

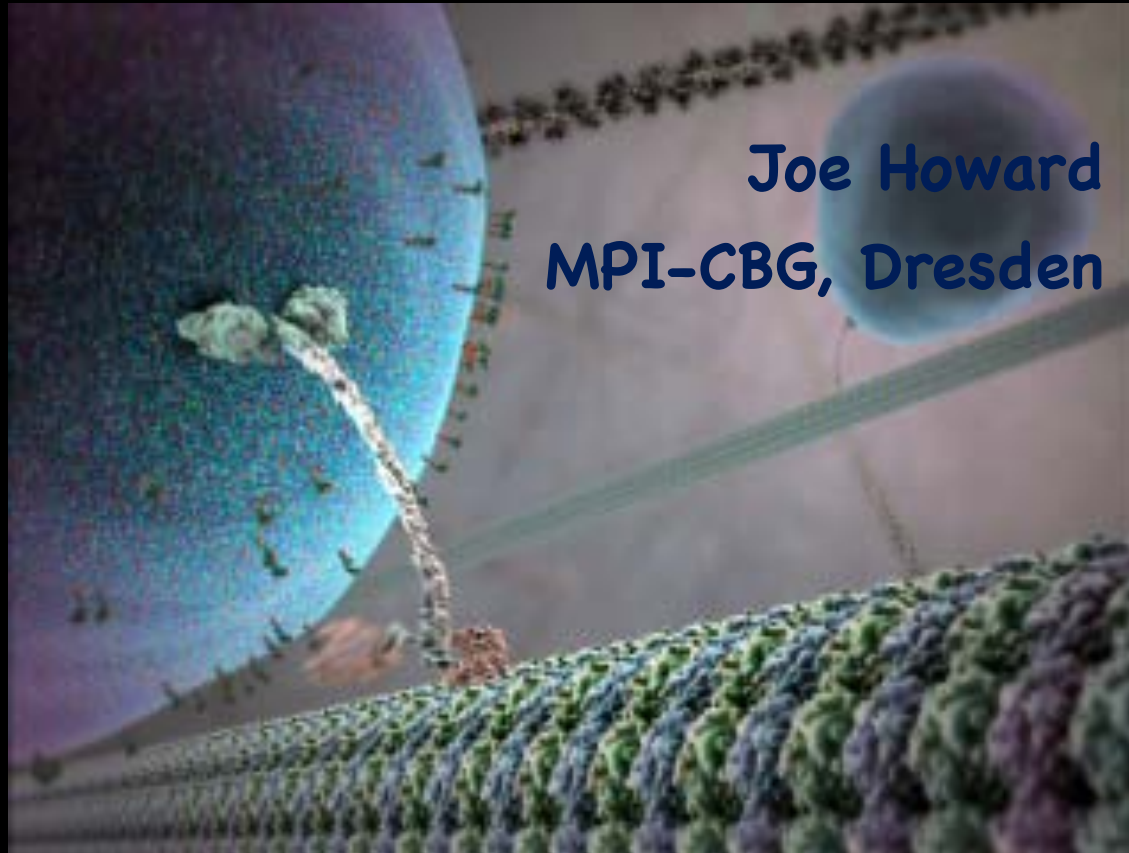


# CBG

Max Planck Institute  
of Molecular Cell Biology  
and Genetics

ICTS-NESP  
Kanpur  
2 February 2010

## Motor Proteins as Nanomachines: Force, Friction and Fluctuations



Joe Howard  
MPI-CBG, Dresden

The inner life  
of the cell  
(Harvard Univ.)

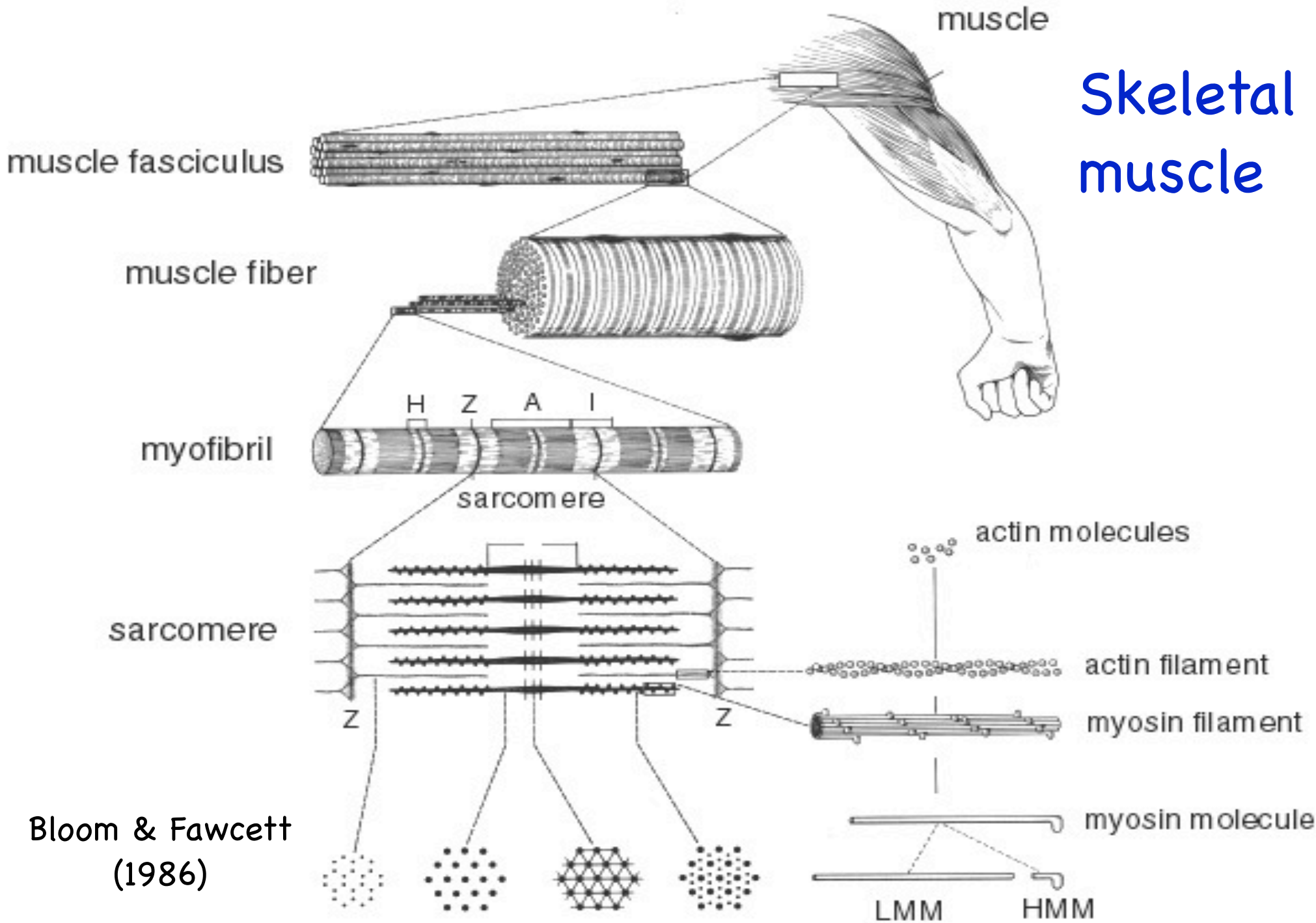


MAX-PLANCK-GESELLSCHAFT

# Outline

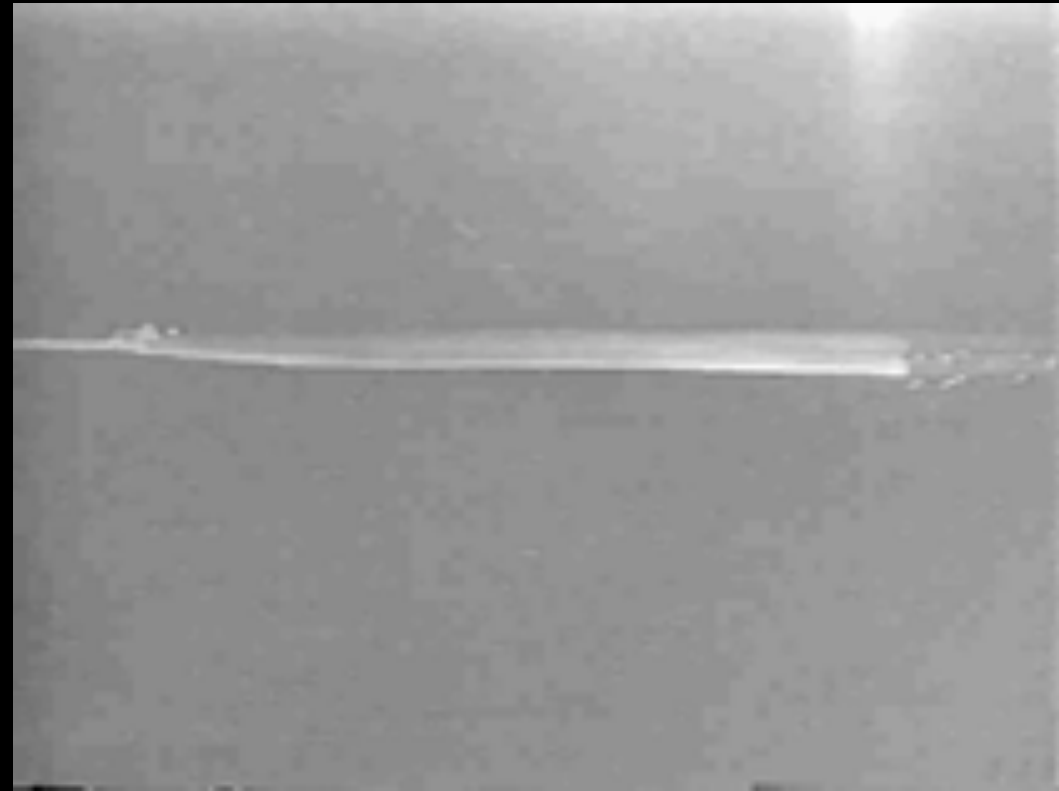
1. **Single-molecule techniques** can be used to study movement of purified motor proteins
2. Role of **fluctuations** in the motor reaction
3. **Protein friction** limits motor speed and efficiency
4. **Force gating of motor proteins:** active mechanical circuits underlying cell motility

# Skeletal muscle

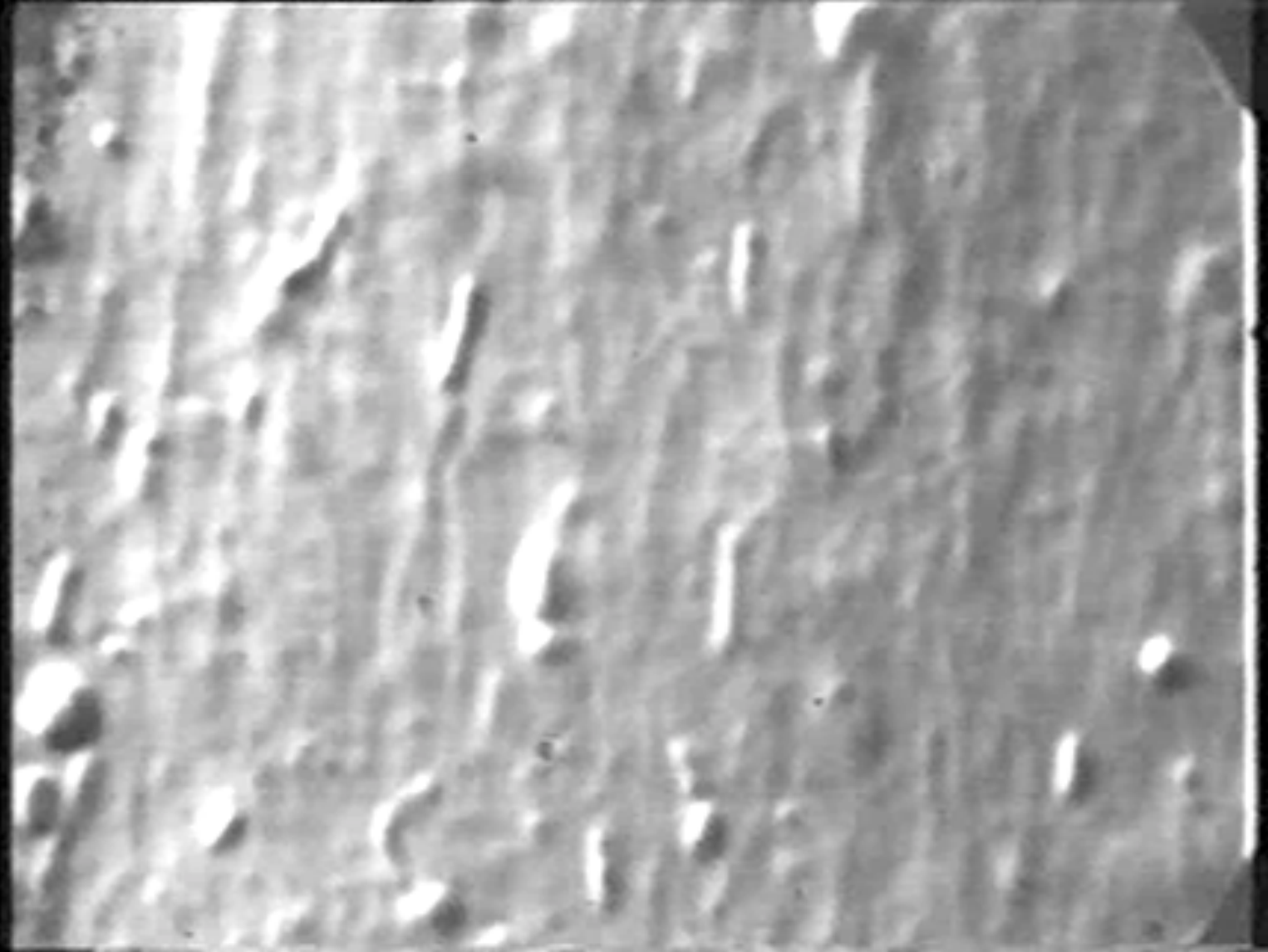


Bloom & Fawcett  
(1986)

# Squid giant axon



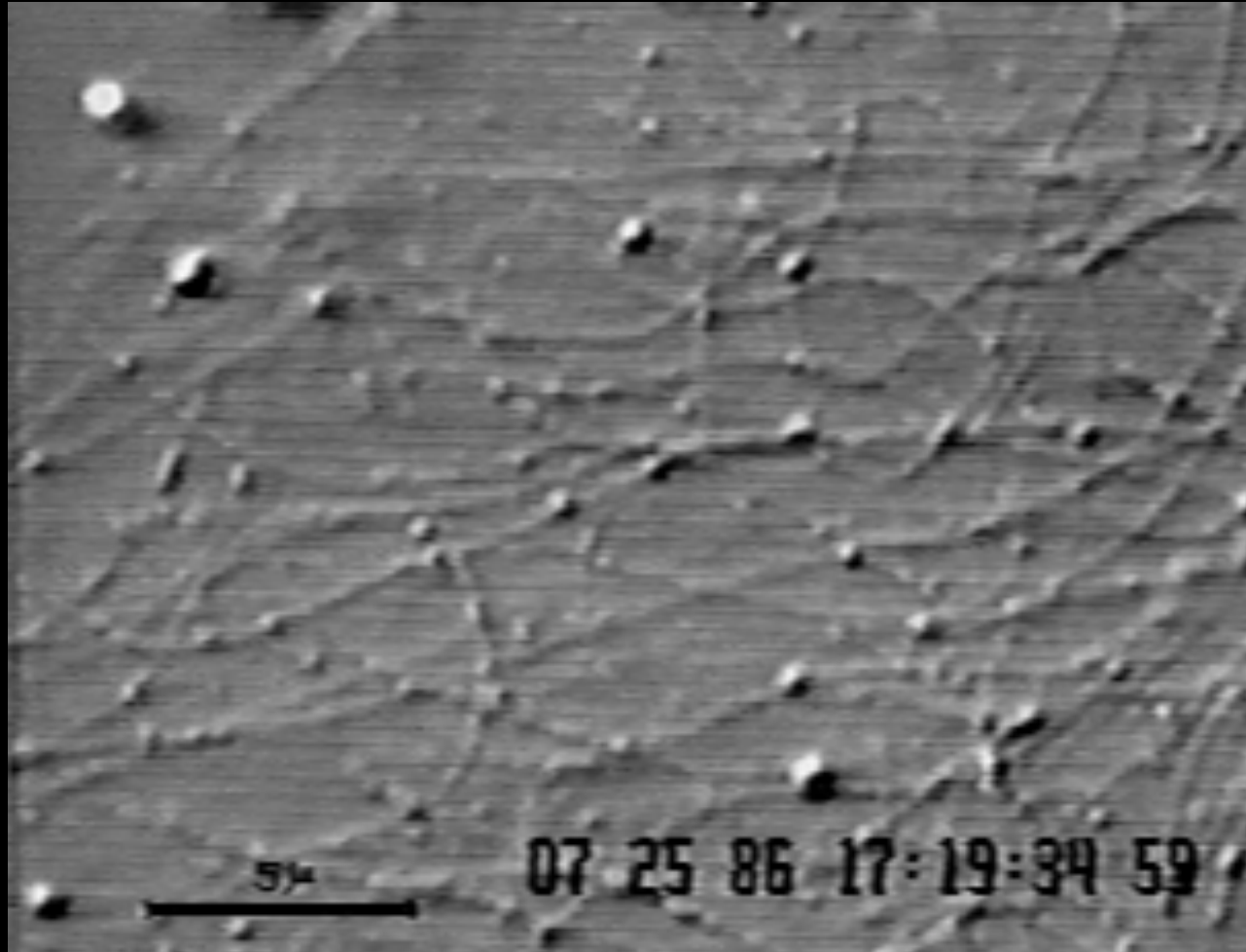
# Organelle transport in squid axoplasm



10  $\mu\text{m}$

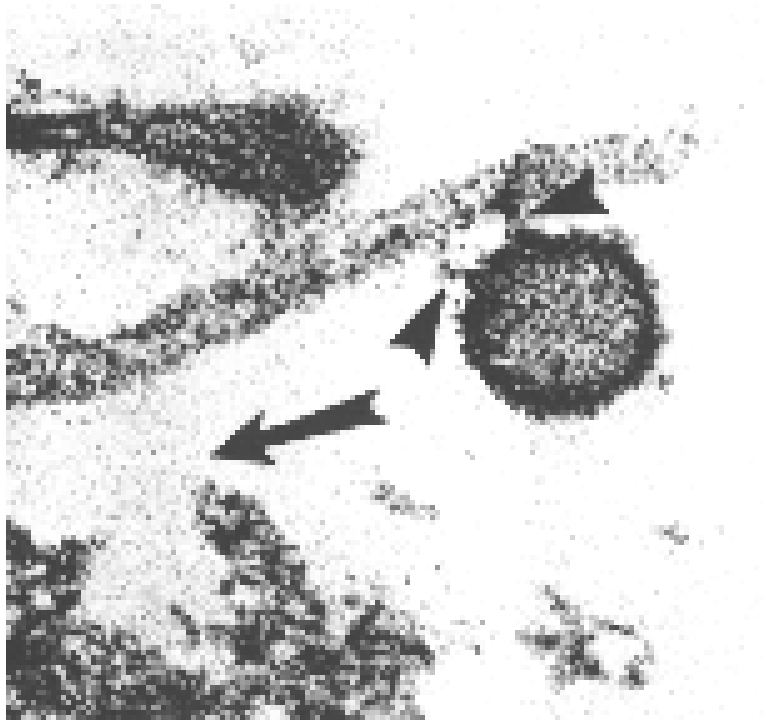
Robert Allen, Woods Hole

# Organelle transport in squid axoplasm



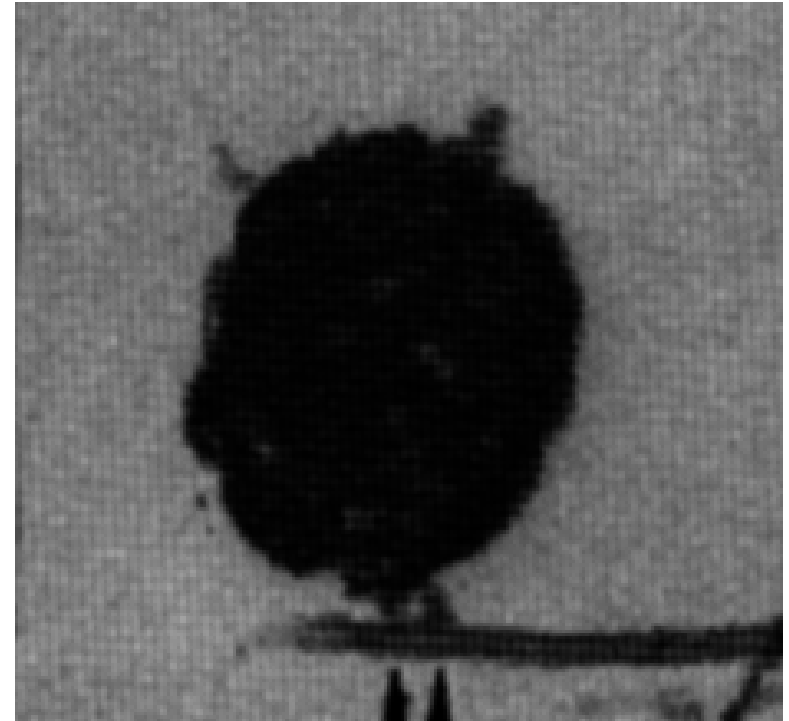
Dieter Weiss, Rostock

# Crossbridges between microtubules and organelles



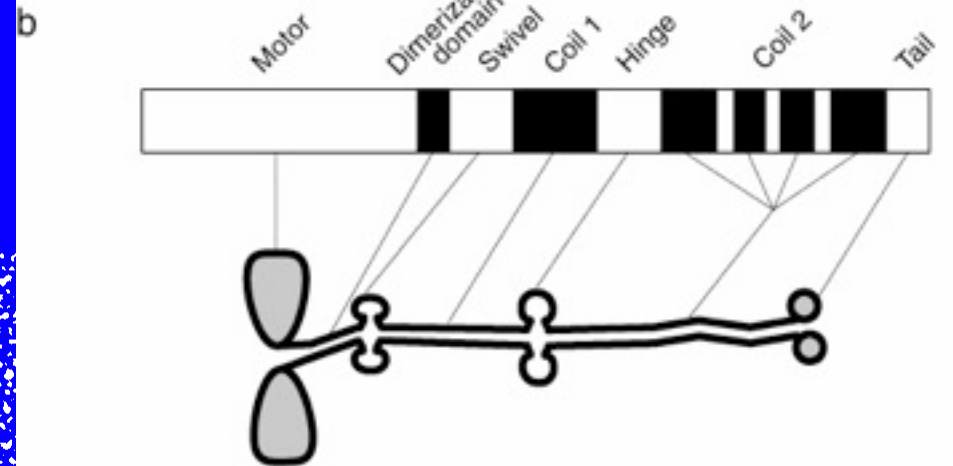
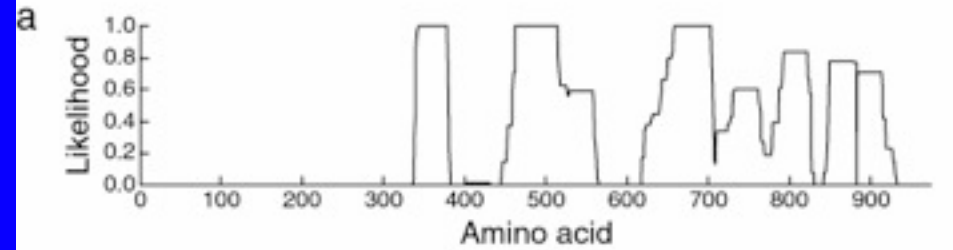
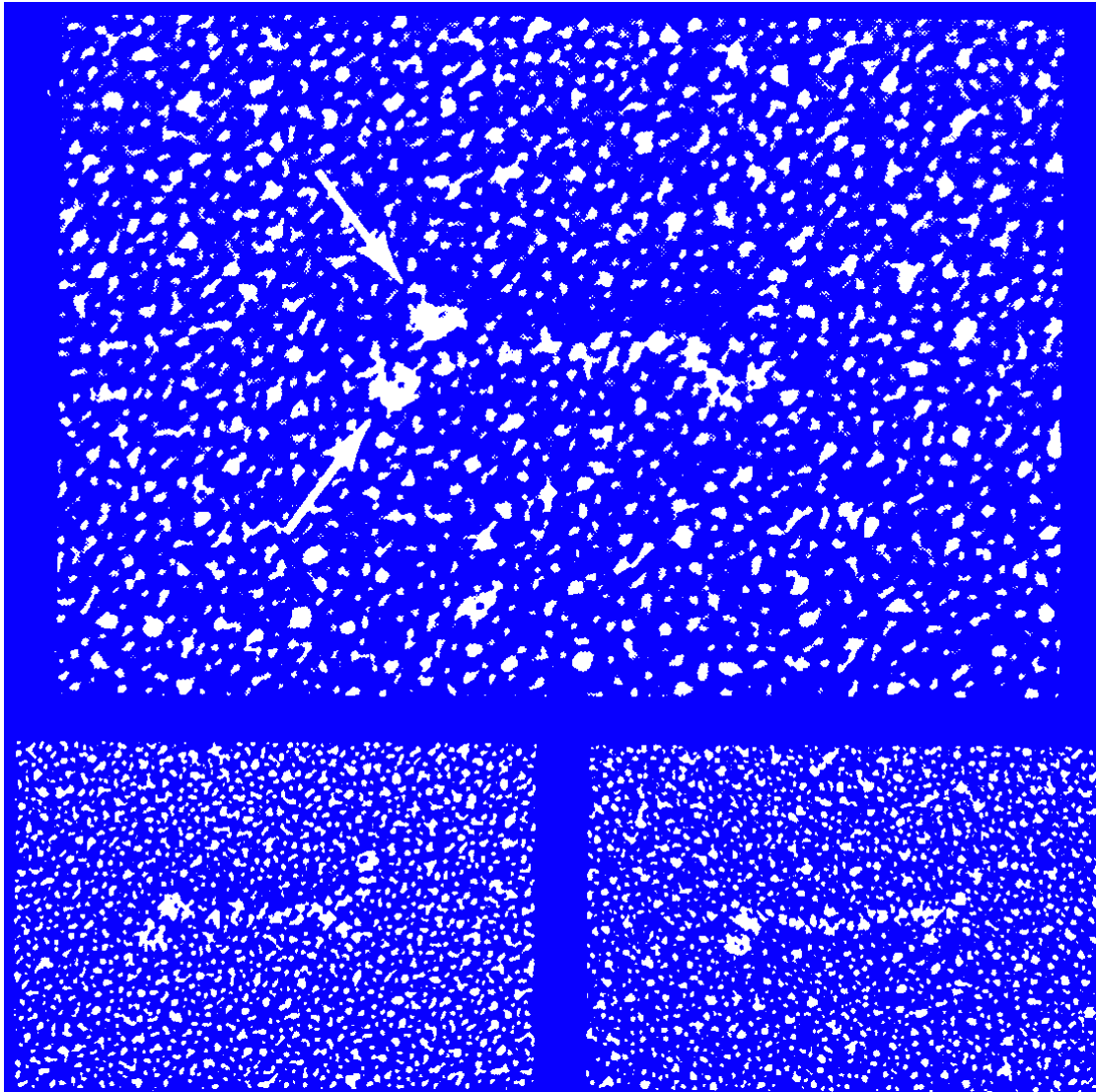
100 nm

Miller & Lasek, J. Cell Biol.  
101: 2181 (1985)



Ashkin et al., Nature 348:  
346 (1990)

