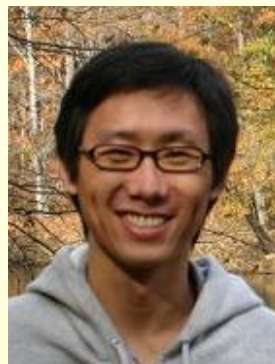


# Control and Optimization of Lignin Biosynthesis in Plant Cell Walls

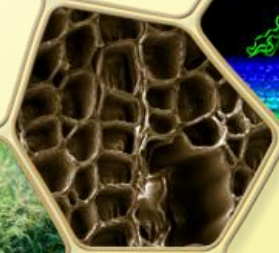
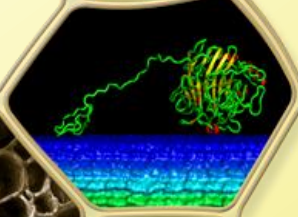
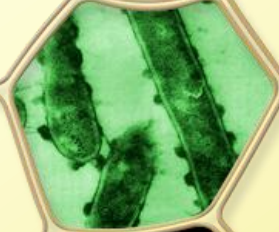
Yun Lee and Eberhard O. Voit

Wallace H. Coulter Department of Biomedical Engineering  
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ICM Satellite Meeting  
Hyderabad, August 16-18, 2010



$$V_i = \gamma_i \prod_{j=1}^{n+m} X_j^{f_{ij}}$$



## **Preamble**

**In College I was told that  
Biology was too complicated  
to use Math.**

**We have learned by now that  
Biology is too complicated  
*not* to use Math.**

# Overview

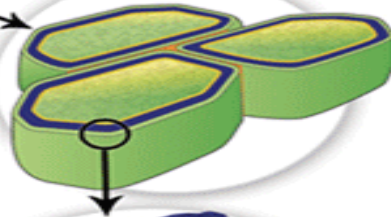
- **Context: Sustainable biofuel production**
- **Plant cell wall composition; role of lignin; monolignols**
- **Recalcitrance directly related to lignin content and composition (S/G/H)**
- **Study lignin biosynthesis in:**
  - **Poplar**
  - **Alfalfa**
  - **Switchgrass**
- **Methods**
  - **Stoichiometric analysis (static network analysis)**
  - **Optimization analysis (FBA, MOMA; constrained network analysis)**
  - **Biochemical Systems Theory (BST; fully kinetic, dynamic analysis)**
- **Results**

