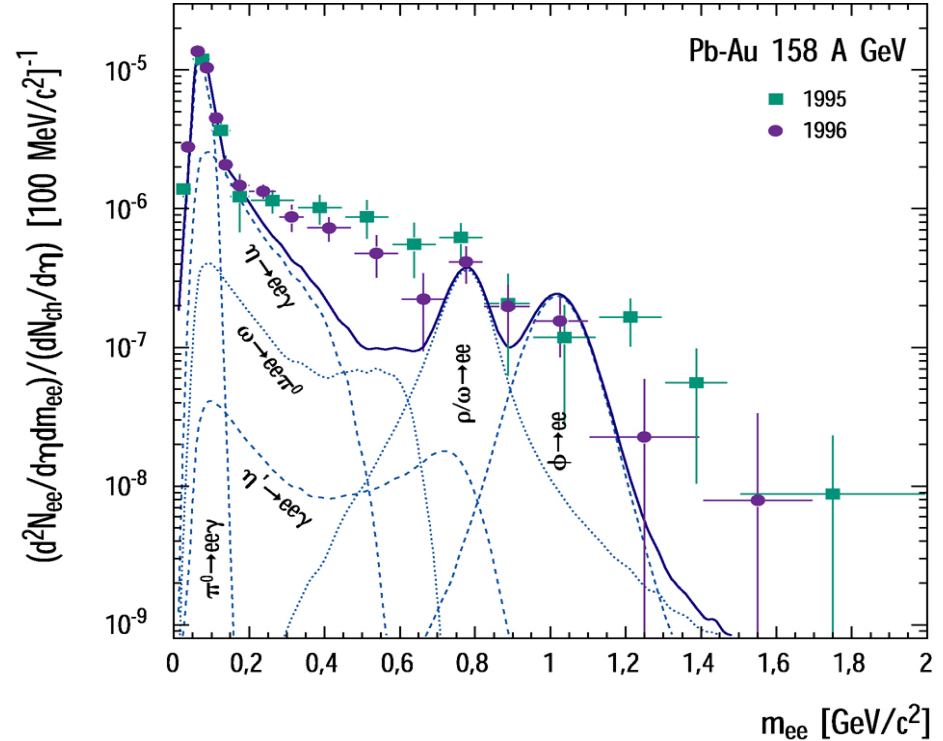
Also Virtual Compton Scattering ) GPs



# So what?

Atoms respond to external E and B fields

- Nucleons respond to external E and B fields
- It is clear that nucleons must respond to large scalar fields known to exist in-medium
- This leads to a mass shift that is non-linear in mean scalar field : scalar polarizability



# Fundamental Question: “What is the Scalar Polarizability of the Nucleon?”

Nucleon response to a chiral invariant scalar field is then a nucleon property of great interest...

$$M^*(\vec{R}) = M - g_\sigma \sigma(\vec{R}) + \frac{d}{2} (g_\sigma \sigma(\vec{R}))^2$$

Non-linear dependence through the scalar polarizability  
 $d \sim 0.22 R$  in original QMC (MIT bag)

Indeed, in nuclear matter at mean-field level (e.g. QMC), this is the **ONLY** place the response of the internal structure of the nucleon enters.



# ORIGIN .... in QMC Model

$$[i\gamma^\mu \partial_\mu - (m_q - g_\sigma q \bar{\sigma}) - \gamma^0 g_\omega q \bar{\omega}] \psi = 0$$

Source of  $\sigma$   
changes:

$$\int_{Bag} d\vec{r} \bar{\psi}(\vec{r}) \psi(\vec{r})$$

**SELF-CONSISTENCY**

and hence mean scalar field changes...

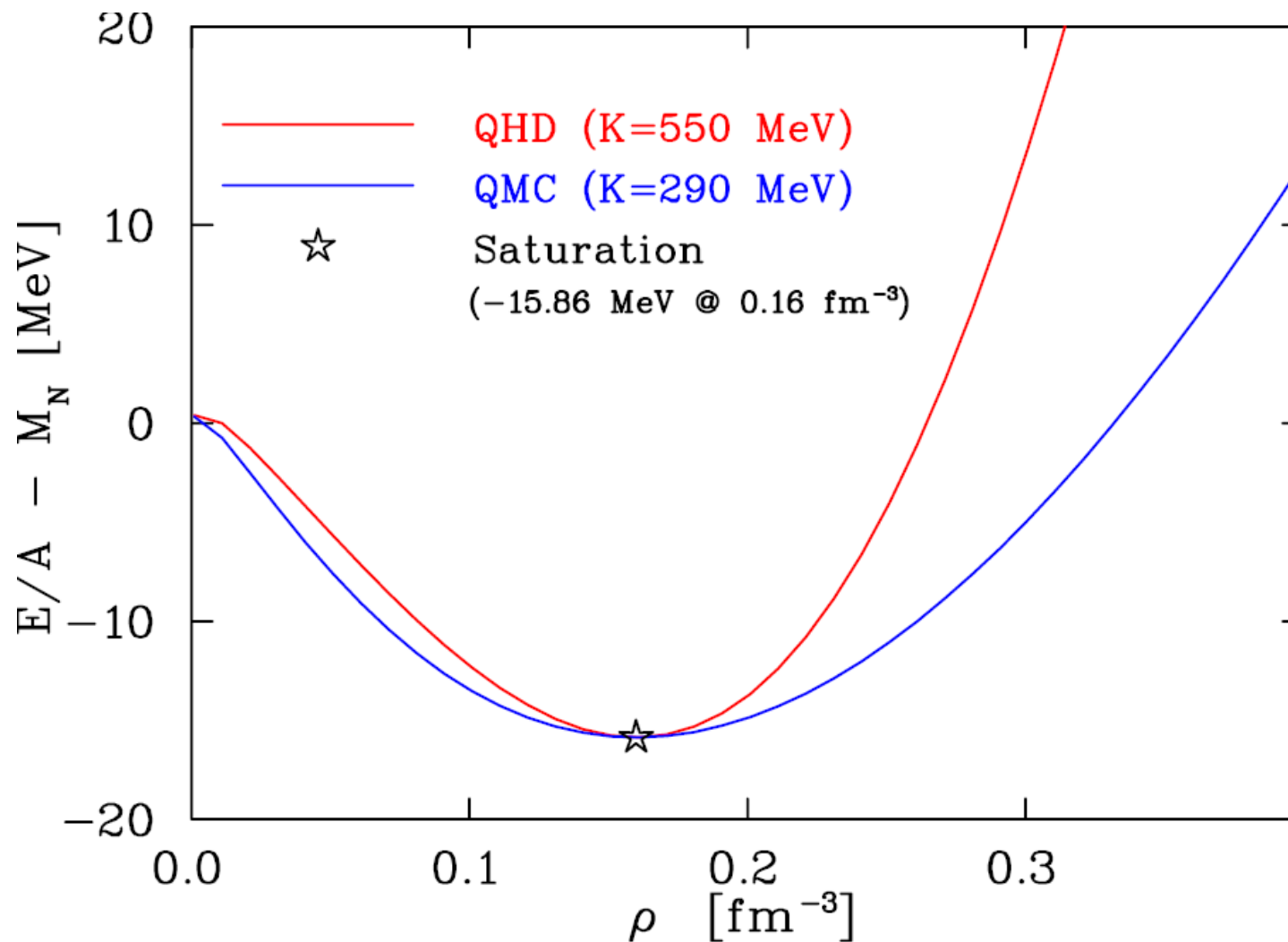
and hence quark wave function changes....

**THIS PROVIDES A NATURAL SATURATION MECHANISM  
(VERY EFFICIENT BECAUSE QUARKS ARE ALMOST MASSLESS)**

source is suppressed as mean scalar field increases  
(i.e. as density increases)

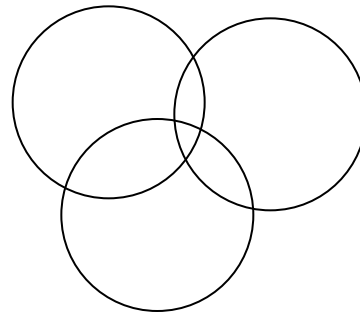
$$M^*(\vec{R}) = M - g_\sigma \sigma(\vec{R}) + \frac{d}{2} (g_\sigma \sigma(\vec{R}))^2$$

# Saturation of symmetric nuclear matter



# Summary : Scalar Polarizability

- Can always rewrite non-linear coupling as linear coupling plus non-linear scalar self-coupling – likely physical origin of non-linear versions of QHD
- In nuclear matter this is the **only** place the internal structure of the nucleon enters in MFA
- Consequence of polarizability in atomic physics is many-body forces:



$$V = V_{12} + V_{23} + V_{13} + V_{123}$$

– same is true in nuclear physics

# Summary so far .....

- QMC looks superficially like QHD but it's fundamentally different from *all* other approaches
- Self-consistent adjustment of hadron structure opposes applied scalar field (“scalar polarisability”)
- Naturally leads to saturation of nuclear matter
  - effectively because of natural 3- and 4-body forces
- Only 3- 4 parameters:  $\sigma$ ,  $\omega$  and  $\rho$  couplings to light quarks (and  $m_\sigma$  ambiguous when theory is quantised)
- Fit to nuclear matter properties and then *predict* the interaction of any hadron in-medium





# Can we Measure Scalar Polarizability in Lattice QCD ?

- IF we can, then in a real sense we would be linking nuclear structure to QCD itself, because scalar polarizability is sufficient in simplest, relativistic mean field theory to produce saturation
- Initial ideas on this published recently:  
the trick is to apply a chiral invariant scalar field  
– do indeed find polarisability opposing applied  $\sigma$  field

**18<sup>th</sup> Nishinomiya Symposium: nucl-th/0411014**  
– published in Prog. Theor. Phys.

# Linking QMC to Familiar Nuclear Theory

Since early 70's tremendous amount of work  
in nuclear theory is based upon effective forces

- Used for everything from nuclear astrophysics to collective excitations of nuclei
- Skyrme Force: Vautherin and Brink

In Paper I: **Guichon and Thomas, Phys. Rev. Lett. 93, 132502 (2004)**

we explicitly obtained effective force, 2- plus 3- body, of Skyrme type

- equivalent to QMC model (required an expansion around  $\sigma = 0$ )

# Comparison Between Skyrme III and QMC

	QMC	QMC	SkIII	QMC(N=3)
$m_\sigma (MeV)$	500	600		600
$t_0 (MeV fm^3)$	-1071	-1082	-1129	-1047
$x_0$	0.89	0.59	0.45	0.61
$t_3 (MeV fm^6)$	16620	14926	14000	12996
$M_{eff} / M$	.915	.814	.763	.821
$5t_2 - 9t_1 (MeV fm^5)$	-7622	-4330	-4030	-4036
$W_0 (MeV fm^5)$	118	97	120	91

Three-body force, arising from scalar polarizability, agrees naturally with force ( $t_3$ ) found phenomenologically - origin is same as that in atomic and molecular physics!



