

# Polymer Crystallization: New Concepts and Implications

(M. Muthukumar)

Nucleation, Aggregation and Growth

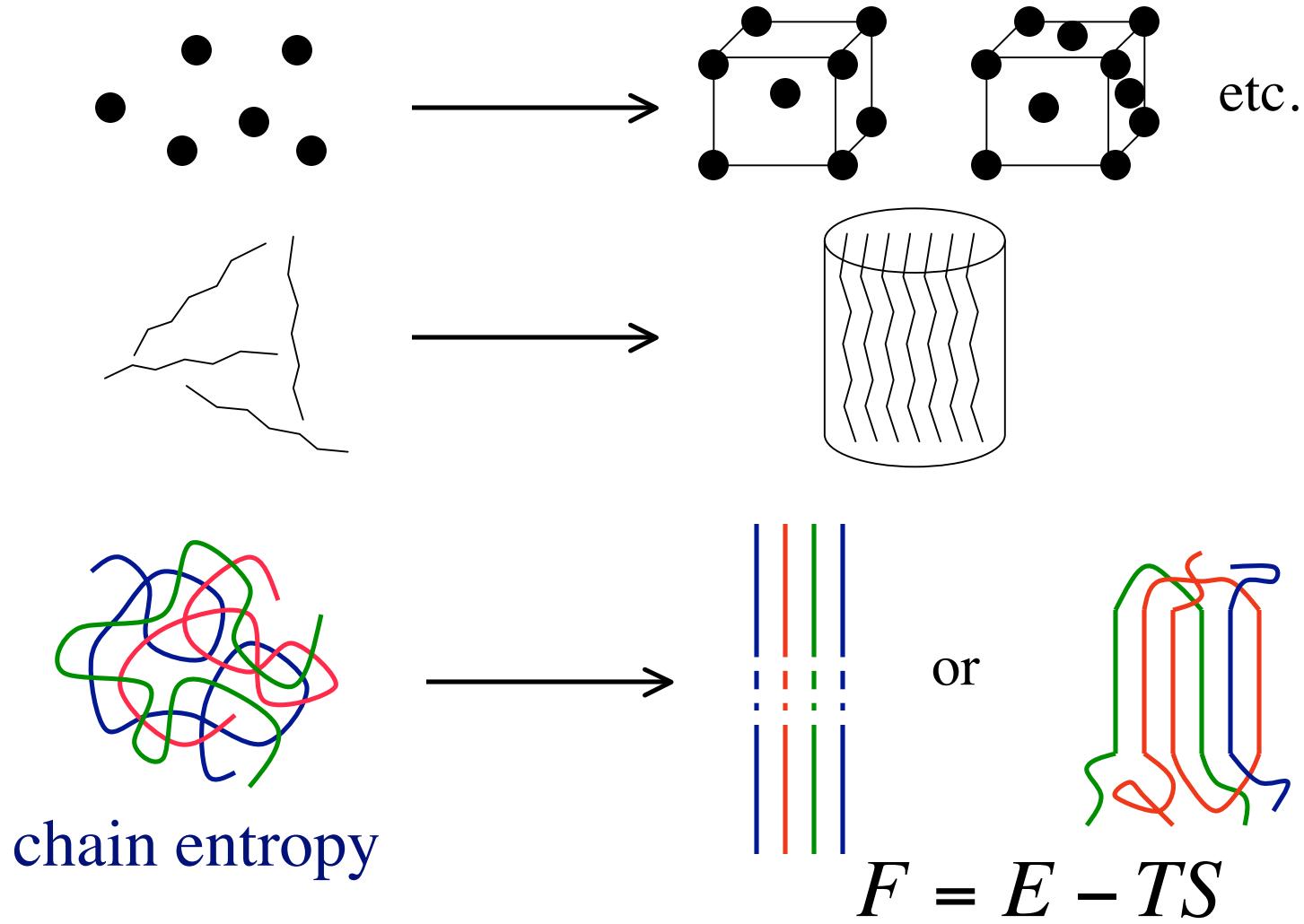
Bengaluru

July 26- July 30, 2010

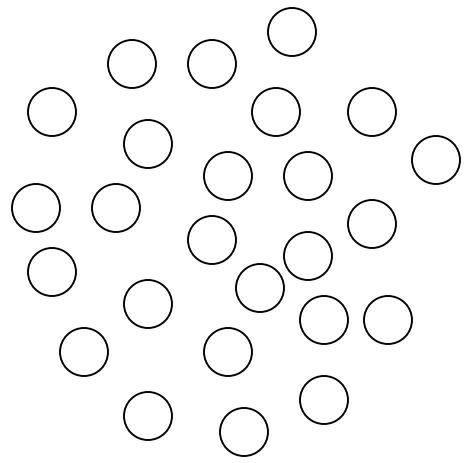


**PS&E** *UMass - Amherst*

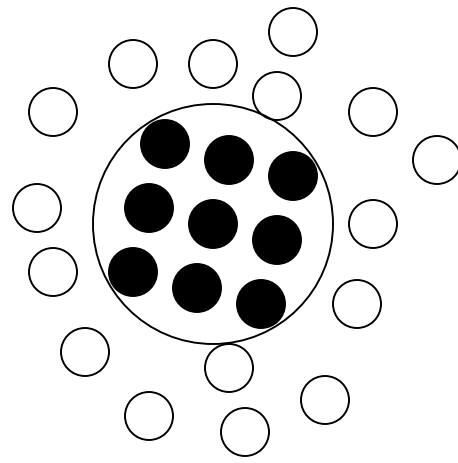
# What distinguishes polymers from small molecules, colloidal particles, and oligomers?



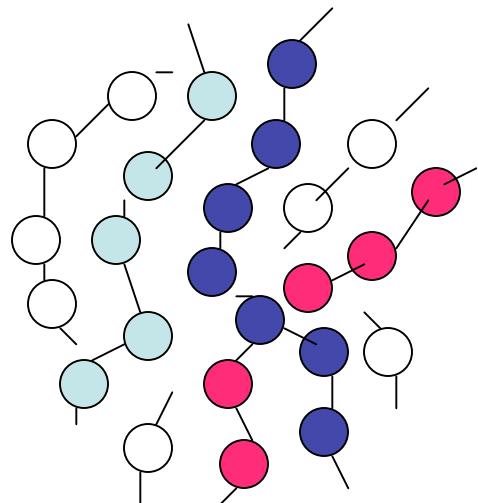
(Is  $TS$  negligible?)



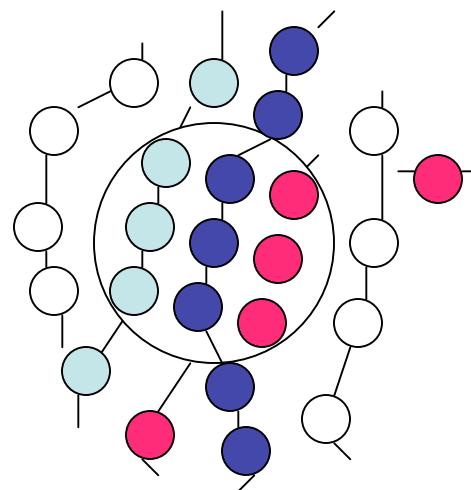
Monomeric liquid



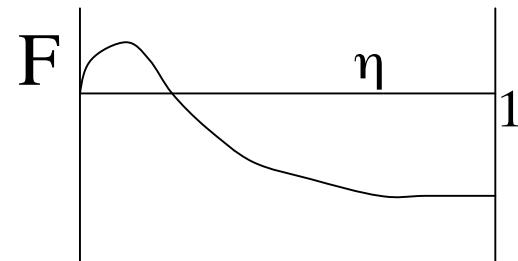
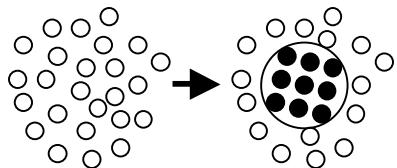
Nucleation



Polymeric liquid

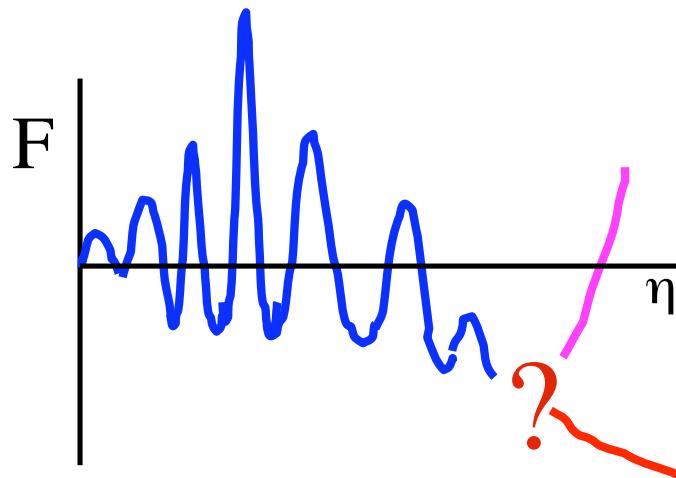
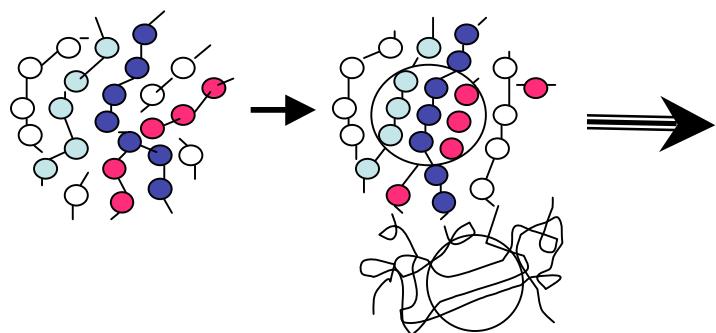


Small molecules:



( $\eta$  = degree of crystallinity,  
lamellar thickness,...)

Polymer molecules:



Conformational entropy

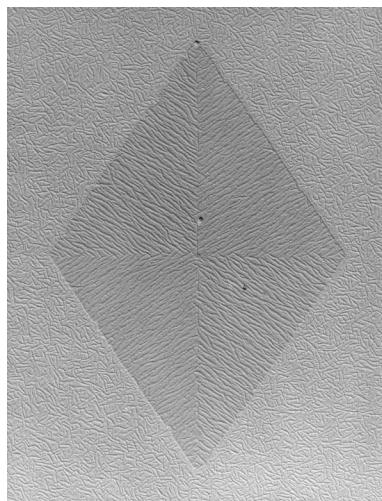
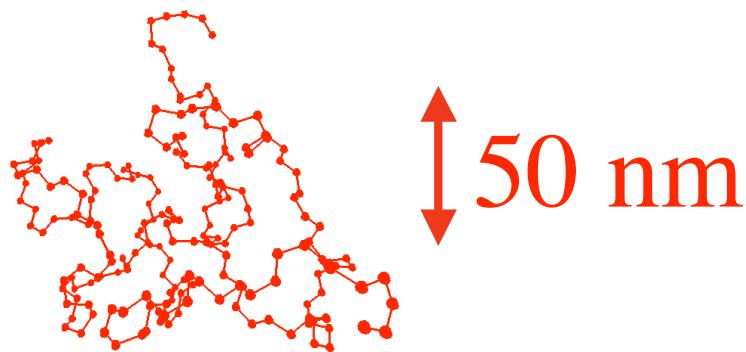
Entropic Frustration

$$F = E - T S$$

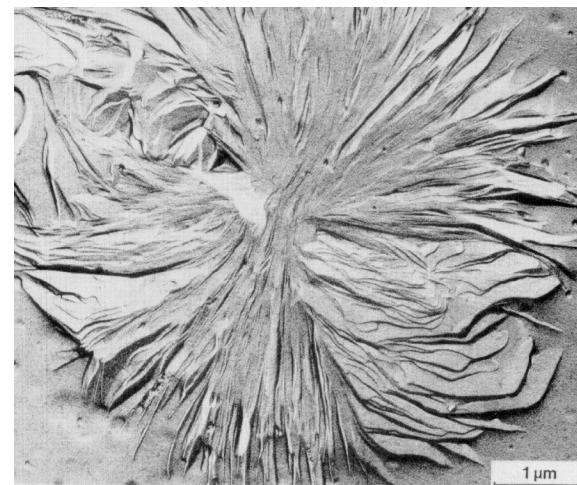
Semicrystallinity = equilibrium  
Semicrystallinity = kinetics

?

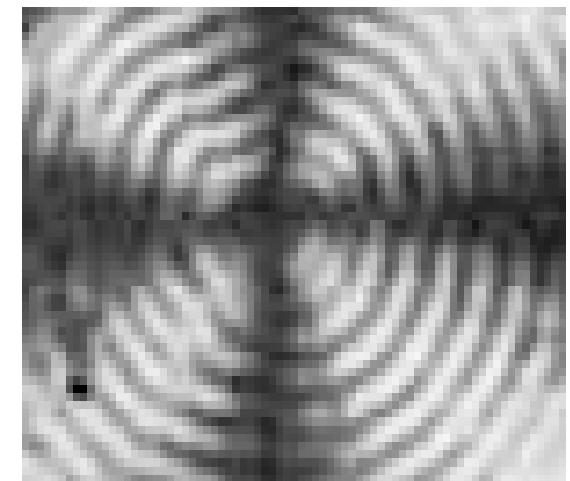
## Crystallization of flexible polymers



Lamella



Spherulites



GIGANTIC CHIRALITY  
in polyethylene crystals  
(ACHIRAL molecules)

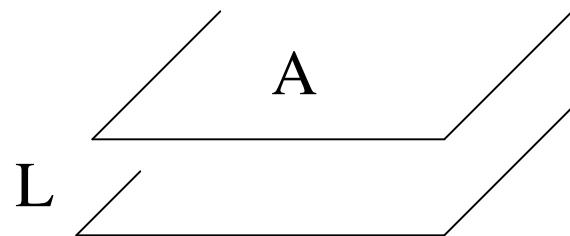
B. Lotz and S.Z.D. Cheng, Polymer, 46, 577 (2005)

H. K. Storks, JACS, 60, 1753 (1938):  
“..macromolecules are folded back and forth  
upon themselves..”

G. Strobl, “The Physics of Polymers” (1997):  
“..is governed by kinetic criteria rather than  
by equilibrium thermodynamics”

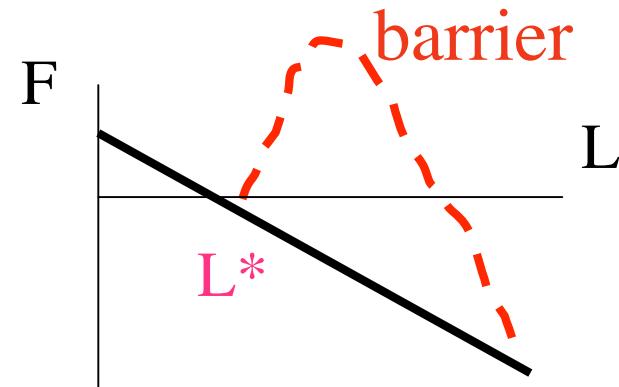
## CLASSICAL VIEW

A. Lamellar Thickness:  $(L = \text{lamellar thickness})$



$$F = -(\Delta F) A L + 2 \sigma A$$

bulk      interface



$$L^* = (2 \sigma / \Delta F) \sim (1/\Delta T)$$

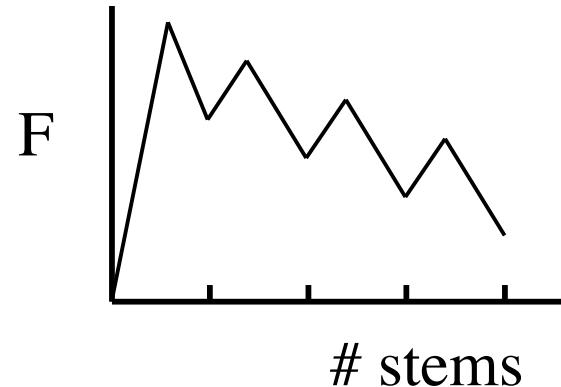
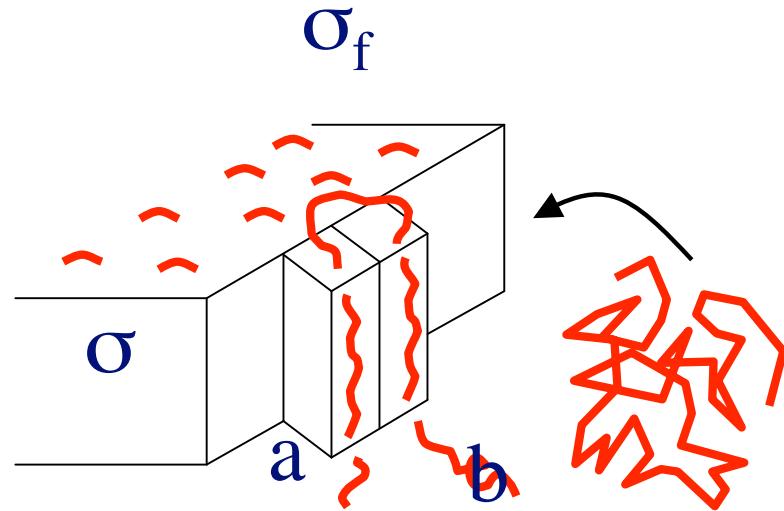
$$\Delta T = T_m - T_c$$

- \* First viable state kinetically stabilized
- \* Eventual extended chain dimension

## CLASSICAL VIEW

### B. Lamellar Growth:

Lauritzen-Hoffman Theory  
(1960)

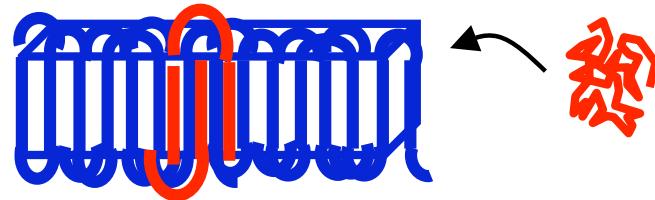


Rate of growth:  $G \sim \exp[-1/T(\Delta T)]$   
(2d-Nucleation)

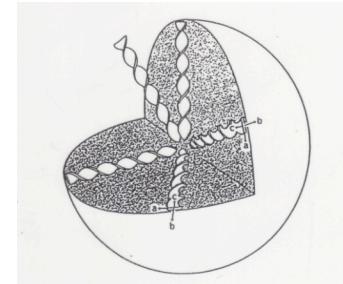
# Central Issues

1. Primordial stage of polymer crystallization
  2. Spontaneous selection of lamellar thickness
    - $L \ll$  extended chain dimension
    - $\sim 10^{-2} \times$  current equilibrium arguments
    - => “KINETICALLY CONTROLLED”
- Interlude from any stable MESOMORPHIC states?