# Biofuel Production

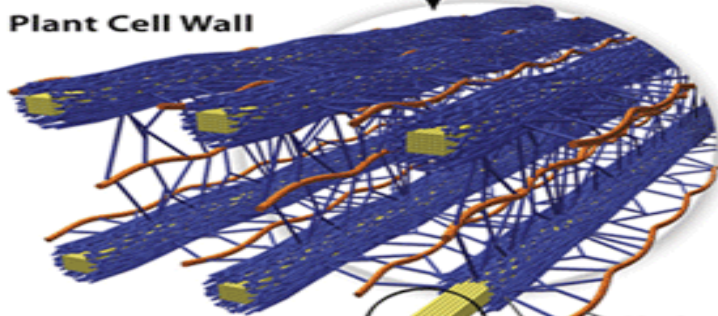
Bioenergy Crop



Plant Cells

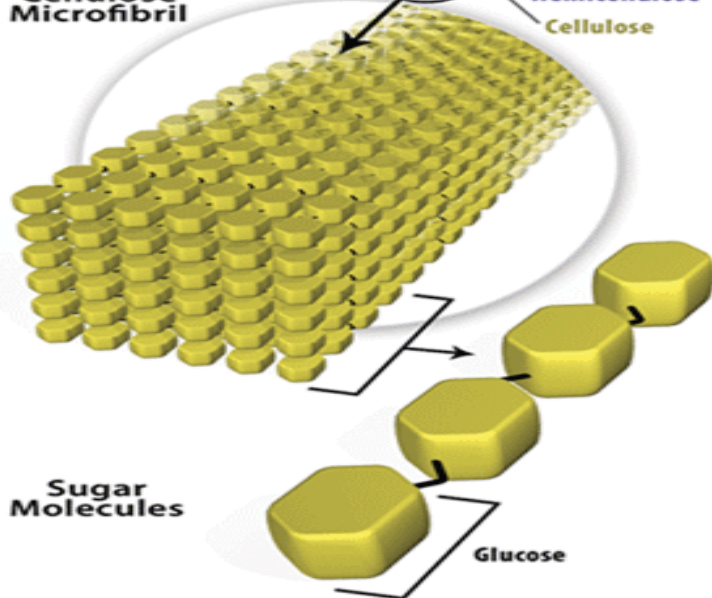


Plant Cell Wall



Cellulose Microfibril

Lignin  
Hemicellulose  
Cellulose



Sugar Molecules

Glucose



Switchgrass



Poplar

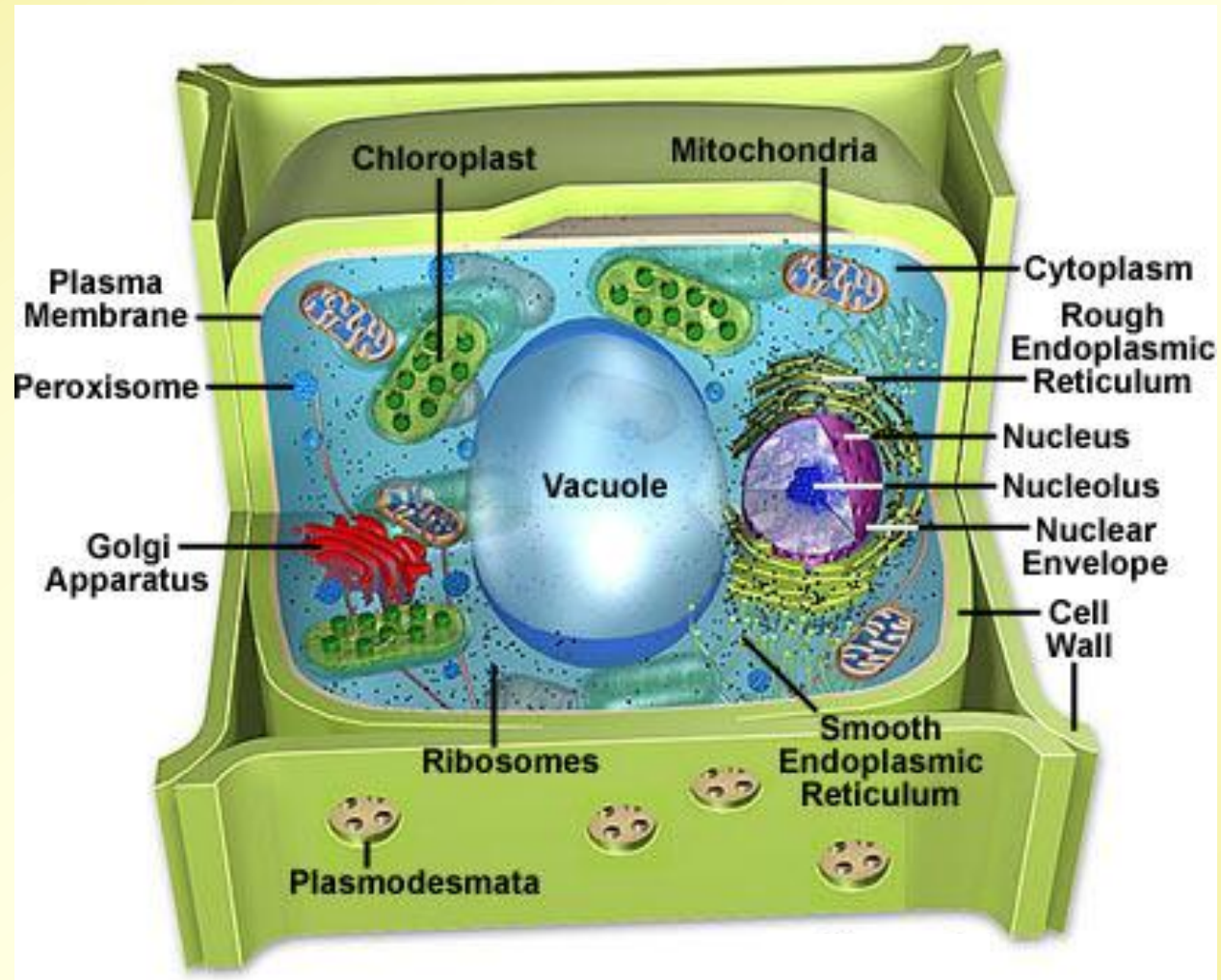
Fermentation



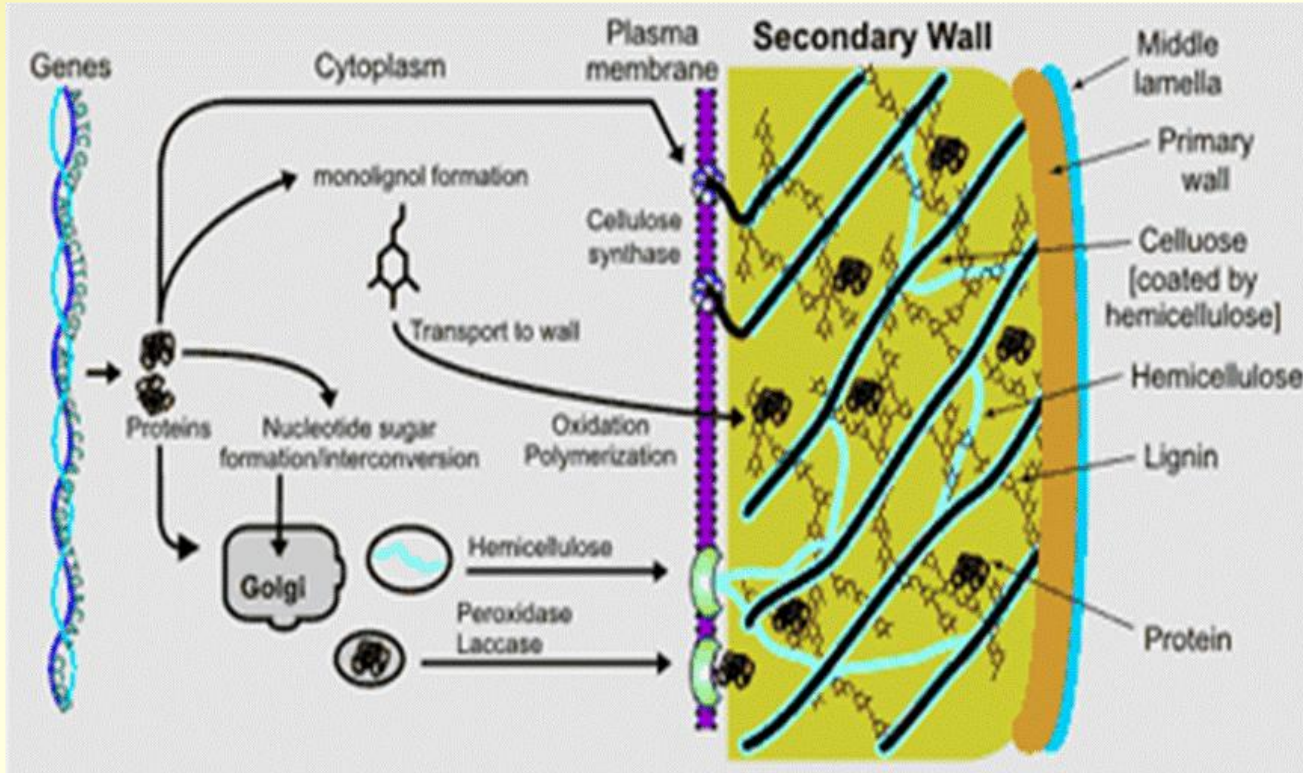
Bacteria,  
Yeast

**Ethanol**

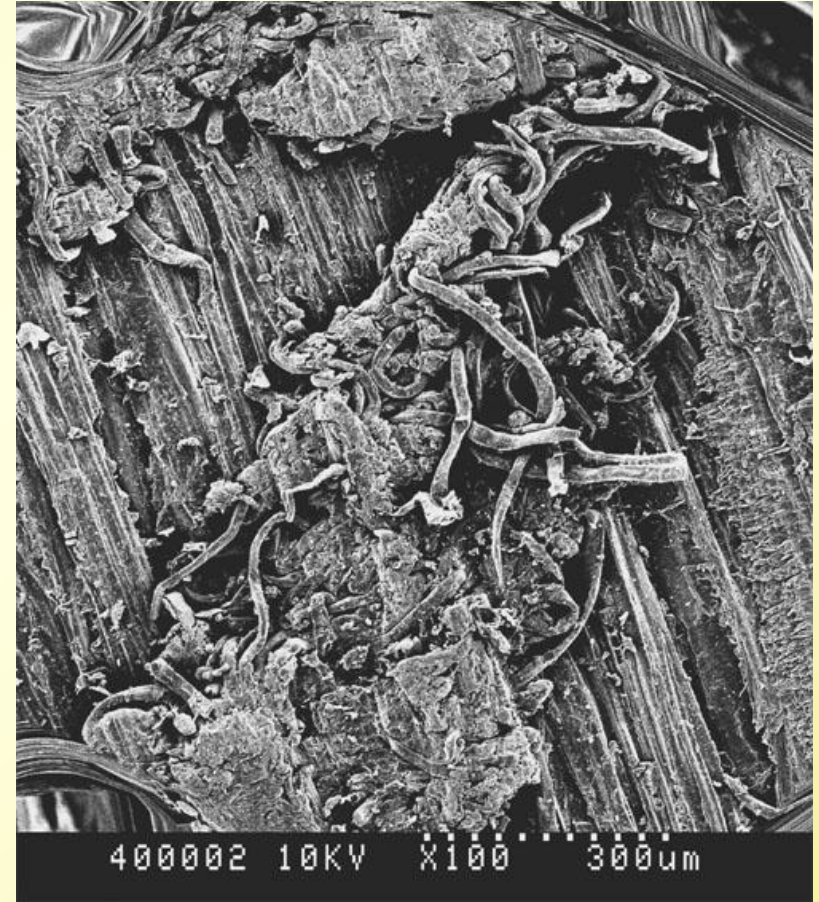
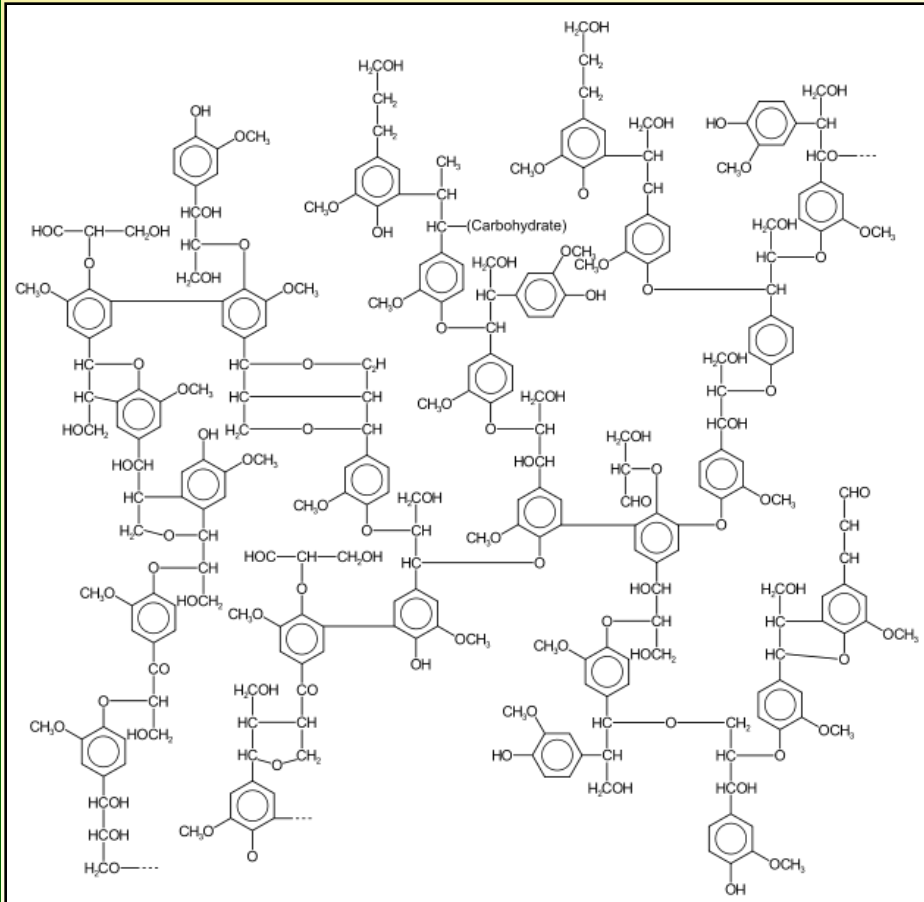
# Plant Cell Walls



# Plant Cell Walls

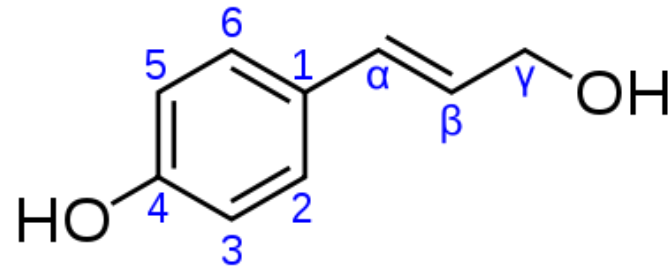


# Lignin is a Natural Polymer ("Wood")

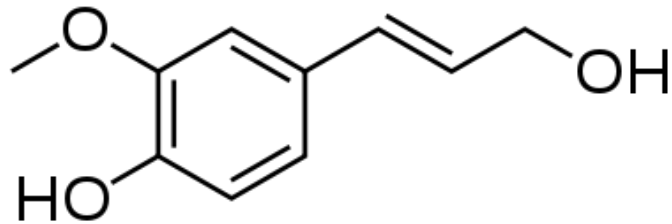


**Task: remove or reduce lignin to access cellulose**

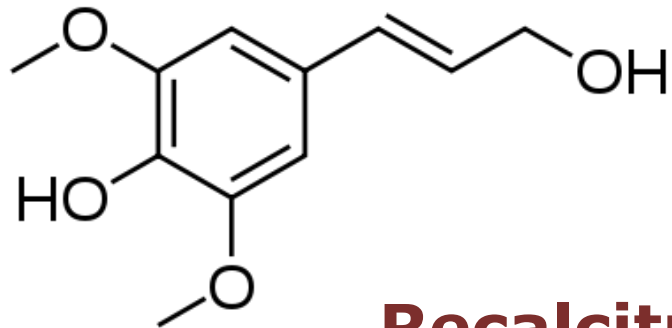
# Monolignols



*p*-Coumaryl alcohol **(H)**



Coniferyl alcohol **(G)**



Sinapyl alcohol **(S)**

**Recalcitrance Related to S/G Ratio**



# **Task: Develop Mathematical Pathway Model for Lignin Biosynthesis**

- Model design
  - Choices of models
    - Stoichiometric
    - Dynamic
- Model analysis
  - Insights into pathways
  - Conversion of stoichiometric into dynamic models
  - Optimization
- Results
  - Suggestions from optimization
  - New postulates

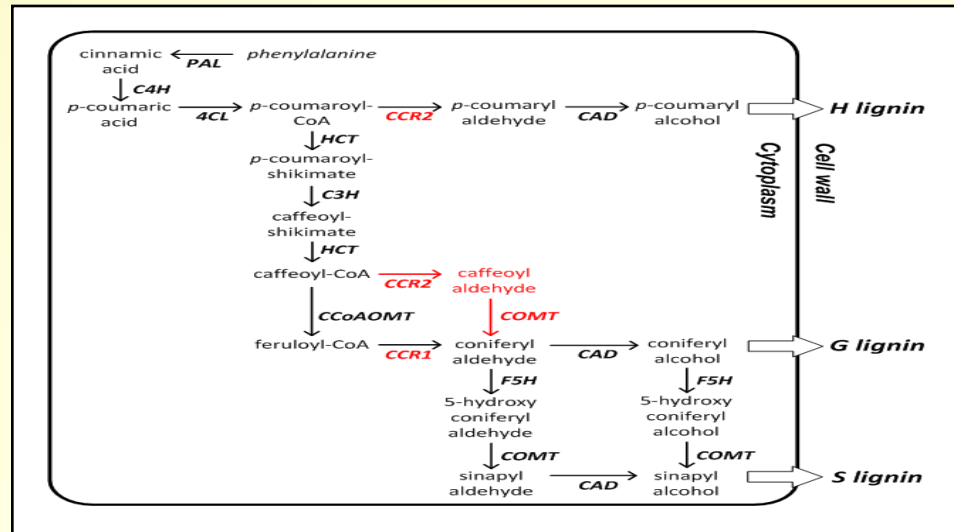
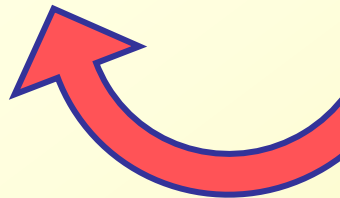
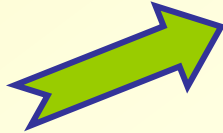
# General Modeling Procedure



e.o.voit



www.ornl.gov



$$\frac{dX_{12}}{dt} = \gamma_{0,12} X_{24}^{f_{0,12,24}} X_{30}^{f_{0,12,30}} + \gamma_{51,12} X_{12}^{f_{51,12,12}} X_{28}^{f_{51,12,28}} X_{51}^{f_{51,12,51}} X_{52}^{f_{51,12,52}}$$

$$+ \gamma_{4,17} X_4^{f_{4,17,4}} X_{22}^{f_{4,17,22}} + \gamma_{6,17} X_6^{f_{6,17,6}} X_{22}^{f_{6,17,22}}$$

% model\_ode

function dy = PP\_ode(t,y)

...

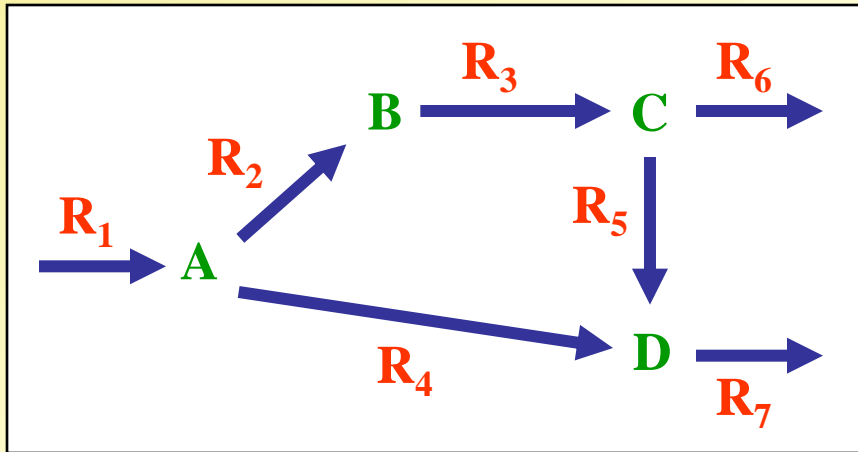
dy(1) = y(1) \* (b1 - b2 \* y(1) - b3 \* y(2));

dy(2) = y(2) \* (b4 \* y(1) + b5 - b6 \* y(2));

end



# Stoichiometric Analysis



	$R_1$	$R_2$	$R_3$	$R_4$	$R_5$	$R_6$	$R_7$	
$\mathbf{N} =$	1	-1	0	-1	0	0	0	$\mathbf{A}$
	0	1	-1	0	0	0	0	$\mathbf{B}$
	0	0	1	0	-1	-1	0	$\mathbf{C}$
	0	0	0	1	1	0	-1	$\mathbf{D}$

- Change in substrate concentrations ( $\mathbf{S}$ ) is a function of fluxes ( $\mathbf{R}$ ) and of the stoichiometric matrix  $\mathbf{N}$ ; at steady state:

$$d\mathbf{S}/dt = \mathbf{N} \cdot \mathbf{R} = 0$$

- No unique solution: optimize some criterion (growth rate)

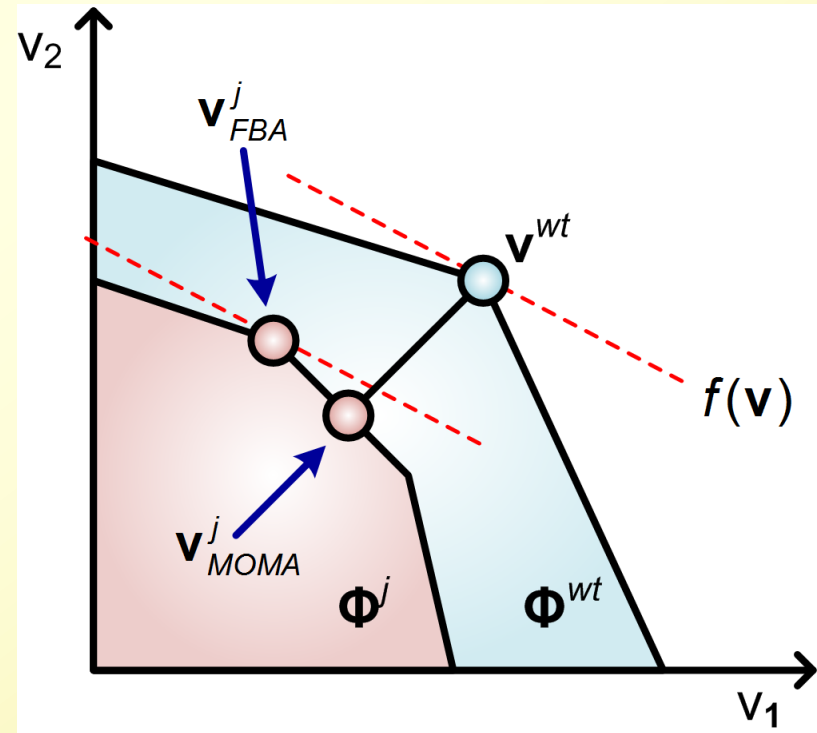
## **Constraint-Based Flux-Balance Analysis (FBA)**

Reduce solution space with physico-chemical constraints

# FBA and MOMA

- Starting Point:  $d\mathbf{S}/dt = \mathbf{N}\cdot\mathbf{R} = 0$  (No unique solution)
- FBA: optimize some criterion under additional constraints
- MOMA ("Minimization of Metabolic Adjustment"):