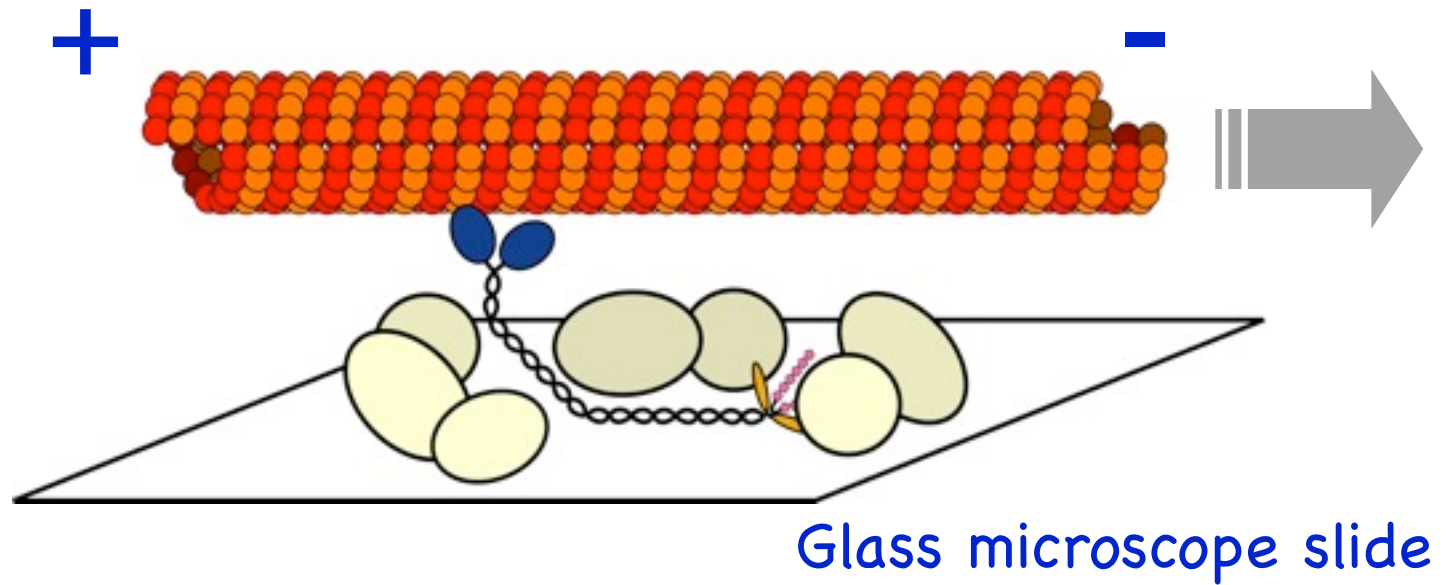
# Kinesin



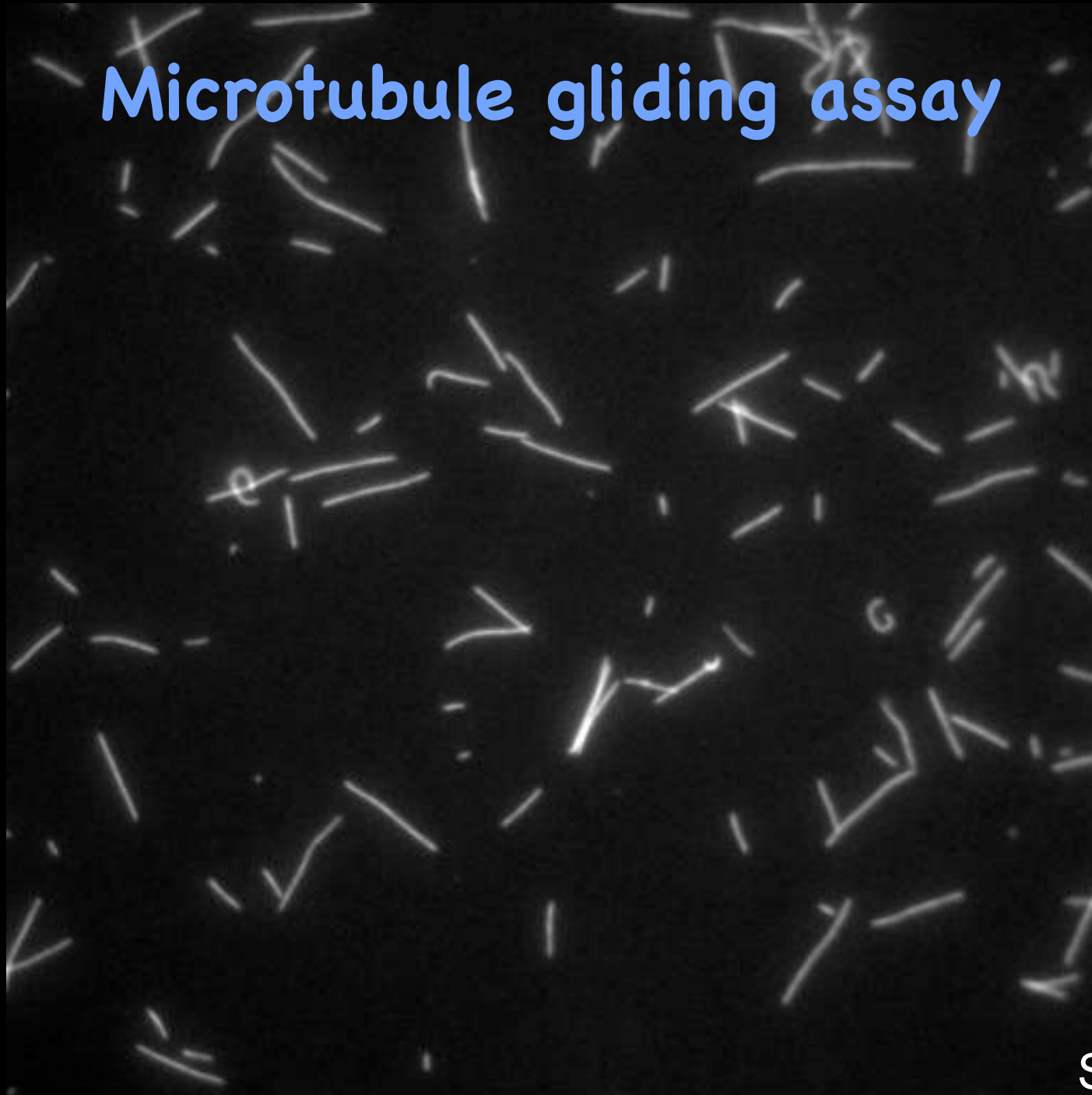
Hirokawa et al., Nature 348: 346 (1990)



# In vitro gliding assay (upside down assay)



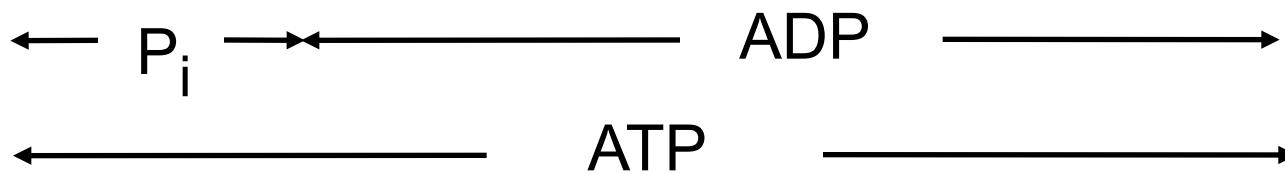
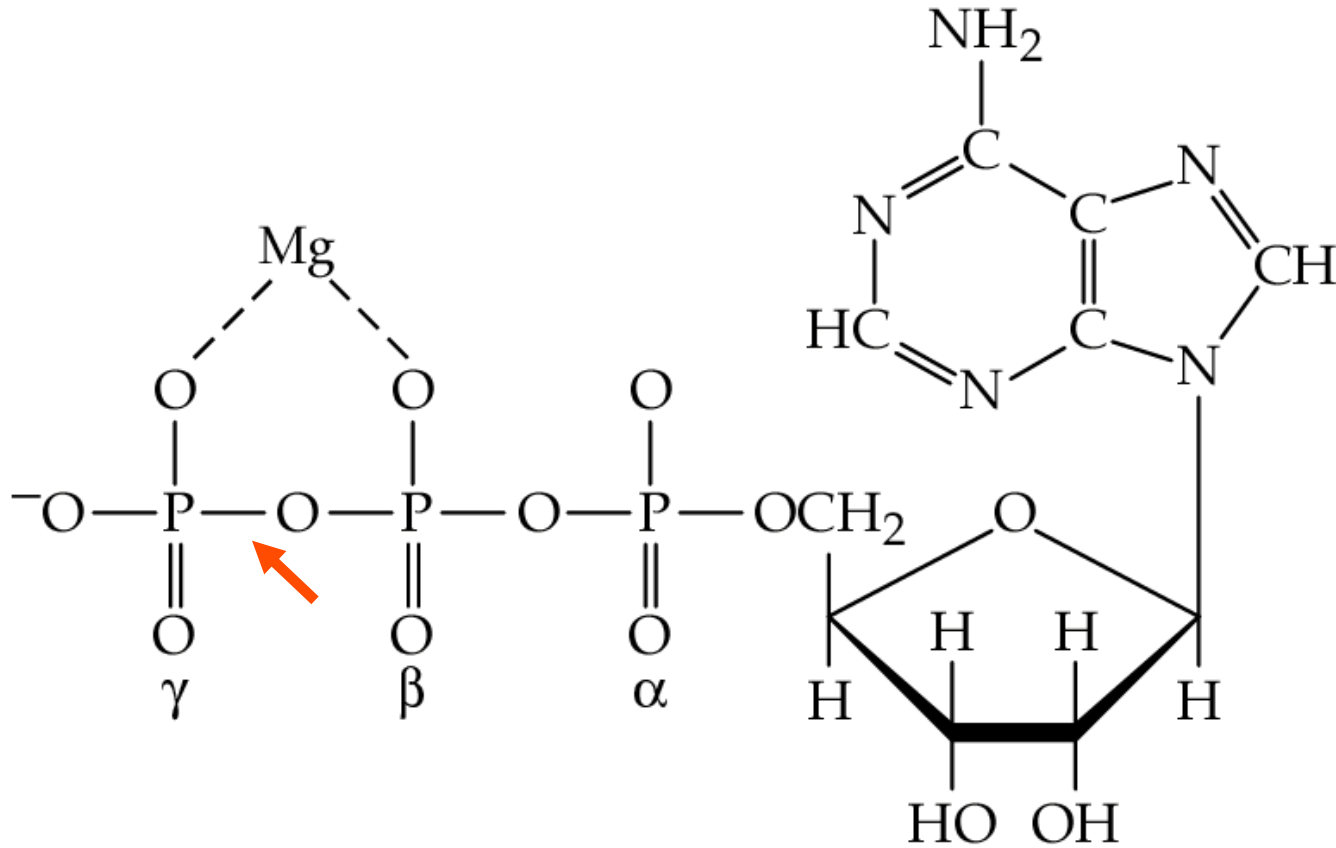
# Microtubule gliding assay



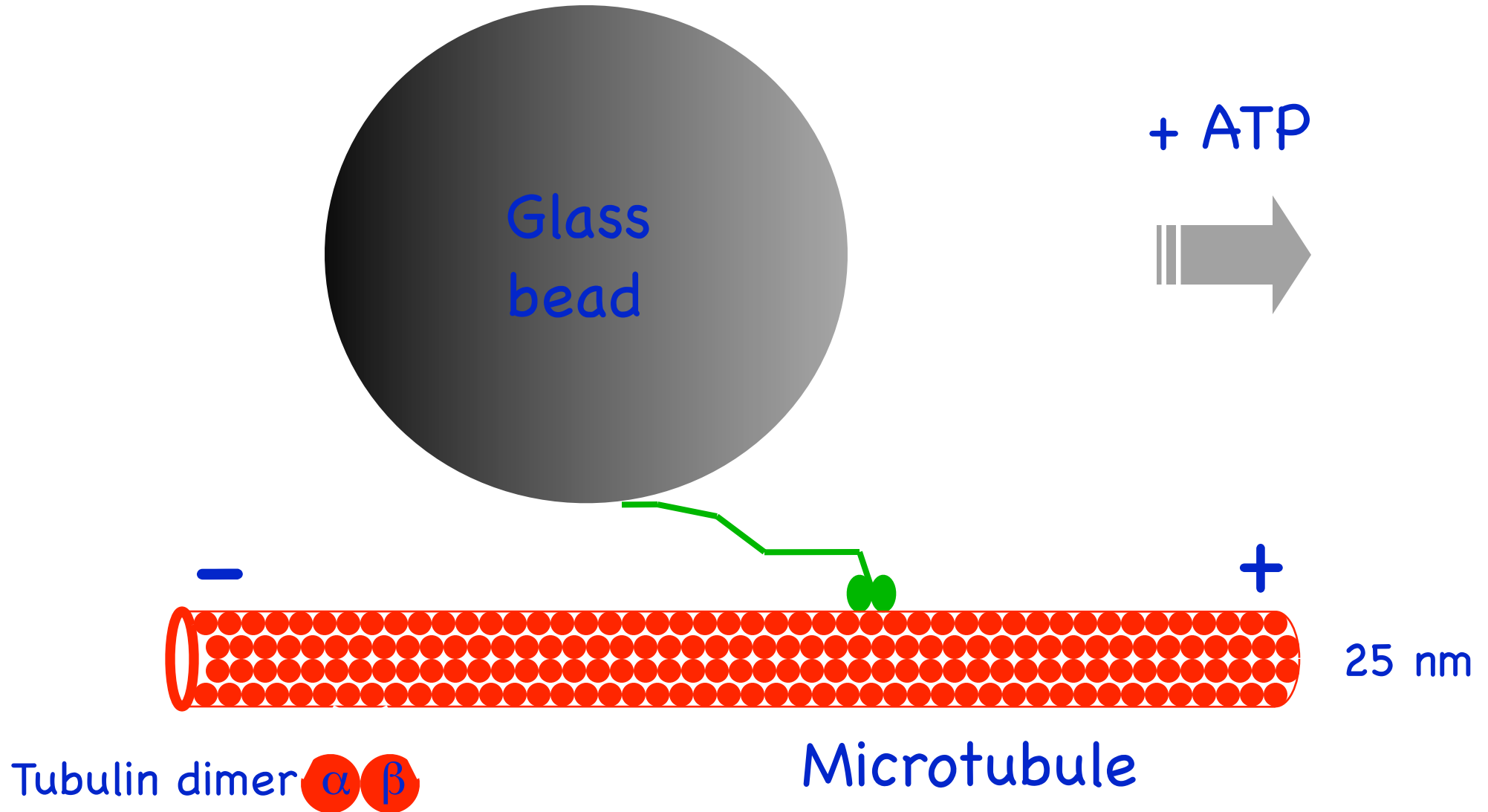
10  $\mu\text{m}$

Sped up 25X

# ATP is required for motility

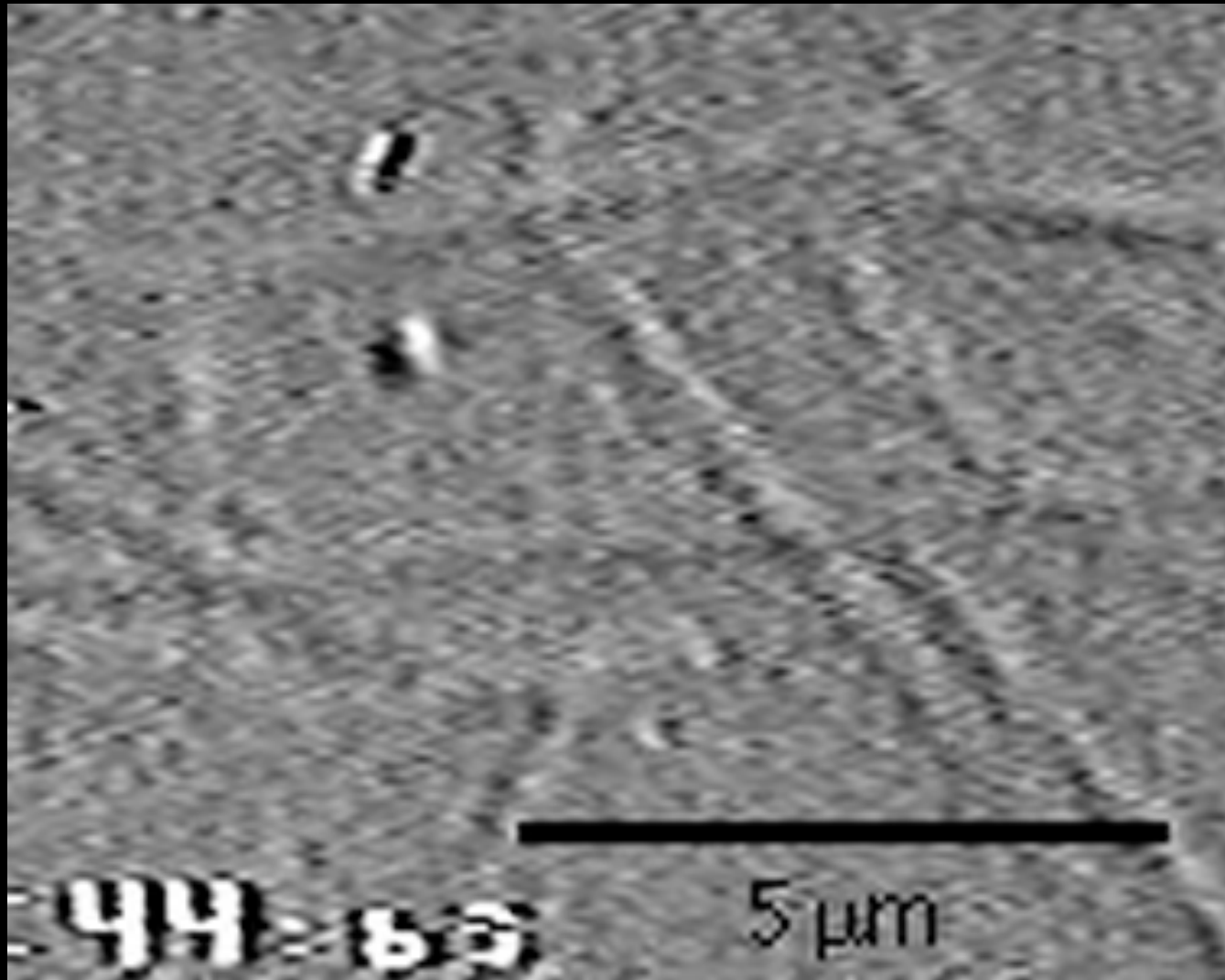


# Bead Assay



Coy et al. J. Biol. Chem., 1999

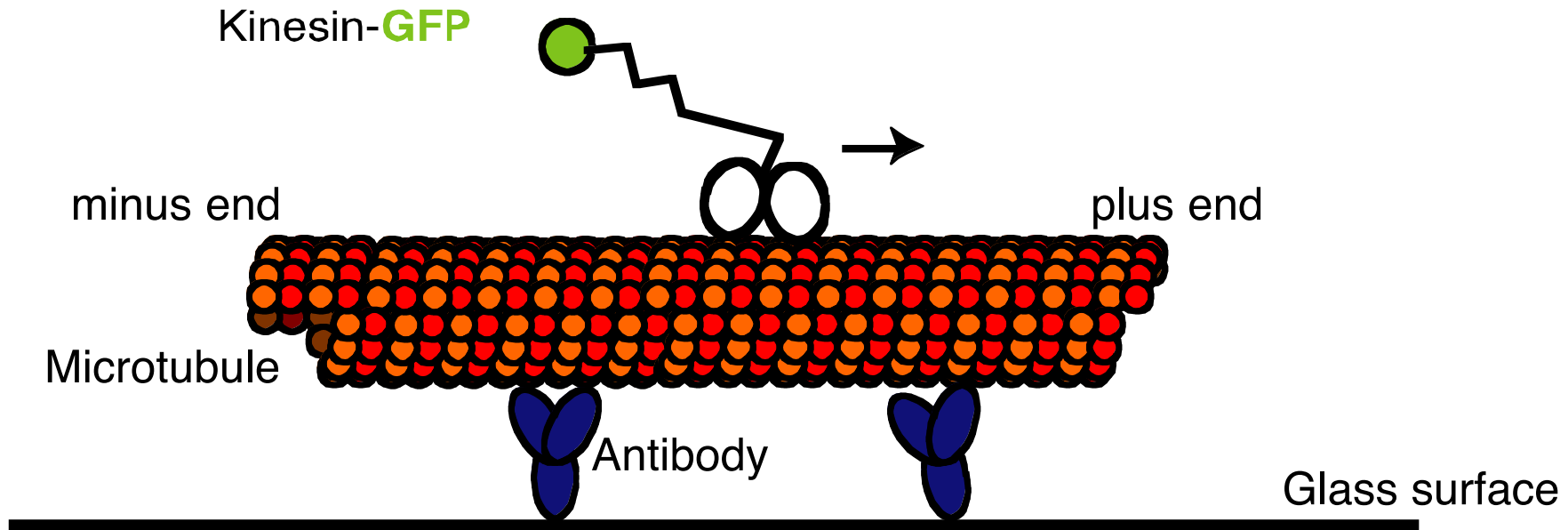
# Bead Assay



real time

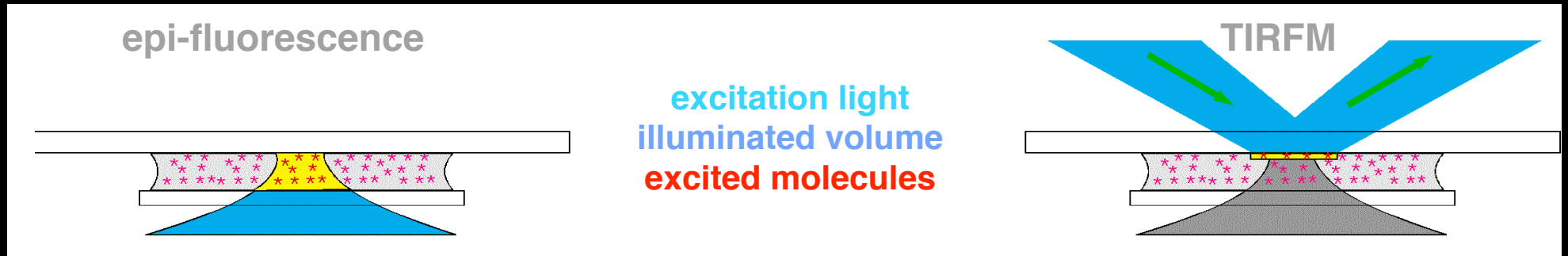
Coy et al. J. Biol. Chem., 1999

# Kinesin is processive: single molecules move



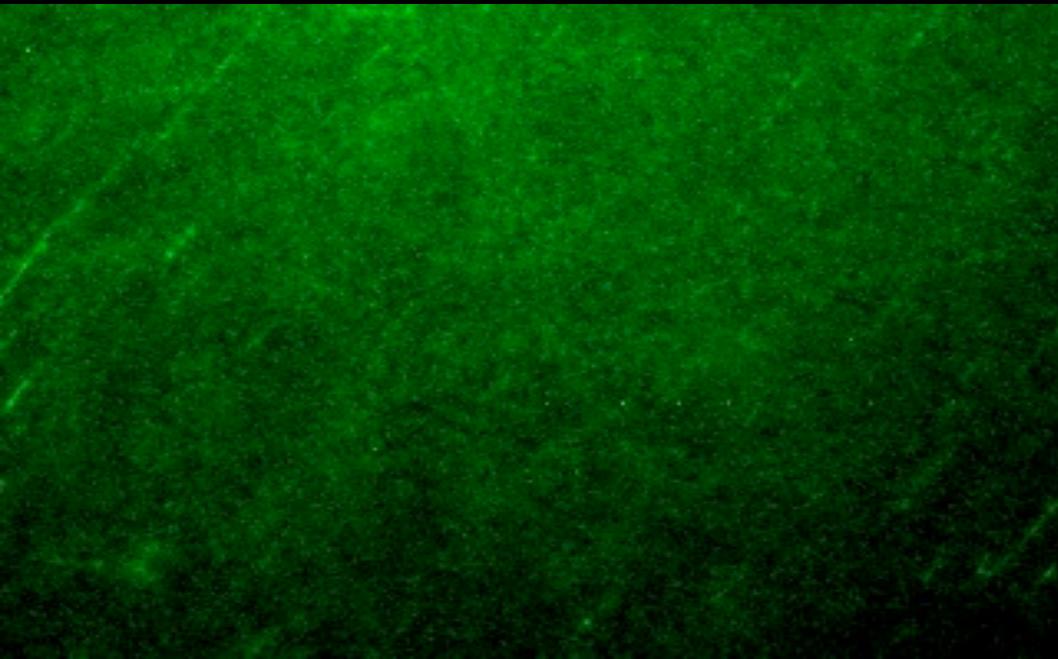
with Stefan Diez

# Total-Internal-Reflection-Fluorescence (TIRF) microscopy

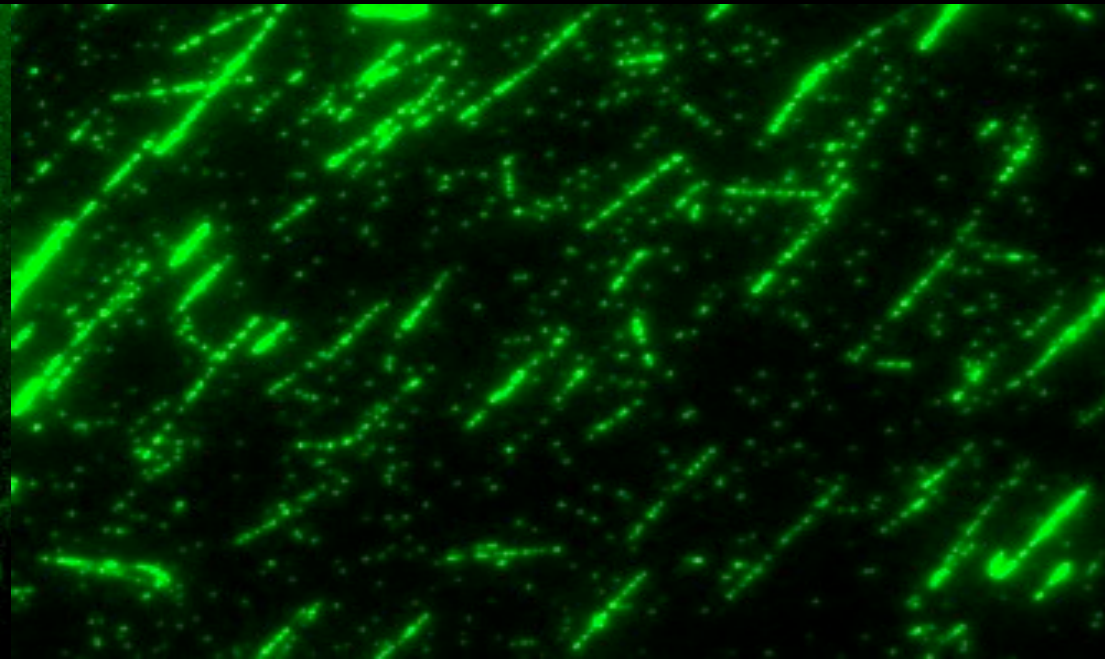


with Stefan Diez

# Total-internal-reflection- fluorescence microscopy (TIRF)



Fluorescence



TIRF

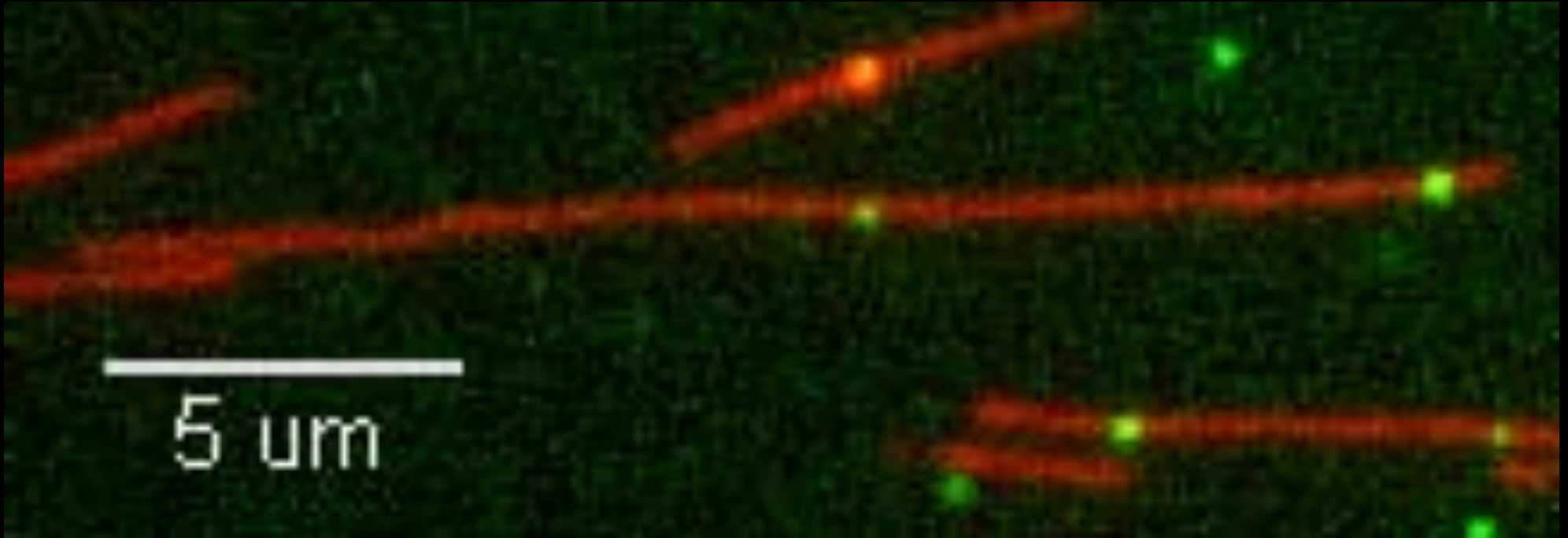
Imaging area - 75  $\mu\text{m}$  x 55  $\mu\text{m}$

