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Raman Research Institute

**GEOMETRY, TOPOLOGY  
AND DYNAMICS IN  
NEGATIVE CURVATURE**

Conference

Monday, 02 Aug, 2010 - Saturday, 07 Aug, 2010

Conference on

**GEOMETRY, TOPOLOGY  
AND DYNAMICS IN  
NEGATIVE CURVATURE**

Monday, 02 Aug 2010 - Saturday, 07 Aug 2010

**Organizers:**

C S Aravinda  
F T Farrell  
J F Lafont  
S K Roushon  
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**Program Link**

<http://www.icts.res.in/program/gtdnc>

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## Program

**NOTE :** Morning Sessions (Plenary Lectures) will be at RRI Main Building Auditorium.  
Afternoon Sessions (Parallel Sessions) will be split between this venue and will be at Library Block Lecture Hall.).

### Monday, August 2

09:30 – 10:00 Inauguration by **Ravi Subrahmanyam**  
Director, RRI, Bangalore  
and Keynote address by **S G Dani**

10:00 – 10:30 Coffee/Tea break

10:30 – 11:30 Plenary Lecture 1  
**Martin Bridson**

11:30 – 12:00 Break

12:00 – 13:00 Plenary Lecture 2  
**Emmanuel Breuillard**

13:00 – 14:30 Lunch break

14:30 – 15:30 Parallel Session 1  
**Pallavi Dani**  
**Anne Thomas**

15:30 – 16:00 Coffee/Tea break

16:00 – 17:00 Parallel Session 2  
**Marc Bourdon**  
**Indira Chatterji**

### Tuesday, August 3

09.00 – 10.00 Plenary Lecture 3  
**Etienne Ghys**

10:00 – 10:30 Coffee/Tea break

10:30 – 11:30 Plenary Lecture 4  
**Marc Burger**

11:30 – 12:00 Break

12:00 – 13:00 Plenary Lecture 5  
**Tom Farrell**

13:00 – 14:30 Lunch break

14:30 – 15:30 Parallel Session 3  
**Uri Shapira**  
**Mahan Mj**

15:30 – 16:00 Coffee/Tea break

16:00 – 17:00 Parallel Session 4  
**Jayadev Athreya**  
**Jens Heber**

### Wednesday, August 4

09.00 – 10.00 Plenary Lecture 6  
**Mladen Bestvina**

10.00 – 10.30 Coffee/Tea break

10.30 – 11.30 Plenary Lecture 7  
**Yves Benoist**

11.30 – 12.00 Break

12.00 – 13.00 Parallel Session 5  
**Gerhard Knieper**  
**Igor Mineuyev**

13.00 – 14.30 Lunch break

14.30 – 15.30 Parallel Session 6  
**Enrico Leuzinger**  
**Igor Belegradek**

15.30 – 16.00 Coffee/Tea break

16.00 – 17.00 PUBLIC LECTURE  
**Speaker: Patrick Eberlein**  
**Title: Ergodic behavior in Negative Curvature**

### Thursday, August 5

09.00 – 10.00 Plenary Lecture 8  
**Francois Labourie**

10.00 – 10.30 Coffee/Tea break

10.30 – 11.30 Plenary Lecture 9  
**Shahar Mozes**

11.30 – 12.00 Break

12.00 – 13.00 Plenary Lecture 10  
**Nimish Shah**

13.00 – 14.30 Lunch break

14.30 – 15.30 Parallel Session 7  
**Chris Connell**  
**Viktor Schroeder**

15.30 – 16.00 Coffee/Tea break

16.00 – 17.00 Parallel Session 8  
**Dave Constantine**  
**Frederic Paulin**

### Friday, August 6

09:00 – 10:00 Plenary Lecture 11  
**Keith Burns**

10:00 – 10:30 Coffee/Tea break

10:30 – 11:30 Parallel Session 9  
**Alex Gorodnik**  
**Jean-Francois Lafont**

11:30 – 12:00 Break

12:00 – 13:00 Parallel Session 10  
**Peter Linnell**  
**Darren Long**

13:00 – 14:30 Lunch break

14:30 – 15:30 OPEN PROBLEMS SESSION  
Chaired by : **S.G. Dani, Mike Davis,**  
**Pedro Ontaneda**