Transgenic strain tries to emulate wild type as much as possible; optimum inferior



# Stoichiometric and Flux Balance Analysis

## ***Advantages:***

No kinetic details needed, just topology and fluxes

Linear system: no real size limitation

Steady-state solution space given by "kernel"

Straightforward optimization

Solution optimizes a desirable criterion (*e.g.*, growth rate)

## ***Limitations:***

Kinetic information cannot be used

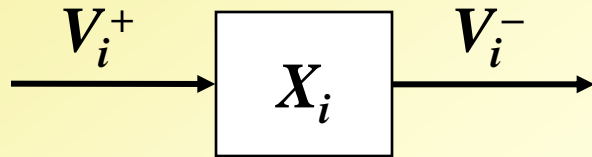
No nonlinearities allowed

No regulatory signals can be considered, but:

Optimal strategies of flux alteration affected by signals

Arbitrariness in objective function for optimization

# Choice of Dynamic Model Structure



$$\dot{X}_i = \frac{dX_i}{dt} = V_i^+ - V_i^-$$

$$V_i^+ = V_i^+ \left( \underbrace{X_1, X_2, \dots, X_n}_{\text{inside}}, \underbrace{X_{n+1}, \dots, X_{n+m}}_{\text{outside}} \right)$$

**complicated**

**Solution with Potential:**

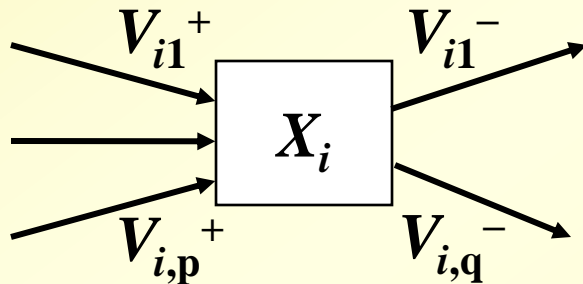
$$V_{ik}^{+/-} = \gamma_{i,k} \prod_{j=1}^n X_j^{f_{k,i,j}}$$

"Biochemical Systems Theory"  
(BST)

# Alternative Formulations Within BST

## S-system Form:

$$\dot{X}_i = \alpha_i X_1^{g_{i1}} X_2^{g_{i2}} \dots X_{n+m}^{g_{i,n+m}} - \beta_i X_1^{h_{i1}} X_2^{h_{i2}} \dots X_{n+m}^{h_{i,n+m}}$$

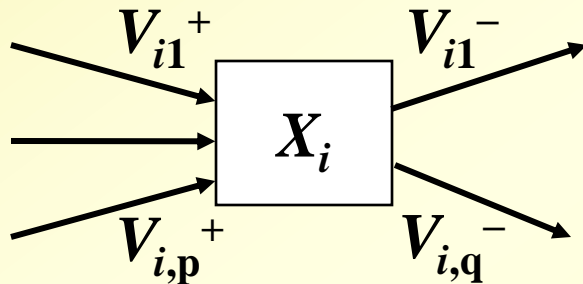


$$\dot{X}_i = \frac{dX_i}{dt} = \sum V_{ij}^+ - \sum V_{ij}^-$$

# Alternative Formulations

## S-system Form:

$$\dot{X}_i = \alpha_i X_1^{g_{i1}} X_2^{g_{i2}} \dots X_{n+m}^{g_{i,n+m}} - \beta_i X_1^{h_{i1}} X_2^{h_{i2}} \dots X_{n+m}^{h_{i,n+m}}$$



$$\dot{X}_i = \frac{dX_i}{dt} = \sum V_{ij}^+ - \sum V_{ij}^-$$

## Generalized Mass Action Form:

$$\dot{X}_i = \sum \pm \gamma_{ik} \prod X_j^{f_{ijk}}$$



# Advantages of BST Models

Prescribed model design: Rules for translating diagrams into equations; rules can be automated

Direct interpretability of parameters and other features

One-to-one relationship between parameters and model structure simplifies parameter estimation and model identification

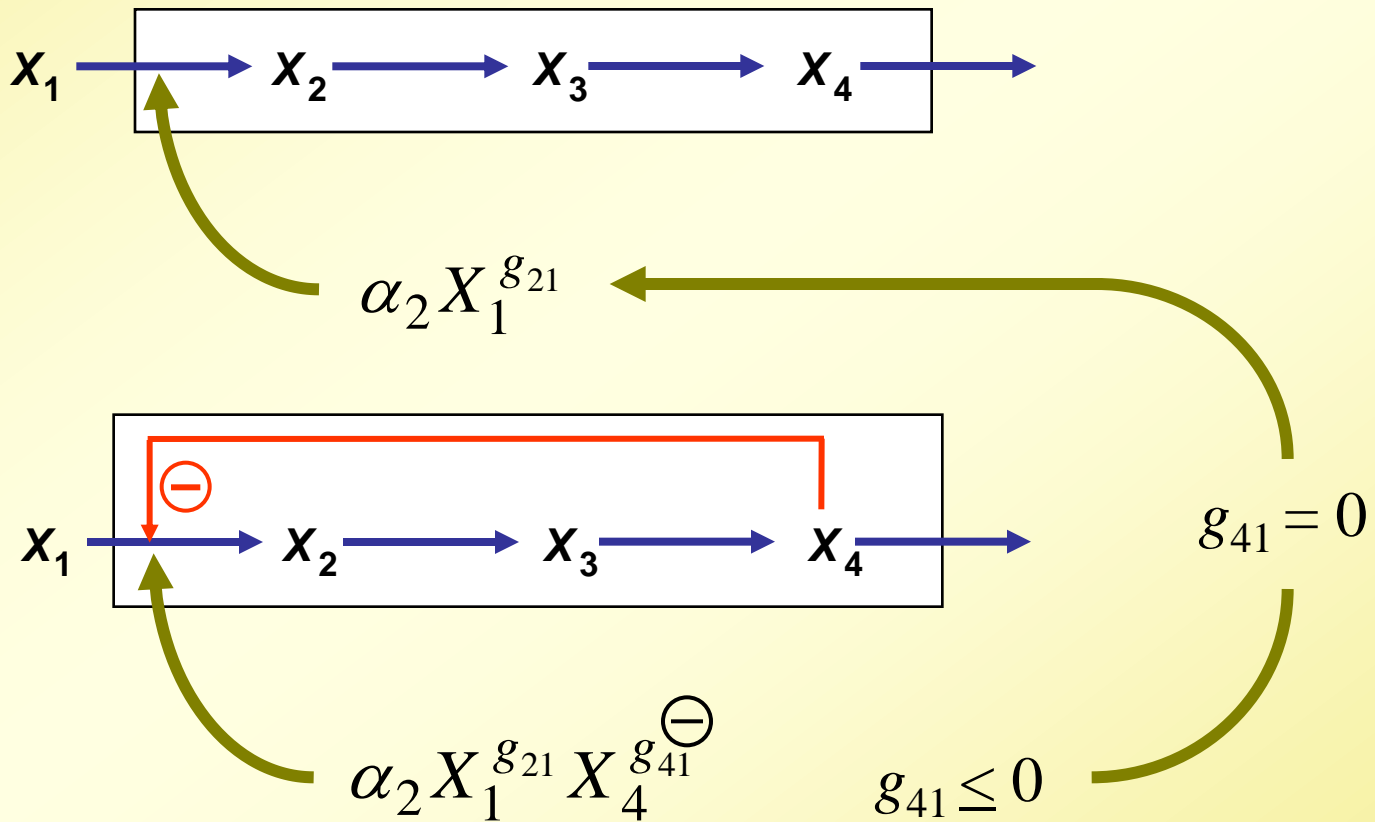
Simplified steady-state computations (for S-systems), including steady-state equations, stability, sensitivities, gains

Simplified optimization under steady-state conditions

Efficient numerical solutions and time-dependent sensitivities

In some sense minimal bias of model choice and minimal model size; easy scalability

# Mapping Structure ↔ Parameters



# S-system Steady-State Equations Linear

$$\dot{X}_i = \alpha_i X_1^{g_{i1}} X_2^{g_{i2}} \dots X_{n+m}^{g_{i,n+m}} - \beta_i X_1^{h_{i1}} X_2^{h_{i2}} \dots X_{n+m}^{h_{i,n+m}} = 0$$

Define  $Y_i = \log(X_i)$ :

$$\begin{aligned} \log \alpha_i + g_{i1} Y_1 + g_{i2} Y_2 + g_{i,n+m} Y_{n+m} \\ = \log \beta_i + h_{i1} Y_1 + h_{i2} Y_2 + h_{i,n+m} Y_{n+m} \end{aligned}$$

$$\mathbf{Y}_D = \mathbf{A}_D^{-1} \cdot \mathbf{b} - \mathbf{A}_D^{-1} \cdot \mathbf{A}_I \cdot \mathbf{Y}_I$$

S-system highly nonlinear, but steady-state equations linear.

# Pathway Optimization with S-systems

Optimization under steady-state (batch) conditions becomes

## ***Linear Program***

even though (nonlinear) kinetics is taken into account:

*maximize*  $\log(\text{flux})$  [or  $\log(\text{variable})$ ]

*subject to:*

Steady-state conditions in  $\log(\text{variables})$

Constraints on  $\log(\text{variables})$

Constraints on  $\log(\text{fluxes})$

# Pathway Optimization (continued)

## **Great Advantage:**

Methods of *Operations Research* applicable

- very well understood
- applicable for over 1,000 simultaneous variables
- robust and efficient
- incomparably faster than nonlinear methods

*Torres, Alvarez, Voit, ...*: Applications (e.g., citric acid, ethanol, glycerol, L-carnitine)

*Hatzimanikatis, Bailey, Floudas, 1996*: Use these features for optimization of pathway structure

*Marin-Sanguino, Torres, Polisetty, Gatzke, Voit, ...*:

Extension to GMA models via

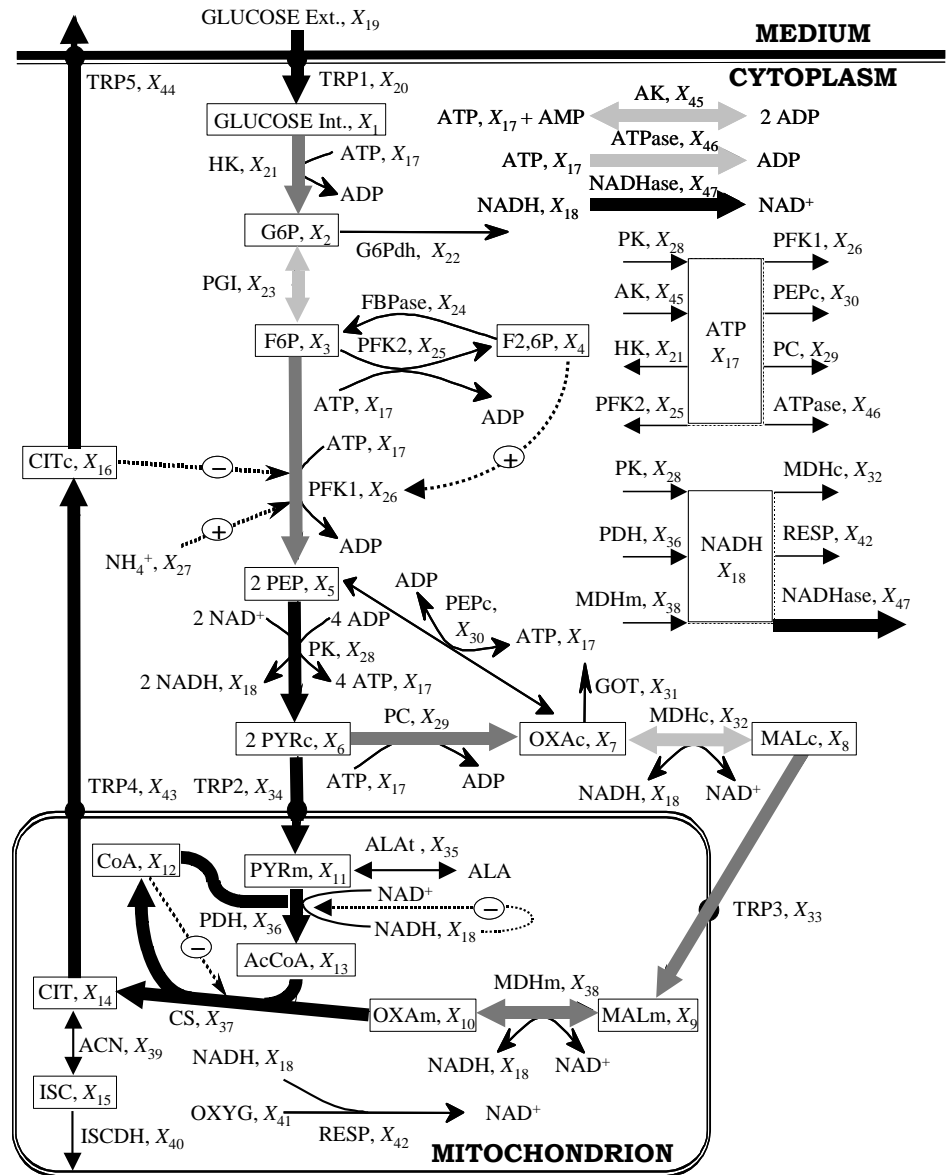
iterative methods, branch-and-reduce methods, geometric programming

# Example

Citric acid yield:

Optimization prescribes enzyme activity levels that lead to maximal citric acid production while satisfying constraints on metabolites and fluxes.