**GFP-MCAK** on microtubules

with Stefan Diez

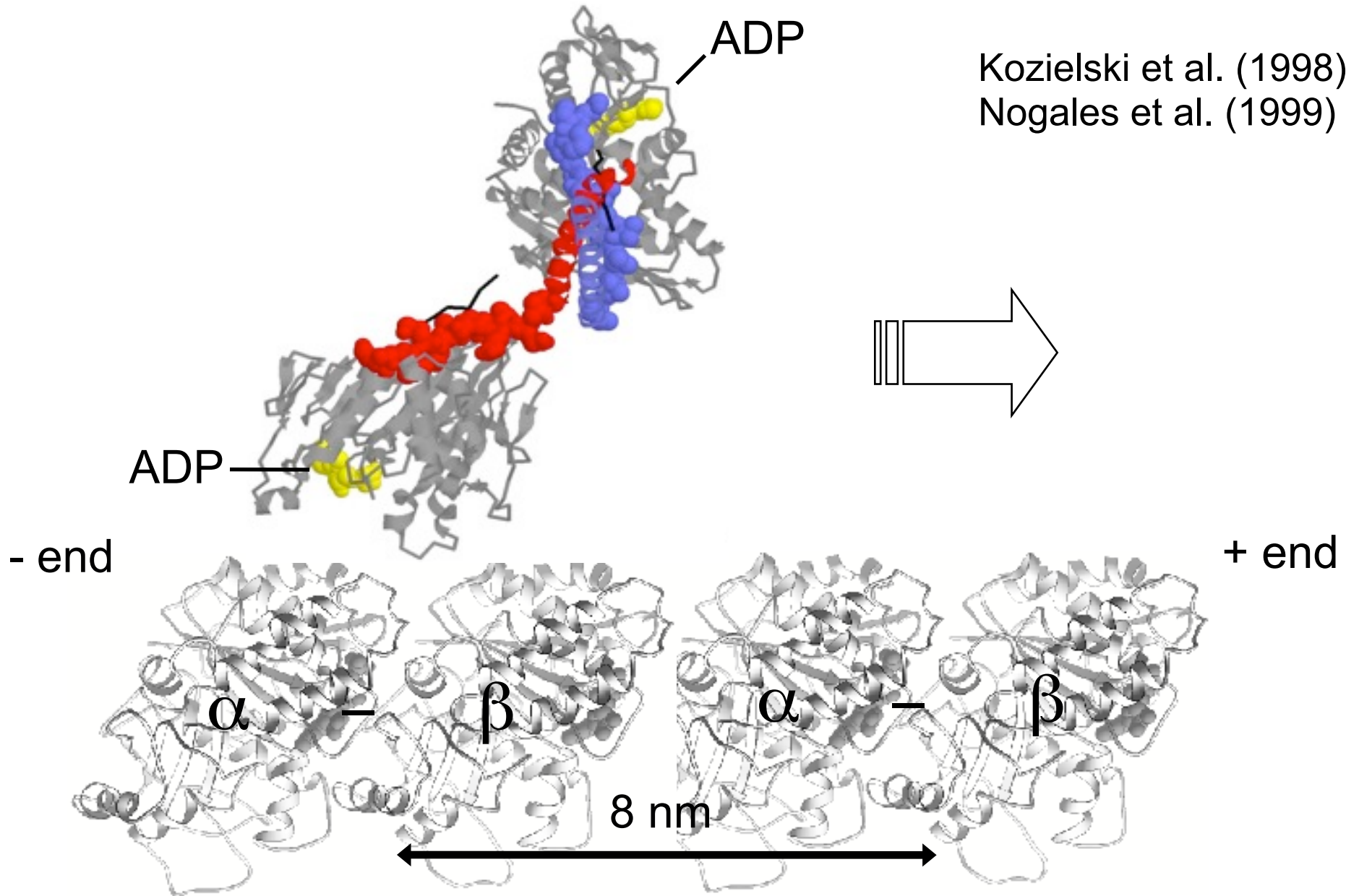


# Processive motility of kinesin



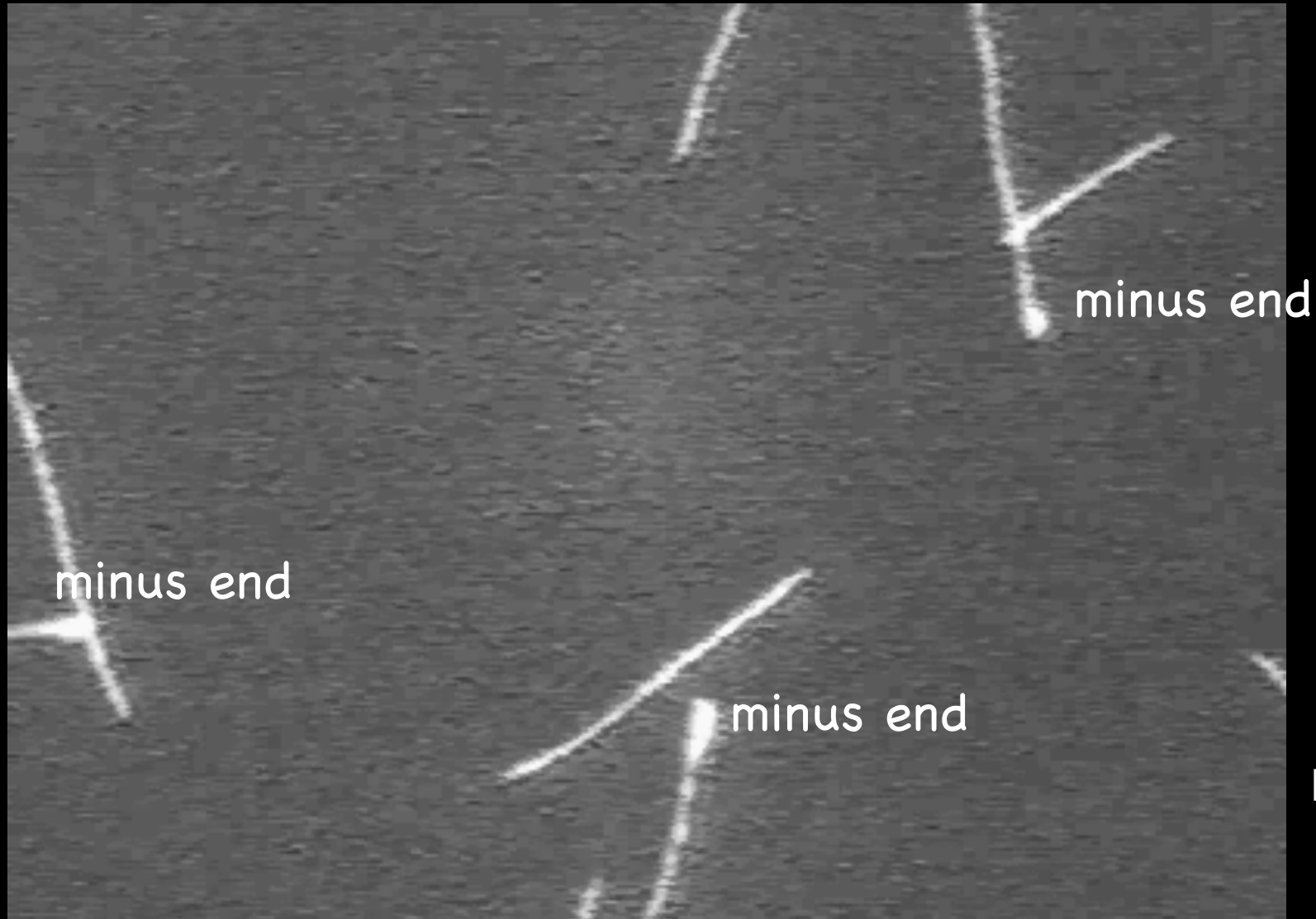
with Stefan Diez

# How does kinesin move?



**In which direction does kinesin move?**

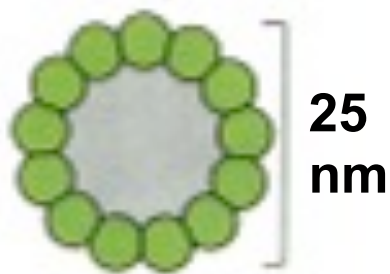
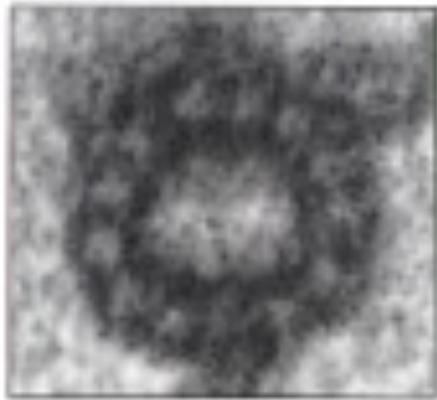
# Kinesin moves towards the plus-end of the microtubule



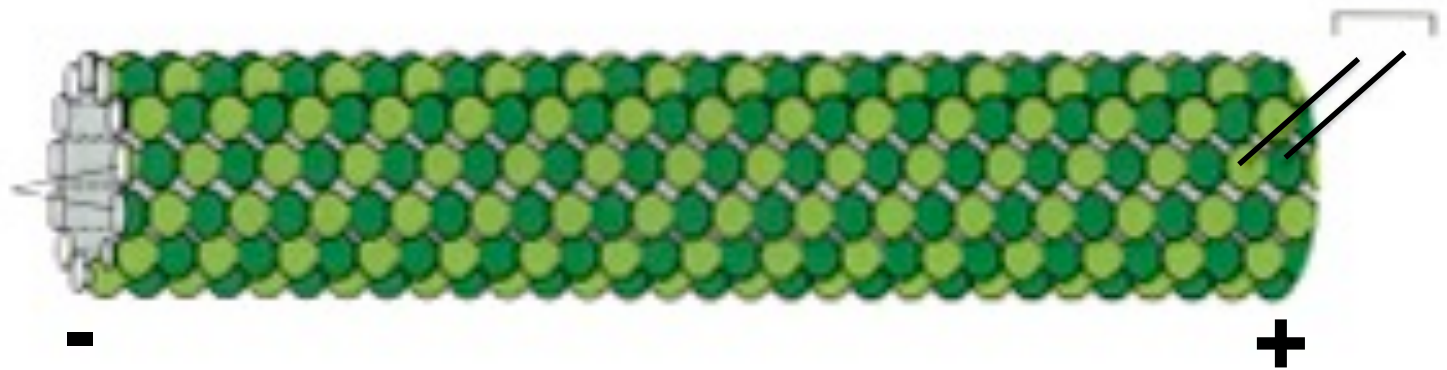
Howard &  
Hyman  
1993

**What path does kinesin follow on the microtubule surface?**

# Lattice structure of the microtubule

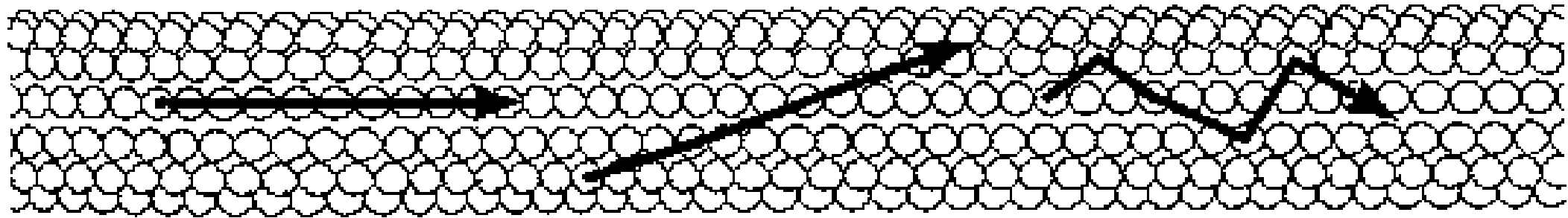


25  
nm



Tubulin dimer  $\alpha \beta$

# Which path does kinesin follow?

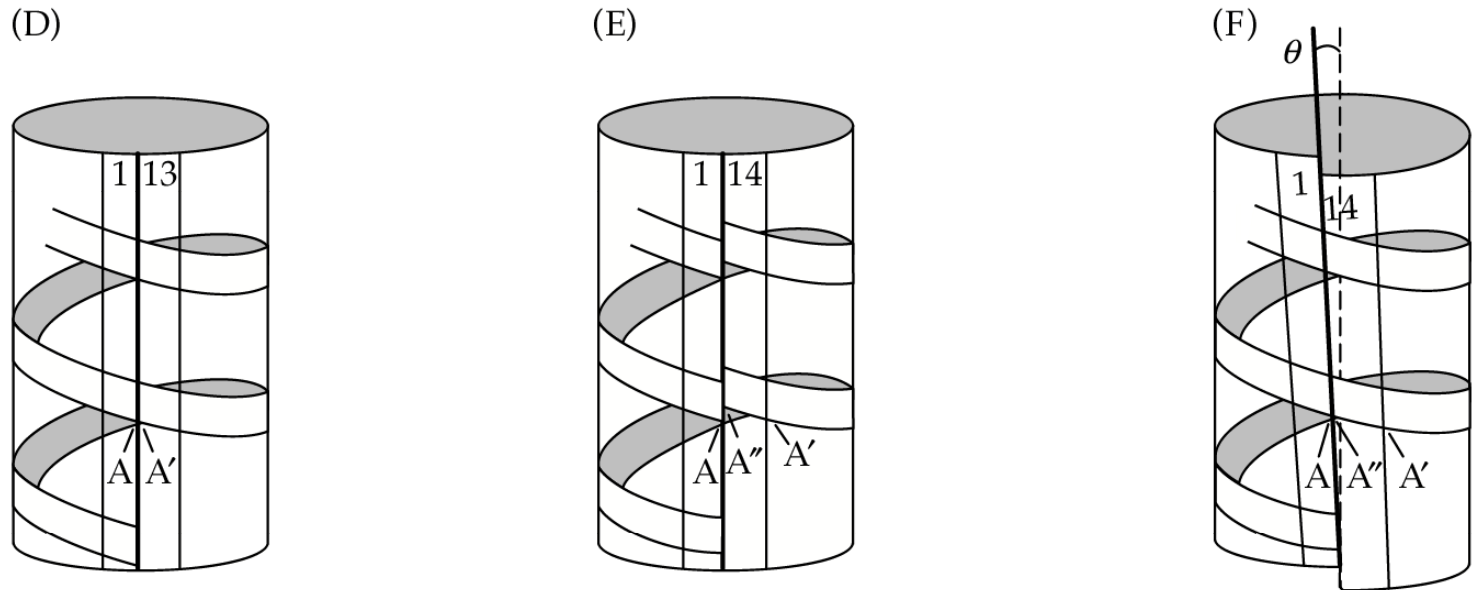
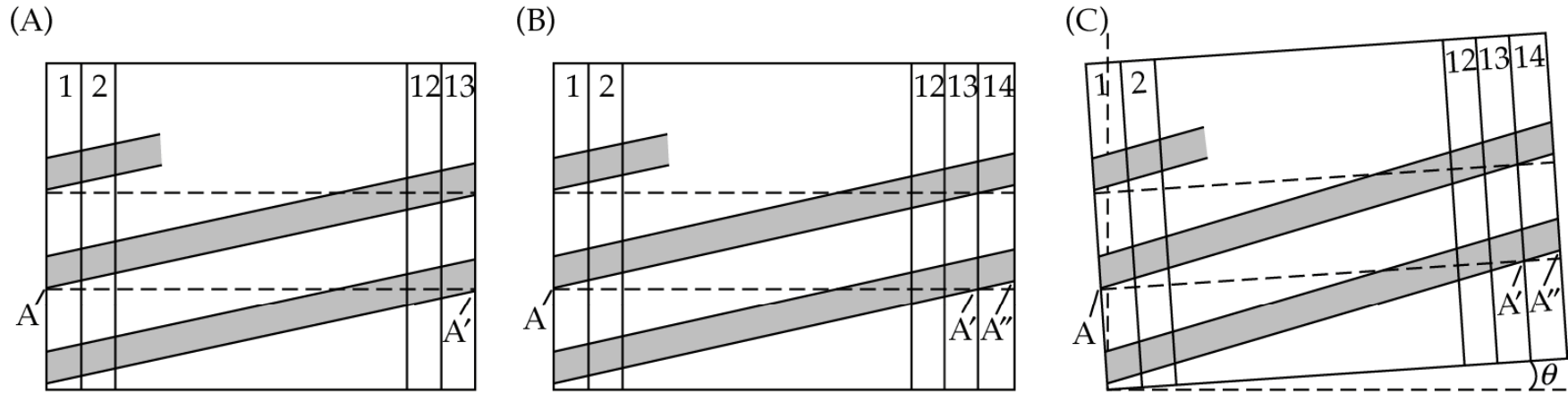


parallel

angled

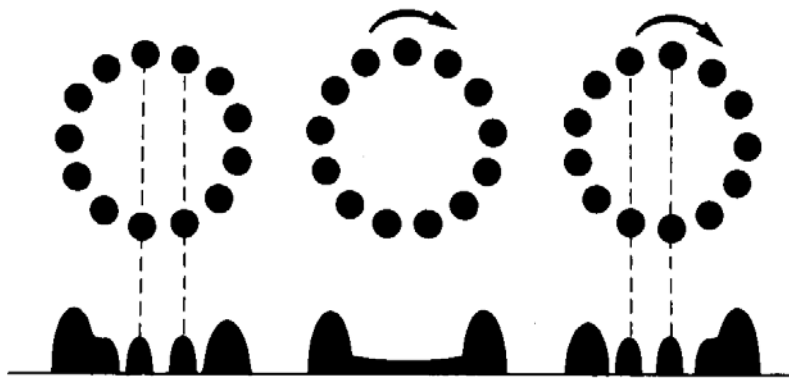
random

# Lattice rotation model

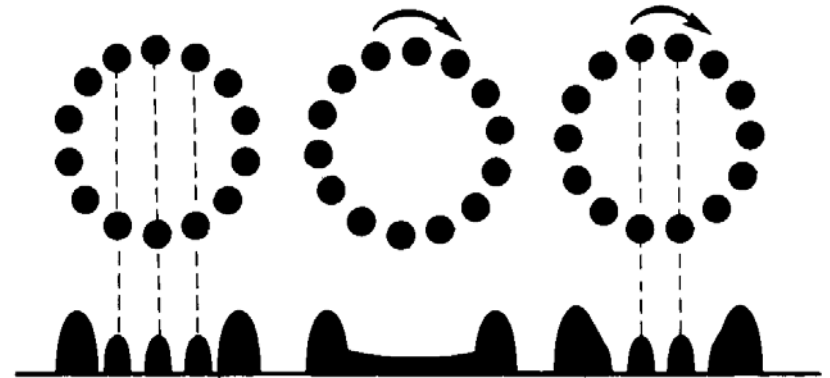




# Moire pattern reveals the supertwist

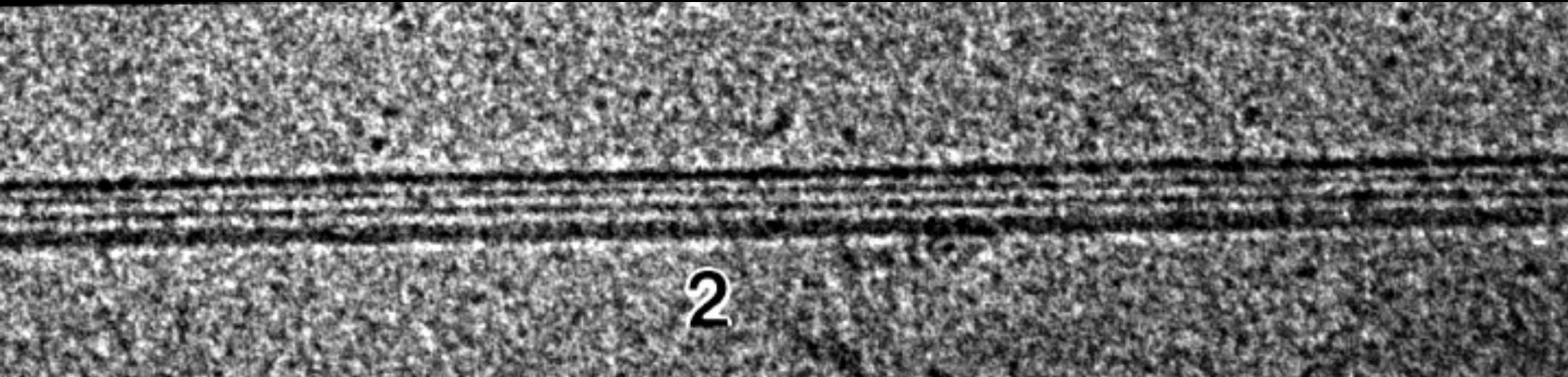


13 protofilaments

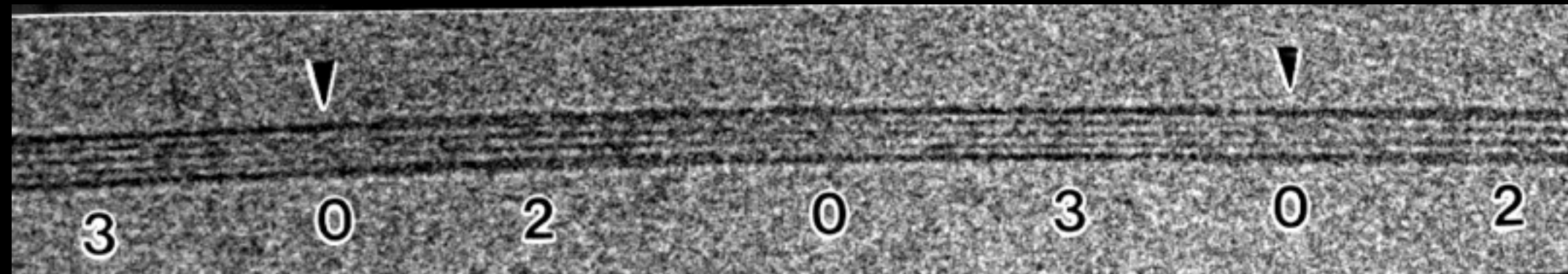


14 protofilaments

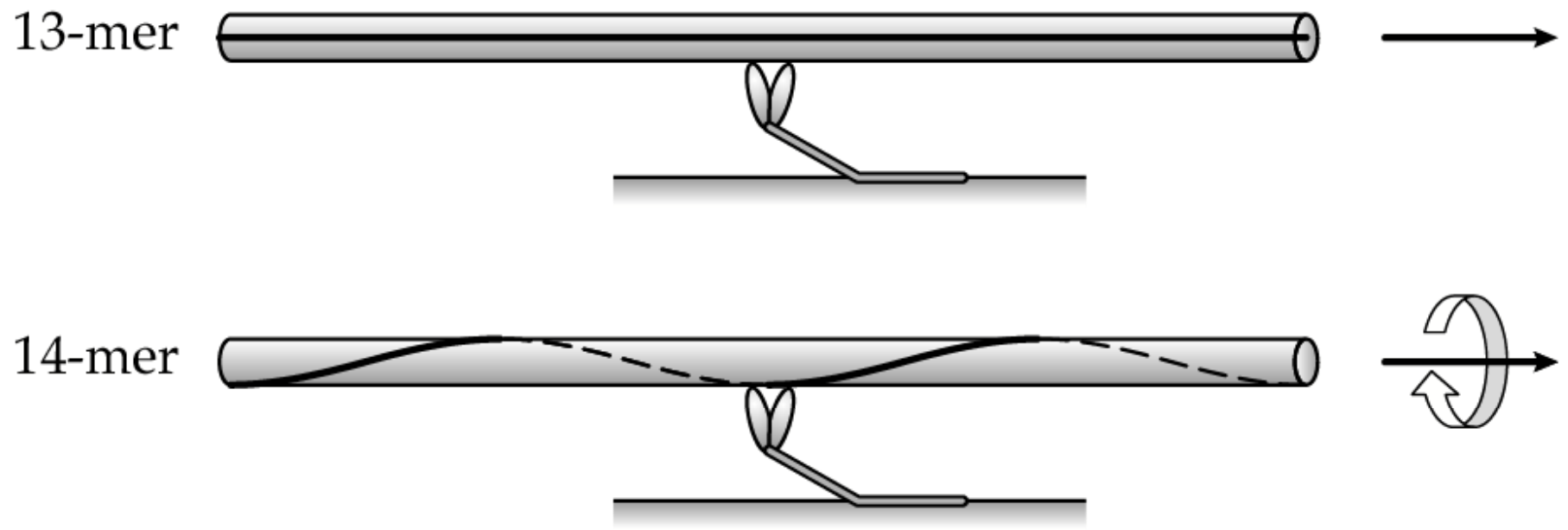
# 13 Protofilaments



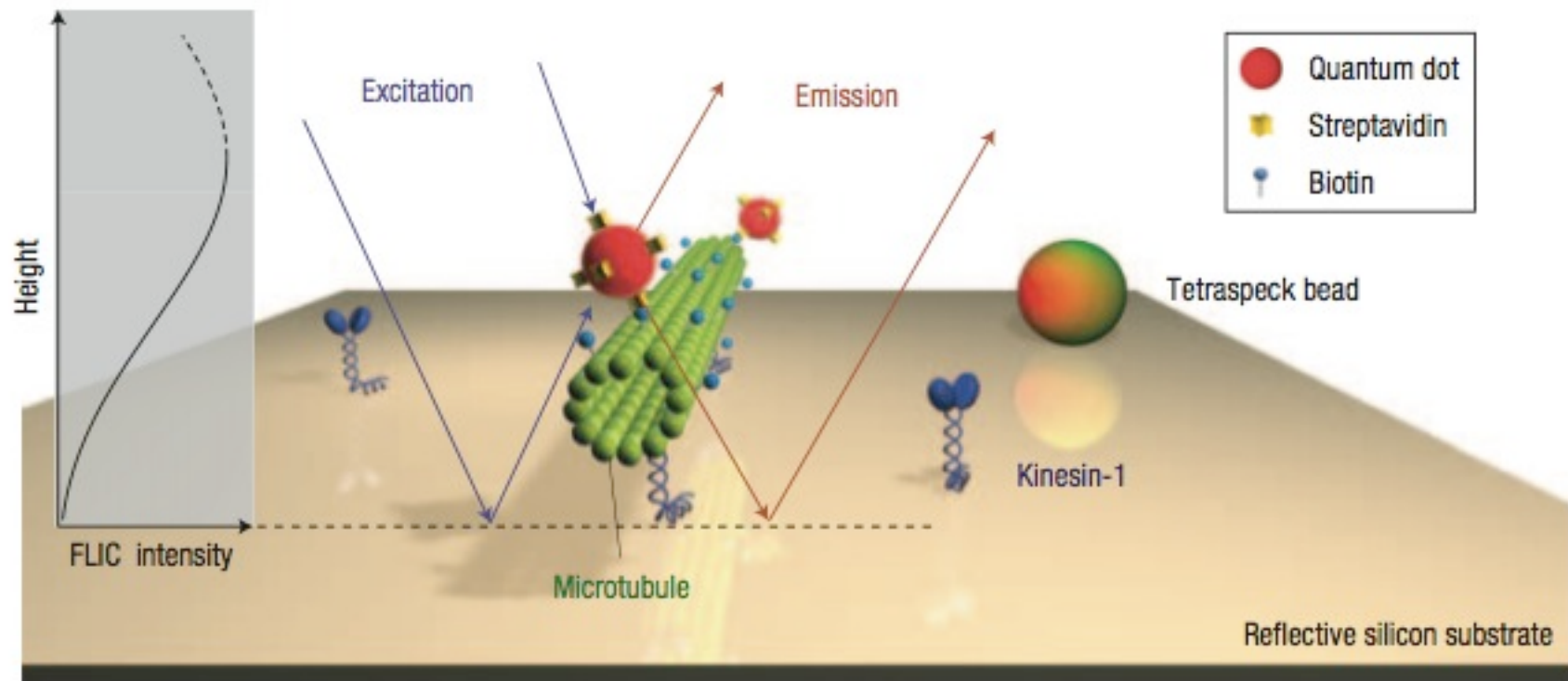
# 14 Protofilaments



# Rotation of supertwisted microtubules



# Fluorescence interference contrast (FLIC) microscopy



Nitzsche et al. Nature Nanotech. (2008)  
(Stefan Diez, Dresden)