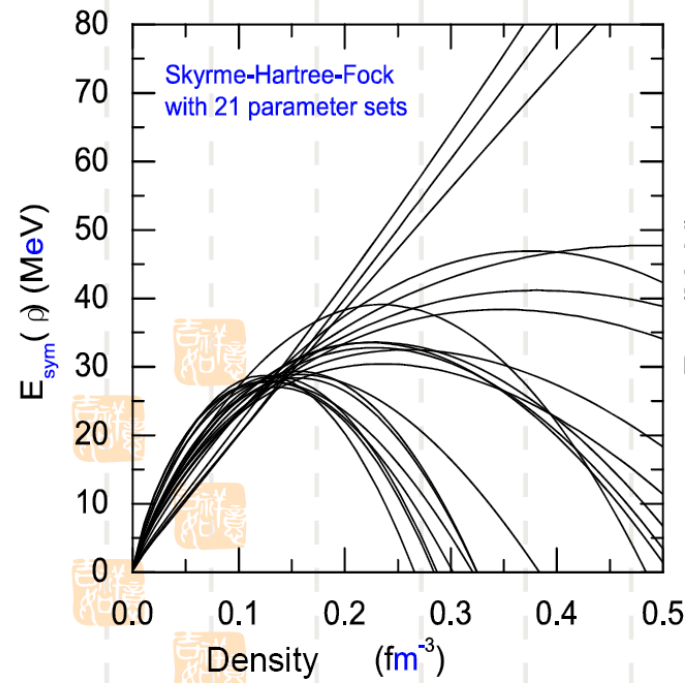
# Density Dependent Skyrme Force(s) are now more widely used

$$\begin{aligned}
 E_o = \frac{\mathcal{E}}{\rho} = & \frac{3\hbar^2}{10M} \left(\frac{3\pi^2}{2}\right)^{2/3} \rho^{2/3} H_{5/3} + \frac{t_0}{8} \rho [2(x_0 + 2) - (2x_0 + 1)H_2] \\
 & + \frac{1}{48} \sum_{i=1}^3 t_{3i} \rho^{\sigma_i+1} [2(x_{3i} + 2) - (2x_{3i} + 1)H_2] + \frac{3}{40} \left(\frac{3\pi^2}{2}\right)^{2/3} \rho^{5/3} (aH_{5/3} + bH_{8/3}) \\
 & + \frac{3}{40} \left(\frac{3\pi^2}{2}\right)^{2/3} \rho^{8/3} [t_4(x_4 + 2)H_{5/3} - t_4(x_4 + 0.5)H_{8/3}].
 \end{aligned}$$

$$a = t_1(x_1 + 2) + t_2(x_2 + 2),$$

$$b = \frac{1}{2} [t_2(2x_2 + 1) - t_1(2x_1 + 1)],$$

$$H_n(y) = 2^{n-1} [y^n + (1-y)^n]. \quad y = Z/A$$



**Skyrme forces fit 10-15 parameters to properties of symmetric nuclear matter as well as selected sets of other data**

**For example:**

- **Sly** : n-matter, n-stars, large-A nuclei
- **SkI** : isotope shifts in Pb region
- **SkM\*** : finite nuclei & actinide fission barriers
- **SSk** : nuclear masses

# In past few weeks: global search on Skyrme forces

## The Skyrme Interaction and Nuclear Matter Constraints

M. Dutra, O. Lourenço, J. S. S. Martins, and A. Delfino

*Departamento de Física - Universidade Federal Fluminense,  
Av. Litorânea s/n, 24210-150 Boa Viagem, Niterói RJ, Brazil*

J. R. Stone

*Department of Physics, University of Oxford,*

*OX1 3PU Oxford, United Kingdom and*

*Department of Physics and Astronomy,*

*University of Tennessee, Knoxville, Tennessee 37996, USA*

C. Providência

*Centro de Física Computacional,*

*Department of Physics,*

*University of Coimbra,*

*P-3004-516 Coimbra, Portugal*

**These authors tested 233  
widely used Skyrme forces  
against 12 standard nuclear  
properties: only 17 survived  
including two QMC potentials**

Furthermore, we considered weaker constraints arising from giant resonance experiments on isoscalar and isovector effective nucleon mass in SNM and BEM, Landua parameters and low-mass neutron stars. If these constraints are taken into account, the number of CSkP reduces to to 9, GSkI, GSkII, KDE0v1, LNS, NRAPR, **QMC700, QMC750** and SKRA, the CSkP\* list.

**Truly remarkable – force derived from quark level does a better job of fitting nuclear structure constraints than phenomenological fits with 4-5 times # parameters!**



# Constraints from Heavy Ion Reactions

– from Dutra et al. (2010)

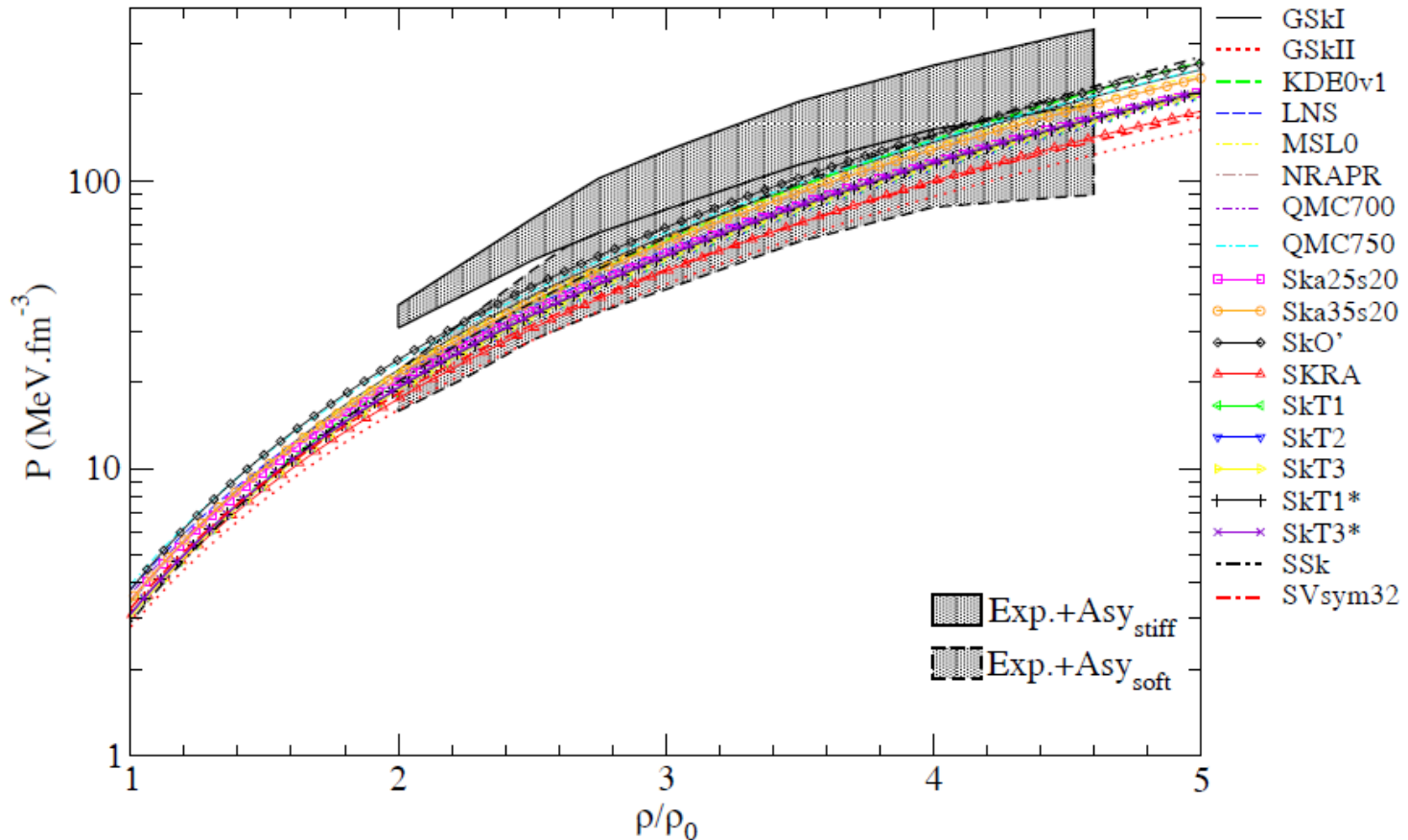


FIG. 4: (color online). Constraint PNM2: Pressure in the pure neutron matter as a function of density in the region  $2 \leq \frac{\rho}{\rho_0} \leq 4.6$ . For detailed explanation see Ref. [24].

# Physical Origin of Density Dependent Force of the Skyrme Type within the Quark Meson Coupling Model

P.A.M. Guichon<sup>1</sup>, H.H. Matevosyan<sup>2,3</sup>, N. Sandulescu<sup>1,4,5</sup> and A.W. Thomas<sup>2</sup>

**Paper II: N P A772 (2006) 1 (nucl-th/0603044)**

**No longer need to expand around  $\langle \sigma \rangle = 0$**

$m_\sigma$ (MeV)	$t_0$ (fm <sup>2</sup> )	$t_1$ (fm <sup>4</sup> )	$t_2$ (fm <sup>4</sup> )	$t_3$ (fm <sup>5/2</sup> )	$x_0$	$W_0$ (fm <sup>4</sup> )	Deviation
600	-12.72	2.64	-1.12	74.25	0.17	0.6	33%
650	-12.48	2.21	-0.77	71.73	0.13	0.56	18%
700	-12.31	1.88	-0.49	69.8	0.1	0.53	18%
750	-12.18	1.62	-0.28	68.28	0.08	0.51	38%
SkM*	-13.4	2.08	-0.68	79	0.09	0.66	0%

Table 2: Comparison of the SkM\* parameters with the QMC predictions for several values of  $m_\sigma$

**BUT density functional not exactly the same  
– QMC yields rational forms**



# Check directly vs data

- That is, apply new effective force directly to calculate nuclear properties using Hartree-Fock (as for usual well known force)

	$E_B$ (MeV, exp)	$E_B$ (MeV, QMC)	$r_c$ (fm, exp)	$r_c$ (fm, QMC)
$^{16}O$	7.976	7.618	2.73	2.702
$^{40}Ca$	8.551	8.213	3.485	3.415
$^{48}Ca$	8.666	8.343	3.484	3.468
$^{208}Pb$	7.867	7.515	5.5	5.42

- Where analytic form of (e.g.  $H_0 + H_3$ ) piece of energy functional derived from QMC is:

$$\mathcal{H}_0 + \mathcal{H}_3 = \rho^2 \left[ \frac{-3 G_\rho}{32} + \frac{G_\sigma}{8 (1 + d \rho G_\sigma)^3} - \frac{G_\sigma}{2 (1 + d \rho G_\sigma)} + \frac{3 G_\omega}{8} \right] + (\rho_n - \rho_p)^2 \left[ \frac{5 G_\rho}{32} + \frac{G_\sigma}{8 (1 + d \rho G_\sigma)^3} - \frac{G_\omega}{8} \right],$$



# Check directly vs data

- That is, apply new effective force directly to calculate nuclear properties using Hartree-Fock (as for usual well known force)

	$E_B$ (MeV, exp)	$E_B$ (MeV, QMC)	$r_c$ (fm, exp)	$r_c$ (fm, QMC)
$^{16}O$	7.976	7.618	2.73	2.702
$^{40}Ca$	8.551	8.213	3.485	3.415
$^{48}Ca$	8.666	8.343	3.484	3.468
$^{208}Pb$	7.867	7.515	5.5	5.42

- Where analytic form of (e.g.  $H_0 + H_3$ ) piece of energy functional derived from QMC is:

$$\mathcal{H}_0 + \mathcal{H}_3 = \rho^2 \left[ \frac{-3 G_\rho}{32} + \frac{G_\sigma}{8 (1 + d\rho G_\sigma)^3} - \frac{G_\sigma}{2 (1 + d\rho G_\sigma)} + \frac{3 G_\omega}{8} \right] + (\rho_n - \rho_p)^2 \left[ \frac{5 G_\rho}{32} + \frac{G_\sigma}{8 (1 + d\rho G_\sigma)^3} - \frac{G_\omega}{8} \right],$$

○ highlights scalar polarizability



# Check directly vs data

- That is, apply new effective force directly to calculate nuclear properties using Hartree-Fock (as for usual well known force) – for example:

	$E_B$ (MeV, exp)	$E_B$ (MeV, QMC)	$r_c$ (fm, exp)	$r_c$ (fm, QMC)
$^{16}O$	7.976	7.618	2.73	2.702
$^{40}Ca$	8.551	8.213	3.485	3.415
$^{48}Ca$	8.666	8.343	3.484	3.468
$^{208}Pb$	7.867	7.515	5.5	5.42

- In comparison with the SkM force:

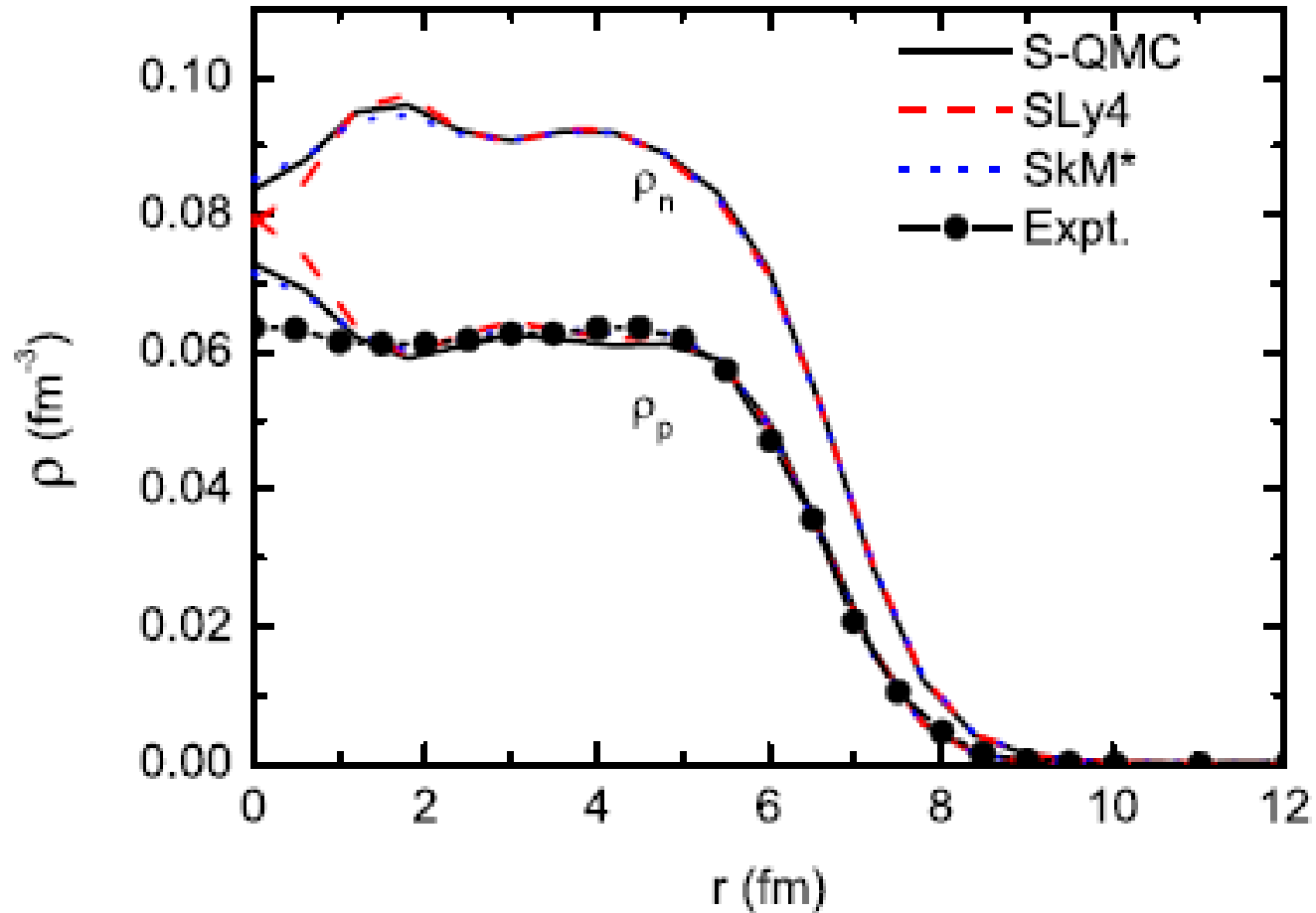
$$\mathcal{H}_0 + \mathcal{H}_3 = \frac{\rho^{\frac{1}{6}} t_3 (2\rho^2 - \rho_n^2 - \rho_p^2)}{24} + \frac{t_0 (\rho^2 (2 + x_0) - (1 + 2x_0) (\rho_n^2 + \rho_p^2))}{4}$$

and full energy functional in both cases is:

$$\langle H(\vec{r}) \rangle = \rho M + \frac{\tau}{2M} + \mathcal{H}_0 + \mathcal{H}_3 + \mathcal{H}_{eff} + \mathcal{H}_{fin} + \mathcal{H}_{so}$$



# Nuclear Densities from QMC-Skyrme



Calculation of Furong Xu (2010)

# Spin-Orbit Splitting

	Neutrons (Expt)	Neutrons (QMC)	Protons (Expt)	Protons (QMC)
$^{16}\text{O}$ $1p_{1/2}-1p_{3/2}$	6.10	6.01	6.3	5.9
$^{40}\text{Ca}$ $1d_{3/2}-1d_{5/2}$	6.15	6.41	6.0	6.2
$^{48}\text{Ca}$ $1d_{3/2}-1d_{5/2}$	6.05 (Sly4)	5.64	6.06 (Sly4)	5.59
$^{208}\text{Pb}$ $2d_{3/2}-2d_{5/2}$	2.15 (Sly4)	2.04	1.87 (Sly4)	1.74

**Agreement generally very satisfactory – NO parameter adjusted to fit**

# Finally: Apply to Shell Structure as $N - Z +$

- Use Hartree – Fock – Bogoliubov calculation
- Calculated variation of two-neutron removal energy at  $N = 28$  as  $Z$  varies from  $Z = 32$  (proton drip-line region) to  $Z = 18$  (neutron drip-line region)
- $S_{2n}$  changes by 8 MeV at  $Z=32$   
 $S_{2n}$  changes by 2–3 MeV at  $Z = 18$
- This strong shell quenching is very similar to Skyrme – HFB calculations of Chabanat et al.,  
**Nucl. Phys. A635 (1998) 231**
- 2n drip lines appear at about  $N = 60$  for Ni and  $N = 82$  for Zr  
(/// to predictions for Sly4 – c.f. Chabanat et al.)



# Great Start: What's Next

Removed small  $\sigma$  field approximation

- Derived density-dependent forms
- Added the pion
- Derived  $\Lambda N$ ,  $\Sigma N$ ,  $\Lambda \Lambda \dots$  effective forces in-medium with no additional free parameters
- Hence attack dense hadronic matter, n-stars, transition from NM to QM or SQM with more confidence

# Hyperons

- $\Lambda$ ,  $\Sigma$  and  $\Xi$  have: one s-quark (S=0 or S=1 light quarks) or two s-quarks – all in s-state (same octet as N)
- Masses in free space 1115 MeV (c.f. 940 MeV for p) 1190 MeV and 1315 MeV
- Attractive and repulsive forces ( $\sigma$  and  $\omega$  mean fields) both decrease as # light quarks decreases
- NO  $\Sigma$  hypernuclei are bound!
- $\Lambda$  bound by about 30 MeV in nuclear matter ( $\sim$ Pb)
- Nothing known about  $\Xi$  hypernuclei – JPARC?

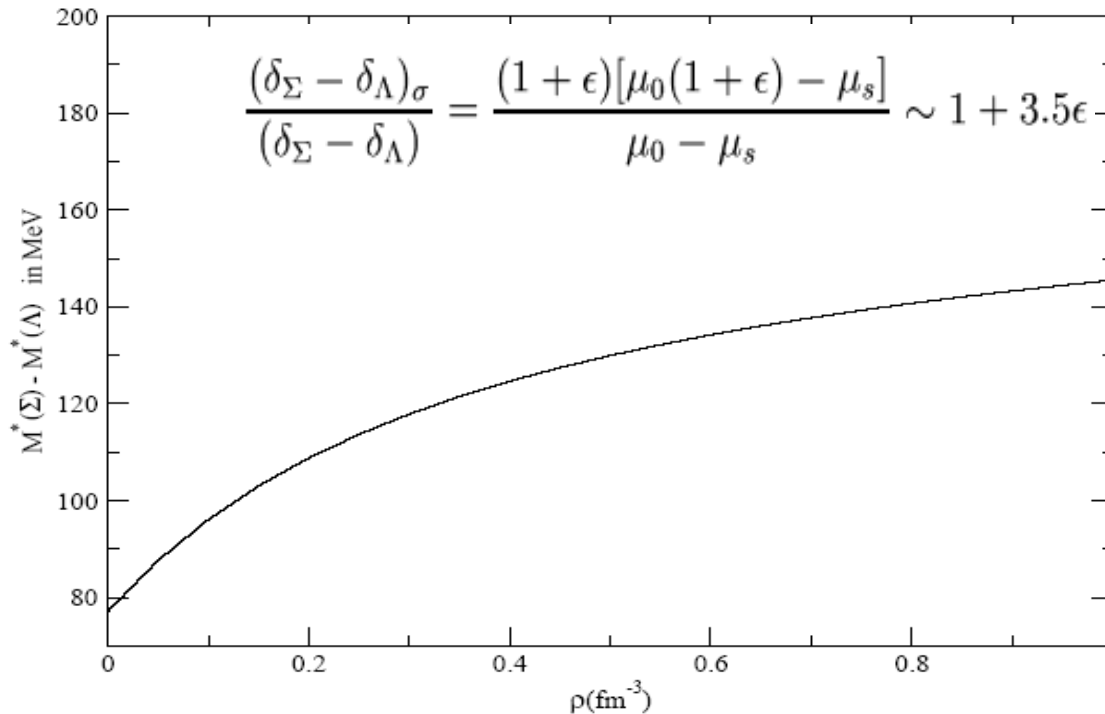




# Medium Modification of Hyperfine Interaction

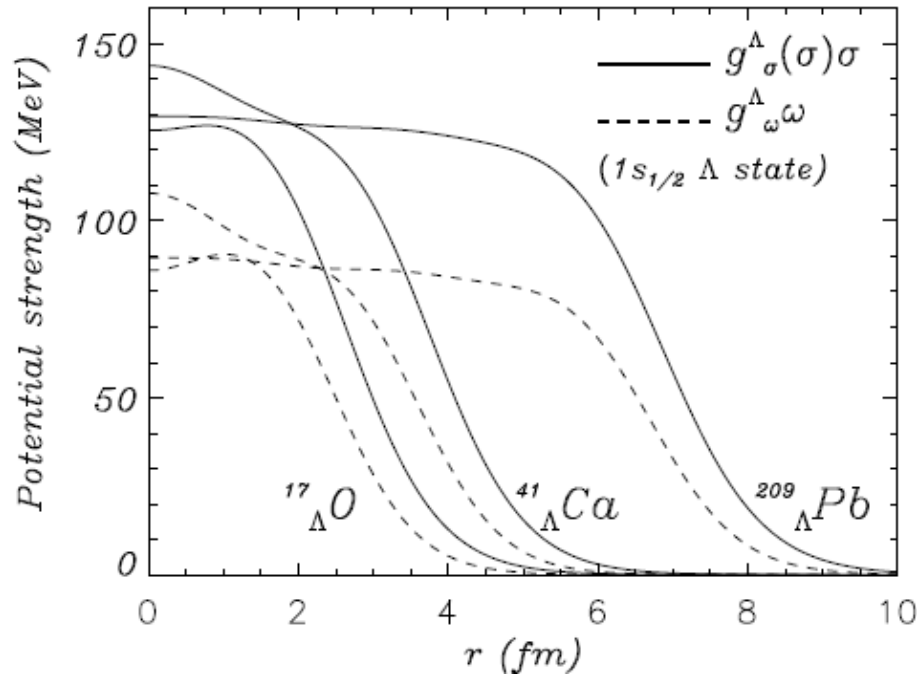
**N -  $\Delta$  and  $\Sigma$  -  $\Lambda$  splitting arise from one-gluon-exchange in MIT Bag Model : as  $\sigma \uparrow$  so does this splitting...**

Difference of Sigma and Lambda effective mass



**Guichon, Thomas, Tsushima: nucl-th/0712.1925**

# Finite Hypernuclei in new QMC Model



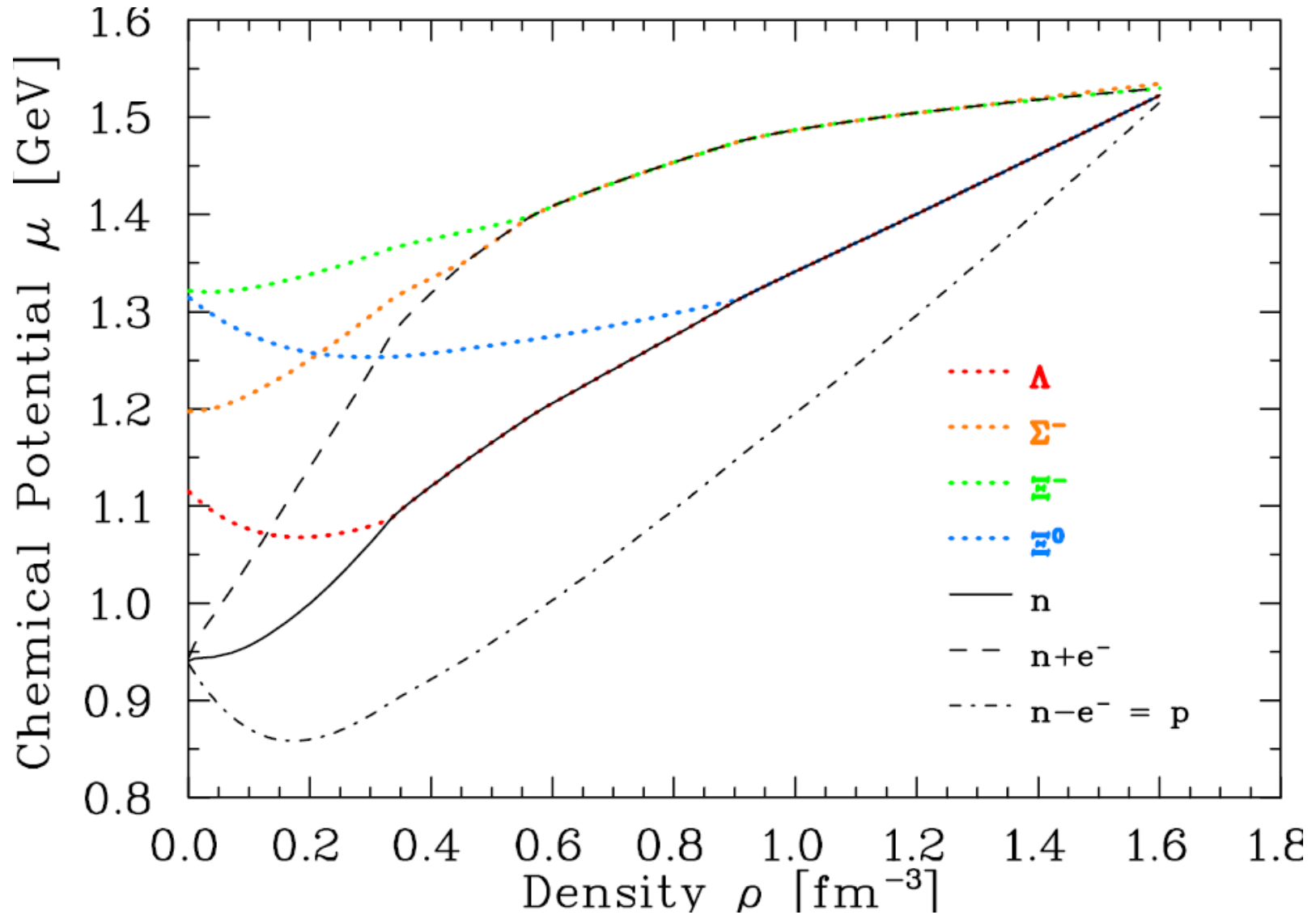
$\Lambda$  energy levels good;  
spin-orbit force naturally  
suppressed;