15:30 – 16:00 Coffee/Tea break

### Saturday, August 7

09:00 – 10:00 Plenary Lecture 12  
**Gerard Besson**

10:00 – 10:30 Coffee/Tea break

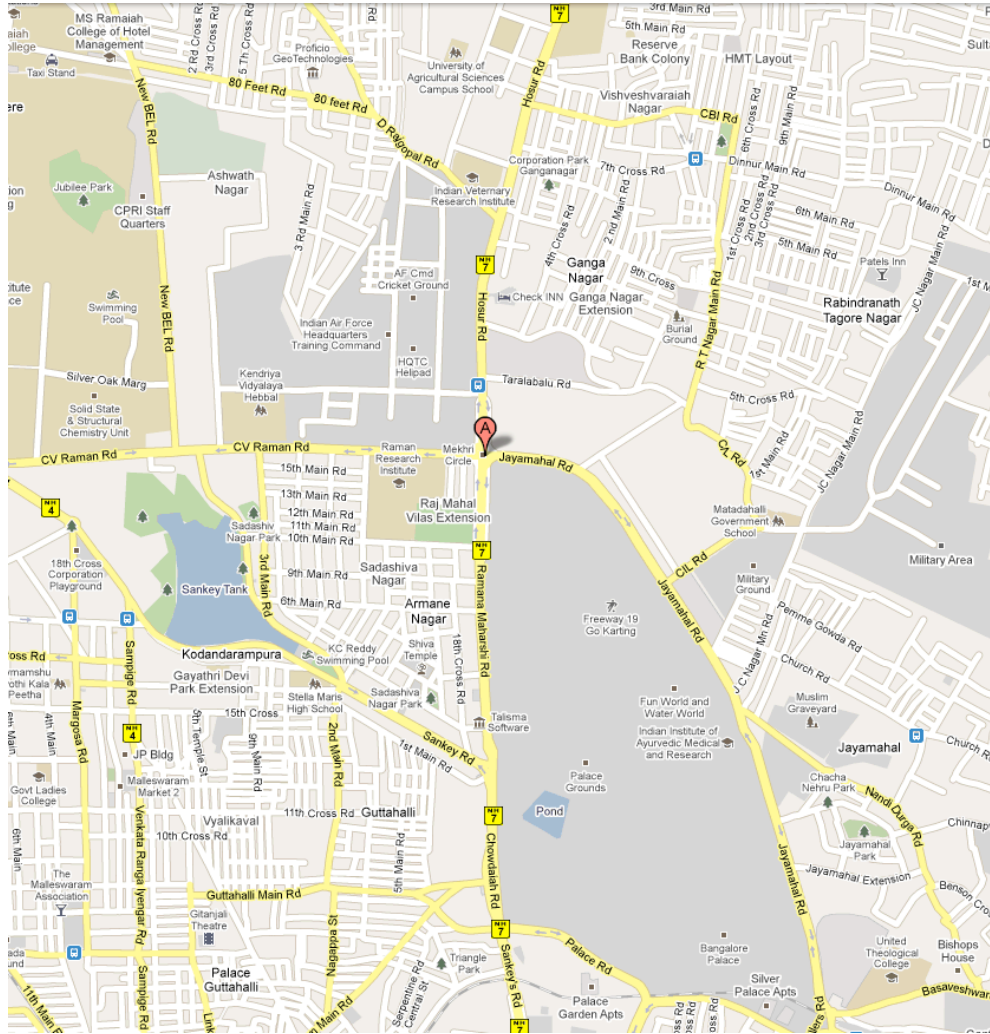
10:30 – 11:30 Plenary Lecture 13  
**Tadeusz Januskiewicz**

11:30 – 12:00 Break

12:00 – 12:30 Valedictory address by : **Ravi Kulkarni**  
and Concluding Session

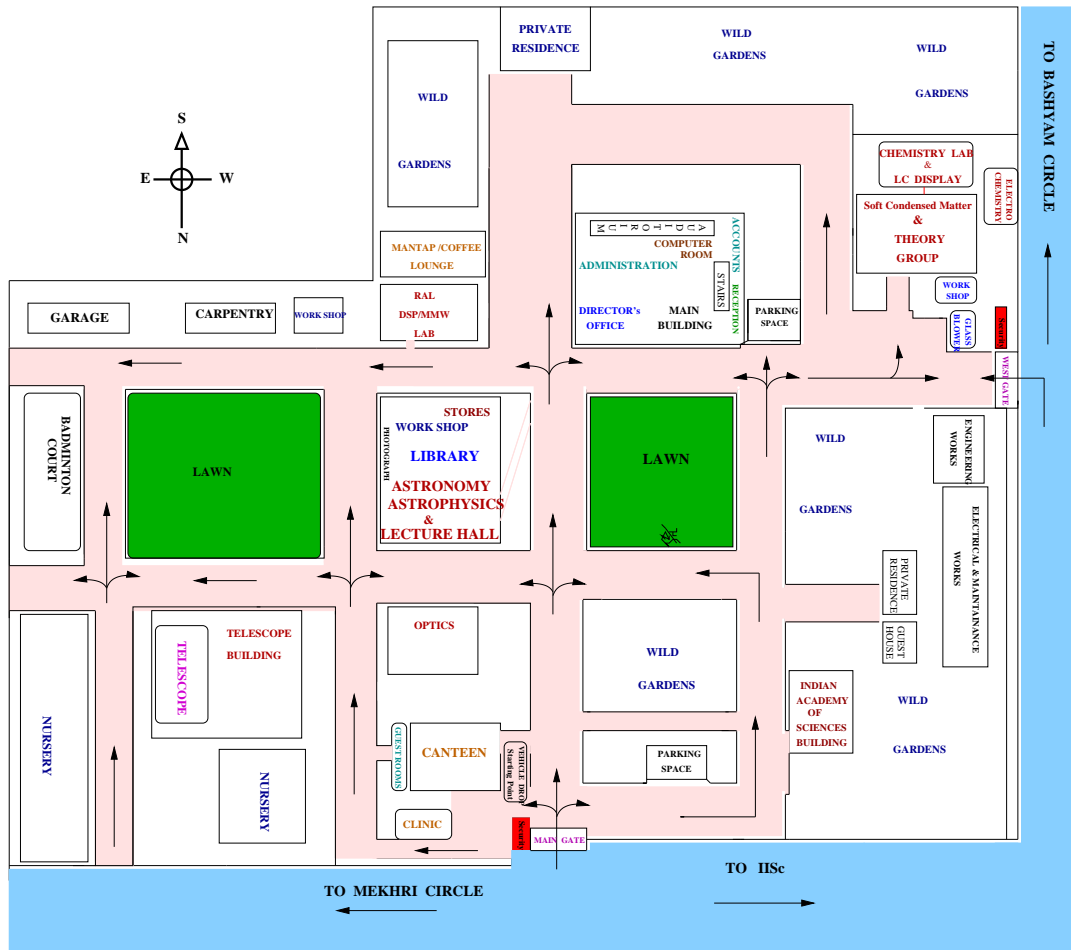
12:30 Proceed for Lunch and disperse

## Local area Map



# Plan of Buildings

## CAMPUS MAP OF RAMAN RESEARCH INSTITUTE





## Places of Accommodation, their contacts and Landmarks

Accommodation for the participants are being provided at the following places:

1. **Tranquil Orchards**

#137/7, 9th Main Road, 6A Cross Street  
Sadashivanagar  
Bangalore - 560 080

Phone: 080-40952255      Mobile: 9840703814

Website: [www.tranquilorchards.com](http://www.tranquilorchards.com)

2. **The Green Path**

# 32/1, New BEL Road  
Seenappa Layout  
R.M.V. Extension  
Bangalore - 560 094

Phone: 080-42664777      Mobile: 9739458684

E-mail: [thegreenpathblr@gmail.com](mailto:thegreenpathblr@gmail.com)

Website: [www.thegreenpath.in](http://www.thegreenpath.in)

3. **United Theological College (UTC)**

# 63, Millers Road  
Benson Town  
Bangalore - 560 046

Phone: (General): 80-23333438 / 23330502

Fax: 80-3330015

E-mail (General): [unitedtcb@gmail.com](mailto:unitedtcb@gmail.com)

*Landmarks to Stay Places will continue in the next page.*

## Landmarks to Stay places from Bangalore Airport

After you land at Bangalore International Air Port, as you leave the terminal, go to the MERU TAXI counter.

Ask to be taken directly to your place of stay; if they ask for a landmark, you may mention **Mekhri Circle**. The fare should be about Rs.600/- (not more than that).

All the three places that we have employed for this conference are within about 3 kilometers radius of the **Mekhri Circle/Raman Research Institute (RRI)**. Consult the attached map to find the exact location: In the map, Mekhri Circle/RRI is more or less in the centre; **Tranquil Orchards (TO)** is just behind RRI; **The Green Path (GP)** is near the top left corner close to “M.S. Ramaiah College of Hotel Management”; and, **United Theological College (UTC)** is near the bottom right corner. Given below are precise addresses of each of the three places and instructions on how to get there:

### Tranquil Orchards

#137/7, 9th Main Road, 6A Cross Street  
Sadashivanagar  
Bangalore - 560 080

As the taxi approaches **Mekhri Circle** from the Airport, it should not go through the underpass but move leftwards so as to be in position to take a right turn.

Turn right onto a divided road. After about 100 metres, you will pass the RRI Campus on your left. It is a wooded campus with a stone wall. Just after the RRI campus ends, there is a left turn (labelled 5th Cross). Skip this turn and take the next left turn (6th A Cross). Continue on this road about 100 metres till it ends in a T junction. At the **T** junction turn left and almost immediately right. **TO** is on your left just after a Bank.

### **The Green Path**

# 32/1, New BEL Road  
Seenappa Layout  
R.M.V. Extension  
Bangalore - 560 094

As the taxi approaches **Mekhri Circle** from the Airport, it should not go through the underpass but move leftwards so as to be in position to take a right turn.

Turn right onto a divided road. After about 100 metres, you will pass the RRI Campus on your left. It is a wooded campus with a stone wall. Keep going for about a Kilometer till you come to a traffic light. Turn right at the light (you will see a police station as you do so) onto new BEL road. After about 2 km, you will pass Ramaiah Hospital on your left. Spot “Raymonds showroom” to your right, immediately after which take a right turn. **GP** is on your left, after about 200 meters.

### **United Theological College (UTC)**

# 63, Millers Road  
Benson Town  
Bangalore - 560 046

As the taxi approaches **Mekhri Circle** from the Airport, it should not go through the underpass but move leftwards so as to be in position to take a left turn. After turning left, proceed about 2 kilometers, turn to your left on Basaveshwara Main Road. After about 100 meters you will see the **UTC** entrance gate to your left. A prominent landmark very close to UTC, that may be mentioned to the Taxi driver is the **Cantonment Railway Station**.

## **Transportation**

### **Getting to the Conference Venue.**

Tranquil Orchards: **TO** is within walking distance of the conference venue. As you leave TO building turn right onto the road, and when this road ends, turn left and then immediately right. Walk three blocks and turn right. You will see the RRI stone wall and a gate (this is the west gate, a side entrance to the Institute). Enter through this gate and walk till you see a lawn with a lone tree. The Main building which faces the lawn is the conference venue.

The Green Path and UTC: Transport is arranged everyday from these places of stay to the conference venue. There will be two trips in the morning (8:00 and 8:30) and two return trips (5:30 and 6:00) each day. If you rise early please go by the first trip so that the van goes as full as possible.

If you are stout of heart and would like to go at your own time, there are three wheelers (called autorickshaws) that you can hire. The minimum fare is Rs 17/- for distances under 2 km. Ask them to go to Mekhri circle.

From UTC: After you reach Mekhri circle continue about 100 metres till you reach the RRI campus (stone wall and wooded). The main RRI entrance gate is on your left.

From Green Path: After you reach Mekhri Circle you have to make a 'U' turn and double back (it is legal) to reach the RRI main entrance.