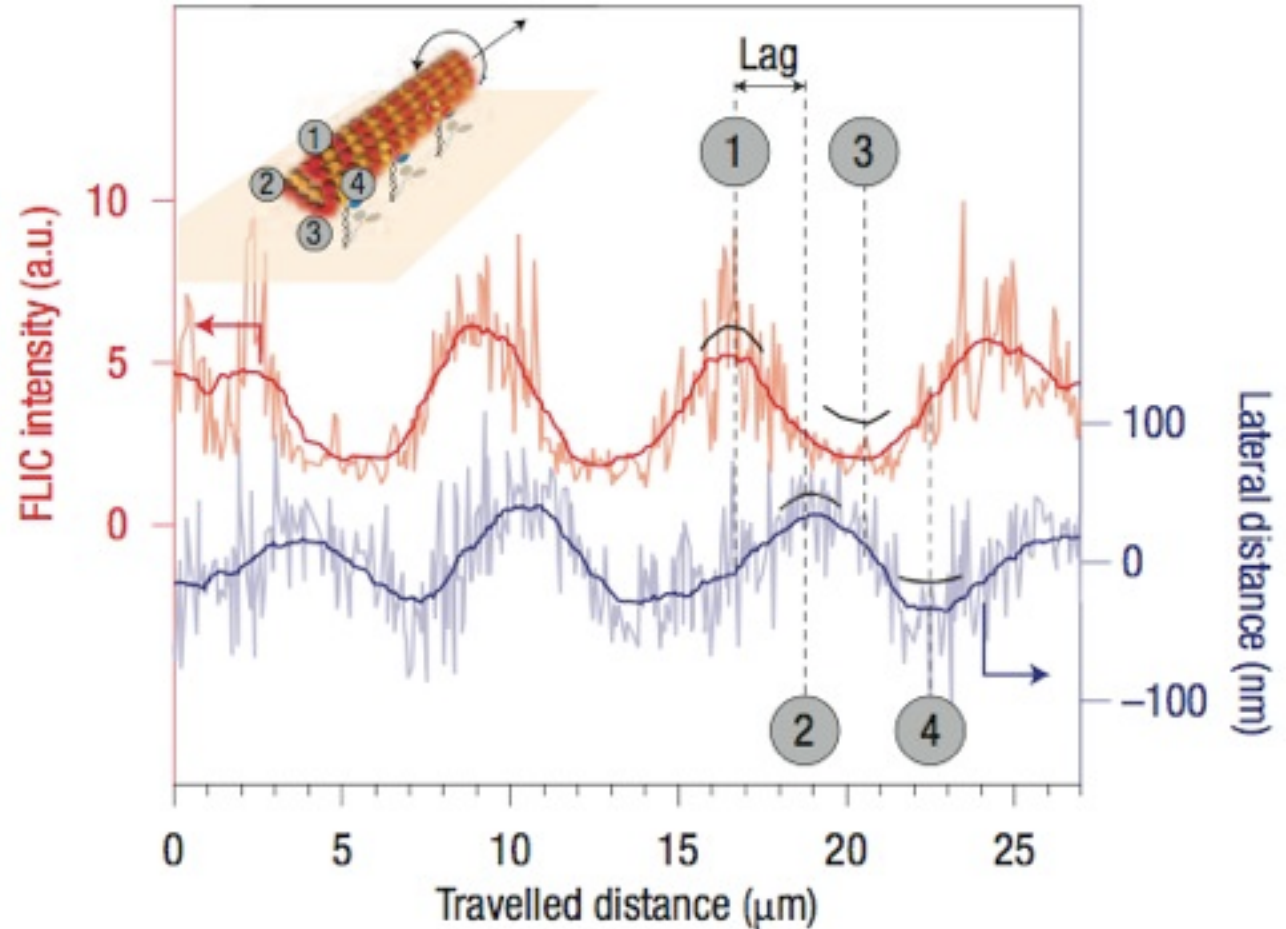
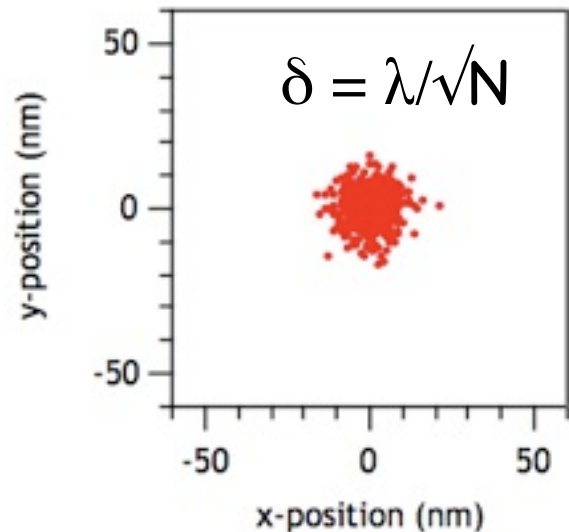
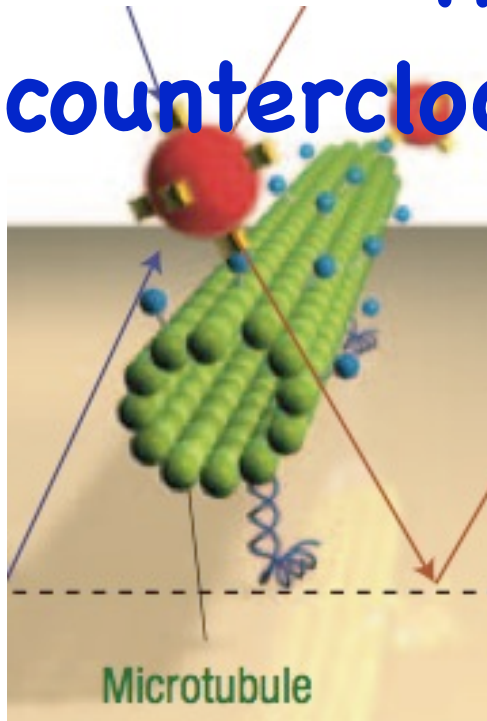
# Rotation of 14-protofilament microtubules



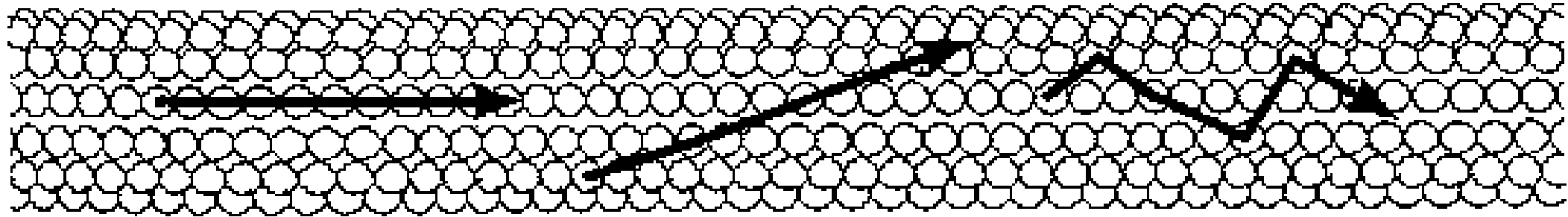
Video

Maximum  
projection

# Handedness of rotation counterclockwise → along the protofilament



# Kinesin follows the protofilament axis



parallel

YES

angled

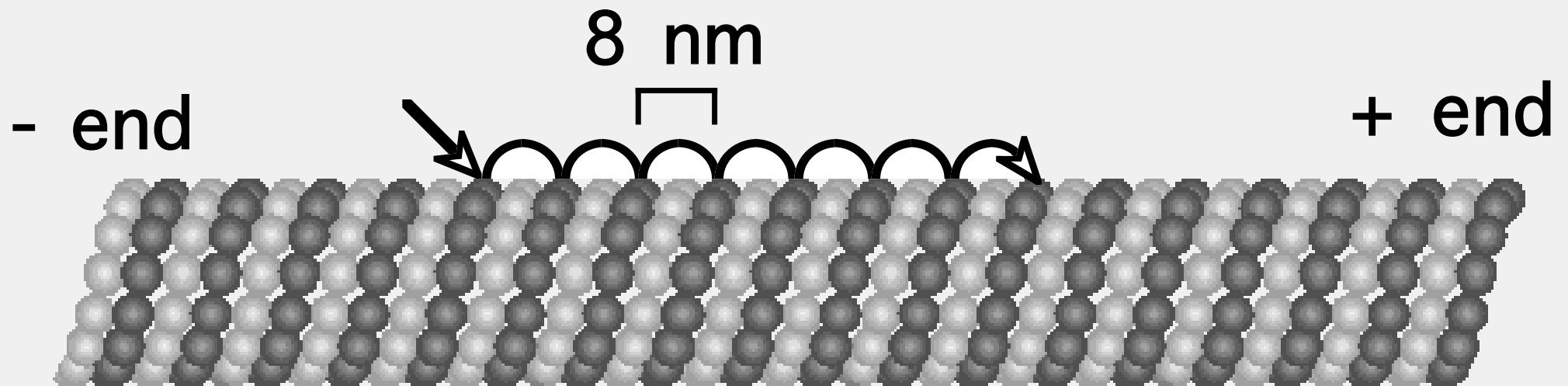
NO

random

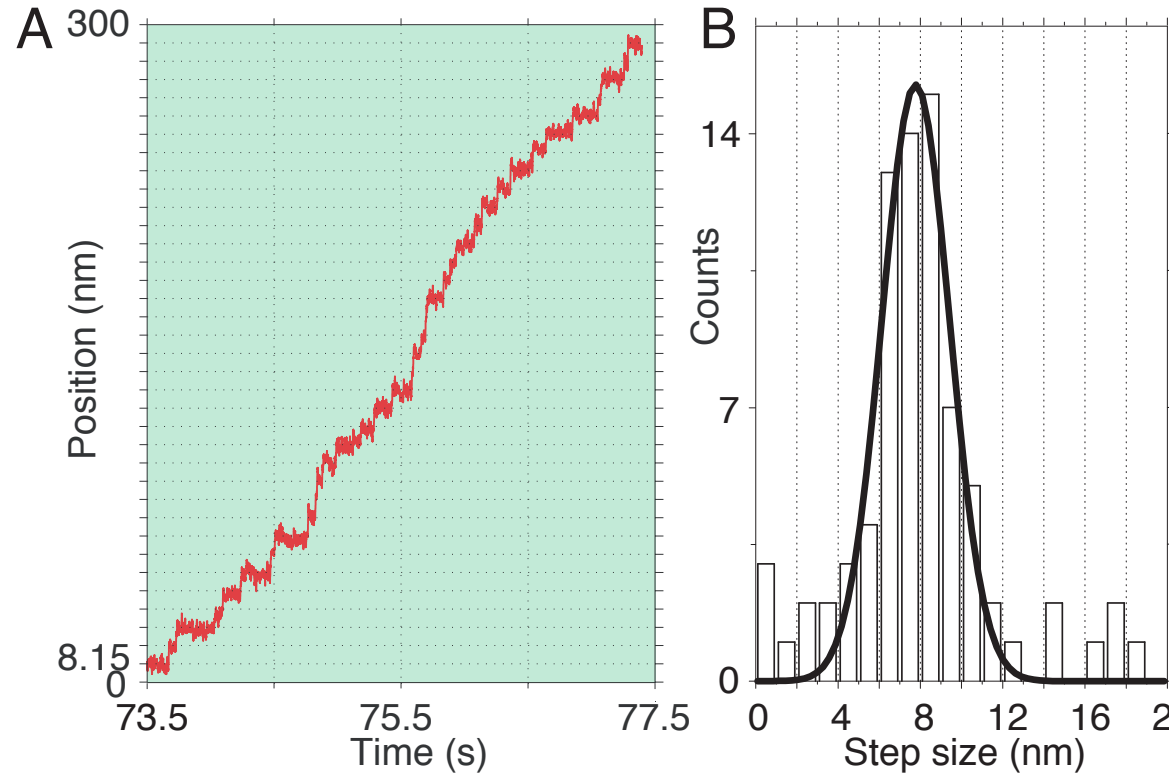
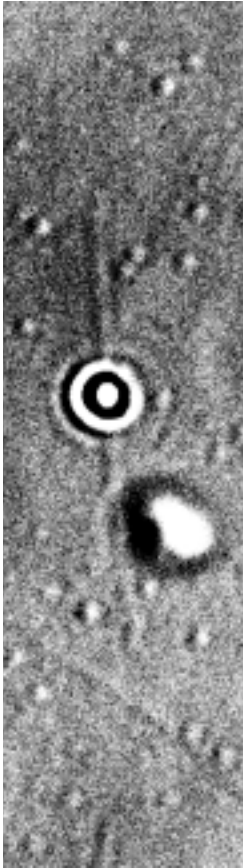
NO



# Kinesin's path on the microtubule

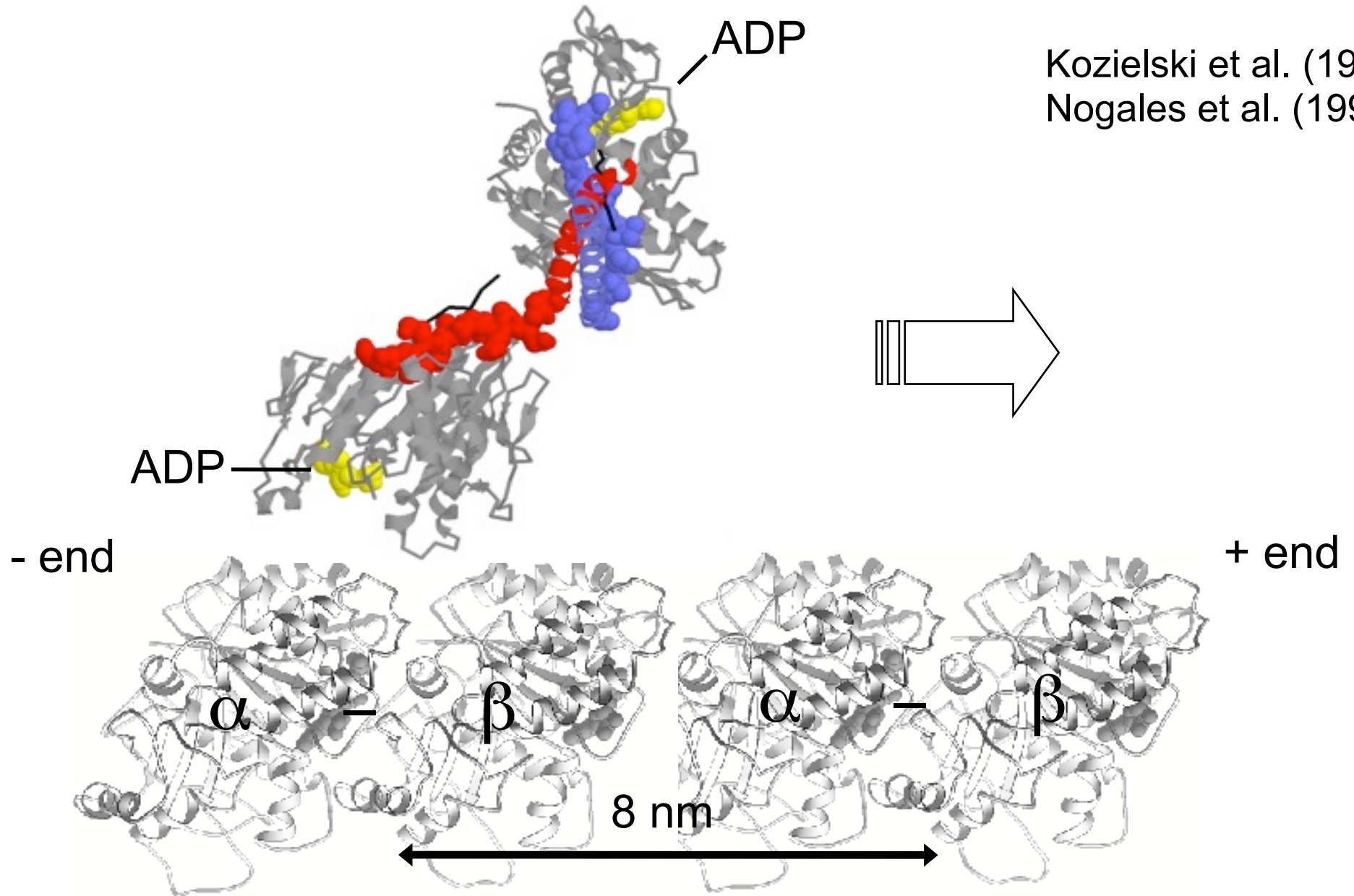


# Direct measurement of 8-nm steps



# How does kinesin get to the next binding site?

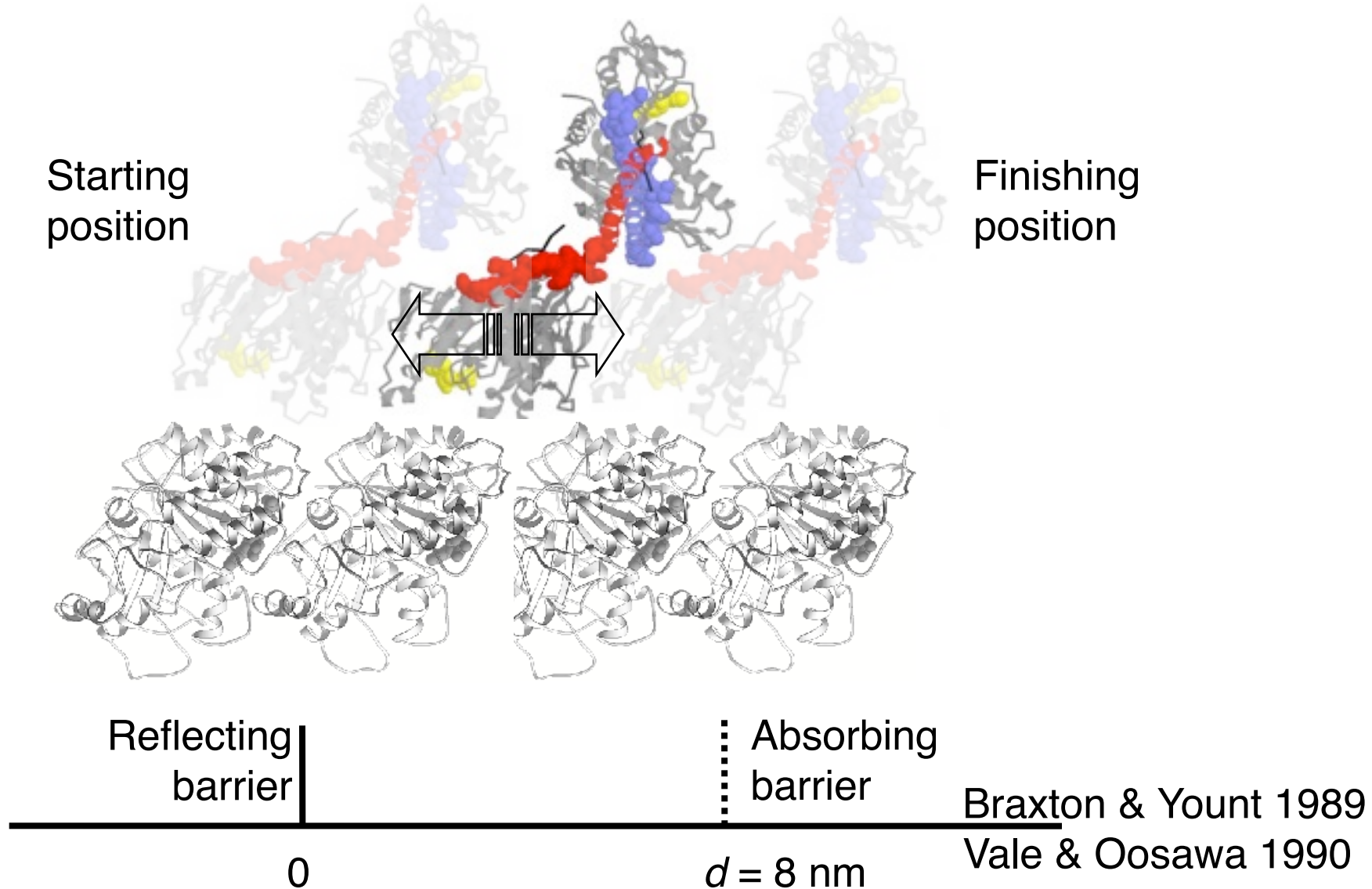
Kozielski et al. (1998)  
Nogales et al. (1999)



# Outline

1. Single-molecule techniques can be used to study movement of purified motor proteins
2. Role of **fluctuations** in the motor reaction
3. Protein friction limits motor speed and efficiency
4. Force gating of motor proteins: active mechanical circuits underlying cell motility

# “Ratchet diffusion” model



# Force generated by the "Ratchet diffusion" mechanism

Prediction:

First-passage time:  $t = d^2/2D = d^2\gamma/2kT$

$d = \text{step size} = 8 \text{ nm}$

$\gamma = \text{viscosity}$

Maximum force against a viscous load:

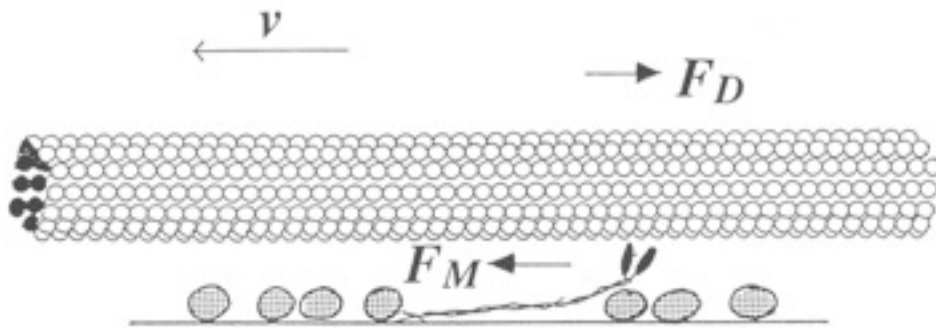
$$f_{\text{drag}} = \gamma v_{\text{max}} = \gamma d/t = 2kT/d = \boxed{1 \text{ pN}}$$



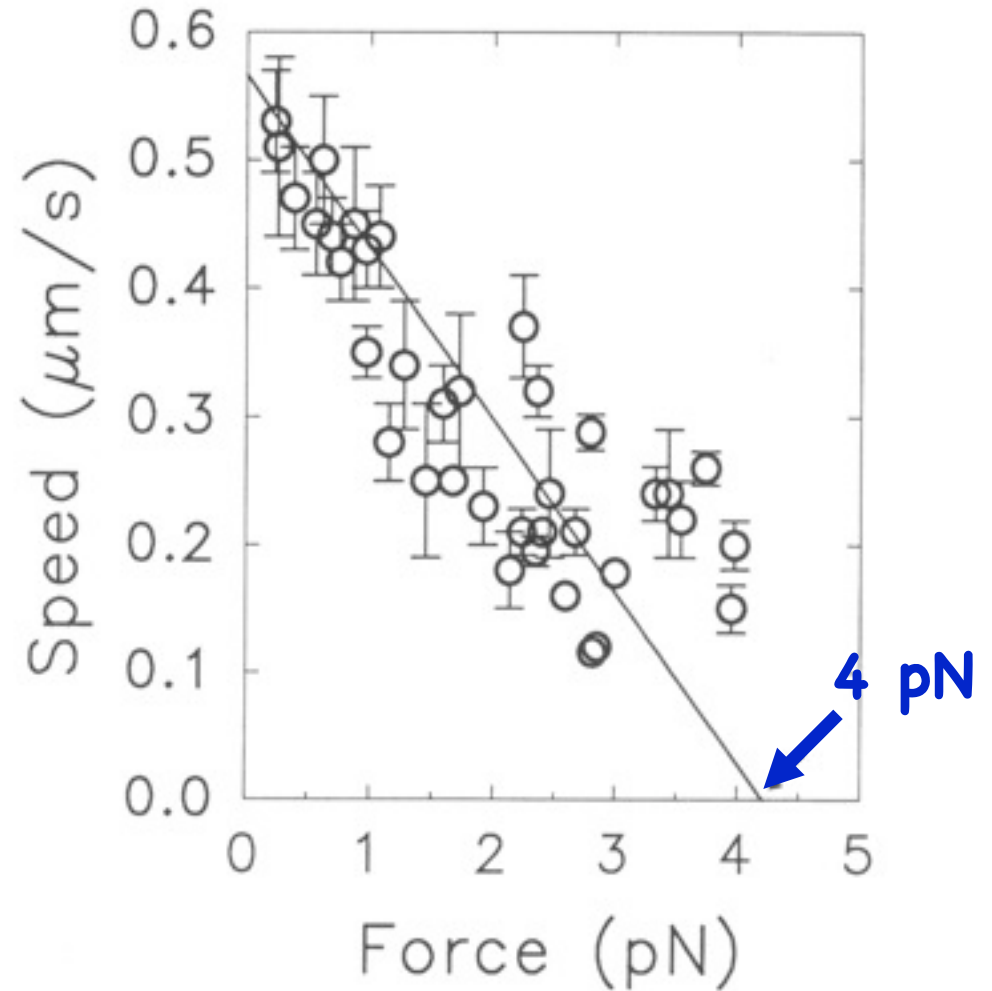
Hunt et al. (1994)

# Single-kinesin force against a viscous load

increase viscosity 100-fold

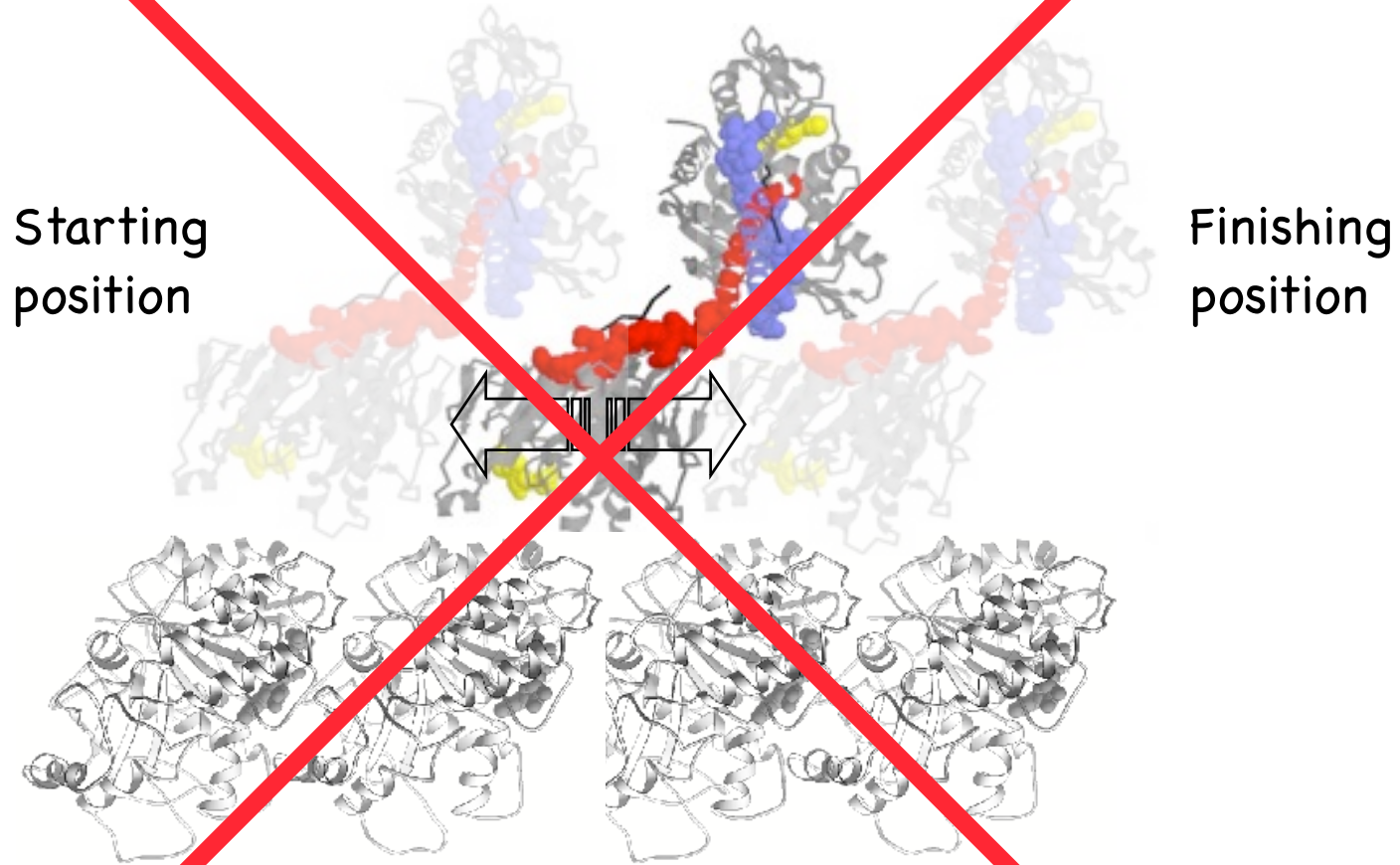


"upside-down assay"