Maximal increase:  
~ 12 fold



## Notable Results

Citric acid system contains  $\sim 20$  accessible enzymes / genes

Optimize by allowing changes in all enzymes:

Yield increased  $\sim 12$  fold

Q: If only a single enzyme may be changed, which one should it be? How much could yield be increased?

A: No matter which enzyme is changed, yield does not really increase!

Q: Change 2, 3, ... enzymes. Yield improvement?

A: 2: none; 3: none, 4-6: almost none; 7 needed for  $\sim 3$  fold yield!

Interpretation: Standard techniques have found the easy solutions!

# Applications of BST

Pathways: purines, glycolysis, citric acid, TCA, red blood cell, trehalose, sphingolipids, lignin, ...

Genes: circuitry, regulation, expression patterns, ...

Signaling: MAPK, BMP4 (atherosclerosis)

Growth, immunology, pharmaceutical science, forestry, ...

Metabolic engineering: optimize yield in microbial pathways

Dynamic labeling analyses possible

Math: recasting, function classification, bifurcation analysis, ...

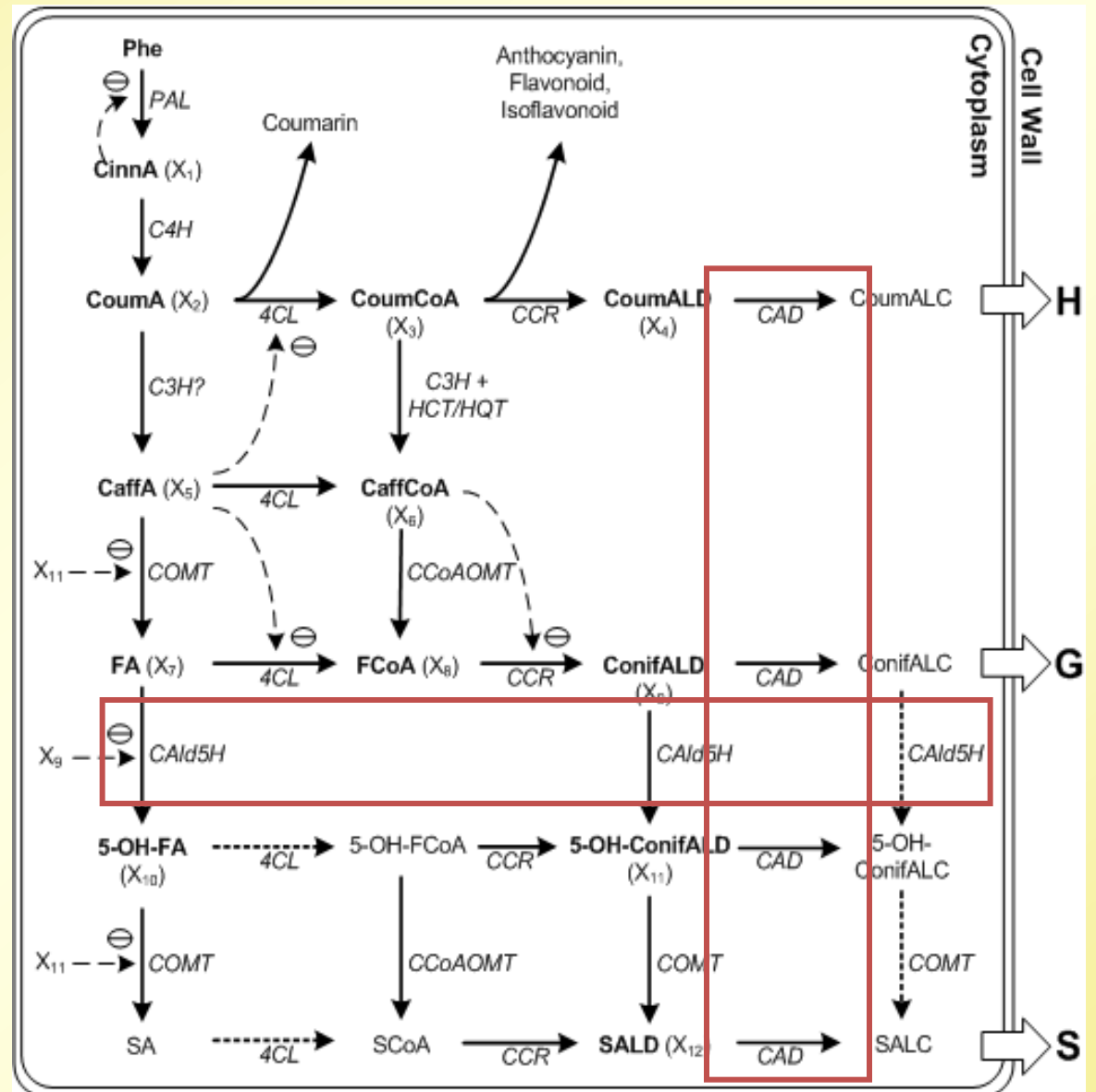
Statistics: S-system representation, S-distribution, trends; applied to seafood safety, marine mammals, health economics



# Lignin Biosynthesis in *Populus*

**Need for a Model:**

Multiple use of the same enzyme

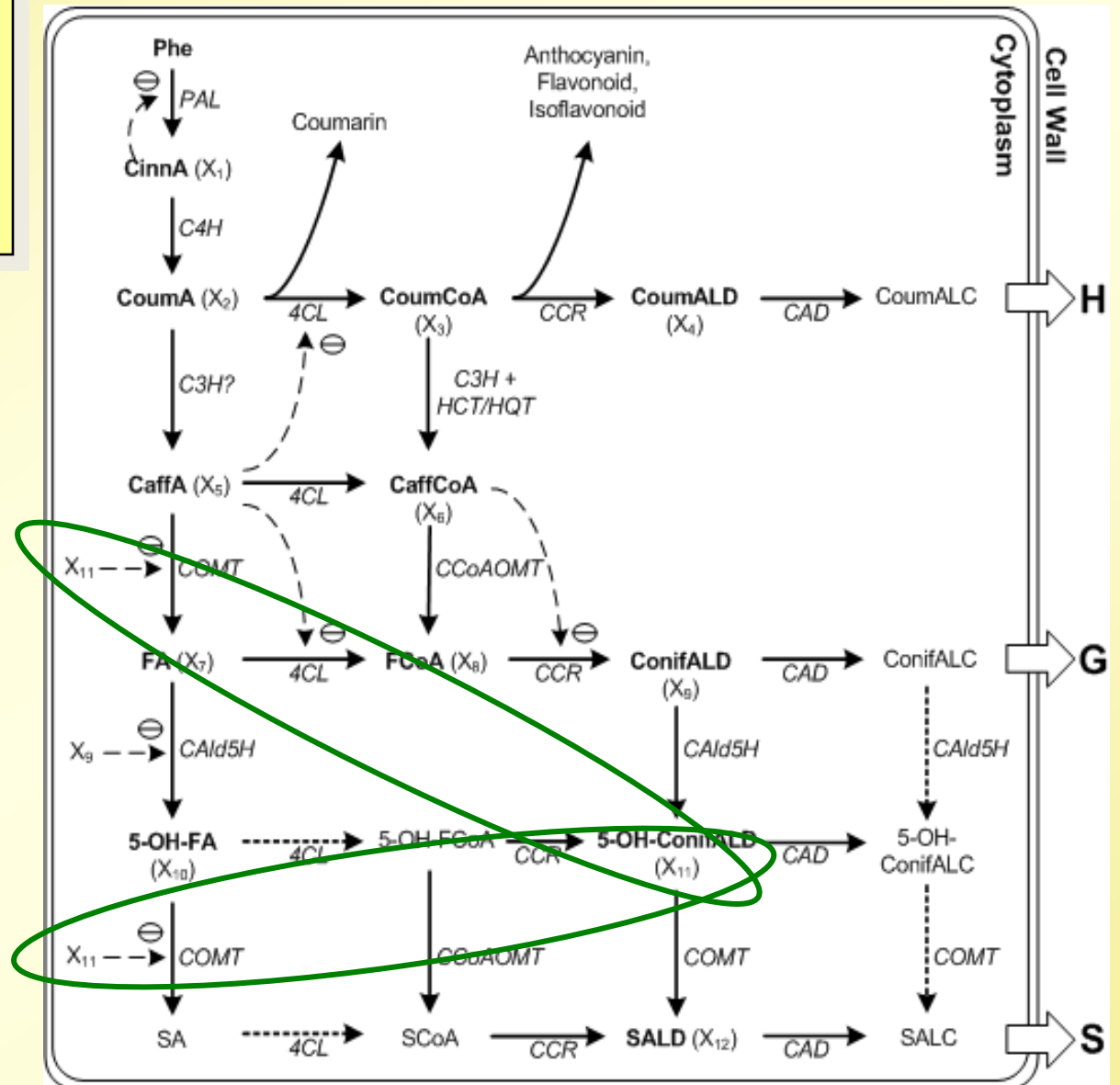


# Lignin Biosynthesis in *Populus*

## Need for a Model:

Multiple use of the same enzyme

Regulatory signals (e.g., feedback)



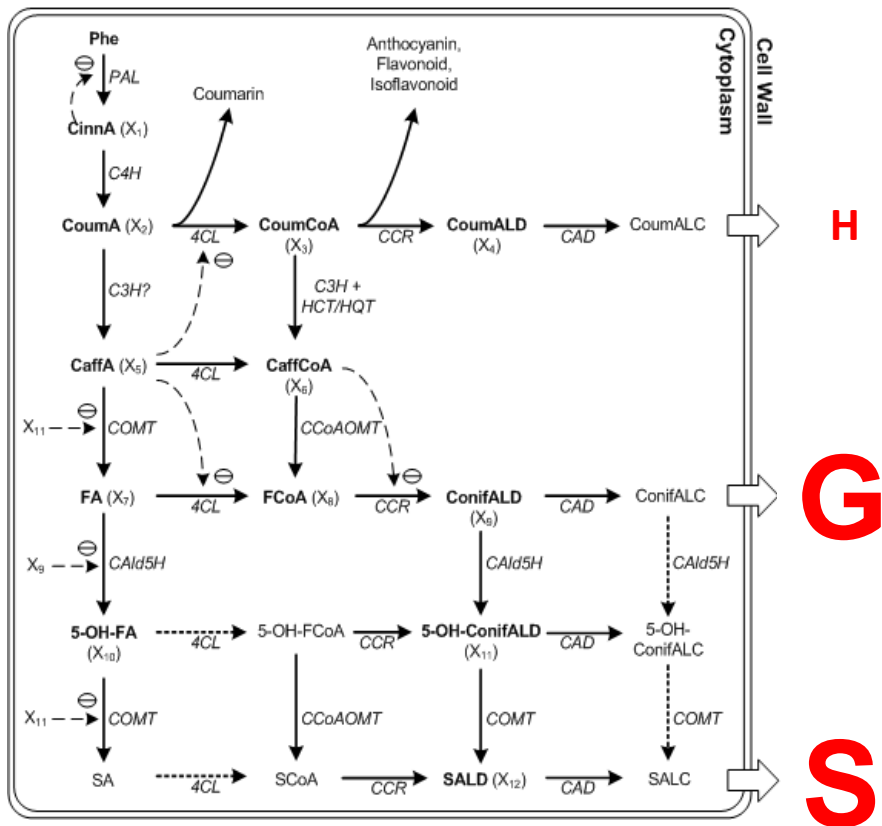
# Modeling Lignin Biosynthesis in *Populus*

## ***Five Modeling Steps:***

1. Use literature info (alleged pathway structure) to set up stoichiometric / FBA model → flux distribution
2. Convert FBA model into dynamic BST model, using additional literature information and default assumptions → dynamic model structure
3. “Train” model with some data (transgenic lines)
4. “Validate” model with other data → dynamic model
5. Use BST model, for instance, to propose optimized strains

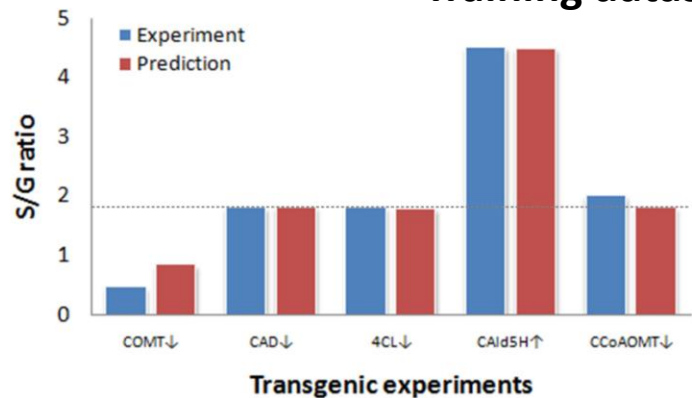
# Lignin Biosynthesis in *Populus* (FBA)