$\Sigma$ -hypernuclei also unbound – e.g. for  $\Sigma^0$  in  $^{40}Ca$ :  
central potential +30 MeV and few MeV attraction  
in surface (-10MeV at 4fm)

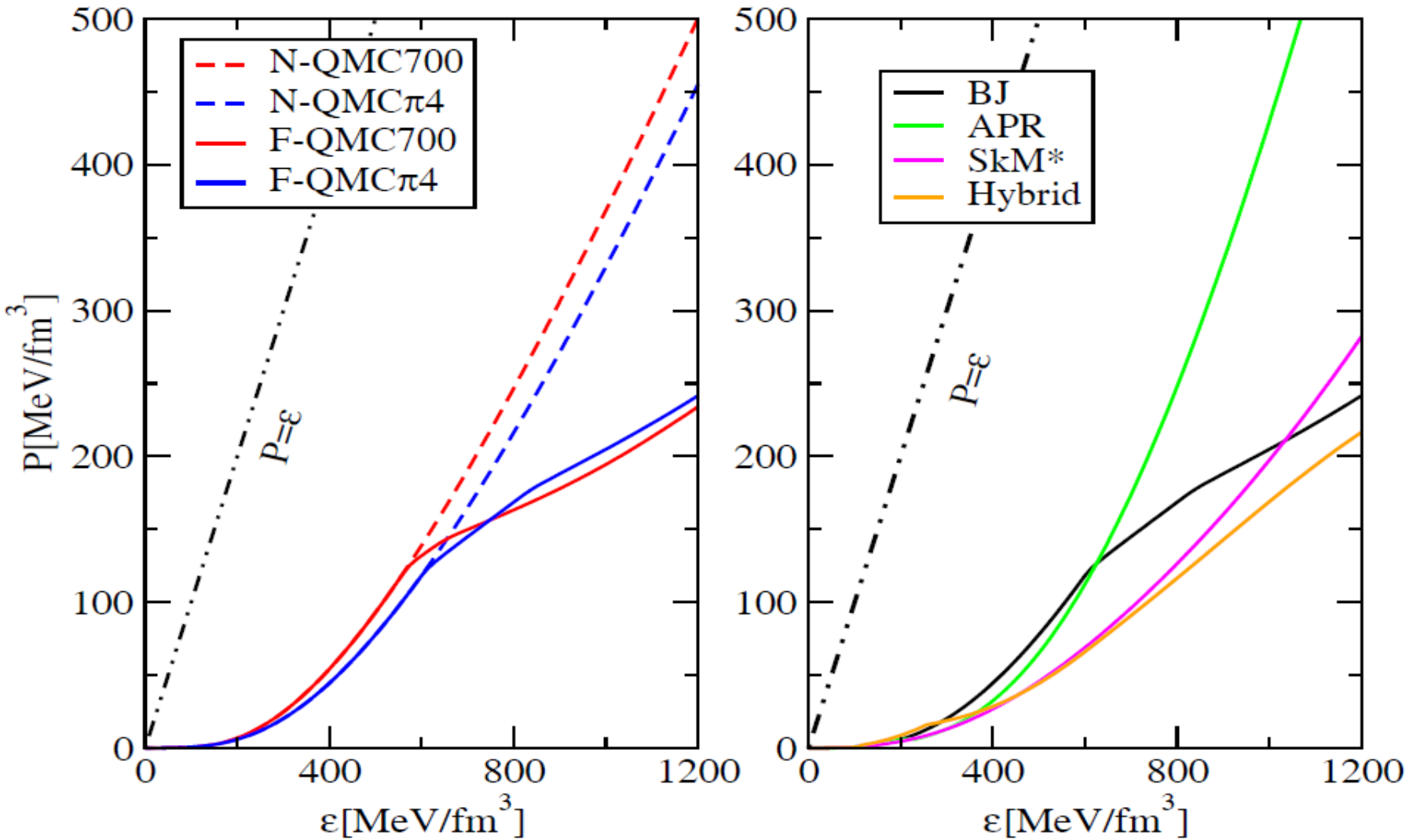
	$^{89}_{\Lambda}Yb$ (Expt.)	$^{91}_{\Lambda}Zr$	$^{91}_{\Xi^0}Zr$	$^{208}_{\Lambda}Pb$ (Expt.)	$^{209}_{\Lambda}Pb$	$^{209}_{\Xi^0}Pb$
$1s_{1/2}$	-22.5	-24.0	-9.9	-27.0	-26.9	15.0
$1p_{3/2}$		-19.4	-7.0		-24.0	-12.6
$1p_{1/2}$	-16.0 (1p)	-19.4	-7.2	-22.0 (1p)	-24.0	-12.7
$1d_{5/2}$		-13.4	-3.1	—	-20.1	-9.6
$2s_{1/2}$		-9.1	—	—	-17.1	-8.2
$1d_{3/2}$	-9.0 (1d)	-13.4	-3.4	-17.0 (1d)	-20.1	-9.8
$1f_{7/2}$		-6.5	—	—	-15.4	-6.2
$2p_{3/2}$		-1.7	—	—	-11.4	-4.2
$1f_{5/2}$	-2.0 (1f)	-6.4	—	-12.0 (1f)	-15.4	-6.5
$2p_{1/2}$		-1.6	—	—	-11.4	-4.3



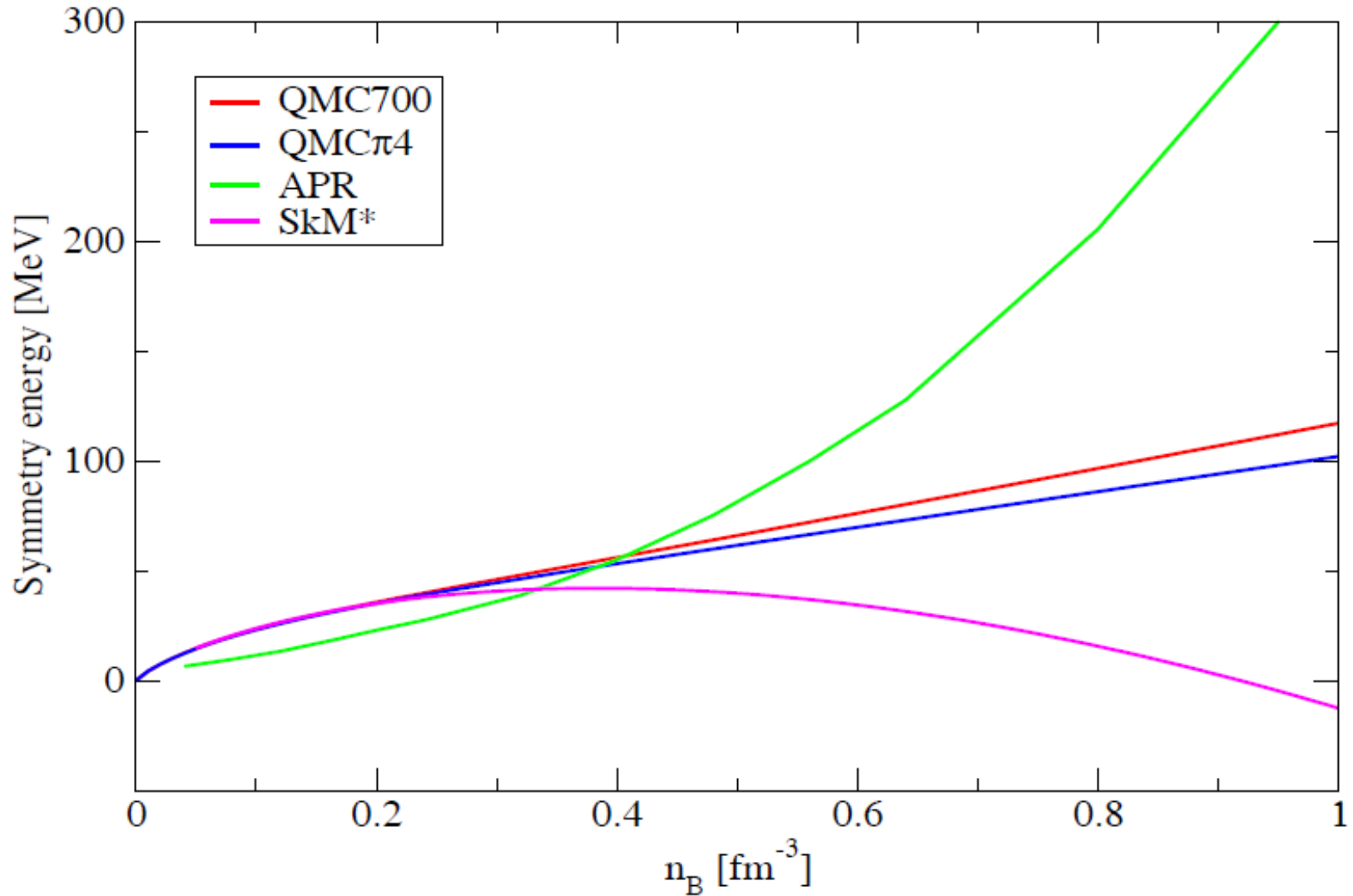
# Nuclear Matter in $\beta$ -Equilibrium



