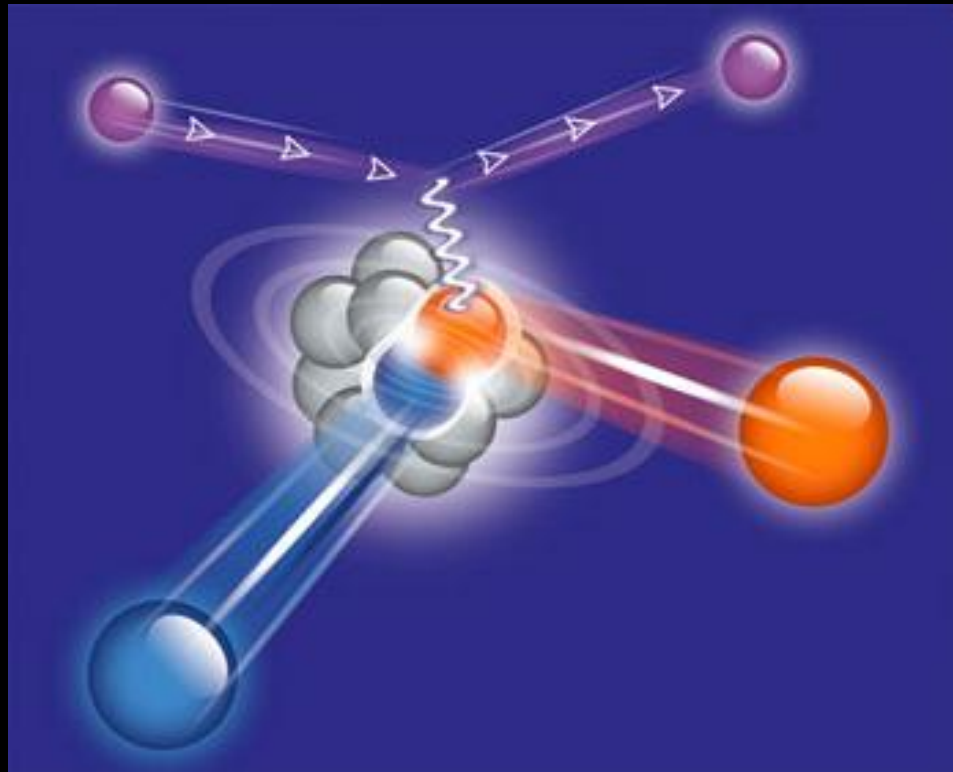


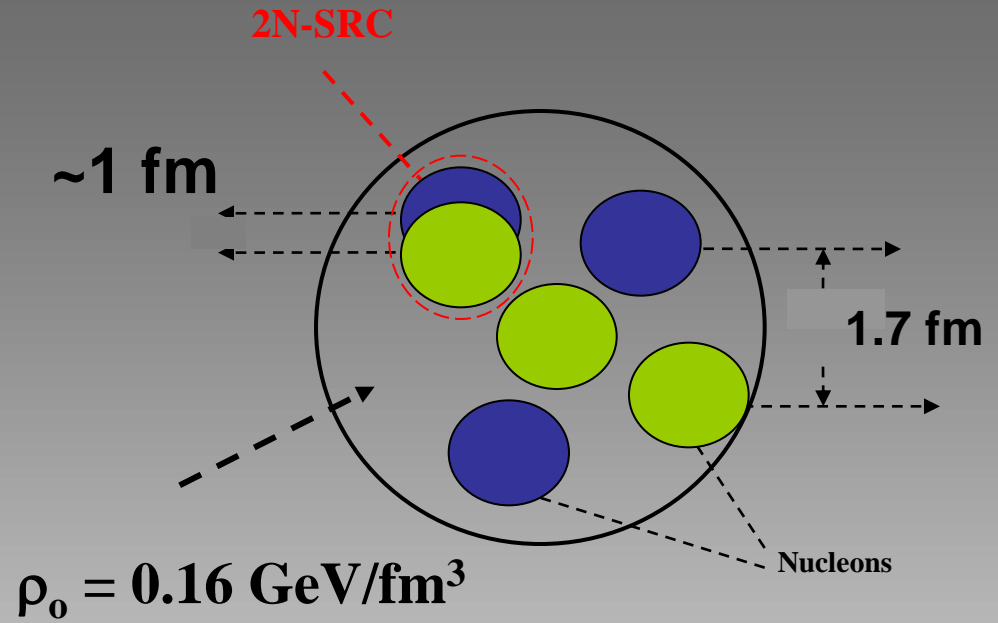
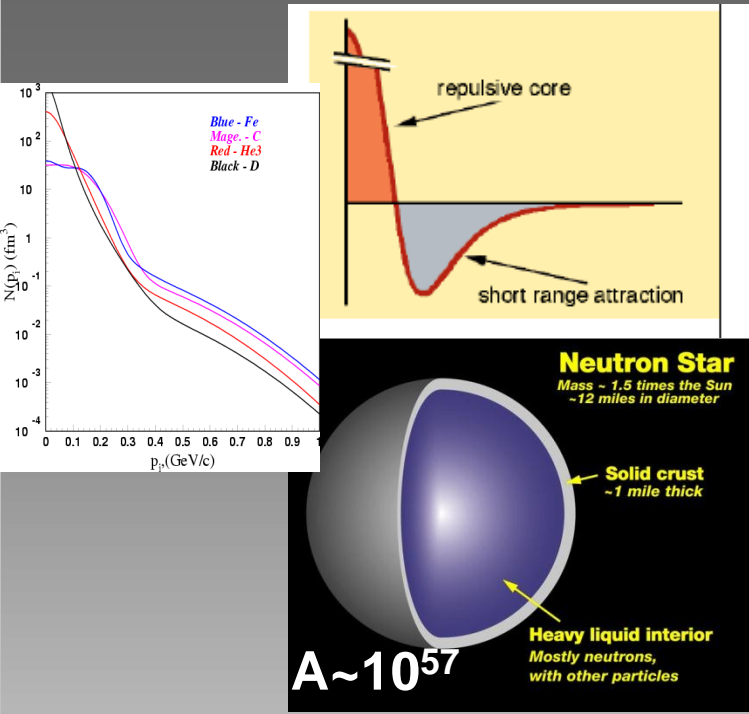


# High-Momentum Components of the Nuclear Wave Function:

Short range correlation, the tensor N-N interaction, and the EMC effect



# Short /intermediate Range Correlations in nuclei



What SRC in nuclei can tell us about:



**High – Momentum Component of the Nuclear Wave Function.**

**SRC  $\sim R_A^{-1}$  LRC  $\sim R_A^{-2}$**   
**The Strong Short-Range Force Between Nucleons.**

tensor force, repulsive core, 3N forces



**Cold-Dense Nuclear Matter (from deuteron to neutron-stars).**



**Nucleon structure modification in the medium ?**

EMC and SRC

# Short range correlations



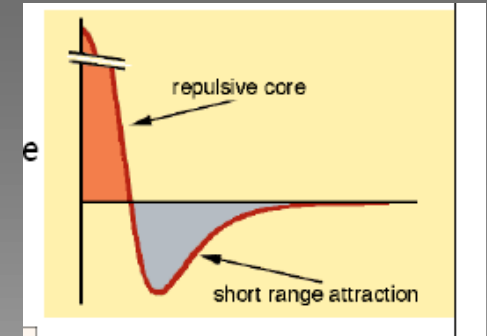
“The **structure of correlated many-body systems**, particularly at distance scales small compared to the radius of the constituent nucleons, **presents a formidable challenge to both experiment and theory**”

(Nuclear Science: A Long Range Plan, The DOE/NSF Nuclear Science Advisory Committee, Feb. 1996 [1].)

A description of nuclei at distance scales small compared to the radius of the constituent nucleons is needed to take into account,

## Short range repulsion

(common to many other systems)



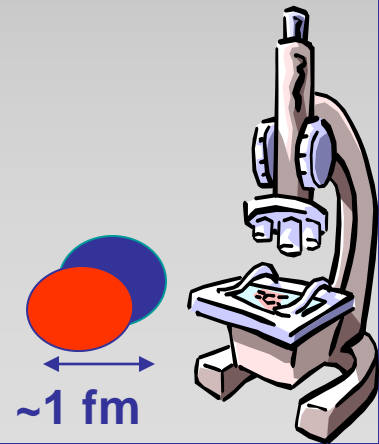
## Intermediate- to long-range tensor attraction

(unique to nuclei)

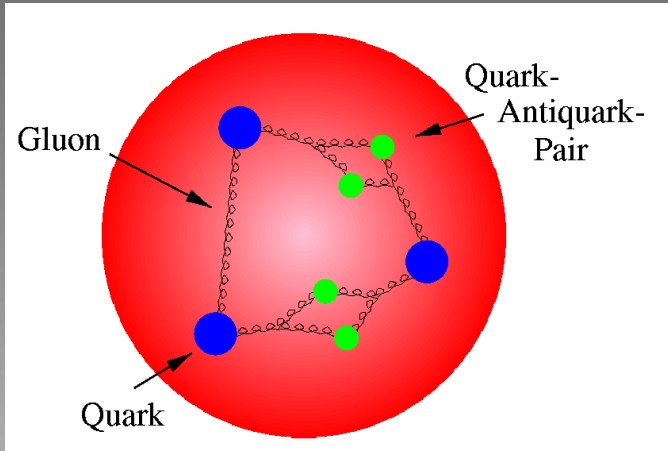
**Very difficult many-body problem**

**presents a challenge to both experiment and theory**

This long standing challenge for nuclear physics can experimentally be effectively addressed thanks to high momentum transfer reached by present facilities.



Hard processes are of particular interest because they have the resolving power required to probe the partonic structure of a complex target



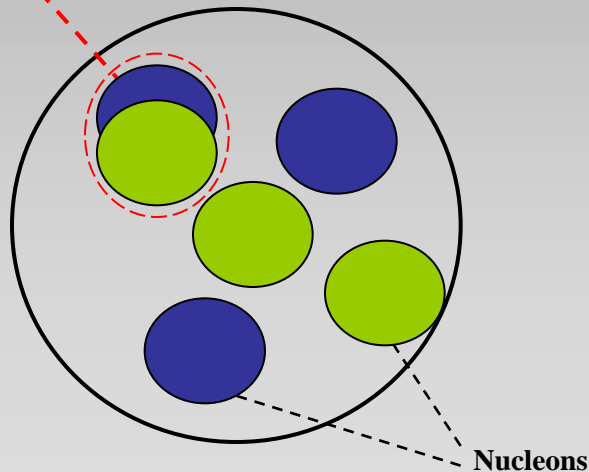
## DIS

partonic structure of hadrons  
Scale: several tens of GeV

## Inclusive electron scattering $A(e, e')$

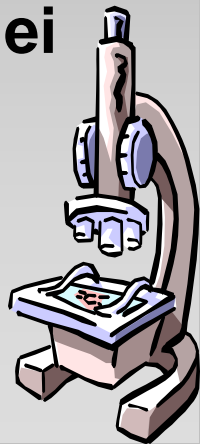
Hard knockout reactions  $A(e, e'p)$  and  $A(e, e'pN)$

2N-SRC



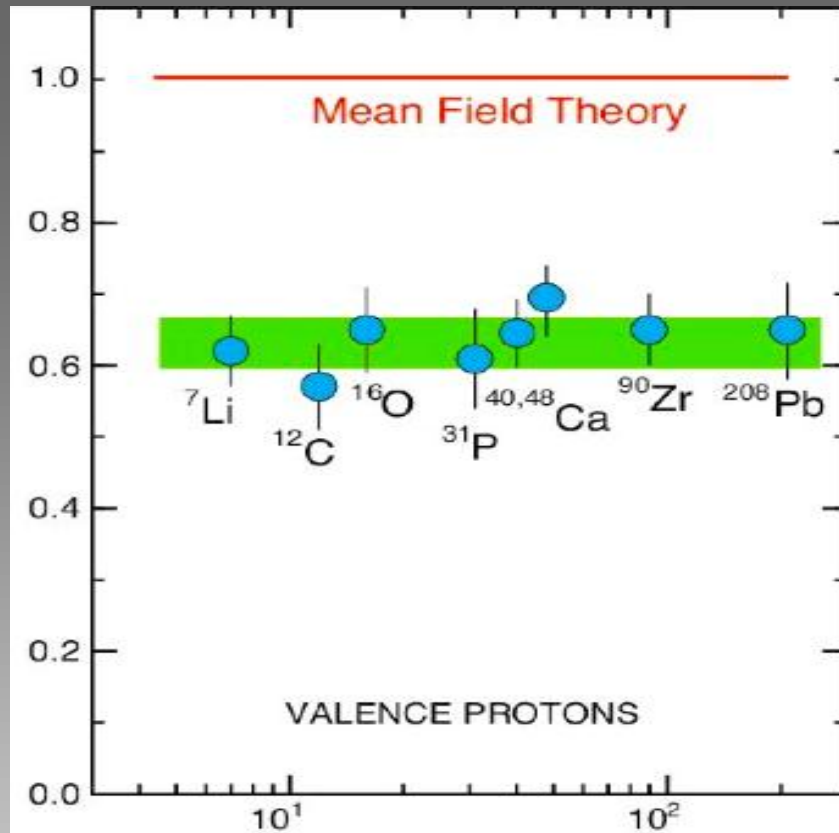
hadronic structure of nuclei

Scale: several GeV



# Spectroscopic factors for (e, e'p) reactions

show only 60-70% of the expected single-particle strength.

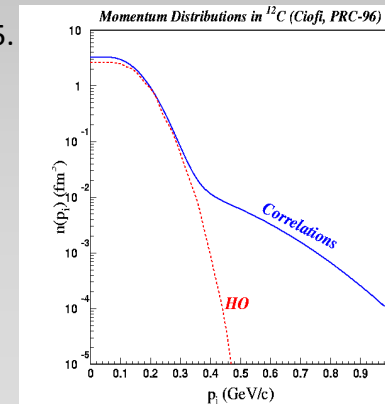
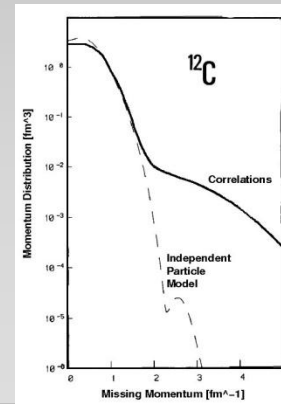


L. Lapikas, Nucl. Phys. A553, 297c (1993)

Benhar et al., Phys. Lett. B 177 (1986) 135.

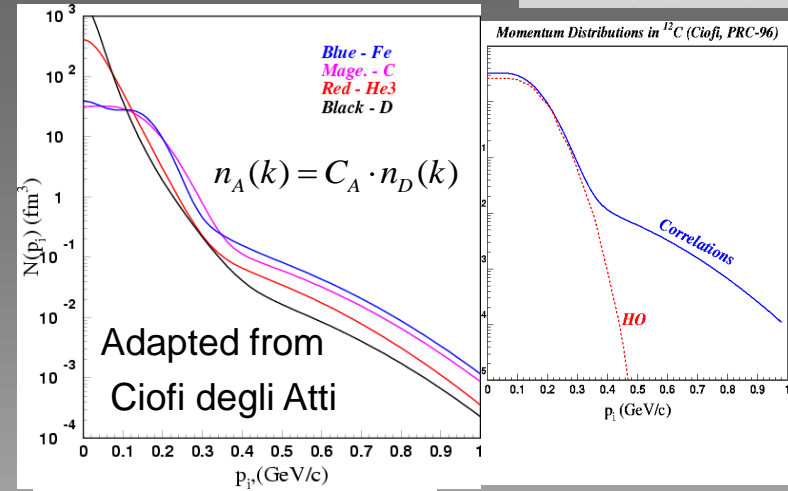
## MISSING :

# Correlations Between Nucleons SRC and LRC



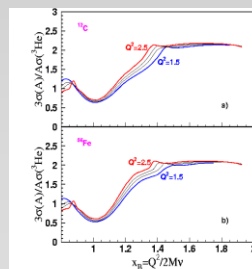
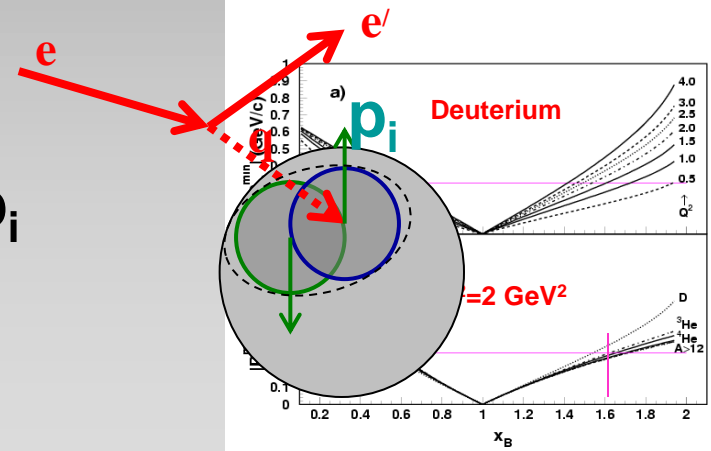
# The inclusive $A(e,e')$ measurements

- At high nucleon momentum distributions are **similar** in shape for light and heavy nuclei: **SCALING**.
- Can be explained by 2N-SRC dominance.
- Within the 2N-SRC dominance picture one can get the probability of 2N-SRC in any nucleus, from the scaling factor.



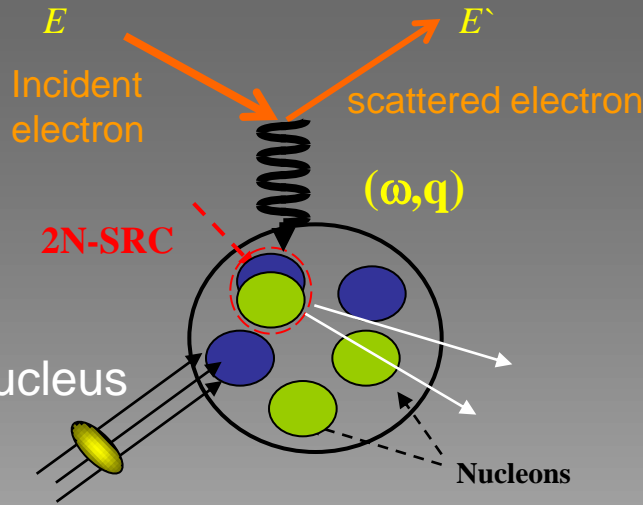
**Problem:** In  $A(e,e')$  the momentum of the struck proton ( $p_i$ ) is unknown.

**Solution:** For fixed high  $Q^2$  and  $x_B > 1$ ,  $x_B$  determines a minimum  $p_i$



Prediction by Frankfurt, Sargsian, and Strikman:

# A(e,e') Kinematics



$$Q^2 = -q_\mu q^\mu = q^2 - \omega^2$$

$$\omega = E' - E$$

$$x_B = \frac{Q^2}{2m\omega} \quad \text{(just kinematics!)}$$

**DIS** off a nucleon:

$$0 \leq x_B \leq 1$$

$x_B$  gives the fraction of the nucleon momentum carried by the struck parton

## HARD KNOCKOUT REACTIONS

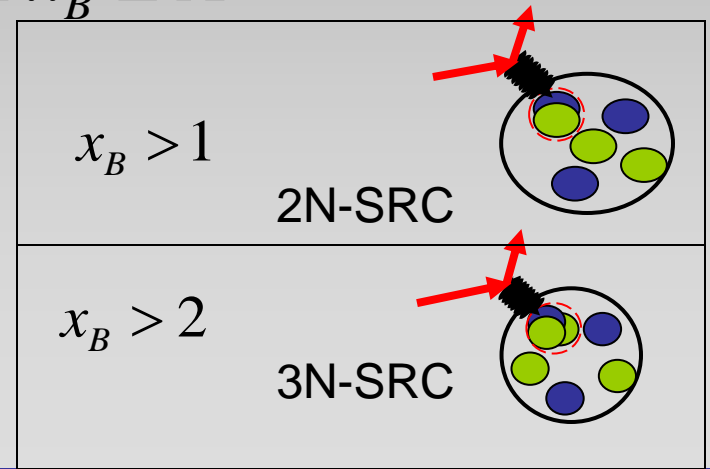
$$0 \leq x_B \leq A$$

For large  $Q^2$ :

$x_B$  counts the number of hadrons involved

$x_B > j \Rightarrow$  at least  $j+1$  nucleons

If exactly  $j+1$  nucleons  $\Rightarrow \frac{\sigma_A}{\sigma_{j+1}}$  scales



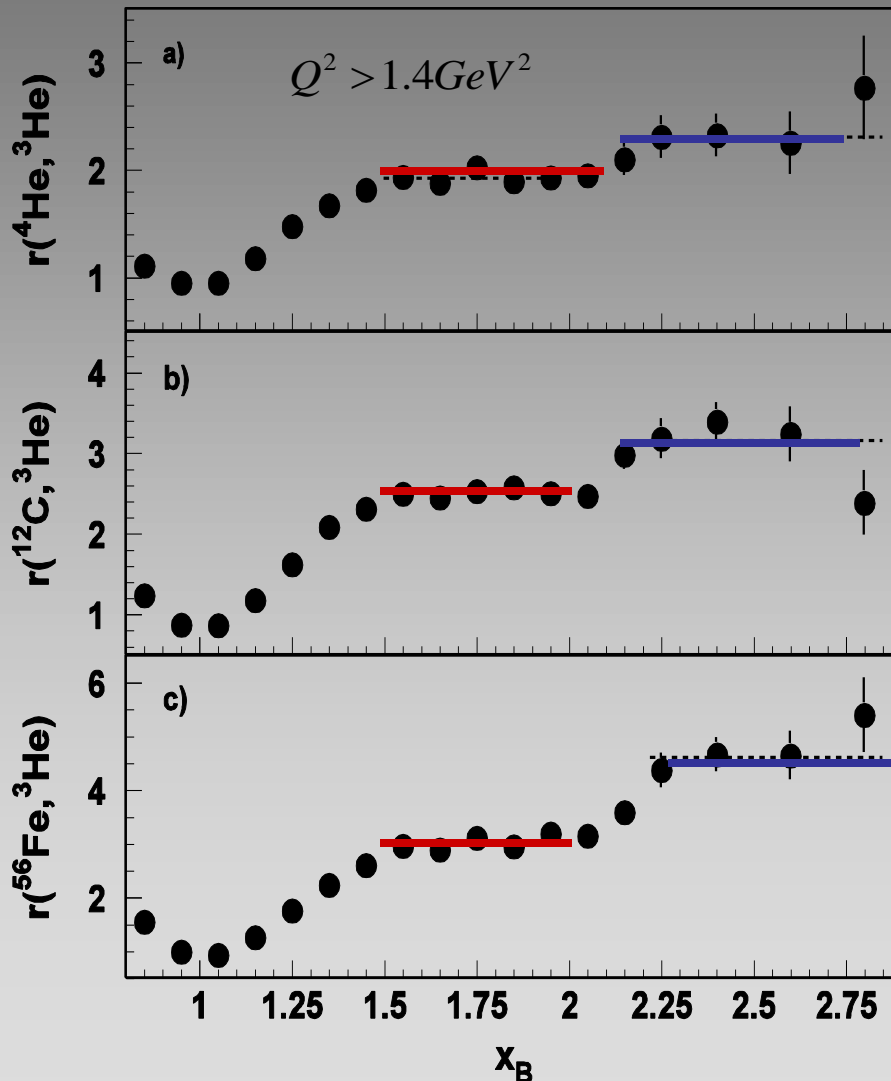




# JLab. CLAS A(e,e') Result

K. Sh. Egiyan et al. PRC 68, 014313 (2003)

K. Sh. Egiyan et al. PRL. 96, 082501 (2006)



The observed "scaling" means that the electrons probe the high-momentum nucleons in the 2(3)-nucleon phase, and the scaling factors determine the per-nucleon probability of the 2(3) N-SRC phase in nuclei with  $A > 3$  relative to  $^3\text{He}$ .

For  $^{12}\text{C}$  2N-SRC (np, pp, nn) =  $20 \pm 4.5\%$ .

The probabilities for 3-nucleon SRC are smaller by one order of magnitude relative to the 2N SRC.

More  $r(A,d)$  data:

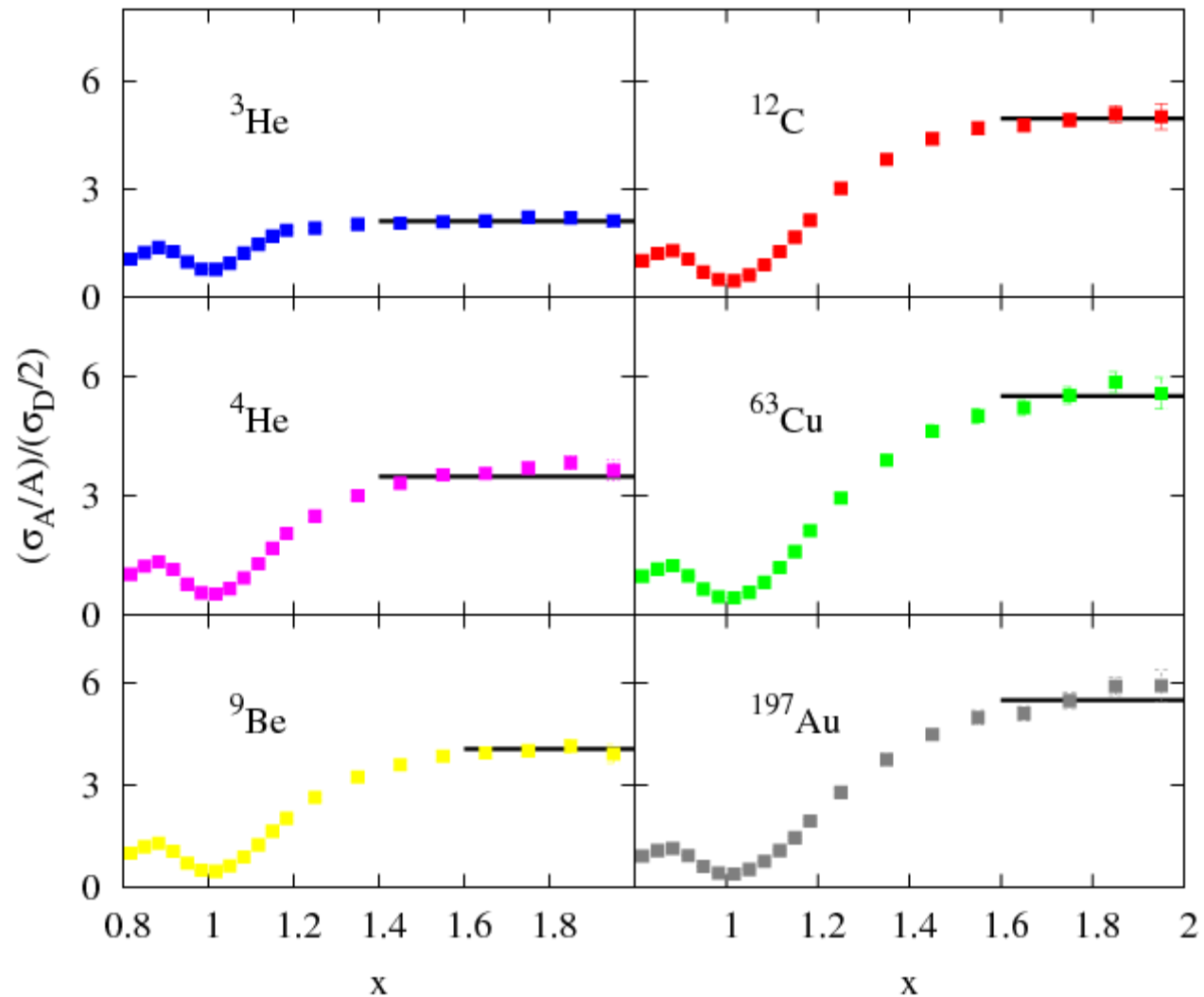
SLAC D. Day et al. PRL 59,427(1987)

JLab. Hall C E02-019

# New Preliminary Results from JLab Hall C (E02-019)

$$Q^2 = 2.5 \text{ GeV}^2$$

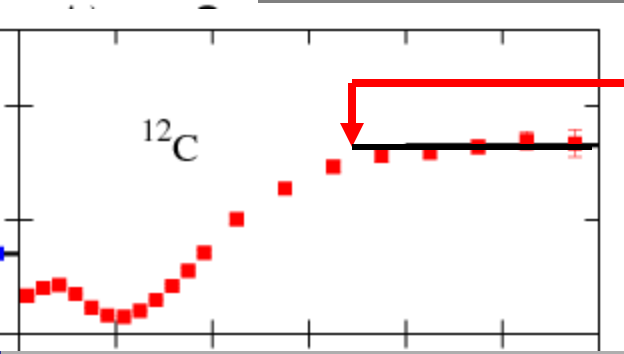
$a_{2N}(A/d)$	
$^3\text{He}$	$2.08 \pm 0.01$
$^4\text{He}$	$3.47 \pm 0.02$
Be	$4.03 \pm 0.04$
C	$4.95 \pm 0.05$
Cu	$5.48 \pm 0.05$
Au	$5.43 \pm 0.06$



# Estimate the amount of 2N-SRC in nuclei

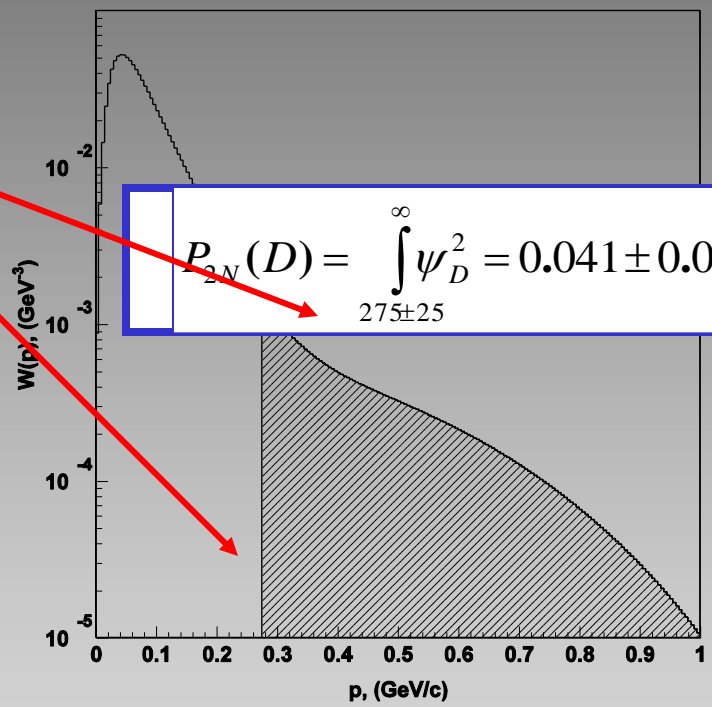
This includes all three isotopic compositions (pn, pp, or nn) for the 2N-SRC phase in  $^{12}\text{C}$ .

$(\sigma_A/A)/(\sigma_D/2)$



$a_{2N}(A/d)$

$P_{\min}$



$a_{2N}(A/d)$

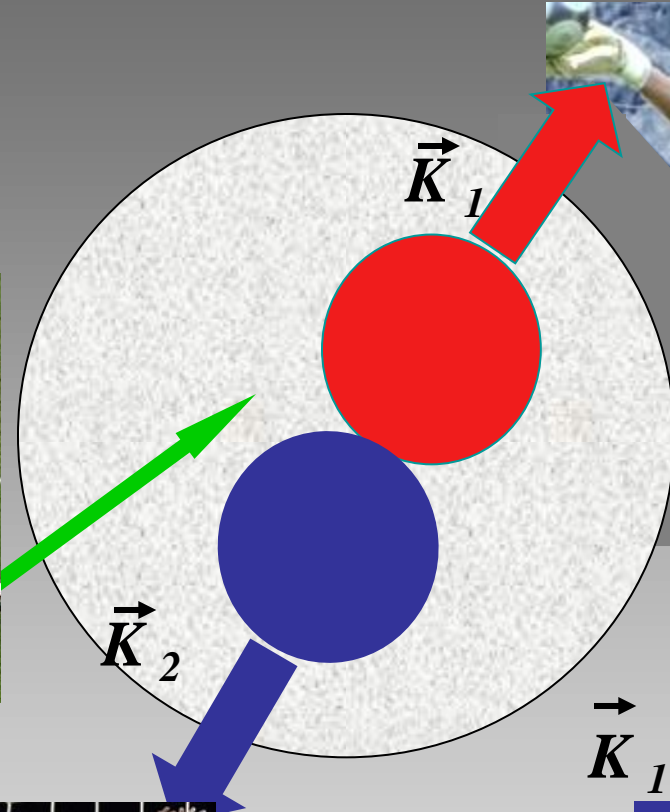
$^3\text{He}$	$2.08 \pm 0.01$
$^4\text{He}$	$3.47 \pm 0.02$
Be	$4.03 \pm 0.04$
C	$4.95 \pm 0.05$
Cu	$5.48 \pm 0.05$
Au	$5.43 \pm 0.06$

$$P_{2N}(A) = a_{2N}(A/d) \cdot P_{2N}(D)$$

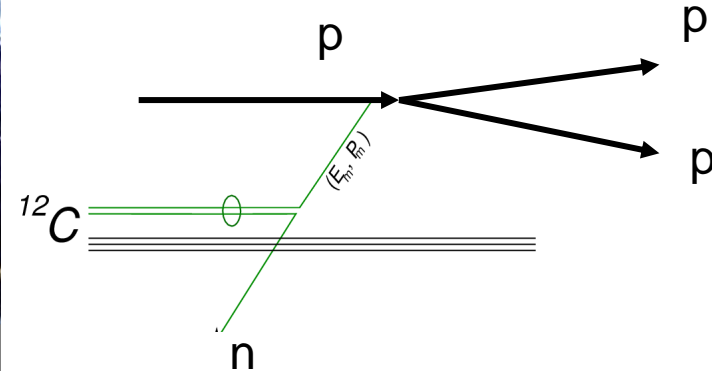
calculations  
measurements

For Carbon:  $P_{2N}(^{12}\text{C}) = 5 \cdot 4\% \approx 20\%$

# A triple – coincidence measurement “Redefine” the problem in momentum space



## EVA / BNL



$$K_1 > K_F, \quad K_F \sim 250 \text{ MeV}/c$$

$K_2 > K_F$  **E01-015 / Jlab**  
**(E07-006)**

$$\vec{K}_1 \cong -\vec{K}_2$$



**A pair with “large” relative momentum between the nucleons and small CM momentum.**

# Why several GeV and up protons are good probes of SRC ?



They have small deBroglie wavelength:

$$\lambda = h/p = hc/pc = 2\pi \cdot 0.197 \text{ GeV}\cdot\text{fm}/(6 \text{ GeV}) \approx 0.2 \text{ fm.}$$



Large momentum transfer is possible with wide angle scattering.