3. Kinetics at growth front



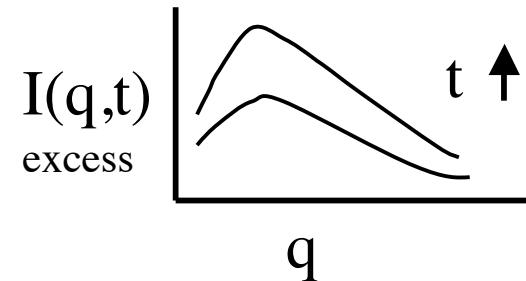
4. Origin of chiral symmetry breaking



5. Composition fluctuations on crystallization kinetics

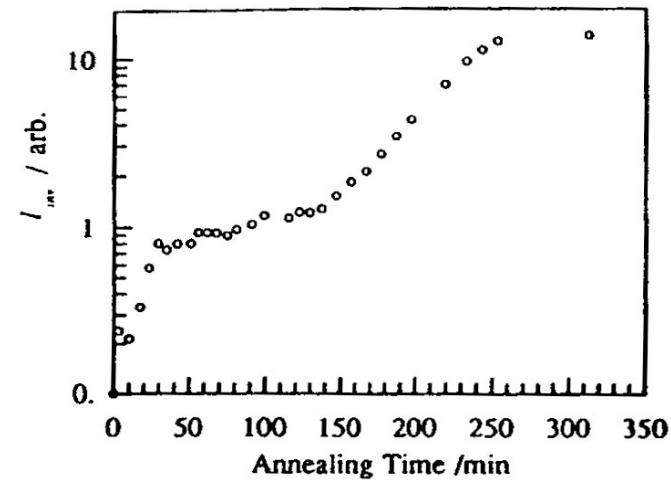
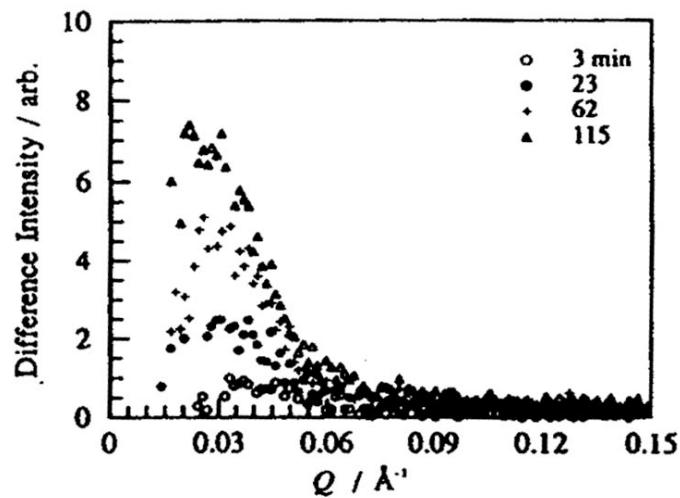
# 1. Primordial stage of polymer crystallization

Density fluctuations **before**  
crystalline signature

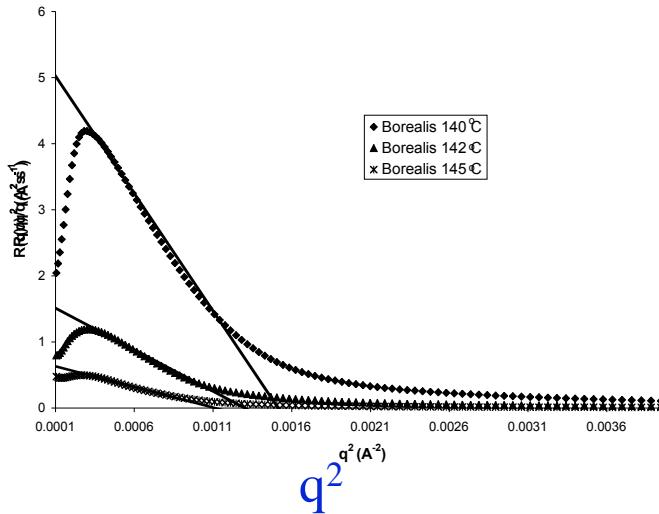


Postulate  
Spinodal Decomposition into  
inter-connected polymer-rich and polymer-poor phases,  
instead of  
Nucleation-Growth

# Scattered Intensity at Early Times



M. Imai et al. *Macromolecules* 1994, 27, 7103.(PET)



Rate:  $R_q/q^2$

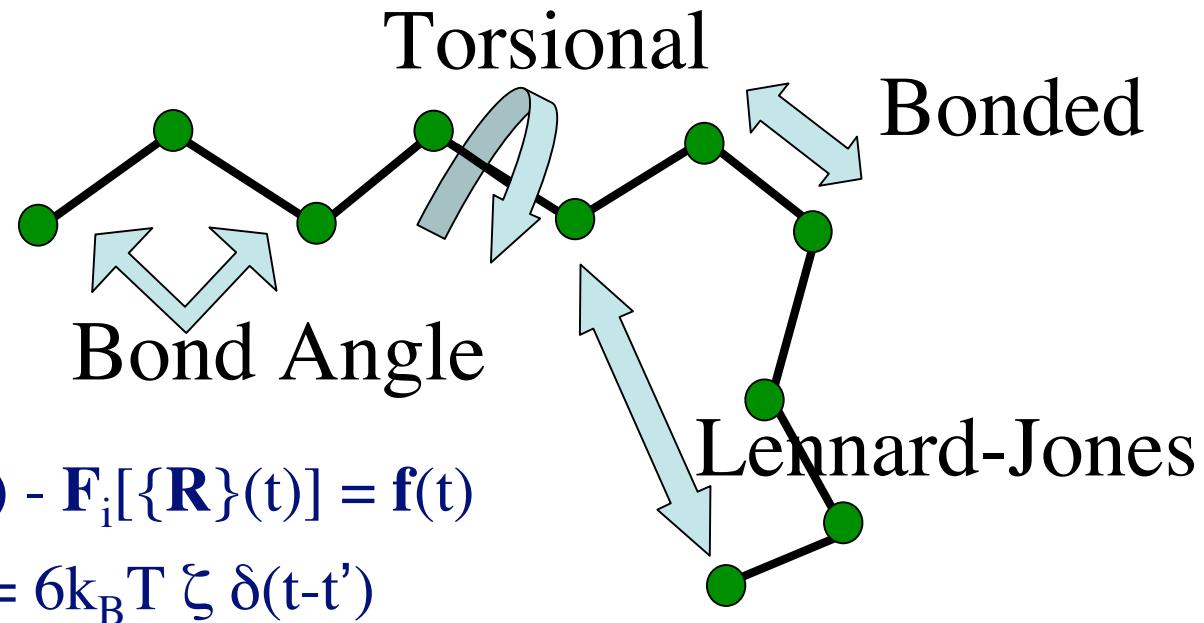
Spinodal Mode

A.J. Ryan and collaborators (I-PP)

# Acknowledgments

## I. Langevin Dynamics Simulations

C. Liu, P. Welch, I. Dukovski, J. Zhang

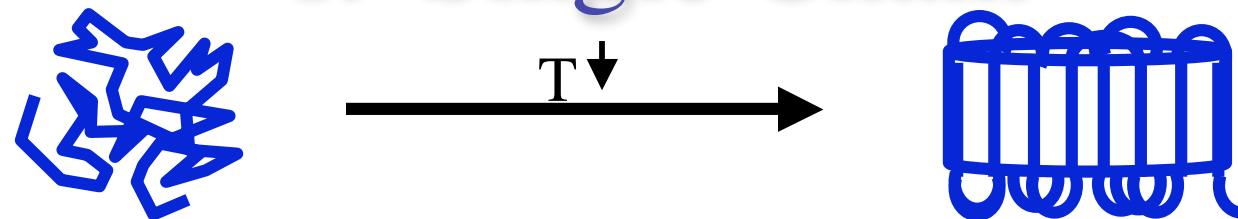


## II. Statistical Mechanics

A. Kundagrami, M.K. Mitra, Y. Hatwalne

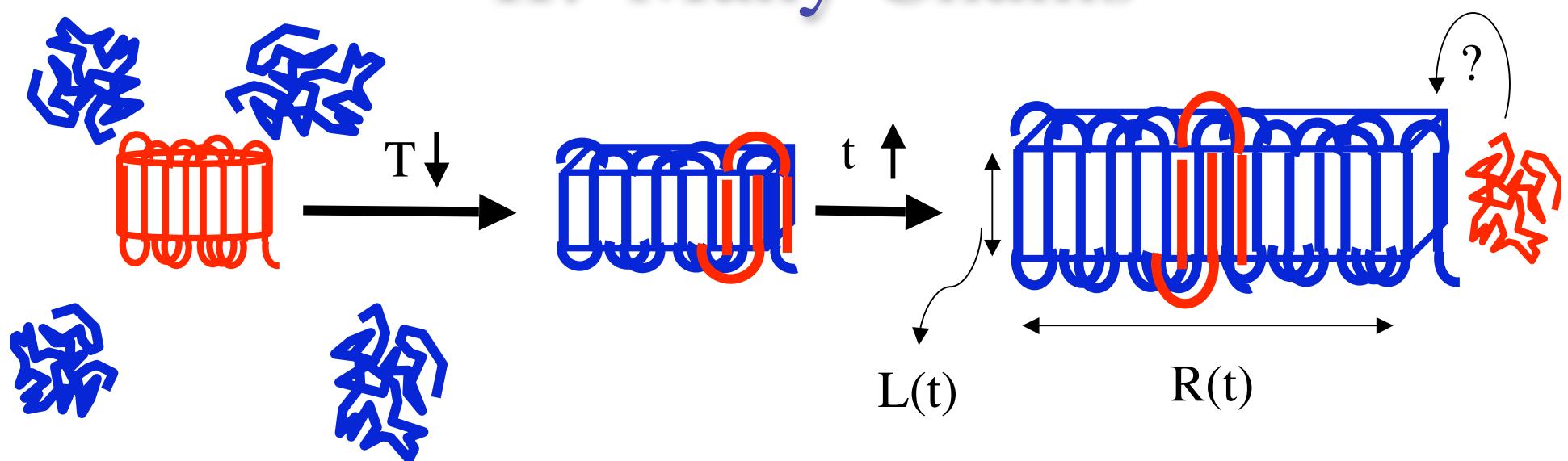
$$e^{-F/k_B T} = \sum e^{-H}$$

# I. Single Chain



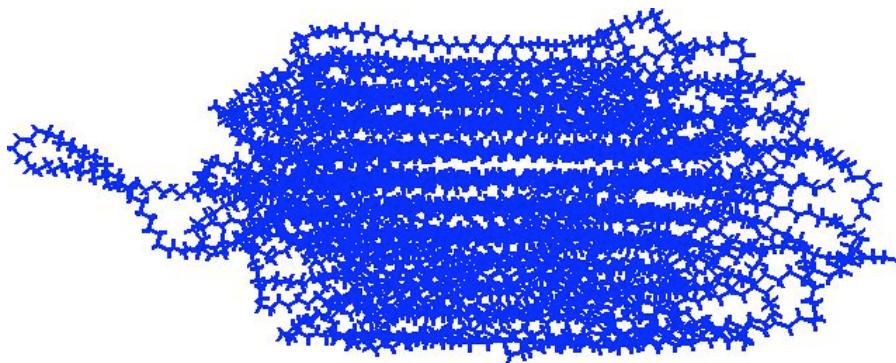
\*Molecular Nature of Kinetics   \*Free Energy Landscape

# II. Many Chains

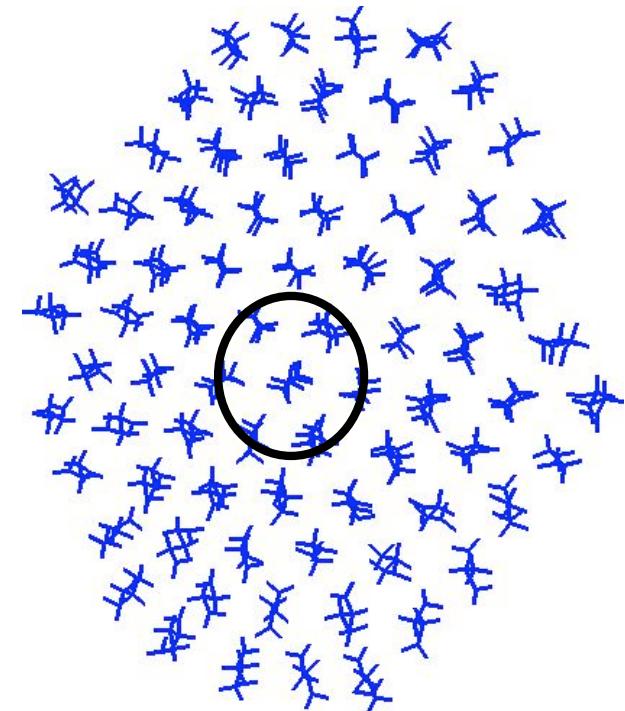


# Atomistic Polyethylene

(20 Chains)

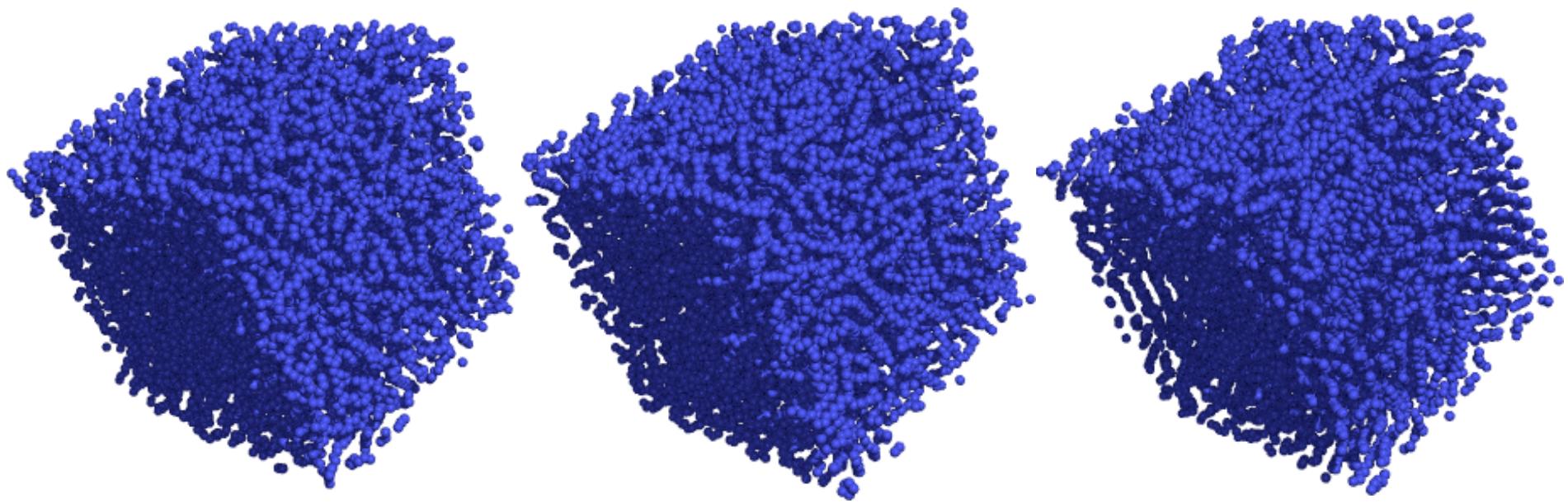


Hexagonal Chain Packing  
Orthorhombic Chain Tilt



(N=12,040)

