TRESURES NEAR THE ABSOLUTE ZERO Bose-Einstein Condensates and more

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PLAN

- 1) A quick summary of laser cooling of atoms to quantum degeneracy
- 2) Bose-Einstein Condensation in an optical trap for neutral atoms at TIFR
- 3) A short glimpse at some features of magnetic and optical trap BECs
- Physics of atoms near the absolute zero: some examples with Bosons and Fermions
- 5) The larger picture

Bose-Einstein Condensation in TIFR

Some features that has attracted attention:

- 1) First BEC in India and the only one at present
- 2) One of the four or five optical trap BECs (spinor condensate) around the world
- Perhaps the largest and the fastest condensing optical trap BEC (1 second). Might cross 10⁵ atoms with some optimization. (typical optical trap BEC is 10⁴ to 3x10⁴)
- 4) Fastest condensations in optical lattices as well (1 s) with >50,000 atoms

Bose-Einstein Condensation

Substantial accumulation in the the lowest energy state of a multi-particle system at a temperature above the absolute zero

Einstein to Ehrenfest (1925):

'From a certain temperature onwards molecules "condense" without attractive forces, that is, they accumulate at zero velocity. The theory is pretty, but is there also some truth to it?'

How did he arrive at this conclusion?

Guartentheorie des inatomign idealer gases Zweite Abhandlung. in decen Brichter (XXII 1924. J.261), In einer neulichverschlenen Abhandlung wurde unter Anwendering einer von Herr D. Bose zur Ableitung der Hausk' sehen Strahlungsformel erdachten Methode ine Theorie des, "Entertung" idealer Guse ungegeben.



Quantentheorie des einatomigen idealen Gases. Zweite Abhandlung.

Von A. EINSTEIN.

In einer neulich in diesen Berichten (XXII 1924, S. 261) erschienenen Abhandlung wurde unter Anwendung einer von Hrn. D. Bose zur Ableitung der PLANCKSchen Strahlungsformel erdachten Methode eine Theorie der »Entartung« idealer Gase angegeben. Das Interesse dieser Theorie liegt darin, daß sie auf die Hypothese einer weitgehenden formalen Verwandtschaft zwischen Strahlung und Gas gegründet ist. Nach dieser Theorie weicht das entartete Gas von dem Gas der mechanischen Statistik in analoger Weise ab wie die StrahEinstein's papers in 1924 and 1925:

E's footnote to Bose's paper: "In my opinion Bose's derivation signifies an important advance. The method used here gives the quantum theory of an ideal gas as I will work out elsewhere."

First paper (1924): The phase space of an elementary object (here of a monatomic gas and in Bose's paper of a light quantum), associated with a given three-dimensional volume is divided into cells of volume h³...

Quantentheorie des einatomigen idealen Gases. Zweite Abhandlung.

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$$\frac{1}{\exp\frac{h\omega}{kT} - 1} \rightarrow \frac{1}{\exp\frac{\left(\varepsilon_i - \mu\right)}{kT} - 1}$$

 $\mu \approx -kT / N$

Second paper in early 1925

$$\frac{1}{\exp\frac{\left(\varepsilon_{i}-\mu\right)}{kT}-1}; \quad \mu \approx -kT/N$$

$$\frac{1}{\exp\frac{\left(\varepsilon_{i}-\mu\right)}{kT}} \quad \text{for } \varepsilon \approx 0 \rightarrow \frac{1}{\exp\frac{\left(\varepsilon_{i}+kT/N\right)}{kT}} \approx \frac{1}{1+\frac{\varepsilon_{i}}{kT}+\frac{1}{N}} \approx \frac{1}{1+O(0)} \approx 1$$

The factor is 1 for ALL low energy states without the 'minus 1' of Planck's law: Equal occupation in all low energy states near ground state

$$\frac{1}{\exp\frac{\left(\varepsilon_{i}-\mu\right)}{kT}-1}\approx\frac{1}{\exp\frac{\left(\varepsilon_{i}+kT/N\right)}{kT}-1}\approx\frac{1}{1+(1/N)-1}\approx N \text{ for } \varepsilon=0$$

$$\frac{1}{1+(1/N)-1}\approx\frac{1}{kT}\approx\frac{1}{\exp\frac{\left(\varepsilon_{i}+kT/N\right)}{kT}-1}\approx\frac{1}{1+(\varepsilon_{i}/kT)+(1/N)-1}\approx\frac{kT}{\varepsilon_{i}} \text{ for } \varepsilon_{i}\neq0$$

Most atoms (~N) in ground states at finite temperature!