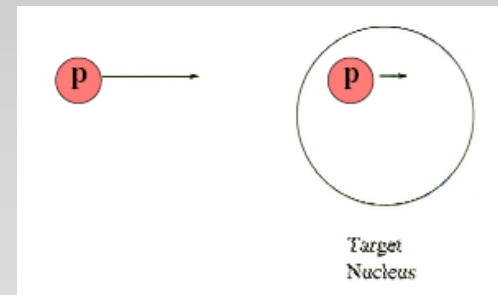


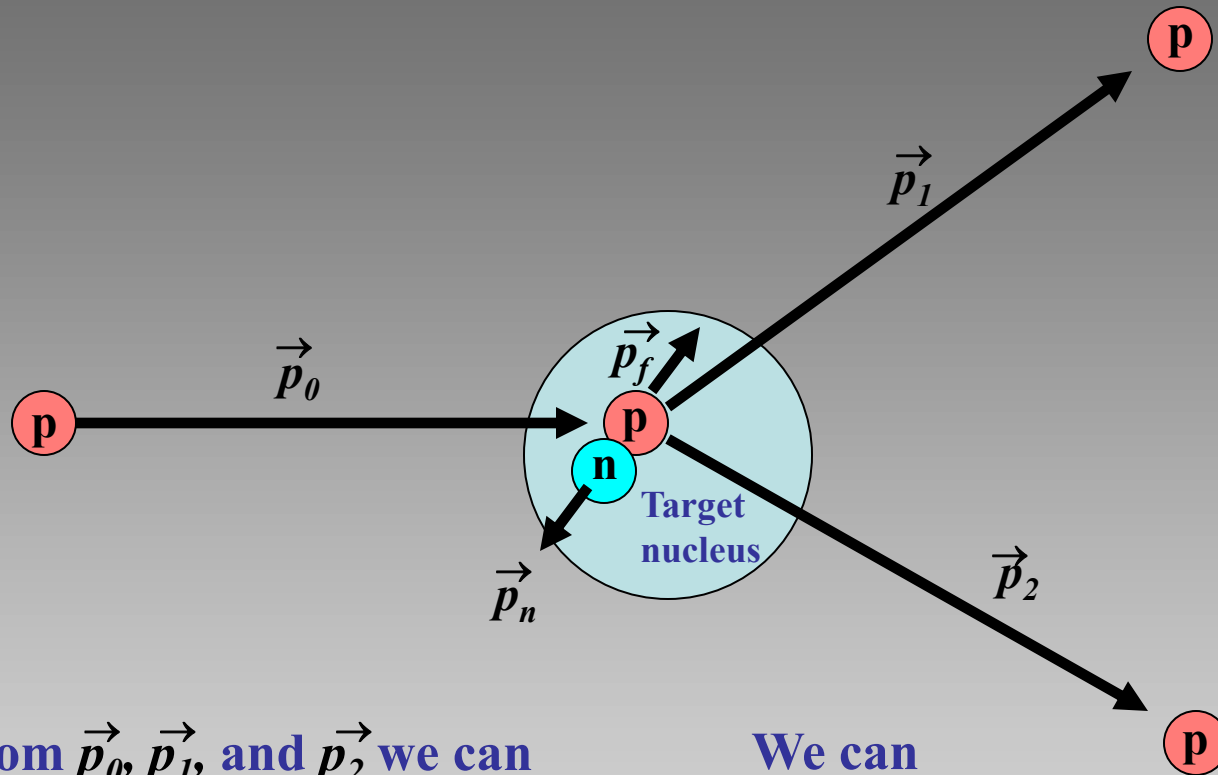
The  $s^{-10}$  dependence of the p-p elastic scattering preferentially selects high momentum nuclear protons.

**For pp elastic scattering near  $90^\circ$  cm**

$$\frac{d\sigma}{dt} \propto s^{-10}$$

**QE pp scattering near  $90^\circ$  has a very strong preference for reacting with forward going high momentum nuclear protons.**



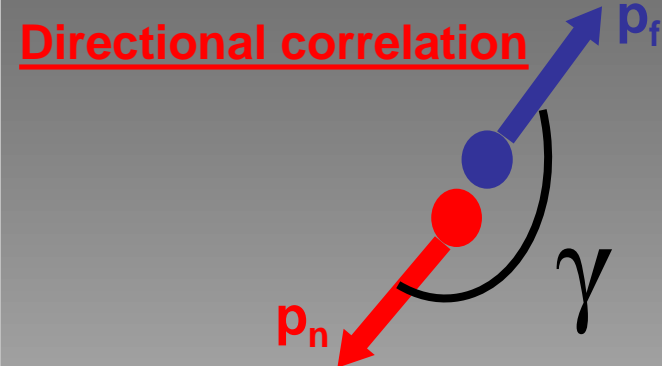


From  $\vec{p}_0$ ,  $\vec{p}_1$ , and  $\vec{p}_2$  we can deduce, event-by-event what  $\vec{p}_f$  and the binding energy of each knocked-out proton is.

We can then compare  $\vec{p}_n$  with  $\vec{p}_f$  and see if they are roughly “back to back.”

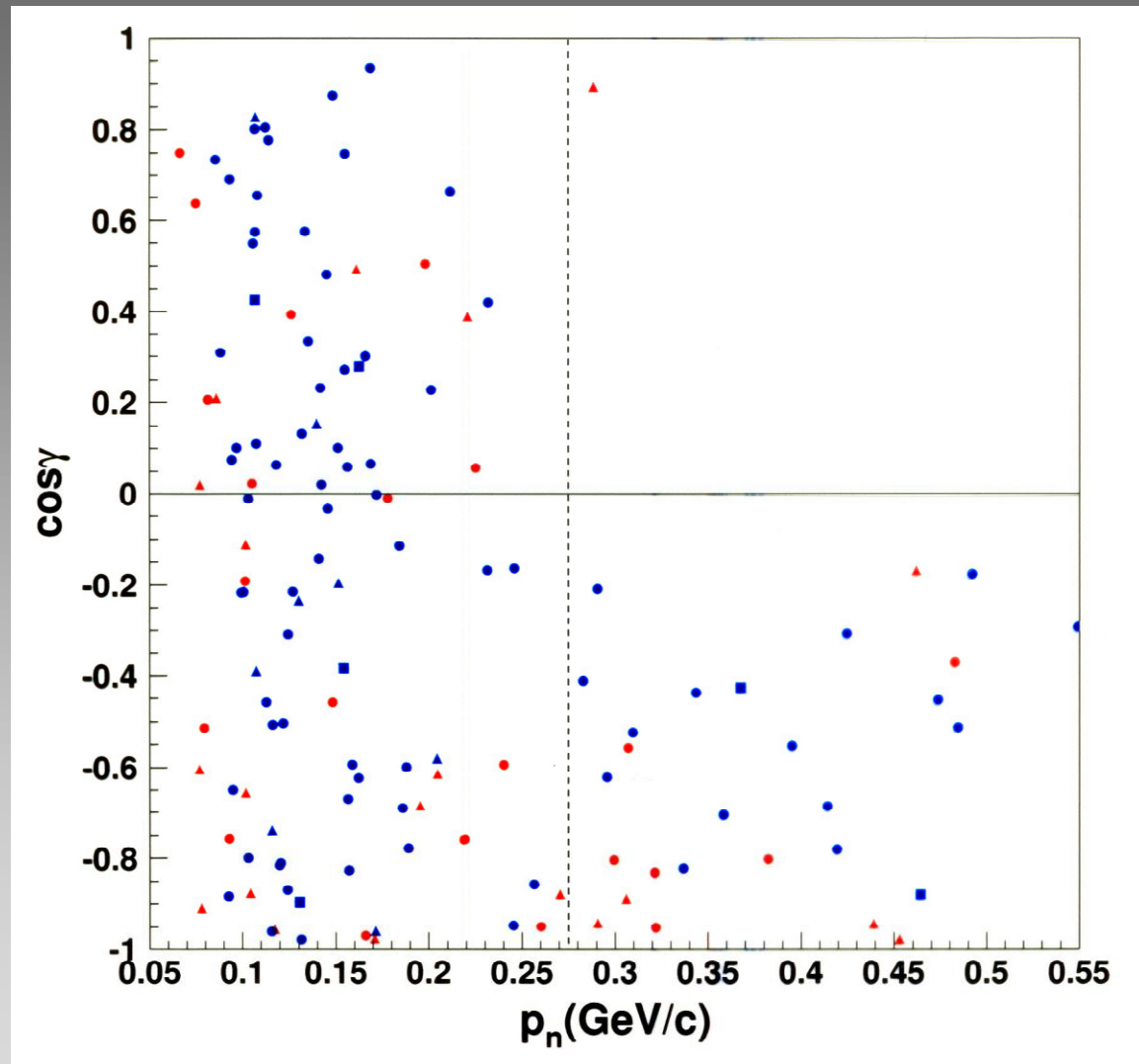
# $^{12}\text{C}(p, p'pn)$ measurements at EVA / BNL

A. Tang et al. Phys. Rev. Lett. 90 ,042301 (2003)



Piasetzky, Sargsian, Frankfurt,  
Strikman, Watson PRL 162504(2006).

Removal of a proton with  
momentum above  $275 \text{ MeV}/c$   
from  $^{12}\text{C}$  is  $92 \pm 8_{18} \%$   
accompanied by the emission  
of a neutron with momentum  
equal and opposite to the  
missing momentum.



$$\sigma_{\text{CM}} = 0.143 \pm 0.017 \text{ GeV}/c$$



Identify pp-SRC pairs in nuclei.

$$(e, e' p p)$$



Determine the abundance of pp-SRC pairs.

$$(e, e' p p) / (e, e' p)$$



Verify the abundance of np-SRC pairs as determined by the EVA / BNL experiment.

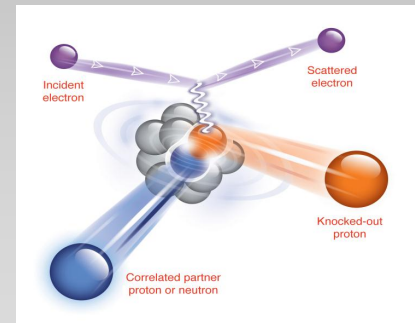
$$(e, e' p n) / (e, e' p)$$



Determine the pp-SRC / np-SRC ratio.

$$(e, e' p p) / (e, e' p n)$$

It is important to identify pp-SRC pairs and to determine the pp-SRC/np-SRC ratio since they can tell us about the isospin dependence of the strong interaction at short distance scale.



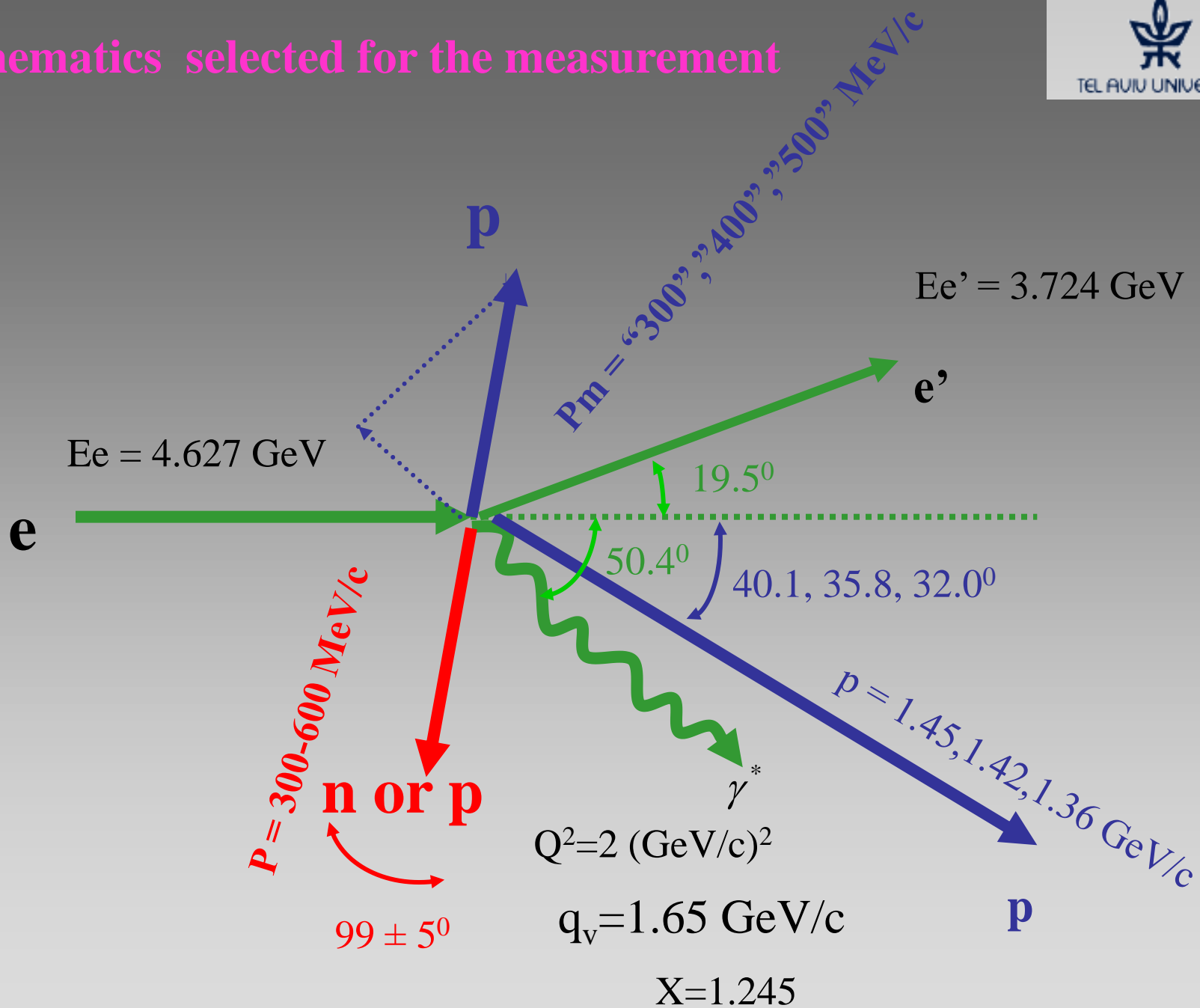
**E01-015**



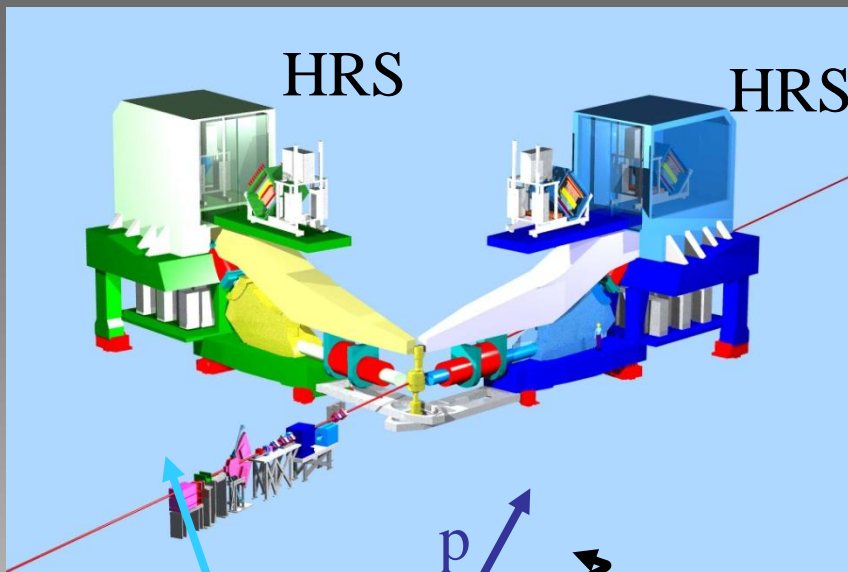
Simultaneous measurements of the  $(e, e' p)$ ,  $(e, e' p p)$ , and  $(e, e' p n)$  reactions.



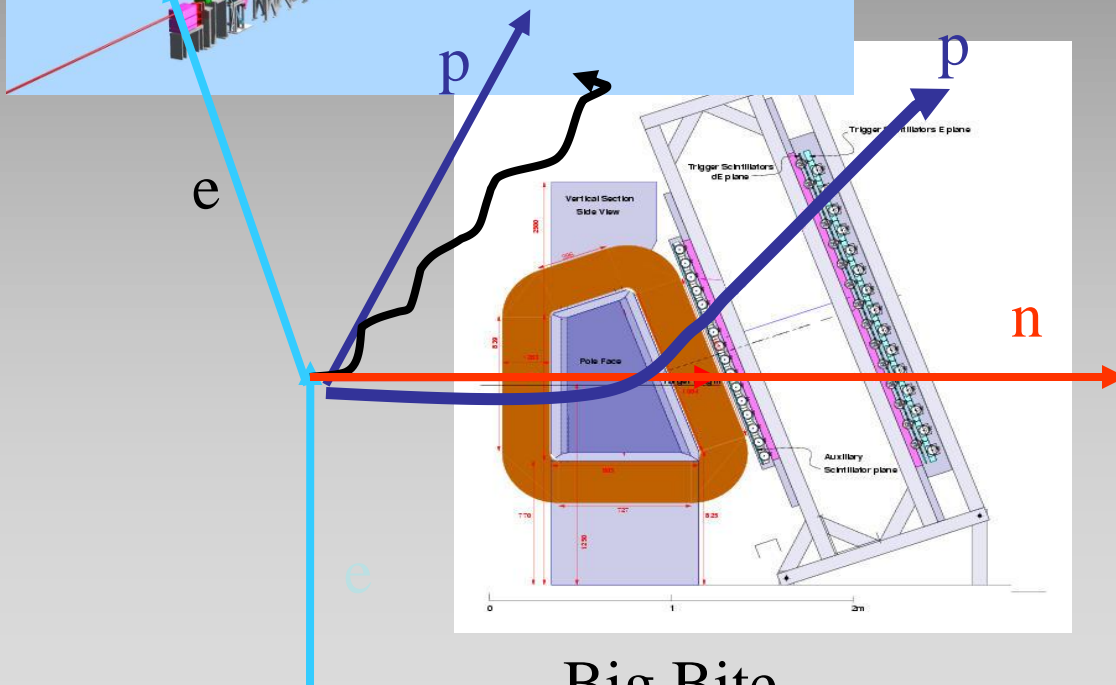
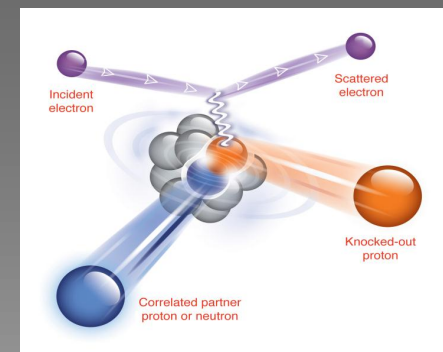
# The kinematics selected for the measurement



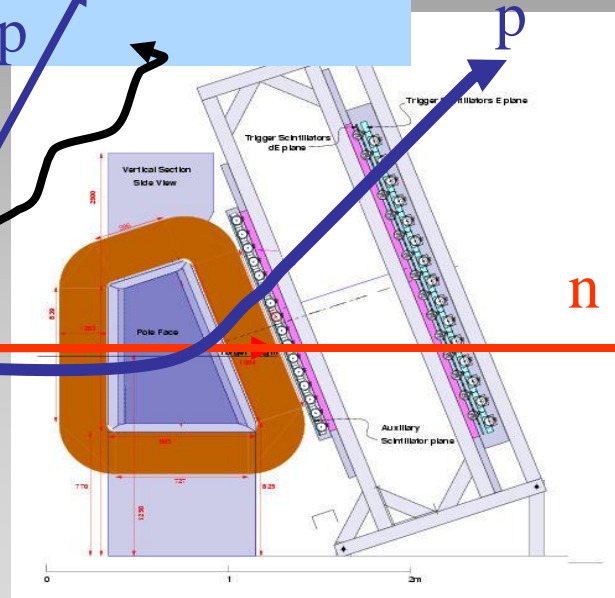
# Simultaneous measurements of the $(e, e' p)$ , $(e, e' p p)$ , and $(e, e' p n)$ reactions.



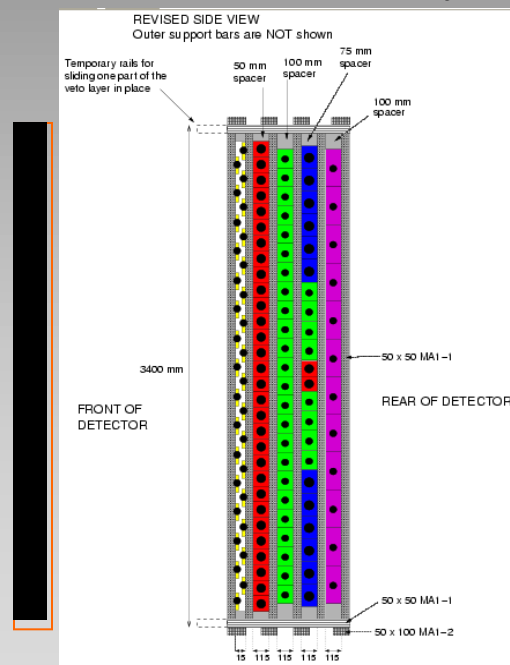
EXP 01-015  
Hall A JLab



n array

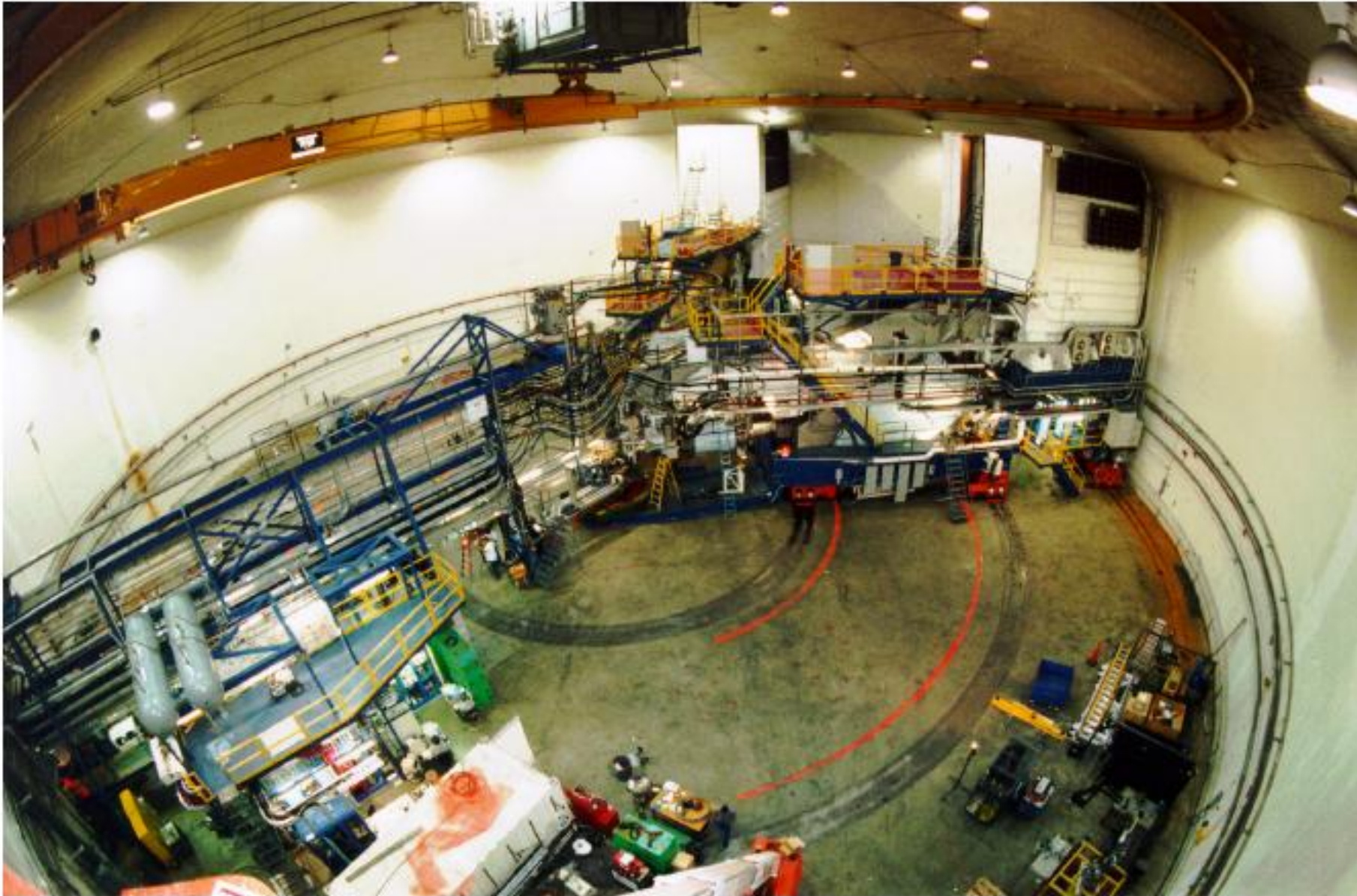


Big Bite



Lead wall

# Jefferson Lab's Hall A



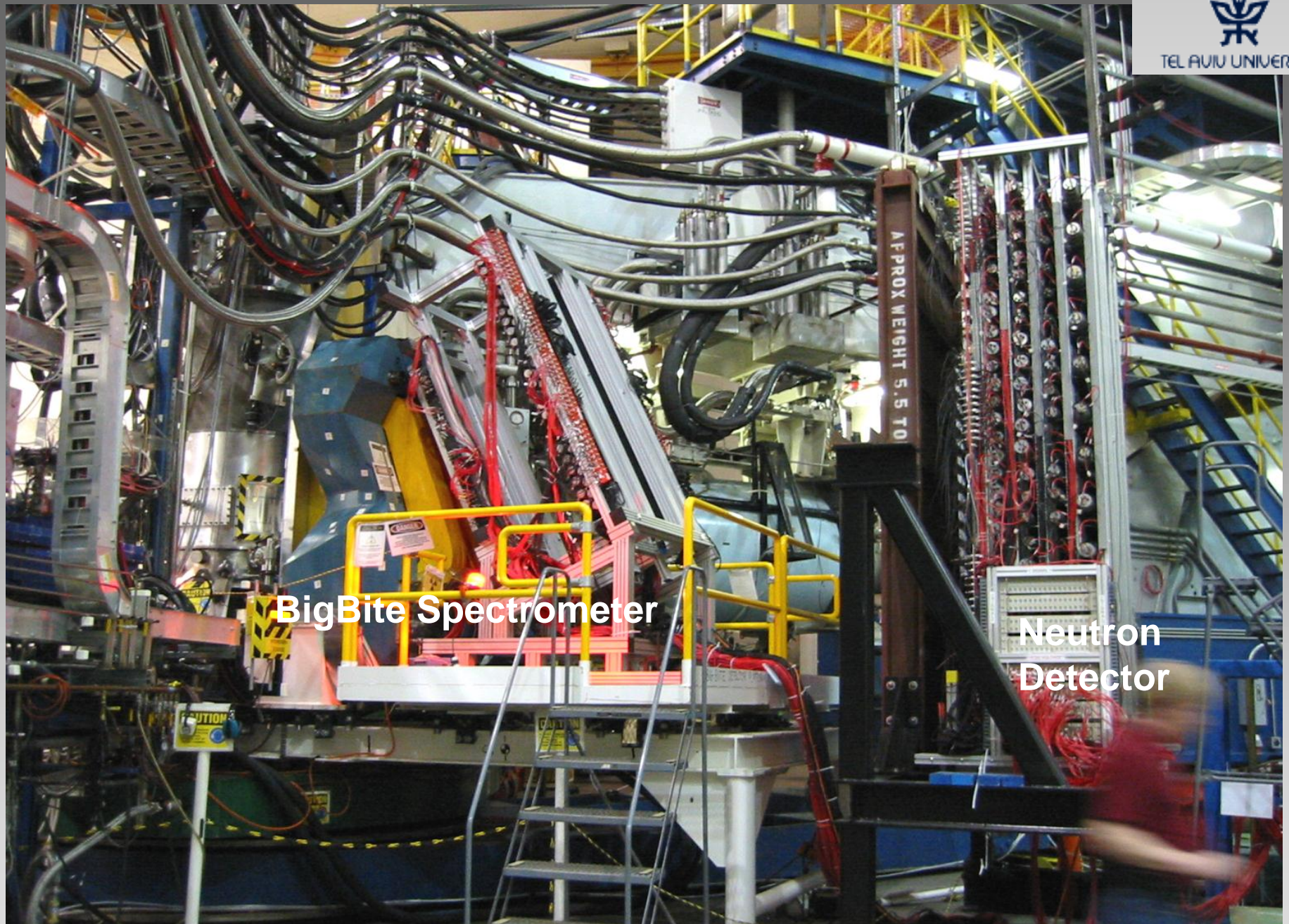


# HAND -The Hall A neutron detector



The Big Bite spectrometer





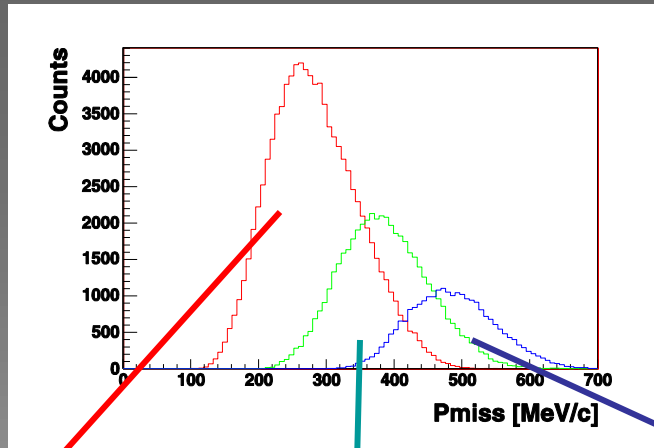
BigBite Spectrometer

Neutron  
Detector



$^{12}\text{C}(e,e'p)$

$x_B > 1$

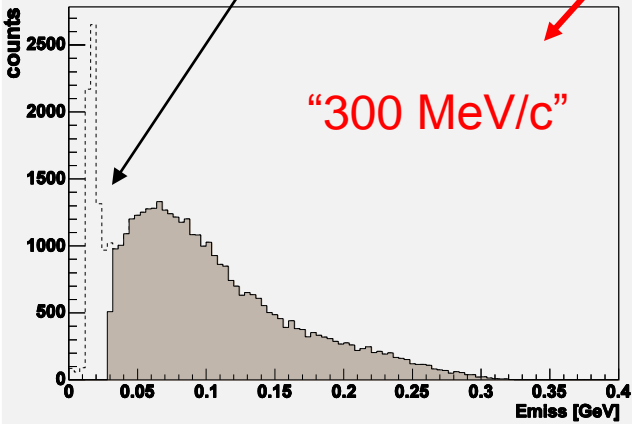


"300 MeV/c"