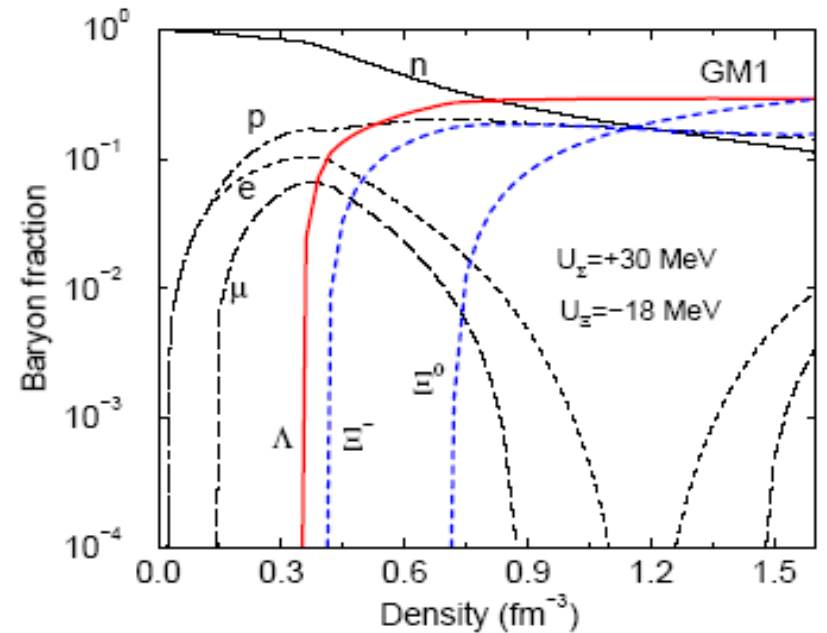
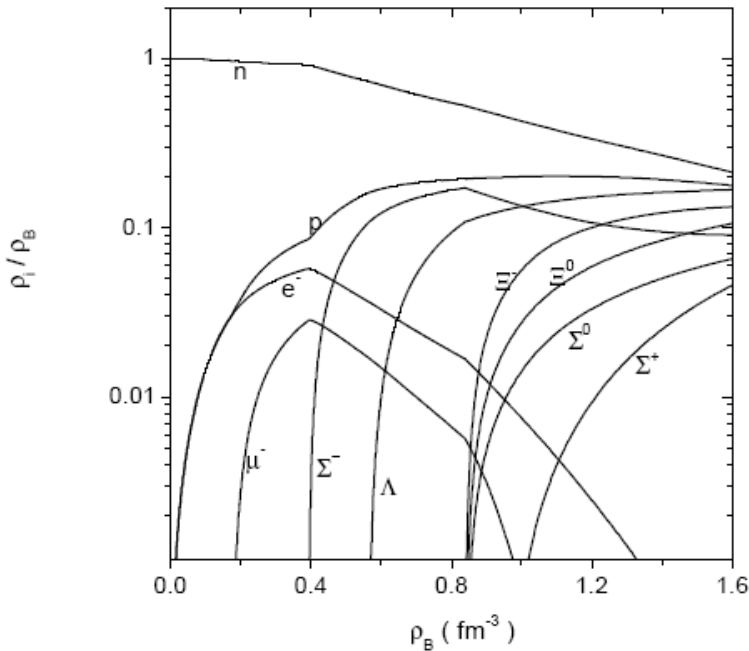
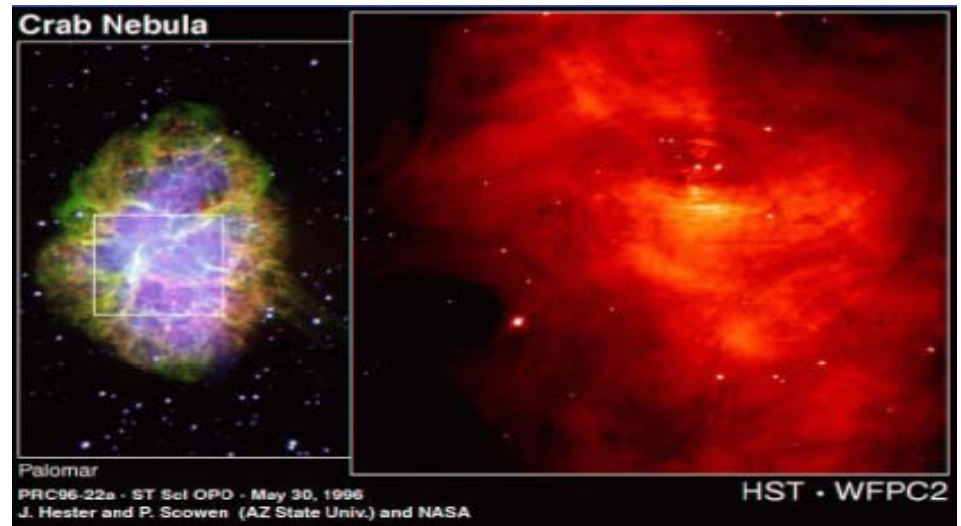
# Equations of State



# Symmetry Energy in $\beta$ -Equilibrium (n,p,e, $\mu$ only)

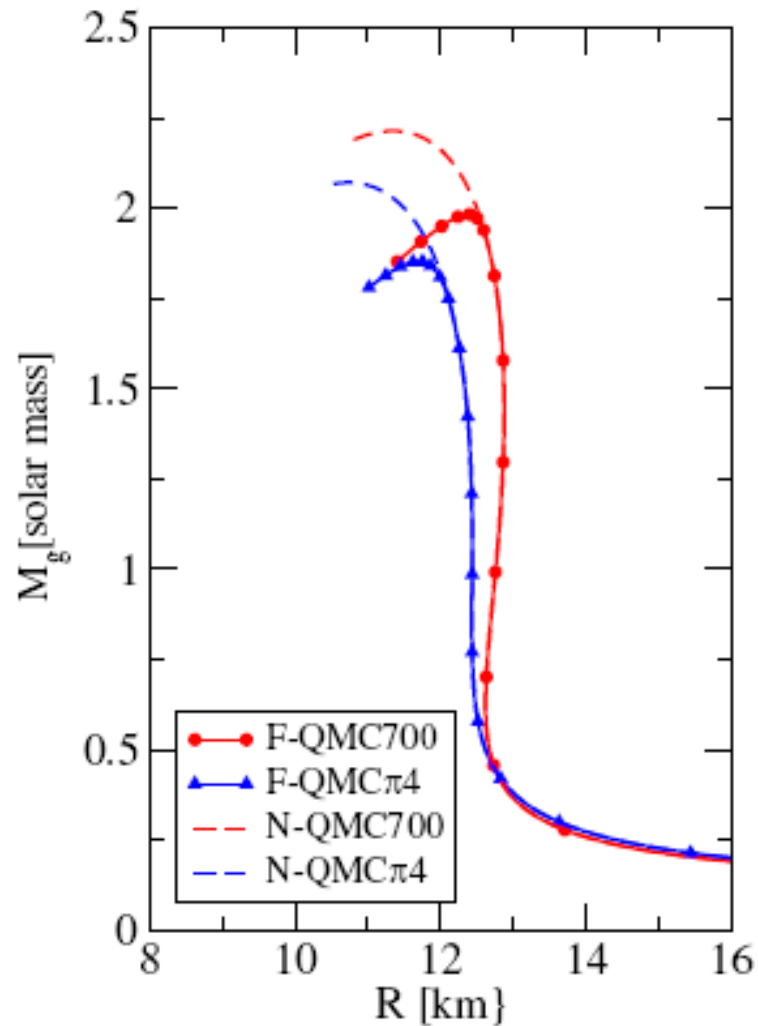


- Hyperons enter at just  $2-3 \rho_0$
- Hence need effective  $\Sigma$ -N and  $\Lambda$ -N forces in this density region!
- Hypernuclear data is important input (J-PARC, FAIR, JLab)

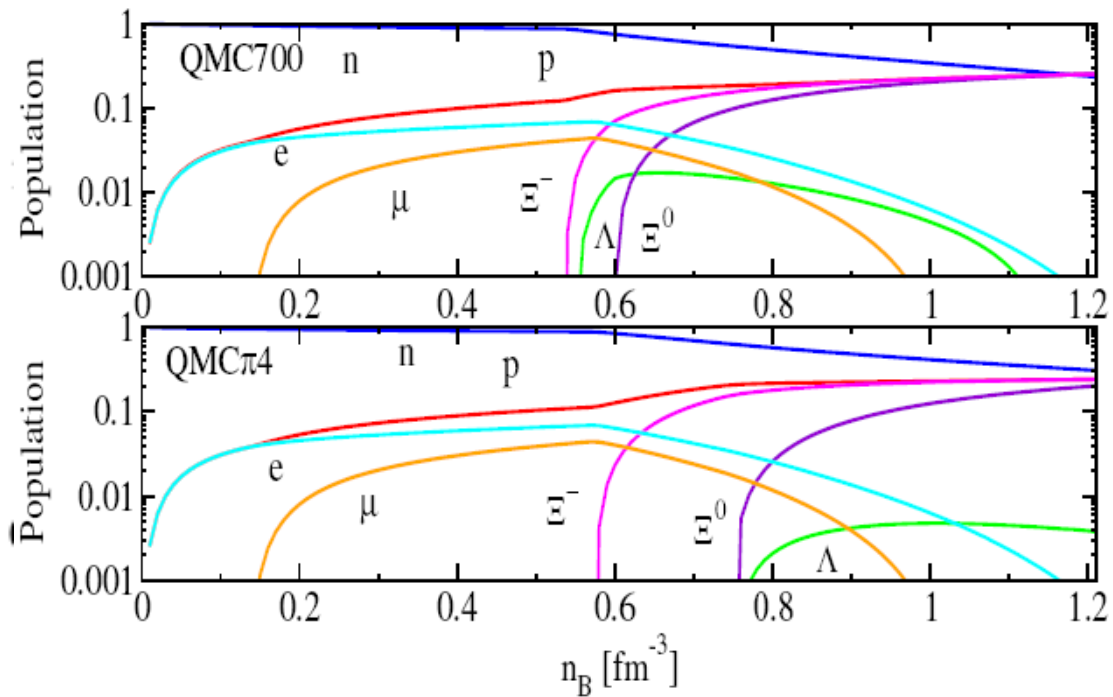


From Schaffner-Bielich (2005)