## Lignin biosynthetic pathway

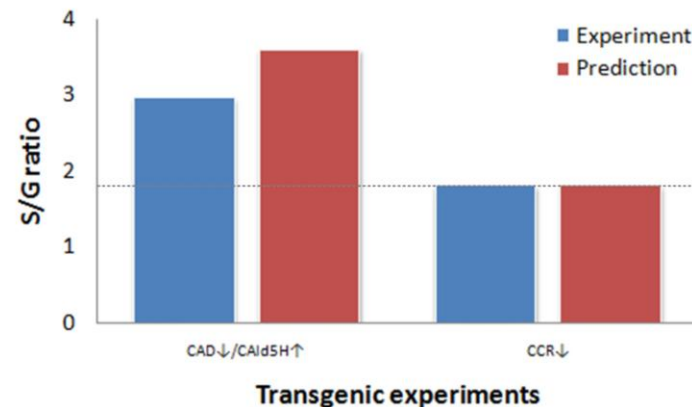


FBA: Computed S/G ratios are optimized to be consistent with experimental S/G ratios

## Training dataset



## Validation experiments



# Dynamic BST Modeling of Lignin Biosynthesis in *Populus*

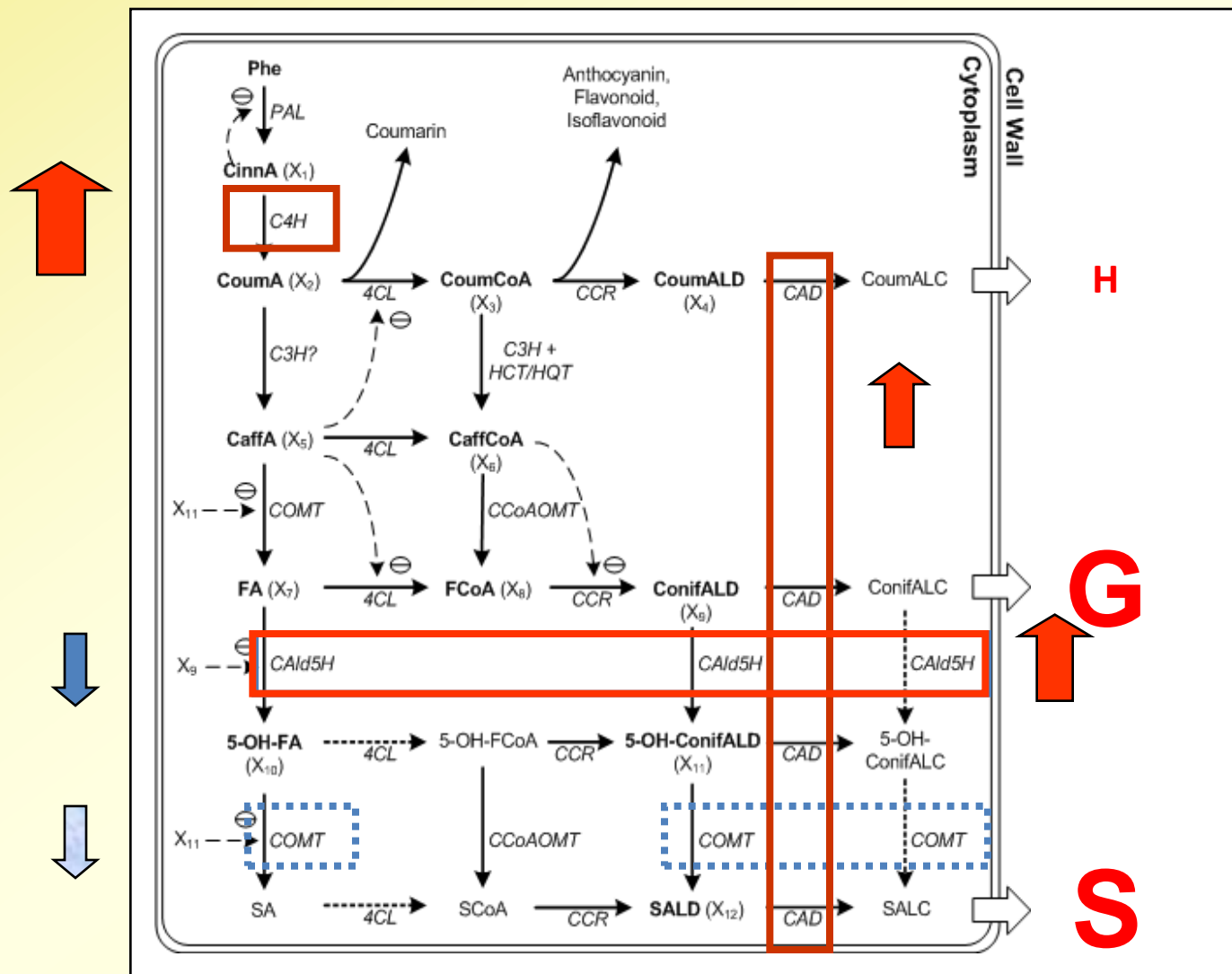
- Convert FBA model into dynamic BST model
- Optimization of the pathway toward higher xylose production by minimization of the S/G ratio

No. of Enzymes	Modified Enzymes	S/G Ratio
Wild-type	N/A	1.8
1	CAld5H (76%)	1.34
2	COMT (96%), CAld5H (71%)	1.29
3	C4H (431%), CAD (167%), CAld5H (134%)	1.11

Red annotations in the table: A red arrow points from 1.8 to 1.34 with the label "↓38%". Another red arrow points from 1.8 to 1.29 with the label "↓25%".

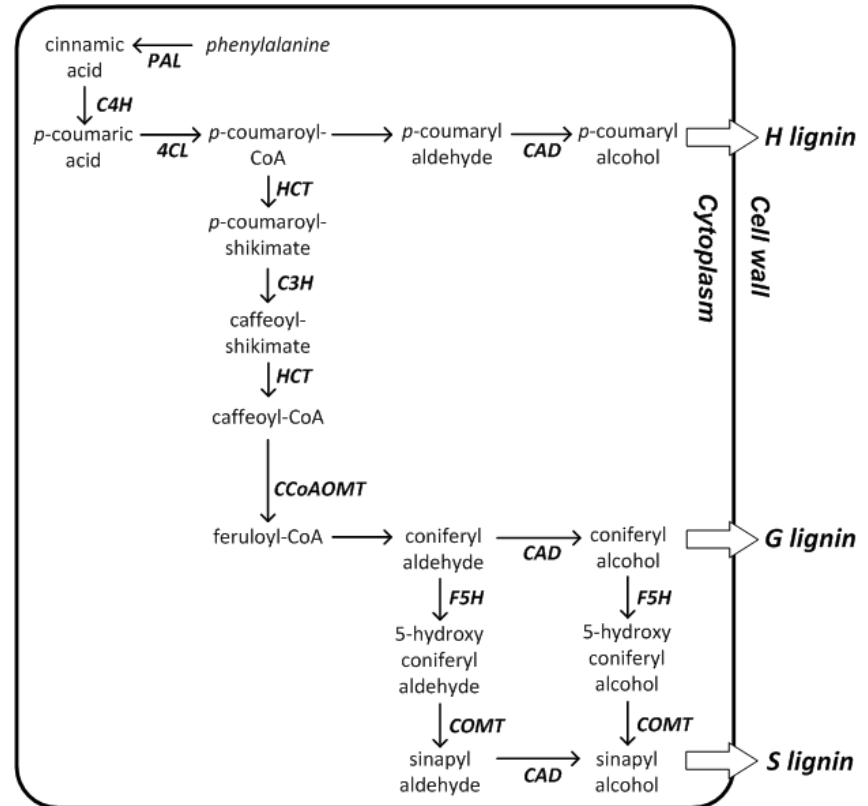
- According to the optimization results, one could achieve ~40% reduction in the S/G ratio by modifying three enzymes and ~25% by modifying just one enzyme (CAld5H)
- The set of two enzymes is not a subset of the set of three enzymes!
- CAld5H: Scenario 1: decrease; Scenario 2: increase!

# Optimization of Lignin Biosynthesis



# Mathematical Modeling of Lignin Biosynthesis in Alfalfa (*Medicago sativa* L.)

- Lignin pathway important:
  - ❑ Model of biofuel production; issues of recalcitrance
  - ❑ Enormously important feedstock; digestibility hindered by lignin



# Modeling Development

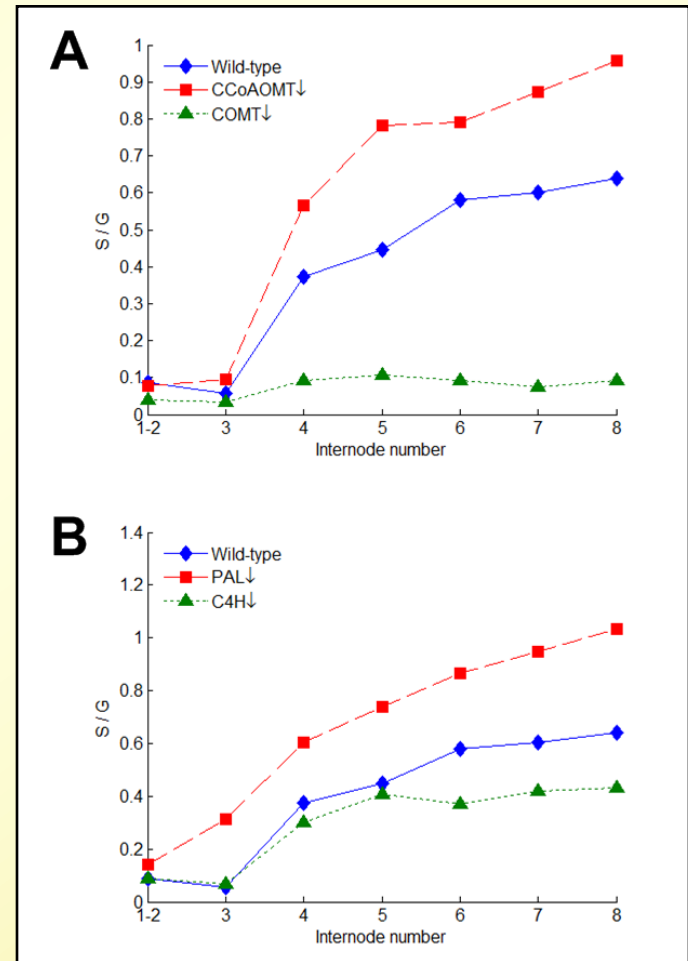
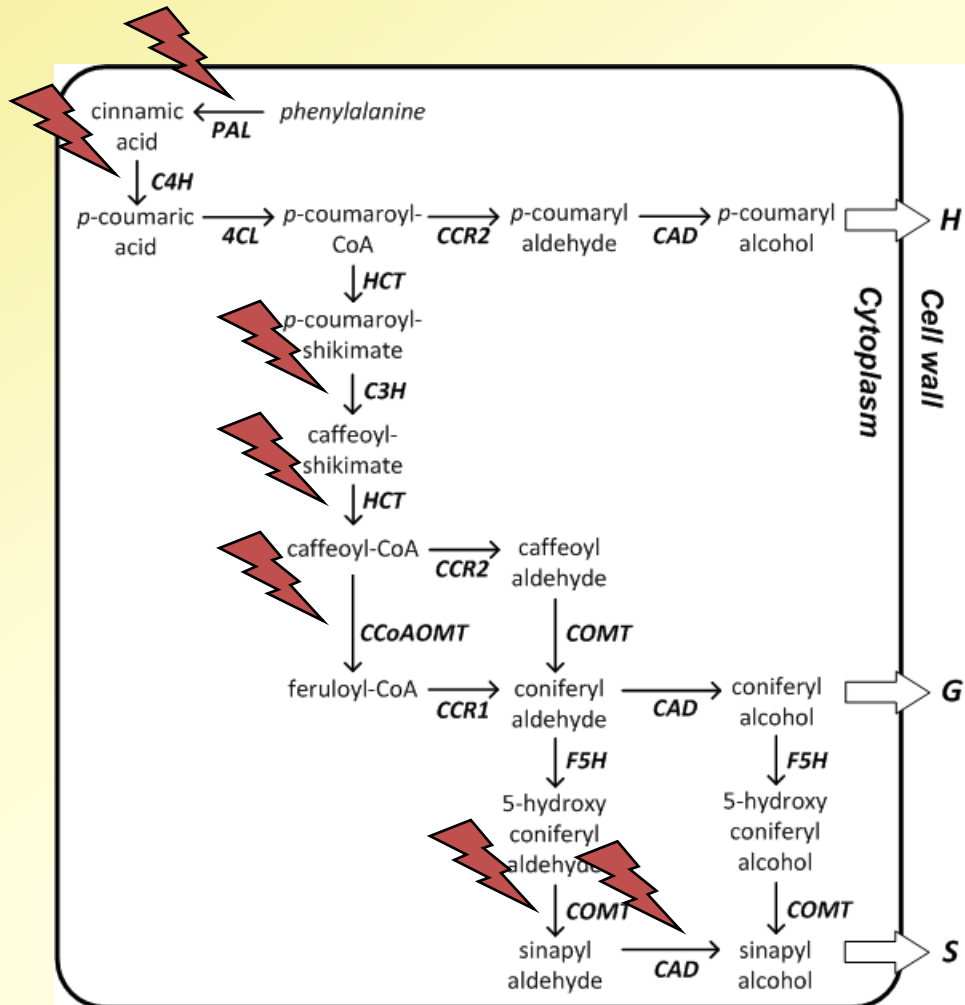
## *Steps of Analysis:*