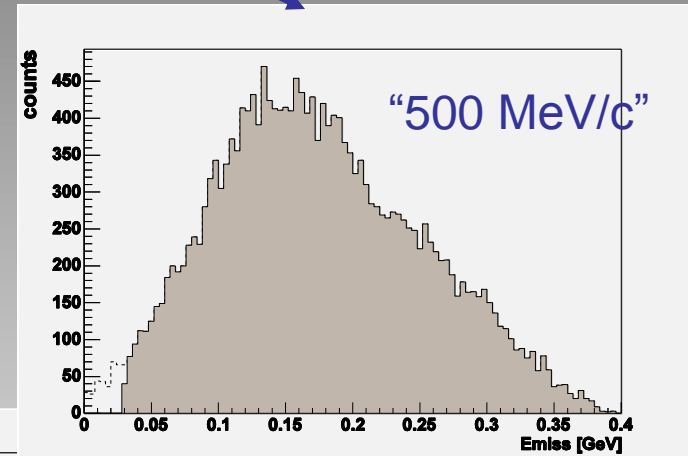
"400 MeV/c"

"500 MeV/c"

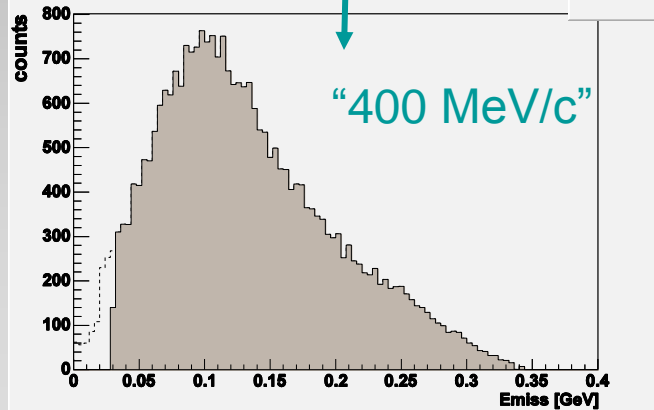
$^{12}\text{C}(e,e'p)^{11}\text{B}$



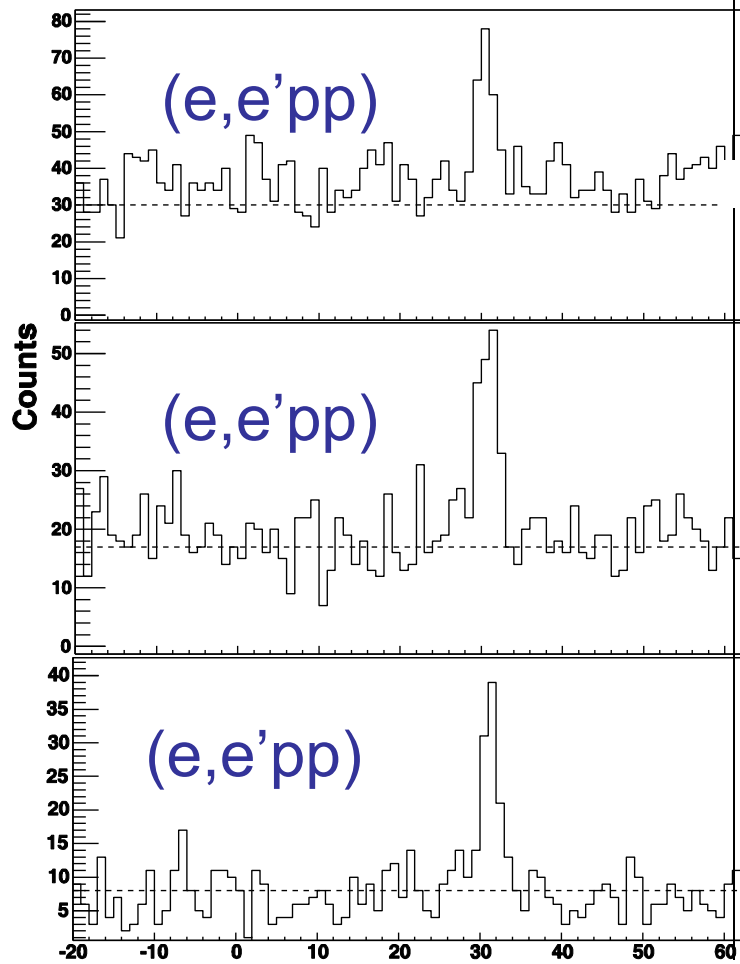
"300 MeV/c"



"500 MeV/c"



"400 MeV/c"



$P_{\text{mis}} = \text{"300"} \text{ MeV/c}$

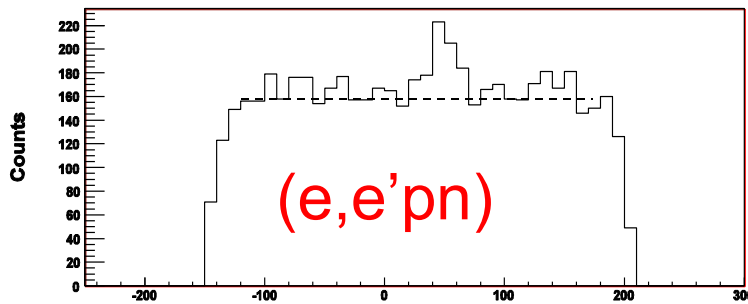
(Signal : BG= 1.5:1)

$P_{\text{mis}} = \text{"400"} \text{ MeV/c}$

(Signal : BG= 2.3:1)

$P_{\text{mis}} = \text{"500"} \text{ MeV/c}$

(Signal : BG= 4:1)



$P_{\text{mis}} = \text{"500"} \text{ MeV/c}$

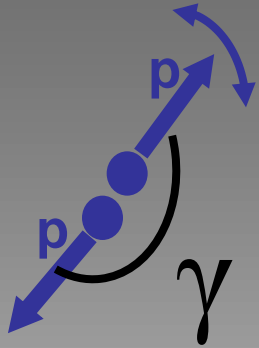
(Signal : BG= 1:7)

TOF [ns]



# Directional correlation

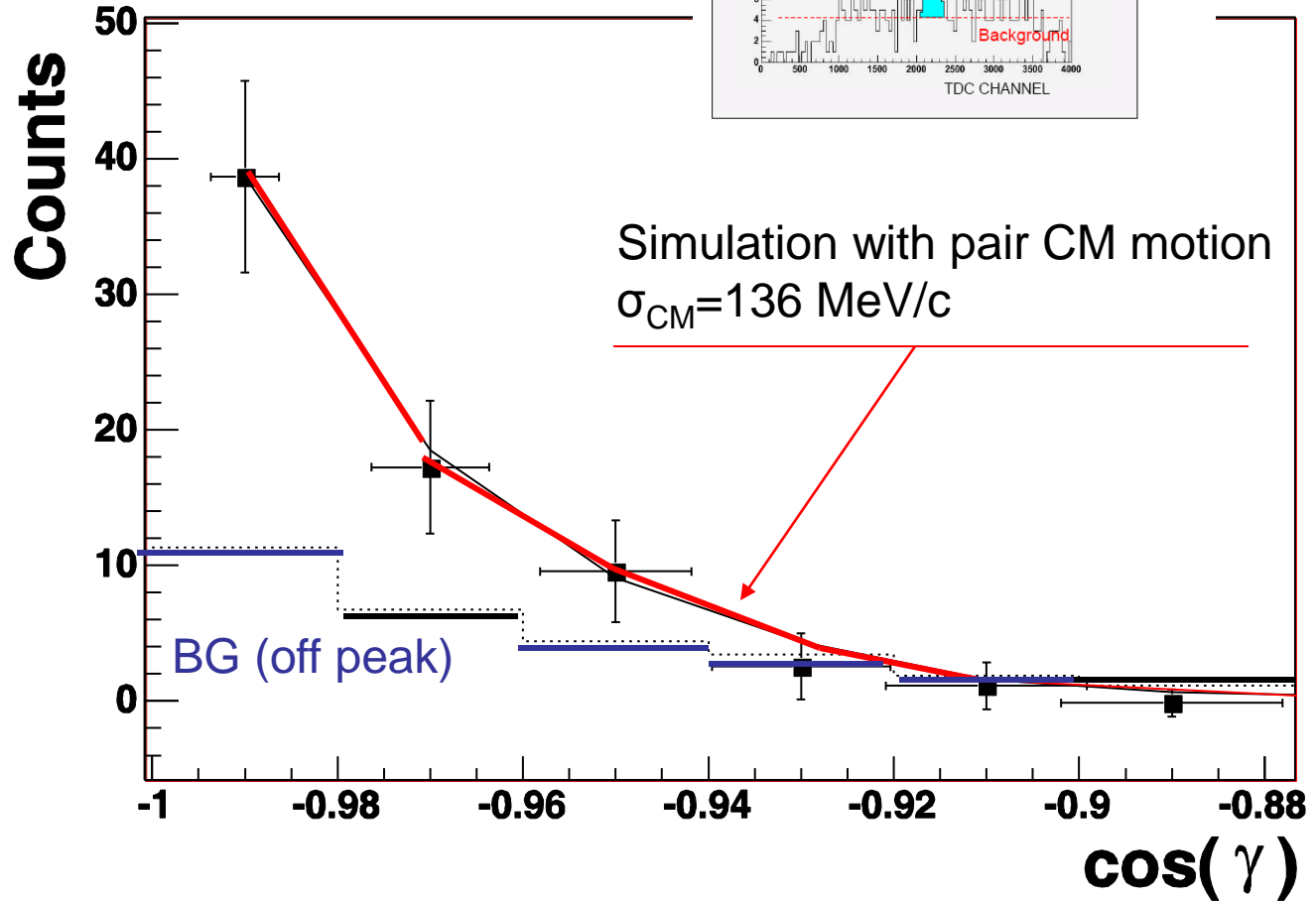
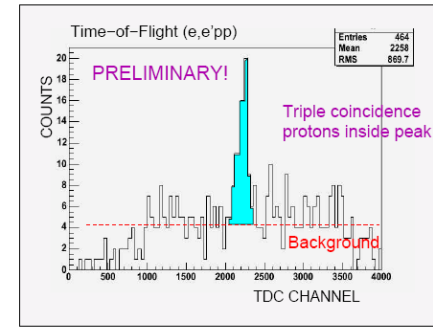
$^{12}\text{C}(e,e'pp)$



Triple Coincidence Events

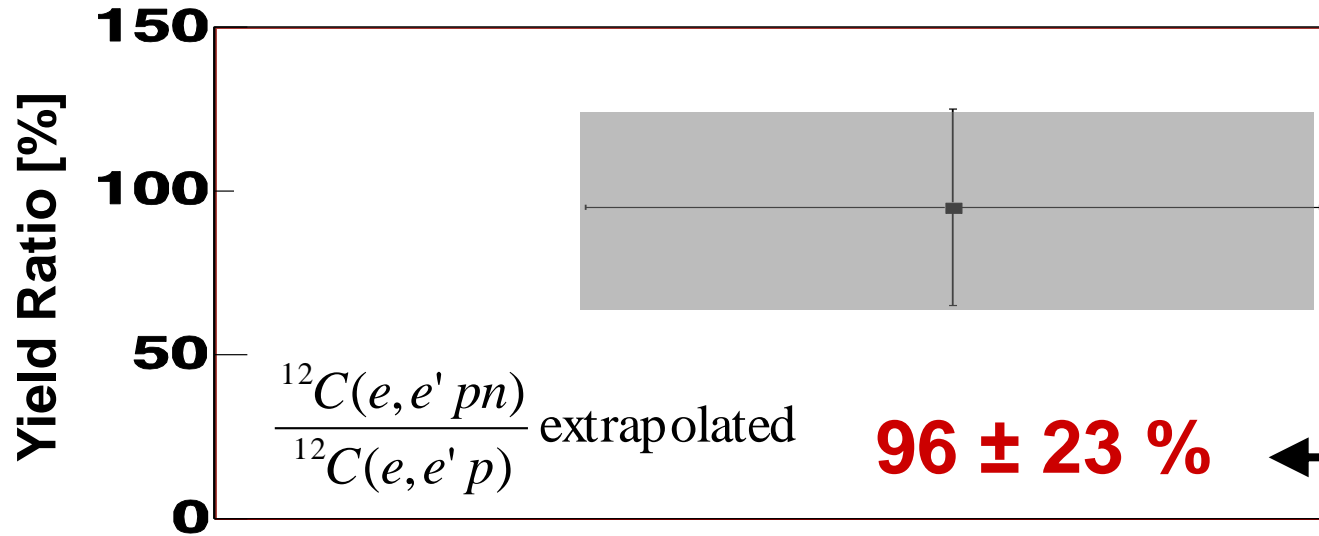


TEL AVIV UNIVERSITY



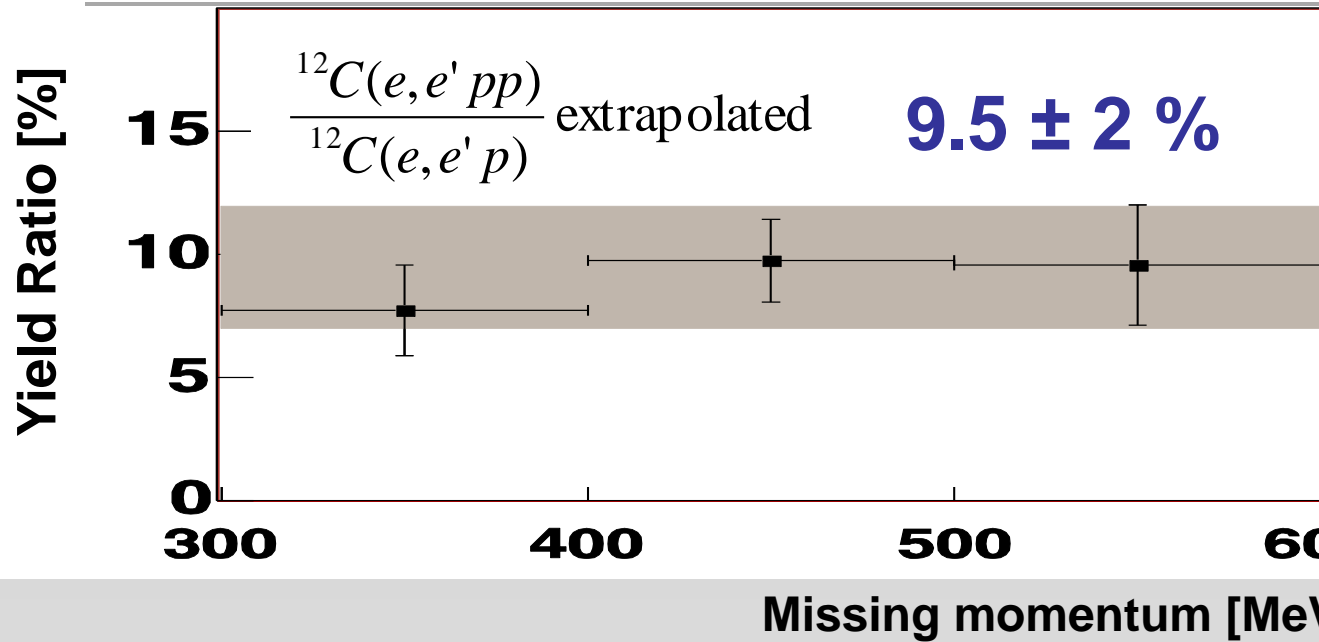
Measured 2 components of  $\vec{p}_{c.m.}$  and 3 kinematical setups  $\Rightarrow \sigma_{\text{CM}} = 0.136 \pm 0.020 \text{ GeV}/c$   
(p,2pn) experiment at BNL :  $\sigma_{\text{CM}} = 0.143 \pm 0.017 \text{ GeV}/c$   
Theoretical prediction (Ciofi and Simula) :  $\sigma_{\text{CM}} = 0.139 \text{ GeV}/c$



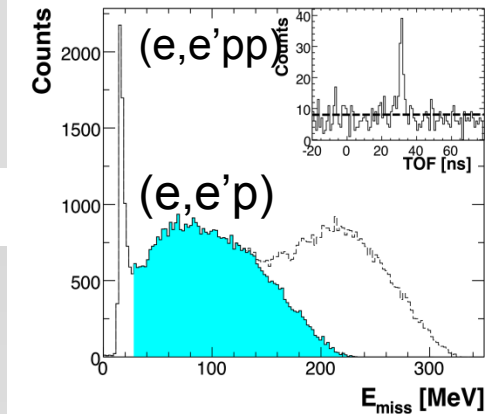


R. Subedi et al.,  
Science 320 (2008) 1476

BNL Experiment  
measurement was **92<sup>+8</sup><sub>-18</sub>%**

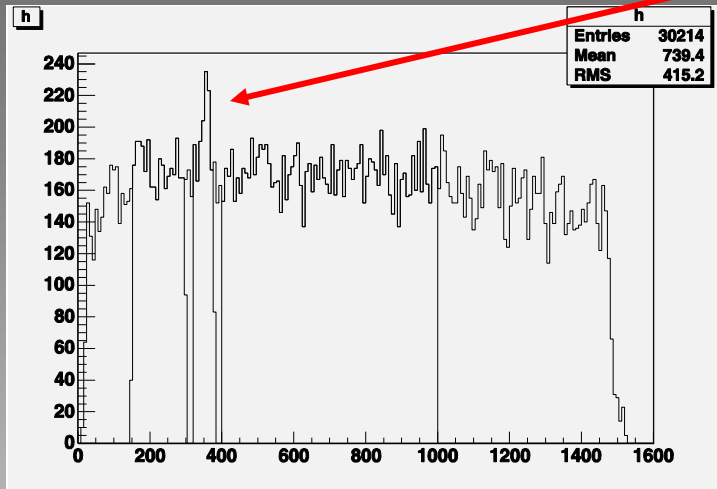


R. Shneur et al.,  
PRL 99, 072501 (2007)

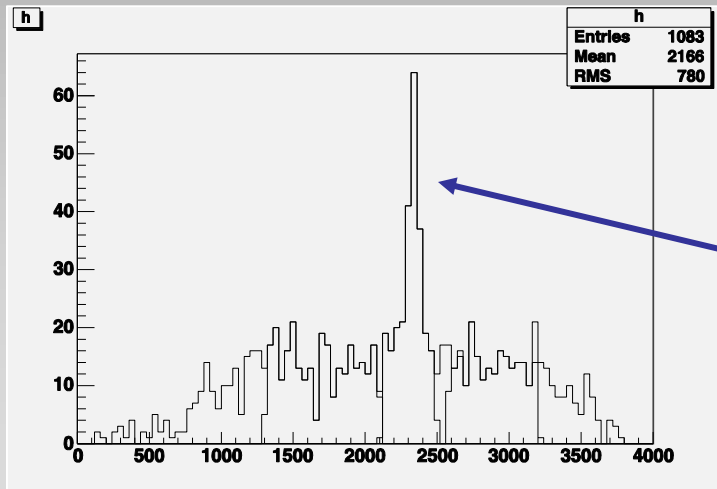


# The $(e, e'pn) / (e, e'pp)$ ratio

**$179 \pm 39$**



TOF for the neutrons [ns]



TOF for the protons [ns]

**$116 \pm 17$**

Corrected for detection efficiency:

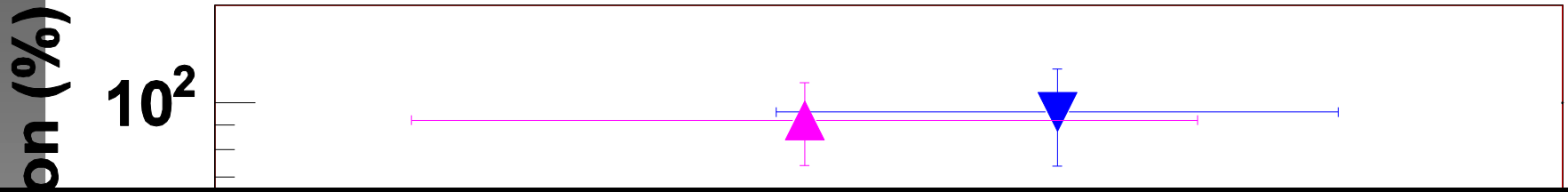
$$\frac{{}^{12}\text{C}(e, e' pn)}{{}^{12}\text{C}(e, e' pp)} = 8.1 \pm 2.2$$

Corrected for SCX (using Glauber):

$$\frac{{}^{12}\text{C}(e, e' pn)}{{}^{12}\text{C}(e, e' pp)} = 9.0 \pm 2.5$$

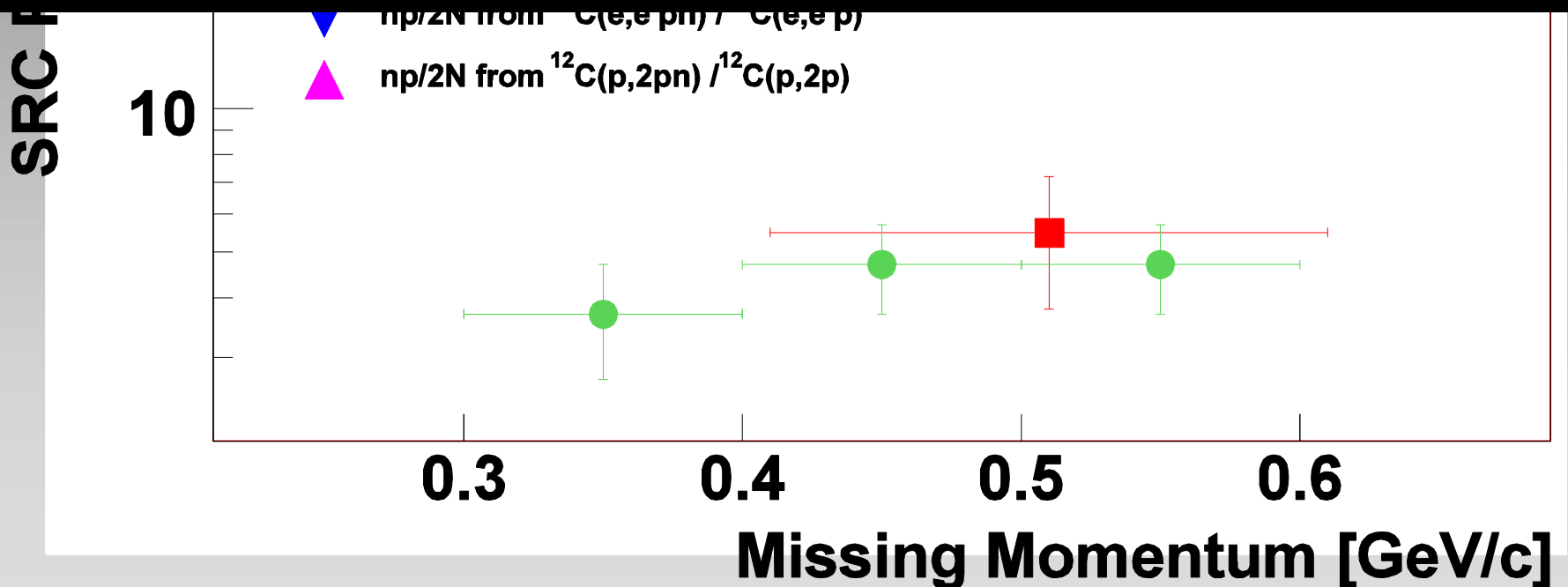
**In Carbon:**

$$\frac{np - \text{SRC}}{pp - \text{SRC}} = 18.0 \pm 5$$

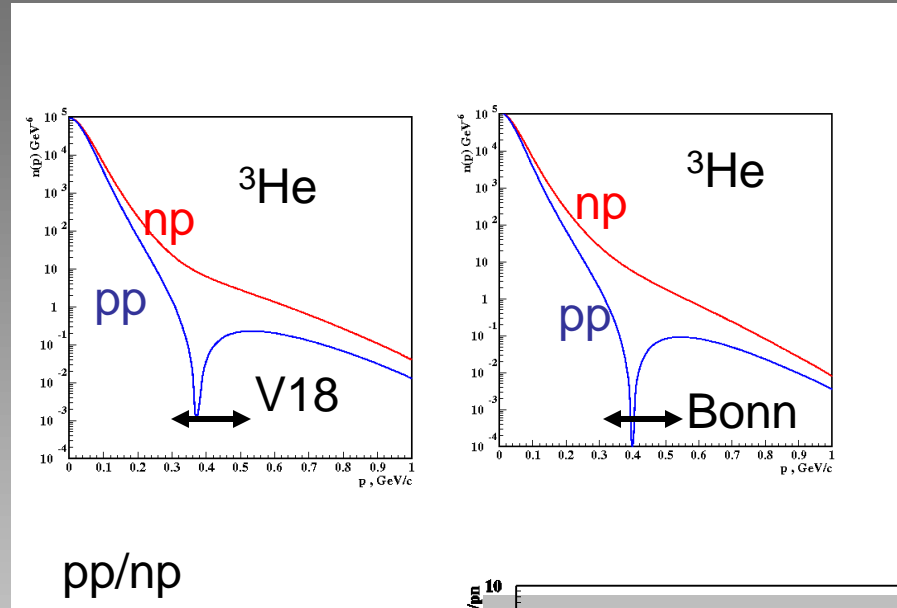
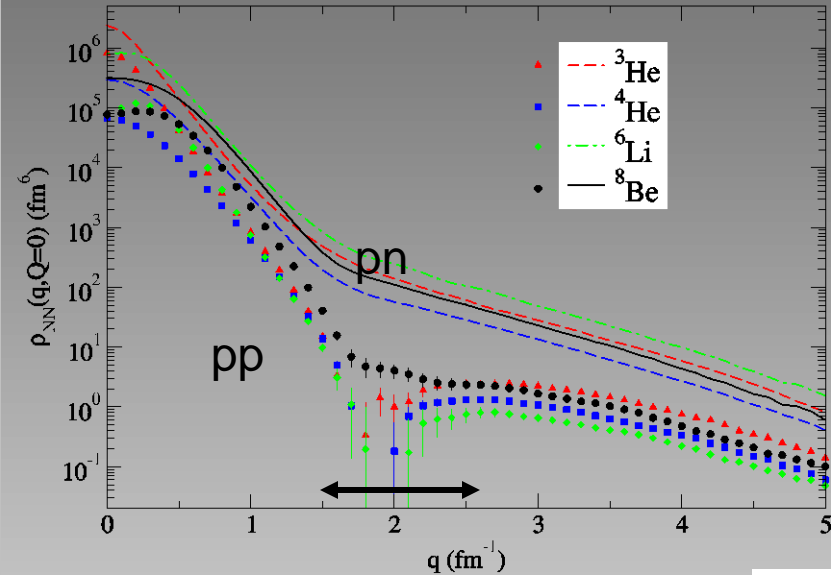


There are  $18 \pm 5$  times more np-SRC than pp-SRC pairs in  $^{12}\text{C}$ .

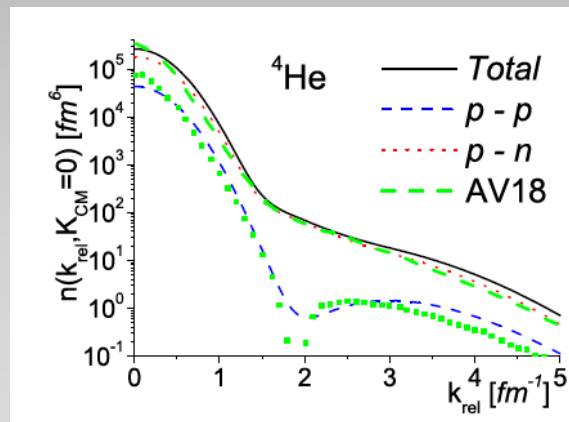
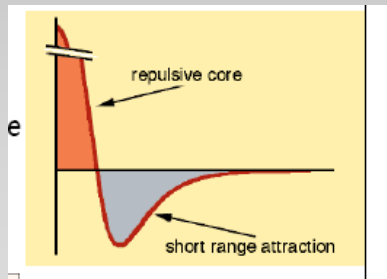
Why ?



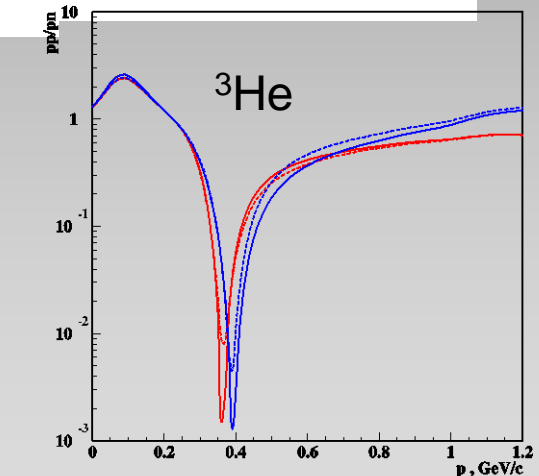
At 300-500 MeV/c there is an excess strength in the np momentum distribution due to the strong correlations induced by the tensor NN potential.



Schiavilla, Wiringa, Pieper, Carson, PRL 98, 132501 (2007).

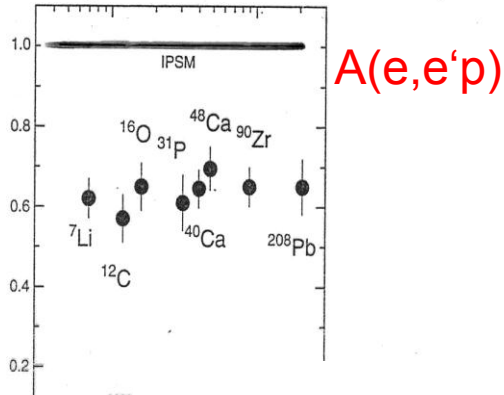


Ciofi and Alvioli, PRL 100, 162503 (2008).

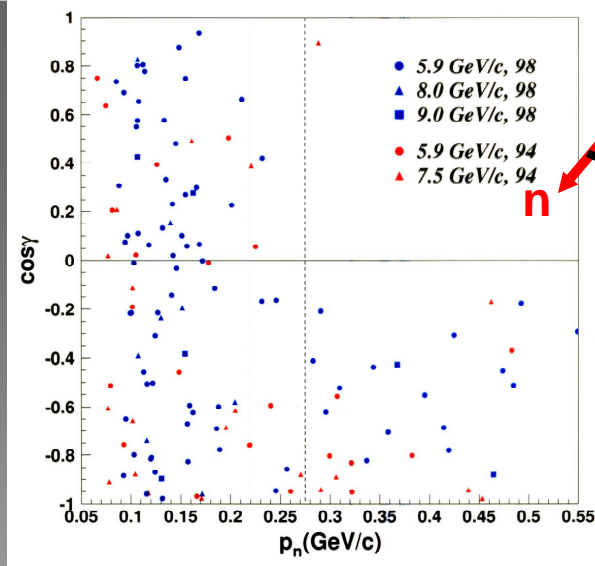


Sargsian, Abrahamyan, Strikman, Frankfurt PR C71 044615 (2005).

# Summary of Results

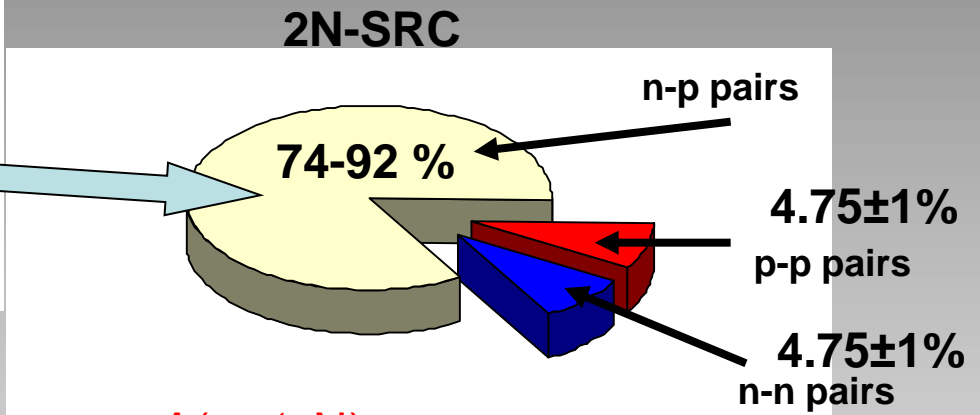
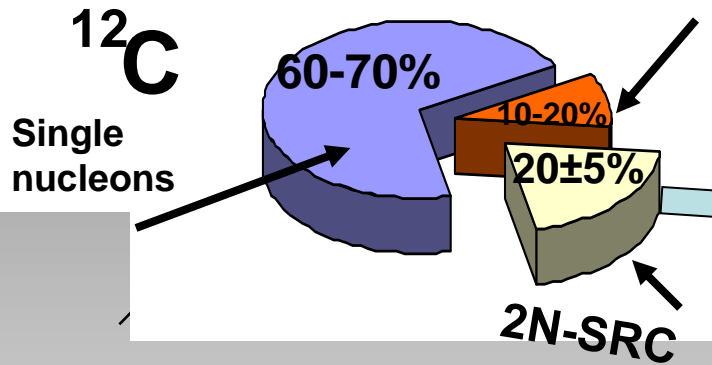


Long range  
(shell model)  
correlations



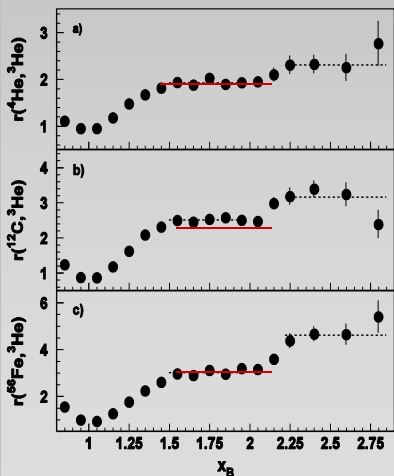
Tang et al.  
PRL 042301 (2003)

Piassetzky, Sargsian,  
Frankfurt, Strikman,  
Watson  
PRL 162504(2006).