# Crystallization (Vol. Fraction = 0.5)

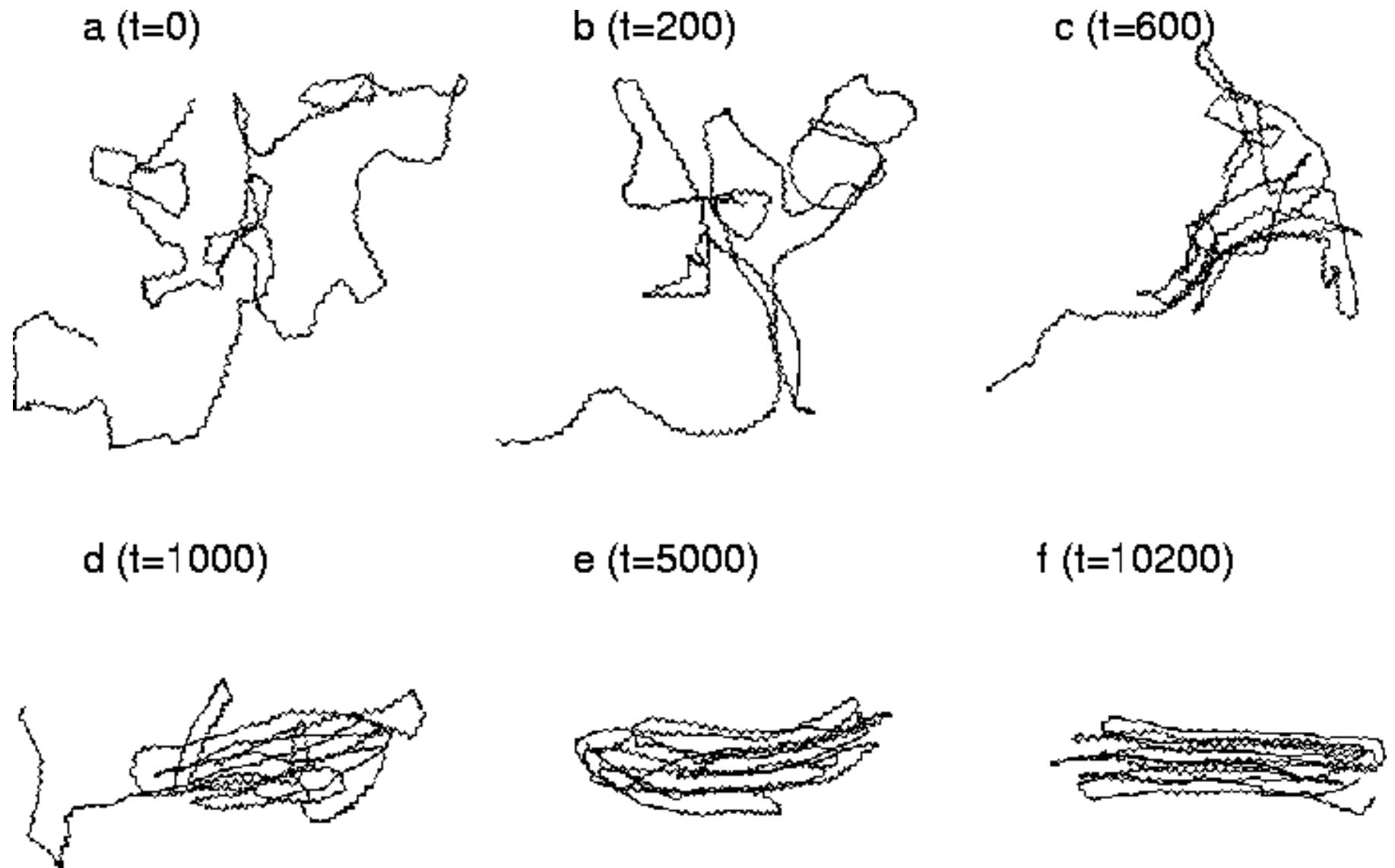


$t < 0$   
 $kT/\epsilon = 20$

$t = 20$   
 $kT/\epsilon = 9$

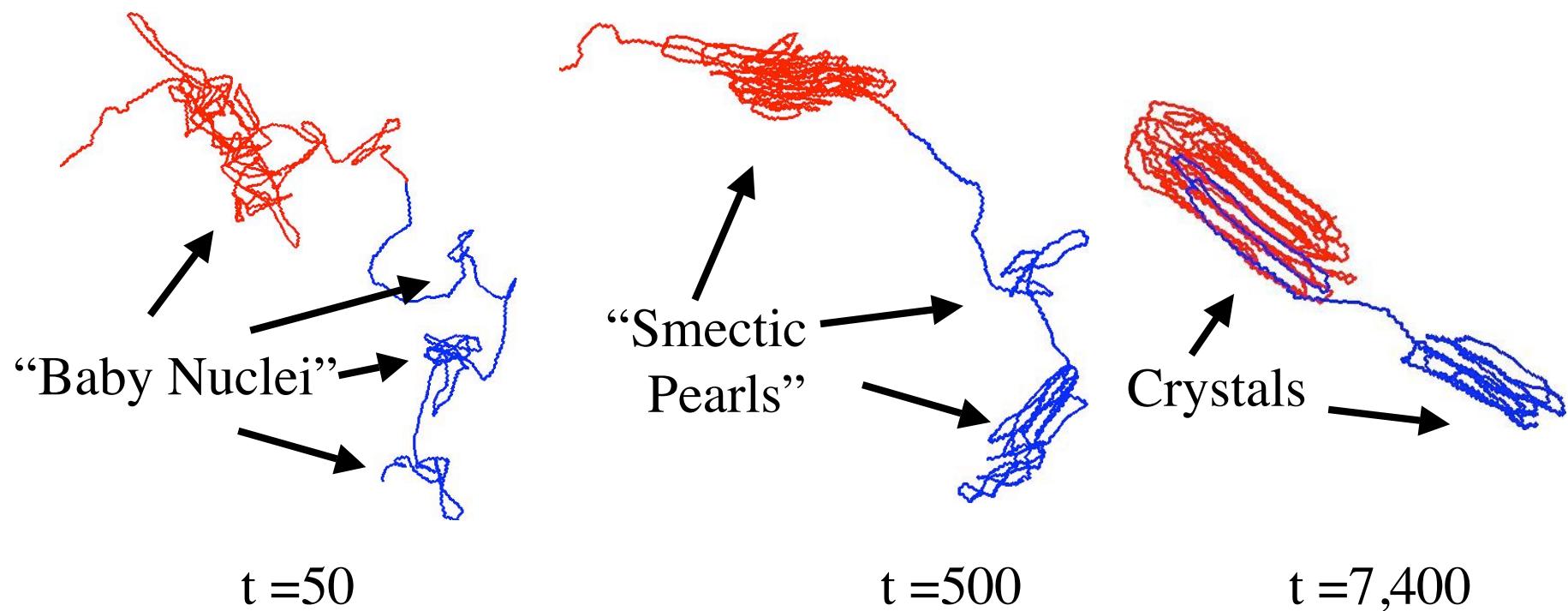
$t = 6860$   
 $kT/\epsilon = 9$

$\Delta T = 2$     $N=200$    75 chains    $N_t = 15,000$

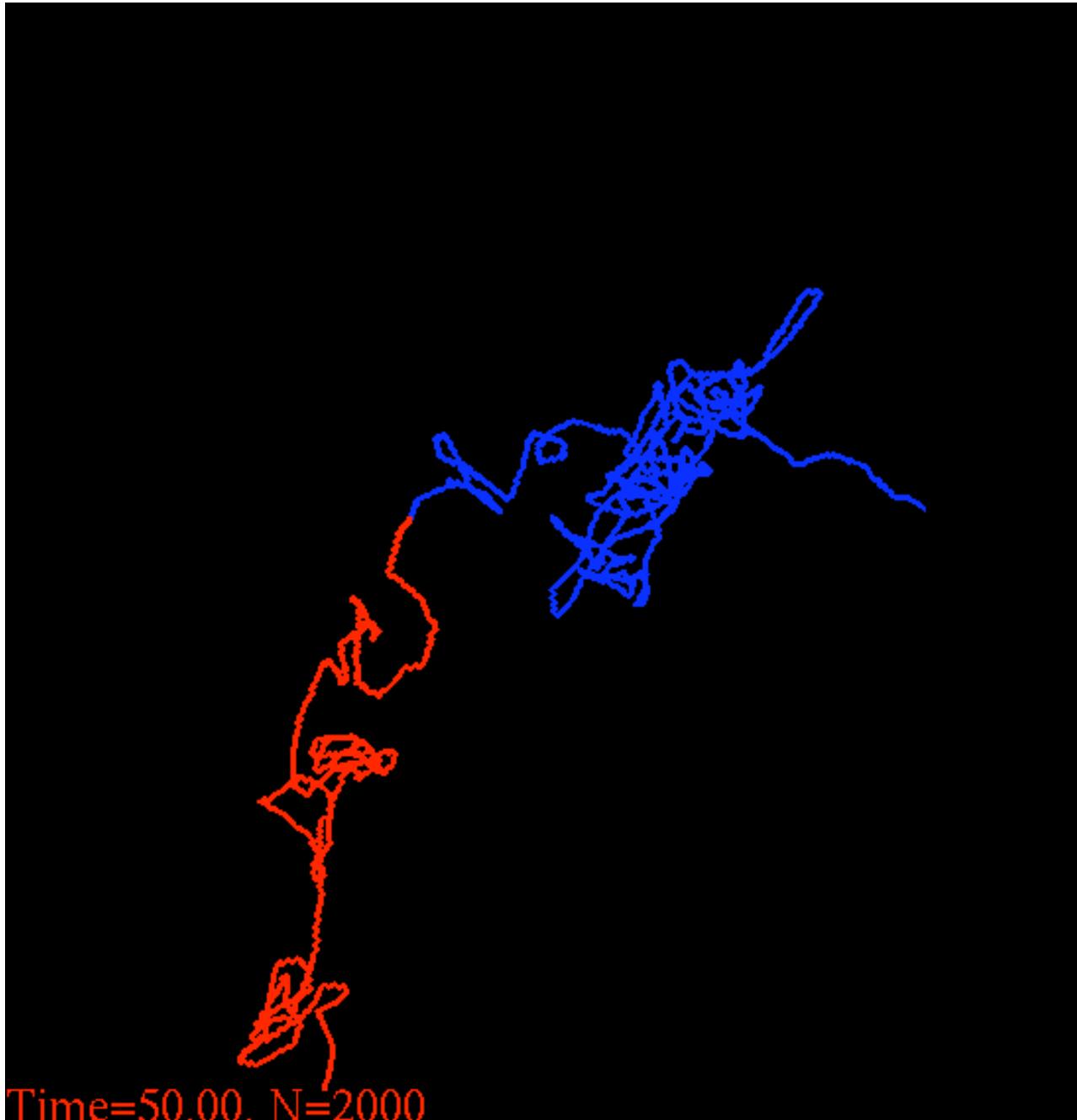


local stiffness versus attraction

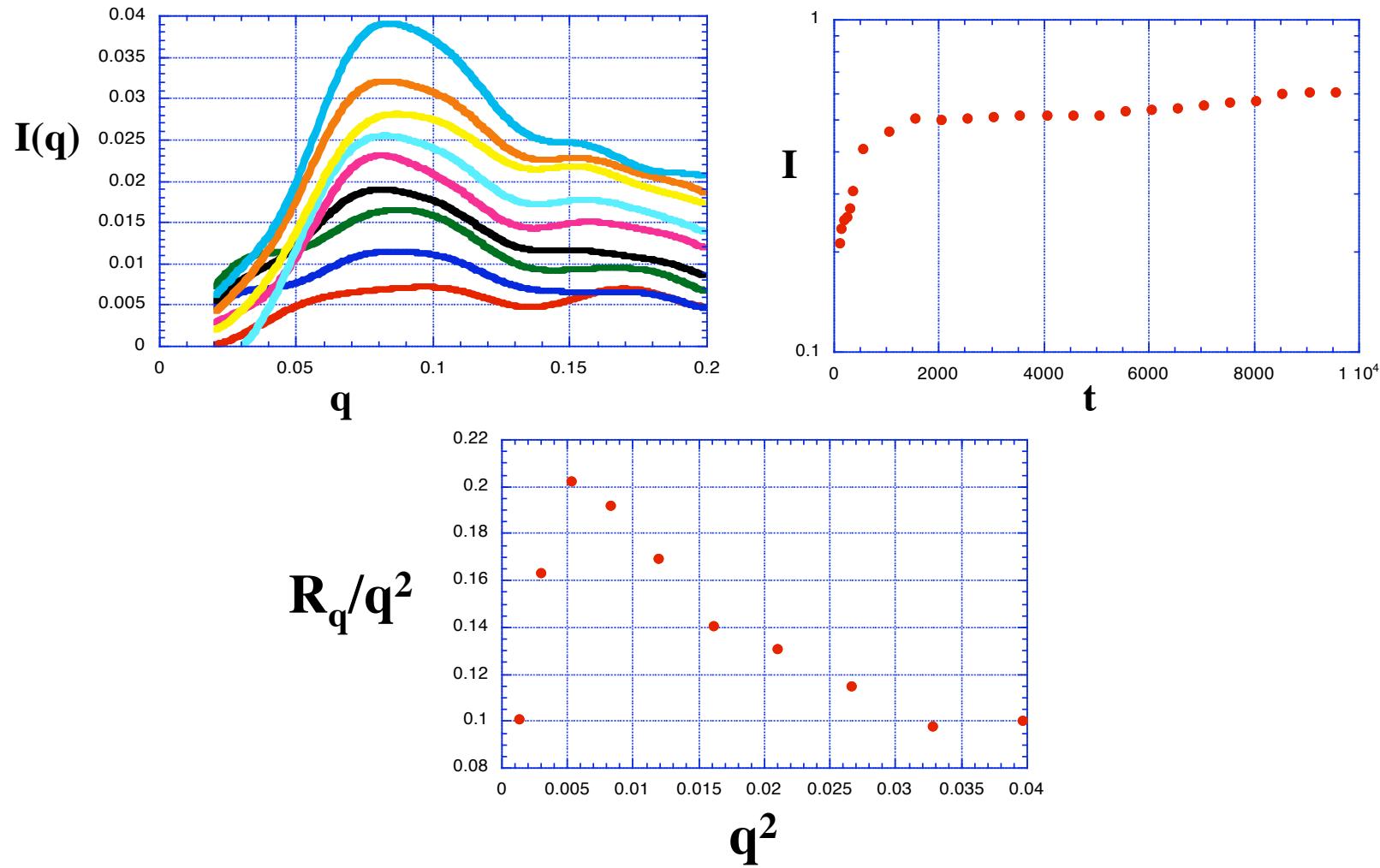
# Early Stage=Nucleation&Growth



MM and P. Welch, *Polymer* **41**, 8833 (2000)



# Simulation Results



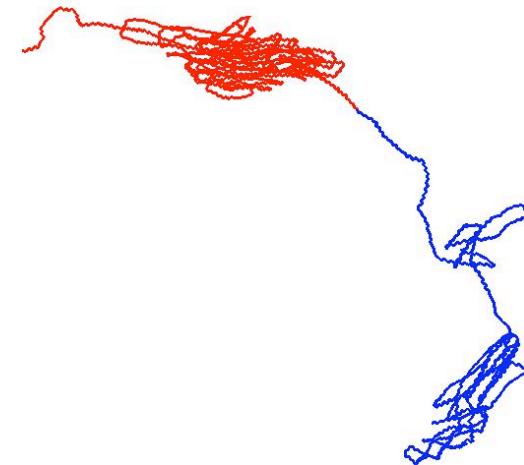
MM and P. Welch, *Polymer* **2000**, *41*, 8833.

# Growth of density fluctuations

$$\Psi = \rho_c - \rho_a$$

$$F \sim \sum_q [-(\Delta T) + q^2 + 1/q^2] |\Psi_q|^2$$

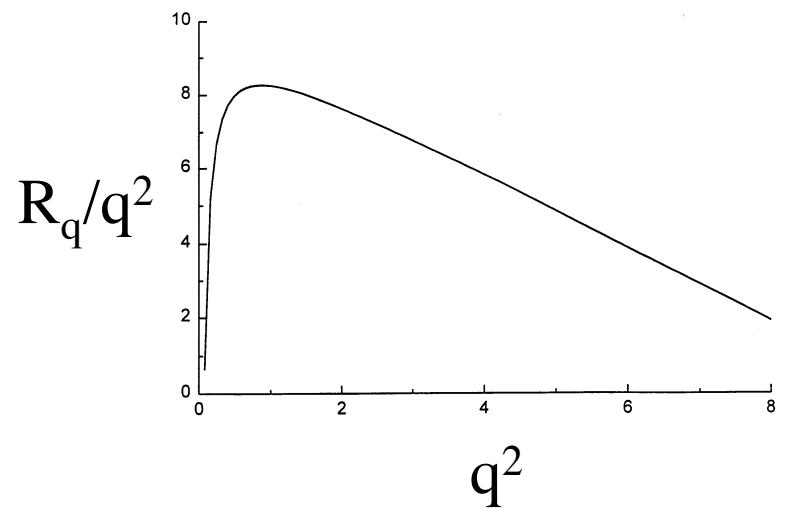
quench depth      crystal-amorphous interface      chain connectivity



$$\partial \Psi_q / \partial t \sim -q^2 [-(\Delta T) + q^2 + 1/q^2] \Psi_q$$

$$\Psi_q(t) \sim \exp(R_q t)$$

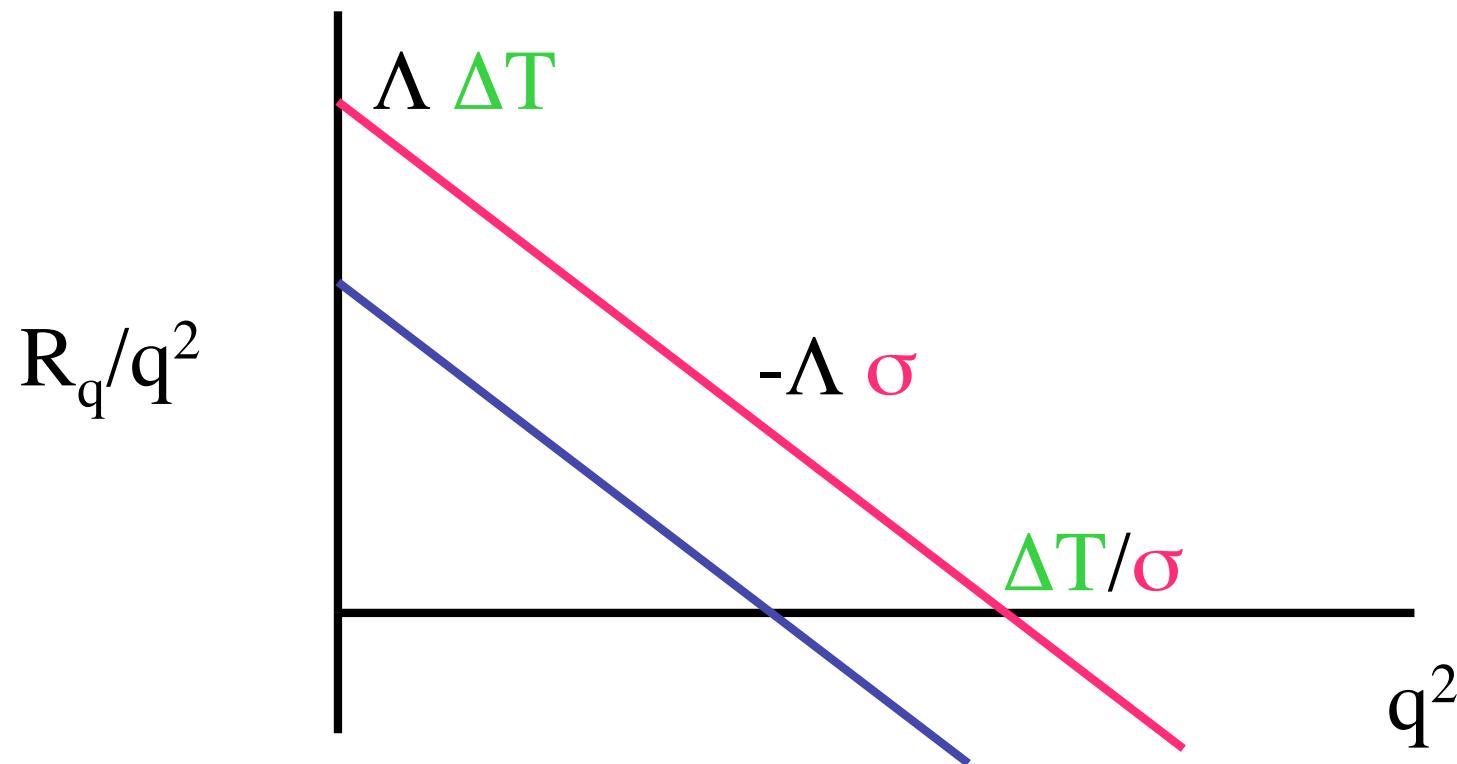
$$R_k/q^2 = \Delta T - q^2 - 1/q^2$$

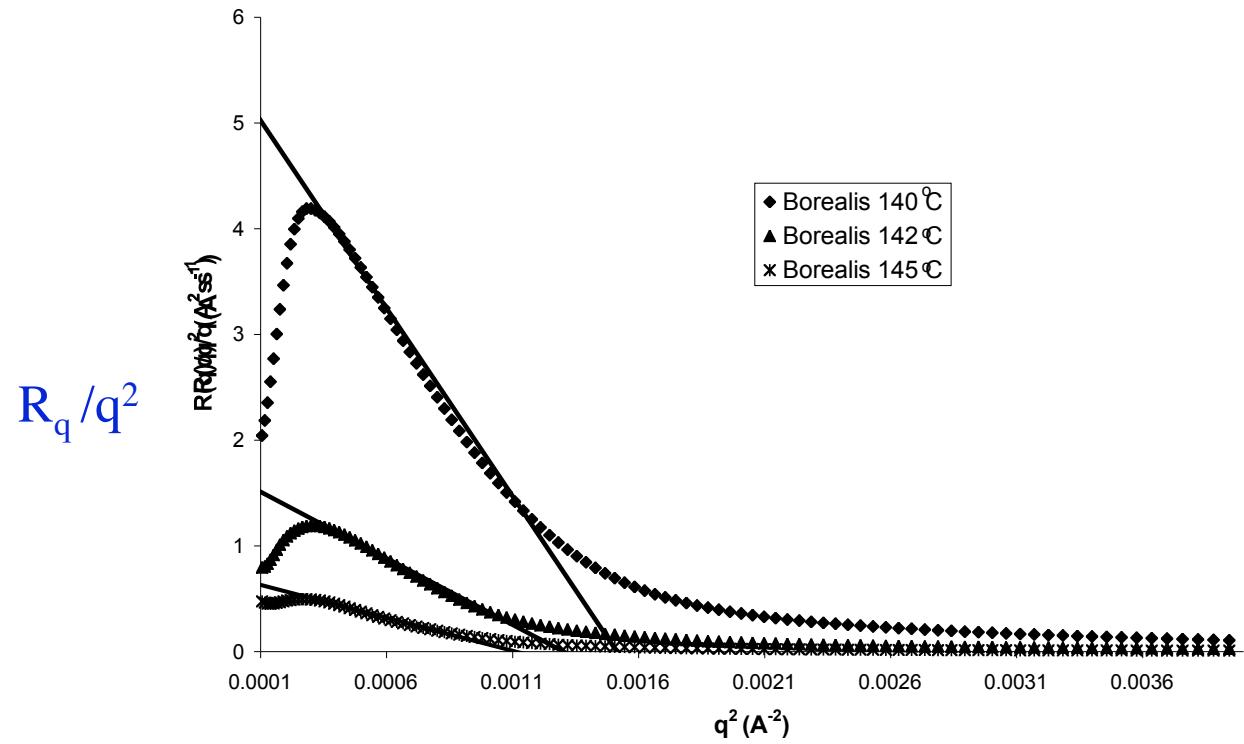


# Spinodal Decomposition

$$F \sim \sum_q [-(\Delta T) + \sigma q^2] |\Psi_q|^2$$

$$\begin{aligned}\partial \Psi_q / \partial t &= -\Lambda q^2 [-(\Delta T) + \sigma q^2] \Psi_q \\ &= R_q \Psi_q\end{aligned}$$





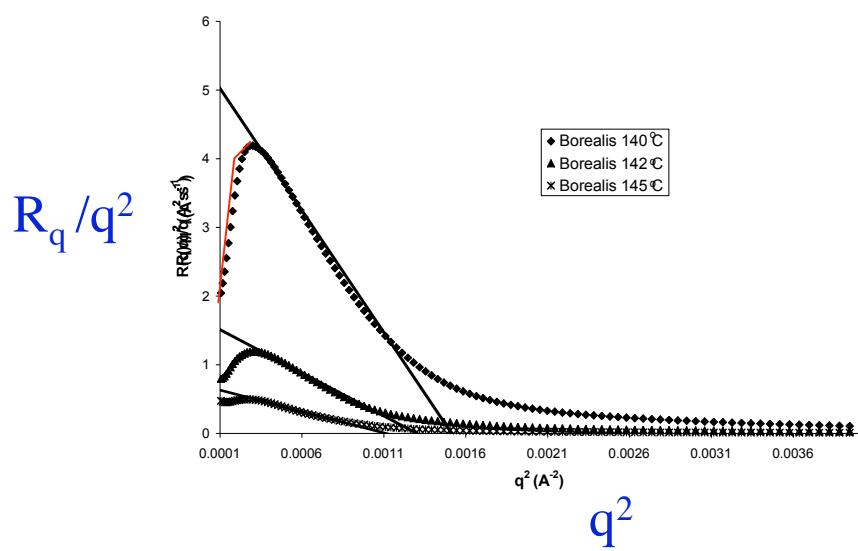
A.J. Ryan and collaborators (I-PP)

# *Early stage of polymer crystallization*

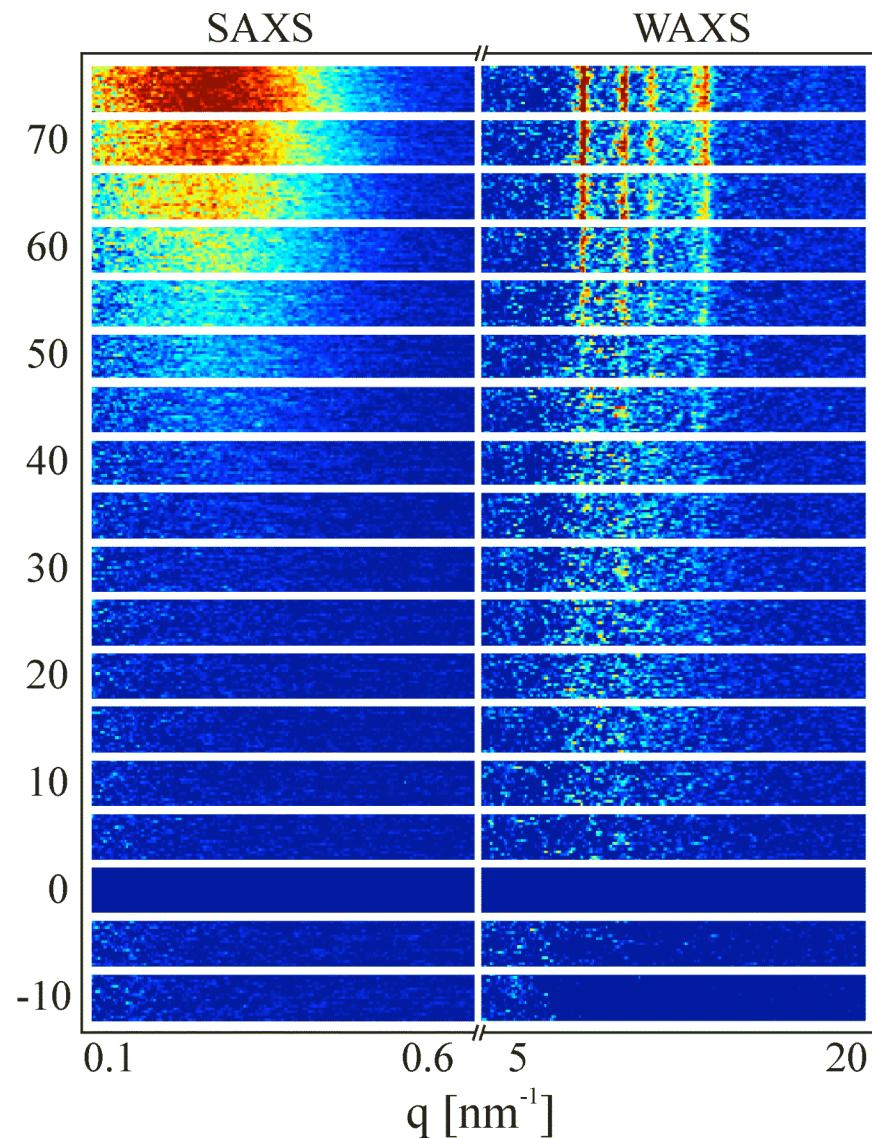
P. Panine *et al.*, Polymer (2008)

## Isotactic polypropylene

Melt is cooled rapidly ( $80\text{ }^{\circ}\text{C}/\text{min}$  from  $210\text{ }^{\circ}\text{C}$  to the crystallization temperature ( $145\text{ }^{\circ}\text{C}$ ))

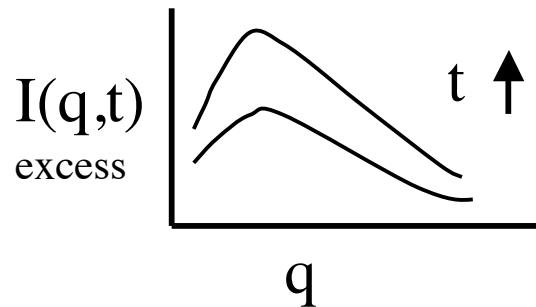


A.J. Ryan and collaborators (I-PP)



# Conclusion #1

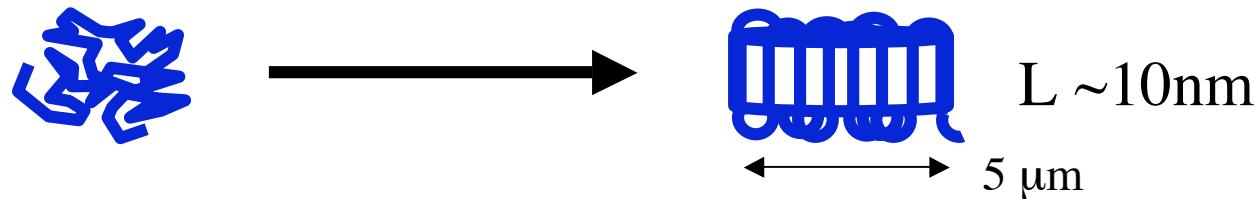
Early stage of polymer crystallization:



Initial stage of crystallization is **NUCLEATION** with each chain participating in several nuclei.