Hunt et al. (1994)

# ~~“Ratchet diffusion” model~~



Reflecting  
barrier

0

Absorbing  
barrier

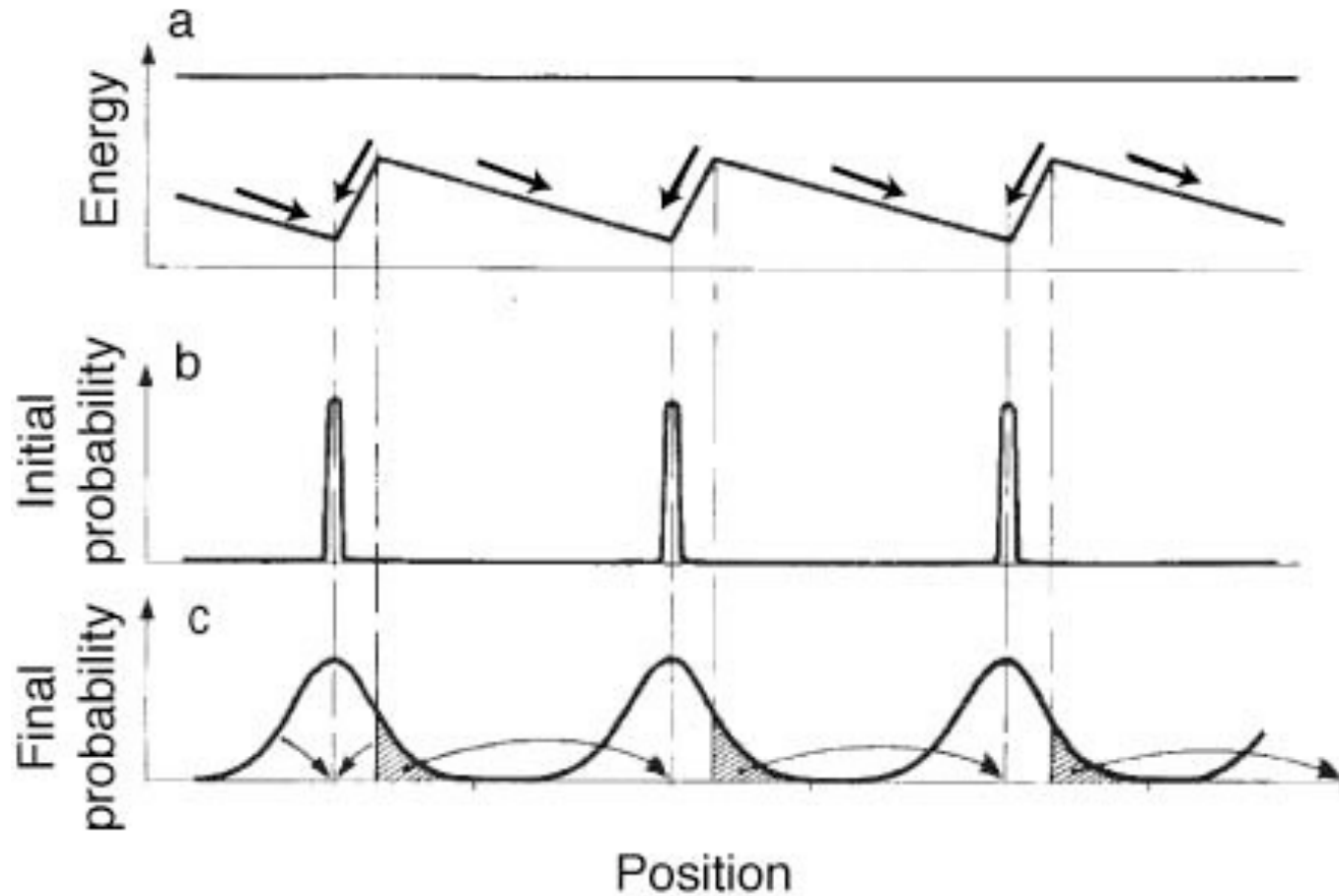
$d = 8 \text{ nm}$

Braxton & Yount 1989

Vale & Oosawa 1990



# Time-varying (flashing) ratchets



Roussellet et al. 1994  
and see also Astumian & Bier 1994

# Time-varying (flashing) ratchets

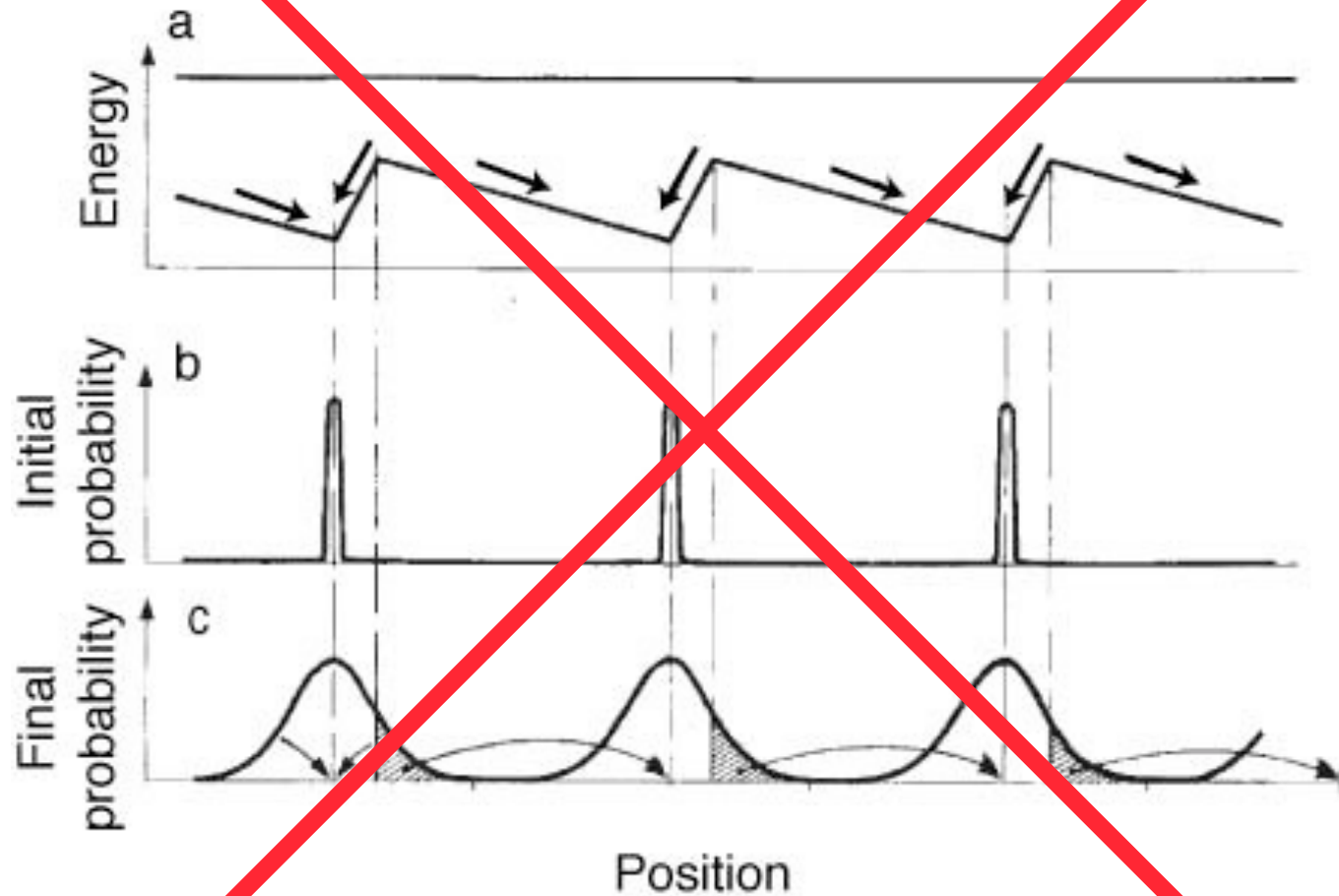
## Prediction:

Because there is only a <50% chance of progressing to the next site (>50% chance of staying put or going backwards) then it takes at least 2 ATP on average to move 8 nm

## Experiment:

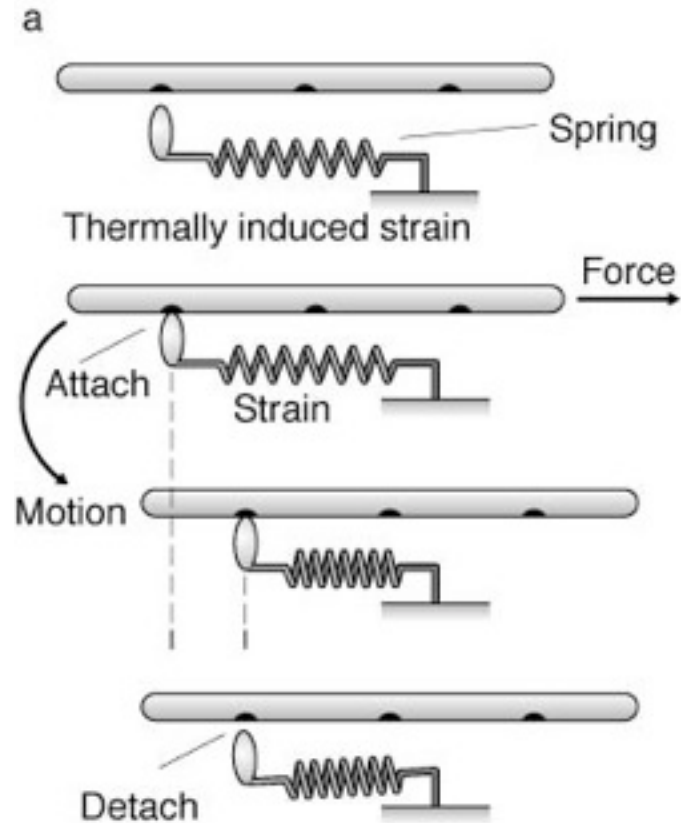
One ATP hydrolyzed per step (Coy et al. J. Biol. Chem. 1999)

# Time-varying (flashing) ratchets



Roussellet et al. 1994  
and see also Astumian & Bier 1994

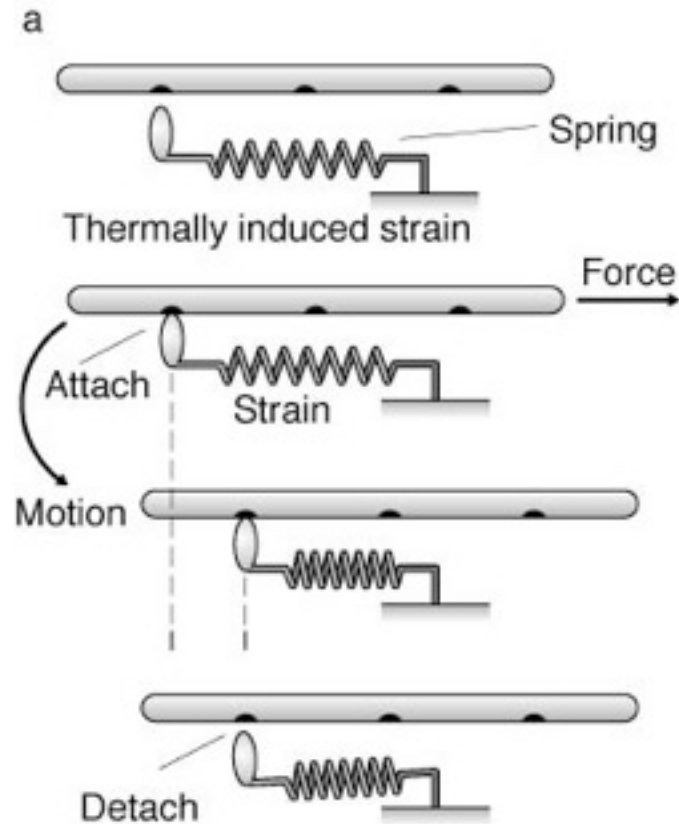
# Thermal ratchet model



Huxley 1957

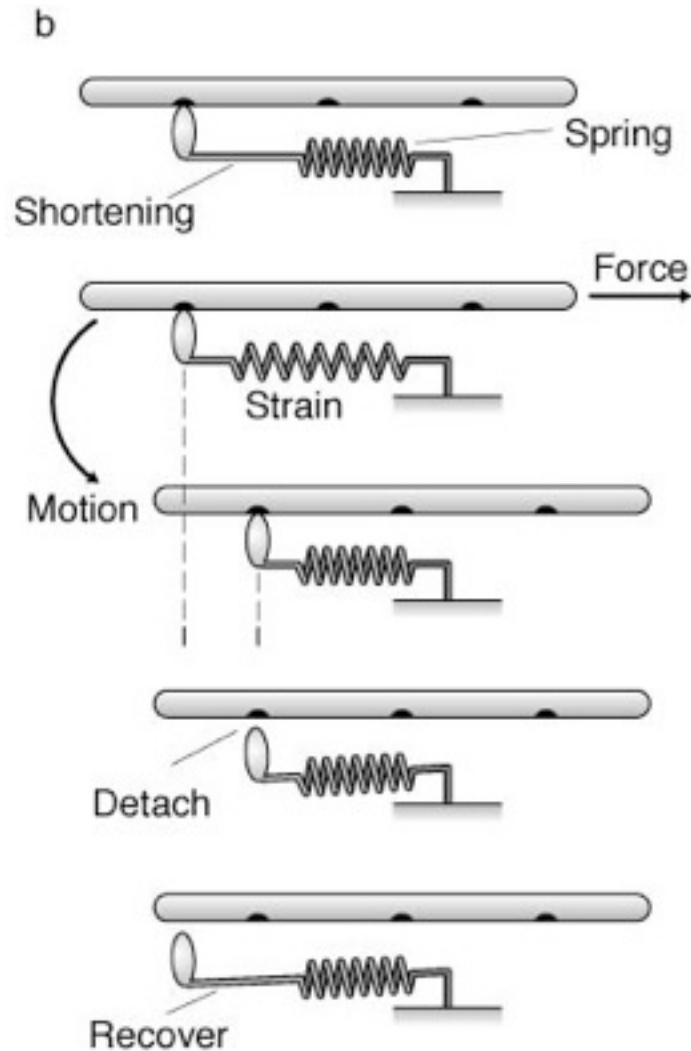
Cordova et al. 1992

# Thermal ratchet model



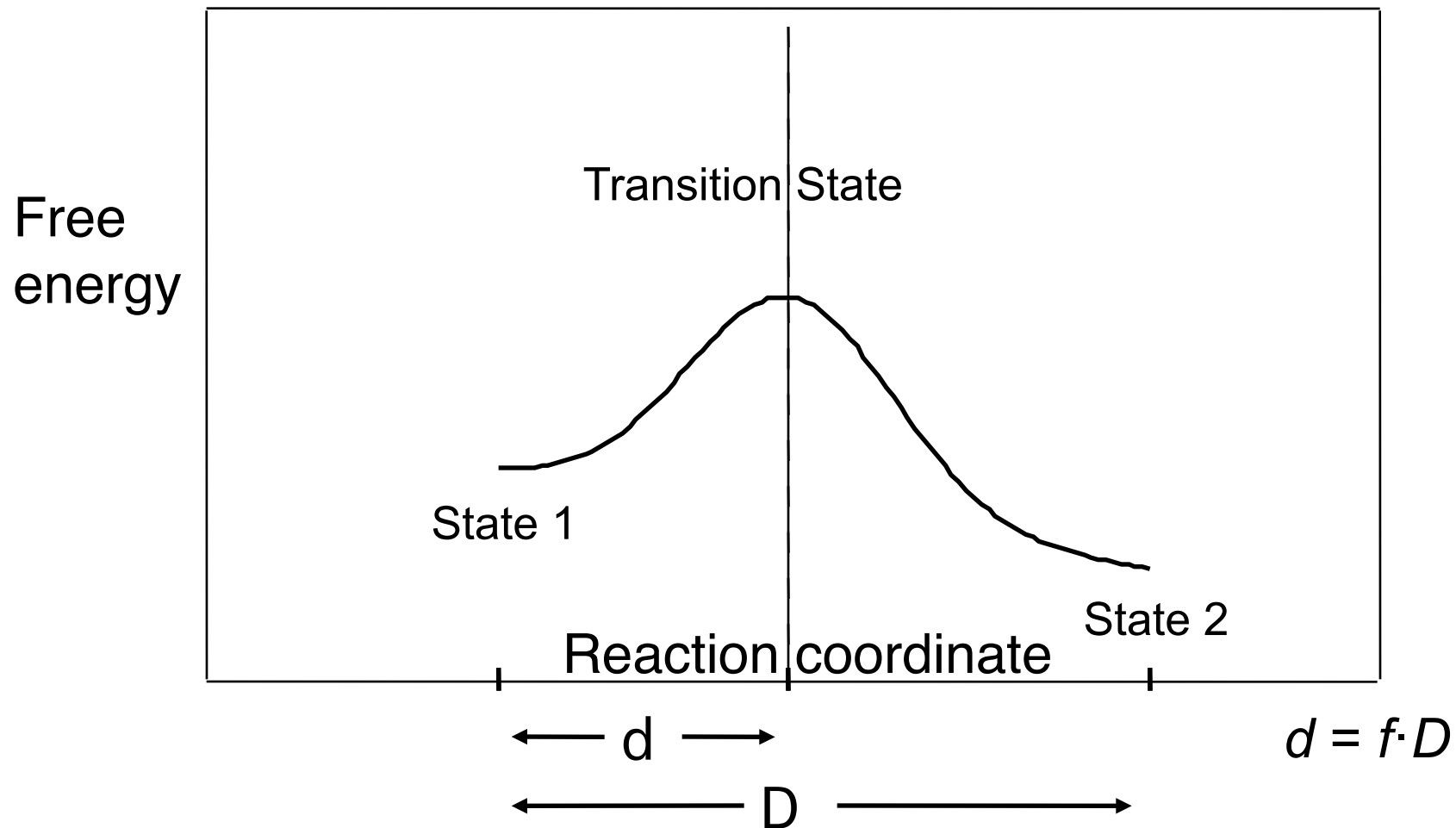
Huxley 1957  
Cordova et al. 1992

# Powerstroke model

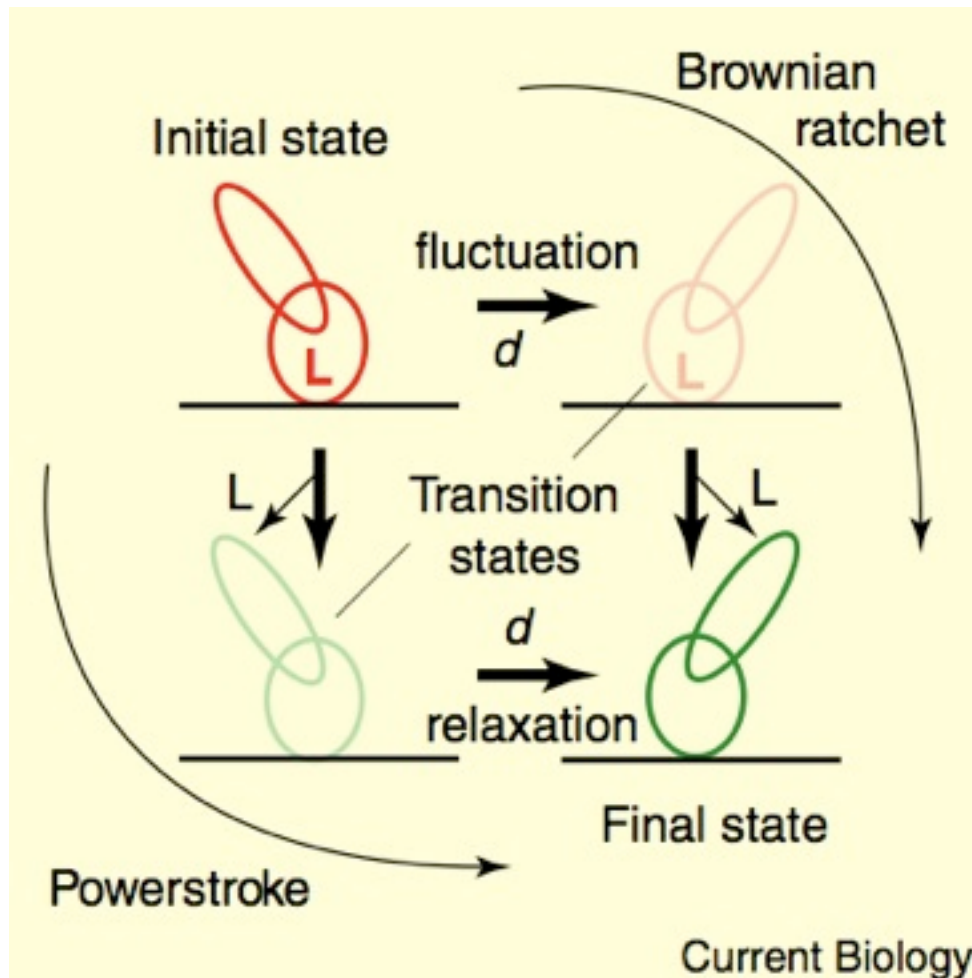


Eisenberg & Hill 1978  
Parmeggiani et al. 1999

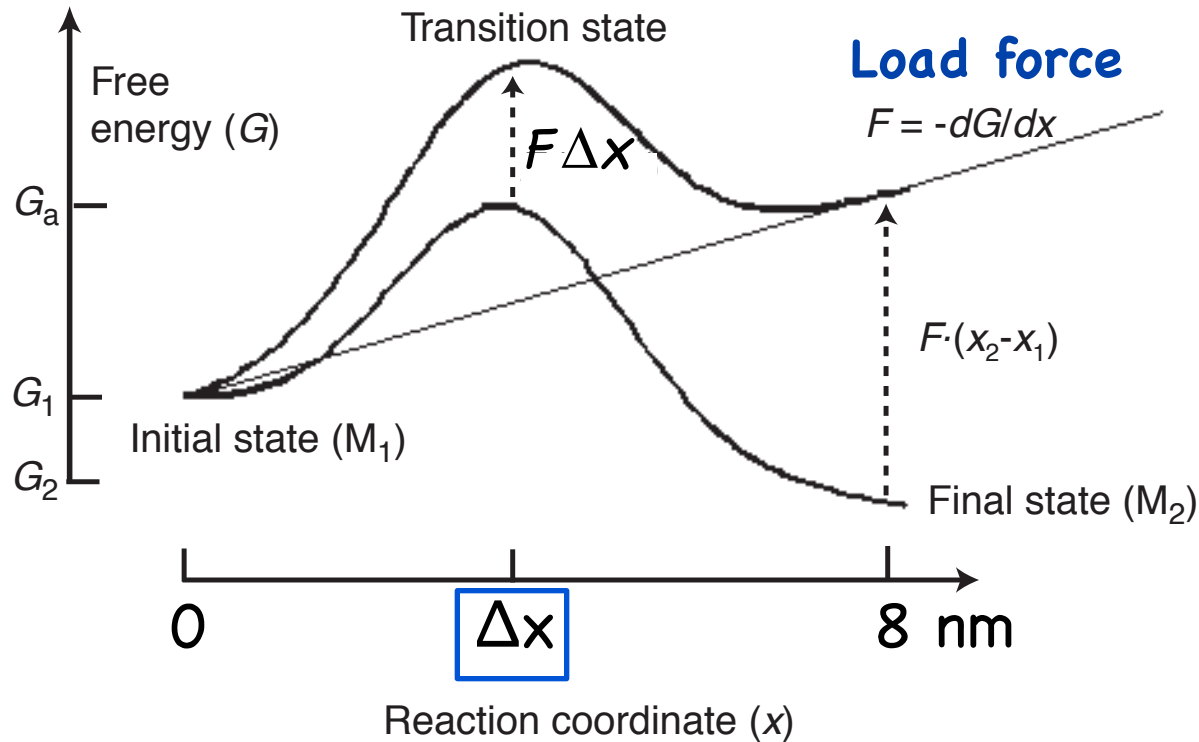
# Transition state concept



# What is the position of the transition state?



# Force can be used to measure the position of the transition state

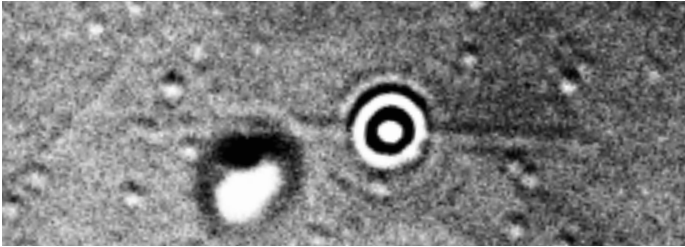


$$k_+ = k_0 \exp\left(-\frac{F \cdot \Delta x}{kT}\right)$$

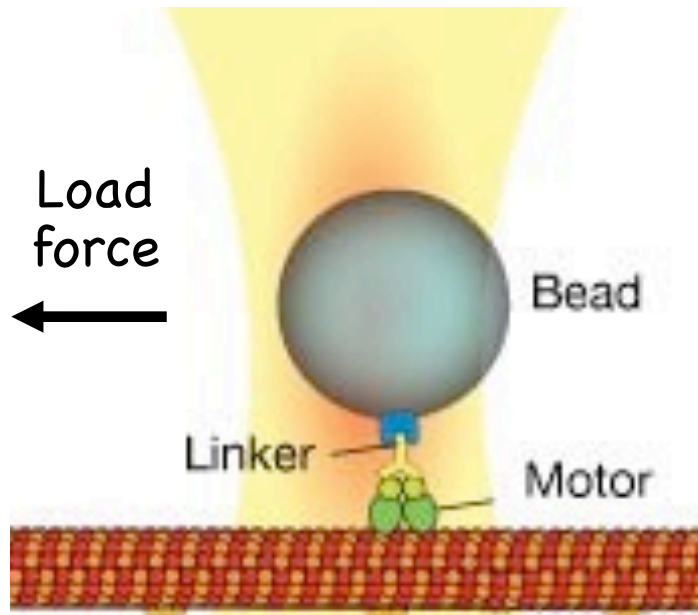
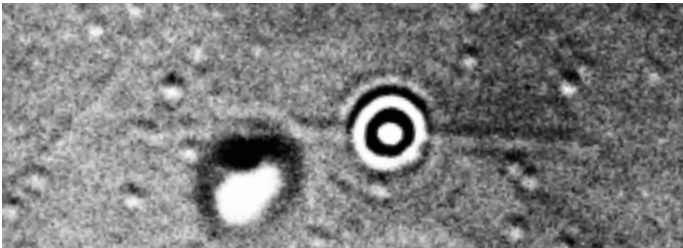
(Kramers 1940)