## Discussion Spaces

There are many places on the campus for informal discussions. There are lounges near the library seminar hall and at the library entrance, in the Theory Group, downstairs as well as up in the theoretical physics floor. In addition, there are discussion rooms inside the library. Most of these spaces have black boards, though you may have to pinch some chalk from the nearest office. Another place outdoors is the VILLAGE near the Canteen, where you can sit at a table and discuss with a writing pad. For peripatetic mathematicians, there are also the woods behind the main building which you can use, with due regard to the private residence at one end. There are still more spaces available in the Water Tower building and the Academy building which you can explore if necessary.

## Computer Access

A wireless connection to the internet can be accessed from your laptop at the following locations: Theoretical Physics Lounge, Library Seminar Hall Lounge, Canteen, both auditoria and the Soft Condensed Matter Lounge Wireless Authentication details:

SSID: rriwlan

Encryption: WEP

Key(Hexadecimal 64-bit): 6465d696cb

Configure the browsers to use proxy server

Proxy: 172.16.1.19

Port: 3128

## **Book Stores and Shopping Places**

There is a book shop, Tata Book House, at IISc. Campus. Indian Institute of Science (IISc.) is located about a kilometer from the Raman Research Institute towards West.

For more general books, there is a book shop, Swapna Book Store, Vyalikaval, Bangalore (its near Bhashyam Circle).

Shopping : The main shopping areas are downtown in M.G. Road (Mahatma Gandhi Road) and Commercial Street. Autorikshwas (three wheelers) are the most convenient form of transport). They charge by the meter. Closer by there is Mantri Mall in Malleswaram.

## Useful information

### Medical Stores (Pharmacies)

There are couple of Medical Stores available near RRI. They do deliver the medicines on request. The addresses are:

#### **Dhanvanthari Medicals and Generals**

502, 10th Cross, 8th Main  
Sadashivanagar  
Bangalore 560080

Phone: 080-2361 0036

#### **Sai Sudha Medicals**

No. 524, 11th Cross  
Rajmahal Vilas Extension  
Sadashivanagar  
Bangalore 560080

Phone: 080-2361 0244

#### **Sri Balaji Medical Centre**

G5, 356/20, Esteem Plaza  
(Next to Coffeeday)  
4th Main Road  
Sadashivanagar  
Bangalore 560080

Phone: 080-2361 0036

### Eating Places

Nearer to Tranquil Orchids and around Bhashyam Circle, there are couple of Eating Places, viz.,

**Shanthi Sagar**

**Mast Kalandar**

**Mint Masala.**



## Speakers and Committee members

1. Y. Benoist
2. G. Besson
3. M. Bestvina
4. E. Breuillard
5. M. Bridson
6. M. Burger
7. K. Burns
8. F. T. Farrell
9. E. Ghys
10. U. Hamenstädt
11. T. Januskiewicz
12. F. Labourie
13. S. Mozes
14. N. Shah
15. J. Athreya
16. I. Belegradek
17. M. Bourdon
18. I. Chatterji
19. C. Connell
20. D. Constantine
21. P. Dani
22. A. Gorodnik
23. J. Heber
24. G. Knieper
25. J.-F. Lafont
26. E. Leuzinger

27. P. Linnell
28. D. Long
29. Mahan, Mj
30. I. Mineyev
31. F. Paulin
32. V. Schroeder
33. U. Shapira
34. A. Thomas
35. S. G. Dani
36. P. B. Eberlein
37. R. S. Kulkarni
38. M. Davis
39. P. Ontaneda
40. C. S. Aravinda
41. Joseph Samuel

## List of Registered Participants

### From Abroad

1. Suarez-Serrato, Pablo
2. Kim, Chang-Wan
3. Yaman, Asli
4. Le Donne, Enrico
5. Ortiz, Ivonne
6. Amchislavska, Margarita
7. Iozzi, Alessandra
8. Shankar, Krishnan
9. Wang, Kun
10. Phan, Tam Nguyen
11. Lytle, Beverly
12. Louwsma, Joel
13. Lassonde, Robin
14. Nicol, Andy
15. Gupta, Subhojoy
16. Francaviglia, Stefano
17. Sorcar, Gangotryi
18. Majumdar, Tapopriya
19. Basak, Tathagata
20. Mitra, Atish

### From India (Outside Bangalore)

1. Aithal, Vikram
2. Bhunia, Sushil
3. Biswas, Kingshook
4. Basu, Bodhisattwa
5. Das, Shubhabrata
6. Das, Bandana
7. De, Dibyendu
8. Debnath, Dipankar
9. Gupta, Punam
10. Kumar, Pradip
11. Mishra, Ashish
12. Mj, Mahan
13. Moosath, Subrahmanian
14. Mubeena, T
15. Paul, Pampa
16. Raveendran, Binoy
17. Sardar, Pranab
18. Sarkar, Himadrisekhar
19. Sankaran, P
20. Shridharan, Shrihari
21. Singh, Sandip
22. Upadhyay, Abhitosh
23. Vemuri, M K
24. Venkatesh, T
25. Yadav, Raj Bhawan

## From Bangalore

1. Adimurthi
2. Bhattacharya, Atreyee
3. Chaudhury, Shion Samadder
4. Choudhury, Anupam Pal
5. Choudhury, Manoj
6. Divakaran, D
7. Ghoshal, Shyam
8. Kulkarni, Dheeraj
9. Kumar, Bharath
10. Maity, Soma
11. Manna, Bhakti Bhushan
12. Muniraja, G
13. Nagaraja, H G
14. Patil, Veerendra
15. Paul, Subhajit
16. Raju, Ramana
17. Sandeep K
18. Serkar, Aswin
19. Seshadri, Harish
20. Shah, Hemangi
21. Somashekhara, G
22. Surendran K
23. Lebow, Eli