**NOT** spinodal decomposition

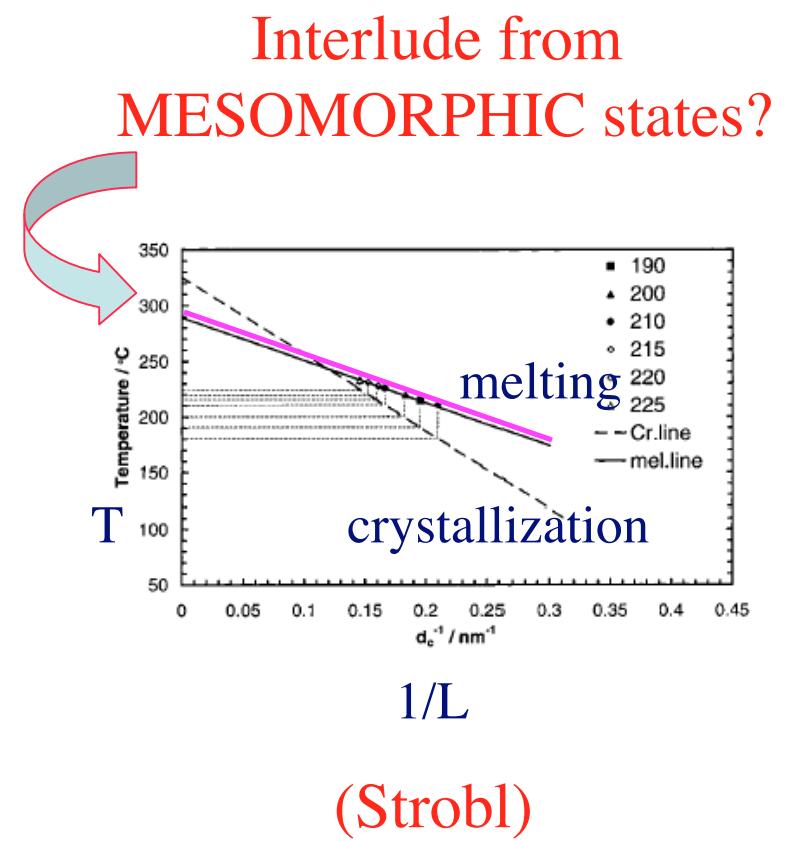
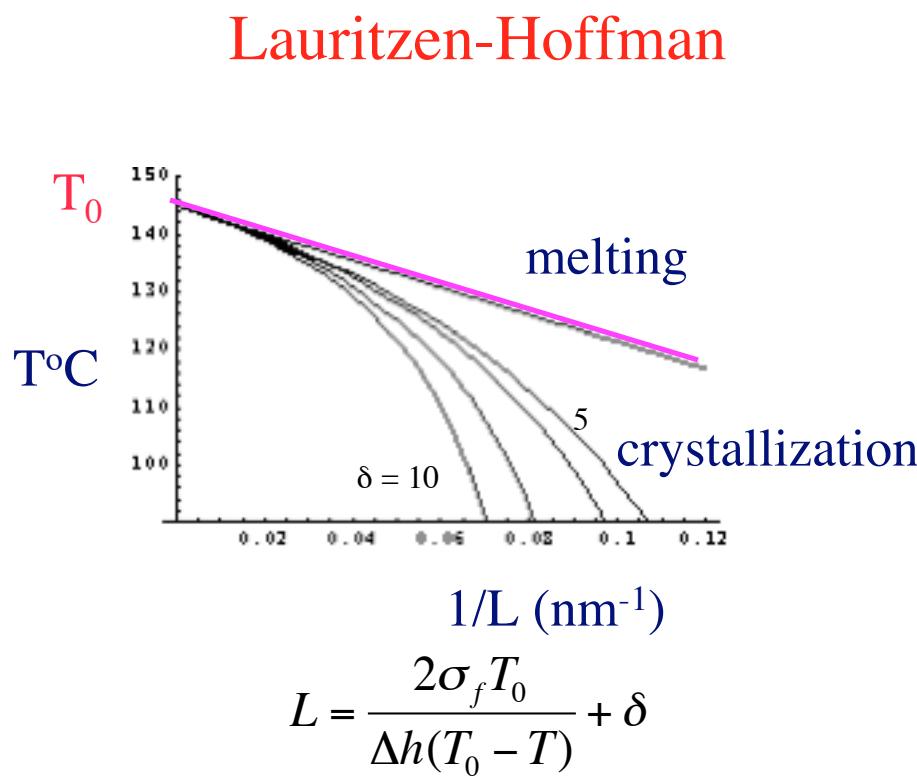
Further support from R. Alamo (FTIR) and  
C. Schick (ultrafast cold crystallization)

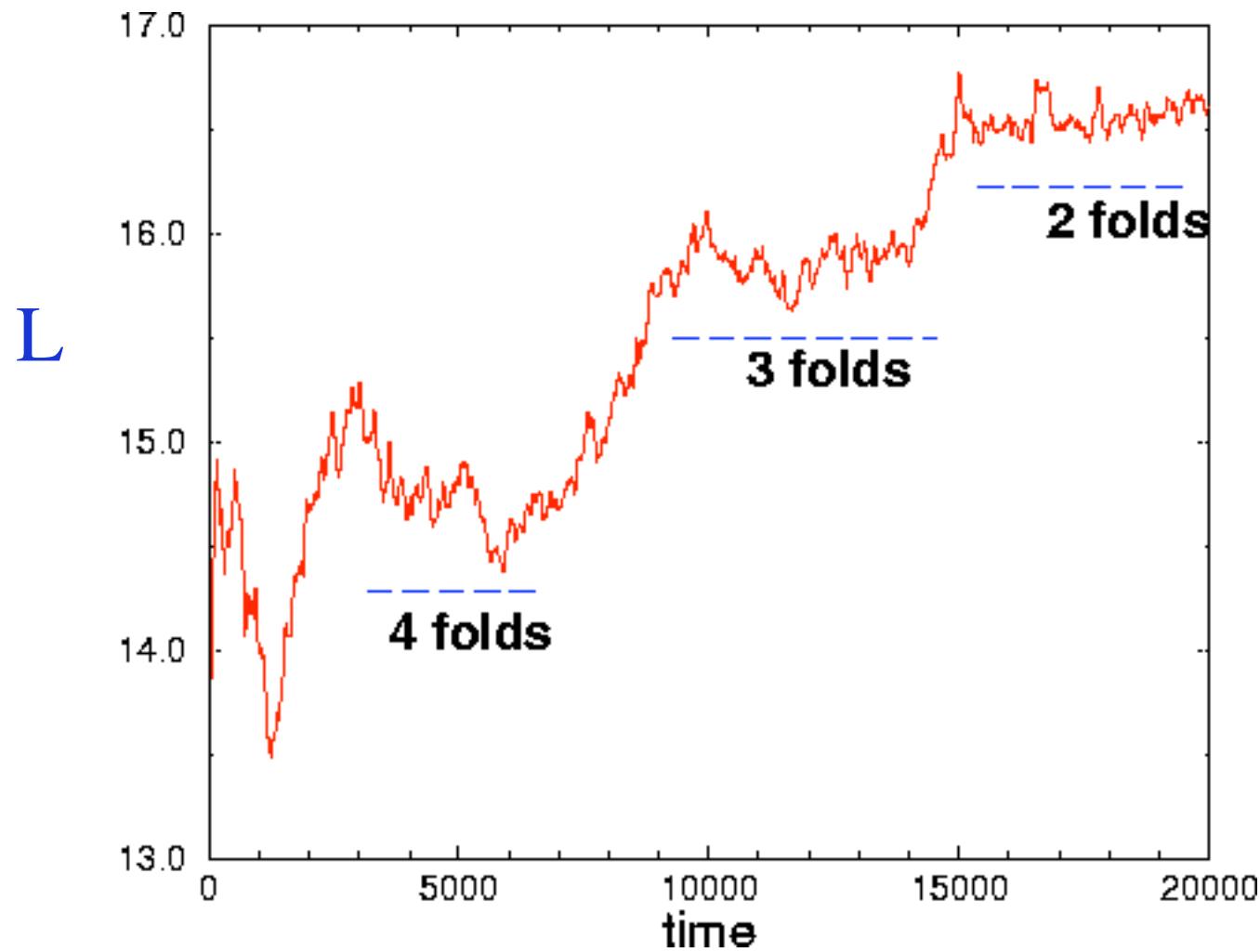


## 2. Spontaneous selection of lamellar thickness

(L << extended chain dimension)

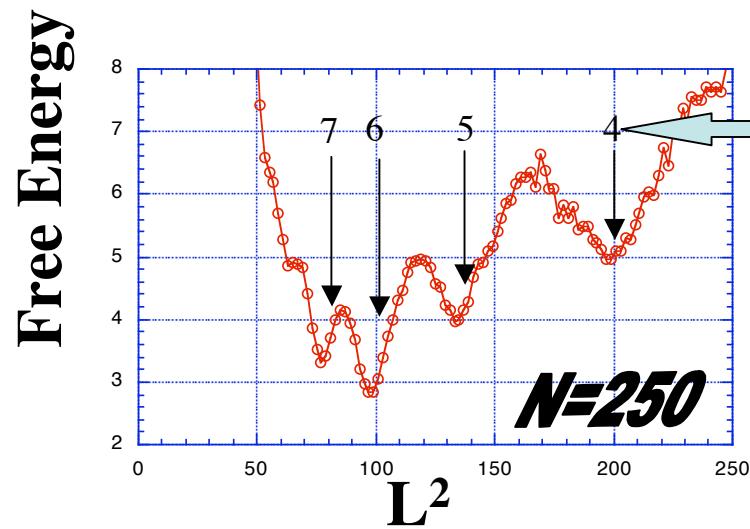
=> “KINETICALLY CONTROLLED”



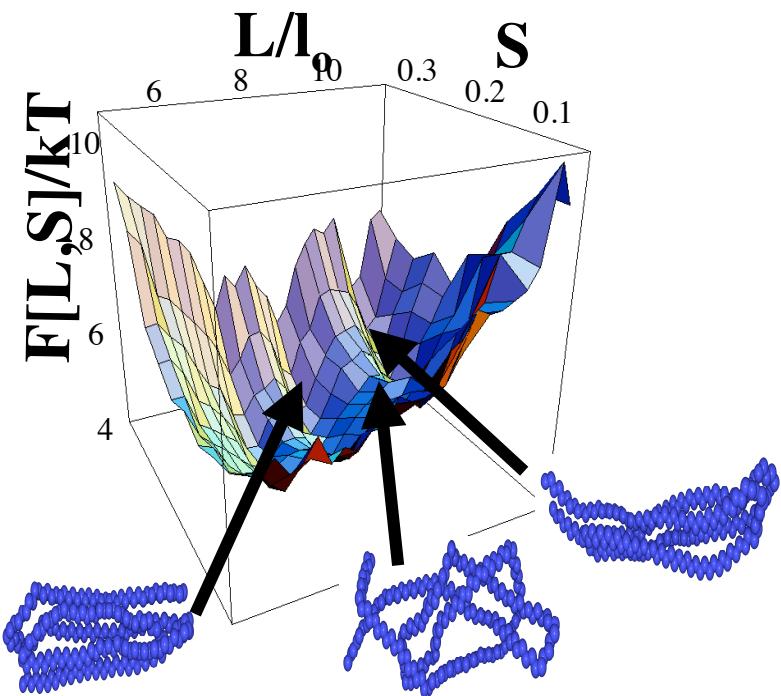


“Quantization of Lamellar Thickness”  
(Agrees with Keller’s experiments)

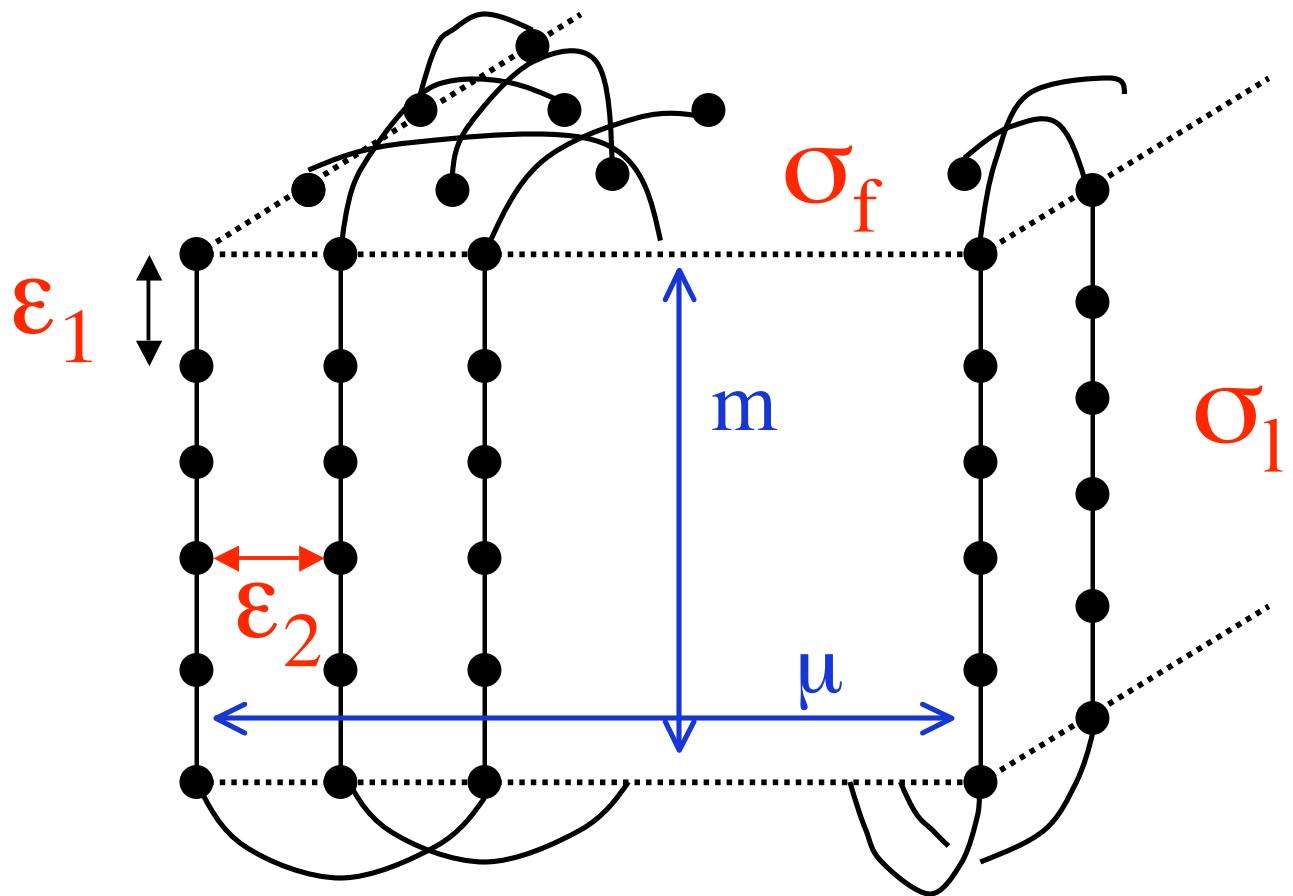
# Simulations



Number of Stems



Welch and MM, *Phys. Rev. Lett.*, **87**, 218302-1 (2001)



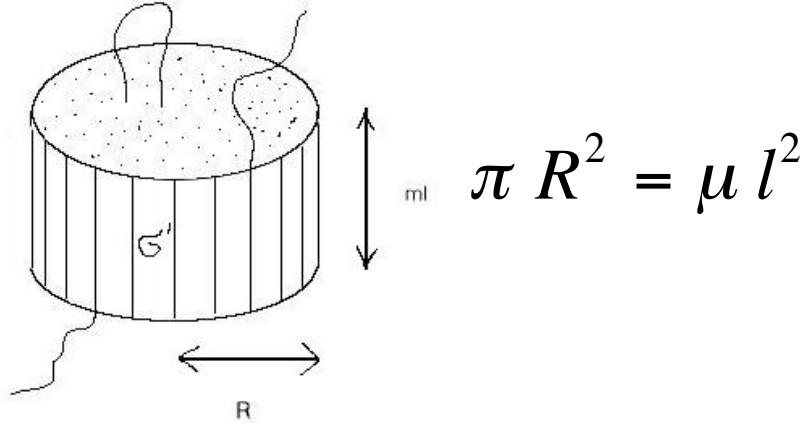
$\varepsilon_1$ =chain stiffness energy

$\varepsilon_2$ =interaction energy of  
non-bonded neighbors

$m$ =lamellar thickness

$\mu$ =number of stems/chain

$$\frac{F}{k_B T} = f_{bulk}(T = \frac{1}{\varepsilon_2}, \varepsilon = \frac{\varepsilon_1}{\varepsilon_2}, m, \mu, N) + f_{loops}(m, \mu, N) + f_{surface}(\sigma_l, \sigma_f)$$



Let one chain have  $\mu$  stems with  $(\mu-1)$  loops and two tails.

$$\frac{F_{m,\mu}}{k_B T} = -\mu m \varepsilon + \sigma \mu^{1/2} m - \ln(Z_{m,\mu})$$

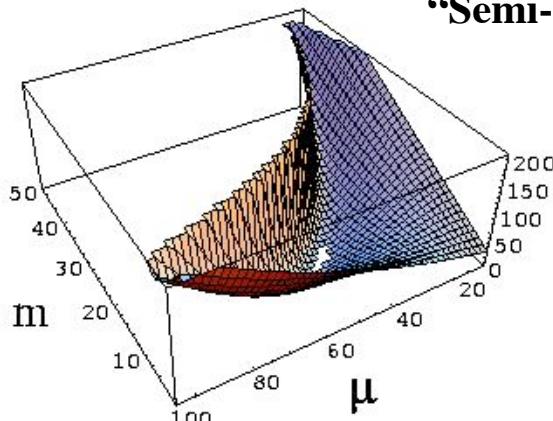
bulk energy                                    lateral surface energy                            chain entropy

**Field Theory:**  
*MM, Phil.Trans.Roy.Soc., 361A, 539 (2003)*

$$Z_{m,\mu} = \oint \frac{dE}{2\pi i} e^{E(N-\mu m)} g_{tail}^2(E) g_{loop}^{\mu-1}(E; l_c)$$

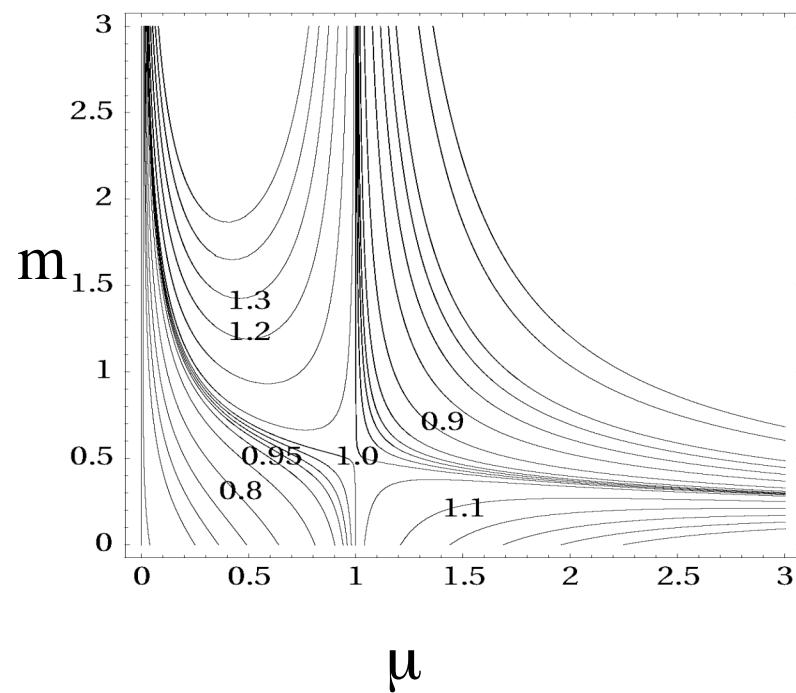
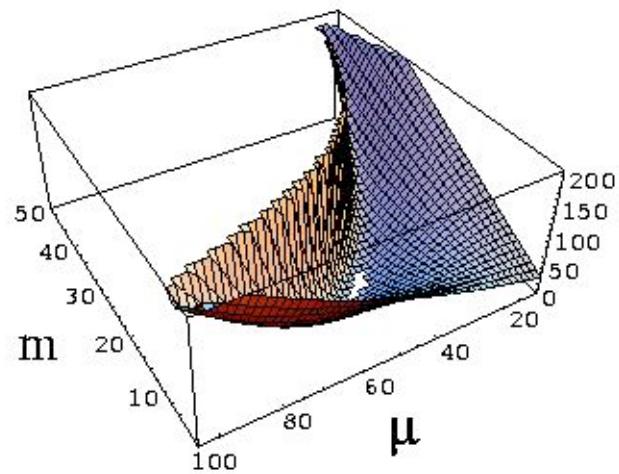
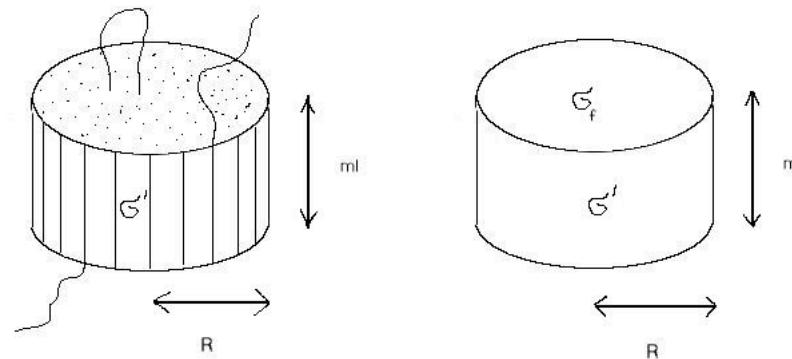
“Semi-infinite space”