Requirement for BEC

Inter-particle separation < Quantum de Broglie wavelength

Phase space density

$$n\lambda^3 > 1$$

n = N / V Atom number density

$$\lambda = \frac{h}{mv} \longrightarrow \lambda \approx \frac{h}{\sqrt{2k_B Tm}} \quad (\text{since } mv^2 \approx k_B T)$$

De Broglie wavelength

0.02 nm @ 300 K, 60 nm @ 30 µK, 0.3 microns @ 1 µK

Inter-particle separation

 $1/n^{1/3} \approx 2 \text{ microns}(a) \ 10^{11} \text{ atoms/cc}, \quad 0.2 \text{ microns}(a) \ 10^{14} \text{ atoms/cc}$

Magneto-optical trap: $n\lambda^3 = 10^{-6}$

ENERGY SCALES:

	Frequency	Equivalent temperature
Thermal atom		300 K
Electronic levels	>3x10 ¹⁴	15000 K
Single photon recoil		0.1 – 0.3 µK
Line-width	6 MHz	300 µK
Hyperfine	1 GHz	50 mK
Harmonic trap	<1 kHz	<50 nK
BEC		200-1000 nK



Velocity-dependent force on atoms: Friction Damping





Fluorescence Image by CCD



Number of atoms: $10^6 - 10^7$ Density ~ 10^{10} atoms/cc Temperature : <100 micro-K

Inter-particle separation: 2 microns De Broglie wavelength: 40 nm

 $n\lambda^3 \approx 10^{10} \operatorname{atomc/cc} \cdot (45 \, nm)^3 \approx 10^{-6}$

Cloud size ~ 1 mm

To reach 1

 $n\lambda^3 \approx 10^{14} \operatorname{atomc/cc} \cdot (300 \, nm)^3 \approx 2.7$



Slow laser cooled atoms at V < 1 m/s are very good for such studies since the signal increases by up to 10^{6} compared to thermal beams

There are also spectral shift and phase changes, enhanced by similar factors. Great advantage for short range experiments.

Reflection of spin-polarized ⁸⁵Rb atoms from magnetic thin film: Measurement of short-range forces



A. K. Mohapatra and CSU, Europhys. Lett (2006), EPJD (2007)



Temperature and speeds

	Temperature	Velocity	
Thermal atom	300 K	300 m/s	Doppler cool
MOT	100 µK	15 cm/s	
MOT with forced sub- Doppler	10 µK	5 cm/s	Sub-Doppler (far detuning)
BEC	200-1000 nK	1 cm/s	Evaporation
Single photon recoil	0.1 – 0.3 µK	1 cm/s	

Last stage of cooling should avoid near-resonant light.



Optical Traps



Most BECs including the first ones in 1995 are produced in magnetic traps, and they are naturally magnetized (one spin-state), whereas an optical trap BEC (2001) is unmagnetized (general superposition or mixture of spin states). This technique of cooling is applicable to atoms with no magnetic moment, or to Fermions, and it allows optical lattice experiments as a simple extension, even in a magnetic field.

Atom in a laser field:

$$\frac{d^2 x}{dt^2} + \omega_0^2 x = \frac{e}{m_e} E(t) \to \times e \to ex^{\mathbf{r}} = \frac{\mathbf{r}}{d}$$

Response to an oscillating electric field,

$$\alpha(\omega) = \frac{e^2}{m_e(\omega_0^2 - \omega^2)}$$

Energy
$$V(r) = -d \cdot E_0 = -\frac{1}{2}\alpha(\omega)E_0^2 = -\frac{1}{2}\alpha(\omega)I(r)$$

The trapping potential follows the 'shape' of the laser beam intensity

Optical dipole trap $V(r) = -\frac{1}{2}\alpha(\omega)E_0^2 = -\frac{e^2E_0^2}{2m_e(\omega_0^2 - \omega^2)}$



Near Resonance, $V(r) \approx -\frac{e^2 E_0^2}{4m_e \omega_0 (\delta \omega)}$: $-I/\delta$

 $V(r) = -\alpha_{stat} I(r) / 2\varepsilon_0 c \quad \text{(Well below res.)}$ $V_0 = \alpha_{stat} I_0 / \varepsilon_0 c, \ I_0 = 2P / \pi w^2$