1. Use gene/enzyme-modulation data from R. Dixon's group (Noble Center, Oklahoma)
2. Consider differences among internodes
3. Train and validate MOMA model with data
4. Analyze S/G trends during growth
5. Interpret results; formulate postulates
6. Convert FBA model into BST model; propose optimized strains (not yet done)





# Data: Enzyme (Gene) Knock-Downs

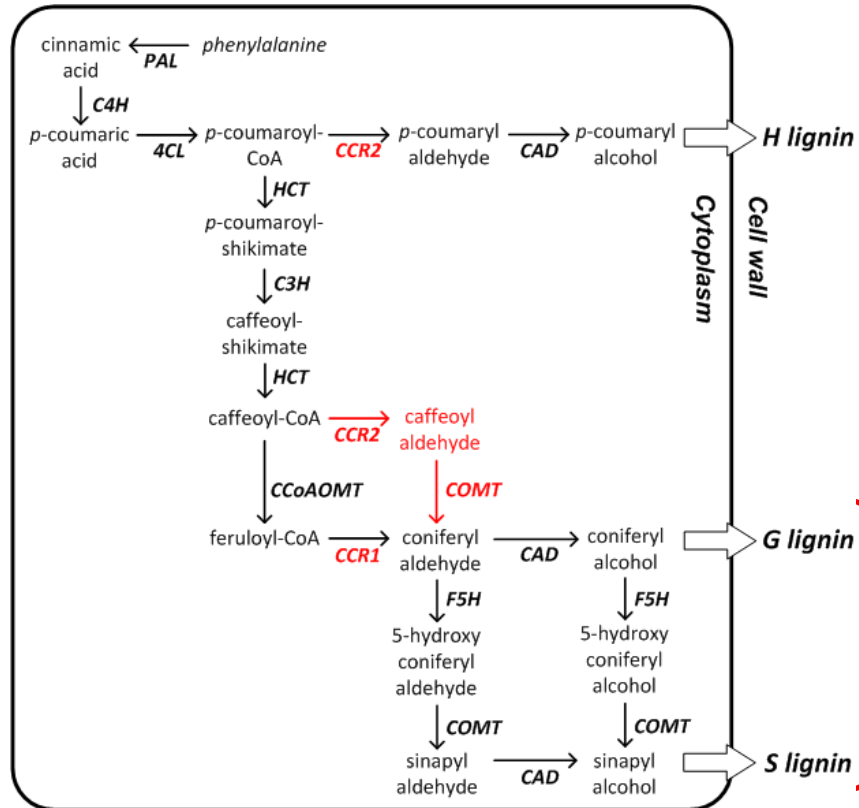


# Critical Questions

- ❑ Is the pathway correct as presently assumed?
- ❑ Are there independent pathways to G and S lignin?

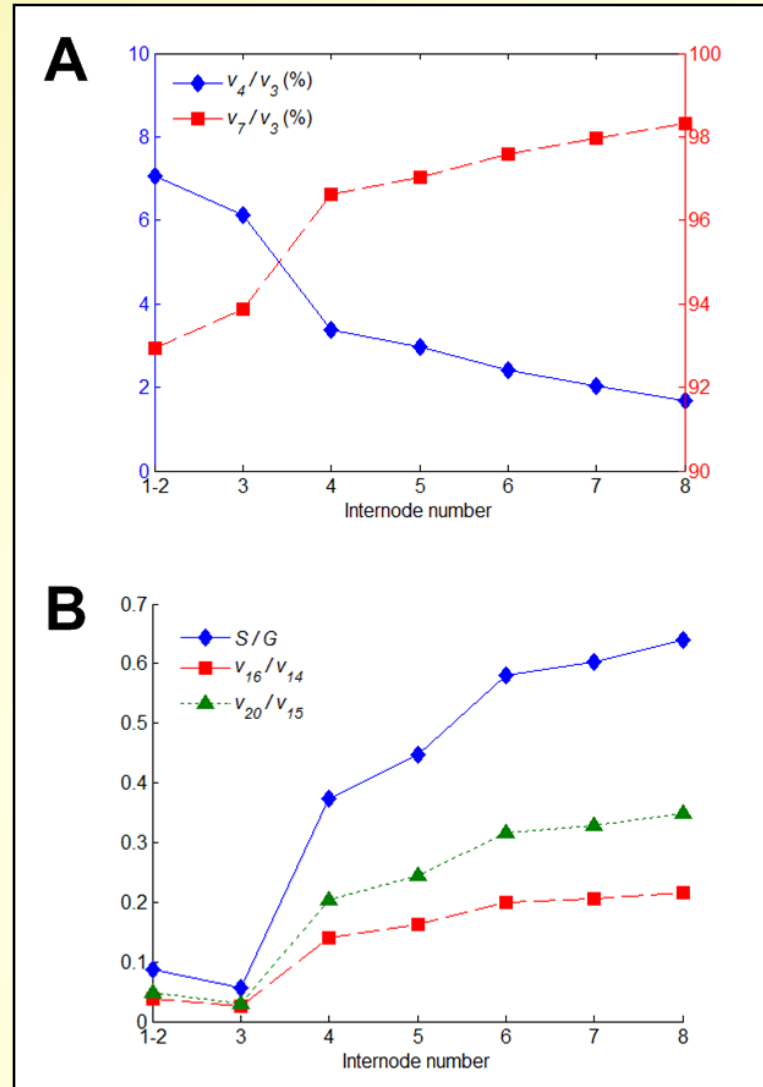
**Answer: NO**

**Revised pathway**



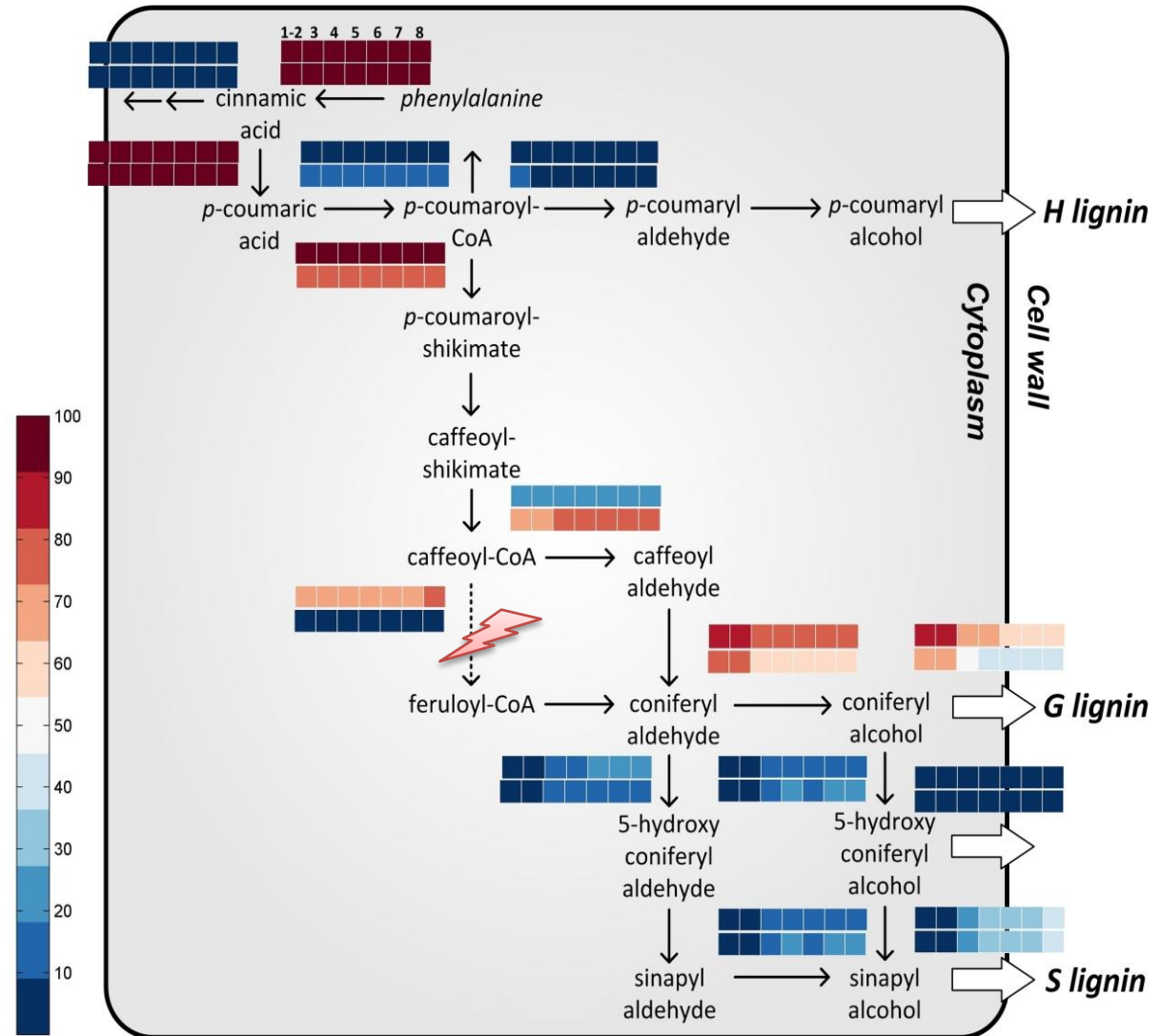
**S/G ↑ ??**

# First Result: Dynamic Flux Distributions



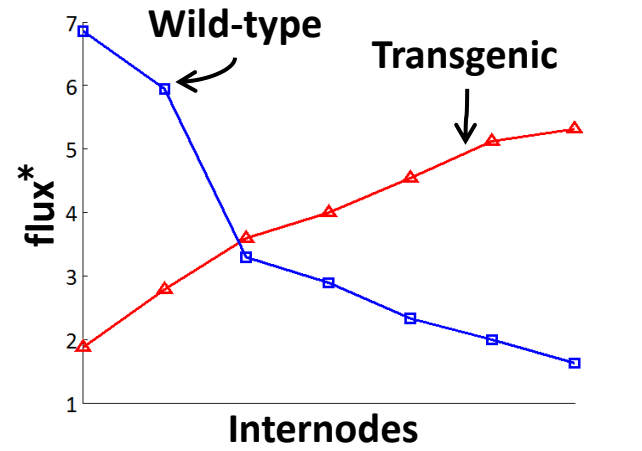
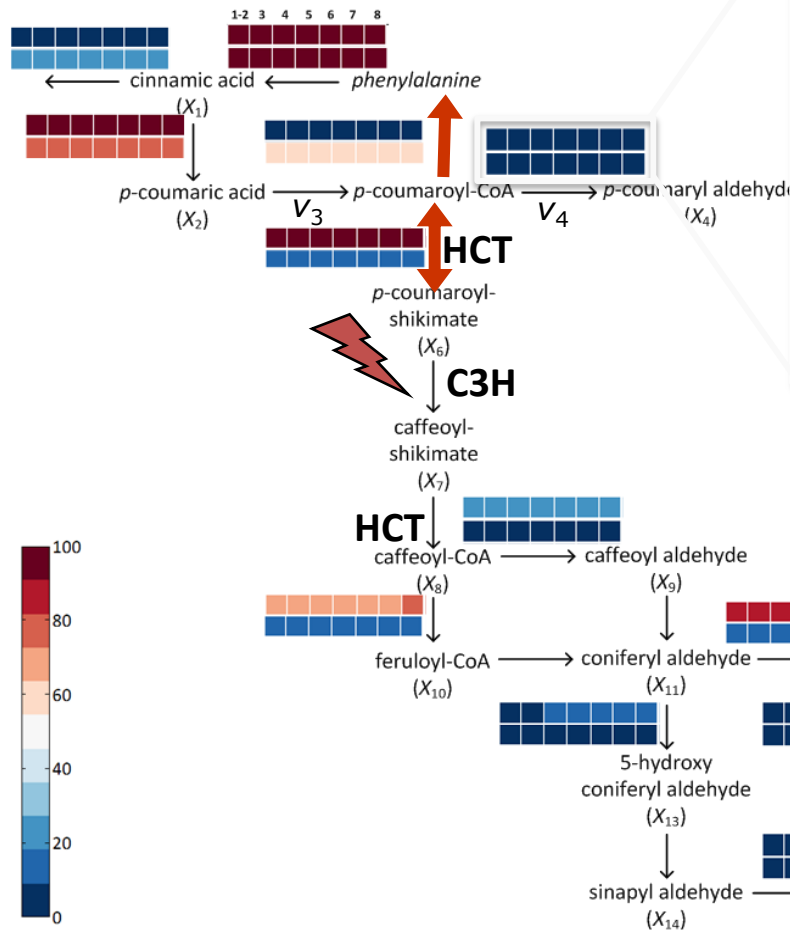
# Representation of Model Results