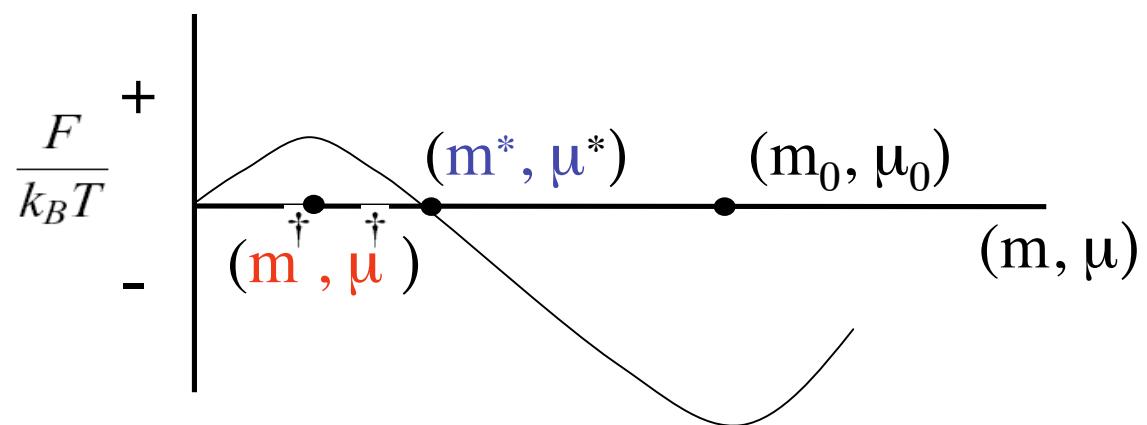
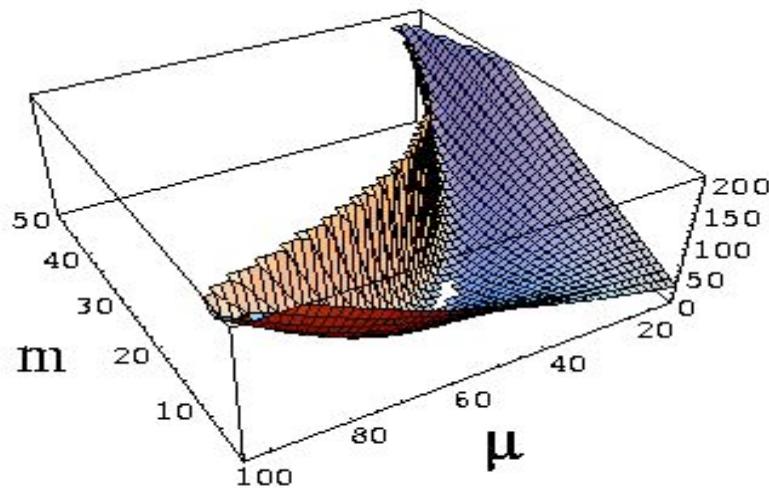
⇒ Finite thickness is Equilibrium

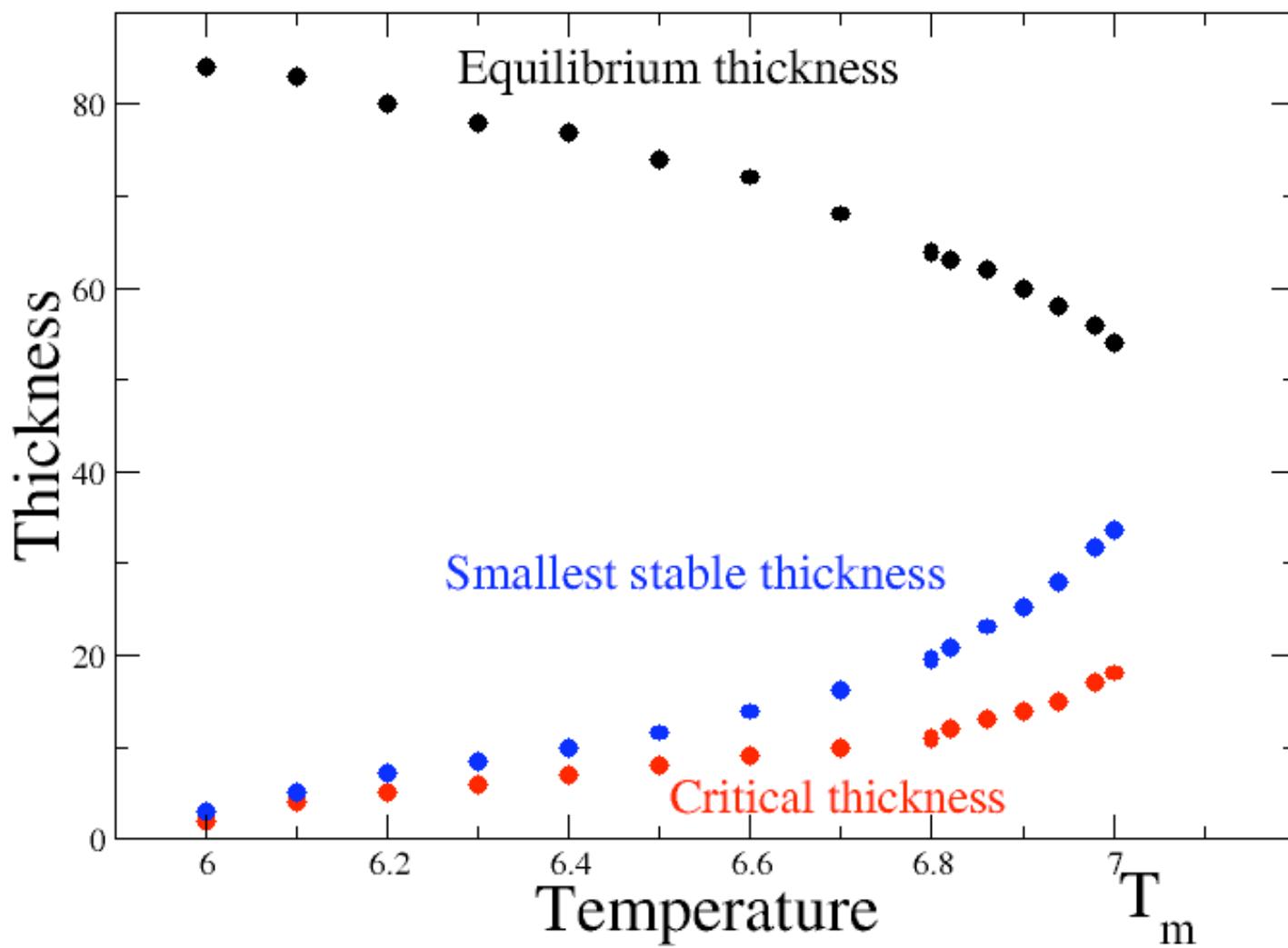
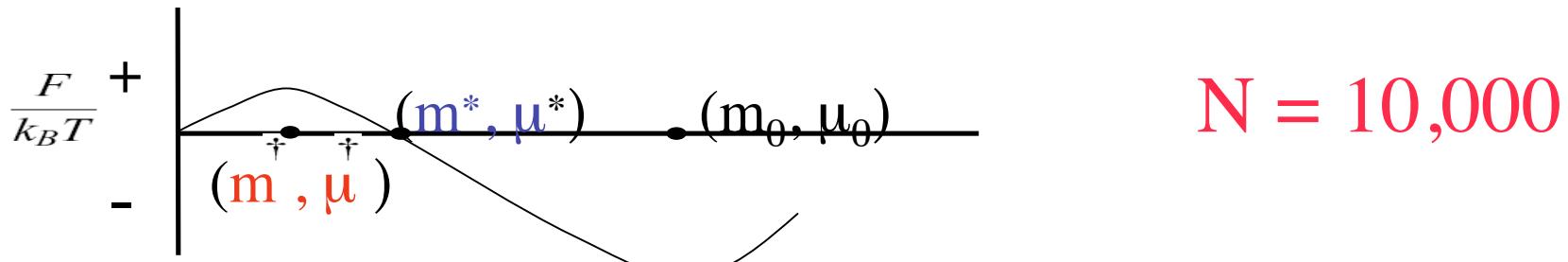


$$N = 1000, \varepsilon = 1, \sigma = 5, l_c/l = \sqrt{32/3}$$

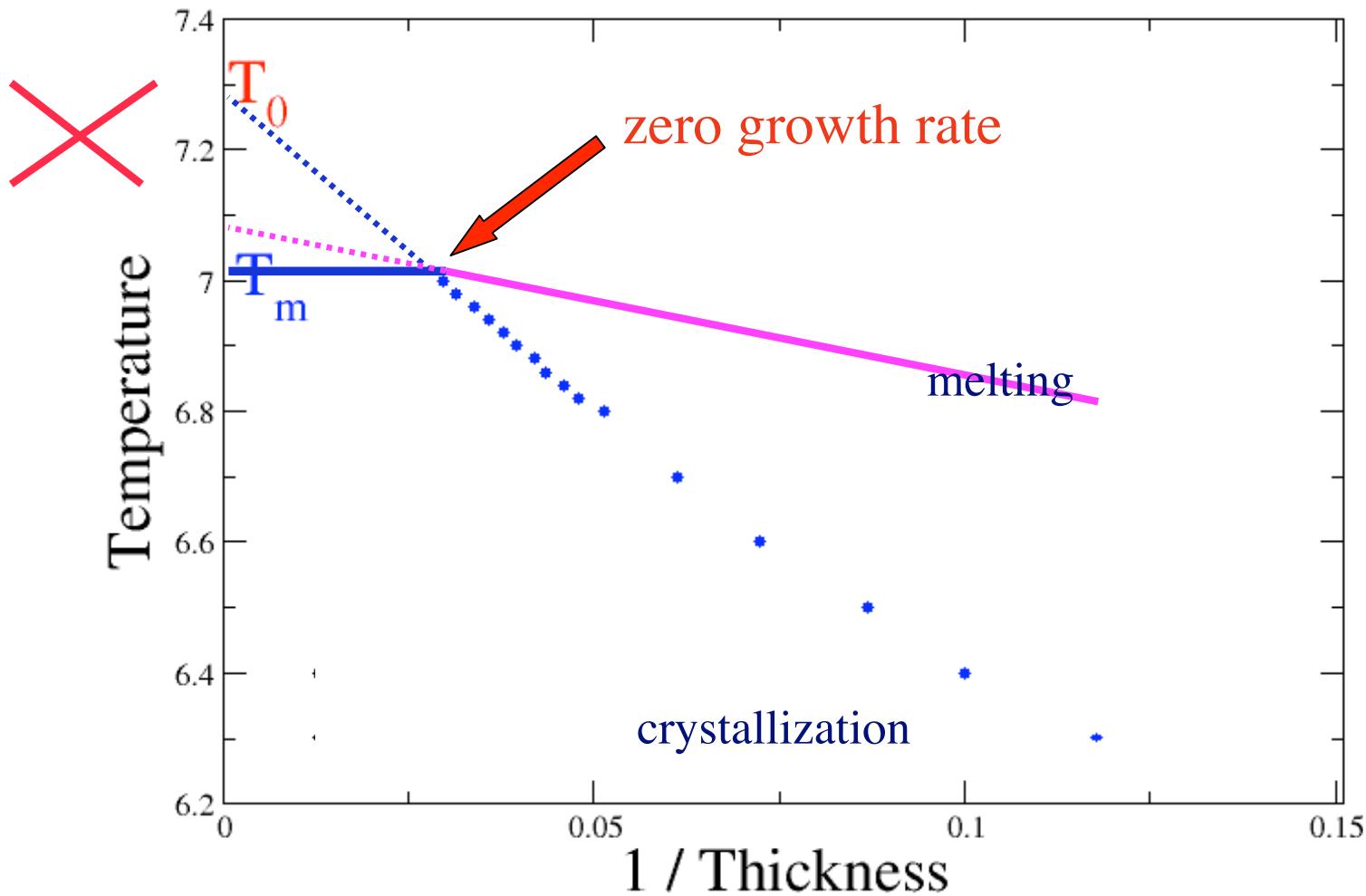
# THEORY





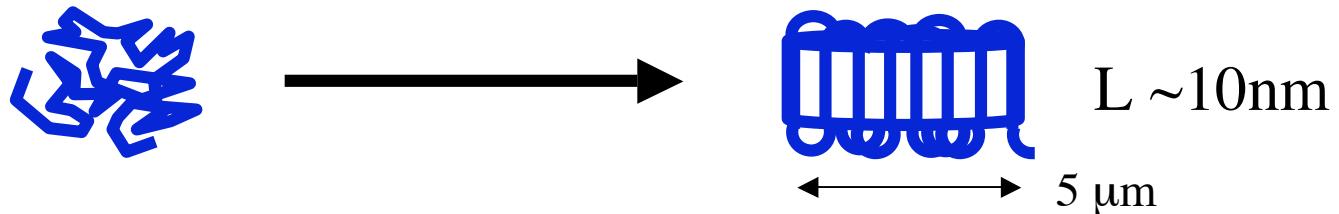


$N = 10,000$



(Experimentally confirmed by Ungar, Rastogi, Strobl,...)

## Conclusion #2



1. Spontaneous selection of lamellar thickness

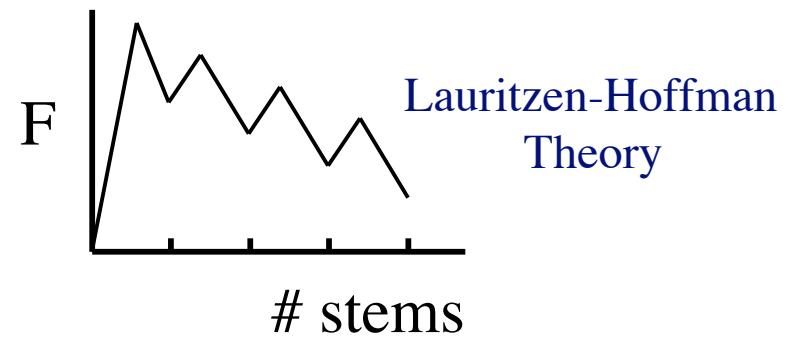
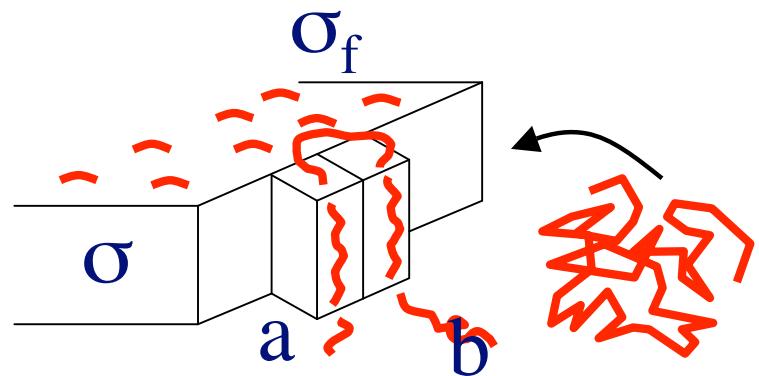
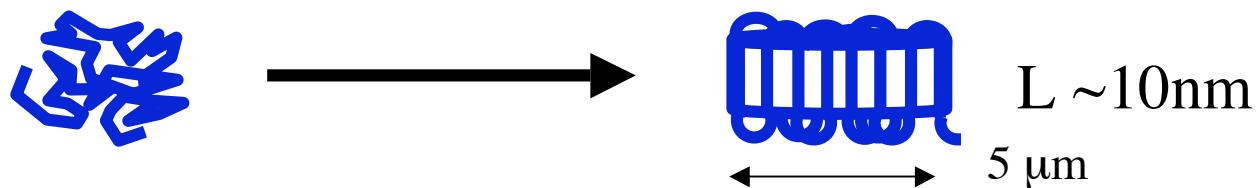
( $L \ll$  extended chain dimension)

=> “KINETICALLY CONTROLLED”

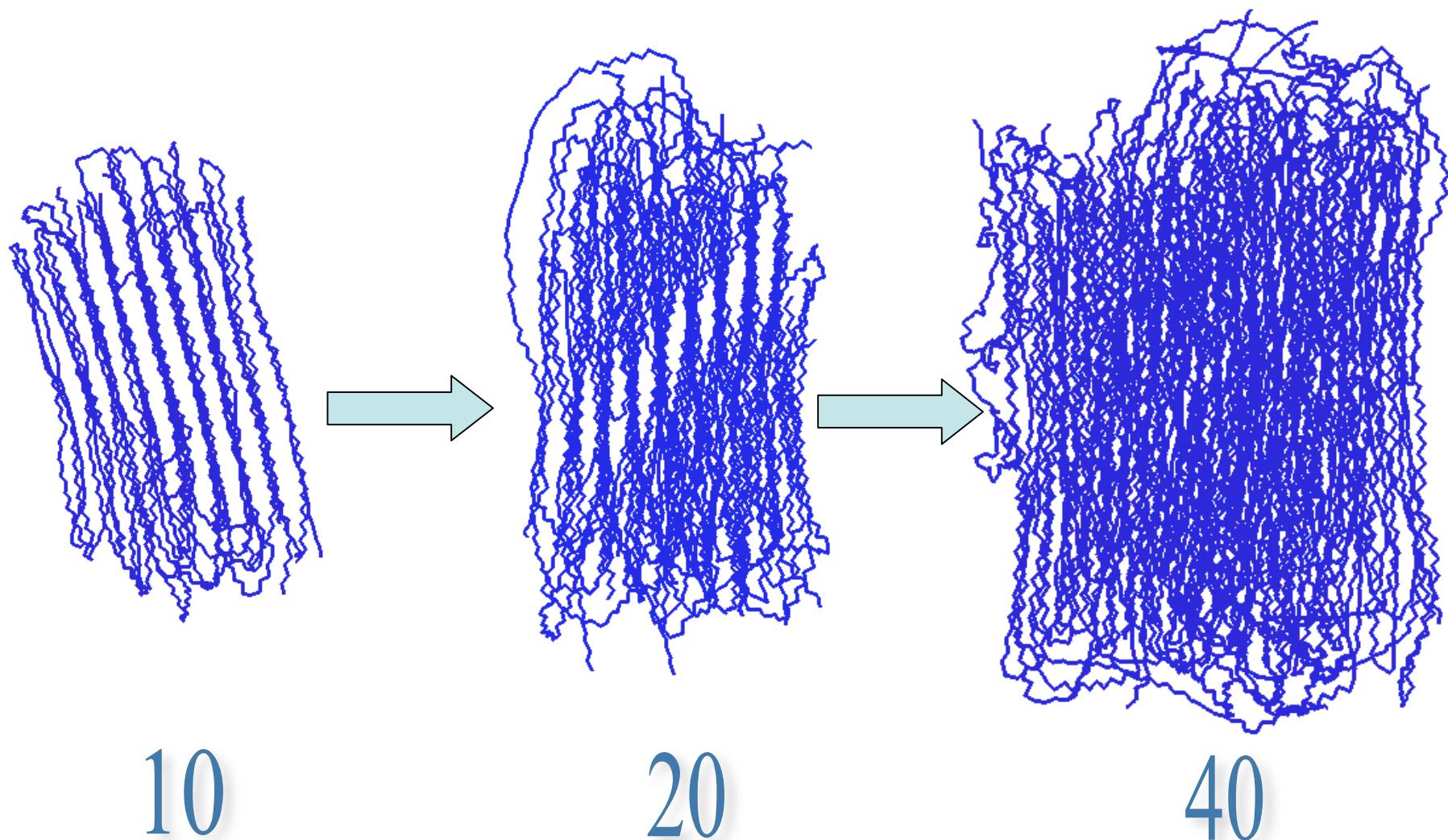
Lamellae evolve through several metastable states to reach an **EQUILIBRIUM** thickness much smaller than the extended chain dimension.