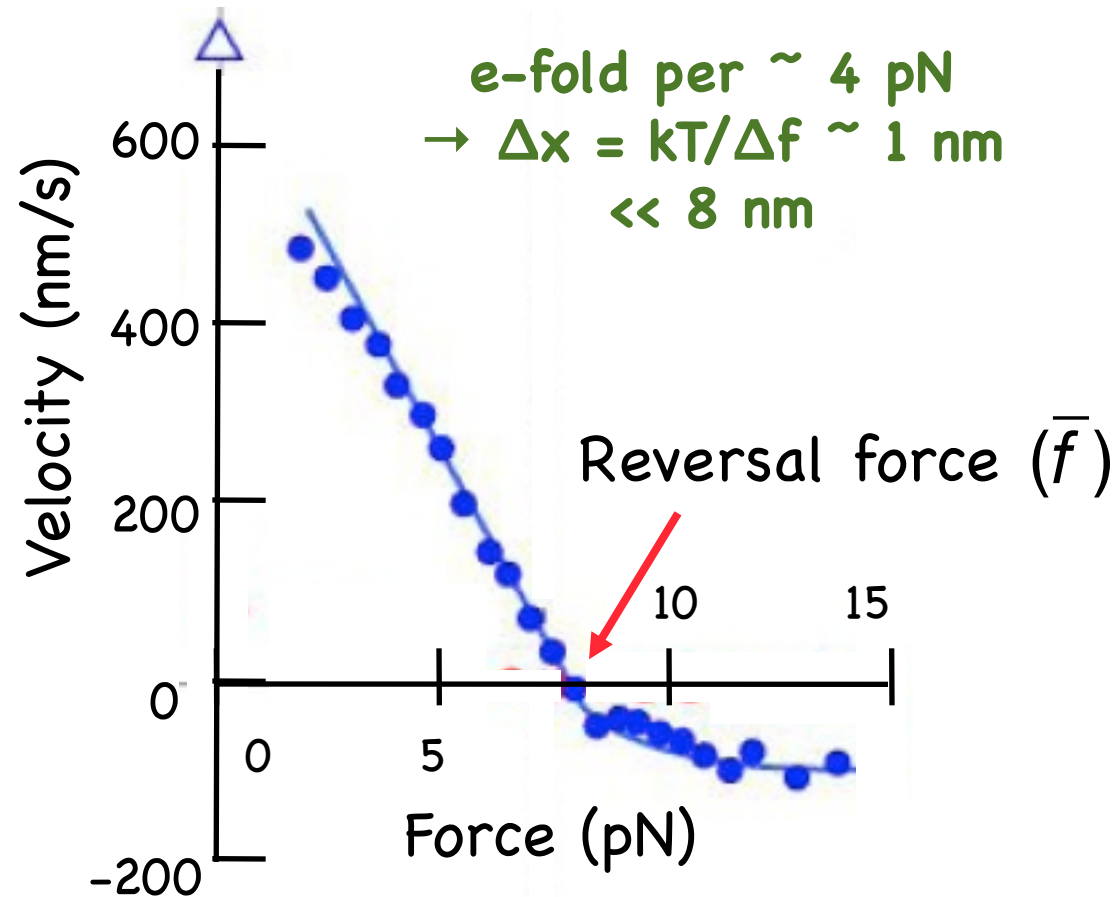
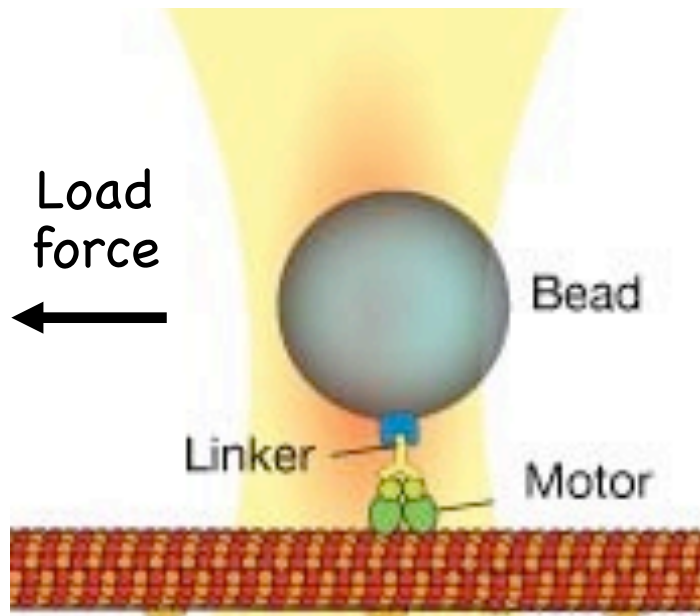
# Force-velocity curve (kinesin)



# Force-velocity curve (kinesin)

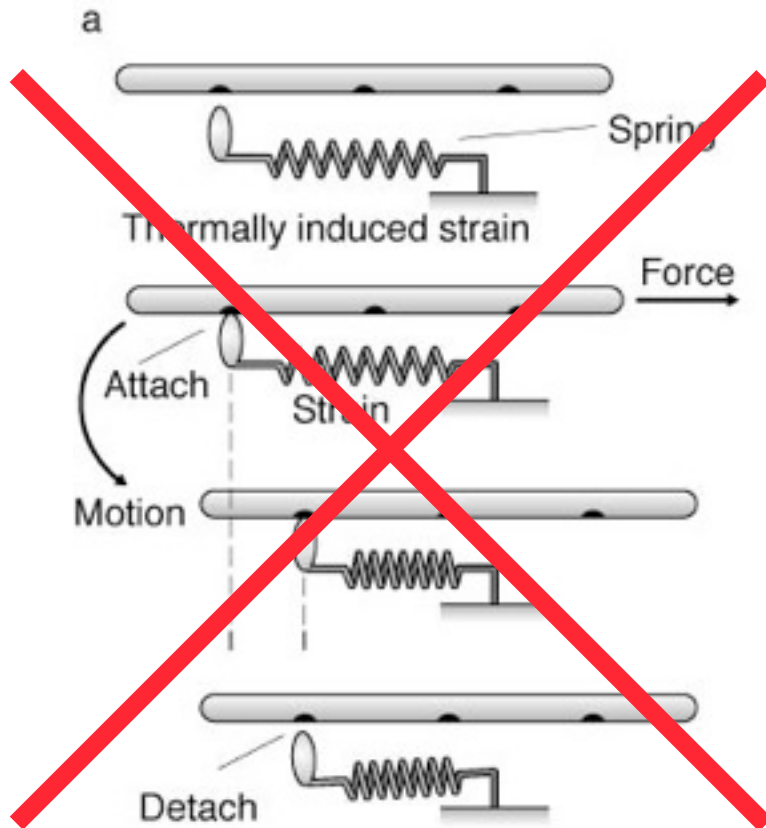


# Force-velocity curve (kinesin)



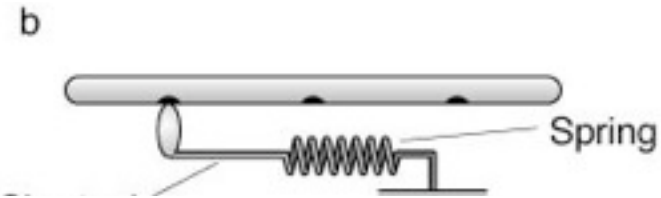
Carter & Cross 2005

# Thermal ratchet model

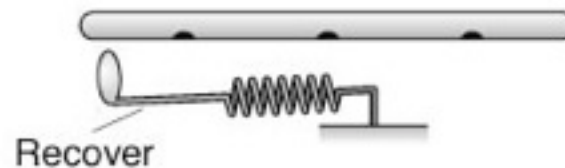


Huxley 1957  
Cordova et al. 1992

# Powerstroke model



small distance to transition state assures reasonable speeds even at high forces

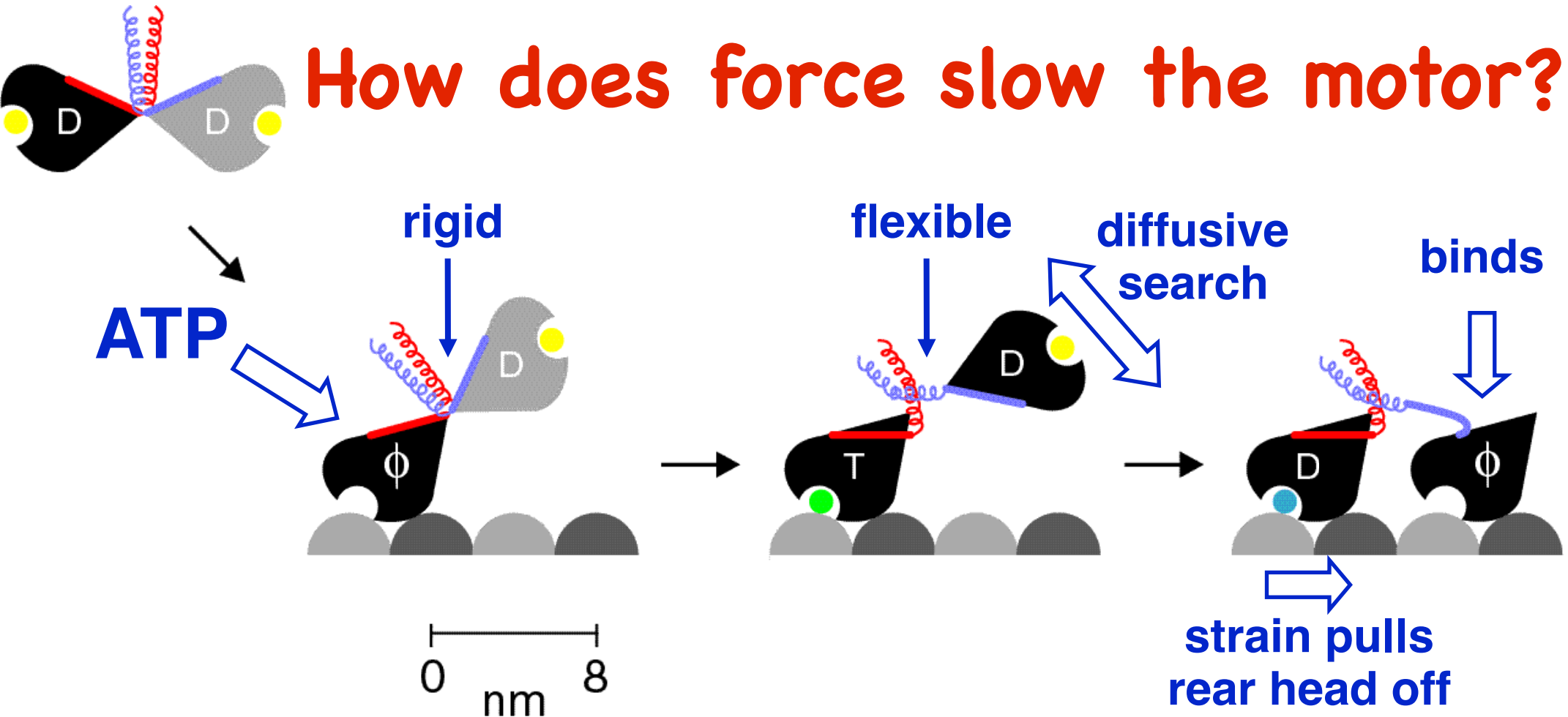


Eisenberg & Hill 1978  
Parmeggiani et al. 1999

**High processivity (kinesin does not let go)**

**⇒ at least two binding sites**

# Hand-over-hand model



# Outline

1. Single-molecule techniques can be used to study movement of purified motor proteins
2. Role of fluctuations in the motor reaction
3. **Protein friction** limits motor speed and efficiency
4. Force gating of motor proteins: active mechanical circuits underlying cell motility

# Friction ...

... resists the relative motion of two bodies in contact.



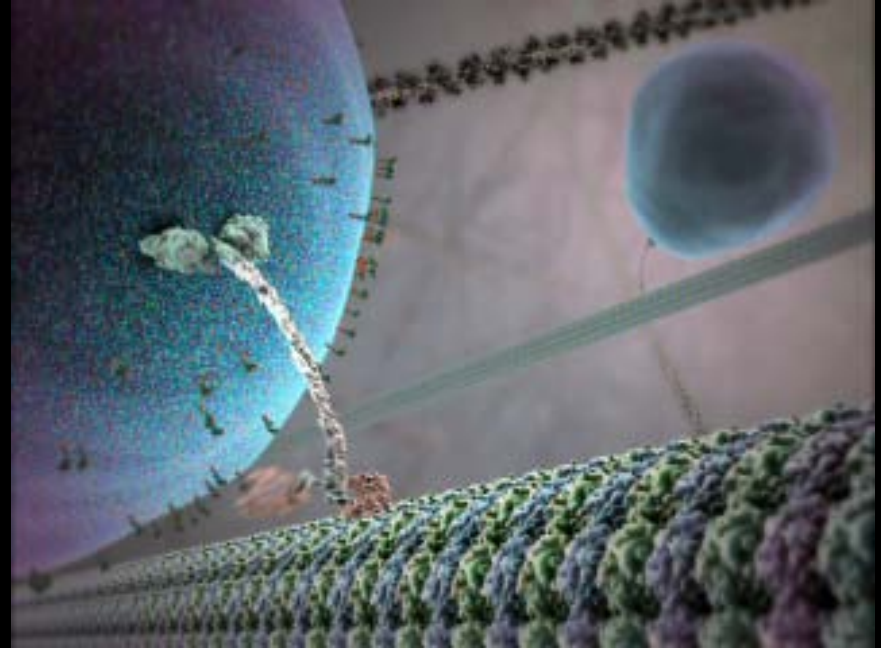
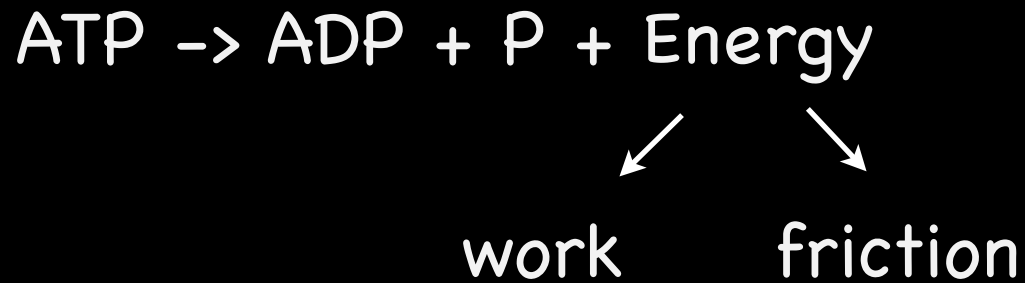
Friction arises from the force necessary to deform and break adhesive bonds.

When a bond breaks, the energy stored in its deformation is dissipated



# 1) Protein Friction ...

... is especially important for motor proteins



Harvard university

Friction forces acting on motors have not been measured

How they depend on speed are unknown

## 2) Protein Friction ...

... is related to diffusion



Diffusion

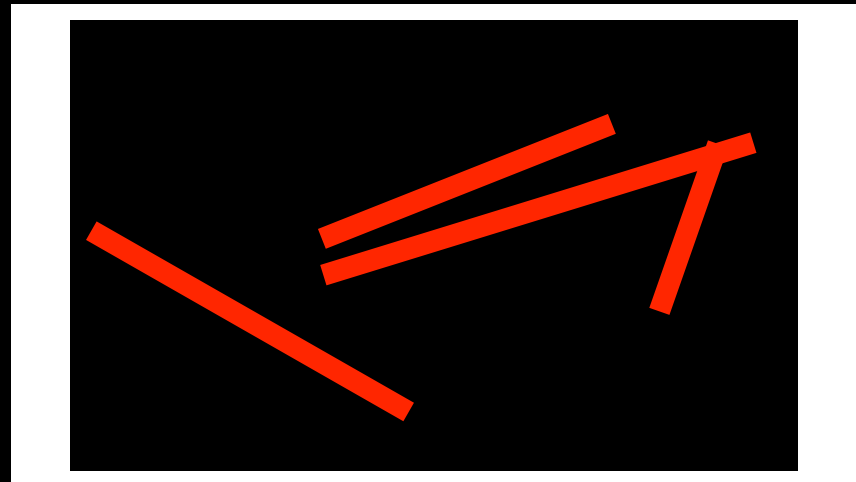
$$D = \frac{k_B T}{\gamma}$$

$$F_{friction} = -\gamma v$$

Friction

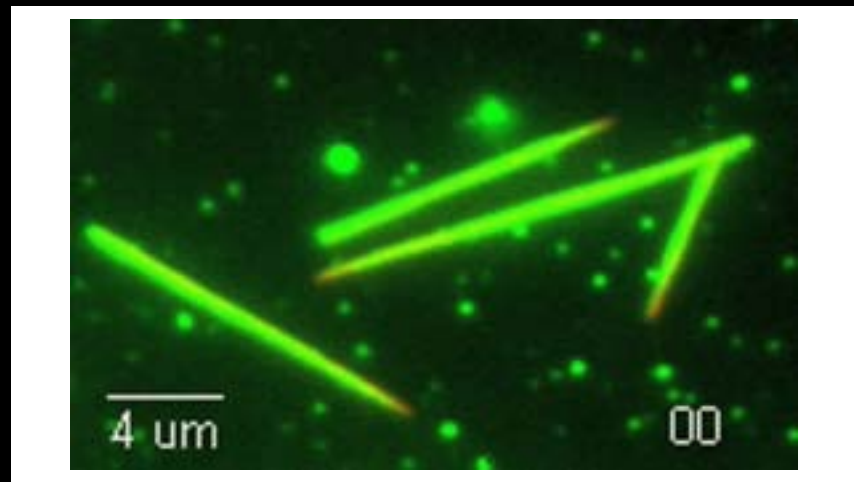


The budding yeast kinesin-8 (Kip3p) is a model system to study protein friction



Varga et. al 2006

The budding yeast kinesin-8 (Kip3p) is a model system to study protein friction

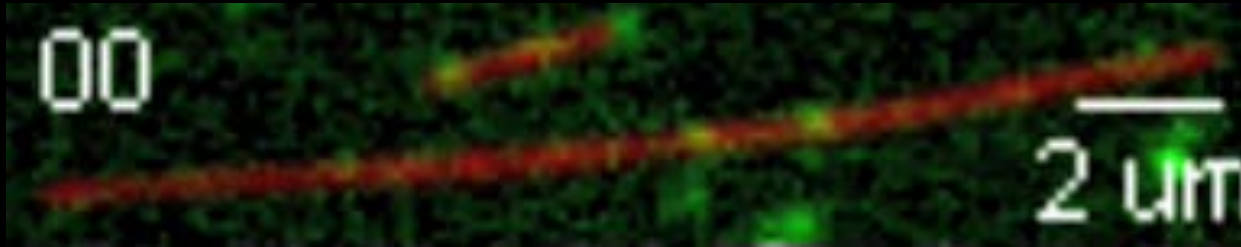


Varga et. al 2006

Microtubule depolymerase

With key role in microtubule length regulation

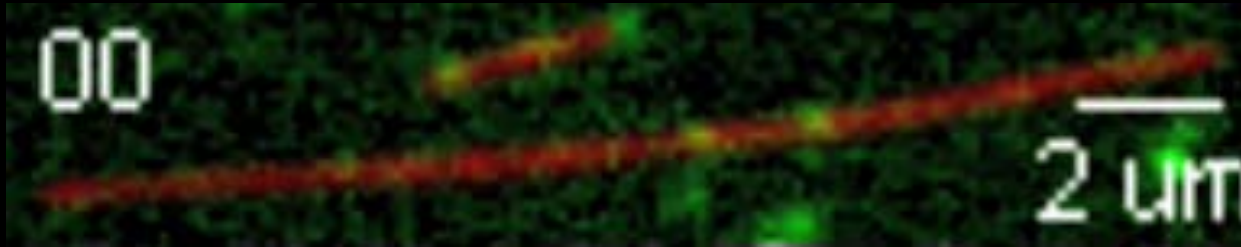
In ATP: Highly processive plus end directed motor



$$v = 3 \mu\text{m}/\text{min}$$

Varga et. al 2006

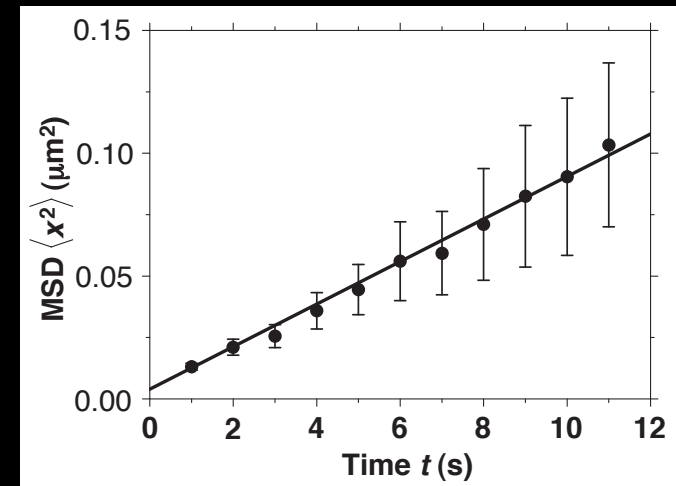
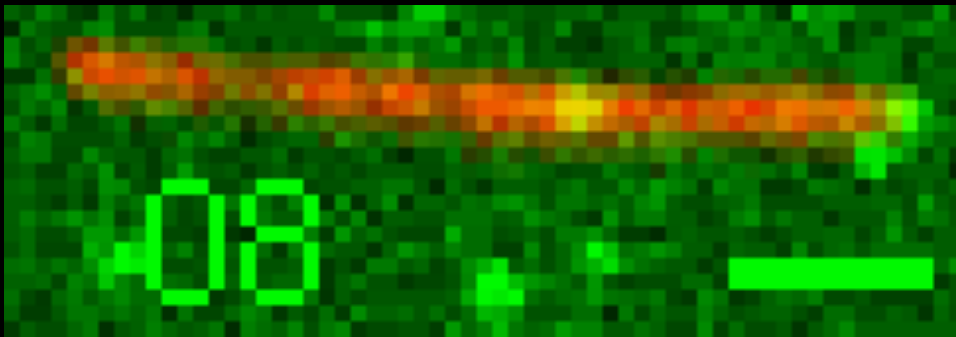
In ATP: Highly processive plus end directed motor



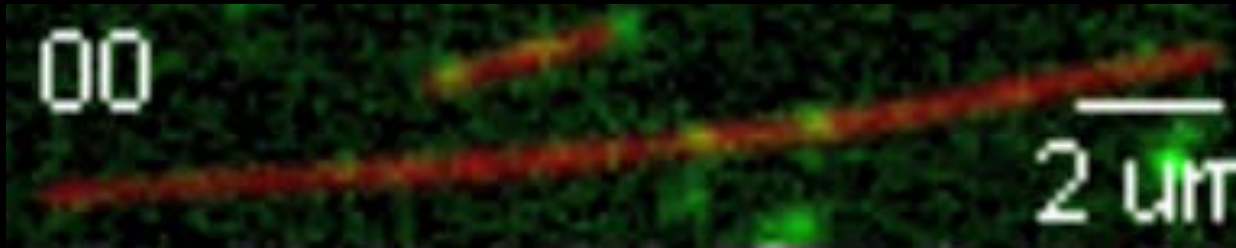
$$v = 3 \mu\text{m}/\text{min}$$

Varga et. al 2006

In ADP: Kip3p diffuses on microtubules



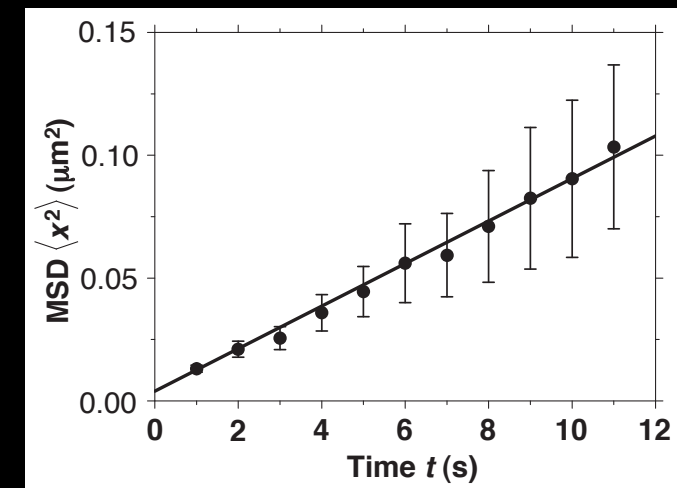
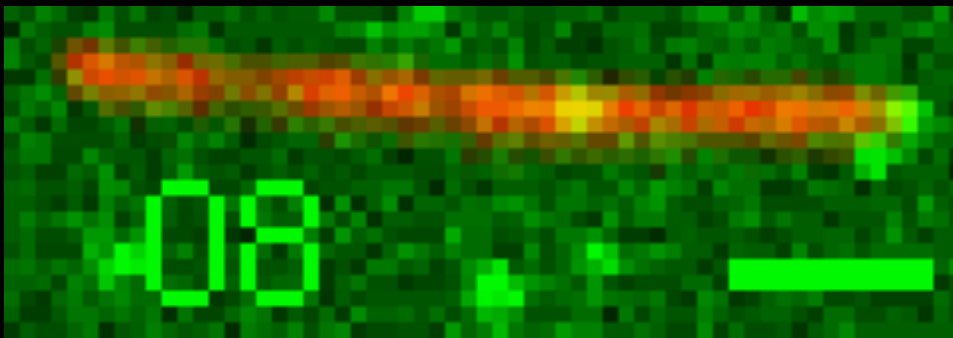
In ATP: Highly processive plus end directed motor



$$v = 3 \mu\text{m}/\text{min}$$

Varga et. al 2006

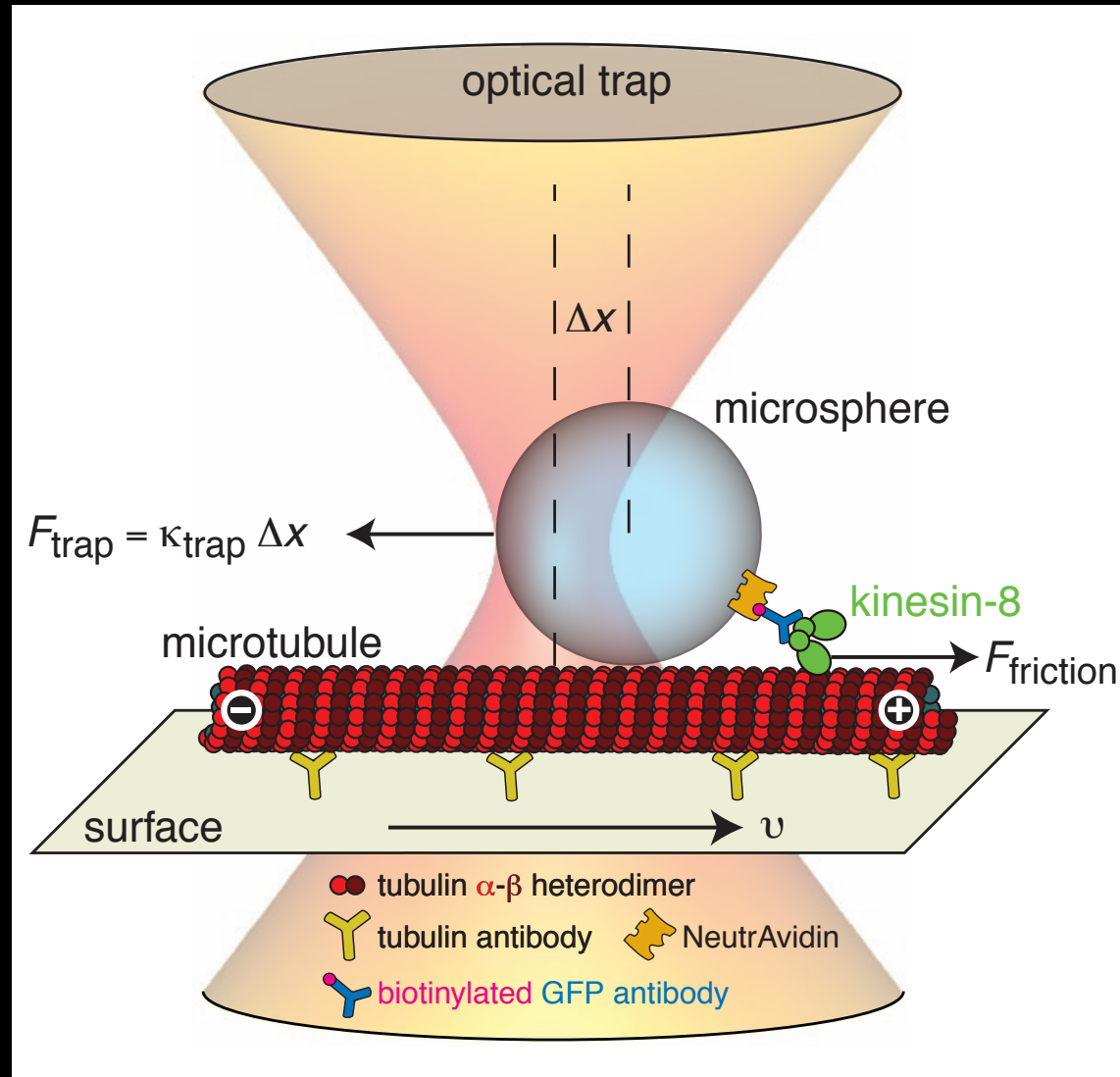
In ADP: Kip3p diffuses on microtubules



$$\gamma = \frac{k_B T}{D} \quad \gamma = 0.95 \pm 0.11 \mu\text{Ns}/\text{m}$$

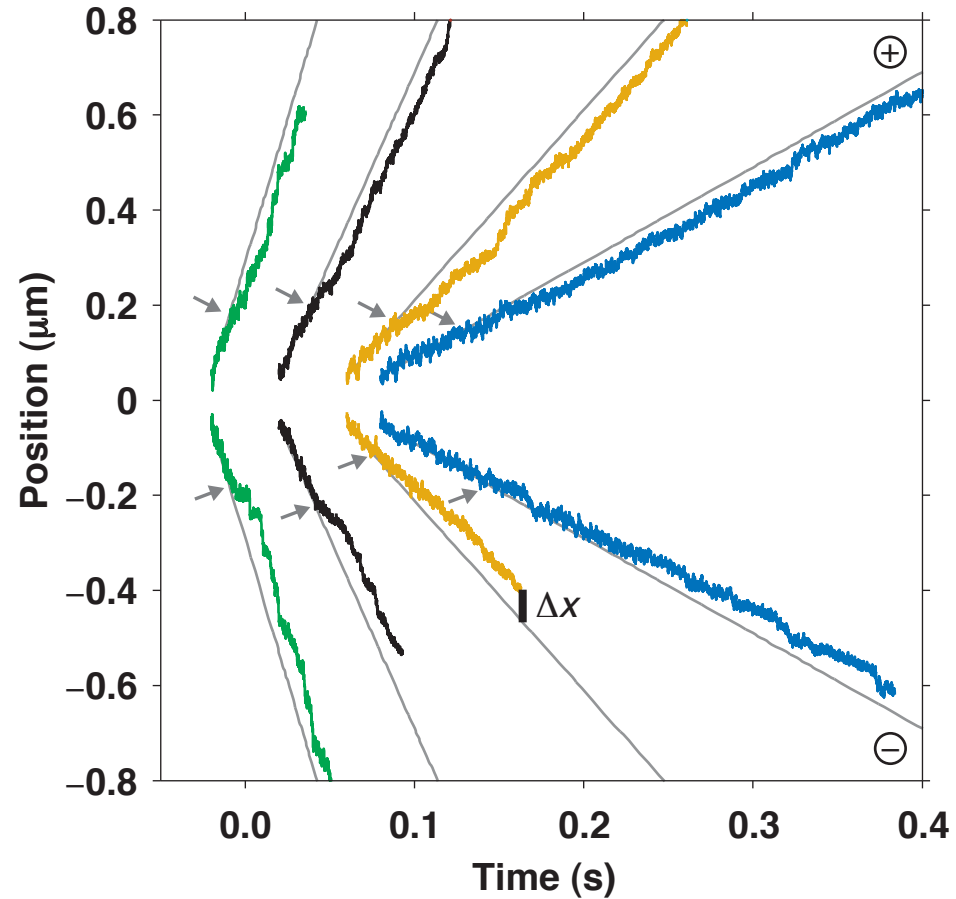
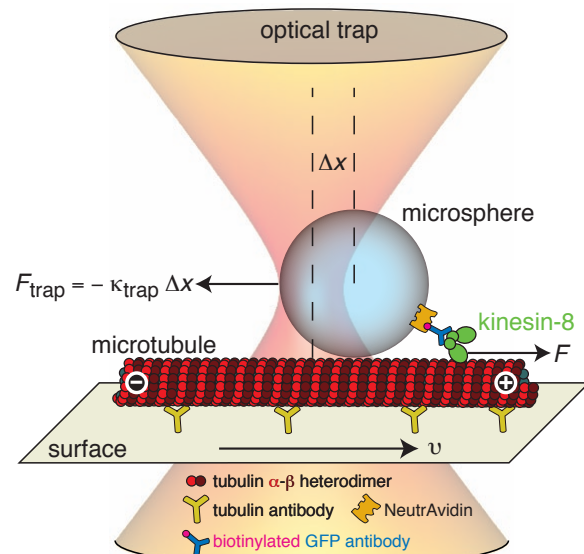
$$v \approx 1 \mu\text{m}/\text{s} \Rightarrow F = \gamma v \approx 1 \text{ pN}$$