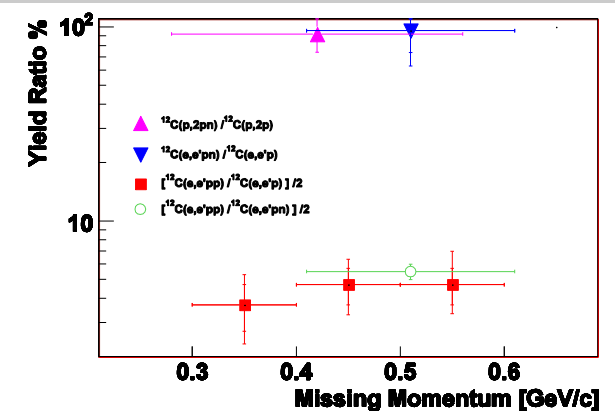
$A(e, e'pN)$

R. Subedi et al.,  
Science 320, 1476 (2008).

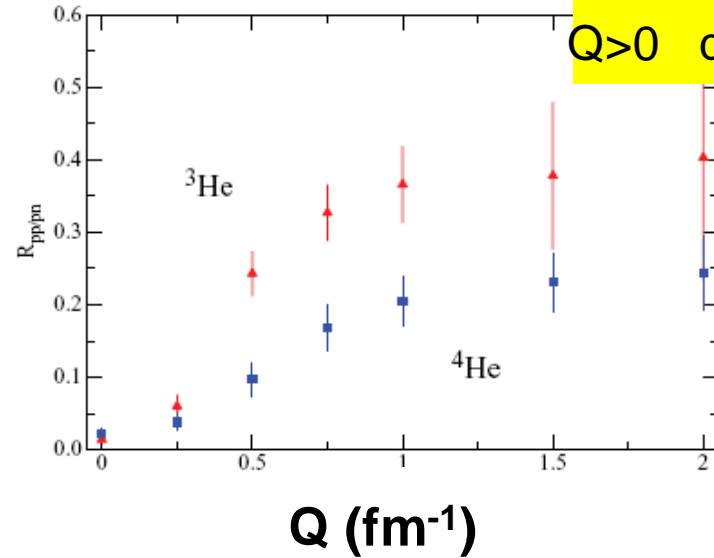
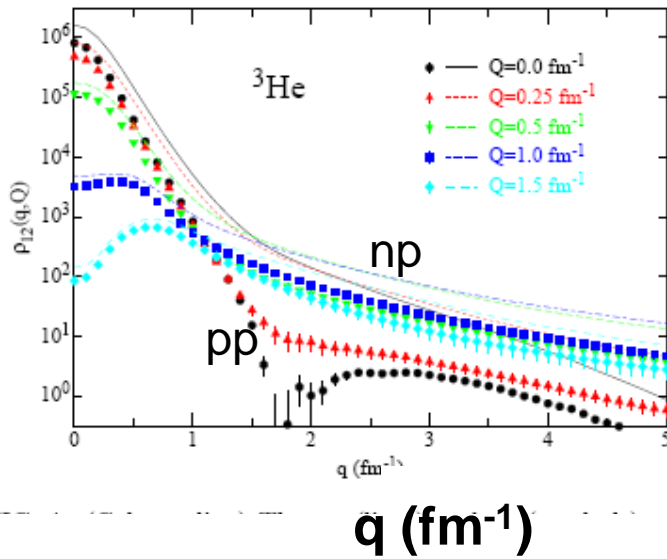


$A(e, e')$

Egiyan et al. PRC 68, 014313.  
Egiyan et al. PRL. 96, 082501 (2006)

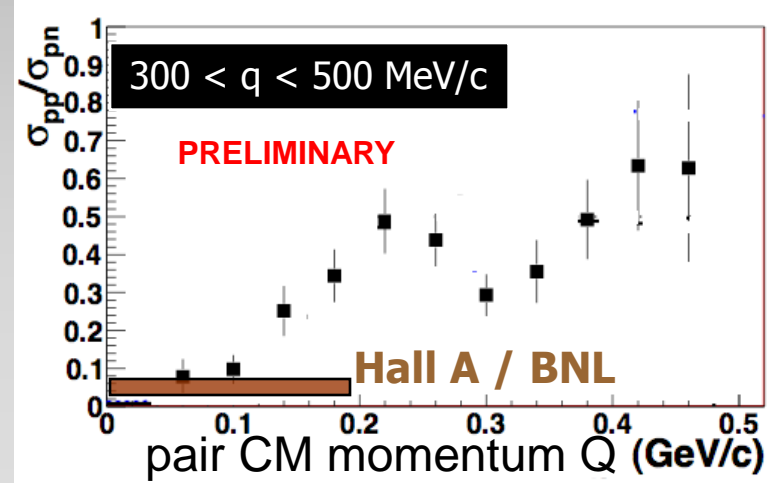
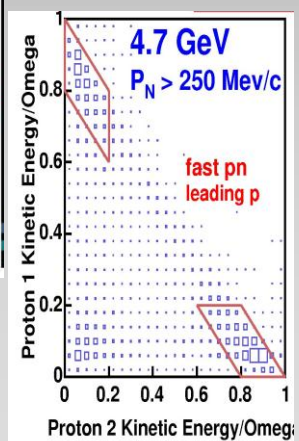
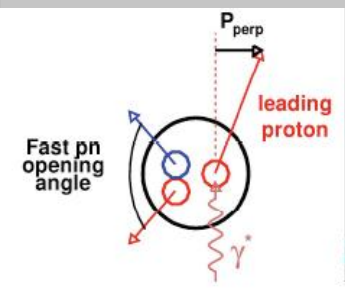


# pp/pn ratio as a function of pair CM momentum



Wiringa, Schiavilla, Pieper, Carlson **PRC** 78 021001 (2008)

**Small Q ⇒ pp pair in s-wave ⇒ large tensor contribution ⇒ small pp/np ratio**



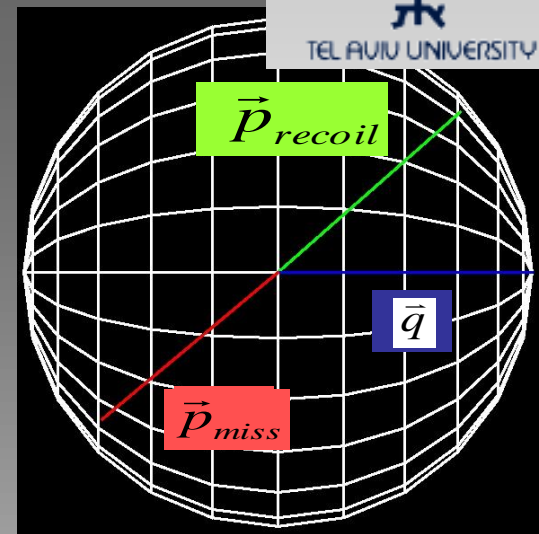
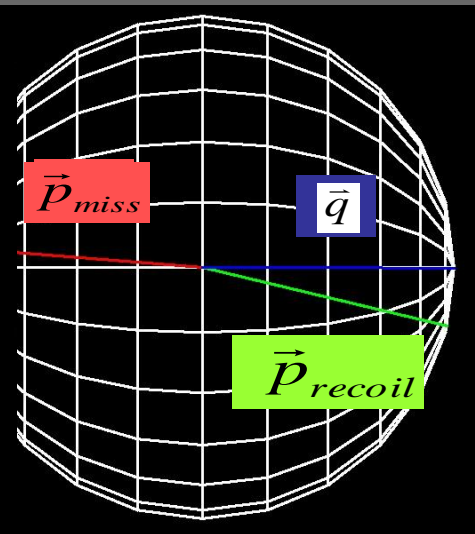
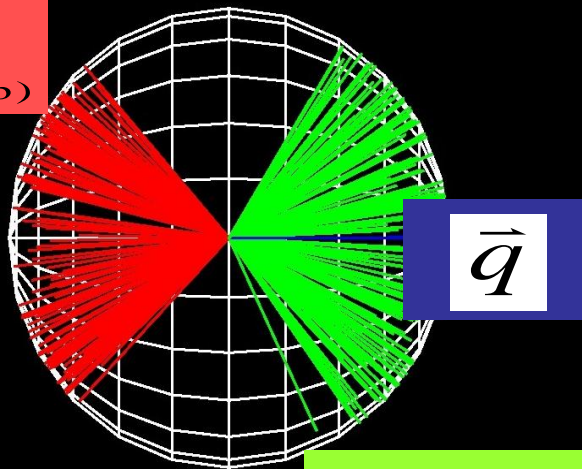
JLab / Hall B preliminary data

Thanks to  
L. Weinstein

$$\frac{pp}{np} \approx \frac{1}{4}$$

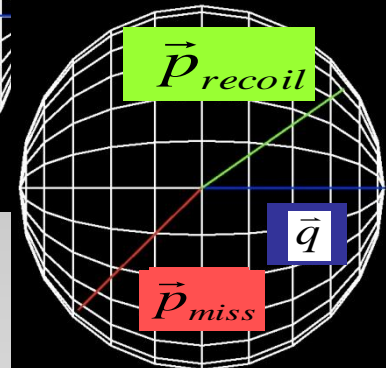
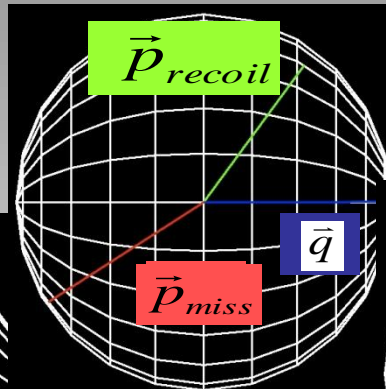
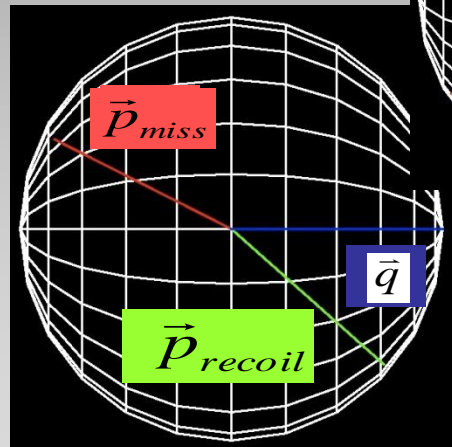
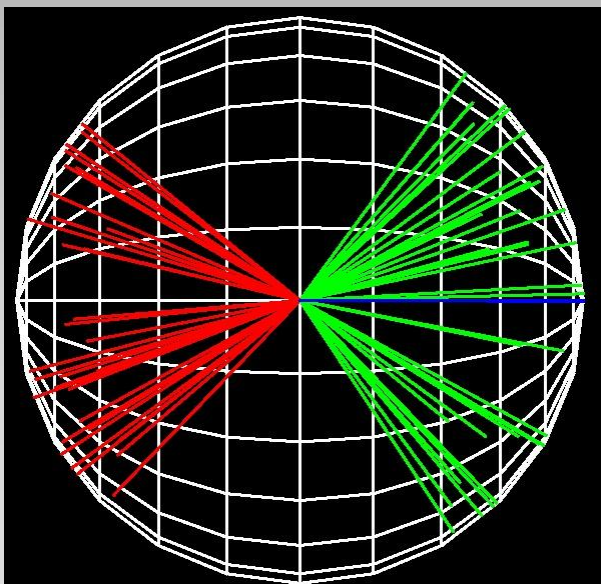
# $F_e(e, e'pp)$

$\vec{P}_{miss}$   
from  $(e, e'p)$



$\vec{P}_{recoil}$

# $P_b(e, e'pp)$



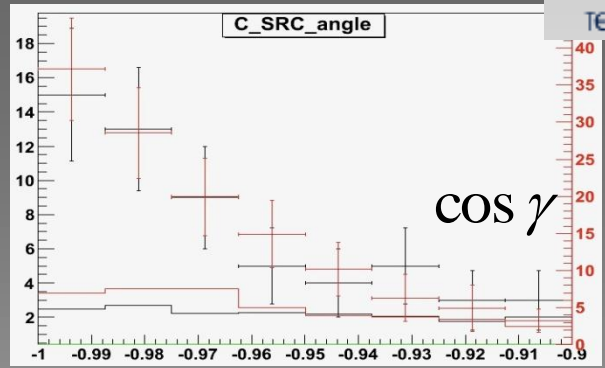
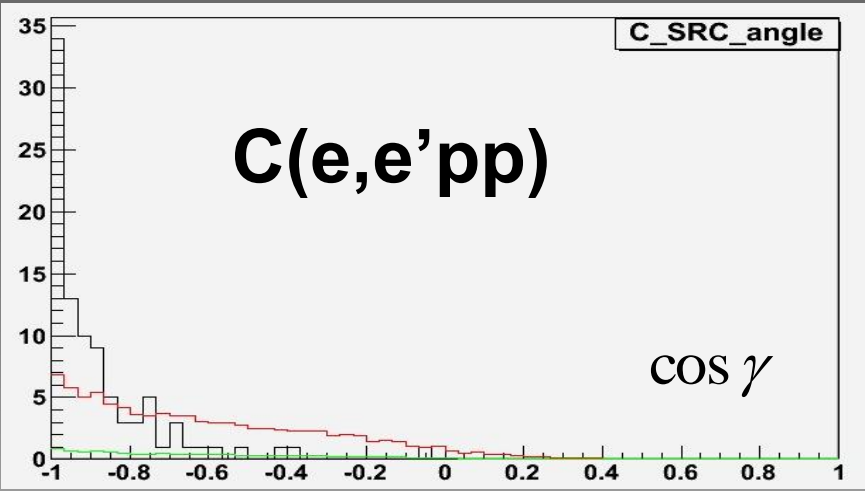
$E_{in} = 5.014 \text{ GeV}$

$Q^2 = 2 \text{ GeV}/c^2 \quad X > 1.2$



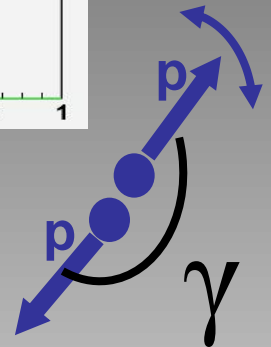


# Directional correlation

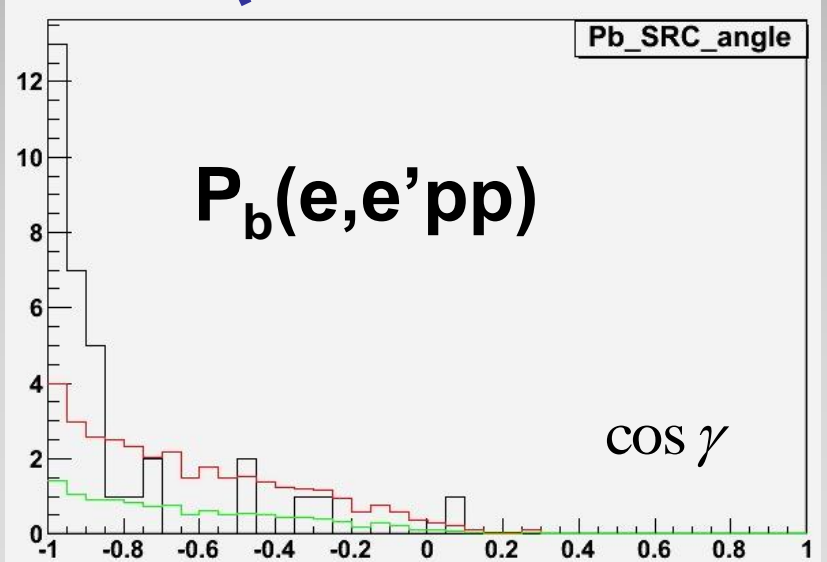
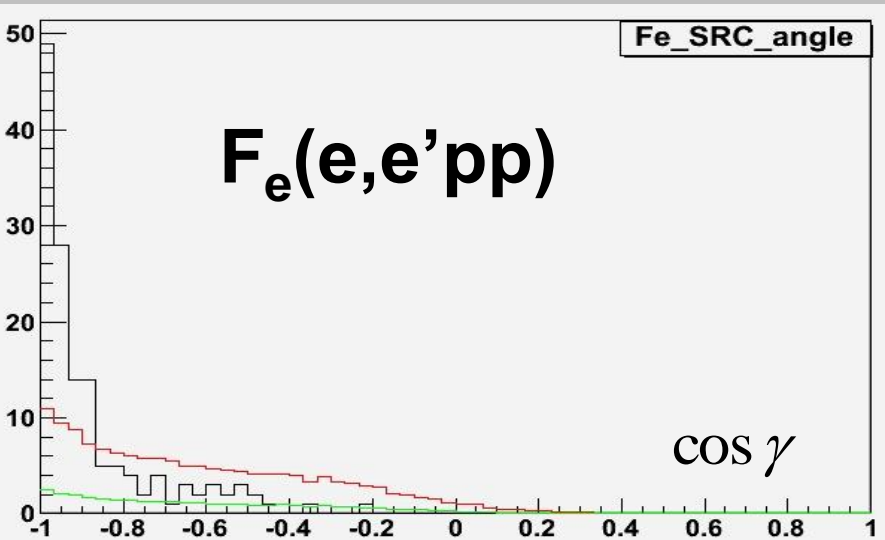


Hall A data PRL 99(2007)072501  
Hall B

JLab / CLAS Data Mining,  
EG2 data set, Or Chen et al.

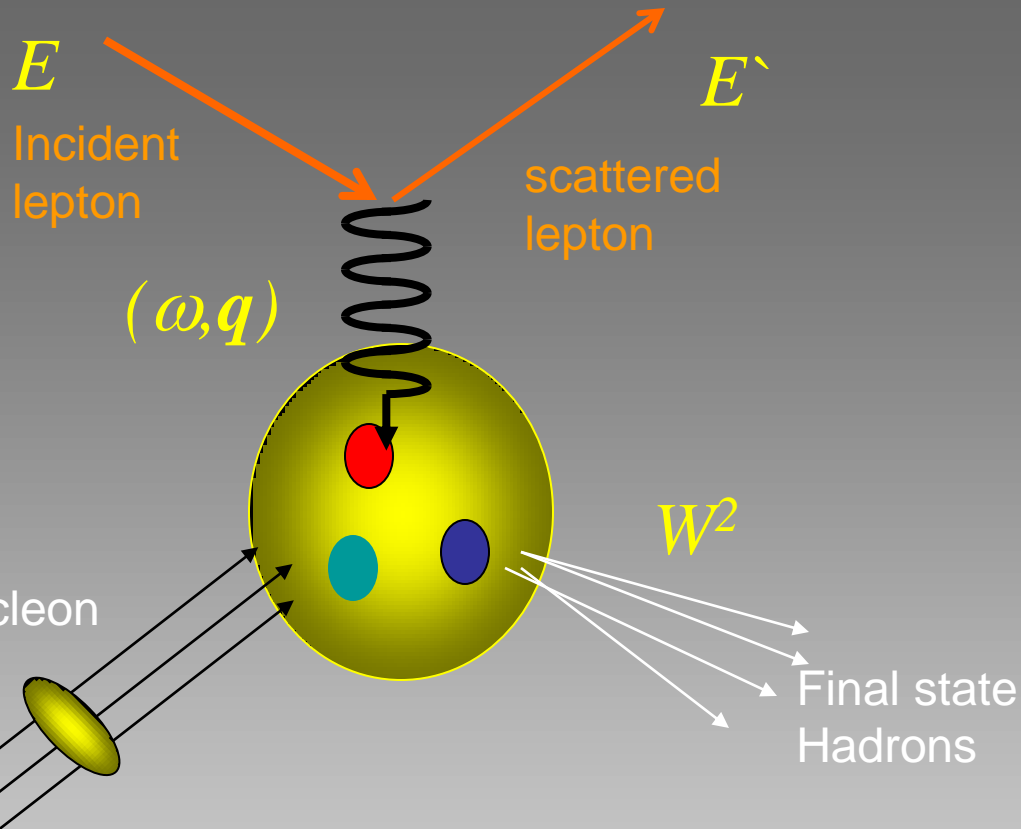


**PRELIMINARY**





# Deep Inelastic Scattering (DIS)



$$Q^2 = -q_\mu q^\mu = q^2 - \omega^2$$

$$\omega = E' - E$$

$$x_B = \frac{Q^2}{2m\omega}$$

**$x_B$  gives the fraction of nucleon momentum carried by the struck parton**

**Information about nucleon vertex is contained in  $F_1(x, Q^2)$  and  $F_2(x, Q^2)$ , the unpolarized structure functions**

Electrons, muons, neutrinos

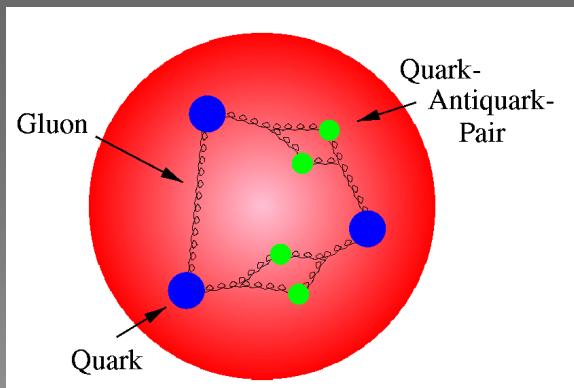
SLAC, CERN, HERA, FNAL, JLAB

$E, E'$  5-500 GeV

$Q^2$  5-50  $\text{GeV}^2$

$w^2 > 4 \text{ GeV}^2$

$0 \leq x_B \leq 1$

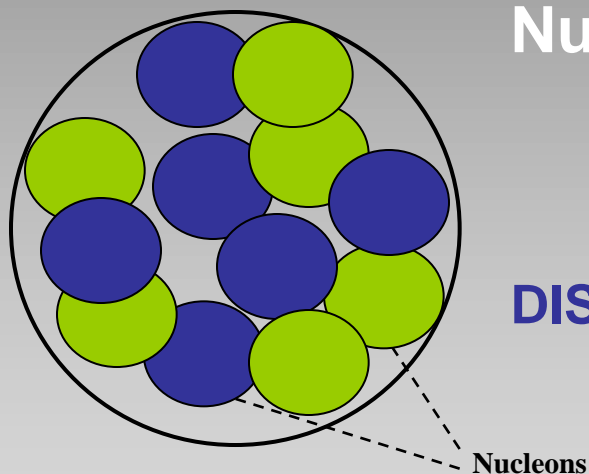


Scale: several tens of GeV

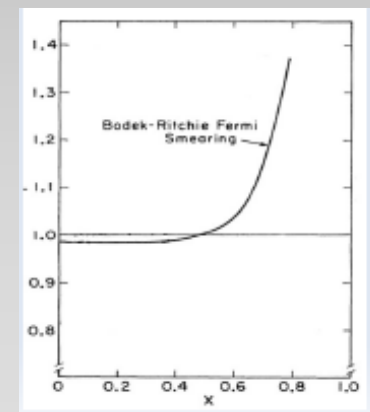
Nucleon in nuclei are bound by  $\sim$ MeV

**Naive expectation :**

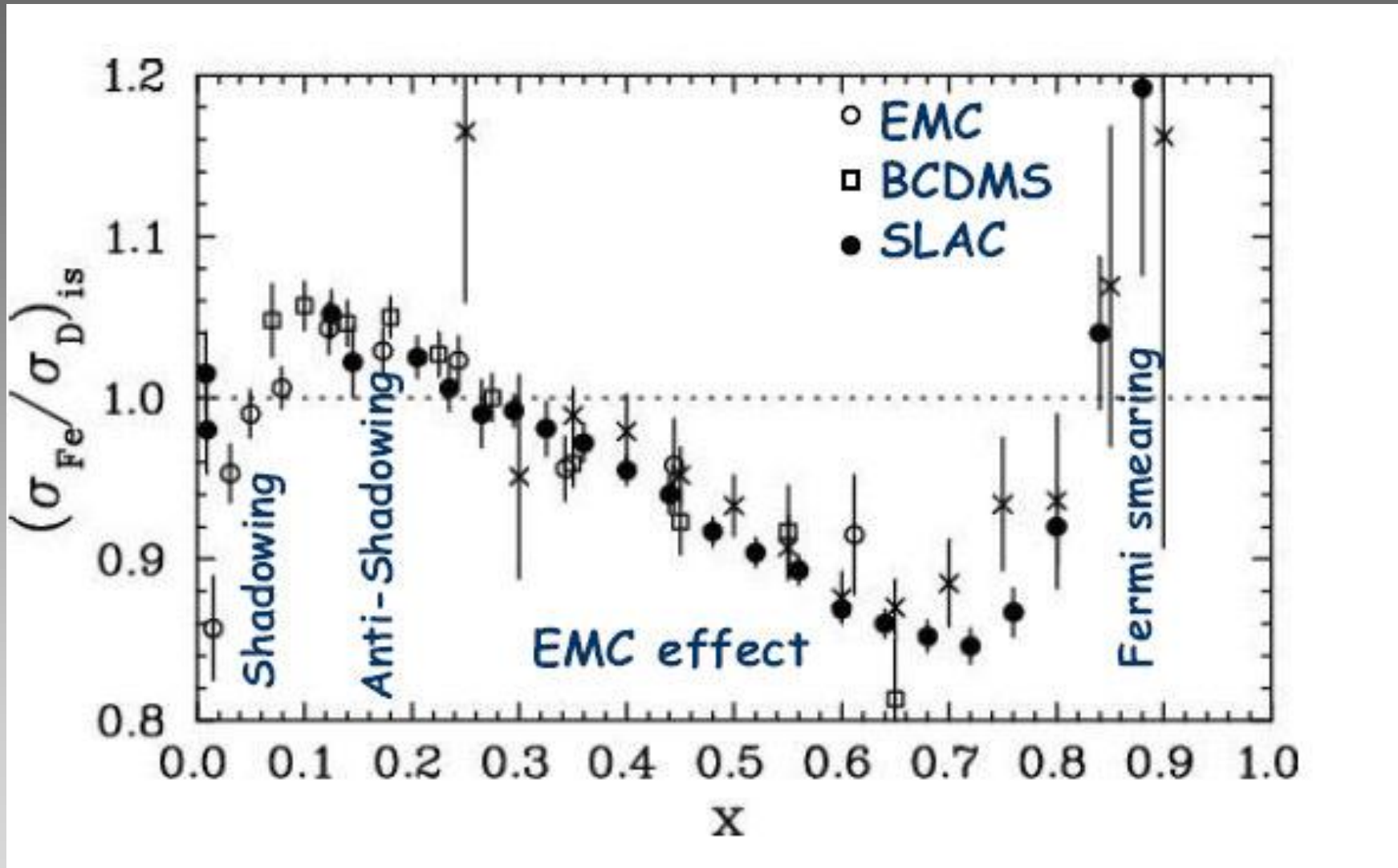
DIS off a bound nucleon  $\equiv$  DIS off a free nucleon



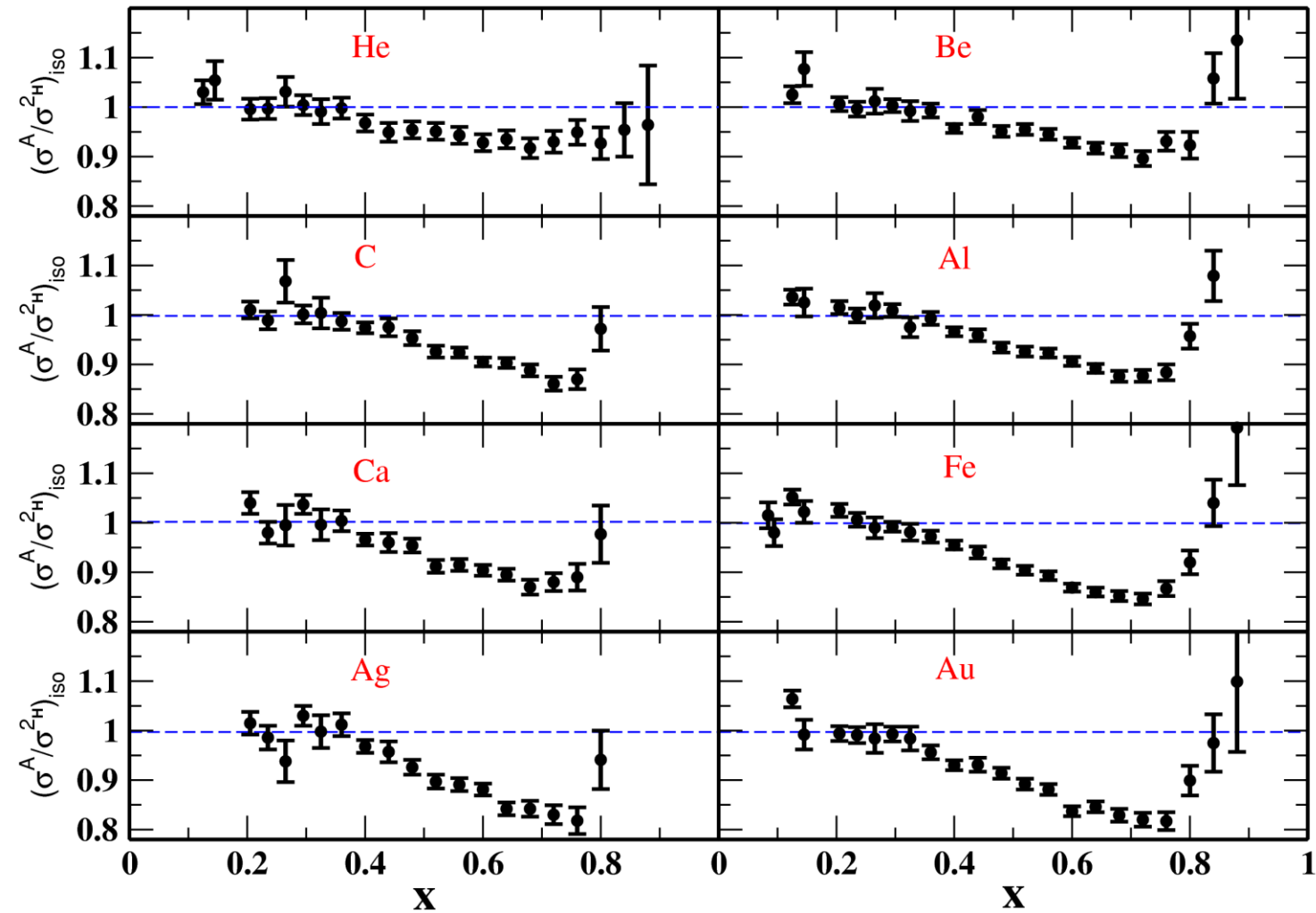
(Except some small Fermi momentum correction)



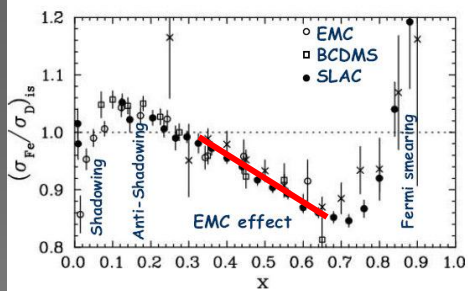
# The European Muon Collaboration (EMC) effect