2. No stable mesomorphic phase for flexible chains

### 3. Kinetics at growth front

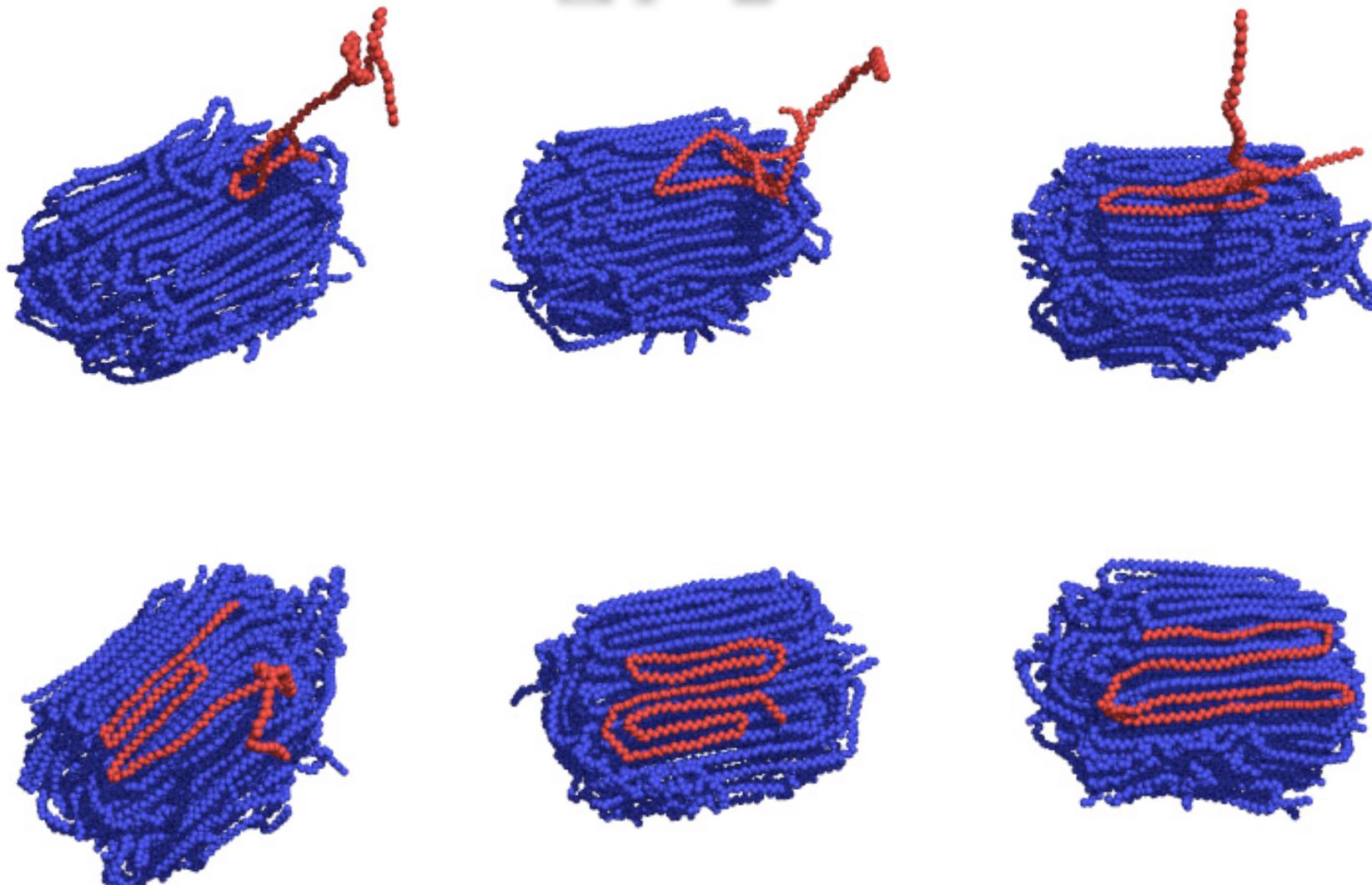


# Multi-Chain Study

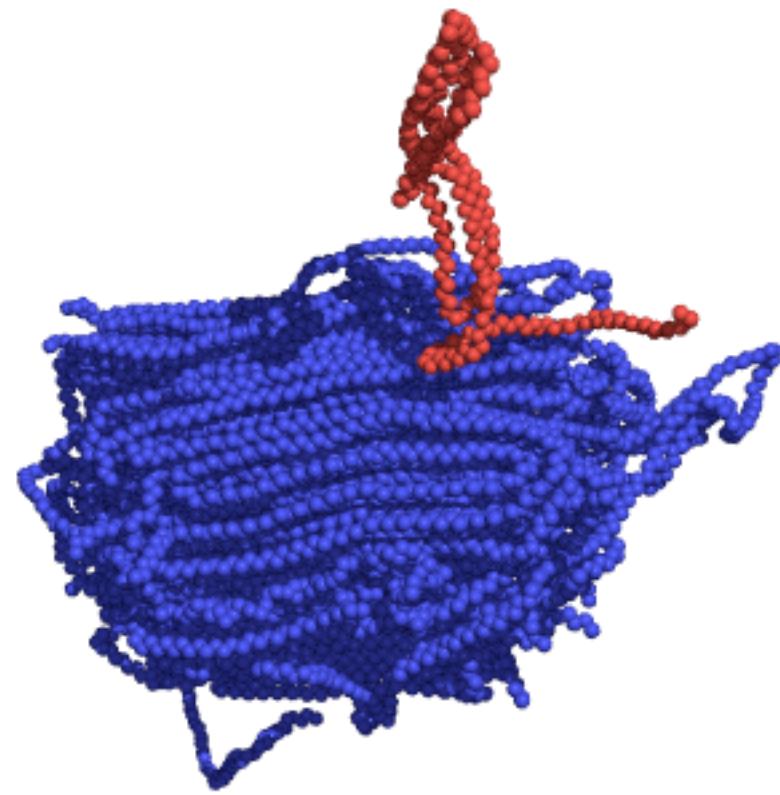


# Addition to the Growth Front

$\Delta T=2$

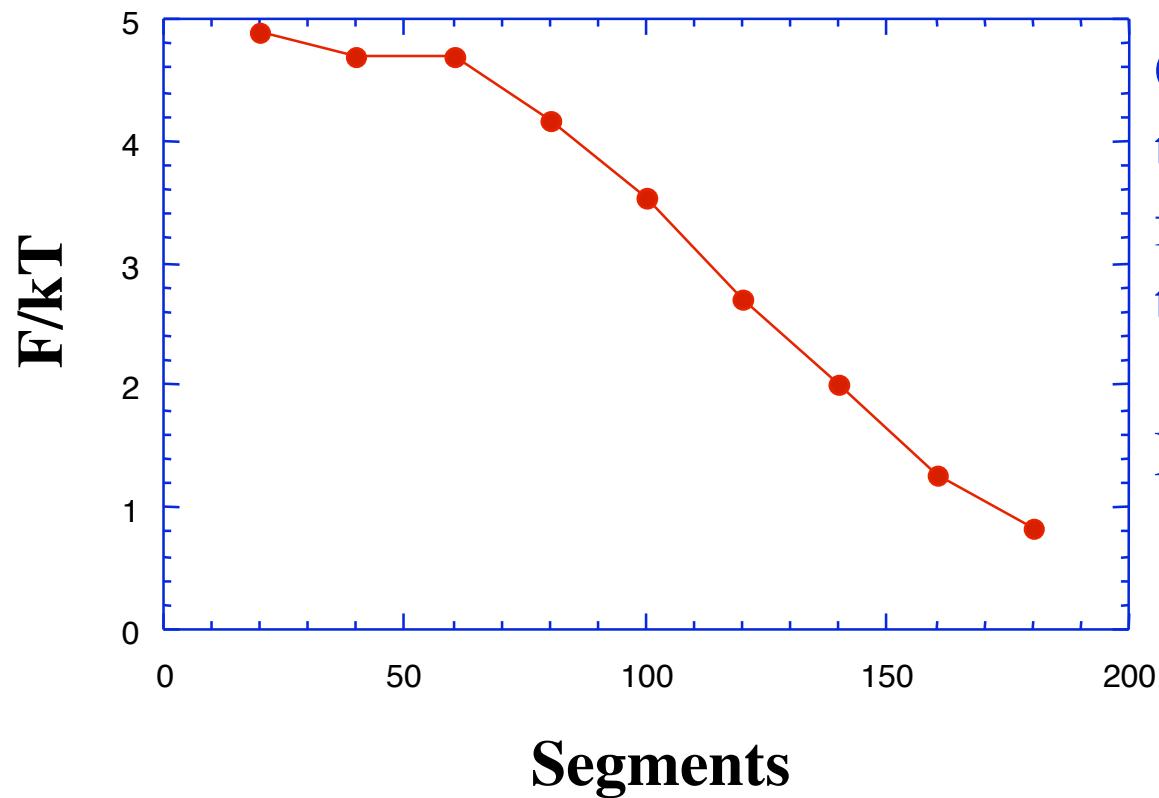


Welch and Muthukumar, *Phys. Rev. Lett.*, **87**, 218302-1 (2001)



# Free Energy

“Lamellar growth is chain **ADSORPTION**”



Our Estimate of  
the Free Energy  
for Segment Addition  
to the Growth Front

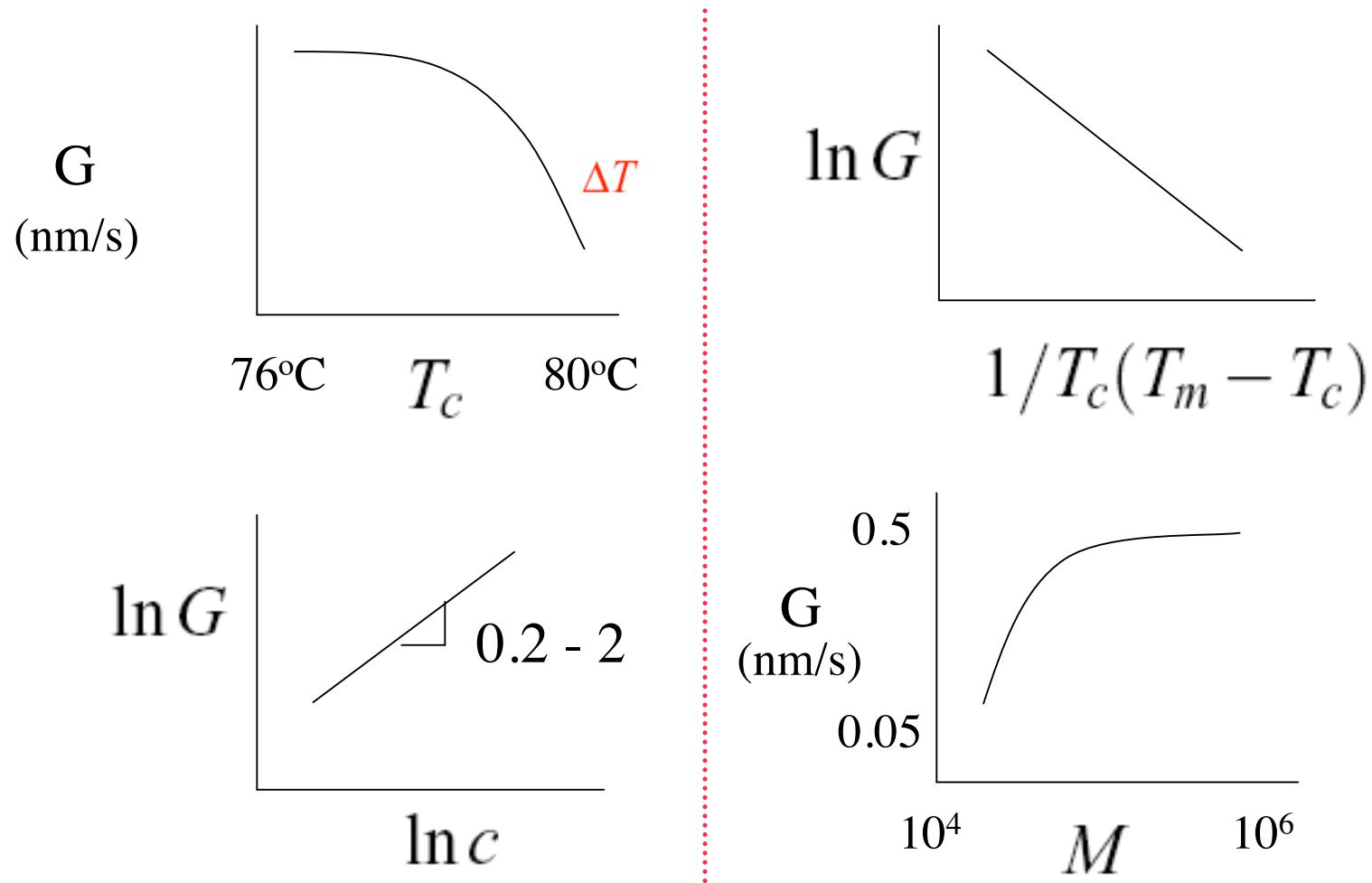
No Barrier is Observed

Based on ~4500 Samples

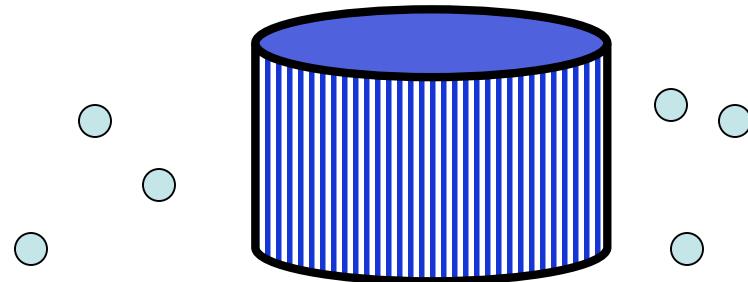
Welch and Muthukumar, *Phys. Rev. Lett.*, **87**, 218302-1 (2001)

# Phenomenology

## Kinetics at GROWTH FRONT



# Surface Growth (small molecules):



Growth rate:

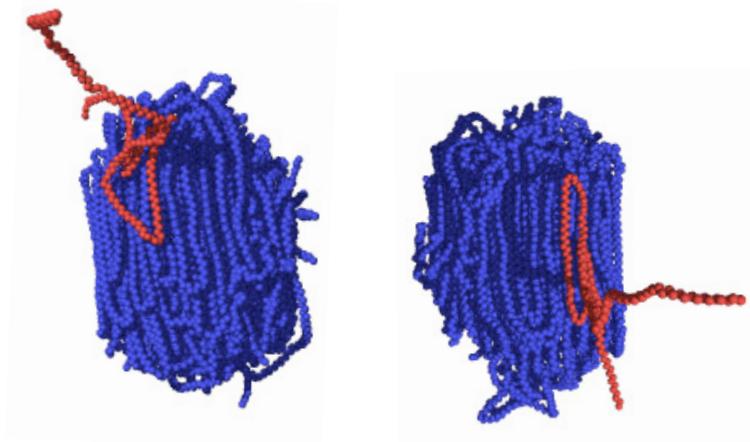
$$G \sim C [1 - e^{-\frac{(\Delta H)(\Delta T)}{kT_m T}}]$$

↑                      ↑  
adsorption            desorption

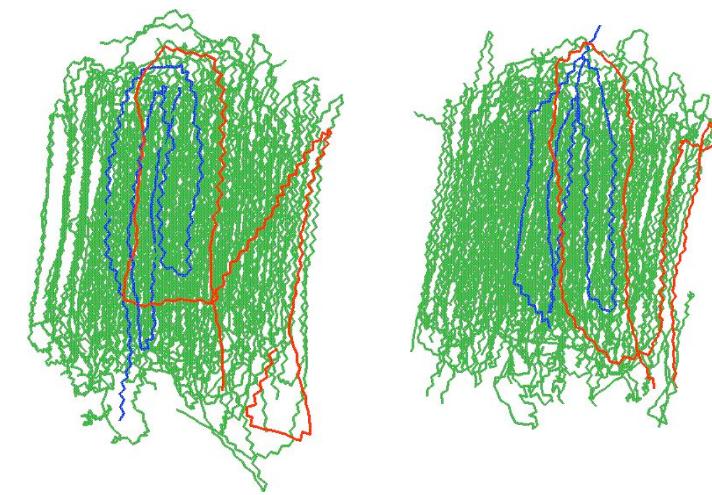
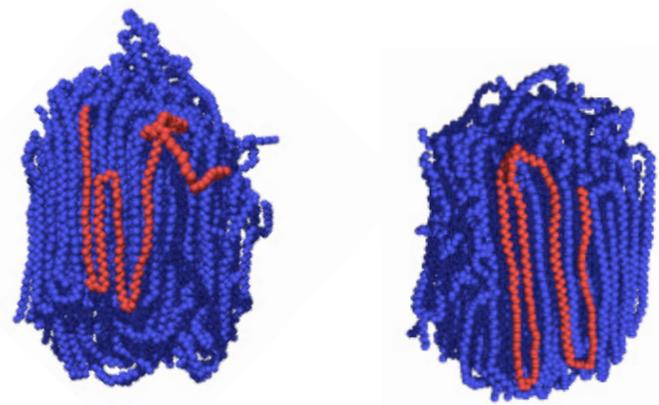
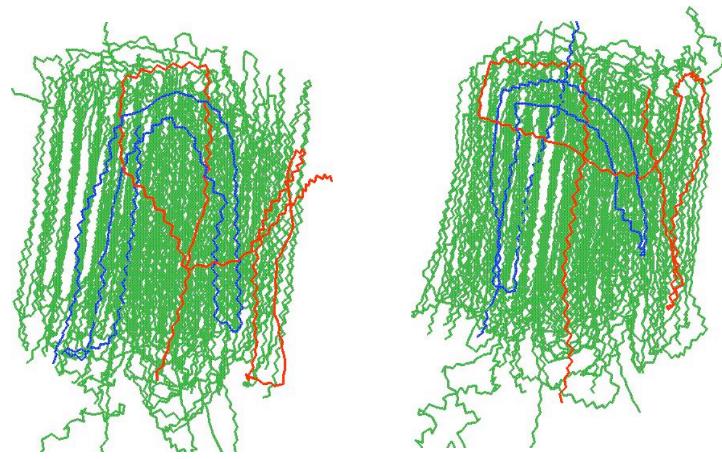
(Detailed Balance)

$$G \sim \Delta T , \quad T_c \rightarrow T_m$$

Dilute

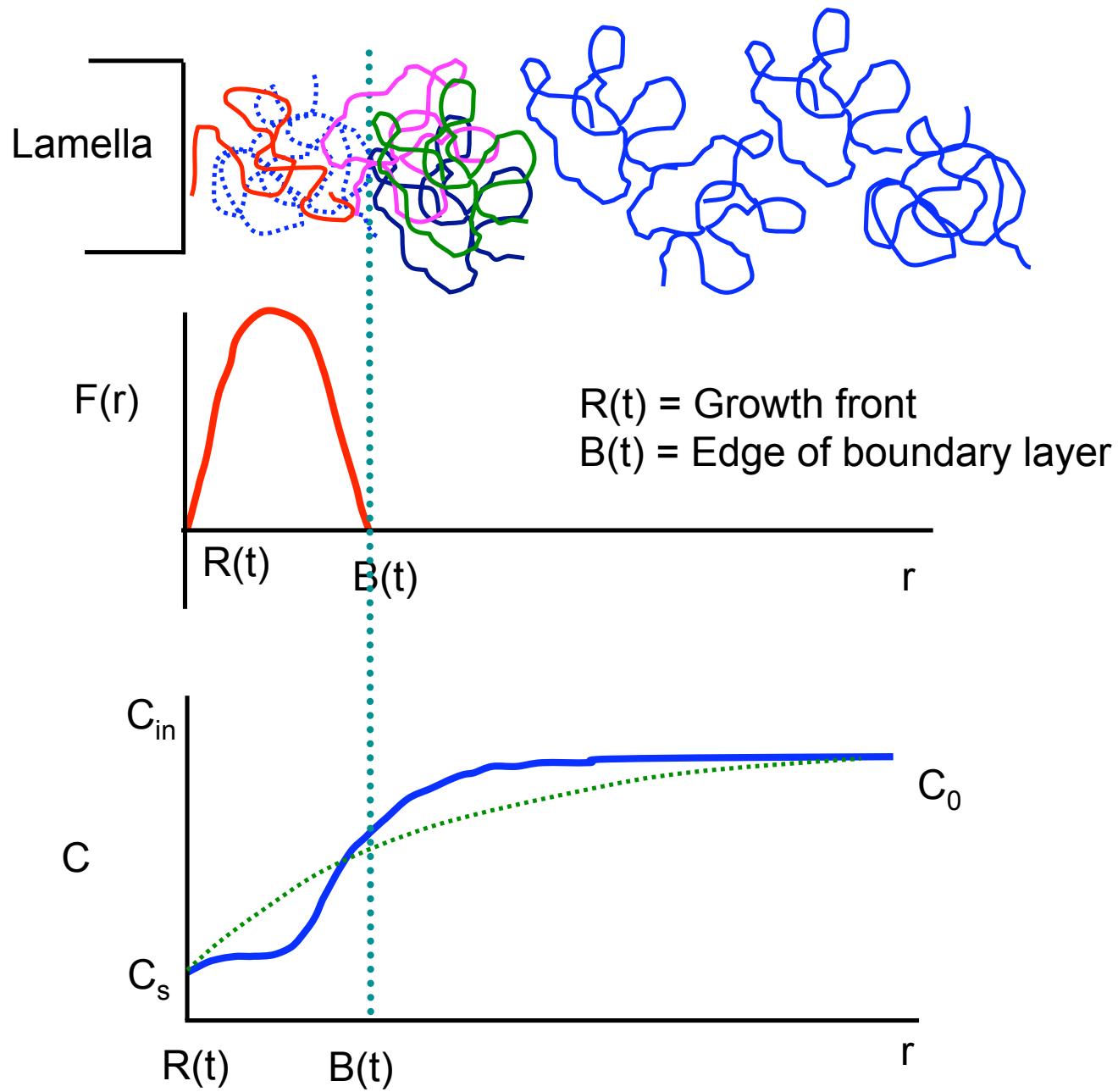


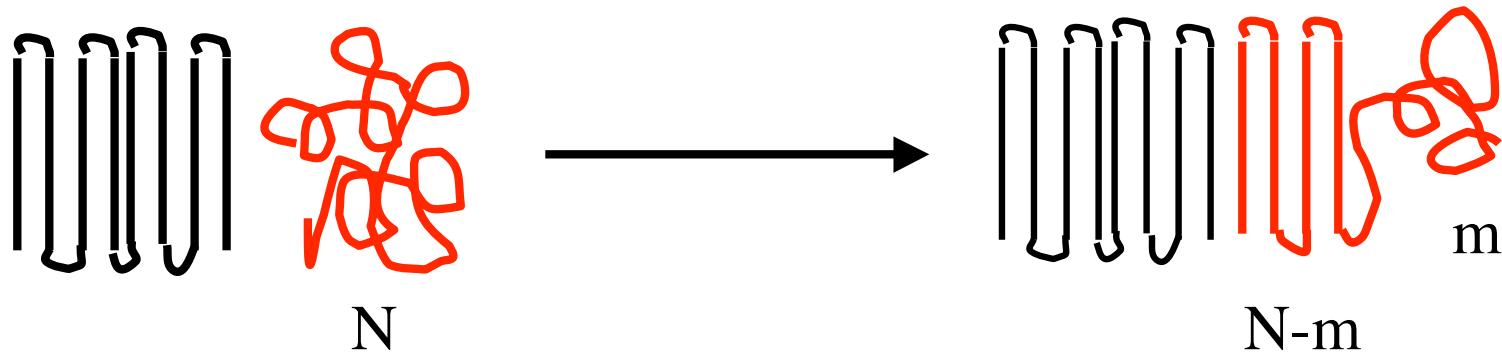
Concentrated



ENTROPIC BARRIER

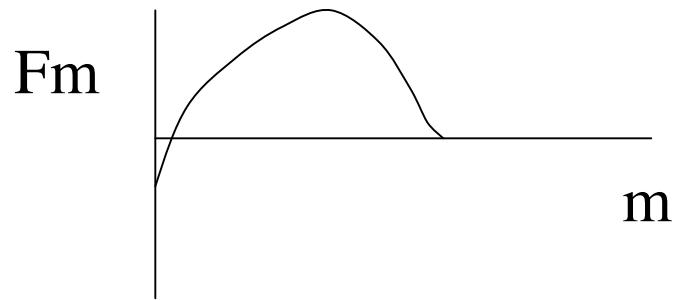
# Entropic Barrier and Jamming





$$F_m = -(N-m)\Delta F + \sigma\sqrt{N-m} + (1-\gamma)lnm$$

[MM, *Phil.Trans.Roy.Soc.*, **361A**, 539 (2003)]