# The friction measurement:

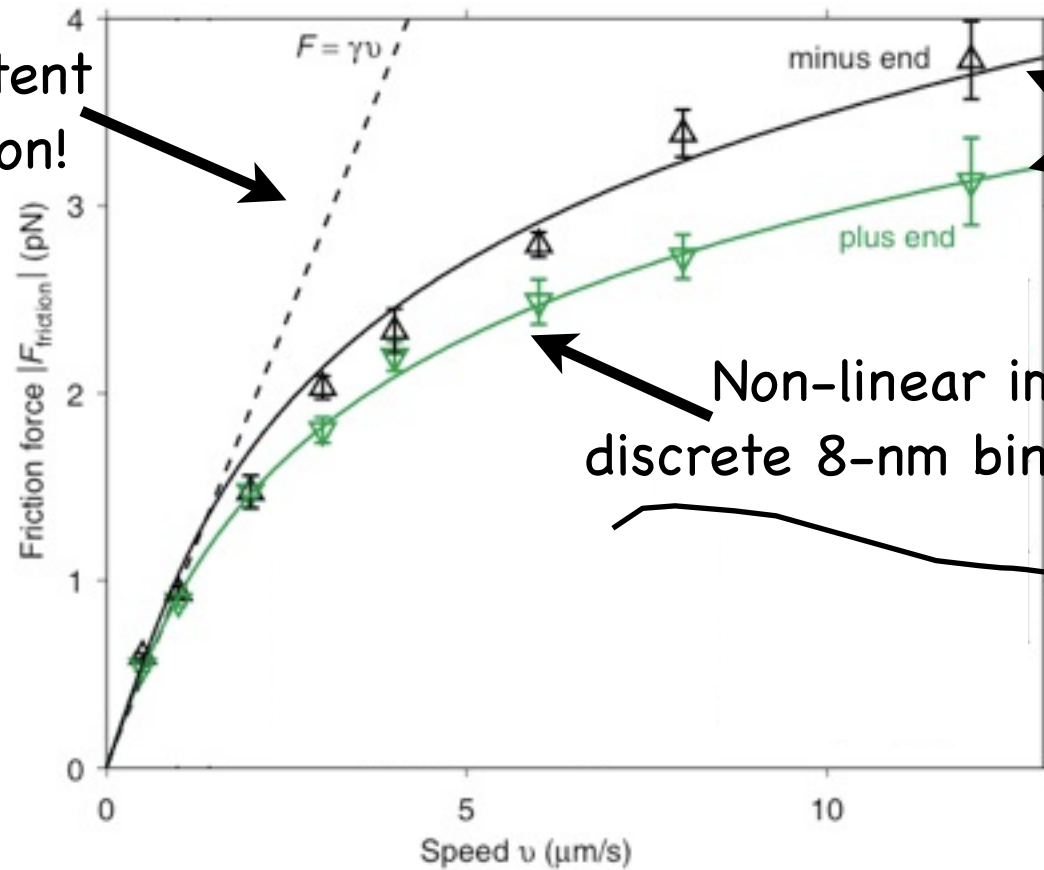




# Optical tweezers can measure friction force



# Kinesin-8 has non-linear protein friction



Slope consistent with diffusion!

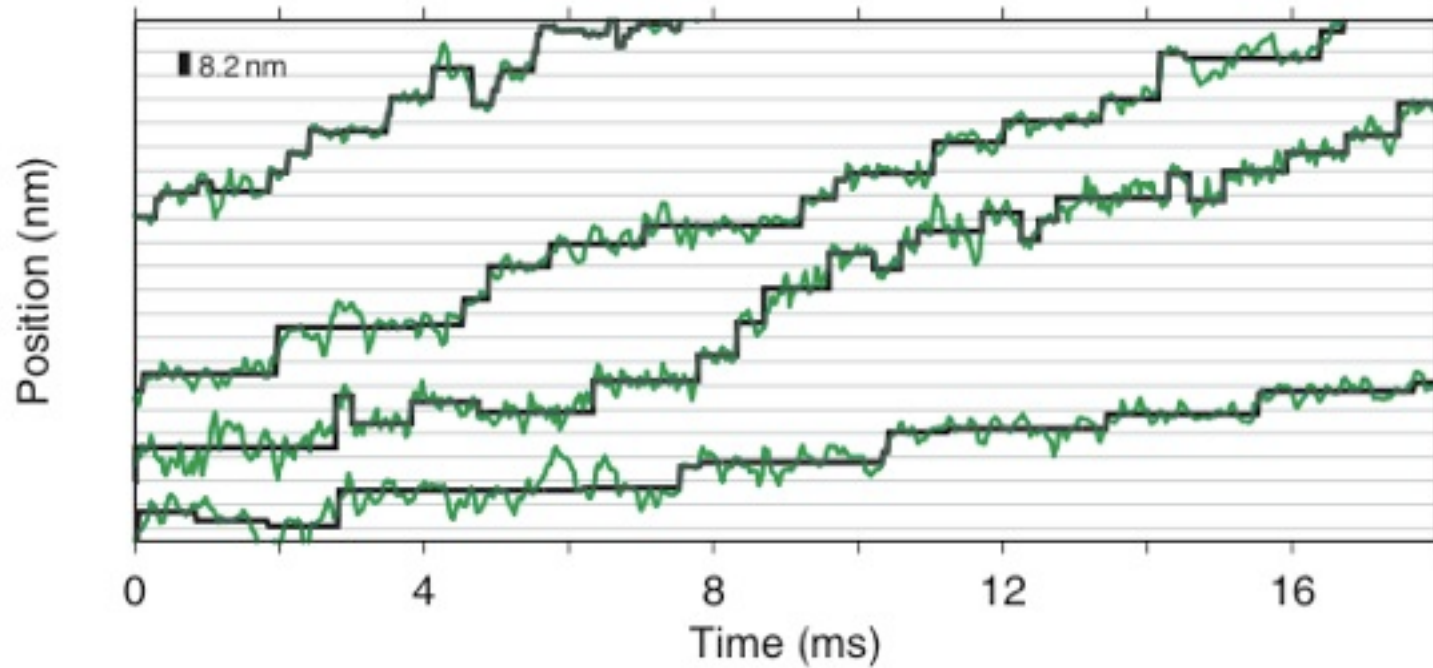
-> big bead is not contributing to the friction

-> consistent with being close to thermal equilibrium

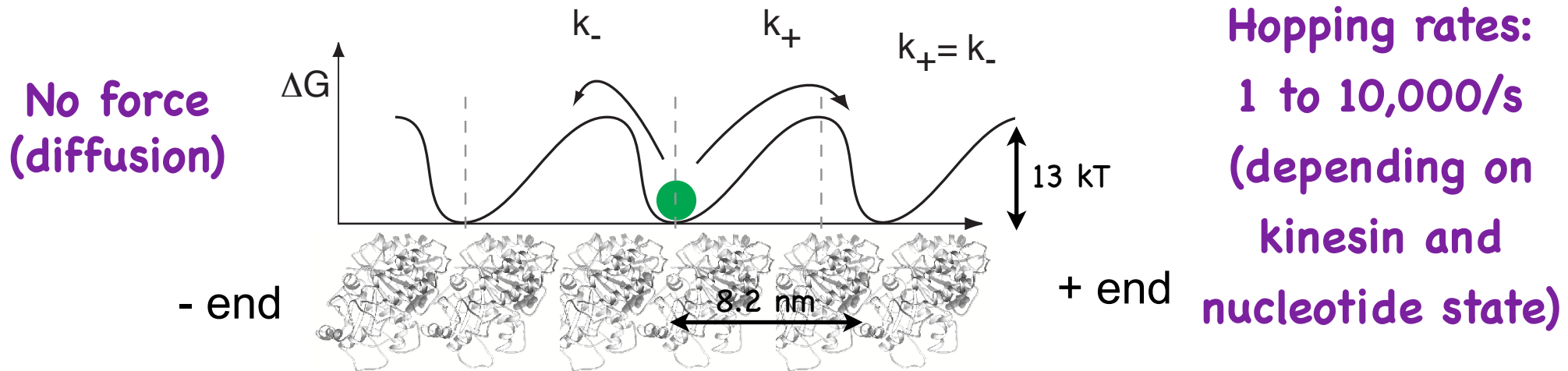
Non-linear implies discrete 8-nm binding sites!

Asymmetry!

# Frictional slipping is in 8-nm steps

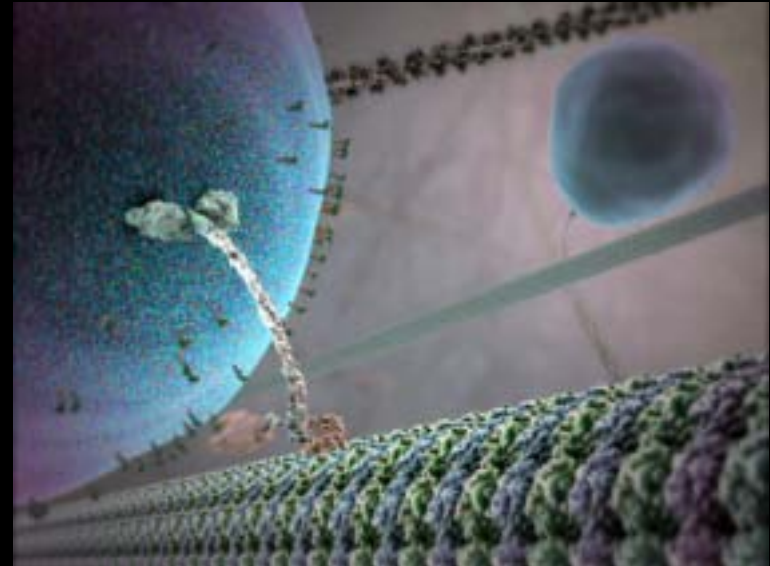
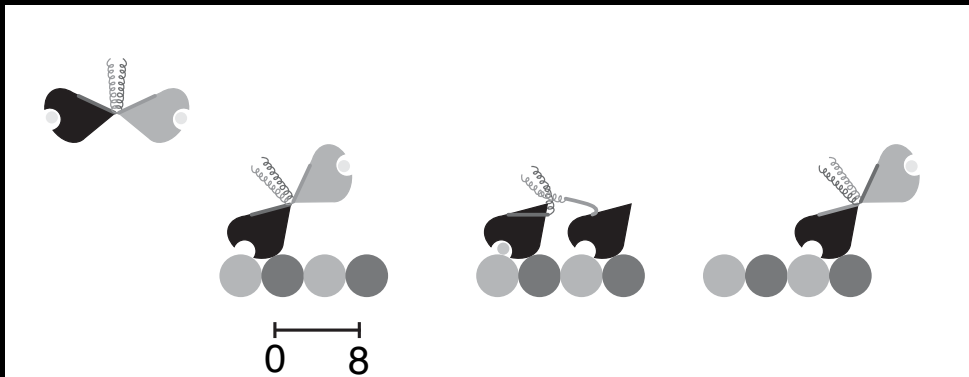


# Diffusion and friction can be described as motion in a periodic potential



How does the measured friction limit the motility of kinesin when it is driven by ATP-hydrolysis?

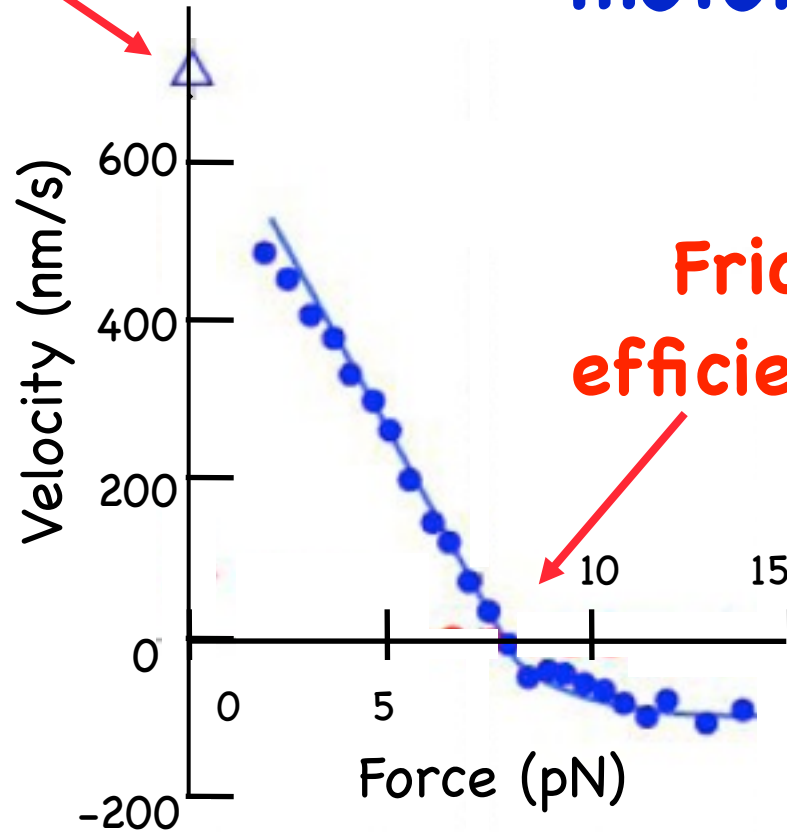
# Picture of a motor as a force generator limited by a damping element



sticky feet

# Friction helps to understand the force-velocity curve of motor proteins

Friction limits maximum speed

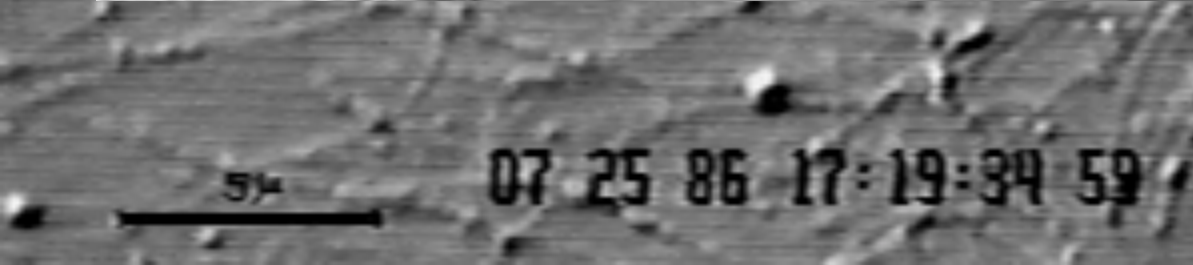
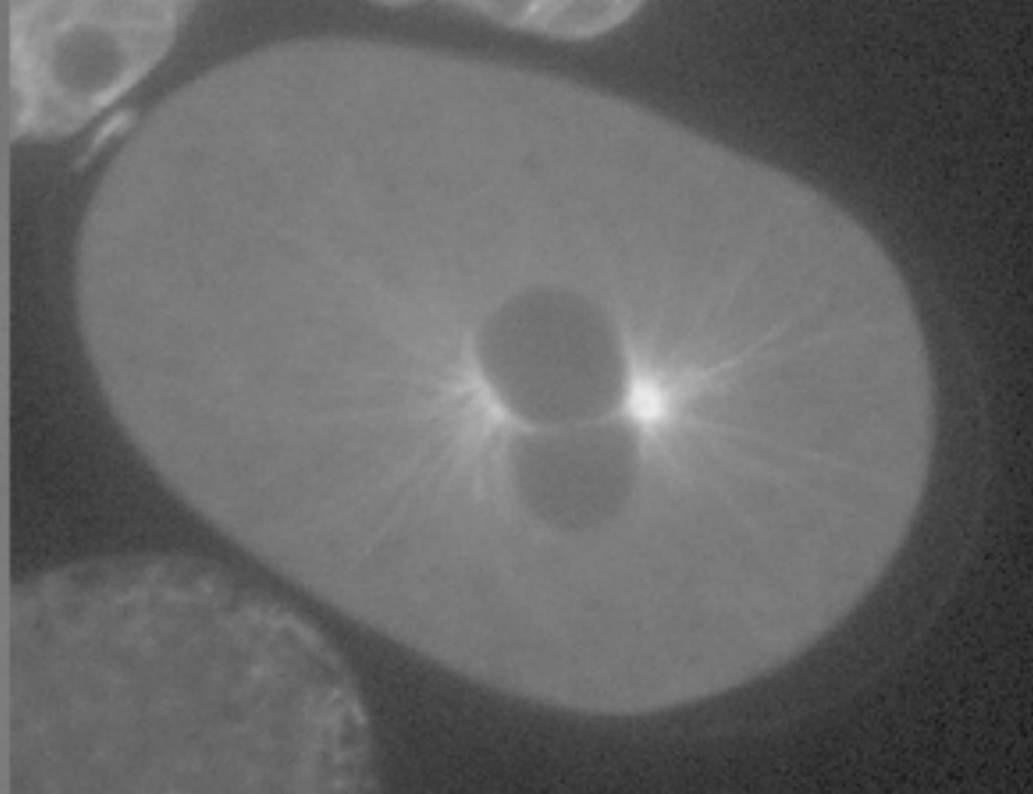


Friction limits efficiency (slipping)

But ... this is boring!

Carter & Cross 2005

# Mechanical switching and oscillations in cells

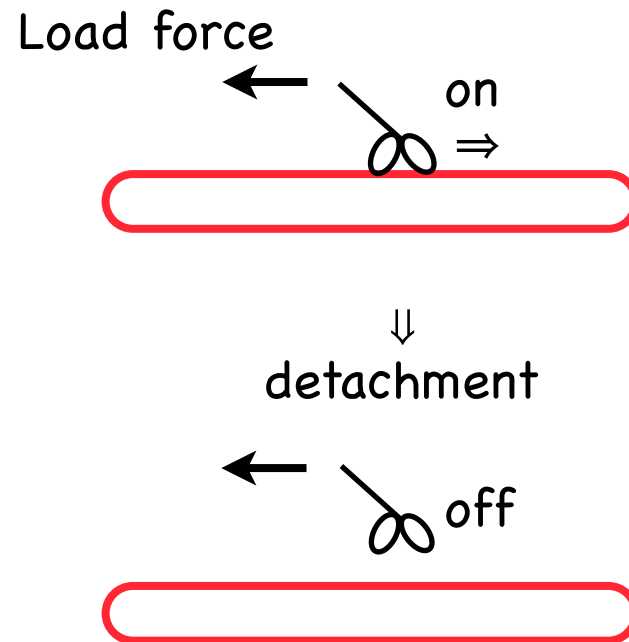




# Outline

1. Single-molecule techniques can be used to study movement of purified motor proteins
2. Role of fluctuations in the motor reaction
3. Protein friction limits motor speed and efficiency
4. **Force gating of motor proteins:** active mechanical circuits underlying cell motility

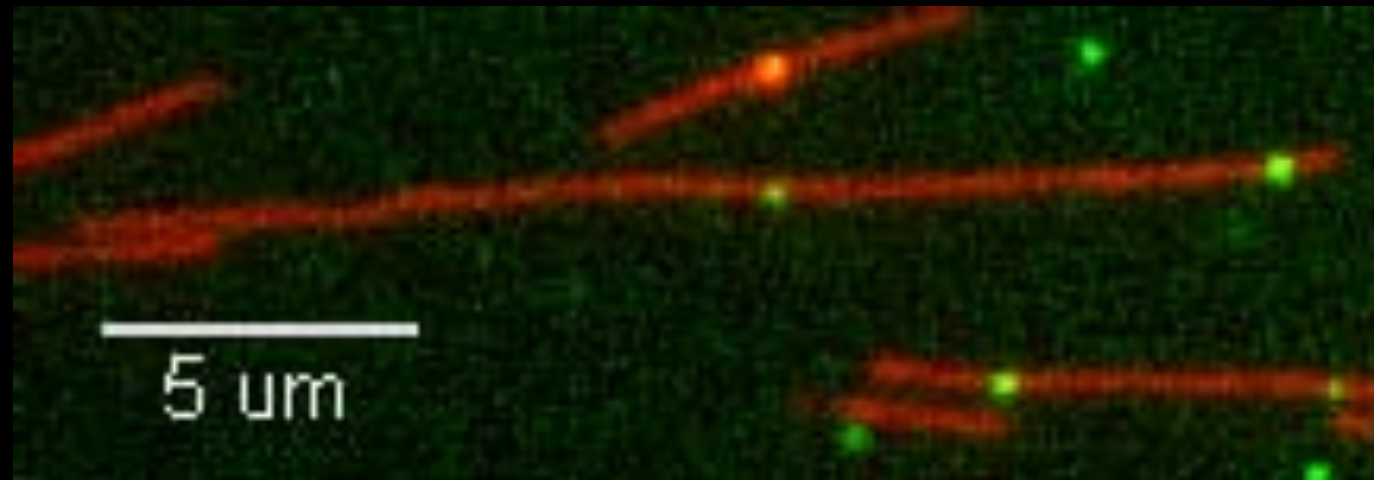
# Force-accelerated detachment of motors



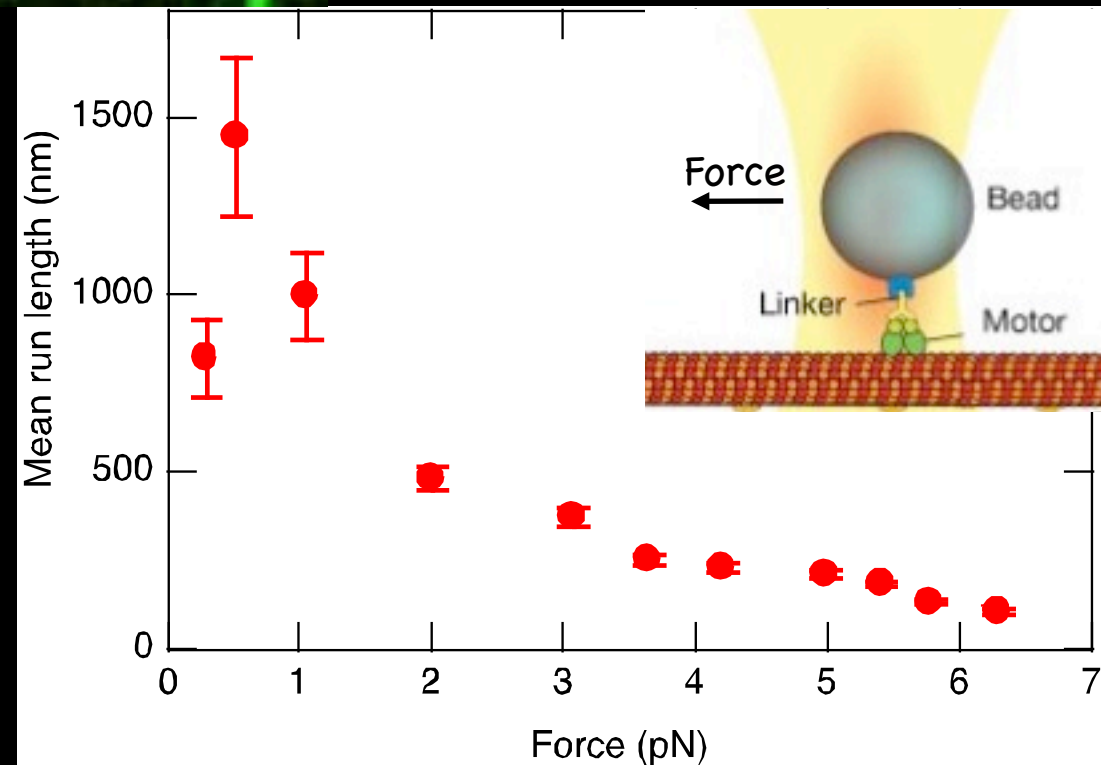
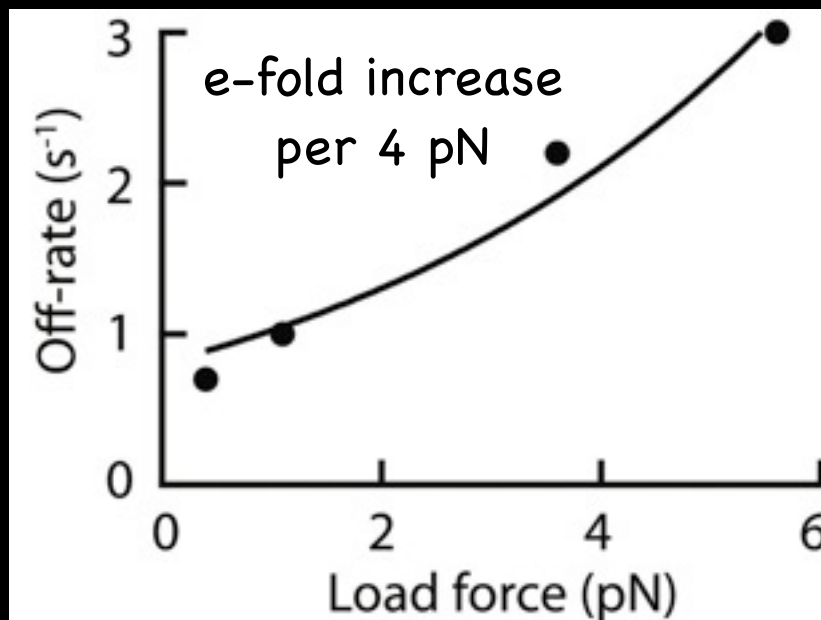
Can give rise to **negative friction**