# Consequences for Neutron Star



Rikovska-Stone et al., NP A792 (2007) 341



# N-star Masses and Radii

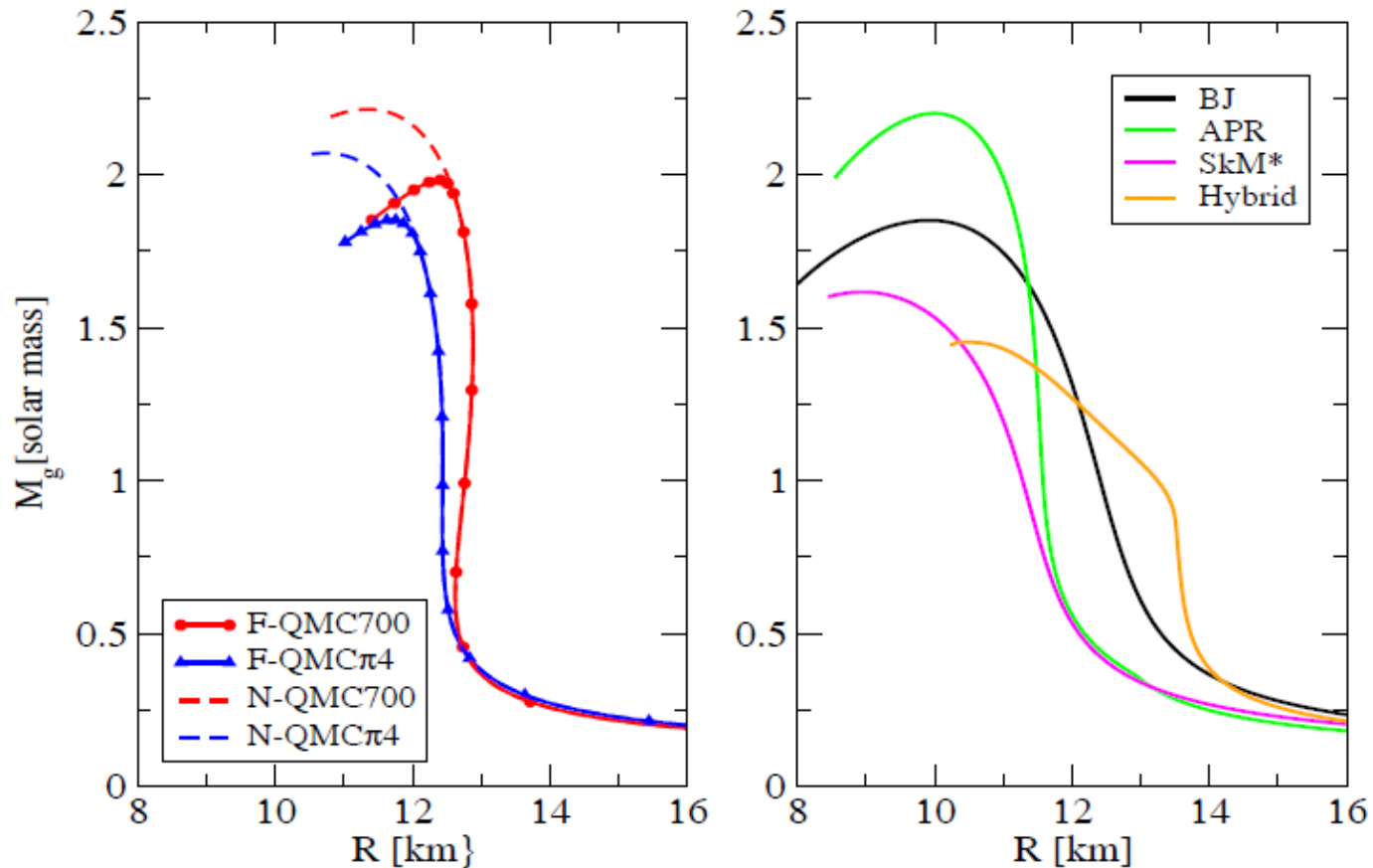


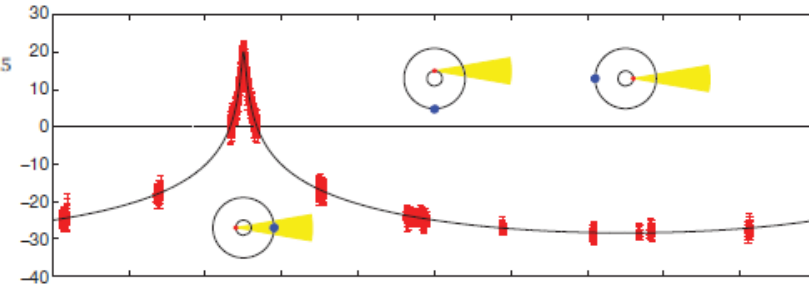
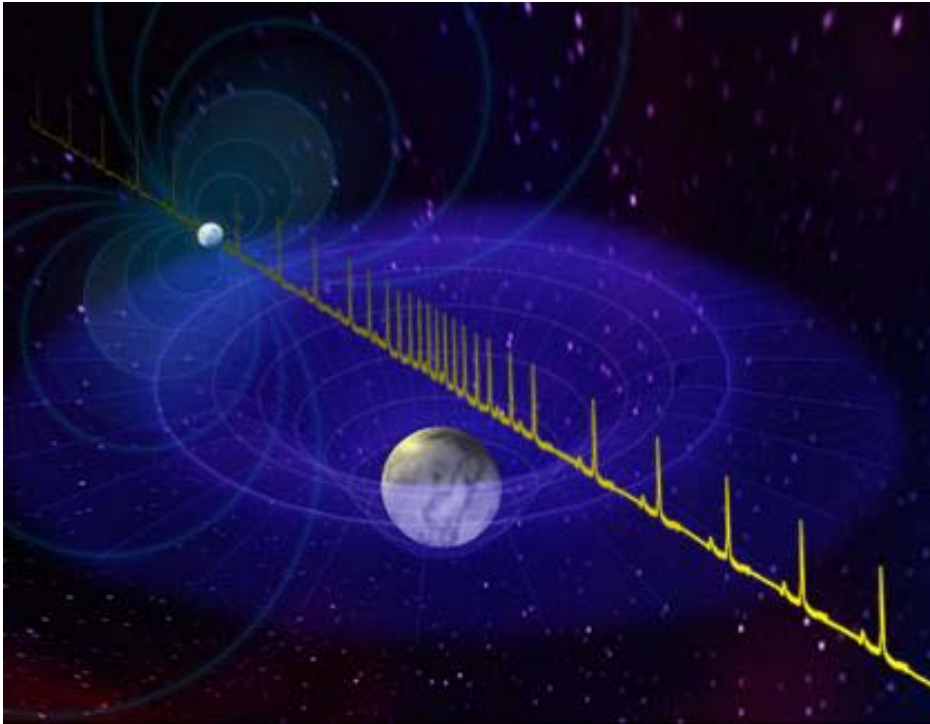
Fig. 5. The gravitational masses of non-rotating neutron-star models (measured in solar masses) plotted against radius (in kilometers), calculated for selected QMC EoS.





# A two-solar-mass neutron star measured using Shapiro delay

P. B. Demorest<sup>1</sup>, T. Pennucci<sup>2</sup>, S. M. Ransom<sup>1</sup>, M. S. E. Roberts<sup>3</sup> & J. W. T. Hessels<sup>4,5</sup>

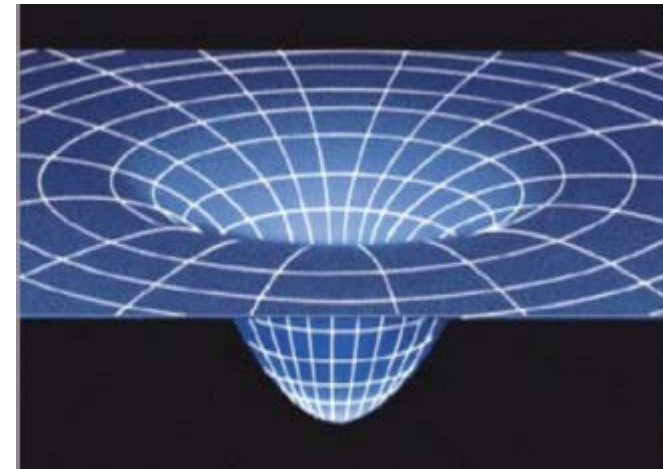
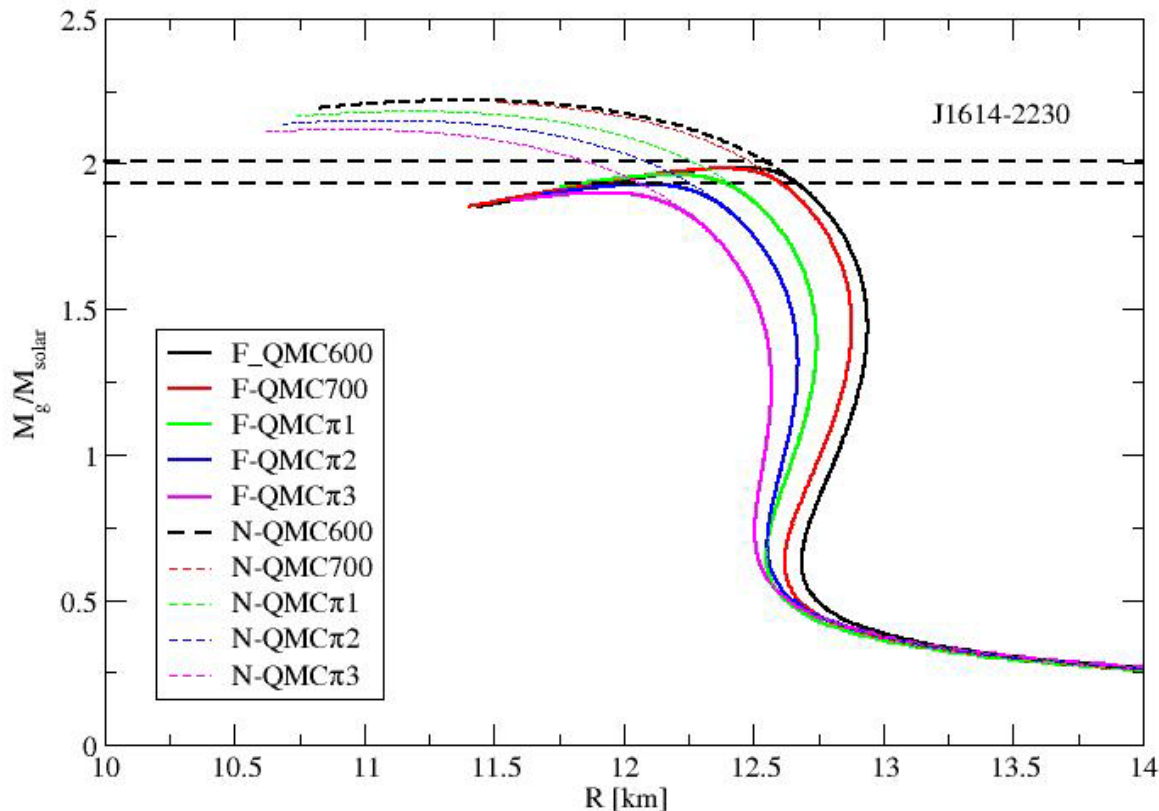


**Report a very accurate pulsar mass much larger than seen before :  $1.97 \pm 0.04$  solar mass**

**Claim it rules out hyperons (particles with strange quarks)**



# Just 3 years ago\* ....



We conclude that the Demorest et al. result, if confirmed, is very significant for neutron star physics and does indeed rule out all EoS which predict a mass-radius curve that does not intersect the J1614-2230 mass line. However, it does not provide any constraint on the possible 'exotic' composition of the high-density neutron star matter.

- Guichon et al., Nucl. Phys. A814 (2008) 66
  - result of an on-going collaboration between CSSM & CEA France with Jirina Stone (Oxford)

# Recently Developed Covariant Model Built on the Same Physical Ideas

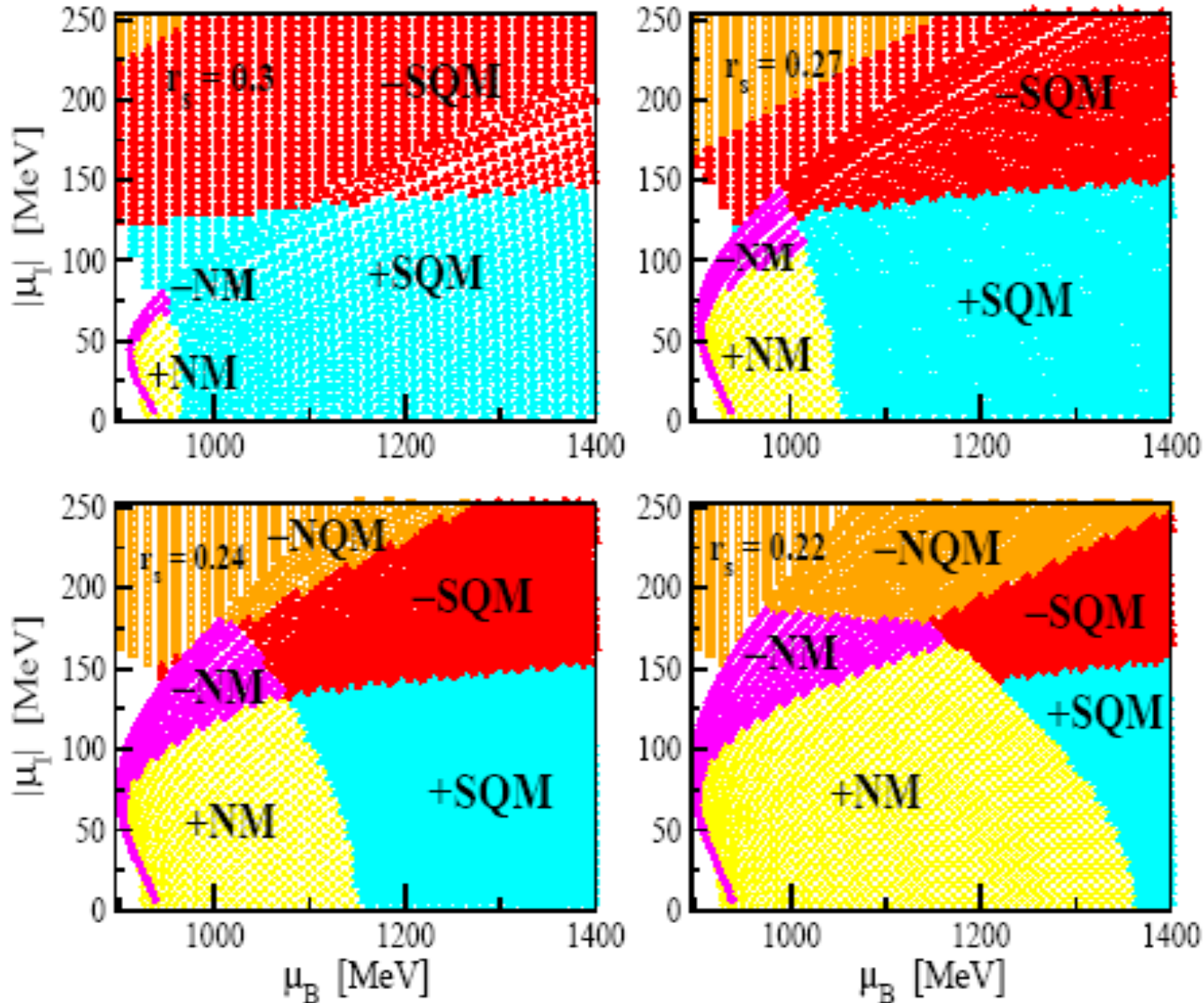
- Use NJL model ( $\chi$ 'al symmetry)
- Ensure **confinement** through proper time regularization (following the Tübingen group)
- Self-consistently solve Faddeev Eqn. in mean scalar field
- This **solves chiral collapse problem** common for NJL (because of scalar polarizability again)
- Can **test against experiment**
  - e.g. spin-dependent EMC effect
- Also apply **same model** to **NM, NQM and SQM** – hence **n-star**