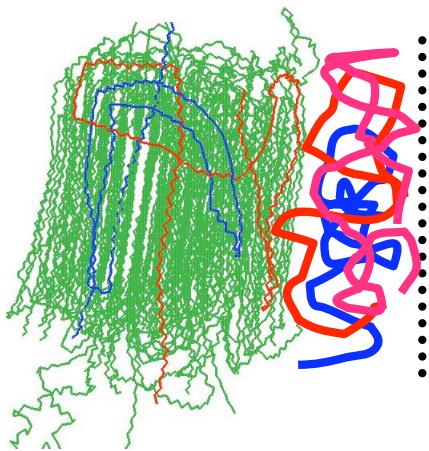
$$G \sim C \ K \ [1 - e^{-\frac{(\Delta H)(\Delta T)}{kT_m T}}]$$

(Barrier)

$$F^* \sim \frac{1}{\Delta T}$$

$$G \sim C \ \frac{D_{in}}{D} e^{-\frac{\alpha}{T \Delta T}} [1 - e^{-\frac{(\Delta H)(\Delta T)}{kT_m T}}]$$

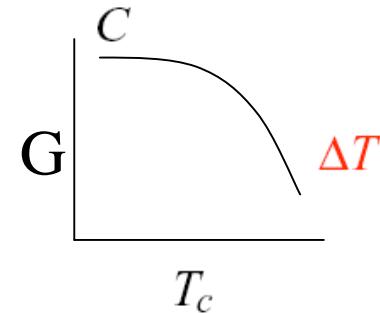
# Kinetics at Growth Front



No barrier:

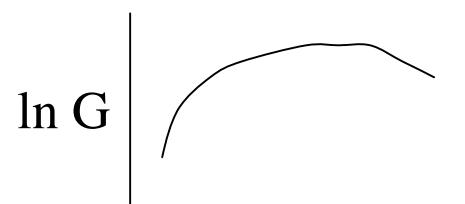
$$G \sim C [1 - e^{-\frac{(\Delta H)(\Delta T)}{kT_m T}}]$$

$\mathcal{L}$

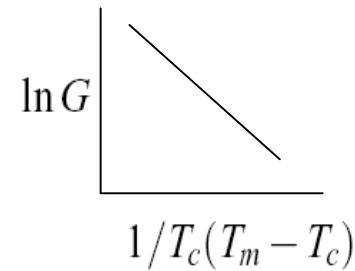


Barrier:

$$G \sim C \frac{D_{in}}{D} e^{-\frac{\alpha}{T \Delta T}} [1 - e^{-\frac{(\Delta H)(\Delta T)}{kT_m T}}]$$



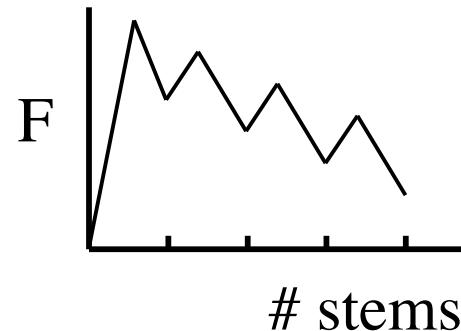
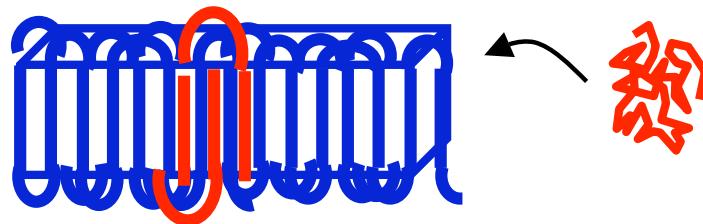
$$G \sim C^\gamma M^{-\mu}$$



- A. Kundagrami and MM, *J. Chem. Phys.* 126, 144901 (2007)  
 J. Zhang and MM, *J. Chem. Phys.* 126, 234904 (2007)  
 M.K. Mitra and MM (unpublished)

# Conclusion #3

Kinetics at growth front



Lauritzen-Hoffman  
Theory

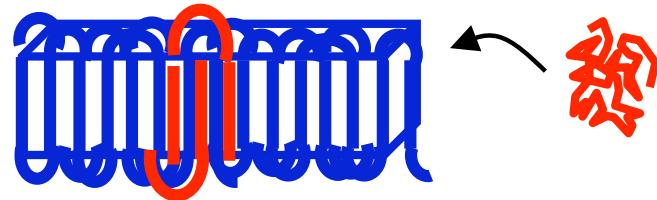
Lamellar growth is chain **ADSORPTION**  
with cooperative dynamics of **all** chains

Boundary layer controls the crystallization kinetics

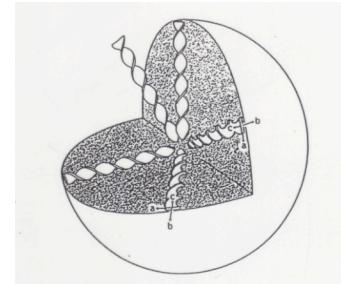
# Central Issues

1. Primordial stage of polymer crystallization
  2. Spontaneous selection of lamellar thickness
    - $L \ll$  extended chain dimension
    - $\sim 10^{-2} \times$  current equilibrium arguments
    - => “KINETICALLY CONTROLLED”
- Interlude from any stable MESOMORPHIC states?

3. Kinetics at growth front

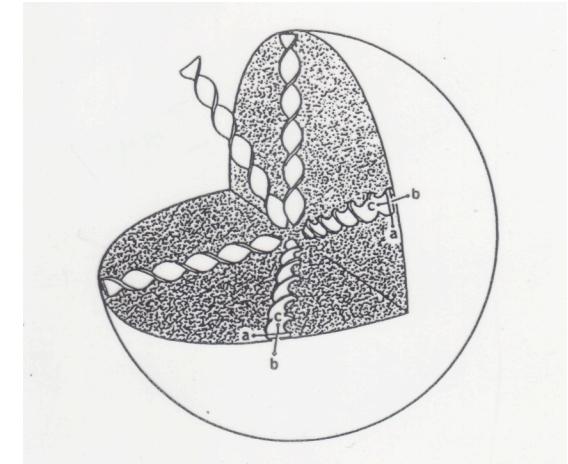
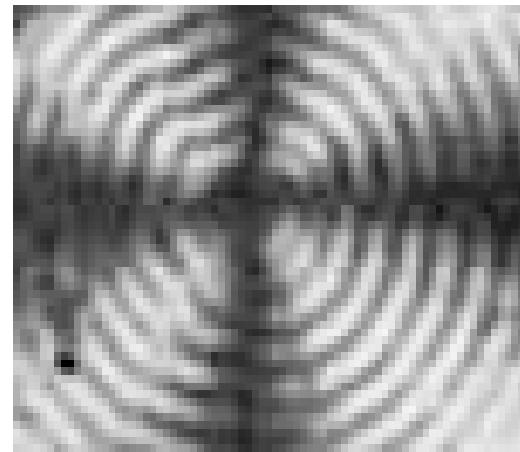
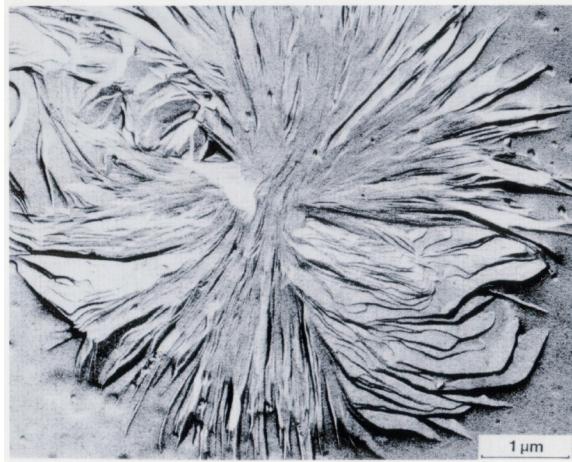


4. Origin of chiral symmetry breaking



5. Composition fluctuations on crystallization kinetics

# Banded Spherulites

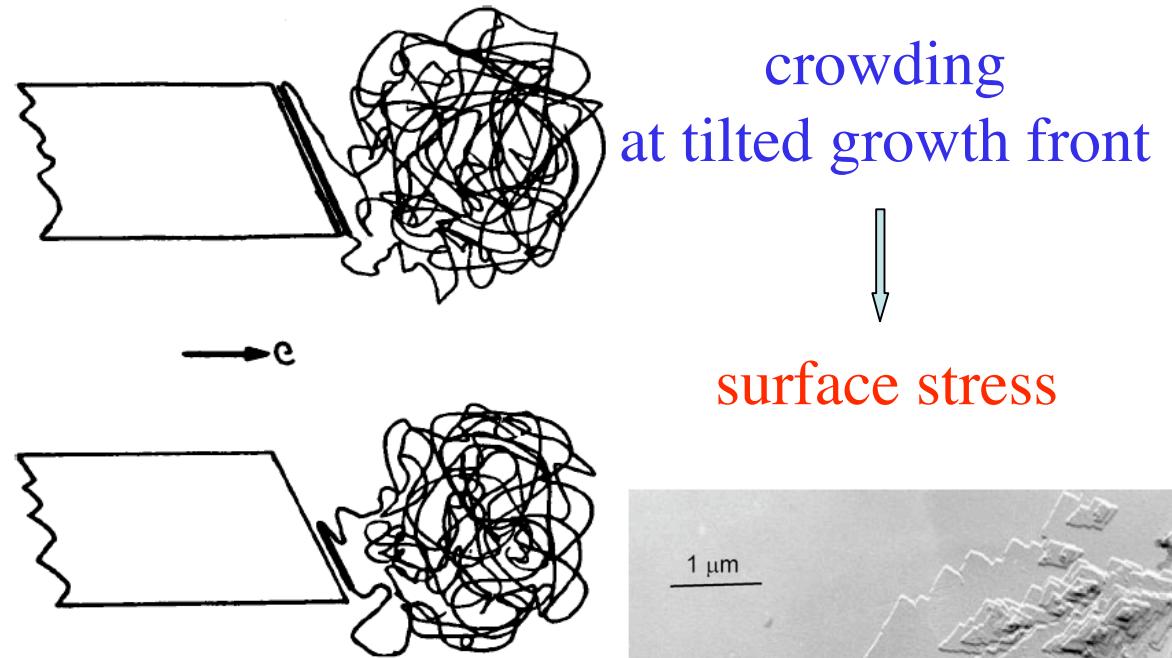


GIGANTIC CHIRALITY  
in polyethylene crystals  
(ACHIRAL molecules)

(Both right-handed and left-handed spherulites)

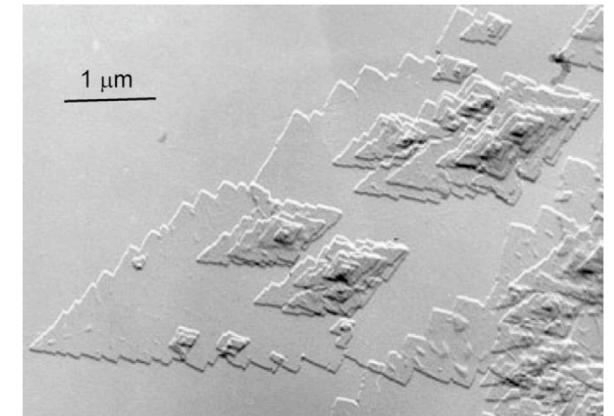
# Banded Spherulites

Keith-Padden:

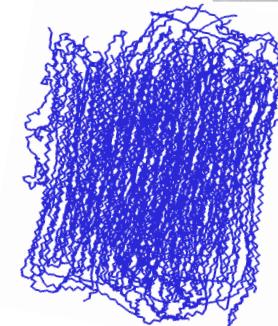


Bassett *et al.*:

DISLOCATIONS



Hatwalne-MM  
DISCLINATIONS



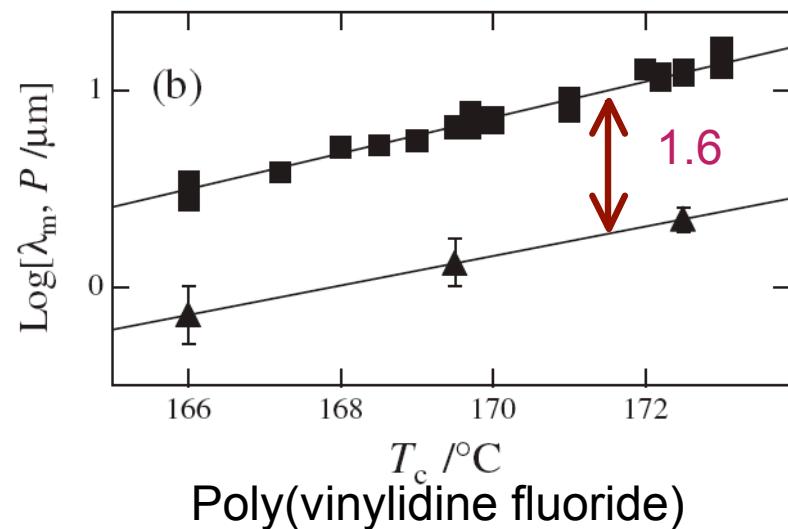
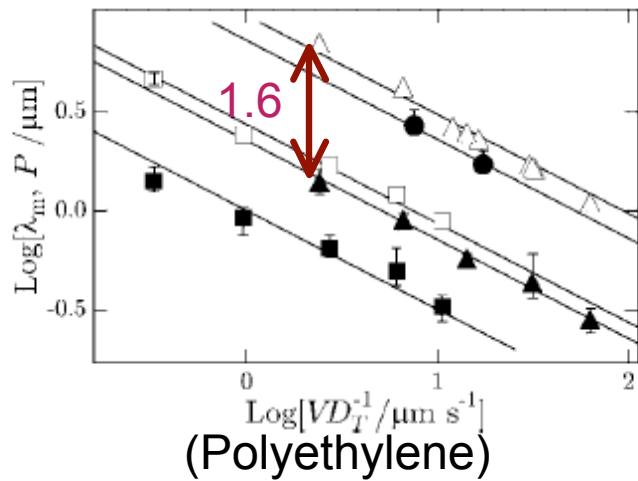
# Conclusion #4

Disclinations + Finite size = Spontaneous Chiral Symmetry Breaking  
(even for ACHIRAL molecules)

Natural selection of ring period and lamellar width:

$$\text{Ring period} = \frac{\pi}{2} \text{ (width)}$$

A. Toda (Hiroshima University):

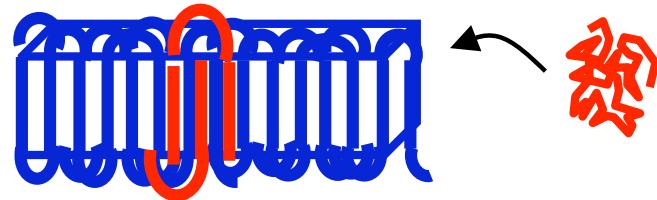


A. Toda *et al.* Macromolecules 41, 2484 (2008); Polymer J, 40, 905 (2008)

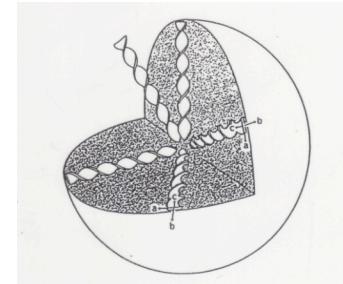
# Central Issues

1. Primordial stage of polymer crystallization
  2. Spontaneous selection of lamellar thickness
    - $L \ll$  extended chain dimension
    - $\sim 10^{-2} \times$  current equilibrium arguments
    - => “KINETICALLY CONTROLLED”
- Interlude from any stable MESOMORPHIC states?

3. Kinetics at growth front



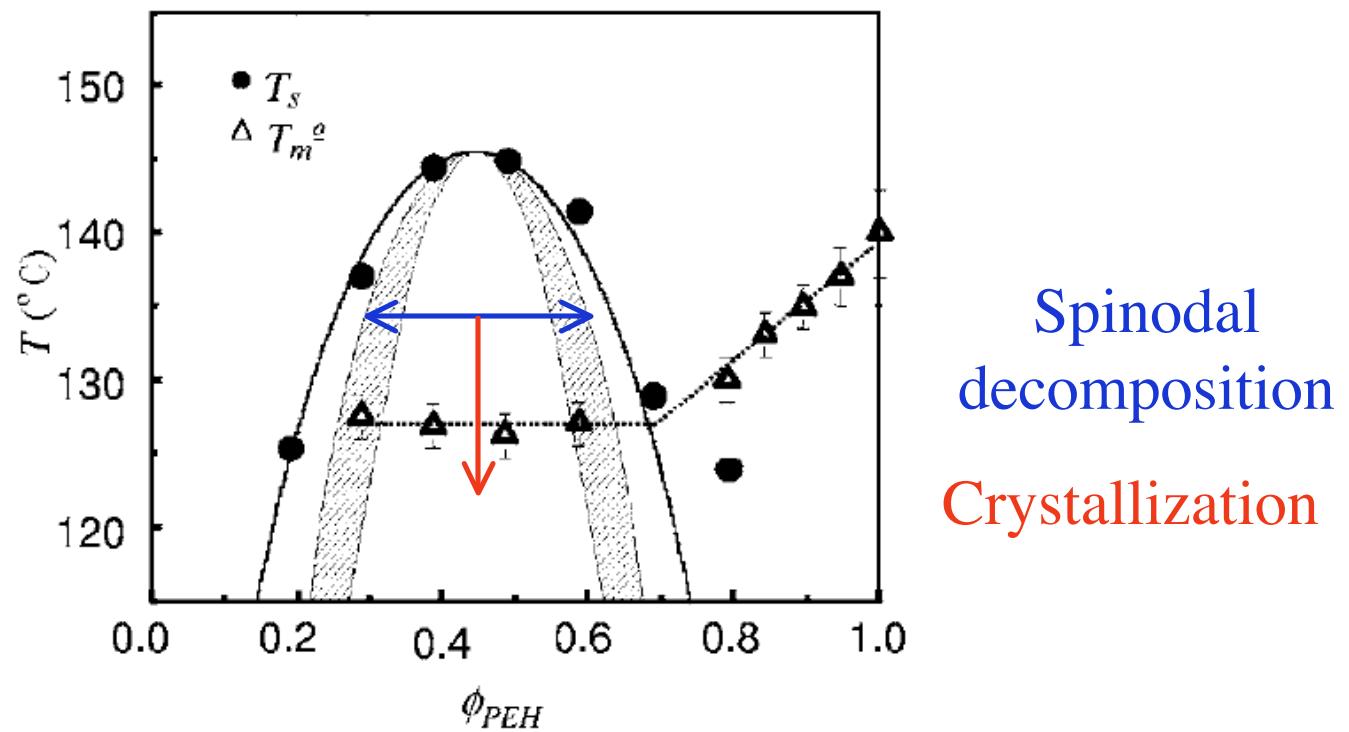
4. Origin of chiral symmetry breaking



5. Composition fluctuations on crystallization kinetics

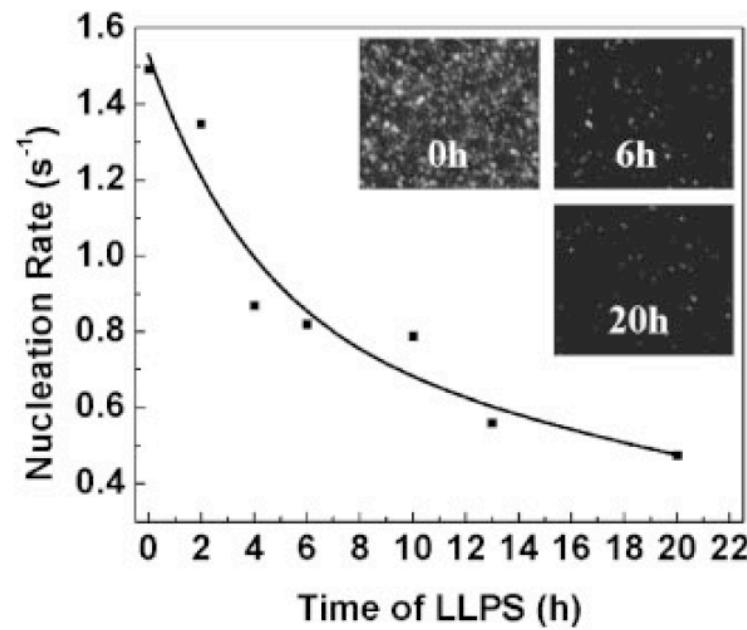
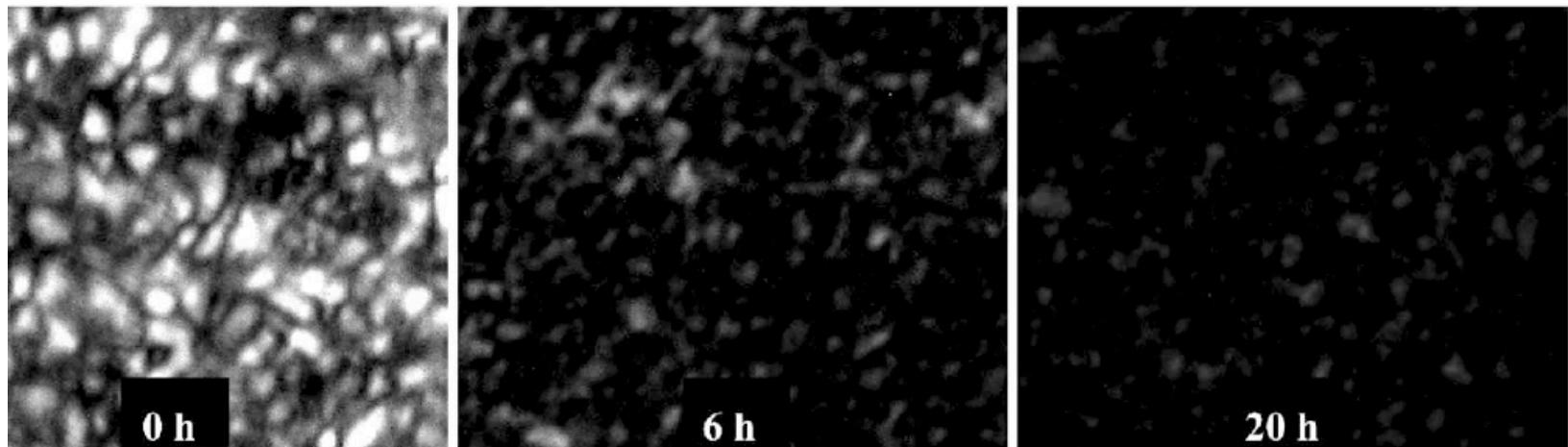
## 5. Composition fluctuations on crystallization kinetics