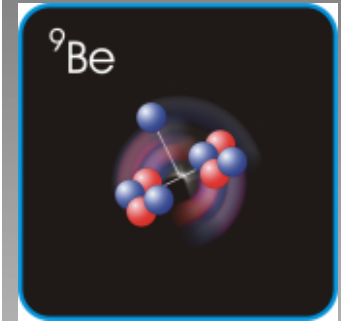
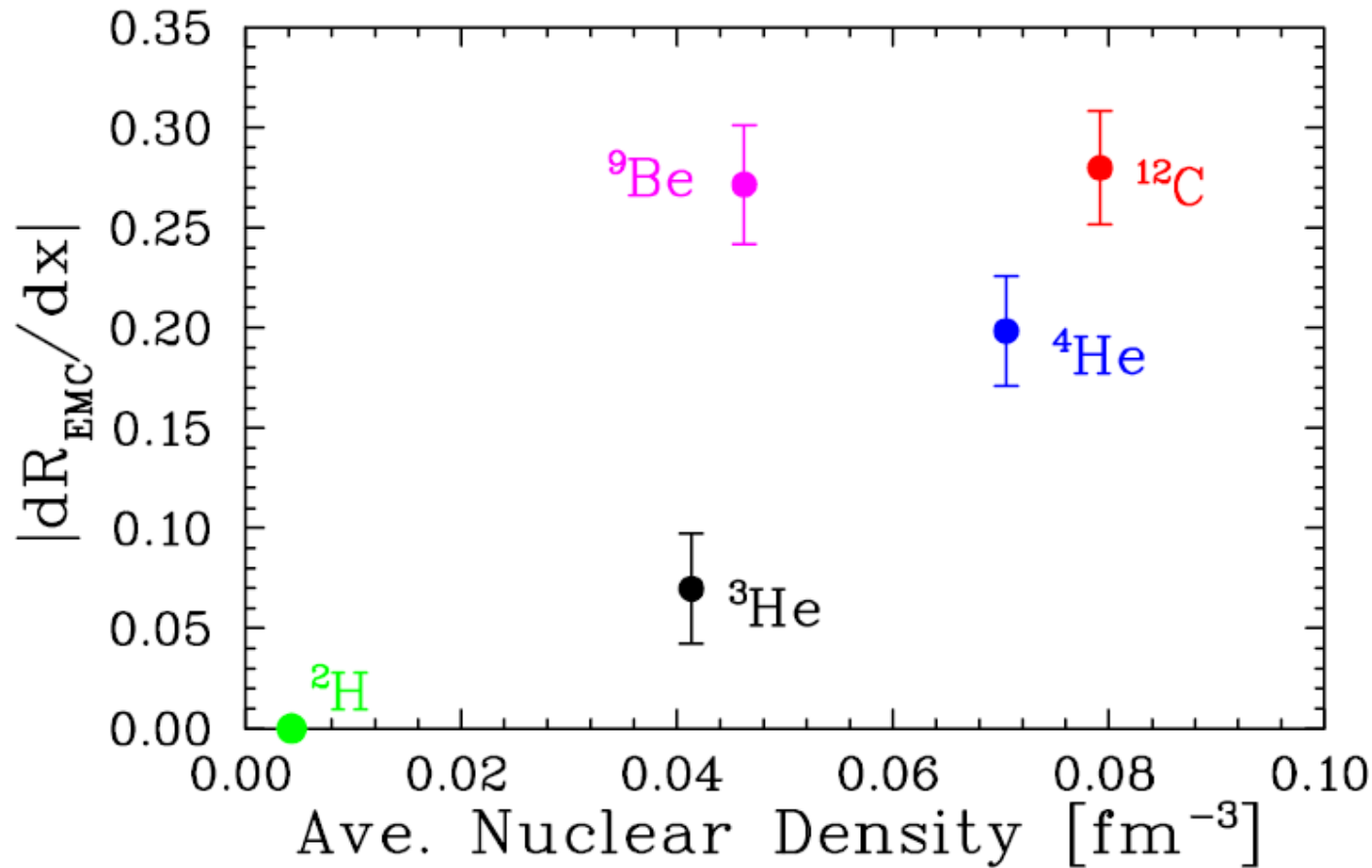
DIS cross section per nucleon in nuclei  $\neq$  DIS off a free nucleon



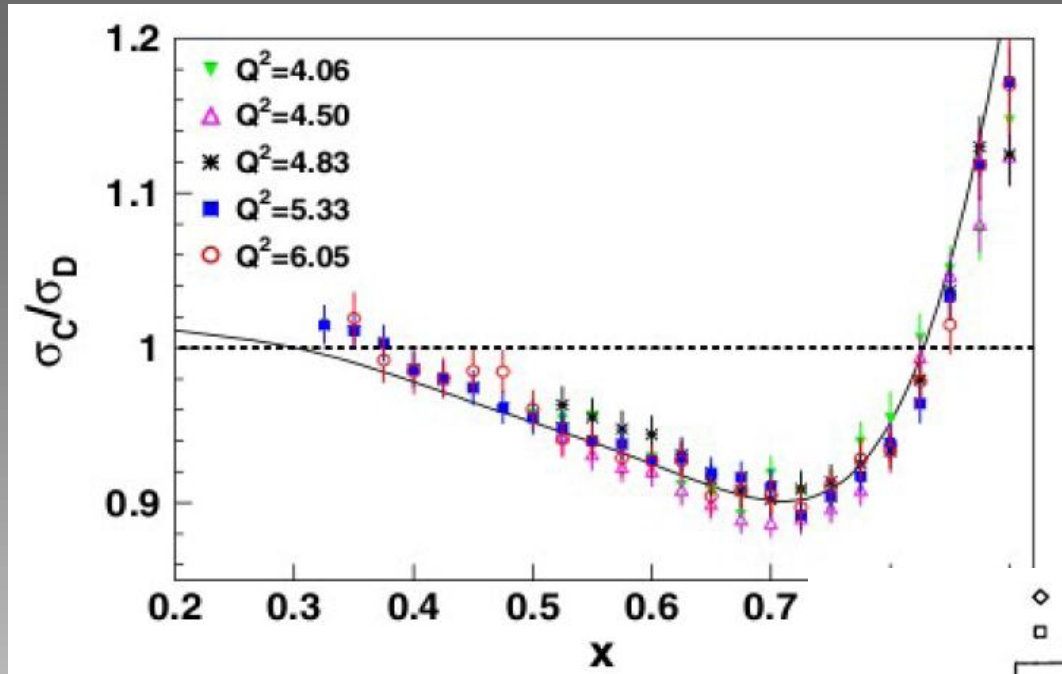
Data from CERN SLAC JLab 1983- 2009



EMC is a **local density or nucleon momentum dependence effect**, not a bulk property of nuclear medium



# Very weak $Q^2$ dependence

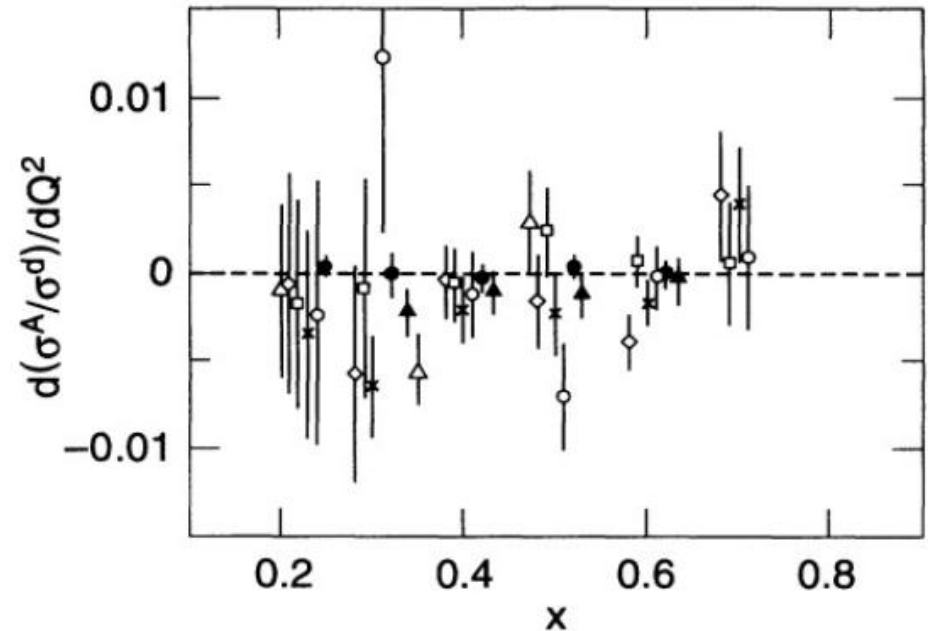


JLab

J. Seely et al.

SLAC

J. Gomez et al.



## Theoretical interpretations: ~1000 of papers

- **Nuclear Effects:** Binding Effects, Pion enhancement, 6-quark clusters, and many more...
- **Modification of the nucleon structure:** dynamical rescaling, Point like configuration suppression, structure function modification in the mean field, and many more...

### EMC recent review papers:

Gessman, Saito, Thomas, Annu. Rev. Nucl. Part. Sci. 45:337(1995).

P.R. Norton Rep Prog. 66 (2003).



## Deep Inelastic Scattering

→ Partonic (quark) Structure of Hadrons

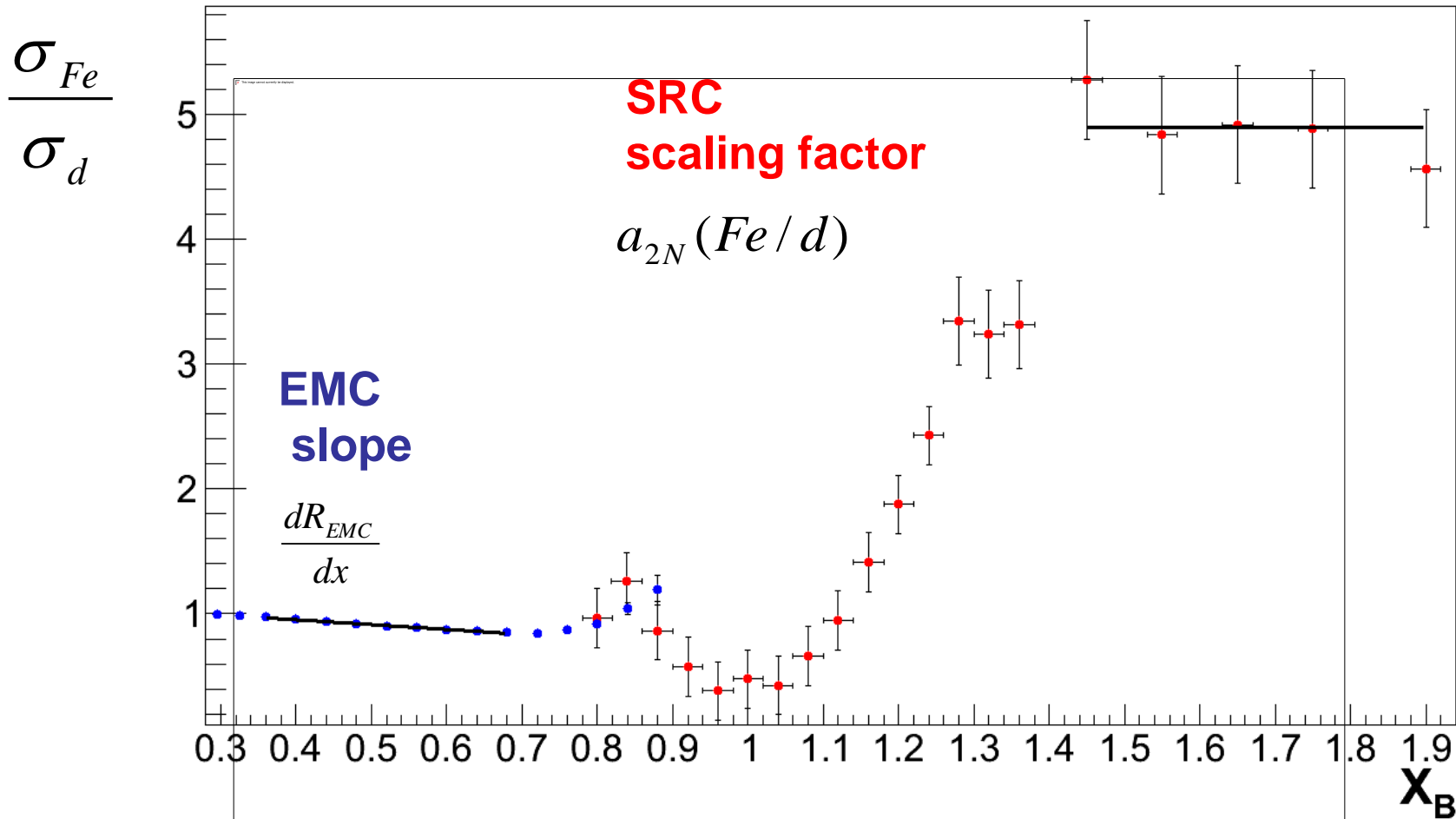
Inclusive Scattering at  $X_B > 1$

$A(e, e')$

→ Partonic (nucleon) Structure of Nucleus



# Comparing the magnitude of the EMC effect and the SRC scaling factors

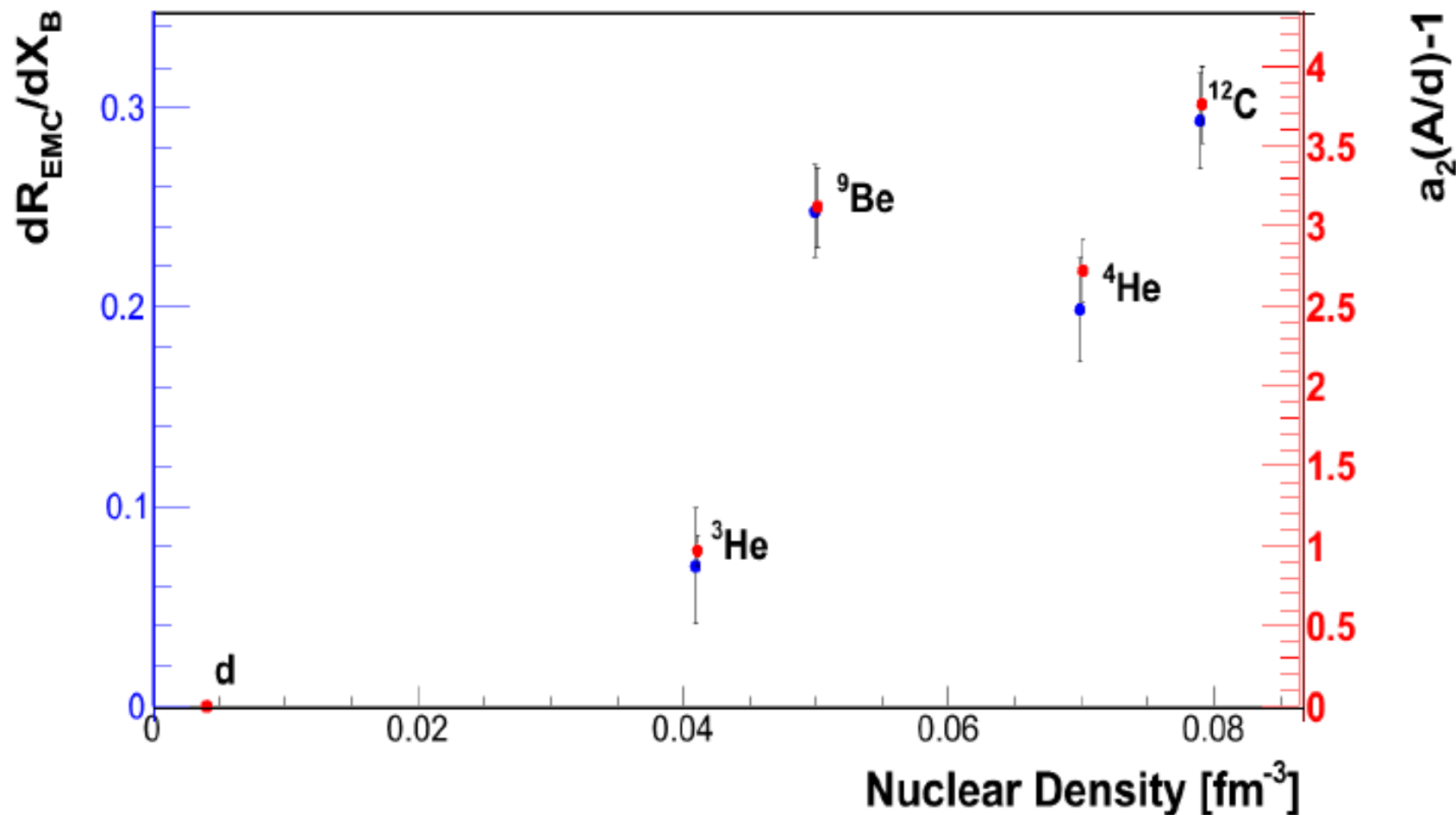


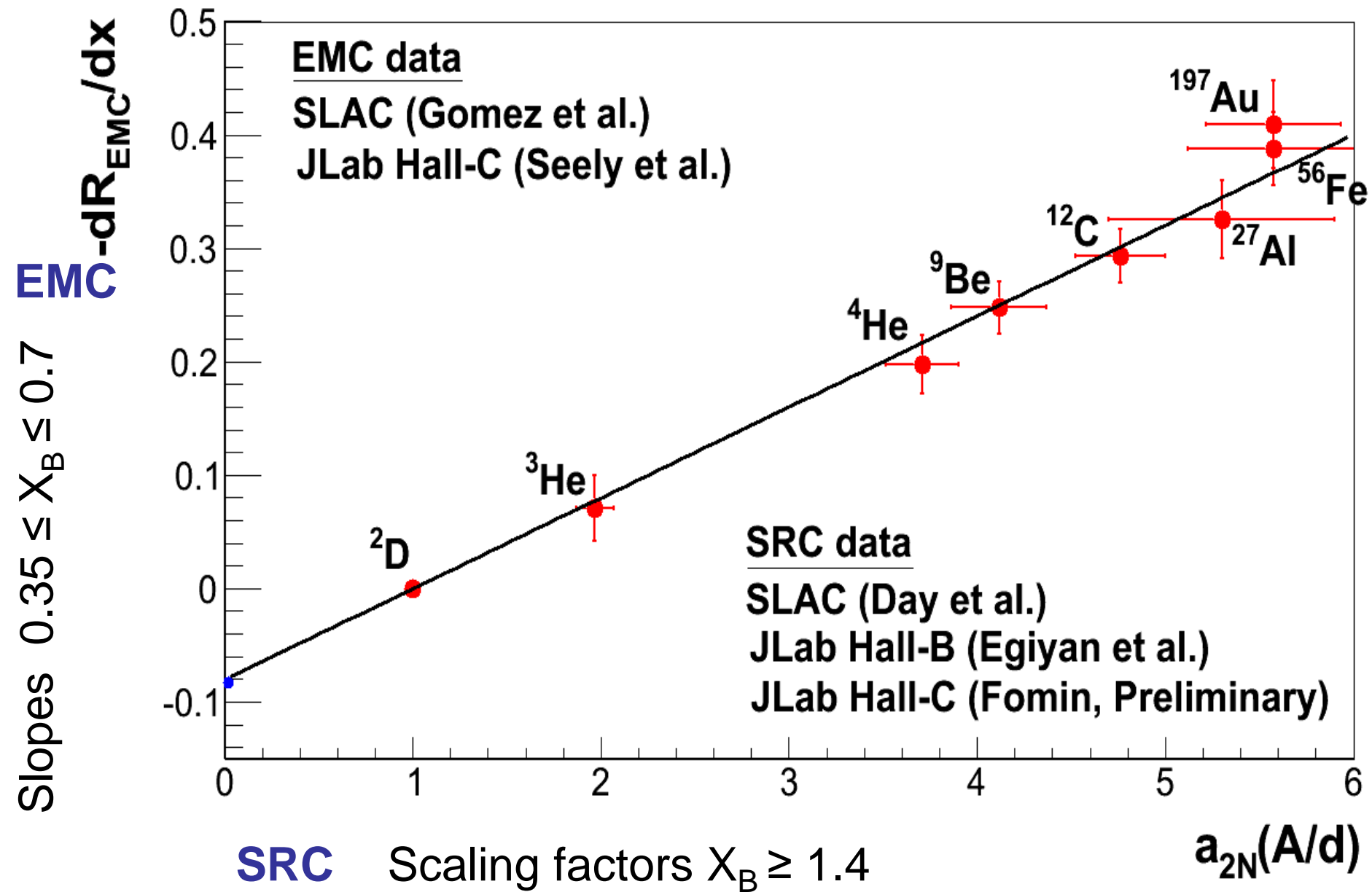
**SLAC data:**

Frankfurt, Strikman, Day, Sargsyan, Phys. Rev. C48 (1993) 2451.  $Q^2=2.3 \text{ GeV}/c^2$

Gomez et al., Phys. Rev. D49, 4348 (1983).

$Q^2=2, 5, 10, 15 \text{ GeV}/c^2$  (averaged)





# Deuteron is not a free np pair

$$\sigma_d \neq \sigma_p + \sigma_n$$

$$\frac{\sigma_d}{\sigma_p + \sigma_n} \approx \frac{\sigma_{^3\text{He}}}{\sigma_d}$$

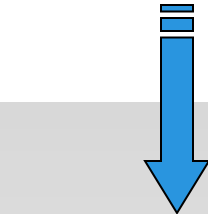
**EMC**

The slopes for  
 $0.35 \leq X_B \leq 0.7$

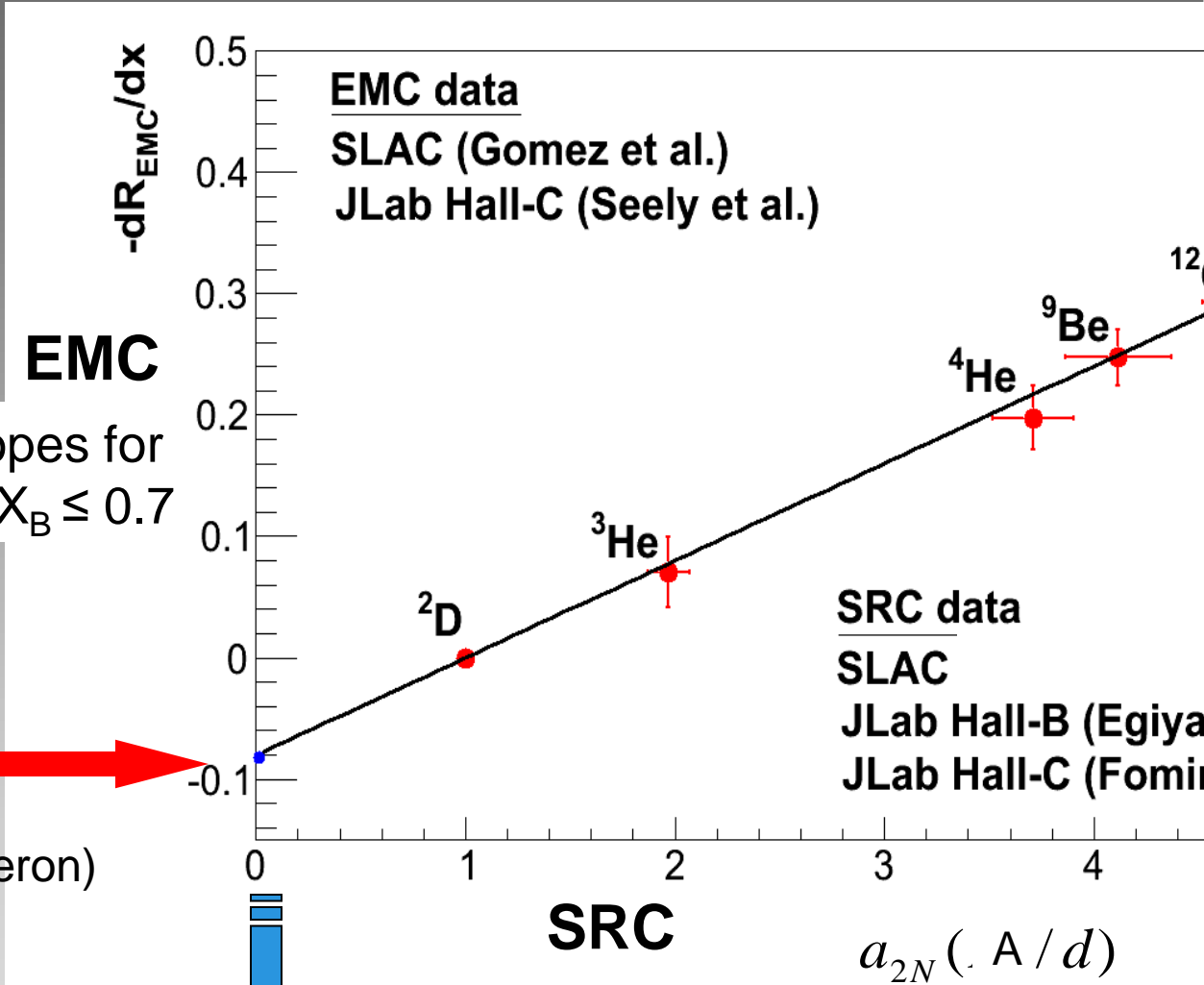
**$0.079 \pm 0.06$**



bound to free n p pairs  
(as opposed to bound to deuteron)



**SRC=0 free nucleons**





# In Medium Correction effect

Due to a lack of a free neutron target the EMC measurements used the deuteron as an approximation to free proton and neutron

**IMC: Ratio of bound to free n p pairs  
(as opposed to bound to deuteron)**

For deuteron:

$$\left| \frac{dR}{dx} \right|_d = 0.078 \pm 0.006$$

For any nuclei:

$$\left| \frac{dR}{dx} \right|_A = \left| \frac{dR}{dx} \right|_{measured} + (0.078 \pm 0.006)$$



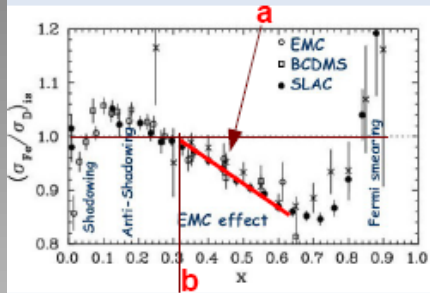
# Virtual free neutron target



# The free neutron DIS cross section

- Assuming linear dependence for  $0.3 < X_B < 0.7$ :

$$\frac{\sigma_d}{\sigma_n + \sigma_p} = 1 - a(X_B - b)$$



$$a = \left| \frac{dR_{EMC}}{dX_B} \right| = 0.079 \pm 0.006$$

$$b = 0.31 \pm 0.04 \rightarrow \text{the intersect of EMC ratio} = 1$$

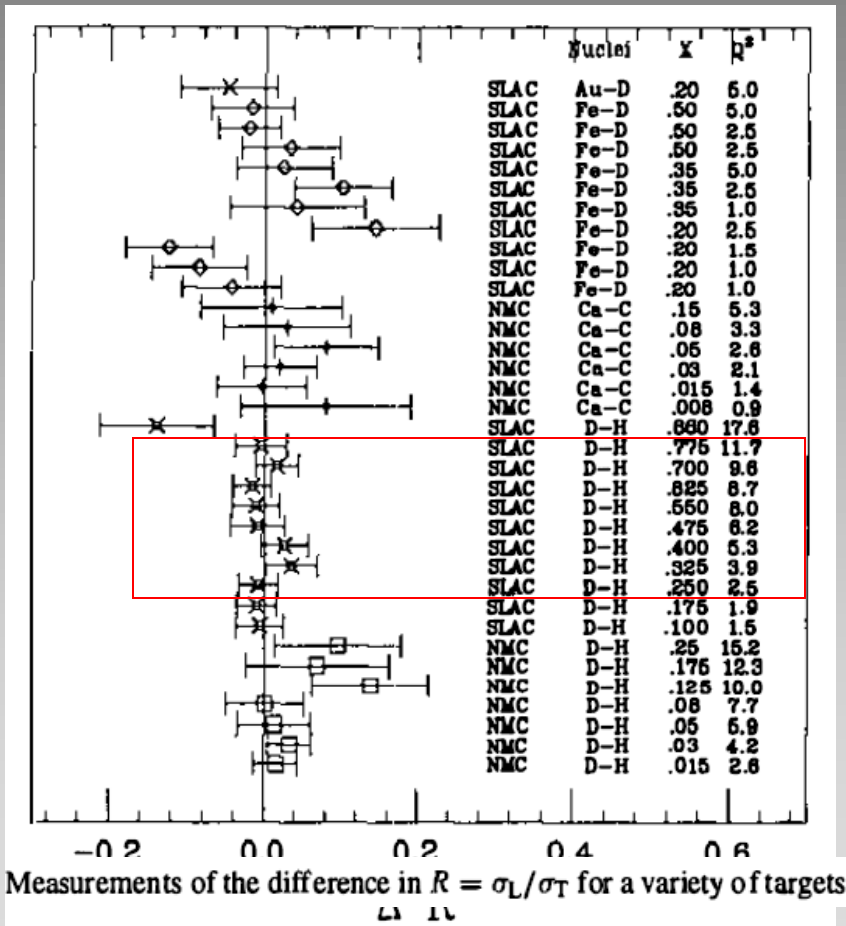
$$\sigma_n = \frac{\sigma_d}{1 - a(X_B - b)} - \sigma_p$$

$$\frac{\sigma_n}{\sigma_p} = \frac{\sigma_d / \sigma_p}{1 - a(X_B - b)} - 1$$



$$F_2 = 2 \cdot x \cdot F_1 \cdot \frac{1 + R}{1 + 2 \cdot M \cdot \omega}$$

Where  $R = \sigma_L / \sigma_T$  is the ratio of cross sections for absorbing a longitudinal to that for a transverse photon.



Assuming that  $R = \sigma_L / \sigma_T$  is the same for n, p, d, the cross section ratio equals the structure function ratio:

$$\frac{F_2^n(X_B, Q^2)}{F_2^p(X_B, Q^2)} = \frac{2F_2^d(X_B, Q^2) / F_2^p(X_B, Q^2)}{1 - a(X_B - b)} - 1$$



# The **free** neutron structure function

$$\frac{F_2^n(x_B, Q^2)}{F_2^p(x_B, Q^2)} = \frac{2F_2^d(x_B, Q^2)/F_2^p(x_B, Q^2) - [1 - a(x_B - b)]}{[1 - a(x_B - b)]}$$

For  $0.35 \leq X_B \leq 0.7$

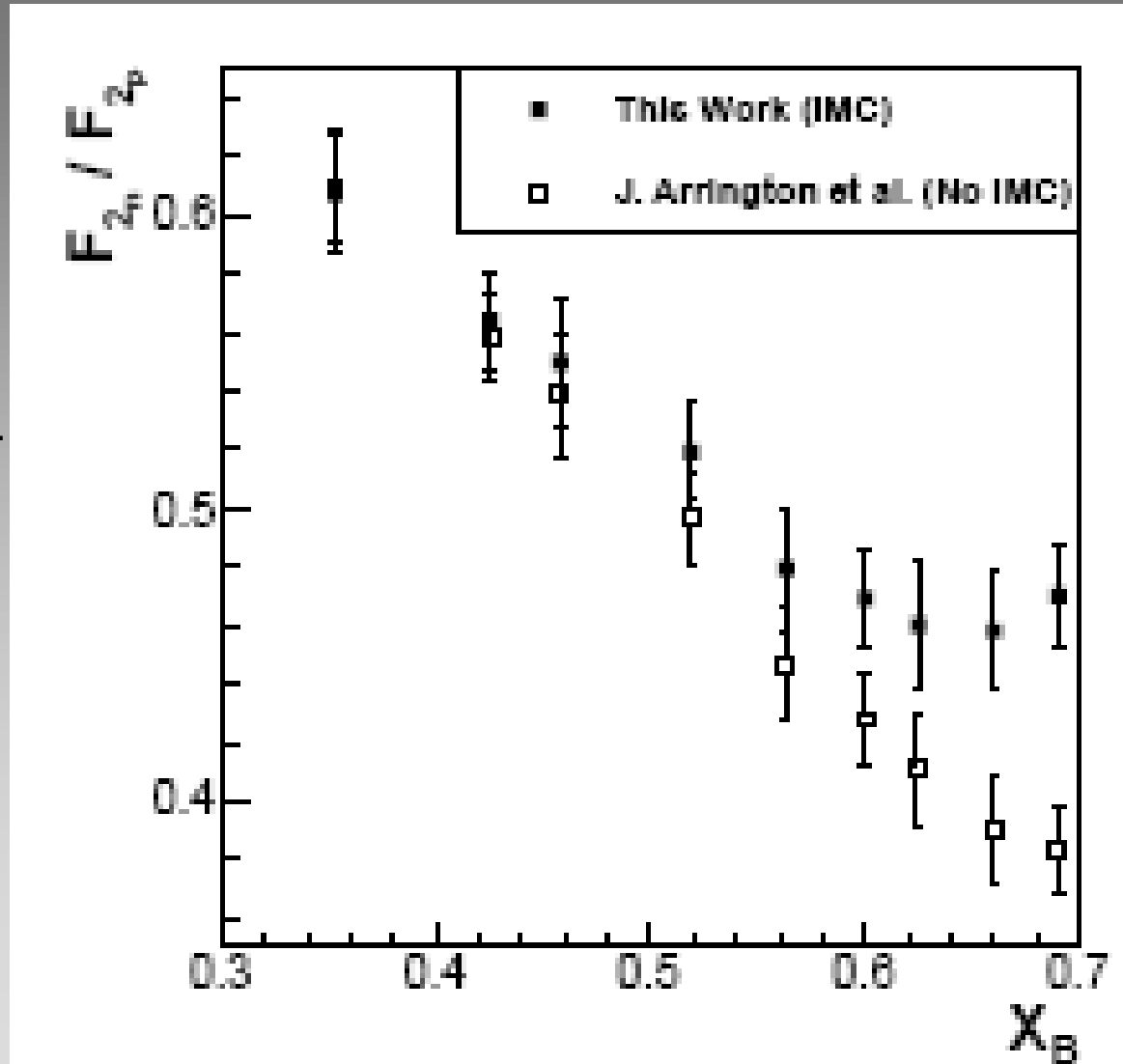
$$\frac{\sigma_d}{\sigma_p + \sigma_n} = 1 - a(x_B - b)$$

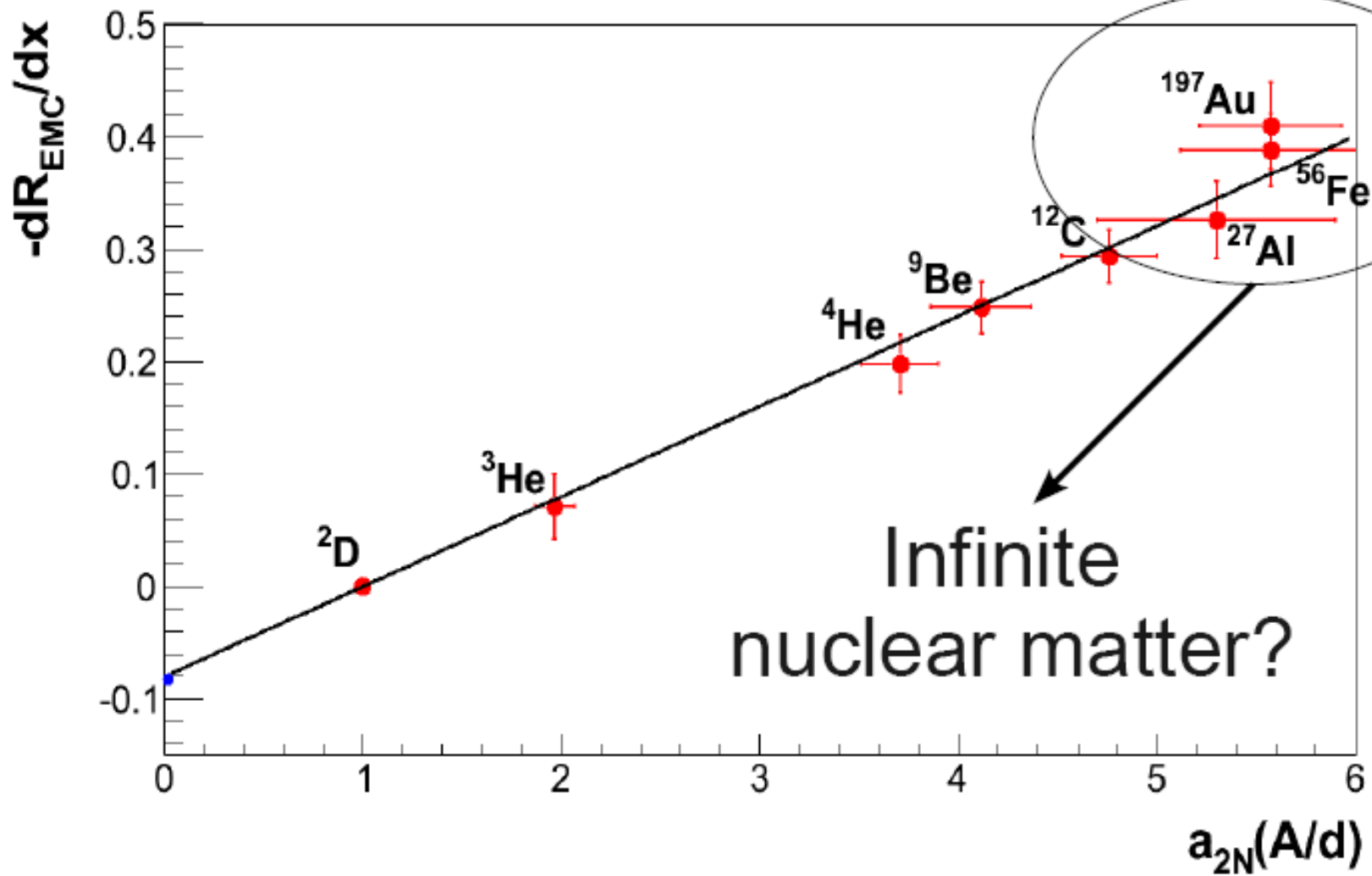
□ SLAC Data, J. Arrington et al. JPG 36(2009)205005.