*ICM Satellite Conference on*  
**Geometry, Topology and Dynamics**  
**in Negative Curvature**

*Venue: Raman Research Institute, 2–7 August, 2010.*

Titles and Abstracts

**Monday, 2nd August, 2010**

10:30 - 11:30 Plenary lecture 1

**Martin Bridson**

**Title:** Rigidity for  $\text{Out}(F)$ , and actions of higher-rank lattices on free groups

**Abstract:** Following a discussion of rigidity for mapping class groups and automorphism groups of free groups, I shall outline the proof of a recent result with Ric Wade: every homomorphism from a higher-rank lattice to the outer automorphism group of a free group has finite image.

12:00 - 13:00 Plenary lecture 2

**Emmanuel Breuillard**

**Title:** Approximate groups

**Abstract:** I will describe a recent joint work with Ben Green and Terence Tao in which we study large finite subsets of an ambient group that are almost closed under multiplication, i.e. the so-called approximate groups. I will first survey the basic definitions and properties regarding approximate groups in a general context. Then, bringing tools from combinatorics and making key use of the geometry of simple algebraic groups I will give a classification of their approximate subgroups. These results bring a new twist to the standard results on the growth of groups in geometric group theory by taking into account the size of the generating set. I will also describe applications of these results to showing that random Cayley graphs of finite simple groups of Lie type are expanders graphs (joint also with Bob Guralnick).

14:30 - 15:30 Parallel session 1

**Pallavi Dani**

**Title:** Filling invariants at infinity

**Abstract:** The  $k$ -dimensional Dehn function of a group captures the difficulty of filling  $k$ -spheres with  $(k + 1)$ -balls in a suitable space associated with the group. On the other hand, divergence is an invariant that measures the spread of geodesics in such a space. These two ideas are united by “higher divergence

functions”, which measure rates of filling spheres by balls “at infinity”, i.e., far from a basepoint. It turns out that these filling rates can detect some geometric properties of the space.

After giving the basic definitions and motivation, I will describe recent joint work with A. Abrams, N. Brady, M. Duchin, and R. Young on higher divergence in the class of right-angled Artin groups.

14:30 - 15:30 Parallel session 1

**Anne Thomas**

**Title:** Lattices in complete Kac-Moody groups

**Abstract:** A complete Kac-Moody group over a finite field is a totally disconnected, locally compact group, which may be thought of as an “infinite-dimensional Lie group”. An example is  $G = SL(n, K)$  with  $K$  the field of formal Laurent series over a finite field. We study uniform and nonuniform lattices in such  $G$  of rank 2, where the associated Bruhat-Tits building is a tree. We use finite group theory and the dynamics of the group action on the tree and its boundary. This is joint work with Inna (Korchagina) Capdeboscq

16:00 - 17:00 Parallel session 2

**Marc Bourdon**

**Title:** Quasiconformal geometry and Coxeter groups (joint work with Bruce Kleiner)

**Abstract:** Every hyperbolic group has a canonical action on its boundary at infinity; with respect to any visual metric, this action is by uniformly quasi-Moebius homeomorphisms. This structure has a central role in the proofs of Mostow’s rigidity theorem and numerous other results in the same vein, which are based on the analytic theory of quasiconformal homeomorphisms of the boundary. With the aim of extending these rigidity results to a larger class of hyperbolic groups, we study a quasi-Moebius invariant property of the boundary, called the Combinatorial Loewner Property.

16:00 - 17:00 Parallel session 2

**Indira Chatterji**

**Title:** Median spaces and property (T)

**Abstract:** We will explain the notion of median spaces as well as the notion of property (T), and show that a group has property (T) if and only if any isometric action on a median space has a bounded orbit. This is joint work with Drutu and Haglund.

## Tuesday, 3rd August, 2010

09:00 - 10:00 Plenary lecture 3

**Etienne Ghys**

**Title:** On cutting cloth, according to Chebyshev

**Abstract:** On August 28th, 1878, Chebyshev gave a talk with the same title in Paris (seventh meeting of the Association for the Progress of Science). Given a shape, like an elbow for example, how should we cut a piece of cloth to cover it, avoiding folds... Chebyshev gave several concrete examples. I would like to revisit this kind of questions and I’ll discuss in particular a good way to cloth a sphere or a large domain in the Poincaré disc.

10:30 - 11:30 Plenary lecture 4

**Marc Burger**

**Title:** Higher Teichmueller Spaces: from  $SL(2, R)$  to other Lie Groups

**Abstract:** In this talk we present various viewpoints on classical Teichmueller theory and show how they lead to different ways of studying the space of representations of the fundamental group of a surface into a Lie group. This will lead to the notion of positive representation in the case of a real split simple Lie group, (work of Hitchin, Fock-Goncharov, Labourie, Guichard, Wienhard), to maximal, and more generally, causal representations, in the case where the group is of hermitian type. We will particularly insist on causal representations, and present some recent works concerning their geometric significance (work with Ben Simon, Hartnick, Iozzi, Wienhard)