X. Zhang, ..., C.C. Han: *Macromol. Rapid Commun.* **26**, 1285 (2005);  
*J. Chem. Phys.* **125**, 024907 (2006).



Blend of poly(ethylene-co-hexene) and poly(ethylene-co-butene)

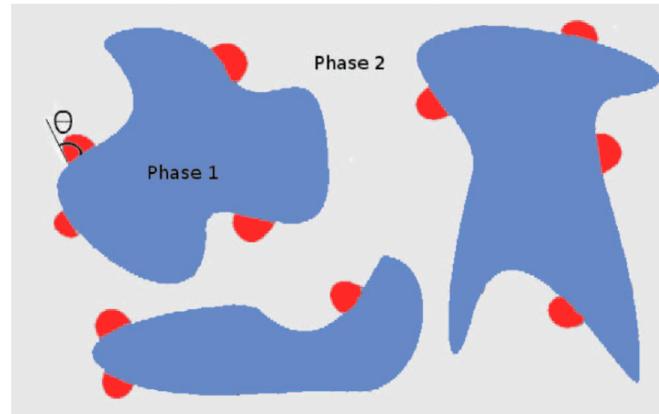
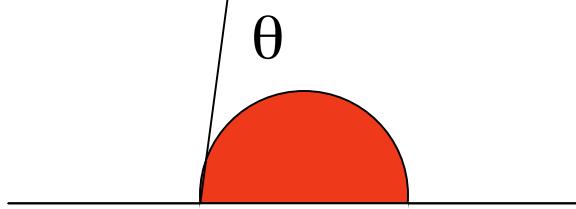
40/60 PEH/PEB,  $T_c = 112^\circ\text{C}$  for 60s, after LLPS at  $135^\circ\text{C}$



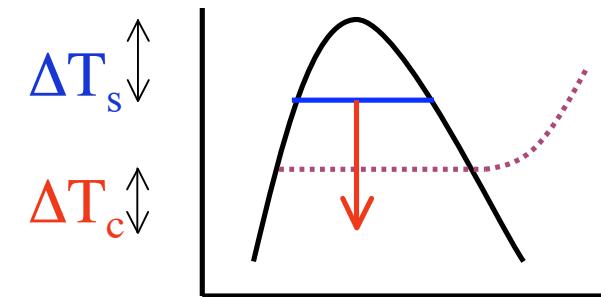
40/60 PEH/PEB,  $T_c = 117.8^\circ\text{C}$  for 120s, after LLPS at  $135.8^\circ\text{C}$

$$L(t) \sim \frac{t^\gamma}{(\Delta T_s)^\delta}$$

$$\delta = \frac{1}{3} = \gamma \quad \text{late regime}$$



M.K. Mitra and MM,  
JCP, 132, 184908 (2010)



$$\text{Nucleation barrier: } \Delta G_c = \frac{\sigma^3 T_m^2}{(\Delta H)^2 (\Delta T_c)^2} f(\theta)$$

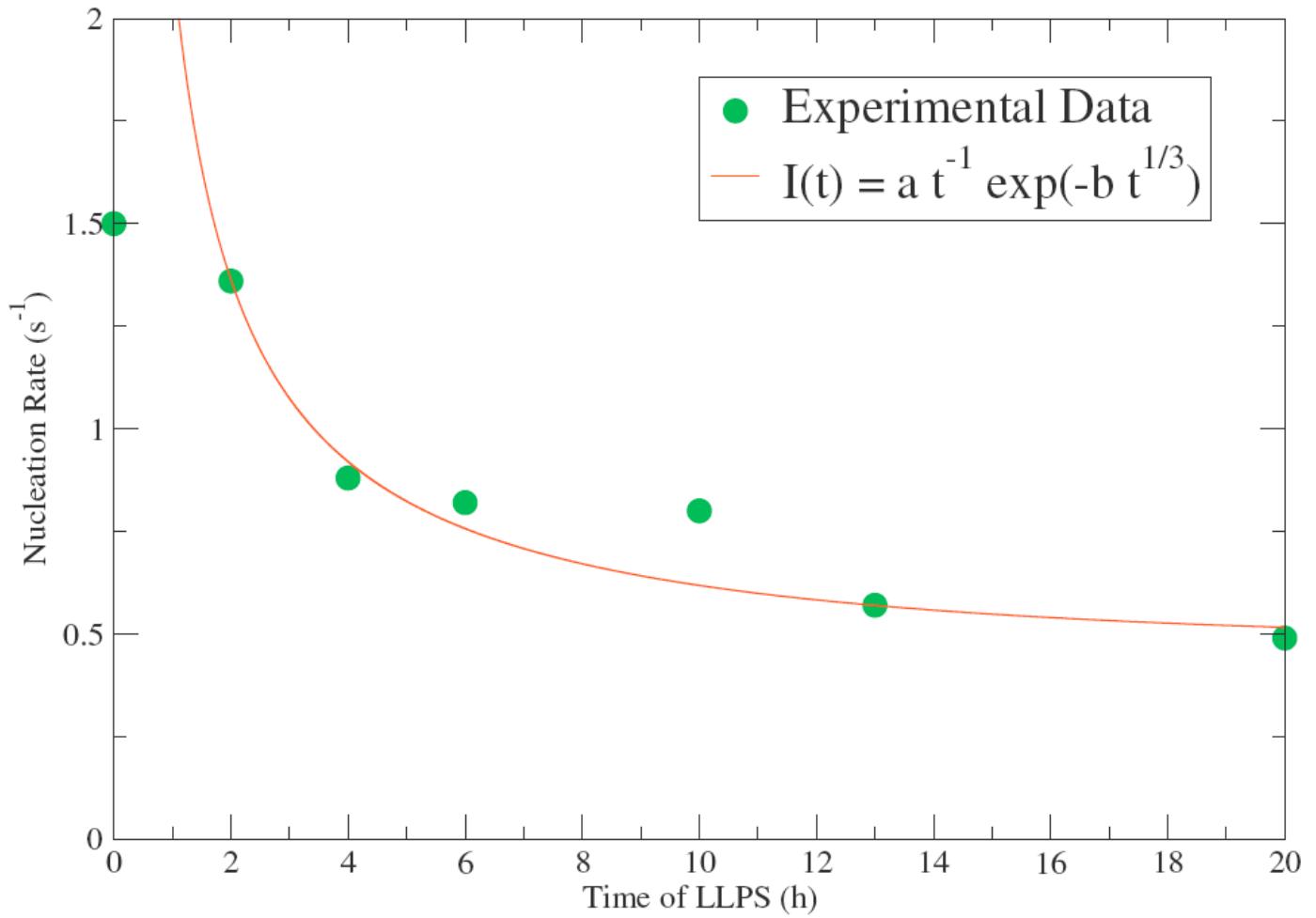
$$\text{Heterogeneous nucleation rate: } I_0 \sim e^{-\Delta G_c / k_B T}$$

$$\text{Competitive nucleation rate in a domain: } I_d = I_0 e^{-I_0 t / m}$$

$$\text{Maximum number of nuclei in a domain: } m \sim \frac{L^2(t)}{r_c^2 \sin^2 \theta}$$

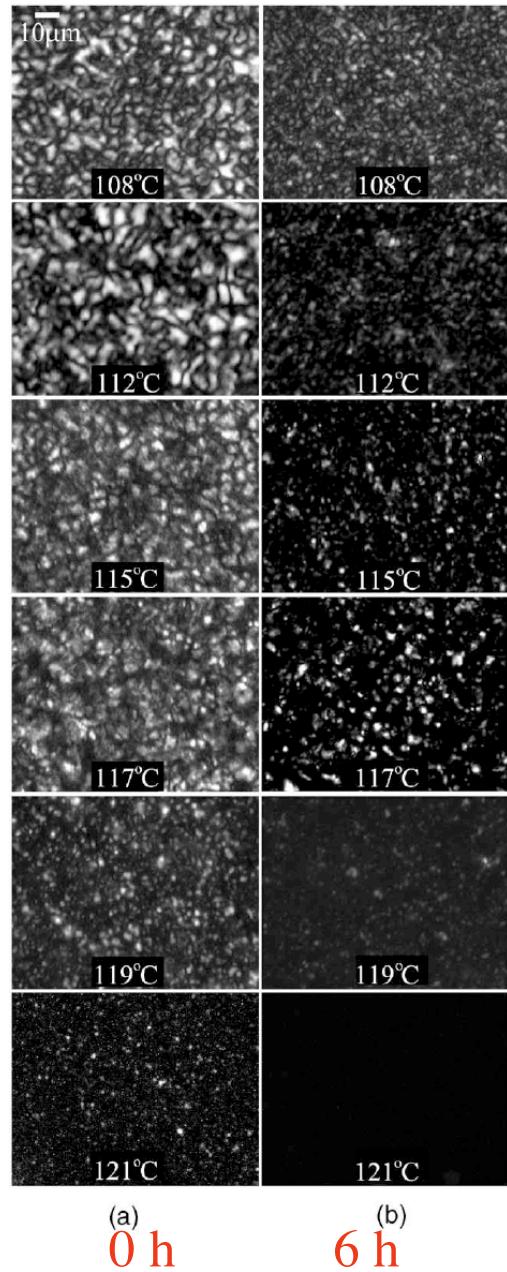
$$\text{Number of domains: } 1/L^3(t)$$

$$\text{Overall nucleation rate: } \frac{1}{L^3(t)} e^{-I_0 t / m} \sim (\Delta T_s)^{3\delta} t^{-3\gamma} e^{-[\frac{1}{(\Delta T_c)^2} (\Delta T_s)^{2\delta} t^{1-2\gamma}]}$$

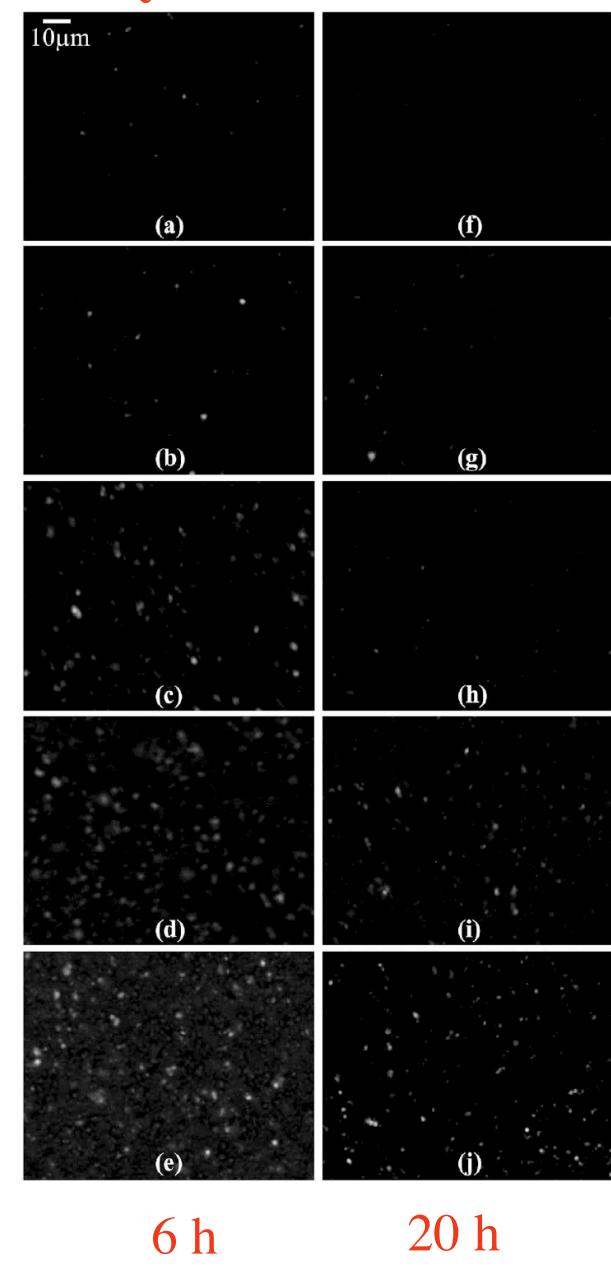


LLPS  
at 135°C

Effect of crystallization T  
(4 min)



Effect of spinodal T  
( $T_c = 117^\circ\text{C}$  for 120s)



# Conclusion #5

## 5. Effect of composition fluctuations

More heterogeneous nucleation at lesser extent of SD

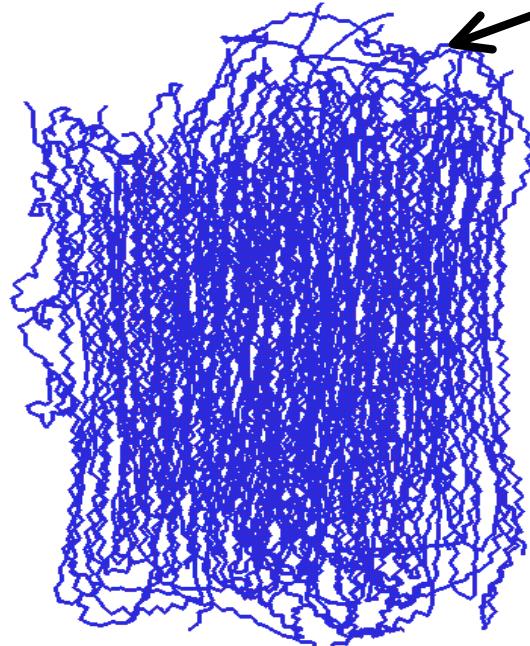
**Deeper spinodal quench, less nucleation**

Deeper crystallization quench, better nucleation

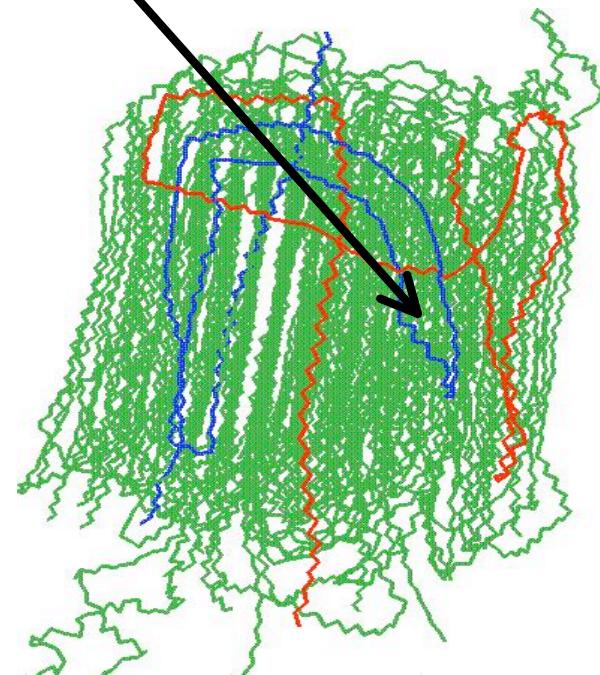
(Consistent with experiments from C. C. Han)

# Polymer Crystallization: Entropically Controlled

$$F = E - TS$$



Folded Chain Crystal

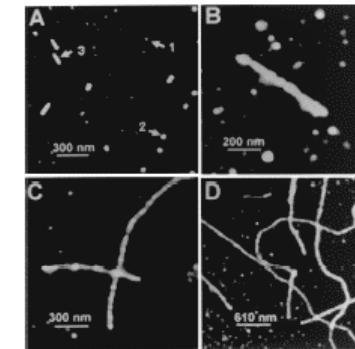


Entropic Barrier and Jamming  
at growth front

Shifting Paradigms in Polymer Crystallization

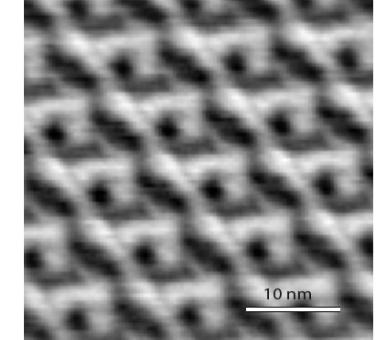
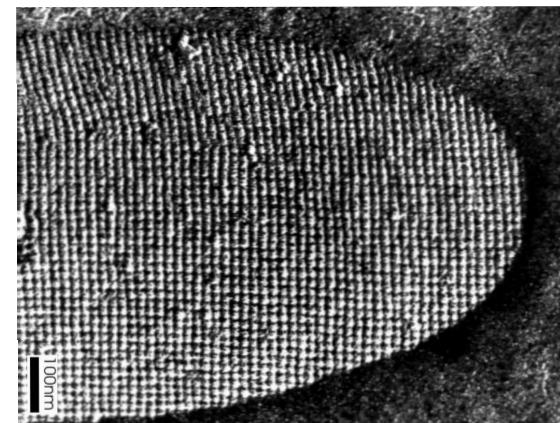
## 1) Amyloid fibrils

DAEFRHDSGYEVHHQLLVFFAEDVGSNLGAIIGLMVGGVIA



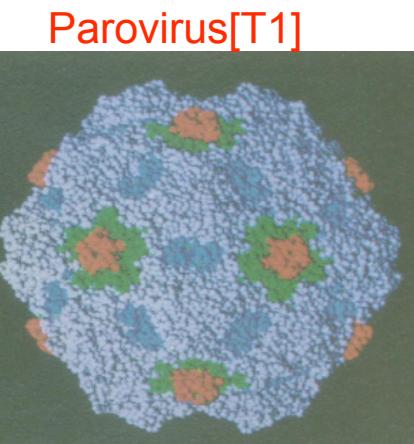
## 2) Bacterial walls

MAQPKSYRKFVATTATAAMVASAVAPVSAASFTDVAPQYKDAIDFLVST  
GATKGKTETKFGVYDEITRLDAAVILARVLKLDVDNAKDAGFTDVKDRAKY  
VNALVEAGVLNGKAPGKFGAYDPLTRVEMAKIANRYKLKADDVKLPFTDV  
NDTWAPYYKALYKYEVTKGKPTSGAYQNITRGDFAQFVYRAVININAVPEI  
VEVTAVNSTTVKVTFNTQIADVFNTFAIDNGLTVKATLSRDKKSVEVVVNK  
PFTRRNQEYYTITATGIKNLKGETAKELTGKFFWSVQDATVVALNNSSLKVGEE  
SGLTVKDQDGDVVGAKVELTSSNTNIVVVSSEEVVSAAKVKVTAVKPGTADV  
TAKVTLPDGVVLNTFKVTEVPVQVQNQGFTLVDNLSAPQNTVAFNKA  
EKVTSMFAGETKTVAMYDTKNGDPETKPVDFKDATVRSLNPIATAINGSE  
LLVTANAGQSGKASFEVTFKDNTKRTFTVDVKKDPVLQDIKVDATSVKLSDE  
AVGGGEVGVNQKTIKVSAVDQYQKEIKFGTKGKVTVTTNEEGLVIKNVNSD  
NTIDFDSGNSATDQFVVVATKDKIVNGKVEVKYFKNASTTPTSTKTITVNVV  
NVKADATPVGLDIVAPSEIDVNAPNTASTADVDFINFESEIYTLDSGNRLK  
KVTPTATTLVGTDYVEVNGNVLQFKGNDELLLTSSSTVNVDTADGITKRI  
PVKYINSASPASATVATSPVKLNSSDNDLTFEELIFGVIDPQLVKDEDIN  
EFIAVSKAAKNDGYLYNKPLVTVKDASGKVIPTGANVYGLNHDATNGNIWF  
EQAGLAKKFSDVHFDVDFSLANVVKTGSGTVSSSPSLSDAIQLTNNSGDAV  
SFTLVIKSIYVKGADKDDNNLLAAPVSVNVTVTK



## 3) Viruses

GVGVSTGSYDNQTHYRFLGDGWVEITALATRLVHLNMPLSENYCCIRV  
HNTTDTSVLGNMLDDAHEQIWTPWSLVDANAWGVWLQPSDWQYIC  
NTMSQLNLVLSLDQEIFNVVLLTVEQDSSGQAIIYNNDLTACMMVAVD  
SNNILPYPTPAANSMETLGFPWLPTIASPYRYYFCVDRDLSVTYENQEG  
TIEHNVMGTPLGMSQFFTTIENTQQITLLRTGDEFATGTYYFDTNPVLLT  
HTWQTNRRQLGQPPLLSTFPEADTDAGTLTAQGSRHGATQMEVNWVSE  
AIRTRPAQVGFCQPHNDFEASRAGPFAAPLVPADVTQGMDREANGSVR  
YSYGLQHGENWAAHGPAPERYTWDETNGSGRDTRDGFIQSAPLVVPQQQIWDLEL  
PPLNGILTNANPIGTLNDIHFSNVFNSYGPLTTFSHSPVYPQQQIWDLEL  
DLEHLPRLHATPVCLNNAPGQMLVRLGPNLTDQYDPNGATLSRIVTYG  
TFFWLGLLTMRALLRANTTWNPVQVSEDNGNSYMSVTLWPTATGN  
MQSVPLITRPVARNTY



# Why aren't we made of spheres or cubes?

$$F = E - TS$$

↓  
**fixed**

Need candidates where  $F$  can be changed dramatically and reversibly at fixed temperature