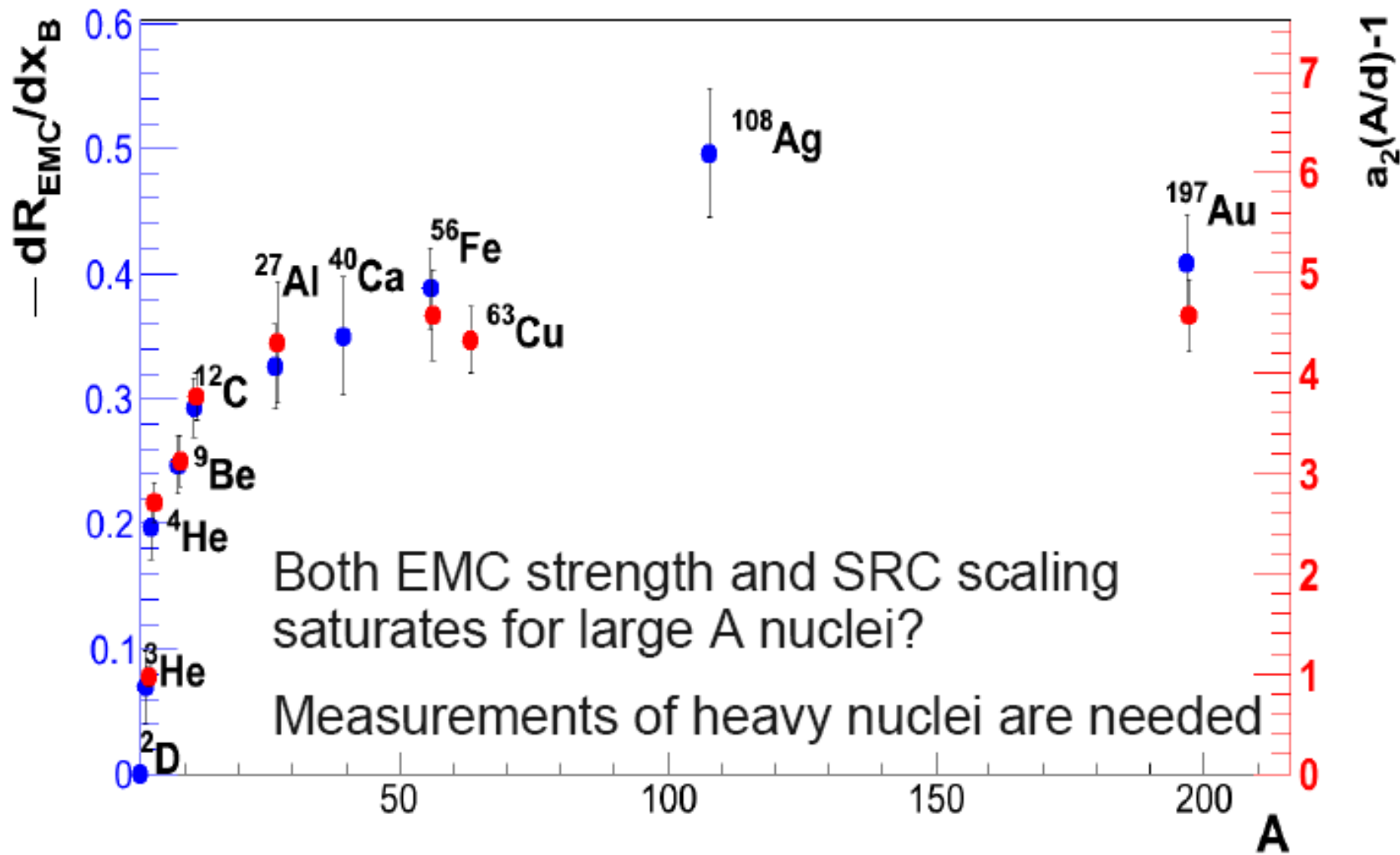
Fermi smearing using relativistic deuteron momentum density

■ Extracted from this work

With medium correction

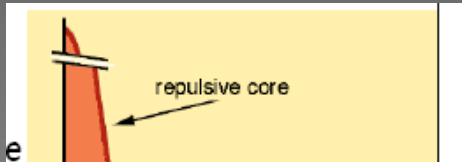






Need more data on heavy nuclei to study the A dependence for large A

# Where is the EMC effect ?



## Possible explanation for EMC / SRC correlation

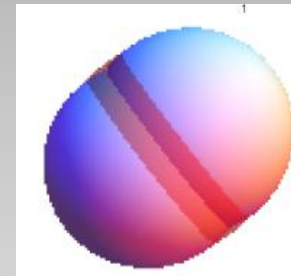
- The EMC effect is related to high momentum nucleons in the nucleus

20% nucleons  
(80% kinetic energy)

pp

nn

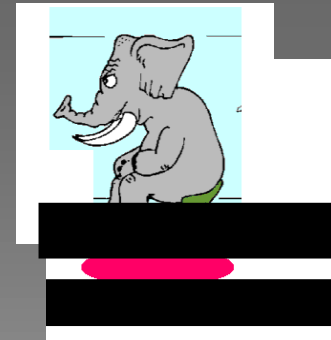
Nuclei are optimized to yield the strongest EMC effect possible



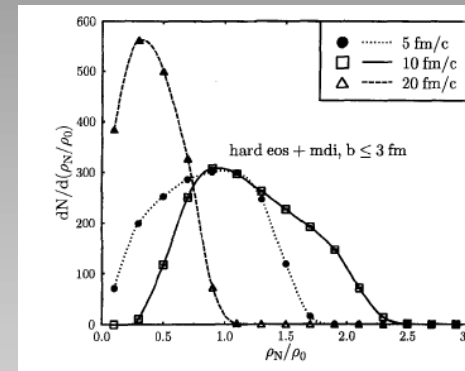
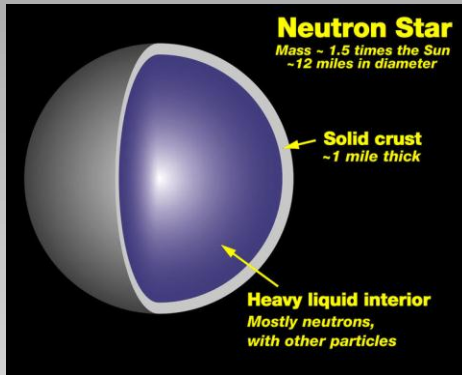
OR

High local nuclear matter density,  
large momentum, large off shell.  
large virtuality ( $v = p^2 - m^2$ )

# How large is EMC effect in dense nuclear systems?



# What are the consequences of a large EMC in these systems?



**Nucleon and baryon densities in heavy ion collisions at 1 GeV/nucleon**  
 S.A. Bass<sup>1,2</sup>, C. Hartnack<sup>2,3</sup>, H. Stöcker<sup>1</sup>, W. Greiner<sup>1</sup> Z. Phys. A 351, 359–360 (1995)

n stars

Central HI collisions

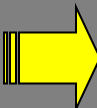


# Summary I

Standard model for short distance structure of nuclei

1 The probability for a nucleon to have momentum  $\geq 300$  MeV / c in medium nuclei is  $\sim 25\%$

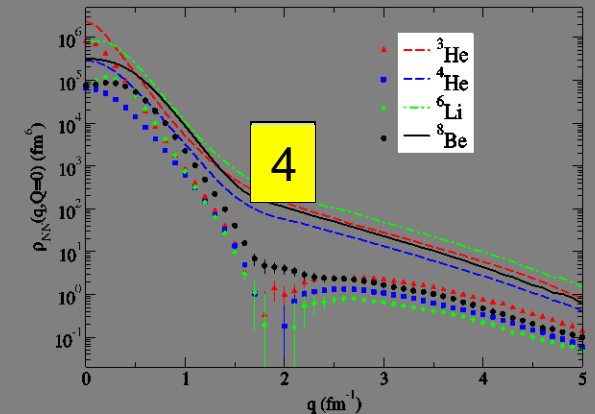
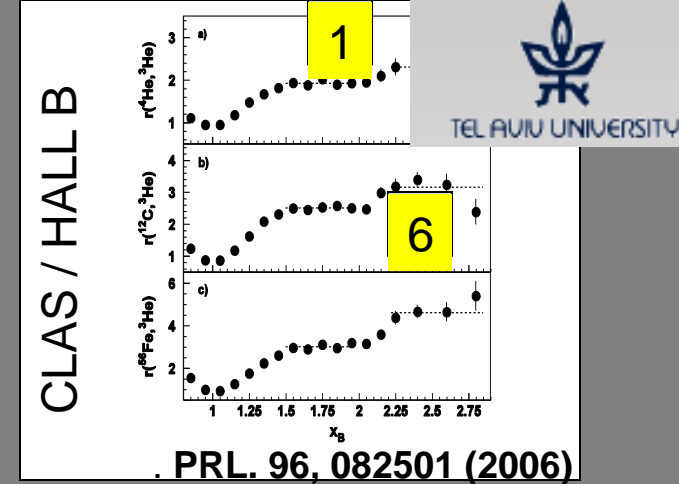
2 More than  $\sim 90\%$  of all nucleons with momentum  $\geq 300$  MeV / c belong to 2N-SRC.

1   $\sim 80\%$  of kinetic energy of nucleon in nuclei is carried by nucleons in 2N-SRC.

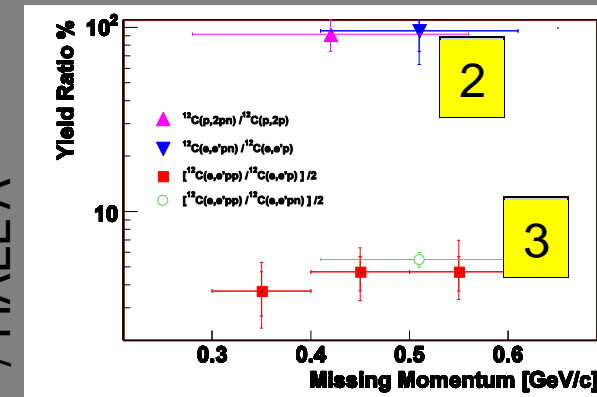
3 Probability for a nucleon with momentum 300-600 MeV / c to belong to np-SRC is  $\sim 18$  times larger than to belong to pp-SRC.

4 Dominant NN force in the 2N-SRC is tensor force.

6 Three nucleon SRC are present in nuclei.

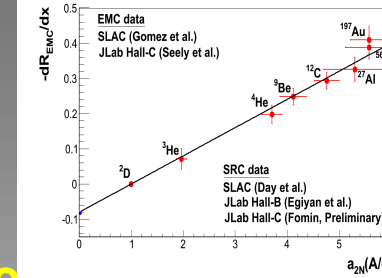
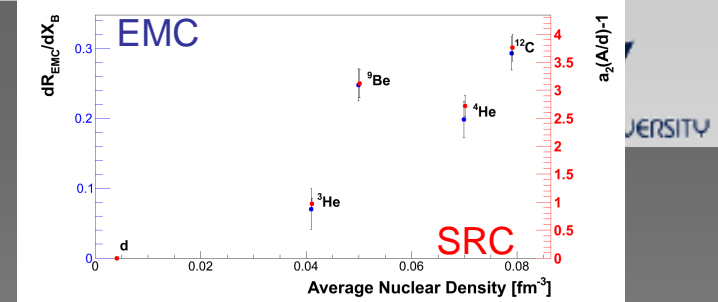


EVA / BNL and Jlab / HALL A



# Summary II

- ★ The EMC is a local density and / or momentum dependent effect not a bulk property of the nuclear medium.
- ★ The magnitude of the EMC effect and SRC scaling factor are linearly related.
- ★ We speculate that observed correlation arises because both EMC and SRC are dominated by high momentum (large virtuality) nucleons in nuclei.



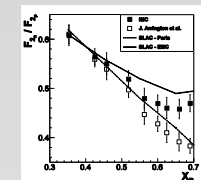
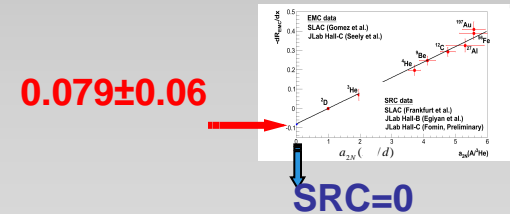
The observed phenomenological relationship is used to extract:

( For  $0.35 < X_B < 0.7$  )

ratio of deuteron to free n p pair cross sections.

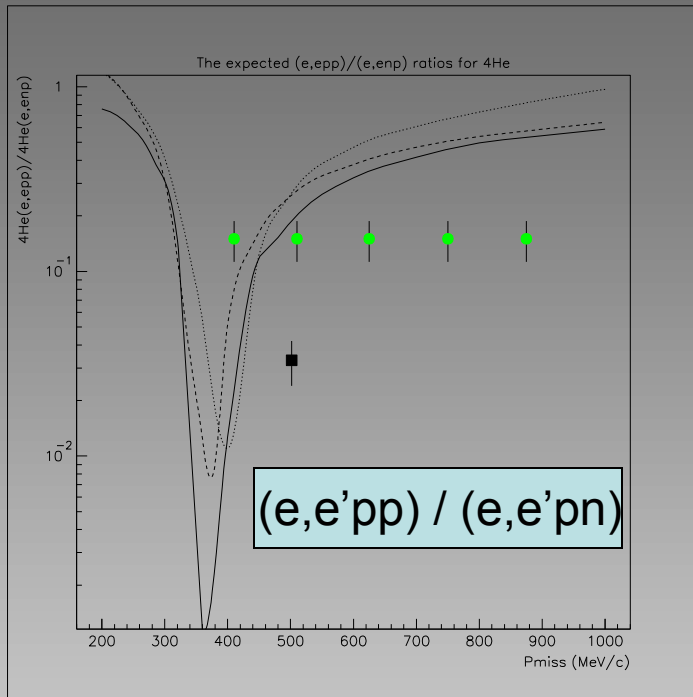
DIS cross section for a free neutron.

$F_2^n(x, Q^2)$ , the free neutron structure function.



# A new experiment scheduled to run 2011 at JLab (E 07-006)

Measurement over missing momentum range from 400 to 875 MeV/c.



QMC

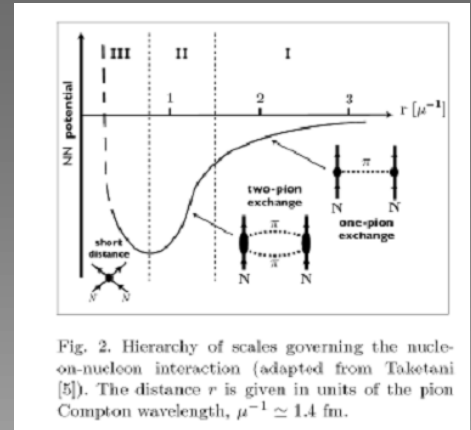
(Thomas)

Taketani, Nakamura, Saaki  
Prog. Theor. Phys. 6 (1951) 581.

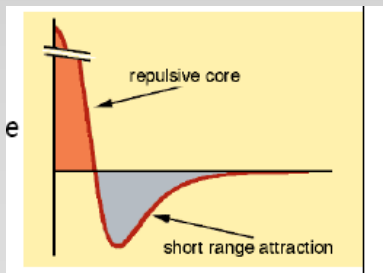
Chiral effective field

(Machleidt)

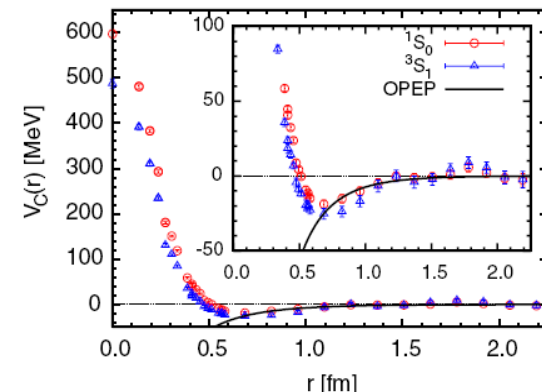
Lattice QCD  
(Doi, Beane)



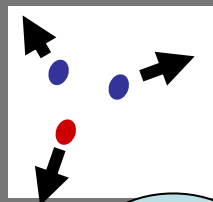
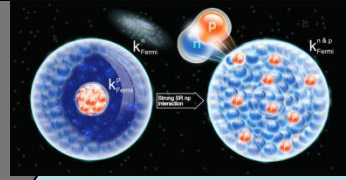
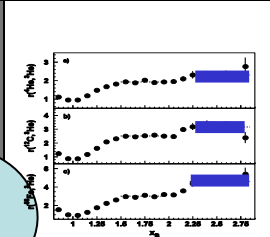
The data are expected to be sensitive to the **NN tensor force** and the **NN short range repulsive force**.



	2N	3N	4N
$\mathcal{O}\left(\frac{Q^0}{\Lambda^0}\right)$	X H	-	-
$\mathcal{O}\left(\frac{Q^2}{\Lambda^2}\right)$	X H H H	-	-
$\mathcal{O}\left(\frac{Q^3}{\Lambda^3}\right)$	X H H H	H H H H	-
$\mathcal{O}\left(\frac{Q^4}{\Lambda^4}\right)$	X H H H H H	H H H H H H	H H H H



# outlook

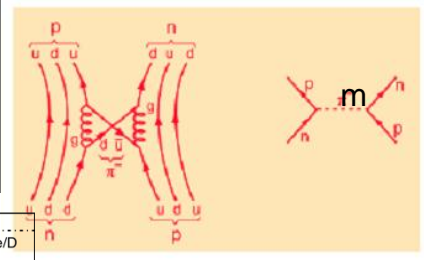


What is the role played by short range correlation of more than two nucleons ?

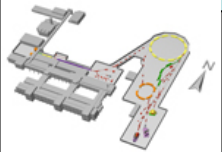
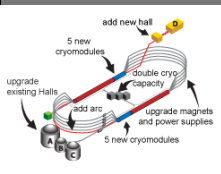
How to relate what we learned about SRC in nuclei to the dynamics of neutron star formation and structure ?



What is the role played by non nucleonic degrees of freedom in SRC ?

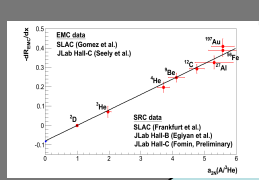
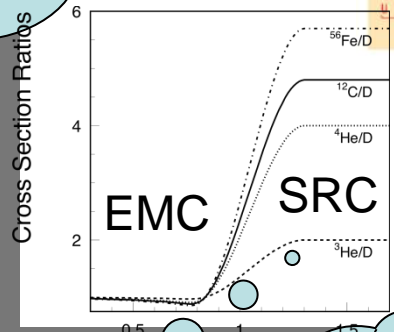


12 GeV JLab

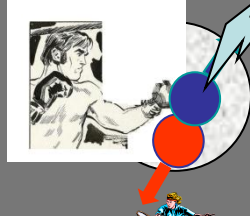
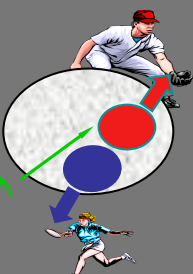


The new facilities will allow even harder knockout reactions

GSI



QE



DIS

What are the observables ?

Optimized kinematics ?

Is theory well enough established to interpret the data ?





INTERNATIONAL  
CENTRE for  
THEORETICAL  
SCIENCES

TATA INSTITUTE OF FUNDAMENTAL RESEARCH

## N-N Interaction & the Nuclear Many-Body Problem

November 18-27, 2010



TEL AVIV UNIVERSITY



**I would like to thank the organizers for the invitation**



# E01-015: A customized Experiment to study 2N-SRC

$$Q^2 = 2 \text{ GeV}/c, \quad x_B \sim 1.2, \quad P_m = 300-600 \text{ MeV}/c, \quad E_{2m} < 140 \text{ MeV}$$

$$\text{Luminosity} \sim 10^{37-38} \text{ cm}^{-2}\text{s}^{-1}$$

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### High energy, Large $Q^2$

The large  $Q^2$  is required to probe the small size SRC configuration.

MEC are reduced as  $1/Q^2$ .

Large  $Q^2$  is required to probe high  $P_{\text{miss}}$  with  $x_B > 1$ .

FSI can be treated in Glauber approximation.

### $x_B > 1$

Reduced contribution from isobar currents.

### Large $p_{\text{miss}}$ and $E_{\text{miss}} \sim p_{\text{miss}}^2/2M$

### Large $P_{\text{miss}_z}$



## FSI

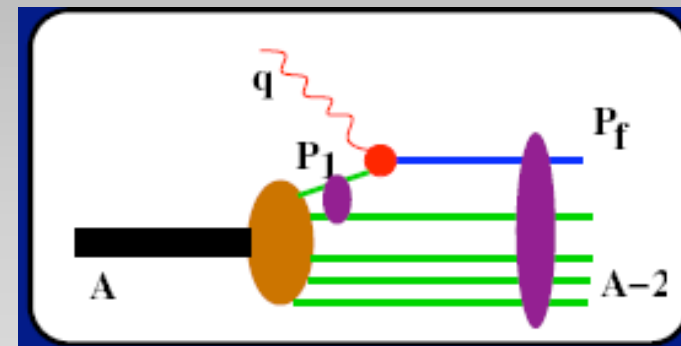
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  - Pauli blocking for the recoil particle.
  - Geometry,  $(e, e'p)$  selects the surface.
- ★ Can be treated in Glauber approximation.
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### FSI in the SRC pair:

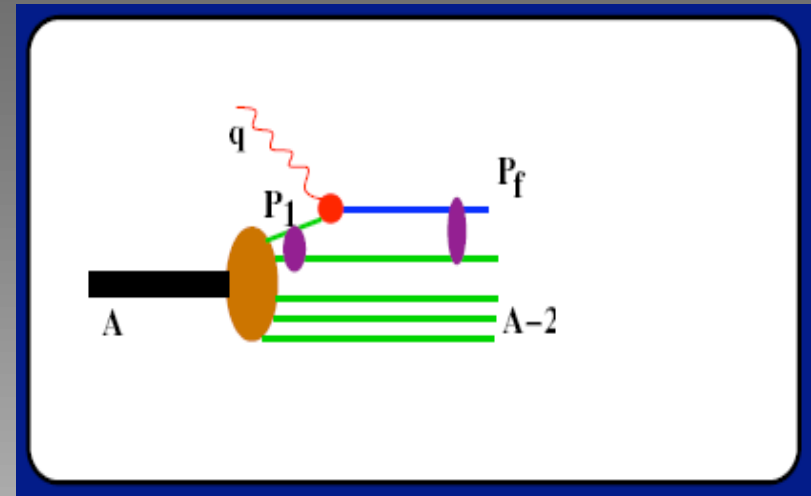
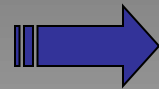
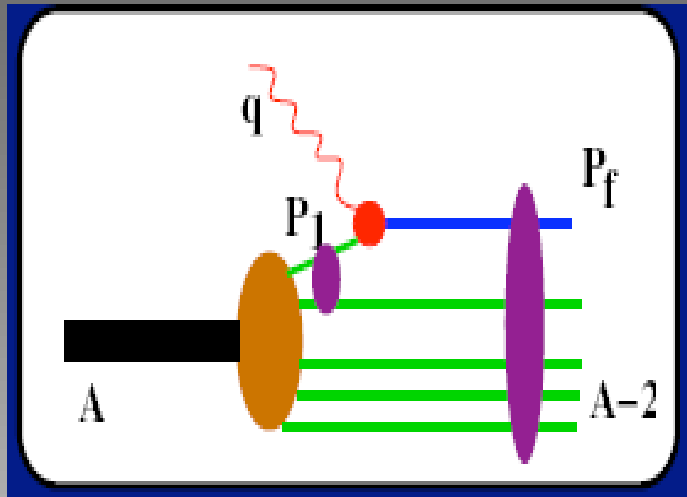
These are not necessarily small, BUT:

- ★ Conserve the isospin structure of the pair .
- ★ Conserve the CM momentum of the pair.



# Why FSI do not destroy the 2N-SRC signature ?

For large  $Q^2$  and  $x > 1$  FSI is confined within the SRC



distances that highly virtual struck nucleon propagates

$$\Delta E = -q_0 - M_A + \sqrt{m^2 + (p_i + q)^2} + \sqrt{M_{A-1}^2 + p_i^2}$$

$$r \approx \frac{1}{\Delta E v} \leq 1 \text{ fm}$$

for  $x > 1.3$

FSI in the SRC pair:



Conserve the isospin structure of the pair .

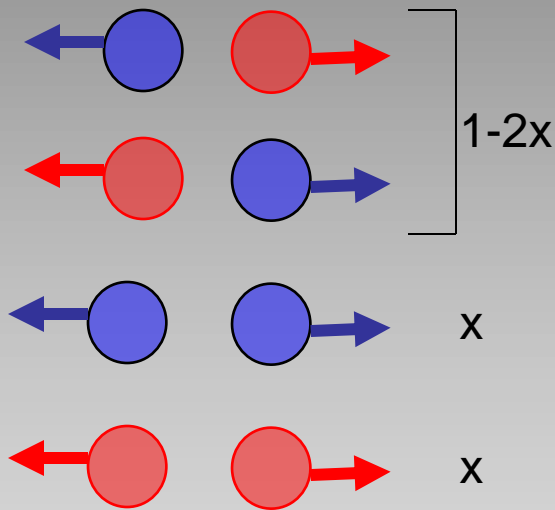


Conserve the CM momentum of the pair.



$$\frac{(e, e' pp)}{(e, e' p)} = 9.5 \pm 2\% \quad \Rightarrow \quad \frac{\text{pp-SRC}}{2N - \text{SRC}} = 4.75 \pm 1\%$$

Assuming in  $^{12}\text{C}$  nn-SRC = pp-SRC and 2N-SRC=100%



A virtual photon with  $x_B > 1$   
“sees” all the pp pairs but  
only 50% of the np pairs.

$$\frac{(e, e' pp)}{(e, e' p)} = \frac{x}{x + (1 - 2x)/2} = 2x$$

$$BNL \quad \frac{(p,2pn)}{(p,2p)} = \frac{np - SRC}{np - SRC + 2(pp - SRC)} = \frac{np - SRC}{2N - SRC} = (74-100) \%$$

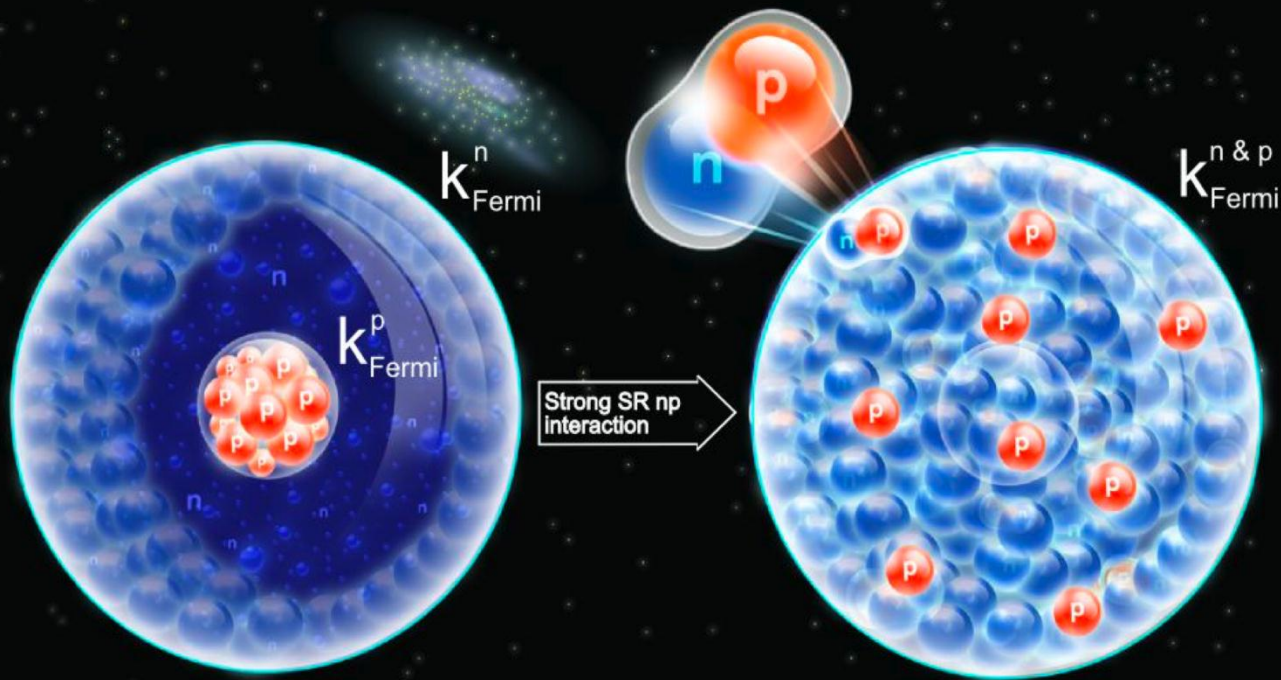
$$Jlab \quad \frac{(e,e'pn)}{(e,e'p)} = \frac{np - SRC}{2N - SRC} = (84 - 100)\%$$

$$Jlab \quad \frac{(e,e'pp)}{(e,e'p)} = (9.5 \pm 2) \% \quad \text{i.e.} \quad \frac{pp - SRC}{2N - SRC} = \frac{nn - SRC}{2N - SRC} = (5 \pm 1)\%$$



$$\frac{np - SRC}{2N - SRC} = (84 - 92)\%$$

# Implications for Neutron Stars



Adapted from: D.Higinbotham,  
E. Piassetzky, M. Strikman  
CERN Courier 49N1 (2009) 22

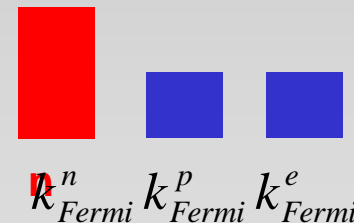
• At the core of neutron stars, most accepted models assume :

~95% neutrons, ~5% protons and ~5% electrons ( $\beta$ -stability).