# Have also Built a Covariant Version of QMC

- **Basic Model: (Covariant, chiral, confining version of NJL)**
- **Bentz & Thomas, Nucl. Phys. A696 (2001) 138**
- **Bentz, Horikawa, Ishii, Thomas, Nucl. Phys. A720 (2003) 95**
- **Applications to DIS:**
- **Cloet, Bentz, Thomas, Phys. Rev. Lett. 95 (2005) 052302**
- **Cloet, Bentz, Thomas, Phys. Lett. B642 (2006) 210**
- **Applications to neutron stars – including SQM:**
- **Lawley, Bentz, Thomas, Phys. Lett. B632 (2006) 495**
- **Lawley, Bentz, Thomas, J. Phys. G32 (2006) 667**

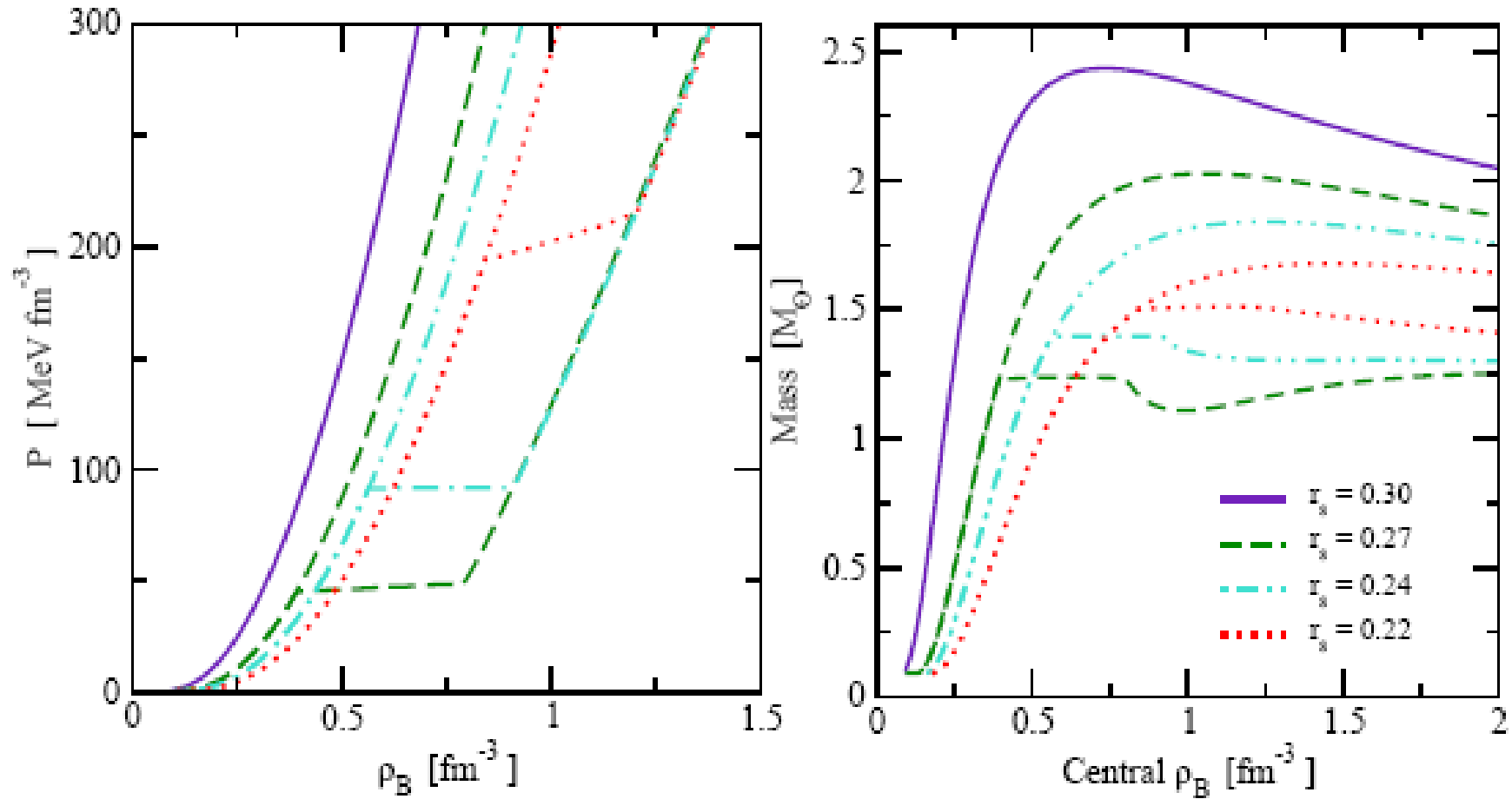


# Phases of Dense Matter : NM to NQM to SQM



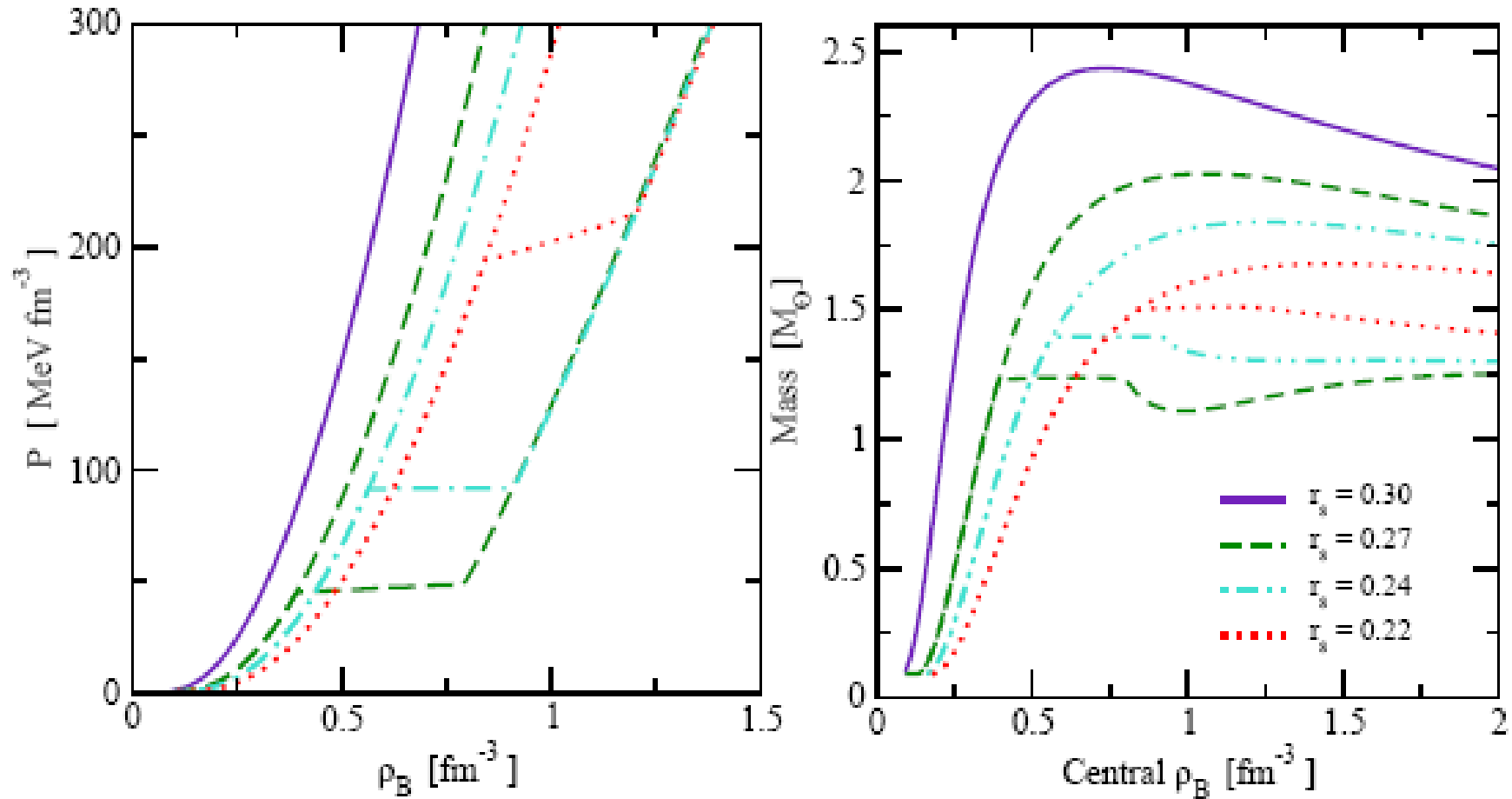
Lawley, Bentz, AWT, nucl-th/0602014 (J Phys G)

# EOS of Dense Matter – n Star Properties



Naturally leads to low mass, hybrid n stars with masses ~ independent of the central density

# EOS of Dense Matter – n Star Properties



**N.B. Hyperons in NM phase would tend to raise transition density a little - still need to include these....**

# Binding of Other Hadrons



# Mesons are Special

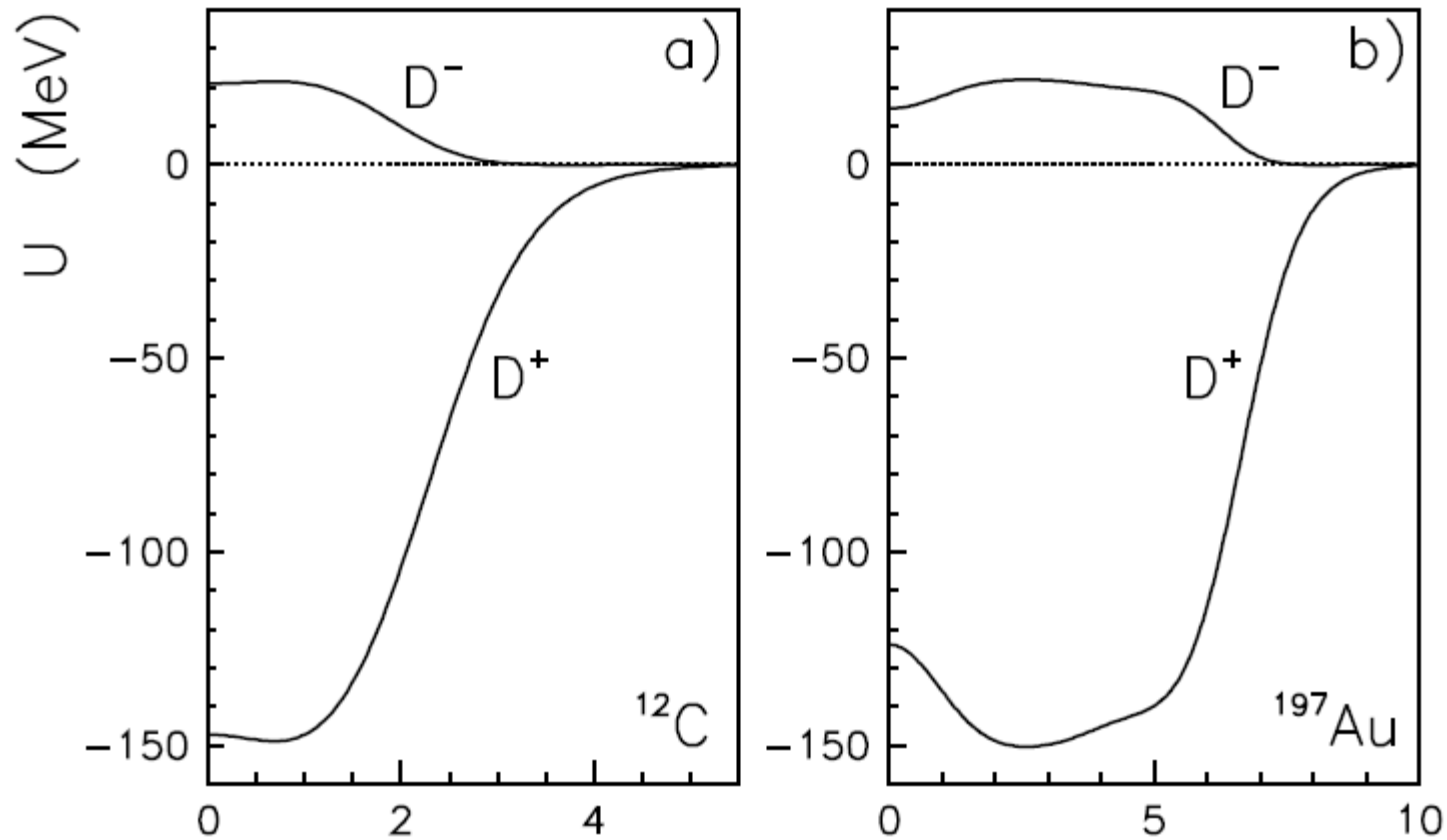
- With valence  $q$  and anti- $q$  net Lorentz vector force is zero!
- Thus, unlike baryons, we see strong scalar attraction
- Pseudo-scalars are complicated by chiral symmetry (need for many-body effects)
- $\rho$  is very broad
- $\omega$  is ideal – expect it to be bound  
– hints from Mainz
- Also naked charm:  $c \bar{q}$  ( $\bar{q}$  feels attractive scalar AND vector force)