12:00 - 13:00 Plenary lecture 5

**Tom Farrell**

**Title:** Space of negatively curved metrics; bundles with negatively curved fibers

**Abstract:** This is a report on joint work with Pedro Ontaneda. Let  $R, G$  and  $T$  denote the spaces of all negatively curved Riemannian metrics, geometries and marked geometries (respectively) on an  $n$ -dimensional closed smooth manifold  $M$ ;  $G$  and  $T$  are quotient spaces of  $R$  where isometric and marked isometric metrics (respectively) are identified. We focus attention on the case where  $n$  is large instead of the classical setting  $n = 2$ . And obtain results on the homotopy and homology of  $R, G$  and  $T$ ; e.g.  $R$  has infinitely many components when  $n > 9$ . And if  $M$  supports a real hyperbolic metric (and  $n > 9$ ) then  $G$  is also disconnected for sufficiently large finite sheeted covers of  $M$ . These results relate to studying bundles equipped with negatively curved fibers.

14:30 - 15:30 Parallel session 3

**Uri Shapira**

**Title:** Dynamics and continued fractions.

**Abstract:** We will present some recent results regarding the continued fraction expansion of certain sequences of numbers. In particular, we will focus on the following result (joint with Menny Aka): Let  $x$  be a quadratic irrational and  $p$  a prime. Then the statistics of the period of the continued fraction expansion of  $p^n x$  converges to the "right" statistics; i.e. to the one given by the Gauss measure.

14:30 - 15:30 Parallel session 3

**Mahan Mj**

**Title:** On Discreteness of Commensurators

**Abstract:** We begin by showing that commensurators of Zariski dense subgroups of isometry groups of symmetric spaces of non-compact type are discrete provided that the limit set on the Furstenberg boundary is not invariant under the action of a (virtual) simple factor. In particular for rank one or simple Lie groups, Zariski dense subgroups with non-empty domain of discontinuity have discrete commensurators.

This generalizes a Theorem of Greenberg for Kleinian groups. We then prove that for all finitely generated, Zariski dense, infinite covolume discrete subgroups of  $\text{Isom}(\mathbf{H}^3)$ , commensurators are discrete. Together these prove discreteness of commensurators for all known examples of finitely generated, Zariski dense, infinite covolume discrete subgroups of  $\text{Isom}(X)$  for  $X$  an irreducible symmetric space of non-compact type.



16:00 - 17:00 Parallel session 4

**Jayadev Athreya**

**Title:** Cusp Excursions on Parameter Spaces

**Abstract:** We describe an axiomatic approach to studying statistical behavior of cusp excursions for diagonal and unipotent flows (arising from an ambient Lie group action) on parameter spaces. Our approach applies in particular to the space of unimodular lattices and the space of quadratic differentials. Some of the results described are joint work with Prof. G. Margulis.

16:00 - 17:00 Parallel session 4

**Jens Heber**

**Title:** Cocompact isometry groups in nonpositive curvature

## Wednesday, 4th August, 2010

09:00 - 10:00 Plenary lecture 6

**Mladen Bestvina**

**Title:** Groups acting on quasi-trees

**Abstract:** If  $G$  is the fundamental group of a closed non-positively curved rank 1 manifold, then  $G$  admits many actions on quasi-trees (spaces quasi-isometric to trees). In fact, groups like mapping class groups and  $Out(F_n)$ , which are not non-positively curved but exhibit rank 1 behavior, also admit actions on quasi-trees. I will present a construction of these actions (joint work with Bromberg and Fujiwara). If time permits, I will describe an application, that mapping class groups have finite asymptotic dimension.

10:30 - 11:30 Plenary lecture 7

**Yves Benoist**

**Title:** Invariant subsets of finite volume homogeneous spaces

**Abstract:** Let  $X$  be a finite volume quotient of a connected semisimple Lie group  $G$  with no compact factor and  $H$  be a Zariski dense subgroup of  $G$ . We prove that every  $H$ -orbit closure is an orbit under a larger group. For that we classify the probability measures on  $X$  which are stationary under a probability measure on  $G$  whose support is compact and spans  $H$ : the ergodic ones are homogeneous under a larger group. This is joint work with Jean-Francois Quint.

12:00 - 13:00 Parallel session 5

**Gerhard Knieper**

**Title:** New results on harmonic manifolds

**Abstract:** The Lichnerowicz conjecture asserts that all harmonic manifolds are either flat or locally symmetric spaces of rank 1. This conjecture has been proved by Z. Szabó for harmonic manifolds with compact universal cover. Furthermore, the conjecture was obtained by Besson, Courtois and Gallot for compact manifolds of strictly negative curvature as an application of their entropy rigidity theorem in combination with the rigidity theorems by Benoist, Foulon and Labourie on stable and unstable foliations.

On the other hand, E. Damek and F. Ricci provided examples showing that in the noncompact case the conjecture is wrong. However, such manifolds do not admit a compact quotient.

In this talk we will show that for all simply connected, noncompact and

nonflat harmonic spaces  $X$  the following properties are equivalent:

- $X$  has rank 1
- $X$  has purely exponential volume growth
- $X$  is Gromov hyperbolic
- The geodesic flow on  $X$  is Anosov with respect to the Sasaki metric

Furthermore we obtain, that no focal points imply the above properties. Combining those results with the above mentioned rigidity theorems shows that the Lichnerowicz conjecture is true for all compact harmonic manifolds without focal points or with Gromov hyperbolic fundamental groups. There is some evidence to believe that all non compact harmonic manifolds have no focal points.