Evaporation can be done by relaxing the trap (Reduce the laser power)



Reflecting on itself gives a series of nodes and antinodes: a lattice of optical trapping potentials

Strategy

- Optical trap instead of the more popular magnetic trap: Conceptually simpler, better control, magnetic state – independent (and rare – only <u>one</u> when we planned in 2003; now about 5)
- 2. Plan for very large number of atoms in the MOT to start with : possibility to start with high density
- 3. Achieve BEC with moderate values for control parameters like trap light intensity (50 watts), focus (70-100 microns)
- 4. Naturally accommodate optical lattices (standing wave of light, and atoms can get trapped in the periodic potential)



S. Chaudhuri, S. Roy, Unnikrishnan, Phys. Rev. A (2006)

Magneto-optic Trap loaded from cold atomic beam

Push the atoms using light



Cold atomic beam



Magneto-Optic Trap

Atomic beam loaded MOT has 1000 times more atoms than background loaded MOT



> 10¹⁰ atoms /second loaded when optimized

Optical dipole trap



CO₂ Laser: Quasi-Electrostatic Trap (QUEST) for atoms

C. K. N. Patel

Crossed beam optical dipole trap



Absorption images of atoms trapped in the optical dipole trap



Number of atoms in the dipole trap $\sim 10^6 - 10^8$

Crossed optical trap and the falling cloud from MOT



Enhancing the density with darkness





Temperature: $40\mu K$ Atom no. density $\approx 5 \times 10^{12}$ atoms/cc

Atoms in the crossed dipole trap (25 micro-K)





350 microns

Peak density > 10¹⁴ atoms/cc

Single beam trap depth (frequency) from parametric resonance

Radial frequency
$$\omega_r = \sqrt{\frac{4U_0}{mw^2}}; \quad U_0 \sim I_0$$



Cooling by spontaneous evaporation





 $T = N^{\alpha}, \alpha : 1 - 2$ 'Efficient' even with T ~ N
Phase space density

 $n\lambda^3 > 1$

In a harmonic trap

$$T_c \approx \frac{h\omega_0 N^{1/3}}{k_B} \rightarrow 10^{-11} \omega_0 N^{1/3}$$

When density is more or less constant, PSD increases as $1/T^{3/2}$

Evaporative cooling to BEC transition



Thermal de Broglie wavelength=0.4 microns; Inter-particle separation=0.15 microns

Evaporative cooling to BEC





600 ms T= 1 μK $\Lambda \approx 0.3$

300 micron

1000 ms **T=140** *nK* $\Lambda \approx 20$

900 ms **T= 400** *nK* $\Lambda \approx 4$

200 ms

BEC Phase transition

100 ms evaporation



400 ms evaporation



200 ms evaporation



600 ms evaporation



BEC in crossed Optical dipole trap



Size of the condensate

$$a_{h} = \left(\frac{h}{m\omega_{0}}\right)^{1/2} \quad 1 \text{ micron}$$

Interactions between the atoms change the equilibrium size

$$R_{BEC} \approx a_h \left(\frac{Na}{a_h}\right)^{1/5} \approx 10a_h$$
 10 microns

Expansion after releasing from the trap:

$$R^{2} = R_{0}^{2}(1 + \omega_{0}^{2}t^{2}) \rightarrow R_{0}^{2}\omega_{0}^{2}t^{2}$$

1 cm/s in our trap



HOW TO PROVE IT?



Inversion of ellipticity



Inversion of Aspect ratio



Description as a phase coherent 'wave'

 $-\frac{h^{2}}{2m}\nabla^{2}\Psi(r) + V(r)\Psi(r) + U_{0}(a)|\Psi(r)|^{2}\Psi(r) = \mu\Psi(r)$

 $n(r) = \left|\Psi(r)\right|^2$

Tunable with magnetic field, light...

Nonlinear

 $ih \frac{\partial \Psi(r,t)}{\partial t}$

Interference effects, Nonlinear effects (four-wave mixing, amplification...) Quantized vortices, Coherent beams (atom lasers) Superfluidity

Spinor condensates:

BEC of atoms that can assume any of the several possible ground states, either of the hyperfine levels, or of the magnetic sub-levels (projections, including $m_F=0$). This occurs naturally in an optical trap, whereas magnetic trap BEC are usually in a single state (weak field seeking state) that can be trapped well in the magnetic trap.