Example:  
Wild Type vs.  
CCoAOMT  
down-regulation



# Model-Based Postulates

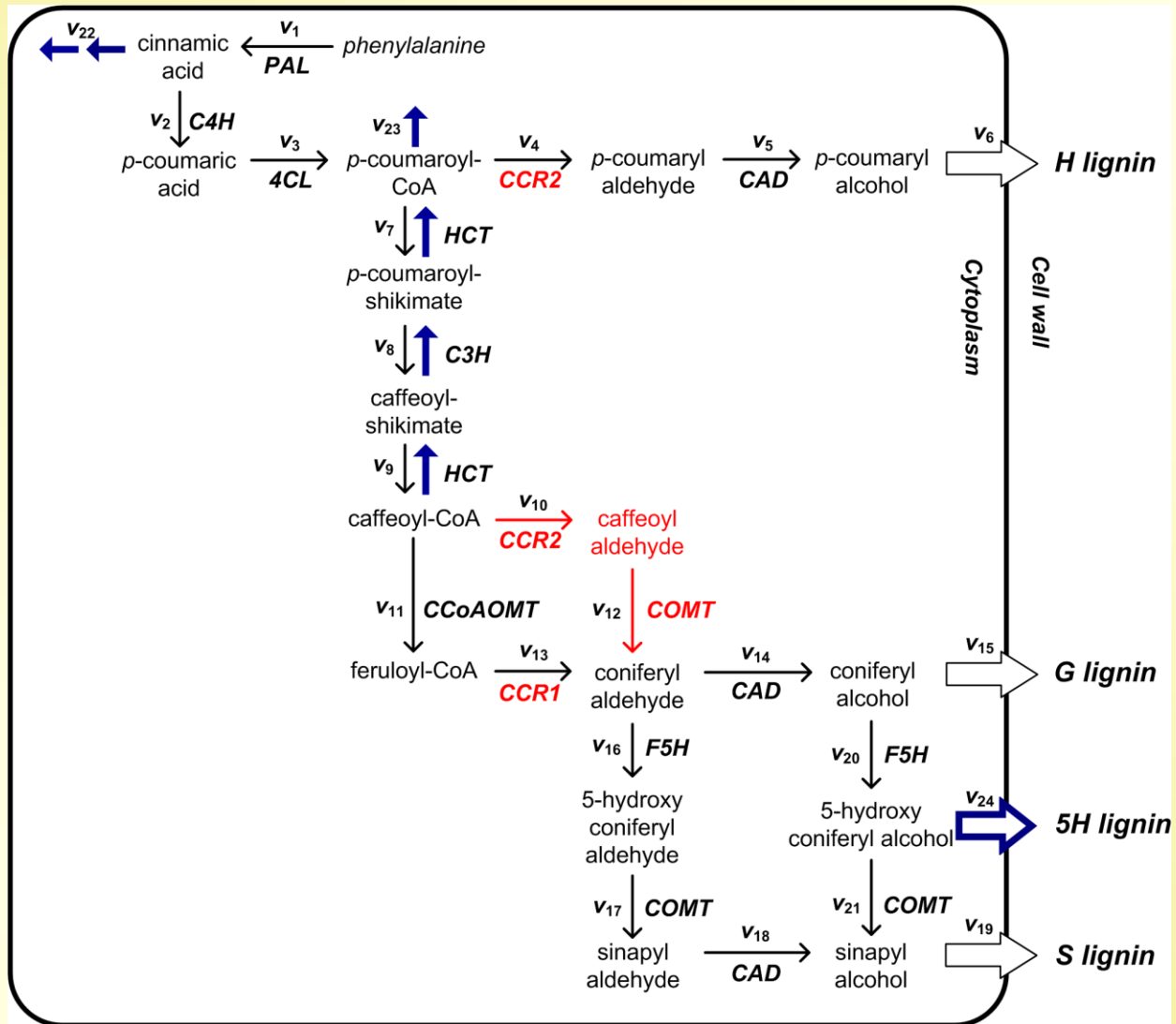
Example: C3H down-regulation: H  $\uparrow$



\* flux  $v_4$  in % of incoming flux  $v_3$

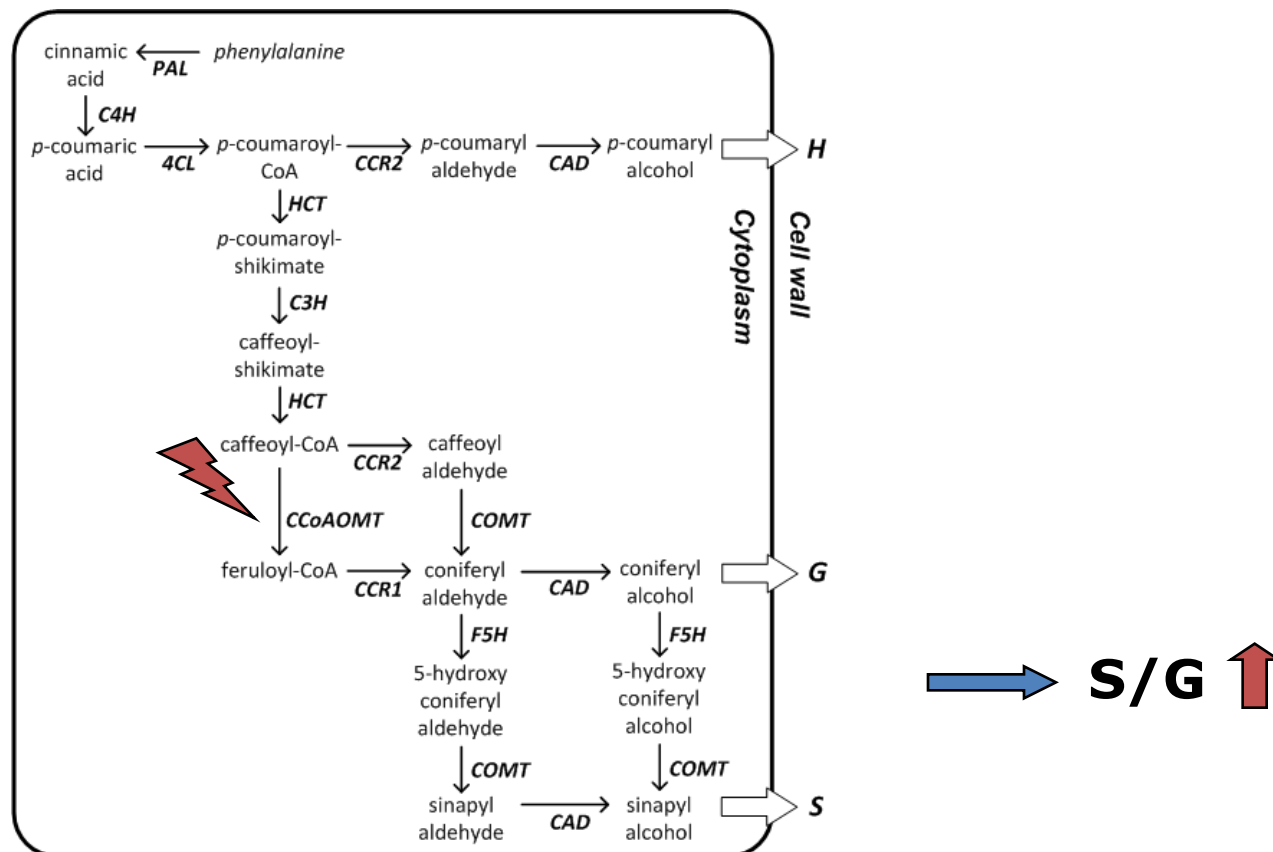
• Postulate 1: HCT must be reversible; excess p-coumaroyl-CoA used elsewhere

# Postulate: Additional Processes



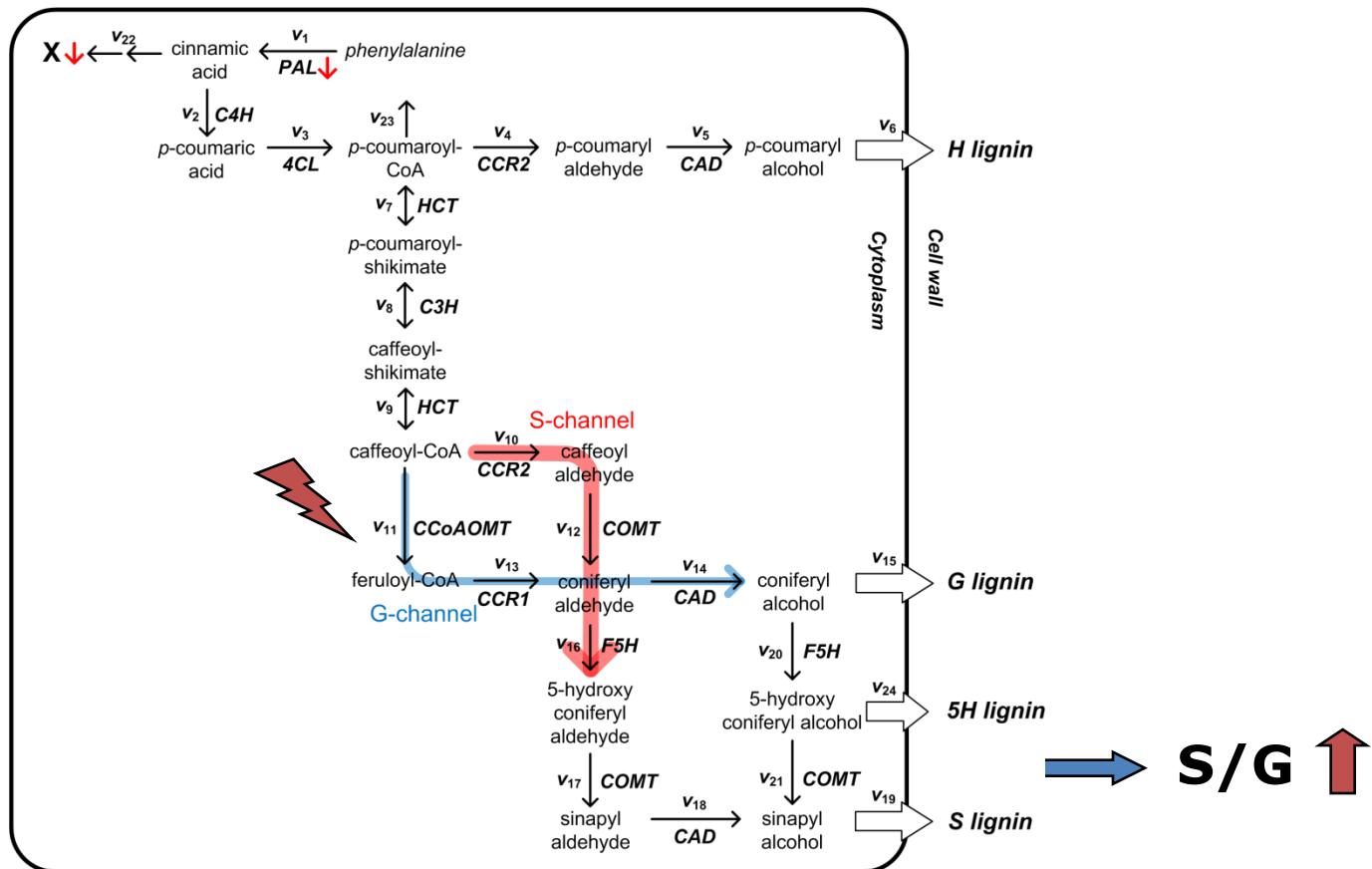
# Model-Based Resolution of a Puzzle

**Puzzle:** Down-regulation of CCoAOMT results in different S/G ratio than wild type, even though alteration occurs before common precursors



# Model-Based Channel Postulate

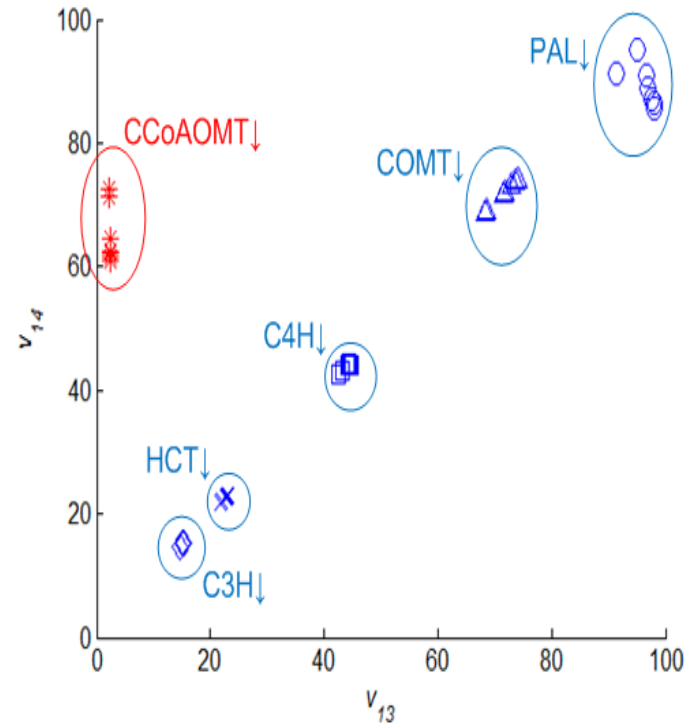
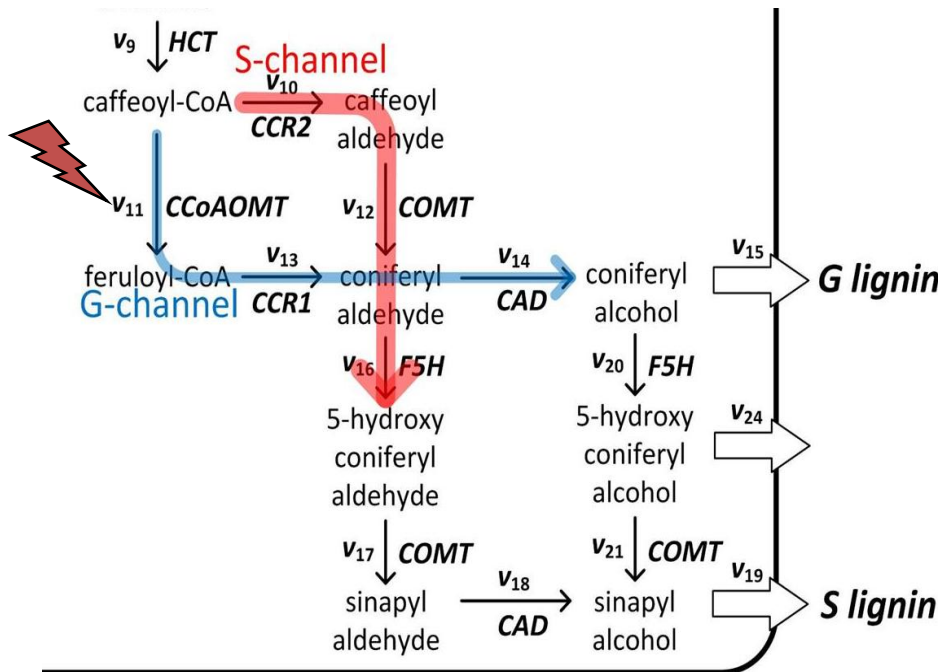
- Postulate 2: Existence of specific “S-channel” and “G-channel”