12:00 - 13:00 Parallel session 5

**Igor Mineyev**

**Title:** Systems of complexes and the Hanna Neumann Conjecture.

**Abstract:** The Hanna Neumann Conjecture is a question about ranks of subgroups in a free group  $\Gamma$ ; it has been open for more than 50 years. In order to generalize the statement of the Strengthened Hanna Neumann Conjecture (SHNC) we use cell complexes and the Murray-von Neumann dimension of Hilbert modules. We define systems of cell complexes which are certain multiple pull-back diagrams and observe that SHNC can be restated in terms of  $\ell^2$ -Betti numbers for such systems consisting of graphs.

The next interesting case is systems consisting of hyperbolic surfaces. We state an analog of SHNC for this situation; it is a (conjectured) inequality in terms of the first  $\ell^2$ -Betti numbers of subgroups of a surface group. This conjecture for surfaces implies the original SHNC. This surface case is of particular interest because it gives still another, geometric, restatement on SHNC: in terms of the areas of surfaces.

We provide several approaches to proving SHNC and its generalizations. They use Hilbert modules and Linnell's result that free groups satisfy the Atiyah conjecture.

Some questions will be posed. For example, we would like to know whether the geometry of surfaces can be directly used to prove the conjecture. Another question that might be appropriate for a conference with "dynamics" in its title: Can one obtain the inequality in SHNC using  $\Gamma$ -actions on probability spaces and Gaboriau's definition of  $\ell^2$ -Betti numbers for equivalence relations?

14:30 - 15:30 Parallel session 6

**Enrico Leuzinger**

**Title:** The asymptotic Schottky problem

**Abstract:** Let  $M_g$  denote the moduli space of compact Riemann surfaces of genus  $g$  and let  $A_g$  be the moduli space of principally polarized abelian varieties of dimension  $g$ . The map  $J : M_g \rightarrow A_g$  which associates to a Riemann surface its Jacobian is injective and the image  $J_g := J(M_g)$  is contained in a proper subvariety of  $A_g$  when  $g \geq 4$ . The classical and longstudied Schottky problem is to characterize the Jacobian locus  $J_g$  in  $A_g$ . In the talk we address a large scale version of this problem posed by B. Farb: What does  $J_g$  look like "from far away", or how dense is  $J_g$  in the sense of coarse geometry?

14:30 - 15:30 Parallel session 6

**Igor Belegradek**

**Title:** Moduli spaces of metrics of nonnegative curvature

**Abstract:** There are analogies between open complete simply-connected manifolds of nonnegative and nonpositive curvature: in either case the structure of

flats and the ideal boundary plays a prominent role, and methods of comparison geometry are fruitful. In the talk I will survey what is known on moduli spaces of metrics of nonnegative curvature on open manifolds, and relate it to cancellation phenomena in topology.

16:00 - 17:00 PUBLIC LECTURE

**Speaker: Patrick Eberlein**

**Title: Ergodic behavior in Negative curvature**

## Thursday, 5th August, 2010

09:00 - 10:00 Plenary lecture 8

**Francois Labourie**

**Title:** An algebra of observables for cross ratios

**Abstract:** We define a Poisson Algebra called the swapping algebra using the intersection of curves in the disk. We interpret a subalgebra of the fraction swapping algebra – called the algebra of multifractions – as an algebra of functions on the space of cross ratios and thus as an algebra of functions on the Hitchin component as well as on the space of  $SL(n; R)$ -opers with trivial holonomy. We finally relate our Poisson structure to the Drinfel'd-Sokolov structure and to the Atiyah-Bott-Goldman symplectic structure for classical Teichmüller spaces and Hitchin components

10:30 - 11:30 Plenary lecture 9

**Shahar Mozes**

**Title:** Stationary measures, stiffness and equidistribution on the torus

**Abstract:** In a joint work with Jean Bourgain, Alex Furman and Elon Lindenstrauss we study stationary measures and equidistribution on the  $d$ -dimensional torus. Let  $\nu$  be a probability measure supported on a (finite) subset of  $SL_d(\mathbb{Z})$ . We show that if the group generated by the support of  $\nu$  is large enough, in particular if this group is Zariski dense in  $SL_d$ , for any irrational point  $x$  in the torus the probability measures  $\nu^{*n} * \delta_x$  tend to the uniform measure on  $T^d$ . If in addition  $x$  is Diophantine generic, we show this convergence is exponentially fast.

12:00 - 13:00 Plenary lecture 10

**Nimish Shah**

**Title:** Counting points or circles in orbits of geometrically finite hyperbolic groups

**Abstract:** In this joint work with Hee Oh, we extend some of the earlier results about counting points on discrete orbits of lattices, to the case of counting on orbits of geometrically finite hyperbolic Pargroups. We also consider the problem of counting circles in circle packings invariant under Kleinian groups.

14:30 - 15:30 Parallel session 7

**Chris Connell**

**Title:** Rigidity for Maps and Measures on Foliated Spaces

**Abstract:** I will present some entropy and volume rigidity statement for general foliated maps between compact foliated spaces in the sense of Besson, Courtois and Gallot. In particular, we establish an iso-entropic inequality with respect to a transverse (quasi-)invariant measure which is optimized when all leaves are

locally symmetric. We will give some applications of this, and indicate how it relates to the entropy rigidity conjecture for higher rank spaces together with a classification of the harmonic measures. Respective portions of this work are joint with either Zhenyu Li or Matilde Martinez.