Magnetically Tunable

 $\frac{4\pi h^2 \overline{a}}{a} + c_s f_i \cdot f_j$

$$E = \sum_{i} p_i^2 / 2m + U(r_i) + \sum_{i} \delta(r_i - r_j)$$

C_s negative -> Ferromagnetic order C_s positive -> Anti-ferromagnetic order

For Rb, F=1, c_s is about -3x10⁻¹⁴ Hz.cm³

Optical Lattice

Operational now







Image of rubidium atoms trapped in (a) one-dimensional CO_2 laser Optical lattice (b) single beam dipole trap.



Image of rubidium atoms trapped in (a) one-dimensional CO₂ laser Optical lattice

(b) single beam dipole trap, after being transferred from an orthogonal single beam dipole trap.





Loading at will – evidence for optical lattice



Loading without lattice



Evaporative cooling in Optical lattice crossed with single beam dipole trap



900 nK

410 nK

250 nK

150 nK



Evaporative cooling in Optical lattice

Expansion time = 4ms



950 ms

1000 ms

1020 ms

BEC Phase transition in Optical Lattice crossed with dipole trap



Evaporative cooling in Optical lattice



BEC Phase transition in Optical Lattice



Experimental data for aspect ratio of BEC produced in Optical lattice



New Experiments (2008-2012):

- Atom-Atom correlations in 2atom or few atom experiments (QED, molecular, spinstatistics etc.)
- 2) Fountain based measurements (atom interferometry/gravity)
- 3) Fermion physics
- 4) Optical lattice physics
- 5) Short range forces
- 6) Physics of quantum entanglement and decoherence





THE SPIN-STATISTICS CONNECTION

Particles with integer spin are bosons and obey the Bose-Einstein statistics (laser, BEC...)

Particles with half-integer spin are fermions and obey the Fermi-Dirac statistics (Pauli exclusion – neutron stars...)

"It appears to be one of the few places in physics where there is a rule that can be stated very simply, but for which no one has found a simple and easy explanation...This probably means that we do not have a complete understanding of the fundamental principle involved." R. P. Feynman, FLP III

We now know what might be the fundamental principle involved here!

There is in fact a cosmic connection that is gravitational ! Unnikrishnan, Cosmic Relativity gr-qc/0406023 gr-qc/0406043

Gravitational potential "here"

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Earth:
$$\frac{GM_E}{c^2 R_E} < 10^{-9}$$

Sun:
$$\frac{GM_S}{c^2 R_S}$$
; 10^{-8}
Galaxy: 10^{-6}

Distant masses dominate!

$$\Phi_{U}: \int_{Overall \ Galaxies} G \cdot (4\pi\rho R^{2} dR) / Rc^{2}$$

$$C = 2\pi G \rho R_{H}^{2} / c^{2} \approx 1$$

$$\Phi_U \approx c^2$$

Our interaction energy with the matter in the Universe is billion time larger than our interaction energy with the Earth!!

What can this large potential do?

Moving through the microwave background



Absolute time Same as average T

Universe is NOT Lorentz invariant



What can these large potentials do?

In fact a lot! All kinematical effects we know of, including Newton's pseudo-forces, ALL relativistic effects wrongly attributed to motion relative to each other (time dilation etc. special relativity), and many quantum effects like finer-structure splitting...

In fact, Newton's law of motion itself, and the equivalence between gravitational and inertial mass are consequences

Cosmic Relativity gr-qc/0406023

But, let us get back to spins...





 $\mathsf{P}_{3/2}$

P_{1/2}







There is most certainly a cosmic connection to the spin-statistics connection


Our experiments with laser-cooled atoms and BECs and the future experiments with Fermionic atoms are all planned in the frame work of our fundamental contribution to relativity, gravity and spin-statistics connection. This is the focal point, and also the main theme. For the present I expect, with good reasons, that my finding that cosmic gravity is responsible for all physical effects usually attributed to kinematics (relativistic effects, laws of motion, spin-stat. connection...) will stand on the long run.

It also provides one of the most versatile laboratory systems at present for studying fundamental interactions, especially short range interactions, and for making precision measurements in atomic physics, condensed matter physics, quantum optics, and atom-light interactions.

With cold atoms and BECs, we can probe fundamental physics from 10⁻⁹ m to 10²⁵ m

The group

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