# Support for Channel Postulate

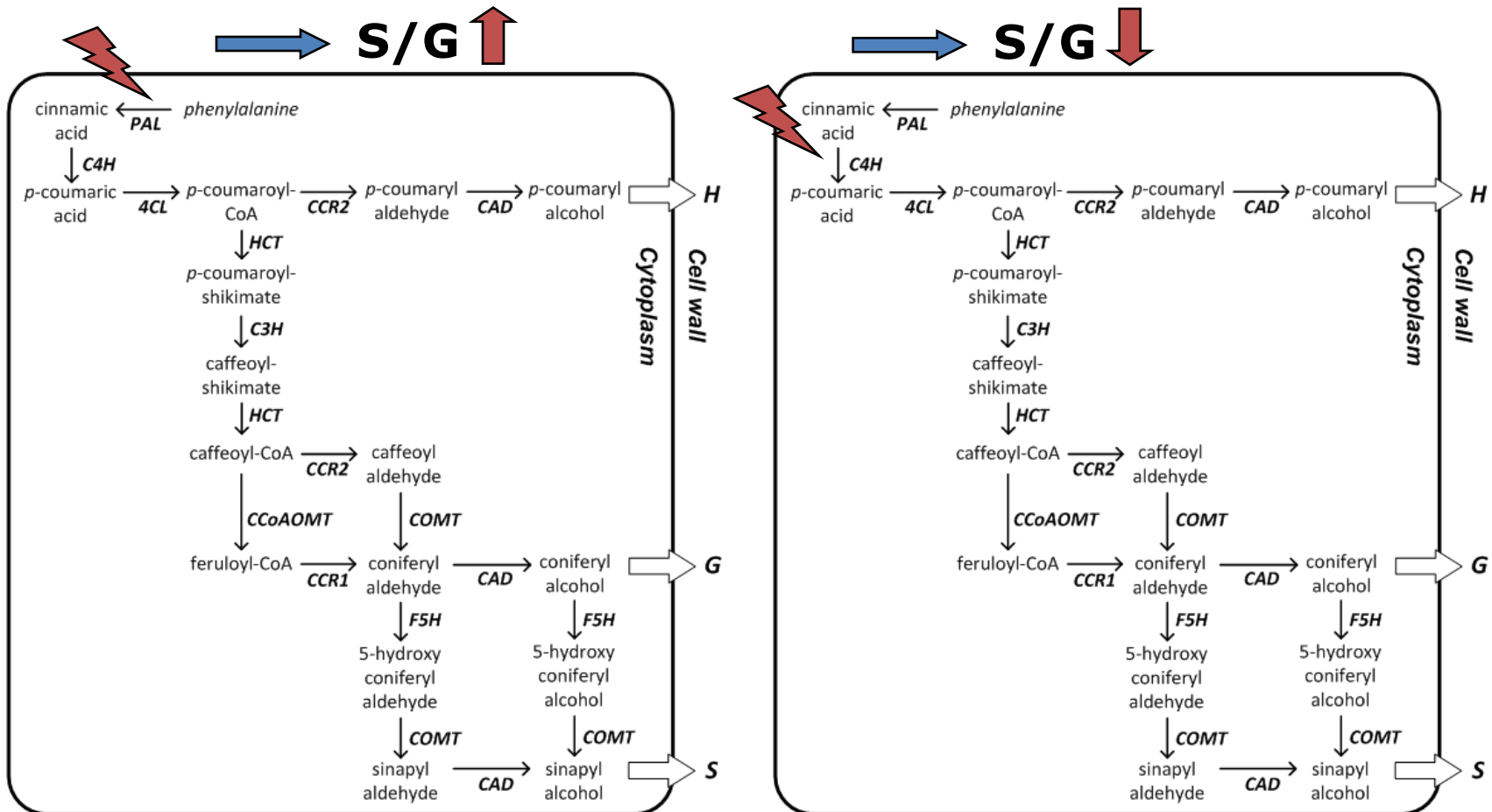
- “G-channel” fluxes very strongly correlated, except for  $\Delta\text{CCoAMT}$



→ S/G ↑

# Model-Based Resolution of a Puzzle

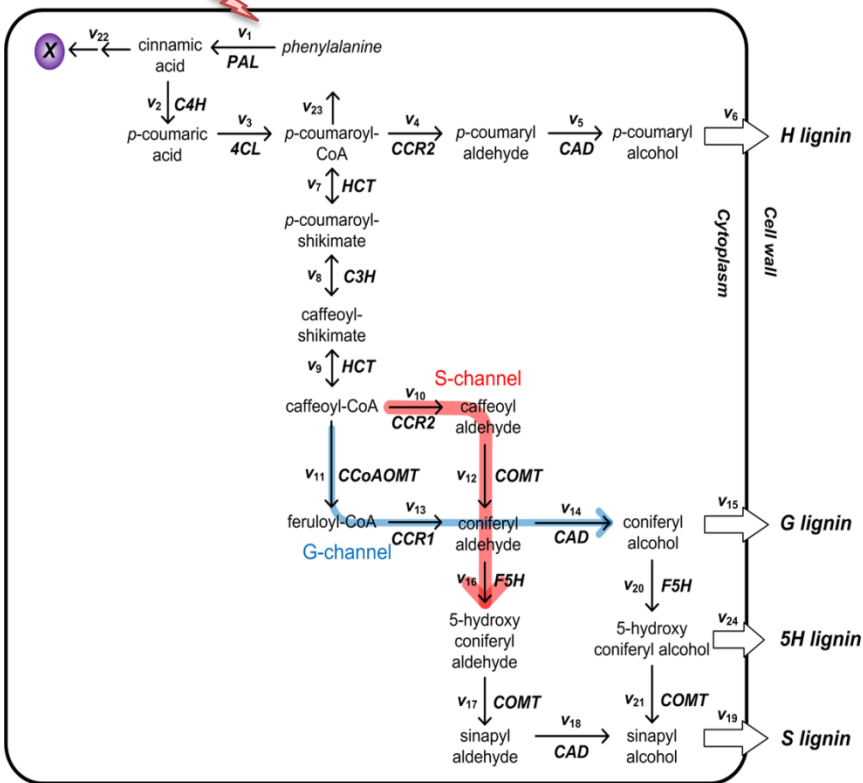
Puzzle: Down-regulation of PAL vs. C4H results in different S/G ratios



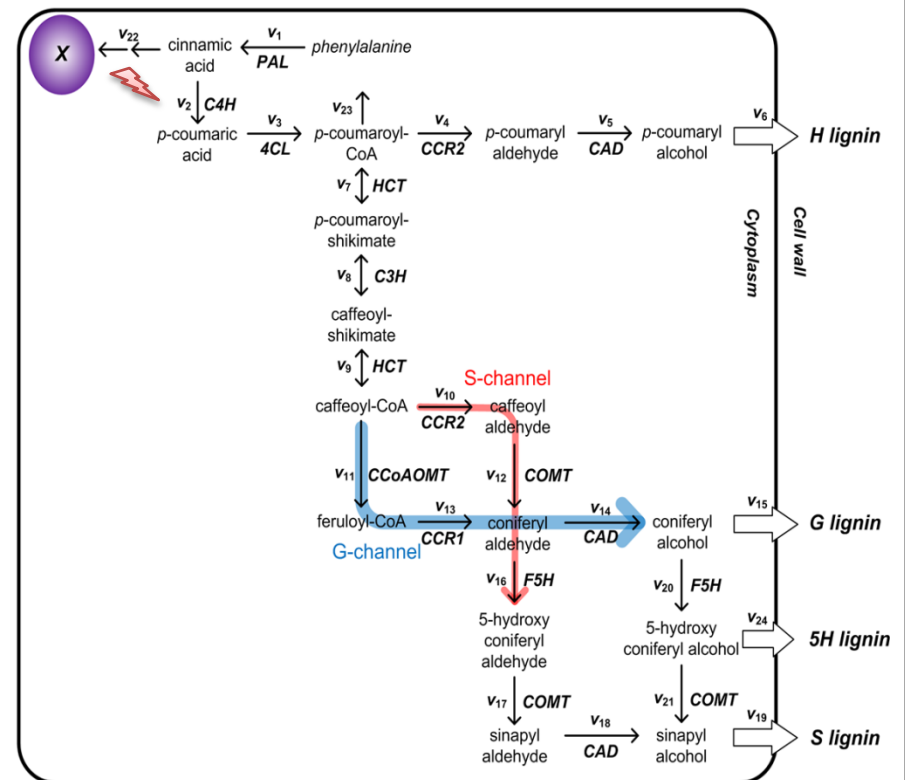
# Model-Based Signal Hypothesis

- Down-regulation of PAL or C4H results in different S/G ratios

PAL ↓, S/G ↑



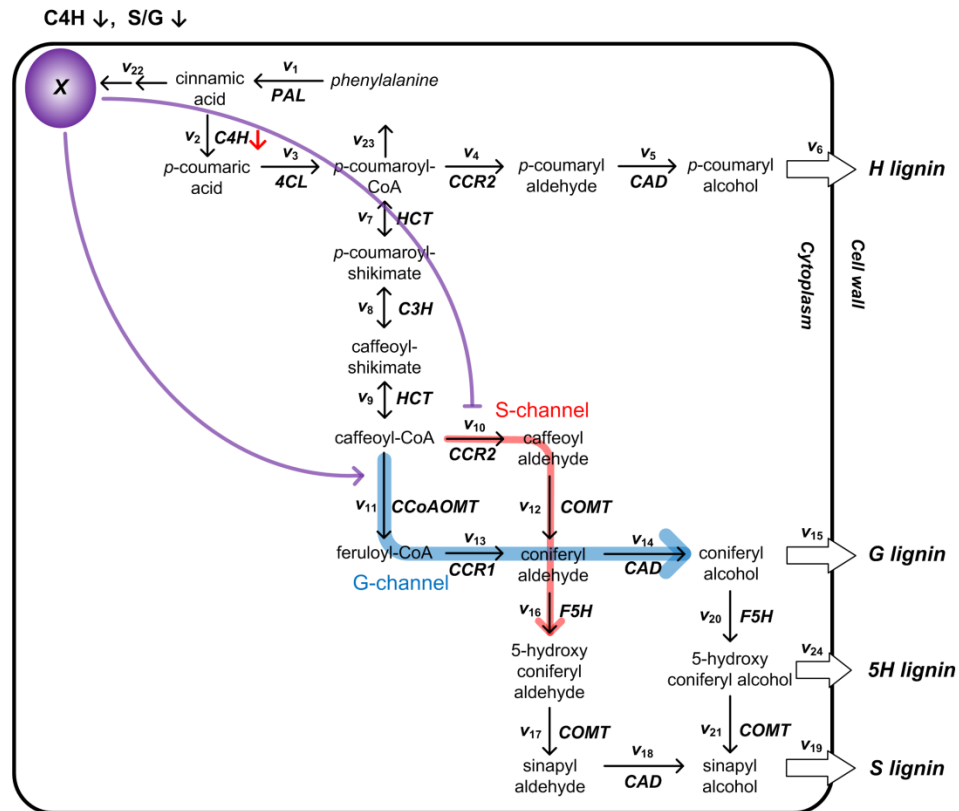
C4H ↓, S/G ↓



- Hypothesis: "S-channel" and "G-channel" are affected

# Model-Based Signal Postulate

- Down-regulation of PAL or C4H results in different S/G ratios



- Postulate:  
Some cinnamic acid derivative X controls “S-channel” and “G-channel”

## Next Steps

Experimental verification / refutation of postulates

Conversion of FBA/MOMA model into dynamic BST model

Optimization of BST model toward reduced S/G ratio

Experimental verification / refutation of knock-down combinations suggested by optimization

Execute similar analysis for switchgrass and other bioenergy crops

# Summary

- o Pathways of lignin biosynthesis are not fully understood
- o Intuitive predictions are problematic because of multiple uses of the same enzymes and because of regulation
- o Modeling can add genuine value to experimental data
- o Kinetic pathway information in the literature is scarce
- o Gene modulation data are of tremendous benefit
- o Principles and methods shown here also apply to modeling of lignin degradation
- o We are very grateful for DOE-BESC support

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