Table 20: Calculated meson-nucleus bound state energies,  $E_j = \text{Re}(E_j^* - m_j)$ , and width  $\Gamma_j$  ( $j = \omega, \eta, \eta'$ ), (in MeV) in QMC [163] and those for the  $\omega$  in QHD, including the effect of  $\sigma$ - $\omega$  mixing [180]. The complex eigenenergies are given by,  $E_j^* = E_j + m_j - i\Gamma_j/2$ . (\* n calculated)

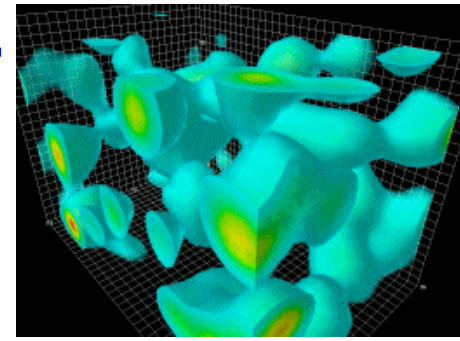
		$\Gamma_\eta^0 = 0$ $\gamma_\eta = 0.5$ (QMC)		$\Gamma_{\eta'}^0 = 0$ (QMC)		$\Gamma_\omega^0 = 8.43$ (MeV) $\gamma_\omega = 0.2$ (QMC)	
		$E_\eta$	$\Gamma_\eta$	$E_{\eta'}$	$E_\omega$	$\Gamma_\omega$	
${}^6_j\text{He}$	1s	-10.7	14.5	*	-55.6	24.7	
${}^{11}_j\text{B}$	1s	-24.5	22.8	*	-80.8	28.8	
${}^{26}_j\text{Mg}$	1s	-38.8	28.5	*	-99.7	31.1	
	1p	-17.8	23.1	*	-78.5	29.4	
	2s	—	—	*	-42.8	24.8	
${}^{16}_j\text{O}$	1s	-32.6	26.7	-41.3	-93.4	30.6	
	1p	-7.72	18.3	-22.8	-64.7	27.8	
${}^{40}_j\text{Ca}$	1s	-46.0	31.7	-51.8	-111	33.1	
	1p	-26.8	26.8	-38.5	-90.8	31.0	
	2s	-4.61	17.7	-21.9	-65.5	28.9	
${}^{90}_j\text{Zr}$	1s	-52.9	33.2	-56.0	-117	33.4	
	1p	-40.0	30.5	-47.7	-105	32.3	
	2s	-21.7	26.1	-35.4	-86.4	30.7	
${}^{208}_j\text{Pb}$	1s	-56.3	33.2	-57.5	-118	33.1	
	1p	-48.3	31.8	-52.6	-111	32.5	
	2s	-35.9	29.6	-44.9	-100	31.7	



# Effective Potentials for $D^\pm$ in nuclei



# BUT Calculating Energies is a **SMALL** Part of the Problem!

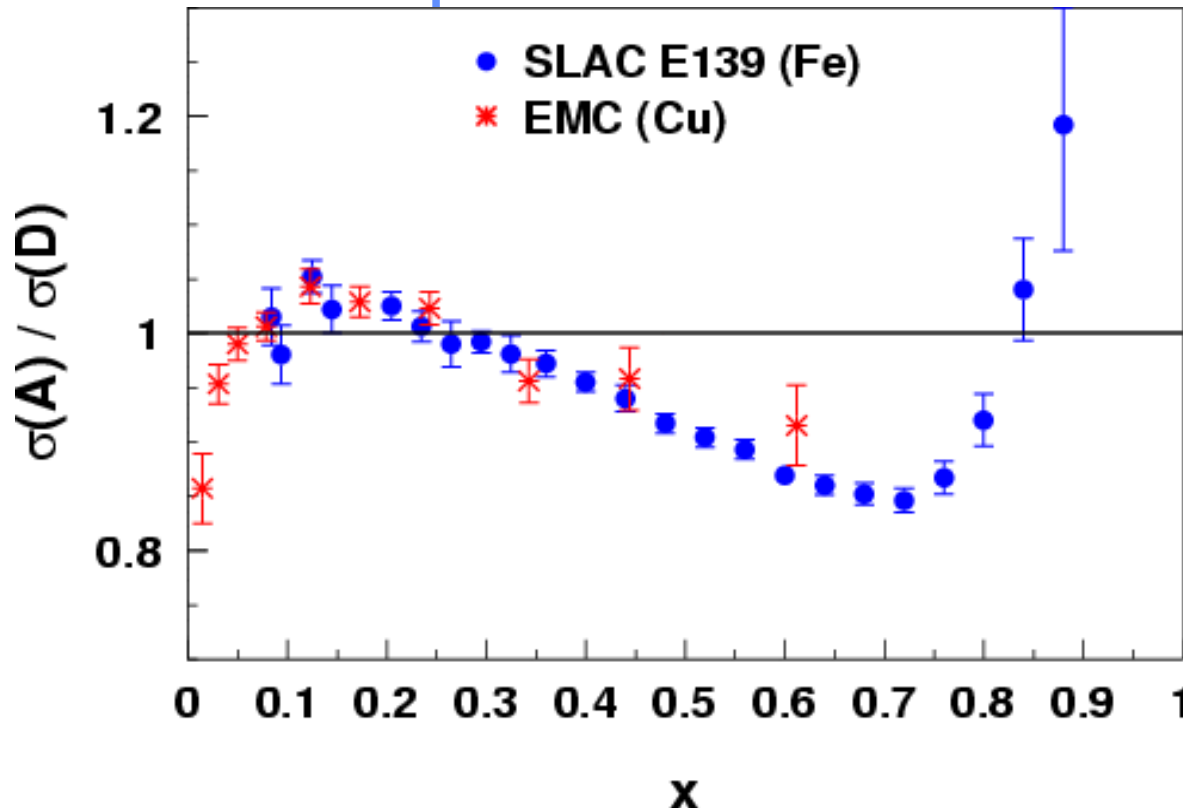


- The self-consistent coupling to the scalar field *fundamentally modifies the structure of the hadron*
- Hence form factors and structure functions change in-medium
- At quark level it's the lower components of the valence quark Dirac wave functions that are most effected
- N.B. calculation relies on Born-Oppenheimer approximation: motion must be slow enough for structure to adjust to the local mean scalar field!



# The EMC Effect: Nuclear PDFs

- Observation **stunned and electrified** the HEP and Nuclear communities 20 years ago
- Nearly 1,000 papers have been generated.....
- What is it that alters the quark momentum in the nucleus?



J. Ashman *et al.*, *Z. Phys. C57*, 211 (1993)

J. Gomez *et al.*, *Phys. Rev. D49*, 4348 (1994)

# Recent Calculations for Finite Nuclei

Spin dependent EMC effect TWICE as large as unpolarized

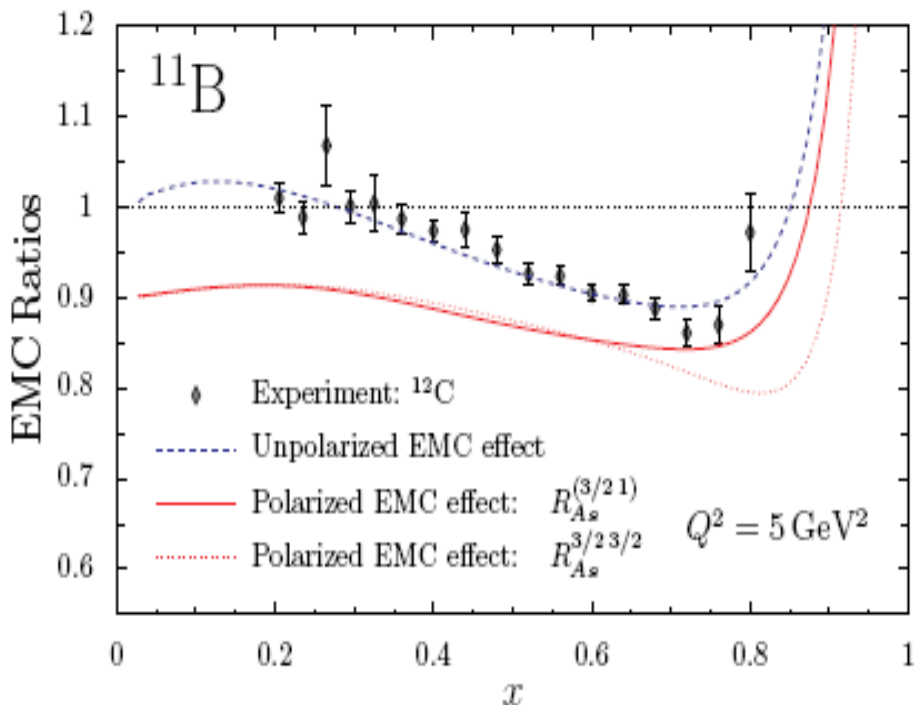


FIG. 7: The EMC and polarized EMC effect in  $^{11}\text{B}$ . The empirical data is from Ref. [31].

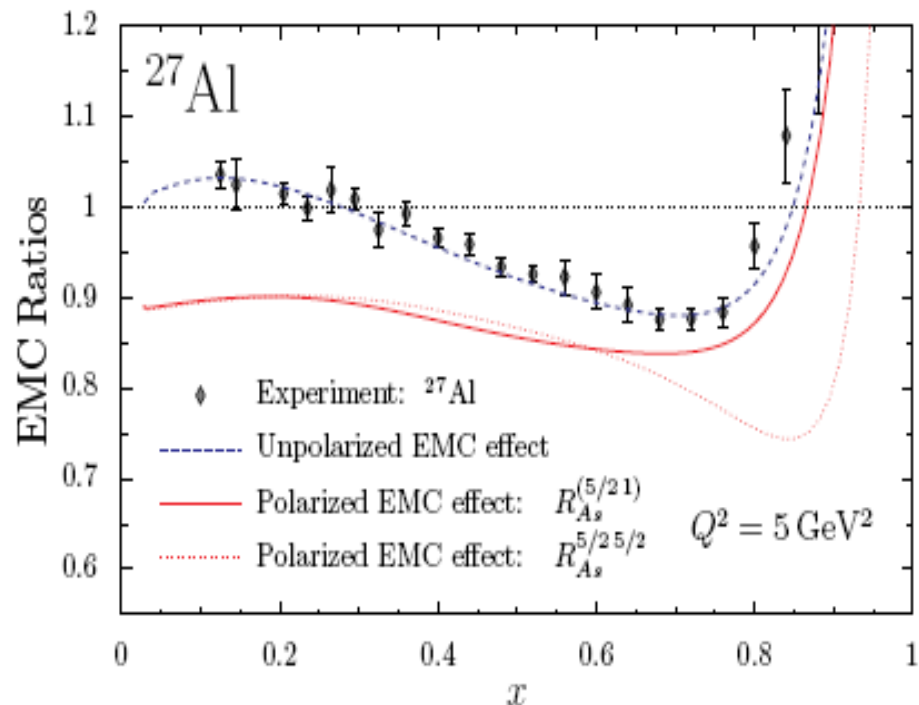


FIG. 9: The EMC and polarized EMC effect in  $^{27}\text{Al}$ . The empirical data is from Ref. [31].

Cloet, Bentz, Thomas, Phys. Lett. B642 (2006) 210 (nucl-th/0605061)

# Summary-1

- For dense matter relativity matters
- Intermediate attraction in NN force is **STRONG** scalar
- This modifies the intrinsic structure of the bound nucleon : profound change in shell model  
what occupies shell model states are **NOT** free nucleons
- Change of intrinsic structure “scalar polarizability”
- This is a natural source of three-body force  
clear physical interpretation
- Resulting, equivalent effective force is remarkably close to successful Skyrme forces



# Summary -2

- Derived, density-dependent effective force gives results better than 95% of the phenomenological Skyrme forces
  - BUT its derived with MANY less parameters
- Encourage community to use it...
- Same model also yields effective, density dependent  $\Lambda$  N,  $\Sigma$  N,  $\Xi$  N forces (not yet published)
- Availability of realistic, density dependent Hyperon-N forces is essential for  $\rho > 2-3 \rho_0$
- Already important results for n stars





# Special Mentions.....