14:30 - 15:30 Parallel session 7

**Viktor Schroeder**

**Title:** Boundaries of rank one symmetric spaces

**Abstract:** The ideal boundary of a rank one symmetric space of noncompact type carries a natural Moebius structure. We characterize this boundary in terms of its Moebius geometry.

16:00 - 17:00 Parallel session 8

**Dave Constantine**

**Title:** Rank-rigidity and frame flow in non-positive curvature

**Abstract:** I will discuss how a condition on curvature, higher hyperbolic rank, and study of the dynamics of the frame flow for a non-positively curved, rank one manifold can be combined to prove that a manifold has constant negative curvature. The result holds when the manifold is of odd dimension, or is of even dimension and has sufficiently pinched curvature. I will mention a few other questions related to the hyperbolic rank condition and what sort of information it and frame-flow dynamics can give us about the curvature.

16:00 - 17:00 Parallel session 8

**Frederic Paulin**

**Title:** Equidistribution, counting and arithmetic applications in hyperbolic manifolds

**Abstract:** Let  $M$  be a finite volume hyperbolic manifold. We show the equidistribution in  $M$  of the equidistant hypersurfaces to a finite volume totally geodesic submanifold  $C$ . We prove a precise asymptotic on the number of geodesic arcs of lengths at most  $t$ , that are perpendicular to  $C$  and to the boundary of a cuspidal neighbourhood of  $M$ . We deduce from it counting results for quadratic irrationals over  $\mathbb{Q}$  or over imaginary quadratic extensions of  $\mathbb{Q}$ , in given orbits of congruence subgroups of the modular groups, as well as counting results for the number of representations of integers by integral indefinite binary Hermitian forms. This is joint work with Jouni Parkkonen.

## Friday, 6th August, 2010

09:00 - 10:00 Plenary lecture 11

**Keith Burns**

**Title:** Ergodicity of the Weil-Petersson geodesic flow

**Abstract:** I will talk about recent joint work with Howie Masur and Amie Wilkinson. We have shown that the geodesic flow for the Weil-Petersson metric on the moduli space of a Riemann surface is ergodic.

10:30 - 11:30 Parallel session 9

**Alex Gorodnik**

**Title:** Diophantine approximation and automorphic spectrum

**Abstract:** We discuss the problem of Diophantine approximation on algebraic

varieties, which was considered by Waldschmidt in the setting of abelian varieties. We investigate this problem for varieties equipped with actions of semisimple groups. Using techniques from the theory of automorphic representations, we establish estimates on the exponents of Diophantine approximation that are optimal in a number of cases. It turns out that the quality of the exponents is very closely related to the Ramanujan conjecture and its generalisations.

14:30 - 15:30 Parallel session 9

**Jean-Francois Lafont**

**Title:** 4-dimensional locally CAT(0)-manifold with no Riemannian smoothing

**Abstract:** I will describe the construction of smooth 4-dimensional manifolds that support locally CAT(0) metrics, but which cannot support any Riemannian metrics of non-positive sectional curvature. This is joint work with Mike Davis and Tadeusz Januszkiewicz.

12:00 - 13:00 Parallel session 10

**Peter Linnell**

**Title:** Approximating Betti numbers over arbitrary fields

**Abstract:** Back in 1994, Lueck proved some beautiful theorems for approximating  $L^2$ -Betti numbers in the case the coefficient field is the rational numbers. This has since been extended to the case where the coefficient field is the algebraic numbers. In this talk, extensions of this result to arbitrary fields, or even arbitrary skew fields, will be discussed. Among the classes of groups considered will be amenable groups and pro- $p$  groups. Applications to ultraproducts and the Atiyah conjecture over  $\mathbb{C}$  will also be discussed.

This is joint work with Wolfgang Lueck, Roman Sauer and Thomas Schick.

12:00 - 13:00 Parallel session 10

**Darren Long**

**Title:** Small subgroups of  $SL(3, \mathbb{Z})$

**Abstract:** The finitely generated infinite index subgroups of  $SL(3, \mathbb{Z})$  are somewhat mysterious. We exhibit some interesting examples and nonexamples, including infinite families of Zariski dense surface groups.

14:30 - 15:30 *OPEN PROBLEMS SESSION* Chaired by:

**S. G. Dani, Mike Davis, Pedro Ontaneda**

**Saturday, 7th August, 2010**

09:00 - 10:00 Plenary lecture 12

**Gerard Besson**

**Title:** Collapsing irreducible 3-manifolds with nontrivial fundamental group

**Abstract:** We shall describe the main ideas of an alternative approach for the last step in Perelman's proof of Thurston's Geometrization Conjecture. This is a joint work with L. Bessieres, M. Boileau, S. Maillot and J. Porti. Using two covering arguments we reduce the problem to Thurston's proof of his conjecture for Haken manifolds. One of the arguments uses Gromov's simplicial volume.

10:30 - 11:30 Plenary lecture 13

**Tadeusz Januskiewicz**

**Title:** Complex links in Kähler polyhedra

**Abstract:** Recently Dmitri Panov introduced and studied the concept of Kähler polyhedra. I will describe this and discuss its relation to nonpositive curvature. Briefly: Kähler polyhedron has both real links, which are piecewise spherical and complex links which are piecewise complex projective.

One can express CAT0 property of a Kähler polyhedron both in terms of real links (CAT1) and complex links (perhaps somewhat surprisingly CAT4). This gives many interesting examples, already in dimension 2, as described by Panov, and many promising higher dimensional possibilities.

12:00 - 12:30 Valedictory address by **Ravi Kulkarni**