Can lead to **switching, oscillations!**

# Load-accelerated dissociation of kinesin-1



Schnitzer et al. 2000

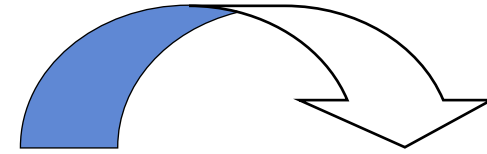


# Load-accelerated dissociation

→ Positive feedback

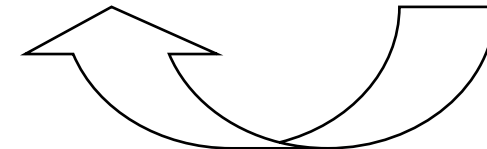


More force generated



Motor binds

Force/bound motor decreases



↓ Load-accelerated detachment

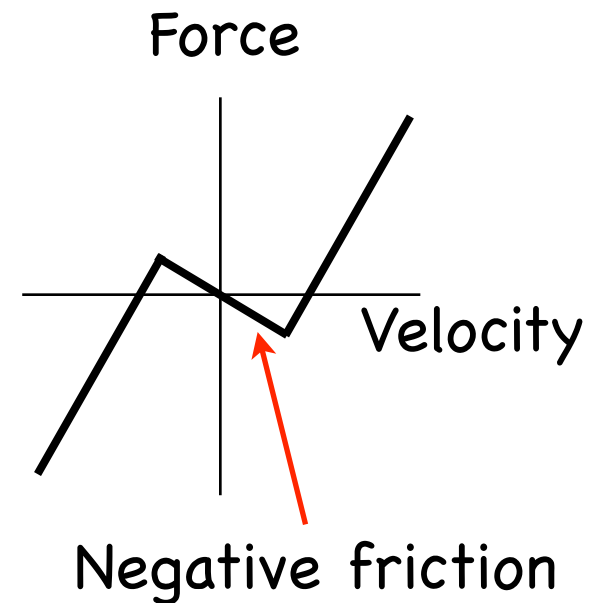
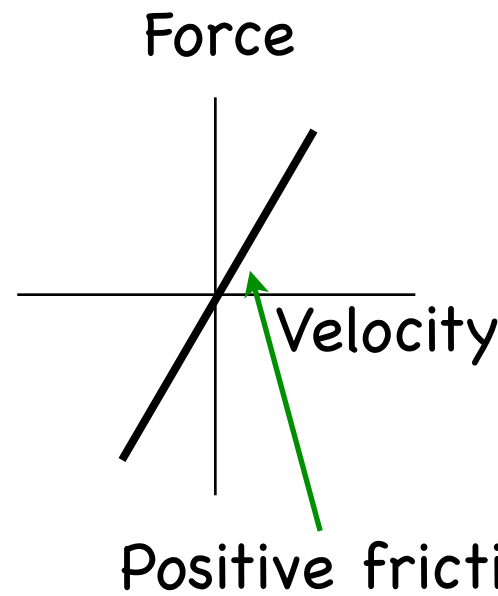
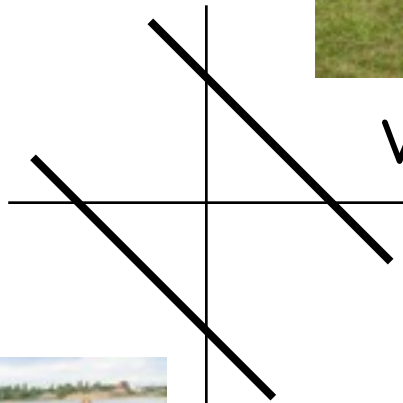
# Load-accelerated dissociation

→ Negative friction

Load force



Velocity

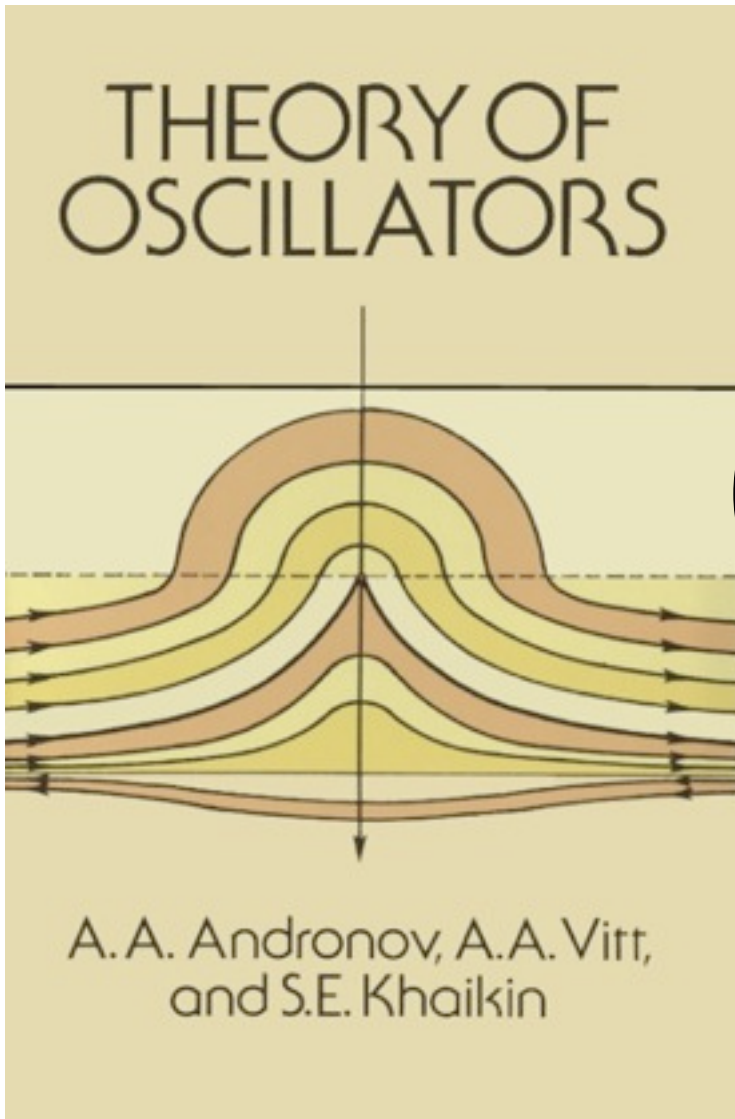


**Mechanical transistor!**

switching, oscillations

(Julicher & Prost, 1995,1997)

# Theory of dynamical systems



First edition, ~1930

What do you need for a self-sustained, stable oscillation?

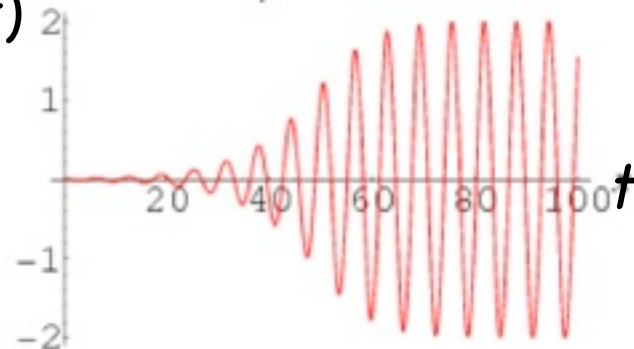
Negative friction

Non-linearity

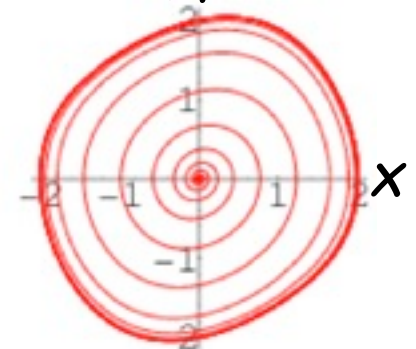
$$m \frac{d^2}{dt^2} x + \gamma \frac{d}{dt} x + kx = 0$$

$$m \frac{d^2}{dt^2} x - \varepsilon (A - x^2) \frac{d}{dt} x + kx = 0$$

$x(t)$



$dx / dt$



# The flagellar beat

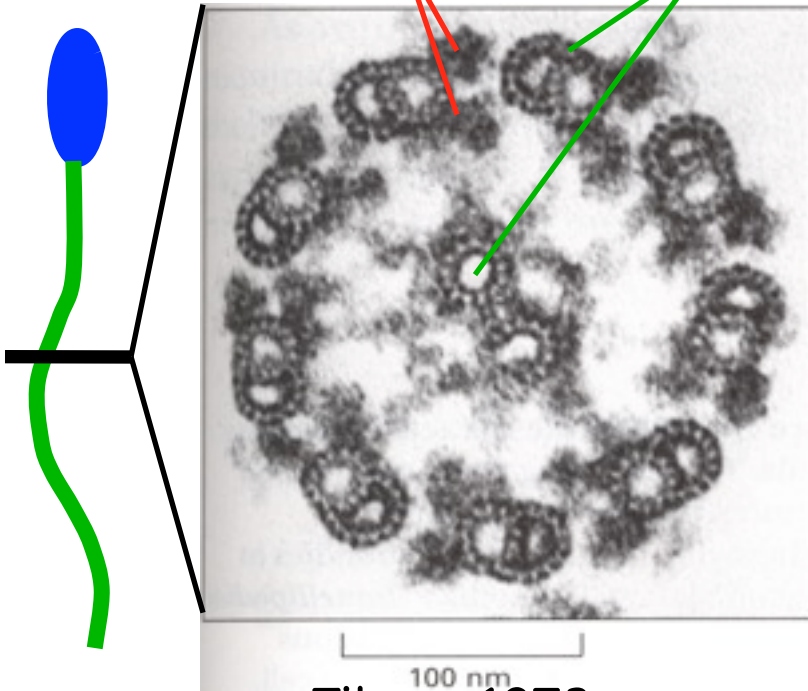


Bull sperm,  $L = 58 \mu\text{m}$ ,  $f = 21 \text{ Hz}$ ,  $22 \text{ }^\circ\text{C}$

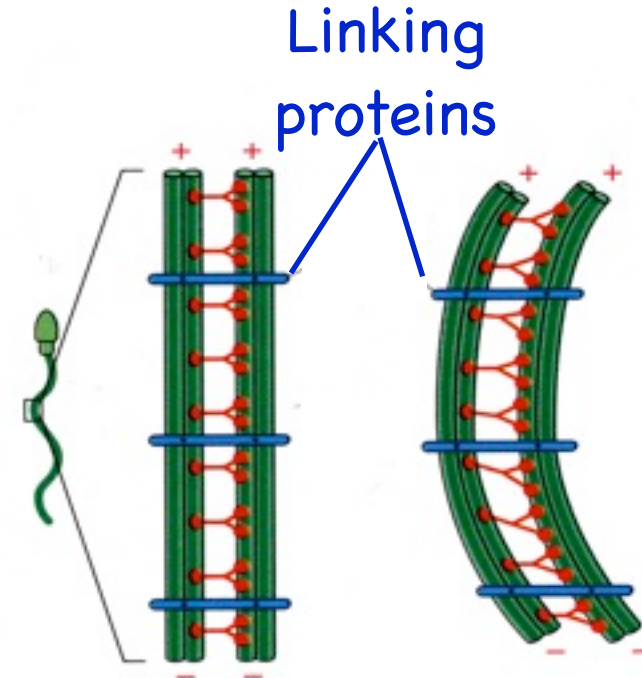
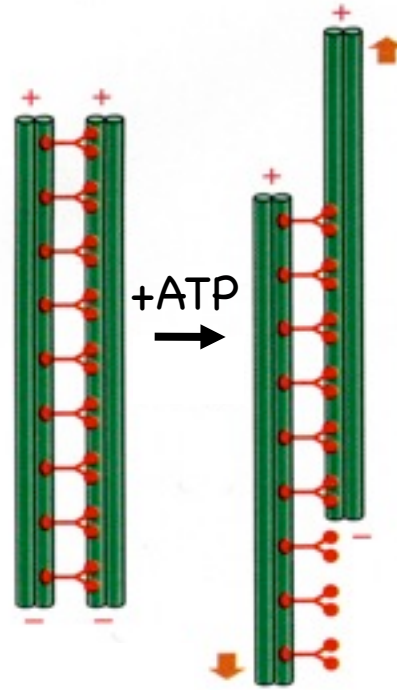
Riedel-Kruse,  
Hilfinger,  
Howard &  
Julicher 2007

# Conversion of sliding to bending

Dyneins Microtubules



Tilney, 1973



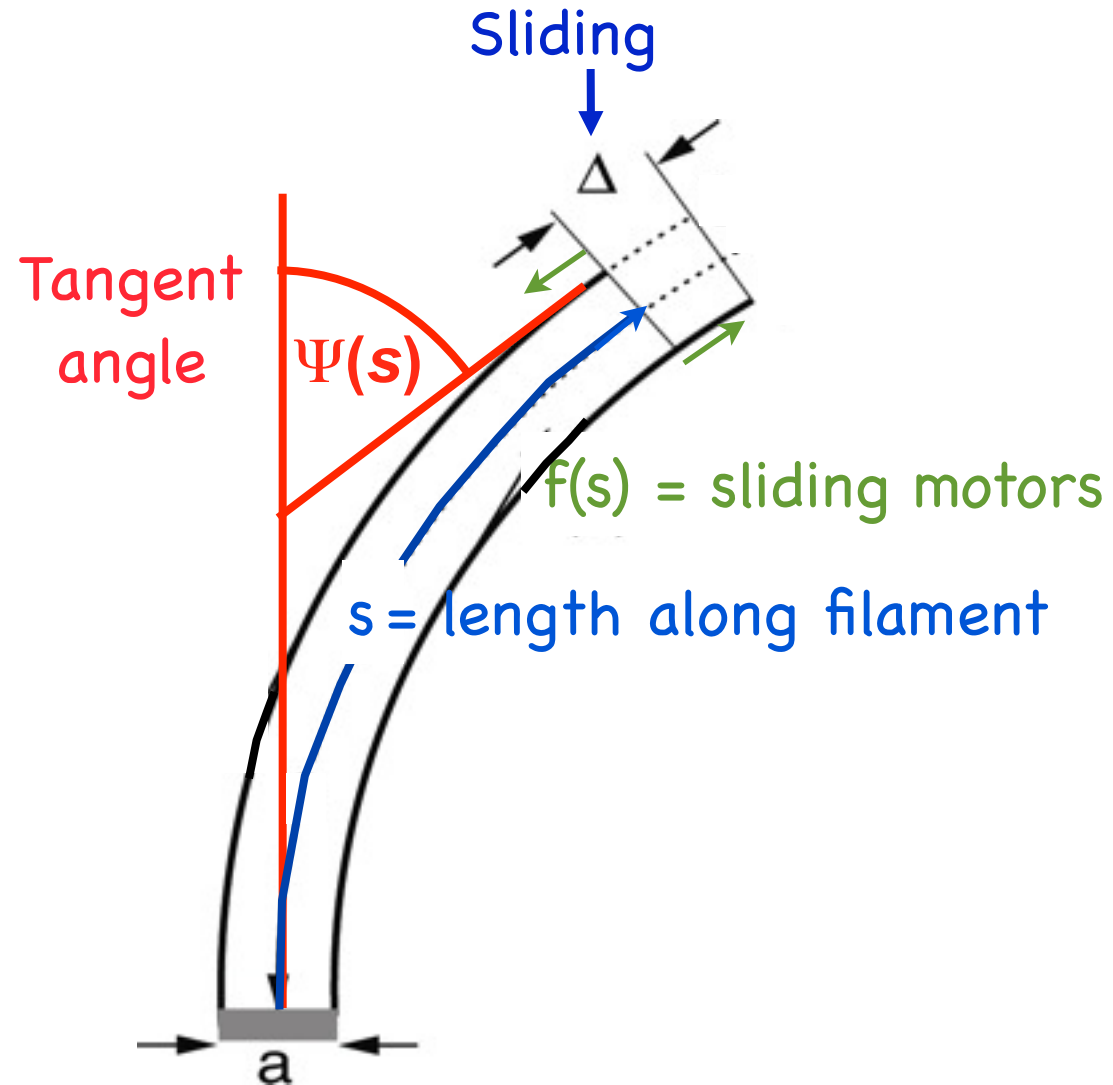
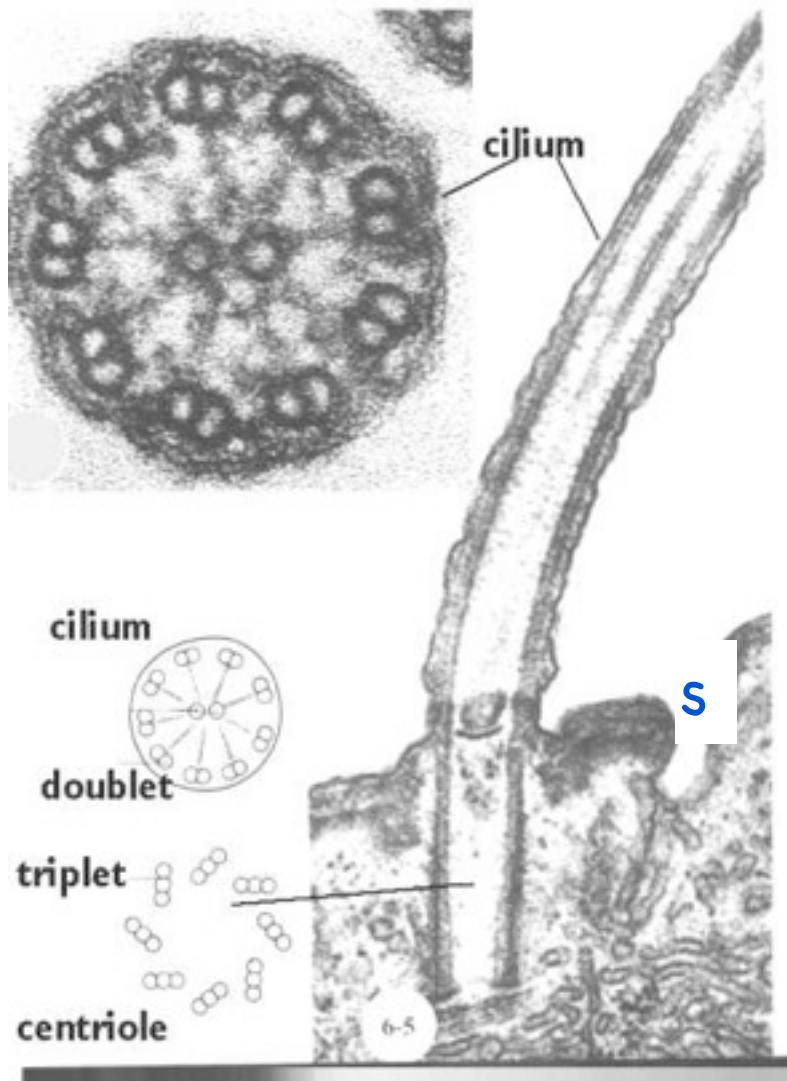
Alberts et al. Molecular Biology of the Cell

Two types of coordination

- across the section
- along the length



# Bending and sliding



Gwen Childs, U. Arkansas

$$\Delta(s,t) = a \cdot \psi(s,t)$$

# Flagellar oscillator

Oscillation requires

1. Negative friction (to supply energy) - load-accelerated detachment
2. Inertial term (delay) - delay of detachment
3. Elastic term (return to the center) - stiffness of the microtubules

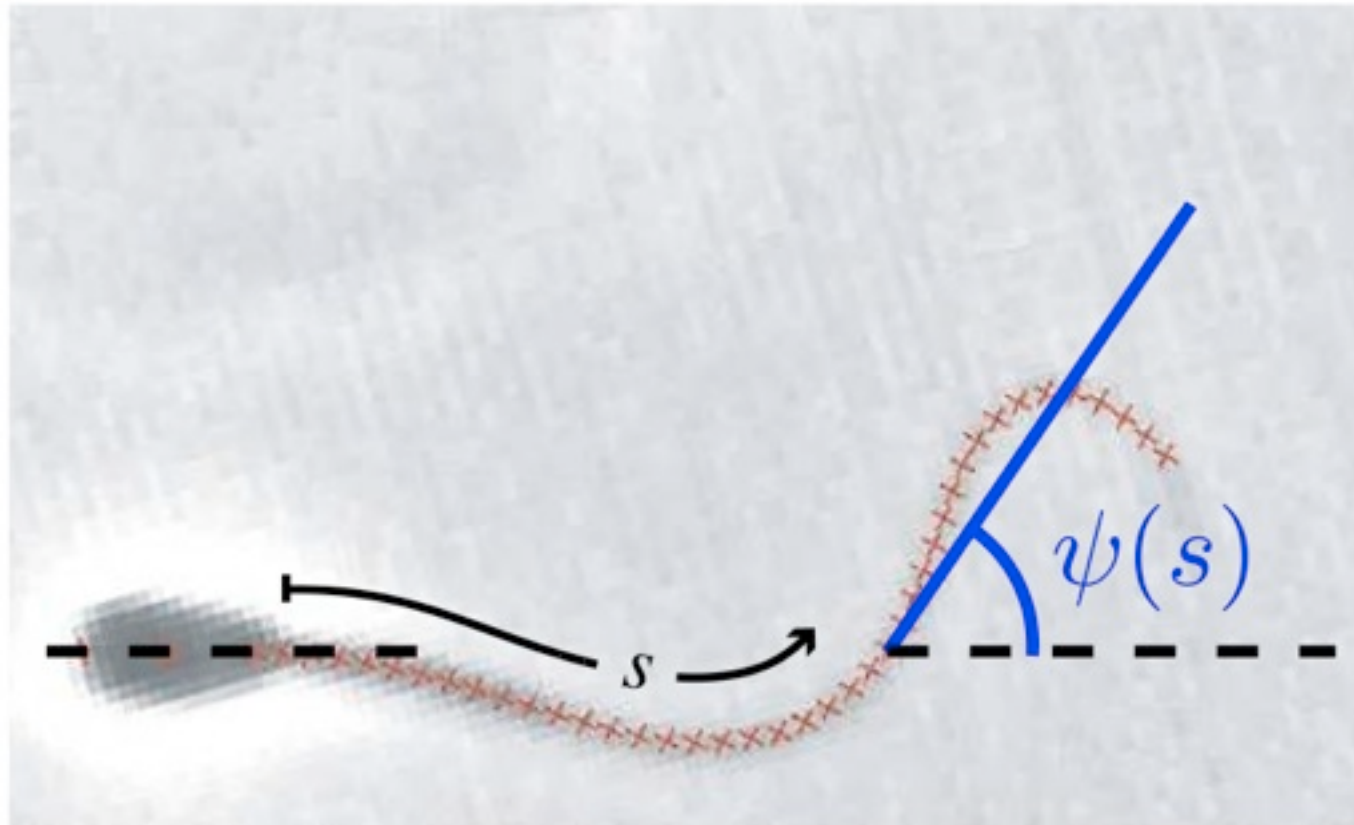


“Sperm equation”

$$a^2 \chi \frac{d^2 \tilde{\psi}}{ds^2}(s) = i\omega \xi_{\perp} \tilde{\psi}(s) + \kappa \frac{d^4 \tilde{\psi}}{ds^4}(s)$$

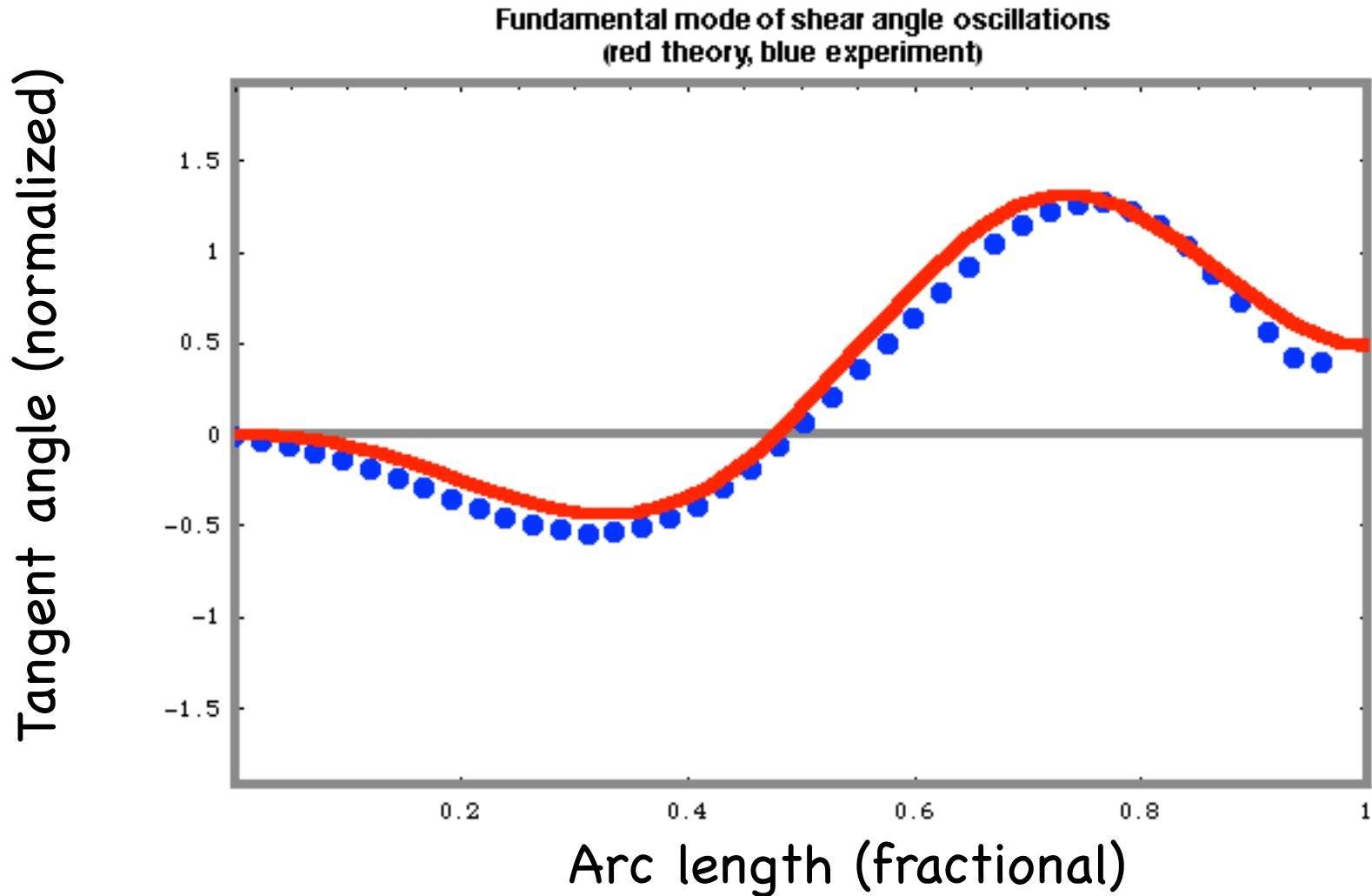
Boundary conditions      no external forces or torques (all internal)

# Determination of beat shape

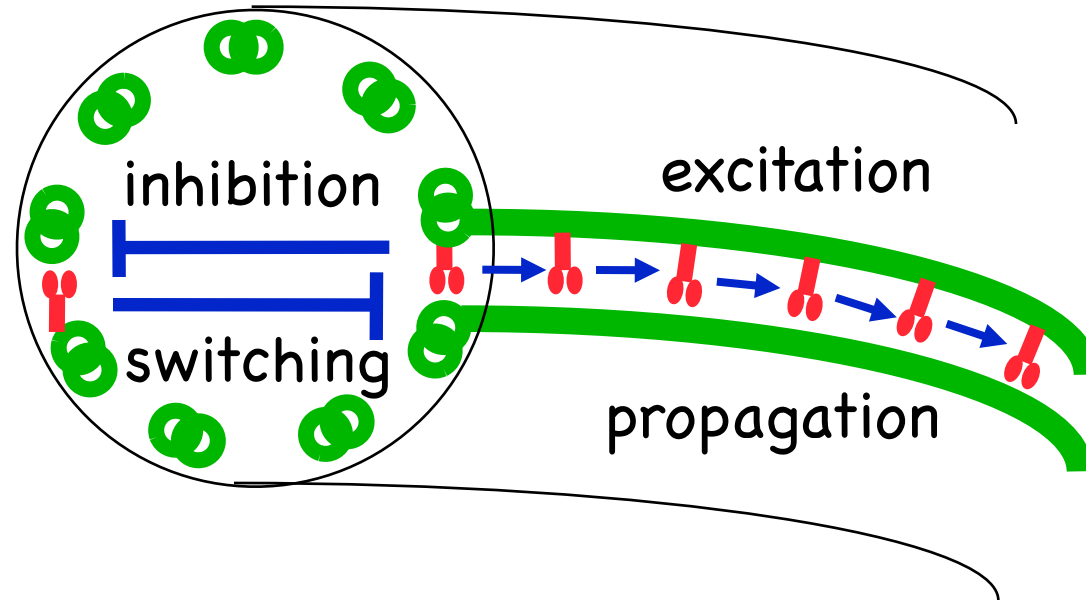


# Agreement between theory and experiment

Clamped head



# Mechanical signaling network in the axoneme





## Advantages of mechanical signaling over chemical signaling

1. can travel over large distances
2. signals move at the speed of sound (in the material)
3. feedback leads to coordination, switching and oscillation

# Summary

1. **Single-molecule techniques** can be used to study movement of purified motor proteins
2. Role of **fluctuations** in the motor reaction
3. **Protein friction** limits motor speed and efficiency
4. **Force gating of motor proteins:** active mechanical circuits underlying cell motility

mpipks



Andy Hilfinger



Frank Jülicher



Volker Bormuth



Jacques Pecreaux



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