• Neglecting the np-SRC interactions, one can assume three separate Fermi gases (n p and e).

• strong np interaction

the n-gas heats the p-gas.



See estimates in Frankfurt and Strikman : [Int.J.Mod.Phys.A23:2991-3055,2008.](#)

# SRC in nuclei: implication for neutron stars



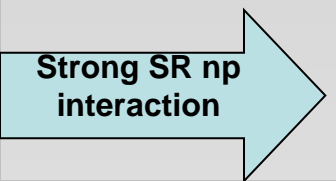
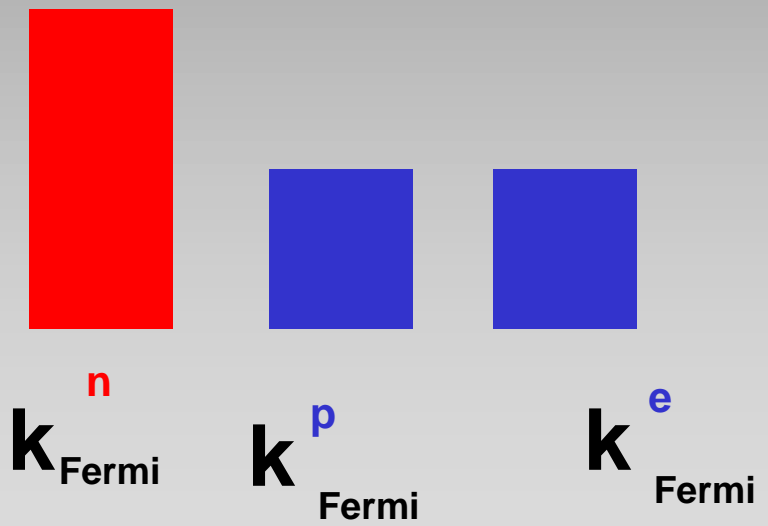
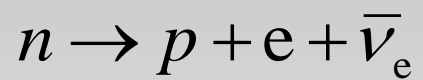
- At the core of neutron stars, most accepted models assume :  
~95% neutrons, ~5% protons and ~5% electrons ( $\beta$ -stability).

- Neglecting the np-SRC interactions, one can assume three separate Fermi gases (n p and e).

At T=0  $k_{Fermi}^n = k_{Fermi}^p + k_{Fermi}^e$   $k_{Fermi}^p = k_{Fermi}^e = \left(\frac{N_p}{N_n}\right)^{1/3} k_{Fermi}^n$

For  $\rho = 5\rho_0$ ,  $k_{Fermi}^n \approx 500 \text{ MeV}/c$ ,  $k_{Fermi}^p = k_{Fermi}^e \approx 250 \text{ MeV}/c$

Pauli blocking prevent direct n decay



## THE MEAN FIELD APPROXIMATION

$$\left[ -\frac{\hbar^2}{2m} \sum_i \hat{\nabla}_i^2 + \sum_{i<j} \hat{v}_{ij} \right] \Psi_o = E_o \Psi_o$$

↓

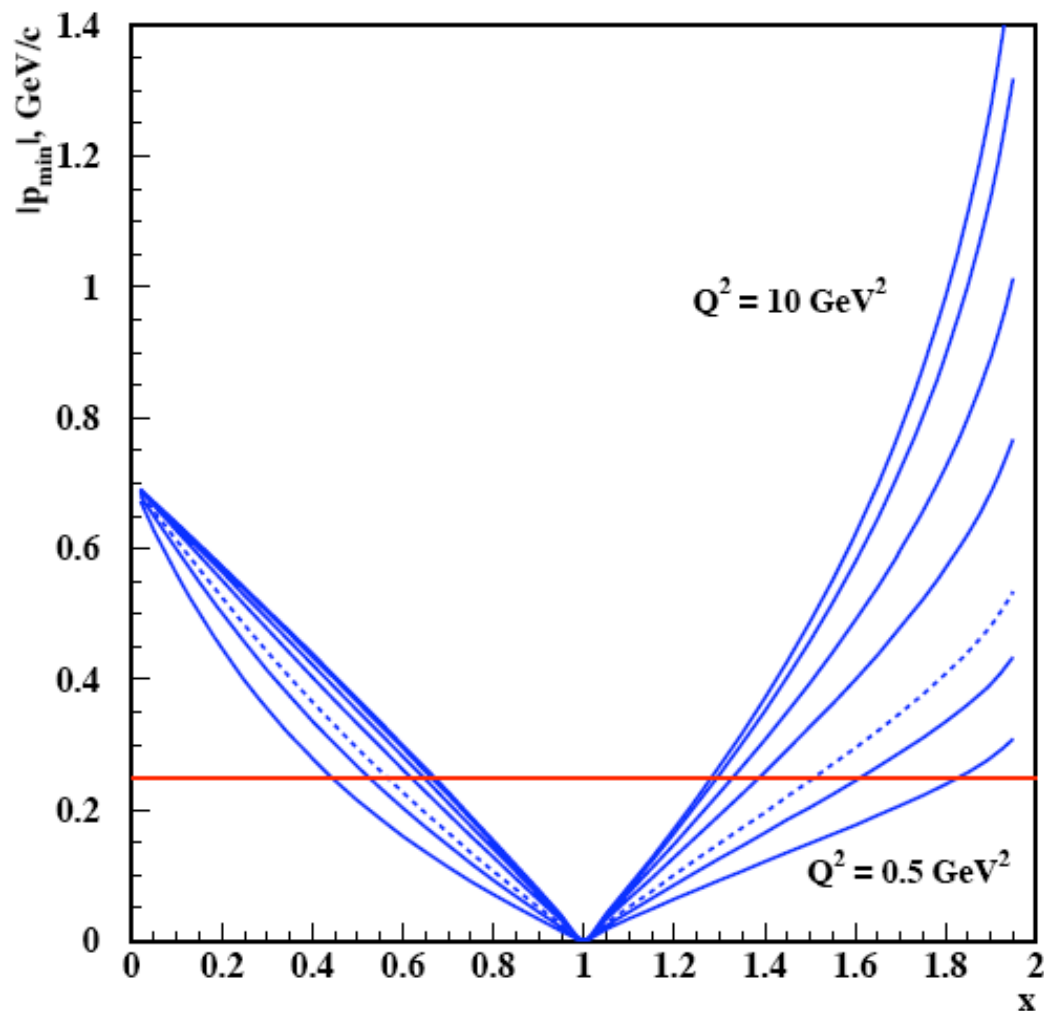
$$\left[ -\frac{\hbar^2}{2m} \sum_i \hat{\nabla}_i^2 + \sum_i V(r_i) \right] \Phi_o = \epsilon_o \Phi_o$$

Variational monte carlo (Urbana Group)

Cluster expansion techniques ( Ciofi, Alvioli, Cda, Morita )



$x > 1$  is not automatically means 2N SRC  
one needs also large  $Q^2$



$Q^2 \uparrow$

$q_+ \gg$

# Brookhaven Experiment

A.Tang et al, PRL 2003

$$F = \frac{\text{Number of (p,ppn) events } (p_i, p_n > k_F)}{\text{Number of (p,pp) events } (p_i > k_F)},$$

$$F = 0.43_{-0.07}^{+0.11} \quad \text{for } 275 \leq p_i, p_n \leq 550 \text{ MeV}/c$$

# Theoretical Analysis

Piasetzky, MS, Frankfurt,  
Strikman, Watson PRL 2007

$$P_{pn/pX} = \frac{F}{T_n R}$$

relative probability of finding pn SRC in the "pX" configuration that contains a proton with  $p_i > k_F$ .

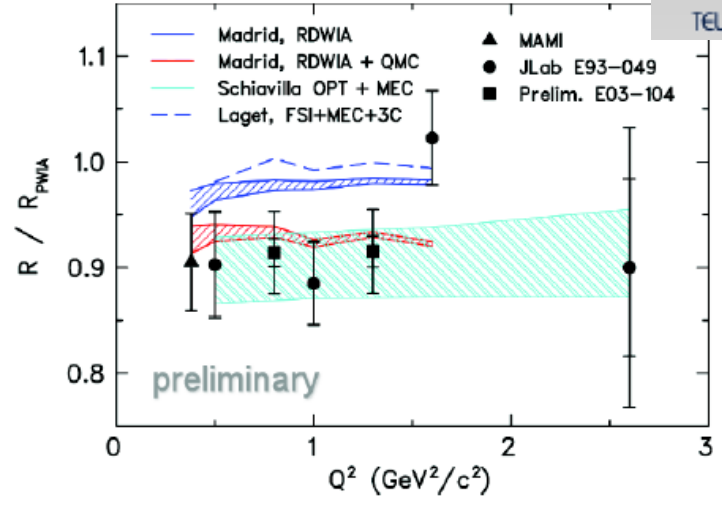
$$R \equiv \frac{\int_{\alpha_i^{min}}^{\alpha_i^{max}} \int_{p_{ti}^{min}}^{p_{ti}^{max}} \int_{\alpha_n^{min}}^{\alpha_n^{max}} \int_{p_{tn}^{min}}^{p_{tn}^{max}} D^{pn}(\alpha_i, p_{ti}, \alpha_n, p_{tn}, P_{R+}) \frac{d\alpha}{\alpha} d^2 p_t \frac{d\alpha_n}{\alpha_n} d^2 p_{tn} dP_{R+}}{\int_{\alpha_i^{min}}^{\alpha_i^{max}} \int_{p_{ti}^{min}}^{p_{ti}^{max}} S^{pn}((\alpha_i, p_{ti}, P_{R+}) \frac{d\alpha}{\alpha} d^2 p_t dP_{R+}}.$$



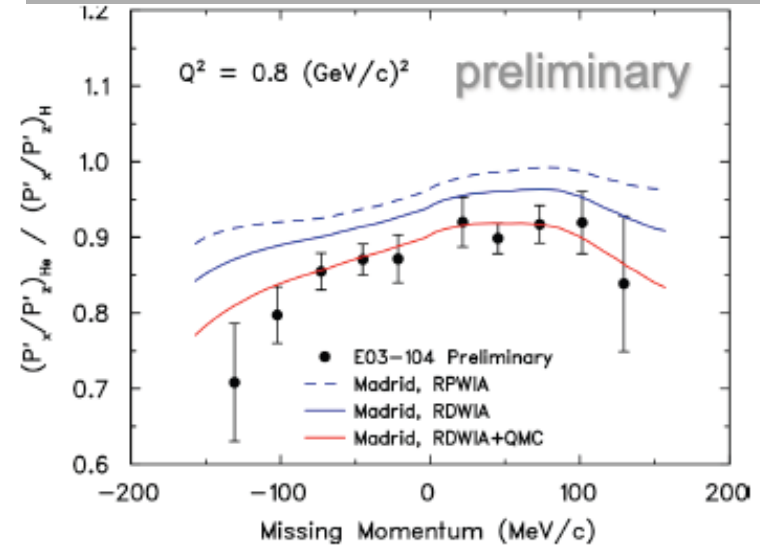
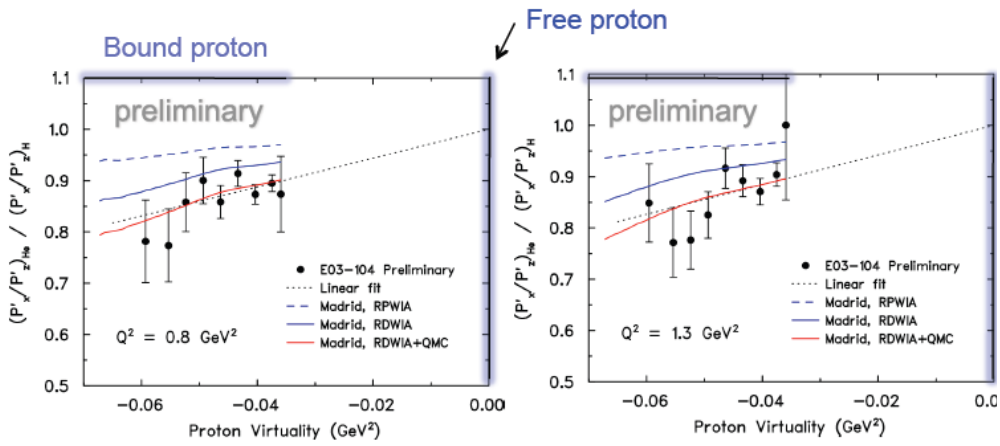
$${}^4\text{He}(\vec{e}, e' \vec{p})$$

# Polarization Transfer

Copied from S. Strauch talk

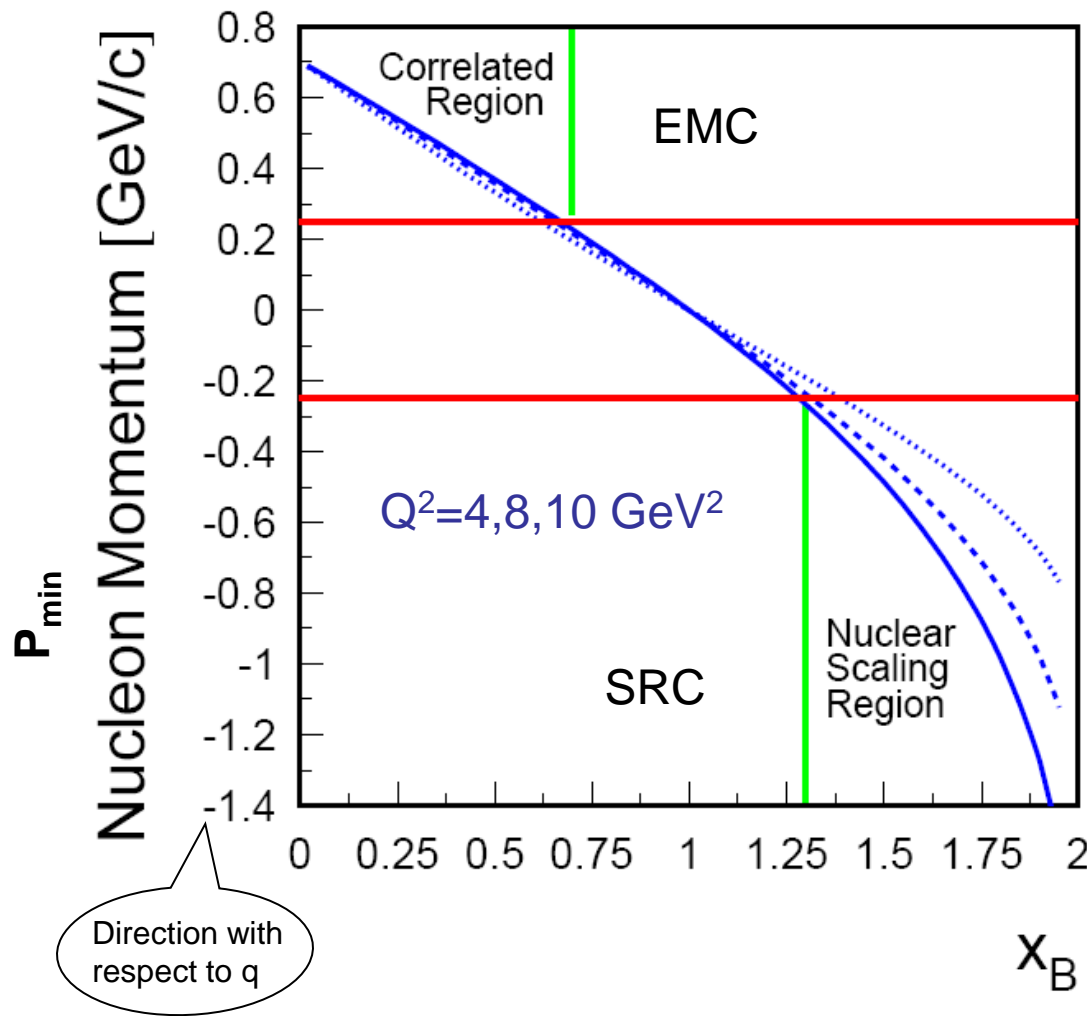


## Proton Virtuality: $v = p^2 - m_p^2$



- Polarization-transfer double-ratio data and calculations show **dependence on proton virtuality** with the trend of  $R \approx 1$  for  $p^2 = m_p^2$ ; as it should be.
- Excellent description of preliminary E03-104 data with the **RDWIA + QMC (in-medium form factors)** model.

see: C. Ciofi degli Atti, L.L. Frankfurt, L.P. Kaptari, M.I. Strikman, Phys. Rev. C 76, 055206 (2007)



The minimum missing momentum of the  $D(e,e')pn$  reaction from conservation of energy and momentum for quasi-elastic scattering

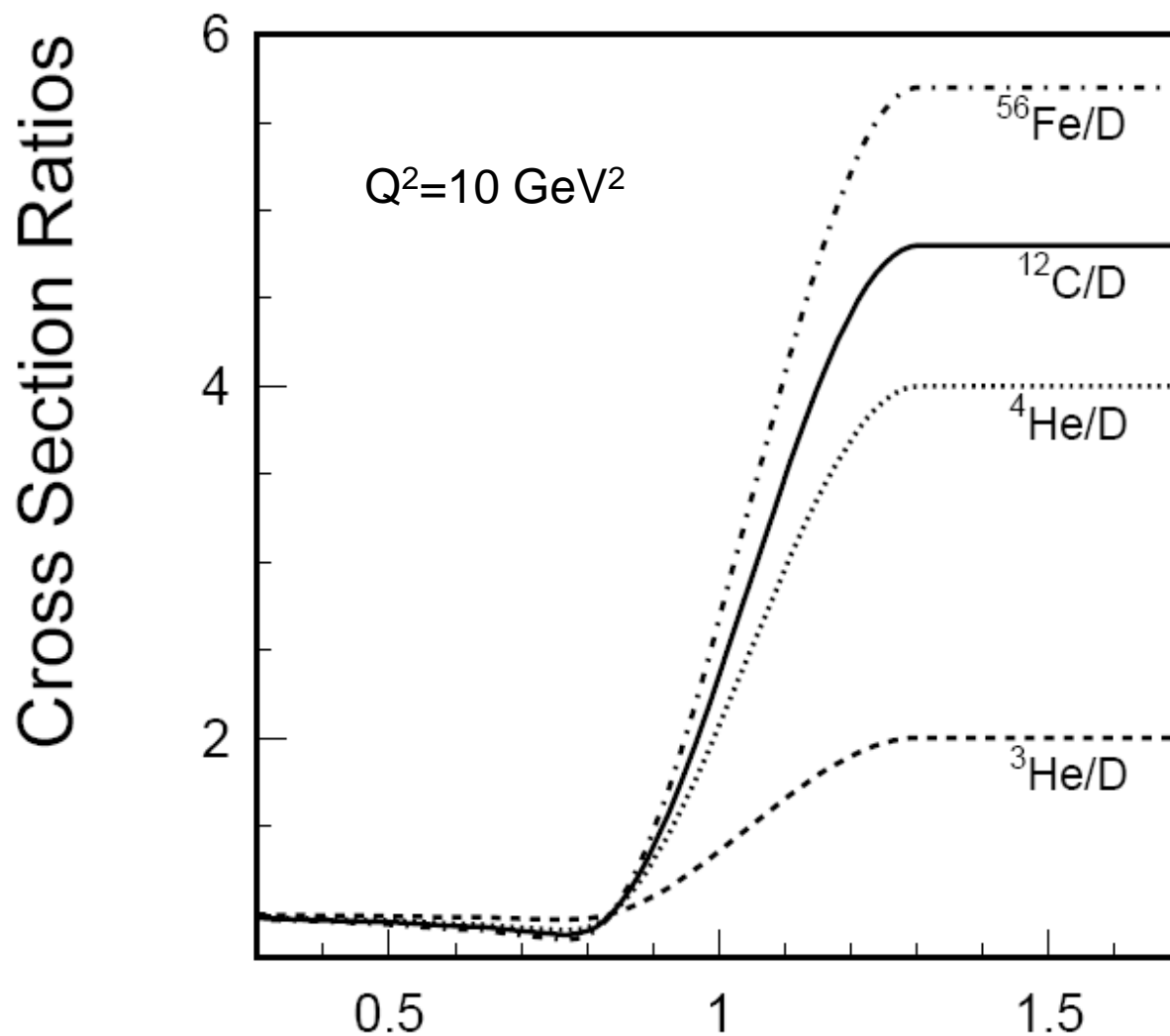
$$(q + p_d - p_n)^2 = m_p^2$$

$$P_d(x_B) = 2\pi \cdot \int_{P_{\min}}^{\infty} p^2 \cdot n_d(p) \cdot dp$$

$$n_A(p) = n_d(p) \cdot a_2(A/d)$$

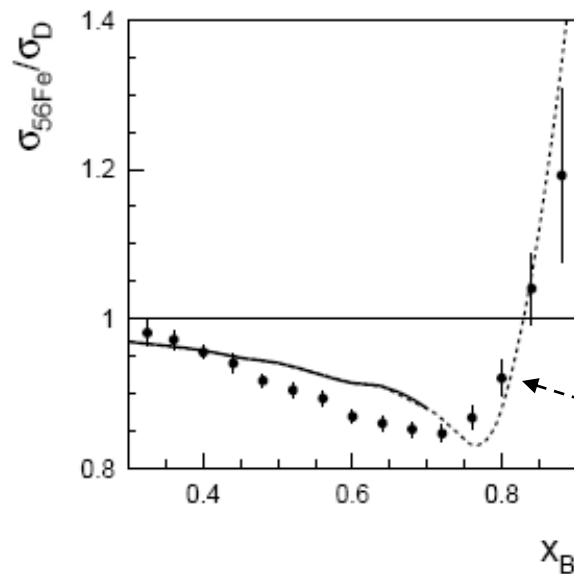
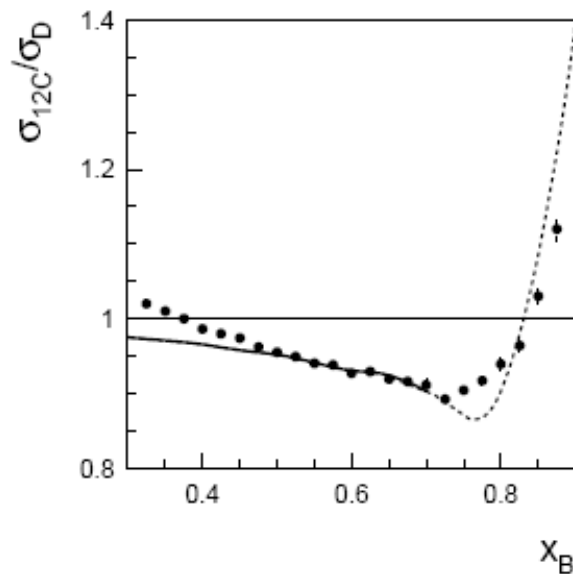
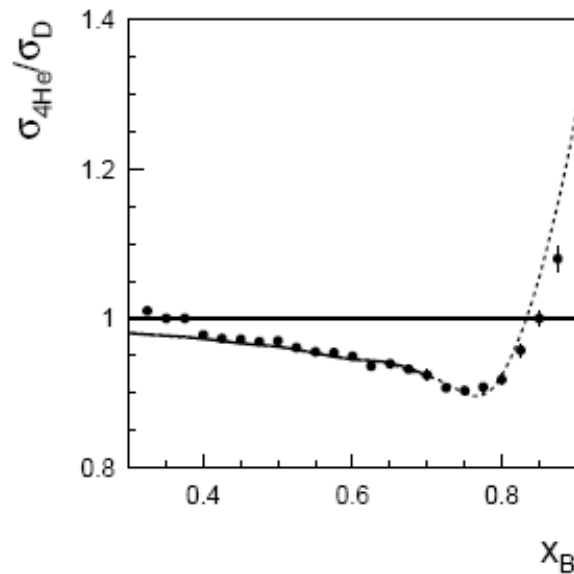
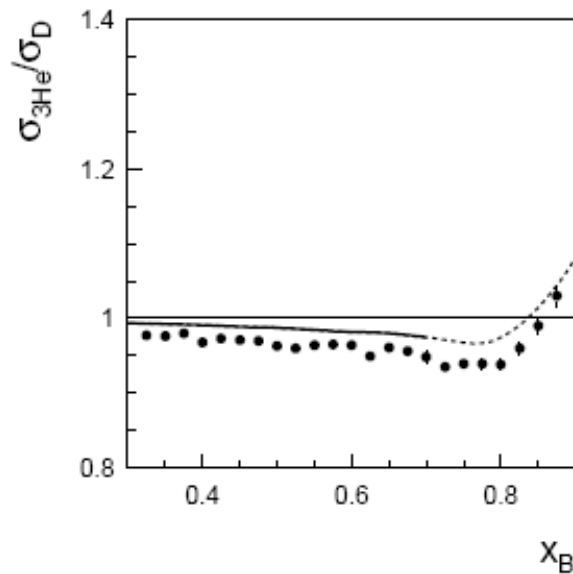
$$P_A(x_B) = 2\pi \cdot \int_{P_{\min}}^{\infty} p^2 \cdot n_A(p) \cdot dp$$

$$\frac{\sigma_A}{\sigma_d} = \frac{1 - P_A(x_B)}{1 - P_d(x_B)}$$



$$\frac{\sigma_A}{\sigma_d} = \frac{1 - P_A(x_B)}{1 - P_d(x_B)}$$

interpolation  $a_2(A/d) X_B$



Data:

$^3\text{He}, ^4\text{He}, ^{12}\text{C}$

J. Seely et al.

PRL 103, 202301 (2009).

$^{56}\text{Fe}$

J. Gomez et al.

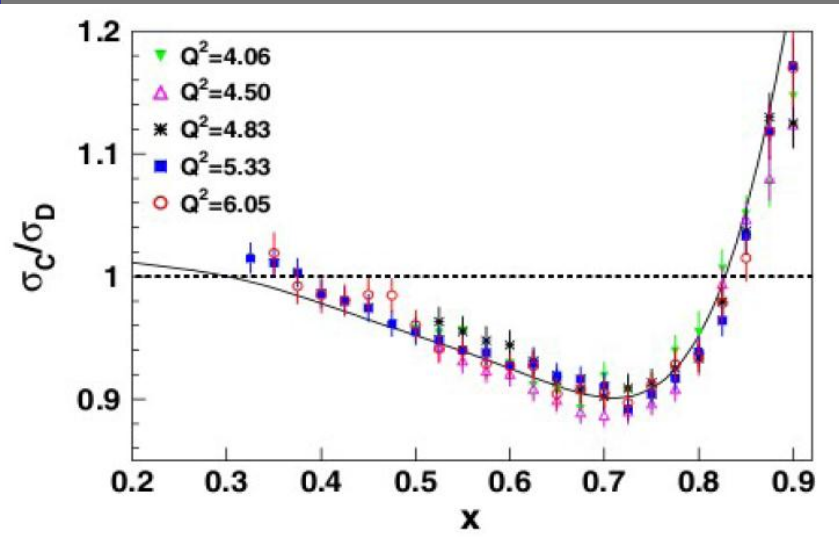
PR D49, 4348 (1994).

# Very weak $Q^2$ dependence

EMC

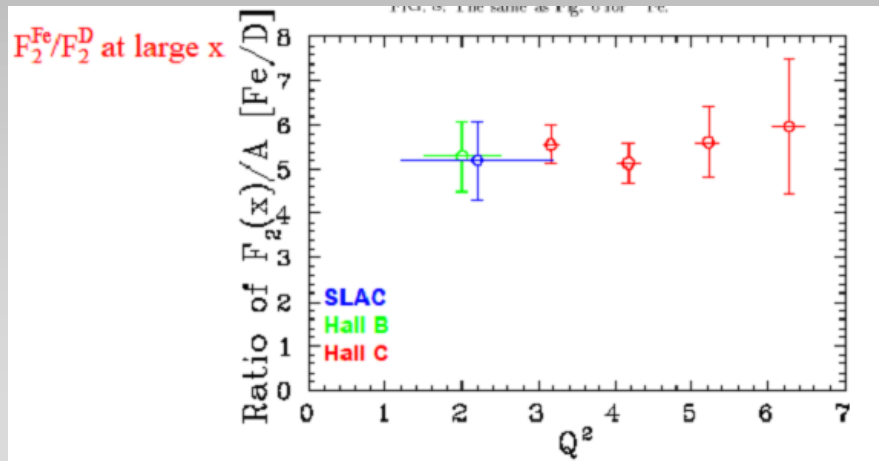
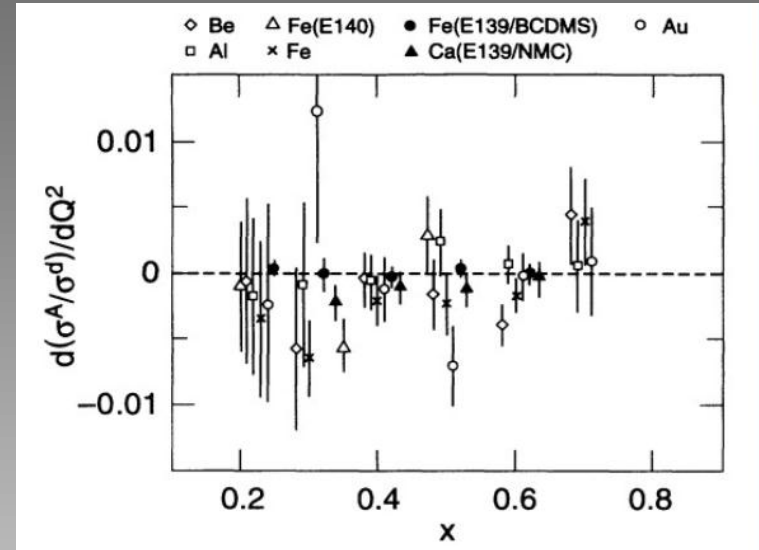
JLab

J. Seely et al.



SLAC

J. Gomez et al.



SRC

J. Arrington talk, Minami 2010.



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## Kinematics optimized to minimize the competing processes

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The large  $Q^2$  is required to probe the small size SRC configuration.

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FSI can be treated in Glauber approximation.

### $x_B > 1$

Reduced contribution from isobar currents.

### Large $p_{\text{miss}}$ and $E_{\text{miss}} \sim p_{\text{miss}}^2/2M$

### Large $P_{\text{miss}_z}$

## FSI

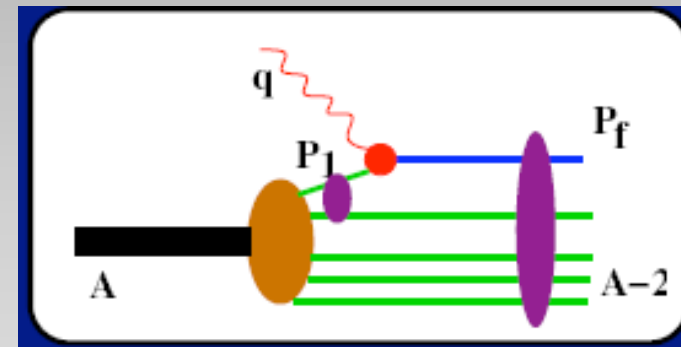
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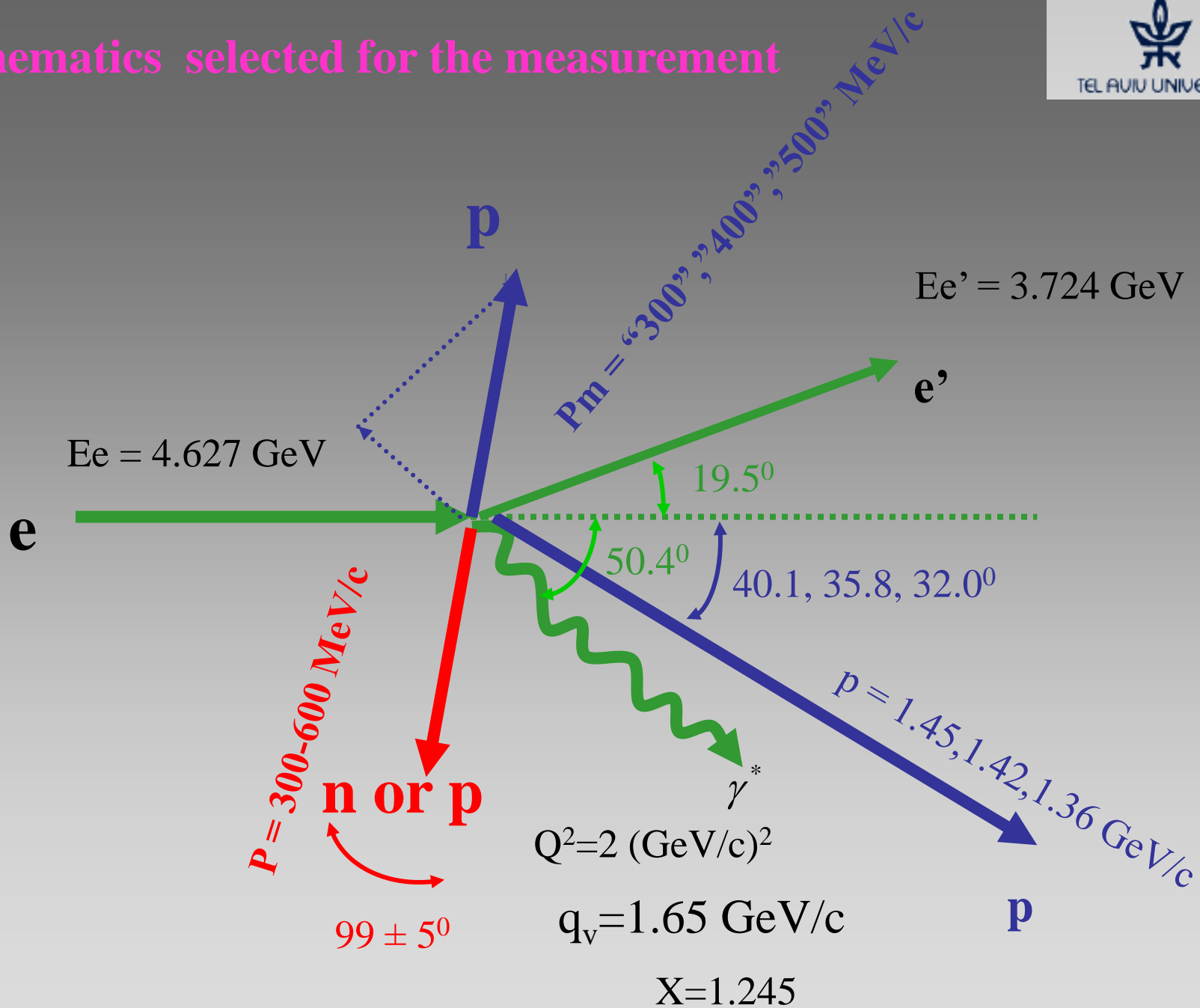
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These are not necessarily small, BUT:

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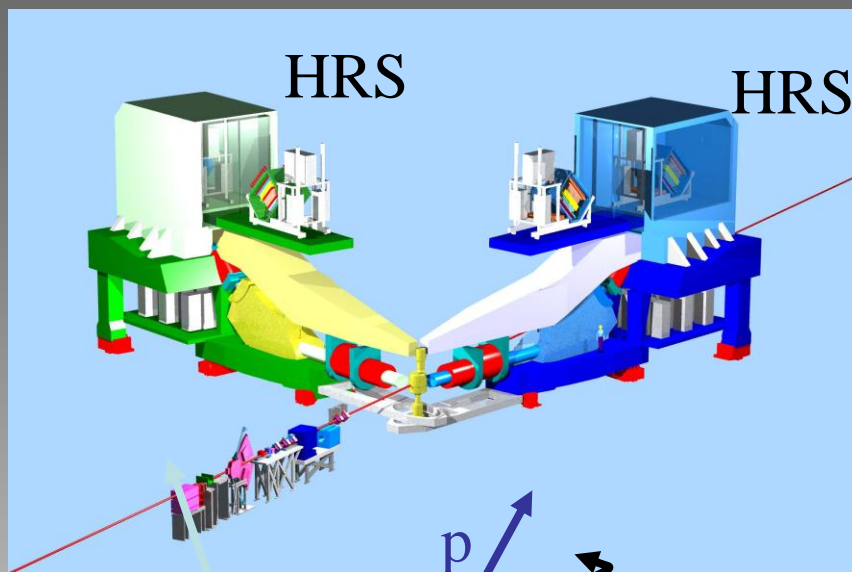
# The kinematics selected for the measurement



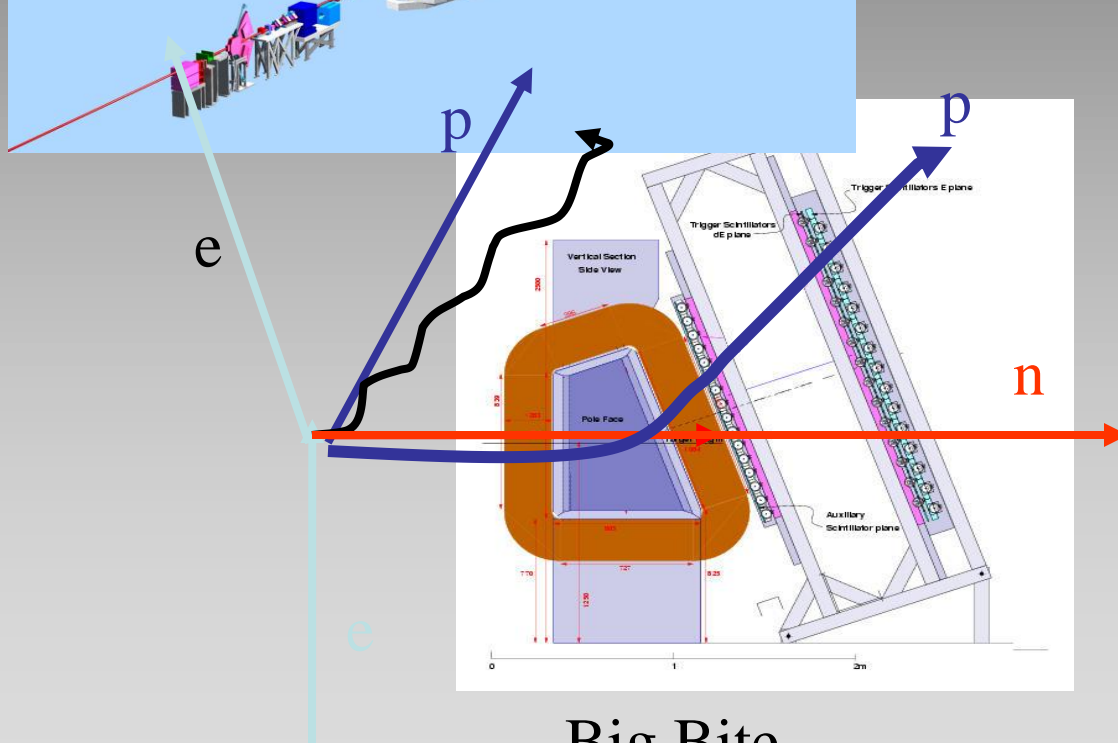


# Experimental setup

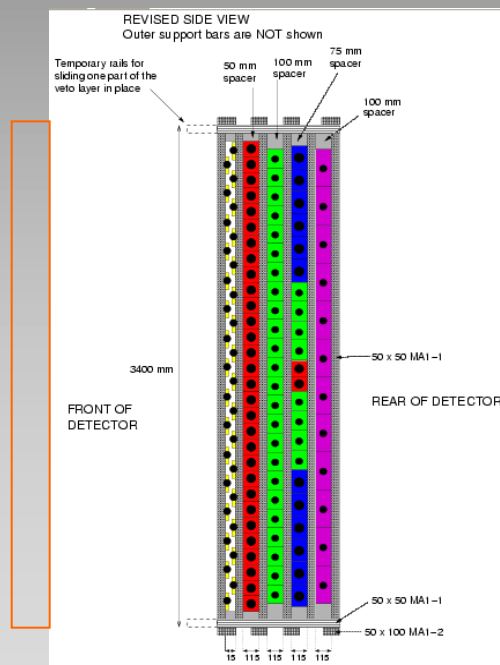
## EXP 01-015 / Jlab



n array

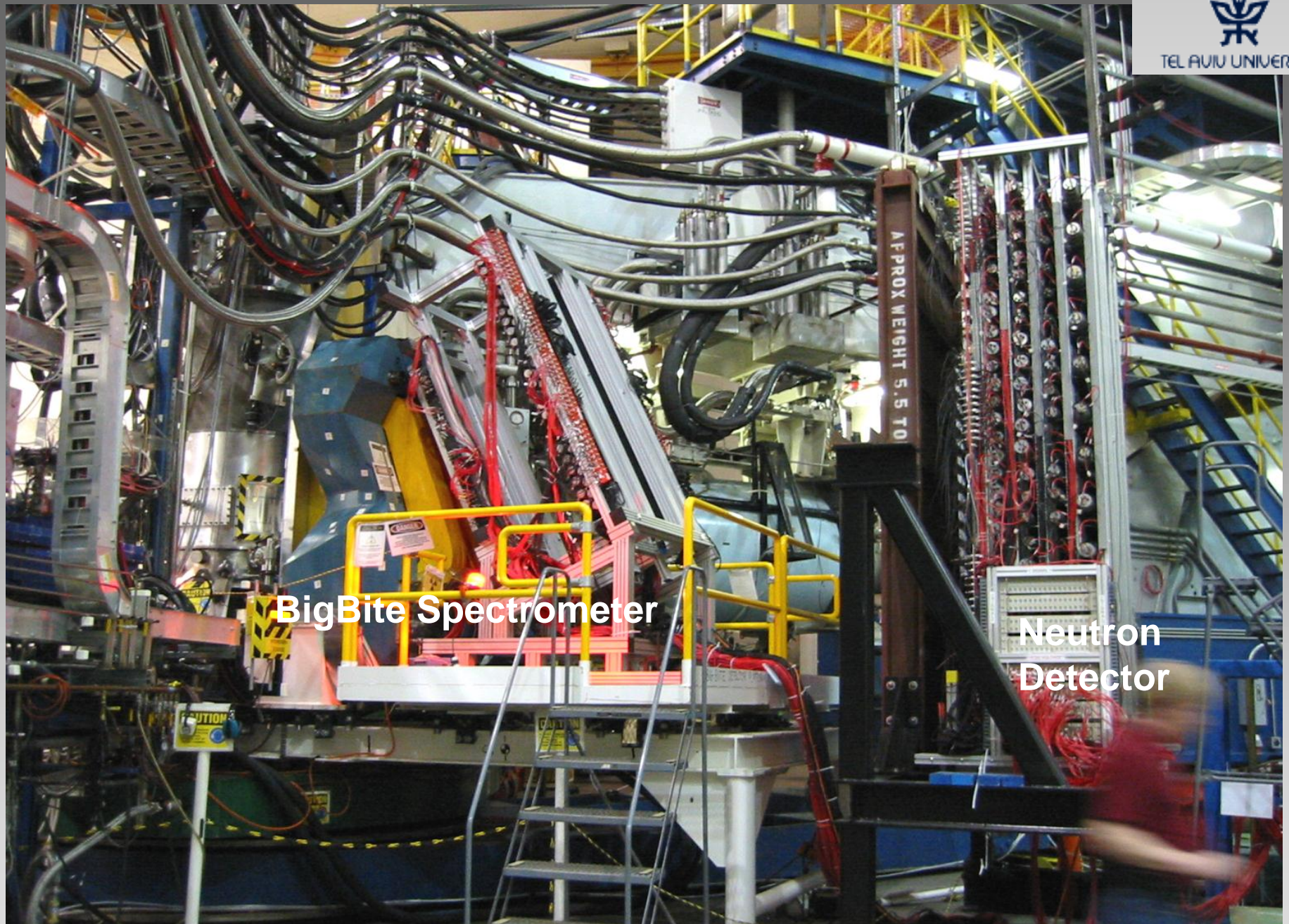


Big Bite



Lead wall





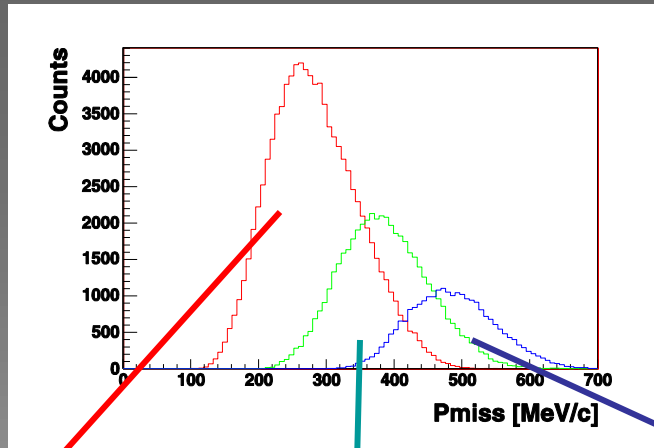
BigBite Spectrometer

Neutron  
Detector



$^{12}\text{C}(e,e'p)$

$x_B > 1$

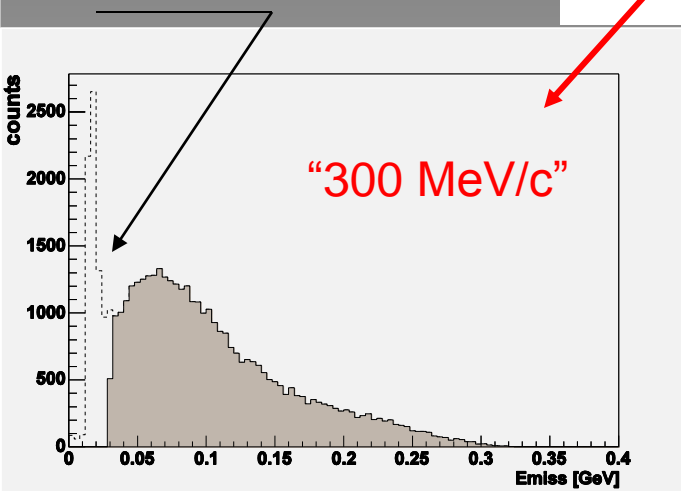


"300 MeV/c"

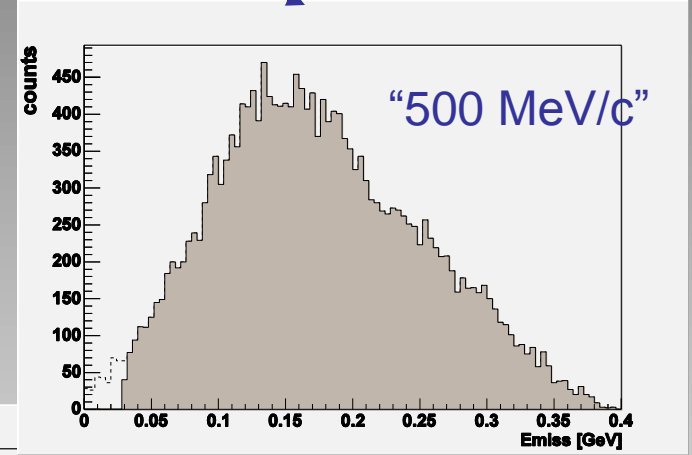
"400 MeV/c"

"500 MeV/c"

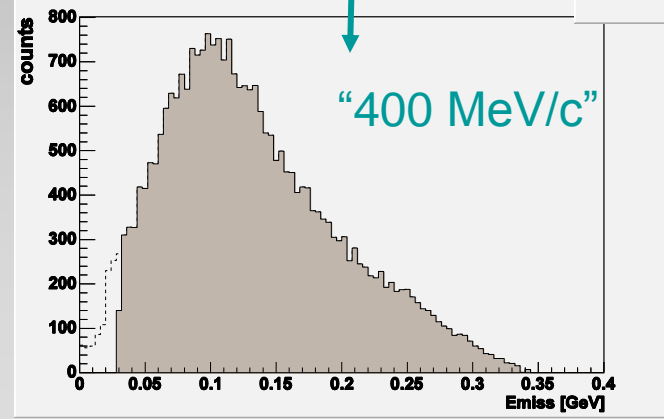
$^{12}\text{C}(e,e'p)^{11}\text{B}$



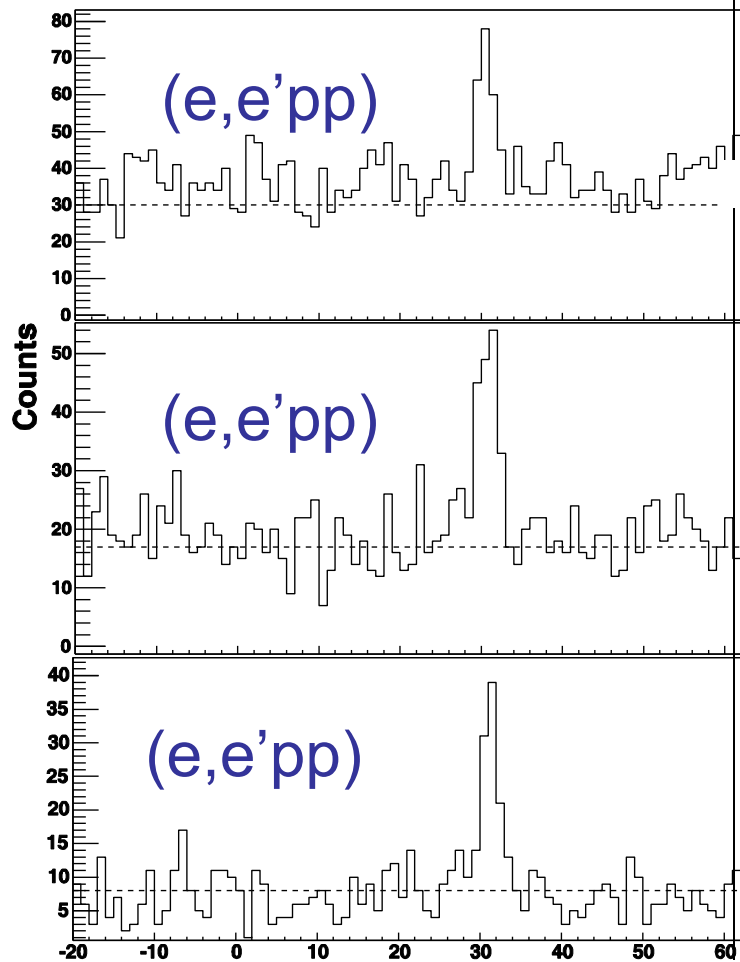
"300 MeV/c"



"500 MeV/c"



"400 MeV/c"



$P_{\text{mis}} = \text{"300"} \text{ MeV/c}$

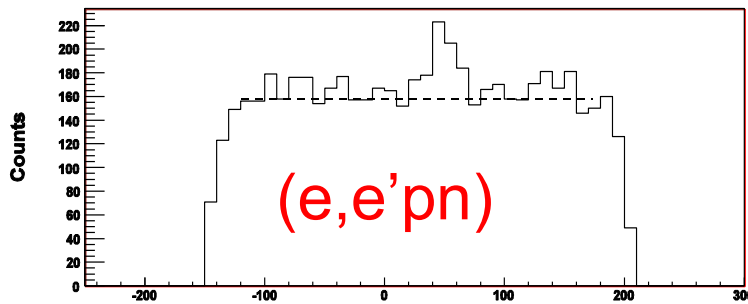
(Signal : BG= 1.5:1)

$P_{\text{mis}} = \text{"400"} \text{ MeV/c}$

(Signal : BG= 2.3:1)

$P_{\text{mis}} = \text{"500"} \text{ MeV/c}$

(Signal : BG= 4:1)



$P_{\text{mis}} = \text{"500"} \text{ MeV/c}$

(Signal : BG= 1:7)

TOF [ns]

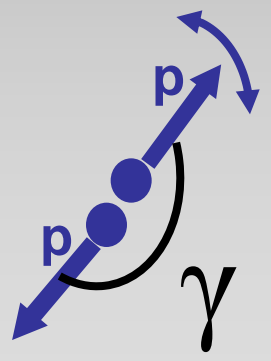
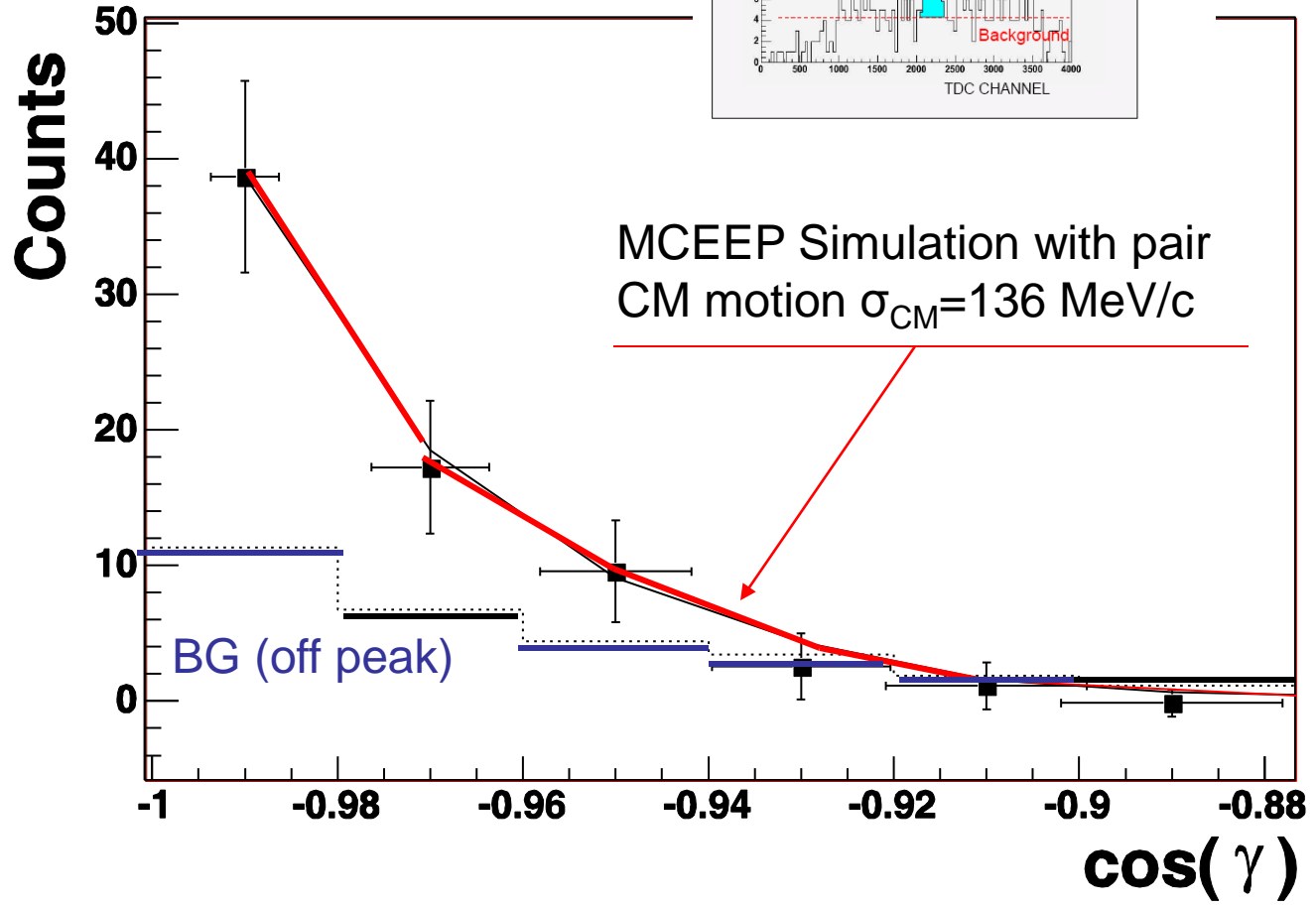
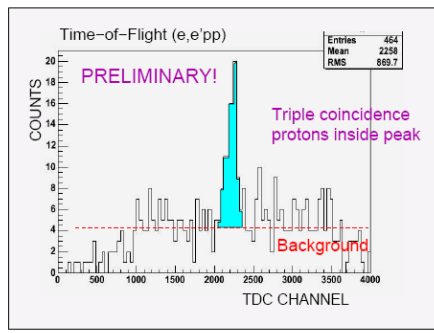


# Directional correlation

Triple Coincidence Events



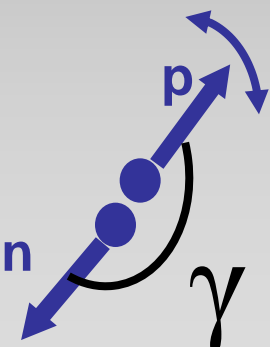
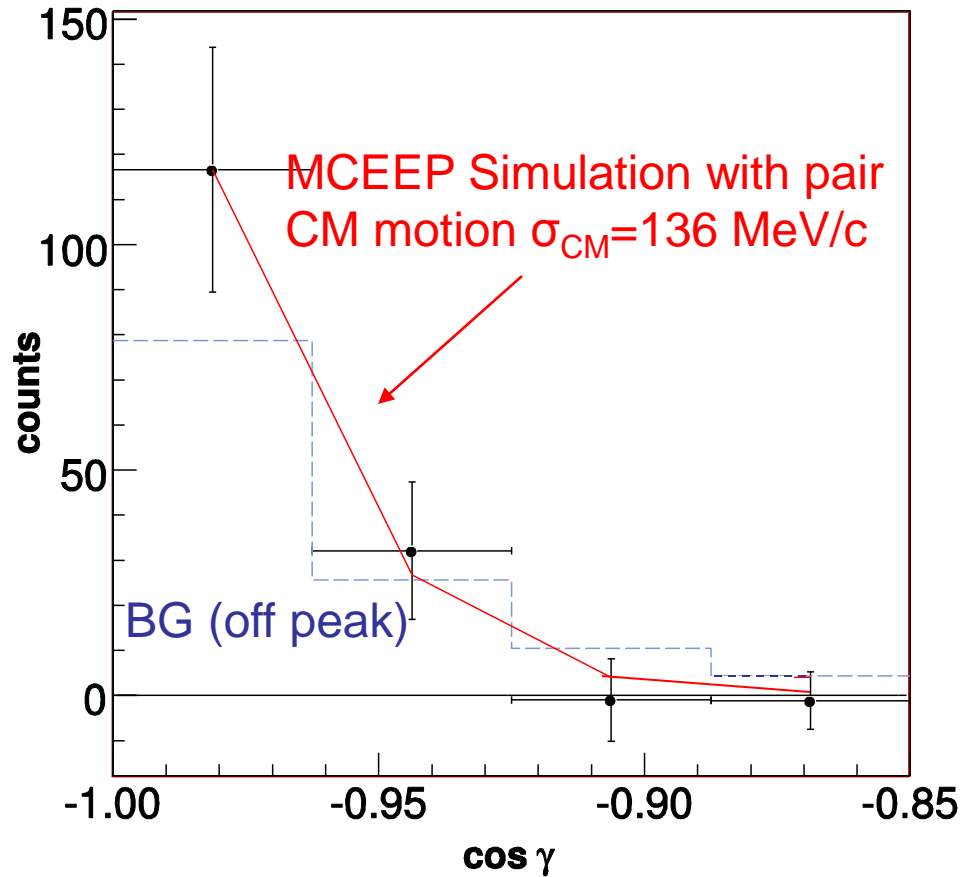
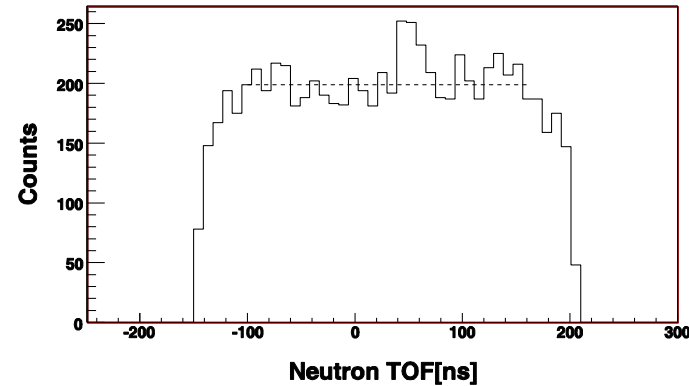
$^{12}\text{C}(e,e'pp)$





# Directional correlation

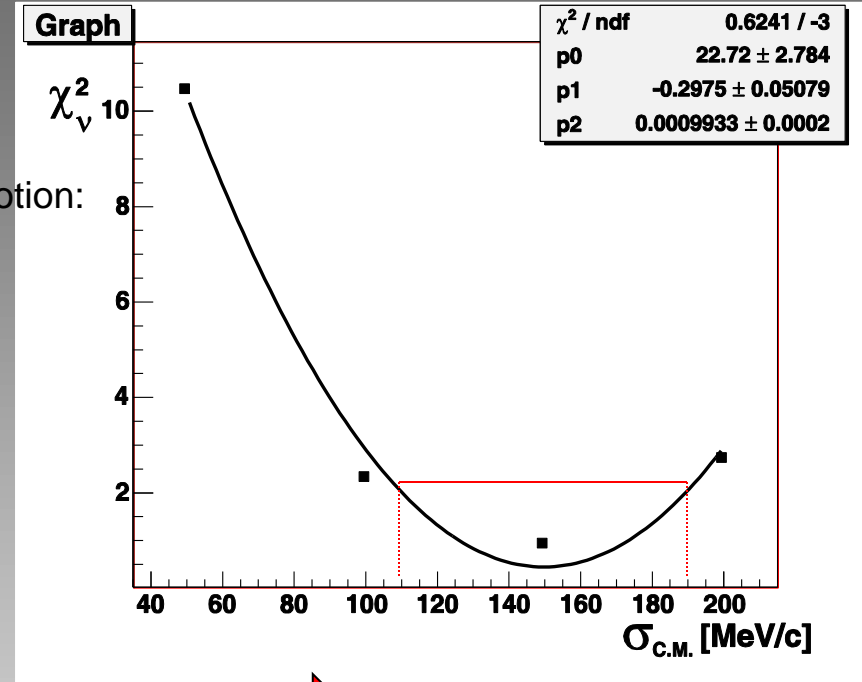
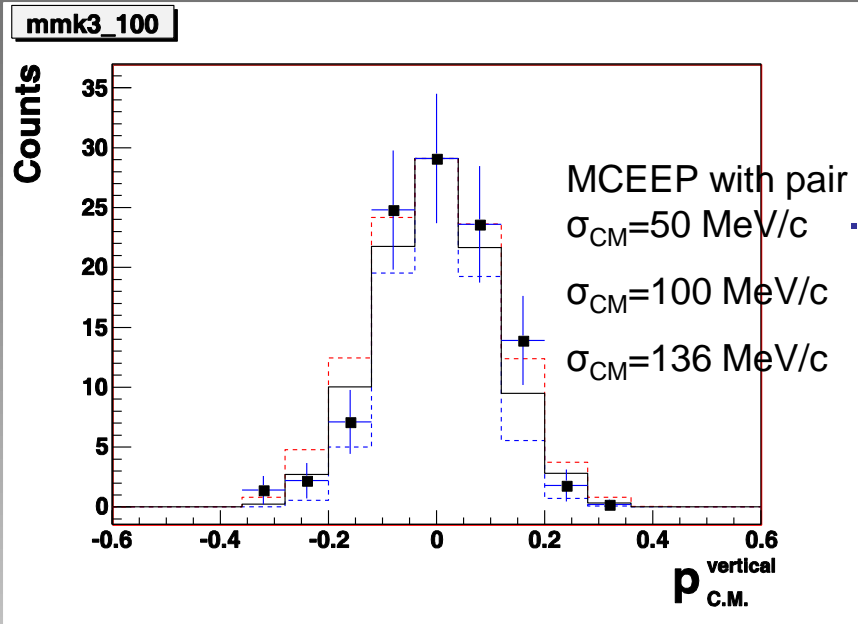
$^{12}\text{C}(e,e'pn)$





# CM motion of the pair:

$P_{c.m.}^{vertical}$  , “500 MeV/c “ setup



2 components of  $\vec{p}_{c.m}$  and 3 kinematical setups



This experiment :  $\sigma_{CM}=0.136 \pm 0.020$  GeV/c

(p,2pn) experiment at BNL :  $\sigma_{CM}=0.143 \pm 0.017$  GeV/c

Theoretical prediction (Ciofi and Simula) :  $\sigma_{CM}=0.139$  GeV/c

# The **free** neutron structure function

$$\frac{F_2^n(x_B, Q^2)}{F_2^p(x_B, Q^2)} = \frac{2F_2^d(x_B, Q^2)/F_2^p(x_B, Q^2) - [1 - a(x_B - b)]}{[1 - a(x_B - b)]}$$

For  
 $0.35 \leq X_B \leq 0.7$

$$\frac{\sigma_d}{\sigma_p + \sigma_n} = 1 - a(x_B - b)$$

Fermi smearing using relativistic  
 deuteron momentum density

□ SLAC Data, J. Arrington et al.  
 JPG 36(2009)205005.

----- World parameterization of Fd, Fp

With medium correction

■ Extracted from this work

— Corrected for the EMC effect  
 as calculated in a PLC model

